

The proton charge radius unsolved puzzle

Paul Indelicato



▲ CREMA: Muonic Hydrogen Collaboration



- Description of the experiment
- spectra for µp
- specta for µd
- Theory
- Results for radii of p and d
- explanations

_**√_LKB** 8 juillet 2010





The size of the proton, R. Pohl, A. Antognini, F. Nez et al. Nature 466, 213-216 (2010).



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Proton Structure from the Measurement of 2S-2P Transition Frequencies of Muonic Hydrogen, A. Antognini, F. Nez, K. Schuhmann *et al.* Science **339**, 417-420 (2013).



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A rapid definition

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Proton form factor

2 quarks up (2/3 e) + 1 quark down (-1/3 e) + strong interaction (gluons)

Vertex EM interaction: Dirac and Pauli Form factors (S, P: spin and 4-momentum of nucleon, f: quark flavor)

$$\begin{split} \langle P', S' | V_{(f)}^{\mu} | P, S \rangle &= \bar{U}(P', S') \bigg[\gamma^{\mu} F_{1}^{(f)}(Q^{2}) \\ &+ i \sigma^{\mu\nu} \frac{q_{\nu}}{2M_{N}} F_{2}^{(f)}(Q^{2}) \bigg] U(P, S), \\ V_{(f)}^{\mu} &= \bar{\psi}_{(f)} \gamma^{\mu} \psi_{(f)}, \end{split}$$

Physical charge density are derived from the Sachs Form factors

$$G_E(Q^2) = F_1(Q^2) - \frac{Q^2}{(2M_N)^2} F_2(Q^2),$$

$$G_M(Q^2) = F_1(Q^2) + F_2(Q^2).$$

Measure the moments of the charge distribution:

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$$< r^n > = \int_0^\infty r^{2+n} \rho(r) dr,$$

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Highest precision experiments

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Hydrogen



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Hydrogen





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Why re-measure the proton charge radius?

1S Lamb shift in hydrogen: $L_{1S}(r_p) = 8171.636(4) + 1.5645 \langle r_p^2 \rangle$ MHz



QED-test is limited by the uncertainty of the proton rms charge radius.

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QED corrections



QED at order α and α^2



Two-loop self-energy (1s)



V. A. Yerokhin, P. Indelicato, and V. M. Shabaev, Phys. rev. A 71, 040101(R) (2005). Mainz MITP Oct. 2013 _**↓**LKB

Two-loop self-energy (1s)

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$$\Delta E_{\text{SESE}} = m \left(\frac{\alpha}{\pi}\right)^2 (Z\alpha)^4 \{B_{40} + (Z\alpha)B_{50} + (Z\alpha)^2 \\ \times [L^3 B_{63} + L^2 B_{62} + L B_{61} + G_{\text{SESE}}^{\text{h.o.}}(Z)] \}$$



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The exotic way...



Lamb shift



Self-energy: The heavier the particle, the smaller (in relative term) it is



Hydrogen (electron) Effect of R: 6x10⁻¹¹



Vacuum Polarization: The closer the particle is, the stronger it is



Muonic Hydrogen (muon 207 times heavier than the electron) Effect of R: 1.7%



Challenges

- production of muonic hydrogen in 2S
- powerful triggerable 6µm laser
- small signal analysis

Aim : better determination of proton radius r_p



The muonic hydrogen experiment

Getting up close and personal with the proton!



Experimental set-up





muon beam apparatus

 $\pi \rightarrow \mu + \nu_{\mu}$

laser hut below concrete blocks

counting room





PSC solenoid,

H2 target, laser cavity, detectors 23

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 μp set up in $\pi E5$



A muon's Odyssey



A muon's Odyssey













Laser chain

MOPA TiSa laser

- •cw laser, frequency stabilized
 - •referenced to a stable FP cavity
 - •FP cavity calibrated with I2, Rb, Cs lines
 - •FP = N . FSR (free spectral range)
 - •FSR = 1497.344(6) MHz
- •cw TiSa frequency absolutely known to 30 MHz
- **Г**_{2P-2S} = **18.6** GHz
- •Seeded oscillator
- •TiSa = cw \rightarrow pulsed TiSa (frequency chirp \leq 100 MHz)
- •Multipass amplifier (2f- configuration) •gain=10



Laser chain : Raman cell



Laser chain : frequency calibration

FSR measured/controlled in cw with I₂ (1 ph abs), Cs (2 ph fluo), Rb (2 ph fluo), lines



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The laser hut





Ti:Sa and raman cell


Λ LKB

Laser chain : multipass cavity

\rightarrow illuminate at 6 µm all the muon stopping volume (5×15×190 mm³)



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1.5

0.5

2.5

3.5

ňΝ

μO

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target in the solenoid

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Example : FP 900 - 11 hrs meas.

- ≽ 400 µ-/s
- > 240 laser shot/s
- 860 000 laser shot/hour
- 1.56 million detector clicks
- 19600 clicks in the laser region
- expected 2-3 laser induced events/hour !



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Time spectra



New analysis: tacking into account more events



1.9 keV Ka x-ray must followed by the detection of an MeV-energy electron, but there are several detectors

Proton Structure from the Measurement of 2S-2P Transition Frequencies of Muonic Hydrogen, A. Antognini, F. Nez, K. Schuhmann et al. Science **339**, 417-420 (2013).

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 \rightarrow proton charge radius (~0.1%)



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Reanalysis 2012





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New resonance 2012

μ p ($2S_{1/2}(\text{F=0}) \rightarrow 2P_{3/2}(\text{F=1})$) at $\lambda = 5.5 \,\mu\text{m}$



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μP : ²S_{1/2}(F=1) - ²P_{3/2}(F=2) uncertainty budget

Statistics

uncertainty on position (fit)

541 MHz (~ 3 % of Γ_{nat})

618 MHz

 $\Delta v_{\text{experimental}}$ = 20 (1) GHz (Γ_{nat} = 18.6 GHz)

Sources :

 Laser frequency (H₂0 calibration, lines known to ~1 MHz) 	300 MHz
 AC and DC stark shift 	< 1 MHz
 Zeeman shift (5 Telsa) 	< 30 MHz
Doppler shift	< 1 MHz
Collisional shift	2 MHz

TOTAL UNCERTAINTY ON FREQUENCY

Broadening :

- 6 µm laser line width
- Doppler Broadening
- Collisional broadening

~ 2 GHz < 1 GHz 2.4 MHz

Updated: v (µp : $2S_{1/2}(F=1)-2P_{3/2}(F=2)$) <1 σ (12.5 ppm) Nature: v (µp : $2S_{1/2}(F=1)-2P_{3/2}(F=2)$) = 49 881.88 (76) GHz (16 ppm)

∕∕_lkb	μP: ² S _{1/2} (F=0) - ²	² P _{3/2} (F=1) u	ncertainty budget
Statistics • uncerta	s ainty on position (fit)		960 MHz
Sources Laser f AC and Zeema Dopple Collision 	: frequency (H ₂ 0 calibration) d DC stark shift in shift (5 Telsa) er shift onal shift		300 MHz < 1 MHz < 30 MHz < 1 MHz 2 MHz
TOTAL L	INCERTAINTY ON FREQUEN	CY	1006 MHz
 Broaden 6 µm la Dopple Collision 	ing : aser line width er Broadening onal broadening	~ 2 GHz < 1 GHz 2.4 MHz	

v (µp : $2S_{1/2}(F=0)$ - $2P_{3/2}(F=1)$) good agreement with the other (18.5ppm)

muonic deuterium : ²S_{1/2}(F=3/2) - ²P_{3/2}(F=5/2)

 $\mu d (2S_{1/2}(F=3/2) \rightarrow 2P_{3/2}(F=5/2)) 50815.491 \pm 0.815 GHz \text{ still preliminary}$



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muonic deuterium : ²S_{1/2}(F=3/2) - ²P_{3/2}(F=5/2)

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LKB muonic deuterium : ${}^{2}S_{1/2}(F=1/2) - {}^{2}P_{3/2}(F=3/2)$ and ${}^{2}S_{1/2}(F=1/2) - {}^{2}P_{3/2}(F=1/2)$









- 2010 CODATA value uses improved theory for hydrogen and Mainz electron-proton scattering is now at 6.9 σ mostly by a reduction of σ :
 - 0.8775 (59) fm 2010
 - 0.8768 (69) fm 2006
- We have analyzed in details the second transition that was observed, using an improved algorithm that correct for the variation of the laser pulse energy from shot to shot
- We take into account more events
- We have reanalyzed the first observed line using the improved method
- This lead to a slightly reduced error bar for the first transition, an accurate value of a second transition which allows to
 - Get a measurement of the magnetic moment distribution mean radius
 - An improved charge radius

µP theory



Main contributions to the μp Lamb shift

Discrepancy Polarisability Finite size Recoil

Muon self-energy + muon VP

Källen Sabry

One-loop VP







_**∕**_lkb

All-order: the charge distribution is included exactly in the wavefunction and in the operator, when relevant. Higher order Vacuum Polarization contribution included by numerical solution of the Dirac equation



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$$\left(c\boldsymbol{\alpha}\cdot\boldsymbol{p}+\beta\mu_{\mathrm{r}}c^{2}+V_{\mathrm{Nuc}}(\boldsymbol{r})\right)\Phi_{n\kappa\mu}(\boldsymbol{r})=\mathcal{E}_{n\kappa\mu}\Phi_{n\kappa\mu}(\boldsymbol{r}),$$

Bohr radius/particle mass:

$$V_{11}^{pn}(r) = -\frac{\alpha(Z\alpha)}{3\pi} \int_{1}^{\infty} dz \sqrt{z^{2}-1} \left(\frac{2}{z^{2}} + \frac{1}{z^{4}}\right) \frac{e^{-2m_{e}rz}}{r}$$

$$= -\frac{2\alpha(Z\alpha)}{3\pi} \frac{1}{r} \chi_{1} \left(\frac{2}{\lambda_{e}}\right)$$

$$= 1 \text{ in hydrogen: a}_{0} = 137\lambda_{e} = 60340 \text{ R}$$

$$= 1 \text{ in h-like } (Z = 52) : a = 2.65\lambda_{e}$$

 Fit to the Coulomb+Vacuum polarization contribution to 2s-2p_{1/2} separation, plus higher order corrections using Friar functional form

$$\begin{split} E_{2p_{1/2}}^{\text{Tot,fs}} - E_{2s_{1/2}}^{\text{Tot,fs}}(R) &= 206.046613695 - 5.226988678R^2 \\ &\quad + 0.03532068001R^3 \\ &\quad + 0.00006692700063R^4 \\ &\quad + 0.0002962967640R^2\log(R) \\ &\quad - 0.00004751147090R^4\log(R) \text{ meV}. \end{split}$$

Nonperturbative evaluation of some QED contributions to the muonic hydrogen n=2 Lamb shift and hyperfine structure, P. Indelicato. Phys. Rev. A 87, 022501 (2013).

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Other contributions for μP

#	Contribution	Reference	Value	Unc.
1	NR three-loop electron VP (Eq. (11), (15), (18) and (23))	[73]	0.00529	
2	Virtual Delbrück scattering (2:2)	[75, 78]	0.00115	0.00001
3	Light by light electron loop contribution (3:1)	[75, 78]	-0.00102	0.00001
4	Mixed self-energy vacuum polarization	[35, 84, 107]	-0.00254	
5	Hadronic vacuum polarization	[108-110]	0.01121	0.00044
6	Recoil contribution Eqs. (82) and (83)	[11, 36, 62, 85]	0.05747063	
7	Relativistic recoil of order $(Z\alpha)^5$ Eq. (84)	[11, 37-39, 41]	-0.04497053	
8	Relativistic Recoil of order $(Z\alpha)^6$ Eq. (86)	[11, 37]	0.0002475	
9	Recoil correction to VP of order m/M and $(m/M)^2$ in Eq. (4)	[72]	-0.001987	
10	Proton Self-energy	[35, 37, 41, 111]	-0.0108	0.0010
11	Proton polarization	[18, 37, 109, 112, 113]	0.0129	0.0040
12	Electron loop in the radiative photon of order $a^2(Z\alpha)^4$	[98, 114–116]	-0.00171	
13	Mixed electron and muon loops	[117]	0.00007	
14	Rad. Recoil corr. $\alpha(Z\alpha)^5$	[61]	0.000136	
15	Hadronic polarization $\alpha(Z\alpha)^5 m_r$	[109, 110]	0.000047	
16	Hadronic polarization in the radiative photon $\alpha^2(Z\alpha)^4m_r$	[109, 110]	-0.000015	
17	Polarization operator induced correction to nuclear polarizability $\alpha(Z\alpha)^5m_r$	[110]	0.00019	
18	Radiative photon induced correction to nuclear polarizability $\alpha(Z\alpha)^5 m_r$	[110]	-0.00001	
	Total		0.0256	0.0041



The role of the nuclear model

Dependence on the charge distribution





- Using the electronic density from Arrington et al. I get
 - Rp = 0.85035 fm Rm = 0.831 fm Rz = 1.0466 fm
- Dirac + Uehling vacuum polarization with this density:
 - E=201.2789 meV
- Dirac + Uehling vacuum polarization with same radius and other models
 - Gauss: E=201.2680 (-0.0109) meV
 - Dipole: E=201.2700 (-0.0089) meV
 - Uniform: E=201.2669 (-0.0120) meV
 - Fermi: E=201.2686 (-0.0102)
- Solving E_{Dipole}(R)=201.2789 meV gives:
 - R=0.84934 (-0.00101) fm

Proton polarization

- Several calculations
 - Rosenfelder (1999)



 $b E^{W_1(0,Q^2)} + 0016 - 0.0127(5) \text{ meV},$

$$\Delta E_{2s}^{\text{p.pol}} = -\frac{136 \pm 30}{n^3} \,\mu\text{eV} = -0.017 \pm 0.004 \,\text{meV}.$$

- Pachucki (1999) $\Delta E_{2s}^{p.pol} = -0.012 \pm 0.002 \text{ meV},$

- Martynenko (2006) $\Delta E_{2s}^{\text{p.pol}} = \Delta E^{\text{subt.}} + \Delta E^{\text{inel.}}$ = 0.0023 - 0.01613 meV = -0.0138(29) meV,
- Carlson and Vanderhaeghen (2011) $\Delta E_{2s}^{\text{p.pol}} = \Delta E^{\text{subt.}} + \Delta E^{\text{inel.}} + \Delta E^{\text{el.}}$
 - = 0.0053(19) 0.0127(5) 0.0295(13) meV= -0.0074(20) 0.0295(13) meV. $\Delta E_{2s}^{\text{p.pol}} = \Delta E^{\text{subt.}} + \Delta E^{\text{inel.}}$ $= \left[\delta E^{W_1(0,Q^2)} + \delta E^{\text{proton pole}} \right] + \delta E^{\text{continuum}}$

Could be wrong by 0.04 meV ——

Proton polarization

Several calculations

КΒ



 Proton polarisability contribution to the Lamb shift in muonic hydrogen at fourth order in chiral perturbation theory, M.C. Birse et J.A. McGovern. Eur. Phys. J. A 48, 1-9 (2012).

We calculate the amplitude TI for forward doubly virtual Compton scattering in heavy-baryon chiral perturbation theory, to fourth order in the chiral expansion and with the leading contribution of the $\gamma N\Delta$ form factor. This provides a model-independent expression for the amplitude in the low-momentum region, which is the dominant one for its contribution to the Lamb shift. It allows us to significantly reduce the theoretical uncertainty in the proton polarisability contributions to the Lamb shift in muonic hydrogen. We also stress the importance of consistency between the definitions of the Born and structure parts of the amplitude. Our result leaves no room for any effect large enough to explain the discrepancy between proton charge radii as determined from muonic and normal hydrogen.

Proton polarization








No radial excitations in low energy QCD. I. Diquarks and classification of mesons, T. Friedmann. The European Physical Journal C 73, 2298 (2013)

No radial excitations in low energy QCD. II. The shrinking radius of hadrons, T. Friedmann. The European Physical Journal C 73, 2299 (2013).



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Deuteron polarization (Friar, Pachucki)



multipole	Eqn.	ZRA	Ref. [5]	diff	%	sum-0	sum-[5]
leading C1	13	1.925	1.910	0.015	0.8	1.925	1.910
sub-leading C1	14	-0.037	-0.035	-0.002	7.0	1.888	1.875
C0	16	-0.042	-0.045	0.003	-7.6	1.846	1.830
retarded C1	17	0.137	0.151	-0.014	-9.4	1.983	1.981
C2	18	-0.061	-0.066	0.005	-7.9	1.922	1.915
M1	19	-0.011	-0.016	0.005	-34.0	1.912	1.899
$\langle r^3 \rangle_{(2)}^{pp}$ f.s.	15	0.030				1.942	
pn correl. f.s.	15	-0.023				1.920	
retarded C1 f.s.	17	0.021				1.941	
C0+ret-C1+C2		0.034	0.040	-0.006	-14.0		
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Deuteron polarization



Chen Ji, Nir Nevo Dinur, Sonia Bacca, Nir Barnea (arXiv:1307.6577)

TABLE I. Nuclear polarization contributions to the 2S-2P Lamb shift $\Delta E \text{ [meV]}$ in μD , compared to Pachucki [17].

	Ref. [17]	This work
$\delta^{(0)}_{D1}$	-1.910	-1.907
$\delta_L^{(0)}$	0.035	0.029
$\delta_T^{(0)}$		-0.012
$\delta_C^{(0)}$	0.261	0.259





Beyond Zemach

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$$\Delta E_{\rm M1}^{HFS} = A \frac{g\alpha}{2M_p} \int_0^\infty dr \frac{P_1(r)Q_2(r) + P_2(r)Q_1(r)}{r^2},$$

$$\Delta E^{BW} = -A \frac{g\alpha}{2M_p} \int_0^\infty dr_n r_n^2 \mu(r_n) \\ \times \int_0^{r_n} dr \frac{P_1(r)Q_2(r) + P_2(r)Q_1(r)}{r^2},$$

$$\begin{split} \Delta E_{\rm HFS}^{\rm Z} &= -\frac{2}{3} \left\langle S_p \cdot S_\mu \right\rangle \left| \phi_{\rm C}(0) \right|^2 \\ &\times \left(1 - 2\alpha m_\mu \int \rho(u) \mid u - r \mid \mu(r) du dr \right), \\ &= E_{\rm F} \left(1 - 2\alpha m_\mu \int \rho(u) \mid u - r \mid \mu(r) du dr \right), \\ \Delta E_{\rm HFS}^{\rm Z} &= E_{\rm F} \left(1 - 2\alpha m_\mu \left\langle r_{\rm Z} \right\rangle \right), \end{split}$$

Hyperfine structure



Fig. 10. Finite charge and magnetic moment distribution energy shift for the 2*s* state as a function of the charge *R* and Zemach radius R_Z for the Gaussian ($R_Z = 1.045$ fm) and exponential model, divided by R_Z . The lines correspond to the function in Eq. (90).

_**↓**∕_lkb

Hyperfine structure FS corrections

- $E_{\text{HFS}}^{2s}(R_Z, R) = 22.807995$ - 0.0022324349R² + 0.00072910794R³ - 0.000065912957R⁴ - 0.16034434R_Z - 0.00057179529RR_Z
 - $-0.00069518048R^2R_Z$
 - $-0.00018463878R^3R_Z$
 - $+ 0.0010566454R_Z^2$
 - $+ 0.00096830453RR_Z^2$
 - $+ 0.00037883473R^2R_Z^2$
 - $-\ 0.00048210961 R_Z^3$
 - $-0.00041573690RR_Z^3$
 - + $0.00018238754R_Z^4$ meV.

- $E_{\rm HFS}^{2s,VP}\left(R_Z,R\right) = 0.074369030 + 0.000074236132R^2$
 - $+ 0.00013277334R^3 8.0987285 \times 10^{-6}R^4$
 - $-0.0017880269R_Z 0.00017204505RR_Z$
 - $-0.00037499458R^2R_Z$
 - $-0.000070355379R^3R_Z$
 - $-0.00022093411R_Z^2 + 0.00035038656RR_Z^2$
 - $+ 0.00020554316R^2R_Z^2 + 0.00025100642R_Z^3$
 - 0.00017200435RR_z³
 - 0.000061266973R⁴_Z meV.



Full calculation beyond Zemach

Nonperturbative evaluation of some QED contributions to the muonic hydrogen n=2 Lamb shift and hyperfine structure, P. Indelicato. Phys. Rev. A **87**, 022501 (2013).







Would need to be evaluated as well

_**∕**_LKB

Results HFS

	#	Ref. [40]	Ref. [70]	This work
Fermi energy	1	22.8054	22.8054	
Dirac Energy (includes Breit corr.)	2			22.807995
Vacuum polarization corrections of orders α^5 , α^6 in 2nd-order	3	0.0746	0.07443	
perturbation theory ϵ_{VP1}				
All-order VP contribution to HFS, with finite magnetisation distribution	4			0.07244
finite extent of magnetisation density correction to the above	5		-0.00114	
Proton structure corr. of order a^5	6	-0.1518	-0.17108	-0.17173
Proton structure corrections of order α^6	7	-0.0017		
Electron vacuum polarization contribution+ proton structure corrections of order a6	8	-0.0026		
contribution of 1γ interaction of order a^6	9	0.0003	0.00037	0.00037
$\epsilon_{VP}2E_F$ (neglected in Ref. [40])	10		0.00056	0.00056
muon loop VP (part corresponding to ϵ_{VP} neglected in Ref. [40])	11		0.00091	0.00091
Hadronic Vac. Pol.	12	0.0005	0.0006	0.0006
Vertex (order a^5)	13		-0.00311	-0.00311
Vertex (order α^6) (only part with powers of $\ln(\alpha)$ - see Ref. [103])	14		-0.00017	-0.00017
Breit	15	0.0026	0.00258	
Muon anomalous magnetic moment correction of order a^5 , a^6	16	0.0266	0.02659	0.02659
Relativistic and radiative recoil corrections with	17	0.0018		
proton anomalous magnetic moment of order a^6				
One-loop electron vacuum polarization contribution of 1y interaction	18	0.0482	0.04818	0.04818
of orders a^5 , a^6 (ϵ_{VP2})				
finite extent of magnetisation density correction to the above	19		-0.00114	-0.00114
One-loop muon vacuum polarization contribution of 1γ interaction of order a^6	20	0.0004	0.00037	0.00037
Muon self energy+proton structure correction of order a^6	21	0.001		0.001
Vertex corrections+proton structure corrections of order a^6	22	-0.0018		-0.0018
"Iellyfish" diagram correction+ proton structure corrections of order α^6	23	0.0005		0.0005
Recoil correction Ref. [104]	24		0.02123	0.02123
Proton polarizability contribution of order a ⁵	25	0.0105		
Proton polarizability Ref. [104]	26		0.00801	0.00801
Weak interaction contribution	27	0.0003	0.00027	0.00027
Total		22.8148	22.8129	22.8111

Results

 Using the second line measured during the experiment we can improve the charge radius and get a value for the Zemach's radius.

```
E_{2p_{12}}^{F=2} - E_{2p_{12}}^{F=1}(R_Z, R) = 209.92451 - 5.2265012R^2
                                                                                E_{2p_{N2}}^{F=1} - E_{2s_{1/2}}^{F=0}(R_Z, R) = 229.66172 - 5.2286594R^2
                 + 0.035105381R^3
                                                                                                          +0.035967212R^{3}
                 + 0.000085386880R^4
                                                                                                          + 0.000011416693R^4
                 +1.5472388 \times 10^{-8} R^{5}
                                                                                                          - 0.12159928Rz - 0.00055788025RRz
                 -2.1359270 \times 10^{-9} R^{6}
                                                                                                          -0.00080263129R<sup>2</sup>Rz
                  + 0.040533092Rz
                  + 0.00018596008RRz
                                                                                                          -0.00019124562R^3R_Z
                  + 0.00026754376R<sup>2</sup>Rz
                                                                                                          + 0.00062678350R_7^2
                 + 0.000063748539R3Rz
                                                                                                          + 0.00098901832RR<sup>2</sup>
                 -0.00020892783Rz^2
                                                                                                          + 0.00043828342R<sup>2</sup>R<sup>2</sup>
                 -0.00032967277RRz^{2}
                 -0.00014609447R^2Rz^2
                                                                                                          - 0.00017332740R3
                  + 0.000057775798Rz<sup>3</sup>
                                                                                                          - 0.00044080593RR<sup>3</sup>
                  + 0.00014693531RRz^3
                                                                                                          + 0.000090840426R_{7}^{4}
                 -0.000030280142Rz^4
                                                                                                          + 0.00029629676R^2 \log(R)
                 + 0.00029629676R2 log(R)
                                                                                                          - 0.000047511471R4 log(R)
                 - 0.000047511471R4 log(R)
                                                                                                                     meV.
                           meV.
```

Simultaneous solution of these two equations with the two line energies Rc = 0.84100(63) fm and Rz=1.086(40) fm Assuming a dipole model, this gives Rm: 0.879(50) fm Mainz results: Rc = 0.879 fm, Rm = 0.777 fm and Rz = 1.047 fm

LKB

 We can extract the magnetic radius by using the dipole model to be consistent withe the calculations.

$$R_{Z}^{\text{Exp.}} = \frac{3R^{4} + 9R^{3}R_{M} + 11R^{2}R_{M}^{2} + 9RR_{M}^{3} + 3R_{M}^{4}}{2\sqrt{3}(R + R_{M})^{3}}$$

Simultaneous solution of the two equations with the two line energies Rc = 0.84100(63) fm and Rz=1.086(40) fm Assuming a dipole model, this gives Rm: 0.879(50) fm Mainz results: Rc = 0.879 fm, Rm = 0.777 fm and Rz = 1.047 fm

A magnetic radius larger than the charge radius leads to large discrepancies when applied to electron proton scattering data

√ _lkb	Summary of results: charge radius						
$\nu(2S_{1}^{F})$	$P_{2}^{=1} \rightarrow 2P_{3/2}^{F=2}) =$	49881.88	(76) GHz	R. Pohl et al., Nature 466, 213 (2010)			
$\nu(2S_{1/}^F)$	$P_{2}^{=0} \to 2P_{3/2}^{F=1}) =$	49881.35 54611.16	64) GHz (1.04) GHz	A. Antognini, F. Nez, K. Schuhmann, et al., Science 339 , 417 (2013).			
Proton	charge radius: <i>r</i> p	= 0.84089 μp theory:	(26) _{exp} (29) A. Antognini, F. Annals o	th = 0.84089 (39) fm . Kottmann, F. Biraben, et al., f Physics 331 , 127 (2013).			
	μр	2012 •		CODATA 2010			
	μр	2010 -	-	Mainz 2010			
	dispersion	-••	_	e-p scatt.			
Mainz MIT	0.8 0.82	0.84 pi	0.86 oton rms ch	0.88 0.9 narge radius r _p (fm)			

/LLKB Summary of results: Zemach radius 2S hyperfine splitting in $\mu{\rm P}$ is: $\Delta E_{\rm HFS} = 22.8089(51) \text{ meV}$ gives a proton Zemach radius $r_Z = \int d^3r \int d^3r' r \rho_E(r)\rho_M(r-r')$ $r_Z = 1.082(31)_{\rm exp}(20)_{\rm th} = 1.082(37) \, {\rm fm}$ μp theory: A. Antognini, F. Kottmann, F. Biraben, et al., Annals of Physics **331**, 127 (2013). µp 2012 Distler 2011 (e-p) Volotka 2005 (H) Friar 2005 (e-p) 0.96 0.98 1.02 1.04 1.06 1.081.14 1 1.1 1.12 proton Zemach radius r₇ (fm)

Summary of present status



High-precision measurement of the proton elastic form factor ratio at low, X. Zhan, et al Physics Letters B **705**, 59-64 (2011).







_**↓**↓LKB







Other measurements

How to get the radius from hydrogen and electron-proton scattering

_____LKB



Hydrogen+Deuterium



Analysis by F. Biraben

Hydrogen+Deuterium

- Needed: new measurements with independent systematic errors and get an independent Rydberg constant value:
 - 2S-4P in H (Garching)
 - 2S-nS,D in H (J. Flowers, NPL)
 - IS-3S (Garching, Paris)
 - transitions between Rydberg states of heavy H-like ion (NIST)
 - IS-2S and IS hfs in μe (A. Antognini, PSI)

_**∕**_LKB

Electron-Proton scattering



_∧_LKB

Electron-Proton scattering



M.O. Distler, Trento, 2012



Possible origin of the discrepancy

Systematic errors or new physics?

- Frequency shift: unlikely several redundant measurements at 708 nm (Fabry-Perot, two-photon transition in Rb) and 6µm (water lines)
- μ e⁻ p molecules or p p μ molecules. Not possible Why Three-Body Physics Does Not Solve the Proton-Radius Puzzle, J.-P. Karr and L. Hilico. Phys. Rev. Lett. 109, 103401 (2012).
- Experimental problems, e.g., a small air leak in the hydrogen target: we see characteristic μN and μO x-rays
 - Less than 1% of all created μP atoms see any N_2 molecules
 - Less than 0.1% of all μP in 2S state see any N_2 molecule during laser time
- µP theory: many checks, no effect seems large enough to explain a 0.3 meV energy shift, probably not even proton polarization (30 times too small)



- Electron-proton elastic scattering data analysis
- Under-estimated systematic errors in some hydrogen measurements
 - possible, but many different kind of experiments (microwave, 1s-3s, 2s-ns and 2s-nd)
- Proton structure
- New physics
 - Constraints:
 - g-2 of the muon (3 σ),
 - g-2 of the electron (Harvard)+fine structure constant from atomic recoil (LKB)
 - Hydrogen
 - Precision highly charged ions experiments at GSI (if long range interaction)
 - •

_____LKB



Reevaluation of the hadronic contributions to the muon g-2 and to $\lambda = M^{2}_{T}$, M. Davier, A. Hoecker, B. Malaescu and Z. Zhang. The European Physical Journal C - Particles and Fields **71**, 1-13 (2011).

Tenth-Order QED Contribution to the Electron g-2 and an Improved Value of the Fine Structure Constant, T. Aoyama, M.

Hayakawa, T. Kinoshita and M. Nio. Phys. Rev. Lett. 109, 111807 (2012).

Complete Tenth-Order QED Contribution to the Muon g-2, T. Aoyama, M. Hayakawa, T. Kinoshita and M. Nio. Phys. Rev. Lett. **109**, 111808 (2012).

_**∕**_LKB

Toward a resolution of the proton size puzzle, G.A. Miller, A.W. Thomas, J.D. Carroll and J. Rafelski. Phys. Rev. A 84, 020101 (2011).



0.31 meV for μ H and 9Hz for hydrogen (with model dependent parametrization)

FIG. 1: Direct two-photon exchange graph corresponding to the hitherto neglected term. The dashed line denotes the

lepton; the solid line, the n and the ellipse the off-shell I

We next seek values of the model parameters λ, b, ξ of $F(-q^2)$. chosen to reproduce the value of the energy shift, 0.31 meV, to resolve the puzzle. With $\xi = 0$, $\tilde{\Lambda} = \Lambda$, $\lambda/b^2 = 2.35/(79 \text{ MeV})^2$ is required. With this value, the corresponding change in the electronic H Lamb shift for the 2S state is about 9 Hz, significantly below the current uncertainty in both theory and experiment [3]. If ξ is changed substantially from 0 to 1 our value of λ would be increased by about 10%. Other tests of this effect could show sensitivity to the value of ξ or $\tilde{\Lambda}$.

No other work supports such a large effect



 Proton Size Anomaly, V. Barger, C.-W. Chiang, W.-Y. Keung et al. Phys. Rev. Lett. 106, 153001 (2011):

A measurement of the Lamb shift in muonic hydrogen yields a charge radius of the proton that is smaller than the CODATA value by about 5 standard deviations. We explore the possibility that new scalar, pseudoscalar, vector, and tensor flavor-conserving nonuniversal interactions may be responsible for the discrepancy. We consider exotic particles that, among leptons, couple preferentially to muons and mediate an attractive nucleon-muon interaction. We find that the many constraints from low energy data disfavor new spin-O, spin-1, and spin-2 particles as an explanation.

 Lamb shift in muonic hydrogen--II. Analysis of the discrepancy of theory and experiment, U.D. Jentschura. Annals of Physics 326, 516-533 (2011).
No unstable vector boson, no millicharged particles,

Mainz MITP Oct. 2013

- New physics and the proton radius problem, C.E. Carlson and B.C. Rislow. Physical Review D 86, 035013 (2012):
 - Particles that couple to muons and hadrons but not electrons
 - For the scalar-pseudoscalar model, masses between 100 to 200 MeV are not allowed.
 - For the vector model, masses below about 200 MeV are not allowed. The strength of the couplings for both models approach that of electrodynamics for particle masses of about 2 GeV.
 - New physics with fine-tuned couplings may be entertained as a possible explanation for the Lamb shift discrepancy.
- New Parity-Violating Muonic Forces and the Proton Charge Radius, B. Batell, D. McKeen and M. Pospelov. Phys. Rev. Lett. 107, 011803 (2011).
 - We identify a class of models with gauged right-handed muon number, which contains new vector and scalar force carriers at the100 MeV scale or lighter, that is consistent with observations.
 - Such forces would lead to an enhancement by several orders-of-magnitude of the parityviolating asymmetries in the scattering of low-energy muons on nuclei.

LKB

Muonic hydrogen and MeV forces, D. Tucker-Smith et I. Yavin. Physical Review D 83, 101702 (2011).

We explore the possibility that a new interaction between muons and protons is responsible for the discrepancy between the CODATA value of the proton-radius and the value deduced from the measurement of the Lamb shift in muonic hydrogen. We show that a new force carrier with roughly MeV-mass can account for the observed energyshift as well as the discrepancy in the muon anomalous magnetic moment. However, measurements in other systems constrain the couplings to electrons and neutrons to be suppressed relative to the couplings to muons and protons, which seems challenging from a theoretical point of view. One can nevertheless make predictions for energy shifts in muonic deuterium, muonic helium, and true muonium under the assumption that the new particle couples dominantly to muons and protons.

LKB

Muonic hydrogen and MeV forces, D. Tucker-Smith et I. Yavin. Physical Review D 83, 101702 (2011).



Nonidentical protons, T. Mart et A. Sulaksono. Phys. Rev. C 87, 025807 (2013).

We have calculated the proton charge radius by assuming that the real proton radius is not unique and the radii are randomly distributed in a certain range. This is performed by averaging the elastic electron-proton differential cross section over the form factor cutoff. By using a dipole form factor and fitting the middle value of the cutoff to the low-Q2 Mainz data, we found the lowest χ^2/N for a cutoff = 0.8203 ± 0.0003 GeV, which corresponds to a proton charge radius $r_E = 0.8333 \pm 0.0004$ fm. The result is compatible with the recent precision measurement of the Lamb shift in muonic hydrogen as well as recent calculations using more sophisticated techniques. Our result indicates that the relative variation of the form factor cutoff should be around 21.5%. Based on this result we have investigated effects of the nucleon radius variation on the symmetric nuclear matter (SNM) and the neutron star matter (NSM) by considering the excluded volume effect in our calculation. The mass-radius relation of a neutron star is found to be sensitive to this variation. The nucleon effective mass in the SNM and the equation of state of both the SNM and the NSM exhibit a similar sensitivity.



No radial excitations in low energy QCD. II. The shrinking radius of hadrons, T. Friedmann. The European Physical Journal C 73, 2299 (2013).

We discuss the implications of our prior results obtained in our companion paper (Eur. Phys. J. C (2013)). Inescapably, they lead to three laws governing the size of hadrons, including in particular protons and neutrons that make up the bulk of ordinary matter: (a) there are no radial excitations in low-energy QCD; (b) the size of a hadron is largest in its ground state; (c) the hadron's size shrinks when its orbital excitation increases. The second and third laws follow from the first law. It follows that the path from confinement to asymptotic freedom is a Regge trajectory. It also follows that the top quark is a free, albeit short-lived, quark.

Note added Nine months after this paper was originally posted to arXiv [32, 33], an experiment studying muonic hydrogen [34], repeated more recently [35], observed a smaller size of the proton than previously expected, consistent with our predictions. It is possible that this is a manifestation of our three laws, and may be a QCD, rather than QED, effect.

.КВ

PROTON RADIUS PUZZLE AND LARGE EXTRA DIMENSIONS, L.B. Wang et W.T. Ni. Modern Physics Letters A 28, 1350094 (2013).

We propose a theoretical scenario to solve the proton radius puzzle which recently arises from the muonic hydrogen experiment. In this framework, 4 + n dimensional theory is incorporated with modified gravity. The extra gravitational interaction between the proton and muon at very short range provides an energy shift which accounts for the discrepancy between spectroscopic results from muonic and electronic hydrogen experiments. Assuming the modified gravity is a small perturbation to the existing electromagnetic interaction, we find the puzzle can be solved with stringent constraint on the range of the new force. Our result not only provides a possible solution to the proton radius puzzle but also suggest a direction to test new physics at very small length scale.
Can Large Extra Dimensions Solve the Proton Radius Puzzle? Zhigang Li, Xuelei Chen (<u>http://arxiv.org/abs/1303.5146v1</u>)

The proton charge radius extracted from the recent muonic hydrogen spectroscopy [Antognini et al. 2013; Pohl et al. 2010] differs from the CODATA 2010 recommended value [Mohr et al. 2012] by more than 4%. This discrepancy, dubbed as the "Proton Radius Puzzle", is a big challenge to the Standard Model of particle physics, and has triggered a number of works on the quantum electrodynamic calculations recently. The proton radius puzzle may indicate the presence of an extra correction which enlarges the 2S-2P energy gap in muonic hydrogen. Here we explore the possibility of large extra dimensions which could modify the Newtonian gravity at small scales and lower the 2S state energy while leaving the 2P state nearly unchanged. We find that such effect could be produced by four or more large extra dimensions which are allowed by the current constraints from low energy physics.





Muonic Helium: experiment set up October 8th, 2013

Muonic He spectroscopy



improve He spectroscopy

Muonic He spectroscopy





Improve statistics...





Moving in on October 3rd beam time until December 19th Mainz MITP Oct. 2013 16% more from the beam time: reliquefying He Better disk laser Much more intensity (no Raman shift)

Conclusions

- We have performed a 12.5 ppm measurement of the Lamb-shift in muonic hydrogen
- The deduced proton radius using a Dipole model is 6.9 standard deviations away from the hydrogen and electron-proton elastic scattering data
- Better modeling of the proton form-factor and polarization required to confirm or reduce the disagreement
- Experiment confirmed with 2nd μH line
- 3 µD lines observed and being analyzed
- No explanation of the discrepancy yet, but possibilities
 - QCD
 - Problems with hydrogen experiments
 - New physics
- Muonic He in 2013 (check of theory, different laser wavelength-in the red) predictions of measurable effects from new physics!!



CREMA 2011

