

CFD Simulations and Experimental Verification on Nucleate Pool Boiling of Liquid Nitrogen

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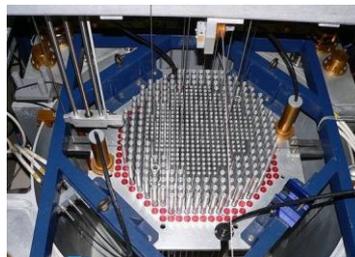
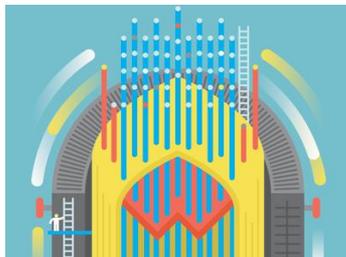
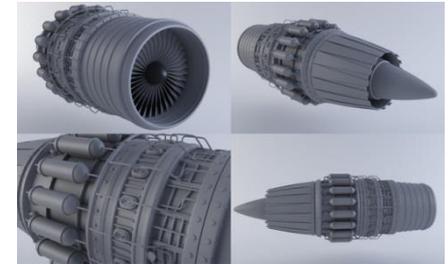
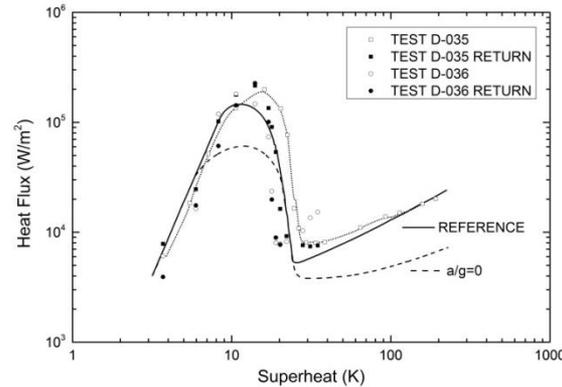
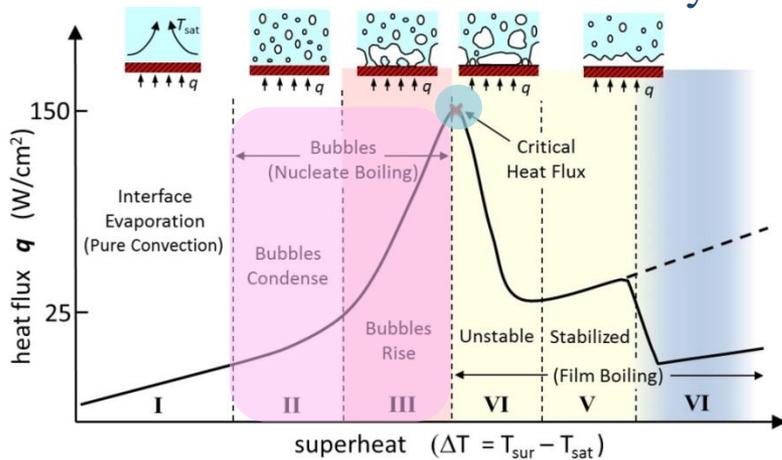
Supported by
National High-Tech Research & Development
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Stories of Boiling

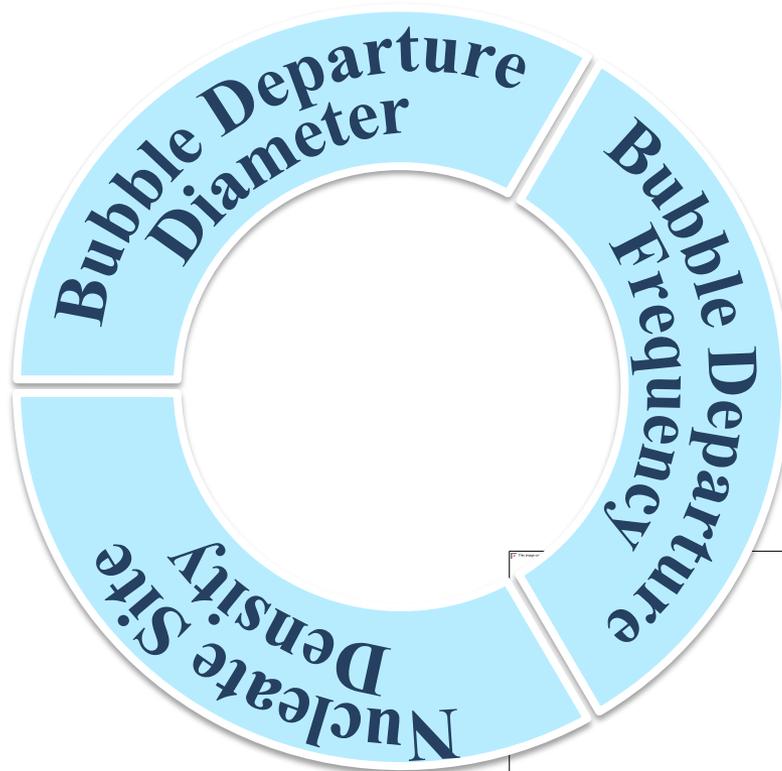
- ❑ Nucleate boiling is a useful and common way of heat transfer in mechanical industry.
- ❑ Bubbles **generated, merged, and coalesced** in the nucleate boiling region, leading to a complicated temperature and pressure field distribution.
- ❑ Experiments using cryogenic fluids are much more intricate and complicated than experiments conducted with common fluids.
- ❑ The UMich and NASA have already conducted profound boiling researches on LH_2 & LN_2 in 1970^[1]. They have formulated boiling curves under various boiling combinations. But they recorded **no photographs or micro bubble analysis**.



[1] Merte H, Laboratory. U O M H. Incipient and steady boiling of liquid nitrogen and liquid hydrogen under reduced gravity[EB/OL]. Heat Transfer Laboratory, University of Michigan, 1970.



State-of-the-art CORRELATIONS





State-of-the-art CORRELATIONS



Contributors	Correlations
Cole	$f = \left[\frac{4g(\rho_l - \rho_g)}{3D_b\rho_l} \right]^{0.5}$
Zuber	$f = \frac{0.59}{D_b} \left[\frac{\sigma g(\rho_l - \rho_g)}{\rho_l^2} \right]^{0.25}$
Kocamustafaogullari and Ishii	$f = \frac{1.18}{D_b} \left[\frac{\sigma g(\rho_l - \rho_g)}{\rho_l^2} \right]^{0.25}$
Hatton and Hall	$f = \frac{3}{\pi\eta_l} \left[\frac{16k_l\sigma T_{sat}}{(h_{fg}\rho_g)^2 D_b D_c} \right]^2$
Ivey	$f = 0.9 \left(\frac{g}{D_b} \right)^{0.5}$ for hydrodynamic region
	$f = 0.44 \left(\frac{g}{D_b^3} \right)^{0.25}$ for transition region
	$f = \frac{c}{D_b^2}$ for thermodynamic region
Stephan	$f = \frac{1}{\pi} \sqrt{\frac{g}{2D_b}} \left[1 + \frac{4\sigma}{D_b^2 \rho_g g} \right]^{0.5}$



State-of-the-art CORRELATIONS



Contributors	Correlations
Fritz	$D_b(D_{bF}) = 0.0208\phi \left[\frac{\sigma}{g(\rho_l - \rho_g)} \right]^{0.5}$
Zuber	$D_b = \left[\frac{6\sigma}{g(\rho_l - \rho_g)} \frac{k\Delta T_{sup}}{Q_w} \right]^{1/3}$
Han and Griffith	$D_b = 0.843\phi \left[\frac{2\sigma}{g(\rho_l - \rho_g)} \right]^{0.5}$
Cole and Shulman	$D_b = \left[\frac{\sigma}{g(\rho_l - \rho_g)} \right]^{0.5} P^{-1}$
Cole	$D_b = \phi \left[\frac{\sigma}{g(\rho_l - \rho_g)} \right]^{0.5} \frac{\rho_l C_{p,l} \Delta T_{sup}}{\rho_g h_{fg}}$
Cole and Rohsenow	$D_b = 1.5 \times 10^{-4} \left[\frac{\sigma}{g(\rho_l - \rho_g)} \right]^{0.5} \left(\frac{\rho_l C_{p,l} T_{sat}}{\rho_g h_{fg}} \right)^{1.25}$
Tolubinskiy and Kostanchuk	$D_b = D_{ref} \exp\left(-\frac{\Delta T_{sub}}{\Delta T_{ref,d}}\right)$
Ünal	$D_b = \frac{2.42 \times 10^{-5} p^{0.709} \alpha}{\sqrt{b\phi}}$ $\alpha = \frac{(Q_w - h_l \Delta T_{sub})^{1/3} k_l}{2C^{1/3} h_{fg} \sqrt{\pi k_l / \rho_l C_{p,l} \rho_g}} \sqrt{\frac{k_w \rho_w C_{p,w}}{k_l \rho_l C_{p,l}}}$ $C = \frac{h_{fg} \mu_l [C_{p,l} / (0.013 h_{fg} Pr^{1.7})]^3}{[\sigma / (\rho_l - \rho_g) g]^{0.5}}$ $b = \Delta T_{sub} / 2(1 - \rho_g / \rho_l)$ $\phi = \begin{cases} \left(\frac{u_l}{0.61}\right)^{0.47} & \text{for } u_l \geq 0.61 \text{ m/s} \\ 1.0 & \text{for } u_l < 0.61 \text{ m/s} \end{cases}$
Kocamustafaogullari and Ishii	$D_b = 0.0012 \left(\frac{\rho_l - \rho_g}{\rho_l} \right)^{0.9} D_{bF}$
Lee, et al	$D_d = 8437.5 \frac{\alpha_l^2 \rho_l}{\sigma} Ja^2$
Kim	$\sqrt{\frac{(\rho_l - \rho_v)}{\sigma}} D_d = 0.1649 Ja^{0.7}$

[1] Carey V P. Liquid-vapor phase-change phenomena : an introduction to the thermophysics of vaporization and condensation processes in heat transfer equipment[M]. Washington, D.C.:



State-of-the-art CORRELATIONS



Contributors	Correlations	
Cornwel and Brown	$N_a \sim T_{sup}^m$	m = 4.5
Lemmert and Chawla	$N_a = [n\Delta T_{sup}]^m$	n = 185, m = 1.805
Koncar et al.		n = 210, m = 1.805
Kurul and Podowski		n = 0.8×10^6 , $\Delta T_{refN} = 10$ K
Krepper et al.	$N_a = n \left[\frac{\Delta T_{sup}}{\Delta T_{refN}} \right]^m$	(Bartolomej et al. [31]) n = 3×10^7 (DEBORA 1-2 [33]) n = 5×10^6 (DEBORA 3-7 [33])
Kirichenko	$N_a = n \left[\frac{\rho_g h_{fg} \Delta T_{sup}}{\sigma T_{sat}} \right]^m$	n = 1×10^{-7} , m = 2, $P/P_{cr} \geq 0.04$ n = 6.25×10^{-6} , m = 3, $P/P_{cr} < 0.04$





State-of-the-art CORRELATIONS

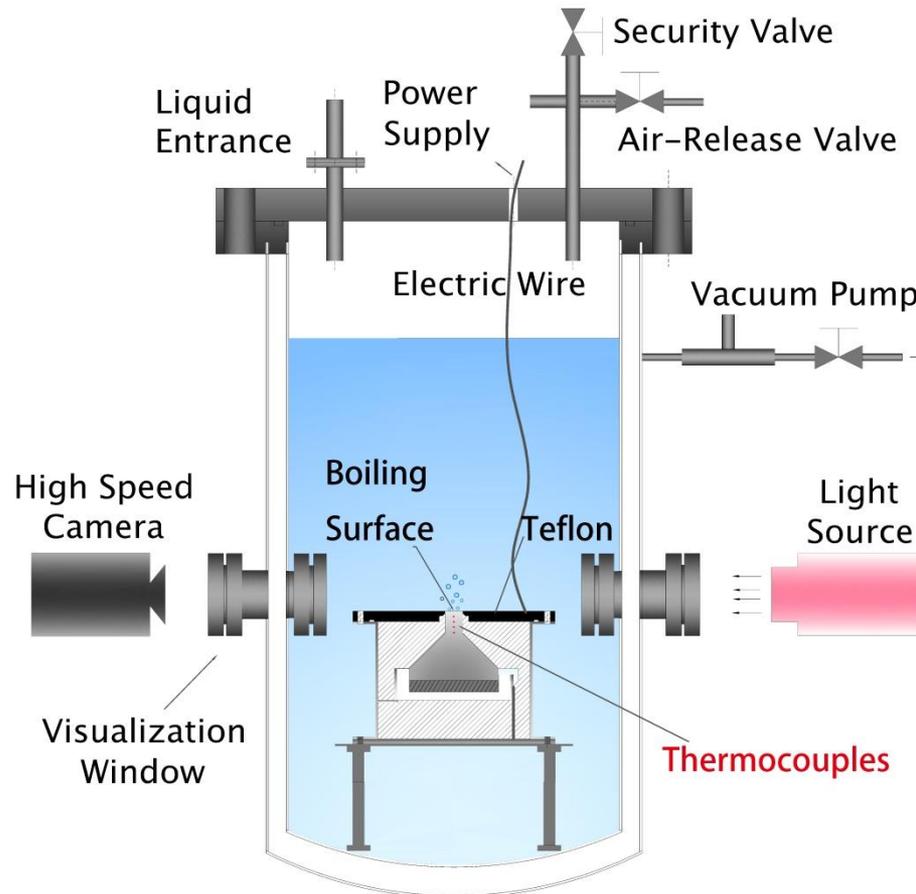


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- ❑ Mostly applied to water, organic fluids, and some common fluids only[1];
- ❑ Researches concerning cryogenic fluids such as He3, H2, and N2 lack enough experimental comparisons and verifications, accuracy can't be guaranteed;
- ❑ Researches on nucleate boiling of LN2 mainly focused on flow boiling in micro tube. It still remains blank in researches on bubble departure frequency and diameter.



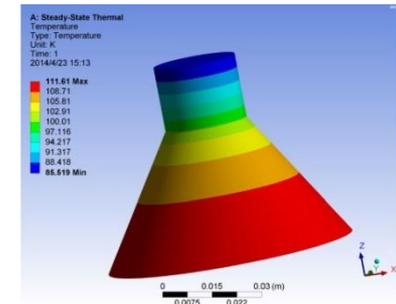
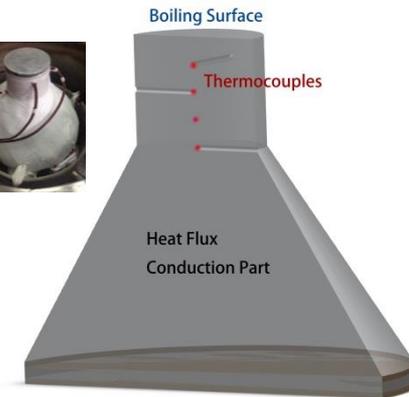
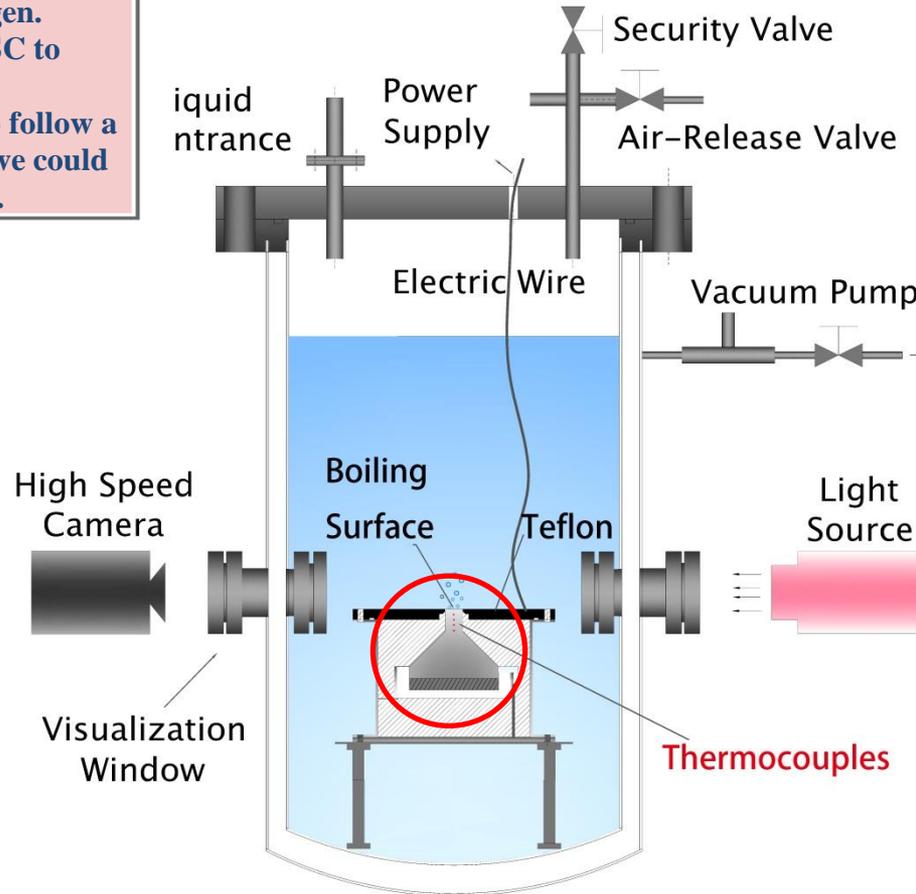
Experimental Setup





Experimental Setup

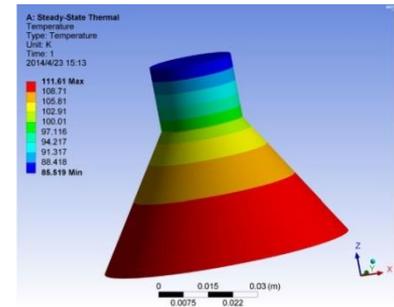
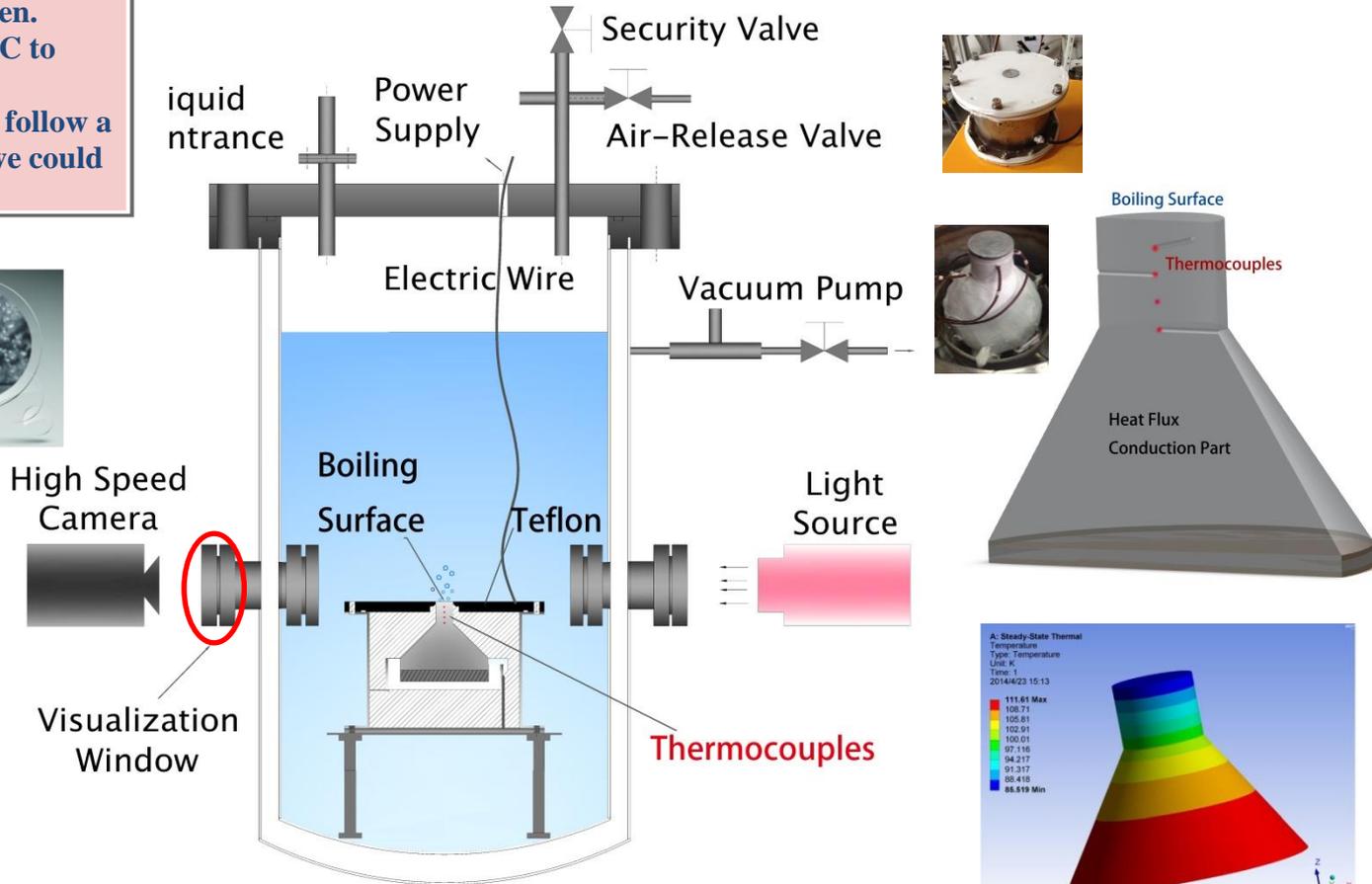
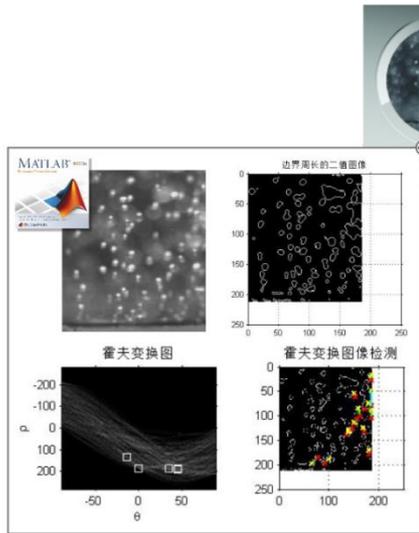
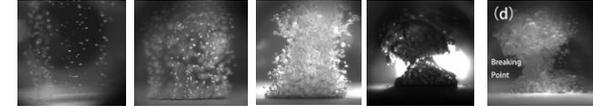
- 4 thermocouples are set in the cone, another thermocouple measures the temperature of liquid nitrogen.
- Using Keithley 2700 and HSC to acquire the measured data.
- The 4 points are expected to follow a linear pattern, from which we could derive the wall temperature.





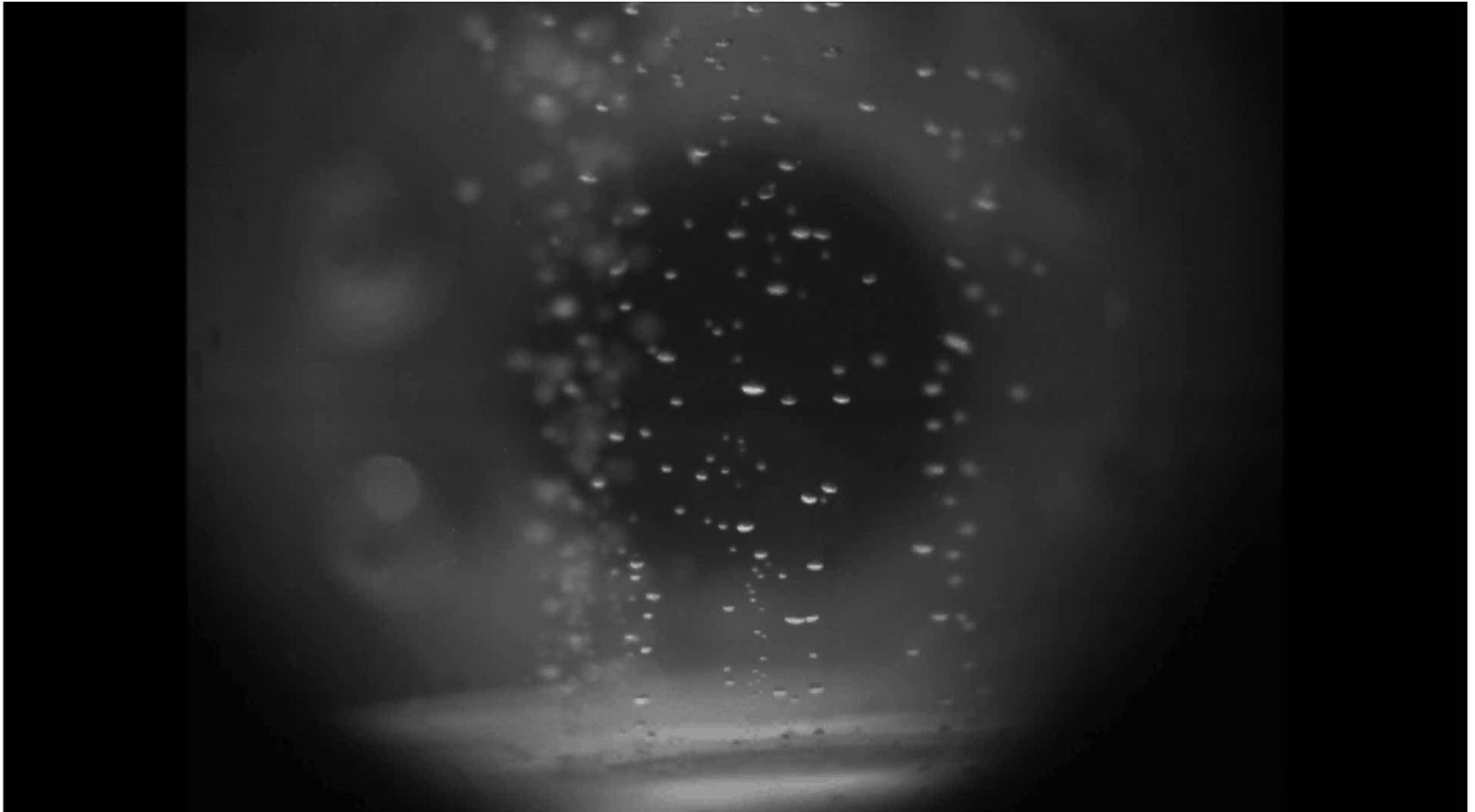
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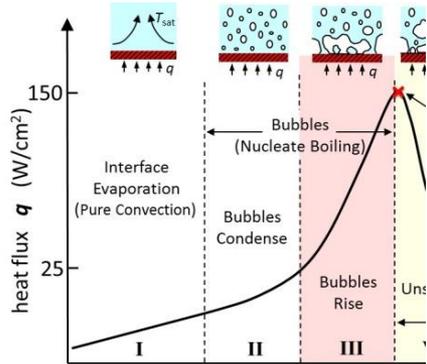
Video Clip From Experiment

What's about this magic?



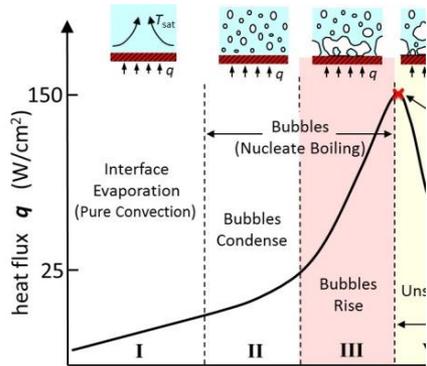


Experimental Phenomena

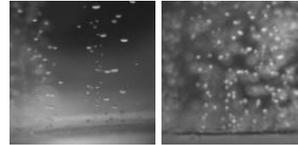




Experimental Phenomena



$$\dot{q} < \dot{q}_{LHF}$$

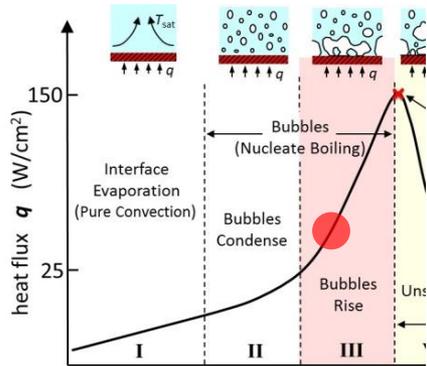


1st Stage: Bubbles tend to be discrete. Experimental data can be **patched into CFD models** for a more accurate verification.

[1] Jin T, Zhang S Y, Tang K, et al. Observation and analysis of the detachment frequency of coalesced bubbles in pool boiling liquid nitrogen[J]. Cryogenics, 2011, 51(9): 516-520.

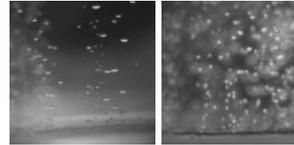


Experimental Phenomena



Low Heat Flux

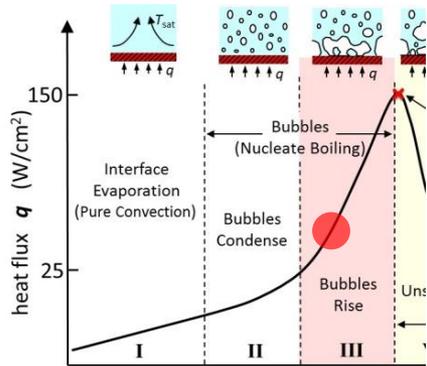
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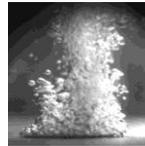
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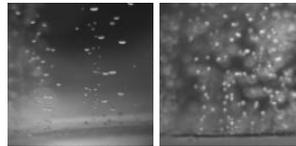
$$\dot{q}_{LHF} < \dot{q} < \dot{q}_{FDNB}$$

Low Heat Flux

$$\dot{q} < \dot{q}_{LHF}$$



2nd Stage: Difficult to define the exact diameter. Bubbles followed a random pattern neither discretely nor as bubble stems.

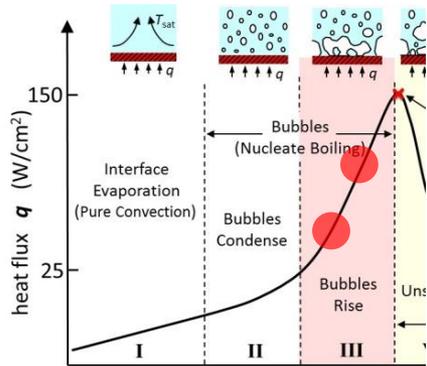


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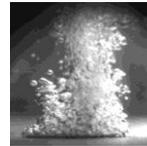
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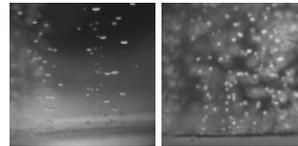
Fully Developed Nucleate Boiling

$$\dot{q}_{LHF} < \dot{q} < \dot{q}_{FDNB}$$

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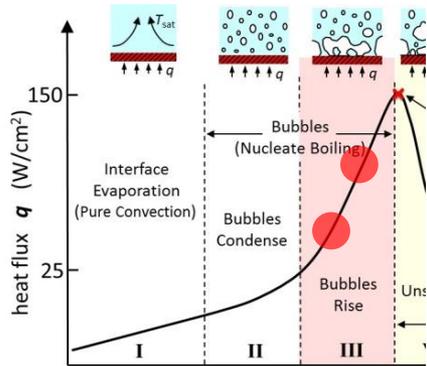


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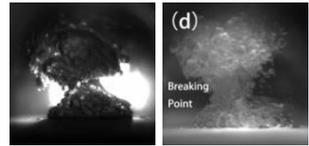
$$\dot{q}_{FDNB} < \dot{q} < \dot{q}_{CHF}$$

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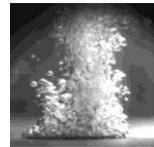
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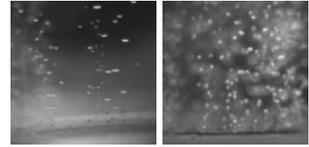
$$\dot{q} < \dot{q}_{LHF}$$



3rd Stage: The merged bubble is a **unity-Bubble Stem**. $f = 13.47s^{-1}$ ^[11], the merged bubble stem is treated as one bulk.



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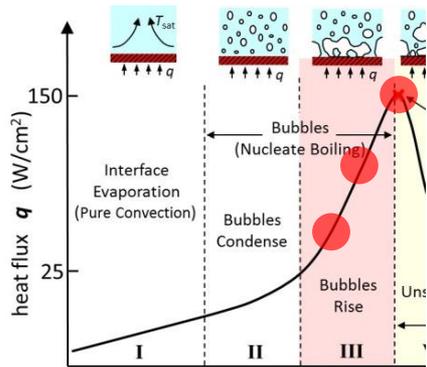


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Experimental Phenomena



Critical Heat Flux

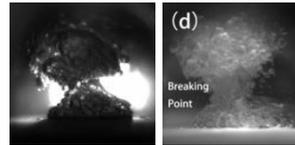
$$\dot{q}_{FDNB} < \dot{q} < \dot{q}_{CHF}$$

Fully Developed Nucleate Boiling

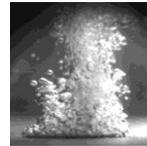
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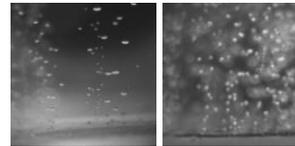
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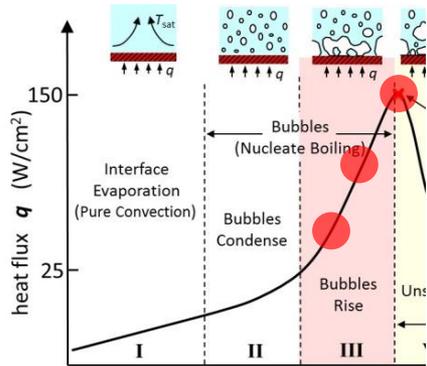
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Experimental Phenomena



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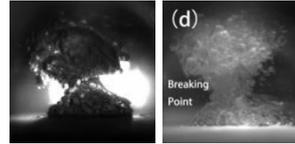
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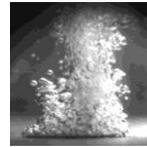
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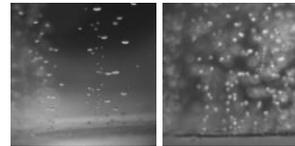
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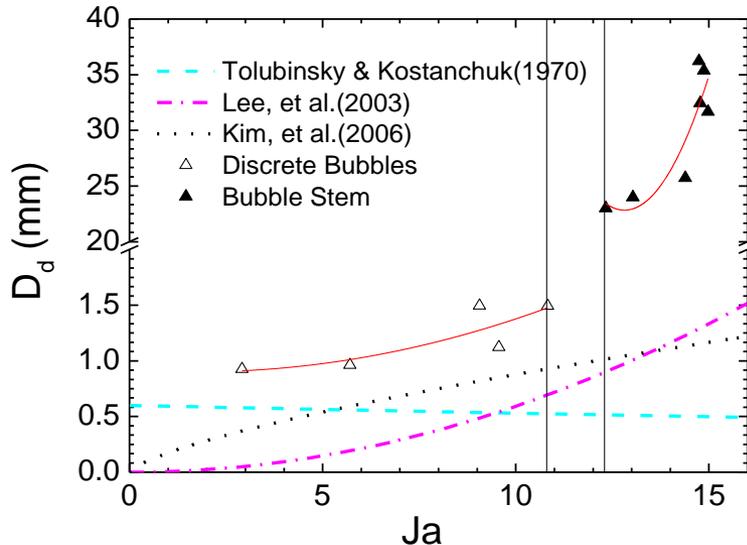
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For low heat flux:

$f = \text{Experimental Data}$

$$D_d = 0.007Ja^2 - 0.024Ja + 0.92 ;$$

For fully developed nucleate boiling:

$f = 13.47s^{-1}$

$$D_d = 2.526Ja^2 - 64.74Ja + 437.63 .$$

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Boiling Models

➤ **Area of influence:**

$$A_b = K N_A \frac{\pi}{4} D_d^2, \quad K = 4.8e^{\left(-\frac{Ja}{80}\right)}$$

➤ **Nucleate side density:**

$$N_A = C \cdot \left(\frac{h_{fv} \rho_v (T_w - T_l)}{\sigma T_{sat}} \right)^3$$
$$C = 625 \times 10^{-16}.$$

➤ **Bubble departure diameter**

$$D_d = 0.007Ja^2 - 0.024Ja + 0.92$$

$$D_d = 2.526Ja^2 - 64.74Ja + 437.63$$

Compared with the observations, the existing correlations are far from satisfactory. Data is correlated based on our experimental results.

➤ **Bubble departure frequency**

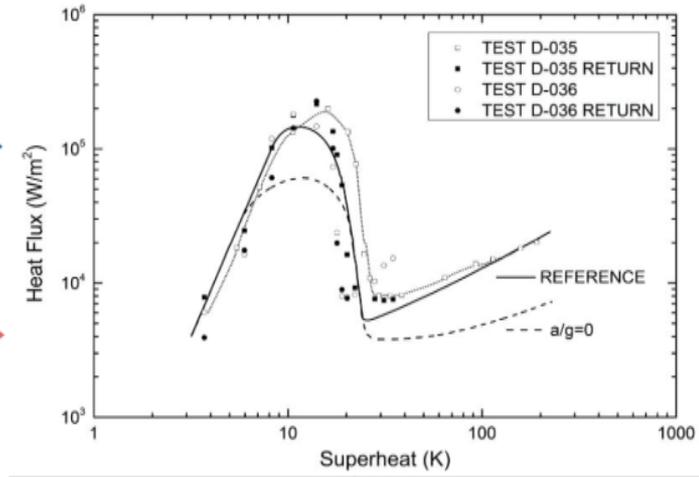
Similar to the situations of the departure diameter, the bubble departure frequency is also obtained from our experimental results.



Research Procedures

UMich & NASA
Experimental
Data

**【Heat Flux】
vs.
【Super-heat】**



**【Heat Flux】
vs.
【Super-heat】**

Our
Experimental
Data

Data

Analyse

Diameter $\sim D$
 Frequency $\sim f$
 Nucleate Site Density $\sim Na$



**【Heat Flux】
vs.
【Super-heat】**

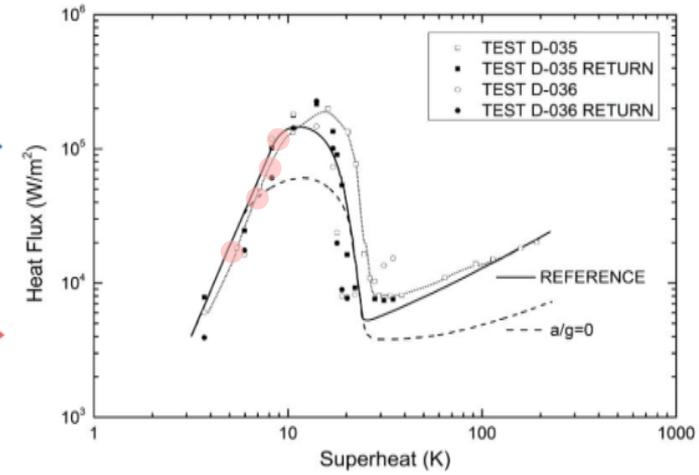
$$f_d^{1/2} D_d = C \cdot f(Ja) \sqrt{3\pi\alpha_l}$$



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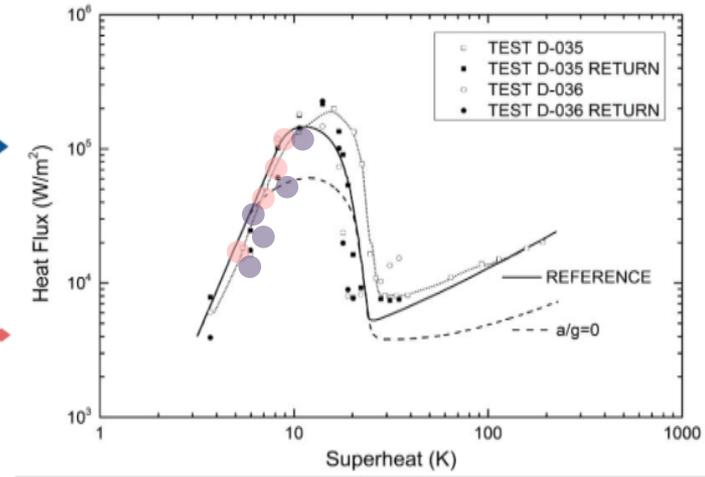
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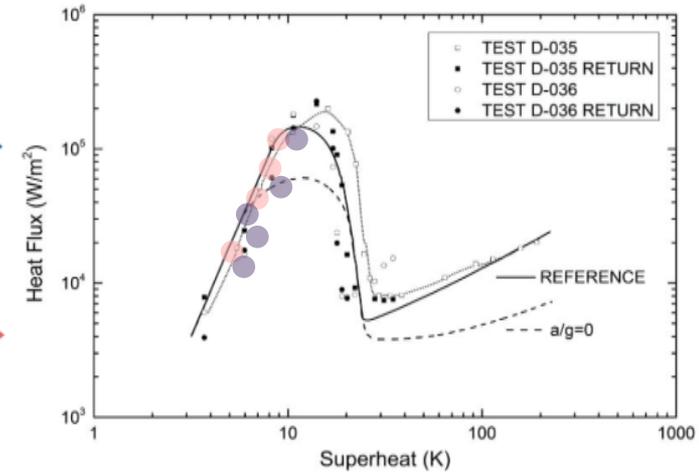
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 Frequency $\sim f$
 Nucleate Site Density $\sim Na$

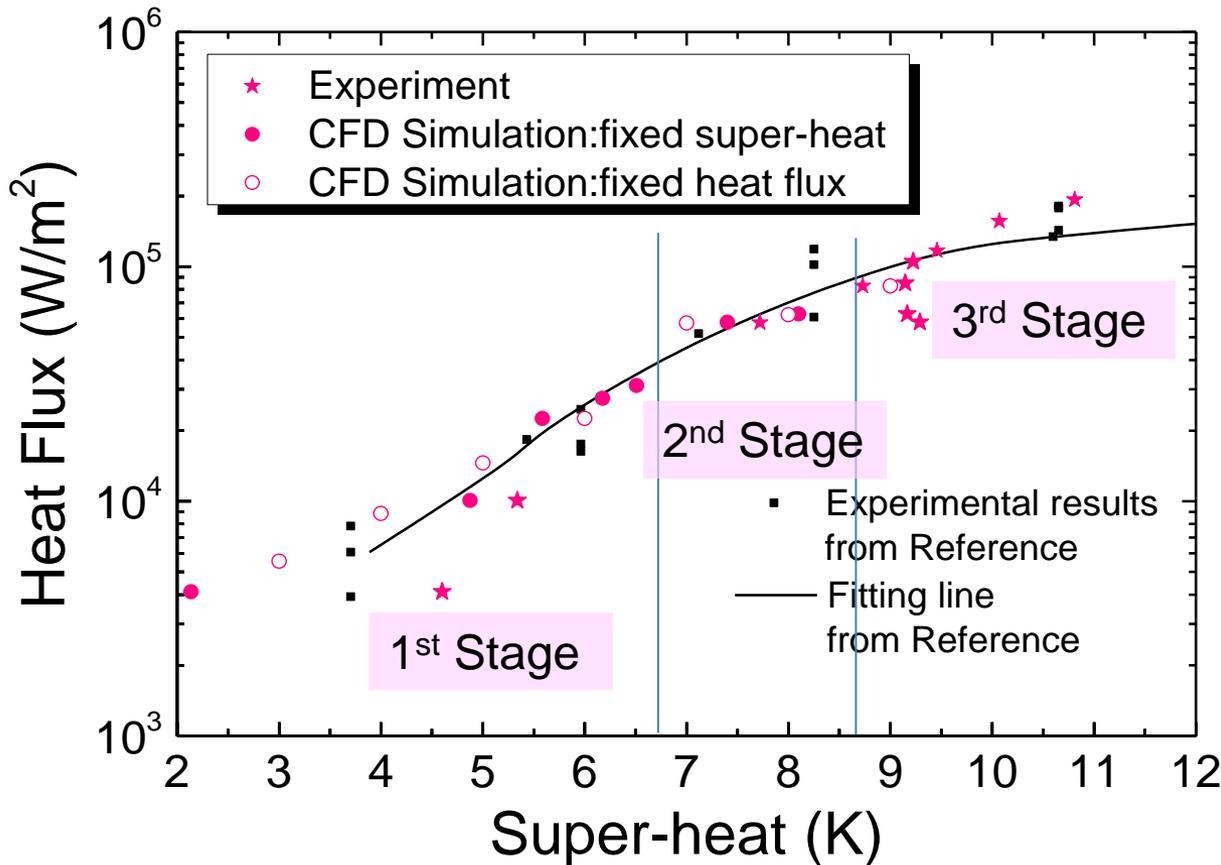


**【Heat Flux】
vs.
【Super-heat】**

$$f_d^{1/2} D_d = C \cdot f(Ja) \sqrt{3\pi\alpha_l}$$



Results & Conclusions



- The measured relation between heat flux and super-heat accorded well with the previous reported experimental data by other researchers.
- Three different boiling stages with different bubble departure structure were distinguished.
- The modeled relations between heat flux and super-heat for LN2 pool boiling were in good accordance with the measured data.

Thank You

