# Search for Rare Z Decays into Two Reconstructed Photons at CDF 

April 15 ${ }^{\text {th }}, 2013$<br>Baylor HEP Seminar<br>Karen Bland<br>for the CDF collaboration

Public webpage:
http://www-cdf.fnal.gov/physics/exotic/run2/Zgamgam/index.html

## Outline

- Introduction
- Tevatron and CDF Detector
- Diphoton Event Selection
- Photon Selection
- Photon ID Efficiency
- Signal MC Samples
- Backgrounds
- Limit Calculation


## Introduction

- Properties of the W and Z bosons have been studied extensively by collider experiments
- Most of the information we know about the vector bosons however comes from leptonic decays, $\mathrm{W} \rightarrow \mathrm{l}^{-} v$ and $\mathrm{Z} \rightarrow 1^{+} 1^{-}$
- In addition to hadronic W and Z decays, there has been interest by theorists to further understand properties of the vector ( V ) bosons by searching for $\mathrm{V} \rightarrow \mathrm{P}+\gamma$, where P is a pseudoscalar meson (such as a pion)
- Observation of such decays would be a sensitive probe of strong interaction dynamics and vector boson couplings to the photon


## Introduction

- The challenge for these decay modes is the very small predicted branching ratios (BR), ranging from about $\sim 10^{-6}$ to $\sim 10^{-11}$ in the SM
- However, with an abundance of vector bosons produced at the Tevatron and LHC, further searches can improve the experimental upper bounds on these branching ratios that were obtained from LEP
- Furthermore, any significant deviations of the SM prediction of the $B R$ of these decays to observation could indicate new physics


## Introduction

- In the analysis presented here, we focus on both rare and forbidden decays of the Z boson*
- Among the rare Z decays, we focus on $\mathrm{Z} \rightarrow \pi^{0} \gamma$, which is experimentally interesting because of the clean signature the decay products leave in the detector


[^0]
## Introduction

- We also search for the forbidden decays, $Z \rightarrow \gamma \gamma$ and $Z \rightarrow \pi^{0} \pi^{0}$
- The Z boson is a spin-1 particle
- Along with conservation of angular momentum, the identity of the final-state particles in the $Z \rightarrow \gamma \gamma$ and $Z \rightarrow \pi^{0} \pi^{0}$ decays forbids them in the SM
- That the $Z \rightarrow \gamma \gamma$ decay is forbidden is due to the Landau-Yang theorem, which forbids a spin-1 particle decaying to two spin-1 particles*
- (Since the Higgs-like particle discovered at the LHC decays to two photons, it is not expected to be a spin-1 particle due to Landau-Yang theorem)
- There exist theory papers that motivate a search for a $Z \rightarrow \gamma \gamma$ decay as a test of Bose-Einstein statistics
*A recent paper gives an argument that would allow this process through an axial coupling (arxiv:1109.0926)


## Introduction

- No limits from Tevatron or LHC on these decays


## $\Gamma(\gamma \gamma) / \Gamma_{\text {total }}$

This decay would violate the Landau-Yang theorem.

- Most stringent limits in PDG on $\mathrm{Br}(Z \rightarrow \gamma \gamma)$ and $\mathrm{Br}\left(Z \rightarrow \pi^{0} \gamma\right)$ are from LEP
- Both are $5.2 \times 10^{-5}$ at $95 \%$ C.L.
- No search has been performed for $\mathrm{Z} \rightarrow \pi^{0} \pi^{0}$

| VALUE | CL\% | DOCUMENT ID |  | TECN |
| :---: | :---: | :---: | :---: | :---: |
| $<5.2 \times 10^{-5}$ | 95 | 62 ACCIARRI | 95G | L3 |
| $<5.5 \times 10^{-5}$ | 95 | ABREU | 94B | DLPH |
| $<1.4 \times 10^{-4}$ | 95 | AKRAWY | 91F | OPAL |

$\Gamma\left(\pi^{0} \gamma\right) / \Gamma_{\text {total }}$

| VALUE | $C L \%$ | DOCUMENT ID |  | TECN |  |
| :---: | :---: | :---: | :---: | :--- | :--- |
| $<5.2 \times 10^{-5}$ | 95 | 61 | ACCIARRI | $95 G$ | L3 |
| $<5.5 \times 10^{-5}$ | 95 | ABREU | 94 B | DLPH |  |
| $<2.1 \times 10^{-4}$ | 95 | DECAMP | 92 | ALEP |  |
| $<1.4 \times 10^{-4}$ | 95 | AKRAWY | $91 F$ | OPAL |  |

PDG Particle Listings: Z Boson
J. Beringer et al. (Particle Data Group), PR D86, 010001 (2012) (URL: http://pdg.lbl.gov)

## Introduction



- $\pi^{0}$ from the $\mathrm{Z} \rightarrow \pi^{0} \gamma$ or $\mathrm{Z} \rightarrow \pi^{0} \pi^{0}$ decay:
- Isolated (not in a jet)
- Decays $98.8 \%$ to a pair of photons
- High momentum $\pi^{0}$ from the $Z$ decay leads to collinear pairs of photons, which often appear as a single electromagnetic shower in the detector rather than separated showers
- Experimentally, the isolated $\pi^{0}$ shower in the detector is nearly indistinguishable from the isolated $\gamma$ shower
- For the $Z \rightarrow \gamma \gamma, Z \rightarrow \pi^{0} \gamma$, and $Z \rightarrow \pi^{0} \pi^{0}$ search then, we use already developed tools from $\mathrm{H} \rightarrow \gamma \gamma$ analysis at CDF to identify events with two reconstructed photons


## Tevatron

- $\mathrm{p} \overline{\mathrm{p}}$ collisions at $\mathrm{V} s=1.96 \mathrm{TeV}$
- Shut down on Sept. 30 ${ }^{\text {th }}, 2011$
- $\mathcal{L} \approx 12 \mathrm{fb}^{-1}$ delivered



## CDF Detector



## CDF Detector and Particle Identification

$e$ 's and $\gamma$ 's interact in calorimetry via electromagnetic cascades

Hadrons interact in calorimetry via cascades of nuclear interactions


The CDF detector is designed to differentiate between many different types of final state particles

## Summary of $H \rightarrow \gamma \gamma$ Techniques

- Event Selection:
- Isolated photon trigger ( 25 GeV cut)
- Identify two 15 GeV CEM photons using central NN selection
- Signal Model:
- Shape and acceptance from Pythia MC
- Isolated photon trigger and photon ID efficiency validated in $\mathrm{Z} \rightarrow \mathrm{e}+\mathrm{e}-$ data
- Background Model:
- Exploit resonant feature of H decay into photons
- Use sideband regions of diphoton mass to determine background shape and rate in signal region

Modifications for $Z \rightarrow \gamma \gamma / \pi^{0} \gamma$ Analysis

- Event Selection:
- Isolated photon trigger
( 25 GeV cut)
- Identify two 15 GeV CEM photons using central NN selection
- Signal Model:
- Shape and acceptance from a modified (angle- or $\pi^{0}$ efficiencyweighted) Pythia MC
- Isolated photon trigger and photon ID efficiency validated in $\mathrm{Z} \rightarrow \mathrm{e}+\mathrm{e}-$ data
- Background Model:
- Exploit resonant feature of $Z$ decay into photons
- Use sideband regions of diphoton mass to determine background shape and rate in signal region
- Model Z $\rightarrow$ e+e- from Pythia MC



## Diphoton Event Selection

- Use data corresponding to $10.0 \mathrm{fb}-1$ of integrated luminosity
- Diphoton data collected from an inclusive photon trigger
- Single EM cluster with $\mathrm{E}_{\mathrm{T}}>25 \mathrm{GeV}$
- Trigger efficiency after offline selection obtained from trigger simulation software (TrigSim)
- MC samples corrected based on trigger efficiency
- Require two central reconstructed photons with $\mathrm{p}_{\mathrm{T}}>15 \mathrm{GeV}$
- Photon selection described in coming slides
- The Z boson mass signal region is chosen to be $80-102 \mathrm{GeV}$, where about $90 \%$ of the signal lies


## Photon Identification

- Basic Photon Signature:
- Compact EM cluster
- Isolated
- No high momentum track associated with cluster
- Profile (lateral shower shape) consistent with that of a prompt photon
- Unlike that of $\pi^{0} \eta \rightarrow \gamma \gamma$ decays inside of jets (the largest background for prompt photons)



## Photon Identification

- Three level selection
- (1) Loose requirements
- Fiducial in shower max detector
- Ratio of hadronic to electromagnetic transverse energy (Had/EM) < 12.5\%
- Calorimeter isolation
- $I=E_{T}^{\text {Tot }}(\Delta R<0.4)-E_{T}^{E M}$
- Cut slides with $E_{T}^{E M}$
- Track isolation
- (2) Track veto
- Number tracks $\leq 1$
- If 1 , then $\mathrm{p}_{\mathrm{T}}{ }^{\text {trk } 1}<1 \mathrm{GeV}$
- (3) Cut on NN Output
- More details on next slides


## Electron Identification

- Three level selection
- (1) Loose requirements
- Fiducial in shower max detector
- Ratio of hadronic to electromagnetic transverse energy (Had/EM) < 12.5\%
- Calorimeter isolation
- $I=E_{T}^{\text {Tot }}(\Delta R<0.4)-E_{T}^{E M}$
- Cut slides with $E_{T}^{E M}$
- Track isolation
- (2) Track veto
- Number tracks $\leq 2$
- If 2 , then $\mathrm{p}_{\mathrm{T}}{ }^{\text {trk } 2}<1 \mathrm{GeV}$
- (3) Cut on NN Output
- More details on next slides
- No pure high statistics data sample of photons to validate ID efficiency
- Selection chosen so can be modified for electrons
- Then use $Z \rightarrow e^{+} e^{-}$decays (more detail later)


## Photon Identification

NN discriminant constructed from seven well understood variables:

- Ratio of hadronic to EM transverse energy
- Shape in shower max compared to expectation
- Calorimeter Isolation
- Track isolation
- Ratio of energy at shower max to total EM energy
- Lateral sharing of energy between towers compared to expectation
- Relative to standard photon selection, increases photon signal efficiency by $5 \%$ and jet background rejection by 12\%

Trained using Monte Carlo (MC) simulated events with photons (blue) and events with jets (red)


## Photon ID Efficiency




- ID efficiency checked in data and MC from $Z \rightarrow e^{+} e^{-}$decays
- Z mass constraint applied to get a pure sample of electrons to probe
- Effect of overlapping collisions (pile-up) seen through $\mathrm{N}_{\mathrm{vtx}}$ dependence
- Net efficiencies obtained by folding $\varepsilon_{\mathrm{vtx}}$ into $\mathrm{N}_{\mathrm{vtx}}$ distribution of diphoton data and signal MC (a weighted average)
- Net photon ID efficiency:

Data: 83.3\% MC: 88.2\%

- Correction factor of $94.4 \%$ applied to signal MC simulation
- Total systematic uncertainty of $\sim 2 \%$ applied from:
- Differences between electron vs photon response (checked in MC)
- Data taking period dependence
- Fits made to $Z$ mass distribution
- Small uncertainties using this method!


## $\pi^{0}$ Photon ID Efficiency

- We use $\gamma$ and $\pi^{0}$ from (particle gun) MC samples to study the photon ID efficiency for neutral pions compared to neutral photons as a function of Et
- $\pi^{0}$ 's from Z boson decays have an average Et around 45 GeV
- For this Et region, the photons from most $\pi^{0}$ decays is highly collinear, appearing as a single EM shower rather than separated as two EM showers
- We find these isolated $\pi^{0}$ 's to have an efficiency to our photon ID selection that is about $2 \%$ smaller on average than isolated photons



## Signal MC Samples

- Pythia has no decay table for $Z \rightarrow \gamma \gamma$, so we first start with a $\mathrm{Z} \rightarrow v_{\mathrm{e}} \nu_{\mathrm{e}}$ Pythia sample and then convert the neutrino/antineutrino to photons before showering in Pythia and passing through CDF detector simulation
- This is called the " $\mathrm{Z} \rightarrow \gamma \gamma$ unweighted model"
- The photons of this sample have a generated angular distribution for that of the neutrino/ antineutrino


## Signal MC Samples

- $\mathrm{Z} \rightarrow \pi^{0} \gamma$ Model
- Determined to have the same angular distribution as the neutrinos $\sim\left(\alpha+\cos ^{2} \theta\right)$ with $\alpha$ a constant
- Slightly different photon defection efficiency $\rightarrow$ The $\pi^{0}$ is then corrected for the observed $2 \%$ difference in $\pi^{0} / \gamma$ efficiency
- $\mathrm{Z} \rightarrow \gamma \gamma$ and $\mathrm{Z} \rightarrow \pi^{0} \pi^{0}$ Models
- Determined to have different angular distribution as the neutrinos (but same as each other)
- We then correct the unweighted $\mathrm{Z} \rightarrow \gamma \gamma$ sample to the expected angular distribution of these decays $\sim\left(\beta-\cos ^{2} \theta\right)$ with $\beta$ a constant
- The $\mathrm{Z} \rightarrow \pi^{0} \pi^{0} \mathrm{MC}$ sample is furthermore corrected based on the $2 \%$ difference observed in in $\pi^{0} / \gamma$ efficiency
- The next dozen slides describe the method for obtaining angular distributions for each decay mode


## Angular Distribution Formulas*

We consider the decay of a particle with spin $s_{0}$ with polarization state $m_{0}$ that decays into two particles that have helicities $\lambda_{1}$ and $\lambda_{2}$. In the helicity basis, the angular distribution of a specific polarization and helicity state is taken to be proportional to a the square of the corresponding d-function:

$$
F_{m_{0} \lambda_{1} \lambda_{2}}(\theta) \propto\left|d_{m_{0} \lambda_{1}-\lambda_{2}}^{s_{0}}(\theta)\right|^{2}
$$

We obtain the net angular distribution by summing over all the polarization and helicity states considered, each weighted by the states probability:

$$
F(\theta)=\sum_{m_{0} \lambda_{1} \lambda_{2}} f_{m_{0} \lambda_{1} \lambda_{2}}\left|d_{m_{0} \lambda_{1}-\lambda_{2}}^{s_{0}}(\theta)\right|^{2}
$$

The following restriction is made on helicity states due to conservation of angular momentum:

$$
\left|\lambda_{1}-\lambda_{2}\right| \leq s_{0}
$$

We apply these formulas to $Z$ boson decays...

## Angular Distribution Formulas*

- Definition of angle $\theta$ :
- In Z boson rest frame, angle between momentum direction of first decay product and spin quantization axis of
Z boson (z-axis)



## Z boson polarization from Drell Yan

A $Z$ boson decay will have $s_{0}=1$. Since we model the $Z$ production and decay using Pythia, the $Z$ is expected to be polarized. For head-on collisions of (massless) quarks, conservation of total angular momentum and of the $z$-component in the lab frame imply the following longitudinal spin orientations:


ISR and UE cause quark collisions to have some angle $\neq 180^{\circ}$ which generate a finite transverse $f_{0}$, which we include as a contribution to the total angular distribution.


We then allow $m_{0}=+1,0$, and -1 , each occurring with probability $f_{+}, f_{-}$, and $f_{0}$, respectively. Due to symmetry, we assume $f_{+}=f_{\text {. }}$.

## $\mathrm{Z} \rightarrow \boldsymbol{v}_{\mathrm{e}} \bar{\nu}_{\mathrm{e}}$ decay

With left-handed (massless) neutrinos and right-handed (massless) antineutrinos,

$\lambda_{\vec{v}}-\lambda_{v}=\frac{1}{2}-\left(-\frac{1}{2}\right)=1 \quad \boldsymbol{V}_{\mathrm{e}}$

where $f_{-}, f_{0}$, and $f_{+}$are the left-handed, longitudinal, and right-handed polarizations of $Z$, and $\theta$ is the angle between $v_{e}$ and the $z$ axis. From symmetry, $f_{-}=f_{+}$. For unpolarized $Z\left(f_{+}=f_{0}\right)$ the sum of the three angular distributions is a constant:

$$
\left(d_{1,1}^{1}\right)^{2}+\left(d_{1,0}^{1}\right)^{2}+\left(d_{1,-1}^{1}\right)^{2}=1
$$

For polarized $Z\left(f_{+} \neq f_{0}\right)$ :

$$
\begin{equation*}
F_{v \bar{v}}(\theta)=f_{+}\left(d_{1,1}^{1}\right)^{2}+f_{0}\left(d_{1,0}^{1}\right)^{2}+f_{-}\left(d_{1,-1}^{1}\right)^{2}=\frac{f_{+}-f_{0}}{2}\left(\frac{f_{+}+f_{0}}{f_{+}-f_{0}}+\cos ^{2} \theta\right) \tag{26}
\end{equation*}
$$

## Angular Distribution of Unweighted Z $\rightarrow \gamma \gamma$ MC Sample

$$
F_{v \bar{v}}(\theta)=\frac{\left(f_{+}-f_{0}\right)}{2}\left(\frac{f_{+}+f_{0}}{f_{+}-f_{0}}+\cos ^{2} \theta\right)
$$

We determine the unknown values of the $f_{+}$and $f_{0}$ parameters by fitting to the neutrino angular distributions in the $Z$ rest frame using the MC simulated data.

$$
\mathrm{Z} \rightarrow v_{\mathrm{e}} \bar{v}_{\mathrm{e}} \text { decay }
$$

We fit to the MC histogram with:

$$
F(\theta)=p_{0}\left(p_{1}+\cos ^{2} \theta\right)
$$

With best fit parameters of $\mathrm{p} 0=2811$ and p1 = 1.32, we obtain
$F_{v \bar{v}}(\theta)=2811\left(1.32+\cos ^{2} \theta\right)$
Which gives $f_{+}=7.26 f_{0}$.


## $\mathrm{Z} \rightarrow \pi^{0} \gamma$ decay

$\lambda_{\gamma}$ can be $\pm 1$ and $\lambda_{\pi}$ can be only zero. We then have the following spin states:

$$
\lambda_{r}-\lambda_{\pi}=1-0=1
$$


$\left(d_{-1,1}^{1}\right)^{2}=\left(d_{1,-1}^{1}\right)^{2}=\frac{1}{4}(1-\cos \theta)^{2}$
$\left(d_{0,1}^{1}\right)^{2}=\left(d_{1,0}^{1}\right)^{2}=\frac{1}{2} \sin ^{2} \theta$

$$
\left(d_{1,1}^{1}\right)^{2}=\frac{1}{4}(1+\cos \theta)^{2}
$$

The angular distributions are the same as with the neutrino decay. No neutrino to reweighting function is then needed to correct the unweighted $\mathrm{Z} \rightarrow \gamma \gamma$ (neutrino) angular distributions to the expected $\pi^{0} \gamma$ angular distributions.

## $\mathrm{Z} \rightarrow \gamma \gamma$ decay

Angular momentum conservation ( $\left|\lambda_{\gamma 1}-\lambda_{\gamma_{2}}\right| \leq s_{z}=1$ ) excludes parallel photon spins and $\lambda_{\gamma 1}=\lambda_{\gamma 2}=0$ scenarios are excluded because photons are massless. We then have:



$$
\left(d_{0,0}^{1}\right)^{2}=\cos ^{2} \theta
$$



$$
\left(d_{1,0}^{1}\right)^{2}=\frac{1}{2} \sin ^{2} \theta
$$

For unpolarized $Z\left(f_{+}=f_{0}\right)$ the sum of the three angular distributions is a constant:

$$
\left(d_{1,0}^{1}\right)^{2}+\left(d_{0,0}^{1}\right)^{2}+\left(d_{1,0}^{1}\right)^{2}=1
$$

For polarized $Z\left(f_{+} \neq f_{0}\right)$ :

$$
F_{r \gamma}(\theta)=f_{+}\left(d_{1,0}^{1}\right)^{2}+f_{0}\left(d_{0,0}^{1}\right)^{2}+f_{-}\left(d_{1,0}^{1}\right)^{2}=\left(f_{+}-f_{0}\right)\left(\frac{f_{+}}{f_{+}-f_{0}}-\cos ^{2} \theta\right)
$$

## Neutrino to Photon Angle-Weight Function

We insert $f_{+}=7.26 f_{0}$ (which we got from the $Z \rightarrow v v$ sample) into

$$
F_{r \gamma}(\theta)=\left(f_{+}-f_{0}\right)\left(\frac{f_{+}}{f_{+}-f_{0}}-\cos ^{2} \theta\right)
$$

to obtain the formula we expect for the photons from $Z \rightarrow \gamma \gamma$ in the Pythia sample:

$$
F_{r \gamma}(\theta)=2811\left(1.16-\cos ^{2} \theta\right)
$$

This gives the following neutrinos-to-photons reweighting function to be used to correct the unweighted $Z \rightarrow \gamma \gamma$ to what we expect for photons:

$$
w_{\gamma \gamma}(\theta)=\frac{F_{v \bar{v}}(\theta)}{F_{\gamma \gamma}(\theta)}=\frac{1.16-\cos ^{2} \theta}{1.32+\cos ^{2} \theta}
$$

Neutrino-photon angular weights correct the unweighted $Z \rightarrow \gamma \gamma$ sample to the expected angular distribution

> Unweighted
$\mathrm{Z} \rightarrow \gamma \gamma$ decay


## Neutrino to Photon Angle-Weight Function

We insert $f_{+}=7.26 f_{0}$ (which we got from the $Z \rightarrow v v$ sample) into

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F_{\gamma \gamma}(\theta)=\left(f_{+}-f_{0}\right)\left(\frac{f_{+}}{f_{+}-f_{0}}-\cos ^{2} \theta\right)
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$$

Neutrino-photon angular weights correct the unweighted $Z \rightarrow \gamma \gamma$ sample to the expected angular distribution

## Angle-Weighted

$\mathrm{Z} \rightarrow \gamma \gamma$ decay


$$
\mathrm{Z} \rightarrow \pi^{0} \pi^{0} \text { decay }
$$

$\lambda_{\pi}$ can be only zero. We then have the following spin states:

$\left(d_{-1,0}^{1}\right)^{2}=\left(d_{1,0}^{1}\right)^{2}=\frac{1}{2} \sin ^{2} \theta$

$$
\lambda_{\pi}-\lambda_{\pi}=0-0=0
$$



$$
\left(d_{0,0}^{1}\right)^{2}=\cos ^{2} \theta
$$



$$
\left(d_{1,0}^{1}\right)^{2}=\frac{1}{2} \sin ^{2} \theta
$$

The angular distributions are the same as with the $\mathrm{Z} \rightarrow \gamma \gamma$ decay. We then apply the neutrino to $\gamma$ reweighting function to the $Z \rightarrow \pi^{0} \pi^{0}$ decay.

## Signal MC Samples: Summary

- Unweighted $Z \rightarrow \gamma \gamma$ MC Sample
- Has angular distribution of neutrinos $\sim\left(\alpha+\cos ^{2} \theta\right)$ with $\alpha$ a constant
- $\mathrm{Z} \rightarrow \pi^{0} \gamma$ Model
- Determined to have the same angular distribution as the neutrinos
- Start with unweighted $\mathrm{Z} \rightarrow \gamma \gamma$ MC sample then, and correct for the observed $2 \%$ difference in $\pi^{0} / \gamma$ efficiency
- $\mathrm{Z} \rightarrow \gamma \gamma$ and $\mathrm{Z} \rightarrow \pi^{0} \pi^{0}$ Models
- Determined to have different angular distribution as the neutrinos (but same as each other)
- Start with unweighted Z $\rightarrow \gamma \gamma$ MC sample, then correct to the expected angular distribution of these decays: $\sim\left(\beta-\cos ^{2} \theta\right)$ with $\beta$ a constant
- The $\mathrm{Z} \rightarrow \pi^{0} \pi^{0}$ decay is furthermore corrected based on the $2 \%$ difference observed in in $\pi^{0} / \gamma$ efficiency


## Signal Diphoton Mass Shapes

- After all corrections, reconstructed mass shape of each decay is obtained
- Expected to be the same for each signal decay mode
- This is because the calorimeter response for $\pi^{0}$ is found to be the same as that for isolated photons for $\pi^{0}$ with Et around 45 GeV , determined by studying energy scale


## Signal Acceptance $\times$ Efficiency

- Both the angular distributions and the photon identification efficiency affect the fraction of $\mathrm{Z} \rightarrow \pi^{0} \gamma$, $\mathrm{Z} \rightarrow \gamma \gamma$ and $\mathrm{Z} \rightarrow \pi^{0} \pi^{0}$ that pass the full diphoton event selection
- Difference in acceptance $\times$ efficiency for $\mathrm{Z} \rightarrow \pi^{0} \gamma$ relative to $\mathrm{Z} \rightarrow \gamma \gamma$ and $\mathrm{Z} \rightarrow \pi^{0} \pi^{0}$ is almost entirely due to difference in angular distribution
- Difference in acceptance $\times$ efficiency for $\mathrm{Z} \rightarrow \gamma \gamma$ relative to $\mathrm{Z} \rightarrow \pi^{0} \pi^{0}$ is due to difference in $\pi^{0} / \gamma$ photon ID efficiency

| Signal Decay Mode | $Z \rightarrow \pi^{0} \gamma$ | $Z \rightarrow \gamma \gamma$ | $Z \rightarrow \pi^{0} \pi^{0}$ |
| :--- | :--- | :--- | :--- |
| Acc * Eff $\left(\mathrm{m}_{\gamma \gamma}=80-102 \mathrm{GeV}\right)$ | $5.5 \%$ | $7.6 \%$ | $7.3 \%$ |

## Signal Yields

- In principle, could obtain signal yields from

$$
\begin{gathered}
N_{\mathrm{Z} \rightarrow \gamma \gamma}=\frac{\sigma(Z \rightarrow e e)}{\operatorname{Br}(Z \rightarrow e e)} \cdot \operatorname{Br}(Z \rightarrow \gamma \gamma) \cdot L \cdot(A \epsilon)_{Z \rightarrow \gamma \gamma}, \\
N_{\mathrm{Z} \rightarrow \pi^{0} \gamma}=\frac{\sigma(Z \rightarrow e e)}{\operatorname{Br}(Z \rightarrow e e)} \cdot \operatorname{Br}\left(Z \rightarrow \pi^{0} \gamma\right) \cdot L \cdot(A \epsilon)_{Z \rightarrow \pi^{0} \gamma}, \\
N_{\mathrm{Z} \rightarrow \pi^{0} \pi^{0}}=\frac{\sigma(Z \rightarrow e e)}{\operatorname{Br}(Z \rightarrow e e)} \cdot \operatorname{Br}\left(Z \rightarrow \pi^{0} \pi^{0}\right) \cdot L \cdot(A \epsilon)_{Z \rightarrow \pi^{0} \pi^{0}},
\end{gathered}
$$

where $\sigma(\mathrm{Z} \rightarrow$ ee $)$ is $250 \mathrm{pb}, \operatorname{Br}(\mathrm{Z} \rightarrow$ ee $)=0.034$, $\mathrm{L}=10.0 \mathrm{fb}-1$, and $\mathrm{A} \varepsilon$ is acceptance $\times$ efficiency values from previous slide

- We assume no theoretical branching ratio however
- Later, signal branching ratios become a parameter of 95\% C.L. limit calculation


## Background Model

- Resonant background ( $2 \%$ of total bkg)
- Drell-Yan
- Modeled with MC

- Smooth $\mathrm{m}_{\gamma \gamma}$ backgrounds ( $\sim 98 \%$ of total bkg )
- Modeled from fit to $\mathrm{m}_{\gamma \gamma}$ sideband region
- Fit is made to Drell-Yan subtracted data
- Composition:
- $\gamma \gamma$ from QCD processes ( $\sim 2 / 3$ of smooth bkg); irreducible
- $\gamma \mathrm{j}$ or jj : one or two jets faking a photon ( $\sim 1 / 3$ of smooth bkg)



## Drell-Yan Background

- Drell-Yan background arises from electrons faking photons
- Use inclusive $\mathrm{Z} \rightarrow \mathrm{e}+\mathrm{e}-$ Pythia MC sample
$\sigma=355 \mathrm{pb}$ and a k -factor $=1.4$
- $\mathrm{L}=10.0 / \mathrm{fb}$
- Acceptance $\times$ diphoton efficiency, $\mathrm{A} \varepsilon_{\gamma v}$, for full mass range: $0.0031 \%$
- N expected $=\sigma^{\bullet} \mathrm{k} \bullet \mathrm{L} \bullet \mathrm{A} \varepsilon_{\gamma \gamma}$

$$
=154 \text { events }
$$

for entire mass range

- 54 of these events expected in signal region, $m_{\gamma \gamma}=80-102 \mathrm{GeV}$



## Non-Resonant Backgrounds

- We do not model the prompt diphoton and jet faking photons background separately
- Instead use mass sidebands to determine shape and yield in signal region
- First subtract Drell-Yan component from data
- Then fit to sideband regions of DY-subtracted data
- Fit is interpolated into signal region


Fit to DY-subtracted data (linear scale)

## Non-Resonant Backgrounds

- We do not model the prompt diphoton and jet faking photons background separately
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- First subtract Drell-Yan component from data
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- Fit is interpolated into signal region


Fit to DY-subtracted data (log scale)

## Background Model versus Data

 Sideband and Signal Region

## Background Model versus Data

Signal Region

| $Z \rightarrow \gamma \gamma / \pi^{0} \gamma / \pi^{0} \pi^{0}$ Search | CDF Run II Preliminary, $10.0 \mathrm{fb}^{-1}$ |
| :---: | :---: |
| Process | Number of Events for $80<m_{\gamma \gamma}<102 \mathrm{GeV}$ |
| Drell-Yan | $54 \pm 5$ |
| $\gamma \gamma, \gamma j$, and $j j$ | $2251 \pm 61$ |
| Total background | $2305 \pm 61$ |
| Data | 2294 |



- No evidence for resonance in diphoton mass distribution
- So we set 95\% C.L. limits on the branching ratios of the signal
- The mass shapes and event yields shown here are inputs to this calculation


## Limit Calculation

- Binned mass shapes given as inputs
- Use mclimit software to set a Bayesian 95\% C.L. upper limit on signal Br
- The binned likelihood as a function of
$f=\operatorname{Br}\left(\mathrm{Z} \rightarrow \pi^{0} \gamma\right), \operatorname{Br}(\mathrm{Z} \rightarrow \gamma \gamma)$, or $\operatorname{Br}\left(\mathrm{Z} \rightarrow \pi^{0} \pi^{0}\right)$ :

$$
\begin{gathered}
L(f)=\prod_{i=1}^{N_{\text {bins }}} \frac{\mu(f)_{i}^{n_{i}} e^{-\mu(f)_{i}}}{n_{i}!} \\
\mu_{i}(f)=f s_{i}+b_{i}
\end{gathered}
$$

- $n_{i}=$ number of data (pseudodata) events for observed (expected) limit
- $s_{i}$ is $\sigma L A \varepsilon$ of signal
- $b_{i}$ is sum of backgrounds
- $95 \%$ confidence limit obtained by finding the value of $f_{95}$ for which:

$$
0.95=\int_{0}^{f_{95}} L(f) d f
$$

- Truncated Gaussian priors for systematic uncertainties integrated out before this


## Limit Calculation

| CDF Run II Preliminary |  | $\int \mathcal{L}=10.0 \mathrm{fb}^{-1}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Signal |  |  | kground |
| Systematic Uncertainties (\%) |  | $Z \rightarrow \gamma \gamma$ | $Z \rightarrow \pi^{0} \gamma$ | $Z \rightarrow \pi^{0} \pi^{0}$ | Drell-Yan | Non-Resonant |
| Luminosity | 6 | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |
| $Z$ Cross Section | 6 | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |
| PDF | 5 | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |  |
| ISR/FSR | 3 | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |  |
| Energy Scale | 0.2 | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |  |
| Trigger Efficiency | 1 | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |
| $z$-Vertex | 0.2 | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |
| Photon ID Efficiency | 4 | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |  |
| $\pi^{0} / \gamma$ Efficiency | 2 per $\pi^{0}$ |  | $\checkmark$ | $\checkmark$ |  |  |
| Electron Fake Rate | 2 |  |  |  | $\checkmark$ |  |
| Sideband Fit | 2.7 |  |  |  |  | $\checkmark$ |

- Drell-Yan: also bin-by-bin statistical uncertainties
- Dominant uncertainty is that for the non-resonant background


## Limit Results

- We cannot distinguish the isolated photon from the isolated neutral pion
- We then calculate $95 \%$ C.L. limits on one at a time, assuming the other signals are not present

| CDF Run II Preliminary |  | $\int \mathcal{L}=10.0 \mathrm{fb}^{-1}$ |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Signal | Expected $\left(\times 10^{-5}\right)$ |  |  |  |  | C.L. Limits |
| Process | $-2 \sigma$ | $-1 \sigma$ | Median | $+1 \sigma$ | $+2 \sigma$ | $\left(\times 10^{-5}\right)$ |
| $\operatorname{Br}(Z \rightarrow \gamma \gamma)$ | 0.88 | 1.19 | 1.66 | 2.34 | 3.20 | 1.66 |
| $\operatorname{Br}\left(Z \rightarrow \pi^{0} \gamma\right)$ | 1.21 | 1.63 | 2.28 | 3.21 | 4.37 | 2.28 |
| $\operatorname{Br}\left(Z \rightarrow \pi^{0} \pi^{0}\right)$ | 0.93 | 1.23 | 1.72 | 2.41 | 3.29 | 1.73 |

- $\operatorname{Br}\left(\mathrm{Z} \rightarrow \pi^{0} \gamma\right)$ and $\operatorname{Br}(\mathrm{Z} \rightarrow \gamma \gamma)$ limits are more sensitive by factors of 3.1 and 2.3 over the previous limits
- The $\operatorname{Br}\left(\mathrm{Z} \rightarrow \pi^{0} \pi^{0}\right)$ limit is the first reported in this decay mode


## Limit Results



## Summary and Conclusions

- We report the most sensitive search to date for forbidden and exotic decays of the Z boson to a pair of photons, a pair of neutral mesons, or a neutral meson and a photon.
- $10 \mathrm{fb}^{-1}$ of diphoton data used in this search
- Observed 95\% C.L. upper limits are:
$-\operatorname{Br}\left(Z \rightarrow \pi^{0} \gamma\right) \quad<2.28 \times 10^{-5}$
$-\mathrm{Br}(\mathrm{Z} \rightarrow \gamma \gamma) \quad<1.66 \times 10^{-5}$
$-\operatorname{Br}\left(\mathrm{Z} \rightarrow \pi^{0} \pi^{0}\right) \quad<1.73 \times 10^{-5}$
- The $\operatorname{Br}\left(Z \rightarrow \pi^{0} \gamma\right)$ and $\operatorname{Br}(Z \rightarrow \gamma \gamma)$ limits are, respectively, 2.3 and $3.1 \times$ better than the previous limits
- The $\operatorname{Br}\left(\mathrm{Z} \rightarrow \pi^{0} \pi^{0}\right)$ limit is the first reported in this decay mode
- Future plans: consider rare Z decays involving eta mesons


## Backup

## Landau-Yang Theorem

- To construct a spin 1 Z from two spin 1 photons, the total $\mathrm{J}=1$ spin function for the Z would be constructed from antisymmetric spin functions.
- For example, the $\mid 1,1>\mathrm{Z}$ state would come from | $1,1>|1,0>-|1,0>| 1,1>$ photon states.
- Then, assuming that the photons conserve linear momentum in the rest frame of the Z , the spatial part of their wave function is symmetric, giving an overall antisymmetric wavefunction.
- Which is not allowed for a total $\mathrm{J}=1$ state, which should be symmetric.


## Summary of $\mathrm{H} \rightarrow \gamma \gamma$ Techniques

- Event Selection:
- Isolated photon trigger ( 25 GeV cut)
- Identify two 15 GeV CEM photons using central NN selection
- Signal Model:
- Shape and acceptance from Pythia MC
- Isolated photon trigger and photon ID efficiency validated in $\mathrm{Z} \rightarrow \mathrm{e}+\mathrm{e}-$ data
- Background Model:
- Exploit resonant feature of H decay into photons
- Use sideband regions of diphoton mass to determine background shape and rate in signal region

Modifications for $Z \rightarrow \gamma \gamma / \pi^{0} \gamma$ Analysis

- Event Selection:
- Isolated photon trigger
( 25 GeV cut)
- Identify two 15 GeV CEM photons using central NN selection
- Signal Model:
- Shape and acceptance from a modified (angle- or $\pi^{0}$ efficiencyweighted) Pythia MC
- Isolated photon trigger and photon ID efficiency validated in $\mathrm{Z} \rightarrow \mathrm{e}+\mathrm{e}-$ data
- Background Model:
- Exploit resonant feature of Z decay into photons
- Use sideband regions of diphoton mass to determine background shape and rate in signal region
- Model Z $\rightarrow$ e+e- from Pythia MC


## Photon Identification

- EM calorimeter segmentation:
- $\Delta \eta \times \Delta \varphi \sim 0.1 \times 15^{\circ}(|\eta|<1)$
- Not fine enough to distinguish $\pi^{0} / \eta$ and photon showers
- Shower max detector
- $\sim 6$ radiation lengths into EM calorimeter
- Finely segmented: Position resolution $\sim 1 \mathrm{~mm}$
- Gives resolution to better distinguish $\pi^{0} \eta \rightarrow \gamma \gamma$ from $\gamma$ at low Et
- For $\pi^{0}$ with sufficiently high Et, collinear photons like single $\gamma$


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## Photon ID Efficiency Scale Factors

- Photon ID efficiency calibrated with $\mathrm{Z} \rightarrow \mathrm{e}+\mathrm{e}-$
- Data (MC) efficiency indicated with points (lines)



## Central p18-p23 Data Efficiencies



## Revisiting the Z polarization from Drell-Yan

We considered all polarization states. In the limiting case (where the collision is of head-on (massless) quarks) only the two states here would be considered:


In this limit $\mathrm{f}_{0}=0$, and then the angular distributions in the Z rest frame for $\mathrm{Z} \rightarrow \mathrm{vv}$ and $Z \rightarrow \gamma \gamma$ events becomes

$$
\begin{aligned}
& F_{v \bar{v}}(\theta)=f_{+}\left(d_{1,1}^{1}\right)^{2}+f_{-}\left(d_{1,-1}^{1}\right)^{2}=f_{+}\left(1+\cos ^{2} \theta\right) \\
& F_{r \gamma}(\theta)=f_{+}\left(d_{1,0}^{1}\right)^{2}+f_{-}\left(d_{1,0}^{1}\right)^{2}=f_{+}\left(1-\cos ^{2} \theta\right)
\end{aligned}
$$

The corresponding weight function would then be:

$$
w_{r \gamma}(\theta)=\frac{F_{v \bar{v}}(\theta)}{F_{\gamma \gamma}(\theta)}=\frac{1-\cos ^{2} \theta}{1+\cos ^{2} \theta}
$$


[^0]:    * CDF has already performed a search for $W \rightarrow \pi^{ \pm} \gamma$ using $4.3 \mathrm{fb}^{-1}$ of data and improved the LEP branching ratio upper limit by a factor of 10.. Phys. Rev. D 85, 032001 (2012)

