

EDMs as Probes of Macroscopic Spin-Dependent Forces

Sonny Mantry

Northwestern University and Argonne National Lab

Collaborators: Mario Pitschmann, Michael J. Ramsey-Musolf

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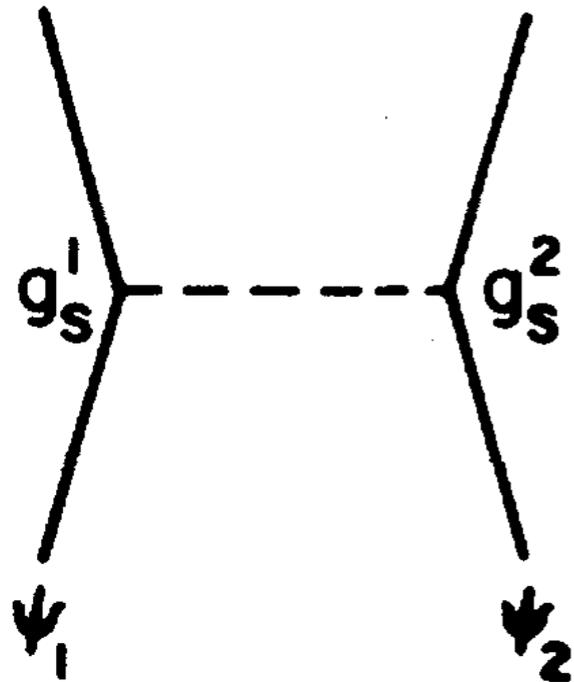
Oct. 8th, 2013

Outline

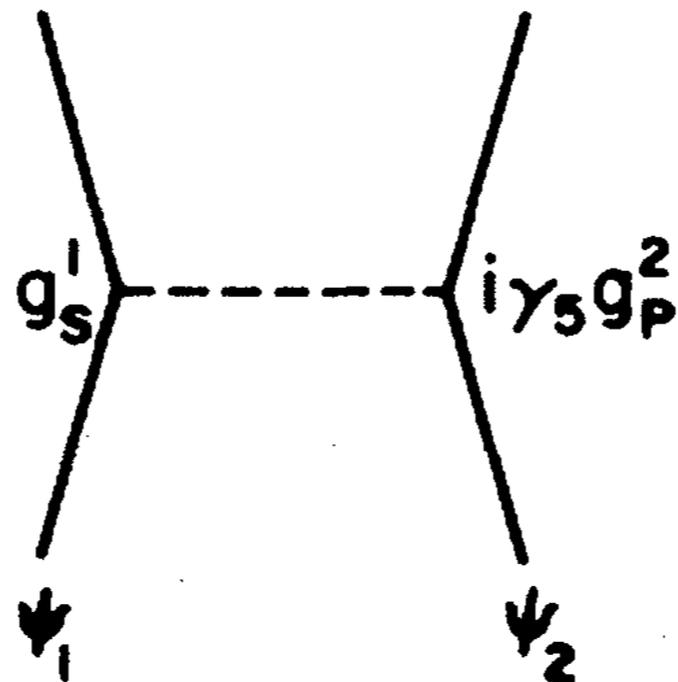
- Short range spin-dependent forces.
- EDMs in the SM.
- Axions: EDMs and short range forces
- Generic scalars: EDMs and short range forces
- Conclusion

Short Range Macroscopic Scalar Forces

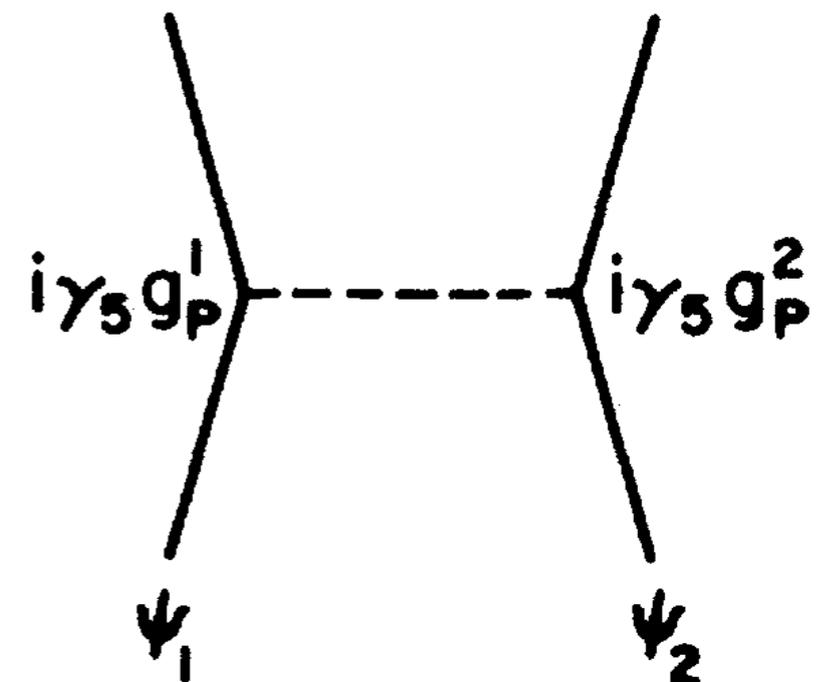
(Moody, Wilczek)



Monopole-Monopole



Monopole-Dipole



Dipole-Dipole

- New short range macroscopic forces beyond the SM?

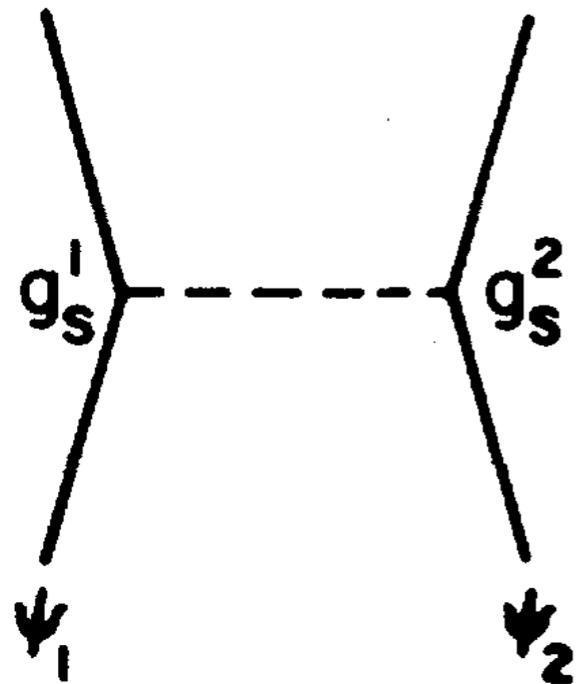
$$m_\varphi \lesssim 10^{-2} \text{ eV} \quad \longrightarrow \quad \lambda \gtrsim 2 \times 10^{-5} \text{ m}$$

$$m_\varphi \gtrsim 10^{-6} \text{ eV} \quad \longrightarrow \quad \lambda \lesssim 2 \times 10^{-1} \text{ m}$$

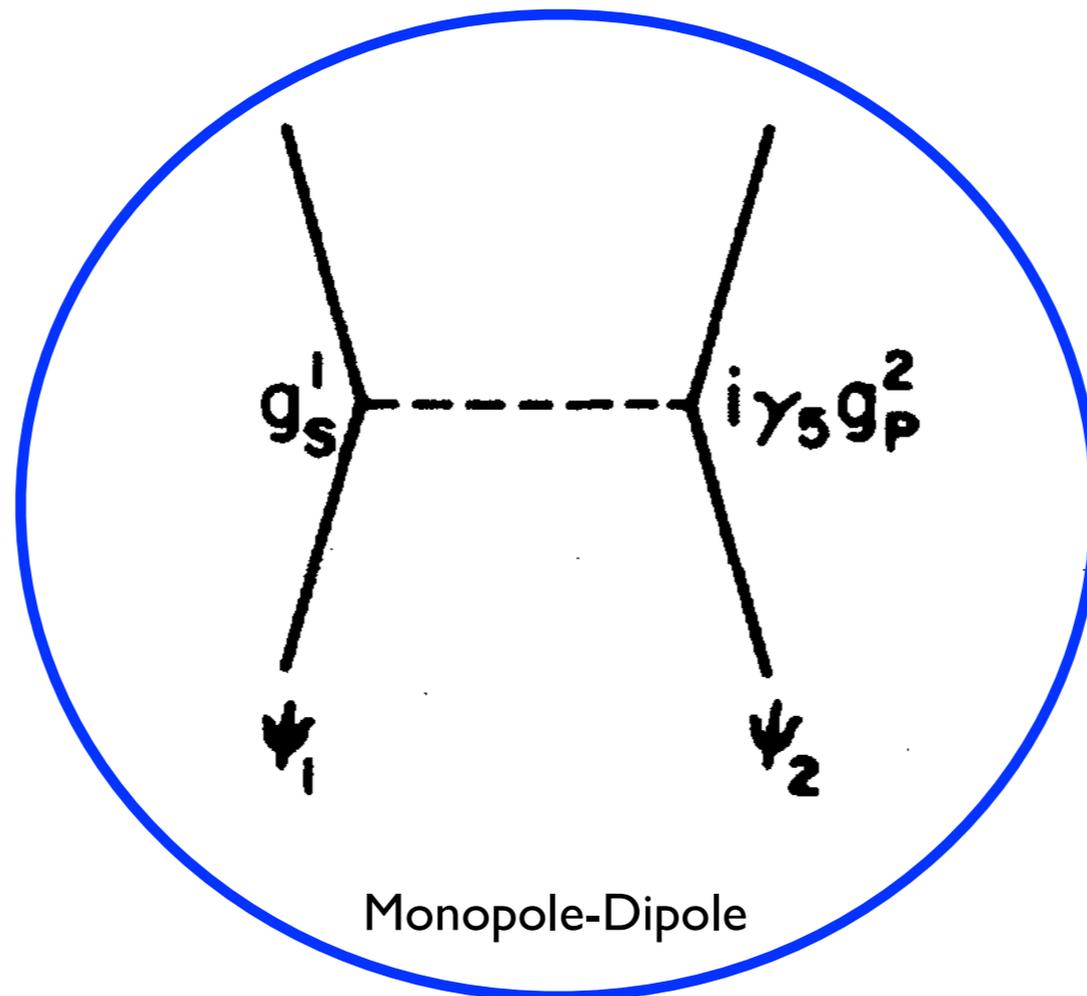
- How can we search for such forces?
- Can they be correlated with CP violation and EDM constraints?

Short Range Macroscopic Scalar Forces

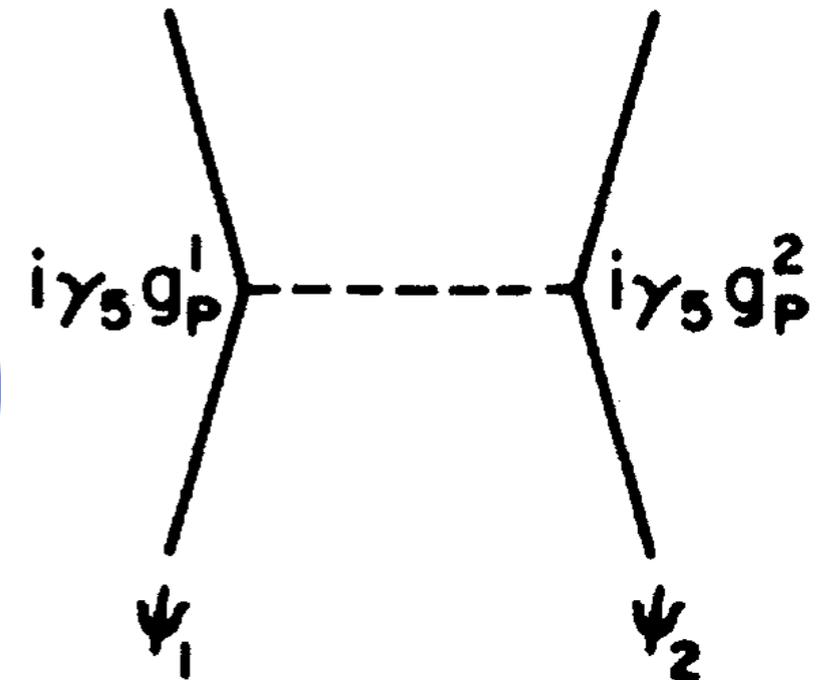
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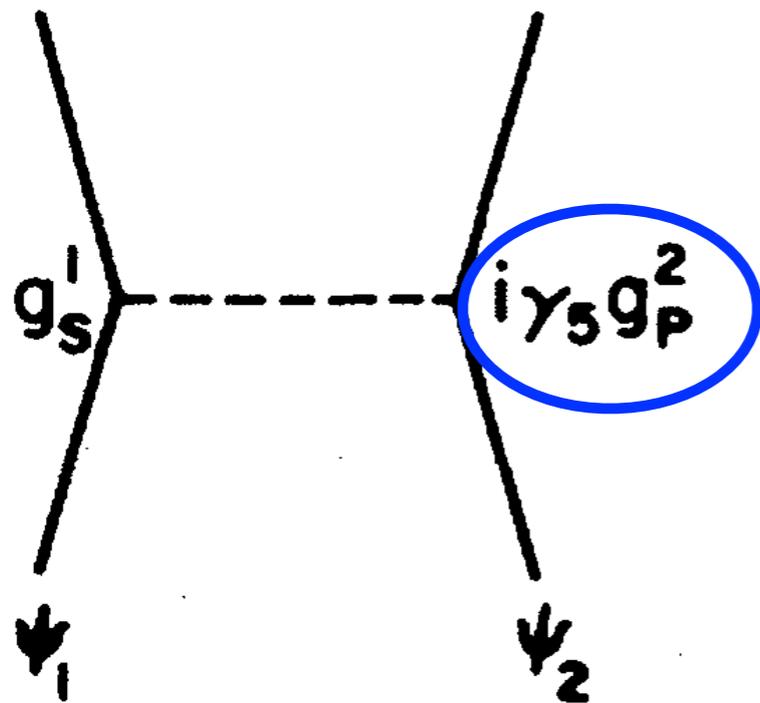
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- How can we search for such forces?

- Can they be correlated with CP violation and EDM constraints?

Spin-Dependent Macroscopic Scalar Forces

(Moody, Wilczek)



Monopole-Dipole

→ CP violating coupling

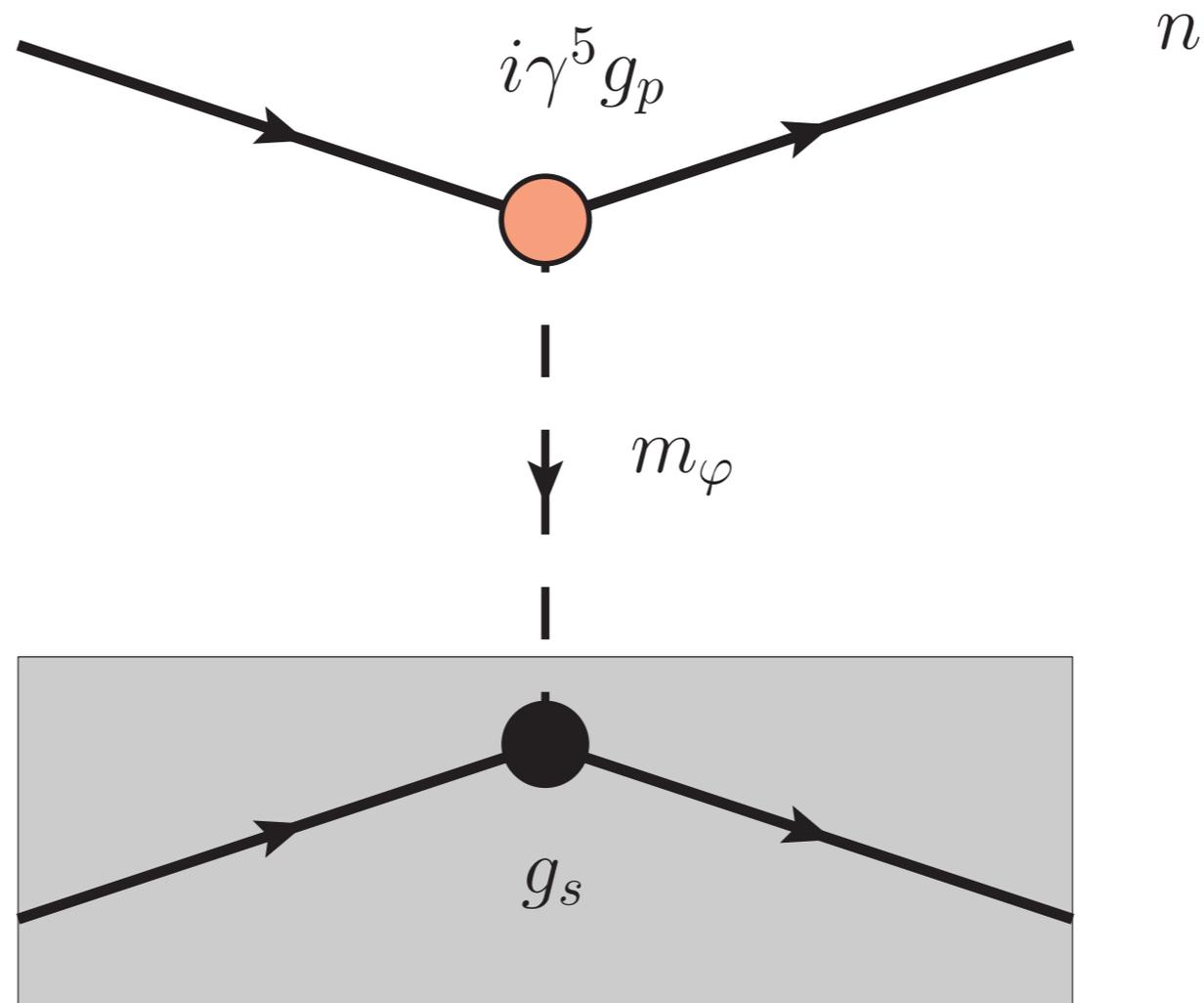
$$\mathcal{L}_{\varphi NN} = g_s \varphi \bar{N} N + g_p \varphi \bar{N} i\gamma_5 N$$

$$V(r) = g_s^1 g_p^2 \frac{\vec{\sigma}_2 \cdot \hat{r}}{8\pi M_2} \left[\frac{m_\varphi}{r} + \frac{1}{r^2} \right] e^{-m_\varphi r}$$

- CP violating coupling can induce non-zero EDMs.
- Fifth-force and EDM experiments can then be complementary probes of such phenomena.

Fifth-Force Experiments

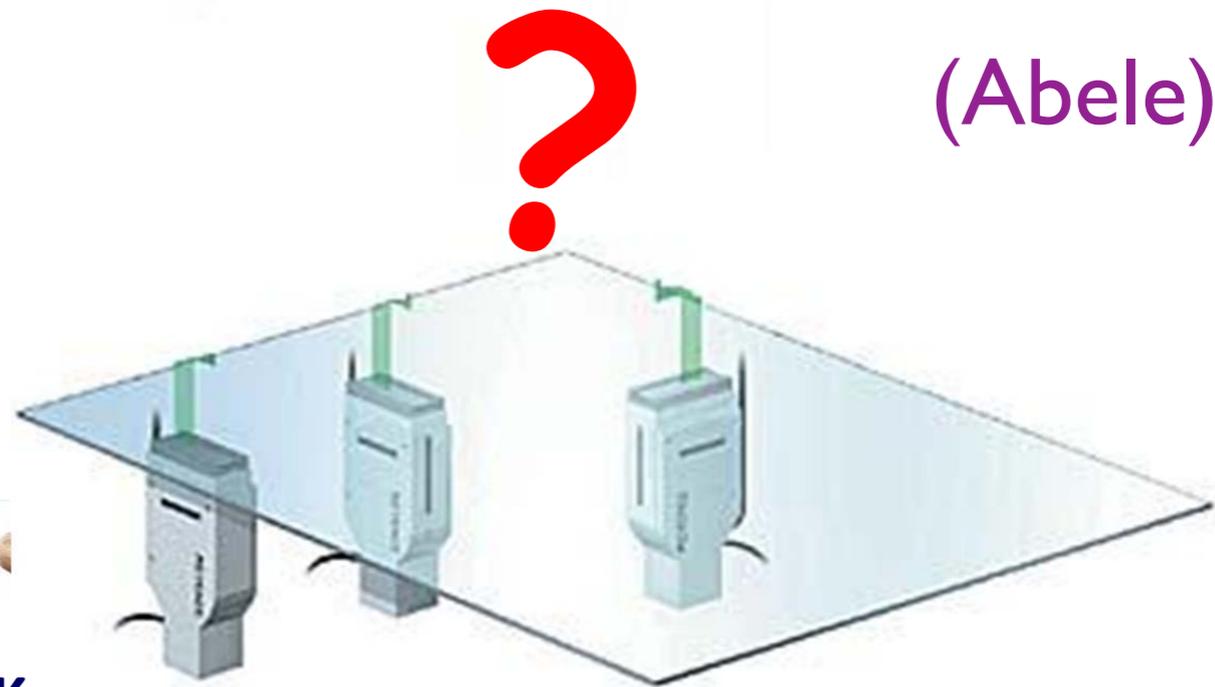
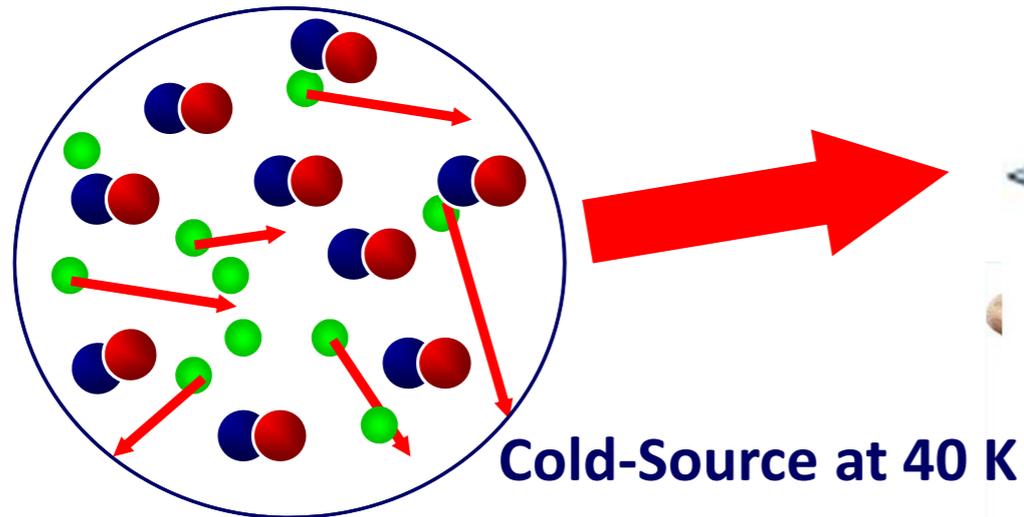
Neutron Q-bounce Experiment



$$V(r) = g_s^1 g_p^2 \frac{\vec{\sigma}_2 \cdot \hat{r}}{8\pi M_2} \left[\frac{m_\phi}{r} + \frac{1}{r^2} \right] e^{-m_\phi r}$$

Quantum Bounce

(Abele)



● System Neutron & Earth

- Neutron bound in the gravity potential of the earth
- $\langle r \rangle = 6 \mu\text{m}$
- Ground state energy of 1.4 peV
- 1 dim.
- Schrödinger Equ.
 - Airy Functions

● Hydrogen Atom

- Electron bound in proton potential
- Bohr radius $\langle r \rangle = 1 \text{ \AA}$
- Ground state energy of 13 eV
- 3 dim.
- Schrödinger Equ.
 - Legendre Polynomials

Neutron Q-bounce Experiment (Abele)

Schrödinger equation:

$$\left(-\frac{\hbar^2}{2m} \frac{\partial^2}{\partial z^2} + mgz \right) \varphi_n(z) = E_n \varphi_n(z)$$

boundary conditions:

$$\varphi_n(0) = 0$$

with 2nd mirror at height l

$$\varphi_n(l) = 0$$

solutions: Airy-functions

scales:

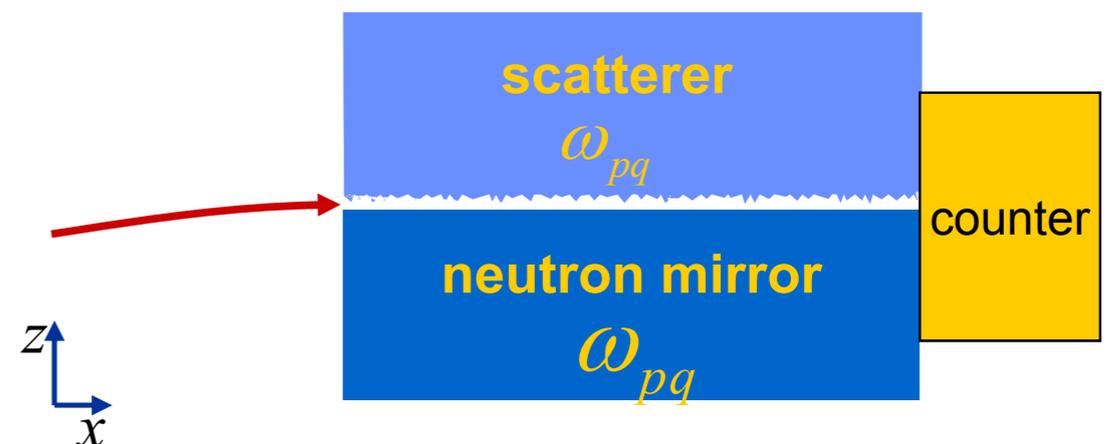
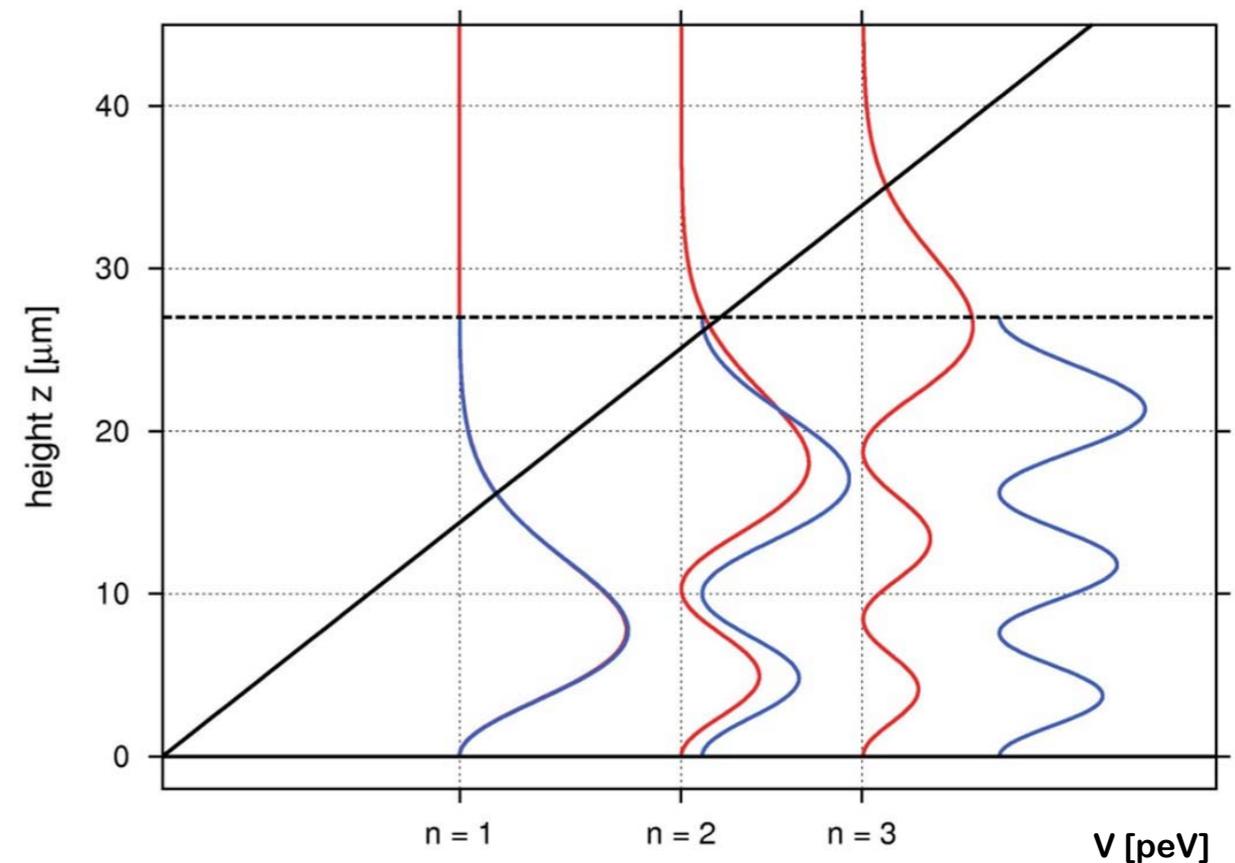
energies: peV
length: μm

neutron mirror

Demonstration of Quantum States
in the Gravity Potential of the Earth

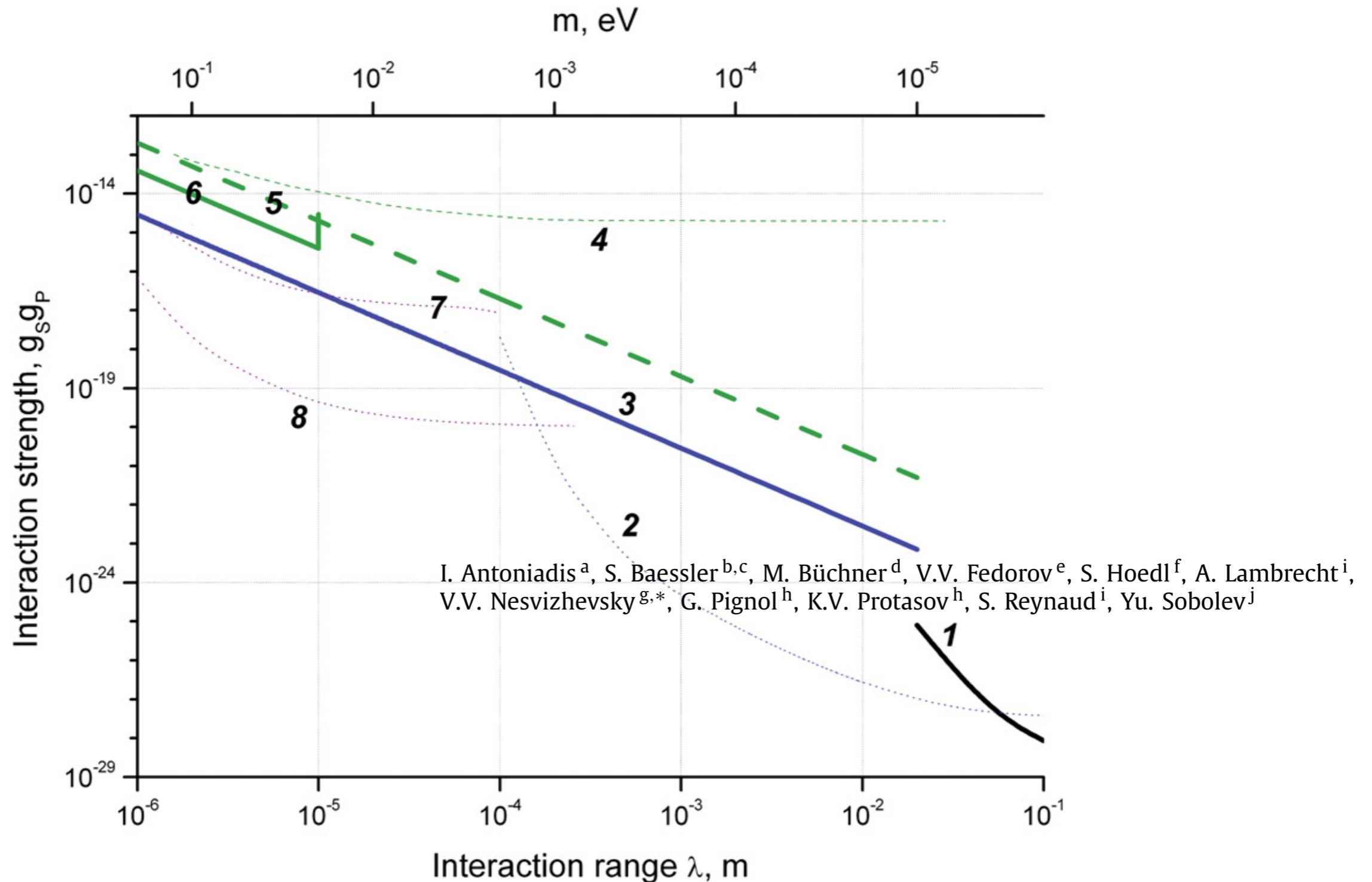
Nesvizhevsky, H.A. et al.
Nature 2002

	E_n	E_n
1st state	1.41peV	1.41peV
2nd state	2.46peV	2.56peV
3rd state	3.32peV	3.97peV



Bounds on Spin-Dependent Fifth Forces

- Summary of bounds from various fifth-force experiments



Electric Dipole Moments

EDMs

- Non-zero EDM arises from term of the form

$$\mathcal{L} = -d \frac{i}{2} \bar{\psi} \sigma^{\mu\nu} \gamma_5 \psi F_{\mu\nu}$$

- In the non-relativistic limit, the EDM interaction with an external field is given by

$$H = -d \vec{E} \cdot \frac{\vec{S}}{S}$$

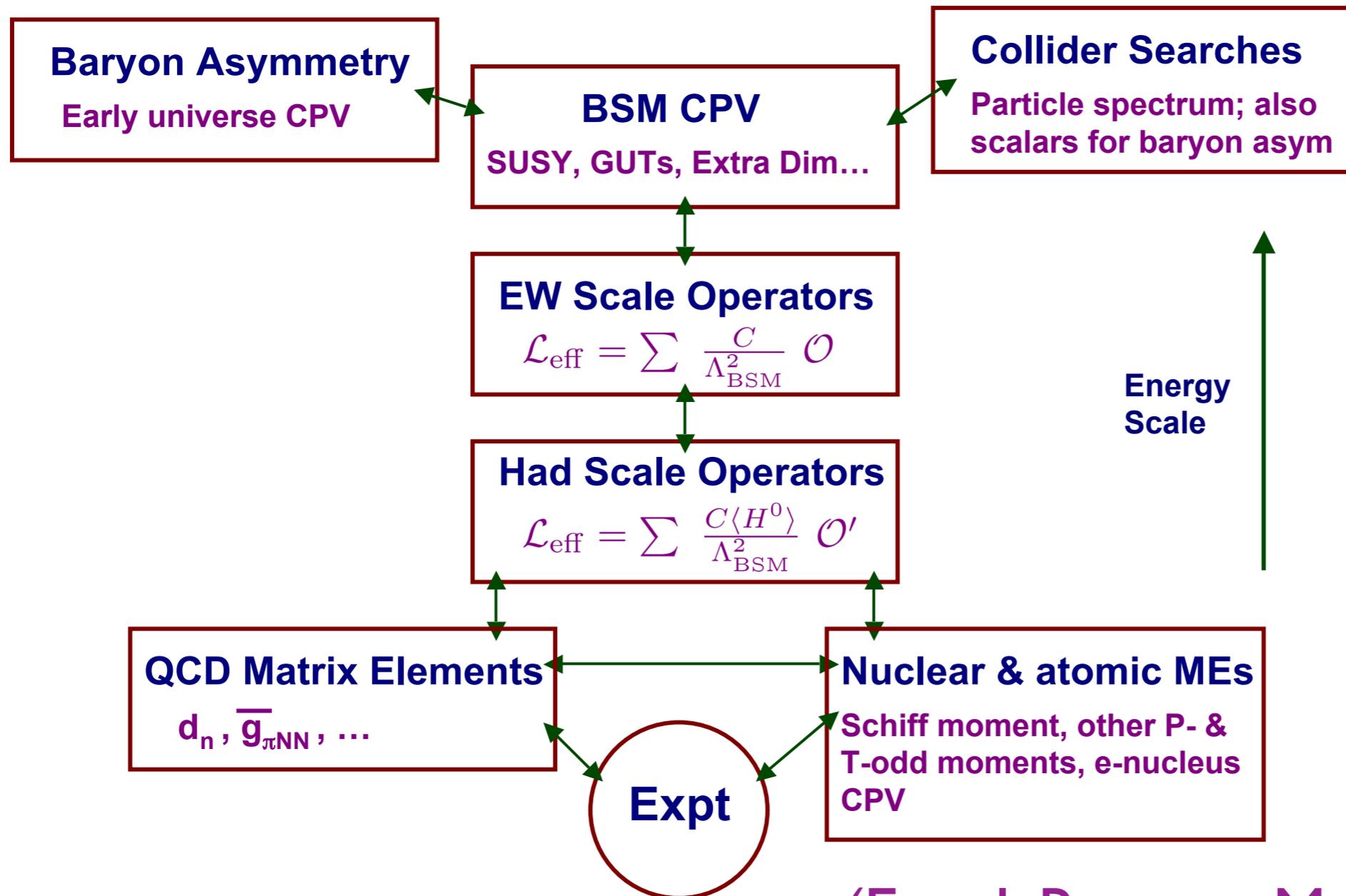
EDMs and CP Violation

- Interaction is T-odd:

$$T(\vec{E} \cdot \vec{S}) = -\vec{E} \cdot \vec{S}$$

- By CPT theorem, a non-zero EDM implies CP violation.
- Any new sources of CP violation can contribute to EDMs.
- How can short range spin-dependent macroscopic forces contribute to EDMs?

The usual paradigm to connect BSM CP violation to EDMs



(Engel, Ramsey-Musolf, Van Kolck)

- Effective operators at hadronic scale. CP violation encoded in Wilson coefficients.

The usual paradigm to connect CP violation sources to EDMs

- For macroscopic short forces:

$$m_\varphi \ll \Lambda_{QCD}$$

- New physics corresponds to a new ultralight degree of freedom.
- Effective operator approach no longer applicable.
- EDM calculations need to incorporate the new light propagating degree of freedom in nuclear and atomic calculations.

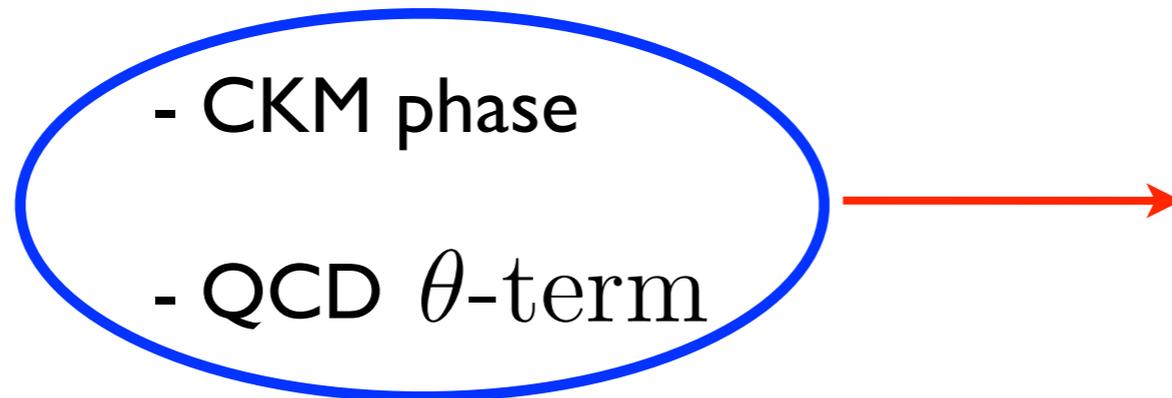
EDM Sources in the SM

- Two sources of CP violation in the SM:
 - CKM phase
 - QCD θ -term
- CKM-generated EDM is too small for current experimental sensitivities
- Thus, a non-zero EDM would be interpreted in the SM as flavor diagonal strong CP violation

$$\mathcal{L}_{QCD}^{CPV} = \bar{\theta} \frac{\alpha_s}{16\pi} G_{\mu\nu}^a \tilde{G}^{a\mu\nu}$$

EDM Sources in the SM

- Two sources of CP violation in the SM:



Effects not associated with a macroscopic force

- CKM-generated EDM is too small for current experimental sensitivities

$$d_n \sim 10^{-31} \text{ e cm}$$

- Thus, a non-zero EDM would be interpreted in the SM as flavor diagonal strong CP violation

$$\mathcal{L}_{QCD}^{CPV} = \bar{\theta} \frac{\alpha_s}{16\pi} G_{\mu\nu}^a \tilde{G}^{a\mu\nu}$$

Connection with Axial U(1)

- U(1) axial rotations

$$\psi \rightarrow e^{-i\alpha\gamma_5}\psi, \quad \bar{\psi} \rightarrow \bar{\psi} e^{-i\alpha\gamma_5}$$

$$\mathcal{D}\psi\mathcal{D}\bar{\psi} \rightarrow \mathcal{D}\psi\mathcal{D}\bar{\psi} \text{Exp} \left[2i\alpha \int d^4x \frac{\alpha_s}{16\pi} G_{\mu\nu}^a \tilde{G}^{a\mu\nu} \right]$$

- Axial U(1) symmetry is anomalous

$$j_\mu^5 = \bar{\psi}\gamma_\mu\gamma_5\psi,$$

$$\partial^\mu j_\mu^5 = 2im_q\bar{\psi}\gamma_5\psi + \frac{\alpha_s}{8\pi} G_{\mu\nu}^a \tilde{G}^{a\mu\nu}$$

- For a massless quark, the net effect is a shift in the θ -parameter

$$\theta \rightarrow \theta + 2\alpha.$$

Connection with Axial U(1)

- In presence of a massless quark, strong CP violation can be rotated away.
- In the absence of a massless quark, strong CP violation can be rotated into the quark mass terms

$$\mathcal{L}_{QCD}^{CPV} = \bar{\theta} \frac{\alpha_s}{16\pi} G_{\mu\nu}^a \tilde{G}^{a\mu\nu}$$



$$\mathcal{L}_{CPV} = i\bar{\theta} \frac{m_u m_d m_s}{m_u m_d + m_u m_s + m_d m_s} [\bar{u}\gamma_5 u + \bar{d}\gamma_5 d + \bar{s}\gamma_5 s]$$

- EDMs can then be generated through matrix elements of the CP violating quark mass terms.

Non-observation of flavor diagonal CP violation is the strong CP problem

Axions

An illustrative model: KSVZ Model

- SM + massless colored quark + complex scalar

$$\delta\mathcal{L} = \partial_\mu\Phi^\dagger\partial^\mu\Phi + \mu_\Phi^2\Phi^\dagger\Phi - \lambda_\Phi(\Phi^\dagger\Phi)^2 + \bar{\psi}i\not{\partial}\psi + y\bar{\psi}_R\Phi\psi_L + h.c.$$

- U(1) Peccei-Quinn symmetry

$$\psi \rightarrow e^{-i\alpha\gamma_5} \psi, \quad \bar{\psi} \rightarrow \bar{\psi} e^{-i\alpha\gamma_5}, \quad \Phi \rightarrow e^{-2i\alpha} \Phi$$

- Spontaneous symmetry breaking of Peccei-Quinn symmetry

$$\langle\Phi\rangle = f_a, \quad \Phi(x) = \frac{f_a + \rho(x)}{\sqrt{2}} e^{ia(x)/f_a}$$

An illustrative model: KSVZ Model

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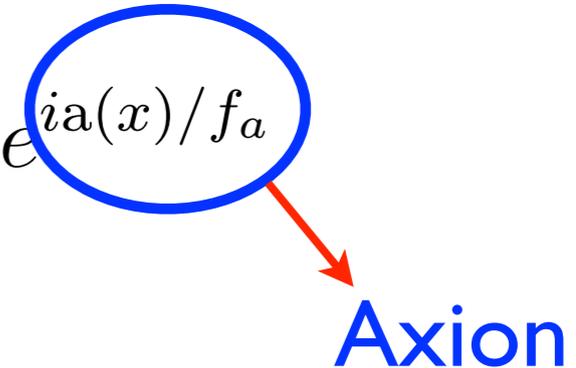
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Axion

An illustrative model: KSVZ Model

- PQ symmetry breaking is typically constrained to be

$$10^9 \lesssim f_a \lesssim 10^{12} \text{ GeV} \quad m_\psi \sim f_a$$

- Integrate out heavy degrees of freedom. Construct low energy EFT: SM + Axion. Note in full theory U(1) PQ causes the shifts:

$$\bar{\theta} \rightarrow \bar{\theta} + 2\alpha, \quad \frac{a(x)}{f_a} \rightarrow \frac{a(x)}{f_a} - 2\alpha.$$

$$\boxed{\bar{\theta} + \frac{a(x)}{f_a}} \longrightarrow \text{Invariant combination}$$

- Effective Axion Lagrangian:

$$\mathcal{L}_a = \frac{\alpha_s}{16\pi} \left(\bar{\theta} + \frac{a}{f_a} \right) G_{\mu\nu}^a \tilde{G}^{a\mu\nu} - m_q \bar{q}q$$

Axial U(1) Rotation

- Axial U(1) transformation can move all CP violation into the quark mass terms:

$$\mathcal{L}_a = \frac{\alpha_s}{16\pi} \left(\bar{\theta} + \frac{a}{f_a} \right) G_{\mu\nu}^a \tilde{G}^{a\mu\nu} - m_q \bar{q}q$$



$$\mathcal{L}_a = -\cos \left(\bar{\theta} + \frac{a}{f_a} \right) m_q \bar{q}q + m_q \sin \left(\bar{\theta} + \frac{a}{f_a} \right) \bar{q}i\gamma^5 q$$

- Axion couplings to the quarks is now manifest.

Axion Vacuum Expectation Value

- Axion can acquire a non-zero vev:

$$a(x) = \langle a \rangle + a(x) \longrightarrow \theta_{\text{ind.}} = \bar{\theta} + \frac{\langle a \rangle}{f_a};$$

- The Axion Lagrangian now takes the form:

$$\mathcal{L}_a = -\cos\left(\theta_{\text{ind.}} + \frac{a}{f_a}\right) m_q \bar{q}q + m_q \sin\left(\theta_{\text{ind.}} + \frac{a}{f_a}\right) \bar{q}i\gamma^5 q$$

Axion Potential

- Axion potential is generated via the quark condensate

$$V\left(\theta_{\text{ind.}} + \frac{a}{f_a}\right) = m_q \langle \bar{q}q \rangle \cos\left(\theta_{\text{ind.}} + \frac{a}{f_a}\right)$$

- The ground state potential can be expanded as

$$V(\theta_{\text{ind.}}) \simeq \frac{1}{2} \chi(0) \theta_{\text{ind.}}^2, \quad \chi(0) = -m_q \langle \bar{q}q \rangle$$

- Minimum of the potential at:

$$\theta_{\text{ind.}} = 0$$

Dynamical relaxation of ground state Axion potential solves the strong CP problem

Higher dimension CP odd operators

- The presence of higher dimensional CP-odd operators can generate linear terms in the potential

$$V(\theta_{\text{ind.}}) \simeq \chi_{\text{CP}}(0) \theta_{\text{ind.}} + \frac{\chi(0)}{2} \theta_{\text{ind.}}^2$$

- The coefficient of the linear term is given by the correlator of the CP-odd higher dimension operator

$$\chi_{\text{CP}}(0) = -i \lim_{k \rightarrow 0} \int d^4x e^{ik \cdot x} \langle 0 | T(G \tilde{G}(x), \mathcal{O}_{\text{CP}}(0)) | 0 \rangle$$

- The minimum is shifted to a non-zero value

$$\theta_{\text{ind.}} = -\frac{\chi_{\text{CP}}(0)}{\chi(0)} \longrightarrow \text{Non-zero EDM}$$

Axion Couplings

- Expanding the Axion Lagrangian gives

$$\mathcal{L}_a = \left(\frac{\theta_{\text{ind.}}}{f_a} a - 1 \right) m_q \bar{q}q + \left(\theta_{\text{ind.}} + \frac{a}{f_a} \right) m_q \bar{q}i\gamma^5 q + \frac{m_q}{2f_a^2} a^2 \bar{q}q + \dots$$


$$g_{a,s}^q = \frac{\theta_{\text{ind.}} m_q}{f_a},$$

Scalar
coupling


$$g_{a,p}^q = \frac{m_q}{f_a},$$

Pseudo-scalar
coupling

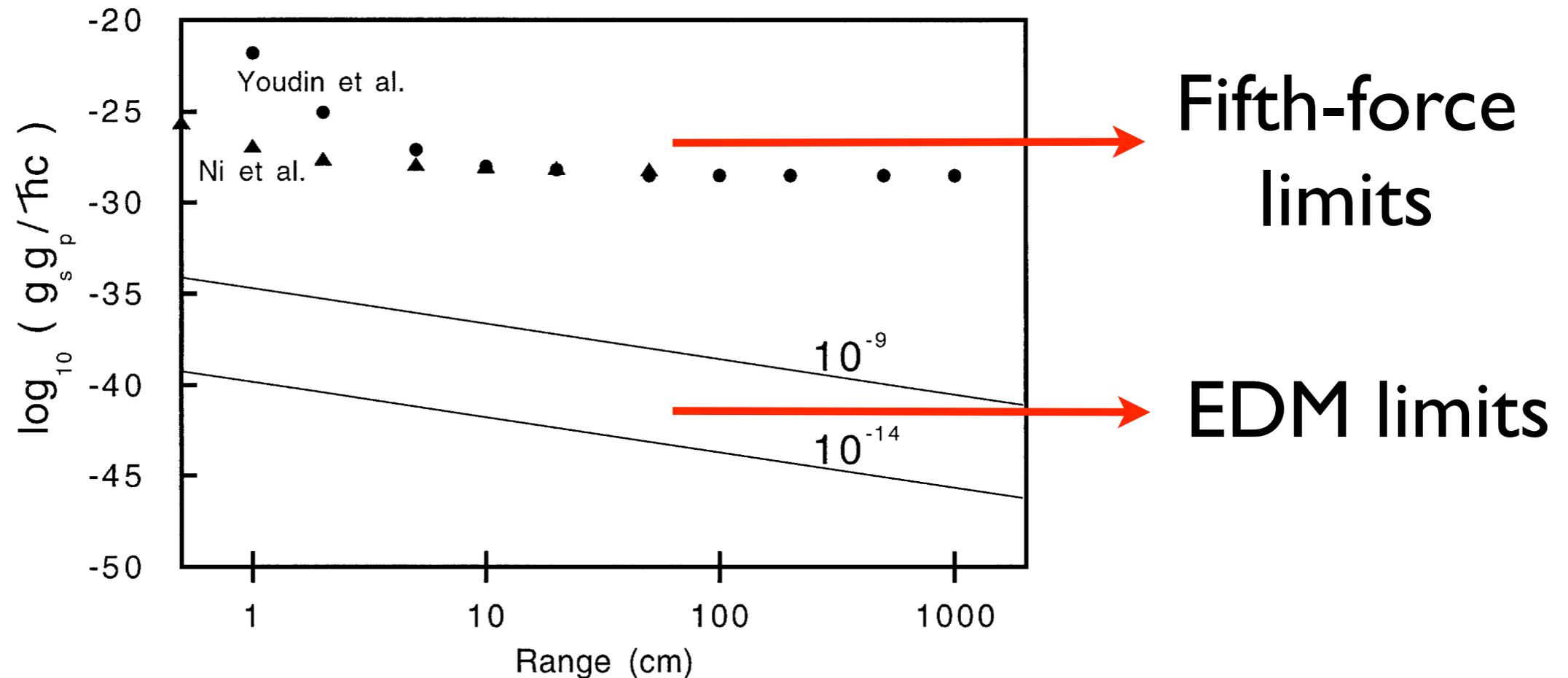

$$m_a \simeq \frac{1}{f_a} |\chi(0)|^{1/2}$$

Axion
mass

- Product of couplings proportional to theta parameter:

$$g_s^1 g_p^2 \propto \theta_{\text{ind.}} \frac{m_q^2}{f_a^2}$$

EDM Limits Dominate over Fifth Force Bounds



(Rosenberg, Bibber)

$$g_s g_p \simeq \frac{\bar{\theta}}{\lambda(\text{mm})^2} 6 \times 10^{-27}$$

EDM limit

$$|\bar{\theta}| \lesssim 10^{-10}$$

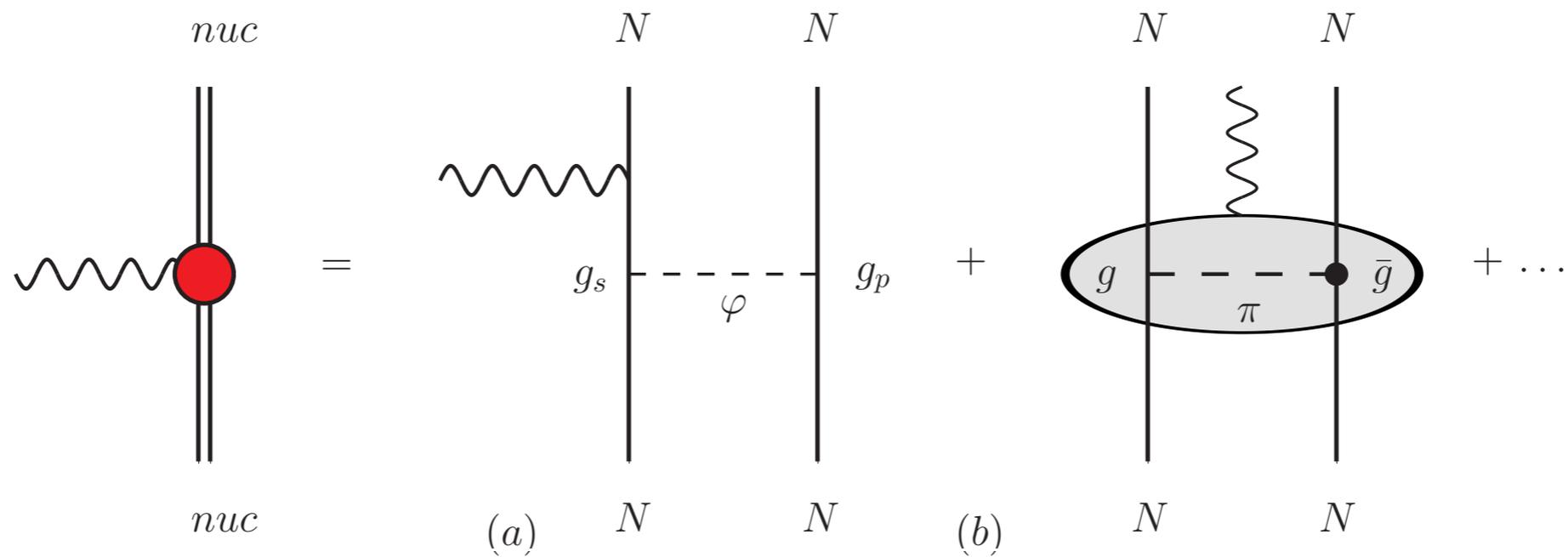
Generic Scalars

Arbitrary Couplings

- Nucleon level couplings:

$$\mathcal{L}_{\varphi NN} = g_s \varphi \bar{N}N + g_p \varphi \bar{N}i\gamma_5 N.$$

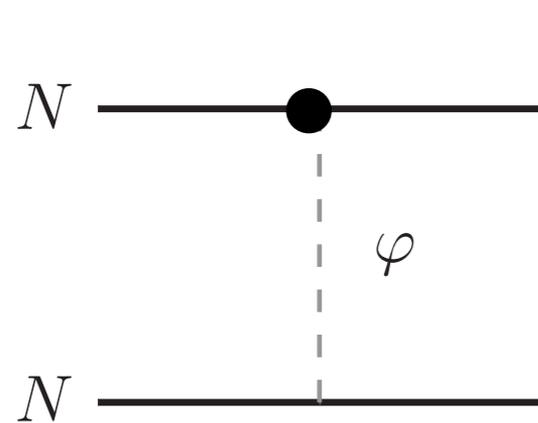
- EDMs induced by dynamical exchanges of light scalar



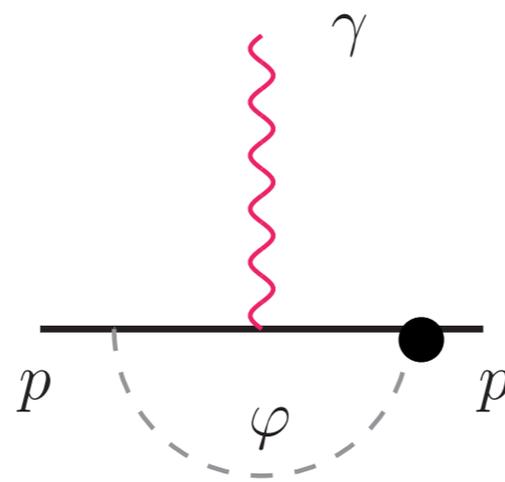
- Full EDM calculation must incorporate this propagating light scalar. Effective operator approach no longer applicable.

Estimate of Contribution to EDMs

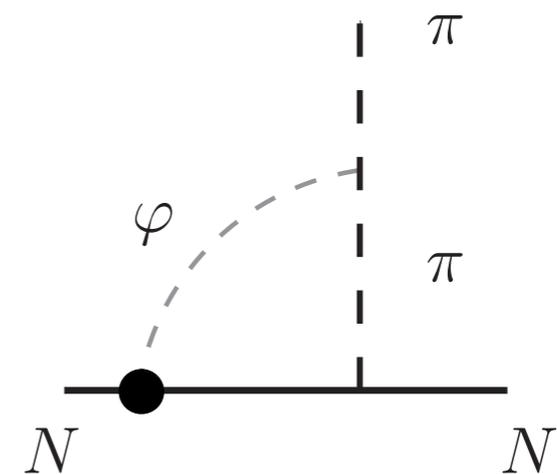
- A full EDM calculation with a new light scalar is beyond the scope of this work.
- Some example nucleon level diagrams that can contribute to the EDM:



Direct
exchange



Proton
EDM

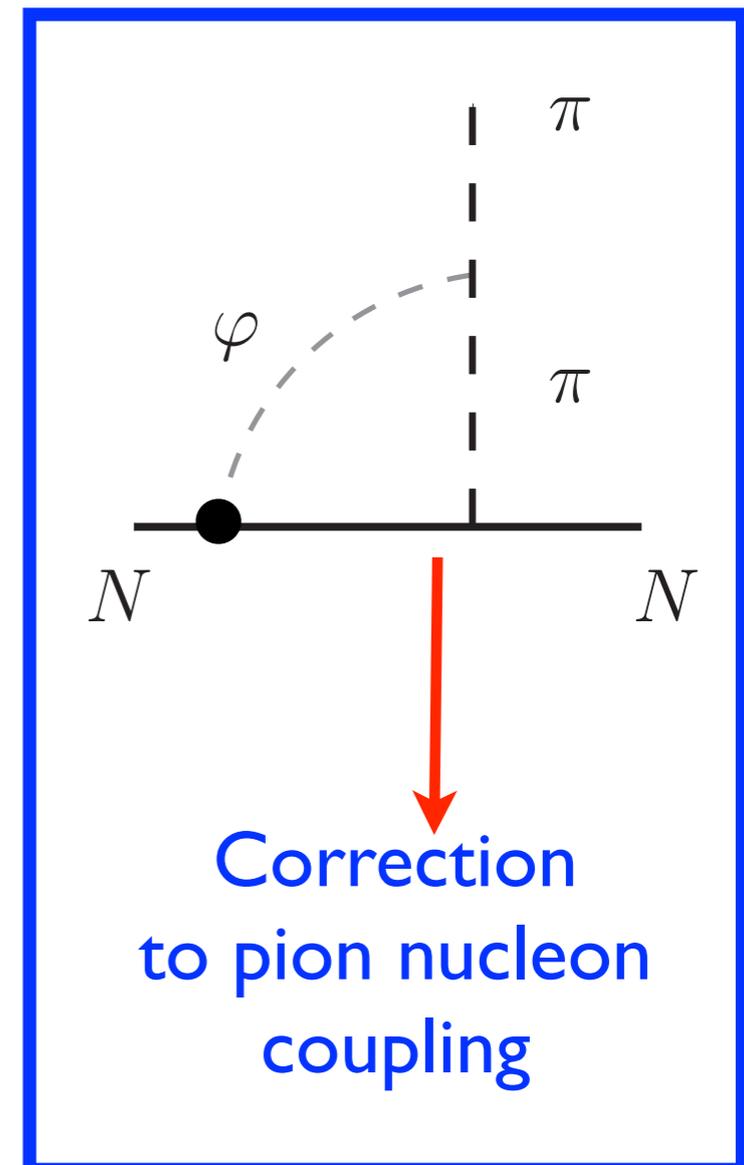


Correction
to pion nucleon
coupling

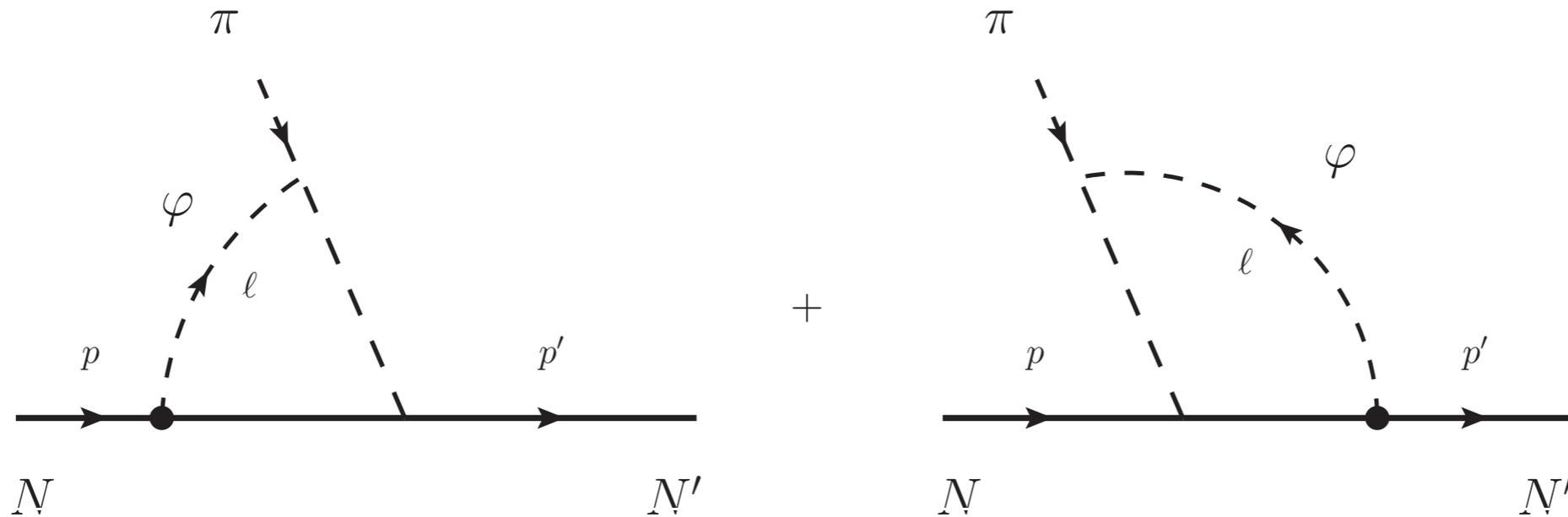
Estimate of Contribution to EDMs

- A full EDM calculation with a new light scalar is beyond the scope of this work.
- Some example nucleon level diagrams that can contribute to the EDM:

- Treat as a shift to pion-nucleon coupling
- Incorporate into existing results for the Schiff moment of the Mercury EDM



- Compute one loop diagrams using Heavy Baryon Chiral Perturbation theory (HBChPT)



$$\mathcal{L}_{\pi\bar{N}N} = \frac{2g_A}{f_\pi} \partial_\mu \pi^a \bar{N}_v \frac{\sigma^a}{2} S^\mu N_v,$$

$$\mathcal{L}_{\varphi\pi\pi} = g_s^\pi \varphi \pi^a \pi^a,$$

$$\mathcal{L}_{\varphi\bar{N}N} = -\frac{g_p}{m_N} \bar{N}_v (S^\mu \partial_\mu \varphi) N_v,$$

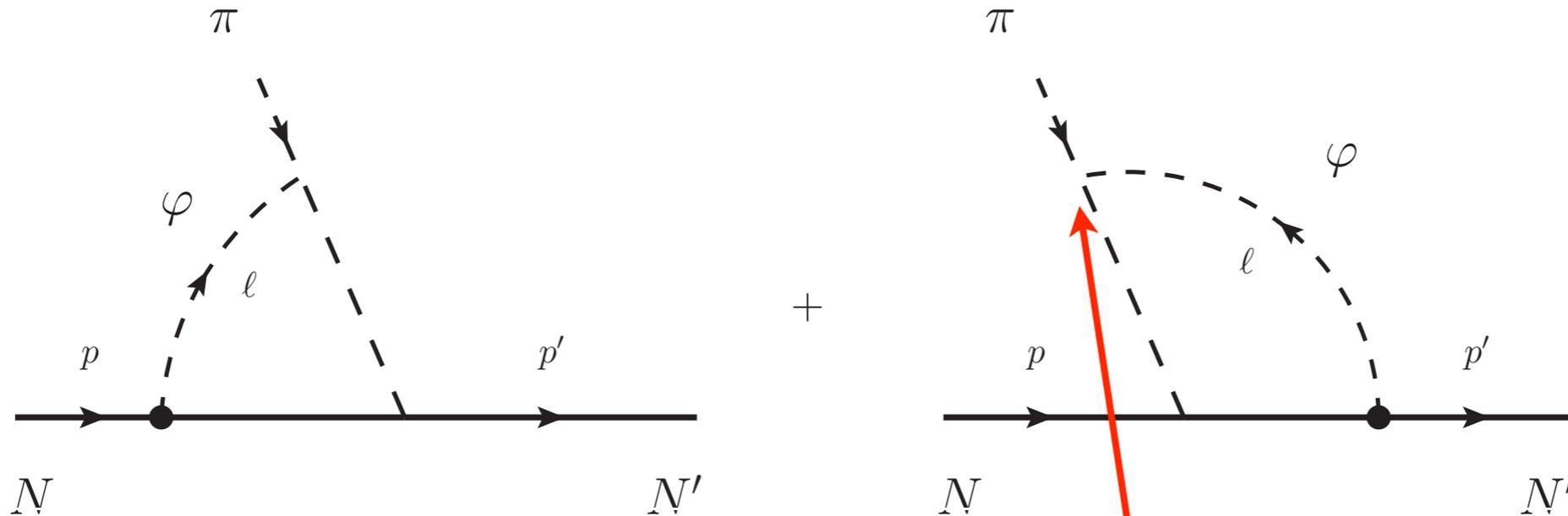
$$g_s^\pi = \frac{\langle \pi | \bar{u}u + \bar{d}d | \pi \rangle}{\langle N | \bar{u}u + \bar{d}d | N \rangle} g_s$$

$$\frac{g_s^\pi}{g_s} \simeq \frac{m_\pi^2}{90 \text{ MeV}} \simeq 218 \text{ MeV}$$

Vertices in HBChPT

Coupling to Pion

- Coupling to pion is related to scalar nucleon coupling:



$$\mathcal{L}_{\pi\bar{N}N} = \frac{2g_A}{f_\pi} \partial_\mu \pi^a \bar{N}_v \frac{\sigma^a}{2} S^\mu N_v,$$

$$\mathcal{L}_{\varphi\pi\pi} = g_s^\pi \varphi \pi^a \pi^a,$$

$$\mathcal{L}_{\varphi\bar{N}N} = -\frac{g_p}{m_N} \bar{N}_v (S^\mu \partial_\mu \varphi) N_v,$$

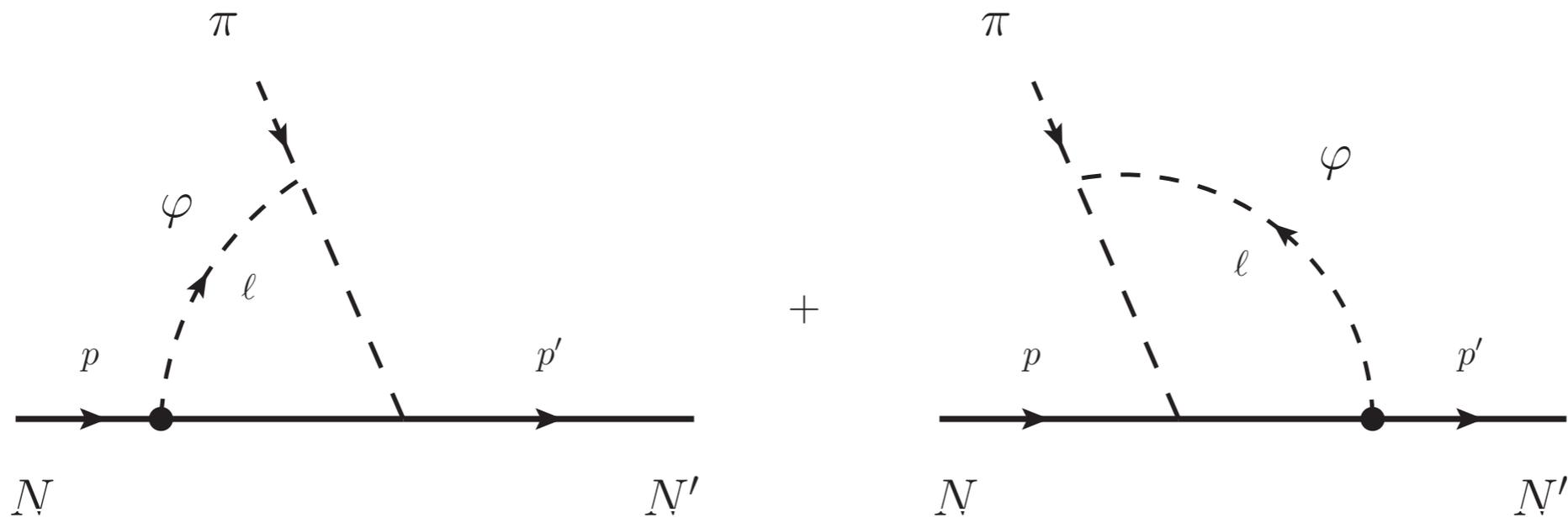
$$g_s^\pi = \frac{\langle \pi | \bar{u}u + \bar{d}d | \pi \rangle}{\langle N | \bar{u}u + \bar{d}d | N \rangle} g_s$$

$$\frac{g_s^\pi}{g_s} \simeq \frac{m_\pi^2}{90 \text{ MeV}} \simeq 218 \text{ MeV}$$

Vertices in HBChPT

Coupling to Pion

- Result of computation



$$\mathcal{M}^a = \frac{i}{16\pi} \frac{m_\pi^2 + m_\pi m_\varphi + m_\varphi^2}{m_\pi + m_\varphi} \frac{g_s^\pi g_p g_A}{m_N f_\pi} \bar{N}_v(p') \sigma^a N_v(p)$$

- Write as new contribution to CP-odd pion-nucleon coupling

$$\mathcal{L}_{\pi\bar{N}N}^{CPV} = \frac{1}{16\pi} \frac{m_\pi^2 + m_\pi m_\varphi + m_\varphi^2}{m_\pi + m_\varphi} \frac{g_s^\pi g_p g_A}{m_N f_\pi} \pi^a \bar{N} \sigma^a N$$

Mercury EDM

- The mercury EDM in terms of the Schiff moment

$$d_{Hg} = -2.8 \times 10^{-4} \frac{S_{Hg}}{\text{fm}^2}$$

(Griffith; de Jesus, Engel)

- Schiff moment in terms of pion-nucleon couplings

$$S_{Hg} = g_{\pi NN} [0.01 \bar{g}_{\pi NN}^{(0)} + 0.07 \bar{g}_{\pi NN}^{(1)} + 0.02 \bar{g}_{\pi NN}^{(2)}] e \text{ fm}^3$$

- Definition of pion-nucleon couplings

$$\mathcal{L}_{\pi NN} = \bar{g}_{\pi NN}^{(0)} \bar{N} \tau^a N \pi^a + \bar{g}_{\pi NN}^{(1)} \bar{N} N \pi^0 + \bar{g}_{\pi NN}^{(2)} (\bar{N} \tau^a N \pi^a - 3 \bar{N} \tau^3 N \pi^0)$$

Shift in the Mercury EDM

- Shift in the Schiff moment will cause a shift in the EDM

$$\delta d_{Hg} = -2.8 \times 10^{-4} \frac{\delta S_{Hg}}{\text{fm}^2}$$

- Shift in the Schiff moment arises from one-loop pion-nucleon couplings

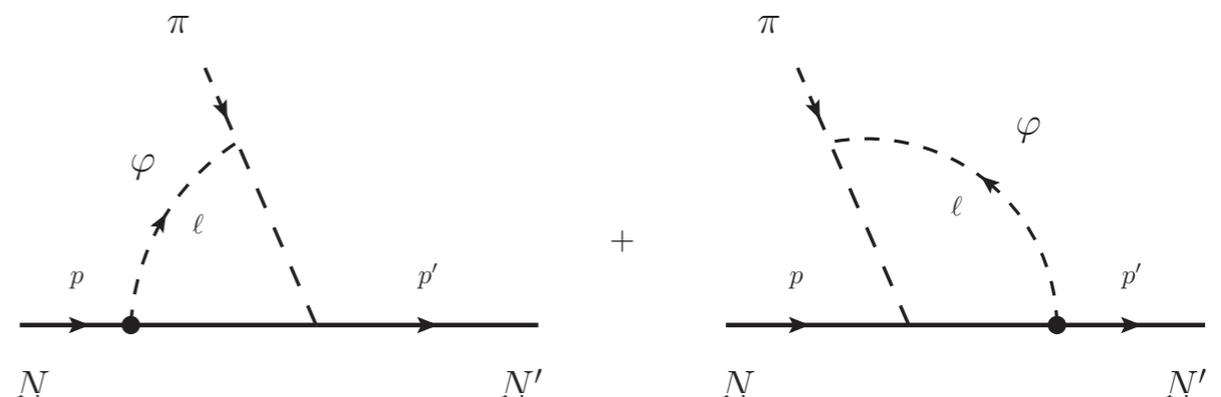
$$\delta S_{Hg} = g_{\pi NN} [0.01 \delta \bar{g}_{\pi NN}^{(0)} + 0.07 \delta \bar{g}_{\pi NN}^{(1)} + 0.02 \delta \bar{g}_{\pi NN}^{(2)}] e \text{ fm}^3$$

- Shift in CP-odd pion-nucleon couplings

$$\delta \bar{g}_{\pi NN}^{(0)} \simeq \frac{1}{16\pi} \frac{m_\pi^2 + m_\pi m_\varphi + m_\varphi^2}{m_\pi + m_\varphi} \frac{g_A m_\pi^2}{90 \text{ MeV} m_N f_\pi} g_s g_p$$

$$\delta \bar{g}_{\pi NN}^{(1)} = 0;$$

$$\delta \bar{g}_{\pi NN}^{(2)} = 0$$



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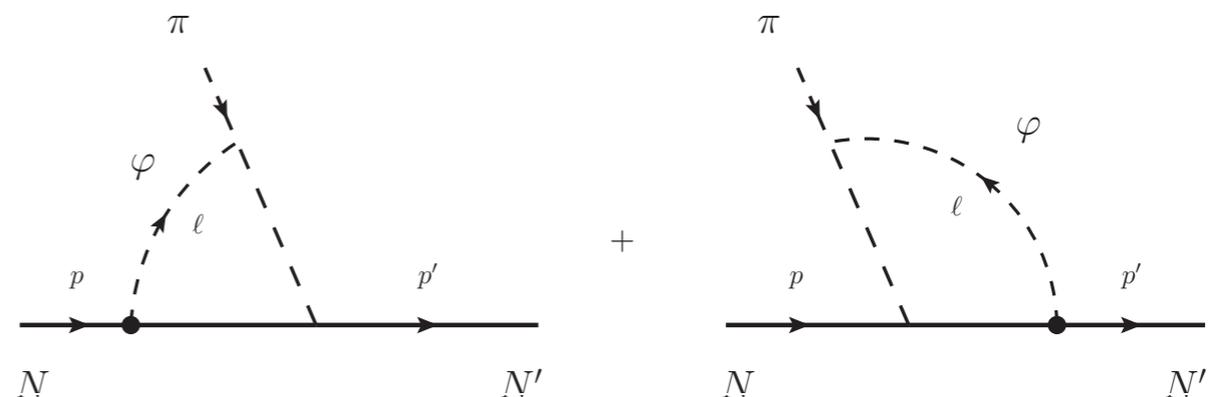
$$\delta S_{Hg} = g_{\pi NN} [0.01 \delta \bar{g}_{\pi NN}^{(0)} + 0.07 \delta \bar{g}_{\pi NN}^{(1)} + 0.02 \delta \bar{g}_{\pi NN}^{(2)}] e \text{ fm}^3$$

- Shift in CP-odd pion-nucleon couplings

$$\delta \bar{g}_{\pi NN}^{(0)} \simeq \frac{1}{16\pi} \frac{m_\pi^2 + m_\pi m_\varphi + m_\varphi^2}{m_\pi + m_\varphi} \frac{g_A m_\pi^2}{90 \text{ MeV} m_N f_\pi} g_s g_p$$

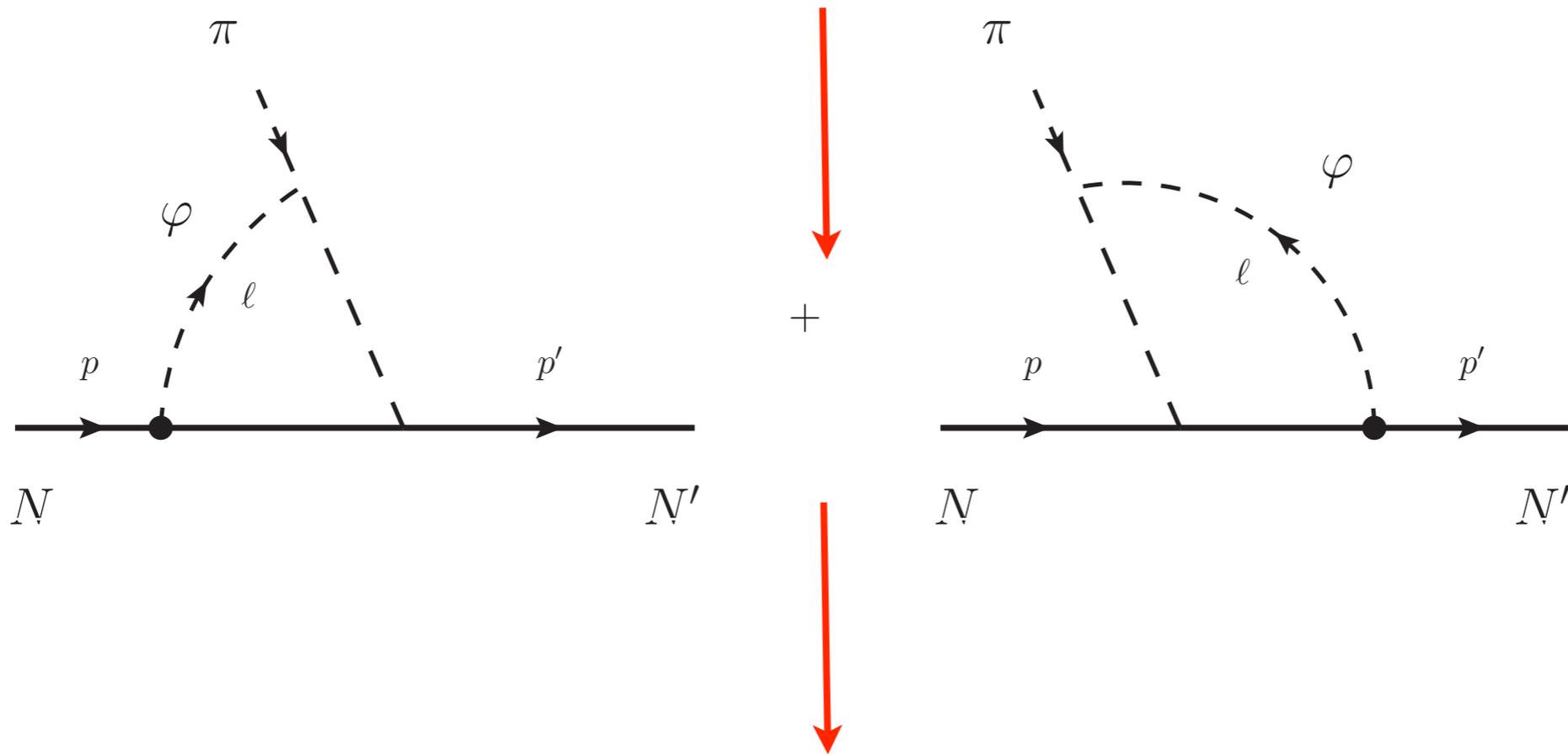
$$\delta \bar{g}_{\pi NN}^{(1)} = 0;$$

$$\delta \bar{g}_{\pi NN}^{(2)} = 0$$



EDM Bound on Macroscopic Spin-Dependent Force

$$|d_{Hg}| < 3.1 \times 10^{-16} \text{ e fm}$$



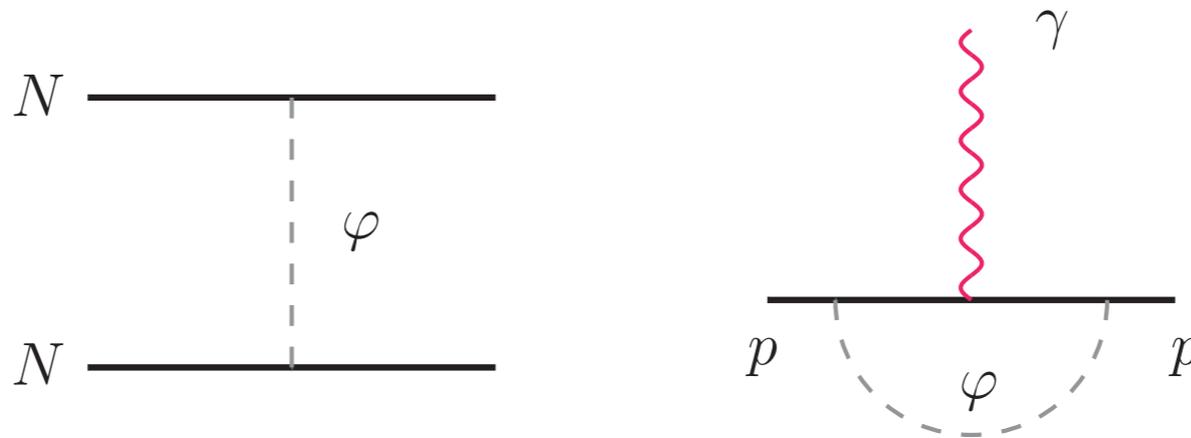
$$|g_s g_p| \lesssim 10^{-9}$$

Corrections

- Bound from the one-loop correction to the CP-odd pion-nucleon coupling

$$|g_s g_p| \lesssim 10^{-9}$$

- This result will be modified by order one nuclear effects and additional diagrams. The tree level diagram can enhance the effect by two orders of magnitude.



- A rigorous calculation with all effects included is expected to yield

$$g_s g_p \lesssim [10^{-11}, 10^{-9}].$$

Comparison with Fifth Force limits

- EDM limit:

$$g_s g_p \lesssim [10^{-11}, 10^{-9}].$$

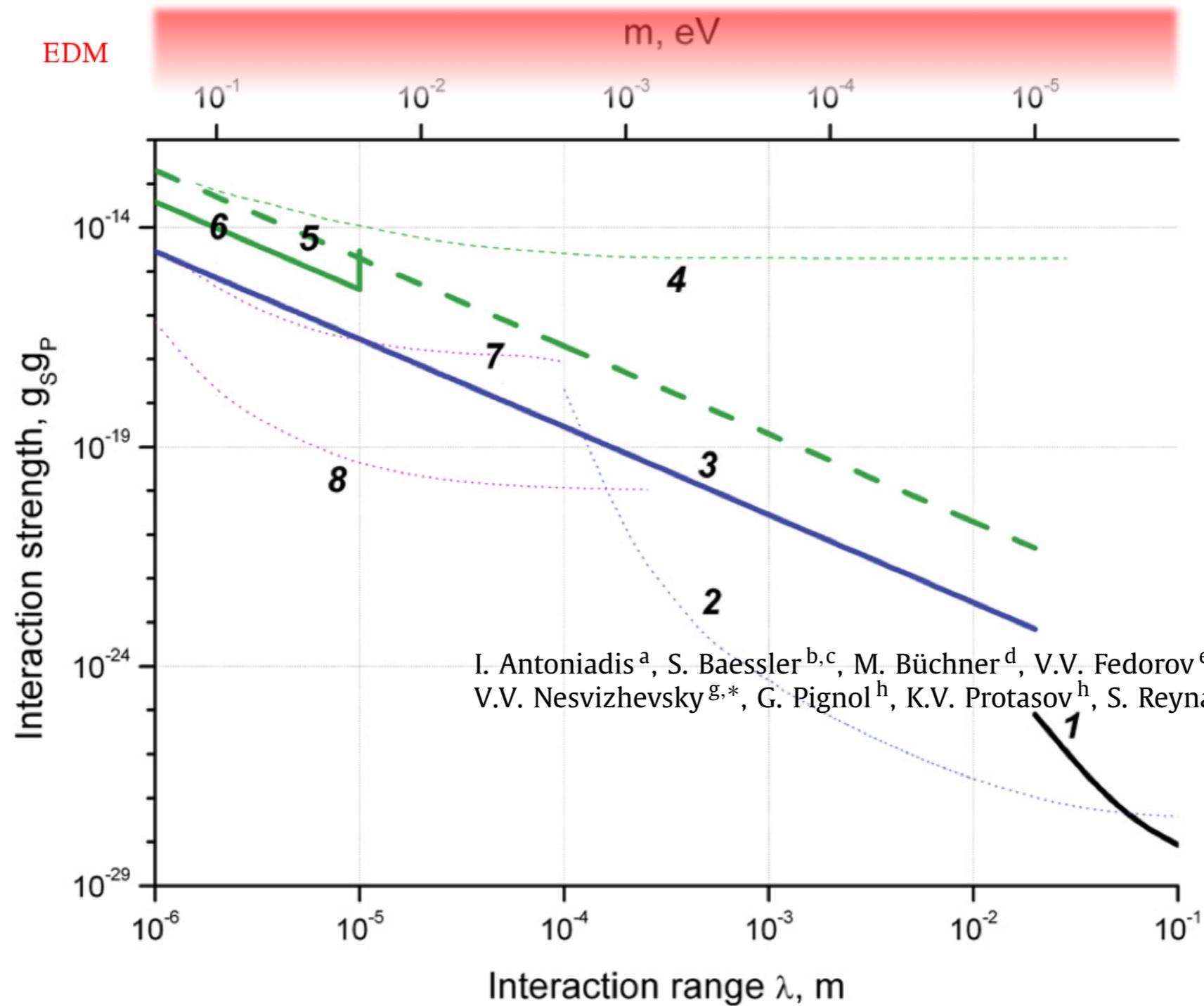
- Fifth force limits:

Interaction range λ [m]	m_φ [eV]	$ g_s g_p $
$\sim 2 \times 10^{-5}$	$\sim 10^{-2}$	$< 10^{-16}$
$\sim 2 \times 10^{-1}$	$\sim 10^{-6}$	$< 10^{-29}$

- EDM limit on axion forces:

$$g_s g_p|_{\text{axion}} \propto \theta_{\text{ind.}} \frac{m_q^2}{f_a^2} < 10^{-40} - 10^{-34}.$$

Comparison with Fifth Force limits



Conclusions

- A signal for short range spin-dependent forces implies CP violation beyond the SM.
- Observations in fifth Force experiments can be correlated with EDM constraints.
- EDM limits always dominate constraints on Axion mediated short range forces.
- For generic scalars EDM and fifth force limits can compete or one can dominate depending on the region of parameter space.