

Geo-neutrino Observations

Can they transform geology?

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Planetary Energy Conservation

– Terrestrial Power Balance

$$- P_{\text{surface}} \approx P_{\text{radiogenic}} + P_{\text{primordial}}$$



– Present Status

- $P_{\text{surface}} = 47 \pm 3 \text{ TW}$
 - » Davies and Davies 2010
- $P_{\text{radiogenic}} = 9 - 27 \text{ TW}$
 - » Ludhova & Zavatarelli 2013
- $P_{\text{primordial}} = 20 - 38 \text{ TW}$

Thermal Evolution and History of Earth

$$Aq = Mh - Mc(\partial T/\partial t)$$

Present temperature decrease rate:
 $\partial T/\partial t = Aq/Mc (Mh/Aq - 1) = 50 \text{ to } 150 \text{ K/Ga}$
Rate of cooling poorly constrained

Present primordial heat loss rate:
 $Aq - Mh = 20 \text{ to } 38 \text{ TW}$
Rate of primordial heat loss poorly constrained

Rates of cooling & primordial heat loss poorly constrained due to uncertainty of radiogenic heating

Motivating Geo-neutrino Observations

- **Questions to address:**
 - **How well does radiogenic heating need to be measured to transform geology?**
 - **Are there levels of precision (± 7 TW? ± 5 TW? ± 3 TW?) for which major geological advances ensue?**
- **Answers to these questions guide geo-neutrino observational program**

Significant Geo-neutrino Observations

- ✓ **Geo-neutrinos: KamLAND (*Nature* 2005)**
- ✓ **Mantle geo-neutrinos: KamLAND + Borexino (*Phys Rev D* 2012)**

Pioneering detections followed by first constraints!

- ✓ **Radiogenic power constraint: KL + BX (*Adv. HEP* 2013)**
- ✓ **Th/U constraint: KamLAND (*Phys Rev D* 2013)**

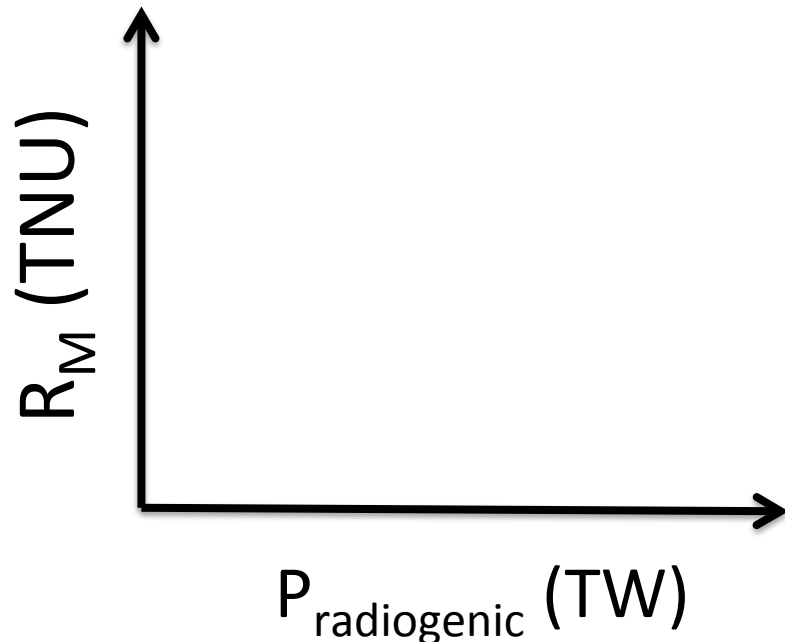
Fantastic! What is next?

- ? **Earth model resolution**
- ? **Constrain thermal evolution? Onset time of plate tectonics?**

Can geo-neutrino observations transform geology?

BSE Modeling

- Model bulk silicate earth (BSE = mantle + crust)
- Calculate mantle geo-nu rate: $R_M = f(P_{\text{radiogenic}})$
- Simple and easy to change parameters



Fortran code

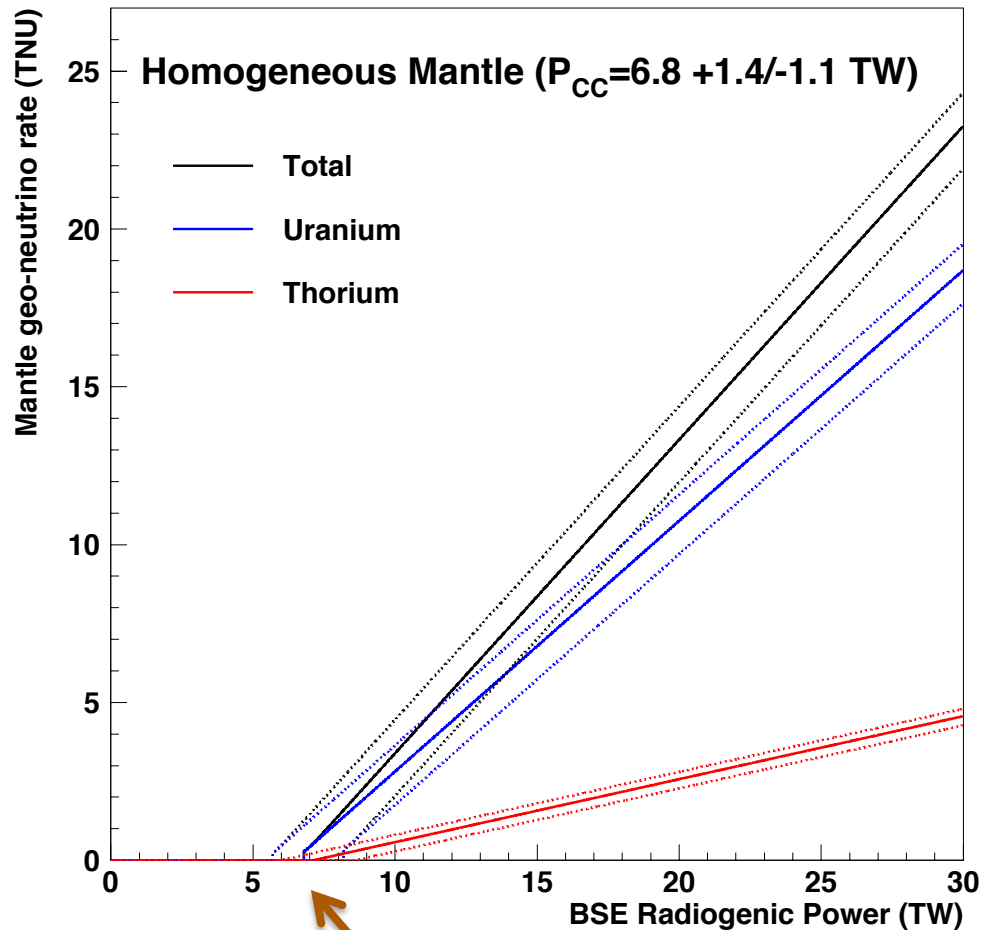
```
program bse
dimension gnrates(4000,2),twerror(4000)
c neutrino luminosity per unit mass of Th and U (#/kg/s)
data ntn/16.266/
data nur/76.466/
c flux to rate conversion
data f2rth/250000./
data f2rur/76000./
c power per unit mass of Th and U (W/kg)
data hth/26.3e-6/
data hur/98.5e-6/
c average neutrino oscillation survival probability
data pes/0.54/
c Huang et al. CC power (TW)
c data pcc/6.8/
c data pcc/8.2/
c data pcc/5.7/
c Workman and Hart DM power (TW)
data pdm/2.0/
c Th/U for PM, CC, and W&H DM
data thupm/3.9/
data thucc/4.3/
data thudm/2.5/
c geo-factors in kg/cm^2
data geoman/1.177e6/
data geoddp/0.292e5/
c masses in kg
data assman/4.002e24/
data assddp/0.132e24/
alpth=th*pes/nth/f2rth
alpur=nur*pes/hur/f2rur
print *,alpth,alpur
pccur=pcc/(1.+thucc*thth/hur)
pccth=pcc-pccur
print *,pccur,pccth
pdmur=pdm/(1.+thudm*thth/hur)
pdeth=pdm-pdmur
print *,pdmur,pdeth
r2hthman=alpth*geoman/assman
r2hurman=alpur*geoman/assman
print *,r2hthman,r2hurman
r2hthddp=alpth*geoddp/assddp
r2hurddp=alpur*geoddp/assddp
print *,r2hthddp,r2hurddp
r2hthdm=alpth*(geoman-geoddp)/(assman-assddp)
r2hurdm=alpur*(geoman-geoddp)/(assman-assddp)
print *,r2hthdm,r2hurdm
```

BSE Power-Mantle Geo-neutrino Model

- **Model input**

- U, Th elemental heat generation per unit mass
- U, Th elemental neutrino luminosity per unit mass
- U, Th flux to signal conversion factors
- $\langle P_{ee} \rangle = 0.54$
- PREM mantle- seismic specification of $\rho(r)$
- $P_M = P_{BSE} - P_{CC}$; $(Th/U)_{BSE} = 3.9$
- $P_{CC} = 6.8 + 1.4/-1.1$ TW ; $(Th/U)_{CC} = 4.3$
- $P_{DM} = 2.0$ TW; $(Th/U)_{DM} = 2.5$
- $P = P_U + P_{Th}$; P_K ignored (refine later)

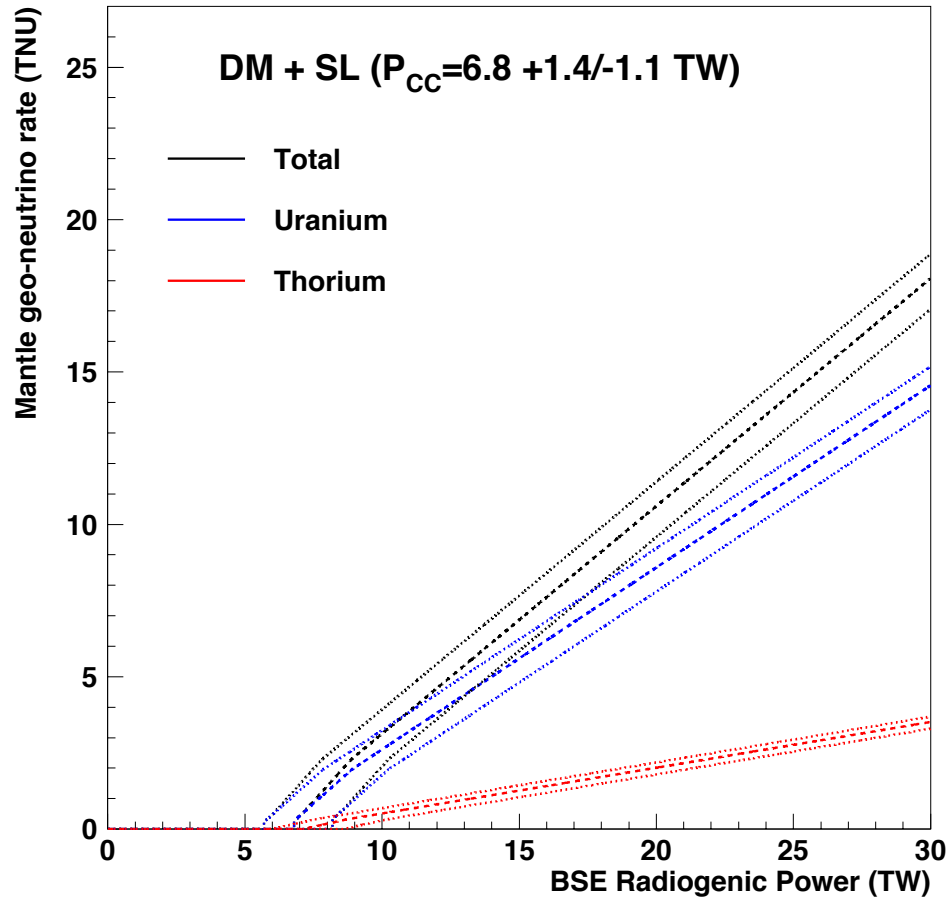
Homogeneous Mantle



$P_{CC} = 6.8 +1.4/-1.1$ TW

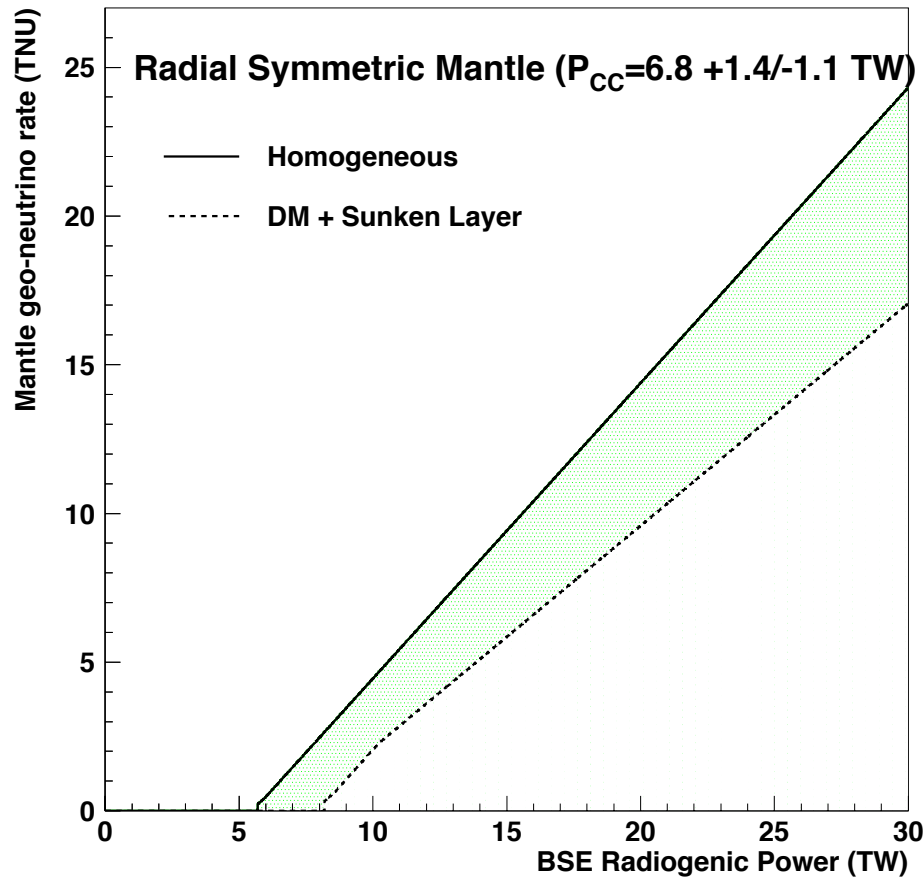
- $P_M = P_{BSE} - P_{CC}$
- Slope ~ 1 TNU/TW
- $R_M \sim \text{slope} * (P_{BSE} - P_{CC})$
- $R_U \sim 4 * R_{Th}$
- Width of bands due to uncertainty in P_{CC}
- Max R_M for given P_{BSE}

Depleted Mantle + Sunken Layer



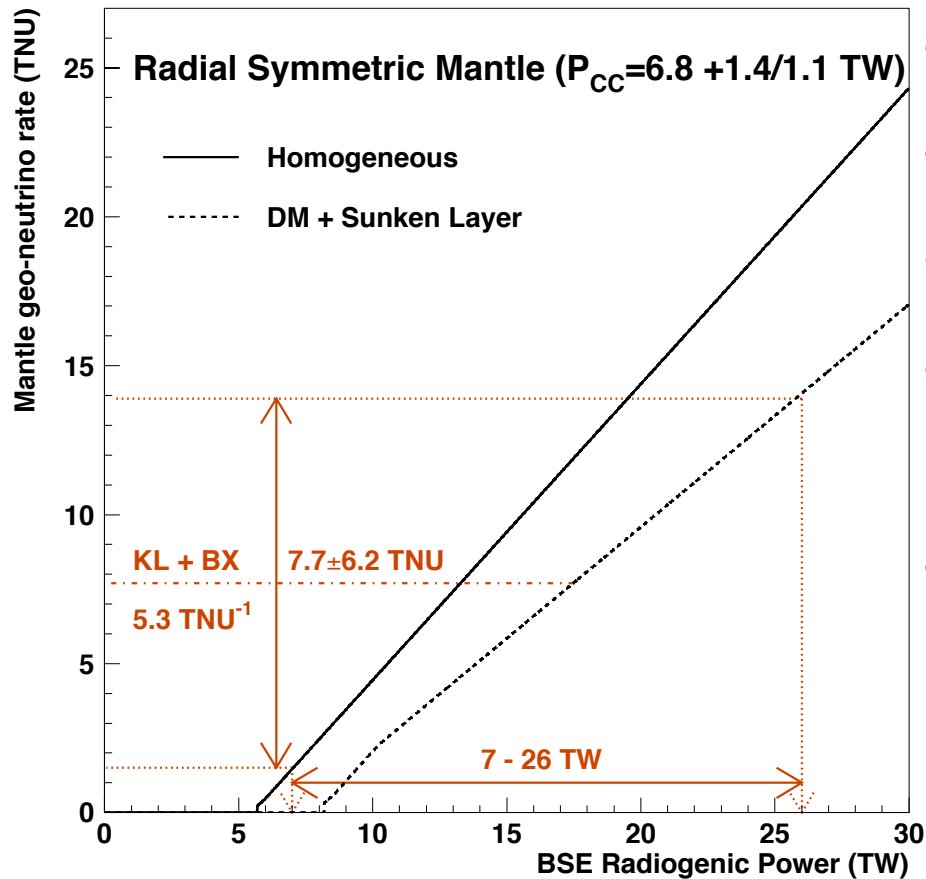
- $P_M = P_{DM} + P_{SL}$
- Sunken Layer is D''
 - $r_{SL} = 3480 - 3630$ km
- Depleted Mantle
 - $P_{DM} = 2.0$ TW
 - $Th/U_{DM} = 2.5$
- $R_U \sim 4 * R_{Th}$
- $R_{DM+SL} < R_M$
- Slope ~ 0.8 TNU/TW

Model Signal-Power Allowed Region



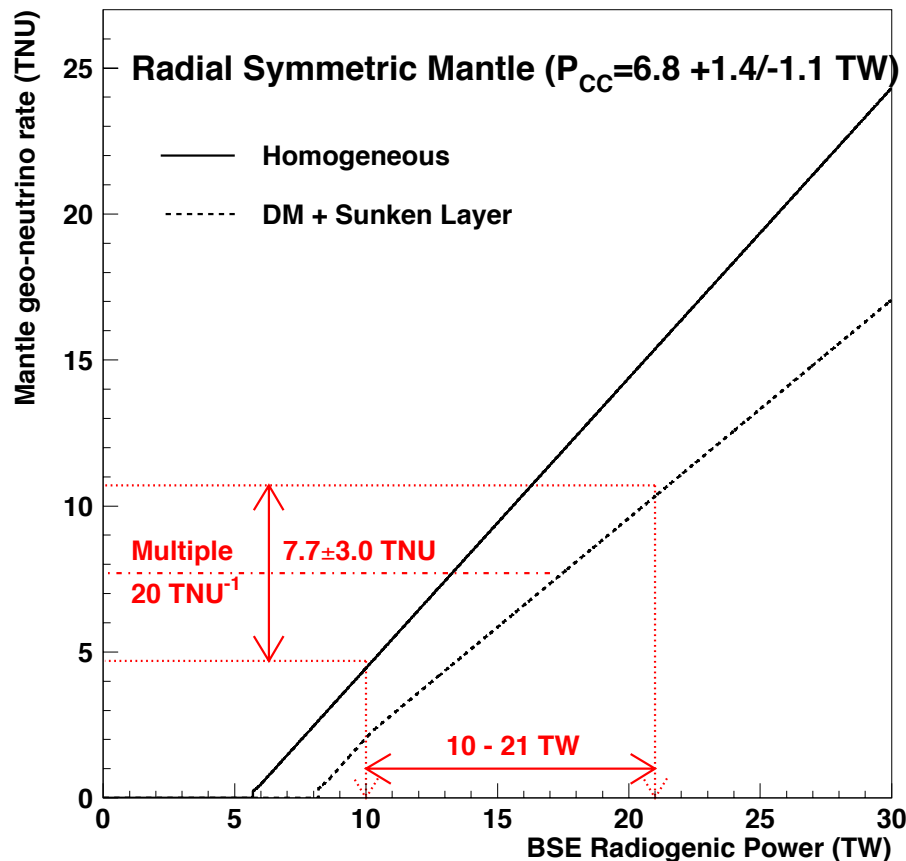
- **Distribution of U, Th in mantle and uncertainty in P_{CC} affect geo-nu measurement of P_{BSE}**
- **Mantle $R_{KL+BX}=7.7\pm 6.2$ TNU**
- **How does this geo-nu measurement constrain model P_{BSE} ?**

Geo-neutrino Constraint of Model P_{BSE}



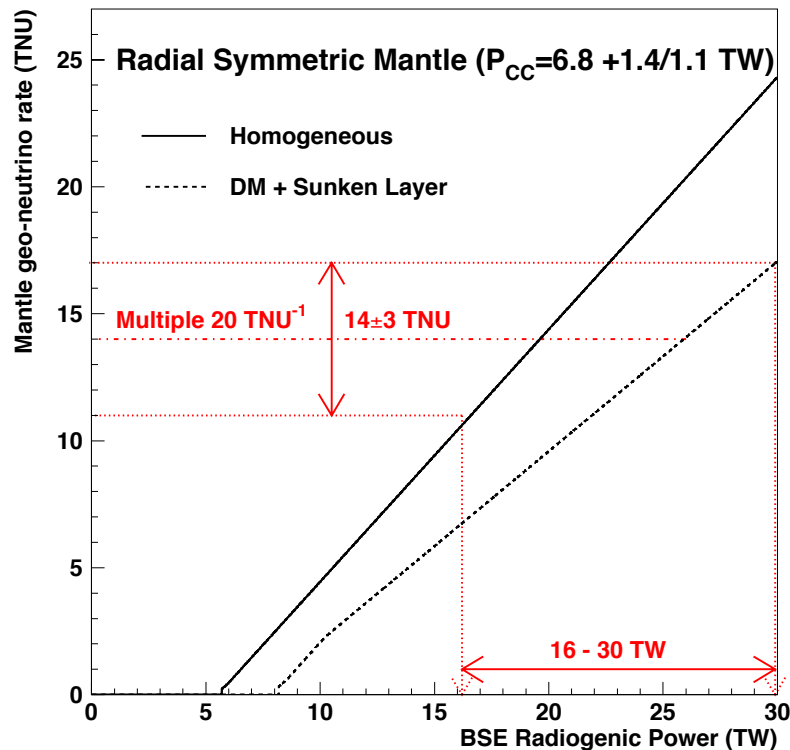
- **KL + BX exposure 5.3 TNU^{-1}**
- **Mantle $R_{KL+BX} = 7.7 \pm 6.2 \text{ TNU}$**
- **Model $P_{BSE} = 7 - 26 \text{ TW}$**
- **Power constrained but earth models not resolved**
- **What might we expect with future measurements?**

Multiple (n=4) Continental Observatories



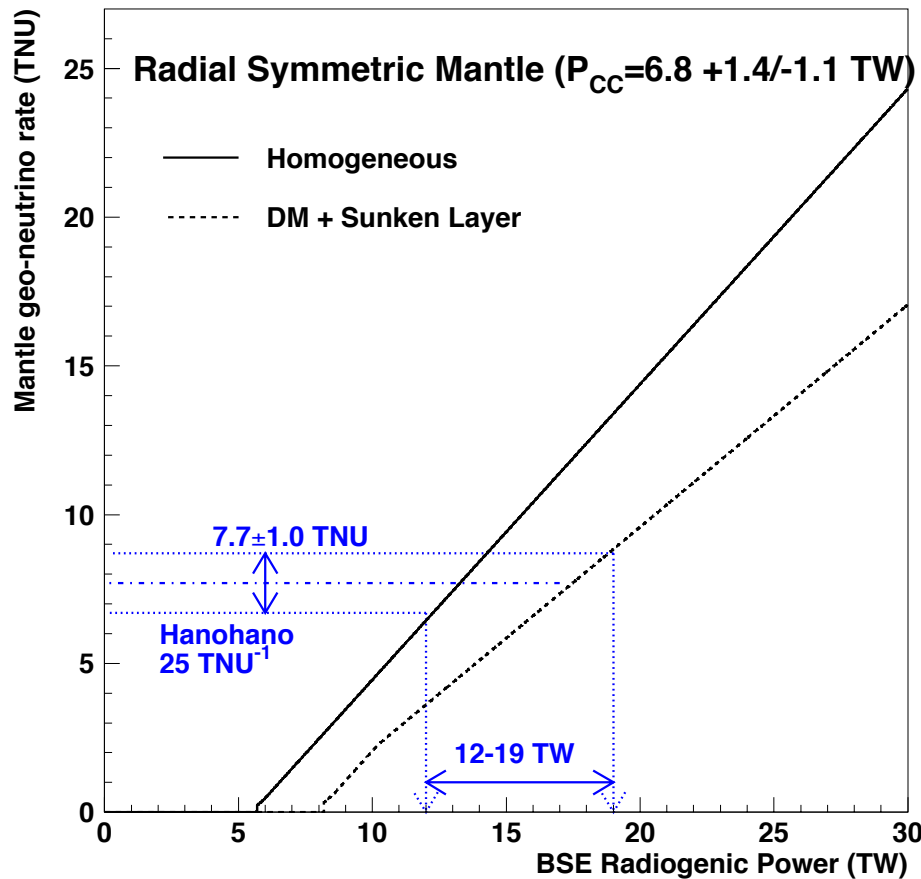
- **Error on mantle R_{KL+BX} is $\sim 1/2$ stat and $\sim 1/2$ sys**
 - 4x exposure reduces statistical error by 2
 - 4 independent obs. reduces systematic error by $\sim 1/\sqrt{4} = 2$
- **Should get to ± 3 TNU**
- **Model P_{BSE} constraint depends on signal size**
- **If $R=7.7 \pm 3.0$, then model $P_{BSE} = 10 - 21 \text{ TW}$**
- **Begin to resolve earth models?**

Multiple (n=4) Continental: High R_M



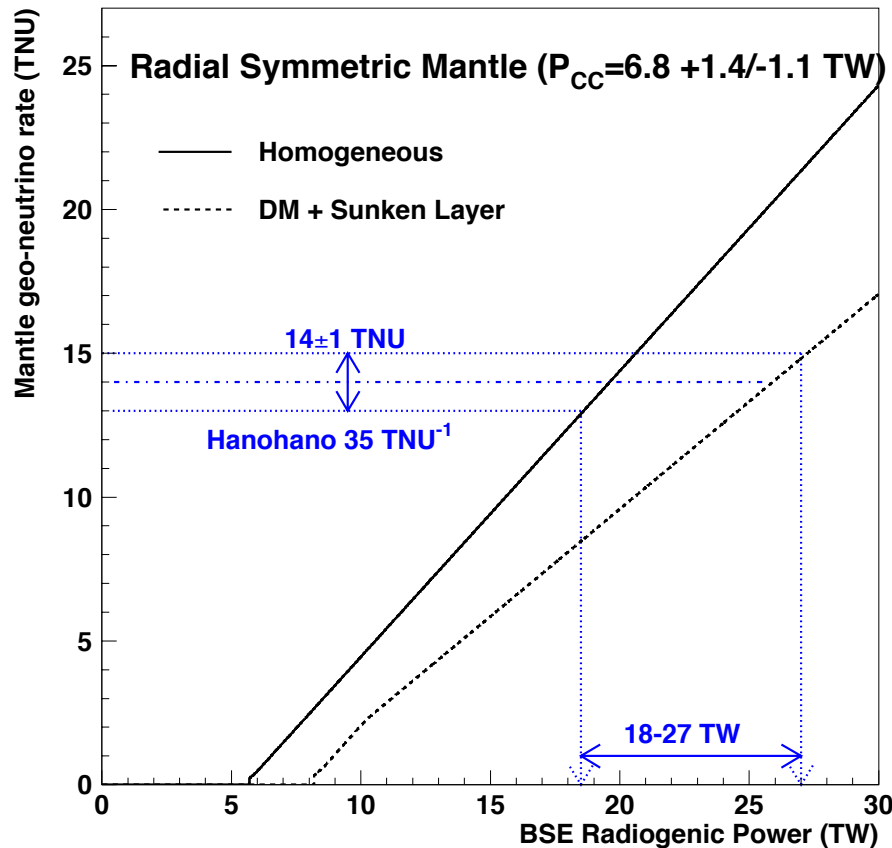
- Higher signal increases value and range of P_{BSE}
- $R_{KL+BX}(\text{max}) \sim 14 \text{ TNU}$
- $R = 14 \pm 3 \text{ TNU}$ gives model $P_{BSE} = 16 - 30 \text{ TW}$
- What improvement would oceanic observatory provide?

Oceanic Observatory



- R_{CC} small can get ± 1.0 TNU with 25 TNU^{-1}
- If $R=7.7 \pm 1.0$ TNU, then model $P_{BSE} = 12 - 19$ TW
- Begin resolve earth model
- However, due to unknown U, Th distribution and uncertainty in P_{CC} the factor of 3 reduction in δR compared with multi-continental reduces δP_{BSE} by ± 2 TW and needs 25% more exposure
- If signal higher, it gets worse

Oceanic Observatory- High R_M



- If $R_{KL+BX}(\text{max}) \sim 14$ TNU
- To get ± 1 TNU requires 35 TNU⁻¹
- If $R = 14 \pm 1$ TNU, then model $P_{BSE} = 18 - 27$ TW
- This is better than multi-continental by $\sim \pm 2$ TW but requires 75% larger exposure

Results of Model BSE Study

δP_{BSE} grows with R_M

$$\delta P_{\text{BSE}}(8 \text{ TNU}) = 10\text{-}21 \text{ TW}$$

$$\delta P_{\text{BSE}}(14 \text{ TNU}) = 16\text{-}30 \text{ TW}$$

$$\delta P_{\text{BSE}}(8 \text{ TNU}) = 12\text{-}19 \text{ TW}$$

$$\delta P_{\text{BSE}}(14 \text{ TNU}) = 18\text{-}27 \text{ TW}$$

- Multi-continental (n=4) mantle geo-neutrino measurement $\delta R = \pm 3$ TNU
- $\delta R = \pm 3$ TNU dominated by systematic error
reduction of multi-continental δR requires *more observatories not more exposure*
- Oceanic observatory can reduce δR significantly, reaching $\delta R = \pm 1$ TNU
- Reduction in model δP_{BSE} is modest due to geological uncertainties
- Requires large exposure (>5 years of Hanohano)

Model BSE Study Conclusions

- **Model BSE study shows potential of geo-nu measurements to inform geology**
- **Geological uncertainties introduce systematic errors**
- **Effort to reduce geological uncertainties very helpful**
- **Refine model by explicitly including K but expect little change**
- **2-TW DM is lowest power predicted; effect of sunken layer decreases as DM power increases**
- **Model with $P_{DM} = 6$ TW would narrow allowed region**

Conclusions

- Will geo-neutrino observations transform geology?
- How well does radiogenic heating need to be measured?
- Outlook
 - **±10 TW present measurement**
 - **±7 TW possible with new observatories**
 - **±5 TW challenging**
 - **±3 TW extremely challenging**
 - **±1 TW improbable**

Thank You

Th/U by Geo-nu

