



Issues in Accelerator-Driven Systems

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source: Government Energy Support Unit (confirmed by OECD)

	Grammes of
Energy source	carbon
Lifergy source	per KWh of
	electricity
Nuclear	4
Wind	8
Hydro electric	8
Energy crops	17
Geothermal	79
Solar	133
Gas	430
Diesel	772
Oil	828
Coal	955









500x less land area than windmills





Leó Szilárd, Ernest Rutherford and the Chain Reaction

- In a Times article on March 6th 1933, Ernest Rutherford asserted:
 - 'The energy produced by the atom is a very poor kind of thing. Anyone who expects a source of power from the transformation of these atoms is talking moonshine'
- Leó Szilárd was apparently annoyed by this, and conceived of the nuclear chain reaction while waiting for traffic lights to changed in Bloomsbury, London, in 1933!







A Little History...

- 1932 Chadwick discovers neutron
- 1932 Lawrence invents cyclotron (or was it Szilard?)
- The University of Manchester 1933 – Rutherford article/Szilard conceives chain reaction
 - 1933 Curie and Joliot produce first artificial radioactivity ٠
 - 1937 Segre discovers first artificially-created element Technetium ٠
 - 1941 Glenn Seaborg makes 239Pu using d on 238U (ugm) ٠
 - 1942 Chicago Pile 1 (criticality) ٠
 - 1945 Trinity Test, Oppenheimer et al. ٠
 - 1949 Goeckermann and Perlman carry out high energy spallation (high ۲ multiplicity)
 - 1950 Lawrence 'Material Testing Accelerator' project approved ٠
 - 1951 EBR-1 (Idaho) first electricity ۲
 - 1952 W B Lewis proposes accelerator breeding of 233U ٠
 - 1956 Calder Hall first nuclear power plant (PIPPA) ۲
 - 1957 Shippingport first commercial plant & LWR & Th breeding ٠





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LWRs: PWRs and BWRs







Boiling Water Reactor



Total available

200





	man hannon hay			
Action	Energy (MeV)	Isotope	${f v}$ Thermal	ν Fast
FPs	168	235U	2.44	2.50
Fission n	5	239Pu	2 87	3 02
Prompt gamma	7	2001 0	2.07	5.02
Decay beta	8	233U	2.48	2.55
Decay gamma	7			
Neutrinos	12			
Capture gamma	5			







Fissile Fuel

Moderator

Coolant

Control

As fissile atoms consumed, fission products and actinides are produced. Other materials (burnable poisons) may also be consumed.



Comparison of Moderators and Coolants

- LWR
 - Abundant
 - Liquid at RTP
 - Transparent
 - High Pressure required at working T (370K)
 - Requires Enriched Fuel
- HWR
 - v. Low absorption can use natU
 - Transparent
 - Abundant, but v. expensive
 - High pressure required

- AGR
 - No phase changes
 - Very high temperatures possible
 - Future limit in He supply?
- SFR
 - Low melting temperature
 - Atmospheric pressure (pool-type)
 - Reasonable experience
 - Flammable with water/air
- LFR
 - Transparent to neutrons: fast spectrum
 - Atmospheric pressure (pool-type)
 - PbBi gives lower temp, but 210Po production



Figure 1 Neutron Life Cycle with $k_{eff} = 1$





Breeding New Fuel

$$B = \eta_f - 1 - (C + L)$$

Isotope	Thermal	Fast
235U	2.08	2.09
239Pu	2.12	2.53
233U	2.28	2.35

has to be bigger than ~2.2







Reactor Control

$$\rho = \frac{1 - k_{eff}}{k_{eff}}$$

$$k_{eff} = \frac{1}{1-\rho} \simeq 1+\rho$$

 $\tau_{\rm n}$ Thermal reactor: 10⁻⁴ s Fast reactor: 10⁻⁷ s

$N_0 \to (1+\rho)^n N_0$

$$n(t) = n_0 \exp(\frac{\rho t}{\tau_n})$$
$$W(t) = W_0 \exp(\frac{\rho t}{\tau_n})$$

Delayed neutrons fix everything!

	eta	$T_d(\text{sec.})$	$ au_d(\mathrm{sec.})$	N/A
^{232}Th	0.0203	6.98	0.141	0.612
^{233}U	0.0026	12.40	0.032	0.605
^{235}U	0.00640	8.82	0.056	0.608
^{238}U	0.0148	5.32	0.079	0.613
^{239}Pu	0.002	7.81	0.020	0.607
^{241}Pu	0.0054	10^{9}	0.054	0.609
^{241}Am	0.0013	10	0.013	0.606
^{243}Am	0.0024	10	0.024	0.609
^{242}Cm	0.0004	10	0.004	0.603





$$\frac{93}{36} \operatorname{Kr} \frac{1.3 \text{ sec}}{\beta^{-}} > \frac{93}{37} \operatorname{Rb} \frac{6 \text{ sec}}{\beta^{-}} > \frac{93}{38} \operatorname{Sr} \frac{7.5 \text{ min}}{\beta^{-}} > \frac{93}{39} \operatorname{Y} \frac{10 \text{ hr}}{\beta^{-}} > \frac{93}{40} \operatorname{Zr} \frac{1.5 \times 10^{6} \text{ yr}}{\gamma^{-}} > \frac{93 \text{ mNb}}{41} \xrightarrow{41} 13 \text{ yr}}{\gamma^{-}}$$

$$\frac{141}{\beta^{-}} \operatorname{Xe} \frac{1.7 \text{ sec}}{\beta^{-}} > \frac{141}{55} \operatorname{Cs} \frac{25 \text{ sec}}{\beta^{-}} > \frac{141}{56} \operatorname{Ba} \frac{18 \text{ min}}{\beta^{-}} > \frac{141}{57} \operatorname{La} \frac{3.9 \text{ hr}}{\beta^{-}} > \frac{141}{58} \operatorname{Ce} \frac{32.5 \text{ d}}{\beta^{-}} > \frac{141}{59} \operatorname{Pr} (\text{stable})$$

But also need either control rod movement, or negative coefficients of reactivity





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PWR Fissile, MA and FP Inventories

Inventories at loading and discharge of a 1 GWe PWR [19]			
Nuclides	Initial load (kg)	Discharge inventory (kg)	
²³⁵ U	954.0	280.0	
²³⁶ U		111.0	
²³⁸ U	26328.0	25655.0	
U total	27 282.0	26047.0	
²³⁹ Pu		56.0	
Pu total		266.0	
Minor actinides		20.0	
⁹⁰ Sr		13.0	
¹³⁷ Cs		30.0	
Long-lived PF		63.0	
PF total		946.0	
Total mass	27 282.0	27 279.0	

- 4.5% of world energy is nuclear
 - 350 Gwe
 - ~440 reactors
 - Most PWR or BWR
- Yearly rates:
- Spent fuel: 8,000 t
- Each 1 GWe reactor:
 - 80,000t U ore (cf. 2M toe)
 - 200t natU
- Yucca Mountain capacity: 70,000 t

Long-lived fi	ssion fragme	nts with their	r half-lives and	production rates	

Nuclide	⁷⁹ Se	⁹⁰ Zr	⁹⁹ Tc	¹⁰⁷ Pd	¹²⁶ Sn	¹²⁹ I	¹³⁵ Cs
$T_{1/2}$ years	70000	$1.5 imes10^6$	$2.1 imes 10^5$	$6.5 imes10^6$	10 ⁵	1.57×10^7	$2 imes 10^6$
Production kg/yr	0.11	15.5	17.7	4.4	0.44	3.9	7.7





U/Pu Cycle and Waste







The Motivation for Transmutation







'Energy Amplifier' (Rubbia)









Rubbia et al., CERN/AT/93-47 (ET), CERN/AT/95-44 (ET) Phys Rev C73, 054610 (2006) also MSR option: C.D.Bowman, NIM A320, 336 (1992)





ADSR as an 'Energy Amplifier'



Reactor part costs about ~2-3 billion to construct Fuel is 'sort-of' free



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MYRRHA - Accelerator Driven System

Accelerator (600 MeV - 4 mA proton) Reactor
Subcritical and Critical modes
65 to 100 MW_{th}

SC Linac 57 MWth reactor Pb-Bi eutectic target/coolant Fuel (MOX) loading from underneath Examine transmutation of waste

Useful proton source in its own right Replaces BR2 isotope reactor

Pb-Bi coolant



http://myrrha.sckcen.be/



MYRRHA Core Layout

k_{eff}≈0.95

183 hexagonal macro-cells

Target-block hole :

3 FA removed

72 positions for fuel assemblies

- (8 IPS positions included)
- > ≈30 % MOX fuel

27 positions for fuel assies or dummy assies (filled with LBE) (yellow)

84 additional cells for core reconfiguration







Neutron multiplication in a sub-critical system

 In an accelerator driven, sub-critical system the "primary" (or "source") neutrons produced via spallation initiate a cascade process. The « source » neutrons are multiplied by fissions and (n,xn) reactions through the multiplication factor M :

$$M = 1 + k + k^{2} + k^{3} + \dots + k^{n} = \frac{k^{n+1} - 1}{k-1} \xrightarrow{n \to \infty} \frac{1}{1-k} \quad \text{for } k < 1$$

• If we assume that all generations in the cascade are equivalent, we can define an average criticality factor k (ratio between the neutron population in two subsequent generations), such that :

$$k = \frac{M - 1}{M} = 1 - \frac{1}{M} < 1$$

 This k ≠ k_{eff}. k_{src} is the value of k calculated from the net multiplication factor M in the presence of an external source.

$$k_{src} = \frac{M-1}{M}$$



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Proton beam requirements for EA/ADSR

The (thermal) power output of an ADSR is given by

$$P_{\text{th}} = \frac{N \times E_{\text{f}}}{v} \cdot \frac{k_{\text{eff}}}{1 - k_{\text{eff}}}$$

with N = number of spallation neutrons/sec E_f = energy released/fission (~200MeV) v = mean number of neutrons released per fission (~2.4) k_{eff} = criticality factor (<1 for ADSR)

So, for a thermal power of 1550MW we require

$$N = 9.6 \times 10^{19} \times \frac{1 - k_{eff}}{k_{eff}} \quad neutrons.s^{-1}$$

Given that a 1 GeV proton produces, say, 24 neutrons (in a lead target) this corresponds to a proton current of

$$I = \frac{9.6 \times 10^{19}}{24} \times 1.6 \times 10^{-19} \times \frac{1 - k_{eff}}{k_{eff}} \quad Amps = 640 \times \frac{1 - k_{eff}}{k_{eff}} \quad mA$$





Proton Beam Requirements



k_{eff}=0.95, i=33.7mA k_{eff}=0.98, i=13.1mA k_{eff}=0.99, i=6.5mA

To meet a constraint of a 10MW proton accelerator we need k_{eff} =0.985













• EAs operate in a non self-sustained chain reaction mode

minimises criticality and power excursions

 ② EAs are operated in a sub-critical mode
 ⇒ stays sub-critical whether accelerator is on or off
 ⇒ extra level of safety against criticality accidents

 The accelerator provides a control mechanism for sub-critical systems

- ⇒ more convenient than control rods in critical reactor
- ⇒ safety concerns, neutron economy

 EAs provide a decoupling of the neutron source (spallation source) from the fissile fuel (fission neutrons)

• EAs accept fuels that would not be acceptable in critical reactors

- ⇒ Minor Actinides
- ⇒ High Pu content
- \Rightarrow LLFF...





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There is a spectacular difference between a critical reactor and an EA (reactivity in $\$ = \rho/\beta; \rho = (k-1)/k):$

- Figure extracted from C. Rubbia et al., CERN/AT/ 95-53 9 (ET) showing the effect of a rapid reactivity insertion in the Energy Amplifier for two values of subcriticality (0.98 and 0.96), compared with a Fast Breeder Critical Reactor.
- 2.5 \$ (Δk/k ~ 6.5×10⁻³) of reactivity change corresponds to the sudden extraction of all control rods from the reactor.





The Thorium Fuel Cycle



Advantages

Thorium supplies plentiful

Robust fuel and waste form

Generates no Pu and fewer higher actinides

²³³U has superior fissile properties

Proliferation resistant



Disadvantages

No fission until ²³³U is produced

²³³U is weapon grade unless denatured

Parasitic ²³²U production results in high gamma activity

Thorex processing of waste needs substantial development

It is generally considered that the neutrons necessary to produce ²³³U from ²³²Th must be introduced by seeding the Th fuel with ²³⁵U or Pu

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Benefits of the Thorium ADS Reactor



"No plutonium is bred in the reactor" COSMOS magazine , "New age nuclear" Issue 8, April 2006

"(Th, Pu)O₂ fuel is more attractive, as compared to (U, Pu)O₂, since plutonium is not bred in the former" IAEA-TECDOC-1450 "Thorium fuel cycle- Potential benefits and challenges", 2005.

"The advantages of the thorium fuel cycle are that it does not produce plutonium" Thorenco LLC website

"Examination of claimed advantages, (a) Producing no plutonium, This is true of the pure thorium cycle" IAEA-TECDOC-1319, "Potential advantages and drawbacks of the Thorium fuel cycle in relation to current practice: a BNFL view" 2002.

"The fuel cycle can also be proliferation resistant, stopping a reactor from producing nuclear weapons-usable plutonium" Power Technology website



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Breeding and Reactor Types



Incident neutron energy





Advantages

²³³U has superior fissile properties

Robust fuel and waste form

Generates no Pu and fewer higher actinides

Proliferation resistant

Disadvantages

Requires introduction of fissile seed (²³⁵U or Pu)

²³³U is weapon grade unless denatured

Parasitic ²³²U production results in high gamma activity.

Thorex processing of waste needs substantial development



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Stable

28.78 y

64.1 h



1.92 s

32.32 s

2.63 mn





Variations in Fission Cross-sections





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Justification for ADS (from E. Gonzalez)

- Efficient
- High (fast) neutron flux
- transmutation High burnup
 - High Pu+MA and low U content \Rightarrow Subcritical
- \Rightarrow Nuclear (Fast) Reactor
- \Rightarrow Flexible

ADS

The most efficient transmutation would be a reactor of significant power (nx100 or 1000 MW), of fast neutron spectrum, with a fuel with very low Uranium content and high concentration of Pu and MA.

A reactor with these characteristics shows an important lack of intrinsic safety:

Low delay neutron fraction Small Doppler effect Bad void coefficient

In addition the reactor needs a large operation flexibility, to be able to handle:

Very high burn-up levels in each irradiation cycle Large reactivity evolution within one irradiation cycle

Very difficult for critical reactors and strong limitation on their transuranium elements load.

Two types of solutions:

A large number of fast reactors with small regions dedicated to transmutation (countries with large park of nuclear power plants)

A small number of subcritical accelerator driven systems, ADS, dedicated to transmutation.











The Lead-Cooled ADS

Subcritical system driven by a proton accelerator:

Fast neutrons (to fission all transuranic elements)

 Fuel cycle based on thorium (minimisation of nuclear waste)

 Lead as target to produce neutrons through spallation, as neutron moderator and as heat carrier

 Deterministic safety with passive safety elements (protection against core melt down and beam window failure)







Resonant Neutron Capture







Resonant Neutron Capture

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Medium lived elements

$_{55}^{137}Cs (\tau = 30.1 y) + n \implies$	$_{55}^{138}Cs \xrightarrow{\beta^{-}(33.2 m)} \sim _{56}^{138}Ba (stable)$
$^{134}_{55}Cs (\tau = 2.06 \text{ y}) + n \Rightarrow$	$^{135}_{55}Cs\ (\tau = 2.6 \times 10^6 y)$
$^{90}_{38}Sr(\tau = 29.1 y) + n \Rightarrow$	$\frac{91}{38}$ Sr $\frac{\beta^{-}(6.63 h)}{29}$ $\stackrel{91}{\succ}$ $\frac{\gamma^{-}(58.51 d)}{40}$ $\stackrel{91}{\sim}$ Zr (stable)
$^{90}_{39}$ Y ($\tau = 64.1 h$) + n \Rightarrow	$\frac{91}{39}Y \xrightarrow{\beta^{-}(58.51 \text{ d})} \frac{91}{40} Zr \text{ (stable)}$

Long lived elements





" An ADS drives nuclear reactions that will stop if the proton beam from the accelerator stops" Nuclearinfo.net

"If the particle beam is switched off, it is impossible for the fuel to enter a chain reaction and cause a meltdown. Instead, the rate of fission will immediately begin to slow and the fuel will eventually cool down and die out" "

COSMOS magazine



Courtesy of David Coates, Cambridge



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ADS operating modes to compensate for reactivity variations:

- Use rods to continually flatten the reactivity variations and maintain fixed k_{eff}
- Use fixed rods to set maximum k_{eff} and use the accelerator to compensate for reactivity movements

Note: The bare reactor is critical and requires rods to achieve sub-critical operation







Critical and ADS Shut-down

Critical – Control Rod Insertion

1)Has an inherent reduction in the reactivity of the system as a direct consequence of the action2)Intrusive – requires a clear path

ADS-Accelerator Trip

- 1) No associated inherent reduction in the reactivity of the system
- 2) Non intrusive
- 3) The system must be sub-critical for this to work

The ADS trip requires the reactor to be sub-critical and remain sub-critical to be effective

Courtesy of David Coates, Cambridge

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Thorium Reactor – Post Shutdown Power Increase







ersi



MYRRHA: EXPERIMENTAL ACCELERATOR DRIVEN SYSTEM A pan-European, innovative and unique facility







MYRRHA: Integration into building









MYRRHA Proton Driver





Proton Driver Alternatives



- Cyclotron
 - Energy limited in classical cyclotron
 - Power perhaps achievable, but difficult
 - Reliability not good enough
- Linac
 - Can meet power requirements (e.g. 2x ESS)
 - May be reliable enough (loss of module okay)
 - But too expensive for commercial use

(JAEA and MYRRHA demonstrators propose linac)

- Synchrotron
 - Can't yet achieve currents (RCS?)
 - More complicated (ramping magnets), therefore reliability probably low
- FFAG
 - Can deliver currents in principle
 - Still quite large
 - Simpler than synchrotron
 - First proton FFAGs only built recently at KEK





High-Power Cyclotron Options

Accelerated Species	Advantages	Disadvantages
H+	Simpler ion source	Poor extraction efficiency Auto-extraction limited to 85%?
H-	Stripping extraction	Lorentz stripping Gas stripping
		Lorentz stripping Gas stripping
H2+	Stripping extraction	Complex extraction path

Favoured option: H2+ Calabretta et al., INFN-Catania arxiv:1107.0652

Rext	4.9m
ext	1.88T
Bmax	< 6.3 T
V	0.5-1 MV/turn
dE	3.6 MeV/turn





MEGAPIE (SINQ Facility, PSI)



Ran successfully for 4 months in 2006

700 kW, CW, liquid Pb-Bi First Pb-Bi spallation target

	Megapie	XT-ADS target
Coolant / target	liquid Pb-Bi	liquid Pb-Bi
Beam energy	595 MeV	600 MeV
Beam current	1.4 mA max	3 mA
Lifetime	4 months	9 months
Accumulated charge	2.8Ah	20Ah
Target diameter	Ø20 cm	Ø10 cm
Accumulated charge / m ²	90 Ah/m²	2500 Ah/m²
Beam interface	window	windowless





ADTR

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- 1st demonstration of ADSR
- Reactor kinetic studies (load-following)
- Source-jerk k_{eff} measurement (ADTR concept)
- Fuel irradiation measurements





Thermal Power (P _{th})	1500 MW th	
Electric Power (Pel)	600 MW _{el}	
Fuel	ThO ₂ /PuO ₂	
	84.5%/15.5% (first cycle)	
Total fuel mass	59 tonne	
Target fuel dwell time	8 - 10 years	
Neutron multiplication	0.995	
coefficient (k _{eff})		
Power density p	55 W/g oxide	
Energetic Gain G	402 to 532	
Coolant	natural lead	
Spallation target	natural lead	
Coolant temperature at	400°C	
core inlet		
Coolant temperature at	540°C	
core outlet		
Four off single loop lo	ead to water/steam heat	
exchangers rated at 375 MW	/ per unit	
Water temperature (feed to	340°C	
system steam generators)		
Steam temperature	450°C	
Steam pressure	183 bara	
Coolant pumps	4 off axial flow	
Sub-critical configuration, accelerator driven		



Proliferation



- Operation Teapot
 - 233U test
 - So you can make a bomb from it
- IAEA enrichment limit is somewhere around 12%
 - Depends on the amount of 235U
- Can be protected by denaturing with 238U
 - (requires enrichment, i.e. won't be done)





of



$$\xrightarrow{n, \gamma} {}^{231}$$
Th $\xrightarrow{\beta^-} {}^{231}$ Pa $\xrightarrow{n, \gamma} {}^{232}$ Pa $\xrightarrow{\beta^-} {}^{232}$ U

ASPECT	DIFFERENCE VS. URANIUM
FRONT END	
Mining	 (a). Thorium is perhaps 3 times more abundant but much less is mined. Best resources are monazite sands in India and Brazil. (b). Because uranium is really mined for its U-235, a once
	-through cycle needs only about 1/10 th as much Thorium.
	(c). U-free Th preferred because of absence of Th-230.
	(d). Tailings less of a problem because Rn-220 has a much shorter half-life than Rn-222.
Enrichment	 (a). Must provide as U-235 or Plutonium (could be from dismantling weapons). (b). Recycled U-233 contains <u>U-232</u>, U-234.
Fabrication	(a). Typically as ThO ₂ using processes similar to UO_2 and PuO_2 (which are incorporated to provide fissile enrichment).
BACK END	
Storage and Transportation	 (a). Pa-233 decay (T 1/2 ~ 27 days) creates more U-233 over first several months. (b). Similar fission product decay heat and gamma emission.
Direct Disposal	(a). ThO ₂ is stable in oxidizing environment (unlike UO ₂ which forms U_3O_8). (b). Factor ~ 10 lower concentration of radiotoxic higher actinides
Reprocessing	(a). Solvent extraction (THOREX) similar to PUREX but same equipment has about half the processing rate, hence $\sim 30\%$ more expensive.
Refabrication	 (a). Need to shield against hard gammas from U-232 decay chain (Bi-212, Tl-208), hence more expensive even than recycled U or Pu. (b). Preferable to delay recycle of Th for ~ 15 years to decay Th-228; one year suffices for Th-234.
Safeguards	 (a). Must denature to ≤ 12% U-233 in U-238. (b). U-232 chain gammas complicate handling.







Key Papers and Books

- Michael Dittmar, 'The Future of Nuclear Energy' Vols 1-4, arXiv (2009)
- R. R. Wilson, 'Very Big Accelerators as Energy Producers', FERMILAB-FN-0298
- Nifenecker et al.: 'Hybrid Nuclear Reactors' Progress in Particle and Nuclear Physics 43 (1999) 683-827
- Nifenecker et al.: 'Basics of accelerator driven subcritical reactors' Nuclear Instruments and Methods in Physics Research A 463 (2001) 428– 467
- IAEA-TECDOC-985 ' Accelerator Driven Systems: Energy Generation and Transmutation of Nuclear Waste'
- Leipunskii et al., 'Development of Nuclear Power with Fast-Neutron Reactors in the USSR', Atomnaya Energiya, 25 (1968), 380-387
- Rubbia et al., CERN/AT/94-47 & CERN/AT/95-44, Phys Rev C73, 054610 (2006)
- S. Andriamonje et al. Physics Letters B 348 (1995) 697–709,
- J. Calero et al. Nuclear Instruments and Methods A 376 (1996) 89–103;