

Dinesh K. Srivastava Variable Energy Cyclotron Centre Kolkata 700 064, India

# **Epilogue as a Prologue**

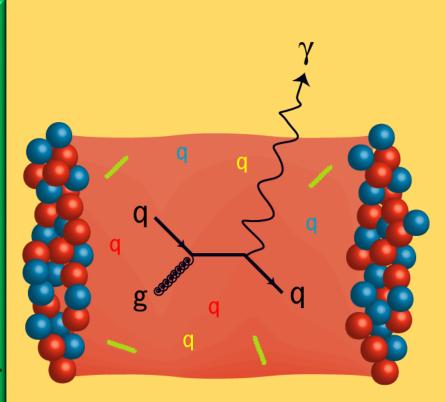
- Observation of Quark Gluon Plasma is one of the most spectacular confirmations of Quantum Chromo-Dynamics- the theory of strong interactions.
- It has led to the creation of the conditions of the Early Universe a few micro-seconds after The Big Bang.
- It required the largest international effort ever mounted with several thousand engineers and scientists working in unison to build several accelerators and detectors costing billions of dollars and inventing computing techniques like grid computing to deal with the enormous bulk of the data generated.
- It has also led to several questions which need to be answered.

#### Thirty seven years ago:

E. L. Feinberg, Nuv. Cim. A 34 (1976) 391, pointed out that:

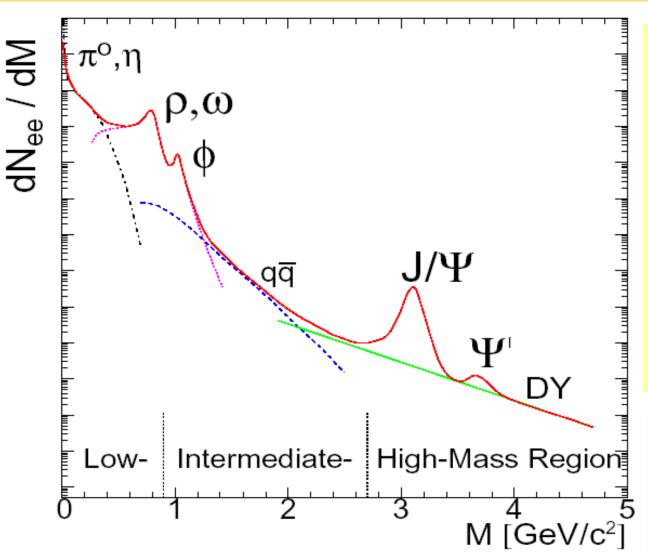
Direct photons; real or virtual are penetrating probes for the bulk matter produced in hadronic collisions, as

- They do not interact strongly.
- They have a large mean free path.



Since then relentless efforts by researchers from across the world have established these as reliable probes of hot and dense matter.

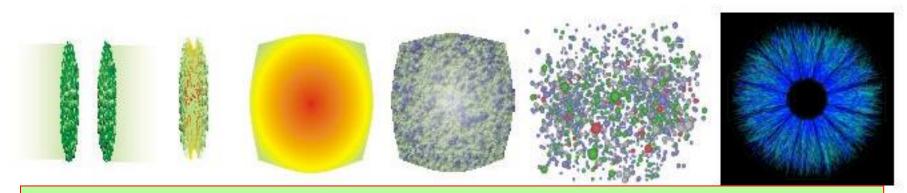
#### Low, Intermediate, & High Mass Dileptons



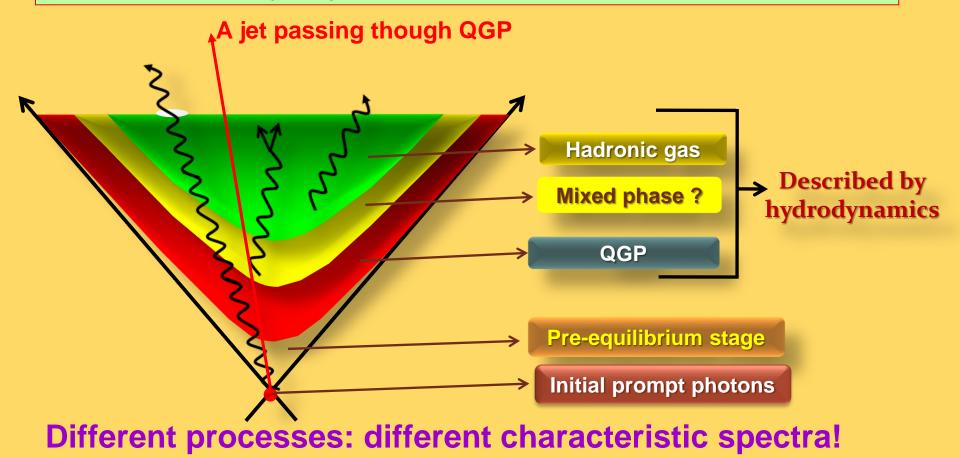
- Low-mass: Medium modified spectral density
- Intermediate mass: Radiation from QGP
- High mass:  $J/\psi$  etc., suppression
- All masses:

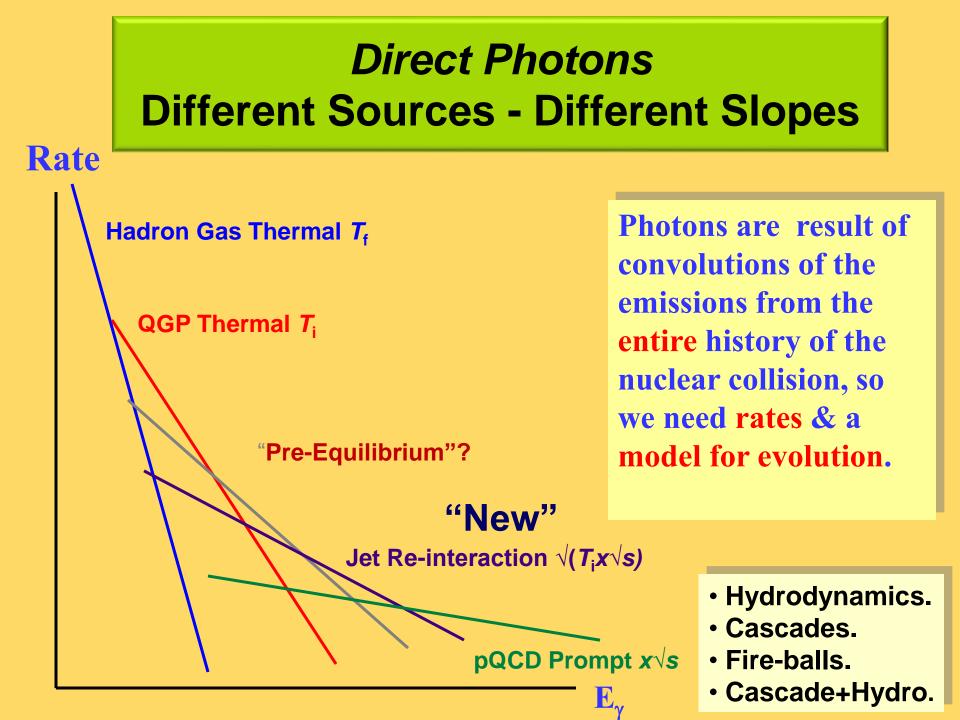
Correlated Charm/ Bottom Decay.

The same model should explain both: Single Photons and Dileptons.

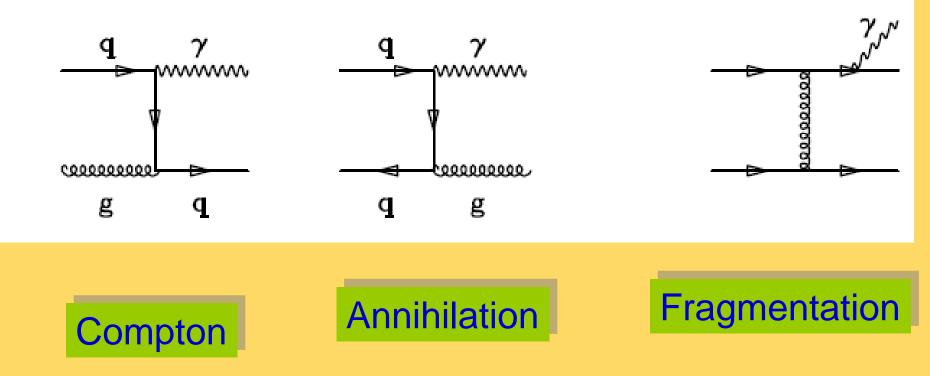


Single photons are penetrating probes. They are emitted at all stages and survive unscathed ( $\alpha_e << \alpha_s$ ). They are "historians" of the heavy ion collision!





#### Partonic Processes for Production of Prompt Photons in Hadronic Collisions

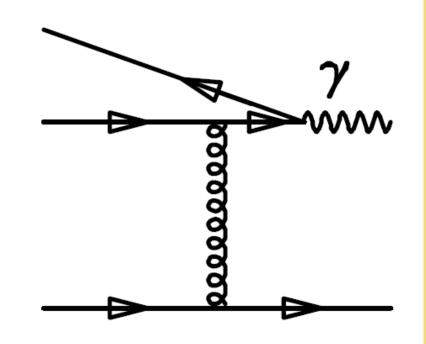


Calculate using NLO pQCD [with shadowing & scaling with T<sub>AA</sub>(b) for AA, partons remain confined to individual nucleons; do not forget the isospin!]

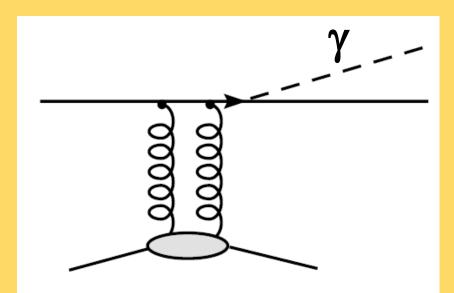
The quarks will lose energy *before fragmenting* if there is QGP; suppressing the fragmentation contribution.

See e.g., Jeon, Jalilian-Marian, Sarcevic, NPA 715 (2003) 795, "QM-2002".

# In the QGP we also have:



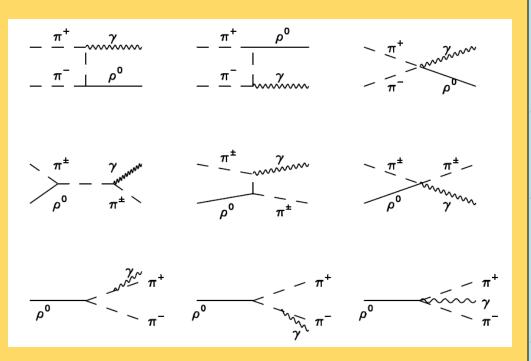
Annihilation with scatterring; *First* calculated by Aurenche et al, PRD 58 (1998) 085003.



Medium induced bremsstrahlung; *First* calculated by *Zakharov*, JETP Lett. 80 (2004) 1; *Turbide et al*, PRC 72 (2005) 014905. Zhang, Kang, & Wang, hep-ph/0609159.

Complete leading order results: Arnold, Moore, Yaffe, JHEP 0112 (2001) 009. NLO is at most 20% and similar in shape (see JHEP 1305 (2013) 010).

#### **Examples of Hadronic Processes Involving** $\pi$ & $\rho$ for Production of Photons

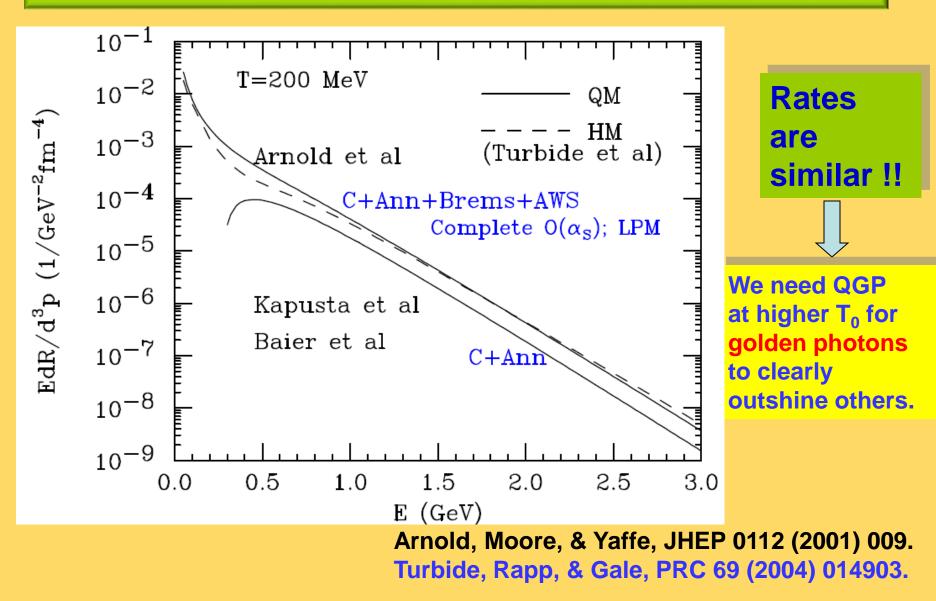


First calculated by Kapusta, Lichard, & Seibert, PRD 44 (1991) 2774.

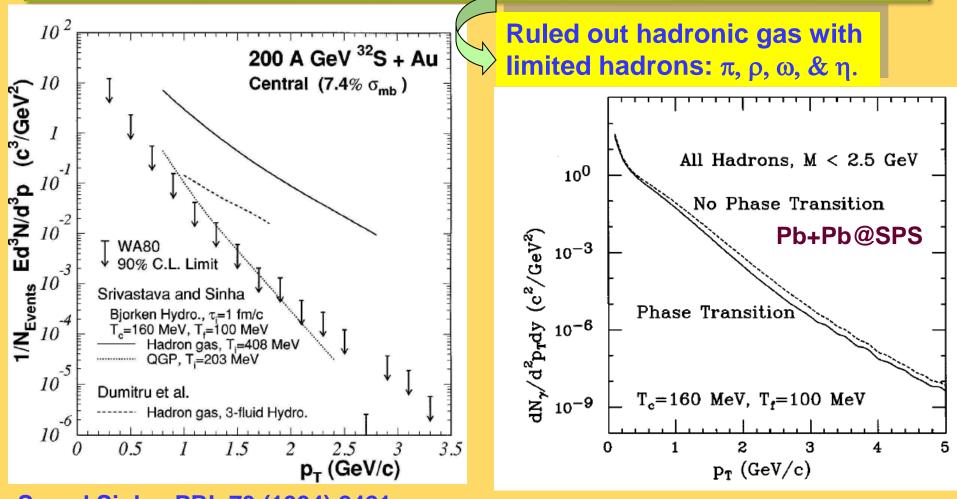
Include πρ→a₁→ πγ
 Xiong et al, PRD 46 (1992) 3798;
 Song, PRC 47 (1993) 2861.

- Include baryonic processes.
   Alam et al, PRC 68 (2003) 031901.
- Medium modifications; (Series of valuable papers, T and μ<sub>b</sub>)
   Alam et al, Ann. Phys. 286 (2001)
   159.
- Include strange sector, massive Yang- Mills theory, form-factors, baryons, t-channel exchange of ω mesons etc. Turbide, Rapp, Gale, PRC 69 (2004) 014903.

#### **Complete Leading Order Rates from QGP & Exhaustive Reactions in Hadronic Matter**



## **Upper Limit of Single Photons, WA80**

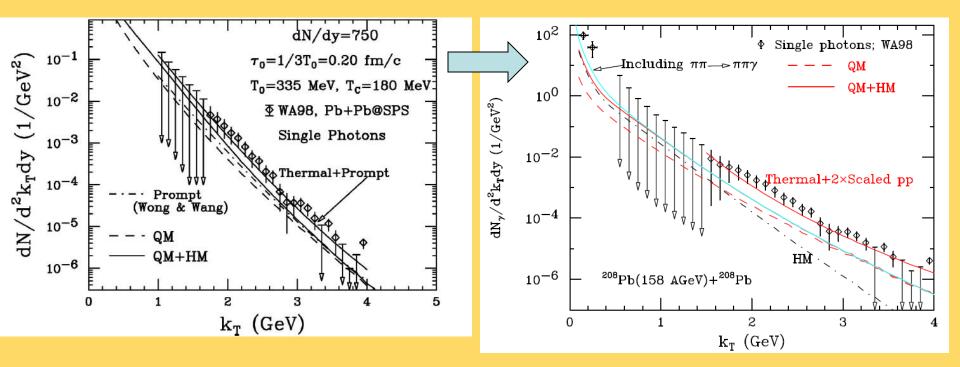


S. and Sinha, PRL 73 (1994) 2421; Dumitru et al., PRC 51 (1995) 2166.

Sollfrank et al., Lee & Brown, Arbex et al., .

Cleymans, Redlich, & S., PRC 55 (1997) 1431. However,  $n_{had} >> 2-3 / \text{fm}^3$ ! For No Phase Transition.

#### WA98: 2-loop $\rightarrow$ Complete O( $\alpha_s$ ) for QGP & $\pi\rho a_1 \rightarrow$ Exhaustive Hadronic Reactions for hadrons

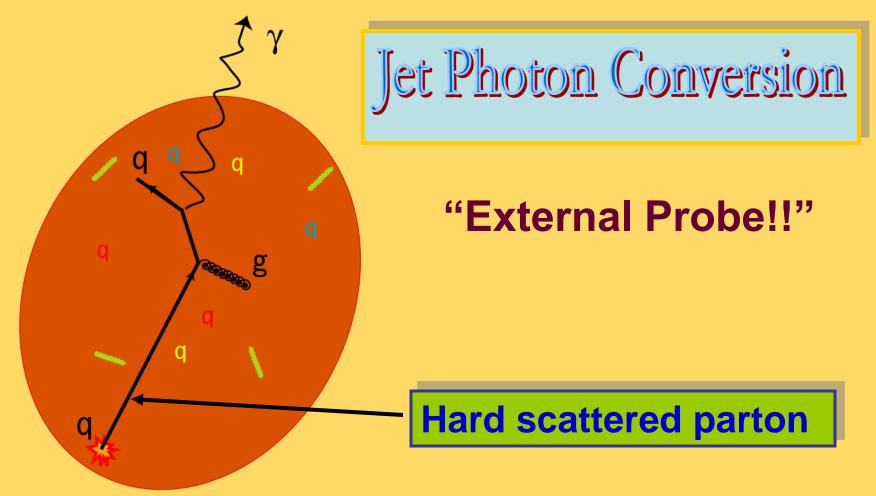


S. & Sinha, PRC 64 (2001)034902 (R).

S., PRC 71 (2005) 034905.

Hydrodynamics, QGP + rich EOS for hadrons & accounting for the prompt photons

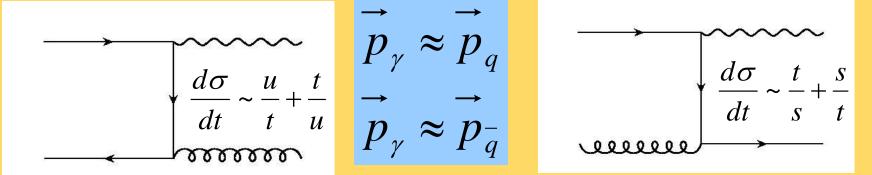
# Interaction of hard-scattered parton with dense matter



Fries, Mueller, & S., PRL 90 (2003) 132301.

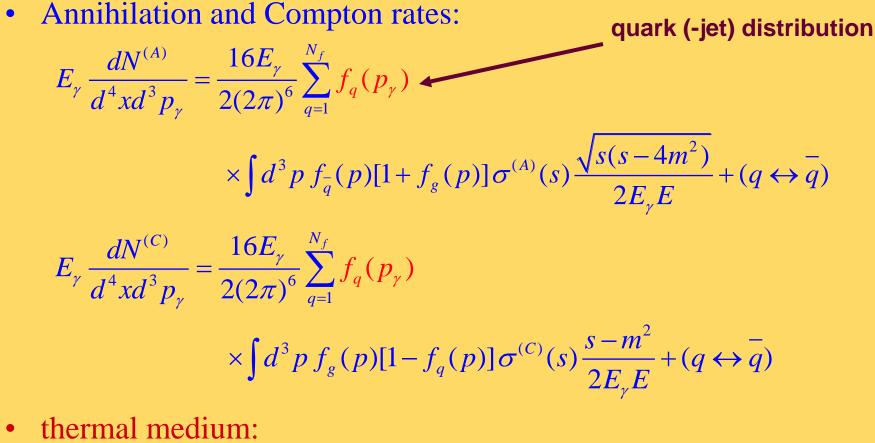
### **Jet-Initiated EM Radiations from QGP**

• Annihilation and Compton processes peak in forward and backward directions:



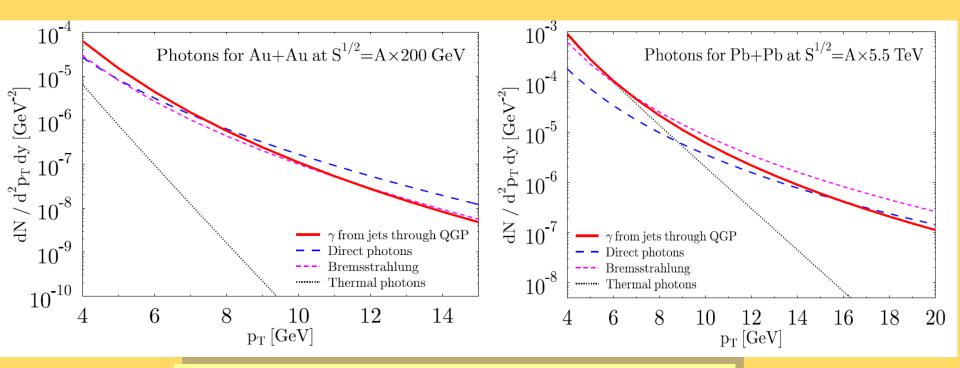
- one parton from hard scattering, one parton from the thermal medium; cutoff  $p_{\gamma,min} > 1$  GeV/c.
- > photon carries momentum of the hard parton
- Jet-Photon Conversion
- This puts photon production and jet-quenching on the same page!!

## **Jet-Photon Conversion: Rates**



$$E_{\gamma} \frac{dN_{\gamma}}{d^3 p_{\gamma}} = \frac{\alpha \alpha_s}{8\pi^2} \int d^4 x \frac{2}{3} \Big[ f_q(p_{\gamma}) + f_{\overline{q}}(p_{\gamma}) \Big] T^2 \left( \ln \frac{4E_{\gamma}T}{m^2} + C \right)$$

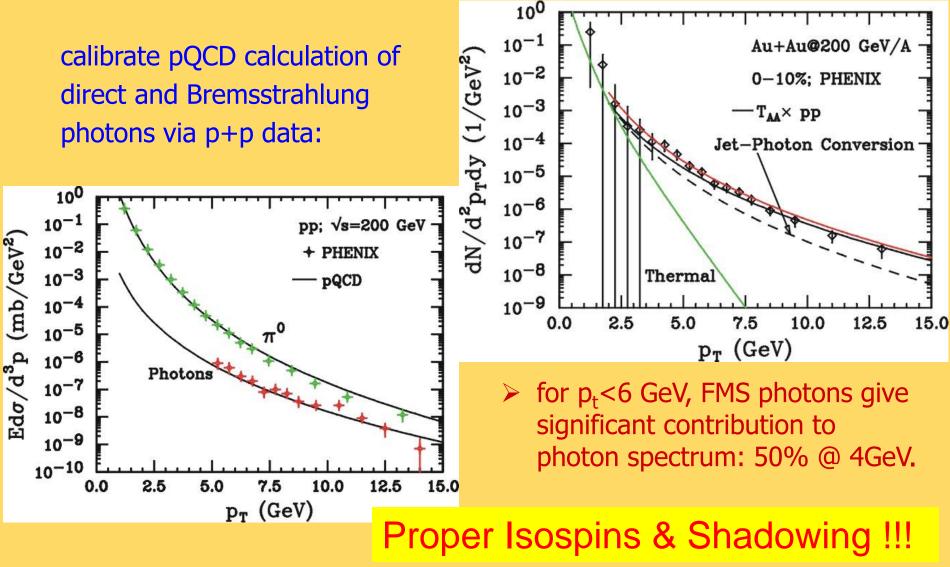
#### Photons from Passage of Jets through QGP



Fries, Mueller, & S., PRL 90 (2003) 132301.

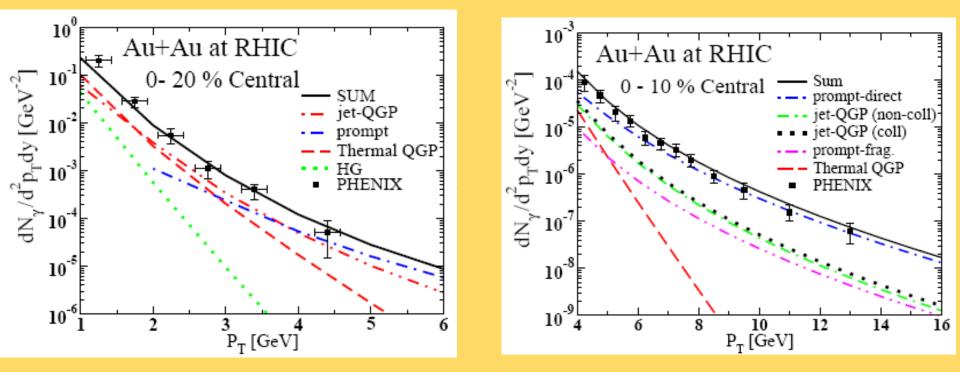
This "bremsstrahlung" contribution will be suppressed due to E-loss and there will be an additional jet-induced bremsstrahlung, which is also similarly suppressed, leaving the jet-conversion photons as the largest source for  $p_T = 4-10$  GeV.

## **FMS Results: Comparison to Data**



Fries, Mueller, & S., PRC 72 (2005) 041902( R).

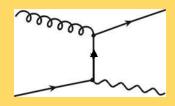
#### AMY and One-Stop Treatment of Jet-Quenching and Jet-Initiated Photons

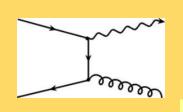


Turbide, Gale, Frodermann, & Heinz, hep-ph/0712.732

This supersedes Turbide, Gale, Jeon, & Moore, PRC 72 (2005) 014906; which used AMY but all the processes were calculated using hard spheres and ignoring transverse expansion.

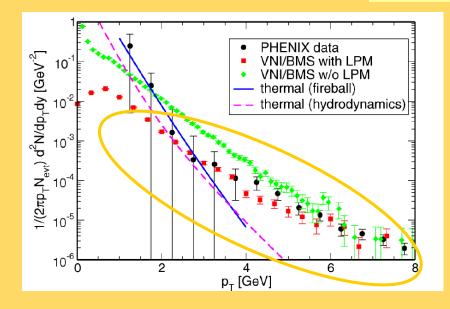
# **Parton Cascade Model**

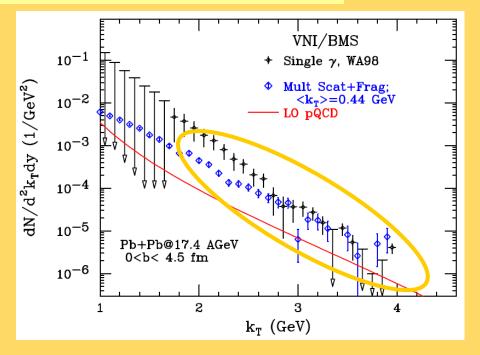






#### **Embedded in the partonic cascades**



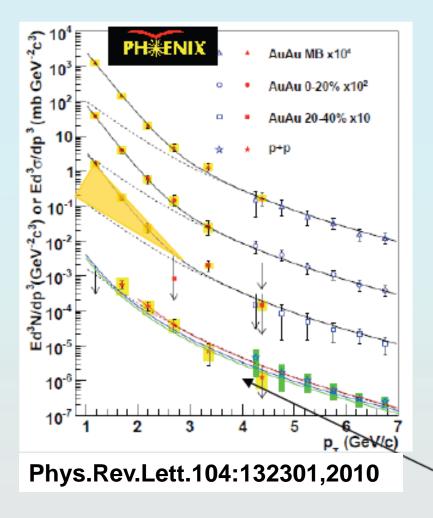


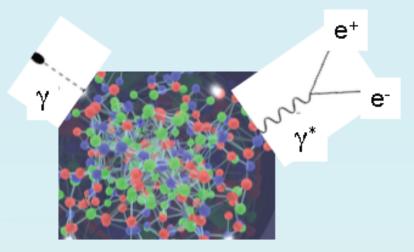
Renk, Bass, & S., PLB 632 (2006) 632.

LPM plays a significant role.

Bass, Mueller, & S., PRC 66 (2002) 061902 (R).

#### Initial temperature? Thermal radiation

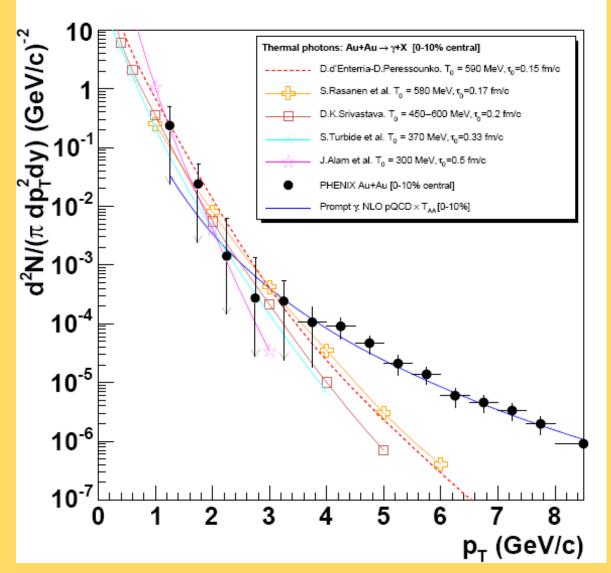




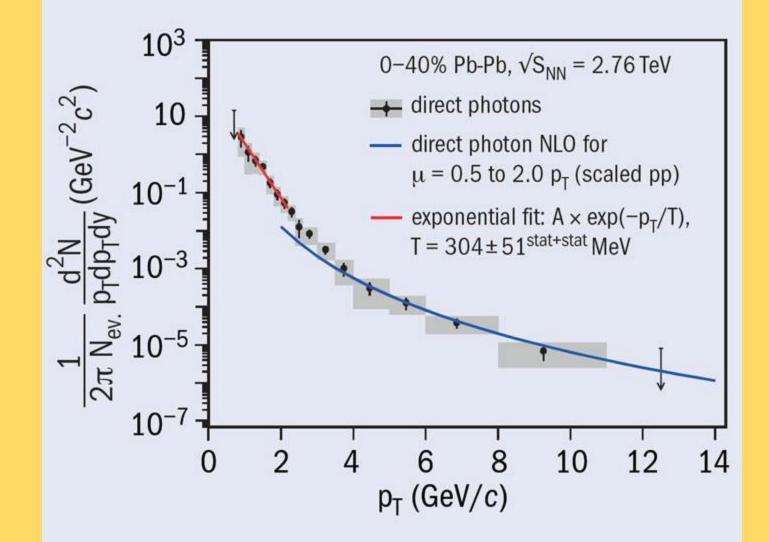
Low mass, high p<sub>T</sub> e<sup>+</sup>e<sup>-</sup> → nearly real photons Large enhancement above p+p in the thermal region

pQCD γ spectrum: q+g→q+γ (Compton scattering @ NLO) agrees with p+p data ₀

## **Thermal photons from Au+Au@RHIC**



d'Enterria & Peressounko, EPJC 46 (2006) 451.



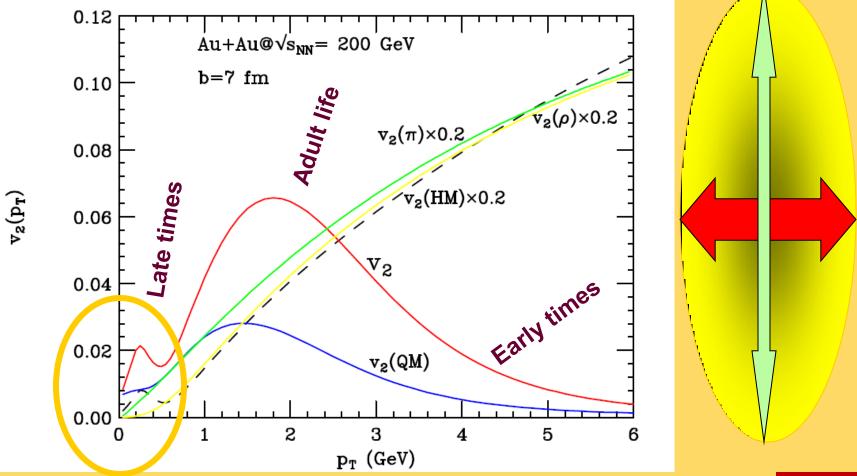
Highest temperature in the Universe since The Big Bang!

# **Anisotropic Flow**

#### - Characterized by the azimuthal Fourier coefficient of the spectrum:

$$\frac{dN(b)}{d\varphi p_T dp_T dy} = \frac{dN(b)}{2\pi p_T dp_T dy} \left[1 + 2v_2(p_T, b)\cos(2\varphi) + \dots\right]$$
  
where  
$$v_2(p_T, b) = \frac{\int d\varphi \cos(2\varphi) E \frac{dN(b)}{d\varphi p_T dp_T dy}}{\int d\varphi E \frac{dN(b)}{d\varphi p_T dp_T dy}}$$

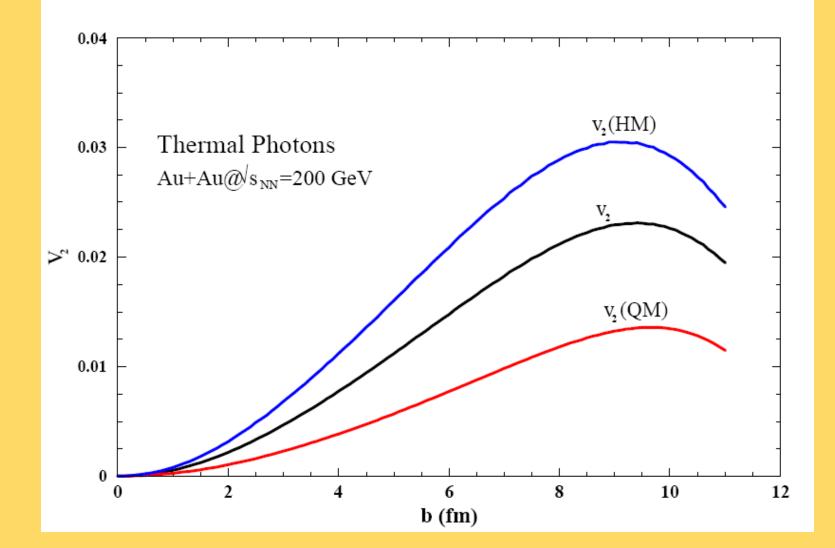
# Elliptic Flow of Thermal Photons: Measure Evolution of Flow !



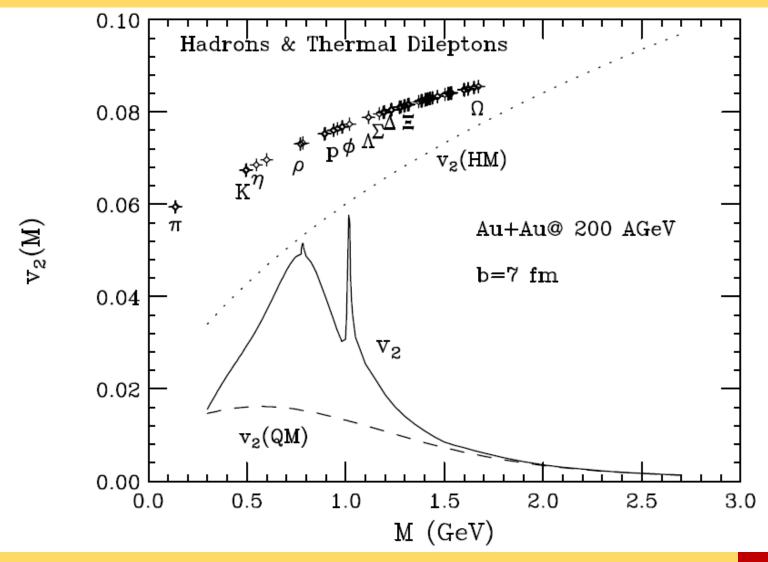
Chatterjee, Frodermann, Heinz, and S., PRL 96 (2006) 202302.



# **Impact Parameter Dependence of v**<sub>2</sub>



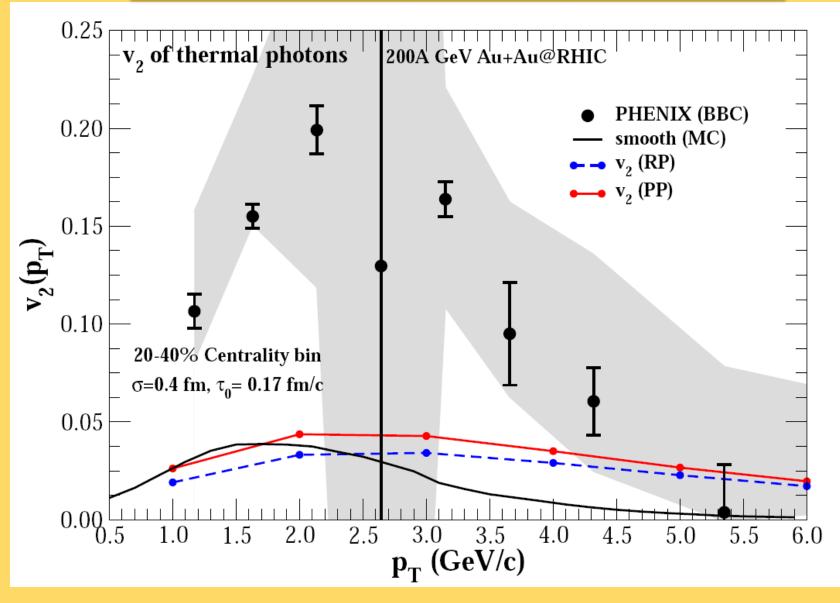
## Elliptic Flow of Thermal Dileptons: Measure Evolution of Flow !



Chatterjee, Heinz, Gale, & S., PRC 75, 054909 (2007).

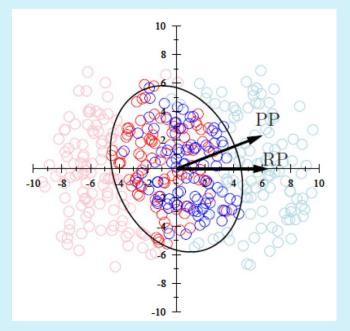
FIRST

#### Elliptic flow of thermal photons



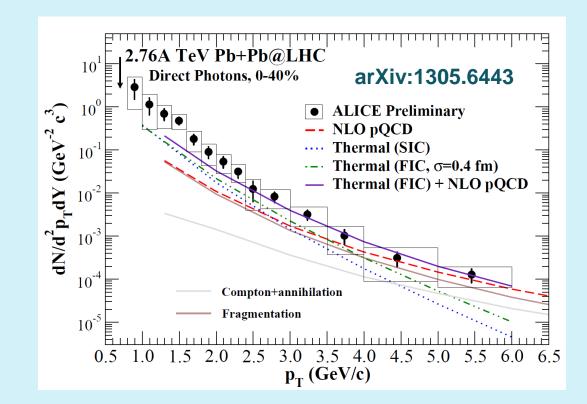
Chatterjee et al.

#### **Event-by-event fluctuating initial density distribution**

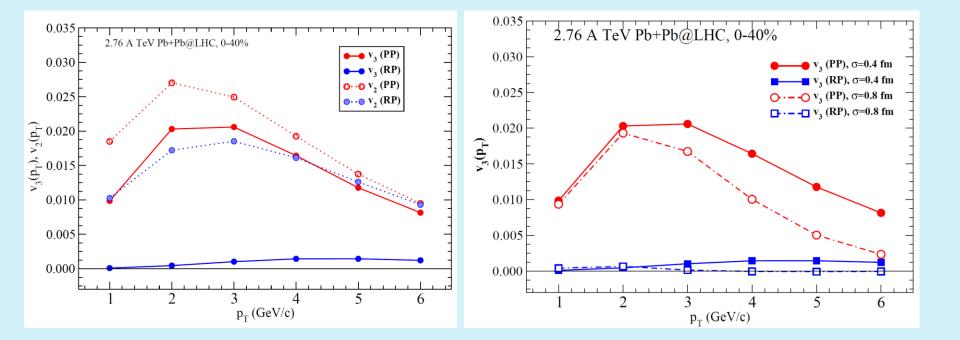


## Fluctuation size parameter $\sigma$ =0.4 fm

The 'hotspots' in the fluctuating events produce more high  $p_T$  photons compared to a smooth initial state averaged profile.



# Triangular flow of thermal photons

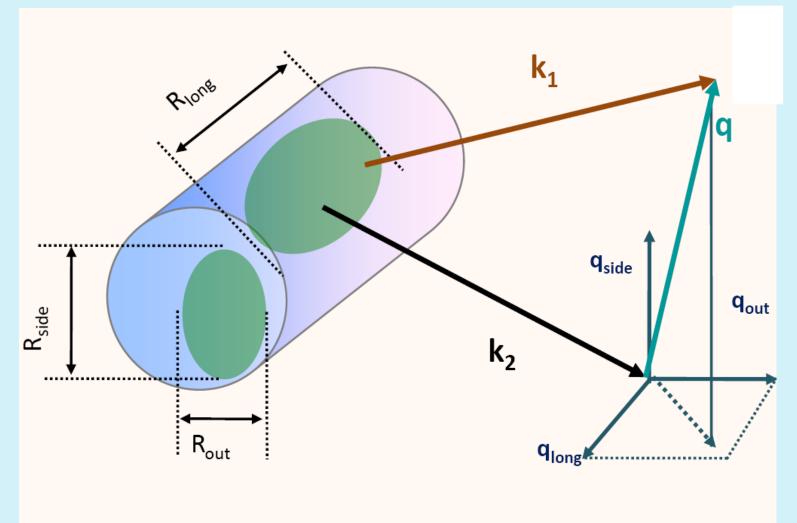


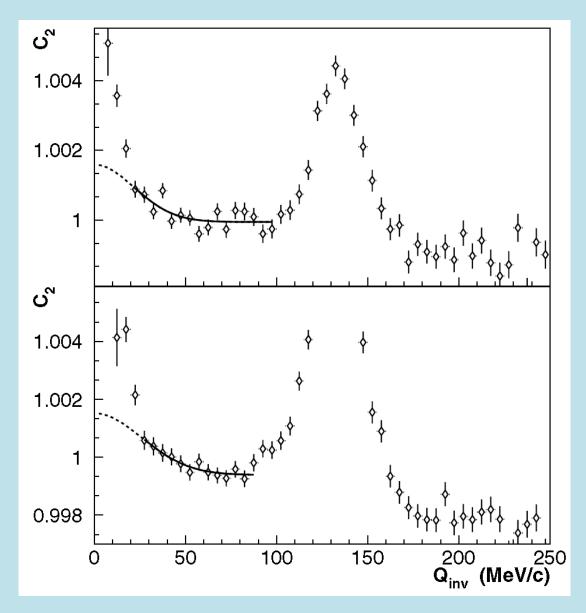
v<sub>3</sub> (p<sub>T</sub>) for 2.76A TeV Pb+Pb@ LHC

 $\sigma$  dependence of  $v_3$ 

Chatterjee, Holopainen, DKS [in preparation]

# Intensity Interferometry of Thermal Photons

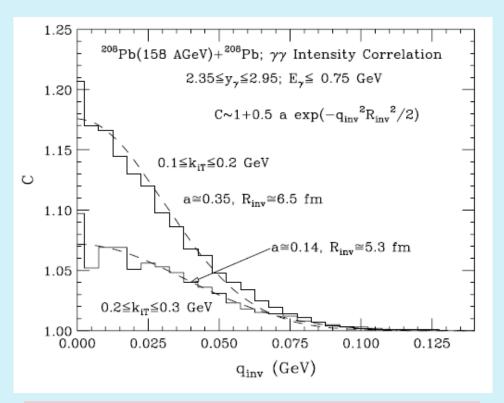




two-photon The correlation function for average photon momenta 100 <  $K_{\tau}$  < 200 MeV/c (top) and 200 <  $K_{\tau}$  < 300 MeV/c (bottom). The solid line shows the fit result in the fit region used (excluding the  $\pi^0$  peak at  $Q_{inv} \approx m_{\pi 0}$ ) and the dotted line shows the extrapolation into the low Q<sub>inv</sub> region where backgrounds are large.

M. M. Aggarwal et al., [WA98 collaboration] PRL 93, 022301 (2004)

# Intensity Interferometry of Thermal Photons @SPS



WA98 measures  $R_{inv}$  as 8.34 ± 1.7 fm and 8.63 ± 2.0 fm, respectively

DKS, PRC 71 (2005) 034905.

A one-dimensional analysis of the correlation function C is performed in terms of the invariant momentum difference as follows:

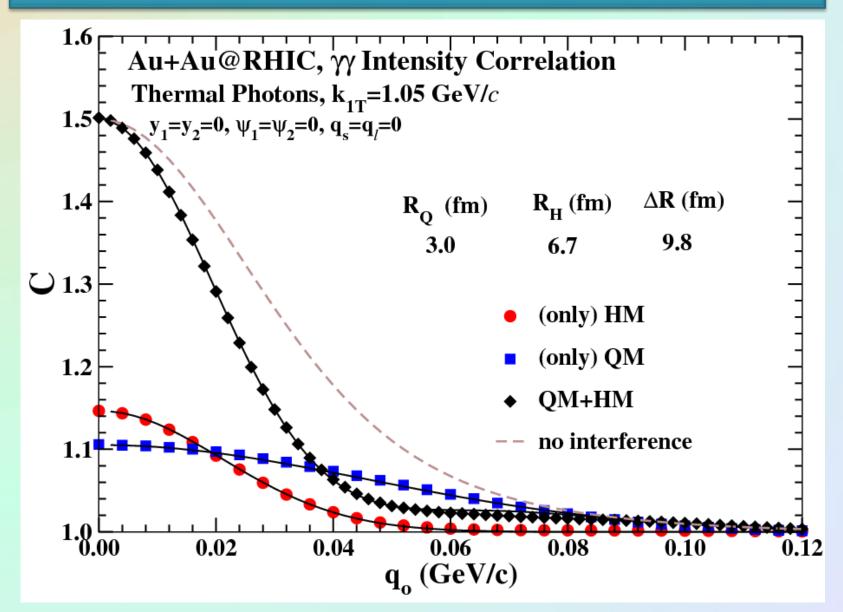
$$C(q_{inv}) = 1 + \frac{1}{2} \lambda \exp\left[-q_{inv}^{2} R_{inv}^{2}/2\right]$$

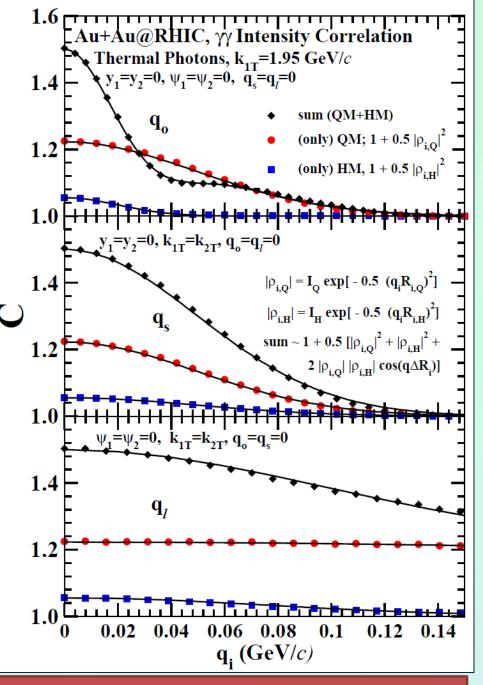
$$q_{inv} = \sqrt{-(k_{1}^{\mu} - k_{2}^{\mu})^{2}} = \sqrt{-q_{0}^{2} + q^{2}}$$

$$= \sqrt{2k_{1T}k_{2T}} \left[\cosh(y_{1} - y_{2}) - \cos(\psi_{1} - \psi_{2})\right]$$
where,  $q^{2} = q_{out}^{2} + q_{side}^{2} + q_{long}^{2}$ 

For  $y_1 = y_2 = 0$  and  $\psi_1 = \psi_2 = 0$ ,  $q_{side} = q_{long} = q_{inv} = 0$ , but  $q_{out} = k_{1T} - k_{2T}$ .ne.0

#### Outward correlation function of thermal photons for 200A GeV Au+Au collision at RHIC





DKS and R. Chatterjee; arXiv: 0907.1360

The outward, sideward, and longitudinal correlation functions for thermal photons produced in central collision of gold nuclei at RHIC taking  $\tau_0 = 0.2$  fm/c. Symbols denote the results of the calculation, while the curves denote the fits.

Correlation function in the two phases can be approximated as

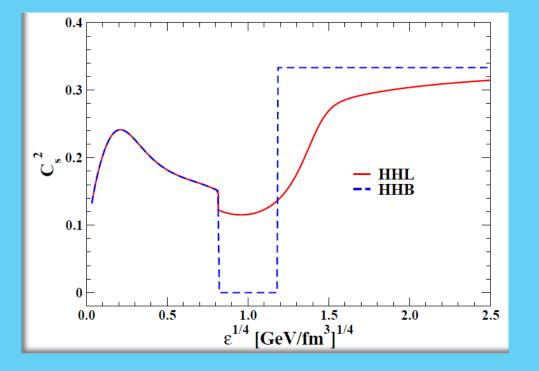
$$C(q_{i,\alpha}) = 1 + 0.5 |\rho_{i,\alpha}|^2$$

where,

$$\rho_{i,\alpha} = I_i \exp[-0.5 q_i^2 R_{i,\alpha}^2]$$

i=out, side, and long α= quark matter (Q) or hadronic matter (H)

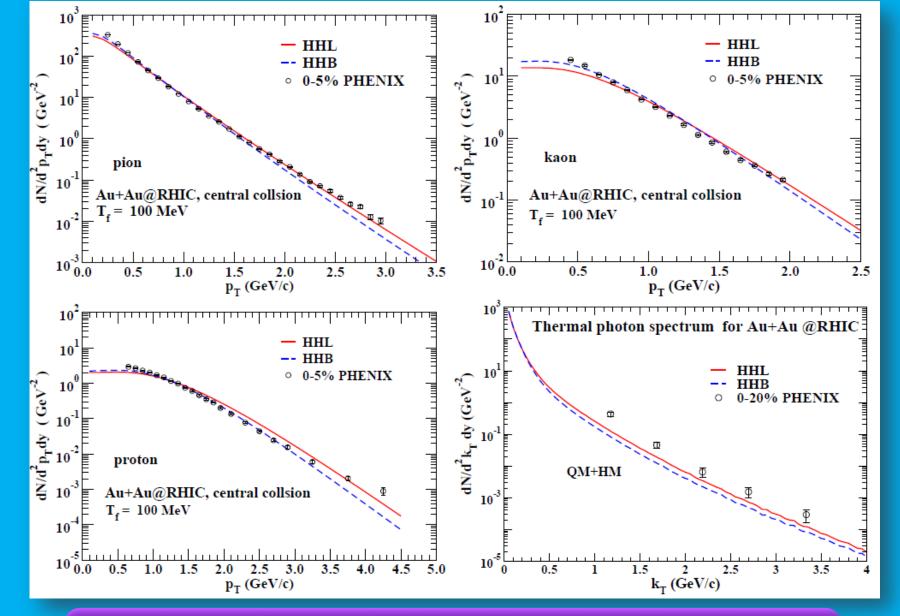
# How Sensitive Are We to Equation of State?



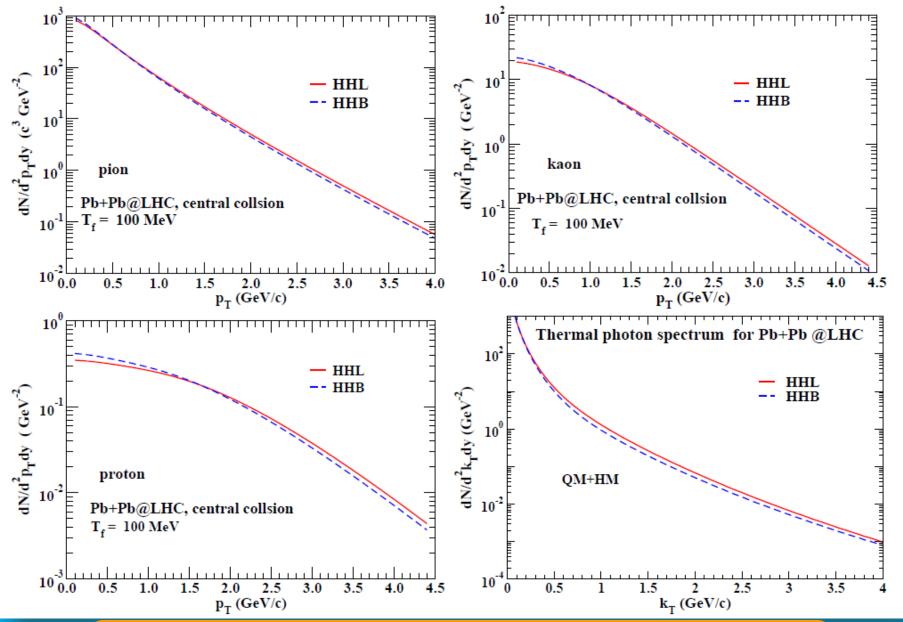
(i) Volume corrected hadron and Hagedorn resonance gas matched with a Bag Model ((HHB).

(v) Volume corrected hadron and Hagedorn resonance gas matched with Lattice calculations (HHL).

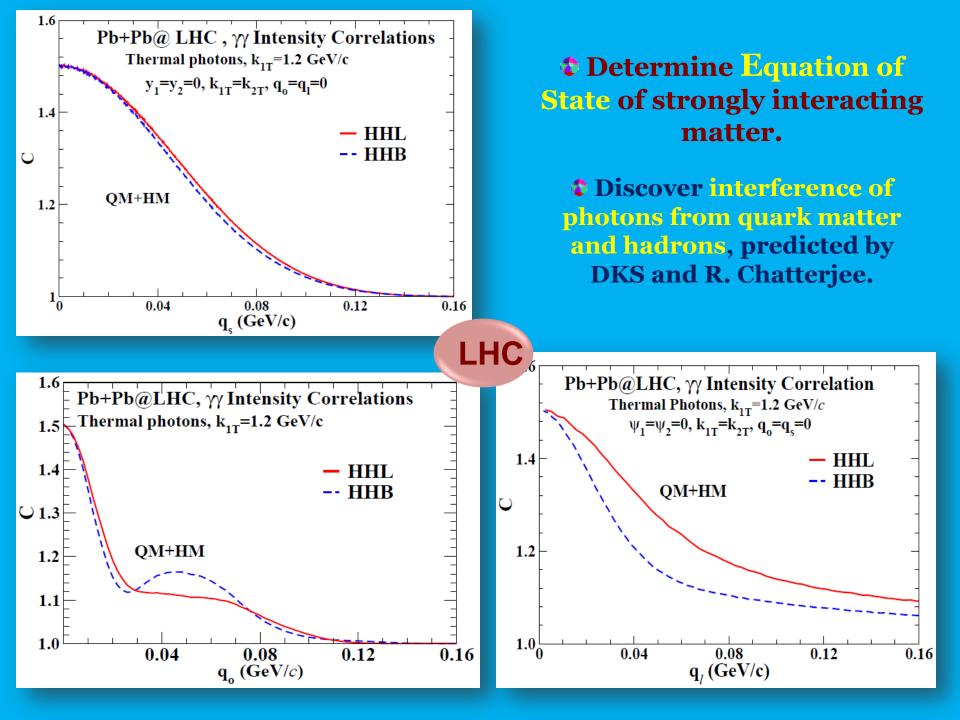
#### **Speed of sound**



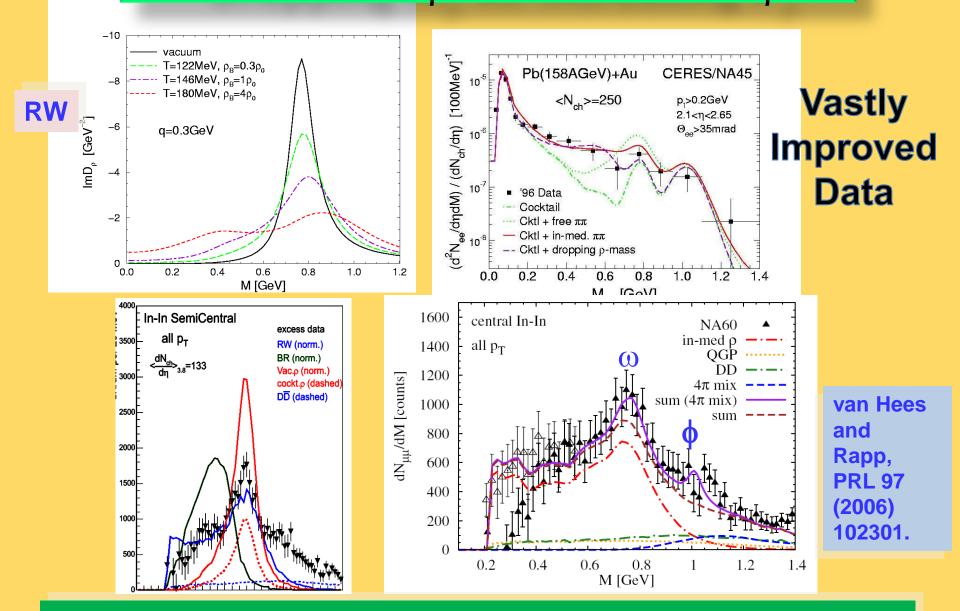
Pion, kaon, proton and thermal photon p<sub>T</sub> spectra at RHIC for the equations of state, HHB and HHL. All the calculations are for impact parameter b=0 fm.



Pion, kaon, proton and thermal photon  $p_T$  spectra at LHC for the equations of state, HHB and HHL. All the calculations are for impact parameter b=0 fm.



### Dropping $m_{\rho}$ vs. increasing $\Gamma_{\rho}$

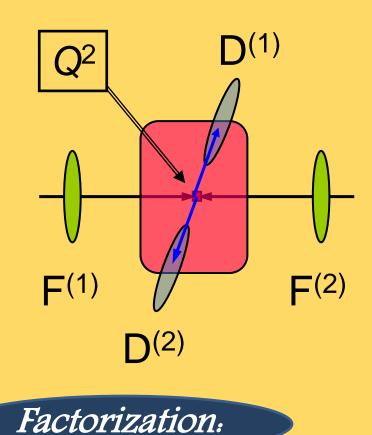


Only brodening of  $\rho$  (RW) observerd, no mass shift (BR)

## Passage of Jets Through QGP

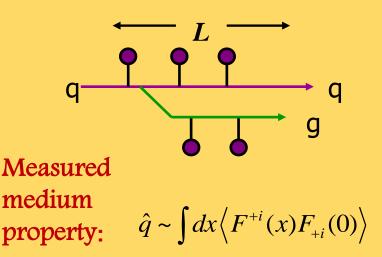
## PQCD framework: Jets

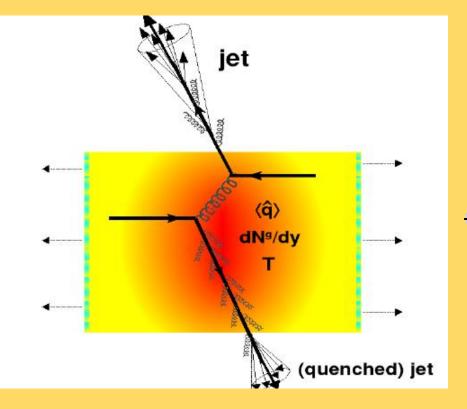
 $\sum_{X} \frac{d\sigma_{AA' \to hh' + X}}{dQ^2} = \sum_{p,p'} F_{A \to p}^{(1)} F_{A' \to p'}^{(2)} \otimes \sum_{\tilde{p}\tilde{p}'} \frac{d\sigma_{pp' \to \tilde{p}\tilde{p}'}}{dQ^2} \otimes \widetilde{D}_{\tilde{p} \to h}^{(1)} \widetilde{D}_{\tilde{p}' \to h'}^{(2)}$ 



Medium modified fragmentation functions.

$$\tilde{D}_{p \to h}(z) = D_{p \to h}\left(\frac{z}{1 - \Delta E / E}\right)$$





+Jet quenching is considered as one of the most promising signatures of formation of QGP

 It is defined as the suppression of high momentum particle spectra, arising due to energy loss of partons prior to fragmentation.

It is quantatively measured through the nuclear modification factor  $R_{AA}$ , which is defined as:

$$R_{AA}(p_T,b) = \frac{d^2 N_{AA}(b) / dp_T dy}{T_{AA}(b) d^2 \sigma_{NN} / dp_T dy}$$

## Dilepton vs. photon tagged jets

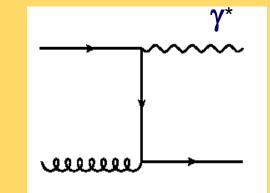
### **Photon tagged jets:**

- Difficult measurement:
- At low  $p_T$ ,  $\pi^0 \rightarrow \gamma\gamma$  large background.
- At higher p<sub>T</sub>, background problem better but opening angle becomes smaller.

### **Dilepton tagged jets:**

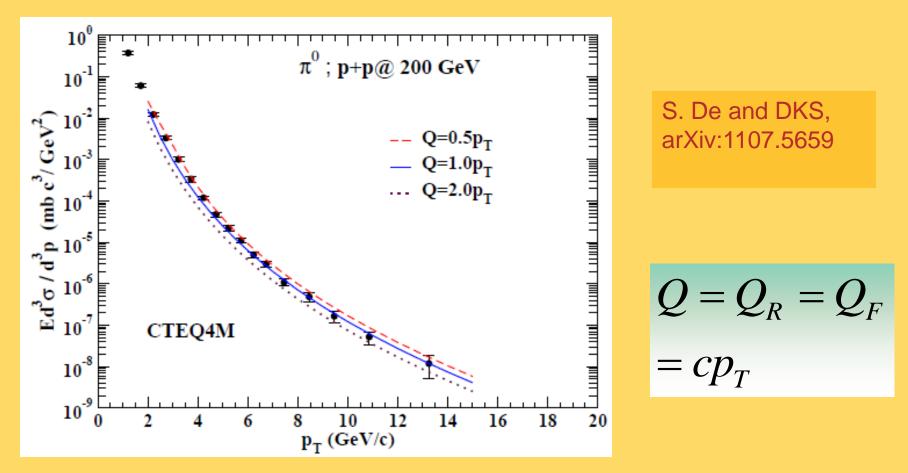
- Lower yield but lower back-ground.
- Charm and beauty decay could be identified.
- M and p<sub>T</sub>: two handles!
- Gold plated standard via Z<sup>0</sup> tagging at LHC.

S., Gale, & Awes, PRC 67 (2003) 054904; Lokhtin et al, PLB 599 (2004) 260.



Compton

#### **Neutral pion production for p-p collisions at RHIC**



•Next-to- leading order  $O(\alpha_s^3)$  calculations are used.

CTEQ4M parton distribution function.

BKK fragmentation function.

While calculating particle production in AA collisions, we include:

Nuclear shadowing. (EKS98 parameterization)

□ Energy loss of partons in the medium.

Average path length traversed by the parton.

The average path length  $L(\phi,b)$  traversed by a parton for non-central collisions of impact parameter b.

$$L(\varphi,b) = \frac{\iint l(x, y, \varphi, b) T_{AB}(x, y; b) dx dy}{\iint T_{AB}(x, y; b) dx dy}$$

We follow a simple phenomenological model based on the formalism of **Baier et.al.** and first used by S. Jeon et al at RHIC energies, to estimate parton energy loss.

The formation time of the radiated gluon:

$$t_{form} = \frac{\omega}{k_T^2}$$

 $\epsilon$  - energy loss per collision,  $\lambda_a\text{-}$  mean free path:

where  $E_{LPM} = \lambda_a \langle k_T^2 \rangle$ 

The probability for a parton to scatter n times before it leaves the medium

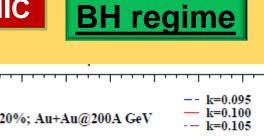
$$P_a(n,L) = \frac{\left(L/\lambda_a\right)^n}{n!} e^{-L/\lambda_a}$$

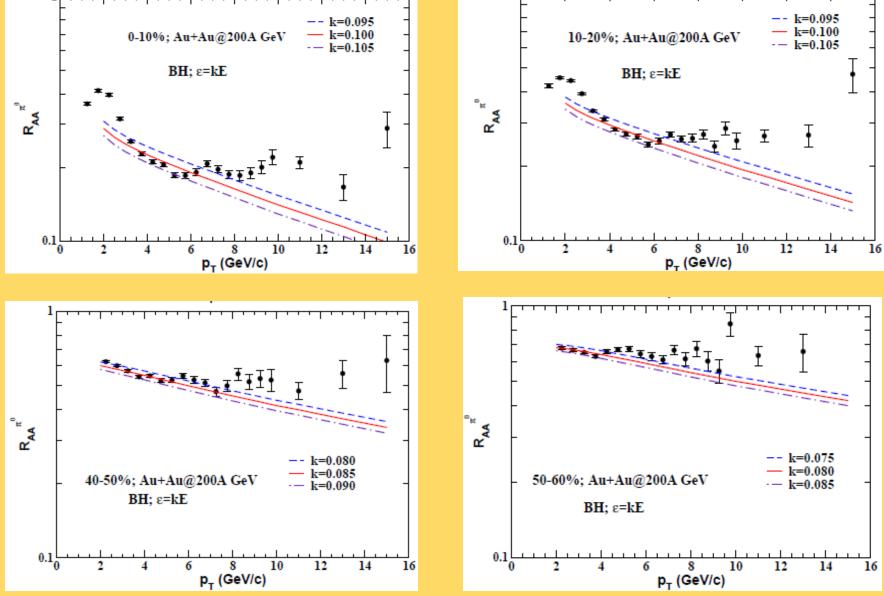
The effect of energy loss of partons and multiple scatterings are implemented through the modification of D<sub>c/h</sub>(z,Q<sup>2</sup>) following the model of Wang-Huang-Sarcevic.

$$zD_{c/h}(z,L,Q^2) = \frac{1}{C_N^a} \sum_{n=0}^N P_a(n,L) \times \left[ z_n^a D_{c/h}^0(z_n^a,Q^2) + \sum_{m=1}^n z_m^a D_{g/h}^0(z_m^a,Q^2) \right]$$

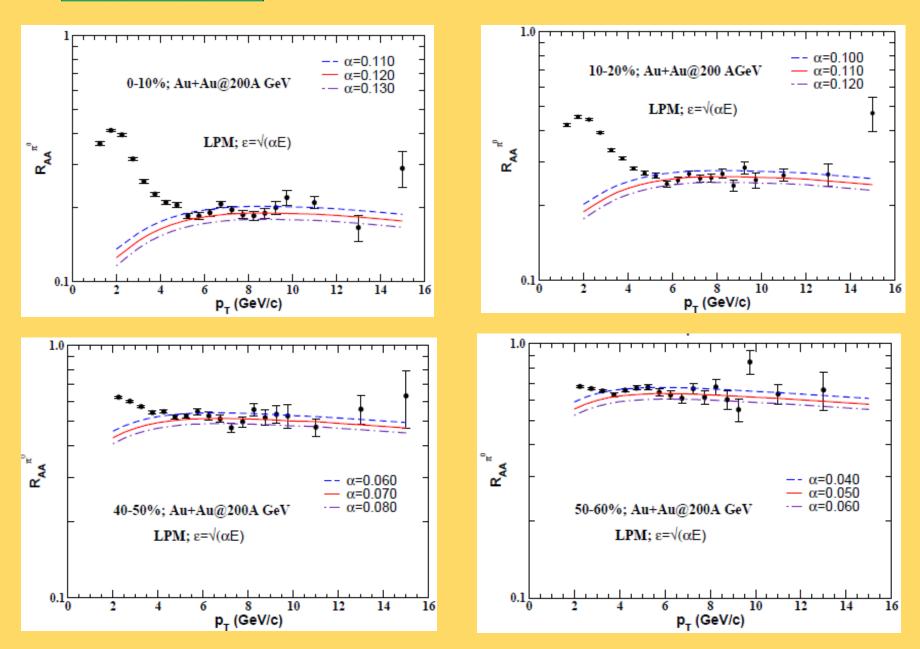
where, 
$$C_{N}^{a} = \sum_{n=0}^{N} P_{a}(n,L)$$
,  $z E_{T}^{a} = z_{n}^{a} (E_{T}^{a} - \sum_{i=0}^{n} \mathcal{E}_{a}^{i})$  and  $z_{m}^{a} \mathcal{E}_{a}^{m} = z E_{T}^{a}$ 

#### **R<sub>AA</sub> of neutral pions for Au-Au collisions at RHIC**

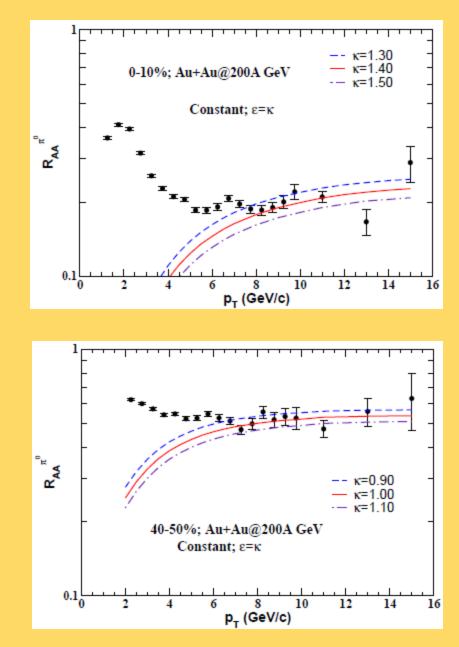


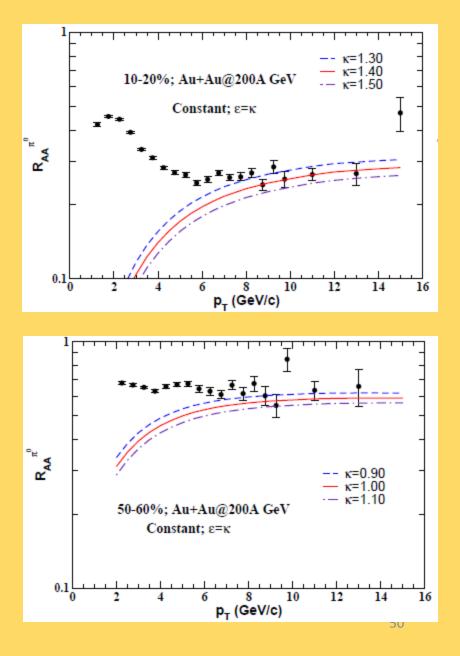




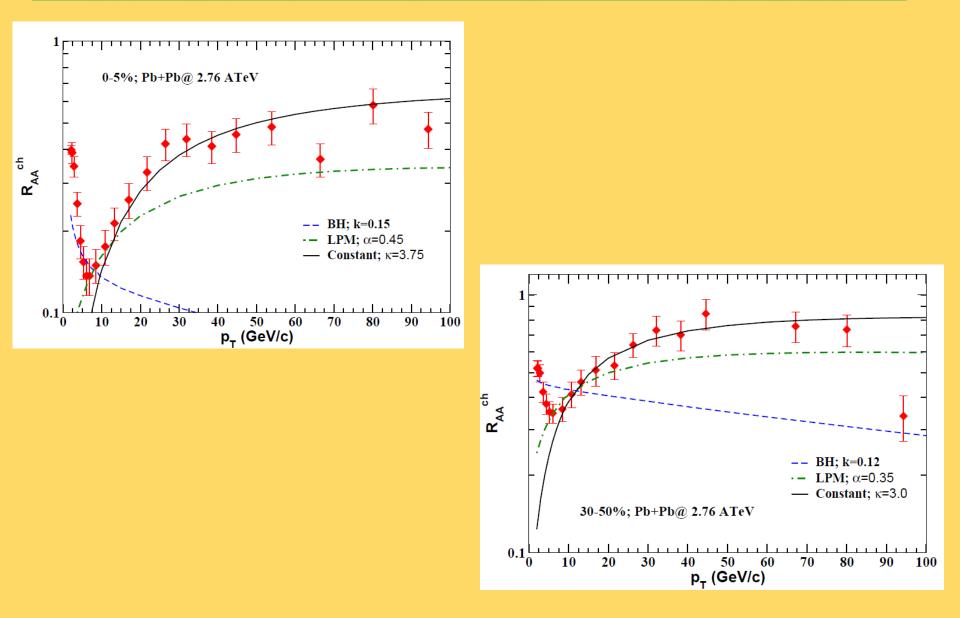


#### **Complete Coherence Regime**





#### **R<sub>AA</sub>** of charged hadrons for Pb+Pb @ 2.76 ATeV : CMS preliminary

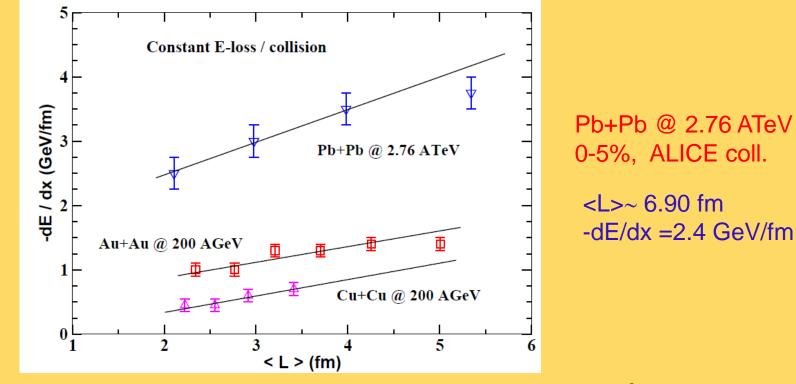


#### Centrality dependence of dE /dx at RHIC & LHC

Taking the case of parton energy loss in the complete coherence regime, - dE/dx =  $\epsilon / \lambda$ 

The concerned partons having  $p_T \ge 8 \ GeV / c$  at RHIC and

 $p_T \ge 10 \ GeV/c$  at LHC



We see that the energy lost by the partons,

 $\Delta E \propto L^2$ 

# **Heavy Quark Propagation**

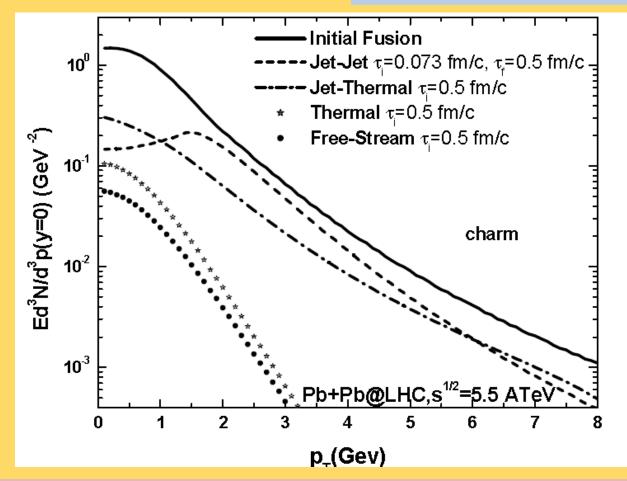
## **4** Initial Fusion

- Jet-jet interaction
- Thermal production
- Passage of jets through Quark Gluon Plasma.
- NLO effects.
- Back to back correlations
- dE/dx



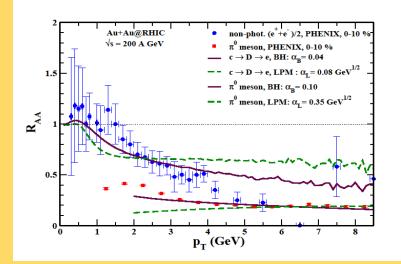
### **Heavy Quark Production**

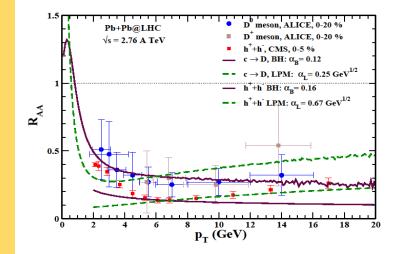
M. Younus & DKS, J. Phys. G 37, 115006 (2010)



Taking pp collisions as the base-line may not be appropriate as mechanisms other than initial fusion may contribute. There is also a growing evidence for multiple scatterings of partons in pp collisions.

#### Energy and flavour dependence of parton energy loss





 $\Delta p = \alpha_{\rm B} p$ 

 $\Delta p = \alpha_L \sqrt{p}$ 

Refs: JPG 39, 095003 (2012); 015001 (2012); arXiv: 1112.2492

Bethe- Heitler Limit of Incoherent Radiation:

LPM Limit of Coherent Radiation:

**RHIC:**  $\alpha_{\rm B}^{\rm Light} \approx 2.5 \, \alpha_{\rm B}^{\rm Heavy}$  **LHC:**  $\alpha_{\rm B}^{\rm Light} \approx 1.3 \, \alpha_{\rm B}^{\rm Heavy}$ 

# Conclusions

- The discovery of quark gluon plasma has provided confirmation of one of the most spectacular predictions of QCD- the theory of strong interactions.
- Single photons, dileptons, jets, and heavy quarks provide interesting details of initial stage of the plasma and its dynamics.
- The initial state in these collisions is hot ~300-500 MeV and dense, 20-100 GeV/fm^3, similar to the matter in early universe.

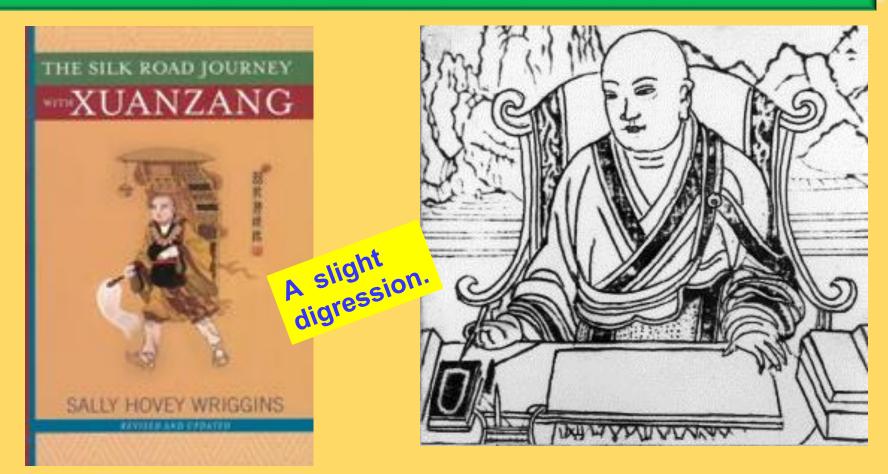


## Back up slides

## If I had more time:

- Intensity Interferometry of direct photons
- **D. K. Srivastava,** PLB 307(1993)1.
- D. K. Srivastava and J. I. Kapusta, PRC 48 (1993) 1335.
- **D. K. Srivastava**, PRD 49 (1994) 4523.
- S. A. Bass, B. Muller, D. K. Srivastava, PRL 16 (2004) 162301;
- **D. K. Srivastava,** PRC 71 (2005) 034905.
- **D. K. Srivastava & R. Chatterjee**, PRC 80(2009) 054914.
- S. De, R. Chatterjee, D. K. Srivastava, J. Phys. G37 (2010) 115004.

### **Most Reliable Historians of Ancient India**

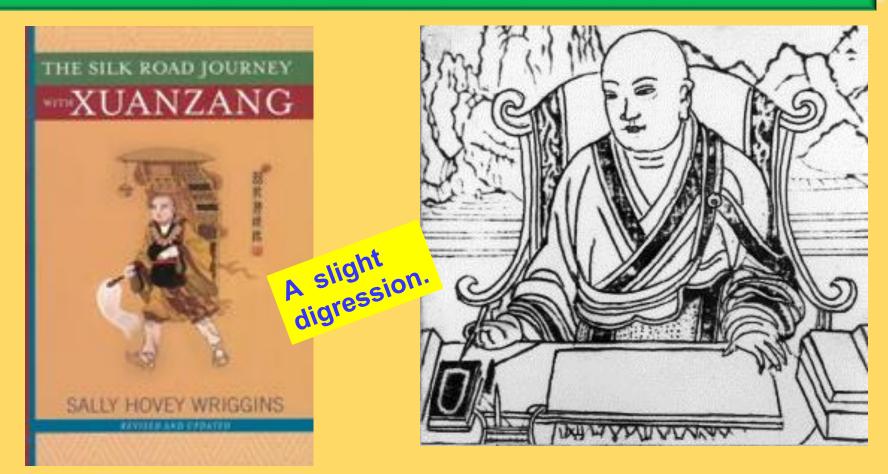


"A Record of Budhist Kingdoms": Fa Hien (337-422 AD): visited India during 399-414 AD.

"Journey to the Western World": Huen Tsang (Yuoan Chwang) 603-664 AD: visited India during 630-645 AD.

They traversed India like photons and dileptons and left most valuable records!!

### **Most Reliable Historians of Ancient India**



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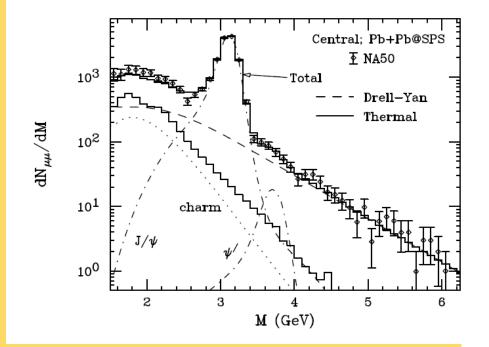
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### Intermediate Mass; NA50

units)

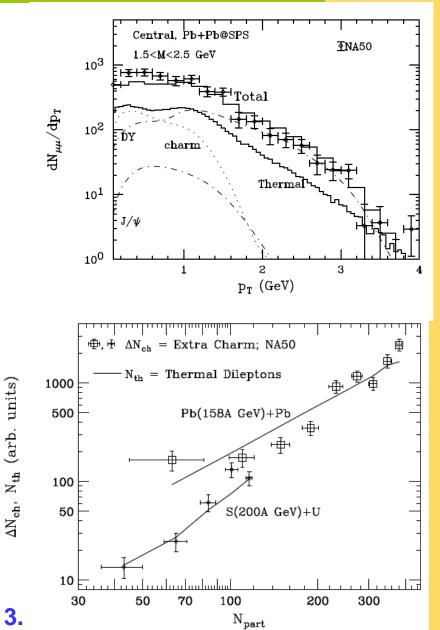
(arb.



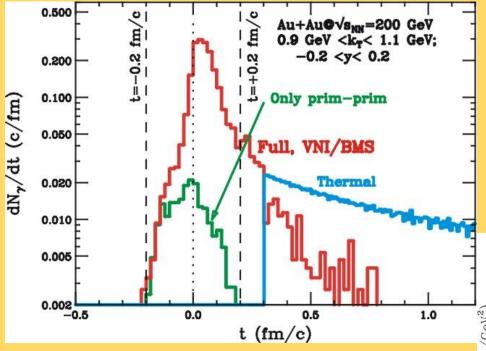
#### Kvasnikova, Gale, & Srivastava, PRC 65 (2002) 064903.

Acceptance and detector resolution accurately modeled.

See also Rapp & Shuryak, PLB 473 (2000) 13.



### Photons: pre-equilibrium vs. thermal



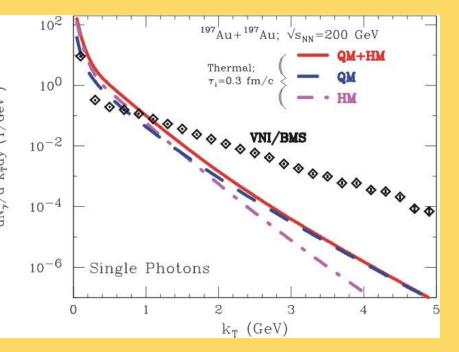
short emission time in the PCM, 90% of photons before 0.3 fm/c

> hydrodynamic calculation with  $\tau_0 = 0.3$ fm/c allows for a smooth continuation of emission rate

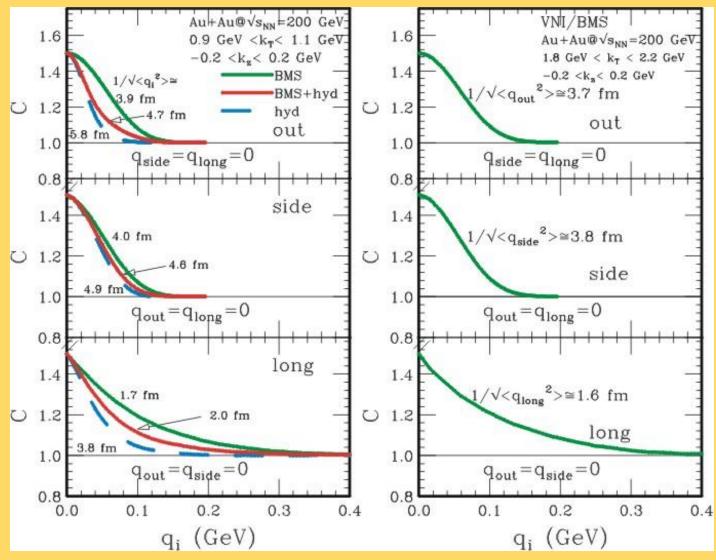
> caveat: medium not equilibrated at  $\tau_0$ 

 pre-equilibrium contributions are easier identified at large p<sub>t</sub>:
 window of opportunity above p<sub>t</sub>=2 GeV

## •at 1 GeV, need to take thermal contributions into account



## **Photons: HBT Interferometry**

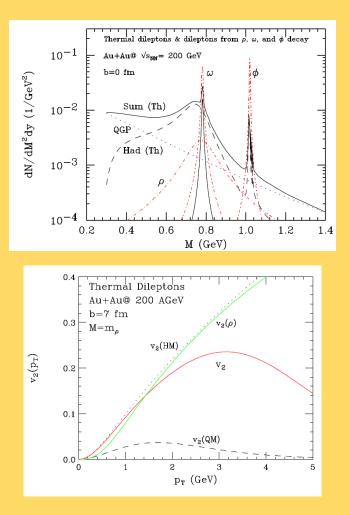


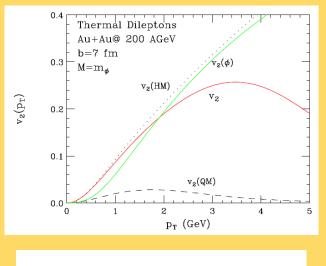
 p<sub>t</sub>=2 GeV: prethermal photons dominate, small radii

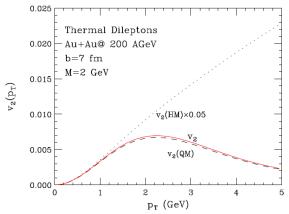
•p<sub>t</sub>=1 GeV: superposition of pre- & thermal photons: increase in radii

Bass, Mueller, & Srivastava, PRL 93 (2004) 16230; Srivastava, PRC 71 (2005) 034905.

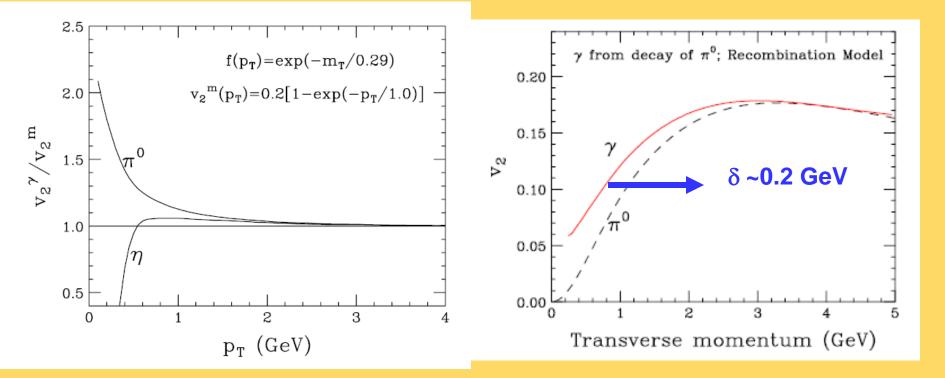
## **Elliptic Flow of Thermal Dileptons**







### **Elliptic Flow of Decay Photons**



$$v_2(k_T) \approx v_2^{\pi^0}(p_T),\tag{7}$$

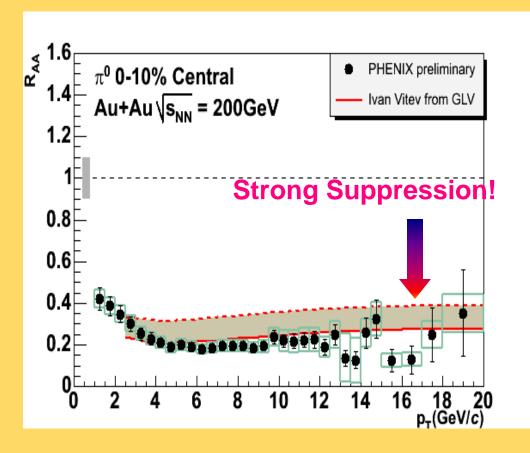
where

$$p_T \approx k_T + \delta \tag{8}$$

and  $\delta \approx 0.1-0.2$  GeV, for  $k_T > 0.2$  GeV, to an accuracy of better than 1%-3%.

## Layek, Chatterjee, Srivastava, PRC 74 (2006) 044901.

## **Theoretical Interpretation of High-p**<sub>T</sub> $\pi^0$ **Suppression**

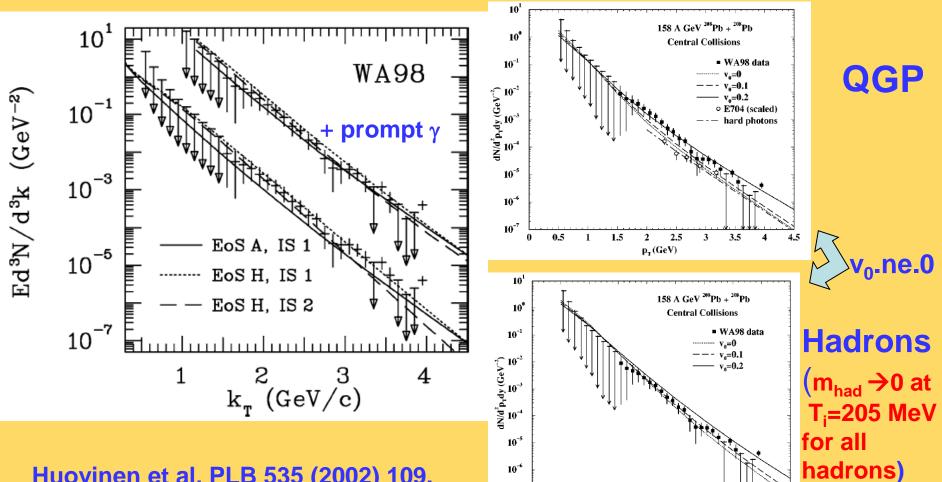


$$R_{AA}(p_T) = \frac{(1/N_{evt}^{AA}) d^2 N_{ch}^{AA}/d\eta dp_T}{\langle N_{coll} \rangle (1/N_{evt}^{pp}) d^2 N_{ch}^{pp}/d\eta dp_T}$$

• Large suppression implies large energy loss. Model calculations indicate high gluon densities  $dN_g/dy \sim 1100$ 

• Implies large energy density (as do also  $E_T$  measurements)  $\epsilon$ > 10 GeV/fm<sup>3</sup> well above critical energy density  $\epsilon_{crit} \sim 1$  GeV/fm<sup>3</sup>

## **QGP or Hot Hadrons? Enter WA98**



 $10^{-7}$ 

0

0.5

1

1.5

2

p<sub>r</sub>(GeV)

2.5

Huovinen et al, PLB 535 (2002) 109. QGP or hadrons ( $n_{had} >> 1/fm^3$ at T<sub>i</sub> = 245-275 MeV)

Alam et al, PRC 63 (2001) 021901 (R).

3

3.5

4

4.5