

Improved strong coupling measurements at TLEP?

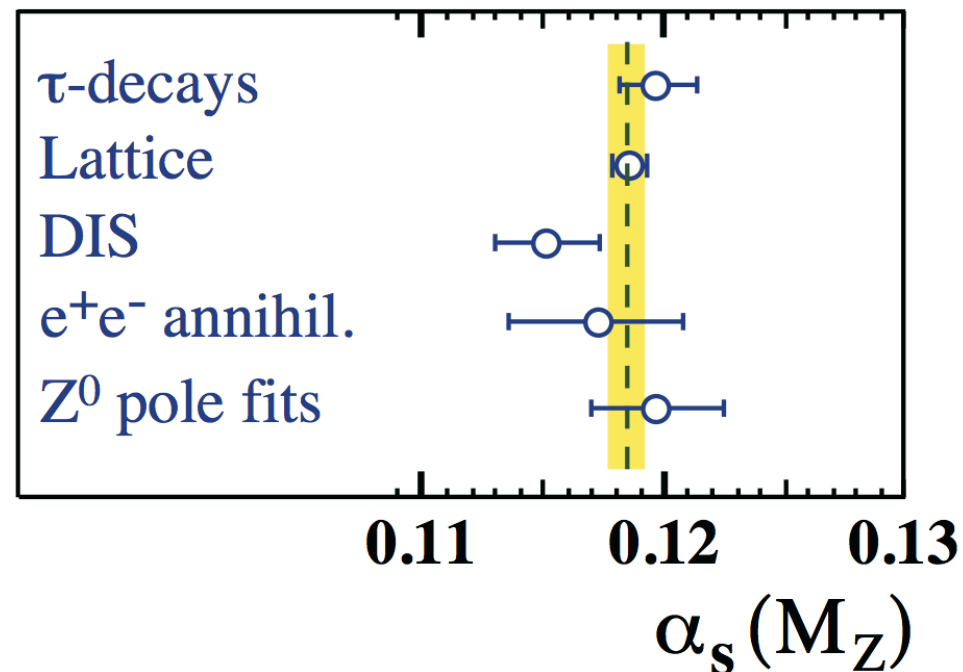
some personal thoughts, plus input from discussion
with Th. Gehrmann (UZH)

G. Dissertori
ETH Zürich

April 2013

Recent summary from the PDG

see Bethke, Dissertori, Salam: <http://pdg.lbl.gov/2012/reviews/rpp2012-rev-qcd.pdf>



current world average:

$$\alpha_s(M_Z) = 0.1184 \pm 0.0007 \quad (0.6 \% \text{ rel.})$$

- central value rather insensitive to choice of input
- uncert. dominated by Lattice results ($\sim 0.6\%$ rel.)

Question:

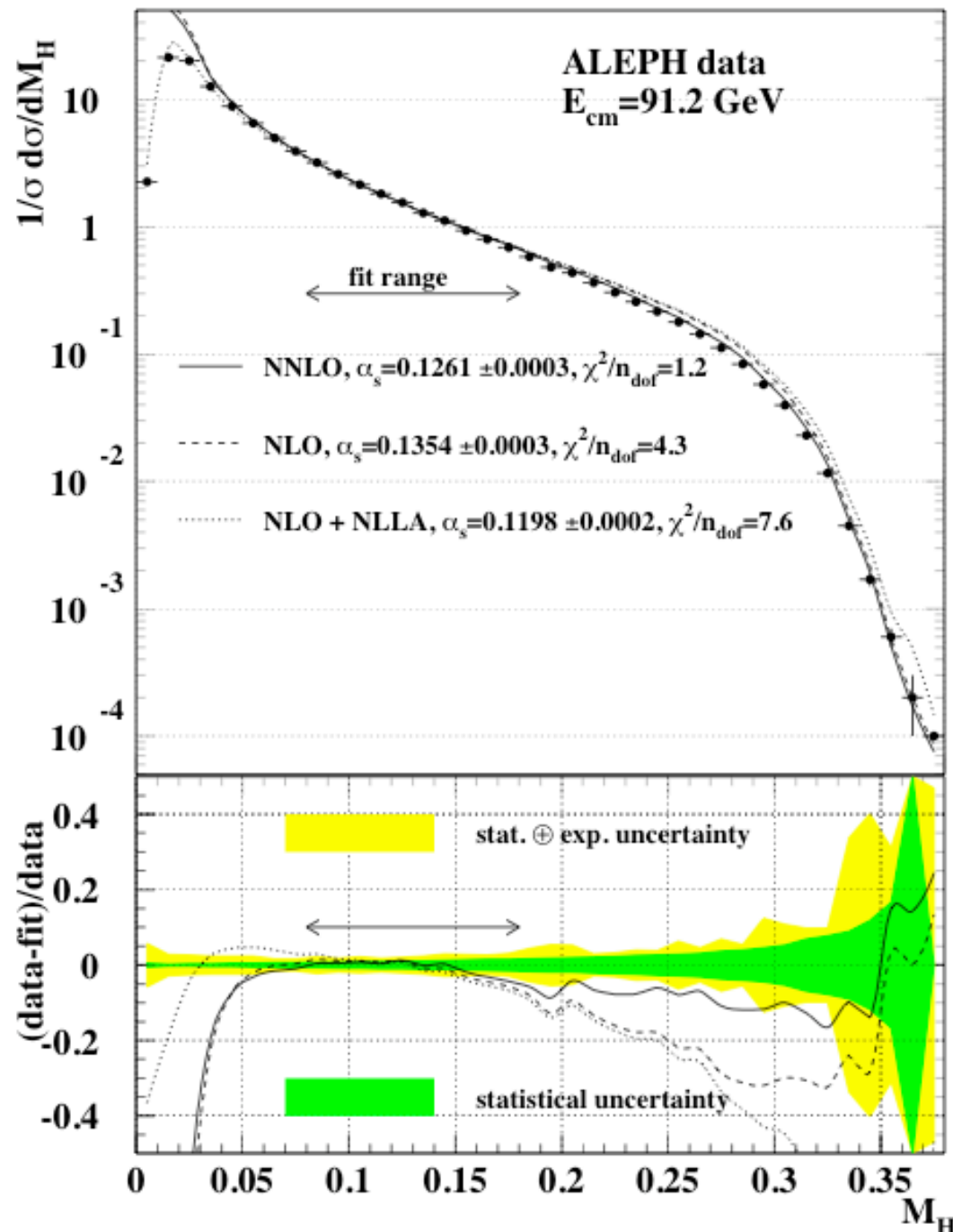
what is interesting (or realistic) goal to take as reference for this discussion?

Let's choose: **0.0001 (abs) or $\sim 0.1\%$ (rel)**

Also: let's focus at Z peak measurements, in order to have an independent $\alpha_s(M_Z)$ as input, eg., for m_{top} determination at $t\bar{t}$ threshold.

Jet rates, event shapes

- “Classical” method, theory known at NNLO+NNLL (NNLO obtained only a few years ago). Current status, typical values:



- Experimental Uncertainties
 - typically $\sim 1\%$ (improvements should be possible)
- Hadronization Uncertainties
 - difference between various models for hadronization,
 - typically around $0.7 - 1.5 \%$
 - going well below 1% seems unrealistic**
- Theoretical Uncertainties (pQCD)
 - renormalization scale variation, matching of (N)NLO with resummed calculation, quark mass effects
 - typically $3 - 5 \%$
 - going well below 1% seems unrealistic**
- my conclusion: this is not the way to go**

- Advantage of inclusive observables:
 - by now known to NNNLO !
 - non-perturbative effects strongly suppressed

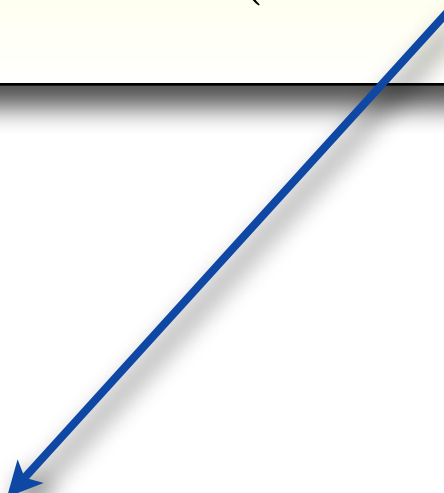
$$R_{\text{exp}} = \frac{\Gamma(Z \rightarrow \text{hadrons})}{\Gamma(Z \rightarrow \text{leptons})} = R_{EW} (1 + \delta_{QCD} + \delta_m + \delta_{np})$$

$$\frac{R_{\text{exp}}}{R_{EW}} = \mathcal{O}(1)$$

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$$c_1 = 1.045 \Rightarrow c_1 \frac{\alpha_s(M_Z)}{\pi} \sim 0.04 = \mathcal{O}(1/25)$$

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calculations can be
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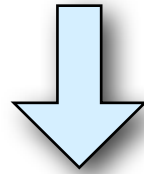
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$$\mathcal{O}\left(\frac{\Lambda^4}{M_Z^4}\right)$$

<< 0.0001, no problem

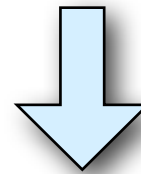
Example (using NNLO)

$$\frac{\Gamma(Z \rightarrow \text{hadrons})}{\Gamma(Z \rightarrow \text{leptons})} = 20.767 \pm 0.025 \quad (0.12 \% \text{ rel. })$$



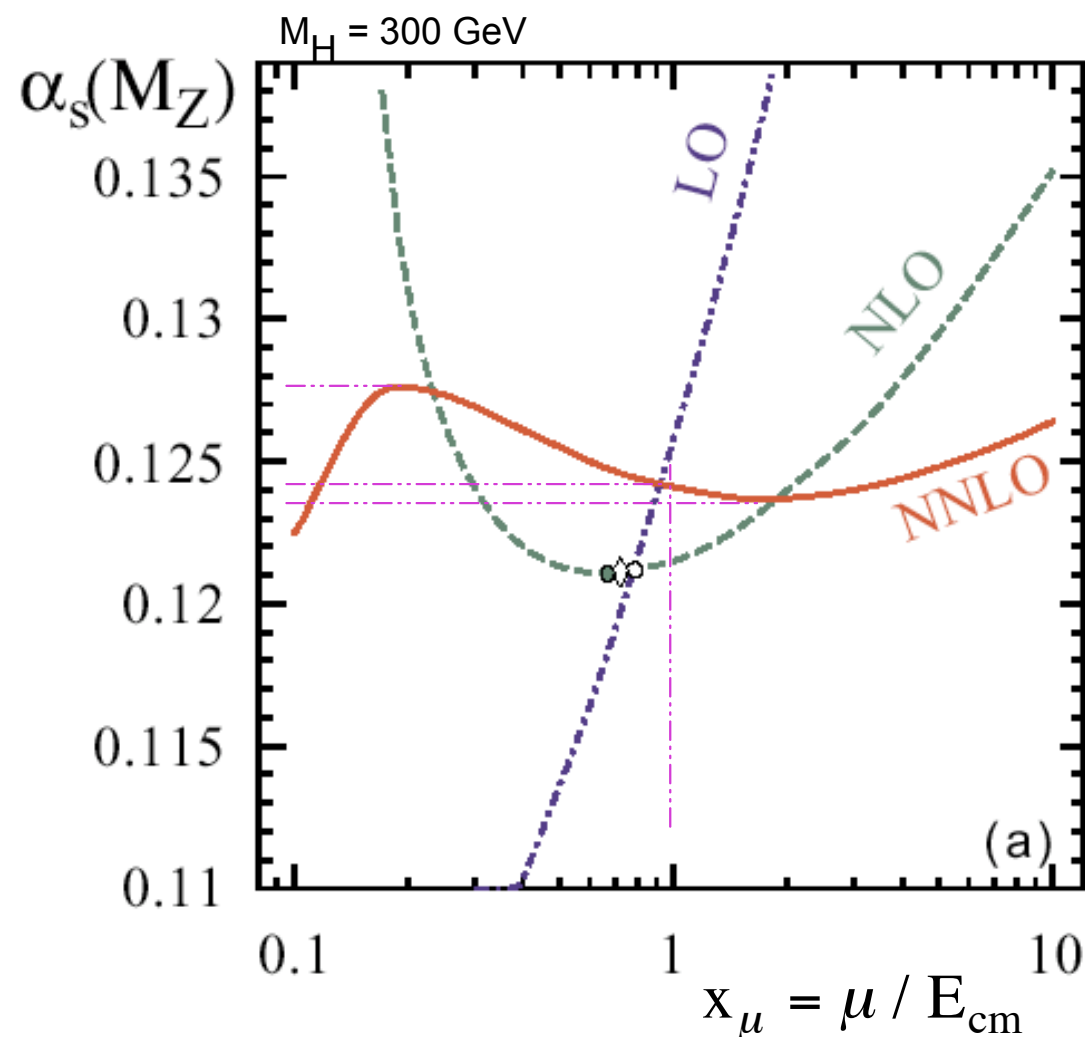
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see next slide

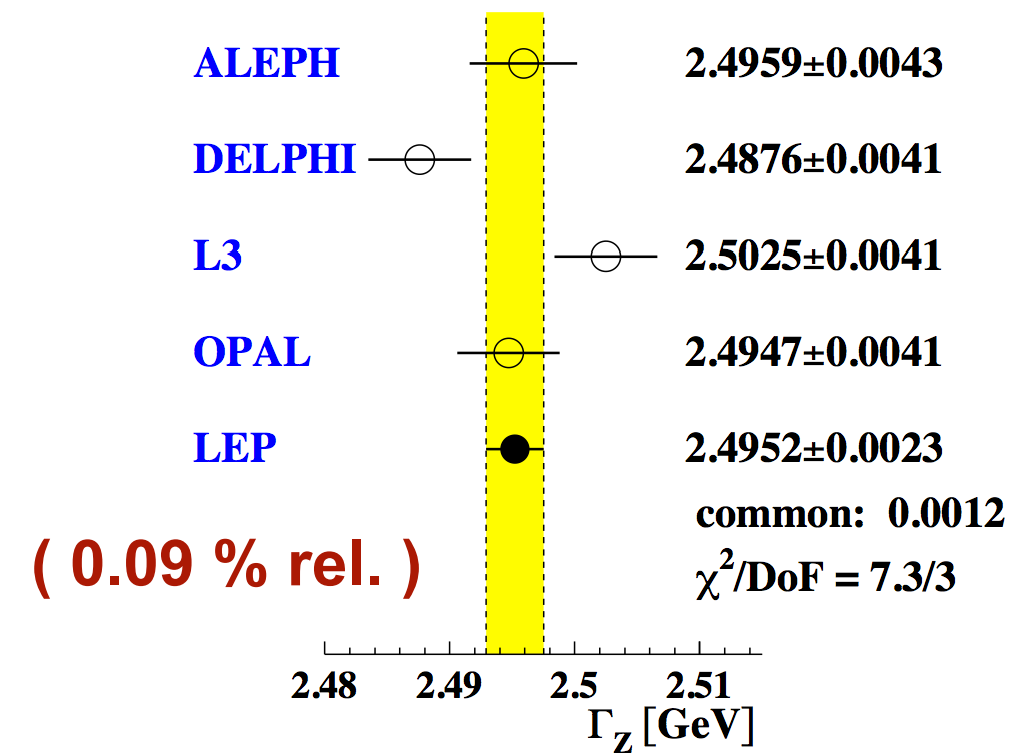
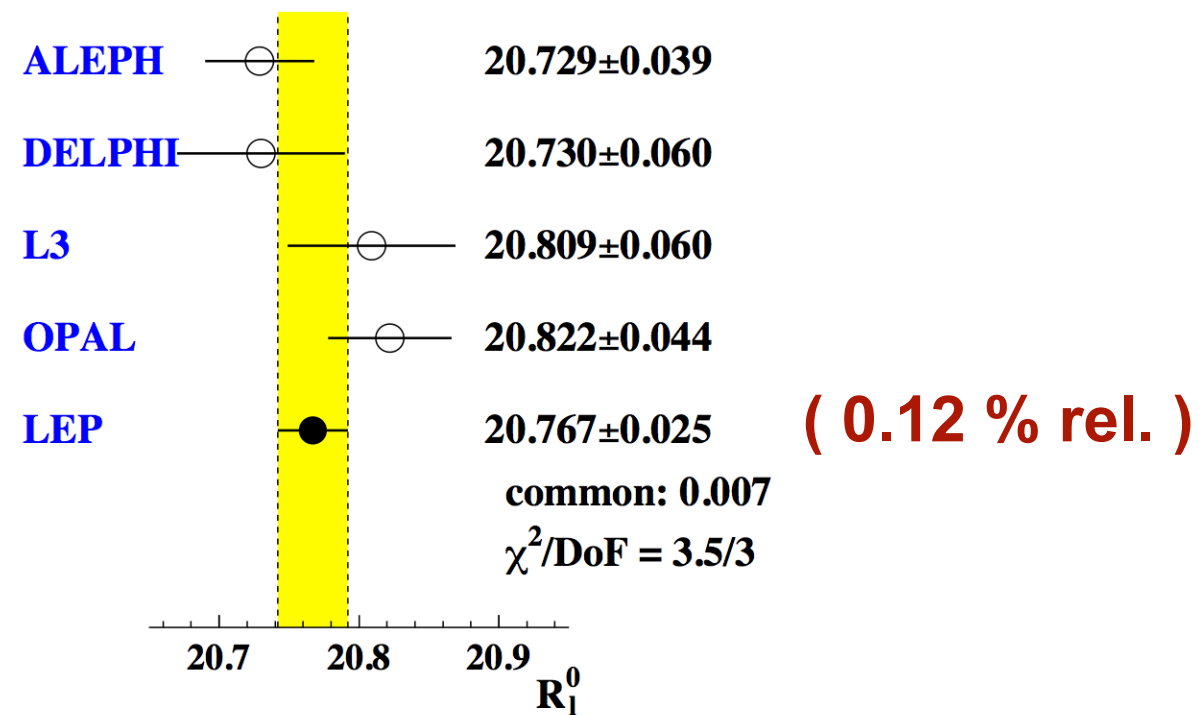
$$\alpha_s(M_Z) = 0.1226 \pm 0.0038 \text{ exp.}$$



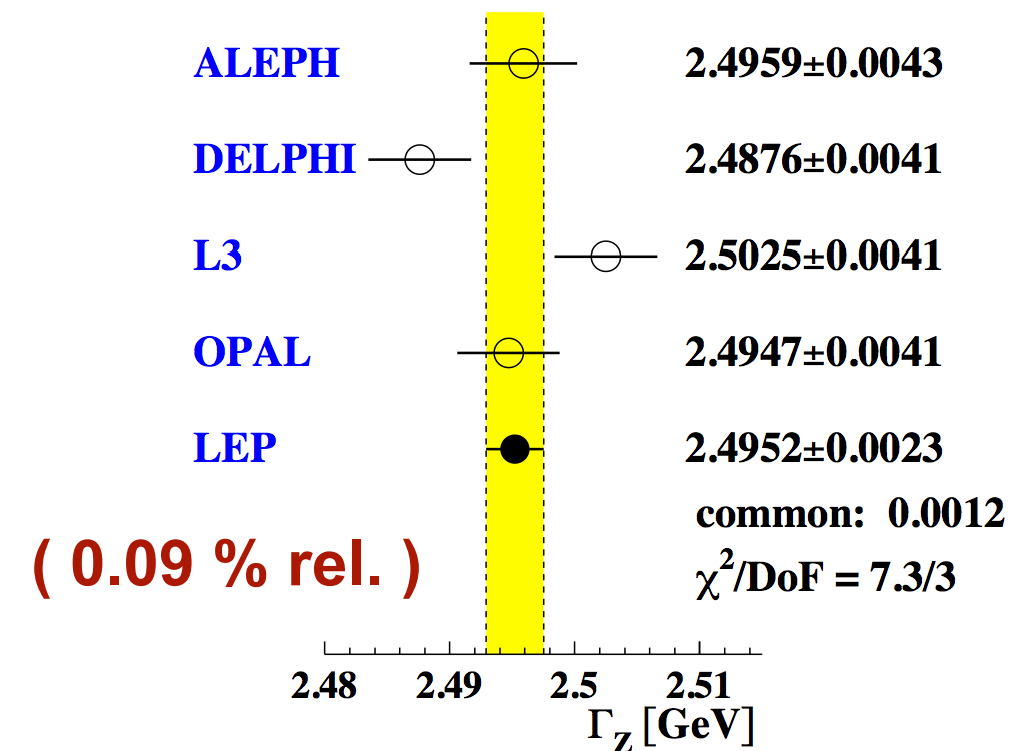
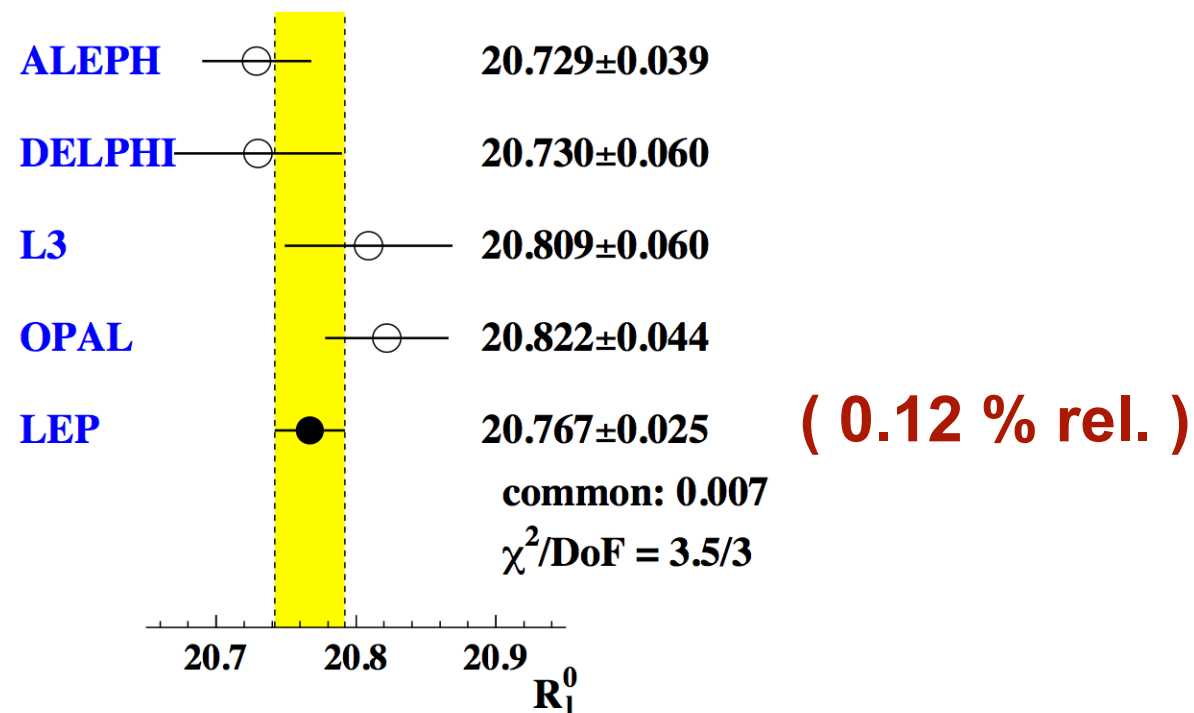
$$\begin{aligned} &+0.0028 \\ &-0.0005 \quad \mu = \frac{2}{0.25} M_Z \\ &+0.0033 \\ &-0.0 \quad M_H = \frac{900}{100} \text{ GeV} \\ &\pm 0.0002 \quad M_t = \pm 5 \text{ GeV} \\ &\pm 0.0002 \text{ renormal. schemes} \end{aligned}$$

$$= 0.1226 \quad \begin{matrix} +0.0058 \\ -0.0038 \end{matrix}$$

Latest results from LEP EW group



Latest results from LEP EW group



Source	δ	Γ_Z [MeV]	σ_{had}^0 [nb]	R_ℓ^0	R_b^0	ρ_ℓ	$\sin^2 \theta_{\text{eff}}^{\text{lept}}$	m_W [MeV]
$\Delta \alpha_{\text{had}}^{(5)}(m_Z^2)$	0.00035	0.3	0.001	0.002	0.00001	—	0.00012	6
$\alpha_S(m_Z^2)$	0.003	1.6	0.015	0.020	—	—	0.00001	2
m_Z	2.1 MeV	0.2	0.002	—	—	—	0.00002	3
m_t	4.3 GeV	1.0	0.003	0.002	0.00016	0.0004	0.00014	26
$\log_{10}(m_H/\text{GeV})$	0.2	1.3	0.001	0.004	0.00002	0.0003	0.00022	28
Theory		0.1	0.001	0.001	0.00002	—	0.00005	4
Experiment		2.3	0.037	0.025	0.00065	0.0010	0.00016	34

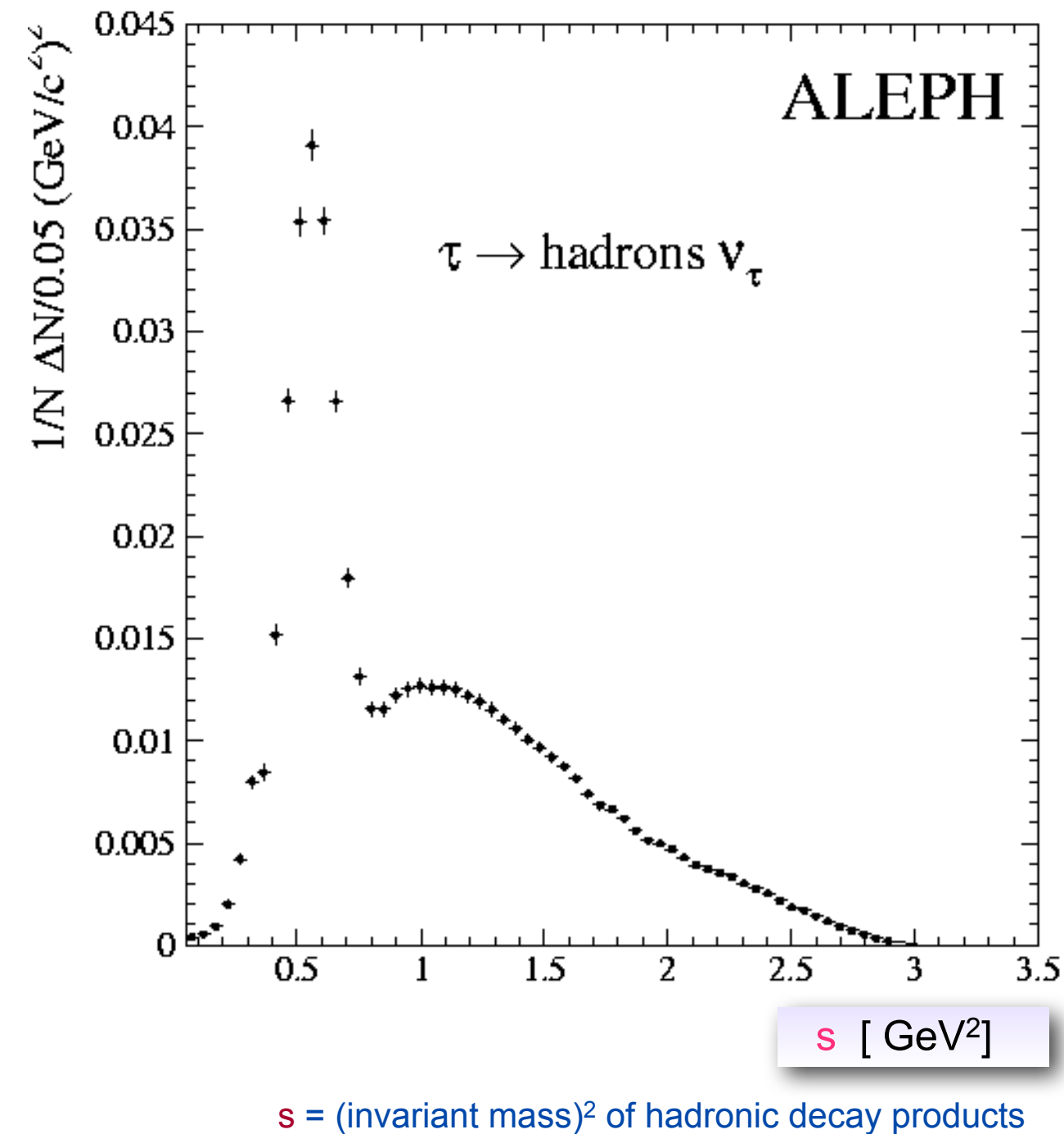
from slide 4:

$$\frac{\Delta \alpha_s}{\alpha_s} \approx 25 \cdot \frac{\Delta R_{\text{exp}}}{R_{\text{exp}}}$$

thus: for a rel. prec. of ~0.1% on α_s we need rel. exp. prec. ~25 times better !!

- uncertainty because of m_H gone, m_{top} dep. no problem
- pQCD scale uncertainty, from latest NNNLO calculation:
 - ~ 0.0002 (absolute uncertainty on α_s), see arXiv:0801.1821 and 1201.5804
- eg. taking Γ_Z : current uncertainty 2.3 MeV
 - ~ 1.2 MeV from beam energy (dominating contribution)
 - remainder: mostly statistical/experimental
 - **so the question is:**
can TLEP measure Γ_Z at a precision of ~ 0.1 MeV ?
or R with an absolute precision of ~ 0.001 ?
- **Note: all this is based on the assumption that there are no BSM effects which affect the Z pole observables at this level of precision.**

R_τ : τ hadronic BR

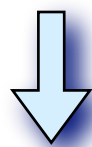


in principle even more inclusive than R at the Z pole, since integrating over hadronic inv. mass spectrum

$$R_\tau = \frac{1}{\pi} \int_0^{m_\tau^2} \frac{ds}{m_\tau^2} \left(1 - \frac{s}{m_\tau^2}\right)^2 \text{Im}\Pi_\tau(s)$$

interesting “advantage”:
“shrinking” of uncertainty just due to running of α_s :

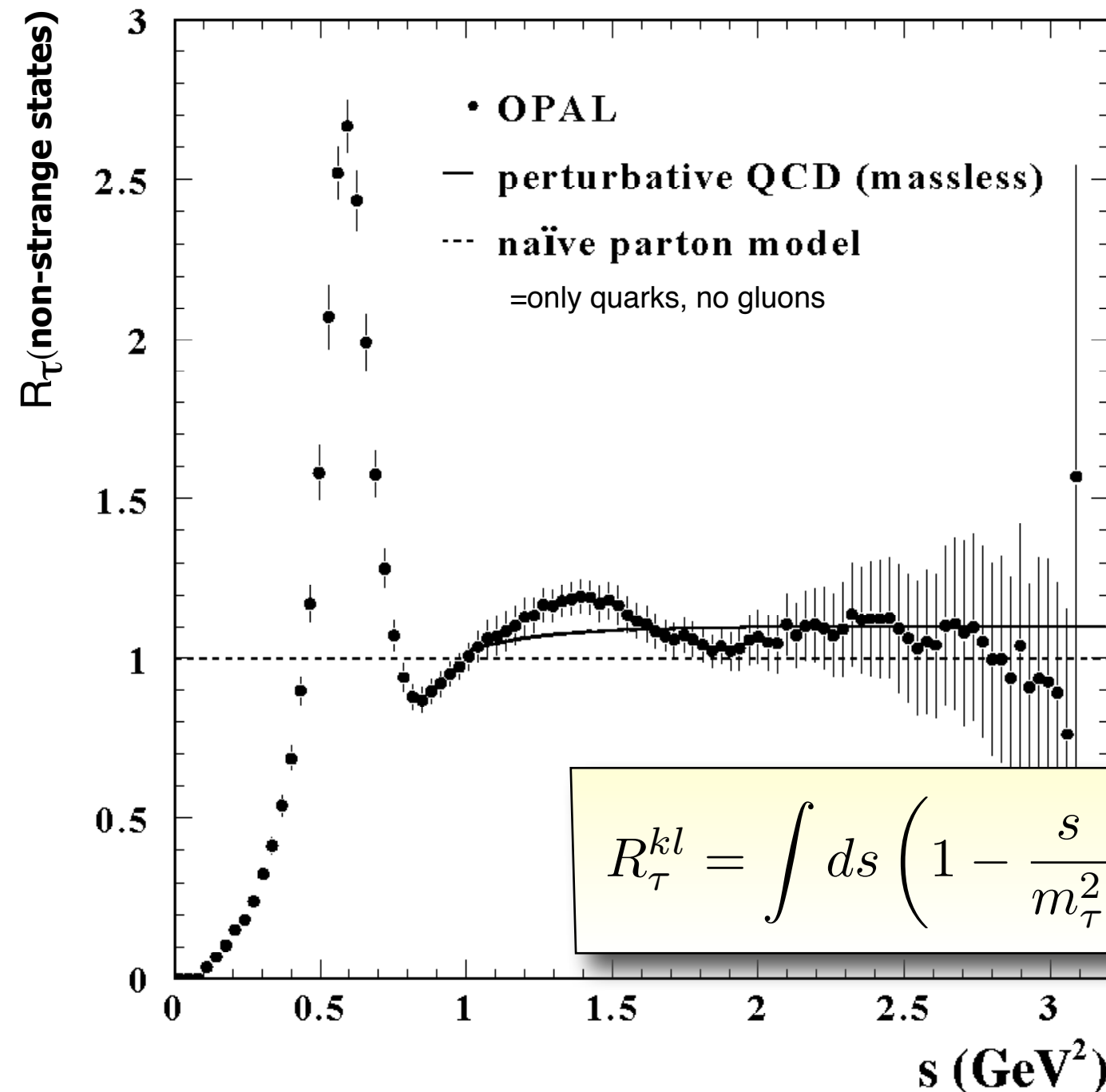
$$\alpha_s(m_\tau) = 0.3285 \pm 0.018 \quad (5.5 \% \text{ rel.})$$



$$\alpha_s(m_Z) = 0.1194 \pm 0.0021 \quad (1.8 \% \text{ rel.})$$

The Beauty of a Moment...

Without phase space factor and taking moments, in order to average out resonances:



approach taken at LEP: fit simultaneously α_s and the non-pert. coefficients, by measuring various moments.

opinions vary about the importance of this “ZERO”,
see eg. Altarelli, arXiv: 1303.6065

$$\delta_{NP} = \frac{\text{ZERO}}{m_{\tau}^2} + c_4 \cdot \frac{\langle O_4 \rangle}{m_{\tau}^4} + c_6 \cdot \frac{\langle O_6 \rangle}{m_{\tau}^6} + \dots$$

$$R_{\tau}^{kl} = \int ds \left(1 - \frac{s}{m_{\tau}^2}\right)^k \left(\frac{s}{m_{\tau}^2}\right)^l \frac{dR_{\tau}}{ds} \propto 3(1 + \delta_{QCD} + \delta_{NP})$$


also known at NNNLO

From moments-measurements at LEP:



-  the non-perturbative contributions turn out to be (surprisingly) small

eg. ALEPH: $\delta_{NP} = -0.0059 \pm 0.0014$

$$\Delta\alpha_s(m_\tau) \approx \pi \cdot \Delta\delta_{NP}$$

-  it would definitely be interesting to measure such moments again, with much improved precision. Eg. an uncertainty on δ_{NP} of < 0.0005

But:

-  various methods of estimating higher-order terms (see eg. Altarelli:1303.6065, or Pich:1303.2262) differ by $>\sim 5\%$ for $\alpha_s(m_{\text{tau}})$, ie. leading to $>\sim 1\%$ at the Z mass scale.
-  Seems difficult (impossible?) to improve on this?

- Jet-or event-shape based measurements, as well as using tau decays:
seems difficult (impossible?) to go well below the 1% rel. uncertainty.
- EWK observables at the Z pole, such as hadronic width (branching ratio):
this could be interesting to be further investigated.