

# Results from the B-Factories

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(BaBar Collaboration)

**Lepton Photon 2013**  
**San Francisco**  
28 June 2013



# e+e- B-factories have a very broad scientific program

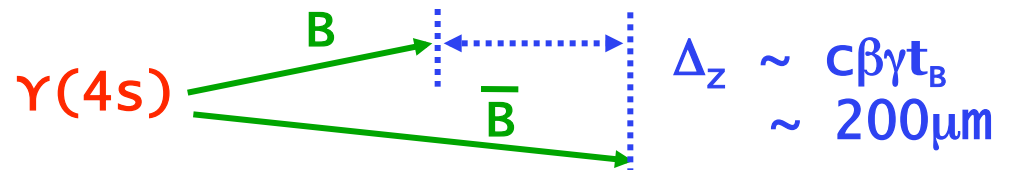
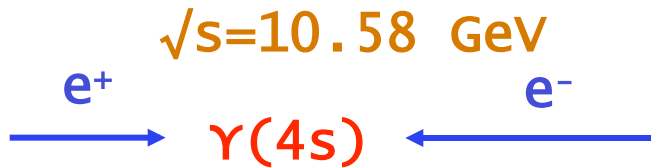
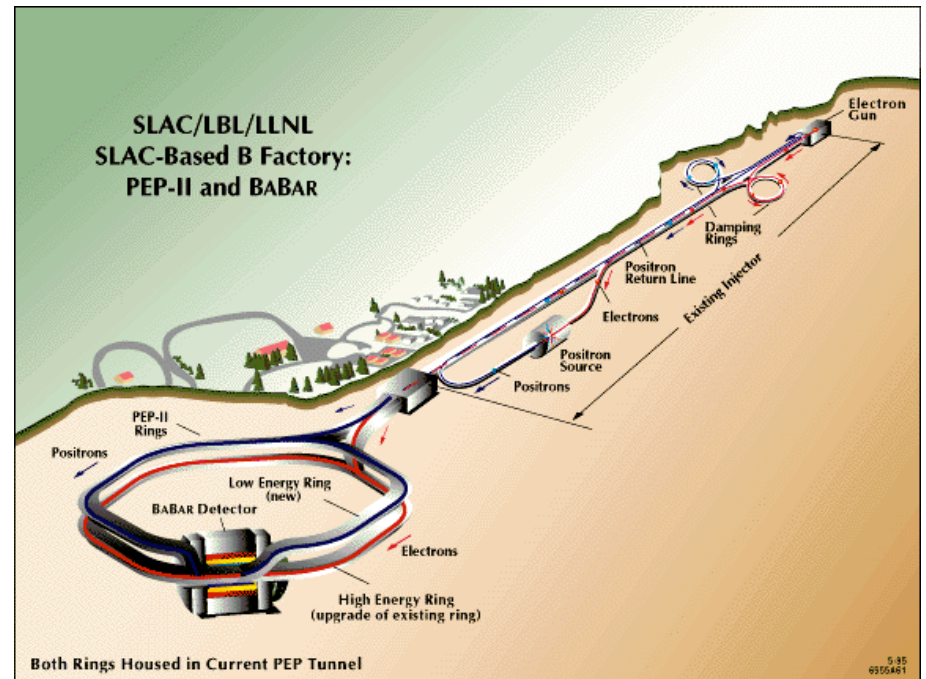
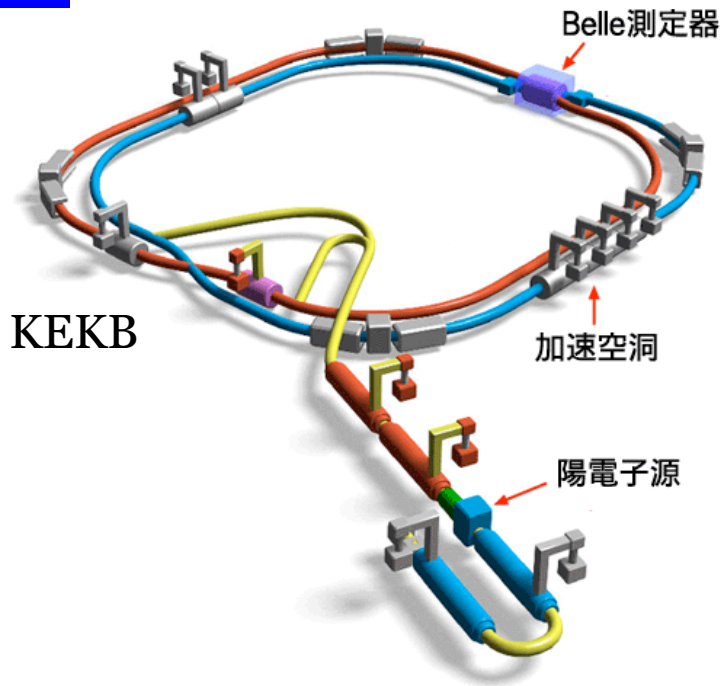
- CP & T-violation
- Precision CKM measurements
- Rare decays
- Searches for Processes beyond the SM
- Hadron production in Initial State Radiation
- Spectroscopy (see e.g. Yuan Changzheng presentation Tues. pm)
- ...

..... can only scratch the surface in this sampling of results

# Flavour physics at the luminosity frontier



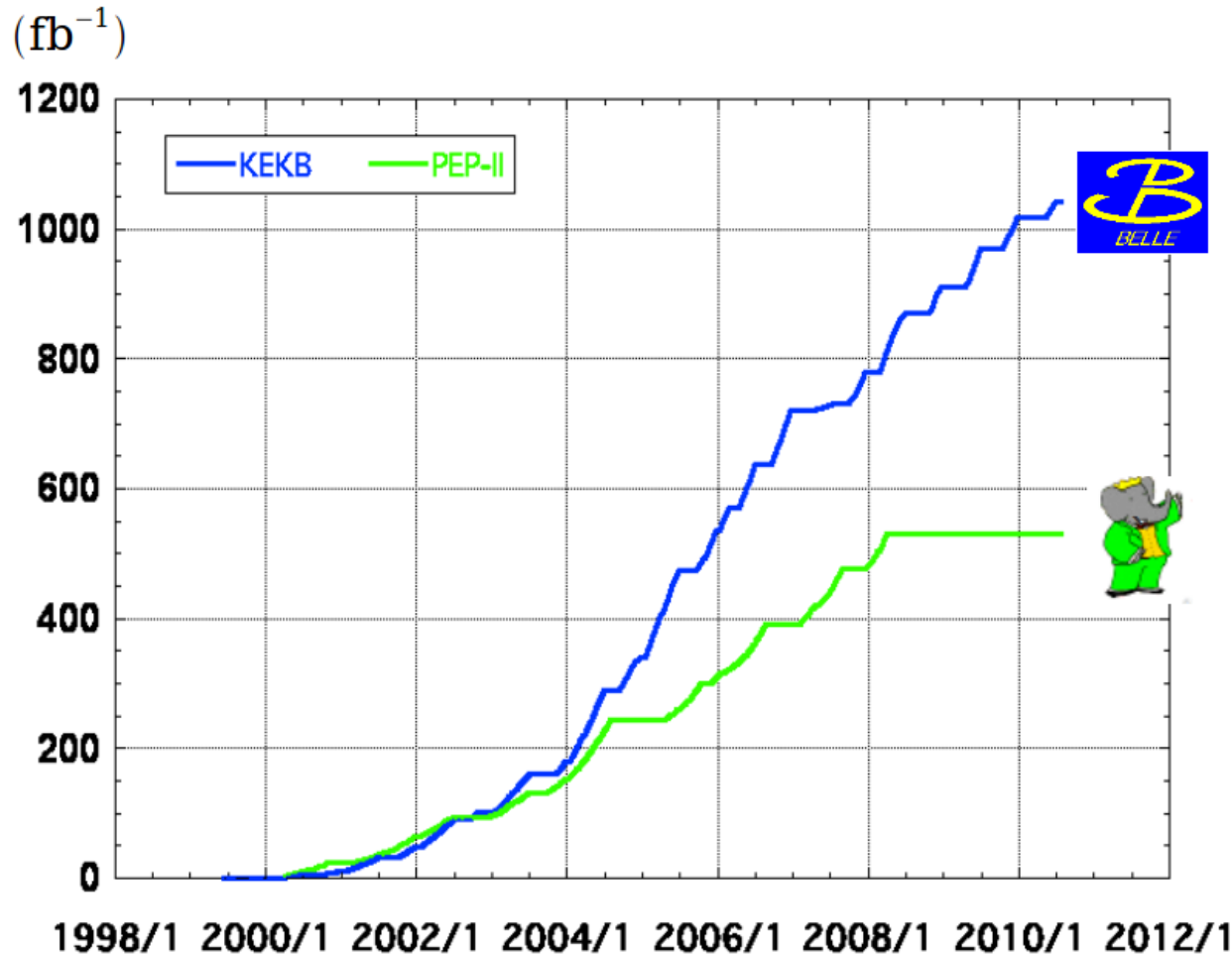
## asymmetric B factories



<b>BaBar</b>	$p(e^-) = 9 \text{ GeV}$	$p(e^+) = 3.1 \text{ GeV}$
<b>Belle</b>	$p(e^-) = 8 \text{ GeV}$	$p(e^+) = 3.5 \text{ GeV}$

$\beta\gamma = 0.56$
$\beta\gamma = 0.42$

## Integrated luminosity of B factories



**> 1  $\text{ab}^{-1}$**

**On resonance:**

$\Upsilon(5S)$ : 121  $\text{fb}^{-1}$

$\Upsilon(4S)$ : 711  $\text{fb}^{-1}$

$\Upsilon(3S)$ : 3  $\text{fb}^{-1}$

$\Upsilon(2S)$ : 25  $\text{fb}^{-1}$

$\Upsilon(1S)$ : 6  $\text{fb}^{-1}$

**Off reson./scan:**

$\sim 100 \text{ fb}^{-1}$

**$\sim 550 \text{ fb}^{-1}$**

**On resonance:**

$\Upsilon(4S)$ : 433  $\text{fb}^{-1}$

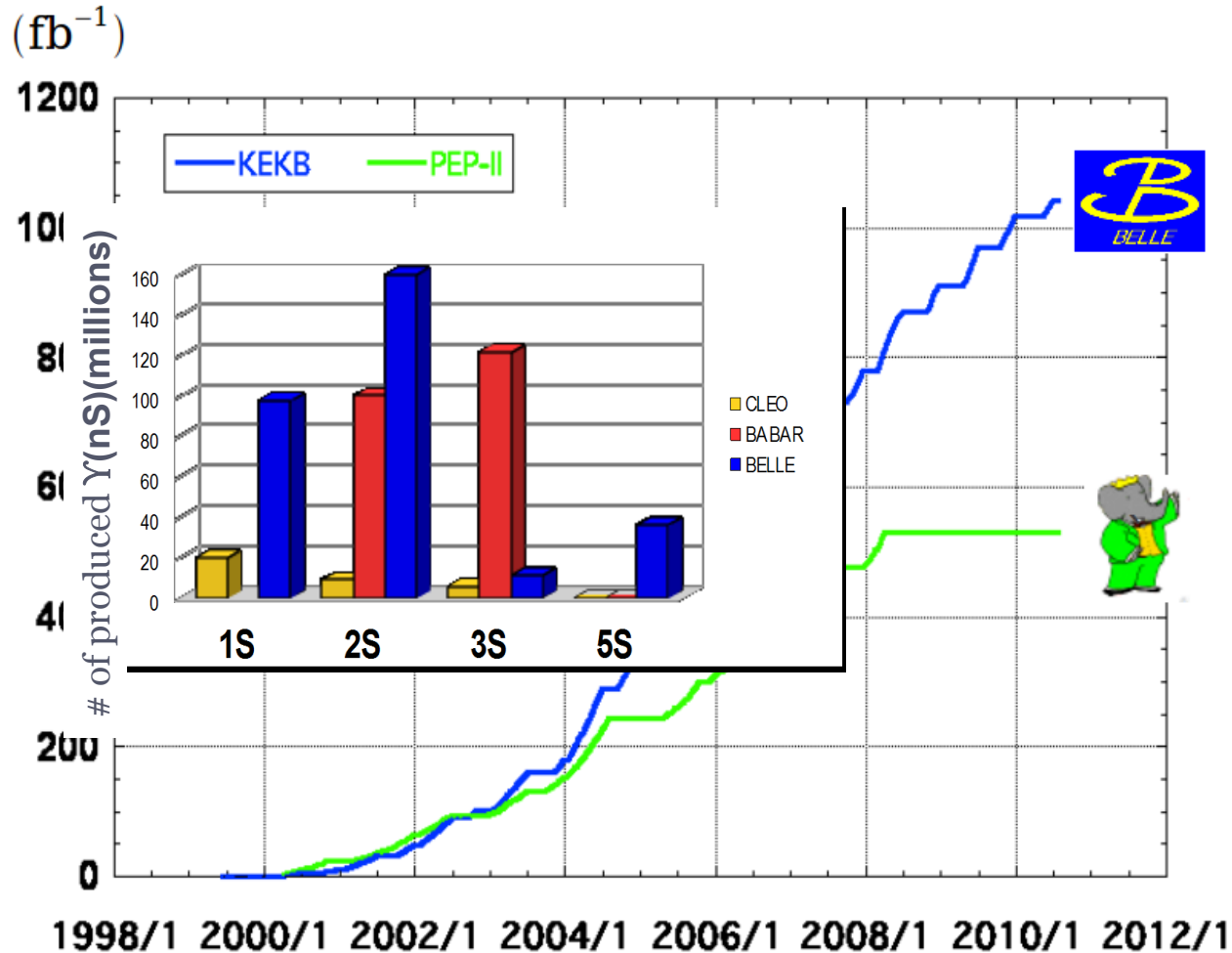
$\Upsilon(3S)$ : 30  $\text{fb}^{-1}$

$\Upsilon(2S)$ : 14  $\text{fb}^{-1}$

**Off resonance:**

$\sim 54 \text{ fb}^{-1}$

## Integrated luminosity of B factories



**> 1 ab<sup>-1</sup>**

**On resonance:**

$Y(5S): 121 \text{ fb}^{-1}$

$Y(4S): 711 \text{ fb}^{-1}$

$Y(3S): 3 \text{ fb}^{-1}$

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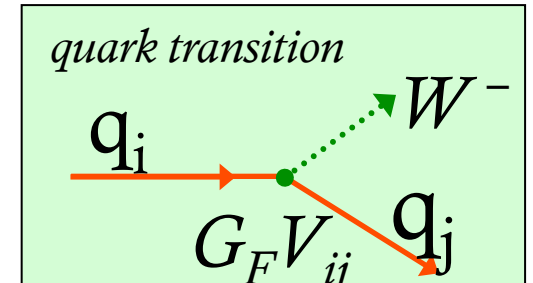
$Y(2S): 14 \text{ fb}^{-1}$

**Off resonance:**

$\sim 54 \text{ fb}^{-1}$

In SM weak charged transitions mix quarks of different generations - encoded in unitary CKM matrix:

$$\begin{pmatrix} d' & s' & b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$



Unitarity → 4 independent parameters

one is the complex phase and sole source of CP violation in SM

In the Wolfenstein parameterisation:

$$\mathbf{V}_{CKM} = \begin{pmatrix} \square & \square & \cdot \\ \square & \square & \cdot \\ \cdot & \cdot & \square \end{pmatrix} = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + O(\lambda^4)$$

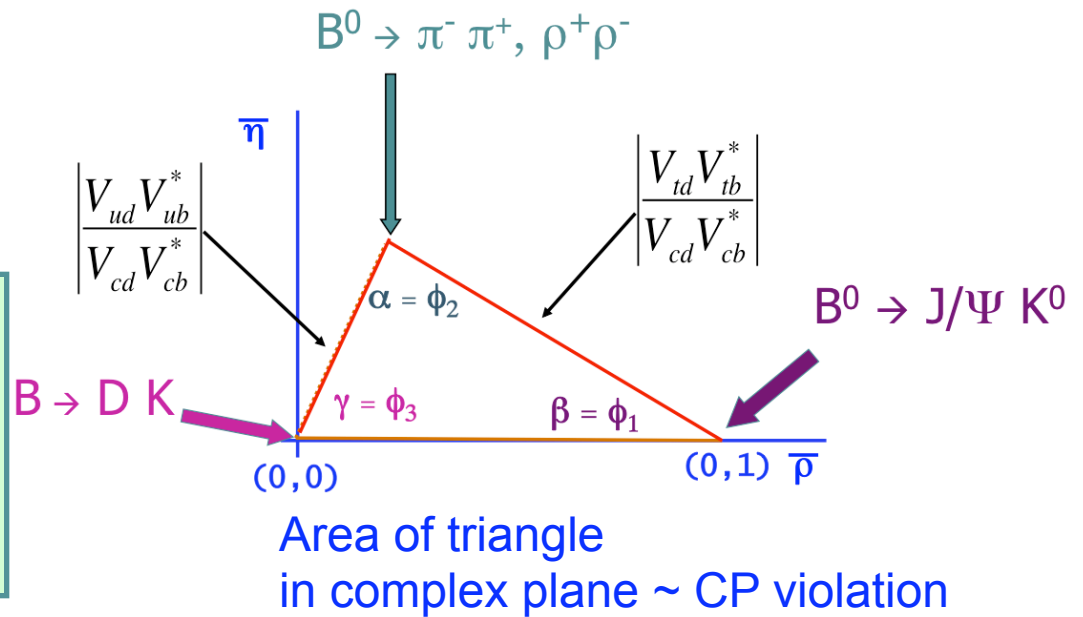
$$\lambda^2 = \frac{|V_{us}|^2}{|V_{ud}|^2 + |V_{us}|^2}; \quad A^2 \lambda^4 = \frac{|V_{cb}|^2}{|V_{ud}|^2 + |V_{us}|^2}; \quad \bar{\rho} + i\bar{\eta} = -\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*}$$

Physics beyond the SM signaled by breakdown of unitarity of CKM matrix: non-closure of the ‘unitarity triangle’

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

$$\alpha = \arg\left(-\frac{V_{td}V_{tb}^*}{V_{ud}V_{ub}^*}\right) \quad \beta = \arg\left(-\frac{V_{cd}V_{cb}^*}{V_{td}V_{tb}^*}\right)$$

$$\gamma = \arg\left(-\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*}\right) \quad \beta_s = \arg\left(-\frac{V_{ts}V_{tb}^*}{V_{cs}V_{cb}^*}\right)$$



- Make as many precision measurements as possible that **overconstrain** the four CKM parameters ( $A, \lambda, \rho, \eta$ )
- New Physics would be revealed in discrepancies between measurements
- Generally requires non-perturbative QCD input to convert measurements to a SM CKM interpretation (but exceptions where single weak phase dominate as in  $J/\psi$  Ks)

Belle and *BABAR* designed to measure and test CKM framework

- Sum of angles:  $\alpha + \beta + \gamma = (177 \pm 9)^\circ$   
 $\alpha = (88.5 \pm 4.5)^\circ \quad \beta = (21.4 \pm 0.8)^\circ \quad \gamma = (67 \pm 8)^\circ$

- Sides of triangle from semileptonic B decays:

$|V_{cb}|$  (Lattice QCD for FF)

$$|V_{cb}|_{\text{excl}}^{LQCD} = (39.04 \pm 0.55_{\text{exp}} \pm 0.74_{\text{th}}) \times 10^{-3}$$

$$|V_{cb}|_{\text{incl}} = (42.01 \pm 0.46_{\text{exp}} \pm 0.59_{\text{th}}) \times 10^{-3}$$

$$|V_{cb}|_{\text{average}} = (40.81 \pm 0.90_{\text{exp}} \pm 1.14_{\text{th}}) \times 10^{-3}$$

NB: errors scaled by 2.4

$|V_{cb}|$  (HF Sum Rules for FF)

$$|V_{cb}|_{\text{excl}}^{HFSR} = (40.93 \pm 0.57_{\text{exp}} \pm 0.94_{\text{th}}) \times 10^{-3}$$

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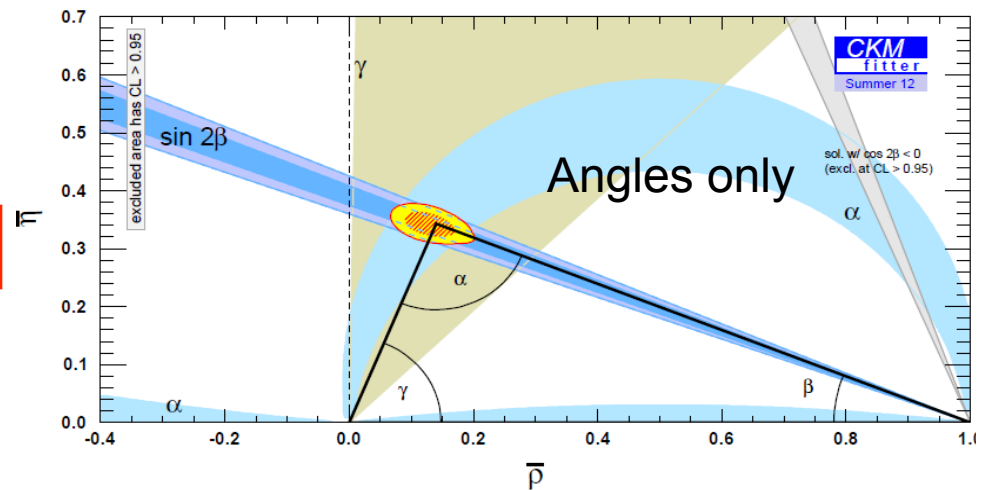
$$|V_{cb}|_{\text{average}} = (41.67 \pm 0.38_{\text{exp}} \pm 0.50_{\text{th}}) \times 10^{-3}$$

$$|V_{ub}|_{\text{excl}}^{LQCD} = (3.26 \pm 0.16_{\text{exp}} \pm 0.24_{\text{th}}) \times 10^{-3}$$

$$|V_{ub}|_{\text{incl}} = (4.42 \pm 0.19_{\text{exp}} \pm 0.15_{\text{th}}) \times 10^{-3}$$

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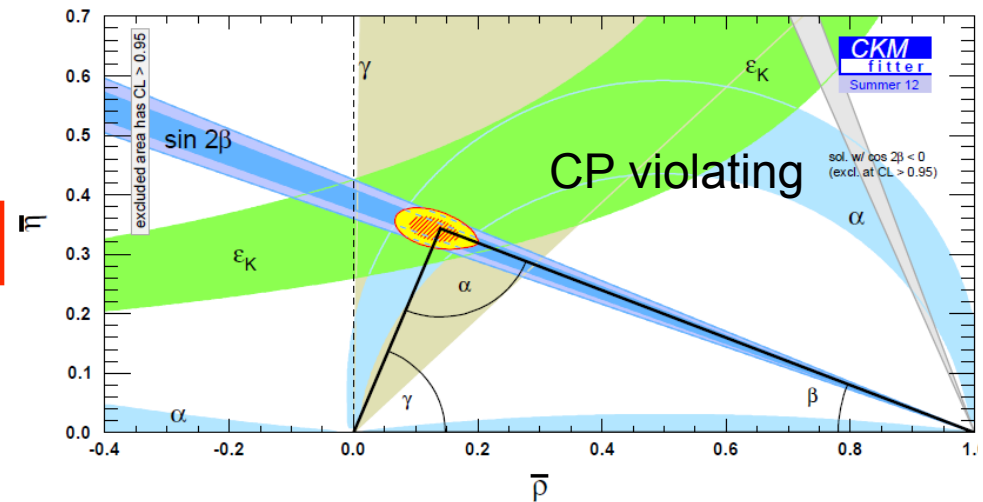
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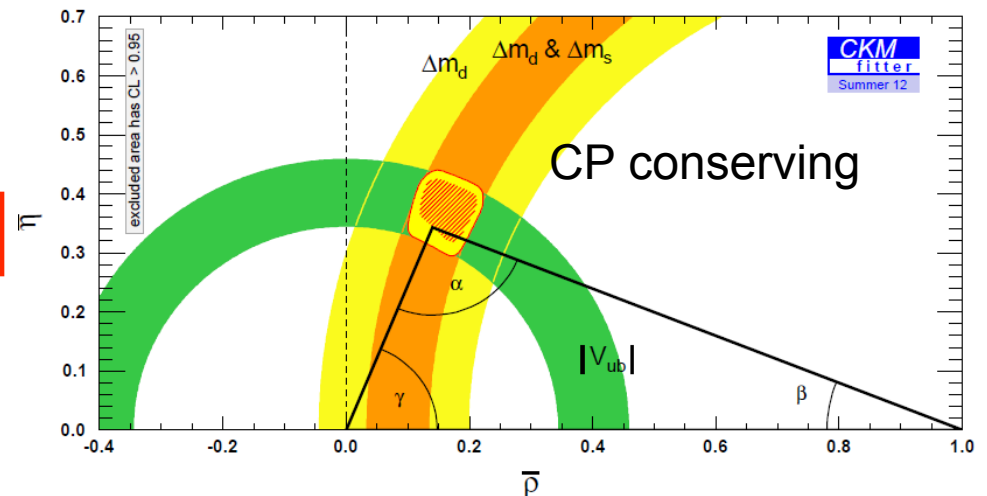
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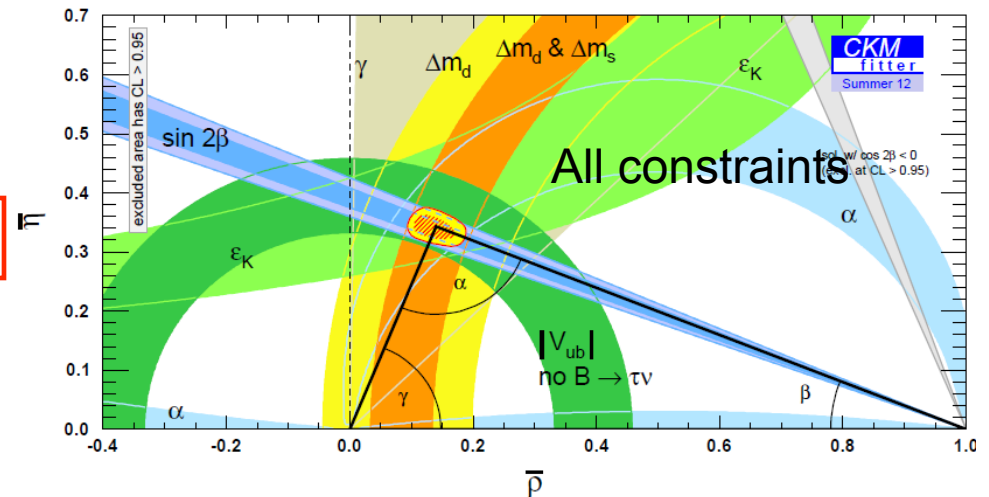
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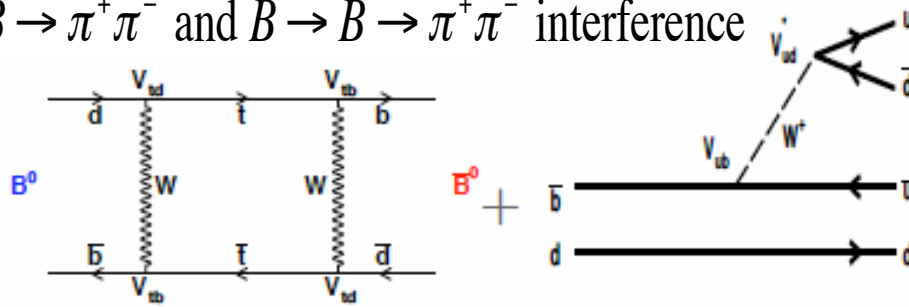
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**Data generally well described  
by CKM framework**

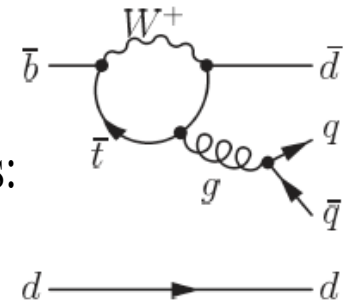


$\alpha = \phi_2$  accessible via  $b \rightarrow u$  transitions in  $B \rightarrow \pi\pi, B \rightarrow \rho\rho$ , or  $B \rightarrow \rho\pi$

e.g.  $B \rightarrow \pi^+\pi^-$  and  $B \rightarrow \bar{B} \rightarrow \pi^+\pi^-$  interference



Complicated by penguins:



Time-dependent decay rate of a  $B$  or a  $\bar{B}$  meson decaying into common  $CP$  eigenstate

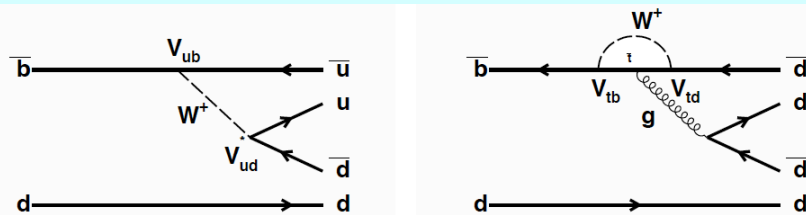
$$\mathcal{P}(\Delta t) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} \left\{ 1 + q \left[ \mathcal{S}_{CP} \sin(\Delta m_d \Delta t) + \mathcal{A}_{CP} \cos(\Delta m_d \Delta t) \right] \right\}$$

$\mathcal{S}_{CP} = \sin 2\alpha$  ;  $\mathcal{A}_{CP} = 0$  at tree level

With additional penguin diagrams ('pollution')

$$\mathcal{S}_{CP} = \sqrt{1 - \mathcal{A}_{CP}^2} \sin 2\alpha_{eff} ; \mathcal{A}_{CP} \neq 0 \text{ allowed}$$

Isospin analysis using, e.g.  $B \rightarrow \pi^0\pi^0$ , recovers  $\sin 2\alpha$   
(penguin dominates over colour suppressed internal tree)



Results from the B-Factories

$\mathcal{A}_{CP}$ : direct  $CP$  violation ( $= -\mathcal{C}_{CP}$ )

$\mathcal{S}_{CP}$ : mixing induced  $CP$  violation

$q$ : flavor of  $B_{tag}$ ,  $q = +1$  for  $B_{tag} = B^0$

$\tau_{B^0}$ :  $B$  life time

$\Delta m_d$ : mass difference of  $B_H$  and  $B_L$

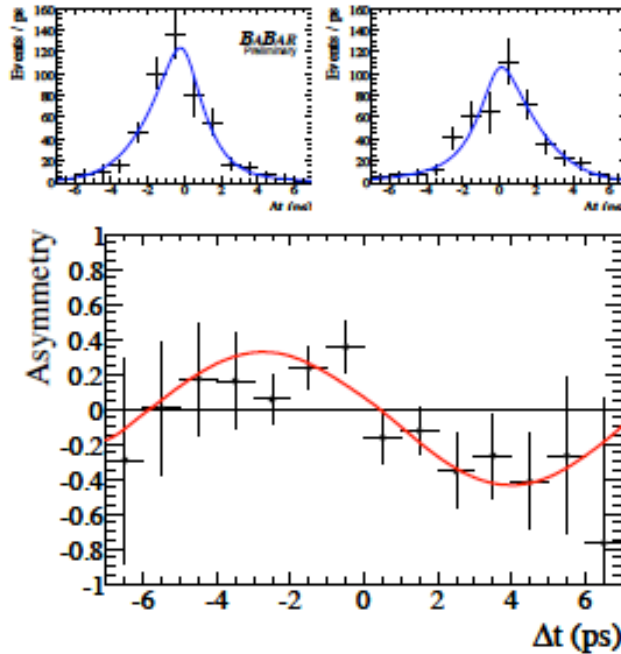
$\Delta t$ : decay time difference of  $B_{CP}$  and  $B_{tag}$

- New published result on  $B \rightarrow \pi^+ \pi^-$  from  $B_{ABAR}$  and Belle ( $B_{ABAR}$  also has  $B \rightarrow \pi^0 \pi^0$  on full dataset)
- $B \rightarrow \rho\rho$ :  $VV$  final state, helicity analysis to measure CP
  - $B \rightarrow \rho^+ \rho^-$  older from  $B_{ABAR}$  and Belle
  - $B \rightarrow \rho^0 \rho^0$  full dataset from  $B_{ABAR}$  and Belle (new 2012)
- $B \rightarrow (\rho\pi)^0$  new result from  $B_{ABAR}$ : warning about lack of robustness in extracting  $\alpha = \phi_2$  with current statistics

$$B \rightarrow \pi^+ \pi^-$$

BaBar PRD **87** 052009(2013)

$467 \times 10^6 B\bar{B}$  pairs

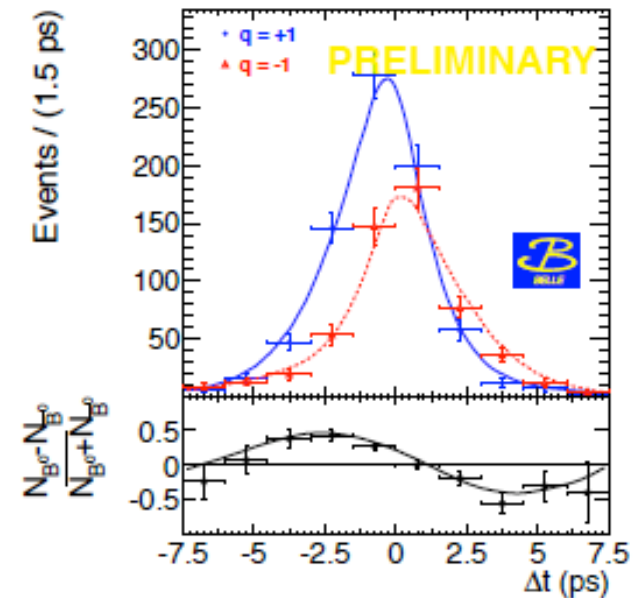


$$S_{CP}^{\pi^+ \pi^-} = -0.68 \pm 0.10 \pm 0.03$$

$$A_{CP}^{\pi^+ \pi^-} = +0.25 \pm 0.08 \pm 0.02$$

Belle arXiv:1302.0551

$772 \times 10^6 B\bar{B}$  pairs



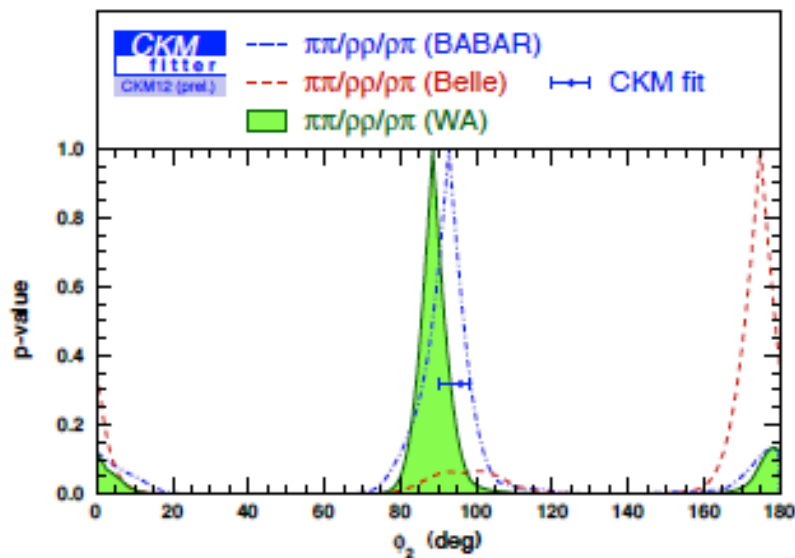
$$S_{CP}^{\pi^+ \pi^-} = -0.636 \pm 0.082 \pm 0.027$$

$$A_{CP}^{\pi^+ \pi^-} = +0.328 \pm 0.061 \pm 0.027$$

$\Rightarrow$  clear mixing induced  $CP$  and presence of penguins

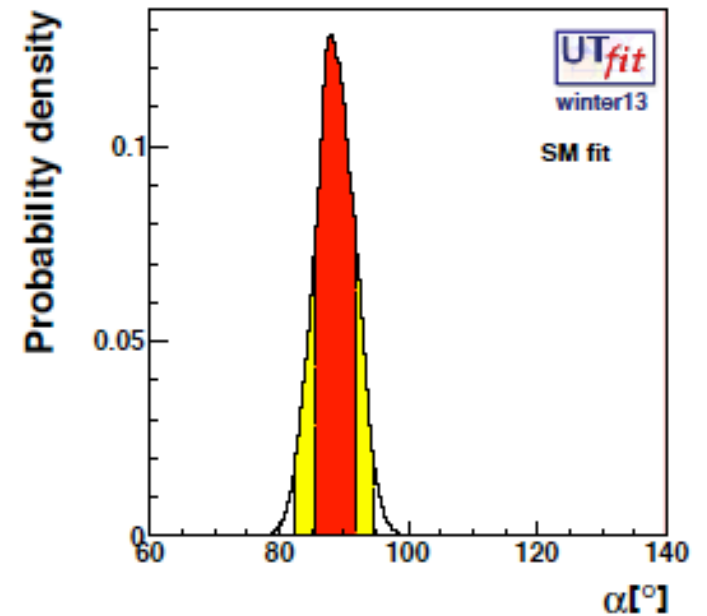
Overall fits for  $\alpha = \phi_2$  using  
 $B \rightarrow \pi\pi$ ,  $B \rightarrow \rho\rho$ , or  $B \rightarrow \rho\pi$

(frequentist)



$$\phi_2/\alpha = (88.5^{+4.7}_{-4.4})^\circ$$

(bayesian)

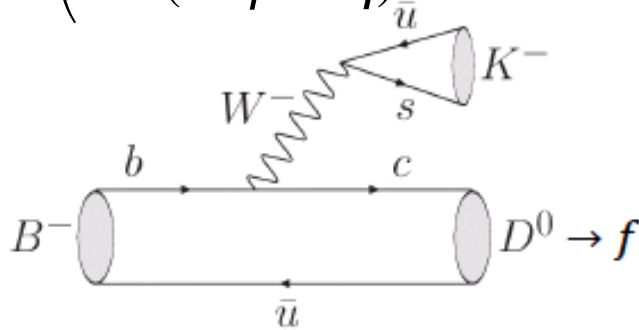


$$\phi_2/\alpha = (88.7 \pm 3.1)^\circ$$

$B^\pm \rightarrow D^{(*)0} K^{(*)\pm}$  decays dominate  $\gamma = \phi_3$  measurements

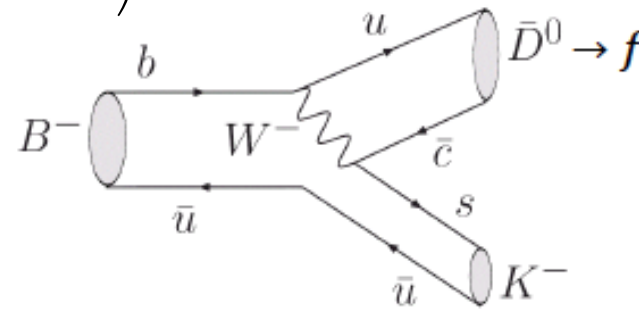
$$V = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + O(\lambda^4)$$

$$|V_{ub}| e^{-i\gamma}$$



color allowed

$$A_1 \propto V_{cb} V_{us}^* \sim A\lambda^3$$



color suppressed

$$A_2 \propto V_{ub} V_{cs}^* \sim A\lambda^3(\rho + i\eta)$$

$$|A_{total}|^2 = |A_1|^2 + |A_2|^2 + 2|A_1||A_2|\cos(-\gamma + \delta)$$

Theoretically clean: no penguin pollution

$$r_b = \left| \frac{A(B^+ \rightarrow D^0 K^+)}{A(B^+ \rightarrow \bar{D}^0 K^+)} \right|$$

strong phase from B and D decay

Unknowns:  $\gamma, r_b, \delta_b + \delta_D$

$r_b$  &  $\delta_b$  B hadronic parameters extracted with  $\gamma$

$\delta_D$  measured at charm factories



$B^\pm \rightarrow D^{(*)0} K^{(*)\pm}$  decays dominate  $\gamma = \phi_3$  measurements

Different methods for extracting  $\gamma = \phi_3$  depending on the D decay mode final state

**GLW** [M. Gronau, D. London, D. Wyler, PLB253,483 (1991); PLB 265, 172 (1991)]

- $D^0$  to two-body CP eigenstates  $K^+K^-$ ,  $\pi^+\pi^-$  (even),  $K_S\pi^0$ ,  $K_S\omega$  (odd)

**ADS** [D. Atwood, I. Dunietz, A. Soni, PRL 78, 3357 (1997)]

- $D^0$  to doubly Cabibbo suppressed decays  $K^+\pi^-$ ,  $K^+\pi^-\pi^0$ , ...

**GGSZ (Dalitz)** [D. Atwood et al., PRL78, 3257 (1997); A. Giri et al., PRD68, 054018 (2003)]

- $D^0$  to 3-body decays  $K_S\pi^+\pi^-$ ,  $K_S K^+K^-$ ,  $\pi^+\pi^-\pi^0$ , etc.
  - Dalitz plot fitted to determine how the strong phase of  $D^0$  decay amplitude varies over the Dalitz plane
  - model independent analysis

*BABAR* and Belle have reconstructed the most sensitive decay modes using all or nearly all of their full datasets  
GLW+ADS+GGSZ Combinations

*BABAR* PRD87 052015 (2013)

$$\gamma = \left( 69^{+17}_{-16} \right)^\circ \pmod{180^\circ}$$

exp+DP model systematic =  $\pm 4^\circ$

*BABAR* and Belle

Physics of the B Factories to be submitted EPJC

$$\gamma = \left( 67 \pm 11 \right)^\circ \pmod{180^\circ}$$

Belle CKM2012 arXiv:1301.2033

$$\gamma = \left( 68^{+15}_{-14} \right)^\circ \pmod{180^\circ}$$

$B^\pm \rightarrow D^{(*)0} K^{(*)\pm}$  decays dominate  $\gamma = \phi_3$  measurements

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*BABAR* and Belle

us

LHCb with  $3\text{fb}^{-1}$

$$\gamma = (67 \pm 12)^\circ \pmod{180^\circ}$$

re decay modes

ts

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Belle CKM2012 arXiv:1301.2033

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- Well established canon of SM that weak interactions maximally violate parity (P) and charge conjugation (C) - neutrinos are LH, antineutrinos are RH.
- CP also measured to be violated in neutral kaon and B-meson systems - phenomena well described within CKM framework
- The CPT Theorem ([Locally Lorentz-invariant QFT conserves CPT](#))  $\rightarrow$  if there is CP violation, there is also violation of time reversal invariance (T)
- Difficult to establish experimentally T violation independent of CPT: need a system where we experimentally know what QM state is in before it decays.

$e^+e^- \rightarrow \Upsilon(4S) \rightarrow B(\alpha) B(\bar{\alpha})$  is an entangled P-wave state: EPR tells us the state of a B-meson prior to its decay if its EPR-entangled partner decays and is identified – it's how BaBar and Belle measure CP violation ...  
can also use this to search for direct T violation and test CPT using this approach

Bernabeu, Martinez-Vidal, Villanueva-Perez, arXiv: JHEP08,064 (2012)

- BABAR uses this approach to measure a non-zero T violation - strength predicted by CPT and the CP violation measured by BABAR and Belle

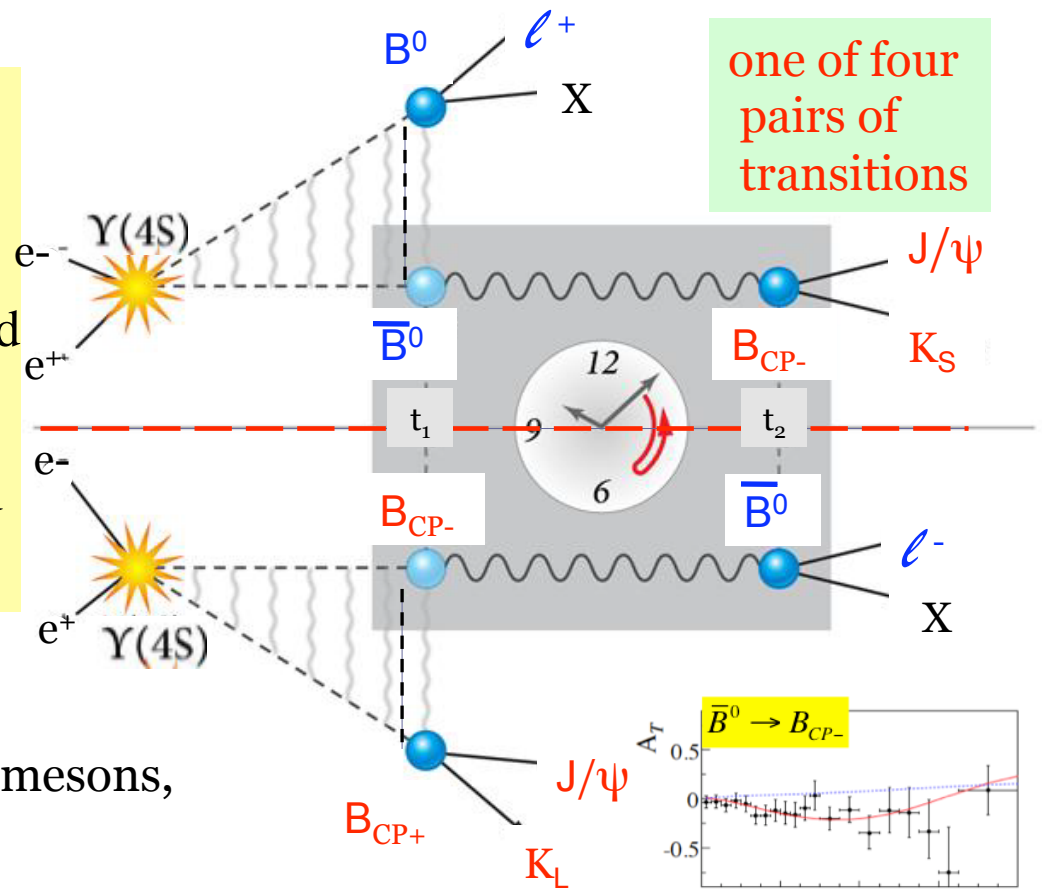
$$|i\rangle = \frac{1}{\sqrt{2}} [B^0(t_1)\bar{B}^0(t_2) - \bar{B}^0(t_1)B^0(t_2)] = \frac{1}{\sqrt{2}} [B_{CP+}(t_1)B_{CP-}(t_2) - B_{CP-}(t_1)B_{CP+}(t_2)]$$

Define ratio

$$A_T = \frac{P(a \rightarrow b) - P(b \rightarrow a)}{P(a \rightarrow b) + P(b \rightarrow a)}$$

a: Flavour eigenstate  $B^0$  or  $\bar{B}^0$  identified by semileptonic decay:  $\ell^+$  or  $\ell^-$

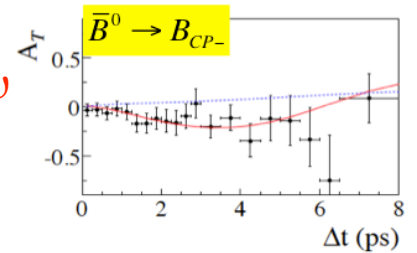
b: CP eigenstate  $B_{CP+}$  or  $B_{CP-}$  identified by decay to:  $J/\psi K_S$  or  $J/\psi K_L$



Measure time-ordered decays of both B-mesons, time difference defined as:

$$\Delta t = t_{CP} - t_{flavour} > 0 \text{ for } B^0 \rightarrow B_{CP-}$$

$$\Delta t < 0 \text{ for } B_{CP-} \rightarrow B^0$$



- Time dependent rate 8 decays

$$g_{\alpha,\beta}^{\pm}(\Delta\tau) \propto e^{-\Gamma\Delta\tau} \{1 + S_{\alpha,\beta}^{\pm} \sin(\Delta m_d \Delta\tau) + C_{\alpha,\beta}^{\pm} \cos(\Delta m_d \Delta\tau)\}$$

S and C probe interference  
in decay-mixing and decay

ML fit to determine 8 pairs  
of  $S_{\alpha,\beta}^{\pm}$  and  $C_{\alpha,\beta}^{\pm}$  parameters

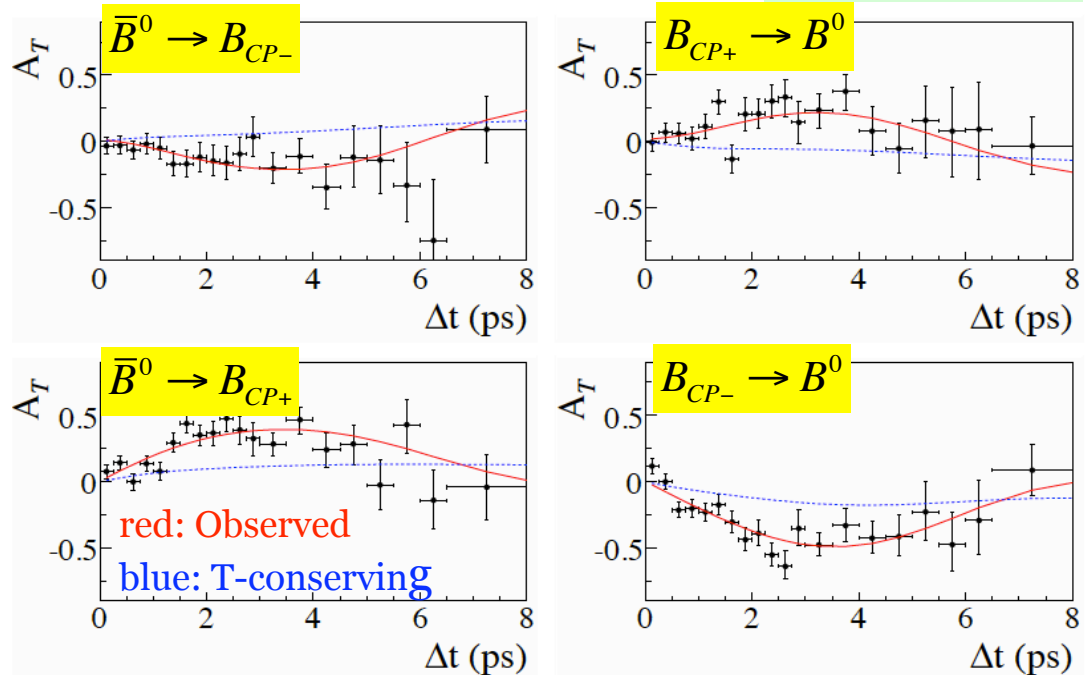
$\pm\{\Delta t > 0, \Delta t < 0\}$

$\alpha$  flavour tag  $\{\ell^+, \ell^-\}$

$\beta$  CP tag  $\{K_L, K_S\}$

$$A_T(\Delta t) \approx \frac{\Delta C_T^+}{2} \cos \Delta m \Delta t + \frac{\Delta S_T^+}{2} \sin \Delta m \Delta t$$

four pairs of  
transitions



Combined Fit results:

$$\Delta S_T^+ = -1.37 \pm 0.14 \pm 0.06$$

$$\Delta C_T^+ = +0.10 \pm 0.14 \pm 0.08$$

$$\Delta S_T^- = +1.17 \pm 0.18 \pm 0.11$$

$$\Delta C_T^- = +0.04 \pm 0.14 \pm 0.08$$

Expected:

$$-2 \sin 2\beta$$

$$0.0$$

$$+2 \sin 2\beta$$

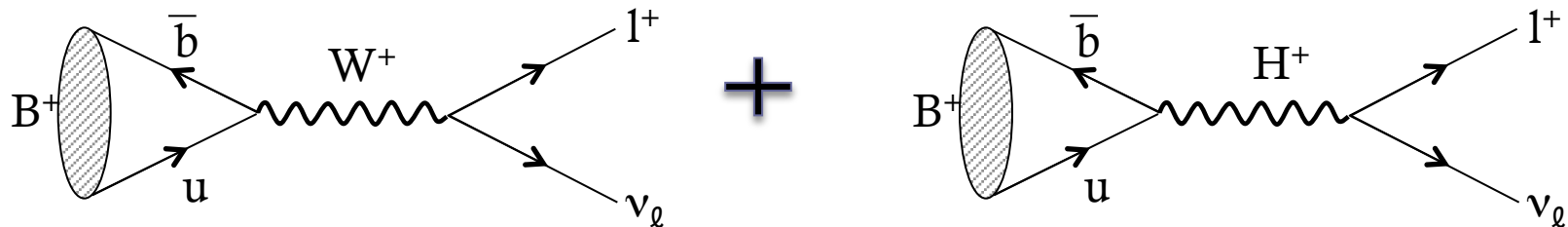
$$0.0$$

**14 $\sigma$  signal**  
**Consistent with  $\sin 2\beta$**   
**results on CP Violation and**  
**with CPT invariance**

$B^- \rightarrow \ell^- \nu_\ell$  simple purely leptonic pseudo-scalar decays  
 carry information about product of CKM element and  
 strong interaction 'decay constant'

$$\mathcal{B}F(B \rightarrow \ell \nu)_{SM} = \frac{G_F^2 m_B m_\ell^2}{8\pi} \left(1 - \frac{m_\ell^2}{m_B^2}\right)^2 |V_{ub}|^2 f_B^2 \tau_M (1 + \delta_{EM}^{B\ell 2})$$

- Interesting because some New Physics theories have charged Higgs contributing to observed decay rate



- Additional tree level contribution from a charged Higgs
  - It does not suffer from helicity suppression, but gets the same  $m_l$  dependence from Yukawa coupling
  - Branching fraction theoretical expression depends on the NP model

$$\mathcal{B}(B \rightarrow l\nu)_{2HDM} = \mathcal{B}(B \rightarrow l\nu)_{SM} \times \left(1 - \tan^2 \beta \frac{m_B^2}{m_H^2}\right)^2$$

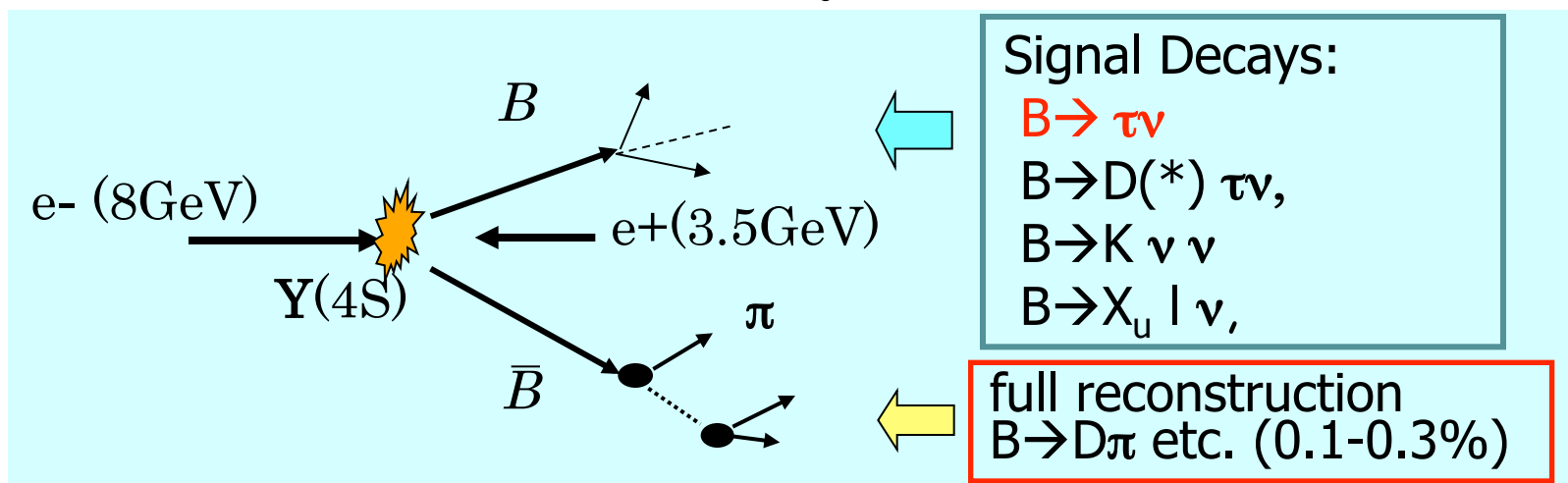
W. S. Hou, Phys. Rev. D 48 (1993) 2342.

$$\mathcal{B}(B \rightarrow l\nu)_{SUSY} = \mathcal{B}(B \rightarrow l\nu)_{SM} \times \left(1 - \frac{\tan^2 \beta}{1 + \epsilon_0 \tan \beta} \frac{m_B^2}{m_H^2}\right)^2$$

A.G. Akeroyd and S.Recksiegel  
 J.Phys.G29:2311-2317,2003

## Uses full reconstruction tagging

- **fully reconstruct** one of the B's to tag B flavour/charge, determine its momentum, and exclude decay products of this B from further analysis



Powerful tool for B decays with neutrino

→ unique feature at  $e^+e^-$  B factories

At the  $Y(4S)$  the  $B^+$  and  $B^-$  decay products overlap, this associates parent B with each particle



# $B^- \rightarrow \tau^- \nu_\tau$ Results

Main discriminating variable on the signal side:  
 remaining energy in the calorimeter, not  
 associated with any charged track or photon  
 → Signal at  $E_{ECL} = 0$

**Belle**

$$Br(B \rightarrow \tau \nu) = [0.72^{+0.27}_{-0.25} \pm 0.11] \times 10^{-4}$$

PRL 110 (2013) 131801

**BABAR**

$$Br(B \rightarrow \tau \nu) = [1.83^{+0.53}_{-0.49} \pm 0.24] \times 10^{-4}$$

arXiv:1207.0698[hep-ex] submitted to PRD

All measurements combined:

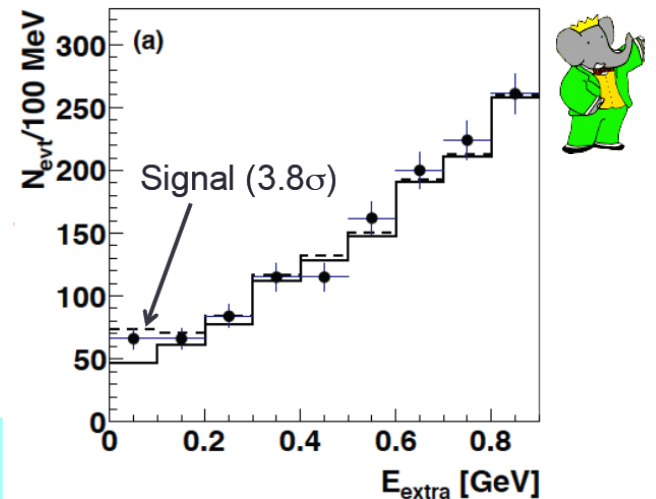
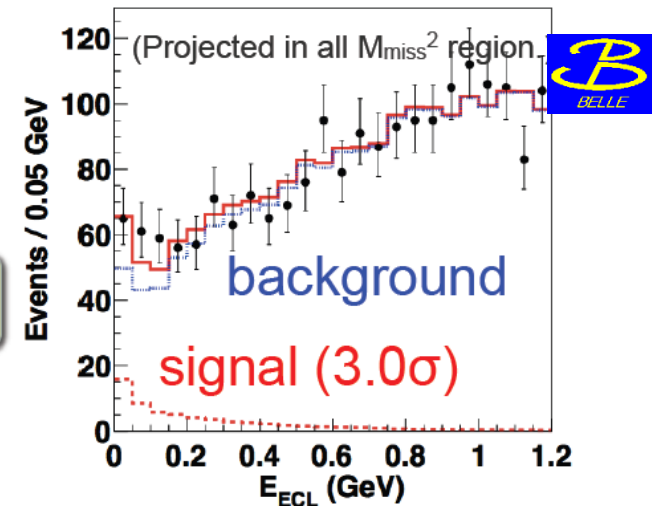
$$BF(B \rightarrow \tau \nu) = (1.15 \pm 0.23) \cdot 10^{-4}$$

cf Standard Model:

$$BF(B \rightarrow \tau \nu)_{SM} = (1.01 \pm 0.29) \times 10^{-4}$$

$$\text{(using } |V_{ub}| = (3.95 \pm 0.38 \pm 0.39) \times 10^{-4} \text{)}$$

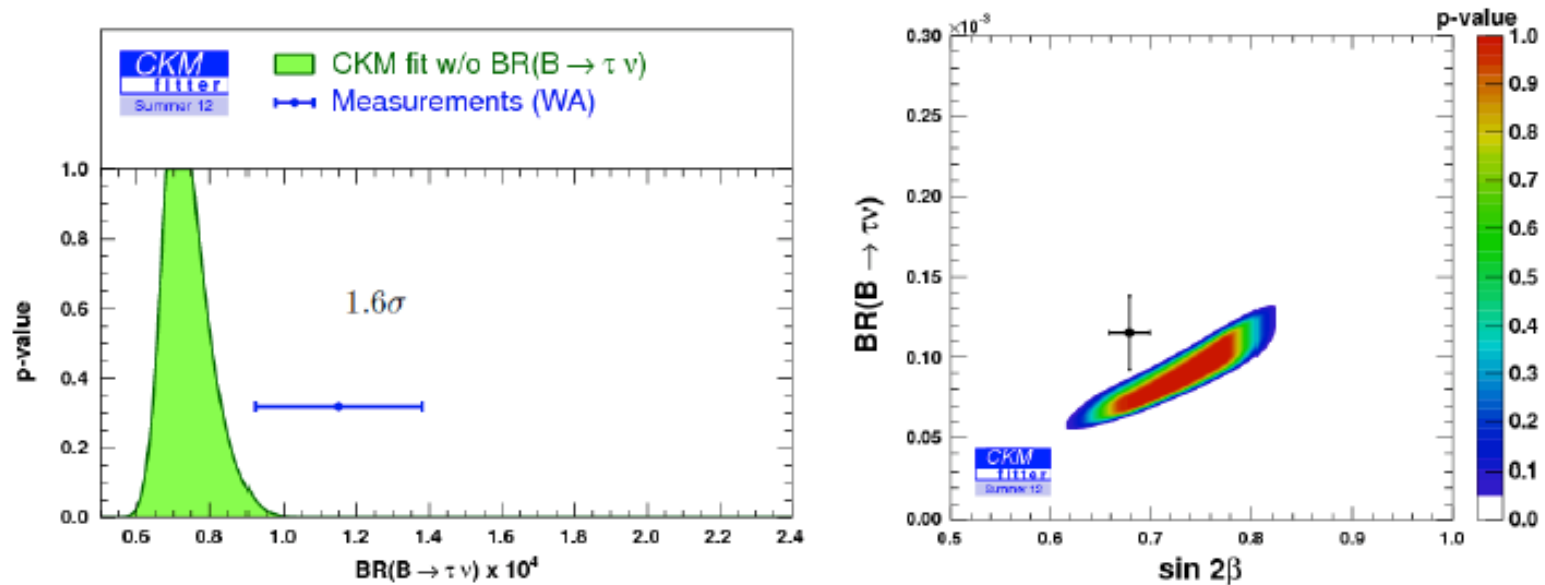
Results from the B-Factories





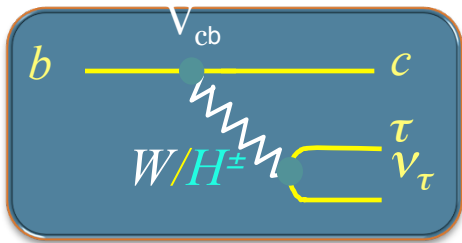
# Results after ICHEP 2012

$$BF(B \rightarrow \tau \nu) = (1.15 \pm 0.23) \cdot 10^{-4}$$



# B → D<sup>(\*)</sup>τν Decays

Semileptonic decay sensitive to charged Higgs



Ratio of τ to μ,e could be reduced/enhanced significantly

$$R(D) = \frac{\Gamma(\bar{B} \rightarrow D\tau\nu)}{\Gamma(\bar{B} \rightarrow D\ell\nu)} \quad R(D^*) = \frac{\Gamma(\bar{B} \rightarrow D^*\tau\nu)}{\Gamma(\bar{B} \rightarrow D^*\ell\nu)}$$

- A well understood process, form factors measured for  $B \rightarrow D^{(*)}\ell\nu$ , decays involving  $\tau$  have additional helicity amplitude
- Several experimental and theoretical uncertainties cancel in the ratio!
- non-SM contribution from  $H^\pm$  expected to change rates for  $B \rightarrow D^{(*)}\tau\nu$

Scalar Helicity Amplitude: (good to 1% for  $m_{H^\pm} > 15\text{GeV}$ )

$$H_S^{2HDM} \approx H_S^{SM} \times \left( 1 - \frac{\tan^2 \beta}{m_{H^\pm}^2} \frac{q^2}{1 \mp m_c/m_b} \right) \begin{array}{l} - \text{ for } B \rightarrow D\tau\nu \\ + \text{ for } B \rightarrow D^*\tau\nu \end{array}$$



BABAR, PRL101802 (2012)

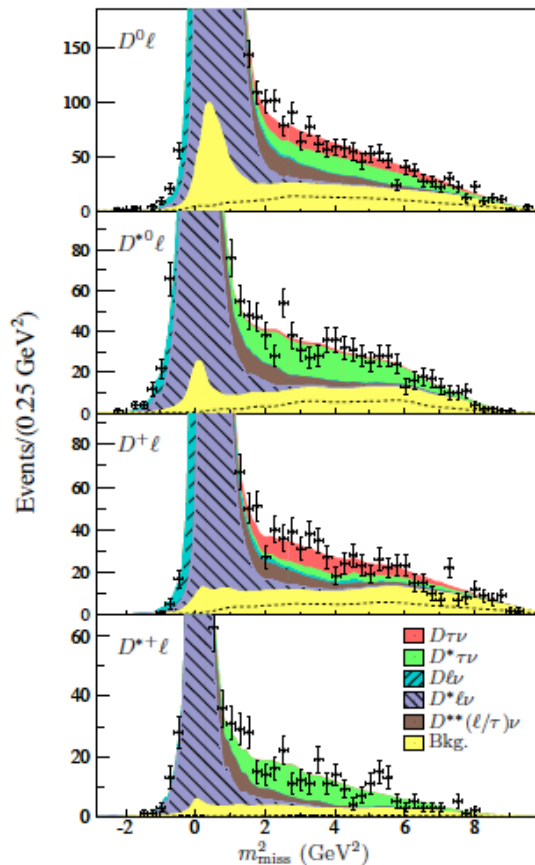
$$\mathcal{R}(D)_{\text{exp}} = 0.440 \pm 0.072 \quad \mathcal{R}(D^*)_{\text{exp}} = 0.332 \pm 0.030$$

$\updownarrow 2.0\sigma$

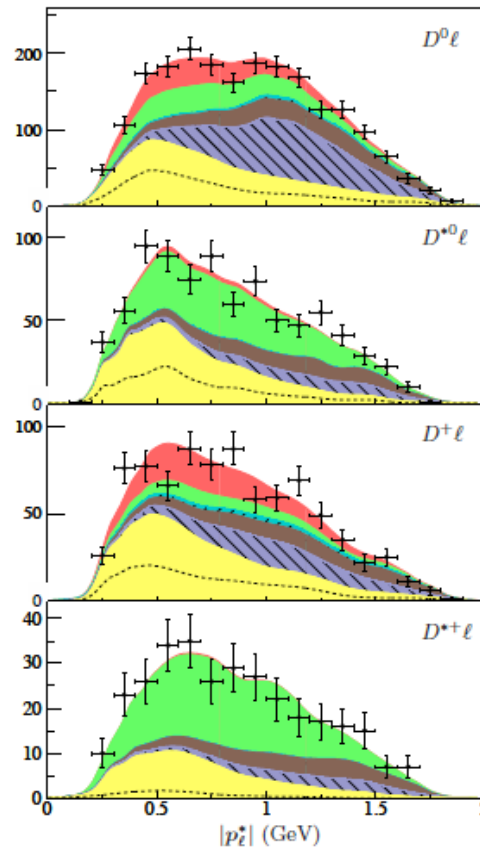
$\updownarrow 2.7\sigma$

$$\mathcal{R}(D)_{\text{SM}} = 0.297 \pm 0.017 \quad \mathcal{R}(D^*)_{\text{SM}} = 0.252 \pm 0.003$$

SM expectations in S. Faifer, J. Kamenik, I. Nisandzic, PRD 85, 094025 (2012).



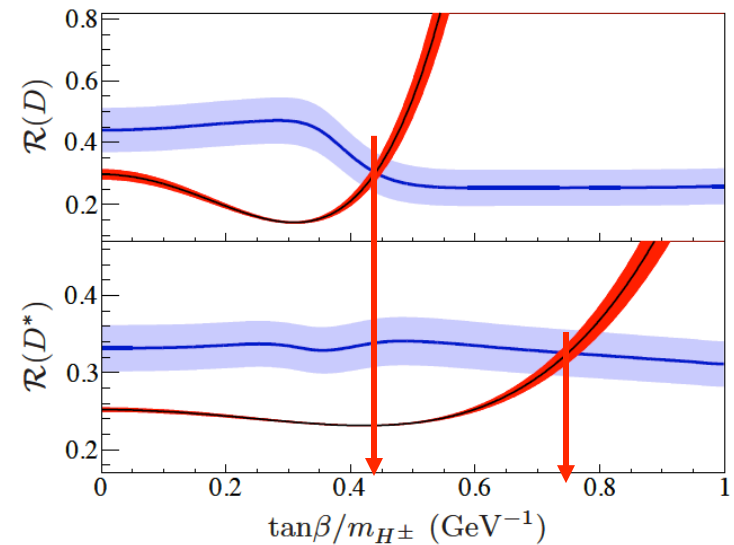
Missing Mass Squared



Lepton momentum in B frame

Results from the B-Factories

Combined BaBar result:  
3.4 $\sigma$  above SM



$$\frac{\text{BF}(B \rightarrow D^{(*)} \tau \nu)}{\text{BF}(B \rightarrow D^{(*)} \ell \nu)} \text{ vs } \tan\beta/m_{H^\pm}$$



BABAR, PRL101802 (2012)

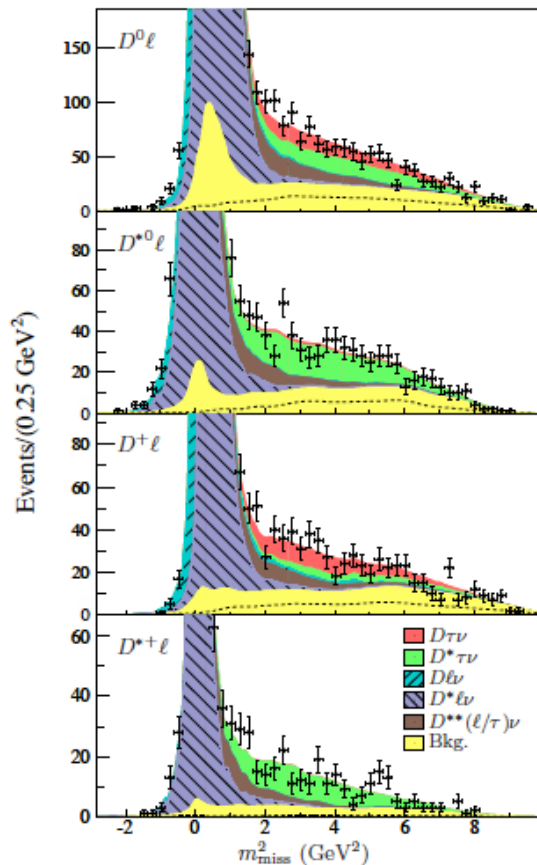
$$\mathcal{R}(D)_{\text{exp}} = 0.440 \pm 0.072 \quad \mathcal{R}(D^*)_{\text{exp}} = 0.332 \pm 0.030$$

↕ 2.0σ

↕ 2.7σ

$$\mathcal{R}(D)_{\text{SM}} = 0.297 \pm 0.017 \quad \mathcal{R}(D^*)_{\text{SM}} = 0.252 \pm 0.003$$

SM expectations in S. Fajfer, J. Kamenik, I. Nisandzic, PRD 85, 094025 (2012).

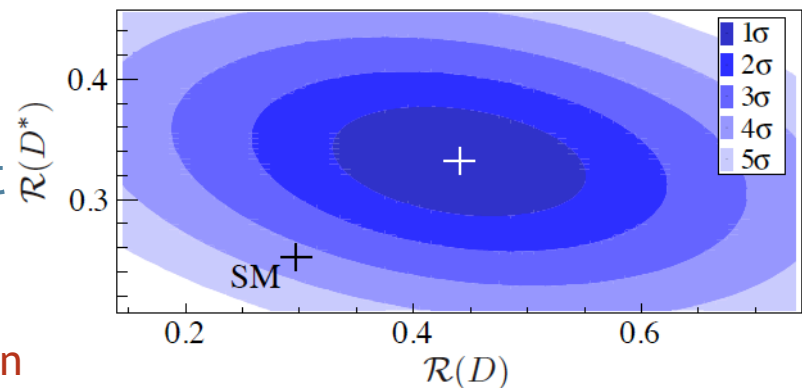


Missing Mass Squared

If discrepancy with SM holds, result cannot be explained by Type II 2HDM; excluded over full parameter space at 99.8%CL

Can be accommodated in more general extensions of Type III 2HDM

Combined BaBar result: 3.4σ above SM



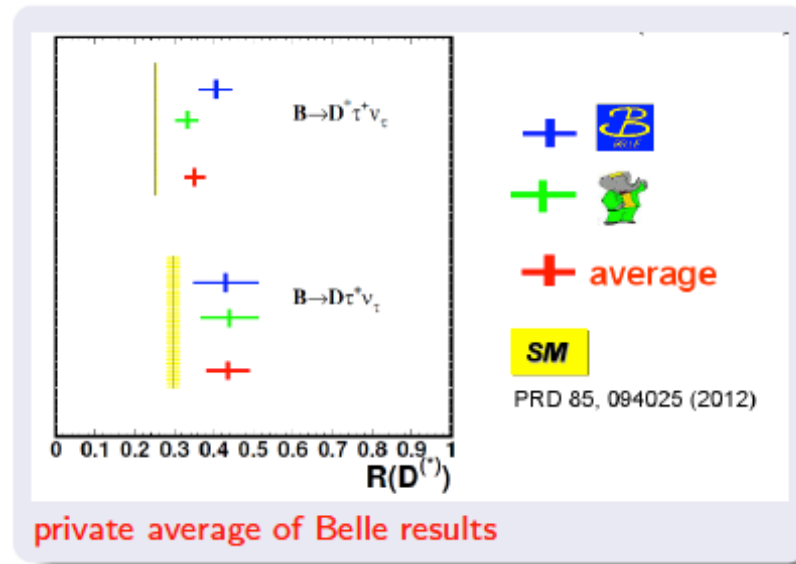
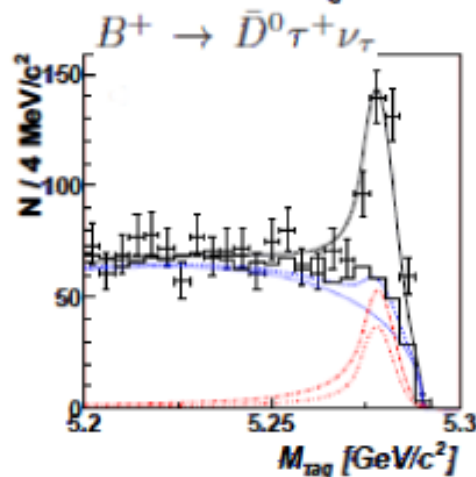
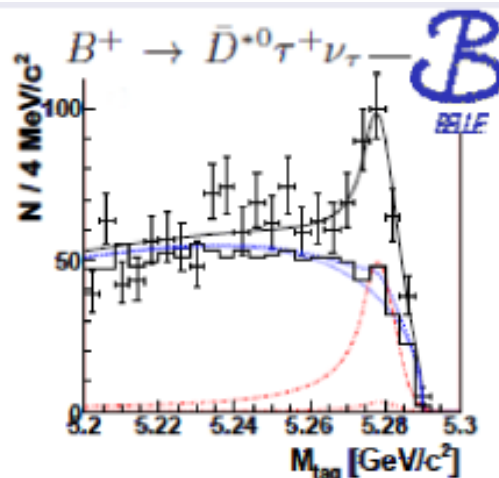


Belle, PRL99, 191807(2007)  
 Belle, PRD 82 (2010)

First observation of B → D<sup>\*</sup>τν by Belle (2007)

Belle did not publish a measurement of the ratio directly for all modes and so did not quote average R values. Publications based on fraction of Belle data

At May 2013 FPCP meeting Andrej Bozek (Belle) presented a 'private average' of the published Belle results



*Belle Deviations from SM based on A. Bozek average of Belle results (FPCP 2013)*  
 $R(D^*) = 3.0\sigma$   
 $R(D) = 1.4\sigma$   
 $R(D^{(*)}) = 3.3\sigma$

Bozek reports a combined BaBar and Belle deviation from the SM of  $4.8\sigma$

# Searches for Light CP-odd Higgs

- $\Upsilon(2S,3S) \rightarrow \gamma A^0, A^0 \rightarrow \text{hadrons}$
- $\Upsilon(1S) \rightarrow \gamma A^0, A^0 \rightarrow \tau^+ \tau^-, \mu^+ \mu^-$

## Dark Higgs Searches

- $e^+e^- \rightarrow A'h', h' \rightarrow A'A', A' \rightarrow h_1h_2 (h_i = e, \mu, \pi)$

**New BABAR result** - shown first here at Lepton Photon 2013:

Search for light Higgs decaying to two gluons or  $s\bar{s}$  in radiative decays of the  $\Upsilon(1S)$

# BaBar Searches for Light CP-odd Higgs

Search for light Higgs decaying to two gluons or  $s\bar{s}$  in radiative decays of the  $\Upsilon(1S)$

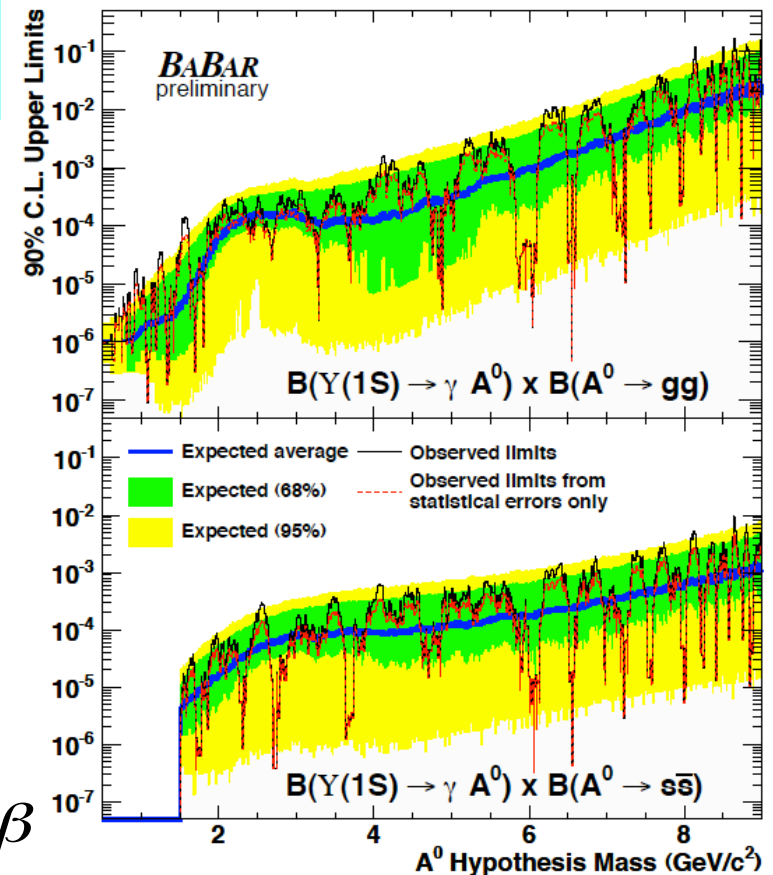
$$e^+e^- \rightarrow \Upsilon(2S) \rightarrow \pi^+\pi^-\Upsilon(1S)$$

$$\Upsilon(1S) \rightarrow \gamma A^0; A^0 \rightarrow gg \text{ or } s\bar{s}$$

Sample:  $17.6 \times 10^6$   $\Upsilon(1S)$  decays

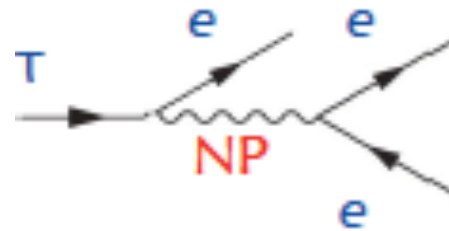
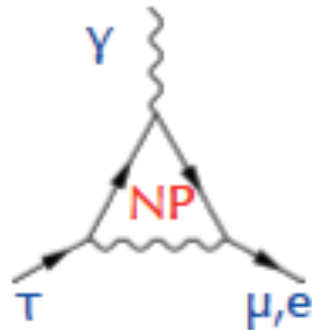
At low Higgs mass,  $m_A < 2m_\tau$  :

- expect  $s\bar{s}$  to dominate rate at high  $\tan\beta$
- expect  $gg$  to dominate rate at low  $\tan\beta$



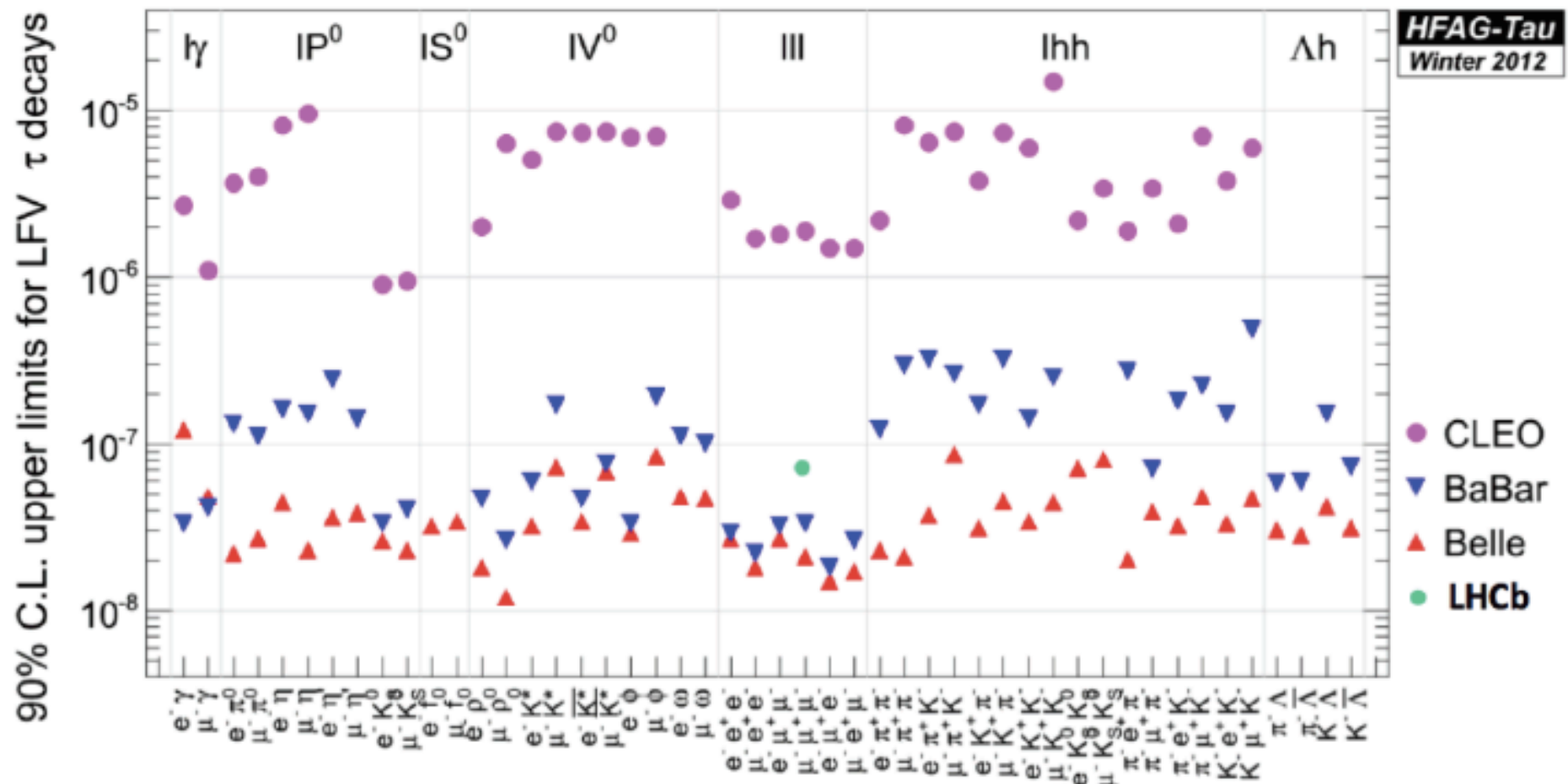
# Lepton Flavour Violation in Tau Decays

LFV is long established way of seeking evidence of New Physics

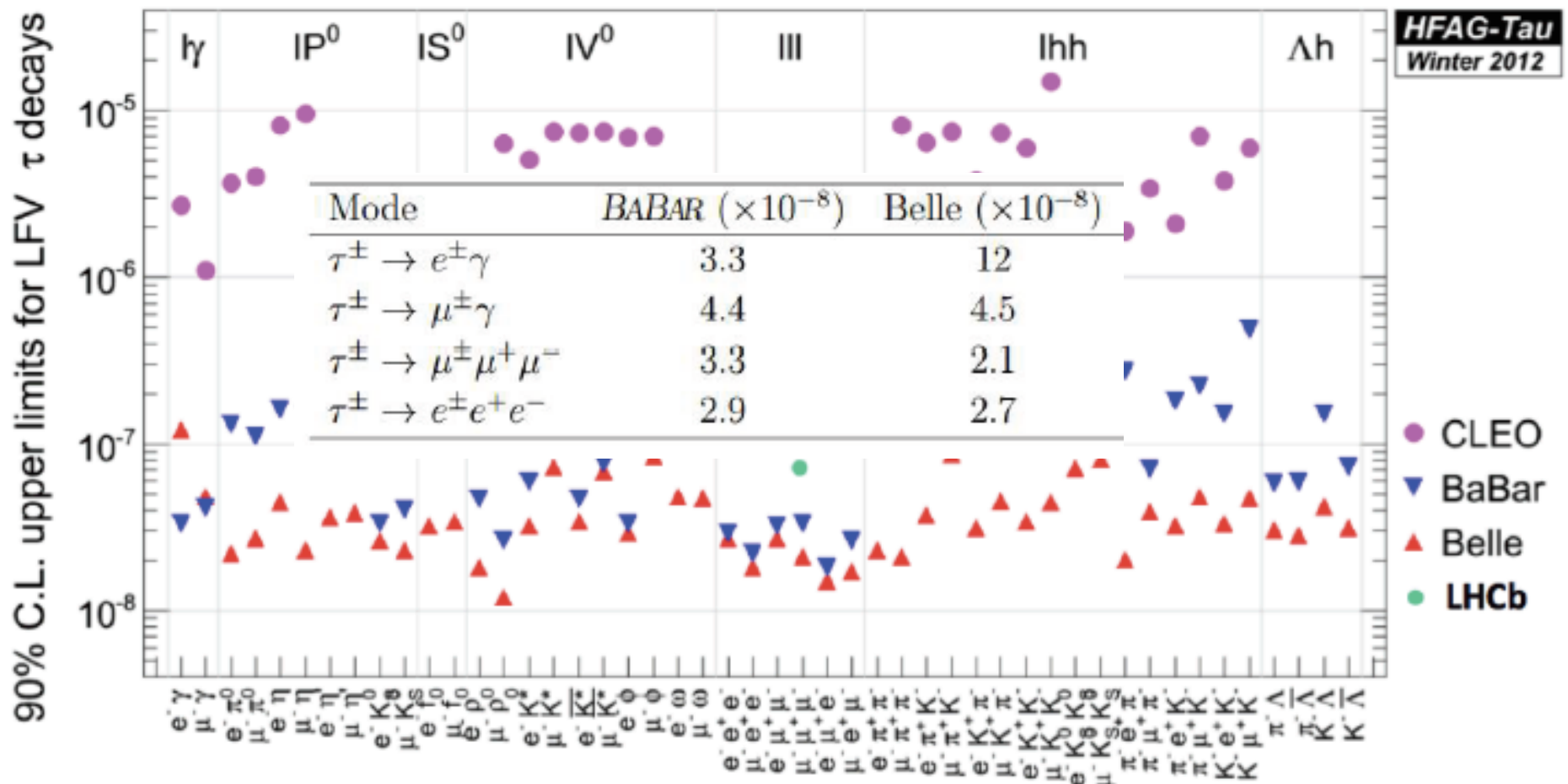




- 48 channels probed by Belle and BABAR
- LHCb has recently entered the game



- 48 channels probed by Belle and BABAR
- LHCb has recently entered the game



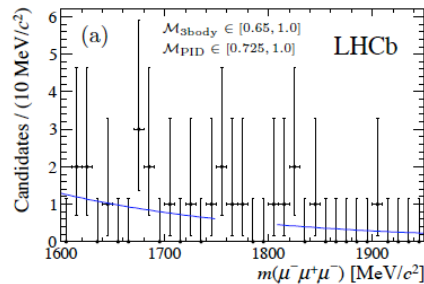
LHCb uses  $D_s \rightarrow \tau \nu$  as source of taus

PhysLett B 7224(2013)

Published on  $\text{fb}^{-1}$  of data looking for LFV and Baryon number and Lepton number non-conserving decays

$$\mathcal{B}(\tau^- \rightarrow \mu^- \mu^+ \mu^-)$$

$$= \mathcal{B}(D_s^- \rightarrow \phi(\mu^+ \mu^-) \pi^-) \times \frac{f_\tau^{D_s}}{\mathcal{B}(D_s^- \rightarrow \tau^- \bar{\nu}_\tau)} \times \frac{\epsilon_{\text{cal}}^{\text{REC\&SEL}}}{\epsilon_{\text{sig}}^{\text{REC\&SEL}}} \times \frac{\epsilon_{\text{cal}}^{\text{TRIG}}}{\epsilon_{\text{sig}}^{\text{TRIG}}} \times \frac{N_{\text{sig}}}{N_{\text{cal}}}$$

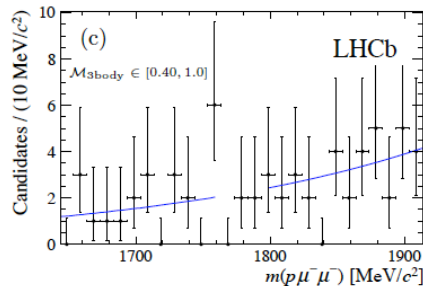
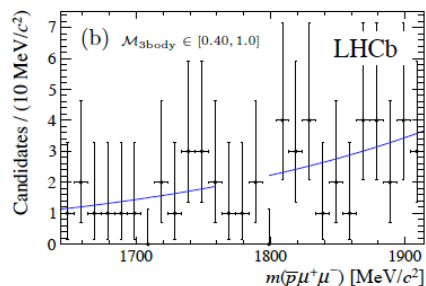


LHCb 90(95)%CL Limits

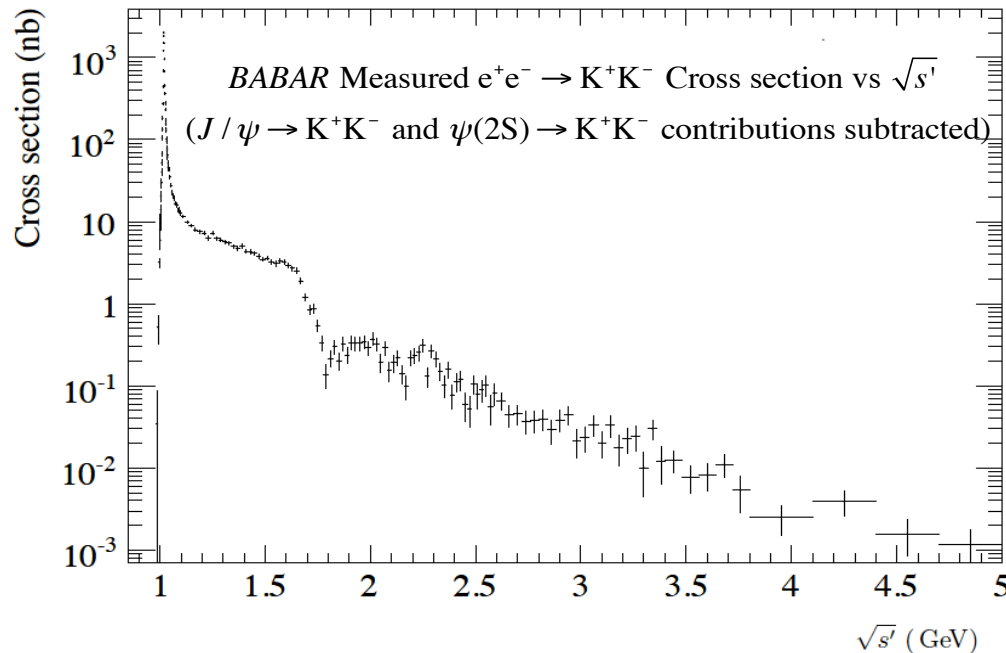
$$\mathcal{B}(\tau^- \rightarrow \mu^- \mu^+ \mu^-) < 8.0 \text{ (9.8)} \times 10^{-8}$$

$$\mathcal{B}(\tau^- \rightarrow \bar{p} \mu^+ \mu^-) < 3.3 \text{ (4.3)} \times 10^{-7}$$

$$\mathcal{B}(\tau^- \rightarrow p \mu^- \mu^-) < 4.4 \text{ (5.7)} \times 10^{-7}$$



# Precision Cross Section of $e^+e^- \rightarrow K^+K^-(\gamma)$ *BABAR*, submitted to PRD arXiv 1306.3600



$e^+e^- \rightarrow \text{hadrons}$  cross section related to  $a_\mu \equiv \frac{(g-2)_\mu}{2}$   
 through dispersion relation:

$$a_\mu^{\text{had,LO}} = \frac{1}{4\pi^3} \int_{m_{\pi^0}^2}^{\infty} ds K(s) \sigma_{e^+e^- \rightarrow \text{hadrons}}(s)$$

Davier *et al* Eur.Phys.J. C71 (2011) 1515

$$a_\mu^{\text{had,LO}} = (692.3 \pm 4.2) \times 10^{-10} \text{ - without BABAR } K^+K^-$$

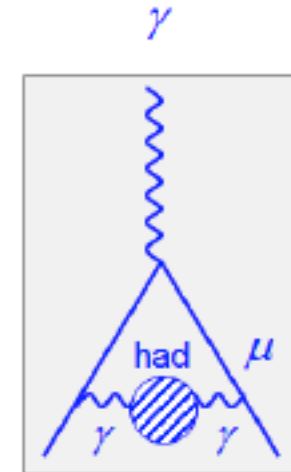
$$a_\mu^{\text{SM}} - a_\mu^{\text{Exp}} = (-28.7 \pm 8.0) \times 10^{-10}$$

$$a_\mu^{\text{KK,LO}} = (22.93 \pm 0.18_{\text{STAT}} \pm 0.22_{\text{SYST}} \pm 0.03_{\text{VP}}) \times 10^{-10}$$

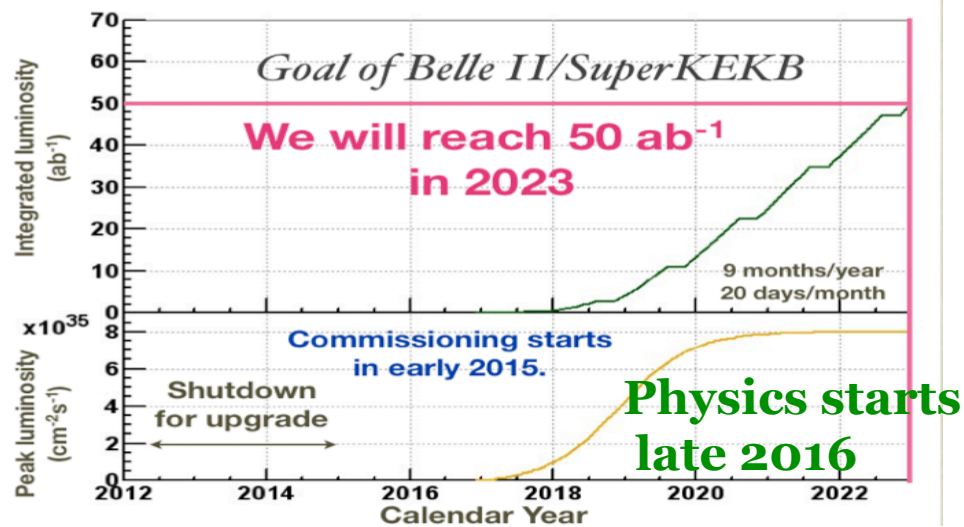
contribution from threshold to 1.8GeV

$$a_\mu^{\text{KK,LO}} = (21.63 \pm 0.27_{\text{STAT}} \pm 0.68_{\text{SYST}}) \times 10^{-10} \text{ - non-BABAR}$$

contribution from threshold to 1.8GeV



# Belle II at SuperKEKB



## Machine design parameters



parameters		KEKB		SuperKEKB		units
		LER	HER	LER	HER	
Beam energy	E <sub>b</sub>	3.5	8	4	7	GeV
Half crossing angle	φ	11		41.5		mrad
Horizontal emittance	ε <sub>x</sub>	18	24	3.2	5.0	nm
Emittance ratio	κ	0.88	0.66	0.27	0.25	%
Beta functions at IP	β <sub>x</sub> <sup>*</sup> /β <sub>y</sub> <sup>*</sup>	1200/5.9		32/0.27	25/0.31	mm
Beam currents	I <sub>b</sub>	1.64	1.19	3.60	2.60	A
beam-beam parameter	ξ <sub>y</sub>	0.129	0.090	0.0886	0.0830	
<b>Luminosity</b>	<b>L</b>	<b>2.1 x 10<sup>34</sup></b>		<b>8 x 10<sup>35</sup></b>		<b>cm<sup>-2</sup>s<sup>-1</sup></b>

- **Small beam size & high current** to increase luminosity
- **Large crossing angle**
- **Change beam energies** to solve the problem of LER short lifetime

## Physics Programme

- Test CKM at 1% level
  - CPV in B decays from new physics (non-CKM)
- B-recoil technique for  $B \rightarrow K^{(*)} \ell^+ \ell^-$ ,  $B \rightarrow \tau \nu$ ,  $B \rightarrow D^{(*)} \tau \nu$
- $\tau$  physics: lepton flavour violation, g-2, EDM, CPV,  $|V_{us}|$ ...
- Charm: mixing, CPV,...
- Many other topics:
  - $\Upsilon(5S)$  physics, , ISR radiative return, spectroscopy, Dark Sector probe, low mass Higgs...
- Physics motivation is independent of LHC
  - If LHC finds NP, precision flavour input essential
  - If LHC finds no NP, high statistics B and  $\tau$  decays are unique way of probing >TeV scale physics

**Belle II and LHCb (and ATLAS & CMS) are Complementary**

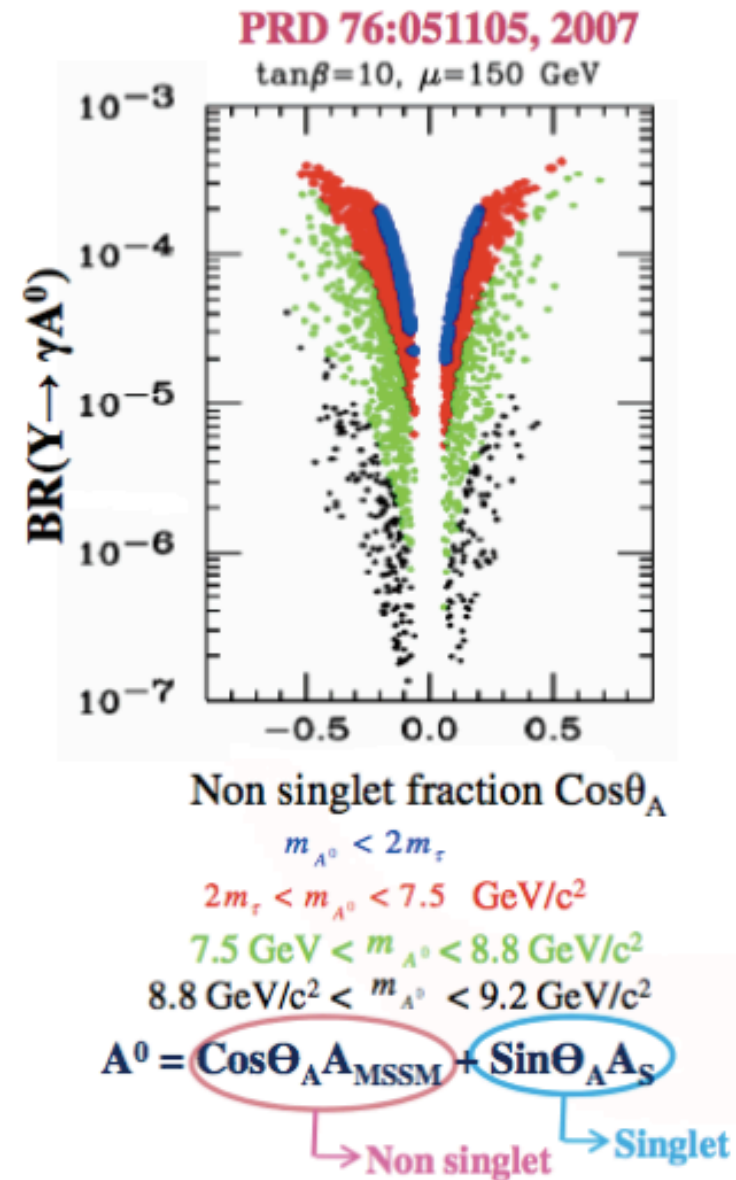
# Summary

- Belle and *BABAR* are continuing to publish
  - Completing Physics of the B-Factories Book summarizing the papers currently published by both collaborations
  - Completing the CKM program but also going into new areas – e.g. T-violation; light Higgs searches, Dark Sector searches
  - CKM is generally describing the data well
- $3.4\sigma$  tension with SM in *BABAR*  $B \rightarrow D^{(*)} \tau \nu$  decays, earlier published Belle results see similar hints
  - eagerly awaiting new analysis on Belle full data set
- Looking forward to future data from Belle II at SuperKEKB and LHCb

# Additional Slides

# NMSSM Parameter Space

- $\text{BF}(\Upsilon(1S) \rightarrow \gamma A^0)$  depends on non-singlet fraction
- High mass Higgs very difficult to exclude

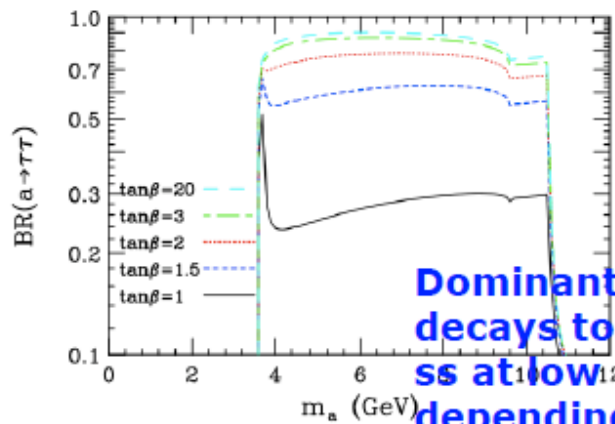




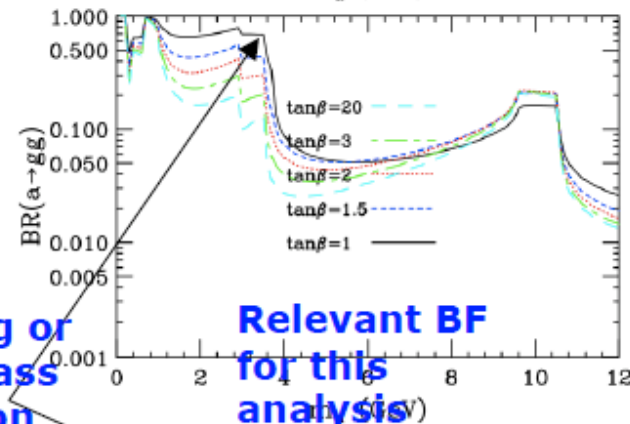
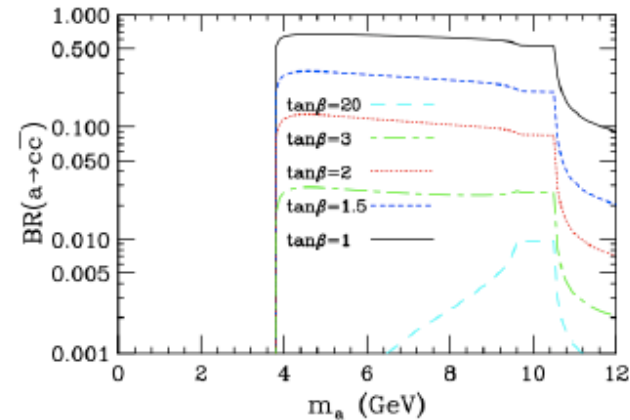
# Higgs Branching Fractions

$$B(A^0 \rightarrow f\bar{f}) \propto m_f^2 / \tan^2 \beta \quad \text{up-type fermions}$$

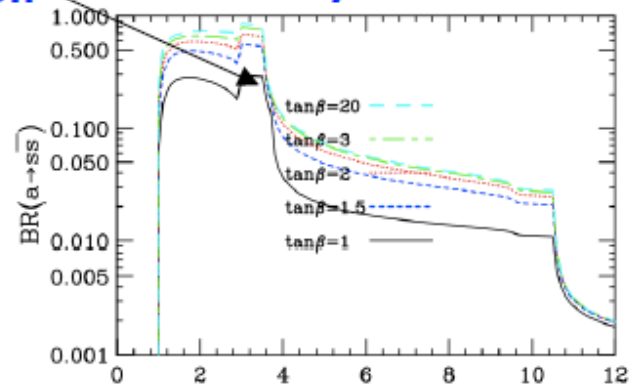
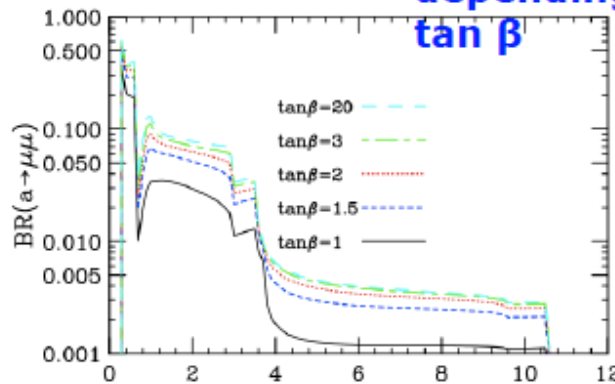
$$B(A^0 \rightarrow f\bar{f}) \propto m_f^2 \tan^2 \beta \quad \text{down-type fermions}$$



Dominantly  
decays to  $gg$  or  
 $ss$  at low mass  
depending on  
 $\tan\beta$



Relevant BF  
for this  
analysis



Channel	$a_{\mu}^{\text{had},LO} [10^{-10}]$	$\Delta\alpha_{\text{had}}(M_Z^2) [10^{-4}]$
$\pi^0\gamma$	$4.42 \pm 0.08 \pm 0.13 \pm 0.12$	$0.36 \pm 0.01 \pm 0.01 \pm 0.01$
$\eta\gamma$	$0.64 \pm 0.02 \pm 0.01 \pm 0.01$	$0.08 \pm 0.00 \pm 0.00 \pm 0.00$
$\pi^+\pi^-$	$507.80 \pm 1.22 \pm 2.50 \pm 0.56$	$34.43 \pm 0.07 \pm 0.17 \pm 0.04$
$\pi^+\pi^-\pi^0$	$46.00 \pm 0.42 \pm 1.03 \pm 0.98$	$4.58 \pm 0.04 \pm 0.11 \pm 0.09$
$2\pi^+2\pi^-$	$13.35 \pm 0.10 \pm 0.43 \pm 0.29$	$3.49 \pm 0.03 \pm 0.12 \pm 0.08$
$\pi^+\pi^-2\pi^0$	$18.01 \pm 0.14 \pm 1.17 \pm 0.40$	$4.43 \pm 0.03 \pm 0.29 \pm 0.10$
$2\pi^+2\pi^-\pi^0$ ( $\eta$ excl.)	$0.72 \pm 0.04 \pm 0.07 \pm 0.03$	$0.22 \pm 0.01 \pm 0.02 \pm 0.01$
$\pi^+\pi^-3\pi^0$ ( $\eta$ excl., from isospin)	$0.36 \pm 0.02 \pm 0.03 \pm 0.01$	$0.11 \pm 0.01 \pm 0.01 \pm 0.00$
$3\pi^+3\pi^-$	$0.12 \pm 0.01 \pm 0.01 \pm 0.00$	$0.04 \pm 0.00 \pm 0.00 \pm 0.00$
$2\pi^+2\pi^-2\pi^0$ ( $\eta$ excl.)	$0.70 \pm 0.05 \pm 0.04 \pm 0.09$	$0.25 \pm 0.02 \pm 0.02 \pm 0.03$
$\pi^+\pi^-4\pi^0$ ( $\eta$ excl., from isospin)	$0.11 \pm 0.01 \pm 0.11 \pm 0.00$	$0.04 \pm 0.00 \pm 0.04 \pm 0.00$
$\eta\pi^+\pi^-$	$1.15 \pm 0.06 \pm 0.08 \pm 0.03$	$0.33 \pm 0.02 \pm 0.02 \pm 0.01$
$\eta\omega$	$0.47 \pm 0.04 \pm 0.00 \pm 0.05$	$0.15 \pm 0.01 \pm 0.00 \pm 0.02$
$\eta 2\pi^+ 2\pi^-$	$0.02 \pm 0.01 \pm 0.00 \pm 0.00$	$0.01 \pm 0.00 \pm 0.00 \pm 0.00$
$\eta\pi^+\pi^-2\pi^0$ (estimated)	$0.02 \pm 0.01 \pm 0.01 \pm 0.00$	$0.01 \pm 0.00 \pm 0.00 \pm 0.00$
$\omega\pi^0$ ( $\omega \rightarrow \pi^0\gamma$ )	$0.89 \pm 0.02 \pm 0.06 \pm 0.02$	$0.18 \pm 0.00 \pm 0.02 \pm 0.00$
$\omega\pi^+\pi^-, \omega 2\pi^0$ ( $\omega \rightarrow \pi^0\gamma$ )	$0.08 \pm 0.00 \pm 0.01 \pm 0.00$	$0.03 \pm 0.00 \pm 0.00 \pm 0.00$
$\omega$ (non- $3\pi, \pi\gamma, \eta\gamma$ )	$0.36 \pm 0.00 \pm 0.01 \pm 0.00$	$0.03 \pm 0.00 \pm 0.00 \pm 0.00$
$K^+K^-$	$21.63 \pm 0.27 \pm 0.58 \pm 0.36$	$3.13 \pm 0.04 \pm 0.08 \pm 0.05$
$K_S^0K_L^0$	$12.96 \pm 0.18 \pm 0.25 \pm 0.24$	$1.75 \pm 0.02 \pm 0.03 \pm 0.03$
$\phi$ (non- $K\bar{K}, 3\pi, \pi\gamma, \eta\gamma$ )	$0.05 \pm 0.00 \pm 0.00 \pm 0.00$	$0.01 \pm 0.00 \pm 0.00 \pm 0.00$
$K\bar{K}\pi$ (partly from isospin)	$2.39 \pm 0.07 \pm 0.12 \pm 0.08$	$0.76 \pm 0.02 \pm 0.04 \pm 0.02$
$K\bar{K}2\pi$ (partly from isospin)	$1.35 \pm 0.09 \pm 0.38 \pm 0.03$	$0.48 \pm 0.03 \pm 0.14 \pm 0.01$
$K\bar{K}3\pi$ (partly from isospin)	$-0.03 \pm 0.01 \pm 0.02 \pm 0.00$	$-0.01 \pm 0.00 \pm 0.01 \pm 0.00$
$\phi\eta$	$0.36 \pm 0.02 \pm 0.02 \pm 0.01$	$0.13 \pm 0.01 \pm 0.01 \pm 0.00$
$\omega K\bar{K}$ ( $\omega \rightarrow \pi^0\gamma$ )	$0.00 \pm 0.00 \pm 0.00 \pm 0.00$	$0.00 \pm 0.00 \pm 0.00 \pm 0.00$
$J/\psi$ (Breit-Wigner integral)	$6.22 \pm 0.16$	$7.03 \pm 0.18$
$\psi(2S)$ (Breit-Wigner integral)	$1.57 \pm 0.03$	$2.50 \pm 0.04$
$R_{\text{data}} [3.7 - 5.0 \text{ GeV}]$	$7.29 \pm 0.05 \pm 0.30 \pm 0.00$	$15.79 \pm 0.12 \pm 0.66 \pm 0.00$
$R_{\text{QCD}} [1.8 - 3.7 \text{ GeV}]_{uds}$	$33.45 \pm 0.28$	$24.27 \pm 0.19$
$R_{\text{QCD}} [5.0 - 9.3 \text{ GeV}]_{udsc}$	$6.86 \pm 0.04$	$34.89 \pm 0.18$
$R_{\text{QCD}} [9.3 - 12.0 \text{ GeV}]_{udscb}$	$1.21 \pm 0.01$	$15.56 \pm 0.04$
$R_{\text{QCD}} [12.0 - 40.0 \text{ GeV}]_{udscb}$	$1.64 \pm 0.01$	$77.94 \pm 0.12$
$R_{\text{QCD}} [> 40.0 \text{ GeV}]_{udscb}$	$0.16 \pm 0.00$	$42.70 \pm 0.06$
$R_{\text{QCD}} [> 40.0 \text{ GeV}]_t$	$0.00 \pm 0.00$	$-0.72 \pm 0.01$
<b>Sum</b>	$692.3 \pm 1.4 \pm 3.1 \pm 2.4 \pm 0.2_{\psi} \pm 0.3_{\text{QCD}}$	$274.97 \pm 0.17 \pm 0.78 \pm 0.37 \pm 0.18_{\psi} \pm 0.52_{\text{QCD}}$

Contributions to  $a_{\mu}^{\text{had},LO}$  and  $\Delta\alpha_{\text{had}}(M_Z^2)$   
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For most of these channels, BaBar provides  
 the most precise measurements from  
 ISR studies

