Higher Twist and Parton Angular Momentum in Parity-Violating Deep Inelastic Electron-Deuteron Scattering

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# Outline:

- 1. Brief review on e-D PVDIS and highertwist correction
- 2. Brief review on nuclear spin problem
- 3. Main results of our work
- 4. Summary



### 1. Brief review on e-D PVDIS and highertwist correction

## The precision frontier

- Precision frontier as an effective probe of BSM physics, compliment to the energy frontier
- Energy frontier searches for "bumps", while precision frontier searches for "deviations"







Polarized electron, unpolarized target

 $d\sigma \sim L^{\mu\nu} W^{\gamma Z}_{\mu\nu}$ 

$$L^{\mu\nu} \sim \overline{u}_{s'}(k')\gamma^{\mu}u_{s}(k)\overline{u}_{s}(k)\gamma^{\nu}(g_{V}^{e}+g_{A}^{e}\gamma_{5})u_{s'}(k')$$

$$W_{\mu\nu}^{\gamma Z} = (-g_{\mu\nu} + \frac{q_{\mu}q_{\nu}}{q^{2}})\frac{F_{1}^{\gamma Z}}{M_{D}} + (P_{\mu} - \frac{P \cdot q}{q^{2}}q_{\mu})(P_{\nu} - \frac{P \cdot q}{q^{2}}q_{\nu})\frac{F_{2}^{\gamma Z}}{M_{D}P \cdot q} + \frac{i\varepsilon_{\mu\nu\alpha\beta}}{2M_{D}P \cdot q}F_{3}^{\alpha}F_{3}^{\gamma Z}$$

## Cahn-Gilman formula for Left-Right Asymmetry

$$y = \frac{E - E'}{E}$$

(fraction of electron energy loss)



$$A_{RL} = \frac{d\sigma_R - d\sigma_L}{d\sigma_R + d\sigma_L}$$

Parton model: 
$$d\sigma = \sum_{i} f_i(x) d\sigma_i$$

After lengthy math, one obtain:

$$A_{RL} = \frac{G_F Q^2}{4\sqrt{2}\pi\alpha \sum_i q_i^2 f_i(x)} \sum_i q_i f_i(x) (g_A^e g_V^i + g_V^e g_A^i \frac{1 - (1 - y)^2}{1 + (1 - y)^2})$$

Assumptions:

- 1. Ignore sea quarks.
- 2. Isospin is good symmetry.

Deuteron being isosinglet  $\Rightarrow f_u(x) = f_d(x)$ 

The PDF-dependence drops out!

#### **Cahn-Gilman Formula:**

$$A_{RL} = \frac{d\sigma_{R} - d\sigma_{L}}{d\sigma_{R} + d\sigma_{L}} = -\frac{G_{F}Q^{2}}{2\sqrt{2}\pi\alpha} \frac{9}{10} \{\tilde{a}_{1} + \tilde{a}_{2}\frac{1 - (1 - y)^{2}}{1 + (1 - y)^{2}}\}$$

$$\widetilde{a}_{1,0} = (1 - \frac{20}{9} \sin^2 \theta_W)$$
  
For SM at leading-twist  
$$\widetilde{a}_{2,0} = (1 - 4 \sin^2 \theta_W)$$

- First PVDIS experiment: Yale-SLAC collaboration (Prescott et. Al), year 1978
- Used to measure weak mixing angle

 The Jefferson Lab 12-GeV upgrade enables for the measurement of A<sub>RL</sub> with 0.5% precision over 0.3<x<sub>B</sub><0.7, providing sensitive probes (or constrains) on many BSM scenarios.



 $\widetilde{a}_i = \widetilde{a}_{i,0}(1 + R_i)$ 

Besides effects of new physics, R<sub>i</sub> includes:

Radiative Correction
Charge Symmetry Violation (CVC) : isospin breaking of PDF
Target Mass Correction : finite hadron and quark masses
Sea Quark Effect
Higher Twist

We have to first understand the SM corrections, before it can be used effectively to probe New Physics

**Higher Twist correction**: Corrections to naïve parton picture which scale as:  $(Q^2)^{-(\tau-2)/2} \quad \tau$ :"Twist" by including the interactions between partons.

In e-D PVDIS, assuming isospin symmetry and neglecting sea quarks, the only twist-4 correction term to  $\tilde{a}_1$  is proportional to the following hadronic matrix element (first discovered by Bjorken and Wolfenstein):

 $< D | \overline{u}(x)\gamma^{\mu}u(x)\overline{d}(0)\gamma^{\nu}d(0) + u \leftrightarrow d | D >$ 



# Previous works on twist-4 contribution to R<sub>1</sub> $4\text{GeV}^2 \le Q^2 \le 12\text{GeV}^2$





Isotropic light cone wavefunction

A.V. Belitsky et al, PRD 84, 014010 (2011)

- Both works give similar R<sub>1</sub> curve shape, but slightly different peak position and size (range from -0.003~-0.005) reflecting the current theoretical uncertainty.
- Both works indicating that the twist-4 contribution to  $R_1$  is right below the reach of the upgraded JLab precision (which measures  $R_1$  at the accuracy of  $\pm 0.005$ )



### 2. Brief review on nuclear spin problem

- Spin structure of nucleon has been a long-lasting problem since EMC's DIS result with polarized muon beams, which contradicted the Ellis-Jaffe sum rule, implying that the spin of a proton is not built up entirely from the quark spin (the "Spin Crisis")
- A key question is now to explain the source of nucleon spin in terms of QCD DOF.
- Further complication arises as the classification of different components of nucleon spin (e.g. parton helicity and OAM), is gauge-dependent. See e.g. R. L. Jaffe and A. Manohar, Nucl. Phys. B337, 509 and X. Ji, Phys. Rev. Lett. 78, 610.



 Under light-cone gauge, non-zero quark OAM are responsible for certain DIS observables, e.g Sivers and Boer-Mulders function

Sivers function:  $f_{1T}^{\perp}(x, \mathbf{k}_{\perp}^{2}) = -i(k^{x} + ik^{y})\frac{M}{2k_{\perp}^{2}}\int \frac{d\xi^{-}d^{2}\boldsymbol{\xi}_{\perp}}{(2\pi)^{3}}$  $\times e^{-i(\xi^{-}k^{+} - \boldsymbol{\xi}_{\perp} \cdot \boldsymbol{k}_{\perp})}$ 

 $\times \langle P \uparrow | \bar{\psi}(\xi^{-}, \xi_{\perp}) \mathcal{L}_{\xi}^{\dagger} \gamma^{+} \mathcal{L}_{0} \psi(0) | P \downarrow \rangle$ 

Boer-Mulders function:

$$h_{1}^{\perp}(x, \boldsymbol{k}_{\perp}^{2}) = \boldsymbol{\epsilon}^{ij} \boldsymbol{k}_{\perp}^{j} \frac{M}{2\boldsymbol{k}_{\perp}^{2}} \int \frac{d\boldsymbol{\xi}^{-} d^{2} \boldsymbol{\xi}_{\perp}}{(2\pi)^{3}} e^{-i(\boldsymbol{\xi}^{-} \boldsymbol{k}^{+} - \boldsymbol{\xi}_{\perp} \cdot \boldsymbol{k}_{\perp})} \frac{1}{2} \\ \times \sum_{\Lambda} \langle P\Lambda | \bar{\psi}(\boldsymbol{\xi}^{-}, \boldsymbol{\xi}_{\perp}) \mathcal{L}_{\boldsymbol{\xi}}^{\dagger} i \sigma^{i+} \gamma_{5} \mathcal{L}_{0} \psi(0) | P\Lambda \rangle$$

(See B. Pasquini and F. Yuan, PRD 81, 114013)

They appear in Semi-Inclusive Deep Inelastic Scattering (SIDIS) with transversely-polarized targets.

- It will be interesting to ask, how the inclusion of parton angular momentum (besides quark helicity) would affect other DIS observables which have been previously studied
- Another question will be: how to interpret any study of parton AM in a gauge-invariant way, and as insensitive as possible to a particular choice of AM decomposition.
- As we will see later, detailed analysis of the affect of parton AM on different DIS observables provides a way to disentangle different components of parton AM and study each of them individually



## 3. Main results of our work

(CYS and Michael J. Ramsey-Musolf, PRC 88, 015202)

Caution: "Quark OAM" we mention here is after assuming light-cone gauge

- Model we use: OAM-dependent light-cone wavefunction, including only three valence quarks
- Nucleon wavefunction with definite helicity can be decomposed into states of definite Lz of the valence quarks

$$|P,\uparrow>=|h=\frac{1}{2}, l_{z}=0>+|h=-\frac{1}{2}, l_{z}=1>$$
$$+|h=\frac{3}{2}, l_{z}=-1>+|h=-\frac{3}{2}, l_{z}=2>$$

- Finite-OAM wavefunction can be obtained from a constituent quark model (e.g. B. Pasquini et al, PRD 78, 034025)
- From nucleon to deuteron: Incoherent Impulse Approximation assumed

An explicit example:

iik

$$|h = \frac{1}{2}, l_z = 0 >= \int d[X_3](\psi^{(1)}(1,2,3) + i\varepsilon^{\alpha\beta}k_{1\alpha}k_{2\beta}\psi^{(2)}(1,2,3)) \times$$

$$\frac{\mathcal{E}^{_{jh}}}{\sqrt{6}} u_{i\uparrow}^{+}(1) \{ u_{j\downarrow}^{+}(2) d_{k\uparrow}^{+}(3) - d_{j\downarrow}^{+}(2) u_{k\uparrow}^{+}(3) \} | 0 >$$

The functions  $\{\psi^{(1)}, ..., \psi^{(6)}\}$  are obtained from constituent quark model.

Only **diagonal** components, i.e. <h|...|h> (same h for initial and final states) will contribute.

#### Our main result after performing numerical integration:



FIG. 3. (Color online) The twist-four correction to  $R_1$  at  $Q^2 = 4 \text{ GeV}^2$ . The blue dashed curve shows the  $l_z = 0$  contribution; purple dot-dashed curve shows the  $l_z = 1$  contribution; brown dot-dashed curve shows the  $l_z = -1$  contribution; the red solid curve is the sum of all.  $l_z = 2$  contribution is negligible and therefore not included.

- Similar curve shape with existing results, all suggesting that R<sub>1</sub>(HT) is beyond the reach of upgraded JLab accuracy.
- Non-intuitive observation: partial cancelation between L<sub>z</sub>=±I contribution, leaving L<sub>z</sub>=0 piece dominant.



#### This cancelation is rather modelindependent!



 Similar property not shared by other DIS observables, e.g. Quark Distribution Function:



FIG. 4. (Color online) The unnormalized QDF of spin-up proton, split into contributions from different  $l_z$  components. Blue thick-dashed curve shows contribution from  $l_z = 0$  component; purple dot-dashed curve shows contribution from  $l_z = 1$  component; brown dot-dashed curve shows contribution from  $l_z = -1$  component; green thin-dashed curve shows contribution from  $l_z = 2$  component; red solid curve is the sum of all contributions.

 Twist-4 correction to e-D PVDIS provides a probe to the L<sub>z</sub>=0 piece of quark OAM! •Gauge-independent Interpretation: twist-4 correction to eD-PVDIS is essentially transparent to the parton AM dynamics that generates Sivers and Boer-Mulders function in SIDIS.

•Detailed study of different DIS observables helps disentangling effects of different parton AM components.

TABLE II. The dependence on different quark light-cone OAM components of various distribution functions.

Distribution functions	Dominant contribution(s)	Subdominant contribution(s)
Quark distribution functions PVDIS twist-four correction Sivers function Boer-Mulders function	$(0 \otimes 0), (1 \otimes 1)$ $(0 \otimes 0)$ $(0 \otimes 1)$ $(0 \otimes 1), (1 \otimes 2)$	$(2\otimes 2)$ $(1\otimes 1), (2\otimes 2)$ $(1\otimes 2)$ -

$$(a \otimes b): \langle |L_z| = b | \dots | |L_z| = a \rangle$$



## 4. Summary

- 1. e-D PVDIS probes not only BSM physics, but also novel features of hadron and nuclear structure.
- 2. Various calculations show that the precision needed for the study of twist-four contribution to R<sub>1</sub> is beyond the reach of the 12GeV-upgrade of JLab.
- 3. Simplification of the interpretation: SM corrections that enter JLab e-D PVDIS result will not include twist-4, unless the existing models are completely wrong.
- 4. Future effort of increasing experimental precision level is worthwhile, because as shown in our work, it comes with a bonus of helping us in understanding the role of parton angular momentum in nucleon structrure.



## **Backup Slides**

From isotropic to non-isotropic wavefunction

• start from isotropic constituent-quark model



• use Melosh rotation to change "instant-form" wavefunction to "light-front" form:

$$\vec{\tilde{k}}, \lambda, \tau \rangle_{[f]} = \sqrt{2\omega} (2\pi)^{3/2} \sum_{\lambda'} D_{\lambda'\lambda}^{1/2} (R_{cf}(\vec{\tilde{k}})) |\vec{k}, \lambda', \tau \rangle_{[c]}.$$
$$\vec{\tilde{k}} = (k^+, \vec{k}_\perp) \qquad \vec{k} = (k_x, k_y, k_z)$$

non-zero OAM components emerges naturally during the rotation

$$A_{UT}^{\sin(\phi_h - \phi_S)} = 2 \frac{\int d\phi_h d\phi_S [d\sigma^{lp^{\uparrow} \to l'hX} - d\sigma^{lp^{\downarrow} \to l'hX}] \sin(\phi_h - \phi_S)}{\int d\phi_h d\phi_S [d\sigma^{lp^{\uparrow} \to l'hX} + d\sigma^{lp^{\downarrow} \to l'hX}]}$$

UT: Unpolarized leptons scattering with Transversely-polarized protons.



M. Anselmino et al, Phys. Rev. D 83, 114019 (2011)

# Bjorken-Wolfenstein's argument

- The operator of our interest is a product between EMcurrent and weak neutral current
- The deuteron is an isosinglet
- We can decompose both currents into isovector (V) and isoscalar (S).
- Since deuteron is isosinglet, so <SV>=<VS>=0.
- For leading twist, <SS>=<VV>. The difference <SS>-<VV> is just the twist-four matrix element we showed before.
- Assumptions we made here: isospin symmetry, and that the contributions from sea quarks are negligible.

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J.D Bjorken, PRD 18, 3239 (1978);
L. Wolfenstein, Nucl. Phys. B 146 477 (1978)
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