

# Color Glass Condensate signatures and phenomenology at RHIC and LHC.

Prithwish Tribedy

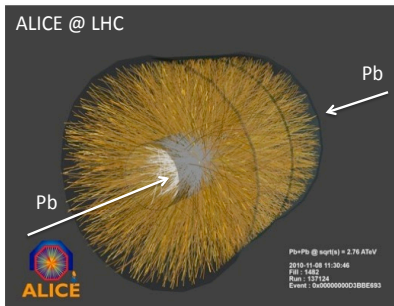
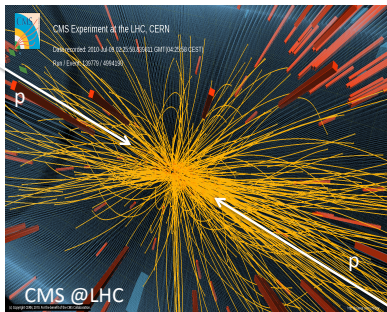
Variable Energy Cyclotron Center, Kolkata, India

Sept 10, 2013

Triggering Discoveries in High Energy Physics, Jammu, India

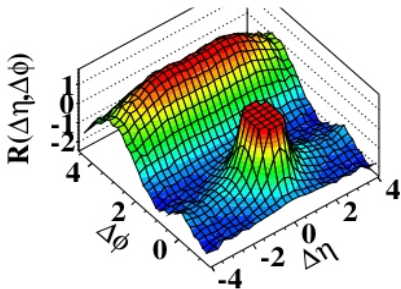
# Outline

- ▶ Introduction.
- ▶ DIS processes at HERA and Gluon Saturation.
- ▶ The Color Glass Condensate & framework of CYM.
- ▶ Inclusive multiplicity & multi-particle correlation.
- ▶ Modelling initial stage geometry in  $p+p$ ,  $p+A$  and  $A+A$  collisions.



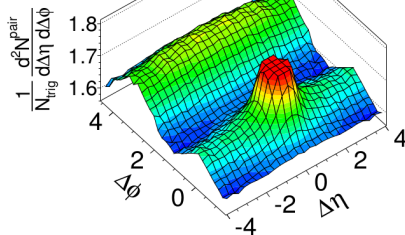
- ▶ Why does number of produced particles fluctuate from event-to-event ?
- ▶ Can we calculate how many particles are produced in an *ab-initio* approach?

(d) CMS  $N \geq 110$ ,  $1.0 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$



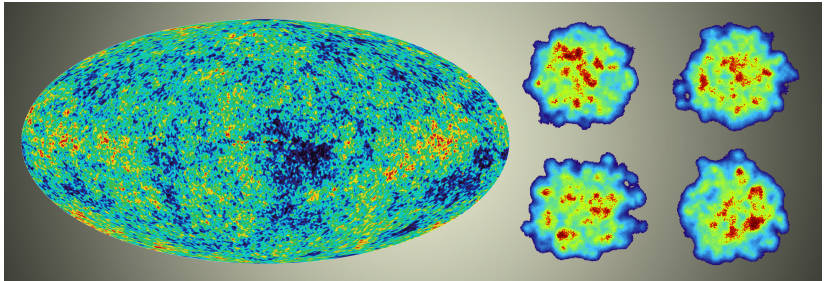
CMS pPb  $\sqrt{s_{NN}} = 5.02 \text{ TeV}$ ,  $N_{\text{trk}}^{\text{offline}} \geq 110$   
 $1 < p_T < 3 \text{ GeV}/c$

(b)

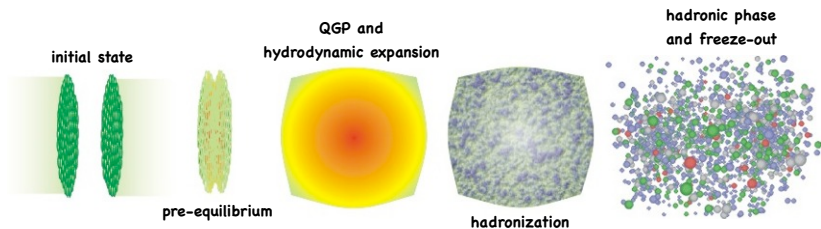


- ▶ How does collimation come? What is the source of intrinsic ridge and long range correlation?





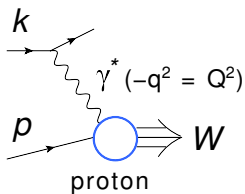
- ▶ What is the scale of initial quantum fluctuations in the mini-bang ?



Standard model of heavy ion collisions:

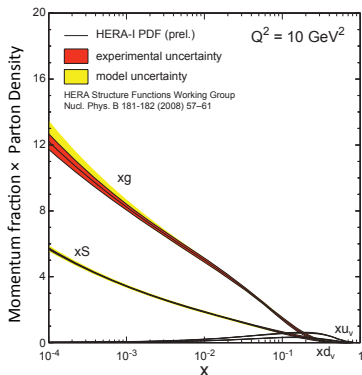
- ▶ How to get an *ab initio* description of the early stages of HIC?
- ▶ How to constrain the transport coefficients ?

# DIS process at HERA



High energy limit  $\rightarrow$  small  $x$  limit of QCD

$$(x \approx \frac{Q^2}{E_{cms}^2} = \frac{Q^2}{s})$$



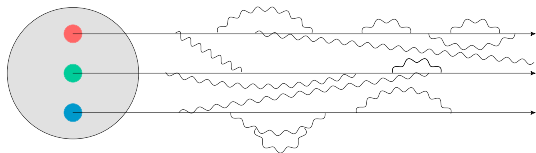
HERA e-p scattering probes protons with :

Transverse resolution  $\Delta r_{\perp} \sim \frac{1}{Q}$

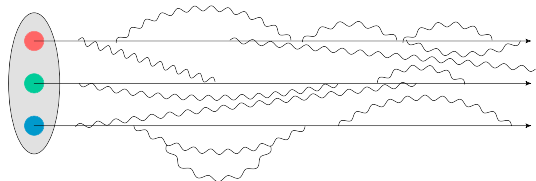
Time resolution  $\Delta t \sim \frac{2xp}{Q^2}$

$\rightarrow$  Rapid growth of gluons at small  $x$

## High energy hadrons/nuclei



Hadron at rest



Boosted hadron

At high energies interaction time scales of fluctuations dilated well beyond typical hadronic time scales.

# DIS: Snapshot of hadrons/nuclei

$$\Delta r_{\perp} \sim \frac{1}{Q} \quad , \quad \Delta t \sim \frac{2xp}{Q^2} \quad , \quad x = \frac{Q^2}{s}$$

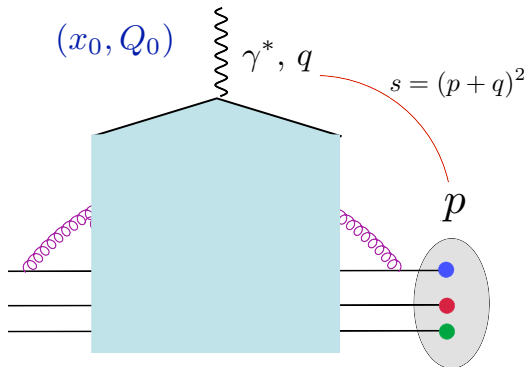
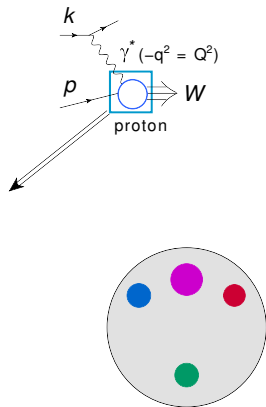


figure: Albacete QM'12



# DIS: Snapshot of hadrons/nuclei

$$\Delta r_{\perp} \sim \frac{1}{Q} \quad , \quad \Delta t \sim \frac{2xp}{Q^2} \quad , \quad x = \frac{Q^2}{s}$$

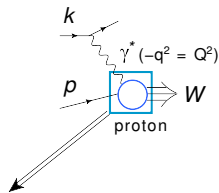
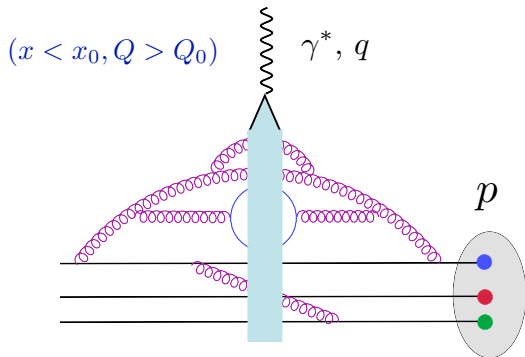


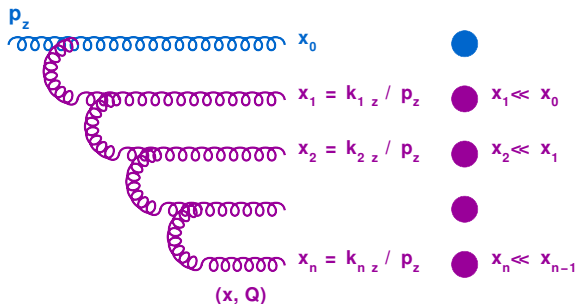
figure: Albacete QM'12

Finer resolution reveals more sub structure (higher Fock states)  
 at smaller  $x$ ,  $|H\rangle = |qqq\rangle + |qqqg\rangle + \dots + |qqqgg \dots gg\rangle$

# QCD evolution equations

$$dP_{q/g \rightarrow g} = \frac{\alpha_s C_F / A}{\pi} \frac{dx}{x} \frac{d^2 k_{\perp}}{k_{\perp}^2}$$

BFKL Evolution  
Fixed  $Q^2, x \rightarrow 0$



Probability of emitting  $n$  gluons  
 → enhanced by large logarithms

$$\mathcal{P}(n) \sim \frac{1}{n!} \left( \alpha_s \ln \left( \frac{x_0}{x} \right) \right)^n$$

# QCD evolution equations

BFKL growth is linear



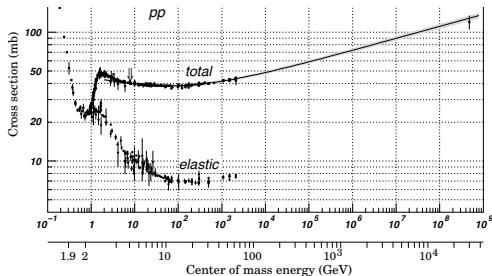
BFKL equation:

$$\text{PDF } xg(x) \approx \int d^2k_{\perp} \phi(x, k_{\perp})$$

$$\frac{\partial \phi(x, k_{\perp})}{\partial \log(x_0/x)} \approx \mathcal{K} \otimes \phi(x, k_{\perp})$$

$$\rightarrow \phi_{\text{BFKL}} \sim x^{\alpha_s}$$

$$\Rightarrow \sigma_{\text{tot}}^{p+p} \sim s^{\alpha_P - 1}$$



(Experimental  $\sigma_{\text{tot}}$   $\rightarrow$  grows logarithmically)

Linear Bremsstrahlung growth of PDF  $\rightarrow$  power law growth of cross section

$\rightarrow$  Violates black disc limit as  $\sigma_{\text{tot}} \leq 2\pi R^2$

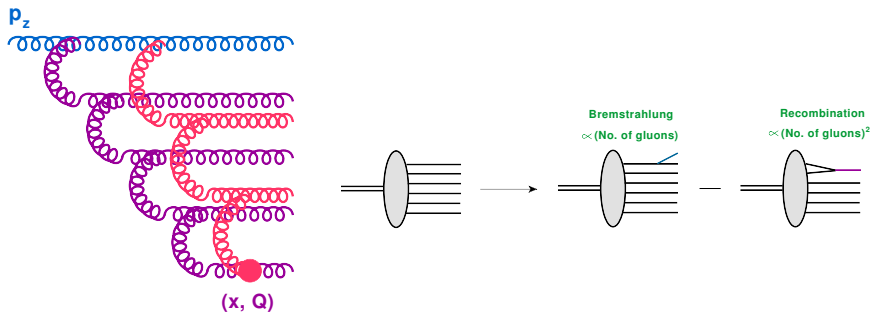
Froissart - Martin unitarity bound ( $\sigma_{\text{tot}} \sim \ln^2 s$ )



# QCD Evolution equations

Non-linear recombination processes constrain the growth

→ Saturation



$$\frac{\partial \phi(x, k_{\perp})}{\partial \log(x_0/x)} \approx \mathcal{K} \otimes \phi(x, k_{\perp}) - \phi(x, k_{\perp})^2 \quad \text{BK/JIMWLK equation}$$

Non-linear equation gives rise a scale,  $Q_s^2(x) \rightarrow$  saturation scale.

# Gluon saturation

Gribov, Levin, Ryskin 1983

No of gluons of a fixed size saturates due to phase space constrain.

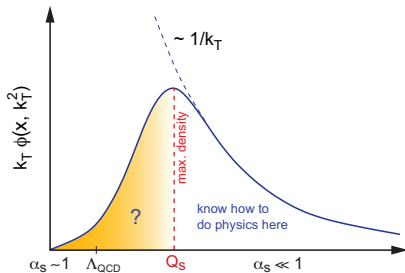
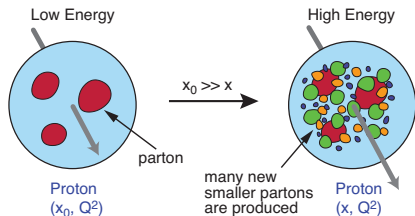


figure: 1212.1701

Density saturates with max. occupancy  $\sim \mathcal{O}(\frac{1}{\alpha_s})$  for  $k_T \leq Q_s(x)$

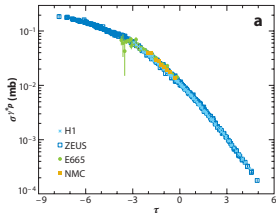
Higher energy  $\rightarrow$  larger  $Q_s \gg \Lambda_{QCD}$ , effective coupling  $\alpha_s(Q_s)$  is small

# Geometric scaling

DIS cross section scales with

$$\tau = \frac{Q^2}{Q_S(x)^2}$$

$$\sigma_{DIS}(x, Q^2) = \sigma_{DIS}(Q^2/Q_S^2(x))$$

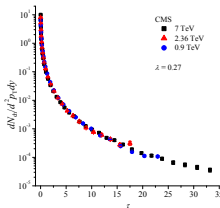


Stasto, Golec-Biernat & Kwiecinski 2001  
Levin, Tuchin '99, Iancu, Itakura, McLerran '02

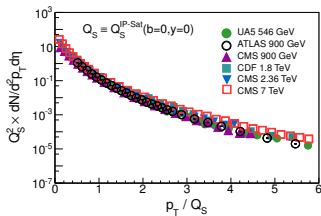
p+p multiplicity scales with

$$\tau = \frac{p_T^2}{Q_S(x)^2} \text{ or } \frac{p_T}{Q_S}, \quad (x \equiv \frac{p_T}{\sqrt{s}} e^{\pm y})$$

$$\frac{1}{\sigma} \frac{dN_{ch}}{d\eta d^2p_T} = F\left(\frac{p_T}{Q_S(p_T/\sqrt{s})}\right)$$



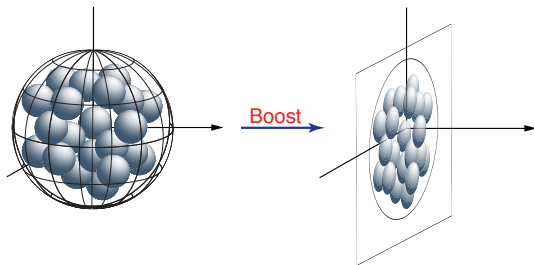
McLerran & Praszalowicz 2010, PT & Venugopalan 2010



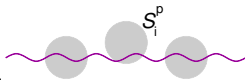
Saturation scale  $Q_S(x)$  is the dominant scale controlling the dynamics of particle production in  $e + p$  and  $p + p$ .

# Universality and Nuclear oomph

Gluon saturation  $\rightarrow$  Universal phenomenon to hadrons/nuclei.



For large nucleus, thickness  $R \sim A^{1/3}$ ,



Gluon momentum gets  $\rightarrow A^{1/3}$  transverse momentum random “kicks”

Nuclear Saturation scale  $(Q_s^A)^2 \approx A^{1/3}(Q_s^p)^2 \rightarrow$  Nuclear *oomph*

# Saturation models of HERA DIS

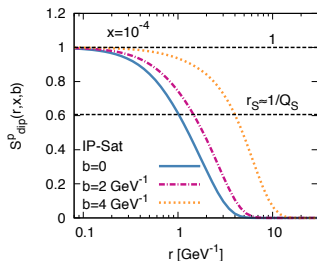
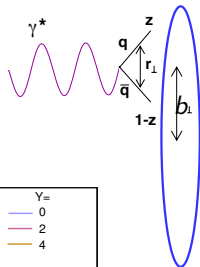
Bartels, Golec-Biernat, Kowalski  
Kowalski, Teaney

How to extract saturation scales/hadronic wave functions from HERA data?

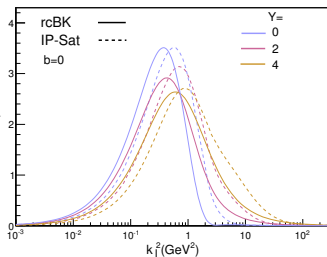
Cross section in  $e + p$  collisions is parametrized

The dipole scattering matrix for proton is

$$S_{\text{dip}}^p(\mathbf{r}_\perp, x, \mathbf{b}_\perp) = \exp(-r^2 Q_s(x, b)^2)$$



Fourier  
Transform



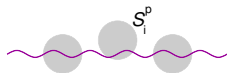
Saturation condition

$$S_{\text{dip}}^p(\mathbf{r}_\perp = r_S, x, \mathbf{b}_\perp) = \exp(-1/2) \implies Q_s^2 = \frac{2}{r_S^2}$$

# Color charge distribution inside Nuclei

The nuclear scattering matrix is obtained as

$$S_{\text{dip}}^A(\mathbf{r}_\perp, x, \mathbf{b}_\perp) = \prod_{i=0}^A S_{\text{dip}}^p(\mathbf{r}_\perp, x, \mathbf{b}_\perp)$$

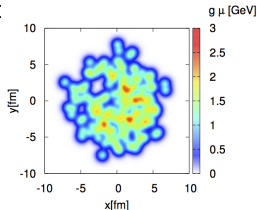


$i \rightarrow$  nucleons are distributed according to Fermi dist

$S_{\text{dip}}^A \rightarrow$  distribution of nuclear saturation scale

$\rightarrow$  distribution of color charge density.

Lumpy color charge density distribution  $g^2\mu(\mathbf{x}_\perp) \sim Q_s(\mathbf{x}_\perp)$



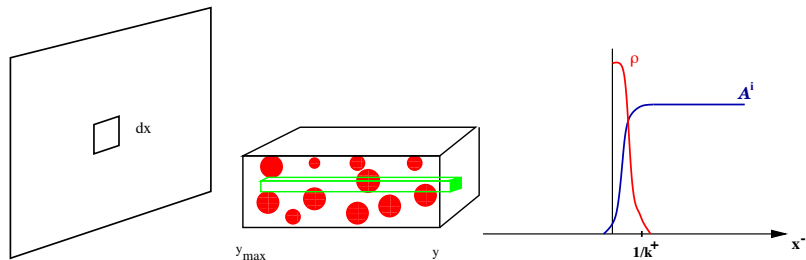
Kowalski, Lappi, Venugopalan 0705.3047

Lappi, arXiv:0711.3039, 1104.3725

# Color Glass Condensate

McLerran & Venugopalan hep-ph/9309289

High energy Nuclei/hadrons  $\rightarrow$  large parton density  $\rightarrow$  classical approx.



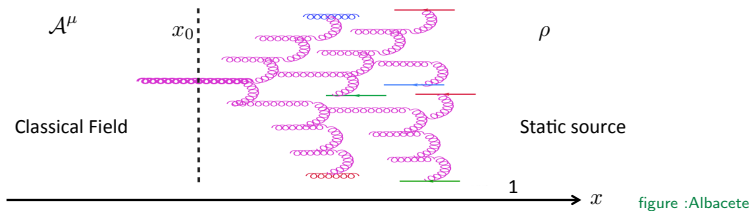
In the limit  $1/Q_S \ll dx \ll 1$  fm one can neglect

$$|[Q^a, Q^b]| = |if^{abc} Q^c| \ll Q^2$$

Random distribution of classical color charge.

# Color Glass Condensate

- ▶ Color: QCD (gluons carry color charge)
- ▶ Glass: Stochastic interactions, dynamics on very long time scales (time dilation).
- ▶ Condensate: Fields with large occupation  $\# \sim 1/\alpha_S$  with mom. peaked at  $k_T \approx Q_S$



A weak coupling effective theory with

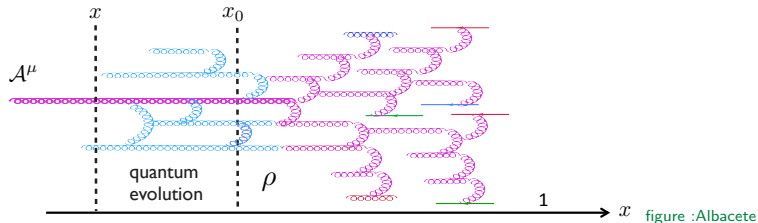
- ▶ Fast (large- $x$ ) partons  $\rightarrow$  static classical color source  $\rho$
- ▶ Slow (small- $x$ ) partons  $\rightarrow$  classical gluon fields  $\mathcal{A}^\mu$ .



# Color Glass Condensate

Quantum evolution of the color sources

- ▶ given by Renormalization Group description (BK/ JIMWLK).



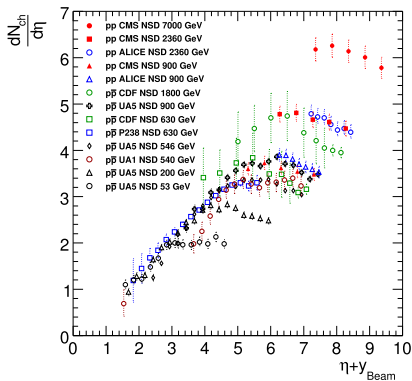
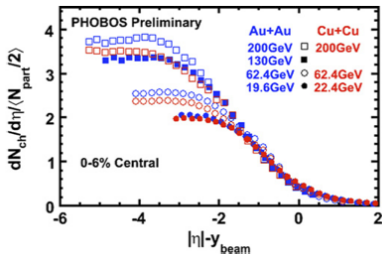
$x_0 \rightarrow x$  Integrating out degrees of freedom between  $x$  and  $x_0$ .

# Color Glass Condensate:

The Renormalization picture is evident in data.

Limiting fragmentation in  $A + A$  and  $p + p$ .

Busza NPA 854(2011) 57-63



$$x \sim e^{\pm y} / \sqrt{s} \Rightarrow$$

- ▶ Large rapidities d.o.f  $\rightarrow$  independent of energy.
- ▶ new physics  $\rightarrow$  additional d.o.f at small rapidity.

# Color Glass Condensate: McLerran-Venugopalan model

- ▶ Solve classical Yang-Mills equations

$$[D_\mu, F^{\mu\nu}] = J^\nu$$

for color current due to colliding sources ( $\rho_1$  and  $\rho_2$ )

$$J_a^\nu = g\delta^{\nu+}\delta(x^-)\rho_{1,a}(\mathbf{x}_\perp) + g\delta^{\nu-}\delta(x^+)\rho_{2,a}(\mathbf{x}_\perp)$$

- ▶ Extract the gauge field after collision for given color charge configuration.
- ▶ Final observables  $\mathcal{O}(\rho_1, \rho_2)$  should be averaged over color charge configuration

$$\langle \mathcal{O} \rangle = \int [d\rho_1][d\rho_2] W_y[\rho_1] W_y[\rho_2] \mathcal{O}(\rho_1, \rho_2).$$

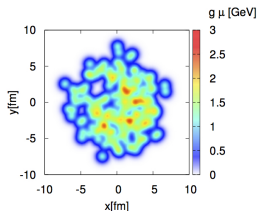
# Color Glass Condensate: McLerran-Venugopalan model

Averaging  $\langle \mathcal{O} \rangle \Rightarrow$  connection between sources  $\Rightarrow$  color correlation.  
In the MV model

$$W[\rho] \equiv \exp \left( - \int d^2 \mathbf{x}_\perp \frac{\rho^a(\mathbf{x}_\perp) \rho^a(\mathbf{x}_\perp)}{2 \mu_A^2} \right)$$

$\rho^a \rightarrow$  random sources distributed from local Gaussian.

fields  $\mathcal{A}(\mathbf{x}_\perp) \sim -\rho(\mathbf{x}_\perp)/\nabla_\perp^2 \Rightarrow \mathcal{A}(\mathbf{k}_\perp) \sim -\rho(\mathbf{k}_\perp)/\mathbf{k}_\perp^2$



Yang-Mills introduces non-local correlation over length scale  $1/Q_s$

$\rightarrow$  Glasma flux tube picture.

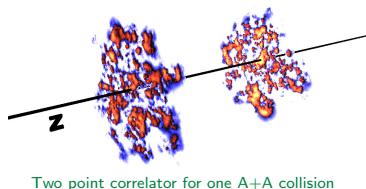
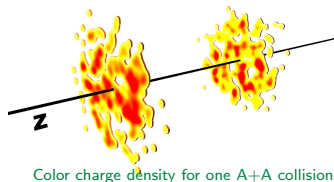
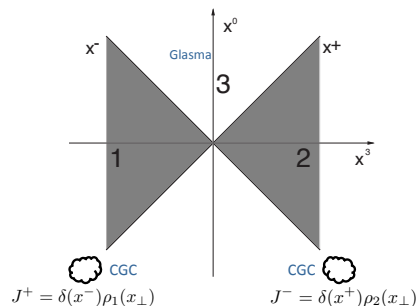
Gauge fields after collisions :

- ▶ **Analytical calculation** possible for lowest order of sources. For dilute-dilute(p+p) or dilute-dense(p+A)  $\rightarrow$   **$k_T$ -factorization**.
- ▶ For dense-dense (A+A) systems  $\rightarrow$  **numerical solution on lattice**.

# IP-Glasma : Classical Yang-Mills approach on 2+1D lattice

Schenke, Tribedy, Venugopalan PRL 108(2012)

E-by-E solve CYM for two colliding nuclei



$\rho(\mathbf{x}_\perp)$  sampled from local Gaussian distribution  $W[\rho]$

$$\langle \rho^a(\mathbf{x}_\perp) \rho^b(\mathbf{y}_\perp) \rangle = \delta^{ab} \delta^2(\mathbf{x}_\perp - \mathbf{y}_\perp) g^2 \mu^2(\mathbf{x}_\perp)$$

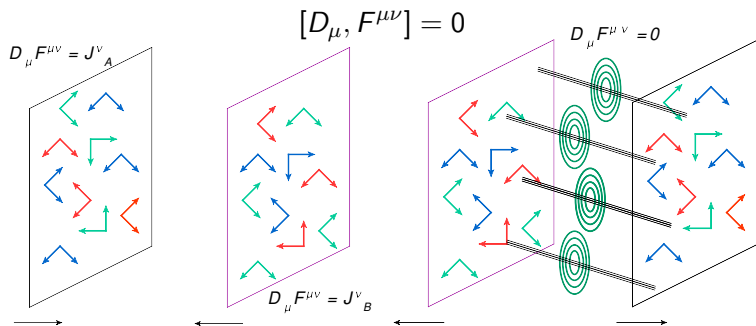
# IP-Glasma : CYM evolution after collision

Kovner, McLerran, Weigert

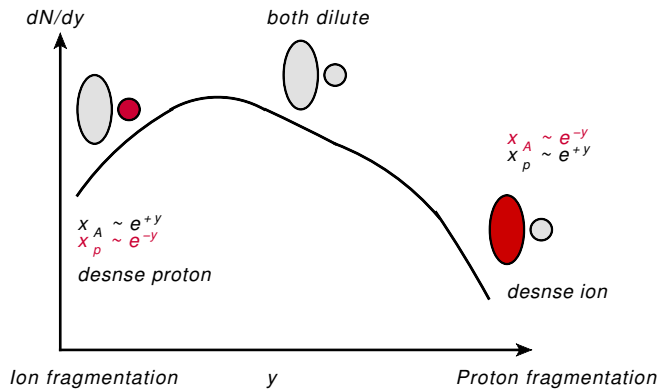
The field after collision at  $\tau = 0$  has simple relation

$$A^i = A_{(A)}^i + A_{(B)}^i, \quad A^\eta = \frac{ig}{2} [A_{(A)}^i, A_{(B)}^i]$$

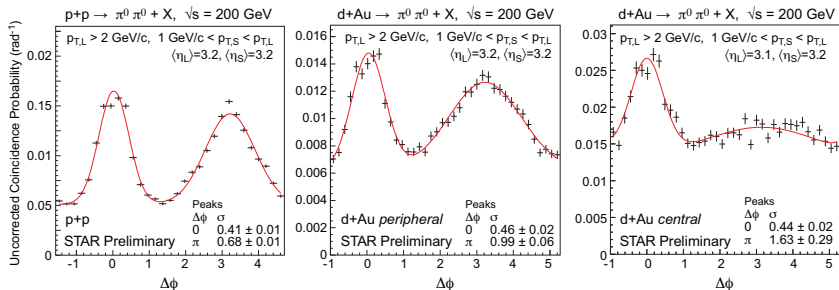
The fields are evolved at  $\tau > 0$  according to



# p+A collision at RHIC/LHC



# di-hadron correlation in d+Au

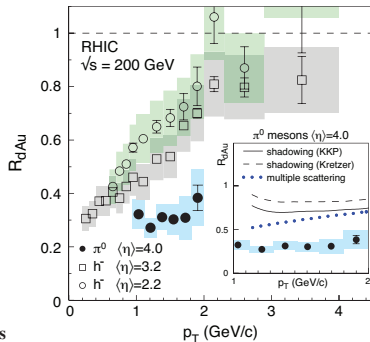
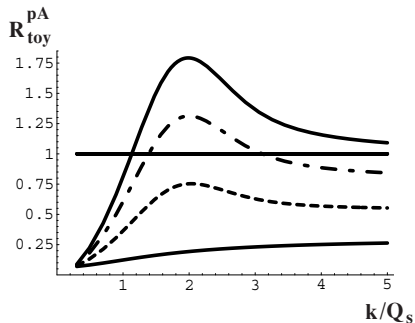


Di-hadron correlations measured at forward rapidities at RHIC:



# Suppression factor in d+A/p+A collisions

Quantum correction to gluon production (BK evolutions) predicts strong suppression at higher energy and larger rapidities.



Khazzeev, Kovchegov, Tuchin '03  
Khazzeev, Levin, McLerran '02, Albacete '03

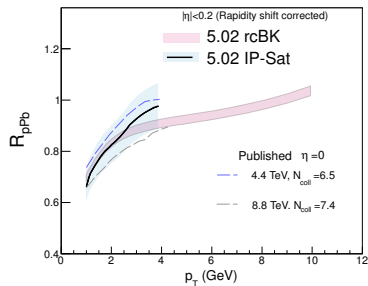
STAR nucl-ex/0602011

No other theory predicts this  $\rightarrow$  confirmed at RHIC.

# Suppression factor in d+A/p+A collisions

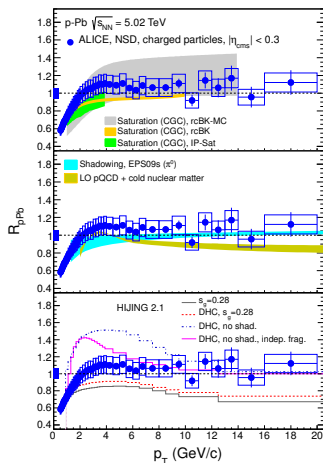
$R_{pA}$  predictions confirmed by ALICE

Tribedy, Venugopalan 1112.2445



$R_{pPb} \sim 1$  for  $p_T \geq 2$  GeV,  
 Growth of proton size (Gribov diffusion) important.

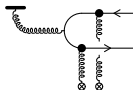
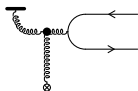
ALICE collab, 1210.4520



# Quark-Pair production in CGC framework

Contributions will come from

Fujii, Gelis, Venugopalan

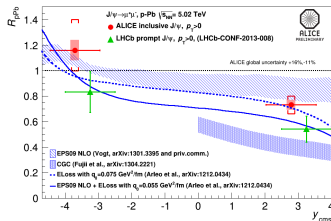
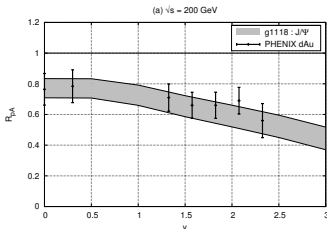


$\otimes$  → classical field insertion from dense target.

$k_T$ -factorization not possible and involves higher point correlators  $\langle \bar{u}\bar{u}^+\bar{u}\bar{u}^+ \rangle$   
 → can be related to  $S(\mathbf{x}_\perp, \mathbf{X}_\perp)$  & un-integrated gluon distribution.

Fujii & Watanabe

Arnaldi INFN '2013



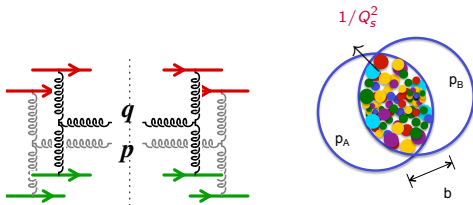
More suppression in proton fragmentation region.

Growth of proton size (b), e-by-e fluctuations effects can also be included.

# Multiparticle production & sub-nucleonic fluctuations.

Dumitru, Gelis, McLerran, Venugopalan 0804.3858

Correlated multi particle production from disconnected diagrams connected by color averaging.



Yang-Mills introduces **non-local gauge-field correlation** over length scale  $1/Q_s \rightarrow$  Glasma flux tube picture.

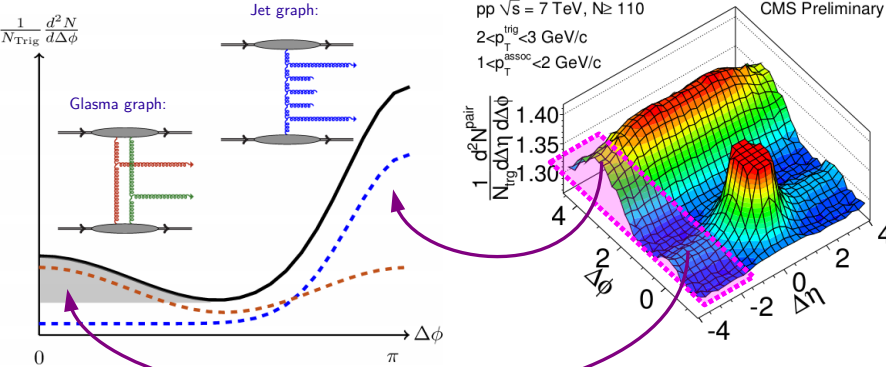
Two-particle correlation  $\rightarrow$  ridge phenomenon.

$n$ -particle correlation  $\rightarrow$  Negative-binomial fluctuation.

Gelis, Lappi, McLerran 0905.3234

# Ridge phenomenon in p+p and p+Pb

Dusling and Venugopalan



Origin of ridge → quantum interference.

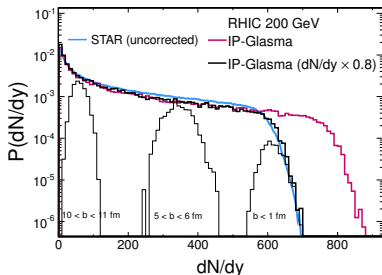
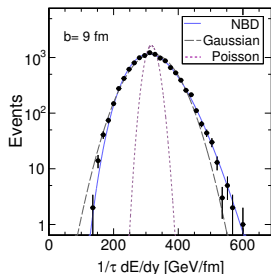
A preferable momentum in hadron w. f. is essential for collimation.

# Negative binomial fluctuation

Sources of multiplicity fluctuations are:

- ▶ Initial color charge fluctuation at sub-nucleonic length scale  $1/Q_s$ .
- ▶ E-by-E fluctuation of nucleon position and impact parameter.

→ IP-Glasma generates negative-binomial **transverse energy** and **multiplicity fluctuation** **Non-perturbatively**.



Limiting case of NBD → Bose-Einstein (BE) distribution.

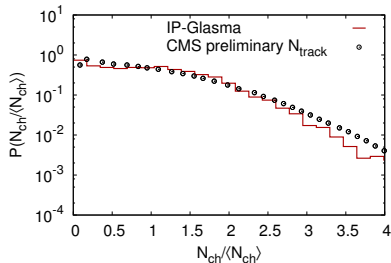
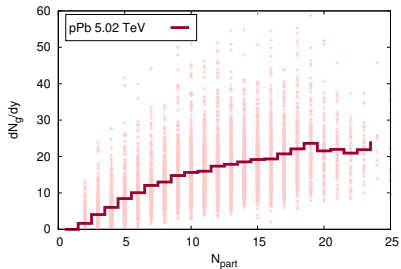
Single color gluon emitted from single flux tube → BE distribution.

Many sources of color → entropy maximisation.

# Multiplicity fluctuation in proton+nucleus collisions

Signatures yet to be tested:

Centrality distribution with number of participants of collisions saturates at large  $N_{part}$ , logarithmic increase. →

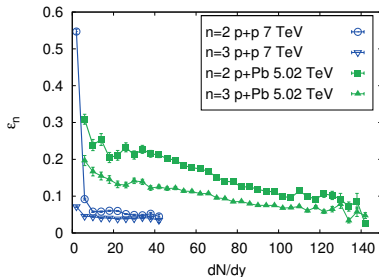
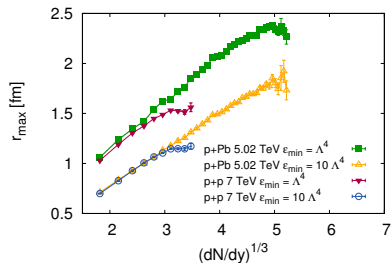


Very different centrality dependence from Wounded nucleon model

Bzdak, Skokov 1307.6168

# Initial geometry in p+p and p+A/d+A collisions

System size (very similar) and initial eccentricities (very different) for same multiplicity.



$r_{max} \rightarrow$  maximal radius with  $\epsilon_{min} \sim \Lambda_{QCD}^4$

$r_{max} \propto (dN/dy)^{1/3}$ , comparable HBT radii in p+p and p+Pb.

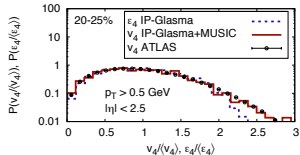
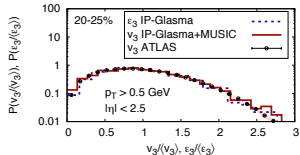
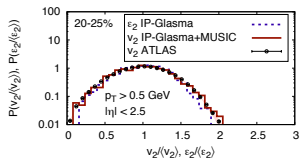
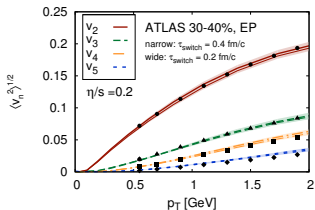
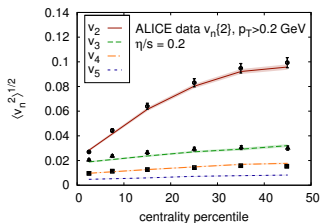
p+p  $\rightarrow \epsilon_{2,3}$  are significantly smaller and flat with multiplicity.

Smaller eccentricities for high multiplicity events.



# Initial geometry and fluctuations in A+A

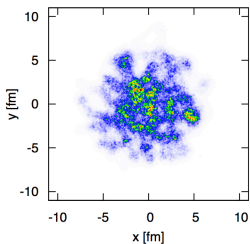
IP-Glasma provides good description of initial geometry and fluctuations in Pb+Pb and Au+Au.



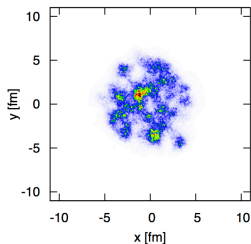
A combined Yang-Mill + viscous hydro calculation for the first time describes all measured harmonics and its e-by-e fluctuations.

# Energy density ( $\epsilon$ ) from IP-Glasma model (at $\tau = 0$ )

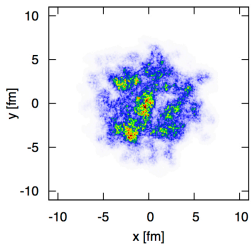
Au+Au (200 GeV)



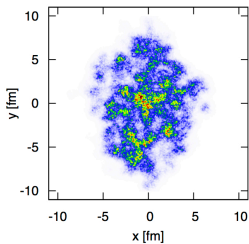
Cu+Au (200 GeV)



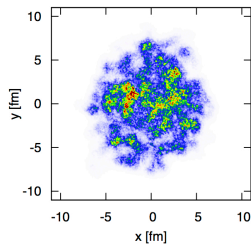
U+U (Tip-Tip)



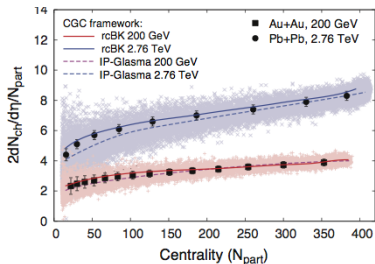
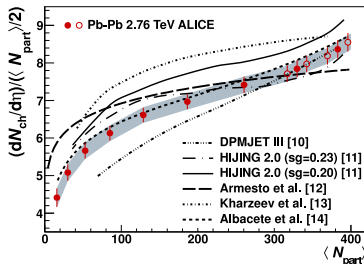
U+U (Side-Side)



U+U (Random)



# Centrality dependence in A+A at LHC

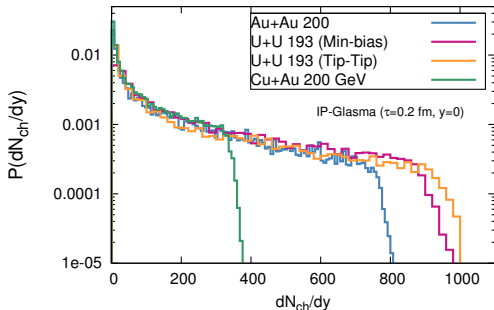
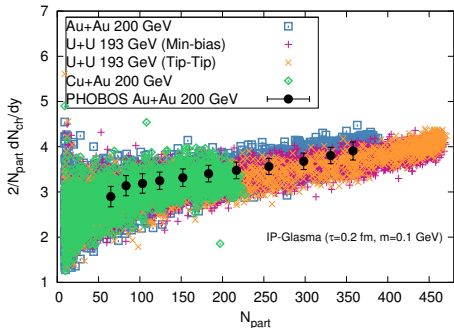


ALICE 1012.1657

CGC centrality dependence of  $A + A \rightarrow$  consistent with ALICE.

# Centrality dependence in A+A at RHIC

- Local Running coupling on each point on lattice  $\alpha_s(Q_s^{max}(\mathbf{x}_\perp))$



Larger systems  $\rightarrow$  smaller multiplicity per participants.

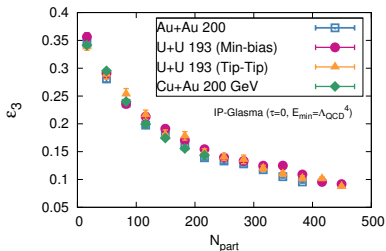
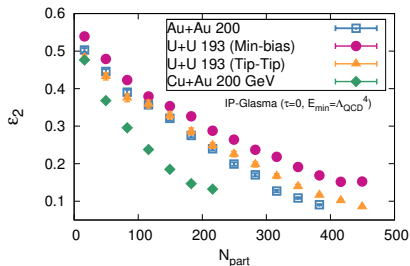
U+U min-bias & tip-tip are very close unlike 2-component model.

$$\frac{dN_{ch}}{dy} \sim \frac{Q_s^2 S_\perp}{\alpha_s(Q_s^{max})}, \text{ for Tip-Tip U+U, } Q_s^2 \uparrow \text{ but } S_\perp \downarrow$$

# Eccentricity for different systems

The spatial eccentricities that characterize the geometry

$$\varepsilon_n = \frac{\sqrt{\langle r^n \cos(n\phi) \rangle^2 + \langle r^n \sin(n\phi) \rangle^2}}{\langle r^n \rangle}, \quad \langle \dots \rangle \rightarrow \text{weight } \epsilon(\mathbf{x}_\perp, \tau)$$



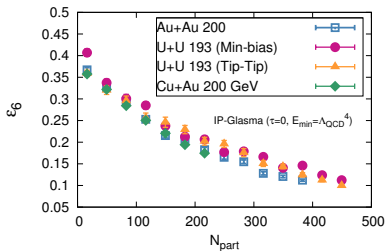
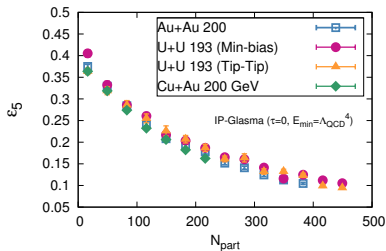
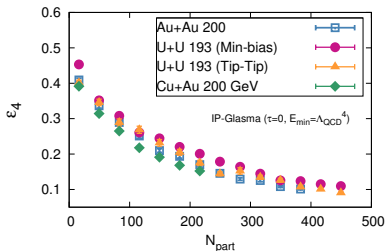
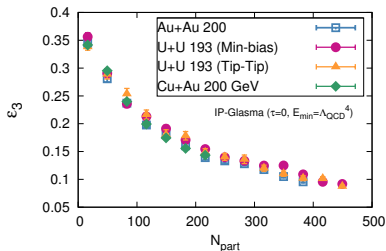
- ▶  $\varepsilon_2$  very sensitive to initial geometry of colliding system.
- ▶ Fluctuation driven moment  $\varepsilon_3$  are very similar for different systems.

# Summary

- ▶ CGC is an universal description of high energy saturated hadron/nucleus, an *ab initio* (first principle) approach.
- ▶ Powerful framework for wide range of system e+p, e+A, p+p, p+A, A+A.
- ▶ Phenomenologically successful in describing bulk features of data, difficult in conventional pQCD approach.
- ▶ Multi particle production can be studied in detail, consistently describes global data over wide range of energies/systems.
- ▶ Framework includes different sources of quantum fluctuations, successful describe the initial dynamics of heavy ion collisions.

# BACK UP SLIDES

# Higher order moments $\epsilon_3, \epsilon_5$

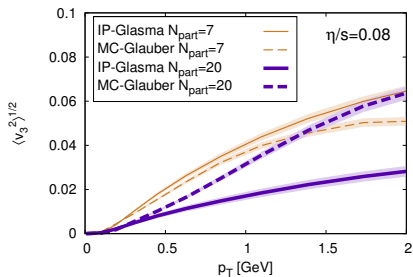
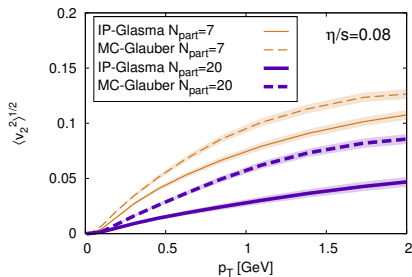


Fluctuation driven moments are very similar for different systems.



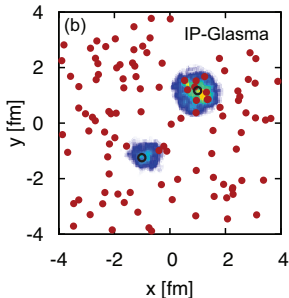
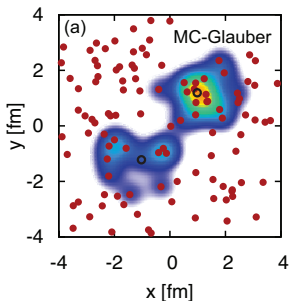
# Flow in p+A collisions.

A strong dependence on choice of initial conditions for large  $N_{part}$ .



Both  $v_2$  and  $v_3$  are smaller in IP-Glasma compared to MC-Glauber.

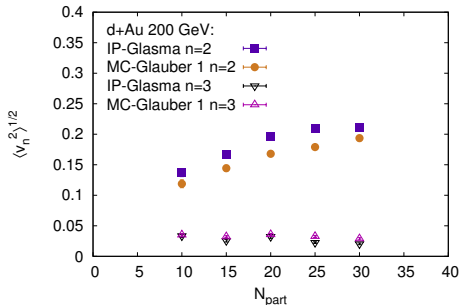
# Flow in d+A collisions at RHIC.



Deuteron nucleus sampled from,

$$\phi_{\text{pn}}(r) = \frac{1}{\sqrt{2\pi}} \frac{\sqrt{ab(a+b)}}{b-a} \frac{e^{-ar} - e^{-br}}{r}$$

$\langle r \rangle \sim 2.52 \text{ fm} \rightarrow$  separated regions



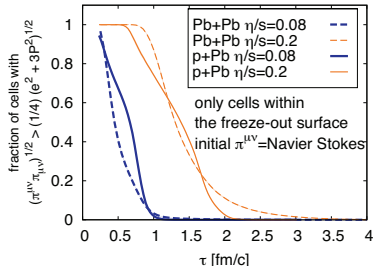
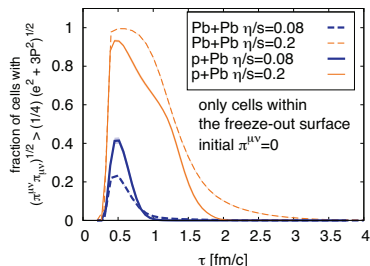
$\epsilon_n$  will influence  $v_n$  only for small  $r$

# Viscous correction in smaller sized systems

Relative magnitude of the ideal and the viscous terms are compared over the evolution time  $T^{\mu\nu} = T_0^{\mu\nu} + \pi^{\mu\nu}$

Switch IP-Glasma  $\leftrightarrow$  Hydro  $\tau = 0.2$  fm,  $\frac{\eta}{s} = 0.2$  (fits to Pb+Pb data),

25 % viscous correction:



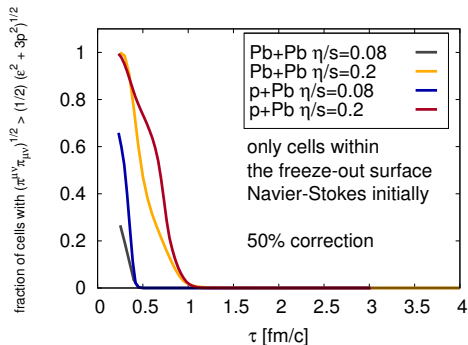
Navier-Stokes initialization  $\pi_0^{\mu\nu} = \eta \left( \nabla^\mu u^\nu + \nabla^\nu u^\mu - \frac{2}{3} \Delta^{\mu\nu} \nabla_\lambda u^\lambda \right)$

Large correction  $(\sqrt{\pi_{\mu\nu}\pi^{\mu\nu}}/\sqrt{e^2 + 3P^2})$  over significant fraction of life time.

## Viscous correction in smaller sized systems

Life time of p+Pb  $\sim \frac{1}{6}$  life time of Pb+Pb.

50 % viscous correction:



Might question reliability of second order viscous hydrodynamics for smaller systems.

# IP-Glasma : Multiplicity and Energy density

E-by-E soln. of CYM equation on 2+1D lattice  $\rightarrow F^{\mu\nu}(\tau, \mathbf{x}_\perp, \eta)$ .

- **Multiplicity (n):**  $F^{\mu\nu}(\tau, \mathbf{x}_\perp, \eta) \rightarrow \mathcal{H}(\mathbf{x}_\perp)$  (Hamiltonian density)  
Fourier transform  $\mathcal{H}(\mathbf{k}_\perp) \rightarrow$  number density  $n(\mathbf{k}_\perp)$  of gluon,  
 $\mathcal{H}(\mathbf{k}_\perp) \sim n(\mathbf{k}_\perp)\omega(\mathbf{k}_\perp)$ , assuming dispersion relation,  $\omega(k) = k$

In the transverse Coulomb Gauge :

$$\frac{dN_g}{dy} = \frac{2}{N^2} \int \frac{d^2 k_T}{\tilde{k}_T} \left[ \frac{g^2}{\tau} \text{tr} (E_i(\mathbf{k}_\perp) E_i(-\mathbf{k}_\perp)) + \tau \text{tr} (\pi(\mathbf{k}_\perp) \pi(-\mathbf{k}_\perp)) \right]$$

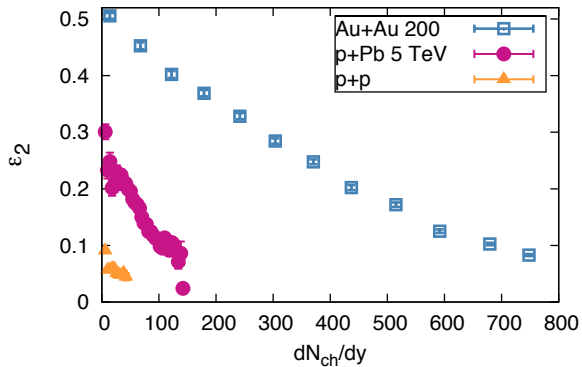
- **Energy density ( $\epsilon$ ):**  $F^{\mu\nu} \rightarrow T^{\mu\nu}$  (stress energy tensor).

$$T^{\mu\nu} = -g^{\gamma\delta} F^\mu_\gamma F^\nu_\delta + \frac{1}{4} g^{\mu\nu} F^\gamma_\beta F_\gamma^\delta$$

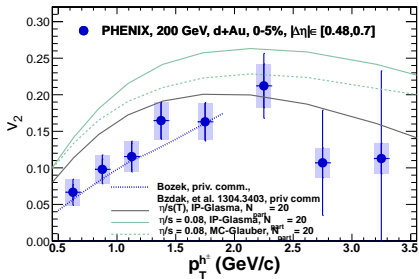
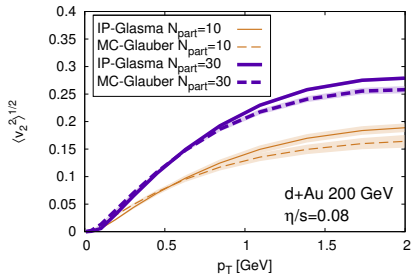
solving eigen value eq.  $u_\mu T^{\mu\nu} = \epsilon u^\nu$  gives  $\epsilon$  and flow  $u^\nu$

$T^{\mu\nu}_{CYM}$  can be Landau matched with viscous hydro.

# p+p, p+A and A+A eccentricities

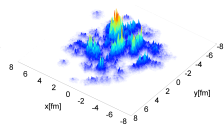
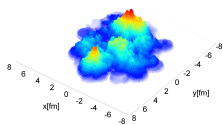
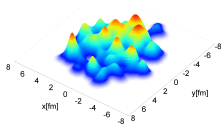


# Flow in d+A collisions at RHIC.



# Different models of initial conditions.

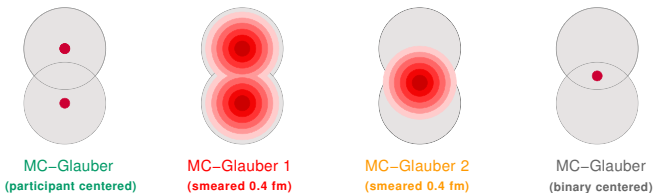
I.C.	Geometry	$k_T$ – factorization	Classical Yang-Mills
framework	2-component model	CGC perturbative	CGC non-perturbative
E-by-E	✓	✓	✓
Sub-nucleonic fluctuation	✗	✗	✓
Time evolution	✗	✗	✓
Initial flow	✗	✗	✓
NBD fluctuation	by hand	by hand	✓



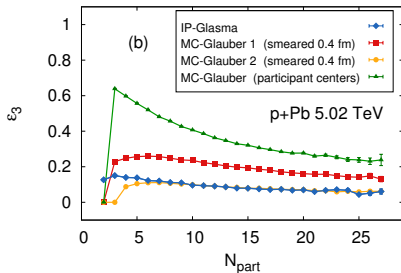
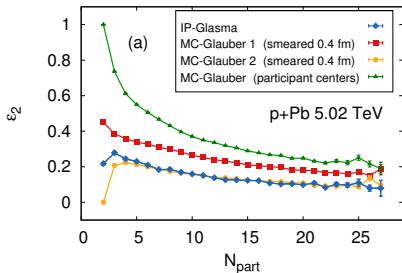


# Comparison with MC-Glauber model

Bzdak, Schenke, PT, Venugopalan



MC-Glauber  $\rightarrow$  smearing width  $\sigma_0 \rightarrow$  free parameter.



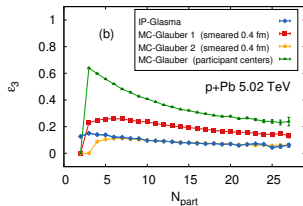
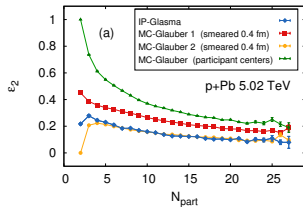
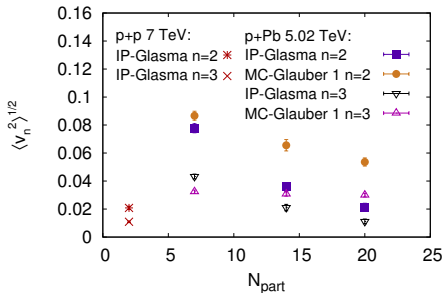
Very different behaviour at small  $N_{part}$ , would effect  $v_n/\epsilon_n$  computation.  
 Binary centered  $\leftrightarrow$  IP-Glasma, no energy deposition due to **pure gauge fields outside overlap**.

# Flow in p+p and p+A collisions.

Viscous hydrodynamic simulation using MUSIC with IP-Glasma & MC-Glauber 1 (participant centred, smeared 0.4 fm)

$$\frac{\eta}{s} = \frac{1}{4\pi}, \tau_0 = 0.2 \text{ fm} \text{ and } T_{f0} = 120 \text{ MeV.}$$

Integrated  $\langle v_n \rangle$  for  $p_T > 0.5 \text{ GeV}$ .



Flow in p+p and p+Pb at large  $N_{part}$  are similar for IP-Glasma.

$N_{part}$  dependence of  $v_2 \rightarrow$  high sensitivity on initial conditions.