# Heavy Ion Physics and Non-Perturbative Renormalization Group Equations

Stefan Flörchinger

CERN Theory Retreat 2013, Les Houches, 07/11/2012

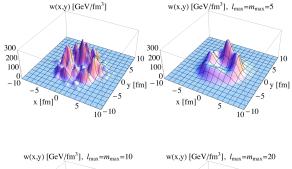
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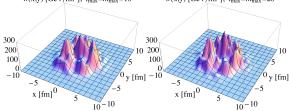
What fluctuations are interesting and why?

- Initial hydro fluctuations: Event-by-event perturbations around the average of hydrodynamical fields at time τ<sub>0</sub>:
  - $\bullet\,$  energy density  $\epsilon$
  - $\bullet~{\rm fluid}$  velocity  $u^{\mu}$
  - shear stress  $\pi^{\mu\nu}$
  - more general also: baryon number density  $n_B$ , electric charge density, electromagnetic fields, ...
- measure for deviations from equilibrium
- contain interesting information from early times
- governed by universal evolution equations
- can be used to constrain thermodynamic and transport properties

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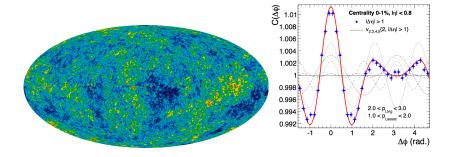
#### Transverse density from Glauber model





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## Similarities to cosmic microwave background



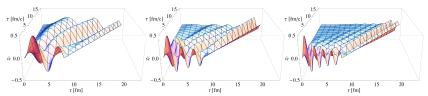
- fluctuation spectrum contains info from early times
- many numbers can be measured and compared to theory
- can lead to detailed understanding of evolution and properties
- could trigger precision era in heavy ion physics

Perturbations in hydrodynamics

• Hydrodynamic description

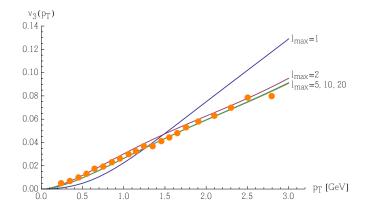
$$D\epsilon + (\epsilon + p)\partial_{\mu}u^{\mu} - u_{\nu}\partial_{\mu}\pi^{\mu\nu} = 0$$
$$(\epsilon + p)Du^{\alpha} + \Delta^{\alpha\beta}\partial_{\beta} p + \Delta^{\alpha}{}_{\nu}\partial_{\mu}\pi^{\mu\nu} = 0$$

- Develop perturbation theory in small fluctuations around smooth average fields:  $\epsilon = \bar{\epsilon} + \delta \epsilon$  etc.
- In spirit similar to treatment of fluctuations in cosmology.



## Harmonic flow coefficients for central collisions

Triangular flow for charged particles



Points: 2% most central collisions, ALICE [PRL 107, 032301 (2011)] Curves: Different maximal resolution  $l_{max}$ 

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#### Non-perturbative Renormalization Group Equations 1 Exact flow equation [S.F. and C. Wetterich, PLB 680, 371 (2011)]

$$\begin{split} \partial_k \Gamma_k[\phi] = & \frac{1}{2} \mathsf{STr} \left( \Gamma_k^{(2)}[\phi] + R_k \right)^{-1} \left( \partial_k R_k - R_k (\partial_k Q_k^{-1}) R_k \right) \\ & - \frac{1}{2} \Gamma_k^{(1)}[\phi] \left( \partial_k Q_k^{-1} \right) \ \Gamma_k^{(1)}[\phi] \end{split}$$

for a variant of the 1-PI or quantum effective action with

 $\lim_{k \to \Lambda} \Gamma_k[\phi] = S[\phi]$  $\lim_{k \to 0} \Gamma_k[\phi] = \Gamma[\phi]$ 

- $R_k$  is an infrared cutoff that is removed when  $k \to 0$
- Fluctuations are included step by step
- Differential formulation of functional integral
- $Q_k$  Implements k-dependent Hubbard-Stratonovich transformation

Non-perturbative Renormalization Group Equations 2

Conceptual topics I work on

- Analytic continuation of flow equations from Euclidean to Minkowski space
- Determination of real-time properties such as decay width and transport coefficients

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- Skale-dependent changes in the relevant degrees of freedom
- Composite fields / bound states

Applications of the formalism I work on

- Scalar O(N)-models
- Yukawa type theories
- Composite fermions