# Coherent X-Ray Cherenkov Radiation (CXCR) Produced by Microbunched Beams

M.A. Aginian<sup>1</sup>, K.A. Ispirian<sup>1</sup>, M.K. Ispiryan<sup>1</sup>, M.I. Ivanian<sup>2</sup>

<sup>1</sup>Alikhanian National Laboratory, Yerevan Physics Institute,

Br. Alikhanians 2, Yerevan, 0036, Armenia

<sup>2</sup> CANDLE Synchrotron Research Institute, Acharyan 31, 0040

Yerevan, Armenia

## 1. Introduction

The density distribution of the Gaussian e-beams of FELs is microbunched according to

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$$f(r,z) = \frac{N_b}{2\pi\sigma_r^2} \frac{\exp(-r^2/2\sigma_r^2)}{(2\pi)^{1/2}\sigma_z} [1 + b_1\cos(k_r,z)]$$
with form factor
$$(2\pi)^{1/2}\sigma_z = (2\pi)^{1/2}\sigma_z$$
(1)

with form factor  $F(\omega,\theta) = \exp\left(-(k\sigma_r\theta)^2\right) \left[\exp\left(\frac{-\omega^2\sigma_z^2}{2V^2}\right) + b_1 \exp\left(-\left(\frac{\omega}{V} - k_r\right)^2 \frac{\sigma_z^2}{2}\right) + b_1 \exp\left(-\left(\frac{\omega}{V} + k_r\right)^2 \frac{\sigma_z^2}{2}\right)\right]$ (2) where  $\lambda_r = 2\pi/k_r = 2\pi c/\omega_r = L_{und}(\frac{1}{b} + K^2/2)/2\gamma^2$  and  $\mathbf{b_1}$  are the microbunching wavelength and the modulation depth,  $N_b$ ,  $L_{und}$  and K ...

in [1]-COTR; in [2]-CXTR; in [3]- CXDR; in [4]- CChR; in [5]-CPXR in [6]-CCUR; in [7]-a review of all. 1. J. Rosenzweig, G. Travish, A. Tremaine, Nucl. Instr. and Meth. A 365 (1995) 255.

The coherent radiation of microbunched beams has been studied:

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Theoretically substituting the calculated values of  $\chi$ ' and  $\chi$ " into X-ray transition radiation (XTR) formulae (see [8]) and experimentally using E=1.5 GeV [9] and 5-10 MeV [10-12] electrons it has been shown that at K-. L- edges in narrow regions where  $n(\omega)>1$ , X-ray Cherenkov radiation (XCR) is produced.

This work is devoted to the theoretical study of coherent X-ray Cherenkov radiation (CXCR) in water window region (ħω=285-550 eV) which can be produced and used at DESY FLASH2 with E=1.2 GeV [13] and at Japan SACLA [14] and DESY EuroFEL [15] with E=8 and 10 GeV electrons.

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#### 2. The Calculation of CXCR

Using the well known relation (see [16])

$$\frac{d^2N_{CXCR}}{d\omega d\theta} \cong N_b^2 F(\omega, \theta) \frac{d^2N_{XCR}}{d\omega d\theta} ,$$
Where the form-factor is given by (2) and 
$$\frac{d^2N_{XCR}}{d\omega d\theta}$$
(3)

by the XTR formula (1.59) of [8] which can be used also for XCR

$$\frac{d^{2}N_{XTR}}{d\hbar\omega d\theta} = \frac{d^{2}N_{XCR}}{d\hbar\omega d\theta} = \frac{2\alpha\theta^{3}}{\pi\hbar\omega} \frac{(\chi'^{2} + \chi''^{2})}{(\theta^{2} + \gamma^{-2})^{2}[(\theta^{2} + \gamma^{-2} - \chi')^{2} + \chi''^{2}]} . (4)$$

Substituting (4) and (2) into (3) one derives for the spectral-angular distribution of CXCR

$$\frac{d^{2}N_{CXCR}}{d\omega d\theta} \cong N_{b}^{2}b_{1}^{2}\frac{2\alpha\theta^{3}}{\pi\omega}\frac{(\chi'^{2}+\chi''^{2})}{(\theta^{2}+\gamma^{-2})^{2}[(\theta^{2}+\gamma^{-2}-\chi')^{2}+\chi''^{2}]}\exp\left(-(k\sigma_{r}\theta)^{2}\right)\exp\left(-\left(\frac{\omega}{V}-k_{r}\right)^{2}\sigma_{z}^{2}\right).$$
(5)

16. N. A. Korkhmazian, L.A. Gevorgian, M. L.Petrosian, Zh. Techn. Fiz. 47, 1583, 1977.

## The angular distribution of CXCR photon number is obtained integrating (5) over $\omega$

$$\frac{dN_{CXCR}}{d\theta} \cong N_b^2 b_1^2 \frac{2\alpha \theta^3 V}{\sqrt{\pi} \sigma_z \omega_r} \frac{(\chi'^2 + \chi''^2)|_{\omega = \omega_r}}{(\theta^2 + \gamma^{-2})^2 [(\theta^2 + \gamma^{-2} - \chi'|_{\omega = \omega_r})^2 + \chi''^2|_{\omega = \omega_r}]} \exp(-(k_r \sigma_r \theta)^2)^{\bullet}$$
(6)

The spectral distribution of CXCR is obtained by integration of (5) over  $\theta$ 

$$\frac{dN_{CXCR}}{d\omega} \cong N_b^2 b_1^2 \frac{2\alpha(\chi'^2 + \chi''^2)}{\pi\omega} I(\omega, \theta_0) \exp\left(-\left(\frac{\omega}{V} - k_r\right)^2 \sigma_z^2\right) , \qquad (7)$$

where

The upper limit of integration in (8) must be taken 
$$\theta_0 >> 1/\gamma$$
, (8)

the radiation intensities decrease sharply after these angles

For  $\gamma >> 1$  one obtains

where

or 
$$\gamma >> 1$$
 one obtains
$$I(\omega, \infty) = \frac{j}{2\chi''} (A - A^*) + B$$

$$A = \frac{1}{2} \frac{e^{-(k\sigma_r)^2(\chi' - j\chi'')} \Gamma(0, -(k\sigma_r)^2(\chi' - j\chi''))}{\chi' - j\chi''}, \quad B = \frac{1}{2} \frac{1 + C + 2\ln(k\sigma_r/\gamma)}{\chi'^2 + \chi''^2}$$
(9)

$$\Gamma(a,z) = \int_{z}^{\infty} t^{a-1} e^{-t} dt$$
 , C=0.577216 (10)

The total number of CXCR photons per bunch obtained by integration of (6) over  $\theta$ , or of (7) over  $\omega$  is equal to

$$N_{CXCR} = N_b^2 b_1^2 \frac{2\alpha V(\chi'^2 + \chi''^2)|_{\omega = \omega_r}}{\sigma_z \sqrt{\pi} \omega_r} I(\omega_r, \theta_0).$$
 (11)

#### 3. Numerical Results

Obtained with the help of (6) - (11) for C are calculated for  $\hbar \omega_r$ = 284 eV (FLASH2) with E=1.2 GeV [13], and SACLA [14] and EuroFEL [15] with E=8 and 10 GeV, respectively, by "tuning" the parameters. The results for Ti are calculated for SACLA [14] and EuroFEL [15]at E=8 and 10 GeV, respectively. In all the cases it is taken b<sub>1</sub>=1,  $\sigma_r = 13 \, \mu m$   $\sigma_z = 15 \, \mu m$ 

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#### 3a. The Angular Distributions of CXCR

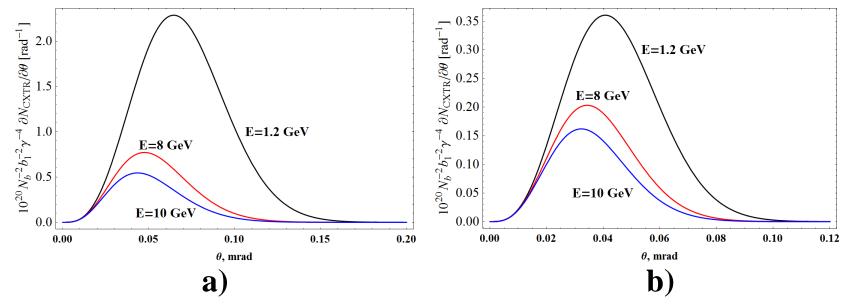


Fig.1 a) and b) for C and Ti, respectively.

It is seen that  $\theta$  are less than  $1/\gamma$ .

### **3b.** The Spectral Distributions of CXCR

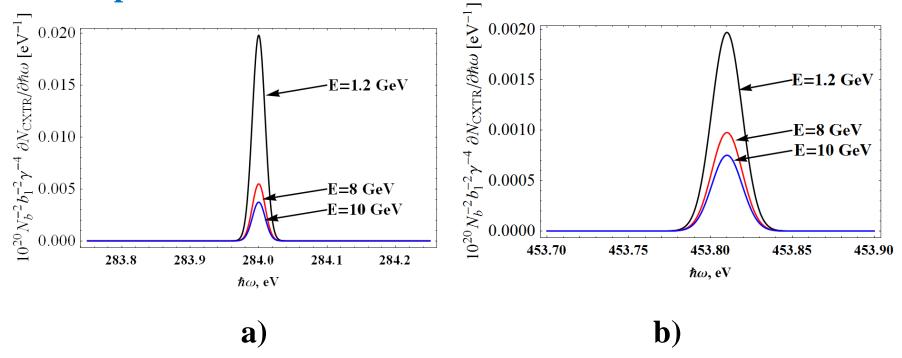
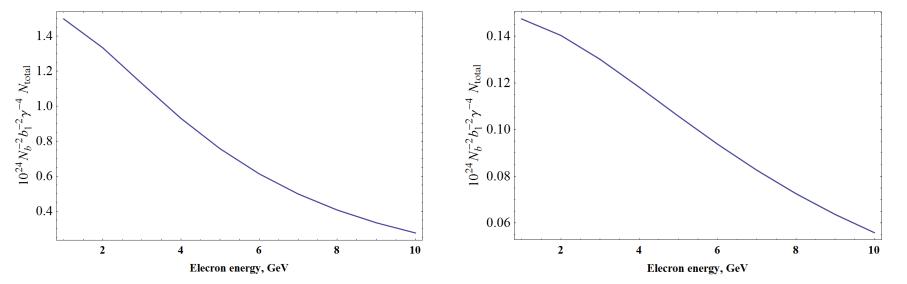


Fig.2 The Spectral Distributions of CXCR for C and Ti, a) and b), respectively

#### **3c.** The Energy Dependence of CXCR



a) Fig.2 a) and b) for C and Ti b) It is seen that N increases slightly more weakly than  $\sim \gamma^4$ .

#### 4. Discussion and Conclusions

For comparison Table gives the main parameters of SASE, XCR and CXCR radiation for C expected at FLASH at E=1.2 GeV.

	SASE	XCR	CXCR
N	$10^{12}$	$3x10^{6}$	$1.8 \times 10^9$
$\Delta\omega/\omega$ (%)	1.0	0.35	0.0014
$\Delta\omega$ (eV)	2.8	1.0	0.027

The situation becomes much better for higher energy electrons and Ti radiator. However, it has been taken  $b_1=1$ , and any real  $b_1<1$  reduces the CXCR intensity  $\sim b_1^2$ . In our knowledge, the values of  $b_1$  have not been measured anywhere.

Let us note that as for the first real X-ray laser [17] the CXCR beam has more stable ħω line since it is the characteristics of radiator atoms

17. N.Rohringer et al, Nature, 481 (2012) 488.

Summarizing one can make the following conclusions: 1) New type of radiation, CXCR, has been predicted and studied. 2) The use of microbunched beams, which are now sent to dumps, can provide CXCR beams very monochromatic and stable. As the beams of [17] they can find application in atomic physics and for the measurement of  $b_1$ . Indeed, if by another simple method, say, measuring the current, one knows the value of  $N_{b_1}$  then the measured intensity can serve for determination of  $b_1$ .

# Thank you