



π^0 Electroproduction and Transversity

Simonetta Liuti

University of Virginia

Collaborators:

Saeed Ahmad

Gary Goldstein

- AHLT (at the University of Virginia)
(Saeed Ahmad, Heli Honkanen*, S.L. and S.K. Taneja⁺)

* University of Iowa

+ Stony Brook

Outline

- Main point:

- π^0 electroproduction always involves *chiral odd* GPDs

- Will show:

- GPDs from proton and neutron data sets \Rightarrow

- ★ New results using Jlab data constraints!

- Model for Q^2 dependence

- Practical method for the extraction of both

tensor charge: δq

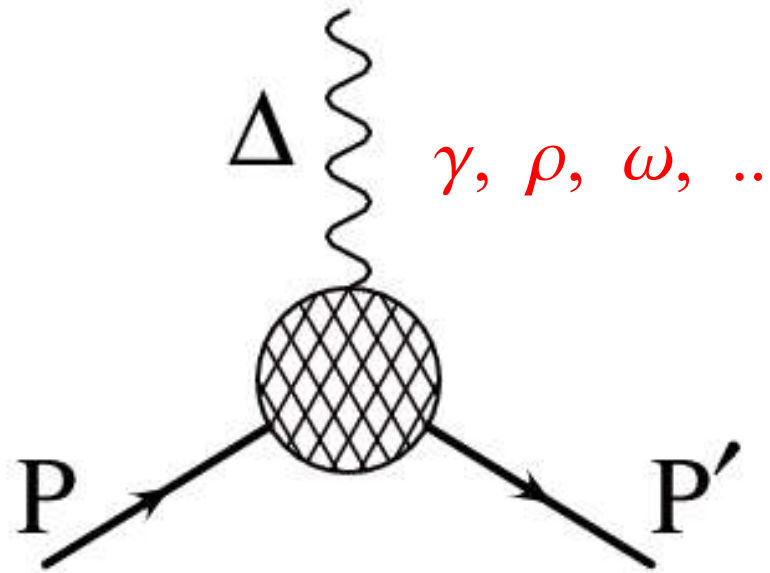
“Burkardt's moment”: $\kappa_T q$

- Conclusions: which experiments, observables, targets for Jlab at 12 GeV?

1. π^0 Electroproduction Observables and GPDs*

*Gary Goldstein's talk

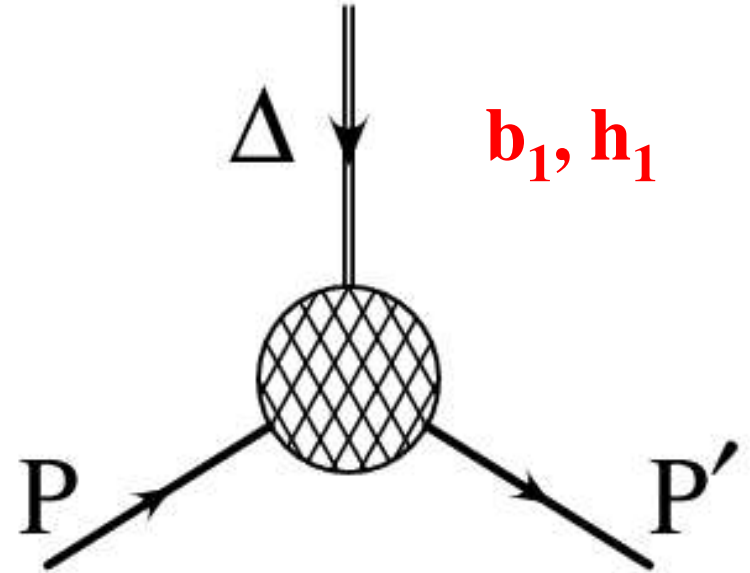
π^0 production proceeds via two types only of JPC exchanges:



JPC=1⁻

$$i\sigma_{\mu\nu}\gamma_5$$

\Leftrightarrow JPC=1⁻, 1⁺⁻, ... \Leftrightarrow H_T, E_T, ...



JPC=1⁺

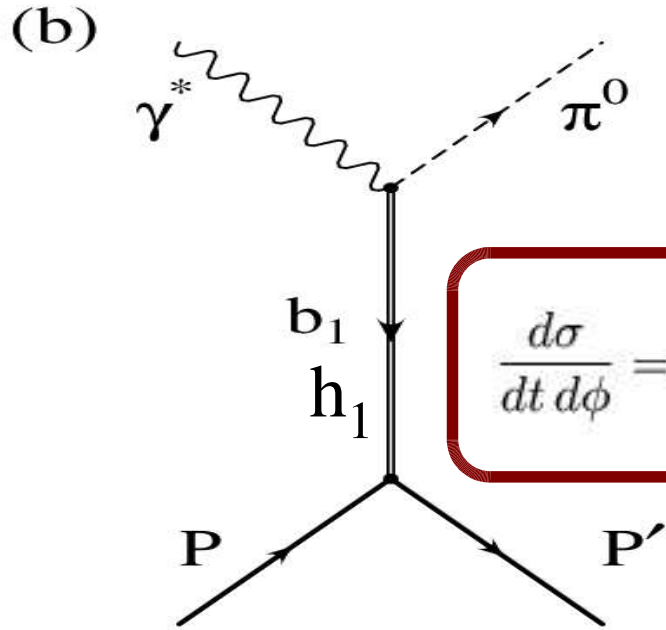
$$\gamma_5$$

\Leftrightarrow JPC=1⁺⁺, ... (a₁-type exchange) \Leftrightarrow \tilde{H} , \tilde{E} , ...

Only chiral-odd GPDs!!! ∇

Exclusive π^0 electroproduction

$$ep \rightarrow e'p'\pi^0$$



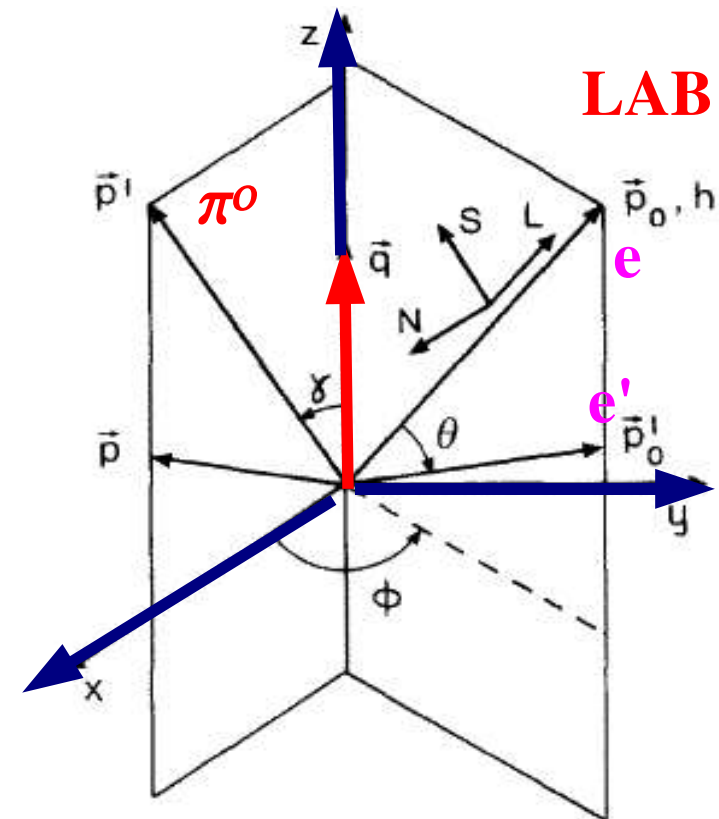
$$\frac{d\sigma}{dt d\phi} = \left(\frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} \right) + \epsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi + \sqrt{2\epsilon(\epsilon+1)} \frac{d\sigma_{LT}}{dt} \cos \phi$$

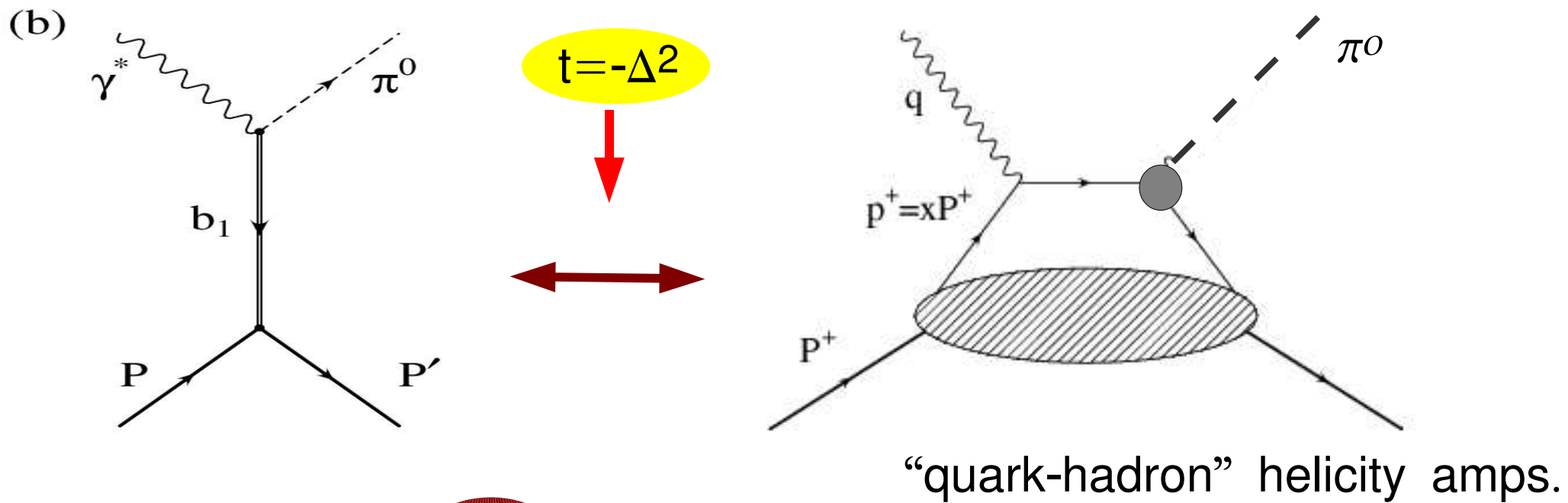
$$d\sigma \propto L_{\mu\nu}^{h=\pi^0} W_{\mu\nu}$$

$L_{\mu\nu}^{h=\pi^0} \approx \gamma^*$ polarization density matrix

$W_{\mu\nu} = \sum J_\mu J_\nu^* \delta(E_i - E_f) =$ hadronic tensor

$$\frac{d\sigma_{TT}}{dt} = W_{yy} - W_{xx} \equiv 2\Re(J_1 J_{-1}^*)$$





$$f_{1,\lambda;0,\lambda'} = \sum_{\lambda,\lambda'} g_{1,\lambda;0,\lambda} A_{\lambda',\lambda';\lambda,\lambda}$$

“Quark-Hadron” Helicity Amplitudes (Marcus Diehl)

$f_1 \equiv f_{1+,0+} \propto A_{++,+-}$	$A_{+-,++} = \frac{1}{2} F_{\pi\gamma^*}^V(Q^2) \frac{\sqrt{t_0-t}}{2M} \left[\tilde{\mathcal{H}}_T + \frac{1+\xi}{2} \mathcal{E}_T - \frac{1+\xi}{2} \tilde{\mathcal{E}}_T \right]$
$f_2 \equiv f_{1+,0-} \propto A_{++,--}$	$A_{++,--} = \frac{F_{\pi\gamma^*}^V(Q^2) + F_{\pi\gamma^*}^A(Q^2)}{2} \sqrt{1-\xi^2} \left[\mathcal{H}_T + \frac{t_0-t}{4M^2} \tilde{\mathcal{H}}_T \right]$
$f_3 \equiv f_{1-,0+} \propto A_{+-,+-}$	$A_{+-,+-} = \frac{F_{\pi\gamma^*}^V(Q^2) - F_{\pi\gamma^*}^A(Q^2)}{2} \sqrt{1-\xi^2} \frac{t_0-t}{4M^2} \tilde{\mathcal{H}}_T$
$f_4 \equiv f_{1+,0+} \propto A_{++,+-}$	$A_{++,-+} = -\frac{1}{2} F_{\pi\gamma^*}^V(Q^2) \frac{\sqrt{t_0-t}}{2M} \left[\tilde{\mathcal{H}}_T + \frac{1-\xi}{2} \mathcal{E}_T + \frac{1-\xi}{2} \tilde{\mathcal{E}}_T \right]$
$f_5 \equiv f_{0+,0-} \propto A_{++,--}$	
$f_6 \equiv f_{0+,0+} = 0$	

What goes into the quark-hadron amplitudes?

$$\mathcal{F}(\zeta, t) = -i\pi \sum_q e_q^2 [F^q(\zeta, \zeta, t) - F^q(-\zeta, \zeta, t)] + \mathcal{P} \int_{1-\zeta}^1 dX \left(\frac{1}{X-\zeta} + \frac{1}{X} \right) F^q(X, \zeta, t).$$

Generalized Form Factors

$$\mathcal{H}_T, \mathcal{E}_T, \tilde{\mathcal{H}}_T, \tilde{\mathcal{E}}_T$$

$$H_T(X, 0, 0) = h_1(X) = \text{transversity}$$

$$\int h_1(X, Q^2) dX = \delta q = \text{tensor charge}$$

$$\tilde{\mathcal{E}}_2 = 2\tilde{\mathcal{H}}_T + \mathcal{E}_T$$

$$\int E_2(X, 0, 0) dX = \kappa_T = \text{Burkardt's moment}$$

$$\int h_{1\perp}(X) dX d^2k_T \sim -\kappa_T \text{ (A.Metz)}$$

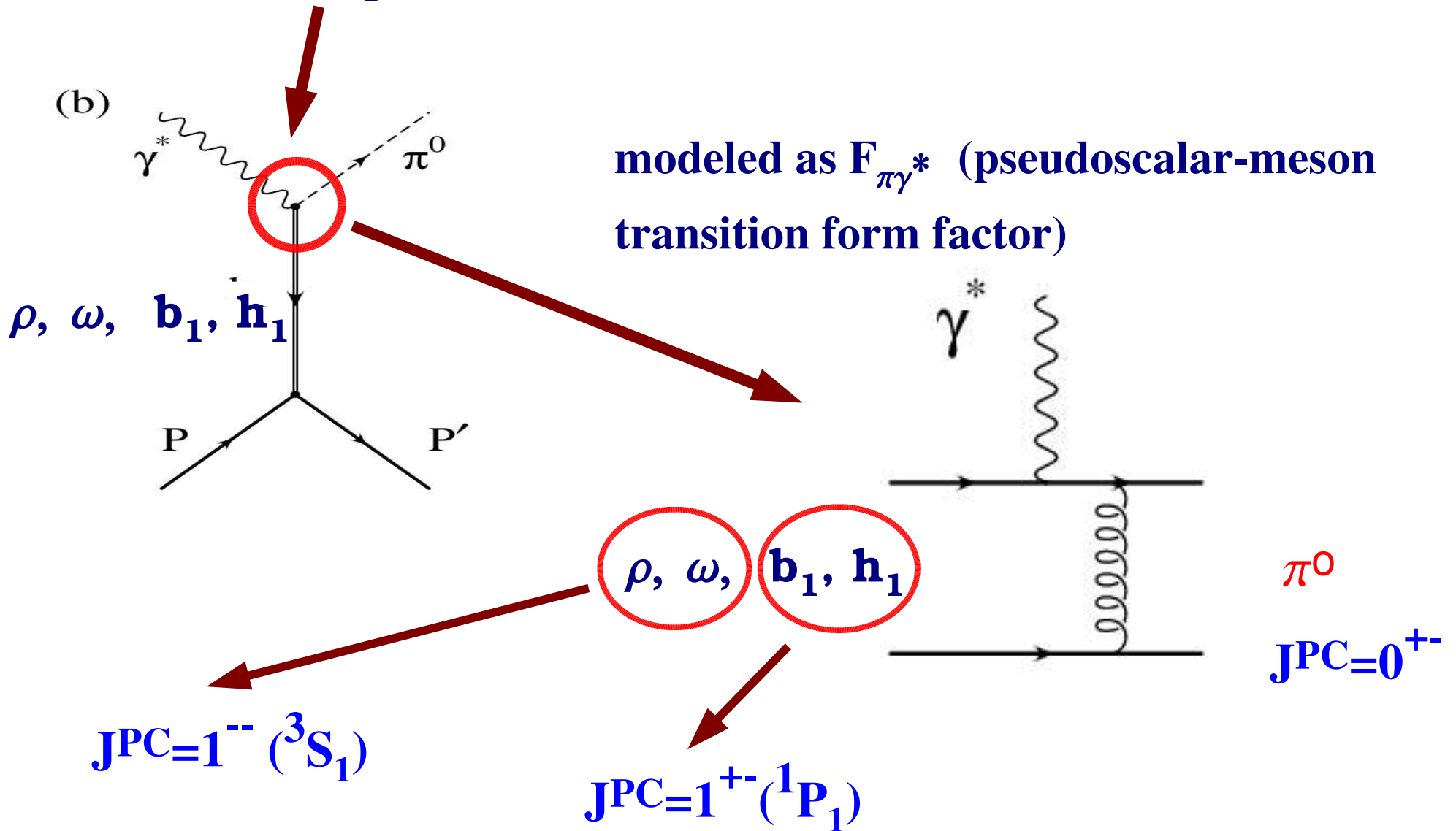
Observables are sensitive to both δq and κ_T !

$$\begin{aligned}
 \frac{d\sigma_T}{dt} &= K \left[\frac{t_0 - t}{8M^2} |\tilde{\mathcal{E}}_2(Q^2)|^2 + (1 - \xi^2) |\mathcal{H}_T(Q^2)|^2 + (1 - \xi^2) \frac{t_0 - t}{8M^2} |\tilde{\mathcal{H}}_T(Q^2)|^2 \right] \\
 \frac{d\sigma_{TT}}{dt} &= K \frac{t_0 - t}{8M^2} \left[(1 - \xi^2) \Re \left(\tilde{\mathcal{E}}_2(Q^2) \mathcal{H}_T^*(Q^2) \right) + \left(\Re \tilde{\mathcal{E}}_2(Q^2) \right)^2 + \left(\Im \tilde{\mathcal{E}}_2(Q^2) \right)^2 \right] \\
 \frac{d\sigma_{LT}}{dt} &= K \frac{t_0 - t}{8M^2} \left[(1 - \xi^2) \Re \left(\tilde{\mathcal{E}}_2(Q^2) \mathcal{H}_T^*(Q^2) \right) + \left(\Re \tilde{\mathcal{E}}_2(Q^2) \right)^2 \right] \\
 A_{UT} &= K \frac{t_0 - t}{8M^2} \left[\frac{\sqrt{t_0 - t}}{2M} \Im \left(\tilde{\mathcal{E}}_2^*(Q^2) \tilde{\mathcal{H}}_T(Q^2) \right) - \sqrt{1 - \xi^2} \Im \left(\mathcal{H}_T^*(Q^2) \tilde{\mathcal{E}}_2(Q^2) \right) \right]
 \end{aligned}$$

... and more ...!!!

2. Q^2 dependence

t-channel exchange vertex



quark content: $\frac{1}{\sqrt{2}} (u\bar{u} \pm d\bar{d})$

Distinction between ρ , ω and \mathbf{b}_1 , \mathbf{h}_1 exchanges

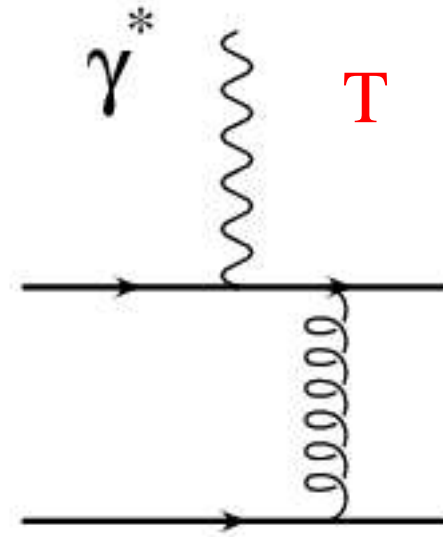
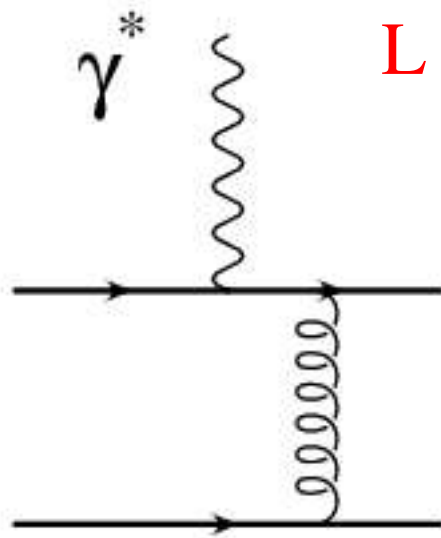
$J^{PC}=1^{--}$ \longrightarrow π^0 : qqbar from (S=1 L=0) \Rightarrow (S=0 L=0) \Rightarrow $\Delta L = 0$

$J^{PC}=1^{+-}$ \longrightarrow π^0 : qqbar from (S=0 L=1) \Rightarrow (S=0 L=0) \Rightarrow $\Delta L = 1$

“Vector” exchanges \Rightarrow no change in OAM

“Axial-vector” exchanges \Rightarrow change 1 unit of OAM!

Reminiscent of PQCD analysis of Nucleon's Pauli Form Factor
(Belitsky, Ji, Yuan, 2003)

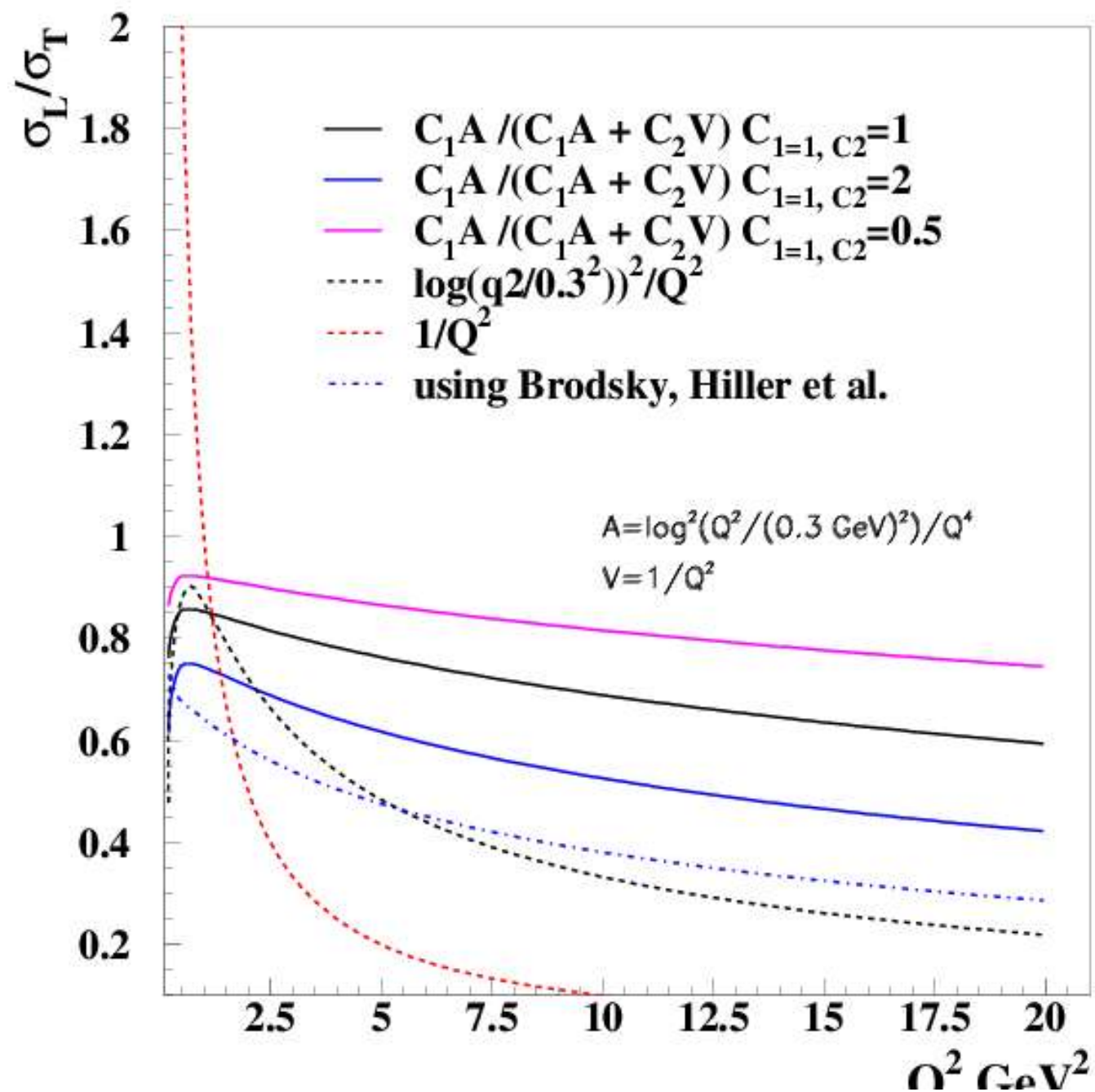


$\Delta L = 1 \Rightarrow A \propto \log^2(Q^2/\Lambda^2)/Q^4 V$

$\Delta L = 0 \Rightarrow V \propto 1/Q^2$
 and $\Delta L = 1$

$\Delta L = 1$ further suppressed by
 Sudakov form factor

Preliminary!



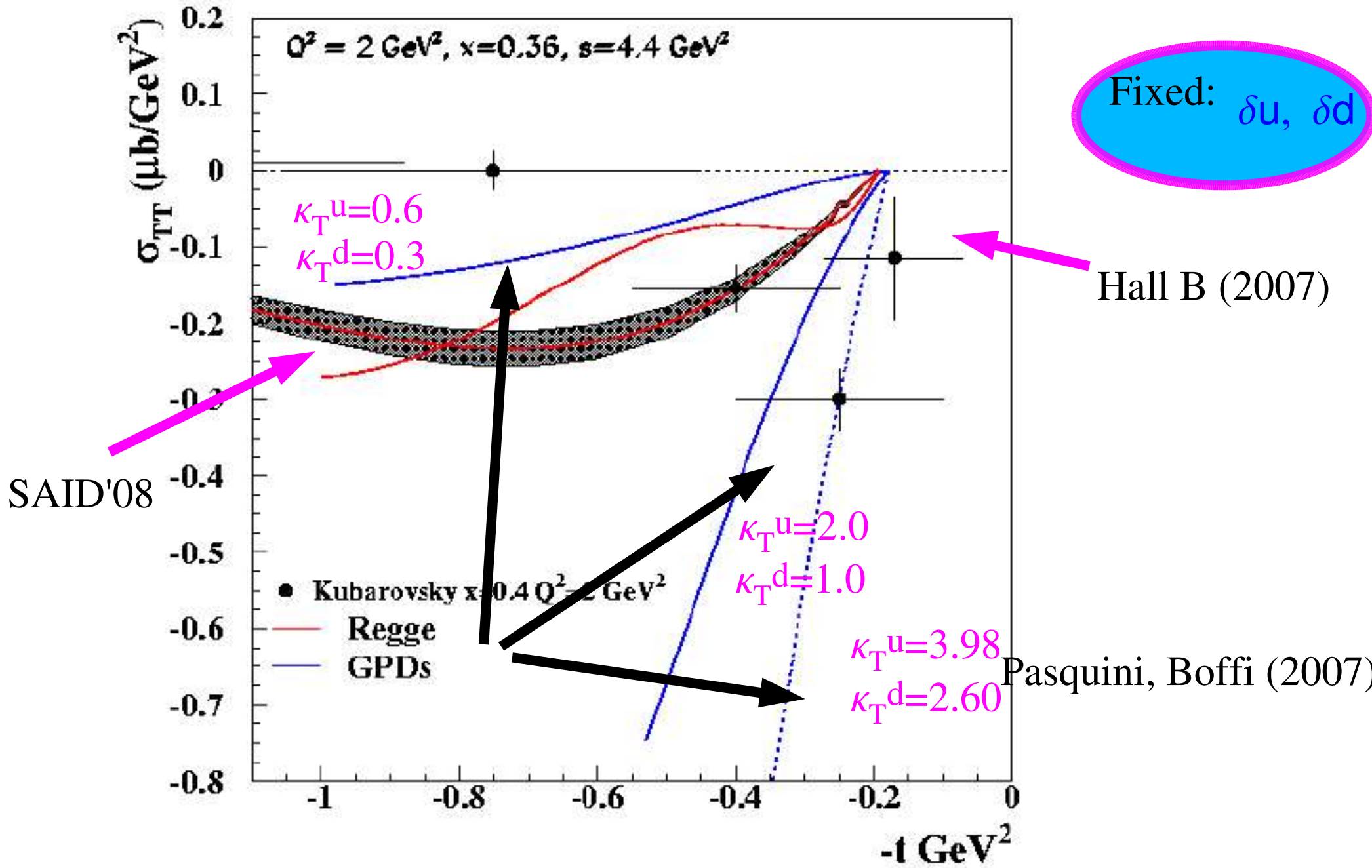
3. Extraction from data needs a reliable GPD model

Reaching a more advanced phase of extracting GPDs from data

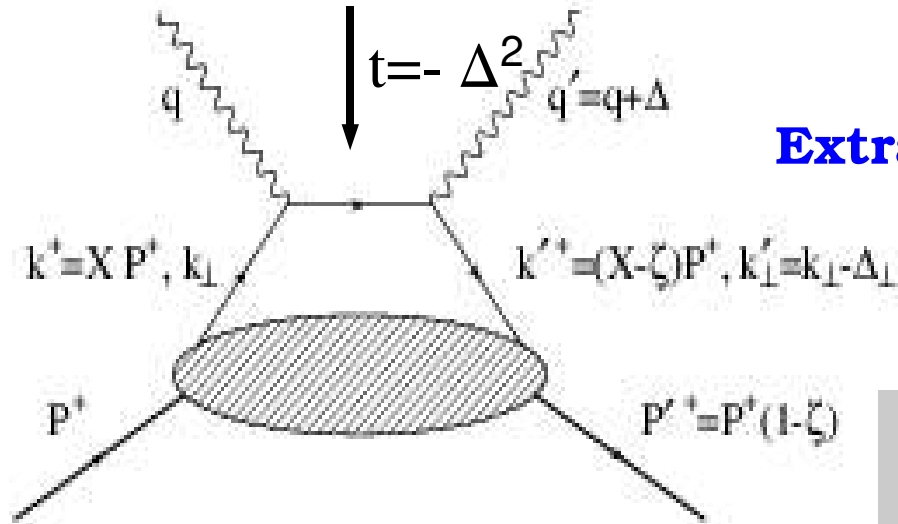
- No longer simple models (agree with Dieter Muller)
- Incorporate Q^2 dependence
- Incorporate all constraints from data “non DVCS, DVMP type” data
- Incorporate new data as they become available
- Lattice + Chiral Extrapolations (see also Philip Hagler)
- Connect various experiments, separate valence from sea, flavors, ...

The observables we singled out are sensitive to $\delta u, \delta d, \kappa_T^u, \kappa_T^d$

Measure interplay of four quantities!



DVCS and Generalized Parton Distributions

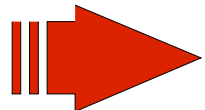


Extract “Generalized Parton Distributions”

$$\bar{p}^+ \int \frac{d\xi^-}{2\pi} e^{ixP^+\xi^-} \langle P', S' | \psi \left(-\frac{\xi^-}{2} \right) \gamma^+ \psi \left(\frac{\xi^-}{2} \right) | P, S \rangle =$$

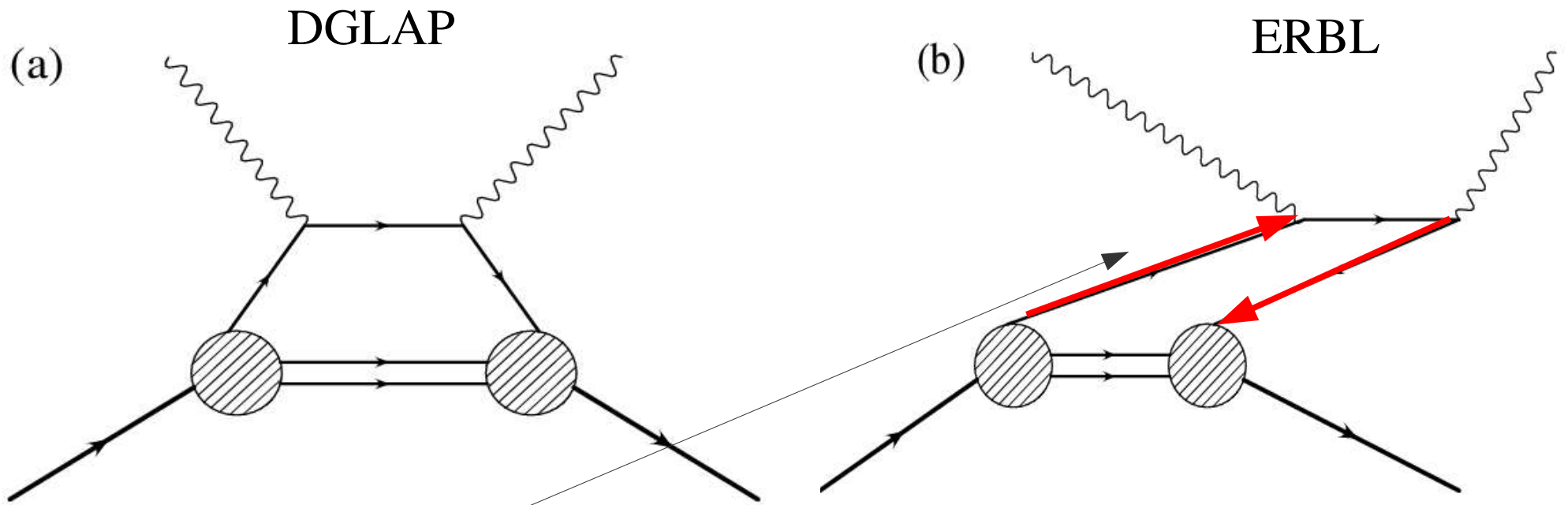
$$\bar{u}(P', S') \left[\gamma^+ H(x, \xi, -\Delta^2) + \frac{i\sigma^{+\nu} q_\nu}{2M} E(x, \xi, -\Delta^2) \right] u(P, S)$$

- GPDs are hybrids of PDFs and FFs: describe simultaneously x and t -dependences !
- GPDs give access to spatial d.o.f. of partons !
- GPDs give access to orbital angular momentum of partons!



$$\int dx x [H_q(x, \zeta, t = 0) + E_q(x, \zeta, t = 0)] = 2J_q \quad \text{X. Ji}$$

Two different time orderings/pole structure!



Quark anti-quark pair describes similar physics (dual to) Regge t-channel exchange!!!

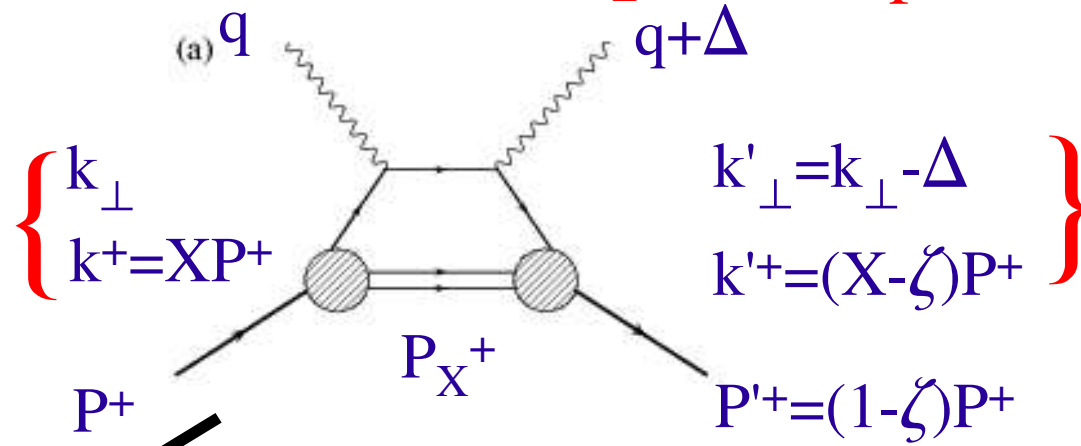
What goes into a theoretically motivated parametrization...?

The name of the game: Devise a form combining essential dynamical elements with a flexible model that allows for a fully quantitative analysis constrained by the data

$$H_q(X,t) = \underbrace{R(X,t)}_{\text{“Regge”}} \underbrace{G(X,t)}_{\text{Quark-Diquark}}$$

Q^2 Evolution is an essential element!!

For $\zeta = 0$ and in the DGLAP region \Rightarrow partonic picture



$$R_{1(2)}^I = X^{-\alpha^I - \beta_{1(2)}^I} (1-X)^{p_{1(2)}^I} t$$

$$G_{M_X}^{\lambda}(X, t) = \mathcal{N} \frac{X}{1-X} \int d^2 \mathbf{k}_{\perp} \frac{\phi(k^2, \lambda)}{D(X, \mathbf{k}_{\perp})} \frac{\phi(k'^2, \lambda)}{D(X, \mathbf{k}_{\perp} + (1-X)\mathbf{\Delta}_{\perp})}$$

Summary of Constraints

Constraints from Form Factors

$$\int_0^1 dX H^q(X, t) = F_1^q(t) \quad \text{Dirac}$$

$$\int_0^1 dX E^q(X, t) = F_2^q(t), \quad \text{Pauli}$$

$$F_{1(2)}^p(t) = \frac{2}{3}F_{1(2)}^u(t) - \frac{1}{3}F_{1(2)}^d(t) + \frac{1}{3}F_{1(2)}^s(t) \quad \text{Dirac(Pauli) proton}$$

$$F_{1(2)}^n(t) = -\frac{1}{3}F_{1(2)}^u(t) + \frac{2}{3}F_{1(2)}^d(t) + \frac{1}{3}F_{1(2)}^s(t), \quad \text{Dirac(Pauli) neutron}$$

Constraints from PDFs

$$q(x) = H_q(x, 0, 0)$$

GPDs from available data 2

Parton Distribution Functions

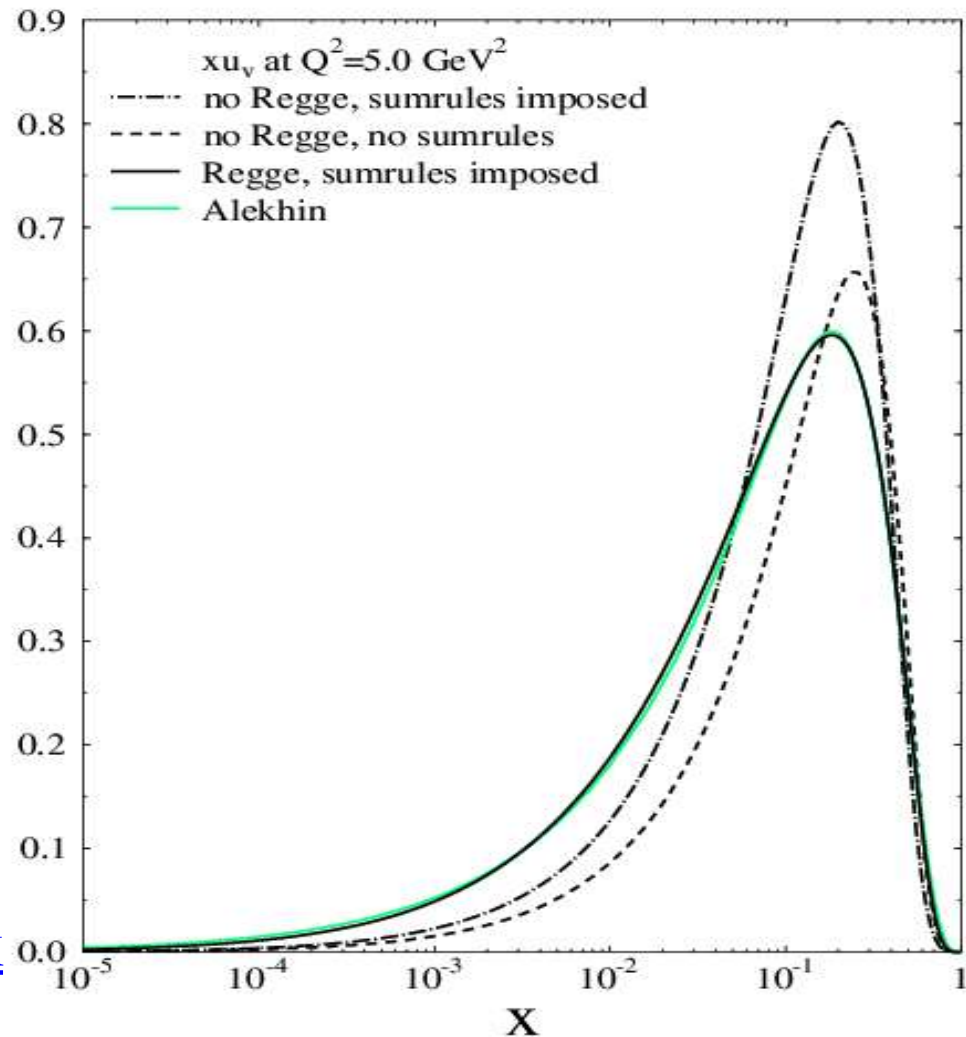
Notice! GPD parametric form is given at $Q^2=\mu^2$ and evolved to Q^2 of data.

Notice! We provide a parametrization for GPDs that simultaneously fits the PDFs:

$$H_q(X,t) = R(X,t) G(X,t)$$

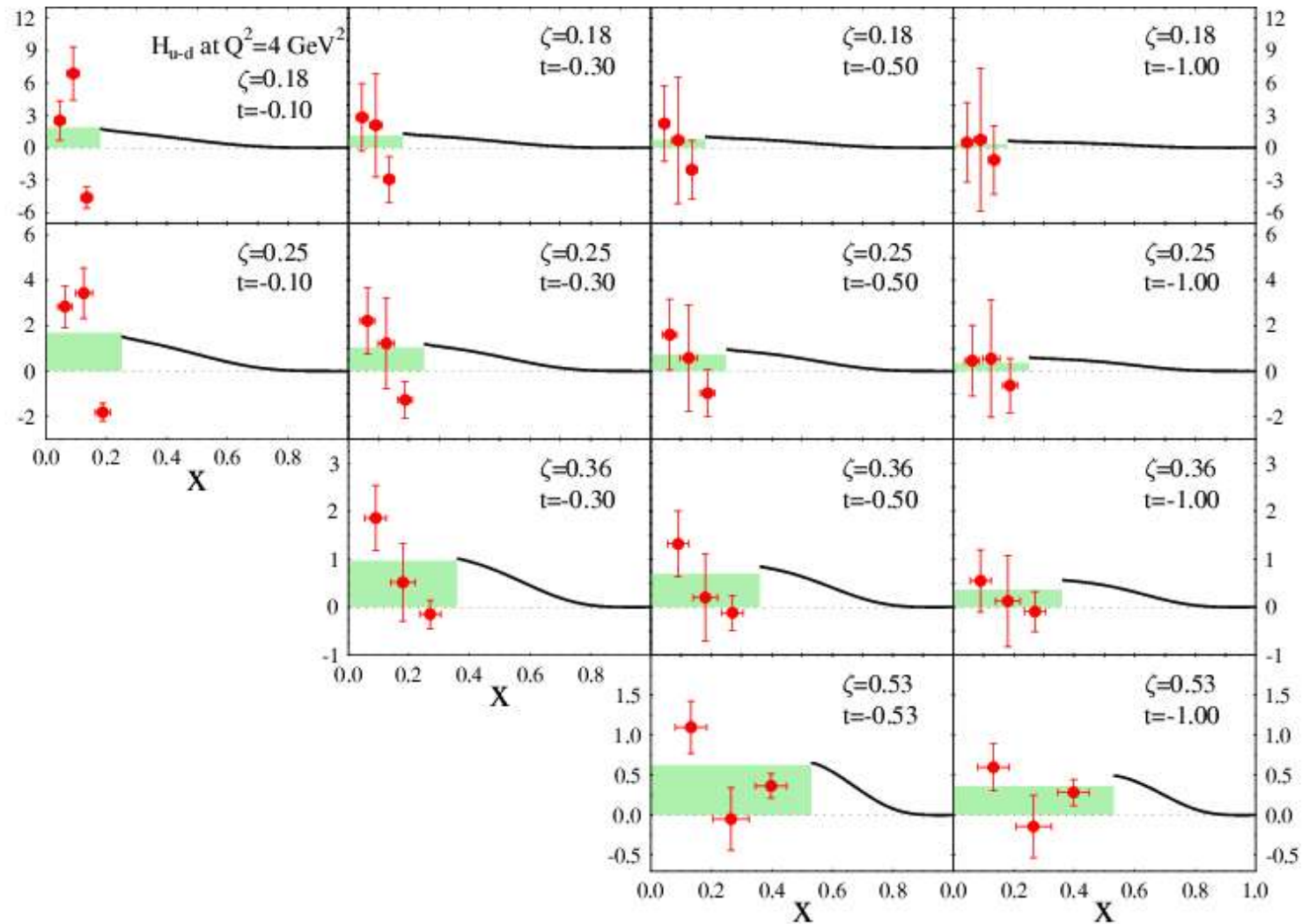
Regge

Quark-Diquark



ERBL Region

AHLT arXiv:0708.0268



First “model independent” extraction of GPDs!!!

GPDs from Bernstein moments

$$\bar{H}(X, \zeta, t) = \frac{(n+1)!}{k!} \sum_{l=0}^{n-k} \frac{(-1)^l}{l!(n-k-l)!} M_{l+k}$$

Mellin moments

$$\bar{H}_{02}(X_{02}) = 3A_{10} - 6A_{20} + 3 \left[A_{30} + \left(\frac{2\zeta}{2-\zeta} \right)^2 A_{32} \right],$$

$$\bar{H}_{12}(X_{12}) = 6A_{20} - 6 \left[A_{30} + \left(\frac{2\zeta}{2-\zeta} \right)^2 A_{32} \right],$$

$$\bar{H}_{22}(X_{22}) = 3A_{30} + \left[\left(\frac{2\zeta}{2-\zeta} \right)^2 A_{32} \right].$$

Weighted Average \Rightarrow

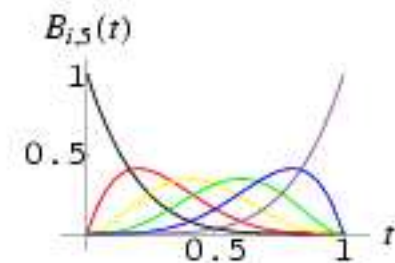
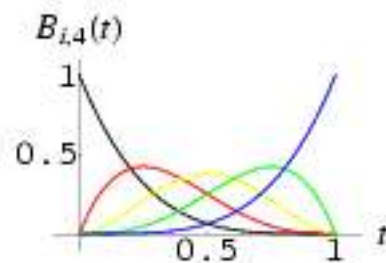
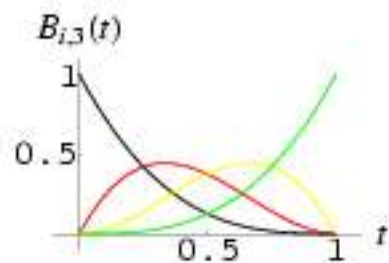
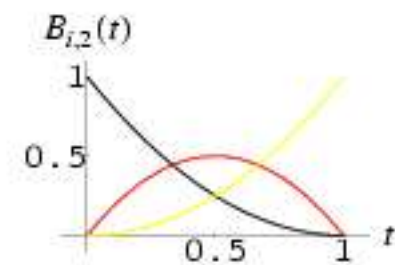
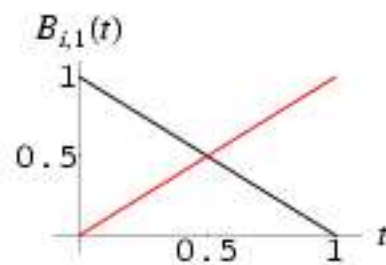
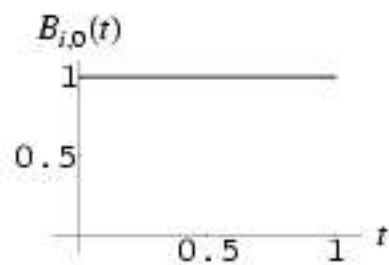
$$\bar{H}(X, \zeta, t) = \int_0^1 H(X, \zeta, t) b_{k,n}(X) dX \quad k = 1, \dots, n,$$

X-bin \Rightarrow

$$\bar{X}_{k,n} = \int_0^1 X b_{k,n}(X) dX = \frac{k+1}{n+1},$$

Dispersion \Rightarrow

$$\Delta_{k,n} = \left(\overline{X^2}_{k,n} - \bar{X}_{k,n}^2 \right)^{1/2}$$

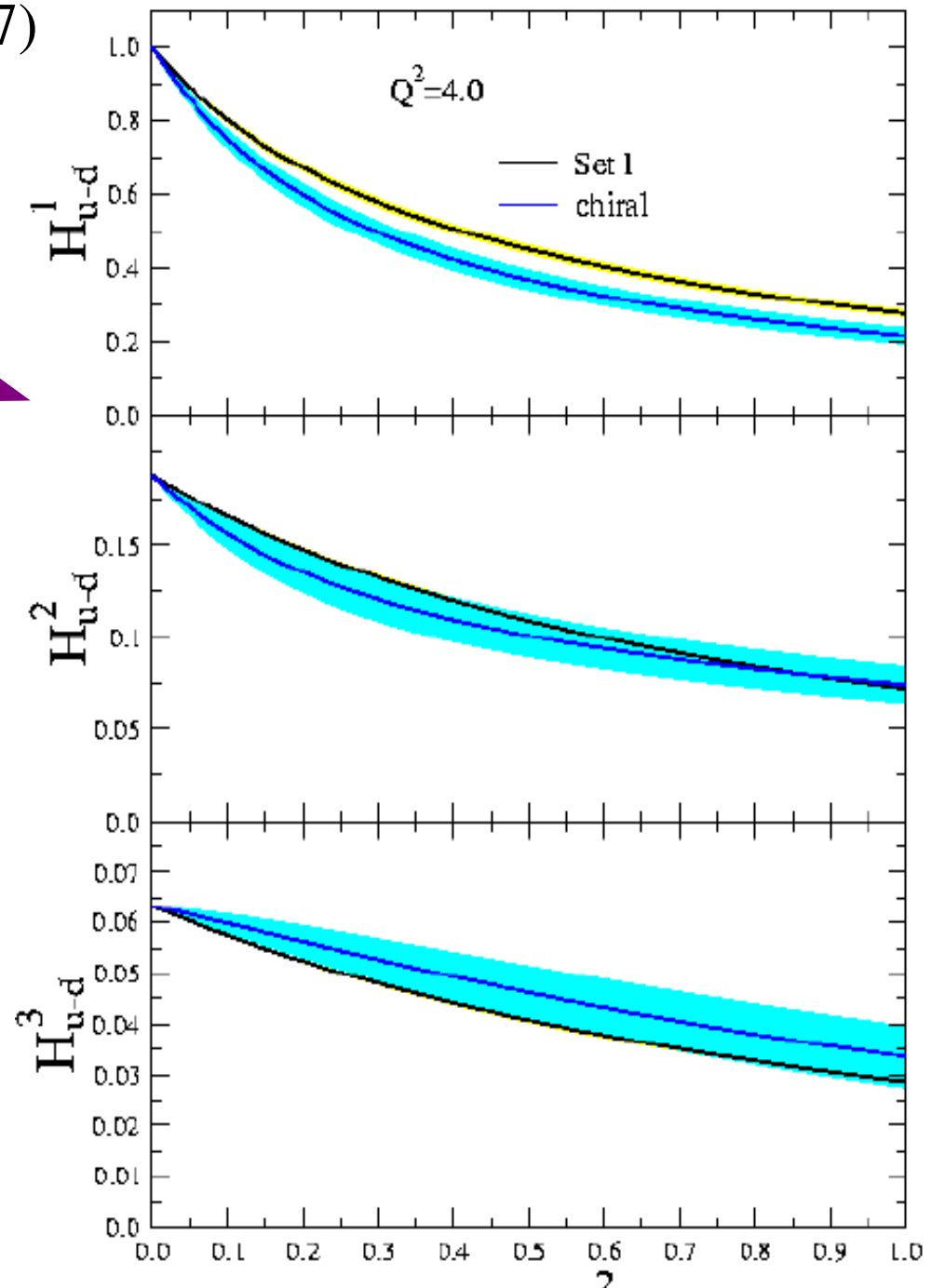
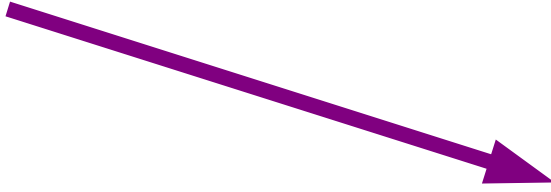


Chiral Extrapolations

Dorati, Gail and Hemmert (2007)

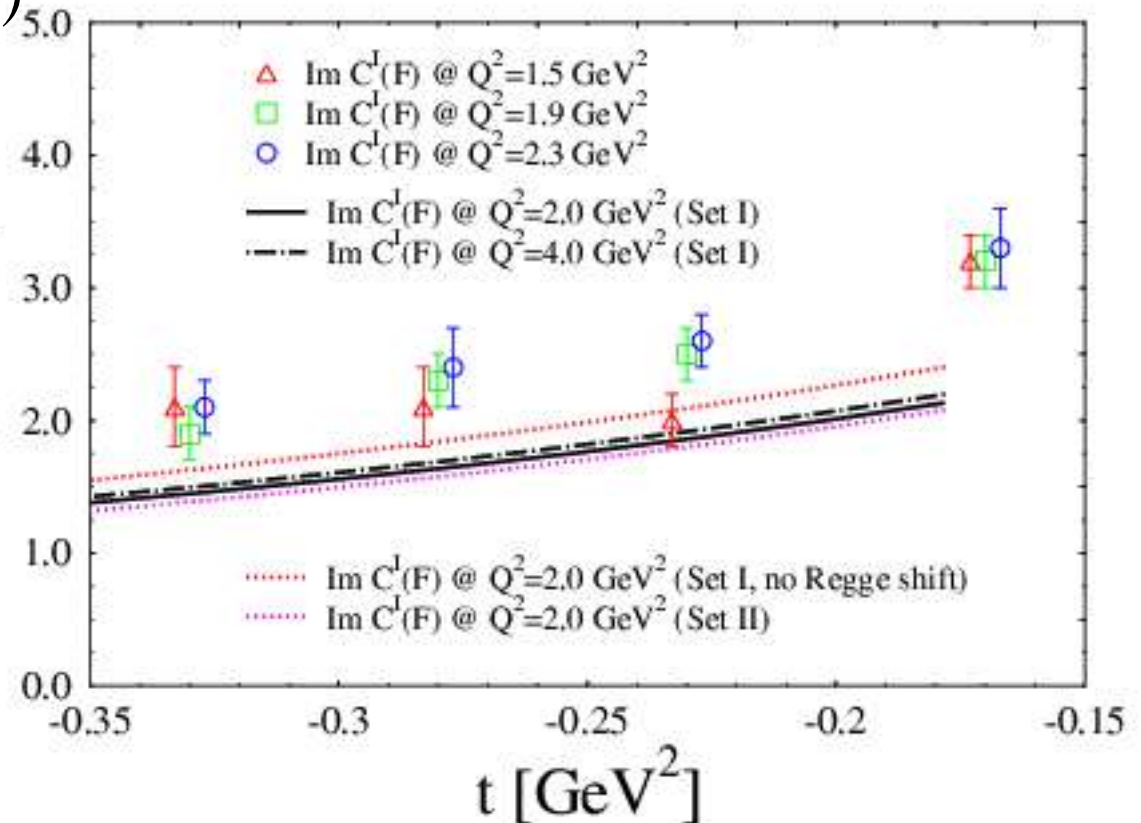
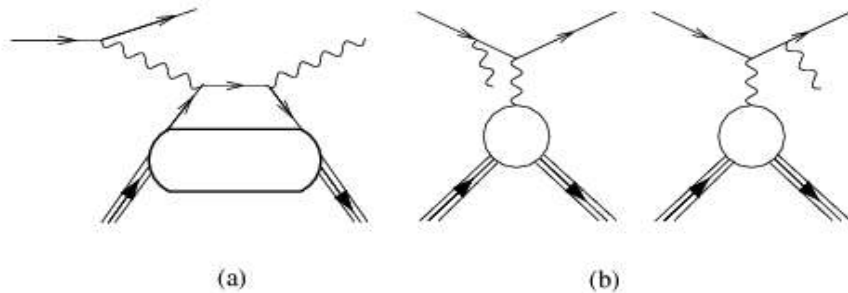
Wang and Thomas (2008)

⇒ Ashley et al. (2003)



Comparison with Jlab Hall A data (proton)

Munoz Camacho et al., (2006)

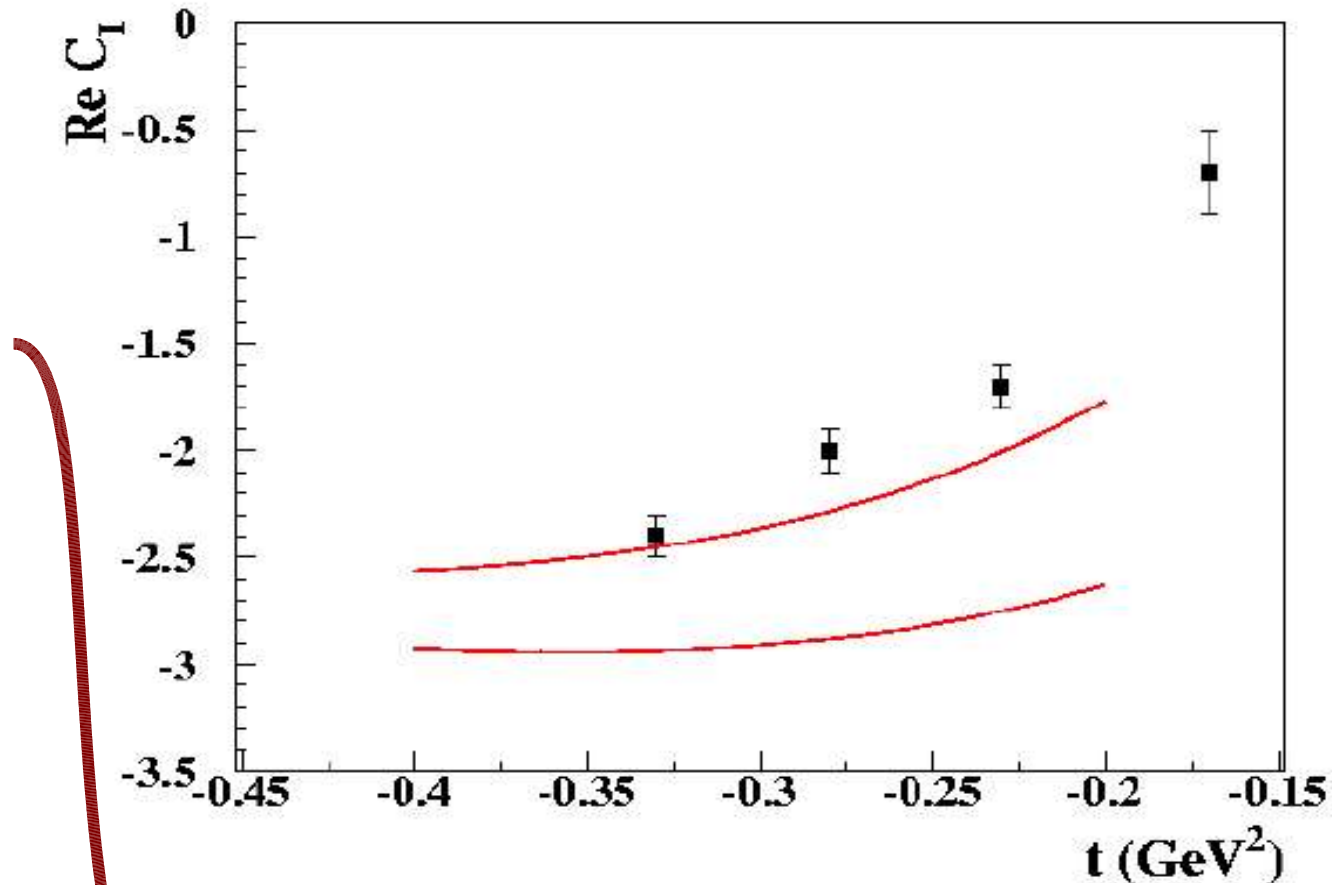


- Observable given by Interference Term between DVCS (a) and BH(b):

$$d\sigma^{\rightarrow} - d\sigma^{\leftarrow} \propto \sin\phi \left[F_1(\Delta^2)\mathcal{H} + \frac{x}{2-x}(F_1 + F_2)\tilde{\mathcal{H}} + \frac{\Delta^2}{M^2}F_2(\Delta^2)\mathcal{E} \right]$$

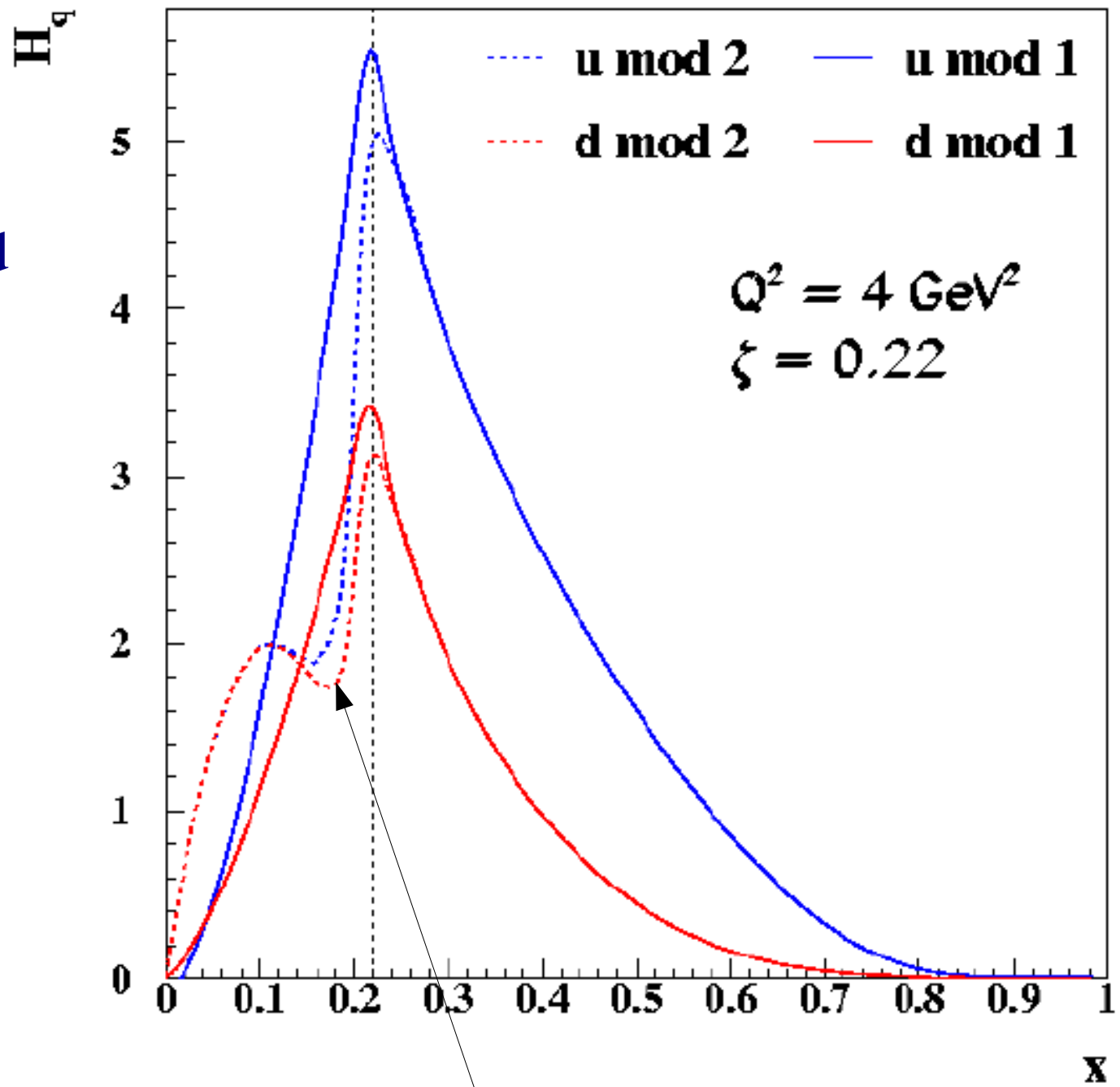
$$\mathcal{H} = \sum_q e_q^2 (H(\xi, \xi, \Delta^2) - H(-\xi, \xi, \Delta^2))$$

Real Part



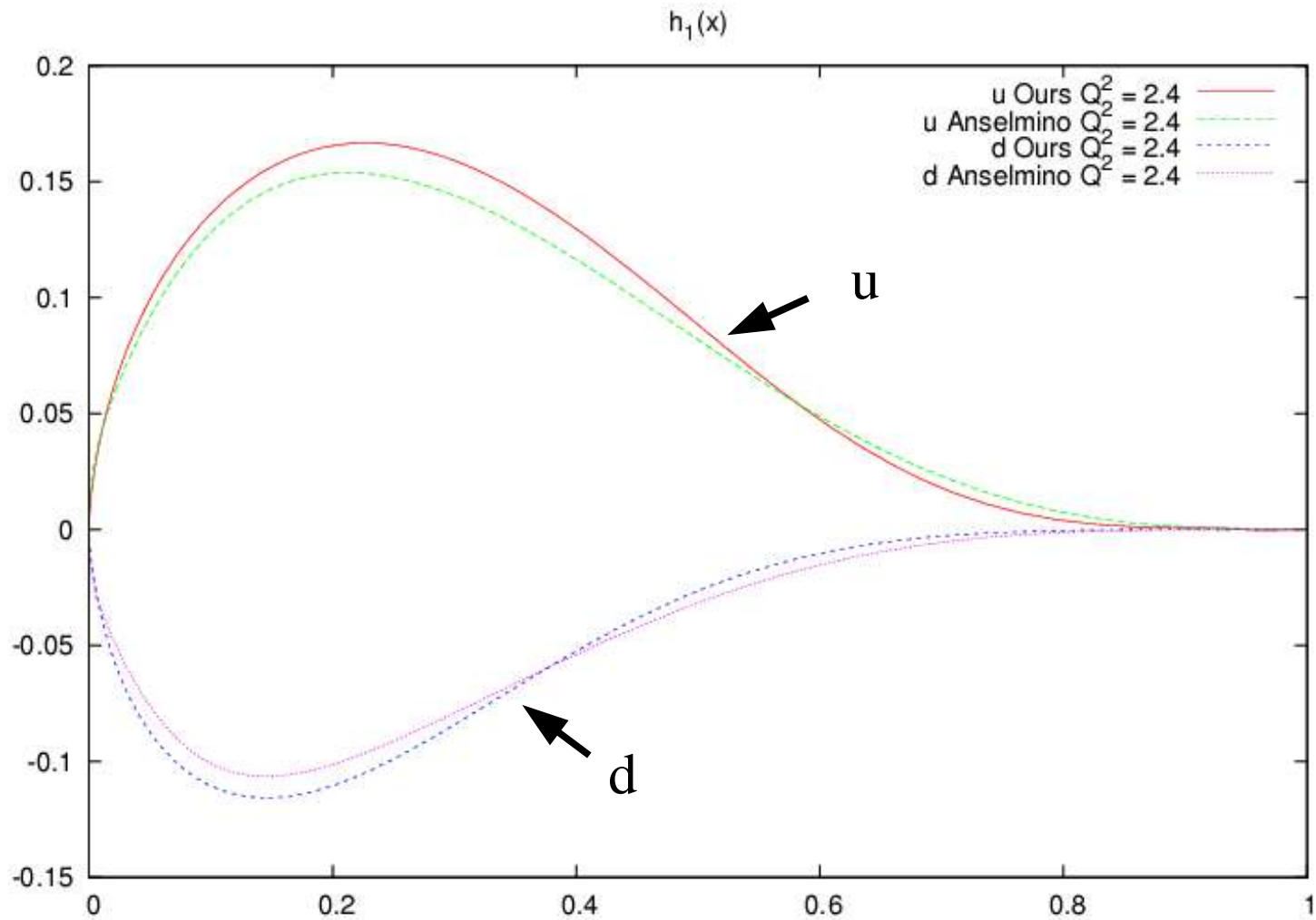
$$\mathcal{F}(\zeta, t) = -i\pi \sum_q e_q^2 [F^q(\zeta, \zeta, t) - F^q(-\zeta, \zeta, t)] +$$
$$\mathcal{P} \int_{1-\zeta}^1 dX \left(\frac{1}{X-\zeta} + \frac{1}{X} \right) F^q(X, \zeta, t).$$

S. Ahmad



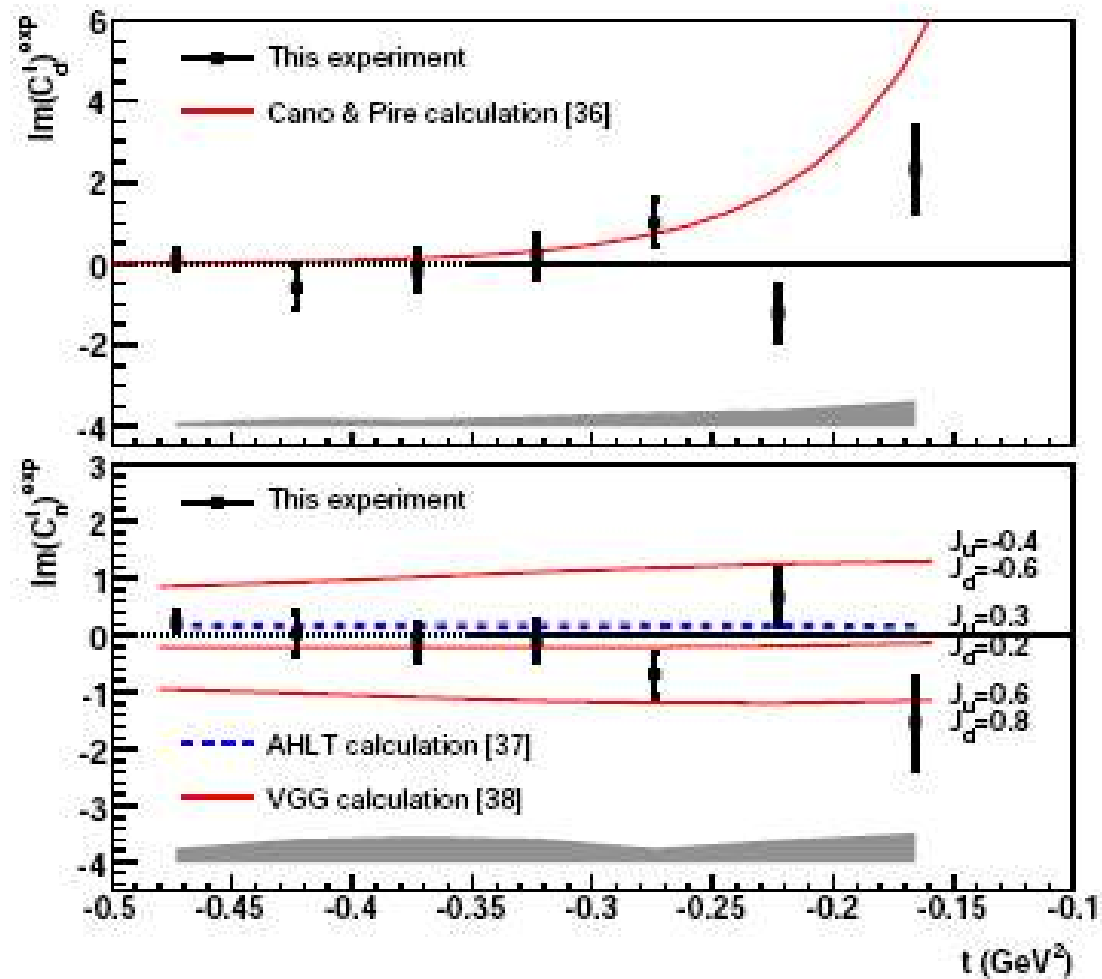
Behavior determined by Jlab data on Real Part and Q^2 dependence

Transversity



Comparison with Jlab Hall A data (neutron)

Mazouzet *al.*, (2007)



Conclusions and Outlook

- We presented a NEW method to extract transversity observables from experimental data on exclusive electroproduction experiments.
- We learn a number of interesting things along the way: physical interpretation of GPDs... (Partons \Leftrightarrow Regge)!
 - GPDs other than what claimed so far appear in pion production (chiral-odd GPDs)
 - Factorization can apply in transverse case as well
 - Paper to be posted shortly, stay tuned..
- νA scattering at Minerva involves GPDs (Spin 0 nuclei!)
- Big part of the program for Jlab at 12 GeV!
- Crossed channels?

