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# HADRONIC D MESON DECAYS

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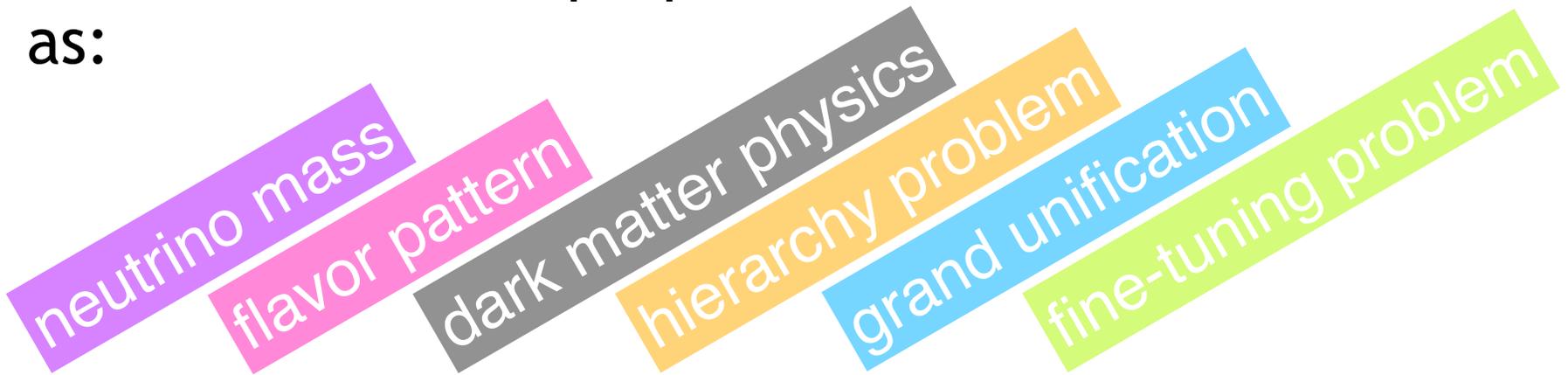
Academia Sinica

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# New Era of Particle Physics

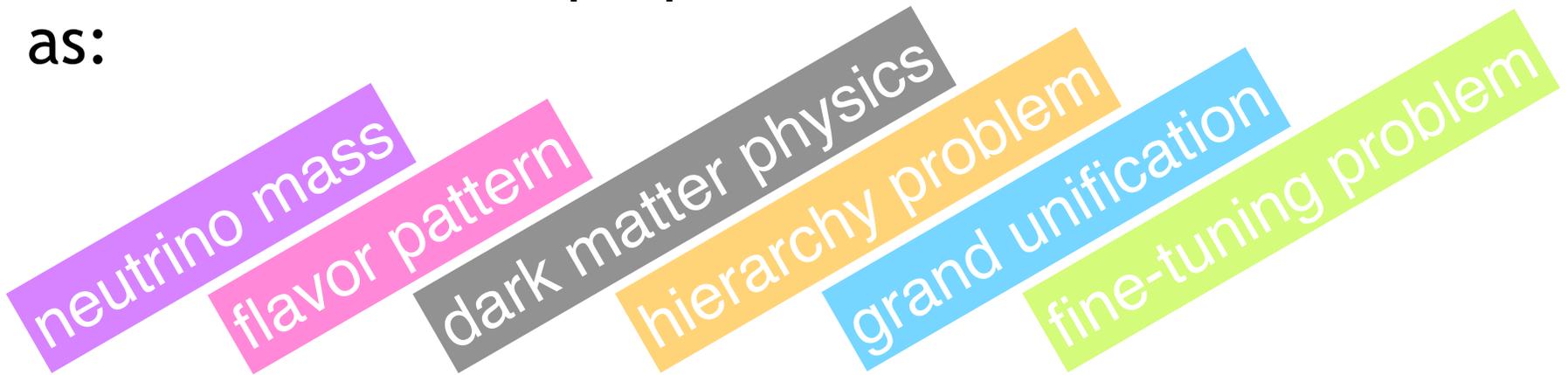
- In past two decades or so, many new physics (NP) models have been proposed to address such issues as:



- Most of them are believed to leave detectable imprints in various low-energy flavor physics.
- Lots of high-precision data have been obtained and more to come. Have we really seen any of it?

# New Era of Particle Physics

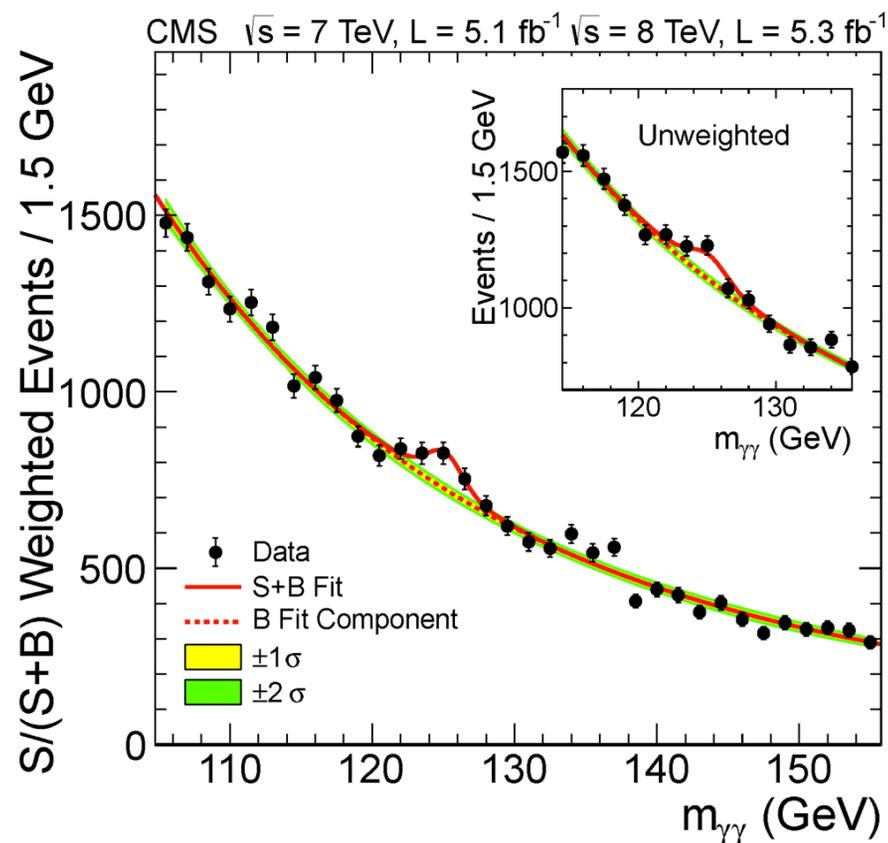
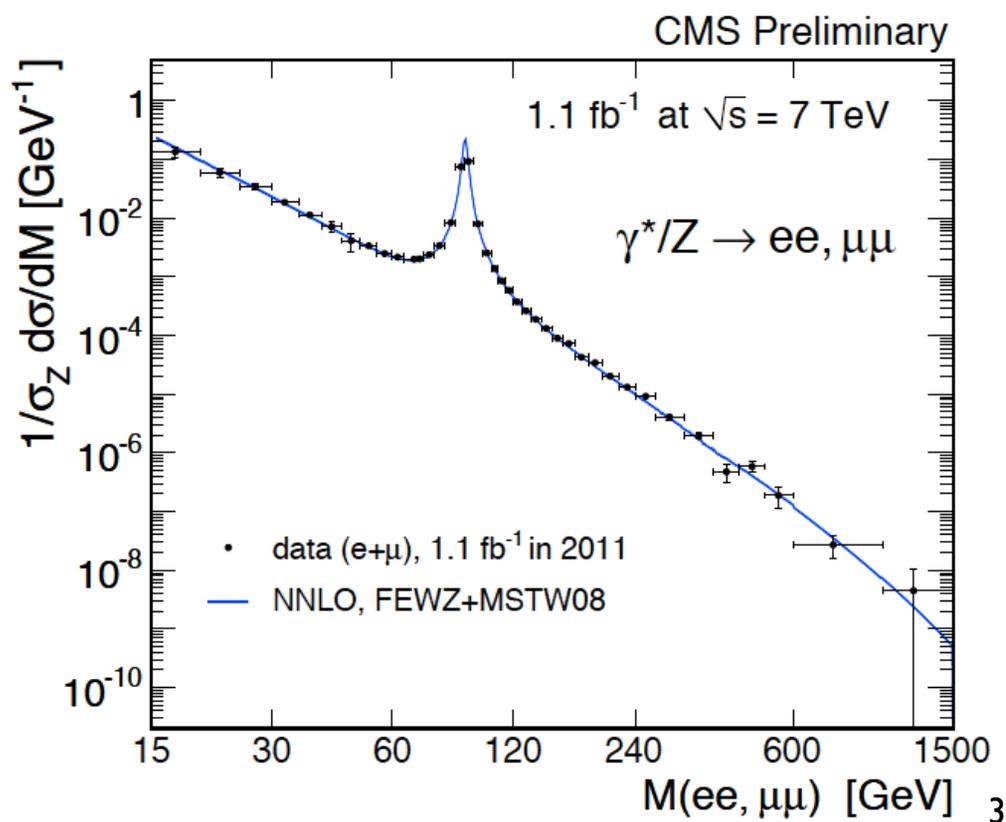
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- Most of them are believed to leave detectable imprints in various low-energy flavor physics.
- Lots of high-precision data have been obtained and more to come. Have we really seen any of it?
- Probing NP in flavor physics = waiting for Godot?

# Energy Frontiers

- LHC experiments have been probing particle physics at unprecedented energy frontier.
- Up to now, no BSM particle from direct searches yet.
- Found a SM Higgs-like resonance at  $\sim 125$  GeV instead.
  - completing the SM



# Precision Frontiers

- Flavor physics experiments have been probing particle physics at precision frontier.
- Many FCNC processes of B physics are used to impose stringent constraints on new physics models.
  - disappearing low-energy anomalies such as  $B_s$  meson mixing and FBA in  $B \rightarrow K^* \mu \mu$
  - reduced tension between  $B \rightarrow \tau \nu$  and  $\sin 2\beta$  about  $|V_{ub}|$ .
  - stronger constraints / bounds from  $BR(B_{s,d} \rightarrow \mu^+ \mu^-)$ .
  - some lingering problems such as  $K\pi$  puzzle and like-sign dimuon asymmetry.
- In general, current data point to **contrived NP models if it has to show up at the TeV scale.**

# What About Charm System?

- Being studied for about 4 decades, a lot of charm data (D meson mixing, decay BR's,  $A_{CP}$ 's) have been collected and analyzed (from BABAR, Belle, CLEO-c, BES-III, and LHCb).
  - ➡ Consistent with SM expectations?
  - ➡ A good place to observe NP?
- Recent direct CPA difference in hadronic D decays
  - ➡ indicating NP beyond the SM?
  - ➡ demanding new understanding of SM?

# Peculiarities of Charm Quark

- Resides at an awkward place in mass spectrum
  - ▣▶ no suitable effective theory to work with, particularly for hadronic decays
- Too light to grant reliable heavy-quark expansions
$$\Lambda_{QCD}/m_c \sim 0.3 \quad \text{vs} \quad \Lambda_{QCD}/m_b \sim 0.1$$
- Too heavy to use chiral perturbation theory
- Strong QCD coupling regime
  - ▣▶ perturbative QCD calculations expected to fail
- Many resonances around
  - ▣▶ nonperturbative rescattering effects kick in
- Flavor SU(3) symmetry for decays to light mesons
- Good realm to test various approaches

# Dominant Charm Decays

- D mesons decay dominantly ( $\sim 84\%$ ) into hadronic final states, 3/4 of which are two-body modes.
  - ▮ unlike B mesons

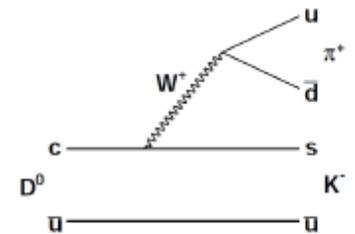
| Mode         | BR           |
|--------------|--------------|
| $PP$         | $\sim 10\%$  |
| $VP$         | $\sim 28\%$  |
| $VV$         | $\sim 10\%$  |
| $SP$         | $\sim 4.2\%$ |
| $AP$         | $\sim 10\%$  |
| $TP$         | $\sim 0.3\%$ |
| 2-body       | $\sim 63\%$  |
| hadronic     | $\sim 84\%$  |
| semileptonic | $\sim 16\%$  |

P: pseudoscalar meson  
V: vector meson  
A: axial vector meson  
T: tensor meson

# Two-Body Hadronic Charm Decays

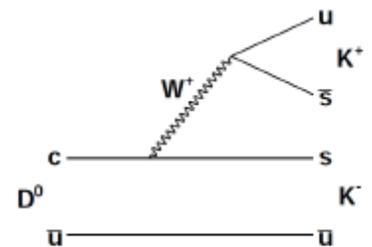
- Cabibbo-favored (CF):

involving  $V_{ud}^* V_{cs} \sim 1 - \lambda^2 \sim 0.95$



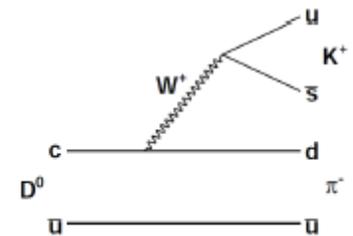
- Singly Cabibbo-suppressed (SCS):

involving  $V_{us}^* V_{cs} / V_{ud}^* V_{cd} \sim \lambda \sim 0.22$



- Doubly Cabibbo-suppressed (DCS):

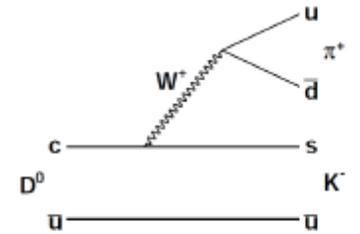
involving  $V_{us}^* V_{cd} \sim \lambda^2 \sim 0.05$



# Two-Body Hadronic Charm Decays

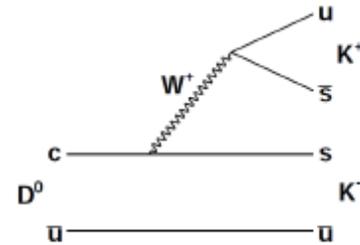
- Cabibbo-favored (CF):

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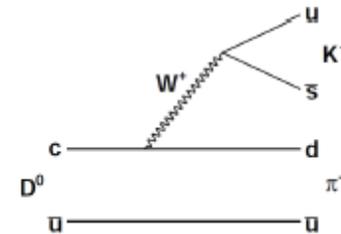
- Singly Cabibbo-suppressed (SCS):

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- Doubly Cabibbo-suppressed (DCS):

involving  $V_{us}^* V_{cd} \sim \lambda^2 \sim 0.05$



- Only SCS decays can possibly involve diagrams with different CKM phases and thus possibly have CPA's:

$$\text{Amp} = V_{cd}^* V_{ud} (\text{trees} + \text{penguins}) \\ + V_{cs}^* V_{us} (\text{trees} + \text{penguins})$$

# CP Violation in SCS Decays

- CPA's in SCS decay modes are expected only at  $10^{-4}$  to  $10^{-3}$  level

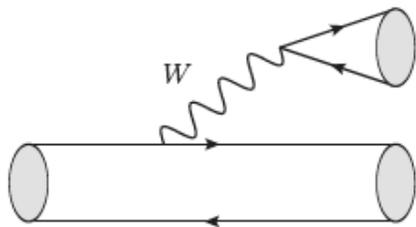
$$a_{CP}^{\text{dir}} = \frac{2\text{Im}(V_{cd}^* V_{ud} V_{cs} V_{us}^*)}{|V_{cd}^* V_{ud}|^2} \left| \frac{A_2}{A_1} \right| \sin \delta = 2 \left| \frac{V_{cb}^* V_{ub}}{V_{cd}^* V_{ud}} \right| \sin \gamma \left| \frac{A_2}{A_1} \right| \sin \delta$$
$$\sim 10^{-3} \left| \frac{A_2}{A_1} \right| \sin \delta \quad (\delta = \text{relative strong phase})$$

⇒ new physics, if measured to be sizable

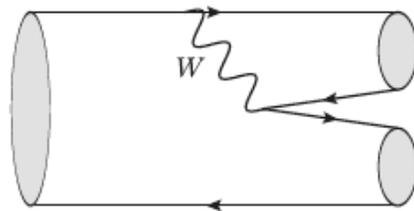
# Flavor Diagrams

- Diagrams for 2-body hadronic D meson decays can be classified according to flavor topology into the tree- and loop-types:

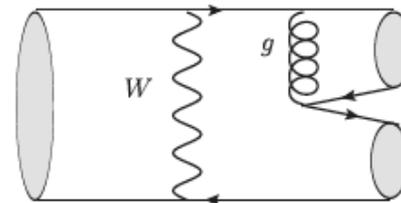
Zeppenfeld 1981  
 Chau and Cheng 1986, 1987, 1991  
 Savage and Wise 1989  
 Grinstein and Lebed 1996  
 Gronau et. al. 1994, 1995, 1995  
 Cheng and Oh 2011



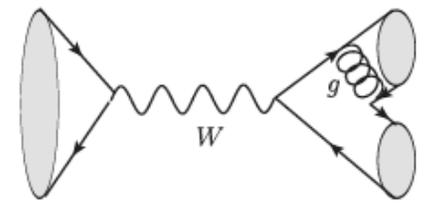
(a)  $T$



(b)  $C$

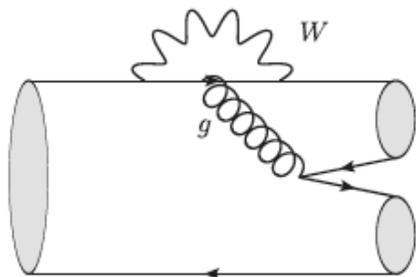


(e)  $E$

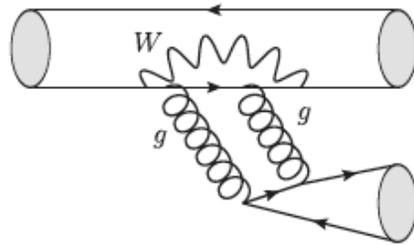


(f)  $A$

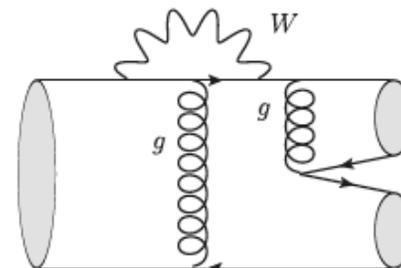
Tree-type



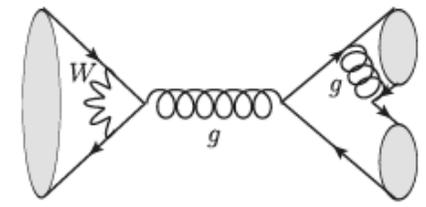
(c)  $P, P_{EW}^C$



(d)  $S, P_{EW}$



(g)  $PE, PE_{EW}$



(h)  $PA, PA_{EW}$

Loop-type

# CF $D \rightarrow PP$ Decays

TABLE I. Branching fractions and invariant amplitudes for Cabibbo-favored decays of charmed mesons to two pseudoscalar mesons. Data are taken from [4]. Predictions based on our best-fitted results in (7) are given in the last column.

| Meson   | Mode              | Representation   | $\mathcal{B}_{\text{exp}}$ (%) | $\mathcal{B}_{\text{fit}}$ (%) |
|---------|-------------------|--|--------------------------------|--------------------------------|
| $D^0$   | $K^- \pi^+$       | $V_{cs}^* V_{ud}(T + E)$   | $3.91 \pm 0.08$                | $3.91 \pm 0.17$                |
|         | $\bar{K}^0 \pi^0$ | $\frac{1}{\sqrt{2}} V_{cs}^* V_{ud}(C - E)$                          | $2.38 \pm 0.09$                | $2.36 \pm 0.08$                |
|         | $\bar{K}^0 \eta$  | $V_{cs}^* V_{ud}[\frac{1}{\sqrt{2}}(C + E) \cos \phi - E \sin \phi]$ | $0.96 \pm 0.06$                | $0.98 \pm 0.05$                |
|         | $\bar{K}^0 \eta'$ | $V_{cs}^* V_{ud}[\frac{1}{\sqrt{2}}(C + E) \sin \phi + E \cos \phi]$ | $1.90 \pm 0.11$                | $1.91 \pm 0.09$                |
| $D^+$   | $\bar{K}^0 \pi^+$ | $V_{cs}^* V_{ud}(T + C)$   | $3.07 \pm 0.10$                | $3.08 \pm 0.36$                |
| $D_s^+$ | $\bar{K}^0 K^+$   | $V_{cs}^* V_{ud}(C + A)$   | $2.98 \pm 0.17$                | $2.97 \pm 0.32$                |
|         | $\pi^+ \pi^0$     | 0  | $<0.037$                       | 0                              |
|         | $\pi^+ \eta$      | $V_{cs}^* V_{ud}(\sqrt{2}A \cos \phi - T \sin \phi)$                 | $1.84 \pm 0.15$                | $1.82 \pm 0.32$                |
|         | $\pi^+ \eta'$     | $V_{cs}^* V_{ud}(\sqrt{2}A \sin \phi + T \cos \phi)$                 | $3.95 \pm 0.34$                | $3.82 \pm 0.36$                |

- $\eta$ - $\eta'$  mixing (with  $\phi = 40.4^\circ$ ): KLOE 2009

satisfactory fit

$$\begin{pmatrix} \eta \\ \eta' \end{pmatrix} = \begin{pmatrix} \cos \phi & -\sin \phi \\ \sin \phi & \cos \phi \end{pmatrix} \begin{pmatrix} \eta_q \\ \eta_s \end{pmatrix} \quad \left[ \eta_q = \frac{1}{\sqrt{2}} (u\bar{u} + d\bar{d}) \quad , \quad \eta_s = s\bar{s} \right]$$

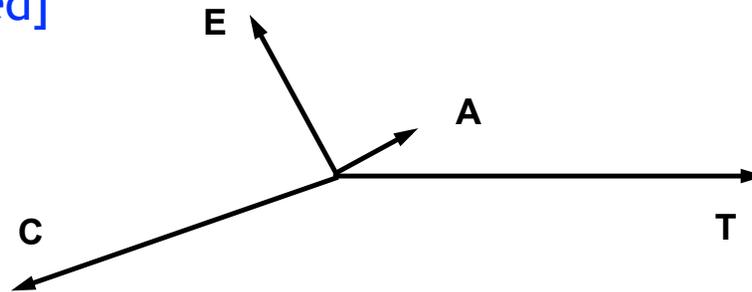
# Extracted Amplitudes

- The amplitudes extracted from Cabibbo-favored modes in units of  $10^{-6}$  GeV are ( $\chi^2/\text{dof} = 0.65$ ):

$$T = 3.14 \pm 0.06, \quad C = (2.61 \pm 0.08)e^{-i(152 \pm 1)^\circ},$$
$$E = (1.53_{-0.08}^{+0.07})e^{i(122 \pm 2)^\circ}, \quad A = (0.39_{-0.09}^{+0.13})e^{i(31_{-33}^{+20})^\circ}.$$

CWC, Luo, Rosner 2002, 2003  
Wu, Zhong, Zhou 2004  
Bhattacharya and Rosner 2008, 2010  
Cheng and CWC 2010

[CKM factors extracted]



- Results are used to predict SCS and DCS decays utilizing the flavor SU(3) symmetry.

# Implications

Cheng and CWC 2010

- T and C are almost opposite in phase, and C and E are quite sizable (*cf.* B decays)
  - ▮ large final-state interaction effects
  - ▮ result of rescattering via abundant resonances around D mesons
  - ▮ failure of perturbative approaches

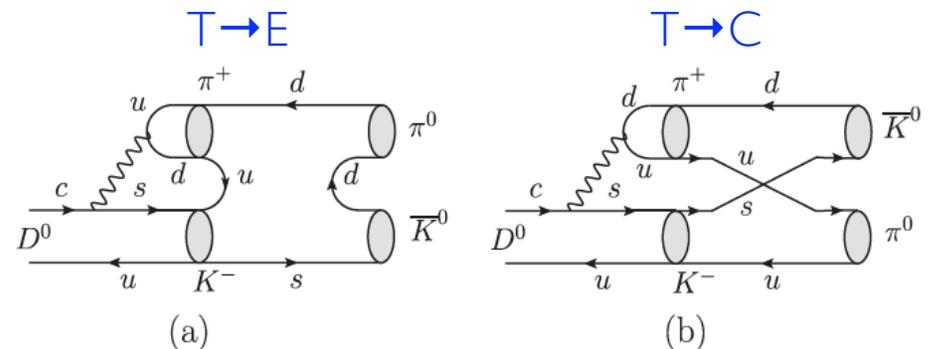
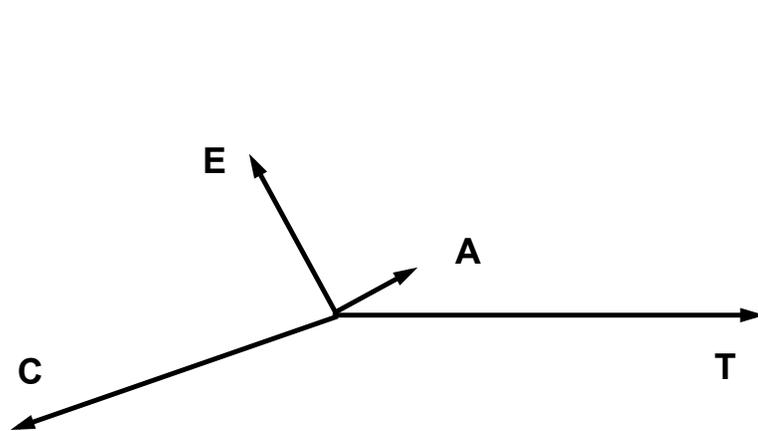


FIG. 1. Contributions to  $D^0 \rightarrow \bar{K}^0 \pi^0$  from the color-allowed weak decay  $D^0 \rightarrow K^- \pi^+$  followed by a resonantlike rescattering (a) and quark exchange (b). While (a) has the same topology as the  $W$ -exchange graph, (b) mimics the color-suppressed internal  $W$ -emission graph.

# SCS $D \rightarrow PP$ Decays -- SU(3) Limit

| Decay Mode                      | $\mathcal{B}_{\text{SU}(3)}$ | $\mathcal{B}_{\text{SU}(3)\text{-breaking}}$  | $\mathcal{B}_{\text{expt}}$ |
|---------------------------------|------------------------------|---|-----------------------------|
| $D^0 \rightarrow \pi^+ \pi^-$   | $2.26 \pm 0.13$              |  | $1.400 \pm 0.026$           |
| $D^0 \rightarrow \pi^0 \pi^0$   | $1.35 \pm 0.08$              |  | $0.80 \pm 0.05$             |
| $D^0 \rightarrow \pi^0 \eta$    | $0.75 \pm 0.05$              |   | $0.68 \pm 0.07$             |
| $D^0 \rightarrow \pi^0 \eta'$   | $0.75 \pm 0.05$              |   | $0.89 \pm 0.14$             |
| $D^0 \rightarrow \eta \eta$     | $1.43 \pm 0.09$              |   | $1.67 \pm 0.20$             |
|                                 | $1.43 \pm 0.09$              |   |                             |
| $D^0 \rightarrow \eta \eta'$    | $1.20 \pm 0.10$              |   | $1.05 \pm 0.26$             |
|                                 | $1.20 \pm 0.10$              |   |                             |
| $D^0 \rightarrow K^+ K^-$       | $1.89 \pm 0.11$              |  | $3.96 \pm 0.08$             |
|                                 | $1.89 \pm 0.11$              |   |                             |
| $D^0 \rightarrow K^0 \bar{K}^0$ | 0                            |  | $0.346 \pm 0.058$           |
|                                 | 0                            |   |                             |
| $D^+ \rightarrow \pi^+ \pi^0$   | $0.88 \pm 0.06$              |   | $1.19 \pm 0.06$             |
| $D^+ \rightarrow \pi^+ \eta$    | $1.49 \pm 0.35$              |   | $3.53 \pm 0.21$             |
| $D^+ \rightarrow \pi^+ \eta'$   | $3.77 \pm 0.33$              |   | $4.67 \pm 0.29$             |
| $D^+ \rightarrow K^+ \bar{K}^0$ | $5.32 \pm 0.55$              |   | $5.66 \pm 0.32$             |
| $D_s^+ \rightarrow \pi^+ K^0$   | $2.78 \pm 0.28$              |   | $2.42 \pm 0.16$             |
| $D_s^+ \rightarrow \pi^0 K^+$   | $0.69 \pm 0.09$              |   | $0.62 \pm 0.21$             |
| $D_s^+ \rightarrow K^+ \eta$    | $0.78 \pm 0.08$              |   | $1.75 \pm 0.35$             |
| $D_s^+ \rightarrow K^+ \eta'$   | $1.05 \pm 0.17$              |   | $1.8 \pm 0.6$               |

# DCS $D \rightarrow PP$ Decays -- SU(3) Limit

- Predictions and measured data agree well.

Cheng and CWC 2010

TABLE III. Branching fractions and invariant amplitudes for doubly Cabibbo-suppressed decays of charmed mesons to two pseudoscalar mesons. Data are taken from [4]. Predictions based on our best-fitted results in (7) with exact flavor SU(3) symmetry are given in the last column.

| Meson   | Mode        | Representation   | $\mathcal{B}_{\text{exp}} (\times 10^{-4})$ | $\mathcal{B}_{\text{theory}} (\times 10^{-4})$ |
|---------|-------------|--|---|--|
| $D^0$   | $K^+ \pi^-$ | $V_{cd}^* V_{us} (T'' + E'')$  | $1.48 \pm 0.07$                             | $1.12 \pm 0.05$                                |
|         | $K^0 \pi^0$ | $\frac{1}{\sqrt{2}} V_{cd}^* V_{us} (C'' - E'')$                             |   | $0.67 \pm 0.02$                                |
|         | $K^0 \eta$  | $V_{cd}^* V_{us} [\frac{1}{\sqrt{2}} (C'' + E'') \cos \phi - E'' \sin \phi]$ |   | $0.28 \pm 0.02$                                |
|         | $K^0 \eta'$ | $V_{cd}^* V_{us} [\frac{1}{\sqrt{2}} (C'' + E'') \sin \phi + E'' \cos \phi]$ |   | $0.55 \pm 0.03$                                |
| $D^+$   | $K^0 \pi^+$ | $V_{cd}^* V_{us} (C'' + A'')$  | $1.72 \pm 0.19$                             | $1.98 \pm 0.22$                                |
|         | $K^+ \pi^0$ | $\frac{1}{\sqrt{2}} V_{cd}^* V_{us} (T'' - A'')$                             |   | $1.59 \pm 0.15$                                |
|         | $K^+ \eta$  | $V_{cd}^* V_{us} (\frac{1}{\sqrt{2}} (T'' + A'') \cos \phi - A'' \sin \phi)$ |   | $0.98 \pm 0.04$                                |
|         | $K^+ \eta'$ | $V_{cd}^* V_{us} (\frac{1}{\sqrt{2}} (T'' + A'') \sin \phi + A'' \cos \phi)$ |   | $0.91 \pm 0.17$                                |
| $D_s^+$ | $K^0 K^+$   | $V_{cd}^* V_{us} (T'' + C'')$  |   | $0.38 \pm 0.04$                                |

↑  
to be checked  
against future data

# Problems With $K^+K^-$ and $\pi^+\pi^-$ Modes

- These two modes are closely related and identical under SU(3) limit:

$$A_{\pi^+\pi^-} = \frac{1}{2}(\lambda_d - \lambda_s)(T + E + \Delta P)_{\pi\pi} - \frac{1}{2}\lambda_b(T + E + \Sigma P)_{\pi\pi}$$

$$\rightarrow \lambda_d(T + E) - \lambda_b\Sigma P \quad [\text{SU(3) limit}]$$

$$A_{K^+K^-} = \frac{1}{2}(\lambda_s - \lambda_d)(T + E - \Delta P)_{KK} - \frac{1}{2}\lambda_b(T + E + \Sigma P)_{KK}$$

$$\rightarrow \lambda_s(T + E) - \lambda_b\Sigma P \quad [\text{SU(3) limit}]$$

$$\Sigma P = (P + PE + PA)_d + (P + PE + PA)_s$$

$$\Delta P = (P + PE + PA)_d - (P + PE + PA)_s$$

$$\lambda_q = V_{cq}^* V_{uq}$$

quark involved in penguin loop

# A Long-Standing Puzzle

- $D \rightarrow \pi^+\pi^-, K^+K^-$  modes are known to deviate from naive expectations for a long time.

- Empirically, the ratio of their decay rates

$$\frac{\Gamma(K^+K^-)}{\Gamma(\pi^+\pi^-)} \simeq 2.8$$

is noticeably **larger than 1** for the SU(3) limit, not to mention that  $K^+K^-$  has **less phase space** than  $\pi^+\pi^-$ .

- SU(3) breaking in factorizable part

$$\frac{T(K^+K^-)}{T(\pi^+\pi^-)} \simeq \frac{f_K}{f_\pi} \simeq 1.22 \text{ or } \frac{f_K}{f_\pi} \frac{F_+^{DK}(m_K^2)}{F_+^{D\pi}(m_\pi^2)} \simeq 1.38$$

is **insufficient** to account for data.

# Direct CP Asymmetry Difference

- Time-integrated asymmetry to first order in the average decay time  $\langle t \rangle$ :

$$A_{CP}(f) \equiv \frac{\Gamma(D^0 \rightarrow f) - \Gamma(\bar{D}^0 \rightarrow \bar{f})}{\Gamma(D^0 \rightarrow f) + \Gamma(\bar{D}^0 \rightarrow \bar{f})}$$
$$\simeq a_{CP}^{\text{dir}}(f) + \frac{\langle t \rangle}{\tau_D} a_{CP}^{\text{ind}}$$

- Consider

$$\Delta A_{CP} \equiv A_{CP}(K^+ K^-) - A_{CP}(\pi^+ \pi^-)$$
$$\simeq a_{CP}^{\text{dir}}(K^+ K^-) - a_{CP}^{\text{dir}}(\pi^+ \pi^-) + \frac{\Delta \langle t \rangle}{\tau_D} a_{CP}^{\text{ind}}$$

- (1) common systematic factors cancel out;
- (2) insensitive to indirect CPV;
- (3) SM and most NP models predict opposite signs.

# $\Delta A_{CP}$ for $K^+K^-$ and $\pi^+\pi^-$ circa 2012

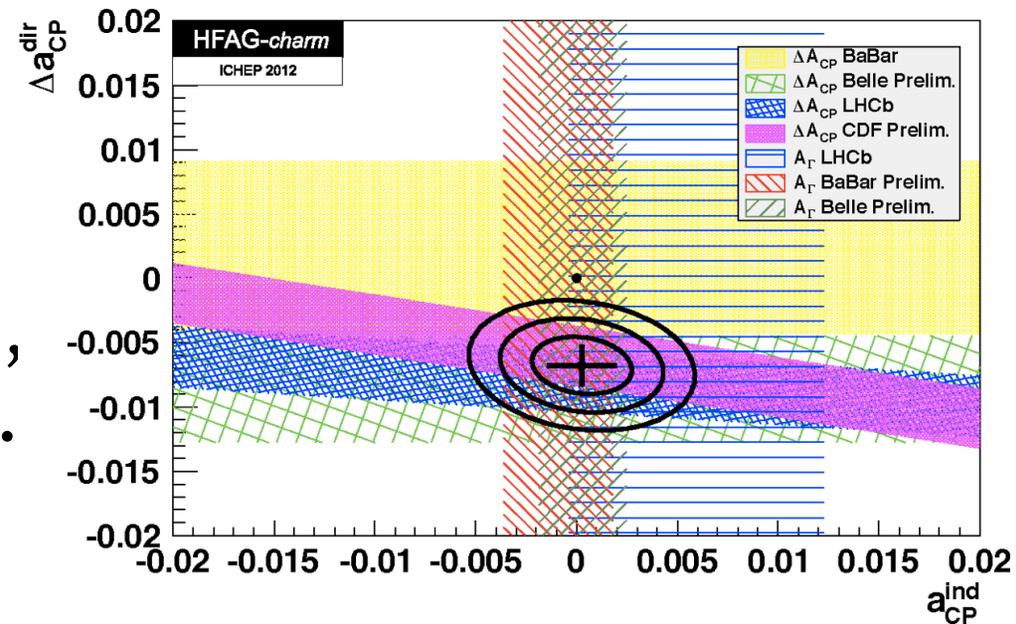
HFAG ICHEP 2012

- Combination of the LHCb, CDF, BaBar and Belle measurements yields

$$a_{CP}^{\text{ind}} = -(0.027 \pm 0.163)\%$$

$$\Delta a_{CP}^{\text{dir}} = -(0.678 \pm 0.147)\%$$

**4.6 $\sigma$  from no CPV**



| Experiment | $A_{CP}(K^+K^-)(\%)$      | $A_{CP}(\pi^+\pi^-)(\%)$  | $\Delta A_{CP}(\%)$       |
|------------|---------------------------|---------------------------|---------------------------|
| BaBar      | $0.00 \pm 0.34 \pm 0.13$  | $-0.24 \pm 0.52 \pm 0.22$ |                           |
| LHCb       |                           |                           | $-0.82 \pm 0.21 \pm 0.11$ |
| CDF        | $-0.24 \pm 0.22 \pm 0.09$ | $0.22 \pm 0.24 \pm 0.11$  | $-0.62 \pm 0.21 \pm 0.10$ |
| Belle      | $-0.32 \pm 0.21 \pm 0.09$ | $0.55 \pm 0.36 \pm 0.09$  | $-0.87 \pm 0.41 \pm 0.06$ |

➡ ~30 theory papers followed

# Large Penguin Within SM -- I

Brod, Grossman, Kagan, Zupan 2012

- Assume **different** and **large** enhancements in d,s-quark penguin contractions  $P_{d,s}$  relative to T.
- Require **U-spin breaking** in T+E:
$$(T+E)_{\pi\pi} = (T+E)(1+\varepsilon_T/2)$$
$$(T+E)_{KK} = (T+E)(1-\varepsilon_T/2)$$
with a complex  $\varepsilon_T$  and  $|\varepsilon_T| \in (0,0.3)$ .
- Large  $\Sigma P$  explains  $\Delta a_{CP}^{dir}$ , while large  $\Delta P$  explains the large disparity in the rates of  $K^+K^-$  and  $\pi^+\pi^-$ .
  - ▮▮▮ A fit to data shows  $|(P_d-P_s)/T| \sim 0.5!$

# Large Penguin Within SM -- II

Bhattacharya, Gronau, Rosner 2012

- Take SU(3) breaking in T by factorization

$$\frac{T_{KK}}{T_{\pi\pi}} = \frac{a_1(KK)}{a_1(\pi\pi)} \frac{f_K}{f_\pi} \frac{F_0^{DK}(m_K^2)}{F_0^{D\pi}(m_\pi^2)} \frac{m_D^2 - m_K^2}{m_D^2 - m_\pi^2} \simeq 1.32$$

- Assume a smaller  $\Delta P$  and  $E_{KK} = E_{\pi\pi}$ .
  - ▮▮▮ A fit to data shows  $|(P_d - P_s)/T| \sim 0.15$
  - ▮▮▮ requiring a  $P_b$  amplitude comparable to T (attributed to “unforeseen QCD effects”)

# Our Analysis

- Significant SU(3) symmetry breaking in E:

$$A(D \rightarrow K^0 \underline{K}^0) = \lambda_d(E_d + 2PA_d) + \lambda_s(E_s + 2PA_s)$$

▮ vanishing in SU(3) limit, but measured to have a nonzero rate

- Fix  $E_d$  and  $E_s$  from rates of  $K^+K^-$ ,  $\pi^+\pi^-$ ,  $\pi^0\pi^0$ , and  $K^0\underline{K}^0$ :

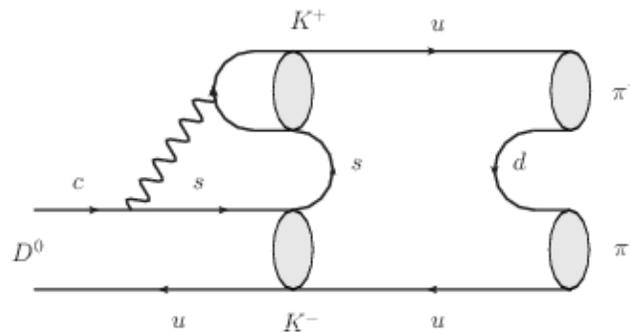
$$(I) \quad E_d = 1.19 e^{i15.0^\circ} E, \quad E_s = 0.58 e^{-i14.7^\circ} E,$$

$$(II) \quad E_d = 1.19 e^{i15.0^\circ} E, \quad E_s = 1.62 e^{-i9.8^\circ} E.$$

- Also SU(3) breaking in T by factorization.
- No attempt is made to fit  $\Delta a_{CP}^{\text{dir}}$  though.
- Accumulation of several SU(3) breaking effects leads to apparently large SU(3) violation seen in the rates of  $K^+K^-$  and  $\pi^+\pi^-$ .

# Penguin Amplitudes

- Short-distance weak penguin exchange/annihilation diagrams are very small
  - ▣▣▣▣  $|PE/T| \sim 0.04$  and  $|PA/T| \sim 0.02$
- Large long-distance contribution to PE can possibly arise from  $D^0 \rightarrow K^+K^-$  followed by a **resonance-like final-state rescattering**, in the same fashion as for E



- It is possible to have **PE**  $\sim$  **E**, just to maximize CPV.
- Use QCDF to estimate other penguin amplitudes.
  - ▣▣▣▣ **negligible  $\Delta P$**

# SCS $D \rightarrow PP$ Decays -- SU(3) Breaking

| Decay Mode   | $\mathcal{B}_{\text{SU}(3)}$ | $\mathcal{B}_{\text{SU}(3)\text{-breaking}}$ | $\mathcal{B}_{\text{expt}}$ |
|--|------------------------------|--|-----------------------------|
| $D^0 \rightarrow \pi^+\pi^-$    | $2.26 \pm 0.13$              | $1.40 \pm 0.11$                              | $1.400 \pm 0.026$           |
| $D^0 \rightarrow \pi^0\pi^0$    | $1.35 \pm 0.08$              | $0.78 \pm 0.06$                              | $0.80 \pm 0.05$             |
| $D^0 \rightarrow \pi^0\eta$  | $0.75 \pm 0.05$              | $0.83 \pm 0.06$                              | $0.68 \pm 0.07$             |
| $D^0 \rightarrow \pi^0\eta'$   | $0.75 \pm 0.05$              | $1.42 \pm 0.08$                              | $0.89 \pm 0.14$             |
| $D^0 \rightarrow \eta\eta$   | $1.43 \pm 0.09$              | $1.68 \pm 0.09$                              | $1.67 \pm 0.20$             |
|  | $1.43 \pm 0.09$              | $1.89 \pm 0.10$                              |                             |
| $D^0 \rightarrow \eta\eta'$  | $1.20 \pm 0.10$              | $0.68 \pm 0.06$                              | $1.05 \pm 0.26$             |
|  | $1.20 \pm 0.10$              | $2.11 \pm 0.20$                              |                             |
| $D^0 \rightarrow K^+K^-$        | $1.89 \pm 0.11$              | $3.89 \pm 0.16$                              | $3.96 \pm 0.08$             |
|  | $1.89 \pm 0.11$              | $3.90 \pm 0.22$                              |                             |
| $D^0 \rightarrow K^0\bar{K}^0$  | 0                            | $0.346 \pm 0.034$                            | $0.346 \pm 0.058$           |
|  | 0                            | $0.345 \pm 0.034$                            |                             |
| $D^+ \rightarrow \pi^+\pi^0$   | $0.88 \pm 0.06$              | $0.96 \pm 0.07$                              | $1.19 \pm 0.06$             |
| $D^+ \rightarrow \pi^+\eta$   | $1.49 \pm 0.35$              | $3.26 \pm 0.39$                              | $3.53 \pm 0.21$             |
| $D^+ \rightarrow \pi^+\eta'$  | $3.77 \pm 0.33$              | $4.70 \pm 0.31$                              | $4.67 \pm 0.29$             |
| $D^+ \rightarrow K^+\bar{K}^0$   | $5.32 \pm 0.55$              | $8.72 \pm 0.85$                              | $5.66 \pm 0.32$             |
| $D_s^+ \rightarrow \pi^+K^0$   | $2.78 \pm 0.28$              | $3.57 \pm 0.33$                              | $2.42 \pm 0.16$             |
| $D_s^+ \rightarrow \pi^0K^+$   | $0.69 \pm 0.09$              | $0.69 \pm 0.09$                              | $0.62 \pm 0.21$             |
| $D_s^+ \rightarrow K^+\eta$  | $0.78 \pm 0.08$              | $0.83 \pm 0.08$                              | $1.75 \pm 0.35$             |
| $D_s^+ \rightarrow K^+\eta'$   | $1.05 \pm 0.17$              | $1.28 \pm 0.20$                              | $1.8 \pm 0.6$               |

Cheng and CWC 2012

# Our $A_{CP}$ Predictions

pQCD results

| Decay Mode                     | $a_{dir}^{(tree)}$ (this work) | $a_{dir}^{(tree)}$ [22] | $a_{dir}^{(tot)}$ (this work) | $a_{dir}^{(tot)}$ [22] | Expt.             |
|--------------------------------|--------------------------------|-------------------------|-------------------------------|------------------------|-------------------|
| $D^0 \rightarrow \pi^+\pi^-$   | 0                              | 0                       | $0.96 \pm 0.04$               | 0.74                   | $2.0 \pm 2.2$     |
| $D^0 \rightarrow \pi^0\pi^0$   | 0                              | 0                       | $0.83 \pm 0.04$               | 0.26                   | $1 \pm 48$        |
| $D^0 \rightarrow \pi^0\eta$    | $0.82 \pm 0.03$                | -0.29                   | $0.06 \pm 0.04$               | -0.61                  |                   |
| $D^0 \rightarrow \pi^0\eta'$   | $-0.39 \pm 0.02$               | 0.43                    | $0.01 \pm 0.02$               | 1.67                   |                   |
| $D^0 \rightarrow \eta\eta$     | $-0.28 \pm 0.01$               | 0.29                    | $-0.58 \pm 0.02$              | 0.18                   |                   |
|                                | $-0.42 \pm 0.02$               | 0.29                    | $-0.74 \pm 0.02$              | 0.18                   |                   |
| $D^0 \rightarrow \eta\eta'$    | $0.49 \pm 0.02$                | -0.30                   | $0.53 \pm 0.03$               | 0.97                   |                   |
|                                | $0.38 \pm 0.02$                | -0.30                   | $0.33 \pm 0.02$               | 0.97                   |                   |
| $D^0 \rightarrow K^+K^-$       | 0                              | 0                       | $-0.42 \pm 0.01$              | -0.54                  | $-2.3 \pm 1.7$    |
|                                | 0                              | 0                       | $-0.54 \pm 0.02$              | -0.54                  |                   |
| $D^0 \rightarrow K^0\bar{K}^0$ | -0.73                          | 0.69                    | $-0.67 \pm 0.01$              | 0.90                   |                   |
|                                | -1.73                          | 0.69                    | $-1.90 \pm 0.01$              | 0.90                   |                   |
| $D^+ \rightarrow \pi^+\pi^0$   | 0                              | 0                       | 0                             | 0                      | $29 \pm 29$       |
| $D^+ \rightarrow \pi^+\eta$    | $0.36 \pm 0.06$                | -0.46                   | $-0.78 \pm 0.06$              | 0.63                   | $17.4 \pm 11.5^a$ |
| $D^+ \rightarrow \pi^+\eta'$   | $-0.20 \pm 0.04$               | 0.30                    | $0.34 \pm 0.07$               | 1.28                   | $-1.2 \pm 11.3^a$ |
| $D^+ \rightarrow K^+\bar{K}^0$ | $-0.08 \pm 0.06$               | -0.08                   | $-0.40 \pm 0.04$              | -0.93                  | $-1.0 \pm 5.9$    |
| $D_s^+ \rightarrow \pi^+K^0$   | $0.08 \pm 0.06$                | -0.01                   | $0.46 \pm 0.03$               | 0.87                   | $66 \pm 24$       |
| $D_s^+ \rightarrow \pi^0K^+$   | $0.01 \pm 0.11$                | 0.17                    | $0.98 \pm 0.10$               | 0.76                   | $266 \pm 228$     |
| $D_s^+ \rightarrow K^+\eta$    | $-0.70 \pm 0.05$               | 0.75                    | $-0.61 \pm 0.05$              | 0.76                   | $93 \pm 152$      |
| $D_s^+ \rightarrow K^+\eta'$   | $0.35 \pm 0.04$                | -0.48                   | $-0.29 \pm 0.12$              | 1.83                   | $60 \pm 189$      |

Cheng and CWC 2012

in units of  $10^{-3}$



# Our $A_{CP}$ Predictions

pQCD results

| Decay Mode                     | $a_{dir}^{(tree)}$ (this work) | $a_{dir}^{(tree)}$ [22] | $a_{dir}^{(tot)}$ (this work) | $a_{dir}^{(tot)}$ [22] | Expt.          |
|--------------------------------|--------------------------------|-------------------------|-------------------------------|------------------------|----------------|
| $D^0 \rightarrow \pi^+\pi^-$   | 0                              | 0                       | $0.96 \pm 0.04$               | 0.74                   | $2.0 \pm 2.2$  |
| $D^0 \rightarrow \pi^0\pi^0$   | 0                              | 0                       | $0.83 \pm 0.04$               | 0.26                   | $1 \pm 48$     |
| $D^0 \rightarrow \pi^0\eta$    | $0.82 \pm 0.03$                | -0.29                   | $0.06 \pm 0.04$               | -0.61                  |                |
| $D^0 \rightarrow \pi^0\eta'$   | $-0.39 \pm 0.02$               | 0.43                    | $0.01 \pm 0.02$               | 1.67                   |                |
| $D^0 \rightarrow \eta\eta$     | $-0.28 \pm 0.01$               | 0.29                    | $-0.58 \pm 0.02$              | 0.18                   |                |
|                                | $-0.42 \pm 0.02$               | 0.29                    | $-0.74 \pm 0.02$              | 0.18                   |                |
| $D^0 \rightarrow \eta\eta'$    | $0.49 \pm 0.02$                | -0.30                   | $0.53 \pm 0.03$               | 0.97                   |                |
|                                | $0.38 \pm 0.02$                | -0.30                   | $0.33 \pm 0.02$               | 0.97                   |                |
| $D^0 \rightarrow K^+K^-$       | 0                              | 0                       | $-0.42 \pm 0.01$              | -0.54                  | $-2.3 \pm 1.7$ |
|                                | 0                              | 0                       | $-0.54 \pm 0.02$              | -0.54                  |                |
| $D^0 \rightarrow K^0\bar{K}^0$ | -0.73                          | 0.69                    | $-0.67 \pm 0.01$              | 0.90                   |                |
|                                | -1.73                          | 0.69                    | $-1.90 \pm 0.01$              | 0.90                   |                |
| $D^+ \rightarrow \pi^+\pi^0$   | 0                              | 0                       | 0                             | 0                      | $29 \pm 29$    |
| $D_s^+ \rightarrow K^+\eta'$   | $0.35 \pm 0.04$                | -0.48                   | $-0.29 \pm 0.12$              | 1.83                   | $60 \pm 189$   |

Cheng and CWC 2012

$\Delta a_{CP}^{dir} = -(0.139 \pm 0.004)\%$  (I)  
 $-(0.151 \pm 0.004)\%$  (II)  
 $\sim 3.6\sigma$  from  $-(0.678 \pm 0.147)\%$

even if  $PE \sim T$ ,  $\Delta a_{CP}^{dir} = -0.27\%$ ,  
 an upper bound in SM,  
 still  $\sim 2.8\sigma$  from data

in units of  $10^{-3}$

# New Physics Interpretations

- Before LHCb result:
  - Extra vector-like quarks, SUSY w/o R-parity, 2HDM, QCD dipole operator from SUSY Grossman, Kagan, Nir 2007
  - Little Higgs with T-parity Bigi, Paul, Rechsiegel 2011
- After LHCb result:
  - FCNC Z Giudice, Isidori, Paradisi; Altmannshofer, Primulando, Yu, Yu
  - FCNC Z'; FCNC heavy gluon Wang and Zhu; Altmannshofer et al
  - 2HDM (charged Higgs) Altmannshofer et al
  - non-MFV SUSY Hiller, Hochberg, Nir; Giudice, Isidori, Paradisi
  - Color-sextet scalar (diquark scalar) Altmannshofer et al; Chen et al
  - Color-octet scalar Altmannshofer et al
  - 4G Rozanov and Vysotsky; Feldmann, Nandi, Soni

# With Constraints

- Some models are ruled out by indirect CPV in D mixing,  $\varepsilon'/\varepsilon$ , etc: FCNC Z, FCNC Z', diquark scalar.
- Some others require fine-tuning in parameters: heavy FCNC gluon, 2HDM, color-octet scalar.

- **The QCD dipole operator**

Grossman, Kagan, Nir 2007  
Giudice, Isidori, Paradisi 2012  
Hiller, Hochberg, Nir 2012

$$O_{8g} = -\frac{g_s}{8\pi^2} m_c \bar{u} \sigma_{\mu\nu} (1 + \gamma_5) G^{\mu\nu} c$$

**is least constrained and can be enhanced.**

- Example: left-right mixing of first two families in up sector,  $(\delta^u_{12})_{LR} \sim 10^{-3}$ , in SUSY
  - usual chiral suppression for D mixing ( $|\Delta C| = 2$ )
  - $m_{\text{SUSY}}/m_c$  enhancement for D decays ( $|\Delta C| = 1$ )

# Large Penguin / QCD Dipole

Cheng and CWC 2012

- Both made to fit  $\Delta a_{CP}^{\text{dir}}$
- Large QCD dipole predicts large CPA's for  $D^0 \rightarrow \pi^0 \pi^0$ ,  $\pi^0 \eta$ , but small ones for  $D^0 \rightarrow \pi^0 \eta'$ ,  $D^+ \rightarrow \pi^+ \eta'$ ,  $K^+ \underline{K}^0$ ,  $D_s^+ \rightarrow \pi^+ K^0$ ,  $K^+ \eta'$
- The other way around for the large penguin scenario
- Discernible using more data

TABLE IV. Direct  $CP$  asymmetries (in units of  $10^{-3}$ ) of SCS  $D \rightarrow PP$  decays estimated in the scenarios with large penguin contributions and large chromomagnetic dipole operator (c.d.o.). The parameters  $\Sigma P$  and  $c_{8g}^{\text{NP}}$  are chosen to fit the data of  $\Delta a_{CP}^{\text{dir}}$ :  $\frac{1}{2} \Sigma P = 2.9 T e^{i85^\circ}$  and  $c_{8g}^{\text{NP}} = 0.017 e^{i14^\circ}$  for Solution I,  $\frac{1}{2} \Sigma P = 3.2 T e^{i85^\circ}$  and  $c_{8g}^{\text{NP}} = 0.012 e^{i14^\circ}$  for Solution II. The number in parentheses is for Solution II of  $E_d$  and  $E_s$  [Eq. (17)].

| Decay mode                      | Large penguins | Large c.d.o.  |
|---------------------------------|----------------|---------------|
| $D^0 \rightarrow \pi^+ \pi^-$   | 3.96 (4.40)    | 5.18 (3.70)   |
| $D^0 \rightarrow \pi^0 \pi^0$   | 0.93 (1.01)    | 8.63 (6.19)   |
| $D^0 \rightarrow \pi^0 \eta$    | 0.09 (0.03)    | -6.12 (-4.15) |
| $D^0 \rightarrow \pi^0 \eta'$   | 2.36 (2.67)    | -0.44 (-0.44) |
| $D^0 \rightarrow \eta \eta$     | -1.79 (-1.64)  | -1.63 (-2.00) |
| $D^0 \rightarrow \eta \eta'$    | 2.65 (1.49)    | -2.30 (-1.08) |
| $D^0 \rightarrow K^+ K^-$       | -2.63 (-2.36)  | -1.46 (-2.88) |
| $D^+ \rightarrow \pi^+ \pi^0$   | 0 (0)          | 0 (0)         |
| $D^+ \rightarrow \pi^+ \eta$    | -3.24 (-3.62)  | -5.35 (-3.67) |
| $D^+ \rightarrow \pi^+ \eta'$   | 2.97 (3.34)    | 0.93 (0.59)   |
| $D^+ \rightarrow K^+ \bar{K}^0$ | -2.95 (-3.28)  | 0.37 (0.29)   |
| $D_s^+ \rightarrow \pi^+ K^0$   | 3.29 (3.66)    | -0.47 (-0.35) |
| $D_s^+ \rightarrow \pi^0 K^+$   | 4.57 (5.08)    | 4.40 (3.14)   |
| $D_s^+ \rightarrow K^+ \eta$    | -0.58 (-0.57)  | 1.59 (0.94)   |
| $D_s^+ \rightarrow K^+ \eta'$   | -5.16 (-5.79)  | 1.76 (1.39)   |

# New LHCb data

- Use  $1.0 \text{ fb}^{-1}$  of data collected in 2011. LHCb 2013
- Include two datasets: prompt (update) and secondary (new as a crosscheck), with little overlap in between.

Prompt:  $\Delta A_{CP} = -(0.34 \pm 0.15 \pm 0.10)\%$

Secondary:  $\Delta A_{CP} = +(0.49 \pm 0.30 \pm 0.14)\%$

- New world average:

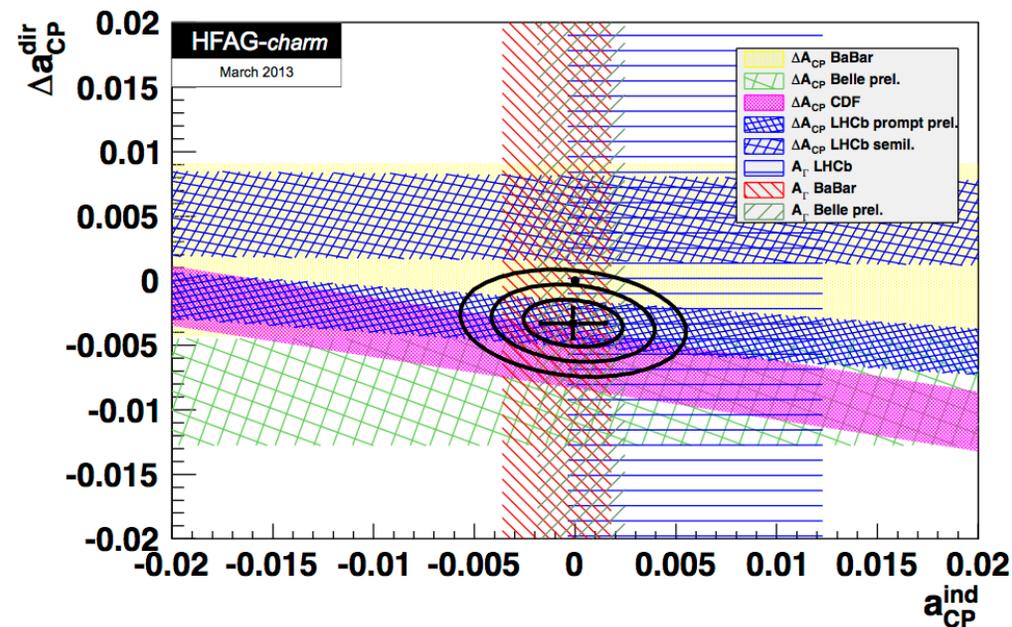
$$a_{CP}^{\text{ind}} = -(0.010 \pm 0.162)\%,$$

$$\Delta a_{CP}^{\text{dir}} = -(0.329 \pm 0.121)\%.$$

$2.7\sigma$  from no CPV  
 $1.5\sigma$  from our estimate

➡ more SM-like now

HFAG 2013



# x and y Parameters

- Assuming no CPV,  $D$ - $\bar{D}$  mixing can be characterized by two parameters

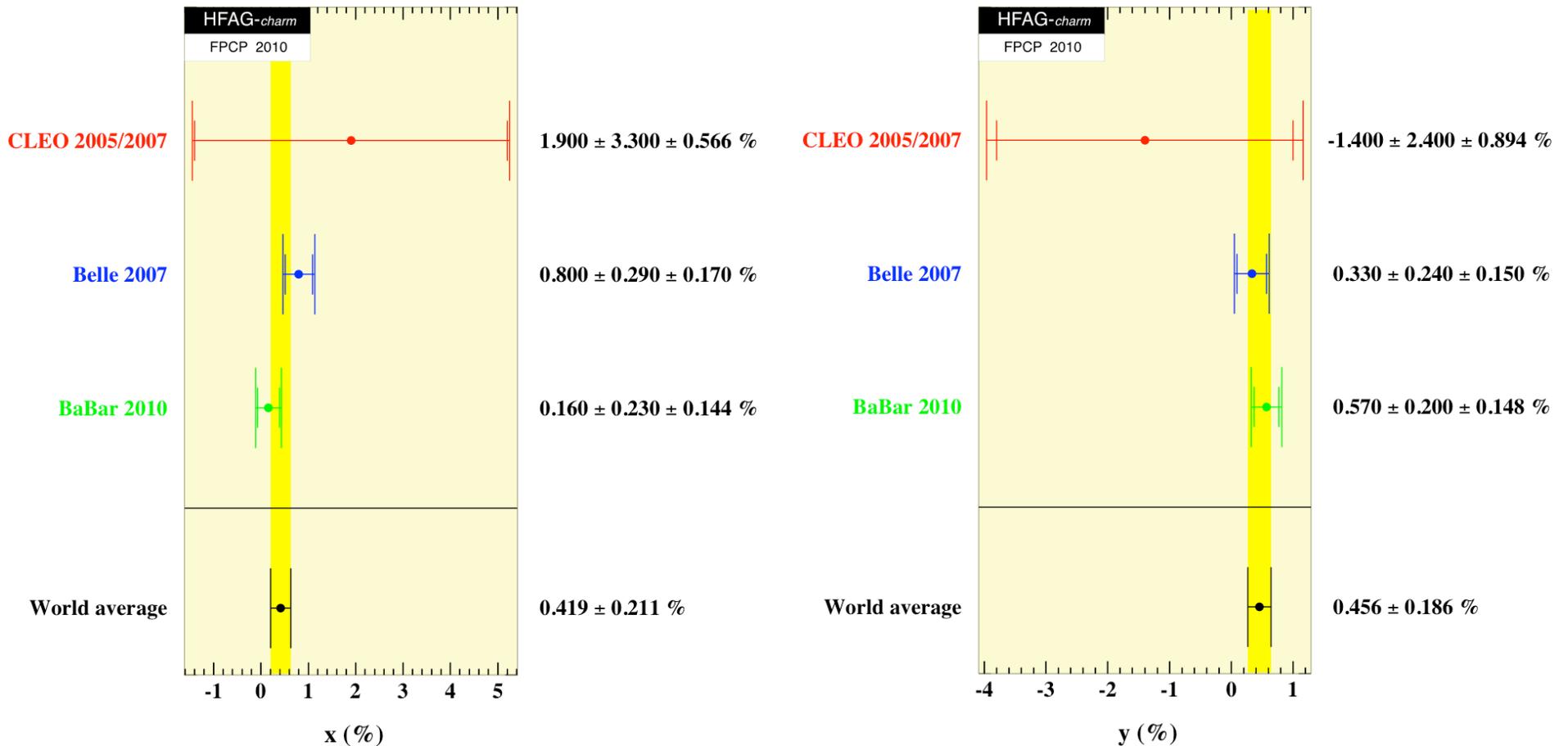
$$x \equiv \frac{\Delta m}{\Gamma} = \frac{m_+ - m_-}{\Gamma} \quad \text{and} \quad y \equiv \frac{\Delta\Gamma}{2\Gamma} = \frac{\Gamma_+ - \Gamma_-}{2\Gamma}$$

where the subscripts (+, -) correspond to the CP eigenstates

$$|D_{\pm}\rangle = \frac{1}{\sqrt{2}}(|D^0\rangle \pm |\bar{D}^0\rangle)$$

- In the SM, the short-distance contributions to these parameters are of order  $10^{-6}$  due to GIM and double Cabibbo suppression. Cheng 1982; Datta and Kumbhakar 1985
- ▶ another good place to look for NP effects?

# x and y from Dalitz Analysis



- They are orders of magnitudes larger than SM short-distance predictions.
- ▣➡ new physics?

# General Properties

- Two approaches:
  - inclusive, depending on heavy-quark expansion;
  - exclusive, summing over all intermediate states.
- In SM,  $x$  and  $y$  are generated at 2nd order in SU(3) breaking:

Falk et al 2002

$$x, y \sim \sin^2 \theta_C \times [SU(3) \text{ breaking}]^2$$

- Inclusive approach generally yields  $x \geq y$ , while exclusive approach tends to have  $x < y$ .
- Possible SU(3) breaking:
  - phase space difference alone can produce  $y \sim 10^{-2}$
  - amplitude difference, depending on model calculations

# Master Formulas for $x$ , $y$

$$x \approx \frac{m_D}{4\pi} \sum_n \eta_{\text{CKM}}(n) \eta_{\text{CP}}(n) \cos \delta_n \sqrt{\mathcal{B}(D^0 \rightarrow n) \mathcal{B}(D^0 \rightarrow \bar{n})} \frac{I(m_1, m_2, \Lambda)}{p_c(n)}$$

$$y \approx \sum_n \eta_{\text{CKM}}(n) \eta_{\text{CP}}(n) \cos \delta_n \sqrt{\mathcal{B}(D^0 \rightarrow n) \mathcal{B}(D^0 \rightarrow \bar{n})} \quad \text{Falk et al 2002}$$

- $\delta_n$  : relative strong phase between  $A(D^0 \rightarrow n)$  and  $A(\underline{D}^0 \rightarrow n)$ .
- $\eta_{\text{CKM}} = \pm 1$ , depending on # of  $s$  and  $\underline{s}$  quarks in final state.
- $\eta_{\text{CP}}$  : CP eigenvalue of state  $n$ .
- $x$  is smaller than  $y$  by about  $4\pi$  because the rest factor  $m_D I(m_1, m_2, \Lambda)/p_c$  is of order 1 (maximal for the  $\pi\pi$  mode and about 2.5).
- Data and predictions based on the flavor symmetry approach are then employed to estimate  $x$  and  $y$ .

# Summary of Experimental Results

| Method   | $x(\times 10^{-3})$                 | $y(\times 10^{-3})$                 | Source     |
|----------|-------------------------------------|-------------------------------------|------------|
| Indirect | $9.8^{+2.4}_{-2.6}$                 | $8.3 \pm 1.6$                       | WA 2008    |
| Direct   | $1.6 \pm 2.3 \pm 1.2 \pm 0.8$       | $5.7 \pm 2.0 \pm 1.3 \pm 0.7$       | BABAR 2010 |
| Direct   | $8.0 \pm 2.9^{+0.9+1.0}_{-0.7-1.4}$ | $3.3 \pm 2.4^{+0.8+0.6}_{-1.2-0.8}$ | Belle 2007 |
| Direct   | $5.6 \pm 1.9^{+0.3+0.6}_{-0.9-0.9}$ | $3.0 \pm 1.5^{+0.4+0.3}_{-0.5-0.6}$ | Belle 2012 |

- **BABAR favors  $x < y$ , while Belle favors the other way.**
- Both of them have results smaller than previous world average from indirect measurements.
- Estimates based on flavor diagram approach give  **$x \sim 0.1\%$  and  $y \sim (0.5-0.7)\%$** , in better agreement with the BABAR result. Cheng and CWC 2010
- No strong indication of new physics with current data.

# Summary

- Flavor diagram approach with SU(3) symmetry breaking effects is useful to explain BR's of SCS  $D \rightarrow PP$  decays.
- Large final-state rescattering effects and thus failure of purely perturbative approach are seen in data.
- Predictions of CPA's are made within SM, and  $\Delta a_{CP}^{\text{dir}}$  is around  $-0.15\%$ ,  $3.6\sigma$  from 2012 data but only  $1.5\sigma$  from new world average.
  - ▣ tension between data and SM predictions is alleviated
- Measurements of other CPA's will help discriminating among different analyses (within and beyond SM).
- Long-distance contributions dominate in the D mixing parameters. Current data do not call for NP.

# Thank You!