

# Hydrodynamical approach to pPb

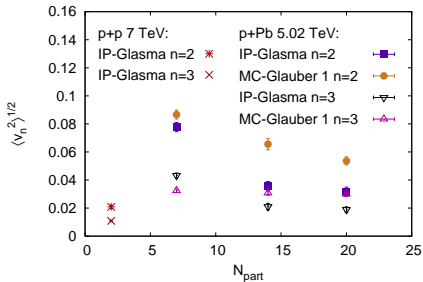
Piotr Bożek

Institute of Nuclear Physics and AGH, Kraków  
with Wojciech Broniowski and Giorgio Torrieri



# Hydrodynamic flow in p-p?

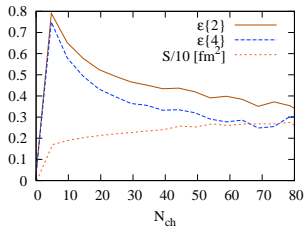
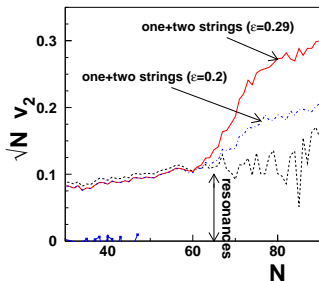
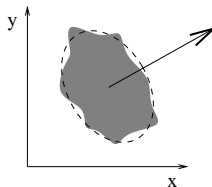
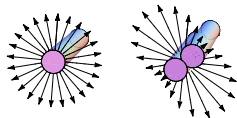
- ▶ Humanic-nucl-th/0612098 (pythia, cascade)
- ▶ Romatschke, Luzum-arXiv:0901.4588 (overlap)
- ▶ Prasad, Roy, Chattopadhyay, Chaudhuri -arXiv: 0910.4844 (overlap)
- ▶ Bozek-arXiv: 0911.2393 (flux-tubes)
- ▶ Yan, Dong, Zhou, Li, Ma, Sa- arXiv: 0912.3342 (transport)
- ▶ Werner, Karpenko, Pierog, Bleicher, Mikhailov-arXiv: 1010.0400 (EPOS)
- ▶ Deng, Xu, Greiner-arXiv: 1112.0470 (hot-spots, transport model)
- ▶ Shuryak, Zahed-arXiv:1301.4470 (symmetric)
- ▶ Bzdak, Schenke, Tribedy, Venugopalan-arXiv: 1304.3403 (IP-Glasma)



Bzdak et al. arXiv: 1304.3403

- Is hydrodynamics valid?
- What is the initial eccentricity?

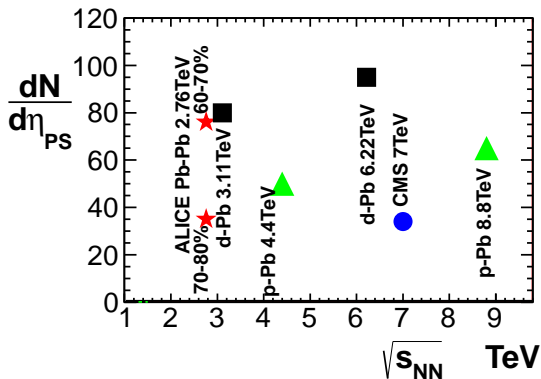
# Fireball shape in pp



Bozek, 0911.2397

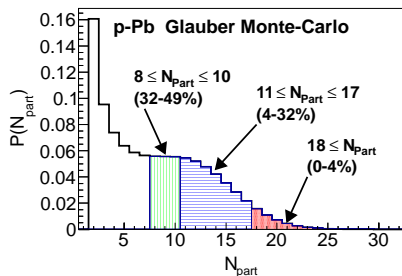
E.Asar et al., 1009.5643

Casalderrey-Solana, Wiedemann, 0911.4400

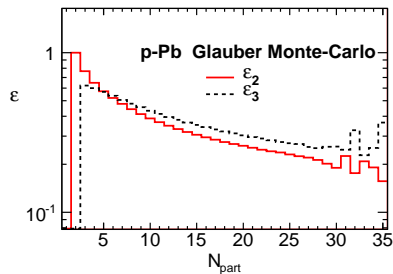


large multiplicity - large fireball - collective expansion?

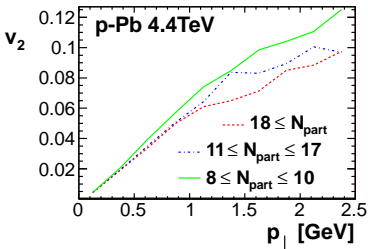
# Fireball in p-Pb



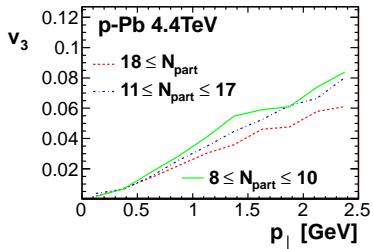
PB, arXiv:1112.0912



- ▶ Large enough density? **yes** yes (high mult.)
- ▶ Large enough eccentricity **yes?** (?)
- ▶ Large enough size? **(?)** (???)  
but should and can be tested
- ▶ Small enough gradients? **no** no!  
- beyond viscous hydro

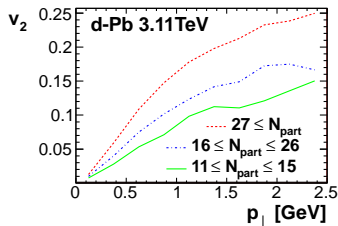
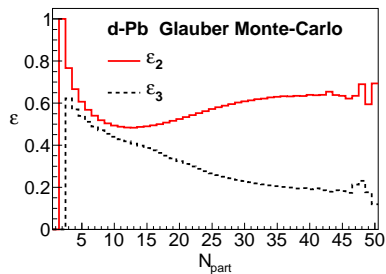


elliptic flow in p-Pb



triangular flow

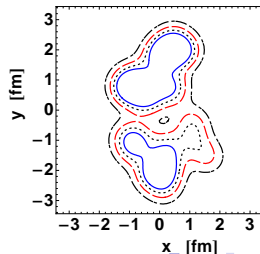
PB, arXiv:1112.0912



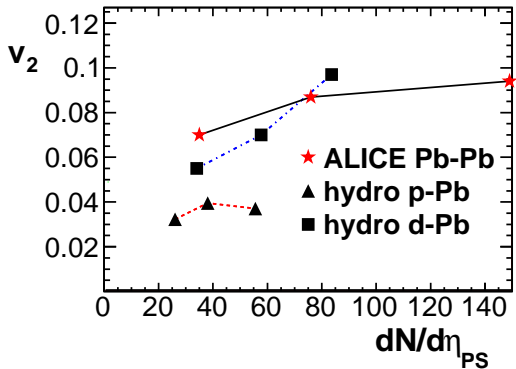
large elliptic flow

PB, arXiv:1112.0912

... it seems very interesting to look for collective effects in d-Au collisions at  $\sqrt{s_N} = 200\text{GeV}$  in RHIC experiments ...





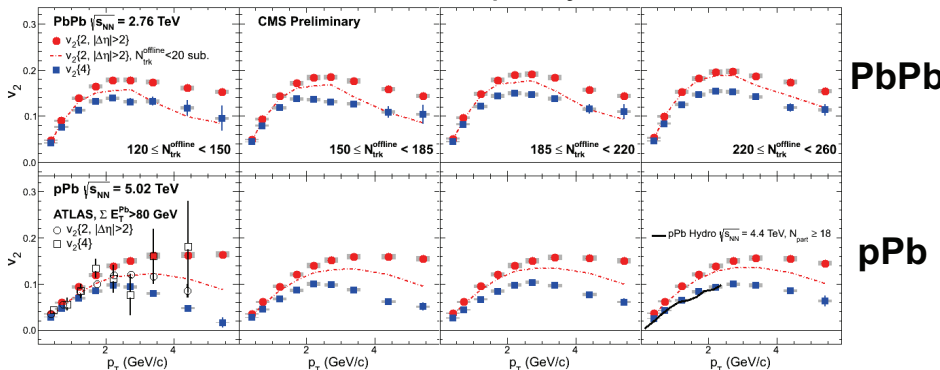


- ▶ collective flow effects  $\simeq$  peripheral Pb-Pb
- ▶ can be observed
- ▶ p-Pb (d-Pb) is not p-p superposition
- ▶ only p-p as baseline

# $v_2$ in pPb and PbPb

Dash-dot line: peripheral subtracted

multiplicity  $\longrightarrow$



$v_2$  shows similar shape in pPb and PbPb, but is smaller in pPb

$v_2\{4\}$  is only 20% smaller than  $v_2\{2\}$  below 2 GeV/c

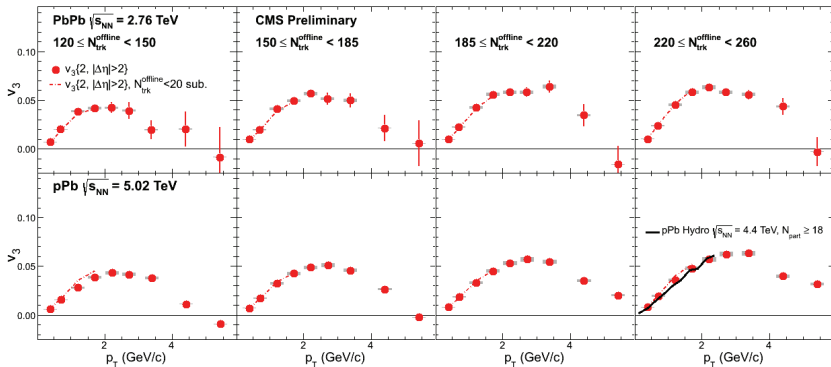
“Peripheral subtraction” has small effect at high multiplicity



# $v_3$ in pPb and PbPb

Dash-dot line: peripheral subtracted

multiplicity  $\longrightarrow$



PbPb

pPb

$v_3$  has similar shape in pPb and PbPb; magnitude comparable

“Peripheral subtraction” makes essentially no difference

Hydro prediction: Bozek,  $v_3\{PP\}$ , not including fluctuations



Gunther Roland

RBRC Workshop, Apr 15-17, 2013



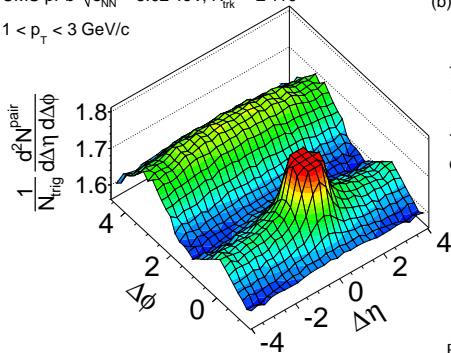
Piotr Bozek

hydrodynamics in pPb

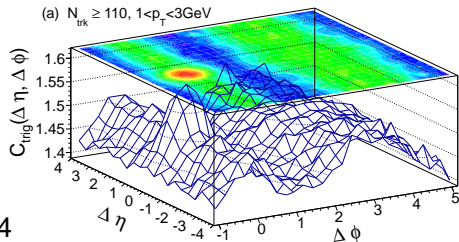
# Ridge in p-Pb

CMS pPb  $\sqrt{s_{NN}} = 5.02$  TeV,  $N_{trk}^{offline} \geq 110$

$1 < p_T < 3$  GeV/c



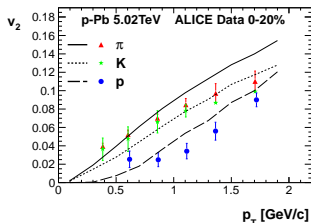
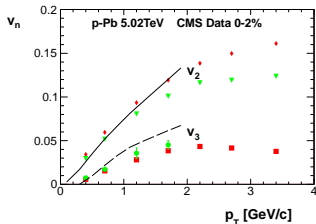
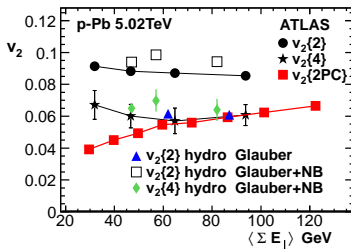
(b)



PB, W.Broniowski, arXiv:1211.0845

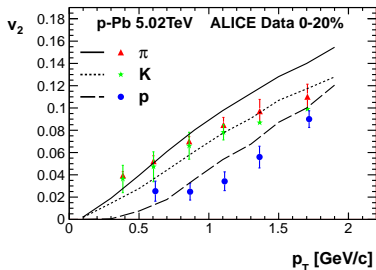
symmetric ridge also from CGC, K.Dusling, R. Venugopalan, arXiv:1210.3890, 1211.3701, 1302.7018

# Elliptic and triangular flow



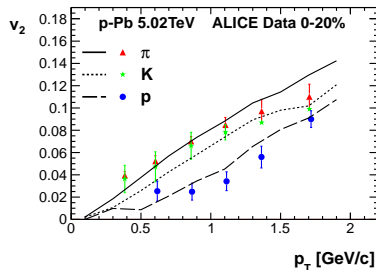
PB, W.Broniowski, G. Torrieri arXiv:1306.5442

## $v_2$ from late stage



$T_f = 150\text{MeV}$

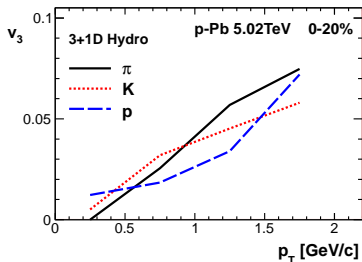
- pions : 0.75 collisions after emission



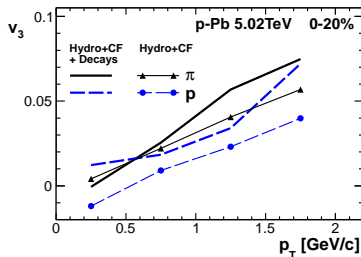
$T_f = 140\text{MeV}$

- pions : 0.65 collisions after emission

## $v_3$ - small mass splitting

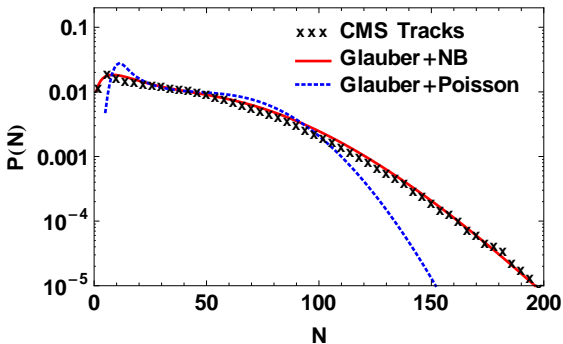


limited mass splitting



resonance decays spoil mass ordering

## Glauber+NB

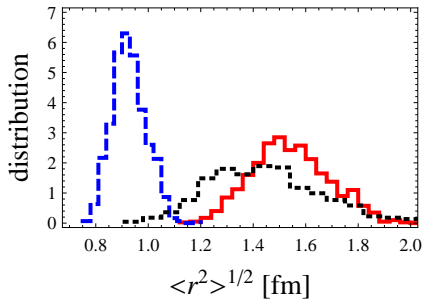


$$P(n) = \sum_i P_{part}(i) N p \lambda_i, \kappa i(n)$$

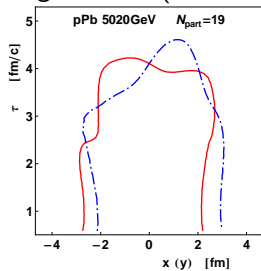
Additional fluctuations of density (compared to Glauber)



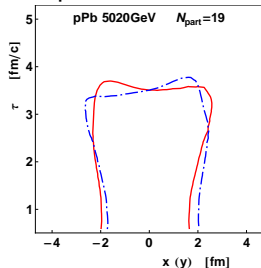
## very different source sizes



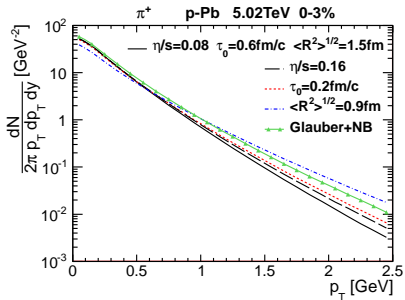
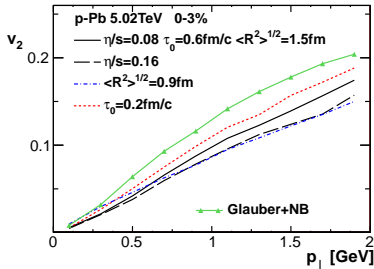
## large source (standard)



## compact source

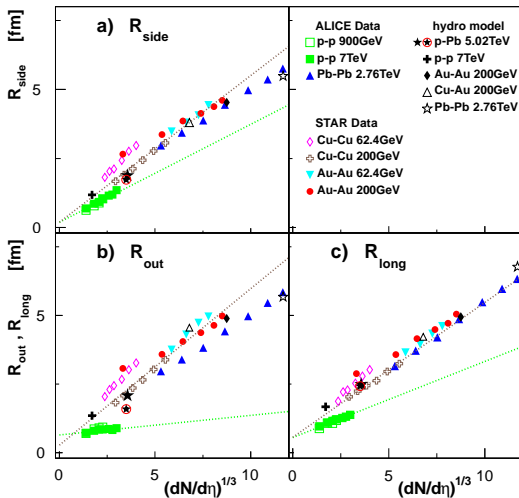


## dependence on model details



- response strength depends on details, initial eccentricity

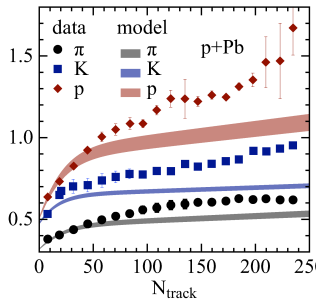
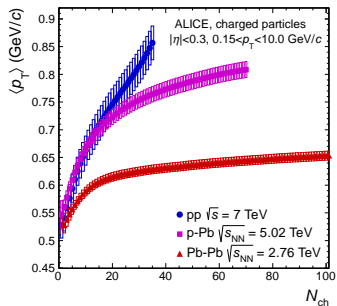
# HBT systematics



PB, W.Broniowski, arXiv:1301.3314

small system corrections!- Sinyukov, Shapoval - arXiv:1209.1747

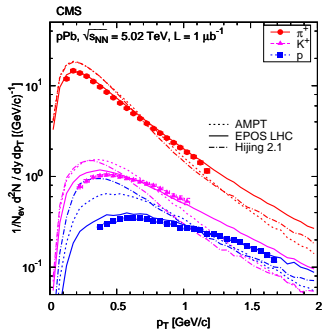
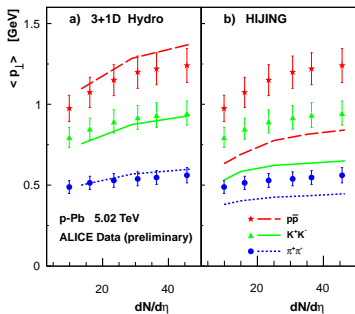
# Spectra - $\langle p_{\perp} \rangle$



larger  $\langle p_{\perp} \rangle$  in smaller systems

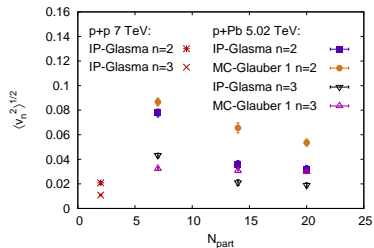
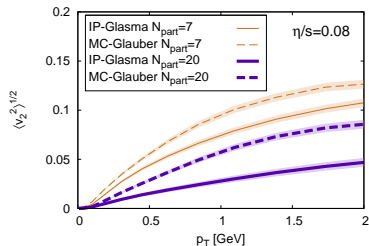
Bzdak, Skokov, arXiv:1306.5442

# Spectra - $\langle p_{\perp} \rangle$



PB, W.Broniowski, G. Torrieri arXiv:1306.5442

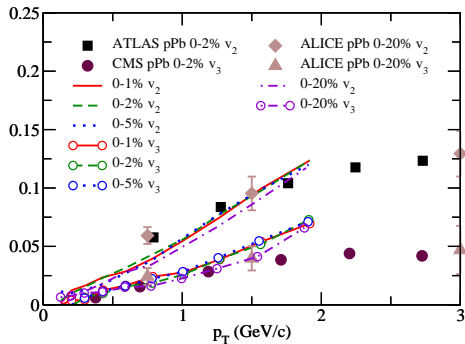
# 3+1D visc. hydro



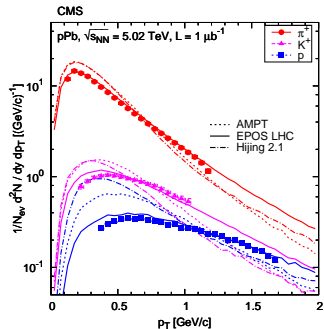
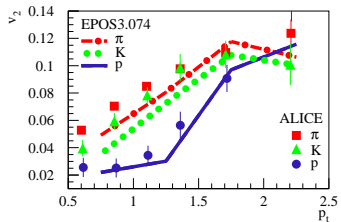
dependence on initial model,  $v_n$  small for IP-Glasma i.c.

A.Bzdak, B.Schenke, P.Tribedy, R.Venugopalan - arXiv: 1304.3403

# 3+1D hydro



G-Y.Qin, B. Müller arXiv: 1306.3439

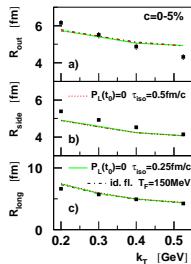
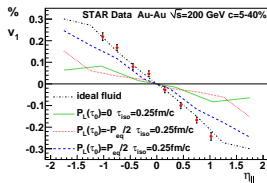
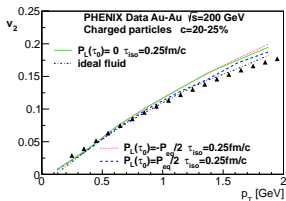
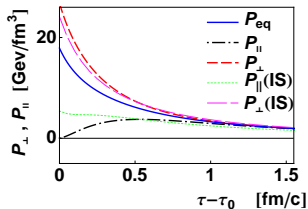


excellent description of spectra

K. Werner, M. Bleicher, B. Guiot, Iu. Karpenko, T. Pierog - arXiv:1307.4379



# pressure anisotropy



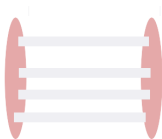
PB, I. Wyskiel - arXiv:1009.0701

- early pressure anisotropy irrelevant!

# FSI scenarios

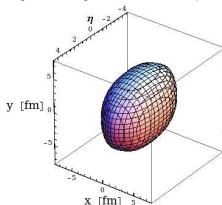
## fields+thermalization

color fields

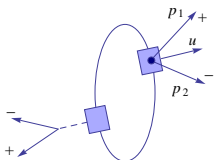


## hydrodynamics

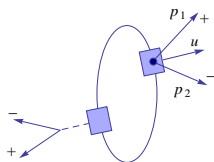
hydrodynamic expansion



local thermalization  $\rightarrow$  hadronization



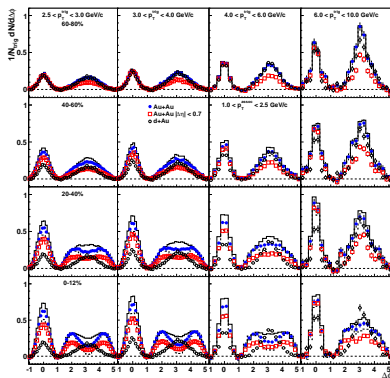
hadronization, statistical emission



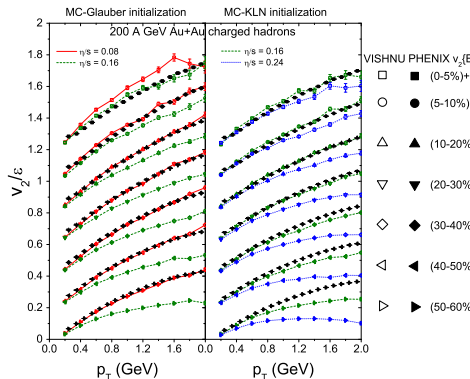
Give similar flow



# Can we reduce uncertainties? go back to very peripheral A-A



STAR-arXiv:1004.2377



Song, Bass, Heinz, Hirano, Shen-arXiv:1101.4638

also jet modification, dijet asymmetry, PID flow, HBT

- ▶ Ev-by-Ev hydro for pPb
- ▶ Collectivity in pPb@LHC explains  $v_2$ ,  $v_3$ , ridge,  $\langle p_{\perp} \rangle$
- ▶ Observations consistent with collective flow  
many exp. results; several calculations
- ▶ HBT radii in p-Pb?
- ▶ Limits of hydro!
  
- ▶ **Why hydrodynamics would work?**
- ▶ **Effective theory for transverse expansion**
- ▶ We need observables for longitudinal pressure

## energy-momentum tensor

$$T^{\mu\nu} = \begin{pmatrix} \epsilon & 0 & 0 & 0 \\ 0 & p + \Pi & 0 & 0 \\ 0 & 0 & p + \Pi & 0 \\ 0 & 0 & 0 & p + \Pi \end{pmatrix} + \pi^{\mu\nu}$$

- ▶ shear viscosity

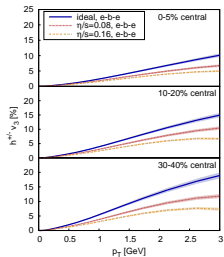
$$\Delta^{\mu\alpha} \Delta^{\nu\beta} u^\gamma \partial_\gamma \pi_{\alpha\beta} = \frac{2\eta\sigma^{\mu\nu} - \pi^{\mu\nu}}{\tau_\pi} - \frac{1}{2}\pi^{\mu\nu} \frac{\eta T}{\tau_\pi} \partial_\alpha \left( \frac{\tau_\pi u^\alpha}{\eta T} \right)$$

- ▶ bulk viscosity

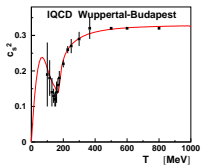
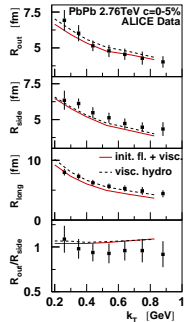
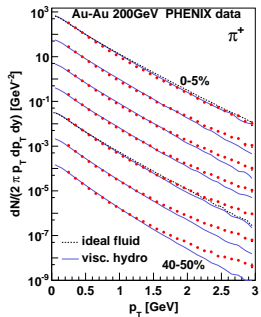
$$u^\gamma \partial_\gamma \Pi = \frac{-\zeta \partial_\gamma u^\gamma - \Pi}{\tau_\Pi} - \frac{1}{2}\Pi \frac{\zeta T}{\tau_\Pi} \partial_\alpha \left( \frac{\tau_\Pi u^\alpha}{\zeta T} \right)$$

- ▶ viscosity corrections from velocity gradients
- ▶ **initial** stress tensor - pressure anisotropy
- ▶ equation of state

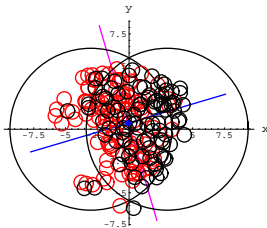
# 3+1D hydrodynamics



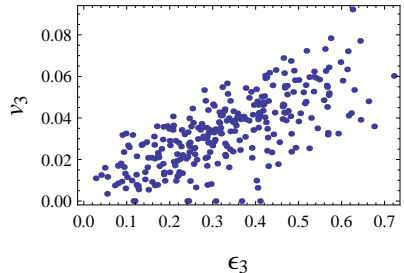
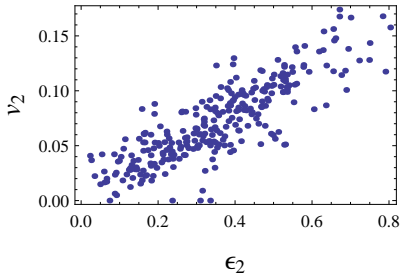
3+1D visc. : B.Schenke et al.



IQCD + Hadron Gas

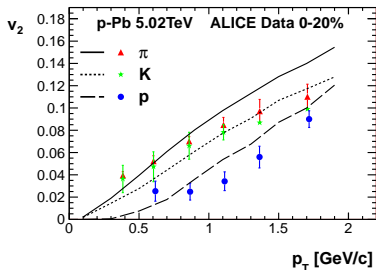


## fireball asymmetry - flow asymmetry



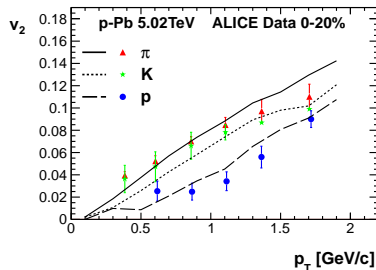
- Ev-by-Ev hydro response to geometry valid
- response strength depends on details

## $v_2$ from late stage



$T_f = 150\text{MeV}$

- pions : 0.75 collisions after emission



$T_f = 140\text{MeV}$

- pions : 0.65 collisions after emission