



Radiative Penguin Decays at e^+e^- Colliders




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representing the BABAR collaboration



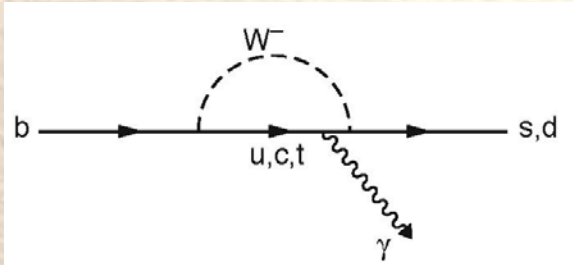
New BABAR Results since FPCP 2012



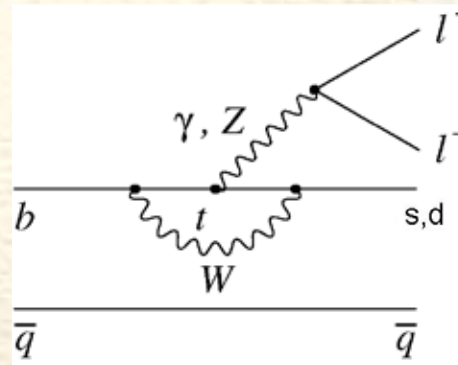
- Review on $b \rightarrow s, d \gamma$ and $b \rightarrow s/d \ell^+ \ell^-$ analyses with focus on 3 new results since FPCP2012
- Study of $B \rightarrow X_s \gamma$ with 424 fb^{-1} using a sum of exclusive modes
● CP asymmetry 
- Analysis of $B \rightarrow \pi/\eta \ell^+ \ell^-$ modes with 424 fb^{-1}
● Branching fraction limits 
BABAR: hep-ex/1303.6010 (2013)
- Study of $B \rightarrow X_{s+d} \gamma$ with 347 fb^{-1} using a fully inclusive method
● γ energy spectrum and γ energy moments
● CP asymmetry 
BABAR: PRL109, 191801 (2012)
PRD86, 112008 (2012)
- All BABAR analyses are blinded

Introduction

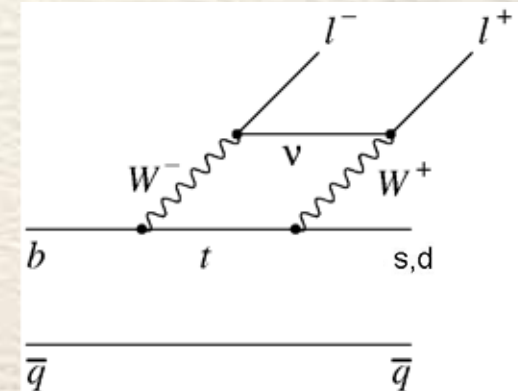
- $B \rightarrow X\gamma$ & $B \rightarrow X\ell^+\ell^-$ are flavor-changing neutral current (FCNC) processes, forbidden in SM at tree level



C_7^{eff} (EM penguin)



C_9^{eff} & C_{10}^{eff} (V & A parts of weak penguin and box)



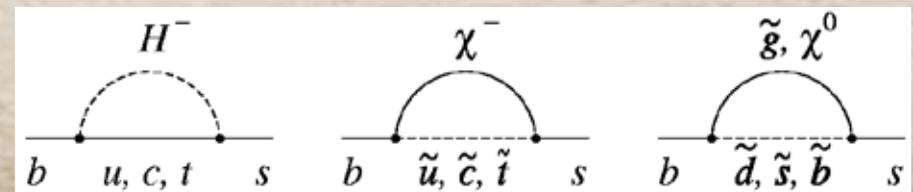
- Effective Hamiltonian factorizes short-distance from long-distance effects [$\mathcal{O}(\alpha_s)$]

$$H_{\text{eff}} = \frac{4G_F}{\sqrt{2}} \sum_i C_i(\mu) \mathcal{O}_i$$

→ 4 effective Wilson coefficient: C_7^{eff} , C_8^{eff} , C_9^{eff} , C_{10}^{eff}

- New physics adds new loops with new particles → modifies SM values of Wilson coefficients and may introduce new terms, e.g. C_S and C_P

- Probe here new physics at a scale of a few TeV



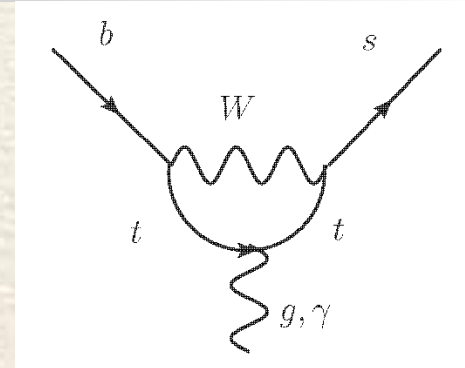


$B \rightarrow X_s \gamma$ Studies

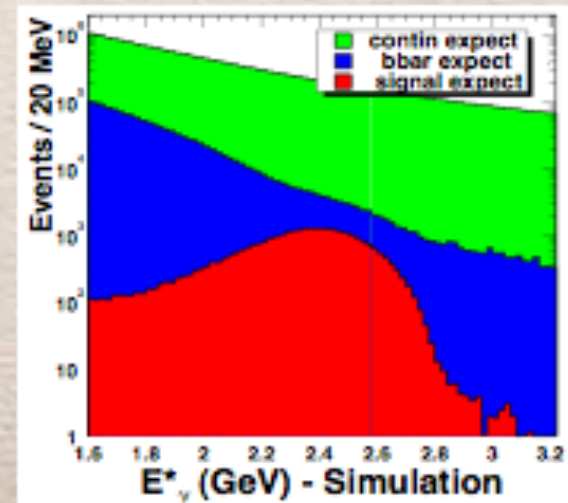
- In the Standard Model (SM) the $B \rightarrow X_s \gamma$ branching fraction is calculated at NNLL (4 loops)

$$\mathcal{B}(B \rightarrow X_s \gamma) = (3.14 \pm 0.22) \times 10^{-4} \quad (E_\gamma > 1.6 \text{ GeV})$$

Misiak *et al.*, PRL98, 022002 (2007); Misiak FCPC 2013



- The shape of the photon energy spectrum depends on b quark momentum inside the B meson (Fermi motion)
- Since the shape function is similar to that in $B \rightarrow X_u \ell \nu$, its measurement helps with determining $|V_{ub}|$
- In the kinetic scheme, measure m_b , energy moments, and HQET parameters, e.g. m_π^2 (kinetic energy of b quark)
- The CP asymmetry is sensitive to new physics
- Three strategies have been used:
 - Fully inclusive analysis with lepton tags ★
 - Semi inclusive analysis ★
 - Fully inclusive analysis with B-reconstruction



Inclusive $B \rightarrow X_s \gamma: E_\gamma$ Spectrum



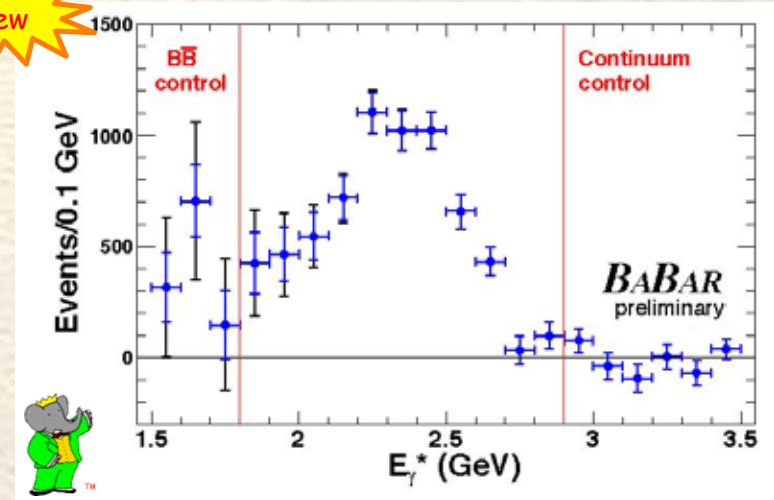
- Use BABAR sample of $(383 \pm 4) \times 10^6$ $B\bar{B}$ events

Measured background subtracted E_γ spectrum

- Tag recoiling B via $Xe^{\pm\nu}$ or $X\mu^{\pm\nu}$ decay to suppress continuum background



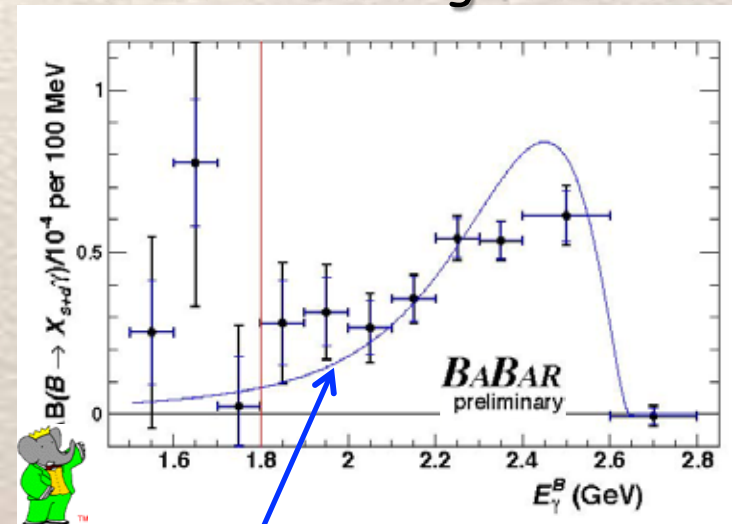
- Use optimized π^0 and η vetoes, E_{miss} , and 2 neural networks (for e, μ each) based on event shape variables



- Signal efficiency is $\epsilon_s \sim 2.5\%$ compared to $\epsilon_{\text{continuum}} = 0.0005\%$ and $\epsilon_{B\bar{B}} = 0.013\%$

Partial branching fraction

- Estimate remaining continuum background from $q\bar{q}$ continuum sample



- From measured E_γ spectrum yield branching fraction after correcting for calorimeter resolution, Doppler smearing and ϵ_{signal}

$$\mathcal{B}(B \rightarrow X_s \gamma) = \left(3.21 \pm 0.15_{\text{stat}} \pm 0.29_{\text{sys}} \pm 0.08_{\text{mod}} \right) \times 10^{-4} \quad (E_\gamma > 1.8 \text{ GeV})$$

Kinetic model with HFAG averages



Inclusive $B \rightarrow X_s \gamma$: Energy Moments

- Total branching fraction from BABAR, Belle and CLEO for different E_γ selection are in good agreement

- Measure energy moments for $E_\gamma > 1.8 \text{ GeV}$

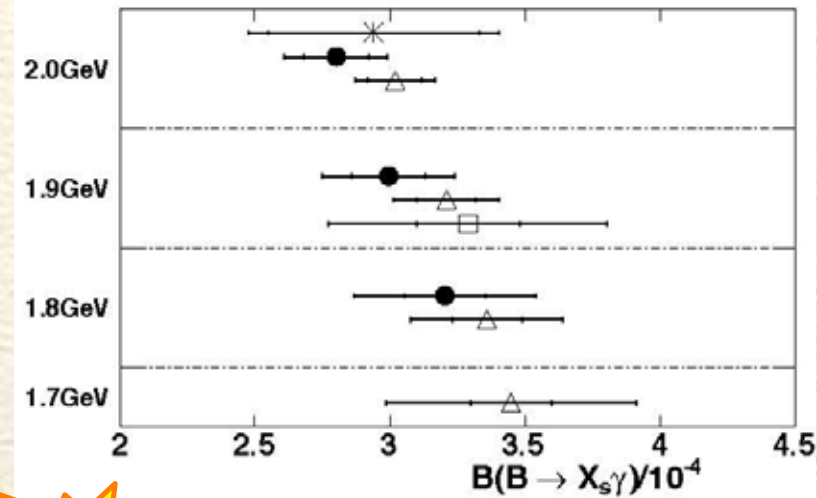


$$\langle E_\gamma \rangle = (2.267 \pm 0.019_{\text{stat}} \pm 0.032_{\text{sys}} \pm 0.003_{\text{mod}}) \text{ GeV}$$

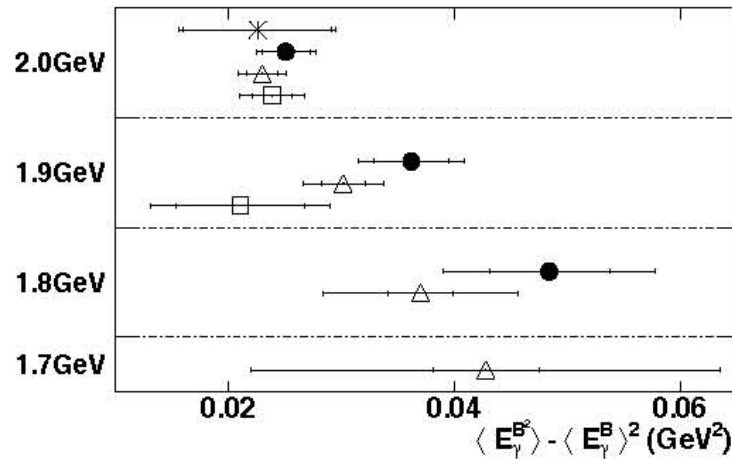
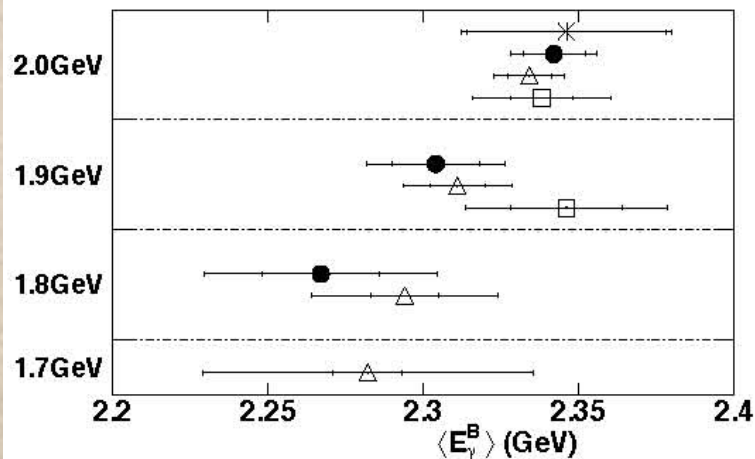
$$\langle (E_\gamma - \langle E_\gamma \rangle)^2 \rangle = (0.0484 \pm 0.0053_{\text{stat}} \pm 0.0077_{\text{sys}} \pm 0.0005_{\text{mod}}) \text{ GeV}^2$$



- Energy moments from BABAR, Belle and CLEO for different E_γ selection are consistent



- BABAR inclusive
- BABAR semi-inclusive
- △ Belle
- * CLEO

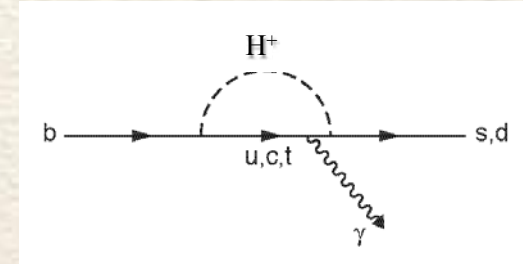


CLEO: PRL 87, 251807 (2001)
 Belle: PRL 103, 241801 (2009)
 BABAR: PRD 72, 052004 (2005)
 BABAR: PRL.100, 191801 (2012)



Inclusive $B \rightarrow X_s \gamma$: New Physics Limits

- In 2Higgs Doublet Models, $B \rightarrow X_s \gamma$ may receive additional contributions from loop diagrams with a charged Higgs



- Extrapolate $\mathcal{B}(B \rightarrow X_s \gamma)$ to $E_\gamma > 1.6 \text{ GeV}$ (1.033 ± 0.006)



$$\mathcal{B}(B \rightarrow X_s \gamma) = (3.31 \pm 0.16 \pm 0.30 \pm 0.09) \times 10^{-4}$$

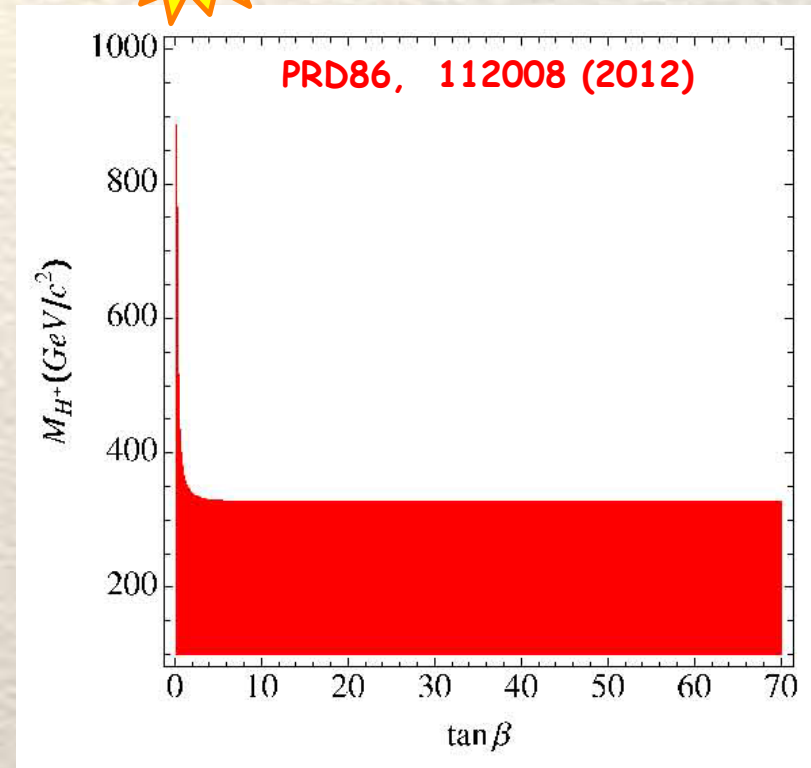


- In good agreement with SM prediction

$$\mathcal{B}(B \rightarrow X_s \gamma) = (3.14 \pm 0.22) \times 10^{-4}$$

- Use extrapolated result to constrain m_{H^\pm} in the type II two-higgs doublet model

- Exclude charged Higgs masses of $m_{H^\pm} < 327 \text{ GeV}$ at 95% CL independent of $\tan \beta$



Haisch: arXiv:0805.2141 (2008)

- Recent BABAR $\mathcal{B}(B \rightarrow D^{(*)} \tau \nu)$ results exclude entire type II 2HDM

hep-ex/1303.0571 (2013)

B → X_sγ: Semi-Inclusive Analysis



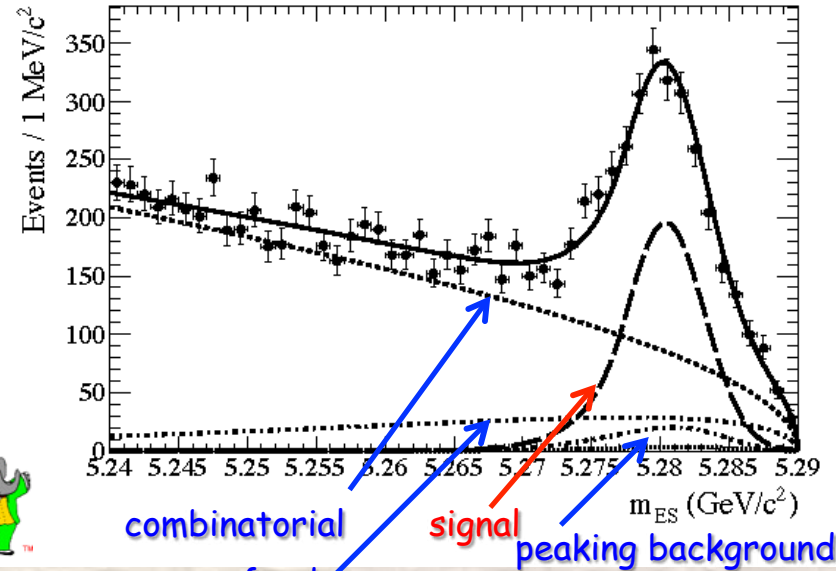
- Use full BABAR sample of $(471 \pm 1) \times 10^6$ $B\bar{B}$ events

$$m_{ES} = \sqrt{\left(\frac{1}{4}E_{CM}^2 - p_B^{*2}\right)}$$

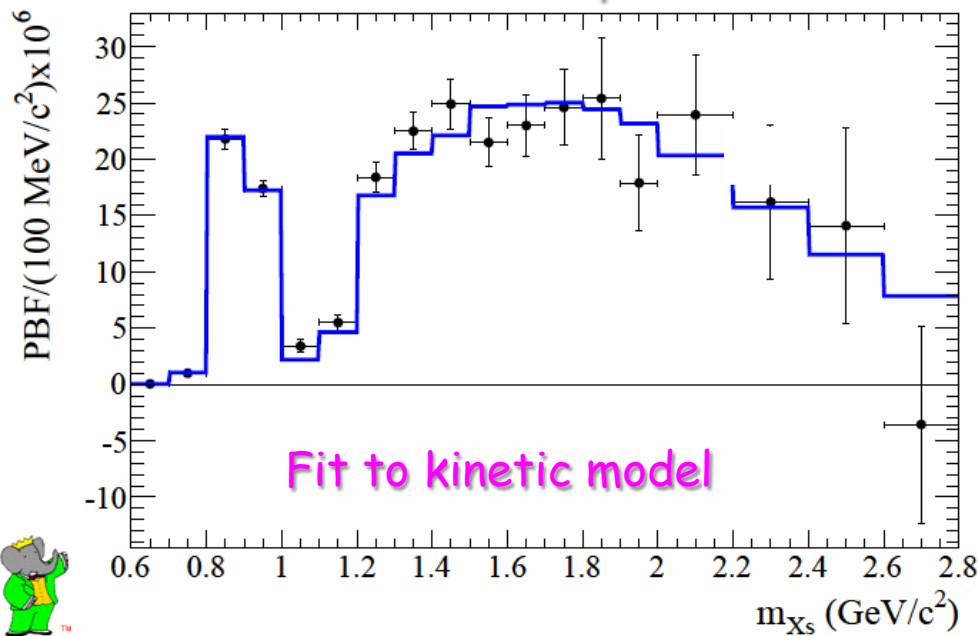
- Reconstruct 38 exclusive X_sγ modes with $\leq 4\pi$ ($\leq 2\pi^0$), 1(3)K ($\leq 1K^0_s$), $\leq 1\eta$

- Measured m_{X_s} is fitted to kinetic and shape function models

PRD86, 052012 (2012)



Hadronic mass spectrum



- BABAR results agree well with WA

BABAR	kinetic model	shape function model
m_b [GeV/c ²]	$4.568^{+0.038}_{-0.036}$	$4.579^{+0.032}_{-0.029}$
μ_π^2 [GeV/c ²]	$0.450^{+0.054}_{-0.054}$	$0.257^{+0.034}_{-0.039}$

World average	kinetic model	shape function model
m_b [GeV/c ²]	4.591 ± 0.031	$4.620^{+0.039}_{-0.032}$
μ_π^2 [GeV/c ²]	0.454 ± 0.038	$0.288^{+0.054}_{-0.074}$

Benson et al., Nucl.Phys B710, 371 (2005)
 Lange et al., Phys Rev D72, 073006 (2005)

G. Eigen, FPCP13 Rio de Janeiro, 22/05/2013

HFAG: arXiv:1010.1589v3 (2011)

$B \rightarrow X_s \gamma$: Branching Fractions

- Reconstruct $X_s \rightarrow$ Calculate E_γ by

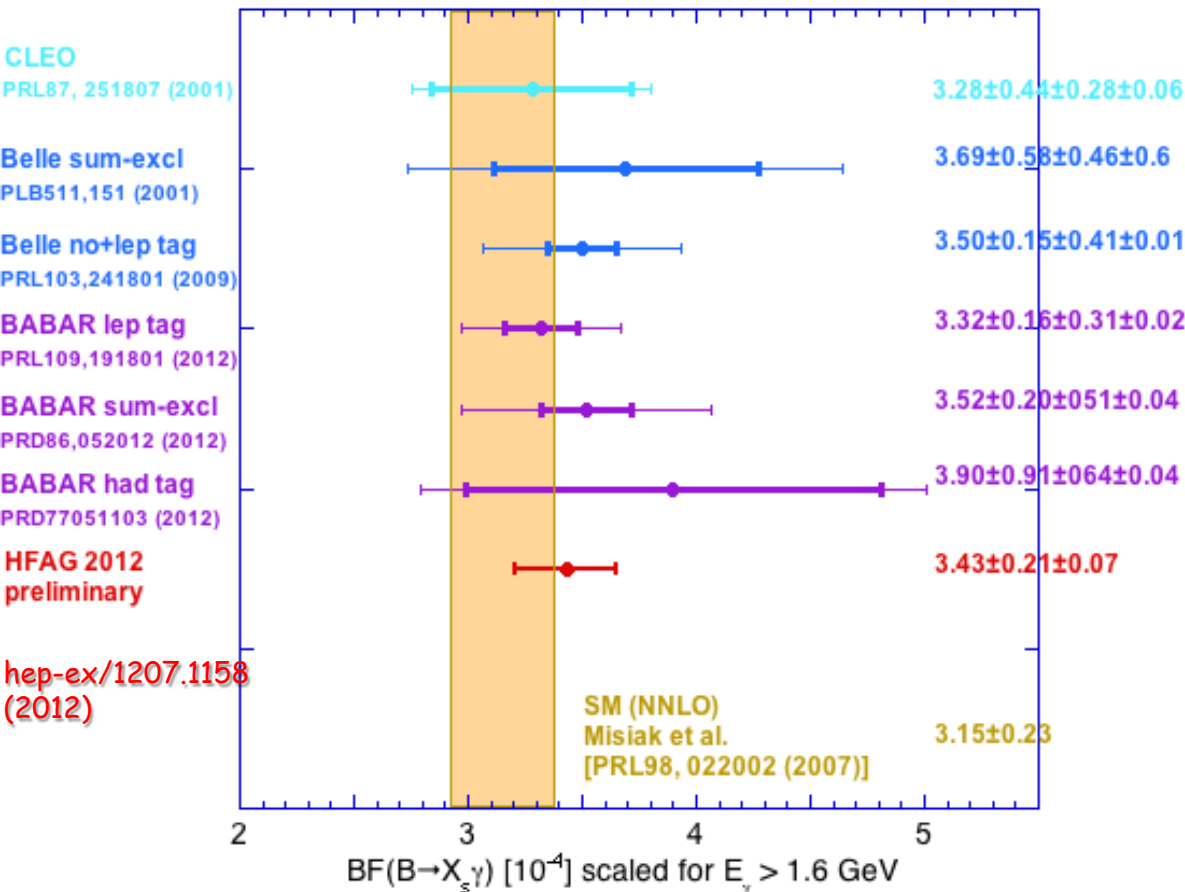
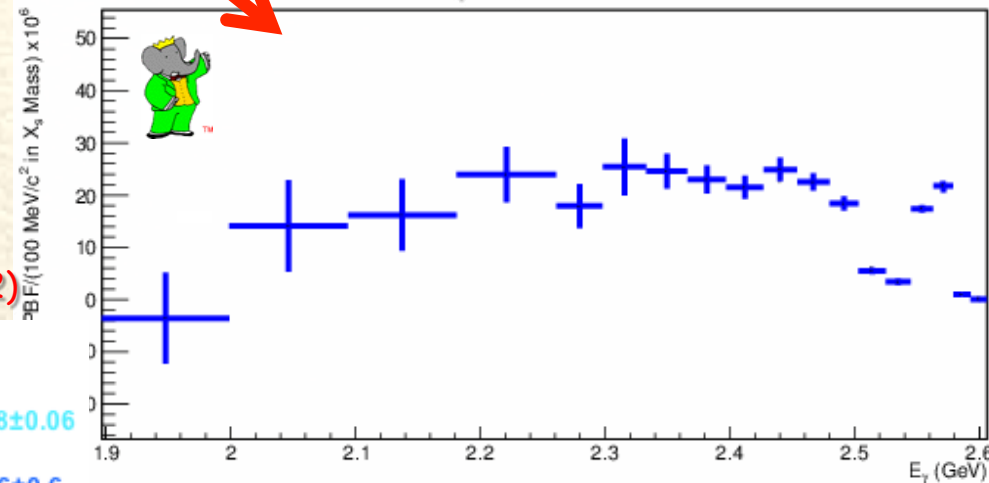
$$E_\gamma = (m_B^2 - m_{X_s}^2) / 2m_B$$

- Sum partial branching fractions in each m_{X_s} bin to yield total branching fraction ($E_\gamma > 1.9$ GeV)

$$\mathcal{B}(\bar{B} \rightarrow X_s \gamma) = (3.29 \pm 0.19_{\text{stat}} \pm 0.48_{\text{sys}}) \times 10^{-4}$$

Phys.Rev. D86, 052012 (2012)

E_γ spectrum



- Compare all $B \rightarrow X_\gamma$ total branching fractions after extrapolating measured values to $E_\gamma > 1.6$ GeV

- All $B \rightarrow X_\gamma$ branching fraction measurements are in good agreement with one another and with the SM prediction

$B \rightarrow X_s \gamma$: Direct A_{CP}

- For the sum of exclusive decays, the CP asymmetry is measured by

$$A_{CP}(X_s \gamma) \equiv \frac{\Gamma(\bar{B} \rightarrow \bar{X}_s \gamma) - \Gamma(B \rightarrow X_s \gamma)}{\Gamma(\bar{B} \rightarrow \bar{X}_s \gamma) + \Gamma(B \rightarrow X_s \gamma)}$$

- The SM predictions yield $-0.6\% < A_{CP}(X_s \gamma) < 2.8\%$

- The present world average is $A_{CP}(X_s \gamma) = -0.8 \pm 2.9$

- The difference for charged and neutral B decays is

$$\Delta A_{CP}(X_s \gamma) = A_{CP}(B^+ \rightarrow X_s^+ \gamma) - A_{CP}(B^0 \rightarrow X_s^0 \gamma)$$

- $\Delta A_{CP}(B \rightarrow X_s \gamma)$ depends on C_7^{eff} and C_8^{eff} :

$$\Delta A_{CP}(X_s \gamma) \approx 4\pi^2 \alpha_s \frac{\bar{\Lambda}_{78}}{m_b} \Im m \frac{C_8^{\text{eff}}}{C_7^{\text{eff}}} \approx 0.12 \frac{\bar{\Lambda}_{78}}{100 \text{ MeV}} \Im m \frac{C_8^{\text{eff}}}{C_7^{\text{eff}}}$$

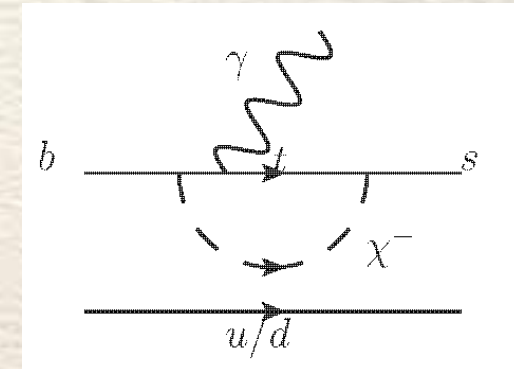
$$17 \text{ MeV} < \bar{\Lambda}_{78} < 190 \text{ MeV}$$

Benzke et al., PRL106, 141801 (2011)

- In the SM, C_7^{eff} and C_8^{eff} are real $\rightarrow \Delta A_{CP}(X_s \gamma) = 0$

- This may be modified by new physics contributions

- BABAR has performed a new semi-inclusive analysis with $471 \times 10^6 B\bar{B}$**



New physics contribution to C_7^{eff}

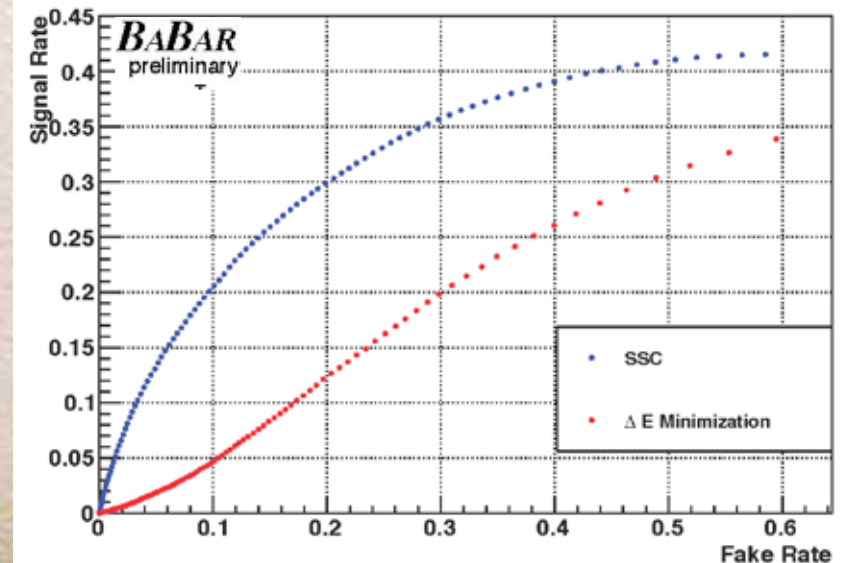
$B \rightarrow X_s \gamma$: Event Selection for A_{CP}



- Use full BABAR sample of $(471 \pm 1) \times 10^6$ $B\bar{B}$ events
- Reconstruct 16 exclusive modes to measure A_{CP} in semi-inclusive analysis
- Maximize signal extraction with **S**ignal **S**electing **C**lassifier \rightarrow bagged decision tree with 6 inputs
- Select candidate with maximum SSC \rightarrow improved efficiency compared to ΔE selection
- Train separate bagged decision tree to separate true primary γ from that of π^0 decay
- Use **B**ackground **R**ejection **C**lassifier to remove continuum background based on bagged decision trees using event shape variables
- Use X_s mass-dependent optimization for $S/(S+B)^{1/2}$ & loose K, π IDs

Final State

$B^+ \rightarrow K_S \pi^+ \gamma$
$B^+ \rightarrow K^+ \pi^0 \gamma$
$B^0 \rightarrow K^+ \pi^- \gamma$
$B^+ \rightarrow K^+ \pi^+ \pi^- \gamma$
$B^+ \rightarrow K_S \pi^+ \pi^0 \gamma$
$B^+ \rightarrow K^+ \pi^0 \pi^0 \gamma$
$B^0 \rightarrow K^+ \pi^- \pi^0 \gamma$
$B^+ \rightarrow K_S \pi^+ \pi^- \pi^+ \gamma$
$B^+ \rightarrow K^+ \pi^+ \pi^- \pi^0 \gamma$
$B^+ \rightarrow K_S \pi^+ \pi^0 \pi^0 \gamma$
$B^0 \rightarrow K^+ \pi^+ \pi^- \pi^- \gamma$
$B^0 \rightarrow K^+ \pi^- \pi^0 \pi^0 \gamma$
$B^+ \rightarrow K^+ \eta (\rightarrow \gamma \gamma) \gamma$
$B^0 \rightarrow K^+ \eta (\rightarrow \gamma \gamma) \pi^- \gamma$
$B^+ \rightarrow K^+ K^- K^+ \gamma$
$B^0 \rightarrow K^+ K^- K^+ \pi^- \gamma$



$B \rightarrow X_s \gamma$: Semi-Inclusive A_{CP} Results

- Fit m_{ES} for \bar{B} and B tagged samples simultaneously to extract A_{CP}
- Correct raw asymmetry for detector bias determined from sidebands
- In full X_s mass region determine corrected A_{CP}



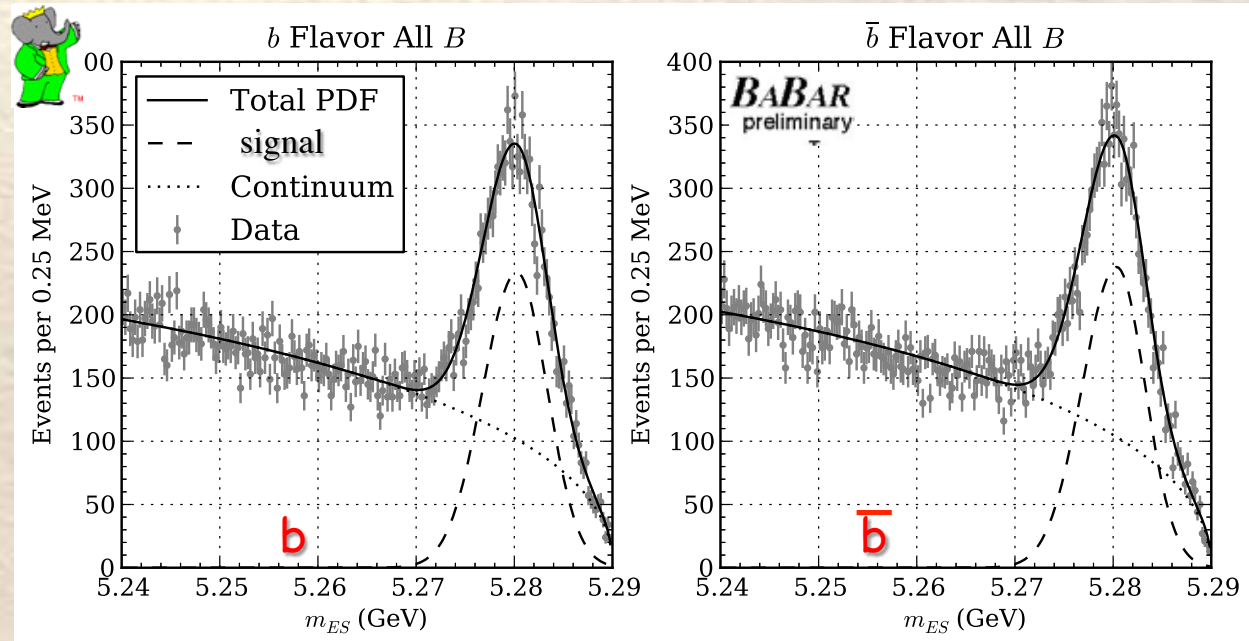
$$A_{CP}(X_s \gamma) = (1.73 \pm 1.93_{\text{stat}} \pm 1.02_{\text{sys}}) \%$$



- This agrees well with the SM prediction

$$-0.6\% < A_{CP}^{SM}(X_s \gamma) < 2.8\%$$

- These new results have the **lowest** uncertainties



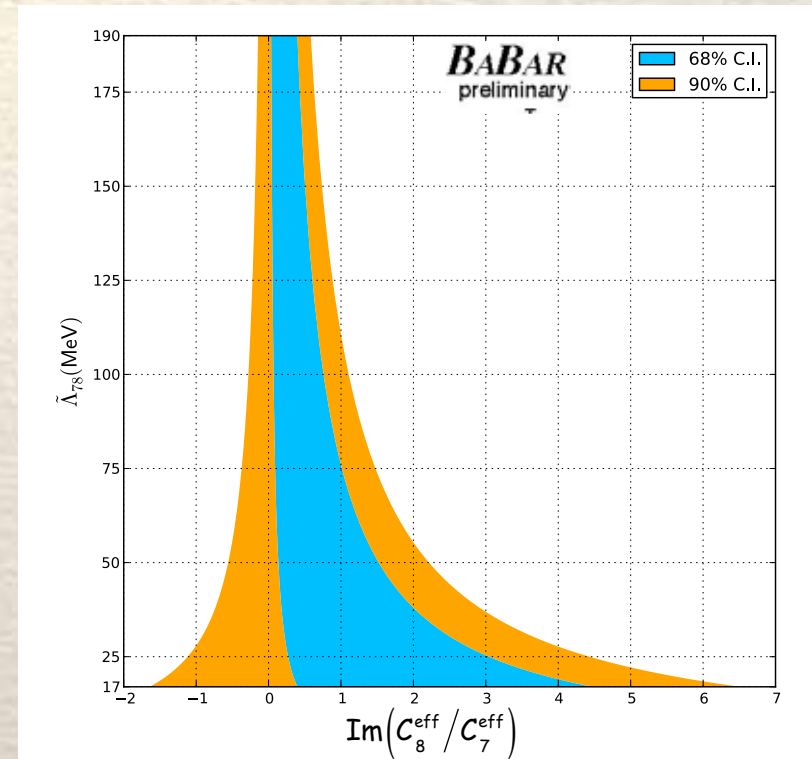
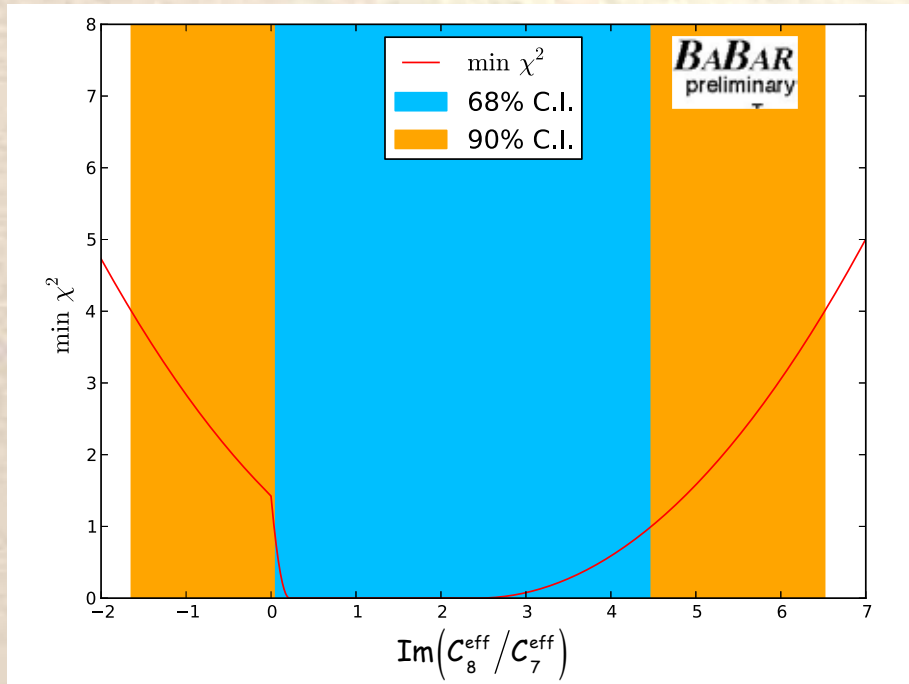
$B \rightarrow X_s \gamma$: Implications on $\text{Im}(C_{8g}/C_{7\gamma})$

- From the simultaneous fits to charged and neutral B samples measure

$$\Delta \mathcal{A}_{CP}(X_s \gamma) = (4.97 \pm 3.90_{\text{stat}} \pm 1.45_{\text{sys}}) \%$$

- Set 90% CL constraints on $\text{Im}(C_8^{\text{eff}}/C_7^{\text{eff}})$

$$-1.64 < \text{Im}(C_8^{\text{eff}}/C_7^{\text{eff}}) < 6.52 \text{ @90\% CL}$$



- This is the **first** $\Delta \mathcal{A}_{CP}(X_s \gamma)$ measurement and the **first constraint** on the ratio of Wilson coefficients $C_8^{\text{eff}}/C_7^{\text{eff}}$ for new physics in this process



$B \rightarrow X_s \gamma$: A_{CP} from Inclusive Decays

- In the fully inclusive analysis, the CP asymmetry involves $b \rightarrow s \gamma$ & $b \rightarrow d \gamma$ contributions



$$A_{CP}(X_{s+d}\gamma) \equiv \frac{B(\bar{B} \rightarrow X_{s+d}\gamma) - B(B \rightarrow X_{s+d}\gamma)}{B(\bar{B} \rightarrow X_{s+d}\gamma) + B(B \rightarrow X_{s+d}\gamma)}$$

- Use BABAR sample of 383×10^6 $B\bar{B}$ events
- Determine B/\bar{B} from the tag charge
- Correct A_{CP} for charge bias and mistagging

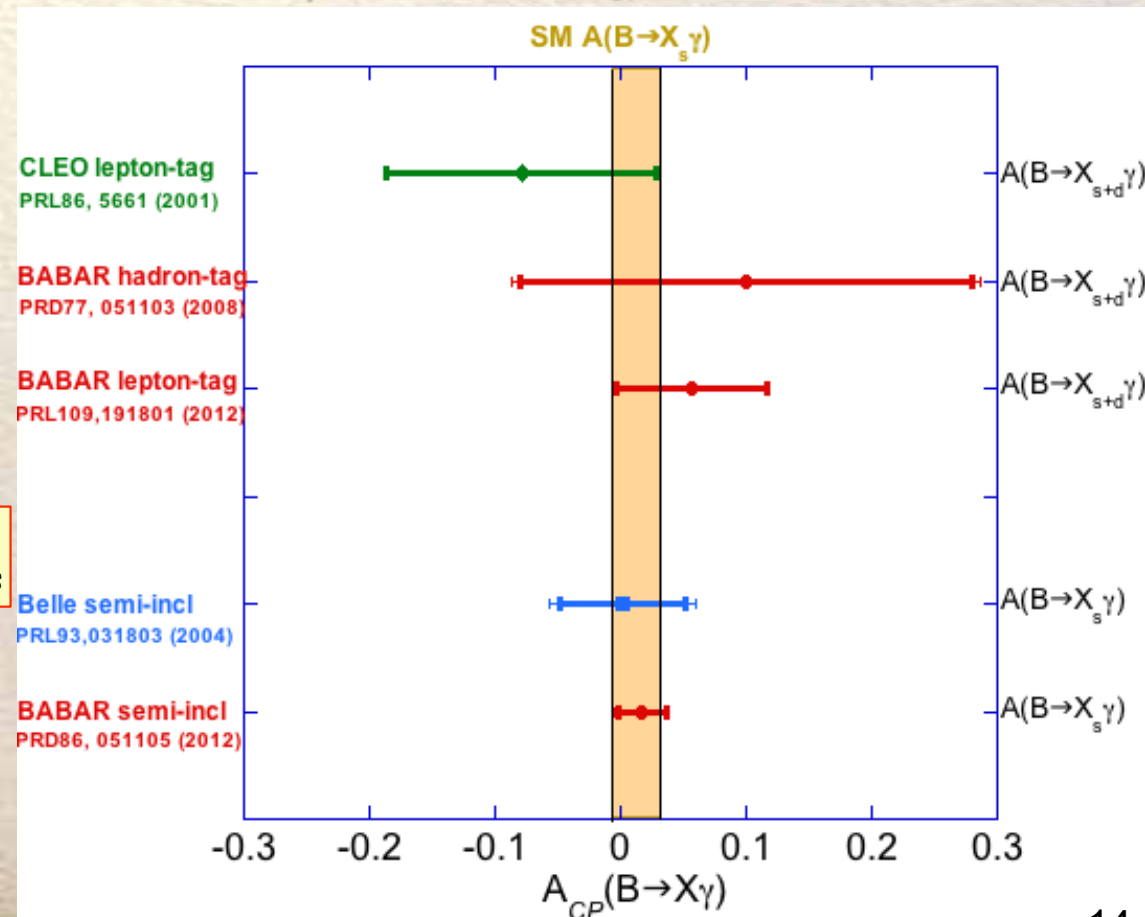


$$A_{CP}(X_{s+d}\gamma) = 0.057 \pm 0.060_{\text{stat}} \pm 0.018_{\text{sys}}$$

PRL109, 191801 (2012)

- All A_{CP} measurements are in good agreement with the SM prediction

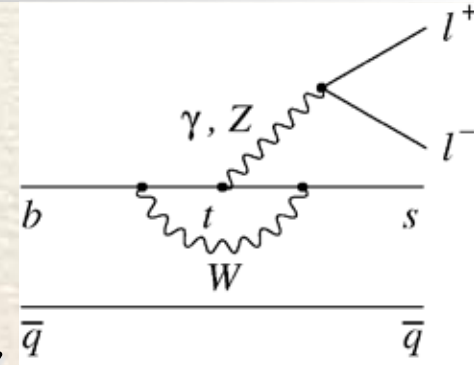
Comparison of A_{CP} Measurements



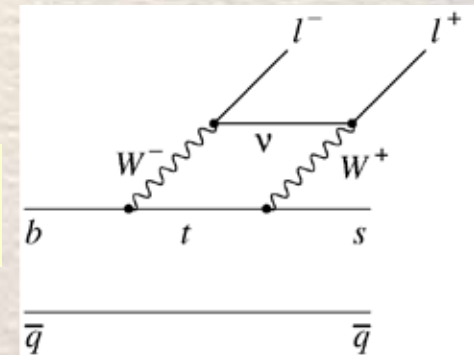
Analysis Methodology for $B \rightarrow K^{(*)} \ell^+ \ell^-$



- Fully reconstruct $B \rightarrow K^{(*)} \ell^+ \ell^-$ final states
 - 8 in **BABAR** ($471 \times 10^6 B\bar{B}$): $K, K^0_S, K^\pm \pi^\mp$ or $K^0_S \pi^\pm$
 - 10 in **Belle** ($657 \times 10^6 B\bar{B}$): $K, K^0_S, K^\pm \pi^\mp, K^\pm \pi^0$ or $K^0_S \pi^\pm$
 - these hadrons recoil against e^+e^- or $\mu^+\mu^-$
 - Select e^\pm with $p > 0.3$ (0.4) GeV/c; μ^\pm with $p > 0.7$ GeV/c
 - Require good particle ID for e, μ, K, π ;
select $K^0_S \rightarrow \pi^+ \pi^-$



- Utilize kinematic variables $m_{ES} = \sqrt{\left(\frac{E_{CM}^2}{4} - p_B^{*2}\right)}$ and $\Delta E = E_B^* - \frac{E_{CM}}{2}$

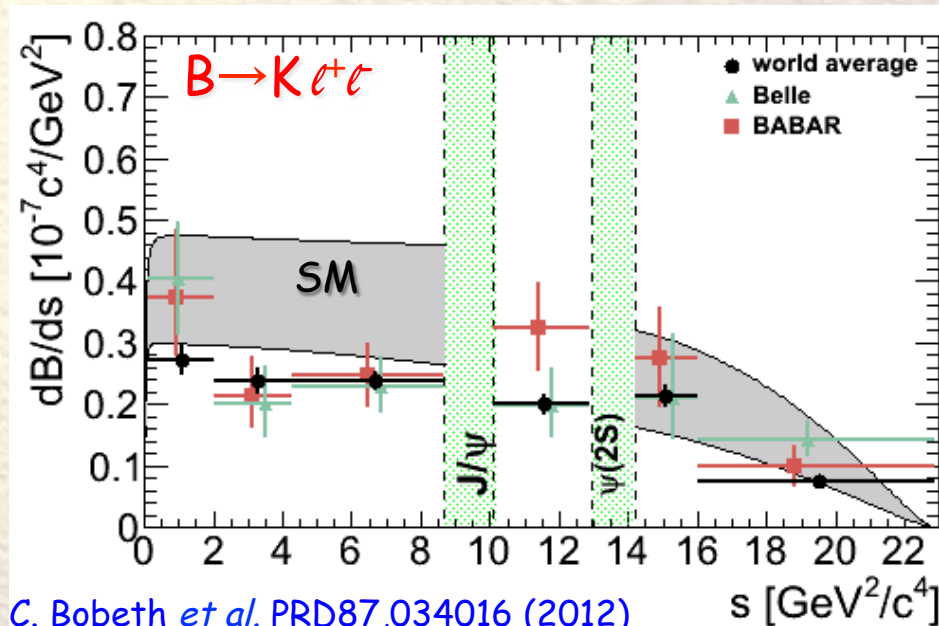


- Suppress combinatorial $B\bar{B}$ & $q\bar{q}$ backgrounds:
 - BABAR** defines 8 boosted decision trees, **Belle** uses likelihood
- Veto J/ψ and $\psi(2S)$ mass regions and use them as control samples
- Use pseudo-experiments to study performance
- Measure branching fractions, rate asymmetries and angular observables

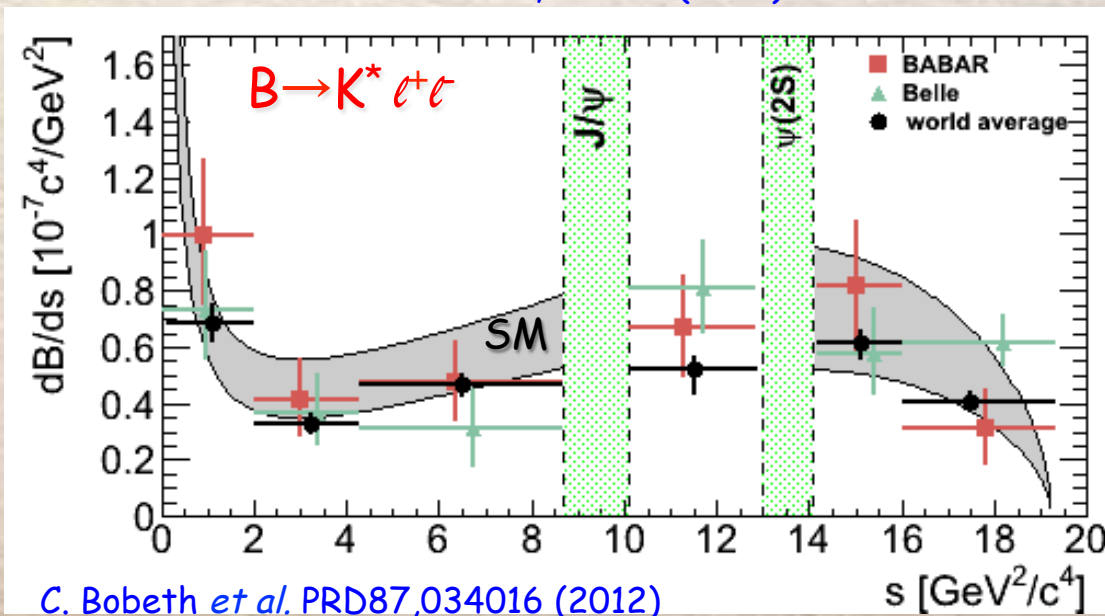


$B \rightarrow K^{(*)} e^+ e^-$: Partial Branching Fractions

- In the SM, partial branching fractions $d\mathcal{B}/ds$ are calculated at
 - Low $s=q^2=m_\ell^2$, large hadronic recoil $E_{K^*} \gg \Lambda \rightarrow$ use QCD factorization
 - High $s \sim \mathcal{O}(m_b)$ small hadronic recoil $E_{K^*} \sim \Lambda \rightarrow$ use OPE in $1/m_b$
 - Large errors come from errors of form factors in hadronic MEs



- $d\mathcal{B}/ds$ is measured in 6 s bins
 - BABAR, Belle: $B \rightarrow K^{(*)} e^+ e^-$
 - CDF, LHCb: $B \rightarrow K^{(*)} \mu^+ \mu^-$
 - CMS, ATLAS: $B \rightarrow K^{*0} \mu^+ \mu^-$
 - Do naive average (WA) (dominated by LHCb)



BABAR	PRD86, 052012 (2012)
Belle	PRL103, 171801 (2009)
CDF	CDF-note 10894 (2012)
CMS	CMS PAS BPH-11-009 (2013)
LHCb	hep-ex/1304.6325 (2013) JHEP1212,125 (2012)

$B \rightarrow K^{(*)} \ell^+ \ell^-$: Total Branching Fractions



At low s ($1 < s < 6 \text{ GeV}^2/c^4$) measure

WA $B(B \rightarrow K \ell^+ \ell^-) = (1.25 \pm 0.08) \times 10^{-7}$

$B(B \rightarrow K^* \ell^+ \ell^-) = (1.77 \pm 0.18) \times 10^{-7}$

BABAR	PRD86, 052012 (2012)	CMS	CMS PAS BPH-11-009 (2013)
Belle	PRL103, 171801 (2009)	LHCb	hep-ex/1304.6325 (2013)
CDF	CDF-note 10894 (2012)		JHEP1212,125 (2012)

Good agreement with the SM

Bobeth et al: Phys.Rev. D87 (2013) 034016,
JHEP 1201 (2012) 107

BABAR B_{tot} measurements yield

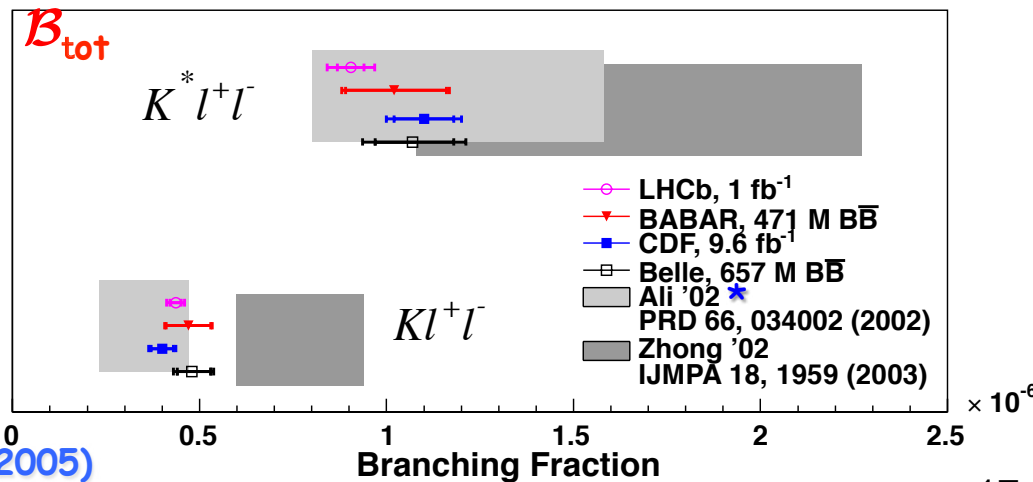
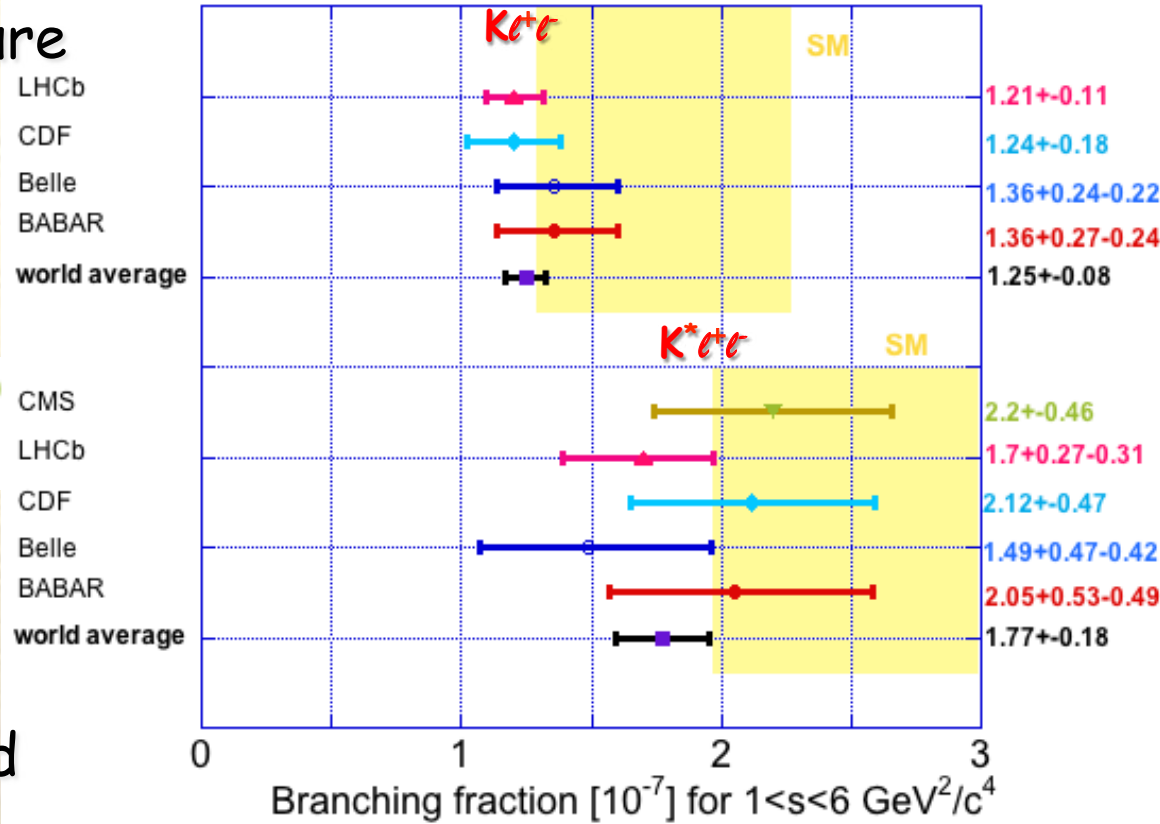
$B(B \rightarrow K \ell^+ \ell^-) = (4.7 \pm 0.6 \pm 0.2) \times 10^{-7}$

$B(B \rightarrow K^* \ell^+ \ell^-) = (10.2^{+1.4}_{-1.3} \pm 0.5) \times 10^{-7}$

BABAR B_{tot} results agree well with the SM prediction by Ali et al. & those of other experiments

Ball and Zwicky, PRD 71, 014015 (2005); ibid 014029 (2005)

G. Eigen, FPCP13 Rio de Janeiro, 22/05/2013





$B \rightarrow K^{(*)} \ell^+ \ell^-$: Isospin Asymmetry

$$A_I \equiv \frac{B(B^0 \rightarrow K^{(*)0} \ell^+ \ell^-) - r_\tau B(B^\pm \rightarrow K^{(*)\pm} \ell^+ \ell^-)}{B(B^0 \rightarrow K^{(*)0} \ell^+ \ell^-) + r_\tau B(B^\pm \rightarrow K^{(*)\pm} \ell^+ \ell^-)}$$

$$r_\tau = \tau_{B^0} / \tau_{B^\pm} = 1 / (1.071 \pm 0.09)$$

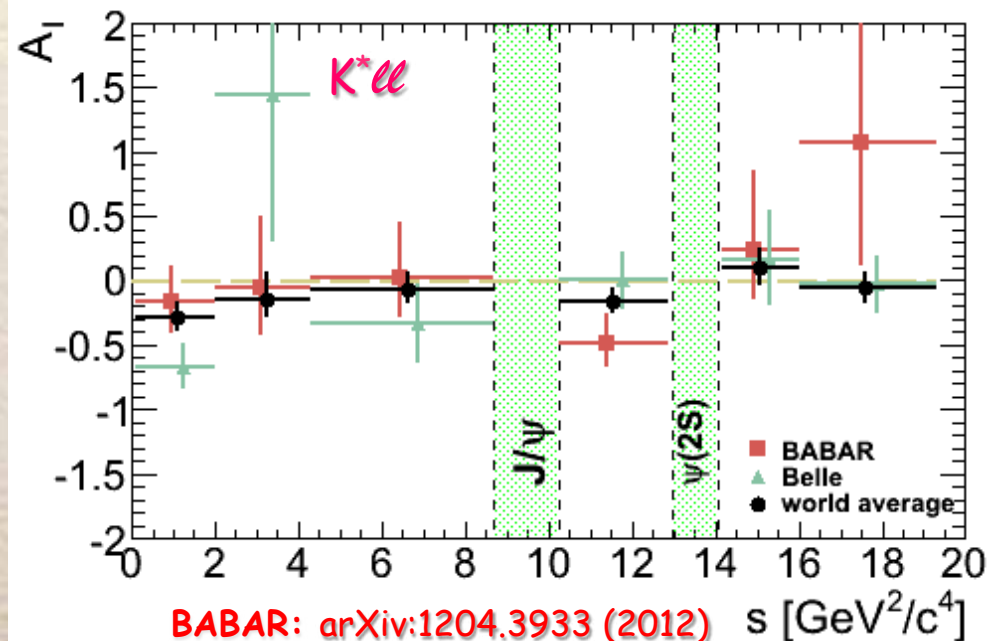
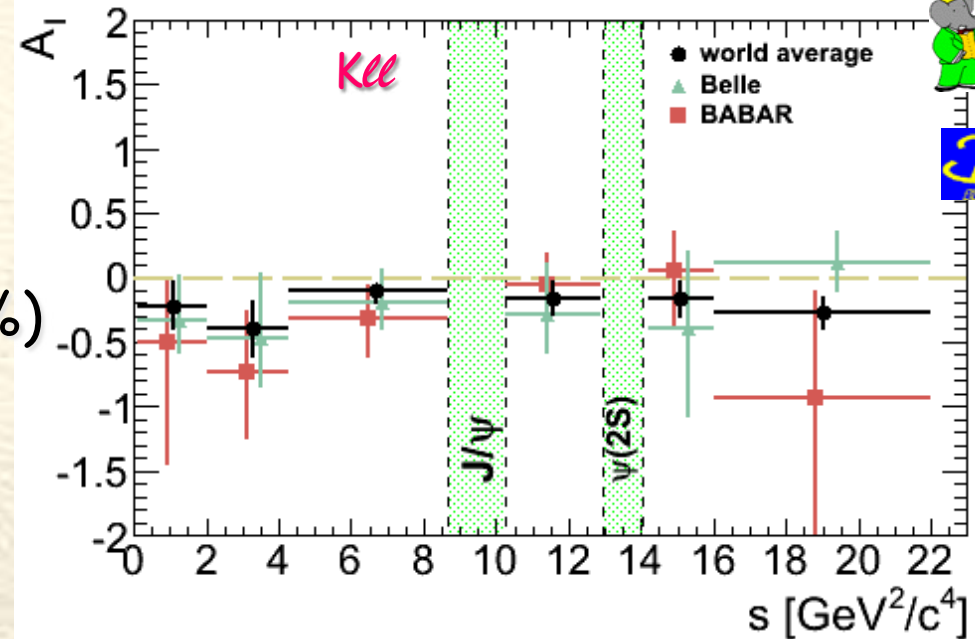
- In the SM, A_I is expected at $\mathcal{O}(+1\%)$
Feldmann & Matias JHEP 0301, 074 (2003)

- Average A_I measurements from BABAR, Belle, CDF & LHCb at low s ($1 < s < 6 \text{ GeV}^2/c^4$)

$$A_I^{\text{low}}(B \rightarrow K \ell^+ \ell^-) = -0.31 \pm 0.12$$

$$A_I^{\text{low}}(B \rightarrow K^* \ell^+ \ell^-) = -0.15 \pm 0.11$$

- At low s , A_I is below the SM, but consistent with the SM
- BABAR results agree with those from Belle and the WA dominated by LHCb



BABAR: arXiv:1204.3933 (2012)

Belle: PRL 103, 171801 (2009)

LHCb: arXiv:1205.3422 (2012)

$B \rightarrow K^{(*)} \ell^+ \ell^-$: CP Asymmetry

$$A_{CP} \equiv \frac{B(\bar{B} \rightarrow \bar{K}^{(*)} \ell^+ \ell^-) - B(B \rightarrow K^{(*)} \ell^+ \ell^-)}{B(\bar{B} \rightarrow \bar{K}^{(*)} \ell^+ \ell^-) + B(B \rightarrow K^{(*)} \ell^+ \ell^-)}$$

- In the SM, $A_{CP} = -0.01$

Krüger *et al.*, PRD 61, 114028 (2000)

Bobeth *et al.*, JHEP 807,106, (2008)

- A_{CP} is measured by BABAR, Belle in $B \rightarrow K^{(*)} \ell^+ \ell^-$

- $e.g.$ in all s , BABAR measured

$$A_{CP}(B \rightarrow K \ell^+ \ell^-) = -0.03 \pm 0.14 \pm 0.01$$

$$A_{CP}(B \rightarrow K^* \ell^+ \ell^-) = 0.03 \pm 0.13 \pm 0.01$$

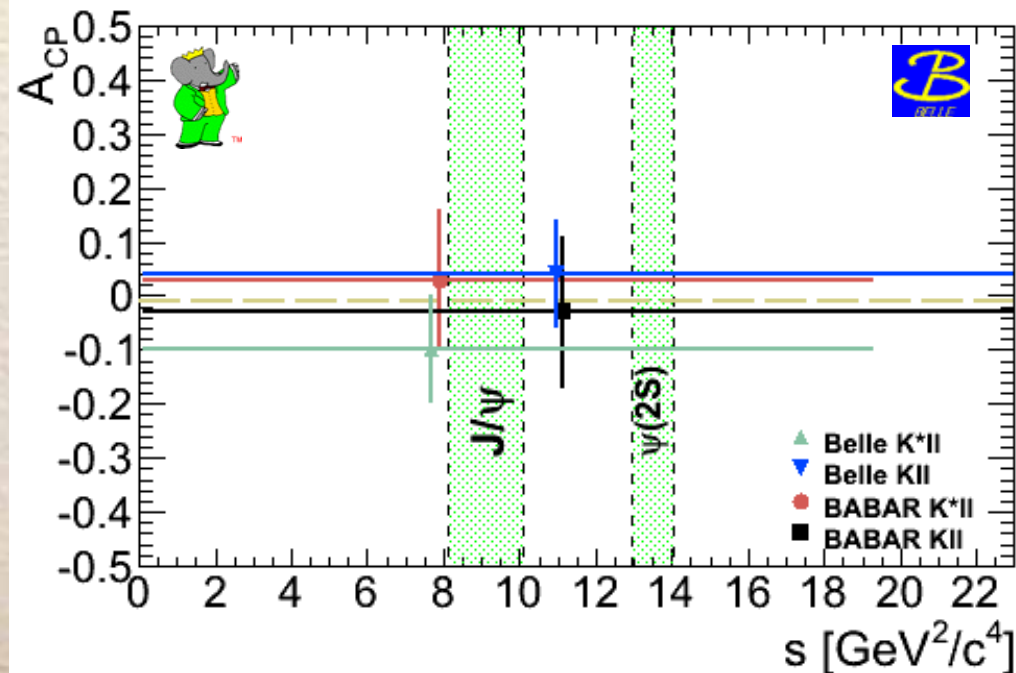
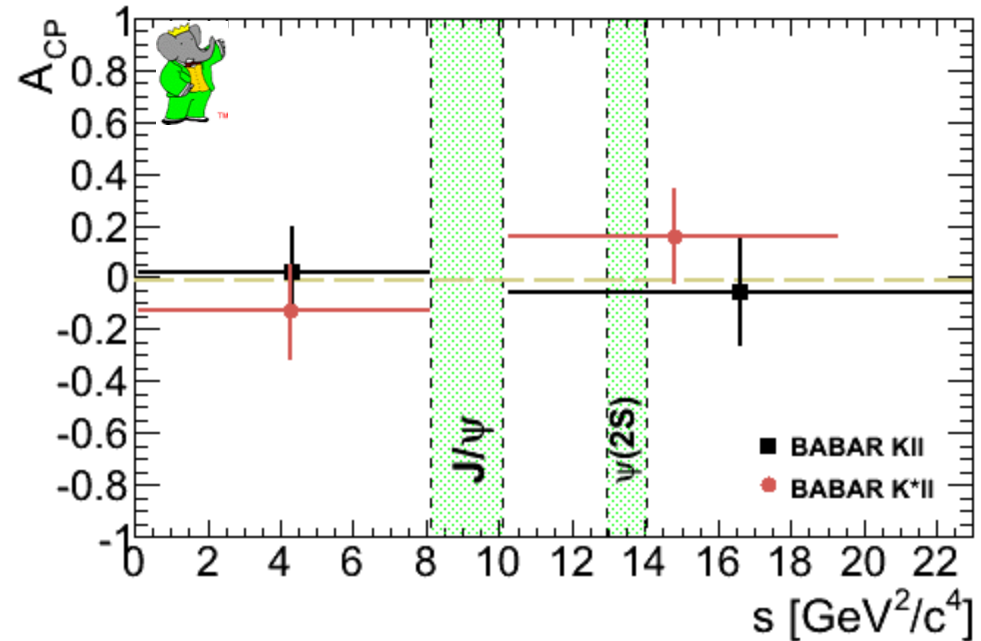
- LHCb measured A_{CP} in $B \rightarrow K^* \mu^+ \mu^-$

LHCb: PRL 110, 031801 (2013)

- All A_{CP} results are consistent with zero \rightarrow agree with small SM value

BABAR: PRD86,032012 (2012)

Belle: PRL 103, 171801 (2009)



$B \rightarrow K^{(*)} \ell^+ \ell^-$: Lepton Flavor Ratio



$$\mathcal{R}_{K^{(*)}} \equiv \frac{\mathcal{B}(B \rightarrow K^{(*)} \mu^+ \mu^-)}{\mathcal{B}(B \rightarrow K^{(*)} e^+ e^-)} \quad s \geq (2m_\mu)^2$$

In the SM, $\mathcal{R}_{K^{(*)}} = 1$ for $s \geq (2m_\mu)^2$

$\mathcal{R}_{K^{(*)}}$ is measured by BABAR, Belle in $B \rightarrow K^{(*)} \ell^+ \ell^-$

e.g. in all s , BABAR measured

$$\mathcal{R}_K(B \rightarrow K \ell^+ \ell^-) = 1.00^{+0.31}_{-0.25} \pm 0.07$$

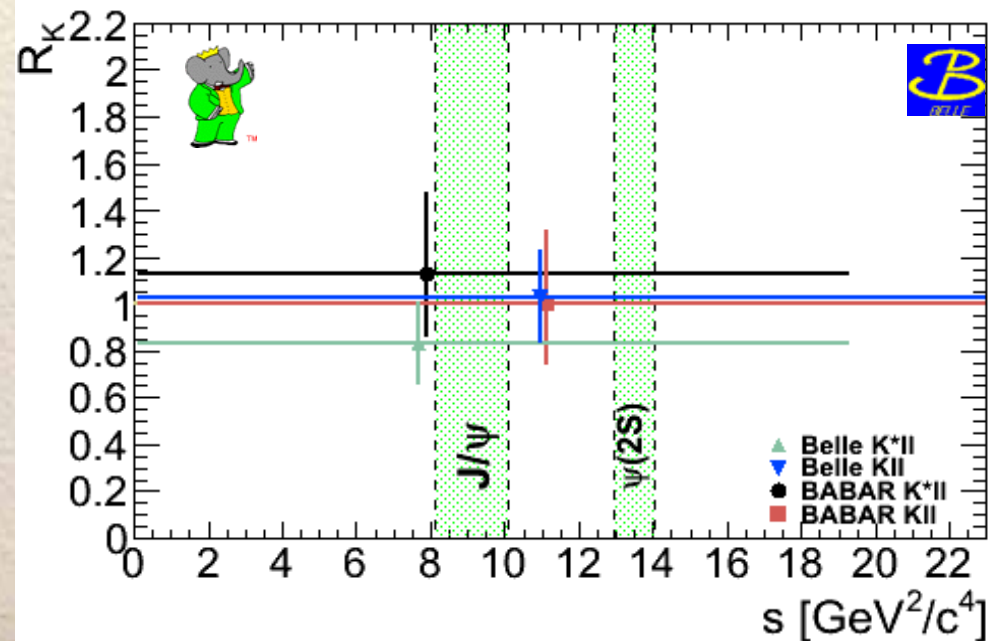
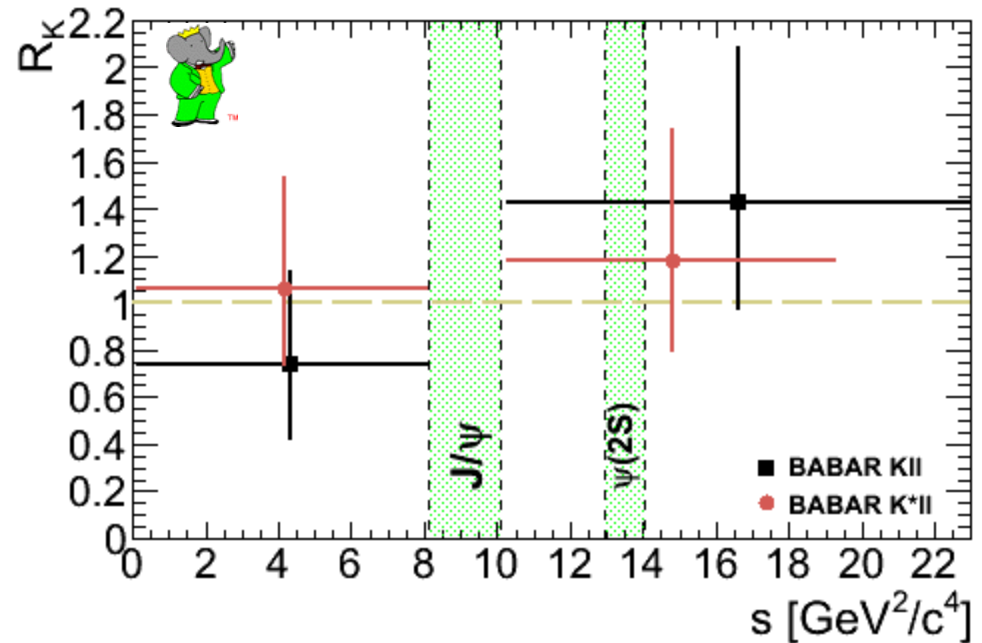
$$\mathcal{R}_{K^*}(B \rightarrow K^* \ell^+ \ell^-) = 1.13^{+0.34}_{-0.26} \pm 0.10$$

All $\mathcal{R}_{K^{(*)}}$ results are consistent with unity \rightarrow agree with SM

Ali et al., PRD 61, 074024 (2000)

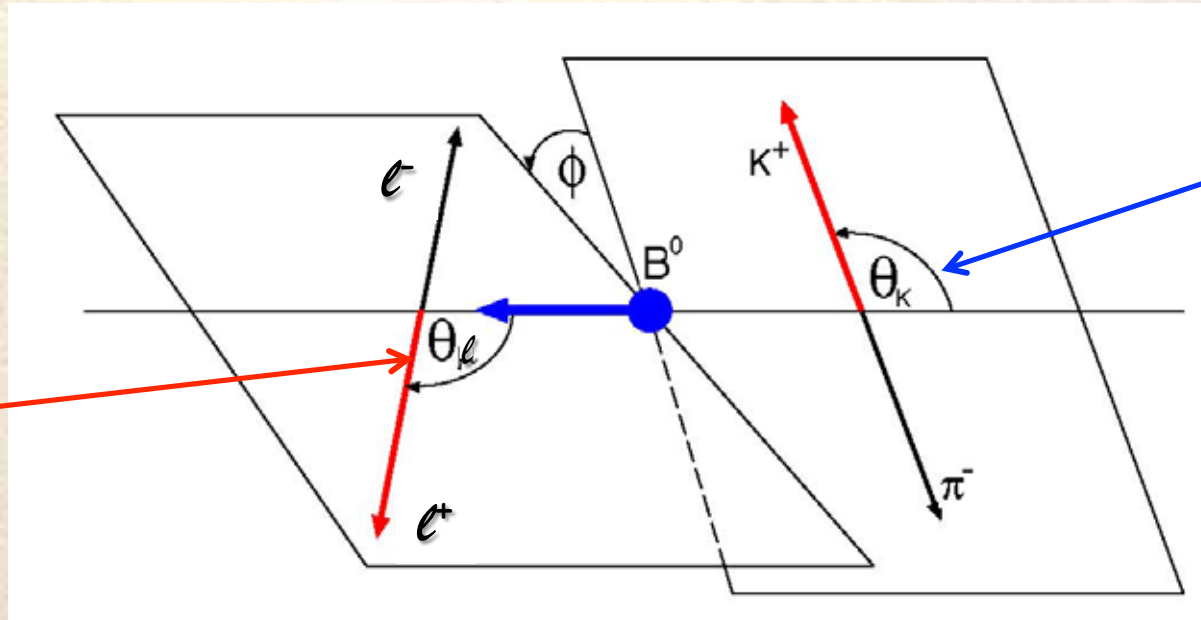
BABAR: PRD86,032012 (2012)

Belle: PRL 103, 171801 (2009)



$B \rightarrow K^* \ell^+ \ell^-$: Angular Observables

- The $B \rightarrow K^* \ell^+ \ell^-$ angular distribution depends on 3 angles θ_K , θ_ℓ , & ϕ



θ_K : angle of K^+ and B in K^* rest frame

θ_ℓ : angle of ℓ^+ and B in $\ell^+ \ell^-$ rest frame

- The 1-d θ_K and θ_ℓ projections depend on the K^* longitudinal polarization fraction \mathcal{F}_L and lepton forward-backward asymmetry \mathcal{A}_{FB}

\mathcal{F}_L :

$$W(\cos \theta_K) = \frac{3}{2} \mathcal{F}_L \cos^2 \theta_K + \frac{3}{4} (1 - \mathcal{F}_L) \sin^2 \theta_K$$

Ali et al., PRD 61, 074024 (2000)
Bobeth et al., JHEP 0712, 040 (2007)

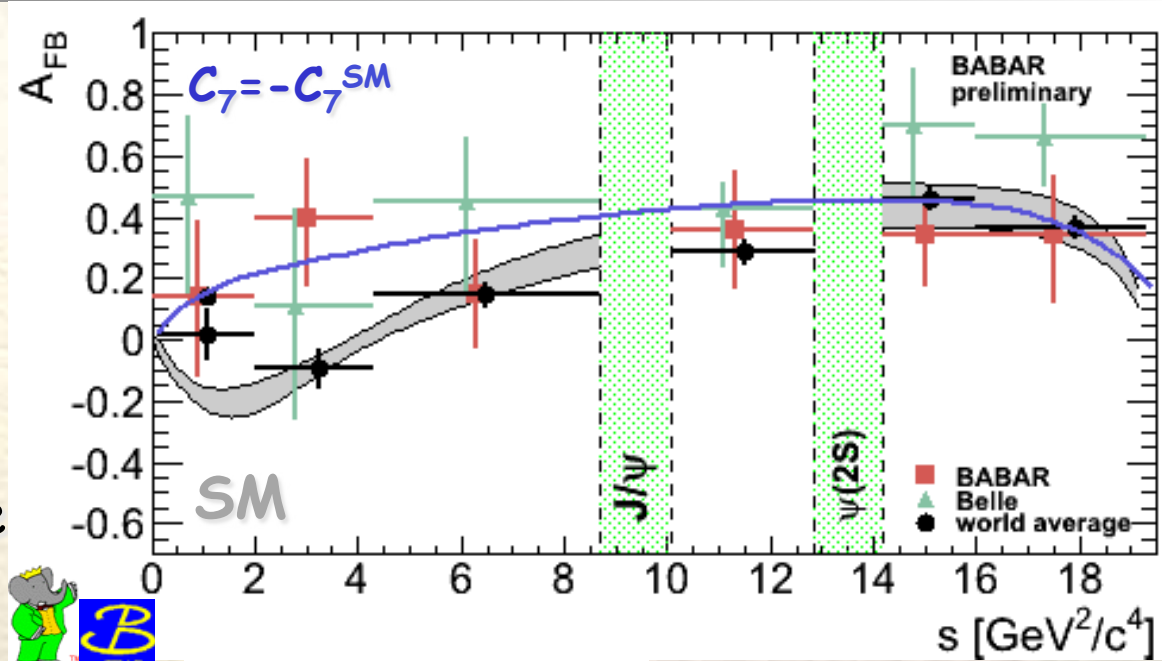
\mathcal{A}_{FB}

$$W(\cos \theta_\ell) = \frac{3}{4} \mathcal{F}_L \sin^2 \theta_\ell + \frac{3}{8} (1 - \mathcal{F}_L) (1 + \cos^2 \theta_\ell) + \mathcal{A}_{FB} \cos \theta_\ell$$

- With limited statistics, we fit the 1-d projections to extract \mathcal{F}_L and \mathcal{A}_{FB}

$B \rightarrow K^* \ell^+ \ell^-$: Forward-Backward Asymmetry A_{FB}

- A_{FB} is measured by
 - BABAR & Belle in $B \rightarrow K^* \ell^+ \ell^-$
 - CDF in $K^* \mu^+ \mu^-$
 - LHCb, CMS and ATLAS in $K^{*0} \mu^+ \mu^-$
- BABAR A_{FB} measurement ($B \rightarrow K^* \ell^+ \ell^-$) is the most precise except for LHCb ($K^{*0} \mu^+ \mu^-$)



ATLAS	Conf-2013-38	CMS	CMS PAS BPH-11-009 (2013)
Belle	PRL103, 171801 (2009)	LHCb	hep-ex/1304.6325 (2013)
CDF	CDF-note 10894 (2012)		JHEP1212,125 (2012)

- All measurements are consistent
- Do naive world average of all A_{FB} results
 → WA (dominated by LHCb) agrees well with the SM

Ali et al. PRD 61, 074024 (2000)
 Buchalla et al. PRD 63, 014015 (2000)
 Ali et al. PRD 66, 034002 (2002)
 Krüger et al. PRD 61, 114028 (2002)
 Krüger & Matias PRD71, 094009 (2005)
 C. Bobeth et al. JHEP 1007, 098 (2010)
 C. Bobeth et al. PRD87,034016 (2012)

- In low mass region ($1 < s < 6 \text{ GeV}^2/c^4$) measure



$$A_{FB}(B \rightarrow K^* \ell^+ \ell^-) = 0.26^{+0.27}_{-0.30} \pm 0.07$$

$1 < s < 6 \text{ GeV}^2/c^4$

- world average: $A_{FB}^{WA}(K^* \ell \ell) = -0.074^{+0.047}_{-0.048}$

SM: $A_{FB}^{SM} = -0.0494^{+0.0281}_{-0.0252} (K^{*0} \ell^+ \ell^-)$



$B \rightarrow K^* \ell^+ \ell^-$: K^* Longitudinal Polarization \mathcal{F}_L

- \mathcal{F}_L is measured by
 - BABAR & Belle in $B \rightarrow K^* \ell^+ \ell^-$
 - CDF in $K^* \mu^+ \mu^-$
 - LHCb, CMS and ATLAS in $K^{*0} \mu^+ \mu^-$

- BABAR \mathcal{F}_L measurement ($B \rightarrow K^* \ell^+ \ell^-$) is the most precise except for LHCb ($K^{*0} \mu^+ \mu^-$)

- All measurements are consistent

- Do naive average of all \mathcal{F}_L results (dominated by LHCb)

→ are consistent with the SM & $C_7 = -C_7^{SM}$ model

- In low mass region ($1 < s < 6 \text{ GeV}^2/c^4$) measure

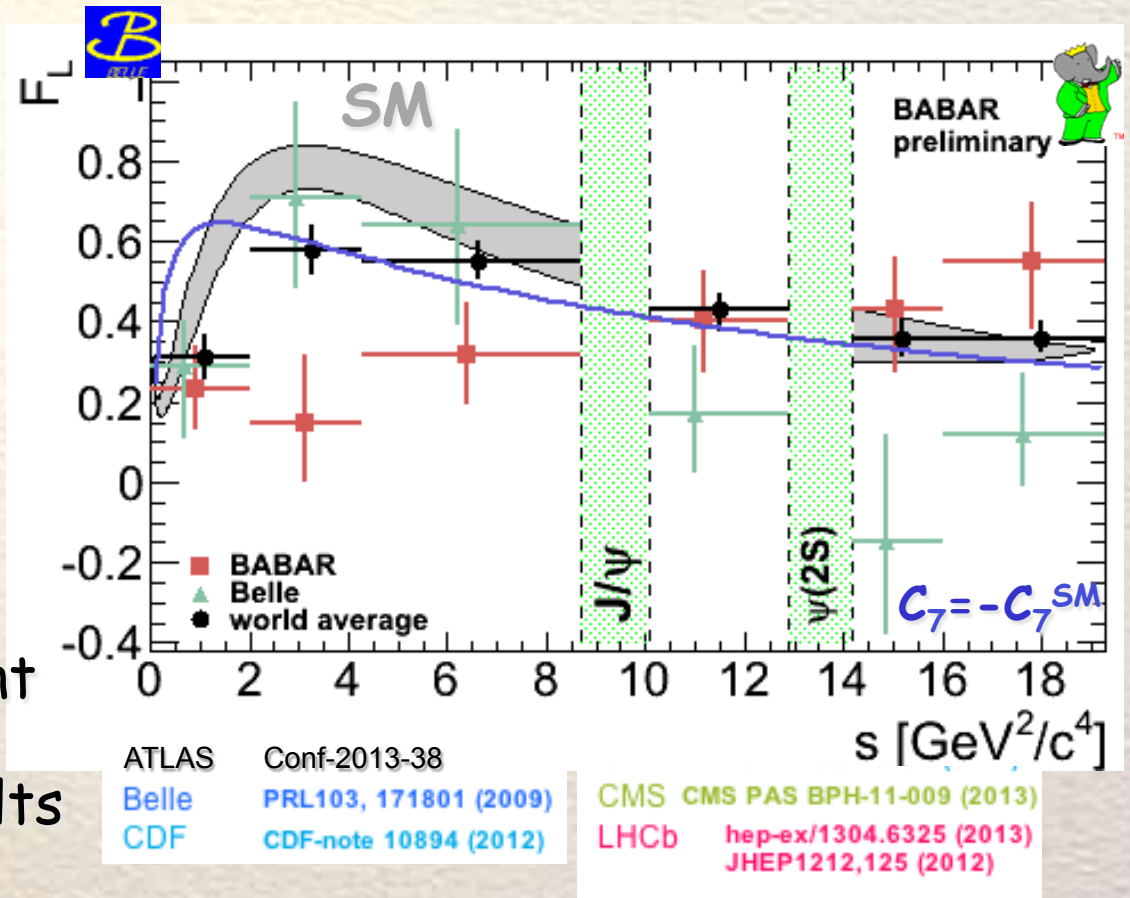


$$\mathcal{F}_L = 0.25^{+0.09}_{-0.08} \pm 0.03$$

- world average: $\mathcal{F}_L = 0.523^{+0.047}_{-0.044}$

$1 < s < 6 \text{ GeV}^2/c^4$

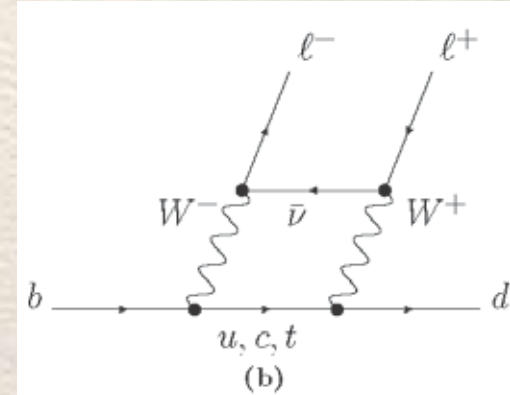
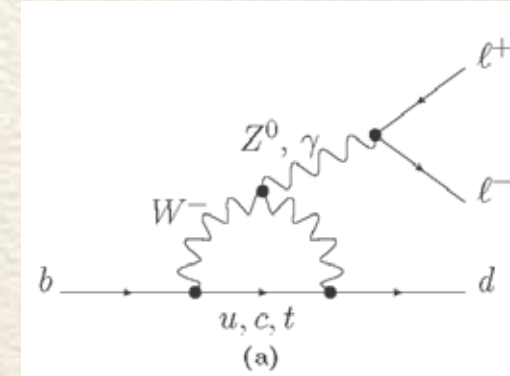
$$\text{SM: } \mathcal{F}_L^{SM} = 0.735^{+0.06}_{-0.07} \left(K^{*0} \ell^+ \ell^- \right)$$



C. Bobeth et al. arXiv:1006.5013
 Krüger & Matias PRD71, 094009 (2005)
 C. Bobeth et al. PRD87,034016 (2012)

Search for $B \rightarrow \pi/\eta \ell^+ \ell^-$ Decays

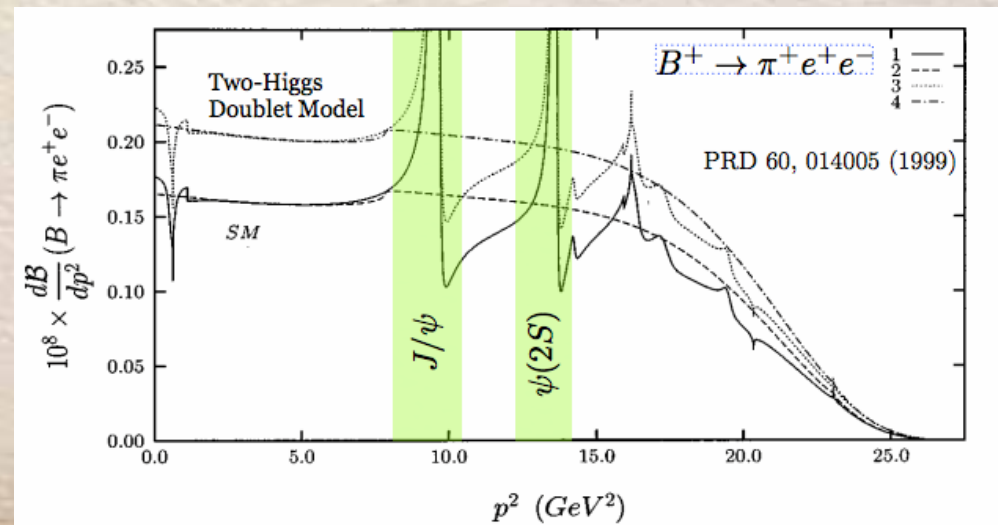
- In the SM, $B \rightarrow X_d \ell^+ \ell^-$ modes are also mediated in lowest order by the photon penguin, Z-penguin and WW box diagrams
- The decays are suppressed by $|V_{td}/V_{ts}|^2 \sim 0.04$ with respect to the related $b \rightarrow s \ell^+ \ell^-$ modes
- In extensions of the SM, rates may increase significantly
- BABAR has updated the search for $B \rightarrow \pi \ell^+ \ell^-$ modes and performed the first search for $B \rightarrow \eta \ell^+ \ell^-$ modes using 471×10^6 BB events



- SM predictions:

$$\mathcal{B}(B^\pm \rightarrow \pi^\pm \ell^+ \ell^-) = (1.96 - 3.30) \times 10^{-8}$$

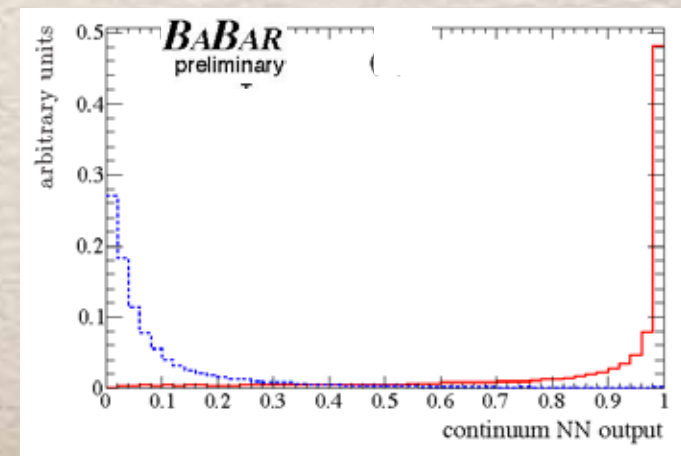
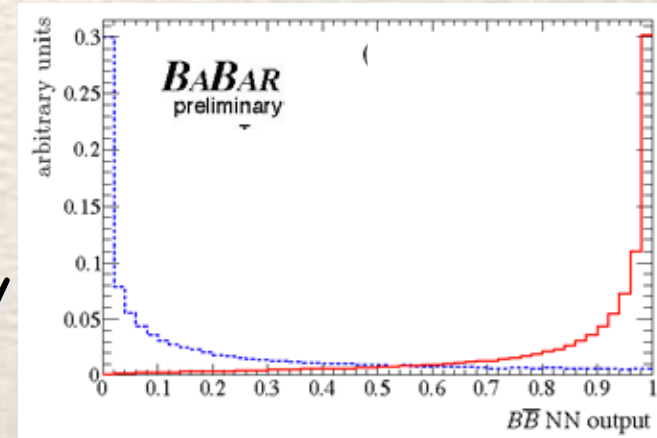
$$\mathcal{B}(B^0 \rightarrow \eta \ell^+ \ell^-) = (2.5 - 3.7) \times 10^{-8}$$



$B \rightarrow \pi/\eta \ell^+ \ell^-$: Analysis Methodology



- BABAR fully reconstructs 8 $B \rightarrow \pi/\eta \ell^+ \ell^-$ final states ($471 \times 10^6 B\bar{B}$)
 - Select $\pi^\pm, \pi^0, \eta \rightarrow \gamma\gamma$, or $\eta \rightarrow \pi^+ \pi^- \pi^0$ recoiling against $e^+ e^-$ or $\mu^+ \mu^-$
 - Select $p_\ell > 0.3 \text{ GeV}/c$, recover e^\pm bremsstrahlung losses, remove $\gamma \rightarrow ee$
 - Require good particle ID for e, μ, π ; for γ require $E_\gamma > 50 \text{ MeV}$
 - Select π^0 : $115 < m_{\gamma\gamma} < 150 \text{ MeV}$; η : $500 < m_{\gamma\gamma} < 575 \text{ MeV}$, $535 < m_{3\pi} < 565 \text{ MeV}$
 - Require $A_\gamma^\eta = (E_{1,\gamma} - E_{2,\gamma}) / (E_{1,\gamma} + E_{2,\gamma}) < 0.8$
- Veto J/ψ and $\psi(2S)$ mass regions
- Suppress combinatorial $B\bar{B}$ & $q\bar{q}$ backgrounds by NNs, 2 each for $e^+ e^-$ & $\mu^+ \mu^-$ modes using 12 and 14 input distributions
- Simultaneous fit to m_{ES} and ΔE distributions
- Use pseudo-experiments for validations





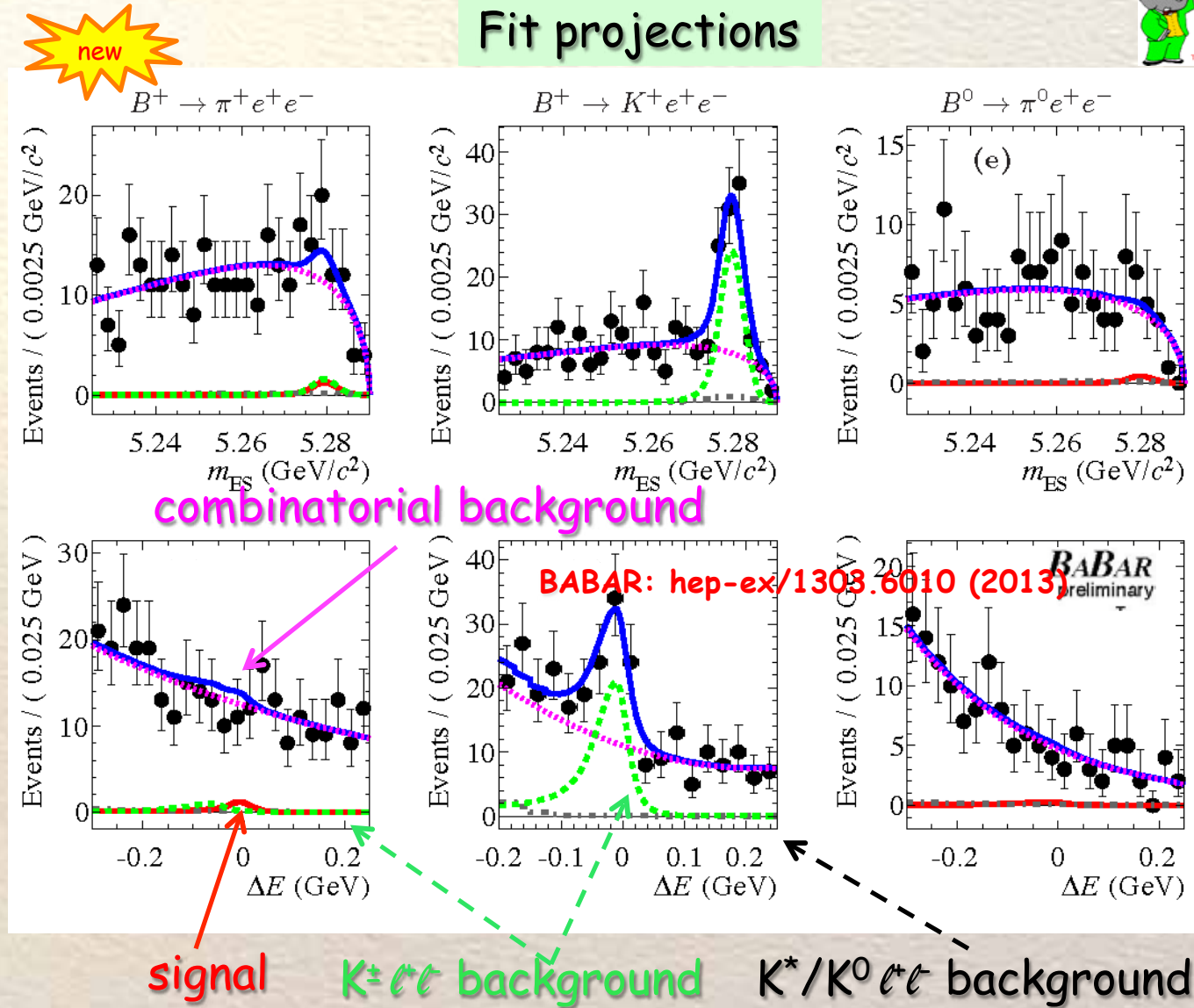
Search for $B \rightarrow \pi \ell^+ \ell^-$ Modes



- Perform simultaneous unbinned maximum likelihood fit to the m_{ES} & ΔE distributions of $B \rightarrow \pi^\pm \ell^+ \ell^-$ & $B \rightarrow \pi^0 \ell^+ \ell^-$, separately for $e^+ e^-$ & $\mu^+ \mu^-$ modes

- Add $B \rightarrow K^\pm \ell^+ \ell^-$ mode in the fit to extract peaking background

- Use vetoed J/ψ and $\psi(2S)$ samples to validate fit and evaluate $B \rightarrow K^\pm \ell^+ \ell^-$



hep-ex/1303.6010 (2013)

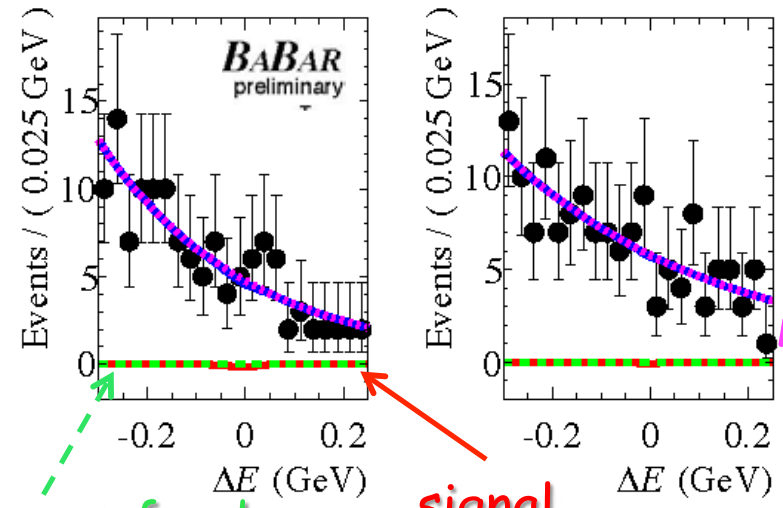
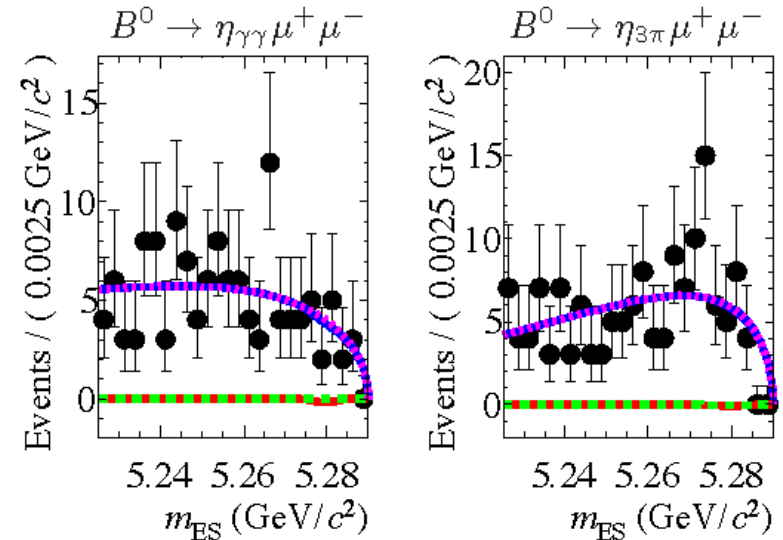


Search for $B \rightarrow \eta \ell^+ \ell^-$ Modes

- Perform simultaneous unbinned maximum likelihood fit to the m_{ES} & ΔE distributions of $B \rightarrow \eta \ell^+ \ell^-$ separately for e^+e^- & $\mu^+\mu^-$ modes
- Use vetoed J/ψ and $\psi(2S)$ samples to validate fit
- In addition, perform fits for
 - Isospin averaged - modes $B \rightarrow \pi e^+e^-$ and $B \rightarrow \pi \mu^+\mu^-$
 - Lepton-flavor averaged modes $B \rightarrow \pi^\pm \ell^+ \ell^-$, $B \rightarrow \pi^0 \ell^+ \ell^-$ and $B \rightarrow \eta \ell^+ \ell^-$
 - Isospins and lepton-flavor averaged modes $B \rightarrow \pi \ell^+ \ell^-$



Fit projections



self crossfeed

signal

combinatorial background

$B \rightarrow \pi/\eta \ell^+ \ell^-$: Branching Fraction Upper Limits

- See no signal in any of these modes new

- Set 90% CL branching fraction upper limits

- LHCb observed $B^{\pm} \rightarrow \pi^{\pm} \mu^+ \mu^-$

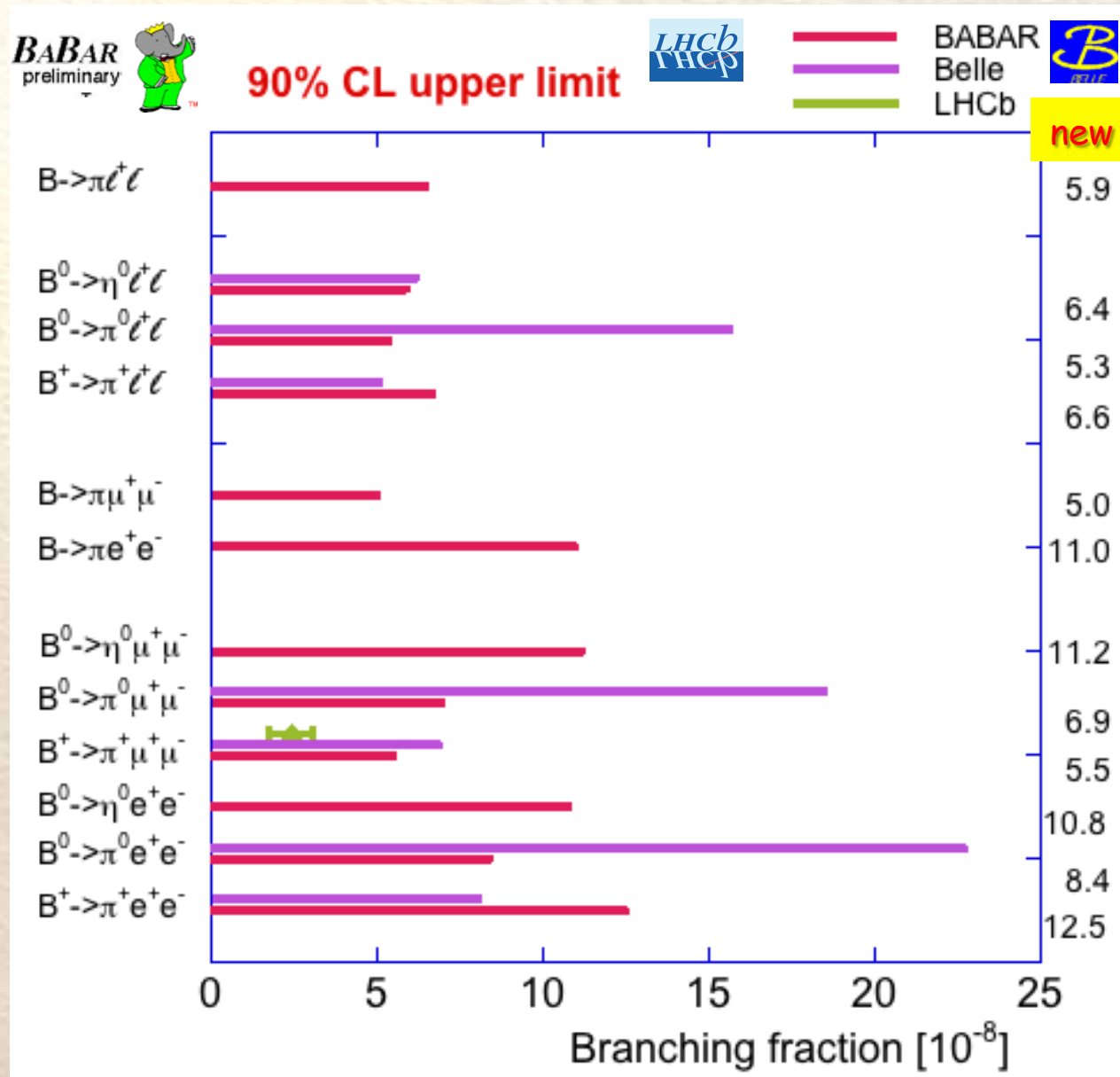
$$\mathcal{B}(B^+ \rightarrow \pi^+ \ell^+ \ell^-) = (2.4 \pm 0.6 \pm 0.1) \times 10^{-8}$$

- Best limit for $B^0 \rightarrow \pi^0 \ell^+ \ell^-$

$$\mathcal{B}(B^+ \rightarrow \pi^0 \ell^+ \ell^-) < 5.3 \times 10^{-8} \text{ (90\%CL)}$$

- First results for $B \rightarrow \eta \ell^+ \ell^-$

- Limits are within a factor 2-3 of the SM predictions





Conclusions

- New BABAR $B \rightarrow X_s \gamma$ results
 - Branching fractions are in good agreement with the SM prediction
 - New \mathcal{A}_{CP} is the most precise and consistent with the SM prediction
 - New measurements on photon energy moments
 - Set limit on charged Higgs boson $m_{H^\pm} > 327 \text{ GeV @ 95\% CL}$
- New BABAR $B \rightarrow \pi/\eta \ell^+ \ell^-$ results on branching fraction upper limits
- Present $B \rightarrow X_\gamma$ and $B \rightarrow X \ell^+ \ell^-$ results are in agreement with the SM
 - Largest deviations are $< 3\sigma$
 - Need higher precision to probe the SM
- Significant progress will come from LHCb and Belle II
- High statistics samples allow for studying new observables
 - probe new angular observables that help in revealing small discrepancies wrt the SM
- LHCb and Belle II will have the first shot at them

Backup Slides



B → X_sγ Exclusive

- Various b → sγ and b → dγ exclusive modes have been measured by BABAR, Belle and CLEO
- B(B → ργ) / B(B → K*γ) yield |V_{td}/V_{ts}|

$$\frac{B(B \rightarrow \rho\gamma)}{B(B \rightarrow K^*\gamma)} = S_\rho \left| \frac{V_{td}}{V_{ts}} \right|^2 \frac{(m_B^2 - m_\rho^2)^3}{(m_B^2 - m_{K^*}^2)^3} \xi^2 [1 + \Delta R(\rho / K^*)]$$

ξ = 0.85 ± 0.1 (ratio of form factors)

ΔR(ρ⁰γ) = 0.092 ± 0.073 (higher-order correct.)

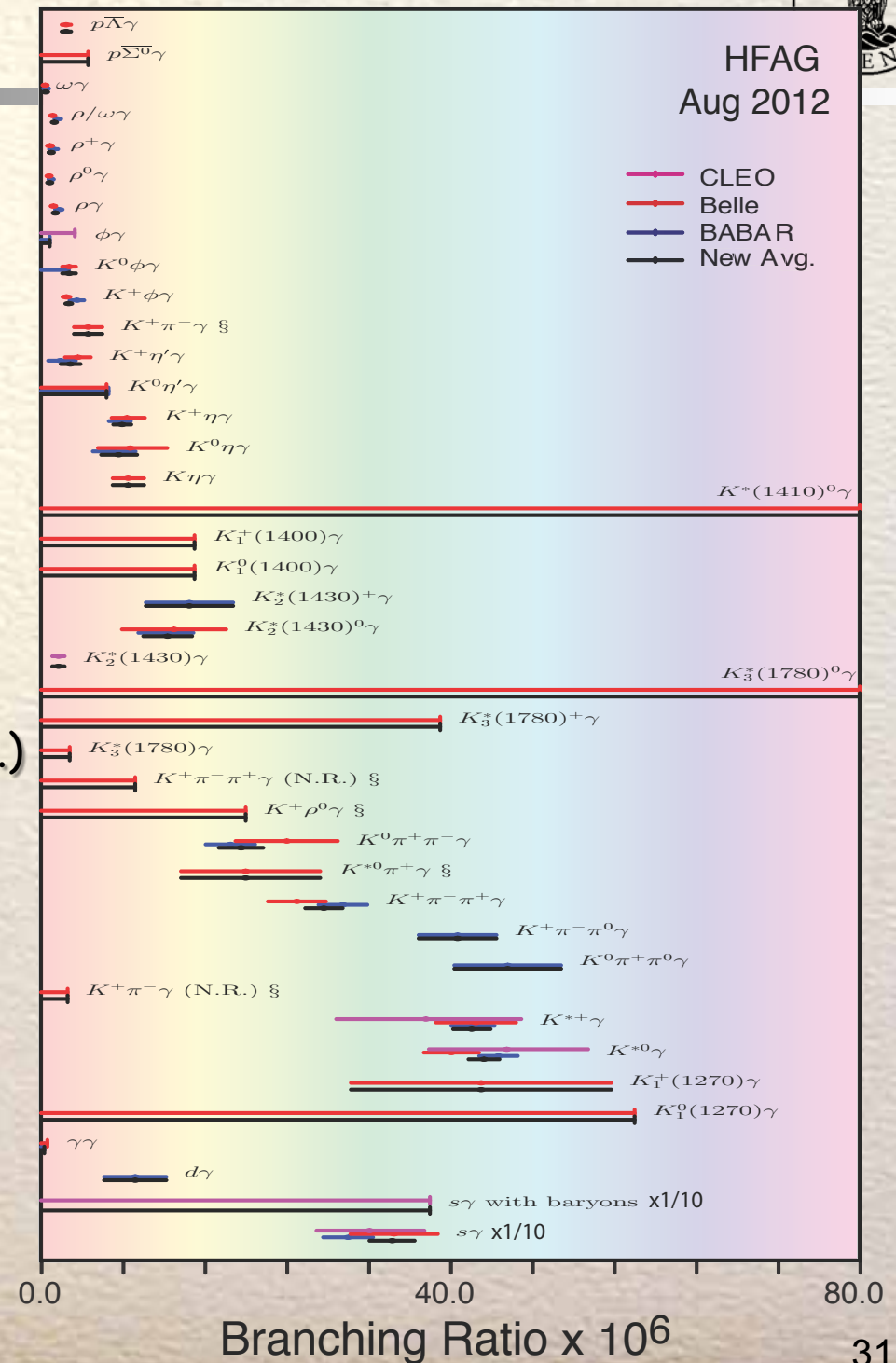
S is isospin factor

- BABAR/Belle average is

$$B(B \rightarrow (\rho, \omega)\gamma) = (1.3 \pm 0.23) \times 10^{-6}$$

- Yield constraint on |V_{td}/V_{ts}|

$$\left| \frac{V_{td}}{V_{ts}} \right|_{\rho/\omega\gamma} = 0.190^{+0.013}_{-0.014} (\text{exp}) \pm 0.015 (\text{th})$$



Angular Distributions for $B \rightarrow K^{(*)} e^+ e^-$

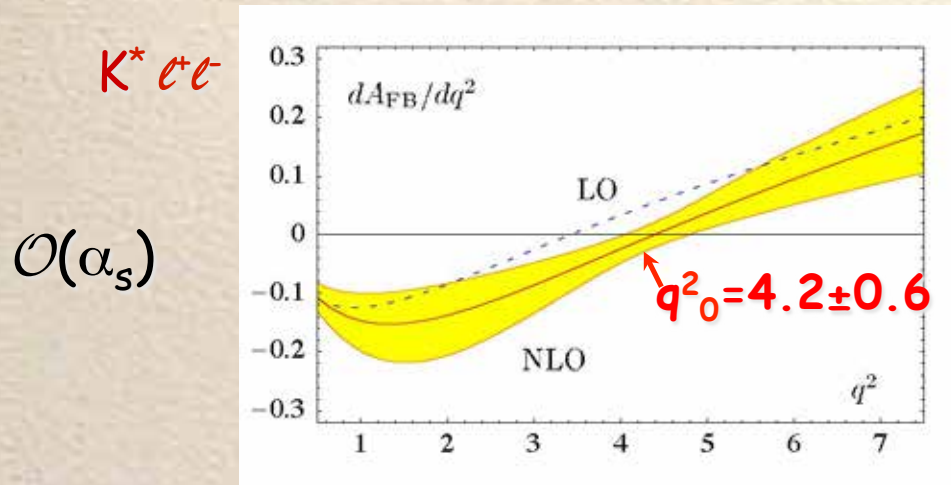


- A_{FB} results from interplay between $C_9(q^2)C_{10}$ and C_7C_{10}/q^2

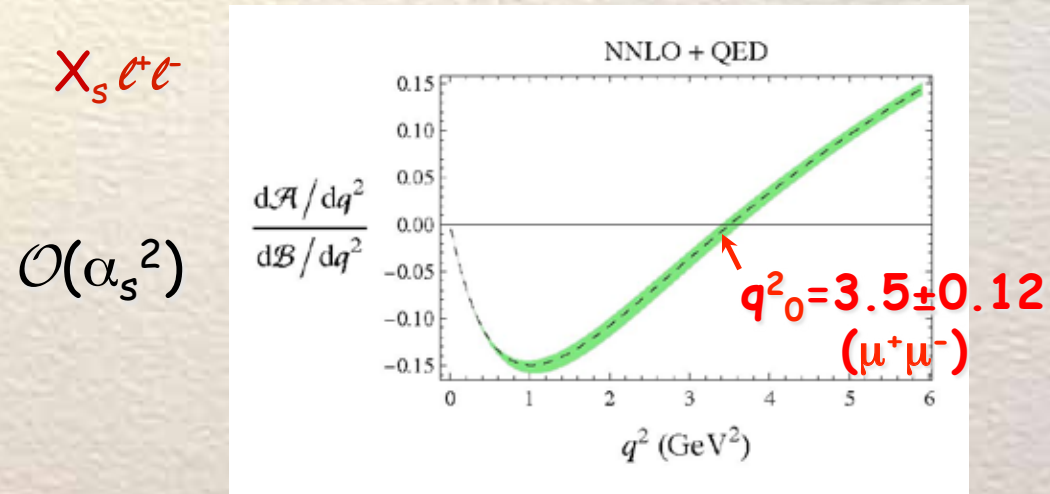
$$\frac{dA_{FB}}{dq^2} \propto - \left\{ \text{Re} \left[C_9^{\text{eff}}(q^2) C_{10} \right] VA_1 + \frac{m_b m_B}{q^2} \text{Re} \left[C_7^{\text{eff}} C_{10} \right] \left[VT_2 \left(1 - \frac{m_{K^*}}{m_B} \right) + AT_1 \left(1 + \frac{m_{K^*}}{m_B} \right) \right] \right\} K^* e^+ e^-$$

form factors

- Recent SM calculations focus on low q^2 -region



Feldmann & Matias JHEP 0301, 074 (2003)



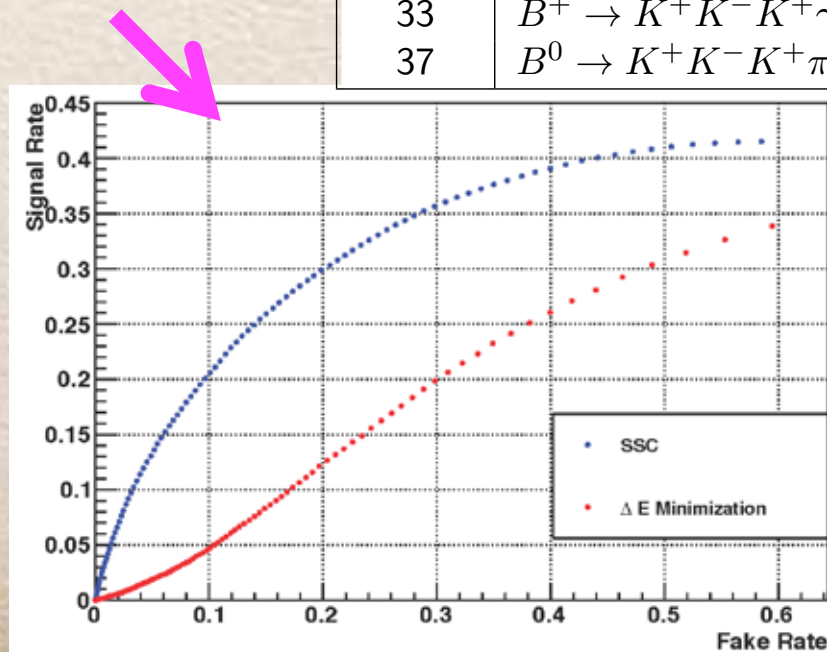
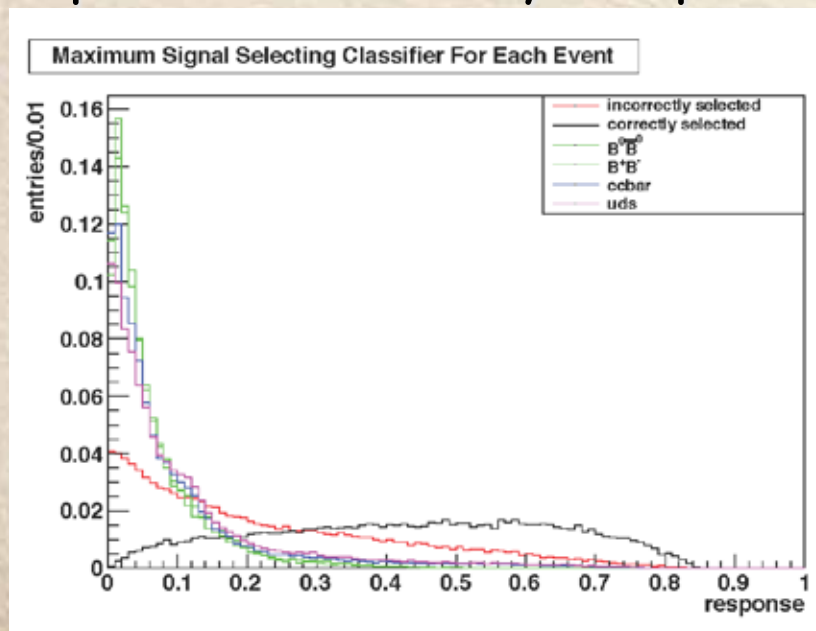
Huber, Hurth & Lunghi, Nucl.Phys B802, 40 (2008)

- In the SM, A_{FB} crosses zero around $q^2_0 = 3.5-4.5 \text{ GeV}^2$

Semi-Inclusive A_{CP} Event Selection

- Use 16 modes for the A_{CP} measurements
- Maximize signal extraction with **Signal Selecting Classifier** → bagged decision tree with 6 inputs
 - $m(X_s)$, $p_{\pi^0}^{\min}$, Thrust(B), $\Delta E/\sigma_E$, R_0 , R_5
 - Trained on 5% signal MC with $m_{ES} > 5.27$ GeV
 - good PID for π, K ; K_S^0 , π^0 , η selection
- Select candidate with maximum SSC
 - improved efficiency compared to ΔE selection

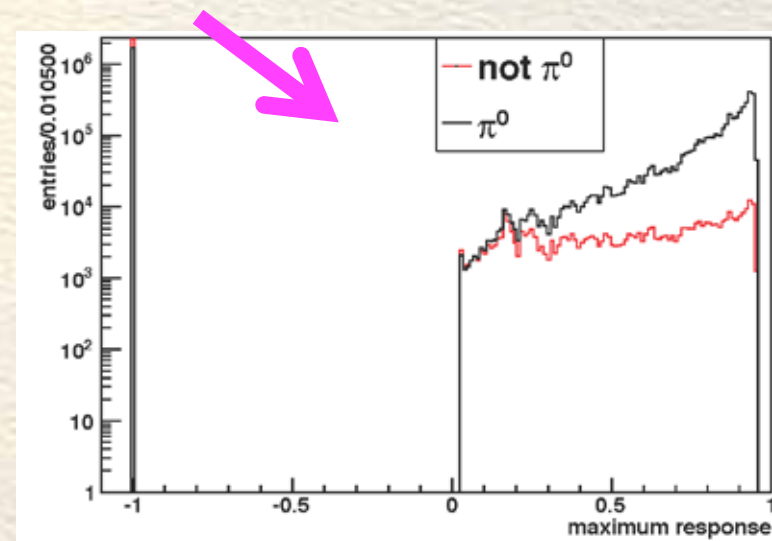
BiType	Final State
1	$B^+ \rightarrow K_S \pi^+ \gamma$
2	$B^+ \rightarrow K^+ \pi^0 \gamma$
3	$B^0 \rightarrow K^+ \pi^- \gamma$
5	$B^+ \rightarrow K^+ \pi^+ \pi^- \gamma$
6	$B^+ \rightarrow K_S \pi^+ \pi^0 \gamma$
7	$B^+ \rightarrow K^+ \pi^0 \pi^0 \gamma$
9	$B^0 \rightarrow K^+ \pi^- \pi^0 \gamma$
11	$B^+ \rightarrow K_S \pi^+ \pi^- \pi^+ \gamma$
12	$B^+ \rightarrow K^+ \pi^+ \pi^- \pi^0 \gamma$
13	$B^+ \rightarrow K_S \pi^+ \pi^0 \pi^0 \gamma$
14	$B^0 \rightarrow K^+ \pi^+ \pi^- \pi^- \gamma$
16	$B^0 \rightarrow K^+ \pi^- \pi^0 \pi^0 \gamma$
23	$B^+ \rightarrow K^+ \eta (\rightarrow \gamma \gamma) \gamma$
27	$B^0 \rightarrow K^+ \eta (\rightarrow \gamma \gamma) \pi^- \gamma$
33	$B^+ \rightarrow K^+ K^- K^+ \gamma$
37	$B^0 \rightarrow K^+ K^- K^+ \pi^- \gamma$



$B \rightarrow X_s \gamma$ Semi-Inclusive Analysis

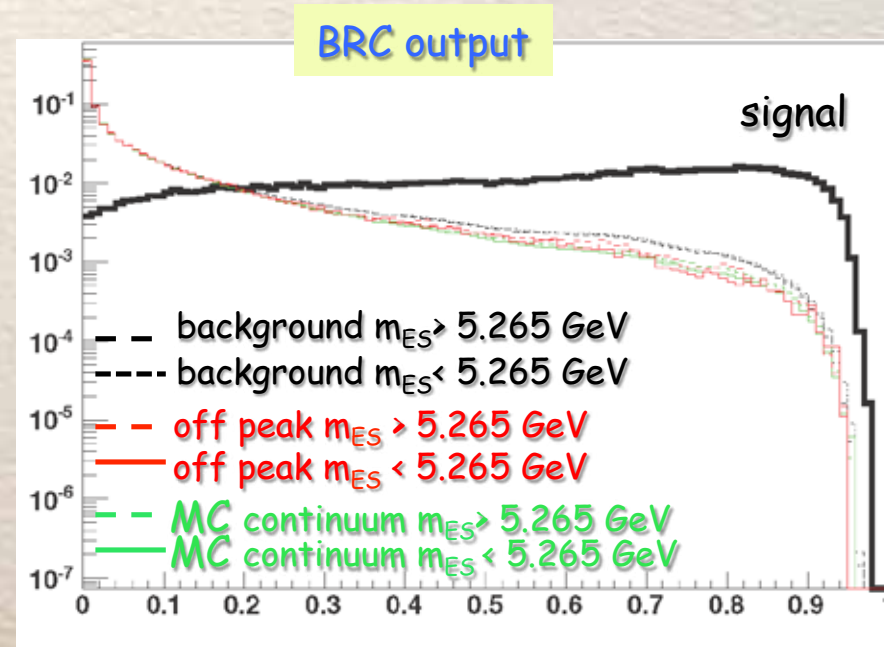


- Train separate bagged decision tree to separate true π^0 from fake π^0
- Use **B**ackground **R**ejection **C**lassifier to remove continuum background
- Train random forest with event-shape variables, *e.g.*
 - Cones of p-flow around B direction
 - L_0, L_1, L_2 of ROE along γ direction
 - L_2/L_0
 - $|\cos \theta_B^*|$, B flight direction (CM)
 - $|\cos \theta_T^*|$, thrust_B - thrust_{ROE} (CM)
 - $|\cos \theta_{\gamma T}^*|$, thrust _{γ} - thrust_{ROE} (CM)



- Use X_s mass-dependent optimization for $S/(S+B)^{1/2}$ & loose K, π IDs

X_s mass (GeV)	SSC	BRC
0.6-1.1	> 0.14	> 0.24
1.1-2.0	> 0.22	> 0.38
2.0-2.4	> 0.39	> 0.52
2.4-2.8	> 0.48	> 0.46





Angular Distributions for $B \rightarrow K^{(*)} \ell^+ \ell^-$



Results on \mathcal{F}_L and \mathcal{A}_{FB}

\mathcal{F}_L

s (GeV ² /c ⁴)	$B \rightarrow K^* \ell^+ \ell^-$	$B^0 \rightarrow K^{*0} \ell^+ \ell^-$	$B^+ \rightarrow K^{*+} \ell^+ \ell^-$
0.1 – 2.00	$0.23^{+0.10}_{-0.09} \pm 0.04$	$0.35^{+0.13}_{-0.12} \pm 0.04$	$-0.06^{+0.14}_{-0.12} \pm 0.06$
2.00 – 4.30	$0.15^{+0.17}_{-0.14} \pm 0.04$	$0.34^{+0.22}_{-0.22} \pm 0.08$	$-0.19^{+0.24}_{-0.24} \pm 0.04$
4.30 – 8.68	$0.32^{+0.12}_{-0.12} \pm 0.06$	$0.50^{+0.18}_{-0.15} \pm 0.05$	$0.14^{+0.15}_{-0.12} \pm 0.05$
10.09 – 12.86	$0.40^{+0.12}_{-0.12} \pm 0.06$	$0.48^{+0.13}_{-0.12} \pm 0.10$	$0.06^{+0.26}_{-0.25} \pm 0.05$
14.18 – 16.00	$0.43^{+0.10}_{-0.13} \pm 0.09$	$0.42^{+0.12}_{-0.16} \pm 0.11$	$0.58^{+0.34}_{-0.35} \pm 0.06$
> 16.00	$0.55^{+0.15}_{-0.17} \pm 0.03$	$0.47^{+0.18}_{-0.20} \pm 0.13$	$0.71^{+0.30}_{-0.32} \pm 0.03$
1.00 – 6.00	$0.25^{+0.09}_{-0.08} \pm 0.03$	$0.47^{+0.13}_{-0.13} \pm 0.04$	$0.03^{+0.11}_{-0.10} \pm 0.03$

\mathcal{A}_{FB}

s (GeV ² /c ⁴)	$B \rightarrow K^* \ell^+ \ell^-$	$B^0 \rightarrow K^{*0} \ell^+ \ell^-$	$B^+ \rightarrow K^{*+} \ell^+ \ell^-$
0.1 – 2.00	$0.14^{+0.15}_{-0.16} \pm 0.20$	$-0.07^{+0.20}_{-0.20} \pm 0.19$	$0.45^{+0.18}_{-0.24} \pm 0.15$
2.00 – 4.30	$0.40^{+0.18}_{-0.22} \pm 0.07$	$0.21^{+0.23}_{-0.34} \pm 0.11$	$0.73^{+0.27}_{-0.42} \pm 0.07$
4.30 – 8.68	$0.15^{+0.16}_{-0.16} \pm 0.08$	$0.20^{+0.19}_{-0.20} \pm 0.08$	$0.06^{+0.27}_{-0.26} \pm 0.07$
10.09 – 12.86	$0.36^{+0.16}_{-0.17} \pm 0.10$	$0.35^{+0.16}_{-0.16} \pm 0.11$	$0.17^{+0.33}_{-0.33} \pm 0.16$
14.18 – 16.00	$0.34^{+0.08}_{-0.15} \pm 0.07$	$0.31^{+0.11}_{-0.19} \pm 0.13$	$0.42^{+0.35}_{-0.23} \pm 0.09$
> 16.00	$0.34^{+0.19}_{-0.21} \pm 0.07$	$0.34^{+0.17}_{-0.26} \pm 0.08$	$0.17^{+0.38}_{-0.38} \pm 0.11$
1.00 – 6.00	$0.17^{+0.12}_{-0.14} \pm 0.07$	$0.02^{+0.16}_{-0.18} \pm 0.07$	$0.31^{+0.12}_{-0.14} \pm 0.07$