

# COHERENCE EFFECTS BETWEEN INITIAL AND FINAL STATE RADIATION IN A DENSE QCD MEDIUM

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**arXiv:1308.2186**



# Motivation

A hot and dense deconfined coloured medium (QGP) is produced in Ultrarelativistic Heavy Ion Collisions

⇒ Nuclear modifications to the fragmentation functions and PDFs

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A hot and dense deconfined coloured medium (QGP) is produced in Ultrarelativistic Heavy Ion Collisions

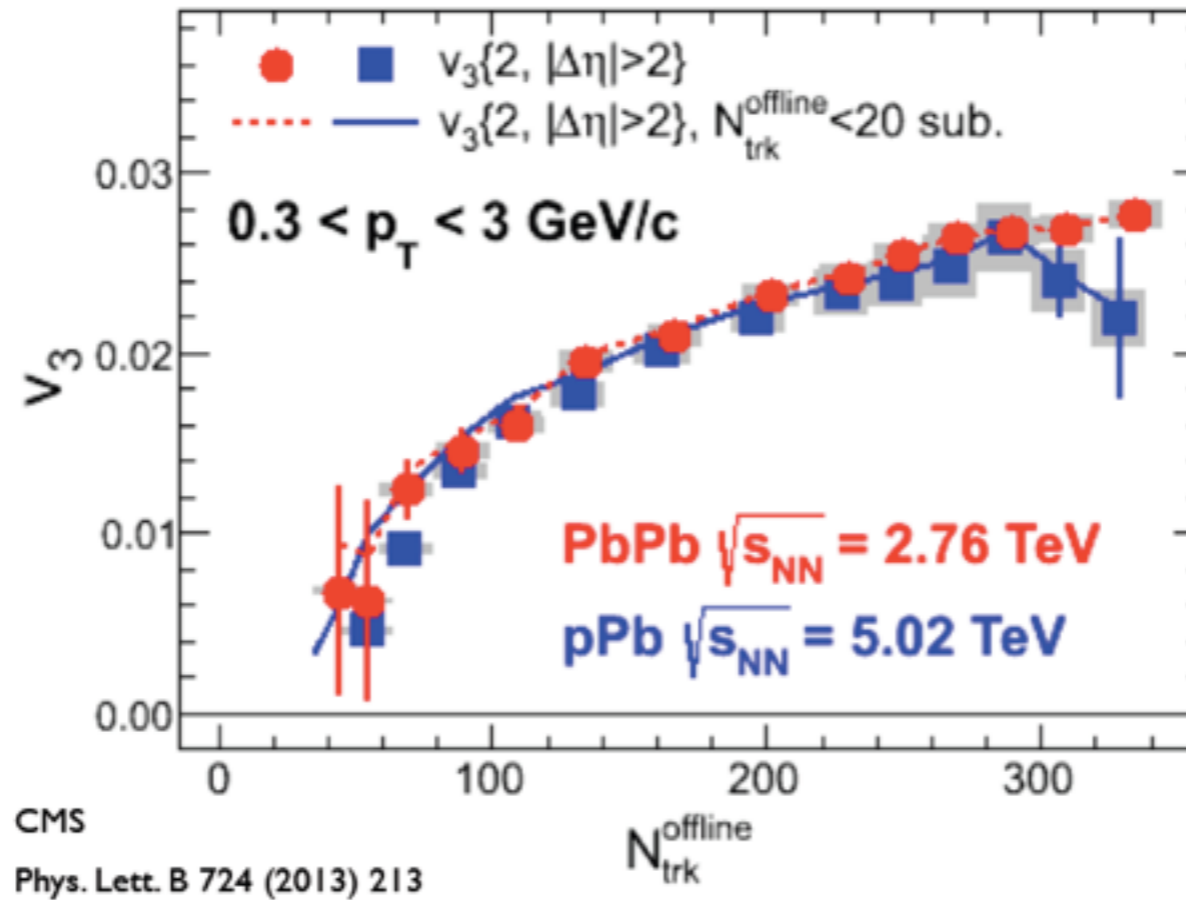
⇒ Nuclear modifications to the fragmentation functions and PDFs

Observables in HI Collisions are related to the properties of the QGP

⇒ Using pA to constrain nuclear PDFs

⇒ Assume no final state interactions. But....

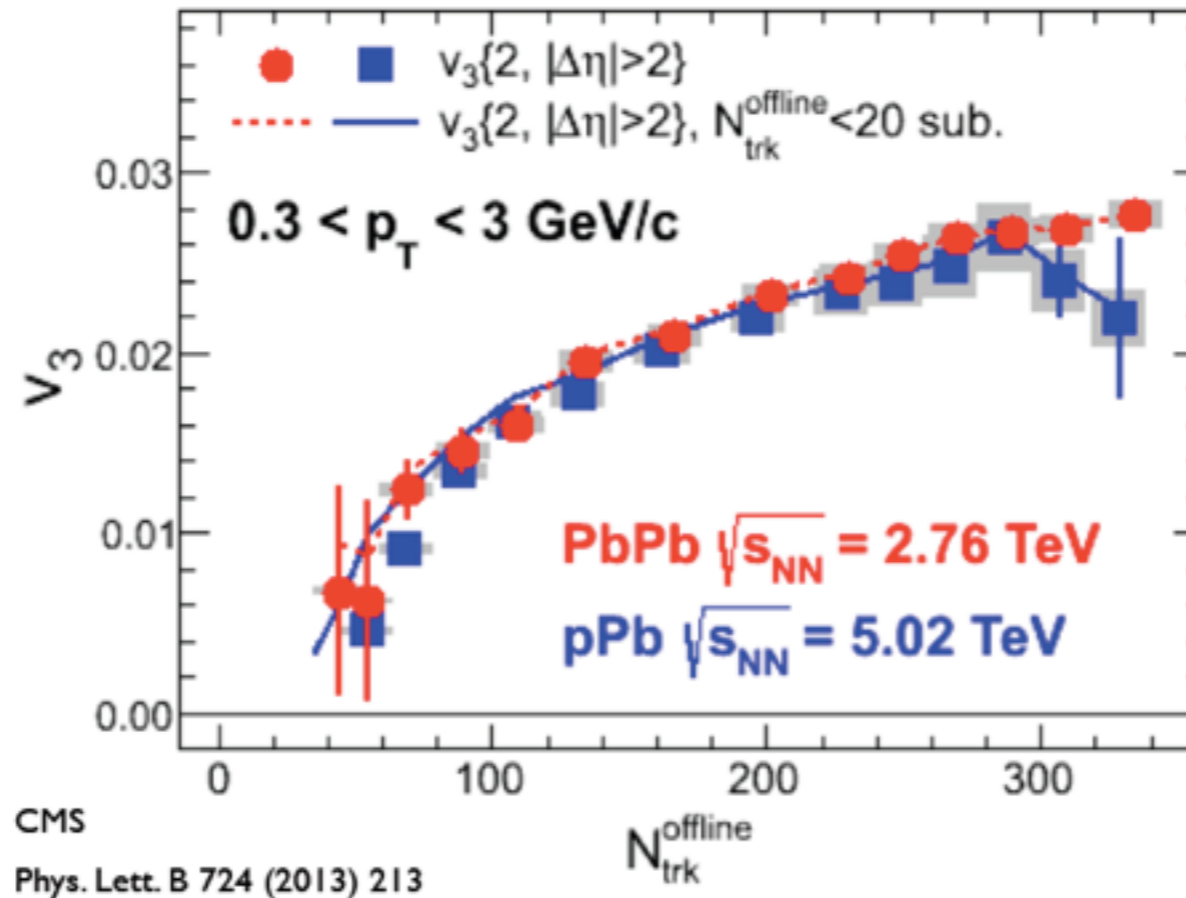
# Motivation



Possible evidence of final state interactions in pA  
 $\Rightarrow$  Flow harmonics comparable to AA



# Motivation



Possible evidence of final state interactions in pA

⇒ Flow harmonics comparable to AA

QCD medium of finite size leads to color decoherence effects

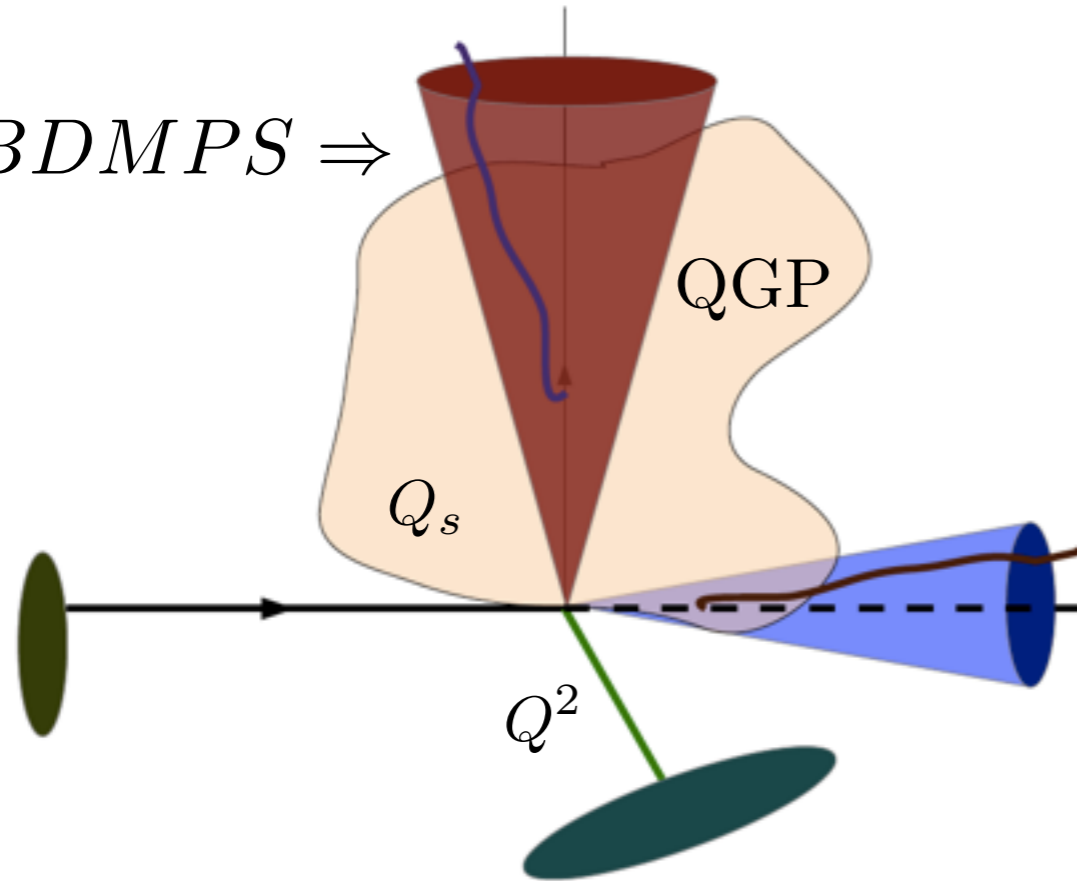
⇒ Modifications to the hadronic outcome subsist for large  $p_T$

⇒ **Jet quenching effects** might be seen in pA

See K. Tywoniuk's talk

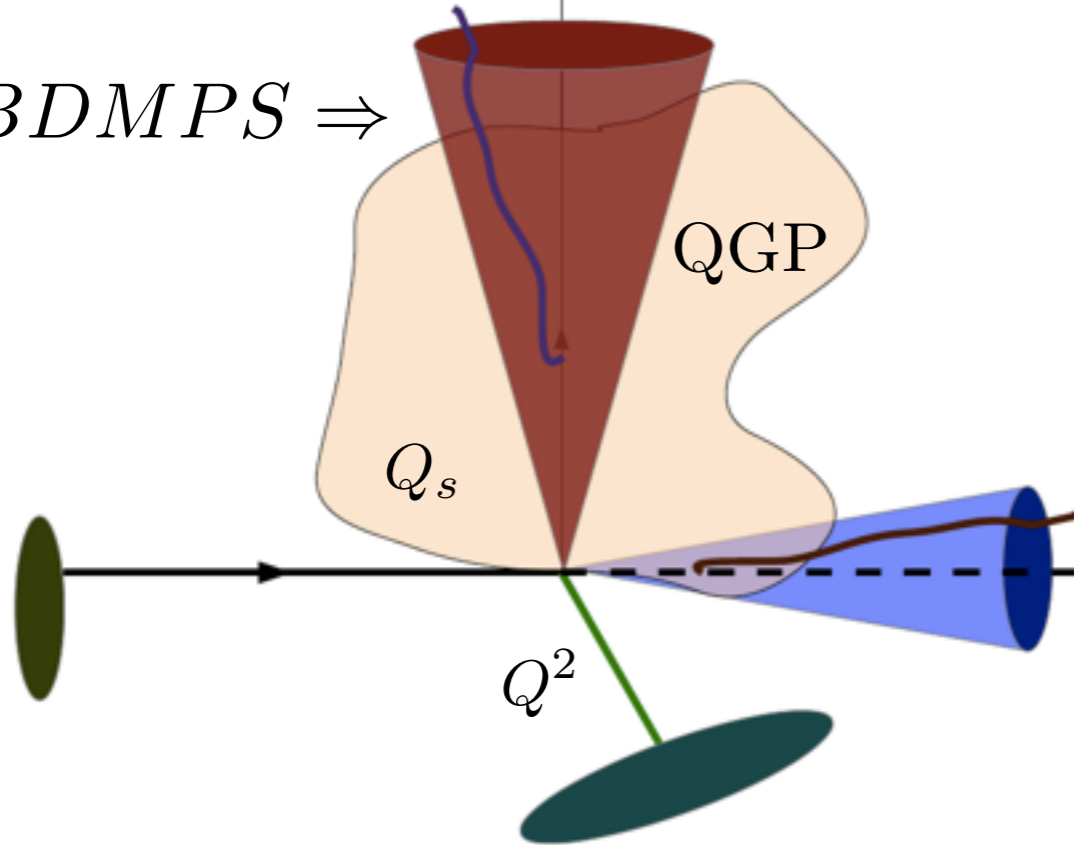
Medium of finite size  
Collinear Factorization

$BDMPS \Rightarrow$



Medium of finite size  
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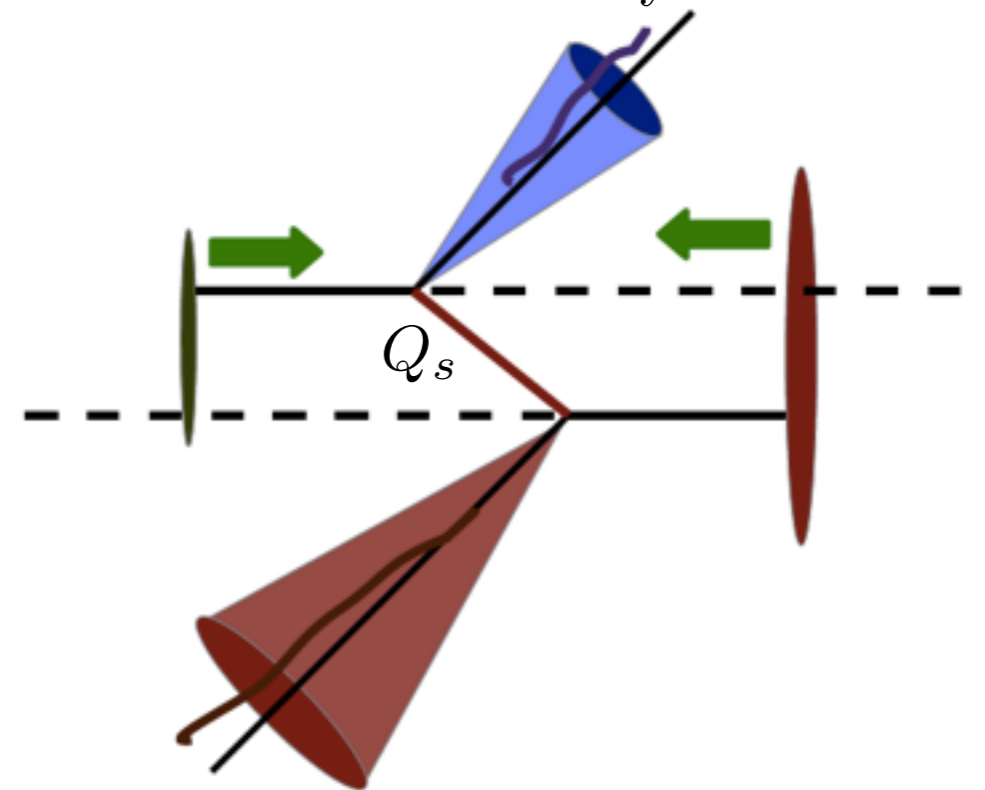
$BDMPS \Rightarrow$



Shockwave

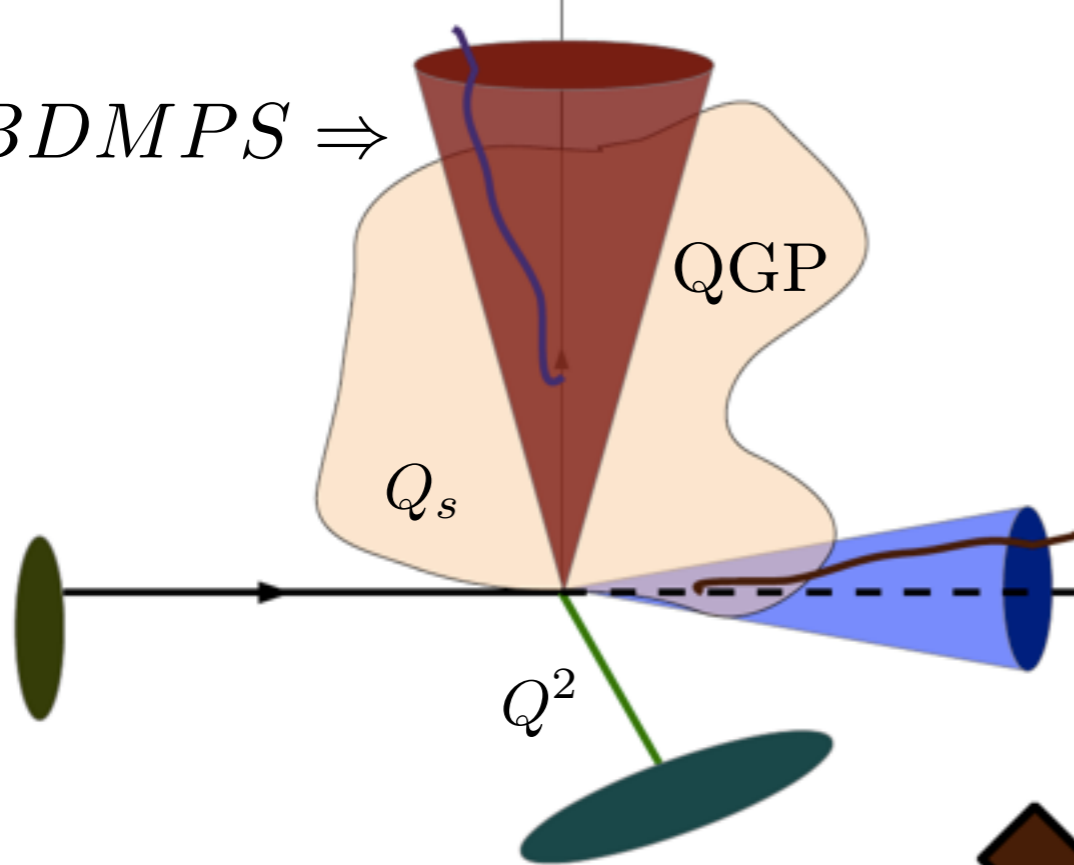
$k_T$  factorization

Hybrid formalism



Medium of finite size  
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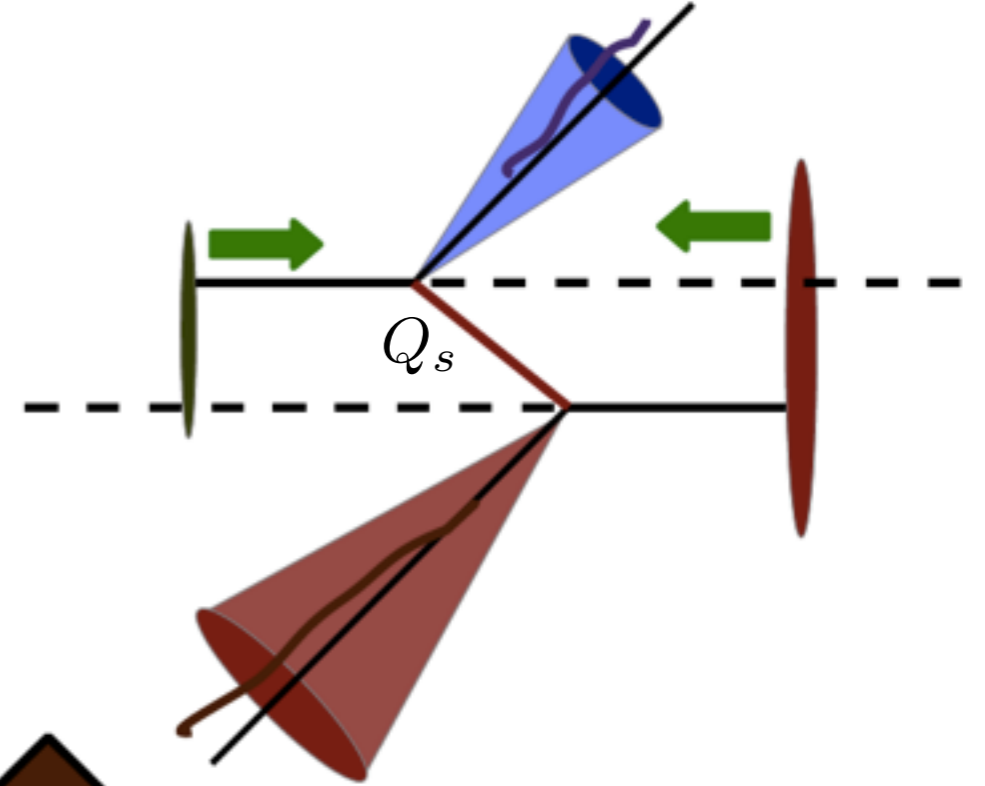
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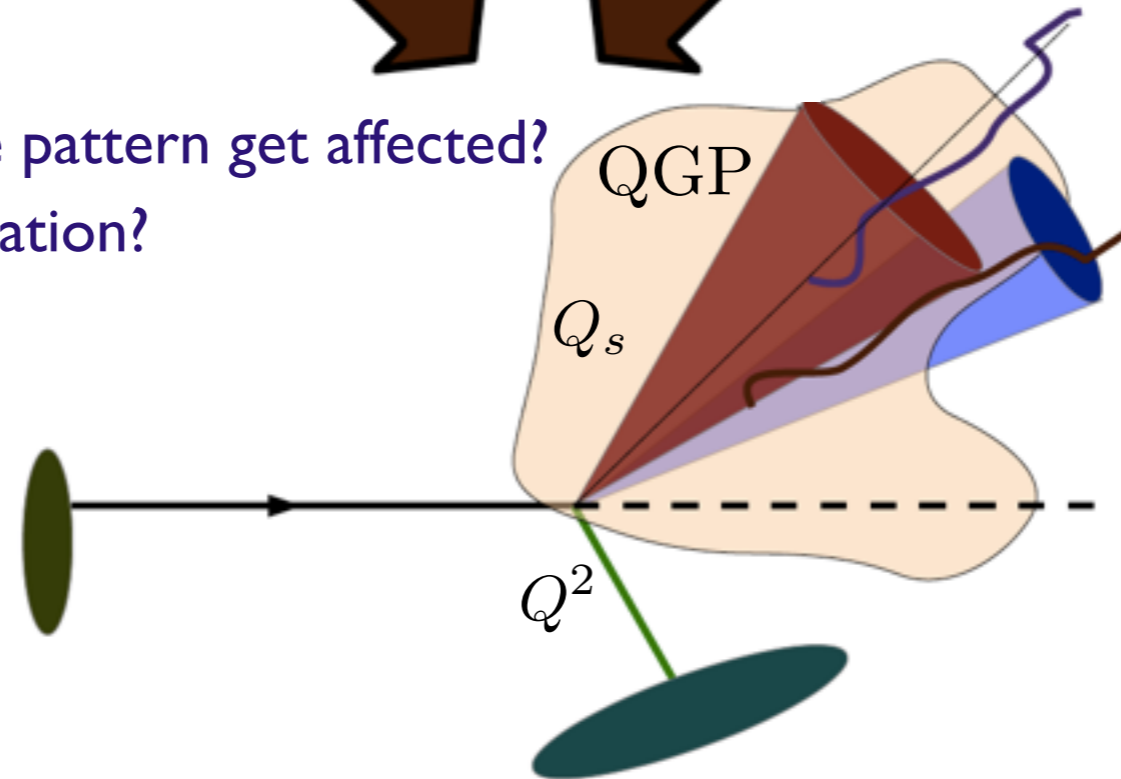
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Hybrid formalism

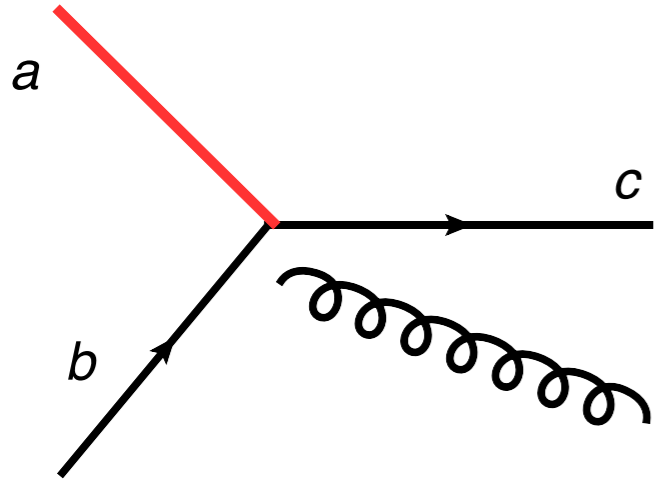


How is the vacuum coherence pattern get affected?  
Do we have: Collinear factorization?

$k_T$  Factorization?  
Something else?

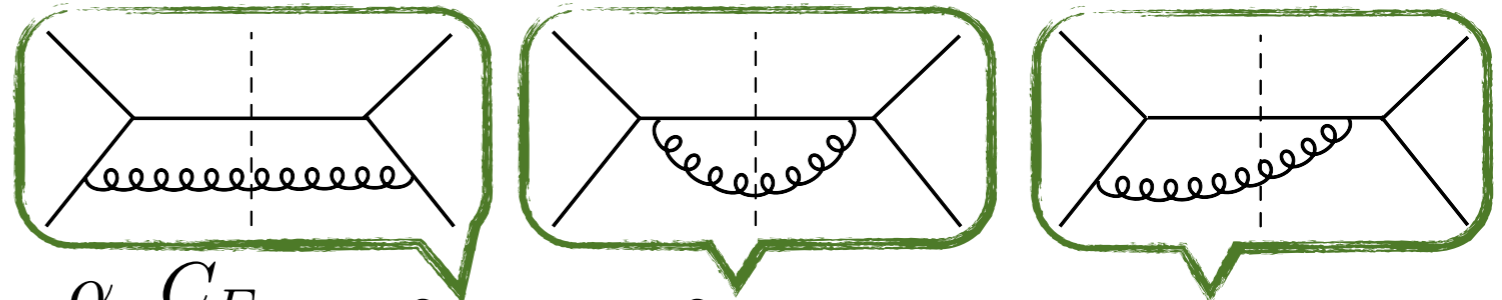


# Color coherence in a DIS-like process



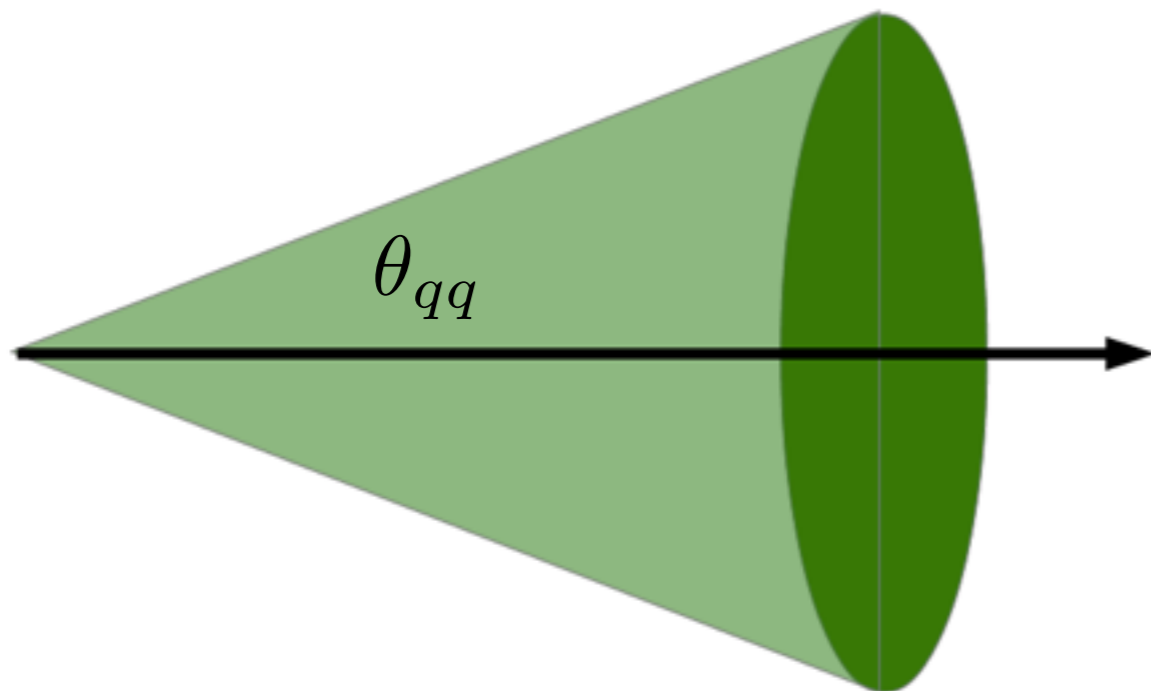
$Q_a = 0 \Rightarrow \text{Singlet}$

$Q_a \neq 0 \Rightarrow \text{Octet}$



$$\omega \frac{dN}{d^3 \vec{k}} = \frac{\alpha_s C_F}{(2\pi)^2 \omega^2} [Q_b^2 \mathcal{R}_b + Q_c^2 \mathcal{R}_c + 2 Q_b \cdot Q_c \mathcal{J}]$$

$$= \frac{\alpha_s C_F}{(2\pi)^2 \omega^2} [\underbrace{Q_b^2 (\mathcal{R}_b - \mathcal{J}) + Q_c^2 (\mathcal{R}_c - \mathcal{J})}_{\text{Coherent radiation}} + \underbrace{Q_a^2 \mathcal{J}}_{\text{Total charge}}]$$

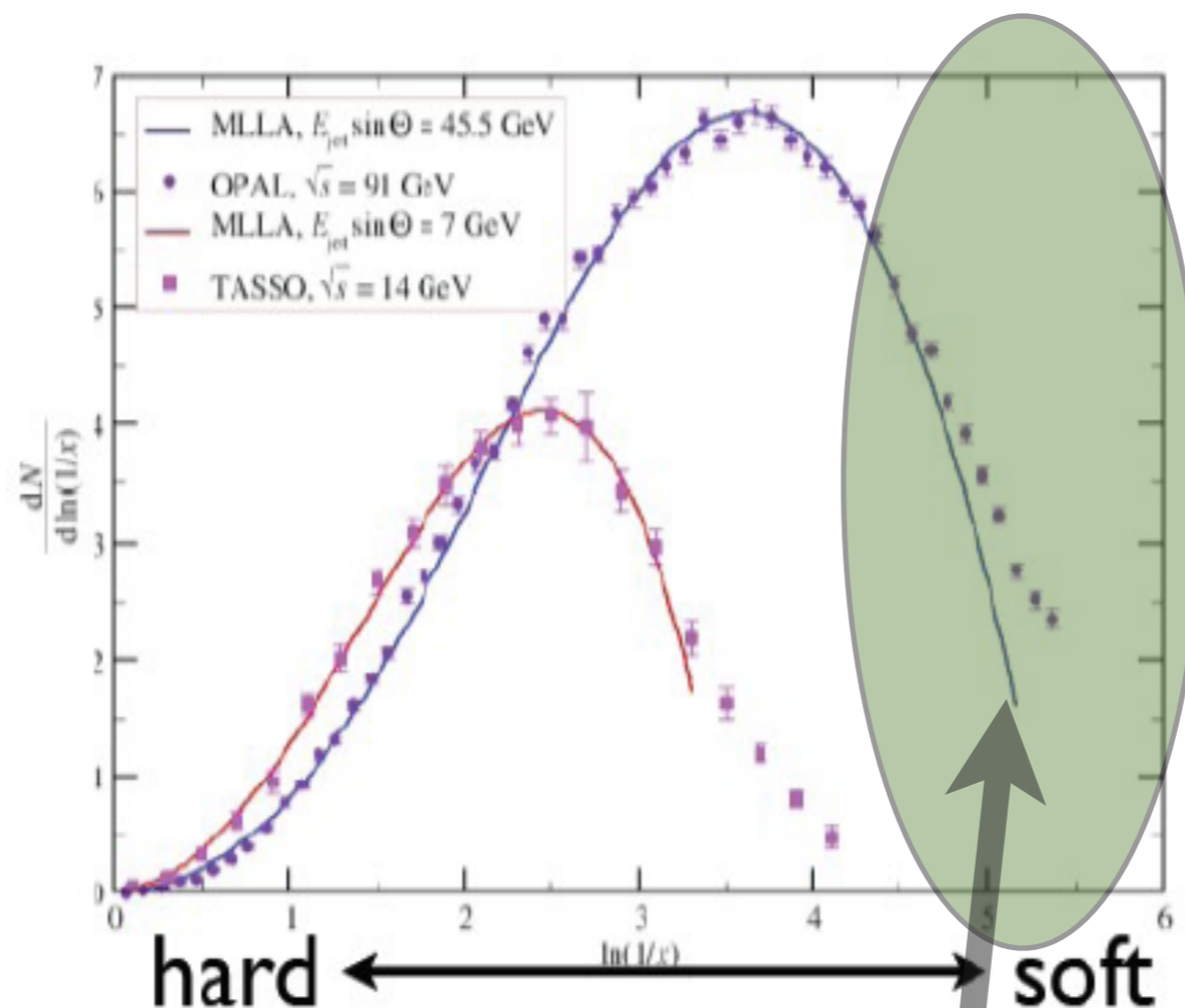


## Coherent spectrum

$$\langle dN_i \rangle_\phi = \frac{\alpha_s C_F}{\pi} \frac{d\omega}{\omega} \frac{d\theta_i}{\theta_i} \Theta(\theta_{qq} - \theta_i)$$

Collinear and soft divergence

# Color coherence: MC implementation and experimental evidence

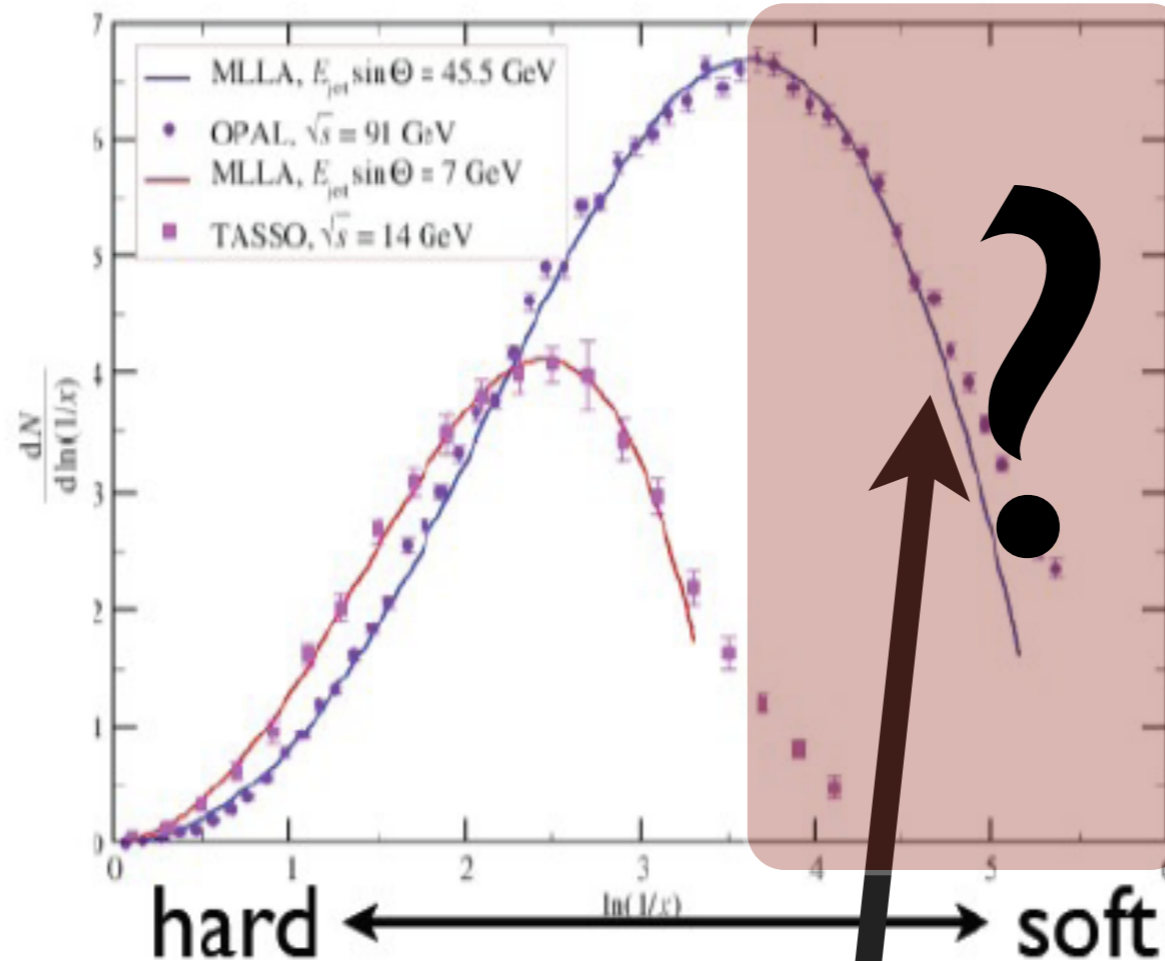


TASSO Collaboration, Z. Phys. C 47 (1990) 187

OPAL Collaboration, Phys. Lett. B 247 (1990) 617

Suppression of soft gluons

# A natural question



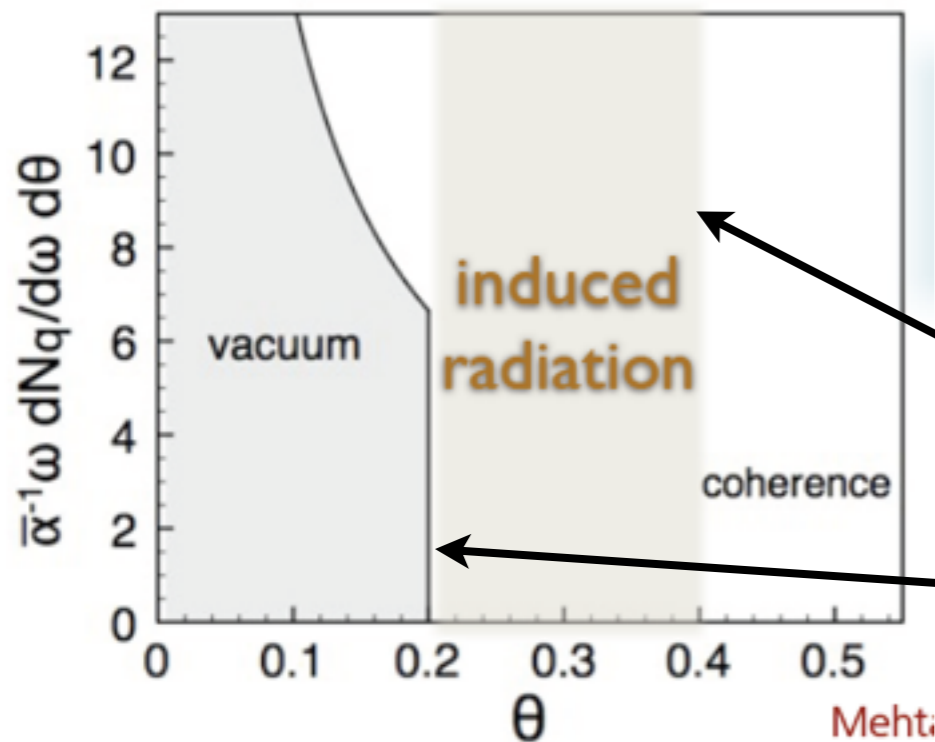
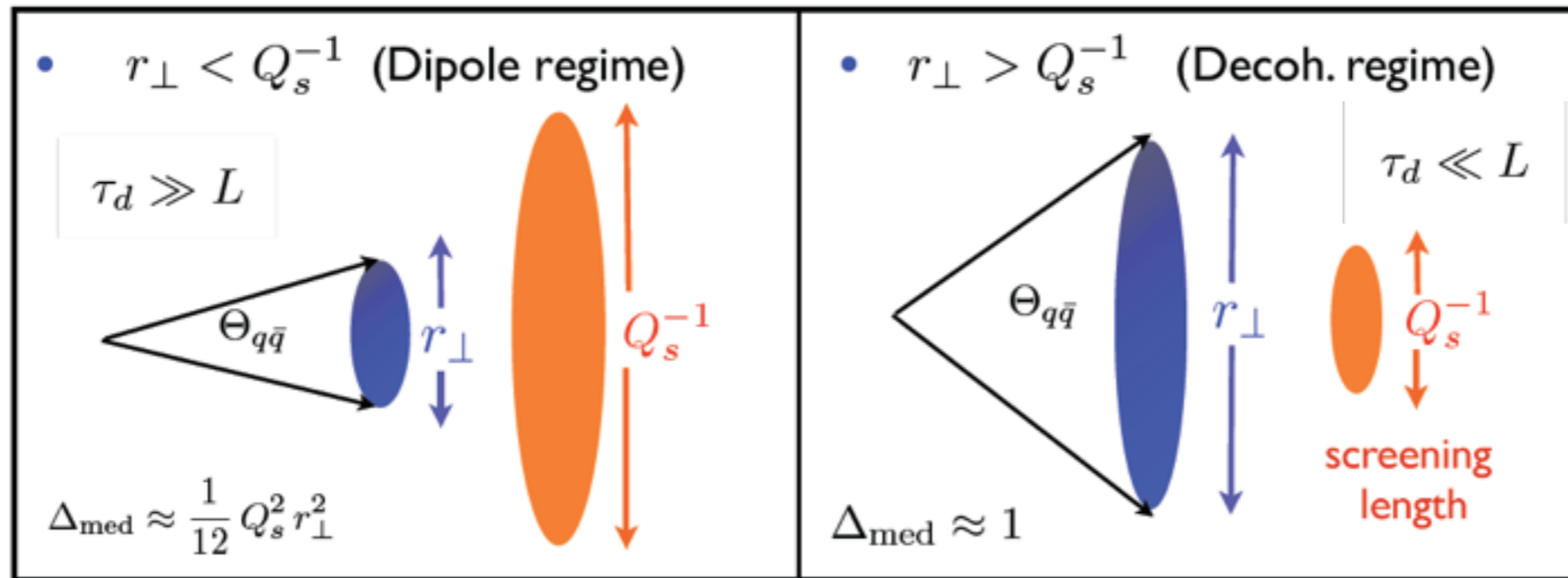
TASSO Collaboration, Z. Phys. C 47 (1990) 187

OPAL Collaboration, Phys. Lett. B 247 (1990) 617

What happens in a QCD medium?



# First steps: antenna inside a QCD medium



$$1 - \Delta_{\text{med}}(t, 0) \simeq \exp \left[ -\frac{1}{12} \hat{q} \theta_{q\bar{q}}^2 t^3 \right] \Rightarrow \tau_d = (\hat{q} \theta_{q\bar{q}}^2)^{-1/3}$$

decoherence parameter characteristic decoherence time

$$Q_{\text{hard}} = \max(r_{\perp}^{-1}, Q_s)$$

$$Q_s^2 = \hat{q}L, \quad r_{\perp} = \theta_{q\bar{q}}L$$

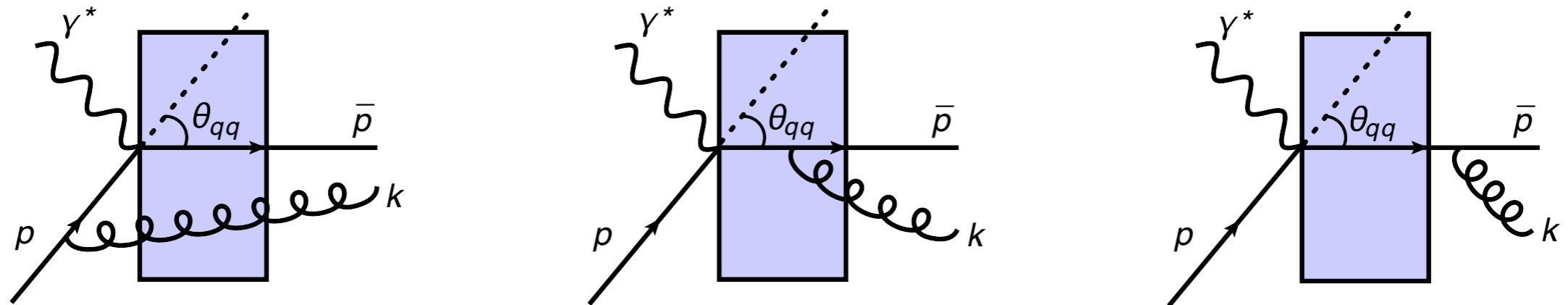
Armesto, Mehtar-Tani, Salgado, Tywoniuk, Iancu, Casalderrey-Solana

# Medium modifications to the initial and final state interference pattern

N. Armesto, Hao Ma, M. Martinez, Yacine Mehtar-Tani, C. Salgado

**Dilute regime:** PLB 717 (2012) 280-286

**Dense regime:** 1308.2186  $\Rightarrow$  *In this talk!!!*

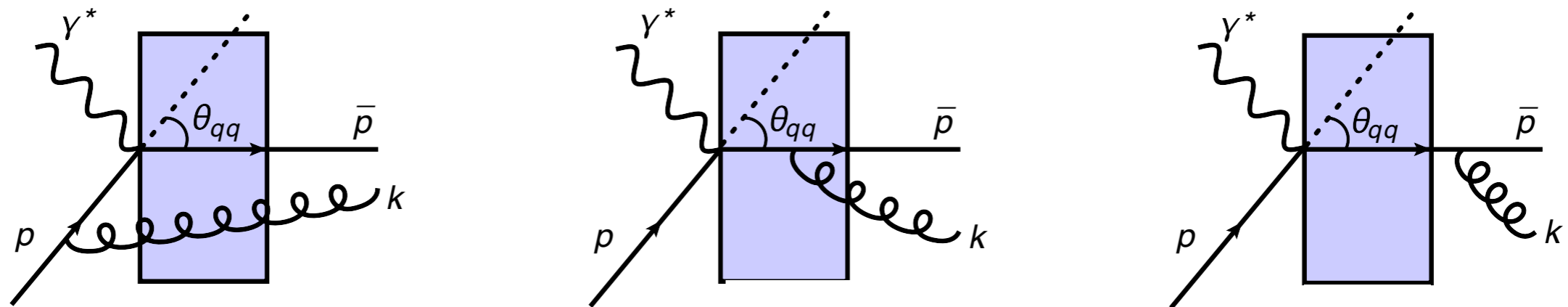


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## GOALS

- ★ Study another configuration relevant to HI collisions
- ★ Playground to investigate medium modifications to the Initial State Radiation

# Classical Yang-Mills Eqs. I

**Evolution of the gauge field:**  $[D_\mu, F^{\mu\nu}] = \mathcal{J}^\nu$

**Color charge conservation:**  $[D_\mu, \mathcal{J}^\mu] = 0$

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**Linearizing around a background field:**  $A^\mu = A_{med}^\mu + a^\mu$

$$\square_x a^i - 2ig [A_{med}^-, \partial_- a^i] = \mathcal{J}^i - \partial^i \left( \frac{\mathcal{J}^+}{\partial_-} \right) \quad \text{LC gauge}$$

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**Reduction formula:**  $\mathcal{M}_\lambda^a = \lim_{k^2 \rightarrow 0} \int d^4x e^{ik \cdot x} \square_x \mathcal{A}_\mu^a(x) \epsilon_\lambda^\mu(\vec{k})$

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**Gluon spectrum:**

$$(2\pi)^3 2k^+ \frac{dN}{d^3k} = \sum_{\lambda=1,2} |\mathcal{M}_\lambda^a(\vec{k})|^2$$

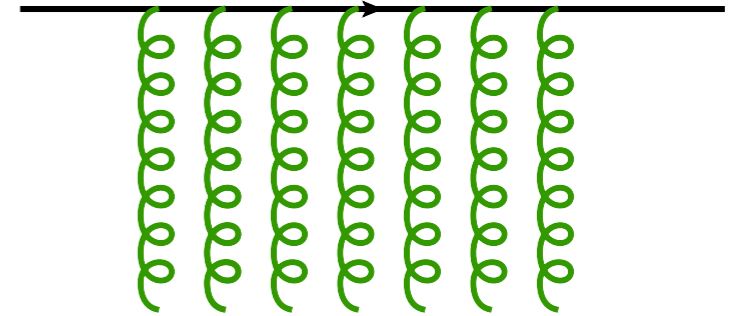


# Classical Yang-Mills Eqs. II

**Eikonal parton in a background field:**

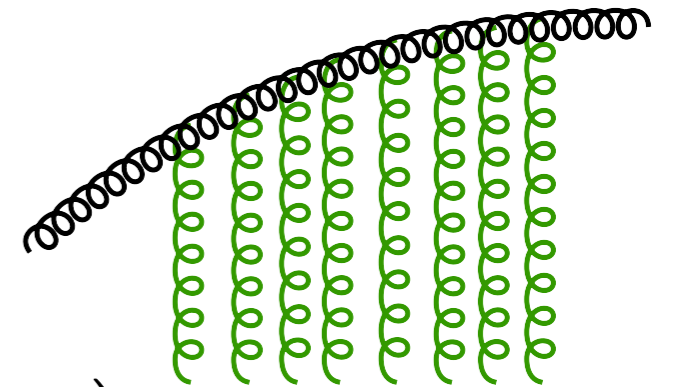
$$\mathcal{J}^\mu(x)_a = g v^\mu \mathcal{U}^{ab}(x^+, 0) \delta^3(\vec{x} - \vec{v}t) \theta(t) Q_b$$

$$\mathcal{U}^{ab}(x^+, y^+) = \mathcal{P} \exp \left[ ig \int_{y^+}^{x^+} dz^+ \mathcal{A}_{med}^-(z^+, \mathbf{r}(z^+)) \right]^{ab}$$



**Soft gluon follows a non-eikonal trajectory**

$$\mathcal{G}_{ab}(x^+, \mathbf{x}; y^+, \mathbf{y} | k^+) = \int_{\mathbf{r}(y^+) = \mathbf{y}}^{\mathbf{r}(x^+) = \mathbf{x}} \mathcal{D}\mathbf{r} \exp \left( i \frac{k^+}{2} \int_{y^+}^{x^+} dz \dot{\mathbf{r}}^2(z) \right) \mathcal{U}_{ab}(x^+, y^+)$$



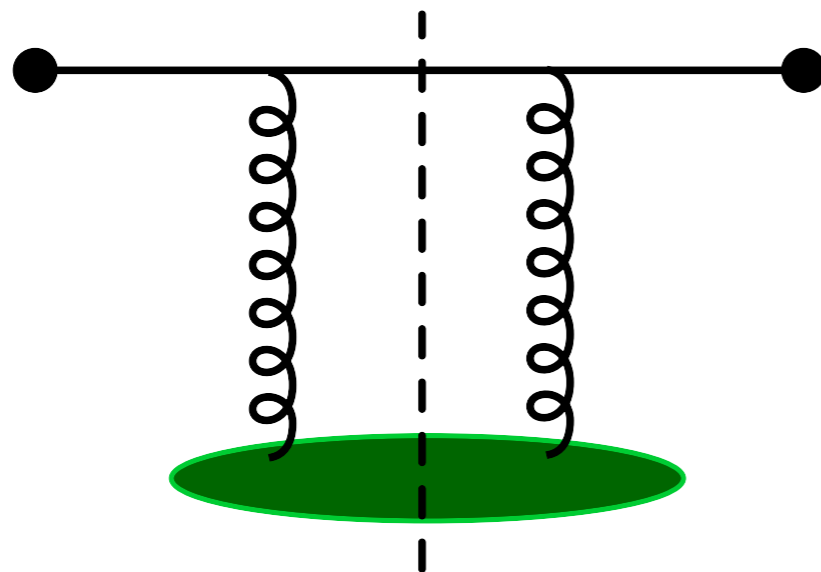
# Modeling the medium

Medium is described as a classical background field:

$$-\partial_{\mathbf{x}}^2 \mathcal{A}_{med}^-(x^+, \mathbf{x}) = \rho(x^+, \mathbf{x})$$

The distribution of color charges is considered to be a Gaussian noise:

$$\langle \mathcal{A}_{med}^{a,-}(x^+, \mathbf{q}) \mathcal{A}_{med}^{*b,-}(x'^+, \mathbf{q}') \rangle = \delta^{ab} n(x^+) \delta(x^+ - x'^+) \delta^{(2)}(\mathbf{q} - \mathbf{q}') \mathcal{V}^2(\mathbf{q})$$

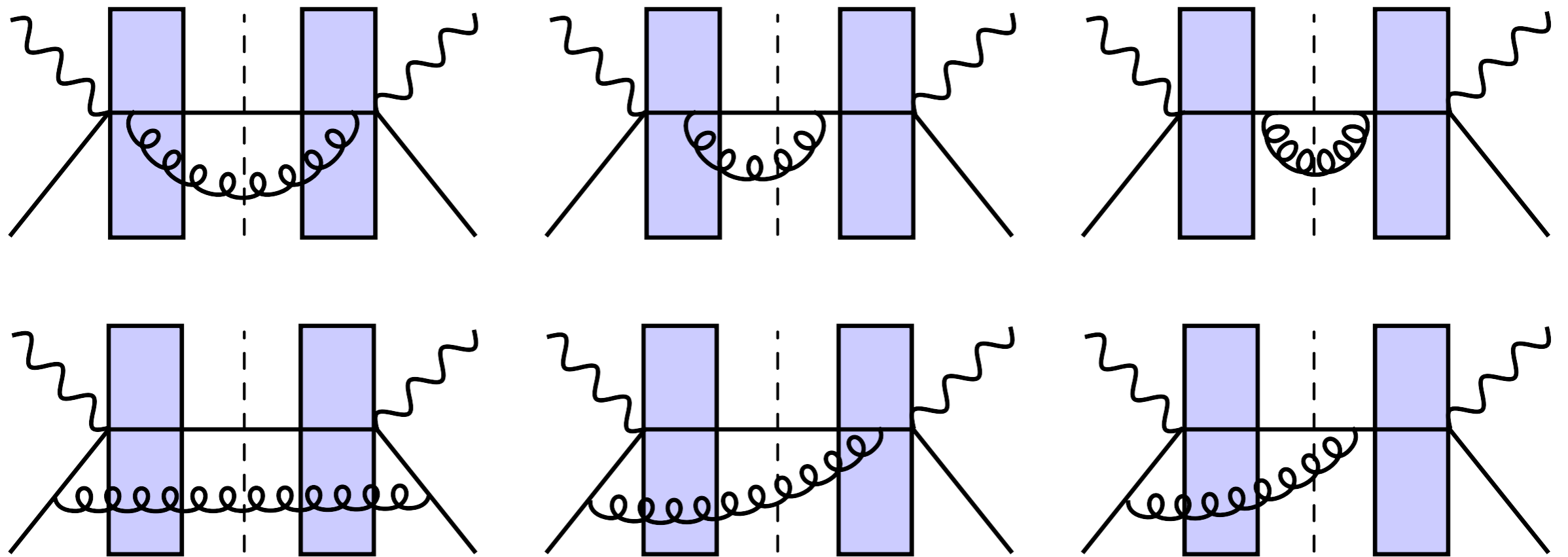


$$\lambda_{mfp} \gg m_D^{-1}$$

$$\mathcal{V}^2(\mathbf{q}) = \frac{m_D^2}{(2\pi)^2 (\mathbf{q}^2 + m_D^2)^2}$$

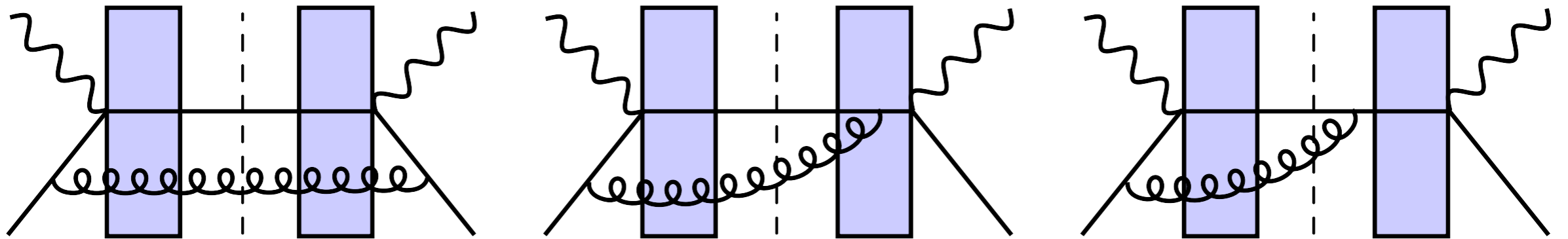
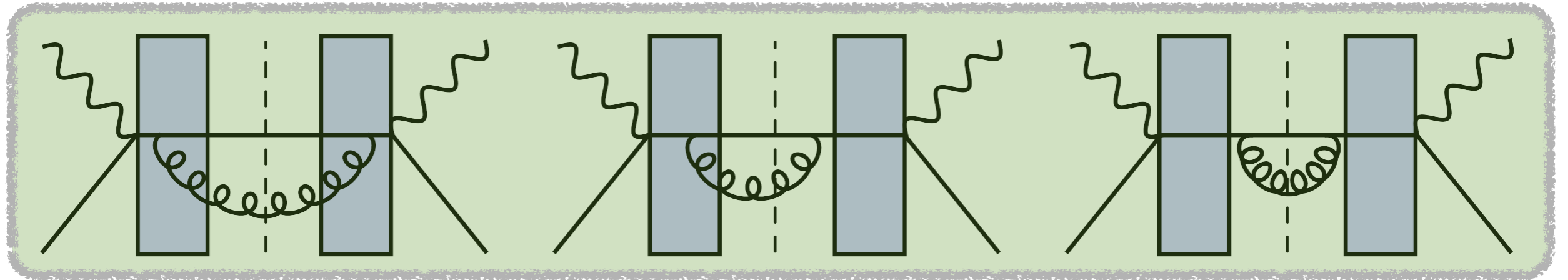
Gyulassy-Wang model: Nucl. Phys. B 420, (1994) 583

# Gluon spectrum



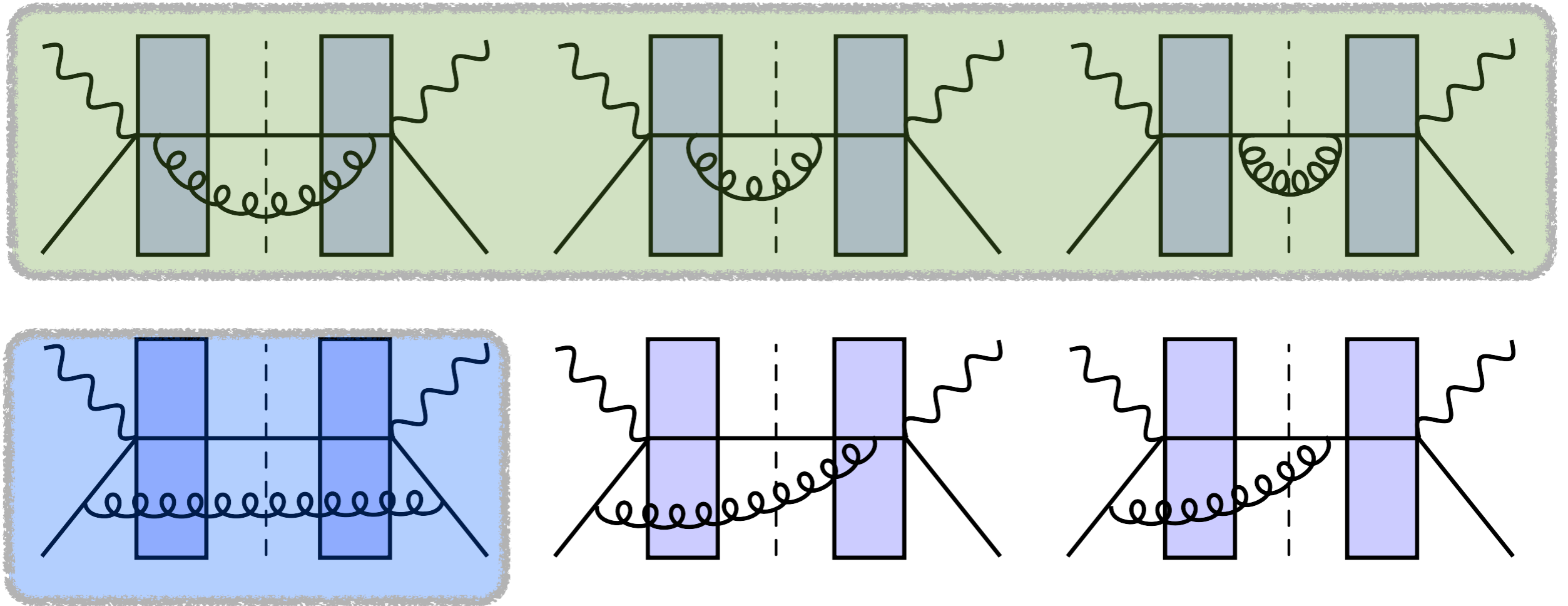
# Gluon spectrum

## BDMPS-Z + vacuum



# Gluon spectrum

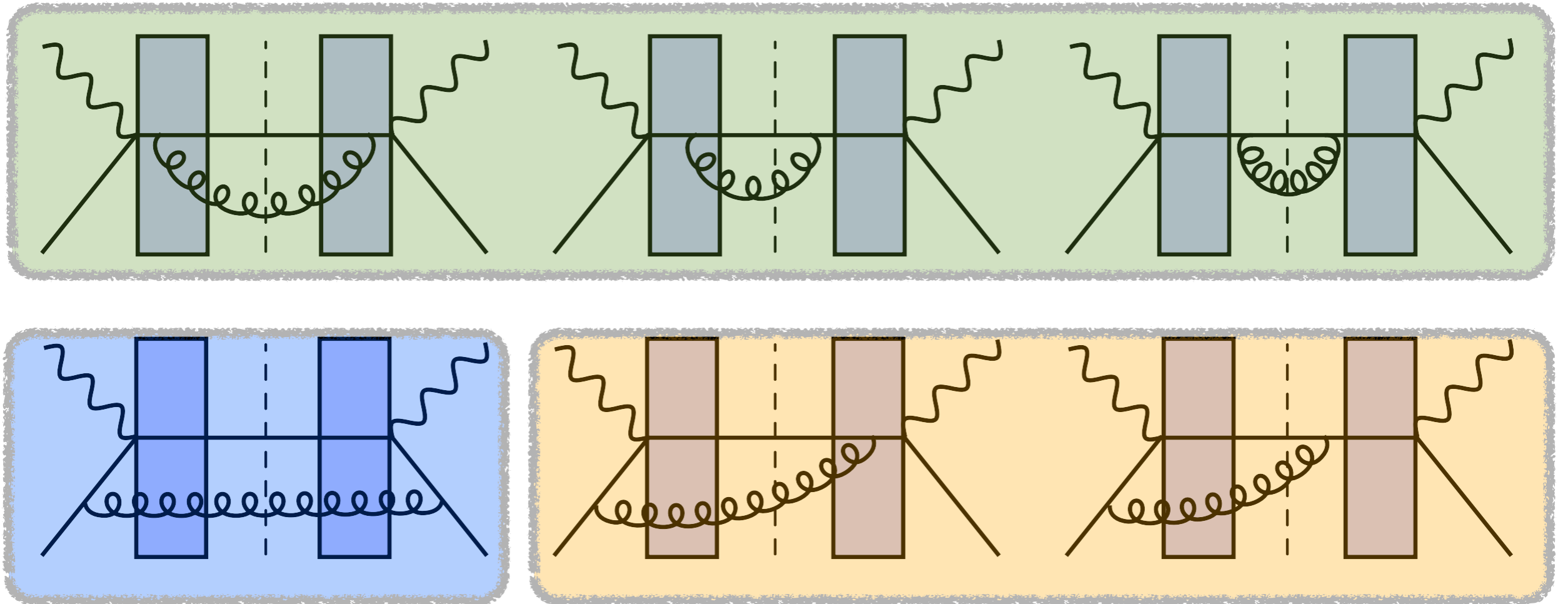
## BDMPS-Z + vacuum



**$P_T$  broadening  
of ISR**

# Gluon spectrum

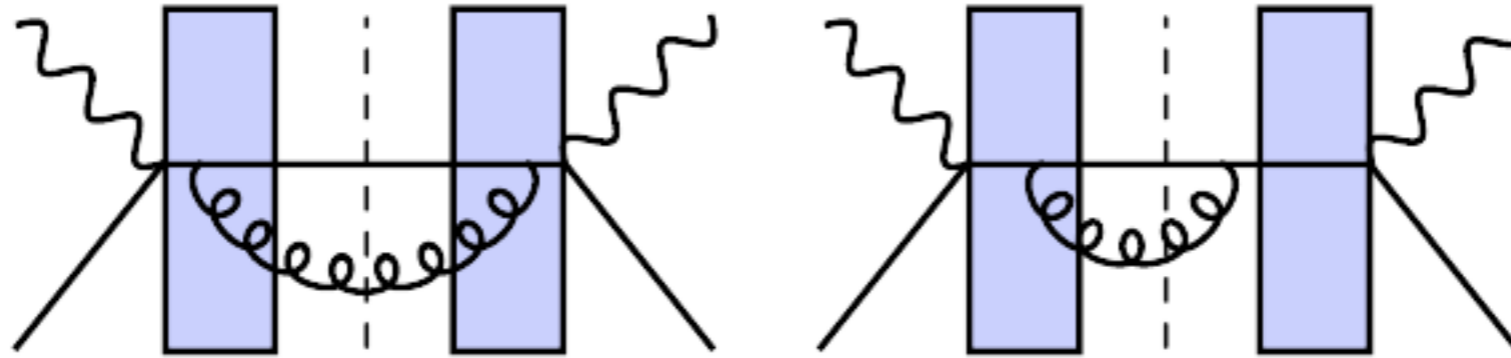
## BDMPS-Z + vacuum



$P_T$  broadening  
of ISR

Interferences in the medium: *New!!*

# BDMPS-Z



$$k_f = \sqrt{\omega \hat{q}}$$

$$\sim \int_0^L dt' \int \frac{d^2 \mathbf{k}'}{(2\pi)^2} \mathcal{P}(\mathbf{k} - \mathbf{k}', L - t') \sin\left(\frac{k'^2}{2k_f^2}\right) e^{-\frac{k'^2}{2k_f^2}}$$

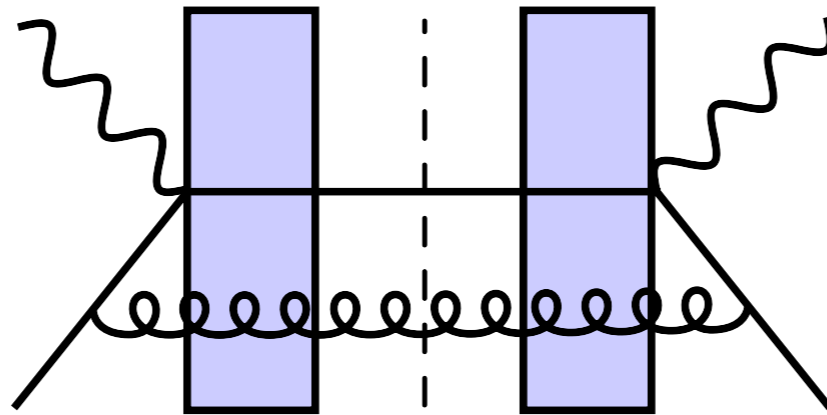
$$\mathcal{P}(k, \xi) = \frac{4\pi}{\hat{q}\xi} e^{-\frac{k^2}{\hat{q}\xi}}$$

Medium induced radiation is a two step process

- Quantum emission + classical broadening
- Scales with the length of the medium



# P<sub>T</sub> broadening of ISR



$$\mathcal{P}(k, \xi) = \frac{4\pi}{\hat{q}\xi} e^{-\frac{k^2}{\hat{q}\xi}}$$

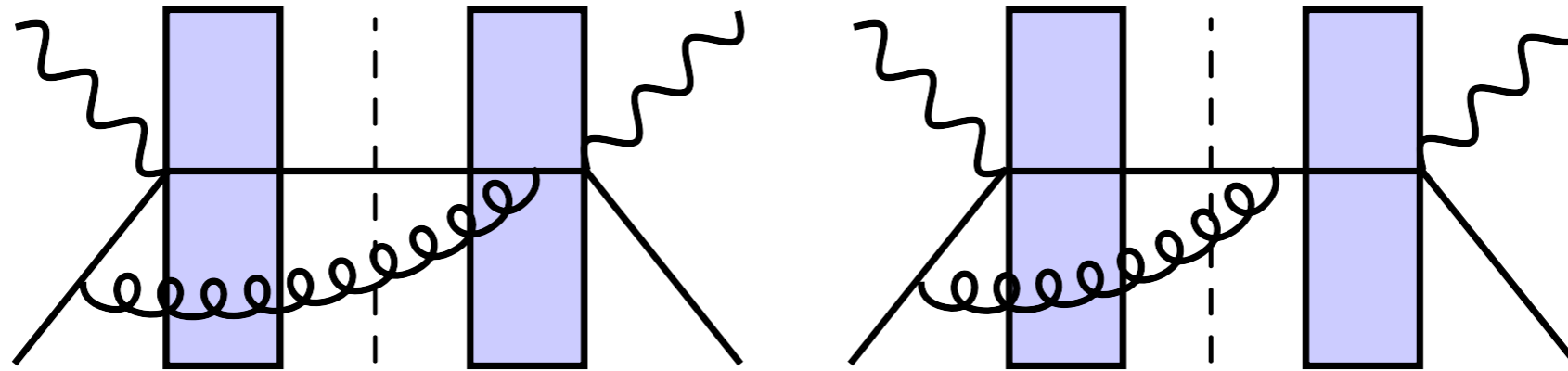
$$\sim \int \frac{d^2 \mathbf{k}'}{(2\pi)^2} \frac{\mathcal{P}(\mathbf{k}' - \bar{\mathbf{k}}, L^+)}{k'^2}$$

P<sub>T</sub> broadening of ISR is a two step process:

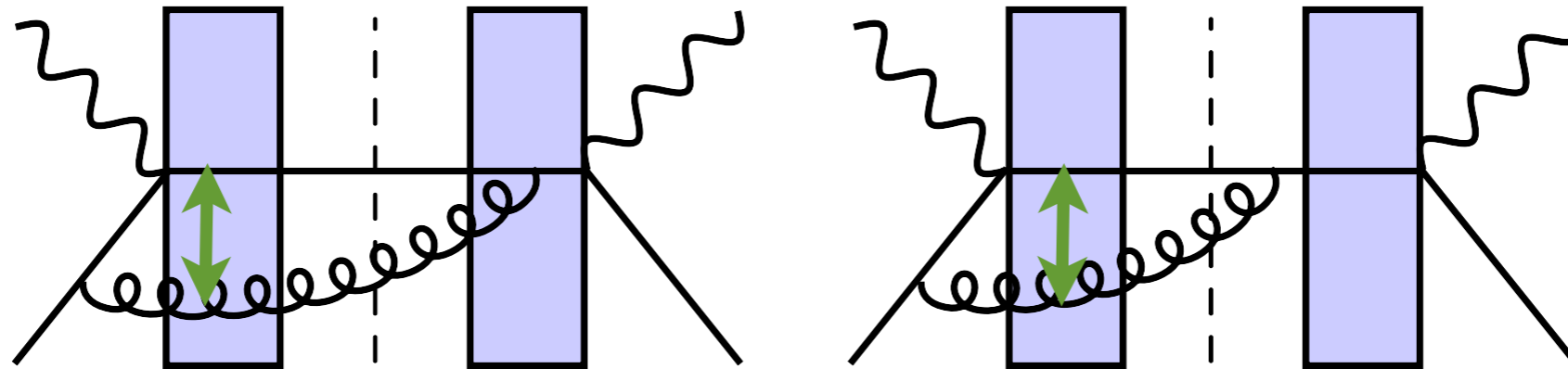
- Collinear Emission + classical broadening
- Reshuffling of the momentum of the gluon emissions

⇒ Typical value of the gluon momenta  $\sim Q_s = \hat{q}L$

# Interferences



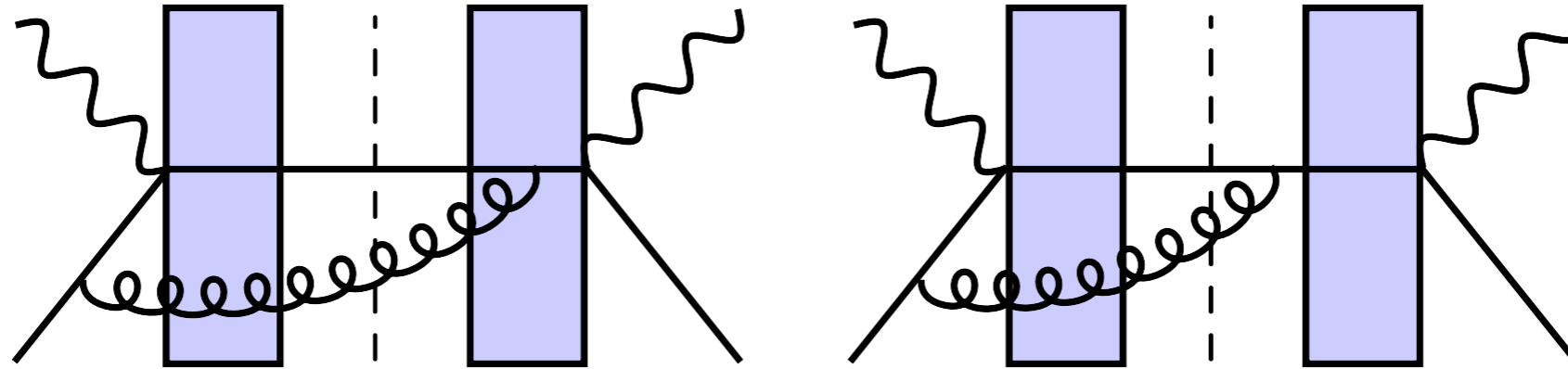
# Interferences



## Transverse size of the Quark-gluon system

- If hard scattering is the largest scale:  
⇒ Insensitive to the medium
- If typical medium induced momentum is the largest scale  
⇒ Medium is able to resolve the qg system

# Interferences

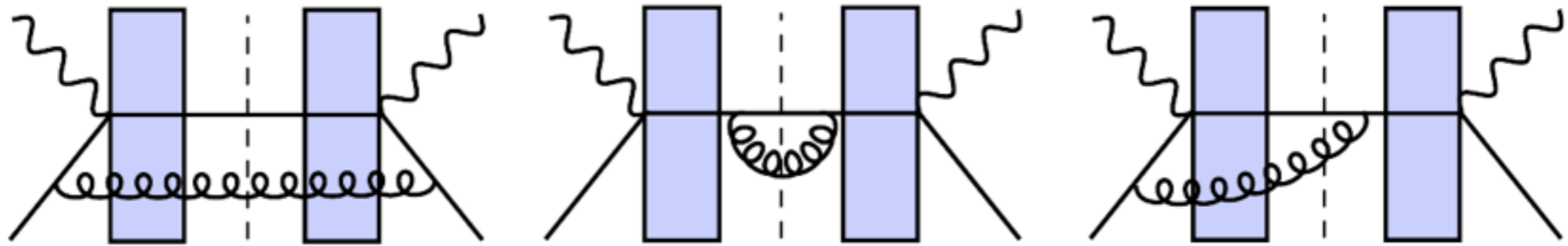


The Color correlation of the Quark-gluon system is measured by

$$\mathcal{K}(x^+, \mathbf{x}; y^+, \mathbf{y} | k^+) = \int_{r(y^+) = \mathbf{y}}^{r(x^+) = \mathbf{x}} \mathcal{D}\mathbf{r} \exp \left[ \int_{y^+}^{x^+} d\xi \left( i \frac{k^+}{2} \dot{\mathbf{r}}^2(\xi) - \frac{1}{2} n(\xi) \sigma(\mathbf{r}(\xi)) \right) \right]$$

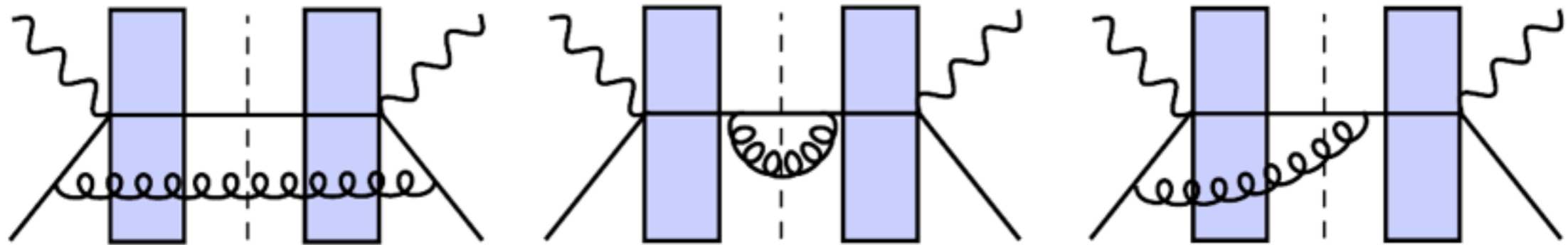
- Describes the Brownian motion of the gluon
- Harmonic oscillator approximation:  $n\sigma(\mathbf{r}) \approx \hat{q}\mathbf{r}^2$
- Two extreme limits
  - $\Rightarrow$  High Energy Limit (Shockwave)  $\tau_f \gg L$
  - $\Rightarrow$  "Infinite" medium length  $\tau_f \ll L$

# Gluon spectrum: High Energy limit

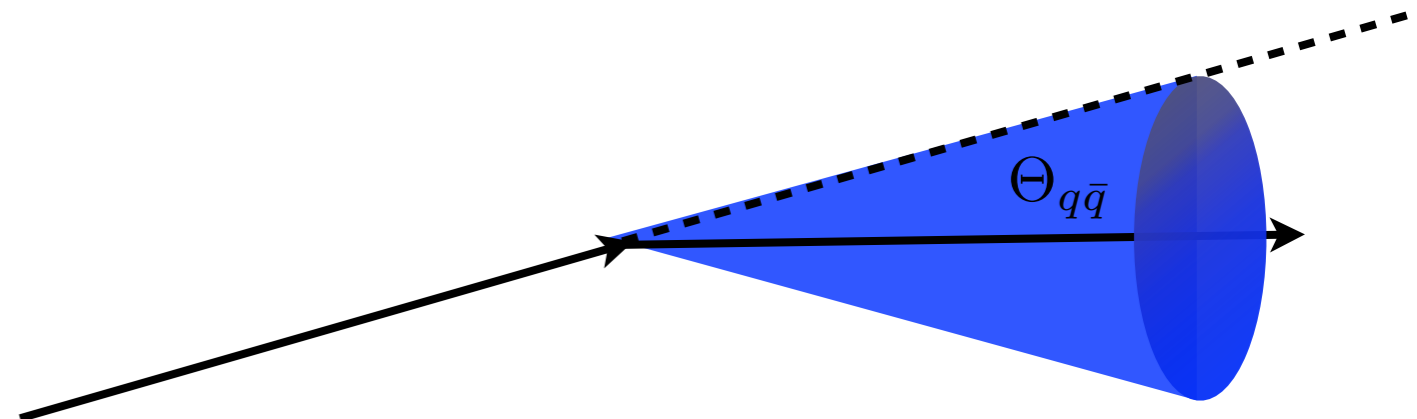
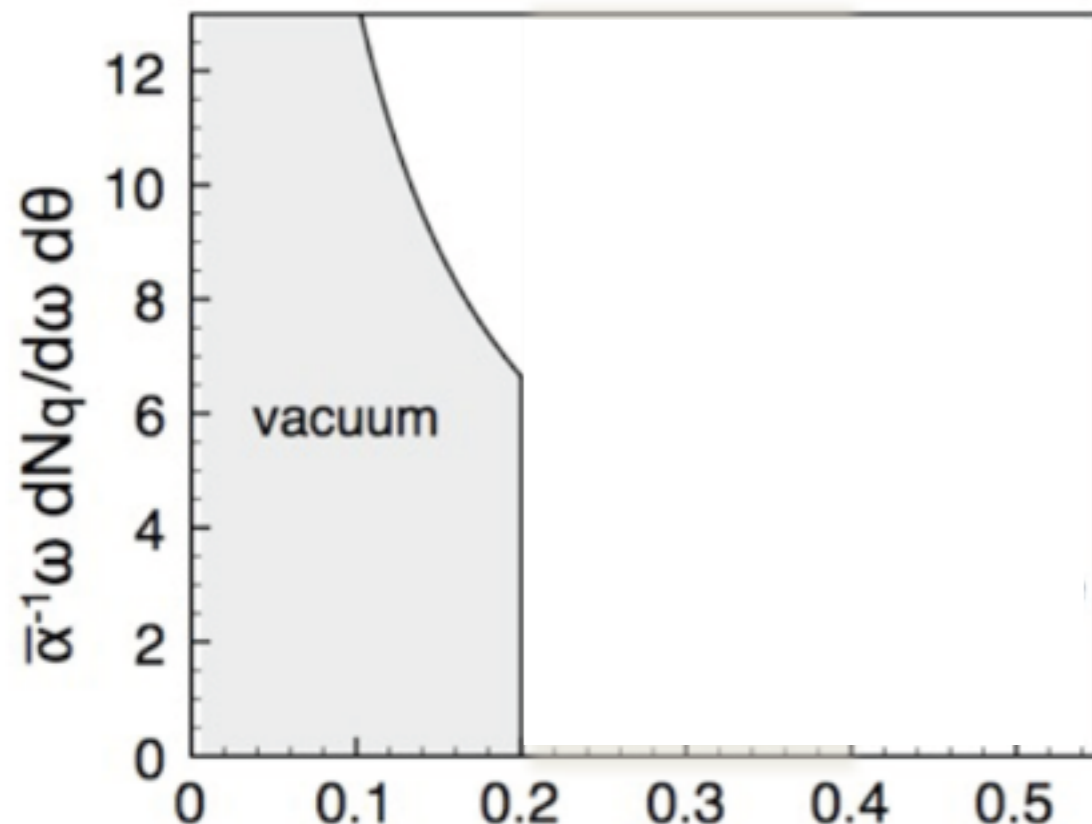


- Medium acts as a unique scattering center
- Interferences are suppressed if  $\mathbf{k} < Q_s$
- Vacuum color coherence is reestablished for  $\mathbf{k} > Q_s$

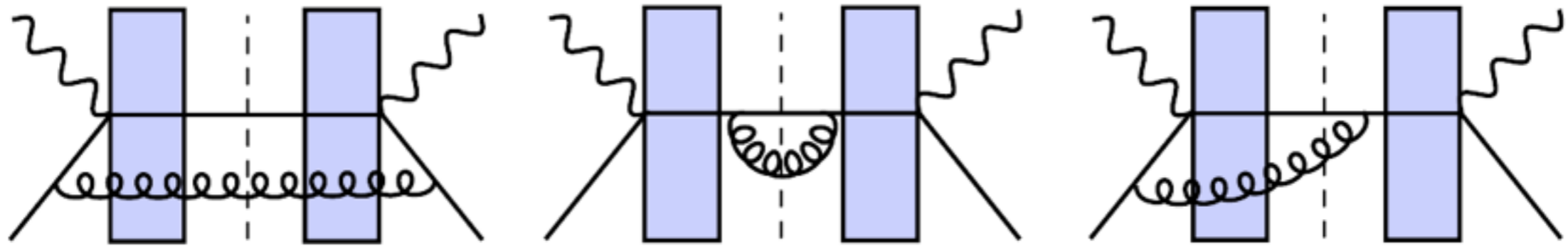
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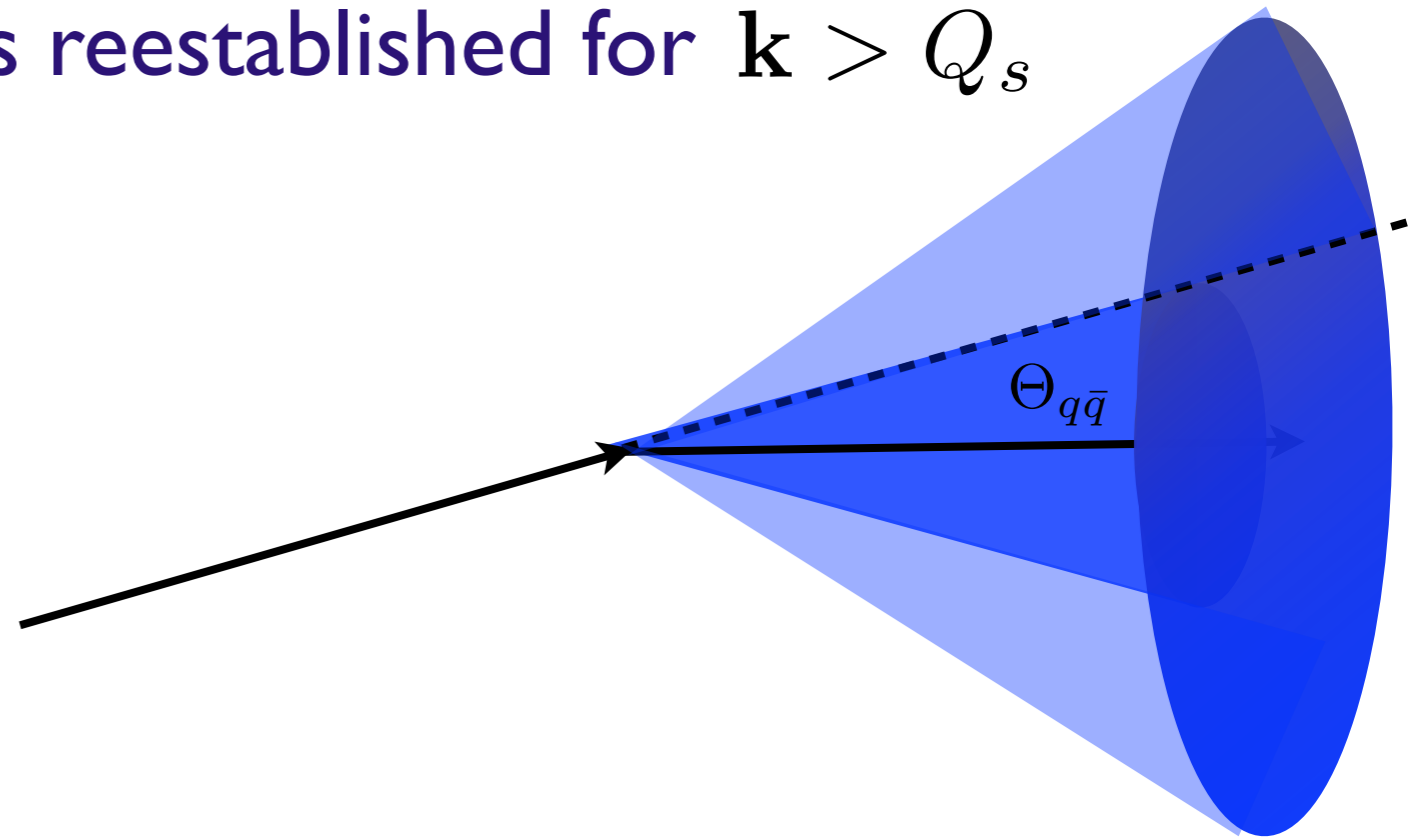
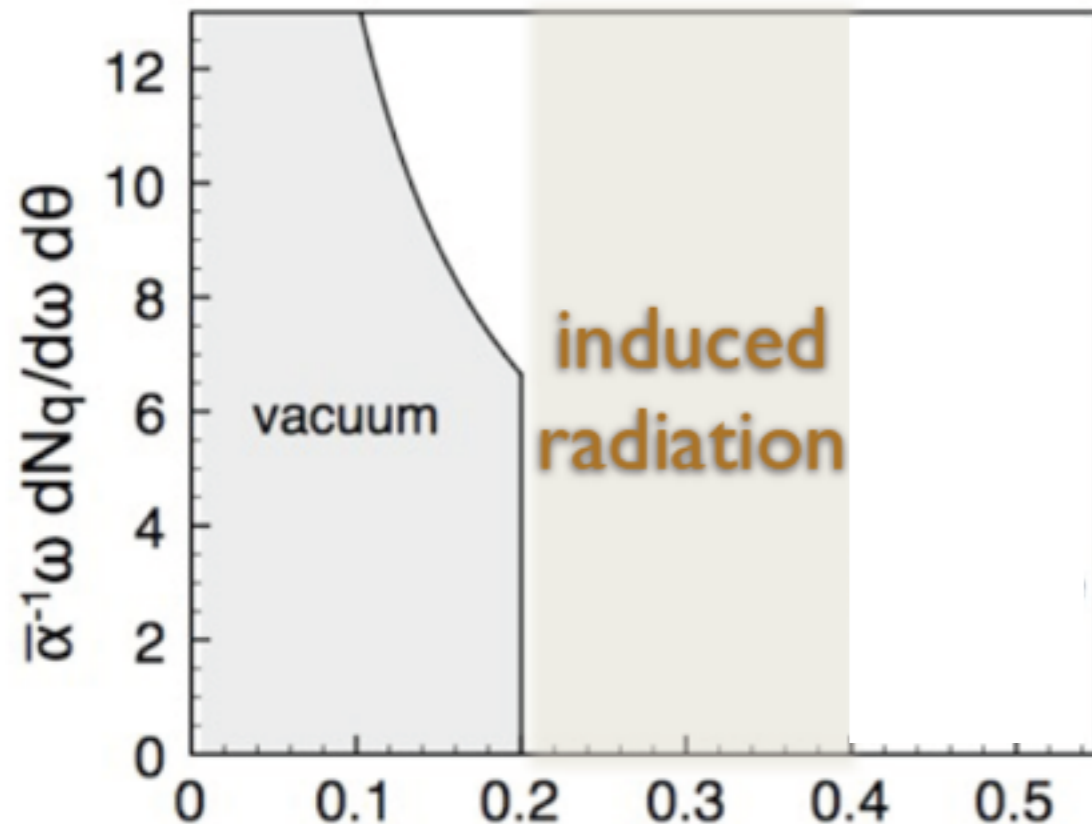
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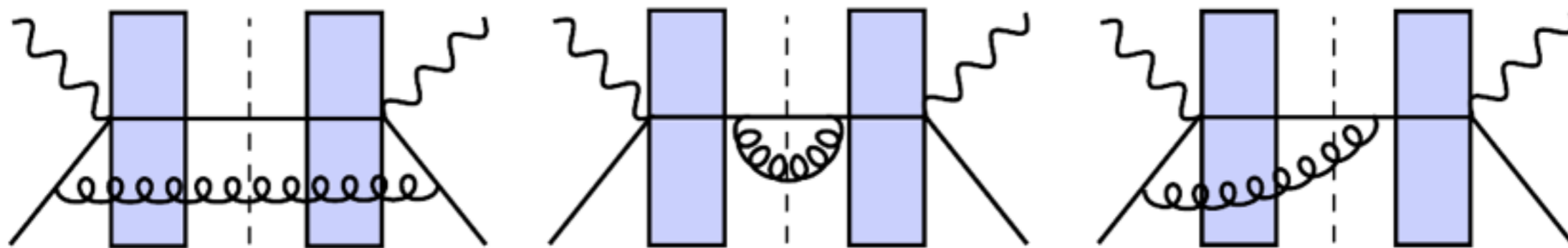


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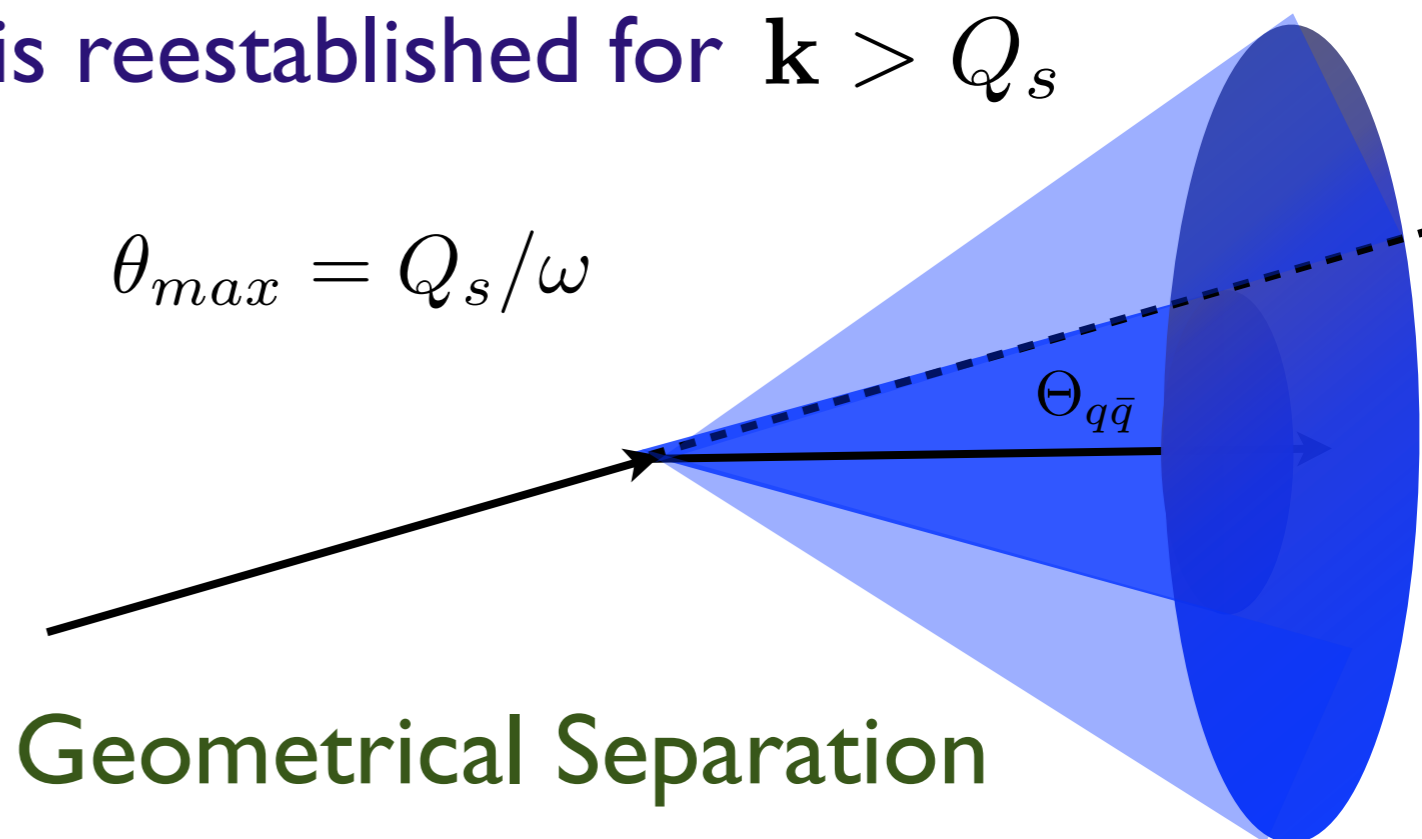
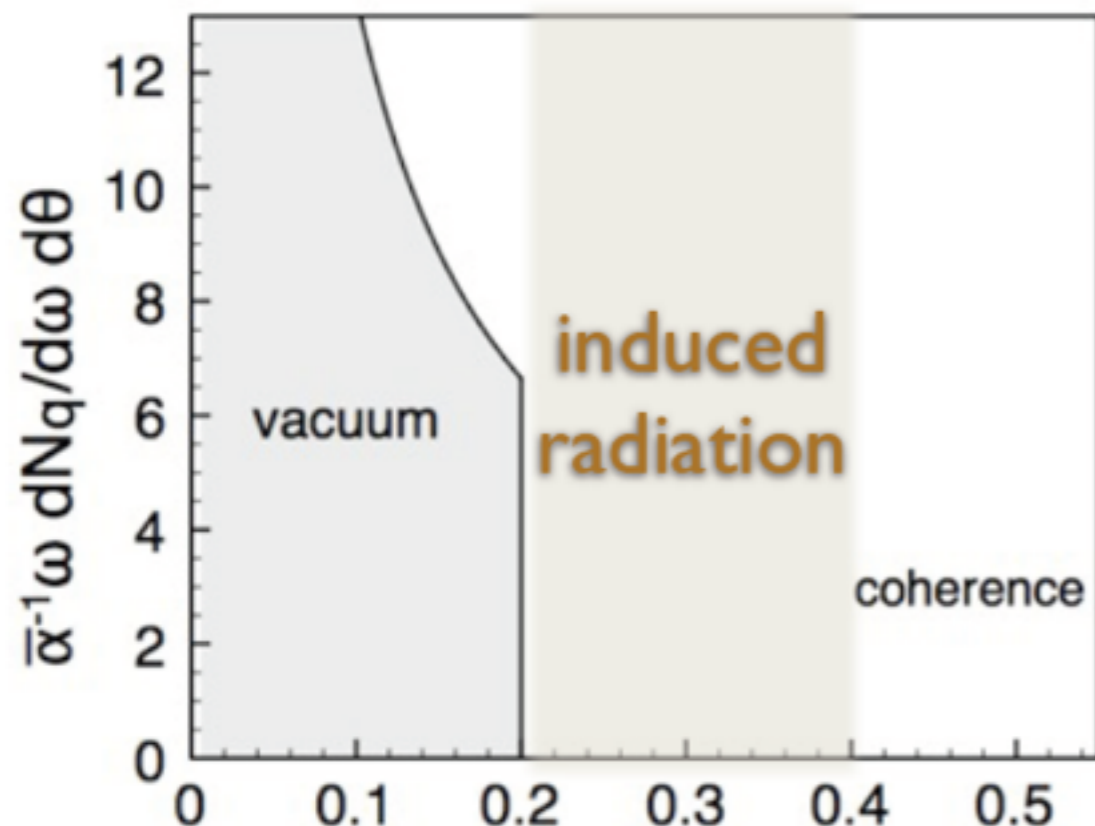




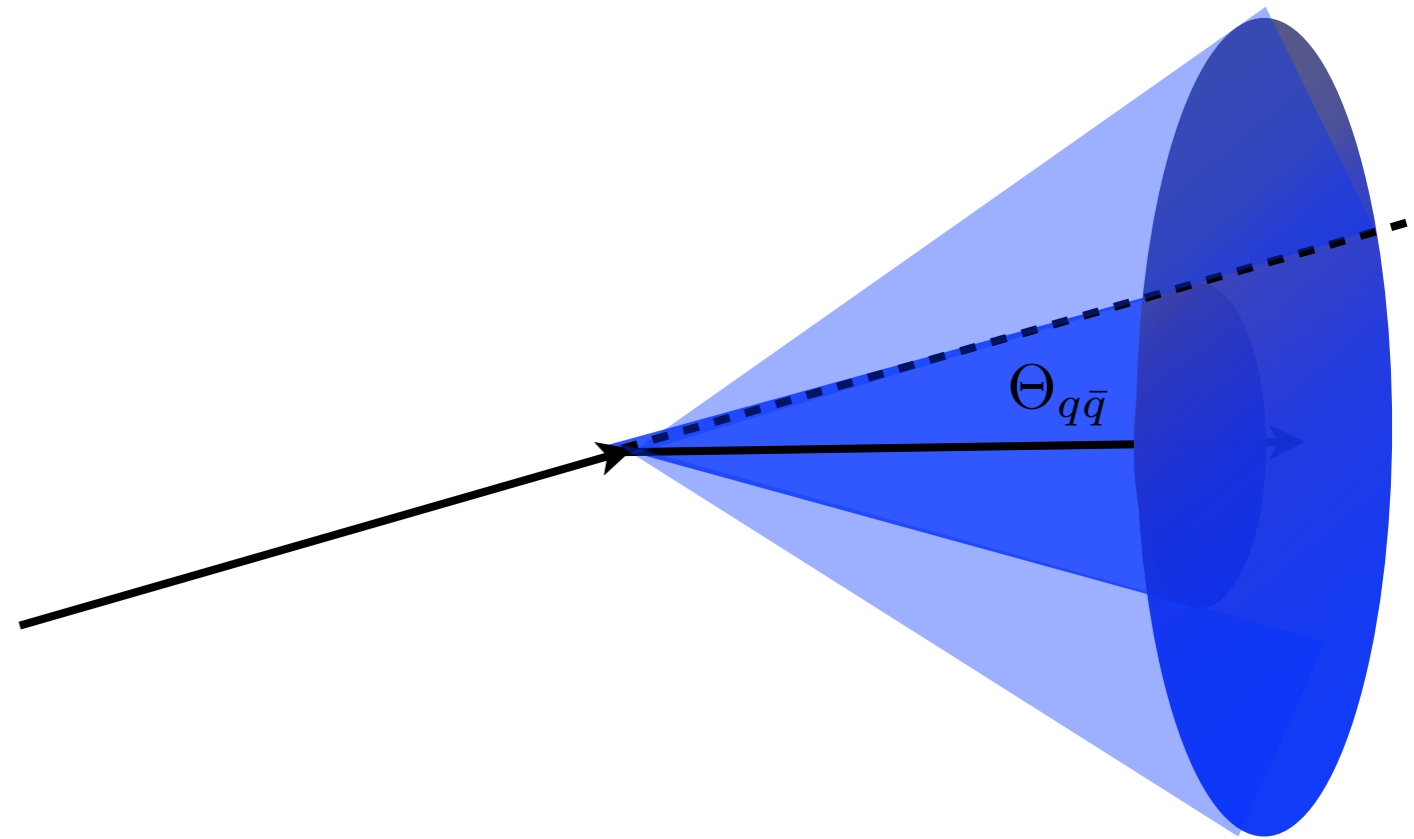
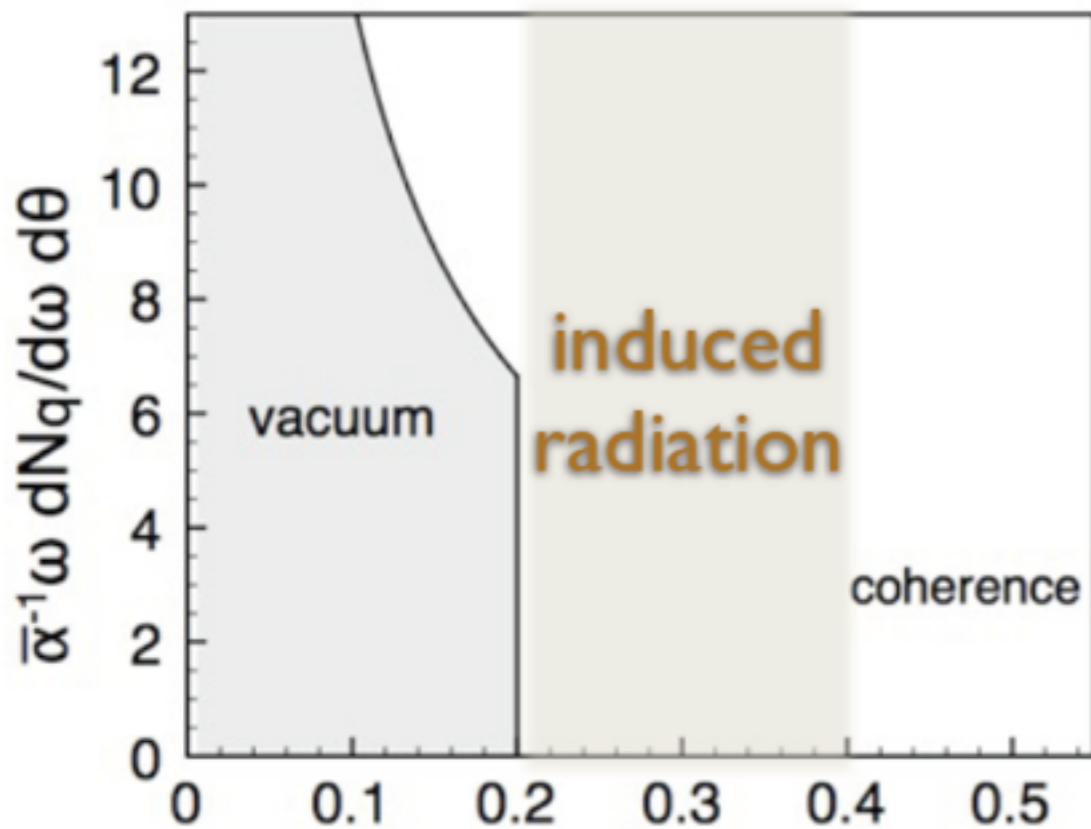
# Gluon spectrum: High Energy limit



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# Gluon spectrum: “Infinite” medium limit



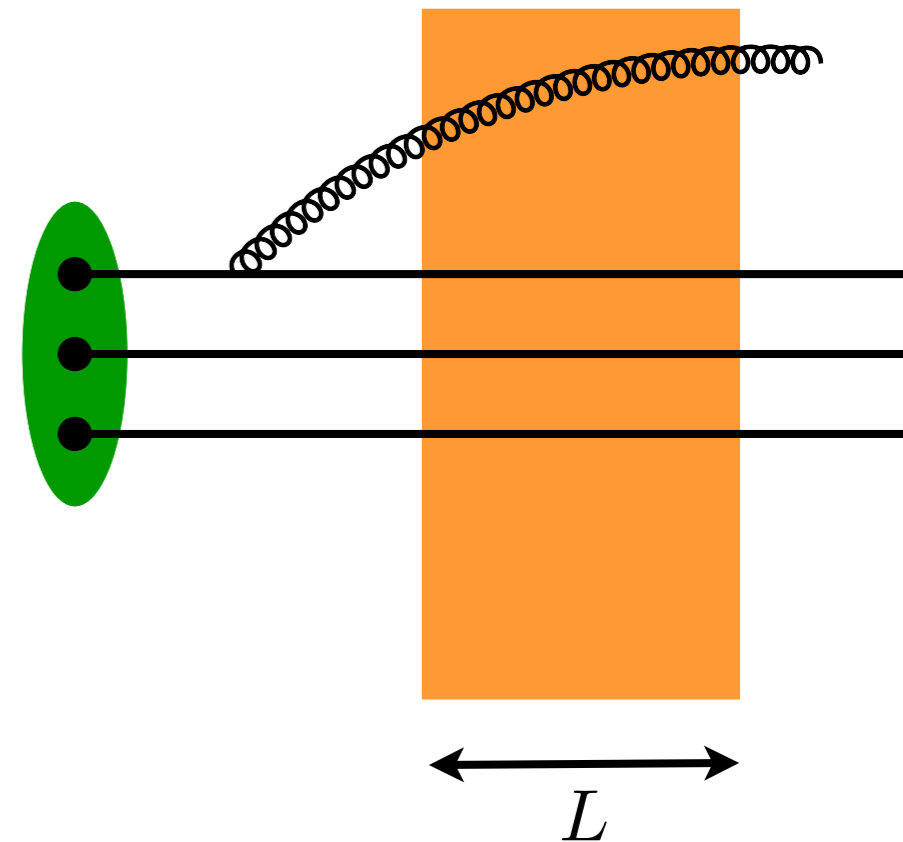
- Interferences play a role at early-times
- Gluon loses vacuum coherence  
 $\Rightarrow$  Open phase space at large angle emissions up to  $\theta_{max} = Q_s/\omega$
- Typical “medium induced” gluon momentum  $\sim Q_s = \hat{q}L$

# pA case

We want:

⇒ Include finite target size effects !!!!

⇒ Study color decoherence in pA !!!!

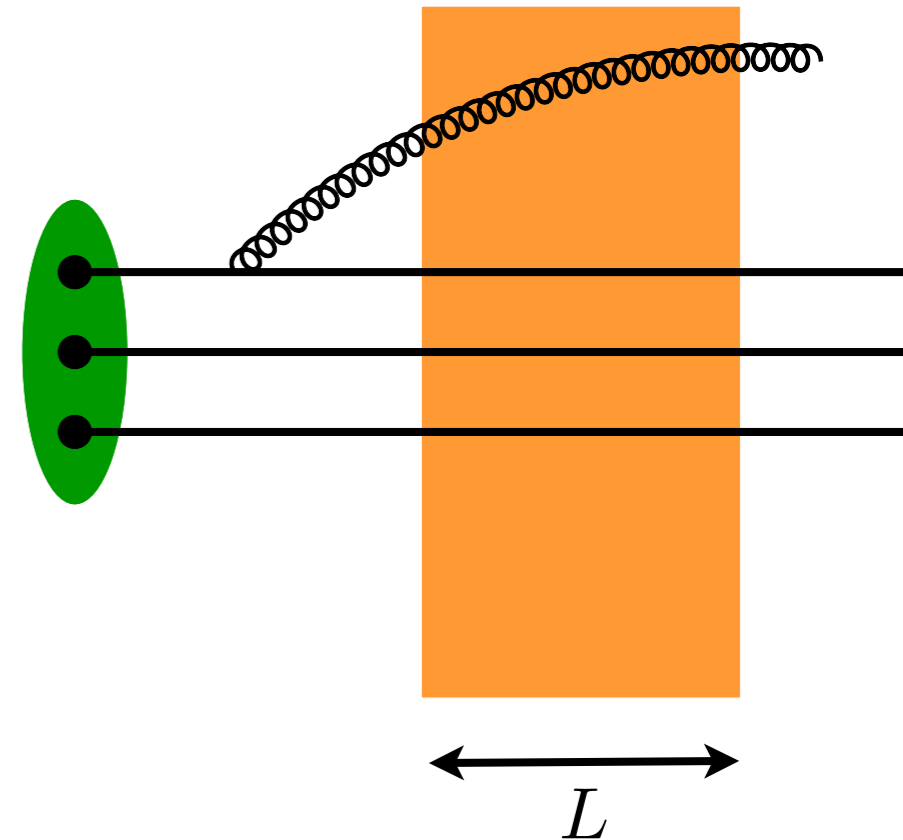


Work in progress (Altinoluk, Armesto, Beuf, Martinez, Salgado)

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- Projectile described by QCD parton model

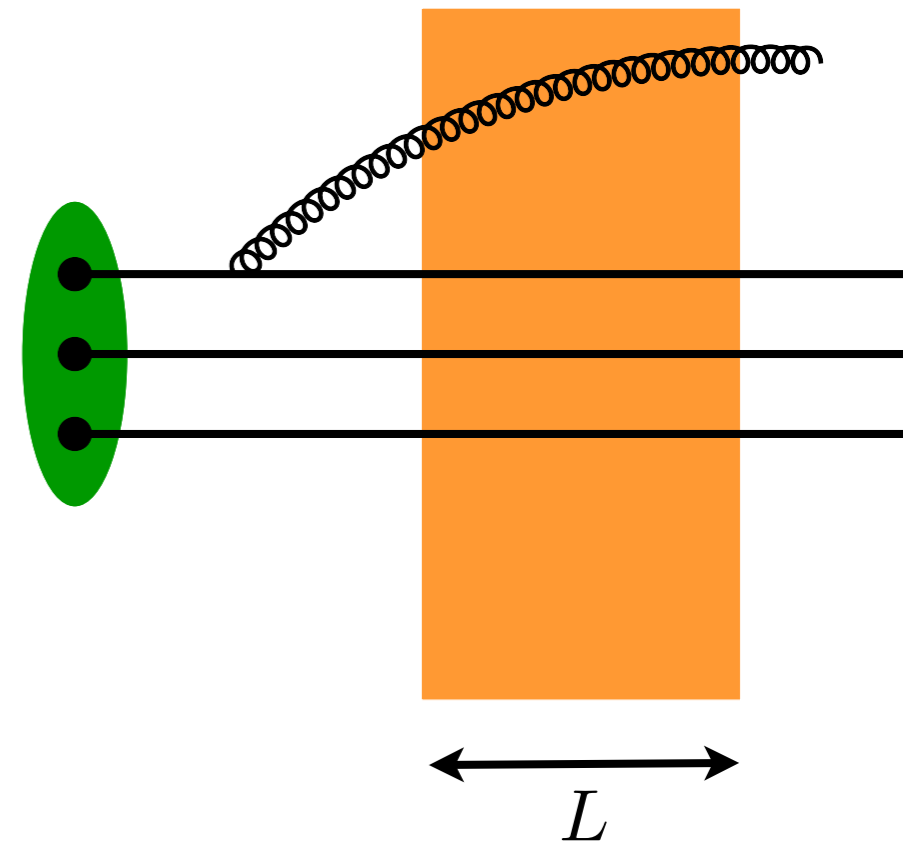


Work in progress (Altinoluk, Armesto, Beuf, Martinez, Salgado)

# pA case

We want:

- ⇒ Include finite target size effects !!!!
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- Projectile described by QCD parton model
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Work in progress (Altinoluk, Armesto, Beuf, Martinez, Salgado)

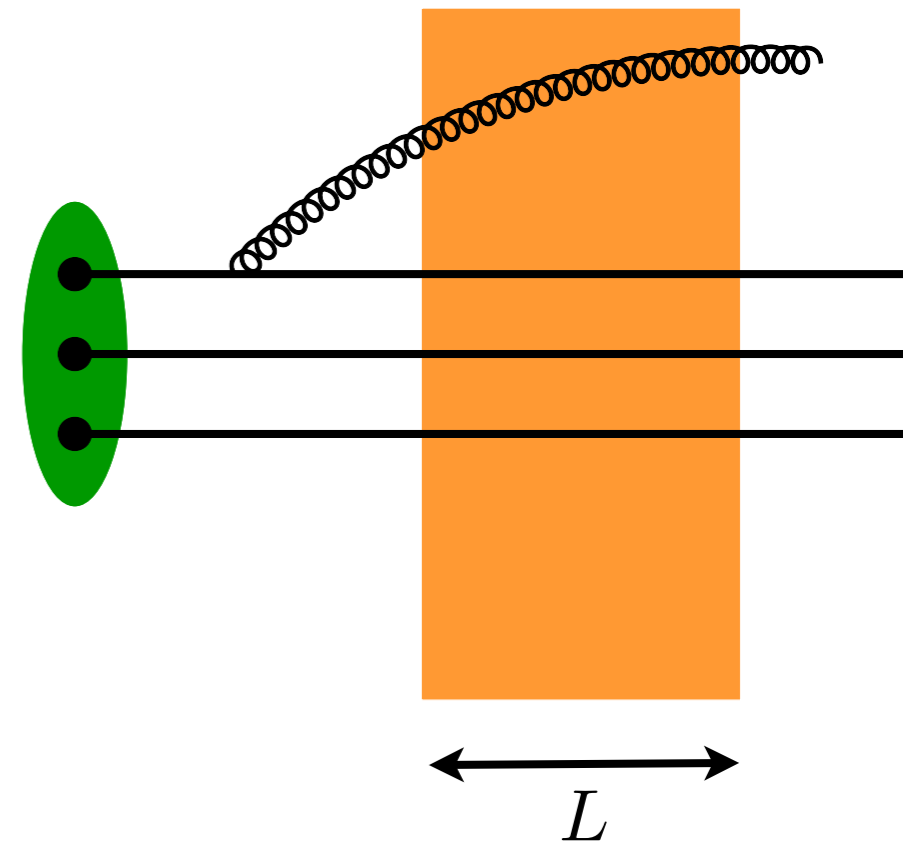
# pA case

We want:

⇒ Include finite target size effects !!!!

⇒ Study color decoherence in pA !!!!

- Projectile described by QCD parton model
- Target described by a gaussian distr. of color charges.
- Emitted gluon follows a non-eikonal trajectory.



Work in progress (Altinoluk, Armesto, Beuf, Martinez, Salgado)

# pA case

Factorized formula:

Finite medium size corrections + Color decoherence effects

$$\omega \frac{dN}{d^3k} \sim \frac{g^2}{\pi^2} \int_{\mathbf{y}, \mathbf{z}, \bar{\mathbf{y}}, \bar{\mathbf{z}}, \mathbf{y}^+, \bar{\mathbf{y}}^+} e^{-i\mathbf{k} \cdot (\mathbf{z} - \bar{\mathbf{z}})} \frac{(\bar{\mathbf{z}} - \bar{\mathbf{y}}) \cdot (\mathbf{z} - \mathbf{y})}{(\bar{\mathbf{z}} - \bar{\mathbf{y}})^2 (\mathbf{z} - \mathbf{y})^2} \text{Probability to emit a soft gluon}$$

$$\left\{ \begin{aligned} & \delta_0 \int_{\bar{\mathbf{z}}'} e^{-i\mathbf{k} \cdot (\bar{\mathbf{z}} - \bar{\mathbf{z}}')} \mathcal{G}^\dagger(L^+, \bar{\mathbf{z}}'; \bar{\mathbf{y}}^+, \bar{\mathbf{z}}) \\ & - \mathcal{U}^\dagger(\bar{\mathbf{y}}^+, 0, \bar{\mathbf{y}}) \left[ \delta_{L^+} - \frac{1}{ik^+} \int_{\bar{\mathbf{z}}'} e^{-i\mathbf{k} \cdot (\bar{\mathbf{z}} - \bar{\mathbf{z}}')} \tilde{\partial}^{\bar{\mathbf{z}}} \mathcal{G}^\dagger(L^+, \bar{\mathbf{z}}'; \bar{\mathbf{y}}^+, \bar{\mathbf{z}}) \right] \end{aligned} \right\}^{bd}$$

Scattering probability of the partonic system

$$- \left[ \delta_{L^+} + \frac{1}{ik^+} \int_{\mathbf{z}'} e^{i\mathbf{k} \cdot (\mathbf{z} - \mathbf{z}')} \tilde{\partial}^{\mathbf{z}} \mathcal{G}(L^+, \mathbf{z}'; \mathbf{y}^+, \mathbf{z}) \right] \mathcal{U}(\mathbf{y}^+, 0, \mathbf{y}) \Big\}^{dc}$$

$$\langle \rho^b(\bar{\mathbf{y}}) \rho^c(\mathbf{y}) \rangle$$

Projectile distribution

Work in progress (Altinoluk, Armesto, Beuf, Martinez, Salgado)



# pA case

Factorized formula:

Finite medium size corrections + Color decoherence effects

$$\omega \frac{dN}{d^3k} \sim \frac{g^2}{\pi^2} \int_{\mathbf{y}, \mathbf{z}, \bar{\mathbf{y}}, \bar{\mathbf{z}}, \mathbf{y}^+, \bar{\mathbf{y}}^+} e^{-i\mathbf{k} \cdot (\mathbf{z} - \bar{\mathbf{z}})} \frac{(\bar{\mathbf{z}} - \bar{\mathbf{y}}) \cdot (\mathbf{z} - \mathbf{y})}{(\bar{\mathbf{z}} - \bar{\mathbf{y}})^2 (\mathbf{z} - \mathbf{y})^2} \text{Probability to emit a soft gluon}$$

$$\left\{ \bar{\delta}_0 \int_{\bar{\mathbf{z}}'} e^{-i\mathbf{k} \cdot (\bar{\mathbf{z}} - \bar{\mathbf{z}}')} \mathcal{G}^\dagger(L^+, \bar{\mathbf{z}}'; \bar{\mathbf{y}}^+, \bar{\mathbf{z}}) \right.$$

$$\left. - \mathcal{U}^\dagger(\bar{\mathbf{y}}^+, 0, \bar{\mathbf{y}}) \left[ \bar{\delta}_{L^+} - \frac{1}{ik^+} \int_{\bar{\mathbf{z}}'} e^{-i\mathbf{k} \cdot (\bar{\mathbf{z}} - \bar{\mathbf{z}}')} \tilde{\partial}^{\bar{\mathbf{z}}} \mathcal{G}^\dagger(L^+, \bar{\mathbf{z}}'; \bar{\mathbf{y}}^+, \bar{\mathbf{z}}) \right] \right\}^{bd}$$

$$\left\{ \delta_0 \int_{\mathbf{z}'} e^{i\mathbf{k} \cdot (\mathbf{z} - \mathbf{z}')} \mathcal{G}(L^+, \mathbf{z}'; \mathbf{y}^+, \mathbf{z}) \right.$$

$$\left. - \left[ \delta_{L^+} + \frac{1}{ik^+} \int_{\mathbf{z}'} e^{i\mathbf{k} \cdot (\mathbf{z} - \mathbf{z}')} \tilde{\partial}^{\mathbf{z}} \mathcal{G}(L^+, \mathbf{z}'; \mathbf{y}^+, \mathbf{z}) \right] \mathcal{U}(\mathbf{y}^+, 0, \mathbf{y}) \right\}^{dc}$$

Non-eikonal corrections!!!

Scattering probability of the partonic system

$\langle \rho^b(\bar{\mathbf{y}}) \rho^c(\mathbf{y}) \rangle$  Projectile distribution

Work in progress (Altinoluk, Armesto, Beuf, Martinez, Salgado)

# pA case

Factorized formula:

Finite medium size corrections + Color decoherence effects

$$\omega \frac{dN}{d^3k} \sim \frac{g^2}{\pi^2} \int_{\mathbf{y}, \mathbf{z}, \bar{\mathbf{y}}, \bar{\mathbf{z}}, \mathbf{y}^+, \bar{\mathbf{y}}^+} e^{-i\mathbf{k} \cdot (\mathbf{z} - \bar{\mathbf{z}})} \frac{(\bar{\mathbf{z}} - \bar{\mathbf{y}}) \cdot (\mathbf{z} - \mathbf{y})}{(\bar{\mathbf{z}} - \bar{\mathbf{y}})^2 (\mathbf{z} - \mathbf{y})^2} \text{Probability to emit a soft gluon}$$

$$\left\langle \rho^b(\bar{\mathbf{y}}) \rho^c(\mathbf{y}) \right\rangle \left\{ \begin{aligned} & \left\{ \bar{\delta}_0 \int_{\bar{\mathbf{z}}'} e^{-i\mathbf{k} \cdot (\bar{\mathbf{z}} - \bar{\mathbf{z}}')} \mathcal{G}^\dagger(L^+, \bar{\mathbf{z}}'; \bar{\mathbf{y}}^+, \bar{\mathbf{z}}) \right. \\ & - \mathcal{U}^\dagger(\bar{\mathbf{y}}^+, 0, \bar{\mathbf{y}}) \left[ \bar{\delta}_{L^+} - \frac{1}{ik^+} \int_{\bar{\mathbf{z}}'} e^{-i\mathbf{k} \cdot (\bar{\mathbf{z}} - \bar{\mathbf{z}}')} \tilde{\partial}^{\bar{\mathbf{z}}} \mathcal{G}^\dagger(L^+, \bar{\mathbf{z}}'; \bar{\mathbf{y}}^+, \bar{\mathbf{z}}) \right] \left. \right\}^{bd} \\ & \left\{ \delta_0 \int_{\mathbf{z}'} e^{i\mathbf{k} \cdot (\mathbf{z} - \mathbf{z}')} \mathcal{G}(L^+, \mathbf{z}'; \mathbf{y}^+, \mathbf{z}) \right. \\ & - \left. \left[ \delta_{L^+} + \frac{1}{ik^+} \int_{\mathbf{z}'} e^{i\mathbf{k} \cdot (\mathbf{z} - \mathbf{z}')} \tilde{\partial}^{\mathbf{z}} \mathcal{G}(L^+, \mathbf{z}'; \mathbf{y}^+, \mathbf{z}) \right] \mathcal{U}(\mathbf{y}^+, 0, \mathbf{y}) \right\}^{dc} \end{aligned} \right.$$

Non-eikonal corrections!!!

Scattering probability of the partonic system

Finite length Corrections!!!

Projectile distribution

Work in progress (Altinoluk, Armesto, Beuf, Martinez, Salgado)

# pA case

High Energy limit  $\Rightarrow$   $k_T$  factorized formula

$$\omega \frac{dN}{d^3k} \sim \frac{g^2}{\pi^2} \int_{\mathbf{y}, \mathbf{z}, \bar{\mathbf{y}}, \bar{\mathbf{z}}} e^{i\mathbf{k} \cdot (\bar{\mathbf{z}} - \mathbf{z})} \frac{(\bar{\mathbf{z}} - \bar{\mathbf{y}}) \cdot (\mathbf{z} - \mathbf{y})}{(\bar{\mathbf{z}} - \bar{\mathbf{y}})^2 (\mathbf{z} - \mathbf{y})^2} \text{Tr.} \left[ \mathcal{U}_{\bar{\mathbf{z}}}^\dagger \mathcal{U}_{\mathbf{z}} + \mathcal{U}_{\bar{\mathbf{y}}}^\dagger \mathcal{U}_{\mathbf{y}} - \mathcal{U}_{\bar{\mathbf{z}}}^\dagger \mathcal{U}_{\mathbf{y}} - \mathcal{U}_{\bar{\mathbf{y}}}^\dagger \mathcal{U}_{\mathbf{z}} \right] \langle \rho^a(\bar{\mathbf{y}}) \rho^a(\mathbf{y}) \rangle$$

This equation leads to the Hybrid Formalism

See T. Altinoluk and A. Kovner; PRD83 (2011) 105004

Work in progress (Altinoluk, Armesto, Beuf, Martinez, Salgado)

# pA case

High Energy limit  $\Rightarrow$   $k_T$  factorized formula

$$\omega \frac{dN}{d^3k} \sim \frac{g^2}{\pi^2} \int_{\mathbf{y}, \mathbf{z}, \bar{\mathbf{y}}, \bar{\mathbf{z}}} e^{i\mathbf{k} \cdot (\bar{\mathbf{z}} - \mathbf{z})} \frac{(\bar{\mathbf{z}} - \bar{\mathbf{y}}) \cdot (\mathbf{z} - \mathbf{y})}{(\bar{\mathbf{z}} - \bar{\mathbf{y}})^2 (\mathbf{z} - \mathbf{y})^2} \text{Tr.} \left[ \mathcal{U}_{\bar{\mathbf{z}}}^\dagger \mathcal{U}_{\mathbf{z}} + \mathcal{U}_{\bar{\mathbf{y}}}^\dagger \mathcal{U}_{\mathbf{y}} - \mathcal{U}_{\bar{\mathbf{z}}}^\dagger \mathcal{U}_{\mathbf{y}} - \mathcal{U}_{\bar{\mathbf{y}}}^\dagger \mathcal{U}_{\mathbf{z}} \right] \langle \rho^a(\bar{\mathbf{y}}) \rho^a(\mathbf{y}) \rangle$$

This equation leads to the Hybrid Formalism

See T. Altinoluk and A. Kovner; PRD83 (2011) 105004

To do list ( Keep tuned !!!! )

- Determine the dominant logarithmic behavior:  
 $\Rightarrow$  Identify the “medium” induced elastic and inelastic terms.
- Make contact and generalize hybrid formalism.

Work in progress (Altinoluk, Armesto, Beuf, Martinez, Salgado)

# Conclusions

- Interference pattern between the initial and final SR is indeed affected in the presence of a QCD medium.
- We observe a partial color decoherence between both emitters
  - ⇒ Opening of phase space for large angle emissions
- We can generalize this setup for pA (work in progress)
  - ⇒ phenomenological consequences at LHC (keep tuned!!!)

# BACKUP SLIDES

# Correlators

## Quark-gluon dipole

$$\frac{1}{N_c^2 - 1} \langle \mathcal{G}(x^+, \mathbf{x}; y^+, \mathbf{y}) \mathcal{U}^\dagger(x^+, y^+) \rangle = \mathcal{K}(x^+, \mathbf{x}; y^+, \mathbf{y} | k^+)$$

$$\mathcal{K}(x^+, \mathbf{x}; y^+, \mathbf{y} | k^+) = \int_{r(y^+) = \mathbf{y}}^{r(x^+) = \mathbf{x}} \mathcal{D}\mathbf{r} \exp \left[ \int_{y^+}^{x^+} d\xi \left( i \frac{k^+}{2} \dot{\mathbf{r}}^2(\xi) - \frac{1}{2} n(\xi) \sigma(\mathbf{r}(\xi)) \right) \right]$$

## Gluon dipole

$$\int d\mathbf{x} d\mathbf{x}' e^{i\mathbf{k} \cdot (\mathbf{x} - \mathbf{x}')} \frac{1}{N_c^2 - 1} \langle \mathcal{G}(x^+, \mathbf{x}; y^+, \mathbf{y}) \mathcal{G}^\dagger(x^+, y^+) \rangle = \mathcal{S}(x^+, y^+, \mathbf{x} - \mathbf{y})$$

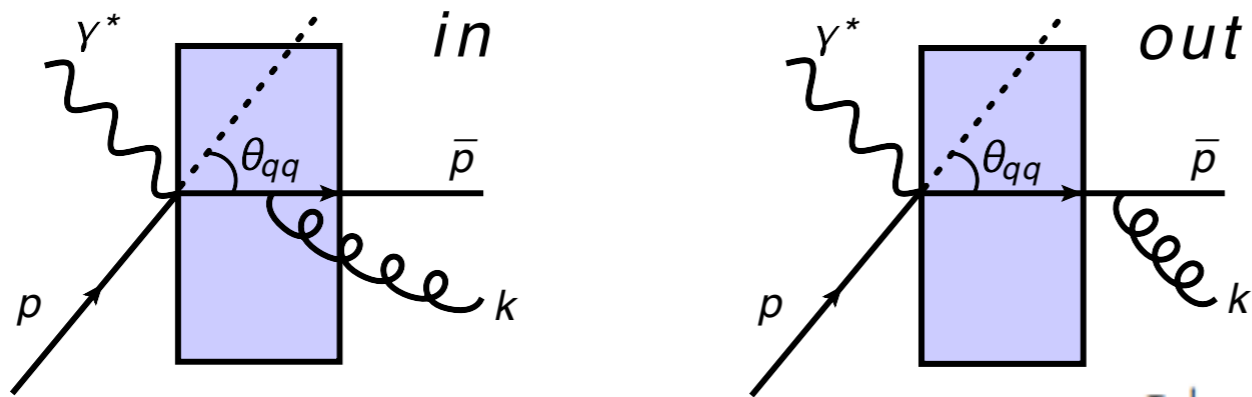
$$\mathcal{S}(x^+, y^+; \mathbf{x} - \mathbf{y}) = \exp \left[ -\frac{1}{2} \int_{y^+}^{x^+} d\xi n(\xi) \sigma(\mathbf{x} - \mathbf{y}) \right]$$

## Dipole cross section

$$\sigma(\mathbf{r}) = \int \frac{d^2\mathbf{q}}{(2\pi)^2} \mathcal{V}(\mathbf{q}) [1 - \cos(\mathbf{r} \cdot \mathbf{q})]$$



# Scattering amplitude from CYM Eqs.

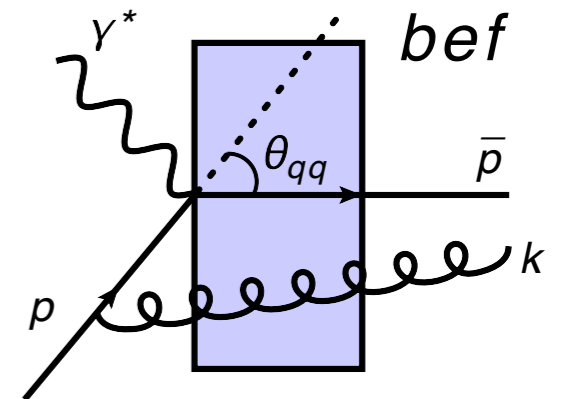


Outcoming parton

$$\begin{aligned} \mathcal{M}_{\lambda, in}^a(\vec{k}) &= \frac{g}{k^+} \int d^2\mathbf{x} e^{i(k^- L^+ - \mathbf{k} \cdot \mathbf{x})} \int_0^{L^+} dy^+ e^{ik^+ \bar{u}^- y^+} \\ &\quad \times \epsilon_\lambda \cdot (i\partial_y + k^+ \bar{u}) \mathcal{G}_{ab}(L^+, \mathbf{x}, y^+, \mathbf{y} = \bar{u} y^+ | k^+) \mathcal{U}_{bc}(y^+, 0) Q_c^{out} \\ \mathcal{M}_{\lambda, out}^a(\vec{k}) &= -2i \frac{\epsilon_\lambda \cdot \bar{\kappa}}{\bar{\kappa}^2} e^{i(k \cdot \bar{u}) L^+} \mathcal{U}_{ab}(L^+, 0) Q_b^{out} \end{aligned}$$

Incoming parton

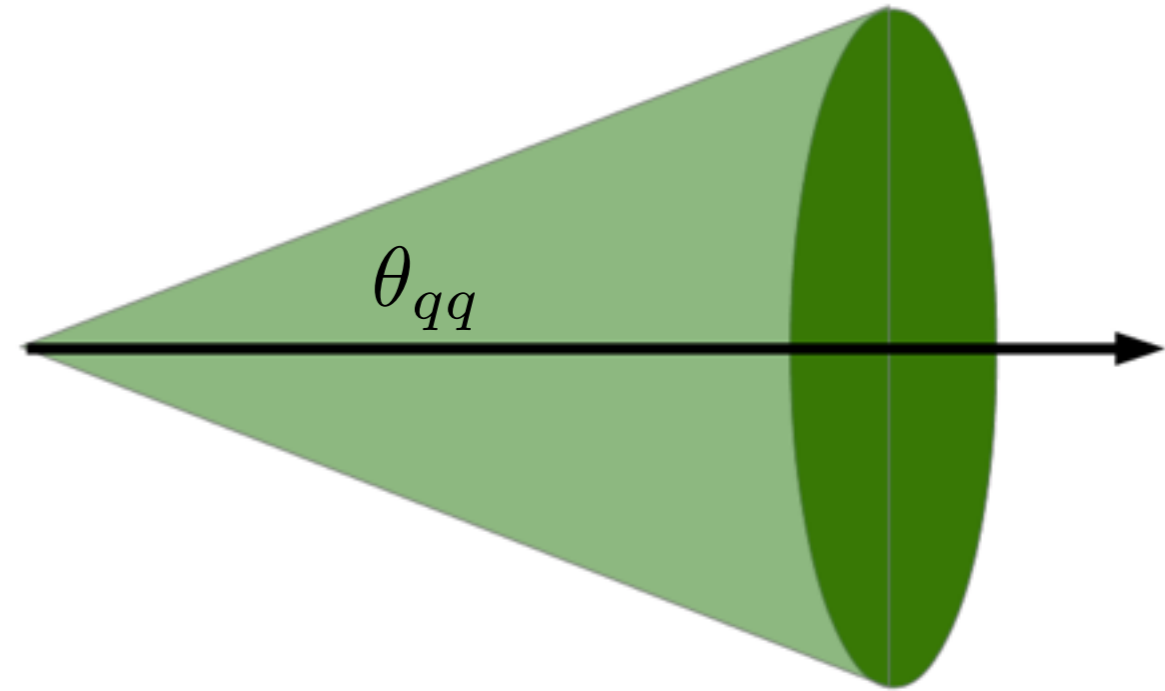
$$\begin{aligned} \mathcal{M}_{\lambda, bef}^a(\vec{k}) &= \frac{g}{k^+} \int_{x^+=\infty} d^2\mathbf{x} e^{i(k^- x^+ - \mathbf{k} \cdot \mathbf{x})} \int_{-\infty}^0 dy^+ e^{ik^+ u^- y^+} \\ &\quad \times \epsilon_\lambda \cdot (i\partial_y + k^+ u) \mathcal{G}_{ab}(x^+, \mathbf{x}, y^+, \mathbf{y} = u y^+ | k^+) Q_b^{in} \end{aligned}$$



# Leading logs and AO

$$\kappa^2 < \delta\mathbf{k}^2 \quad \delta\mathbf{k}^2 \equiv Q^2$$

$$\omega \frac{dN}{d\omega d\kappa^2} = \frac{1}{\kappa^2} \quad (\text{DGLAP})$$



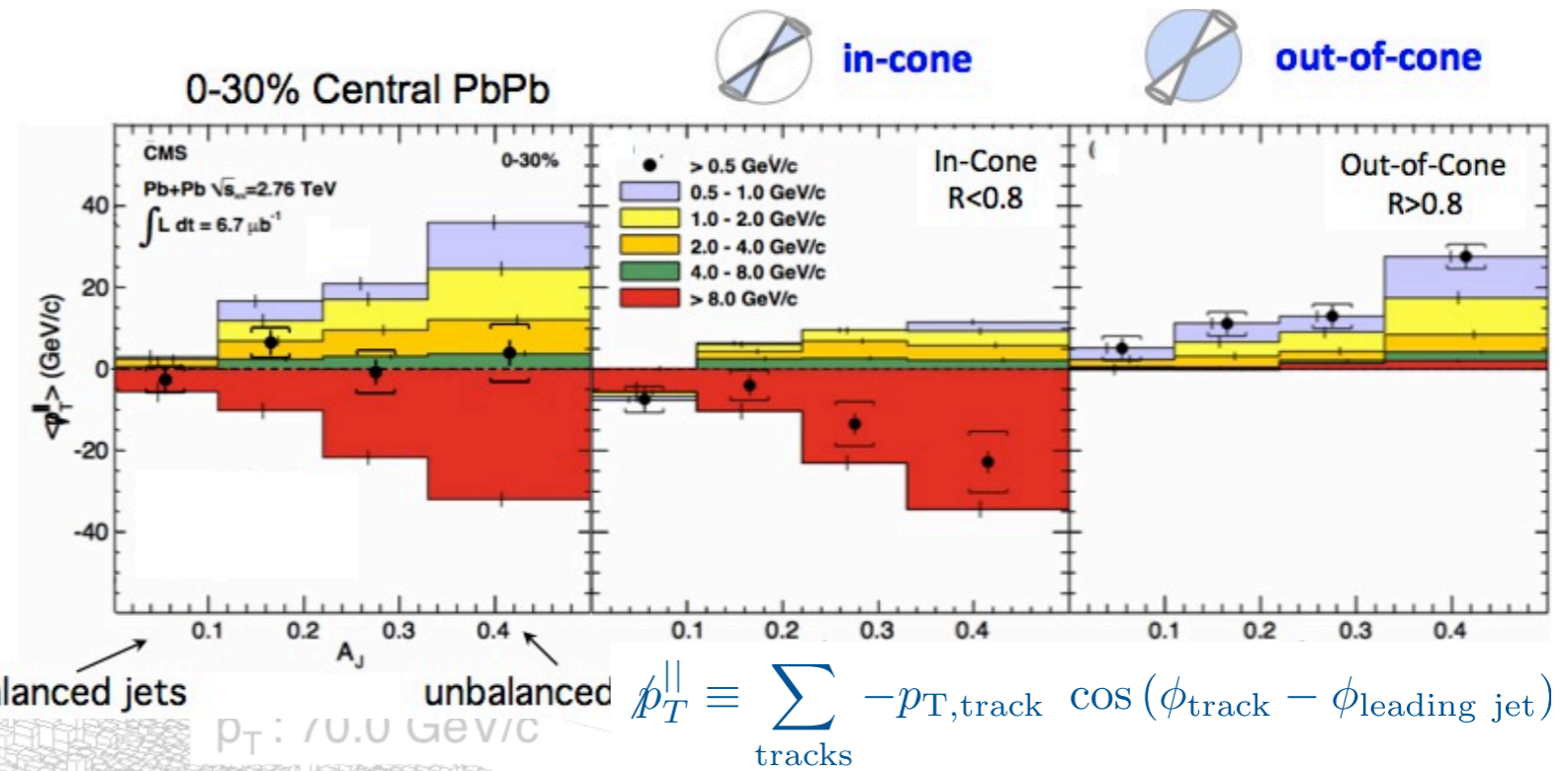
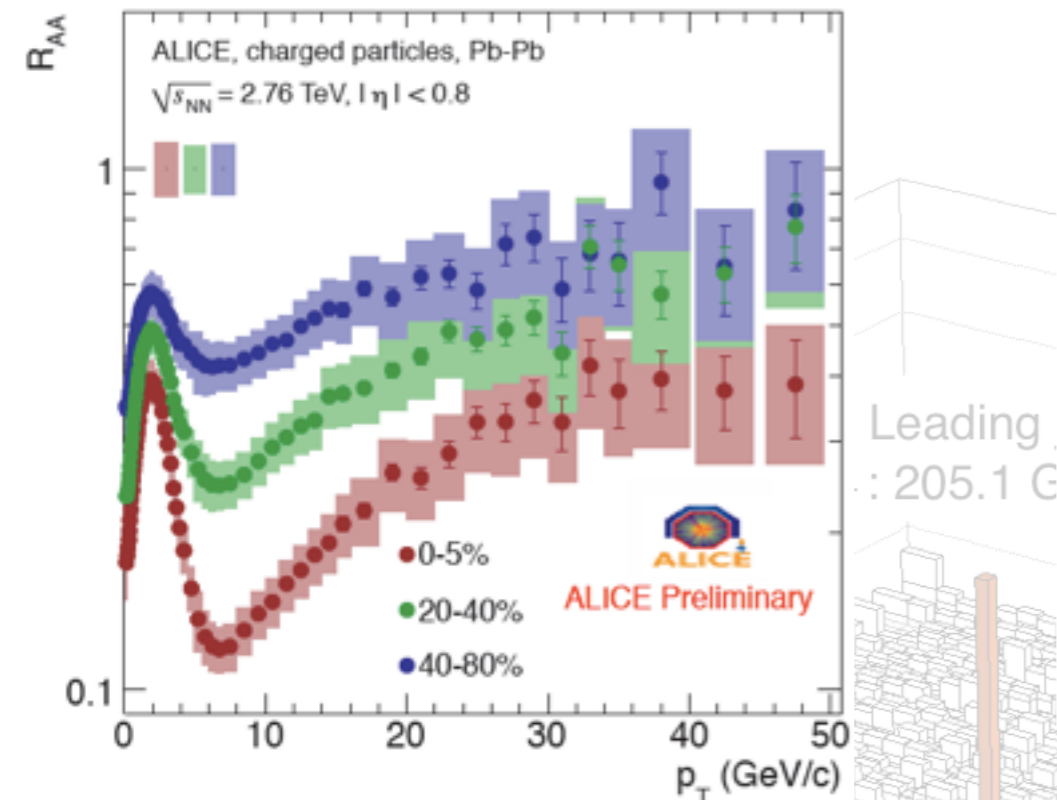
$$\omega \frac{dN}{d\omega} = \int_{Q_0^2}^{\delta\mathbf{k}^2} \frac{d\kappa^2}{\kappa^2} = \log\left(\frac{\delta\mathbf{k}^2}{Q_0^2}\right) \sim \log\left(\frac{Q^2}{Q_0^2}\right) \quad \text{L. L.}$$

$$N \propto \int_{Q_0^2}^{Q^2} \omega \frac{dN}{d\omega} = \frac{1}{2} \left[ \log\left(\frac{Q^2}{Q_0^2}\right) \right]^2 \quad \text{D. L. L.}$$

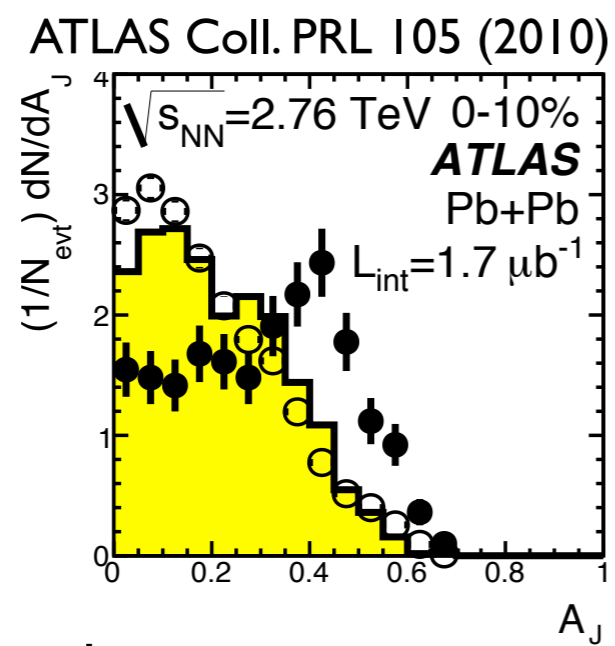
# Jets in HIC @ LHC

(i) Suppression of high- $p_T$  hadrons

(ii) Soft large angle emissions



$$\Delta\phi > \pi/2$$



$$A_J = \frac{E_{T1} - E_{T2}}{E_{T1} + E_{T2}}$$

(iii) Significant dijet asymmetry

