

# NLO improved pQCD initial state + saturation + hydrodynamics model for $A+A$ collisions

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This work:

- Rigorous NLO pQCD calculation for  $E_T$  production from minijets
- Saturation for  $E_T$  production

Compute IC for fluid dynamics in  $A+A$

Roots in the old EKRT model [Nucl. Phys. B 570, 379 (2000)]

- Apply viscous hydrodynamics

$\frac{dN_{\text{ch}}}{d\eta}$ ,  $\frac{dN_{\text{ch}}}{dp_T d\eta}$  and  $v_2(p_T)$  simultaneously at LHC and RHIC

[Paatelainen, et al, Phys Rev C 87 044904 (2012)]

[Paatelainen, Niemi, Eskola and Tuominen, work in progress]

# Minijet $E_T$ production: pQCD calculation

We compute the minijet  $E_T$  production in  $A+A$  and  $\Delta y$

$$E_T(p_0, \sqrt{s}, \Delta y, \mathbf{s}, \mathbf{b}) = \int d^2\mathbf{s} T_A(\mathbf{s} + \mathbf{b}/2) T_A(\mathbf{s} - \mathbf{b}/2) \sigma \langle E_T \rangle_{p_0, \Delta y}$$

$\mathbf{s}$  = transverse position,  $\mathbf{b}$  = impact parameter

Ingredients:

- Nucleon thickness functions  $T_A T_A$  account for the nuclear collision geometry (Optical Glauber, Woods-Saxon profile)
- LO pQCD (collinear factorization)

$$\sigma \langle E_T \rangle \propto \int_{p_0^2} dp_T^2 p_T \int_{\Delta y} dy_1 dy_2 \sum_{ijkl} x_1 f_{i/A} \otimes x_2 f_{j/A} \otimes \frac{d\sigma^{ijkl}}{dt}$$

## Rigorous NLO pQCD computation of $\sigma\langle E_T \rangle$

$$\sigma\langle E_T \rangle = \frac{1}{2!} \int [\text{DPS}]_2 \frac{d\sigma^{2 \rightarrow 2}}{[\text{DPS}]_2} \tilde{S}_2(p_1, p_2) \\ + \frac{1}{3!} \int [\text{DPS}]_3 \frac{d\sigma^{2 \rightarrow 3}}{[\text{DPS}]_3} \tilde{S}_3(p_1, p_2, p_3)$$

- Partonic  $2 \rightarrow 2$  and  $2 \rightarrow 3$  processes for LO & NLO corrections
  - UV renormalized  $|M|^2$  in  $4 - 2\epsilon$  dimensions (R.K Ellis & Sexton; My PhD thesis)
  - IR/CL divergencies handled with NLO def. of PDFs & Ellis-Kunszt-Soper subtraction method
- The measurement functions  $\tilde{S}_2$  and  $\tilde{S}_3$  fulfil the IR/CL criteria  $\rightarrow$   $\sigma\langle E_T \rangle$  is a well defined IR/CL safe quantity

$$\tilde{S}_2 = \{\epsilon(y_1) + \epsilon(y_2)\} p_{T2} \Theta(p_{T2} \geq p_0)$$

$$\tilde{S}_3 = \{\epsilon(y_1)p_{T1} + \epsilon(y_2)p_{T2} + \epsilon(y_3)p_{T3}\}$$

$$\Theta(p_{T1} + p_{T2} + p_{T3} \geq 2p_0) \Theta(E_T \geq \beta \times p_0)$$

where  $\epsilon(y_i) = 1$  if  $y_i \in \Delta y$  otherwise  $\epsilon(y_i) = 0$

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- Def.  $E_T$  in  $\Delta y$  and  $\Theta(\dots)$  hard scattering of partons

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- $\tilde{S}_3 \rightarrow \tilde{S}_2$  at IR/CL limits
- Def.  $E_T$  in  $\Delta y$  and  $\Theta(\dots)$  hard scattering of partons
- $0 \leq \beta \leq 1$  defines the minimum amount of  $E_T$  in  $\Delta y$
- Any  $\beta \in [0, 1]$  is IR/CL safe, thus equally good – leave  $\beta$  free



Nuclear PDFs  $f_{i/A}(x, Q^2, \mathbf{s})$  for each parton flavor  $i$

$$f_{i/A}(x, Q^2, \mathbf{s}) \equiv R_i^A(x, Q^2, \mathbf{s}) f_i^p(x, Q^2)$$

$R_i^A$  denotes the nuclear modification to the free proton PDF  $f_i^p$

- $f_i^p$ : CTEQ6 NLO parton densities
- $R_i^A$ : EPS09s (spatially dependent) NLO nuclear modifications

EPS09s [Helenius, Eskola, Honkanen and Salgado JHEP (2012) 073]

# Saturation criterion for $E_T$

Determine  $p_0(\mathbf{s}) = p_{sat}(\mathbf{s})$  from local saturation criterion of  $E_T$ :

$$\frac{dE_T}{d^2\mathbf{s}dy} (2 \rightarrow 2) \sim \frac{dE_T}{d^2\mathbf{s}dy} (3 \rightarrow 2)$$

$$(T_{AGA})^2 \frac{\alpha_s^2}{p_0} \sim (T_{AGA})^3 \left( \frac{\alpha_s}{p_0} \right)^3 \Rightarrow T_{AGA} \sim \frac{p_{sat}^2}{\alpha_s} \Rightarrow \frac{dE_T}{d^2\mathbf{s}dy} \sim p_0^3$$

$$\begin{aligned} \frac{dE_T}{d^2\mathbf{s}}(p_0, \sqrt{s}, \Delta y, \mathbf{b}, \mathbf{s}, \beta) &= \Delta y \left( \frac{K_{sat}}{\pi} \right) p_0^3 \\ \Rightarrow p_0 &= p_{sat}(\sqrt{s}, \mathbf{b}, \mathbf{s}; \beta, K_{sat}) \end{aligned}$$

Analogy to old EKRT saturation, but now for IR/CL safe  $E_T$

# 1. Simplest case: pQCD + non-local saturation ( $\mathbf{b} = 0$ ) + ideal hydro

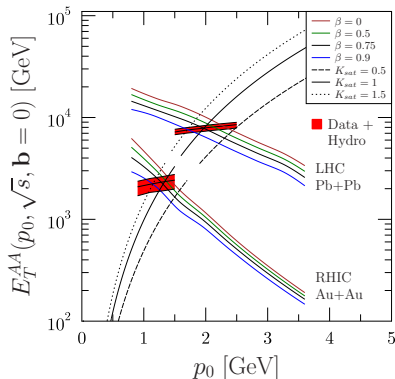
Integrate over the transverse plane  $d^2\mathbf{s} \rightarrow$

$$E_T(p_0, \sqrt{s}, \Delta y, \mathbf{b} = 0, \beta) = K_{\text{sat}} R_A^2 p_0^3 \Delta y$$
$$\Rightarrow p_0 = p_{\text{sat}}(\sqrt{s}; \beta, K_{\text{sat}})$$

- start hydro at  $\tau_0 = 1/p_{\text{sat}}$  with the computed  $E_T(p_{\text{sat}})$
- assume BC (or WN) profile for energy density

$$e(\tau_0) = \frac{dE_T}{d^2\mathbf{s}} \frac{1}{\tau_0 \Delta y}$$

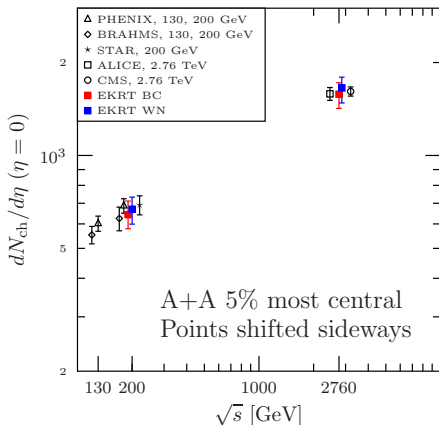
- Understanding  $(K_{\text{sat}}, \beta)$  systematics at LHC and RHIC; possible saturation solutions at the curve crossings



- Red bands tell how much initial  $E_T(p_{\text{sat}})$  we need to reproduce the measured multiplicities
- Multiple  $(\beta, K_{\text{sat}})$  pairs reproduce both LHC and RHIC multiplicity

# Result for central collisions: Multiplicity and Identified particle $p_T$ -spectra

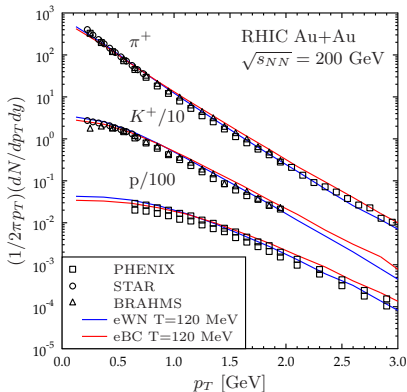
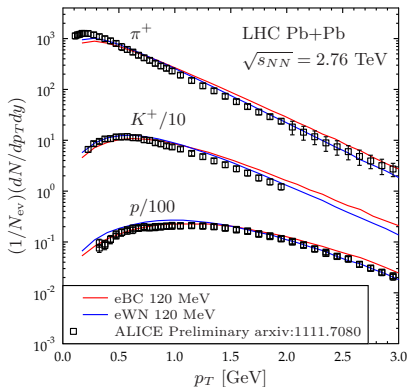
- Ex. with  $\beta = 0.75$  and  $K_{\text{sat}} = 1$



[Phys Rev C 87 044904 (2012)]

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- Ex. with  $\beta = 0.75$  and  $K_{\text{sat}} = 1$



[Phys Rev C 87 044904 (2012)]

## 2. pQCD + local saturation ( $\mathbf{b} \neq 0$ ) + viscous hydro

Now we calculate the transverse profiles....

## LOCAL SATURATION

- Solve saturation equation for  $p_0(\mathbf{b}, \mathbf{s}) = p_{\text{sat}}(\mathbf{b}, \mathbf{s})$  at different  $\mathbf{b}$
- Observation  $p_{\text{sat}}(\mathbf{b}, \mathbf{s}) \propto [T_A(\mathbf{s} + \mathbf{b}/2)T_A(\mathbf{s} - \mathbf{b}/2)]^n$

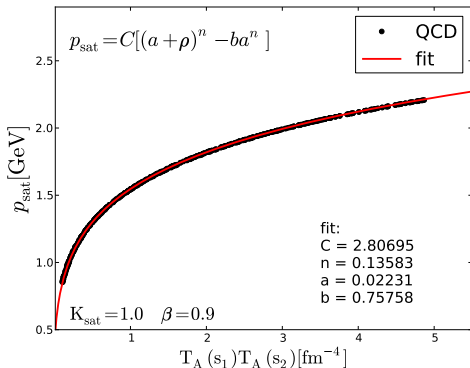


Fig:  $p_{\text{sat}}(\mathbf{b}, \mathbf{s})$  at LHC for  $\mathbf{b} = 0, 2.35, 7.87$  and  $10.6$  fm



## FLUID DYNAMICS: 3 steps to initialize Hydro

**STEP 1:** Solving the saturation equation we can write energy density  $e$  at time  $\tau_{\text{sat}} = 1/p_{\text{sat}}(\mathbf{s})$

$$e(\mathbf{s}, \tau_{\text{sat}} = 1/p_{\text{sat}}(\mathbf{s})) = \frac{K_{\text{sat}}}{\pi} p_{\text{sat}}(\mathbf{s})^4$$

At this level two unknown parameters:

- $K_{\text{sat}}$  in the saturation condition
- $\beta \in [0, 1]$  in the def. of  $E_T$  measurement functions

**STEP 2:** For fluid dynamics we need  $e$  at fixed proper time  $\tau_0$

- Need to evolve the energy density  $e(s)$  to a same time  $\tau_0$
- Largest time given by  $\tau_{\max} = 1/p_{\text{sat}}^{\min}$ , where  $p_{\text{sat}}^{\min} \sim 1 \text{ GeV}$ , the smallest scale we can still trust the pQCD calculation;  $\tau_0 = \tau_{\max}$

We consider two limits:

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We consider two limits:

- **Free streaming** (conserves  $E_T$ )

$$e(\tau_0) = e(\tau_{\text{sat}} = 1/p_{\text{sat}}) \left( \frac{\tau_{\text{sat}}}{\tau_0} \right)$$

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$$e(\tau_0) = e(\tau_{\text{sat}} = 1/p_{\text{sat}}) \left( \frac{\tau_{\text{sat}}}{\tau_0} \right)$$

- **Bjorken scaling** (conserves entropy)

$$e(\tau_0) = e(\tau_{\text{sat}} = 1/p_{\text{sat}}) \left( \frac{\tau_{\text{sat}}}{\tau_0} \right)^{4/3}$$

Saturation calculation extends only to  $e_{\min} = \left(\frac{K_{\text{sat}}}{\pi}\right) p_{\text{sat}}^{\min}(\mathbf{s})^4$

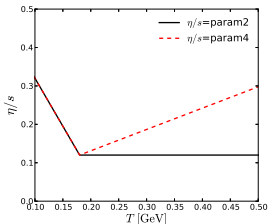
**STEP 3:** Continuation of  $e(\tau_0)$  below  $e_{\min}$

- Smoothly connect the computed  $e$ -profile to  $e \propto \rho_{\text{bin}}$
- small uncertainty at LHC central collisions, more effect in peripheral collisions and at RHIC

# FLUID DYNAMICS: Hydro Evolution (H. Niemi)

2+1D viscous hydro, eqs. from Denicol et al, Phys. Rev. D85 (2012) 114047, Molnar et al, arXiv:1308.0785 [nucl-th]:

- Equation of state
  - Lattice parametrization by Petreczky/Huovinen and (partial) chemical freeze-out at  $T_{\text{chem}} = 175$  MeV (s95p-PCE175-v1)
  - Hadron Resonance Gas (HRG) up to  $m \sim 2$  GeV
- Temperature dependent  $\eta/s$



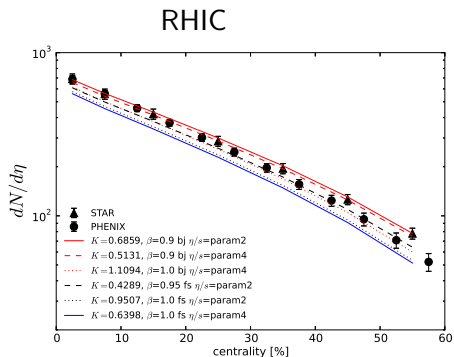
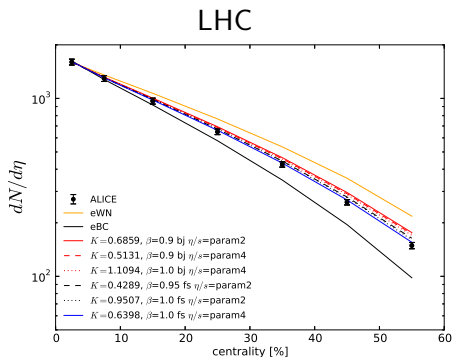
motivation from [H. Niemi et al Phys Rev C 86 014909 (2012)]

- Decoupling temperature  $T_f = 100$  MeV

# RESULTS (preliminary)

Centrality dependence of multiplicity at the LHC  $\sqrt{s} = 2.76$  TeV and RHIC  $\sqrt{s} = 200$  GeV

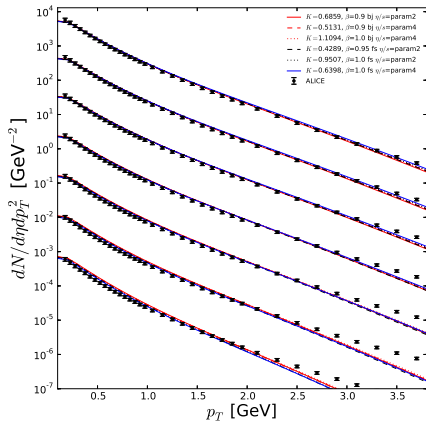
- Choose parameters ( $K_{\text{sat}}, \beta, \text{fs/bj}, \eta/s$ ) such that the most central LHC multiplicity is reproduced
- LHC centrality dependence favors  $\beta \in [0.9, 1]$  and fs-to- $\tau_0$  scenario



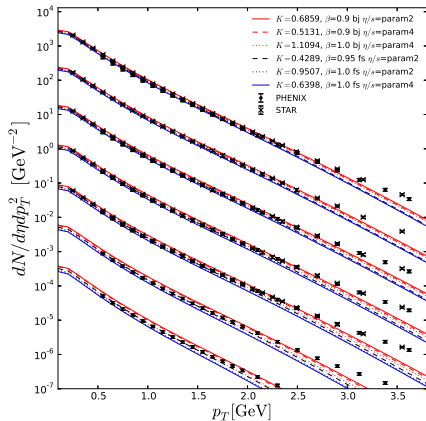
# Charged particle $p_T$ spectra VS Data at the LHC and RHIC

- $T_{\text{chem}}$  determines the low  $p_T$  shape of the spectra (better shape with PCE 175 MeV than 150 MeV)

LHC



RHIC

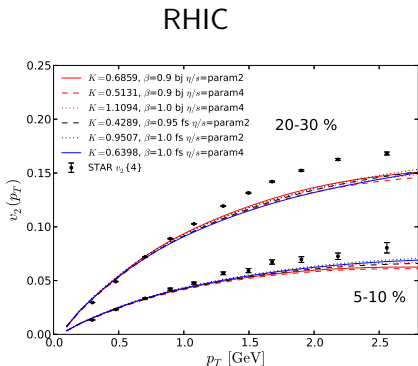
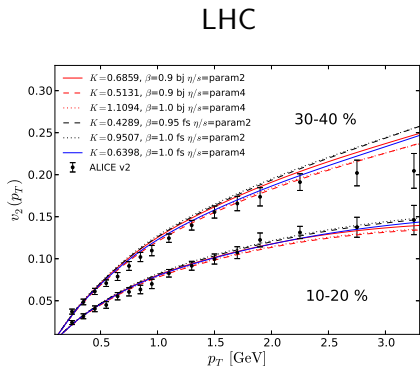




# Elliptic flow $v_2(p_T)$ VS Data at the LHC and RHIC

For  $\eta/s(T)$  studied so far:

- Good low- $p_T$  agreement with the data at both LHC and RHIC
- Note:  $\eta/s(T)$  same at RHIC and LHC



→ Ongoing: can we finetune  $\eta/s(T)$  further ?

# Summary and outlook

- Rigorous NLO pQCD computation for  $E_T(p_0, \beta, \mathbf{b}, \dots)$
- $E_T$  saturation
- Computation of the initial  $e$ -profiles at LHC and RHIC
- Viscous hydro evolution

Results for the centrality dependence of the **multiplicity**,  **$p_T$ -spectra** and  **$v_2(p_T)$**  look promising; finetuning of  $\eta/s(T)$  ongoing

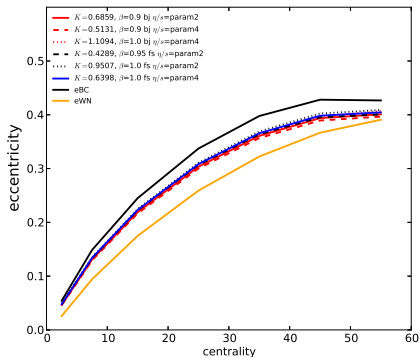
Further studies:

- Geometrical fluctuations from Event-By-Event simulation
  - $\rightarrow$  Study  $v_n$ 's

- Profile eccentricity VS centrality
  
  
  
  
  
  
  
  
  
  
- Effect from the edge

## Profile eccentricity VS centrality at the LHC and RHIC

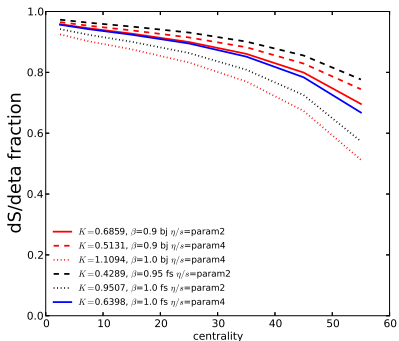
- **Computed profiles** (LHC) are between the usual BC and WN profiles



## Effect from the edge at the LHC and RHIC

- fraction of the total entropy computed from pQCD at LHC and RHIC

LHC



RHIC

