



# LE ROLE DES AIMANTS DANS LES ACCELERATEURS DES PARTICULES

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# CONTENTS



- Units for energy: TeV, J
- Lorentz force: two ways of accelerating
  - Linear
  - Circular
- Synchrotrons
- Stability and quadrupoles
  - Tune



# ENERGY



- Different units to express the same idea: ability of making a work
- Physics: Joule = Force \* displacement [N m]  
ex: at fitness rising 40 kg of 1 m

$$L = m g h = 40 * 9.8 * 1 = 400 \text{ J}$$

- Power: Joule/s = Watt

Ex: 1 series of 12 in half a minute

$$P = L / t = 400 * 12 / 30 = 160 \text{ W}$$



- Typical power of a normal human being ~150 W

# ENERGY



- Different units to express the same idea: ability of making a work
- High energy physics: ElectronVolt = e charge \* 1 volt [eV]  
the energy acquired by one electron (or proton)  
accelerated by a potential of 1 volt

$$L = q V \quad 1 \text{ eV} = 1.6 \times 10^{-19} \text{ J}$$

- $1 \text{ KeV} = 10^3 \text{ eV} = 1.6 \times 10^{-16} \text{ J}$
- $1 \text{ MeV} = 10^6 \text{ eV} = 1.6 \times 10^{-13} \text{ J}$
- $1 \text{ GeV} = 10^9 \text{ eV} = 1.6 \times 10^{-10} \text{ J}$
- $1 \text{ TeV} = 10^{12} \text{ eV} = 1.6 \times 10^{-7} \text{ J}$

Looks very small but we put all energy just in ONE particle

# ENERGY



- $1 \text{ TeV} = 10^{12} \text{ eV} = 1.6 \times 10^{-7} \text{ J}$ 
  - Looks very small but we put all energy just in ONE particle
  - $7 \text{ TeV} = 7 \times 10^{12} \text{ eV} = 1.1 \times 10^{-6} \text{ J}$
- We have about 110 billions of protons per bunch, with 2800 bunches per beam, so 310 000 billions of protons
  - Looks a lot, but 1 g of matter has about  $\sim 10^{23}$  protons
- Energy of one beam  $310 \times 10^{12} \times 1.1 \times 10^{-6} \text{ J} = 340 \text{ MJ}$
- Energy stored in the magnetic field
  - Energy density:  $B^2/2\mu$
  - For a LHC dipole 7 T, 28 mm aperture radius
    - Area:  $0.045 \text{ m}^2$  (two apertures)
    - Stored energy: 7 MJ for one dipole (both apertures), 8400 MJ all LHC
  - So energy of the magnetic field is much larger than energy of the beam

- Energy stored in the LHC
  - 8400 MJ in the LHC dipoles
  - 340 MJ per beam
- Assuming that the cycling time is one day, power is
  - $8800 / 24 / 3600 \text{ W} = 100 \text{ kW}$
  - Consumption power with all accelerators on is about 200 MW - no surprise the machine is not at all effective

- Different units to express the same idea: ability of making a work
  - For food we use calories (in the communist era, they used kJ, it was much simpler ...)
  - $1 \text{ cal} = 4.18 \text{ J}$ 
    - Just to add confusion, what you see on food box is NOT calories but kcal!
- [thanks to Paolo for telling me, I was lost]
- So a big Mac is not 500 cal but  $500 \text{ kcal} = 2 \text{ MJ}$
- So LHC beam has the energy of 170 BigMac concentrated in a 300 000 billion of protons
- Human need per day:  $2000 \text{ kcal} = 4 \text{ BigMac} = 8 \text{ MJ}$ 
  - Power estimate:  $8 \cdot 10^6 / 24 / 3600 = 92 \text{ W}$  (that fit with previous estimate)



# ENERGY



LHC beam energy [A. Warhol, 1986]

E. Todesco - Superconducting magnets 8



# LORENTZ FORCE



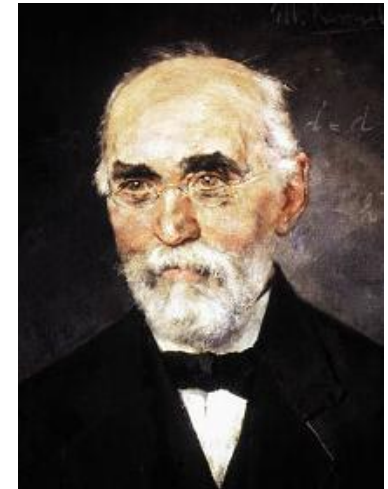
- How to accelerate particles?
- Lorentz force acts on charged particles
  - Protons, electrons, muons, ... but not neutrons, neutrinos
- Electrical field accelerates particles

$$\vec{F} = e\vec{E}$$

- Magnetic field bends particles

$$\vec{F} = e\vec{v} \times \vec{B}$$

- Very strange force: does not increase velocity but changes direction



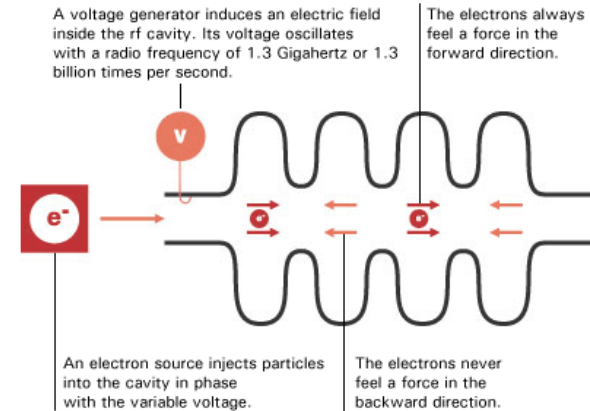
Hendrik Antoon Lorentz, Dutch  
(18 July 1853 – 4 February 1928),  
painted by Menso Kamerlingh Onnes,  
brother of Heinke, Nobel prize for  
discovery in superconductivity

# LINEAR AND CIRCULAR



- First idea: using electrical field to increase energy, like a gun

$$\vec{F} = e\vec{E}$$



- Energy proportional to length of the machine and to the electrical field
- Radiofrequency technology – present limit to  $\sim 35$  MV/m (ILC)
  - So, 10 km of machine accelerates to  $\sim 350$  GeV
- CLIC aims at factor 3 larger 100 MV/m

# LINEAR AND CIRCULAR



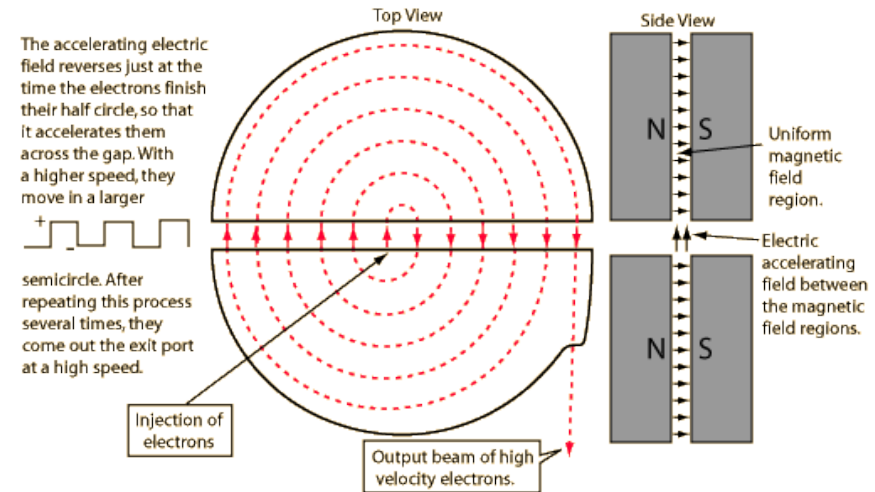
- Alternative idea: using magnetic field to bend particles, one small section accelerates and the beams goes back

$$\vec{F} = e\vec{E} \quad \vec{F} = e\vec{v} \times \vec{B}$$

- Main relation

$$E[GeV] = 0.3 \times B[T] \times \rho[m]$$

Constant ↙



Cyclotron idea [1932, LBL]

- Energy (momentum  $p$ ) proportional to curvature radius  $\rho$  and magnetic field  $B$ 
  - If the field is fixed (permanent magnets), energy increases, radius of the orbit increases and finally particles escape the cyclotron

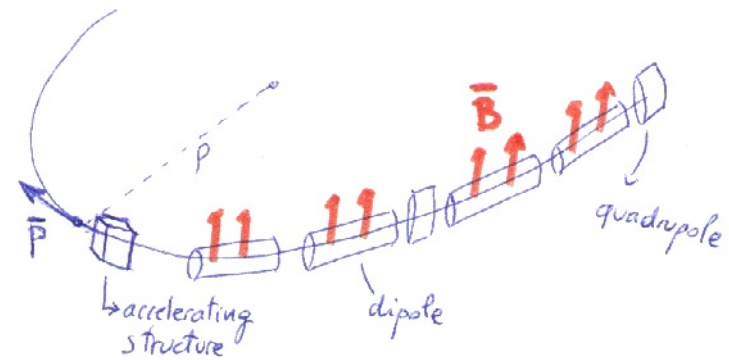
# PRINCIPLES OF A SYNCHROTRON



- Idea: use electromagnet, increase field with energy to keep the same orbit
  - First for electrons McMillan, 1945
  - First for protons E. Oliphant, 1952

$$E[\text{GeV}] = 0.3 \times B[\text{T}] \times \rho[\text{m}]$$

↑                      ↑                      ↓  
Constant



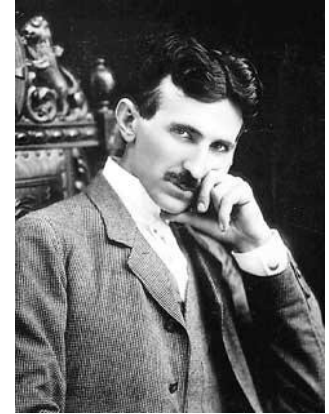
- Limits to the increase in energy
  - The **maximum field of the dipoles** (proton machines)
    - This is why high field magnets are important to get high energies!
    - This is a strange accelerator since most of it does not increase energy, but only bends ...

# TESLA INTERLUDE



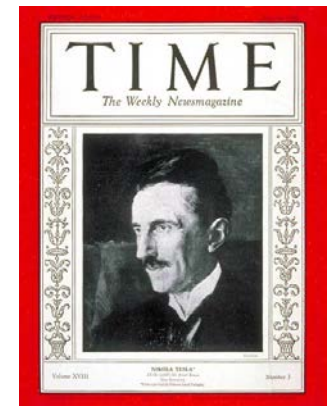
## Nikolai Tesla (10 July 1856 - 7 January 1943)

- Born at midnight during an electrical storm in Smiljan near Gospić (now Croatia)
- Son of an orthodox priest
- A national hero in Serbia – but also in the other republics of ex-Yugoslavia



## Career

- Polytechnic in Gratz (Austria) and Prague
- Emigrated in the States in 1884
- Electrical engineer
- Inventor of the alternating current induction motor (1887)
- Author of 250 patents

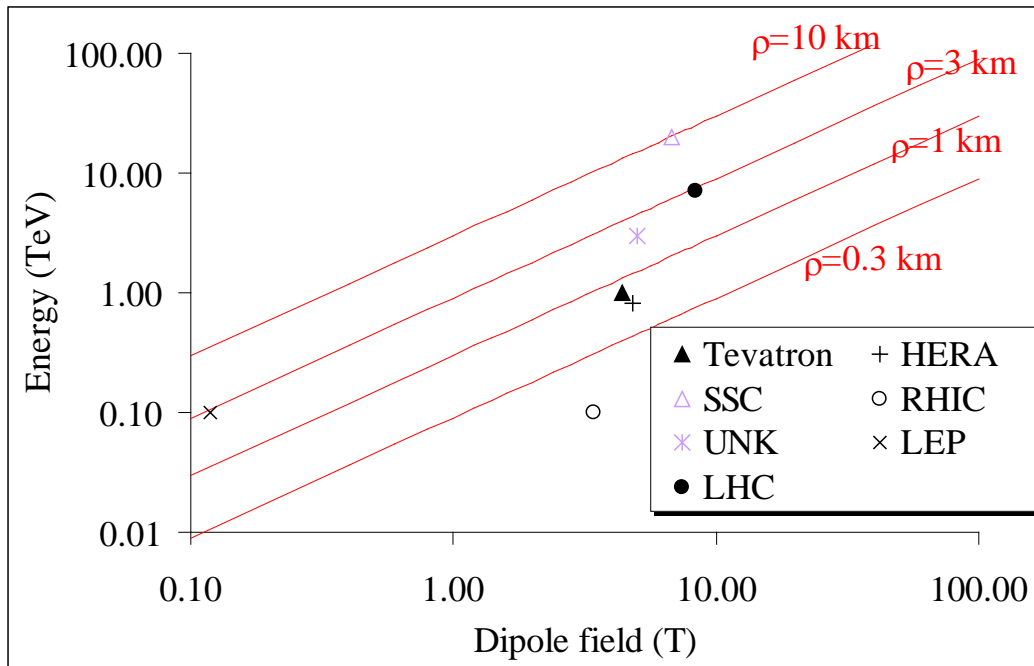


A rather strange character, a lot of legends on him ...

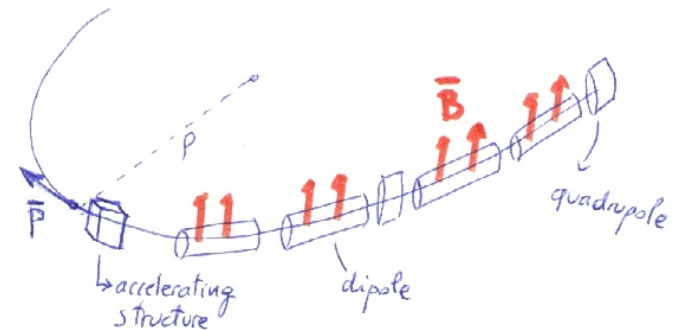
# PRINCIPLES OF A SYNCHROTRON



- Relation momentum-magnetic field-orbit radius
  - Having 8 T magnets, we need 3 Km curvature radius to have 7 TeV
  - Present limit of technology 8 T (LHC after LS1)
  - Future: to 11-12 T (11 T and QXF for Hi Lumi 2016-2022)
  - Future: to 15-20 T (~2030)



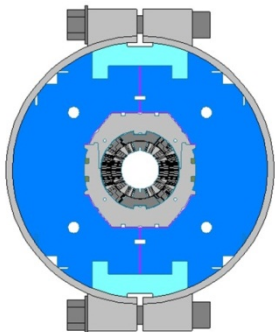
$$E[\text{GeV}] = 0.3 \times B[\text{T}] \times \rho[\text{m}]$$



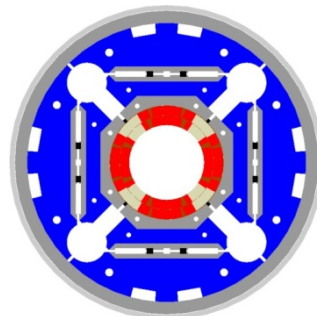
# PRINCIPLES OF A SYNCHROTRON



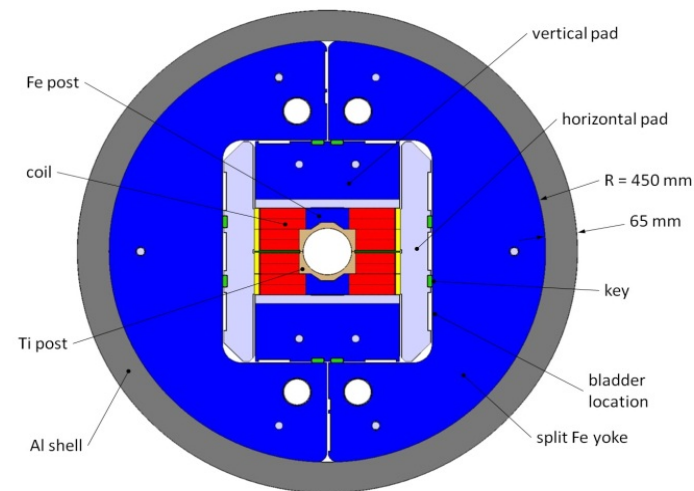
- The path towards high fields
  - Present limit of technology 8 T (LHC after LS1)
  - World record in accelerator magnet 13.8 T (LBL HD2)
  - Near future: towards 11-13 T with Nb<sub>3</sub>Sn
    - 11 T dipole
    - 12 T peak field in QXF insertion quadrupole
    - 13 T Fresca2 (large aperture dipole for test station)
  - Mid-term future: 15-20 T with Nb<sub>3</sub>Sn and HTS



11 T [M. Karppinen et al.]

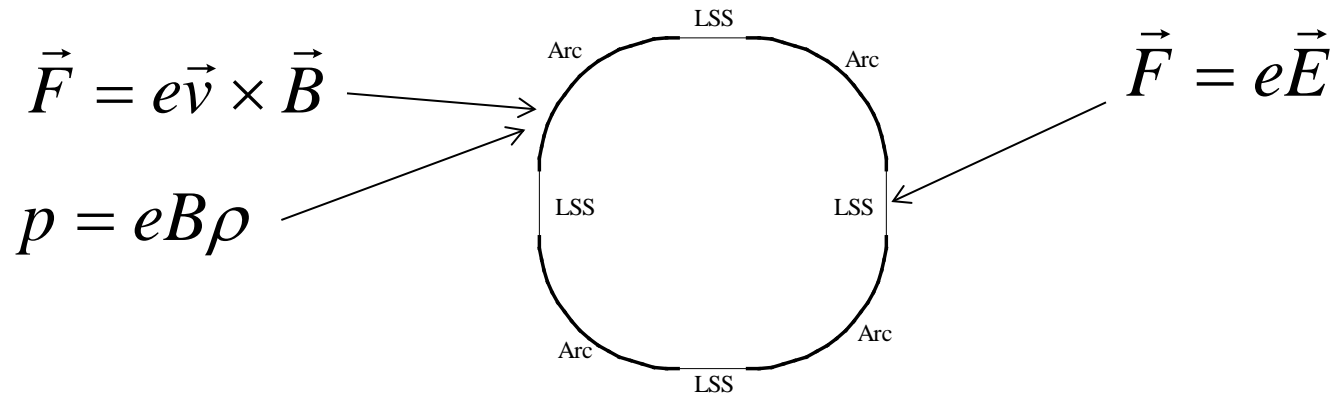


QXF [P. Ferracin et al.]



Fresca2 [G. De Rijk et al.]

# PRINCIPLES OF A SYNCHROTRON



- Colliders: two beams with opposite momentum collide
  - This **doubles the energy** !
  - **One pipe** if particles collide their antiparticles (LEP, Tevatron)
  - Otherwise, **two pipes** (ISR, RHIC, HERA, LHC)

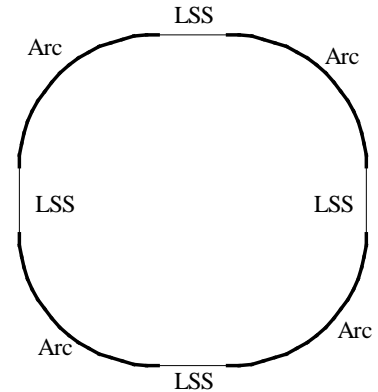


# PRINCIPLES OF A SYNCHROTRON



- **The arcs:** region where the beam is bent

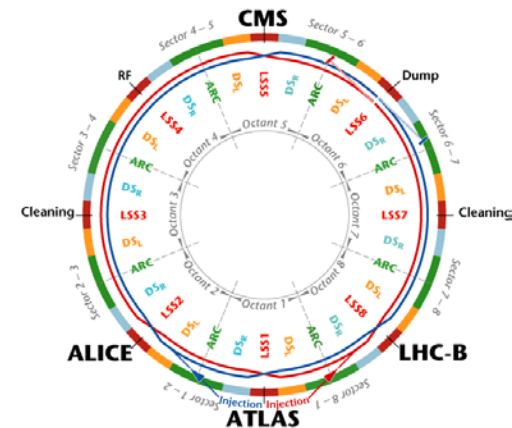
- Dipoles for **bending**
- Quadrupoles for **focusing**
- Correctors



A schematic view of a synchrotron

- **Long straight sections (LSS)**

- **Interaction regions (IR)** where the experiments are housed
  - Quadrupoles for strong focusing in interaction point
  - Dipoles for beam crossing in two-ring machines
- Regions for other services
  - Beam injection (dipole kickers)
  - Accelerating structure (RF cavities)
  - Beam dump (dipole kickers)
  - Beam cleaning (collimators)

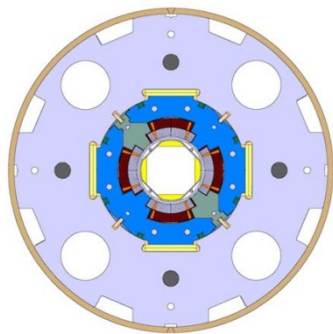
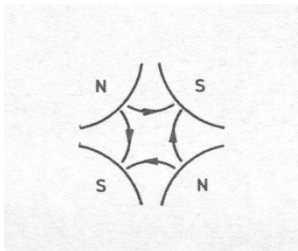


The lay-out of the LHC

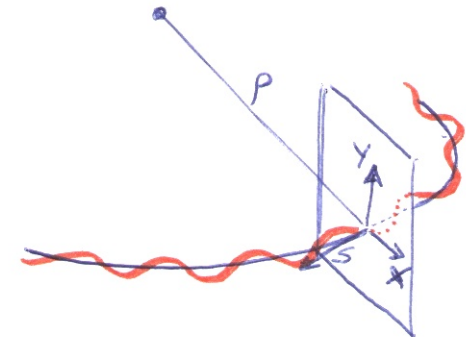
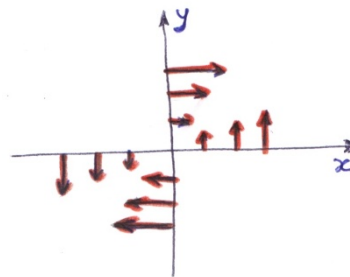
# LINEAR STABILITY AND QUADRUPOLES



- LHC case:
  - Bending radius is 2.8 km
  - Error of 1% in the magnetic field changes the orbit of 2.8 m, but the beam tube is 100 times smaller (28 mm radius !)
    - We would need a huge precision in our magnets to have the particles in the beam tube
- You need a force to bring back the particle to the center of the tube: given by the quadrupole
  - If the particle is in the center, no field – otherwise the quadrupolar field brings it back



MQXC [G. Kirby, et al.]



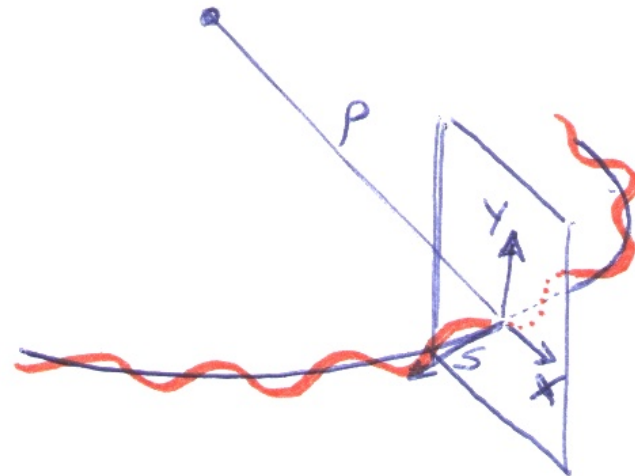
# LINEAR STABILITY AND QUADRUPOLES



- The oscillations of the beam around the central orbit are called betatron oscillations
  - The number of oscillations in one turn of the machine is called tune
  - For the LHC tune is 59.28, 63.31
    - Please note these numbers are not integers
    - Resonances !! Any imperfection can cause instability if the effect is resonant – this is why we need correctors



Resonant forcing of harmonic oscillator

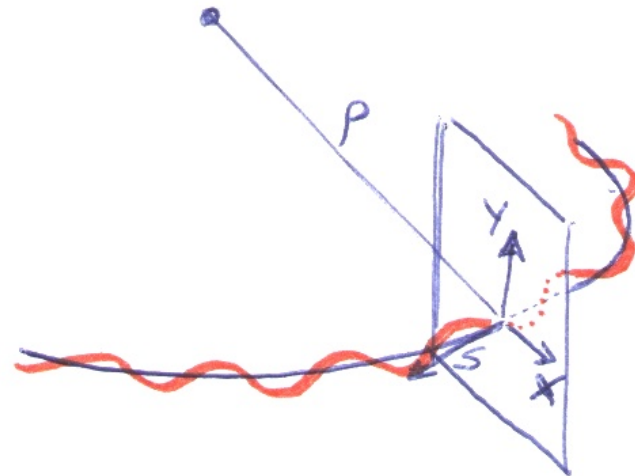
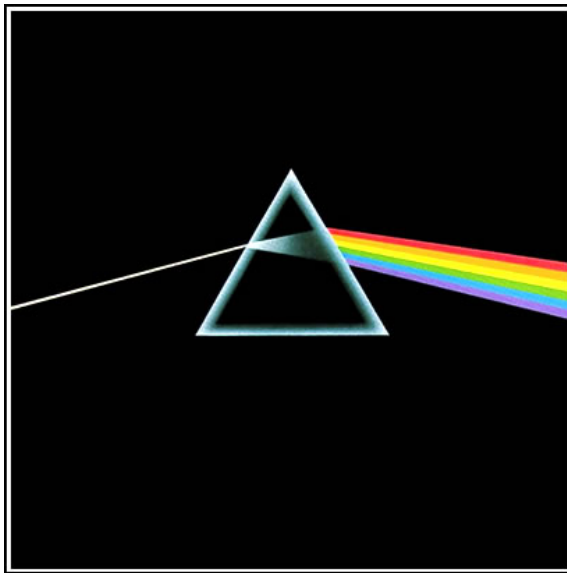


Betatronic oscillations

# CHROMATICITY AND SEXTUPOLES



- The tune of the machine should not cross resonances
  - Little variation of energy produce variations of tune (chromaticity) – analogy with optics
    - Typically in the LHC protons have different energy by 1 per mil
  - A sextupole can correct and minimize this effect
  - And so on ... we have up to dodecapole in the LHC !!



# SUMMARY



- One can accelerate charged particle thanks to Lorentz force
- Synchrotrons are compact machines to get very large energies
  - A lot of energy in a few particles
  - The accelerating part is a small fraction, most of the work is the magnetic field to bring the beam back
- Limits to circular machines: magnets 8 T
  - Higher energies can be obtained by larger machines or higher fields
- We push towards 11-12 T to break the Nb-Ti barrier
- We aim at 15-20 T in 10 years from now
  
- Quadrupoles are needed to focus the beam
  - High order correctors to stabilize it