

Theories of the Explosive Death of Massive Stars

Adam Burrows, Eli Livne, Luc Dessart, Christian Ott
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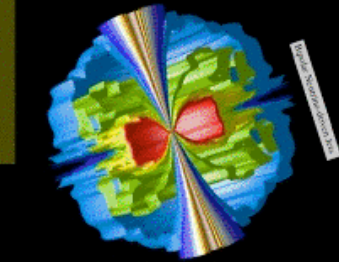
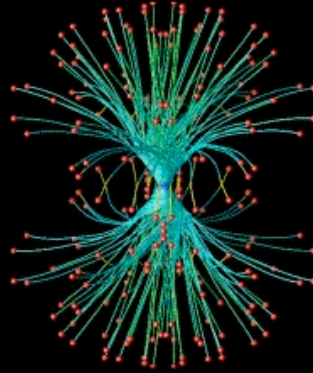
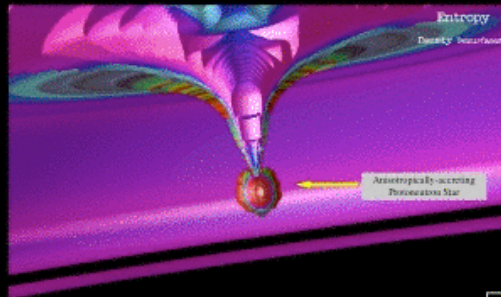
NSF

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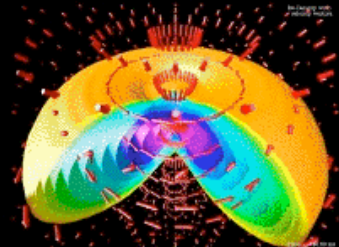
Multi-Dimensional Core-Collapse
Simulations: Explosion Mechanisms

(A. Burrows, L. Dessart, E. Livne, C. Ott, I. Hubeny, & J. Murphy)

Core-Oscillation - Acoustic Mechanism



Accretion-Induced Collapse of a White Dwarf



2 1/2-D Multi-Group Radiation Magneto-Hydrodynamic Capability:
VULCAN

Many New Simulation Results

New BETHE Code Development: Multi-D Neutrino Mechanism

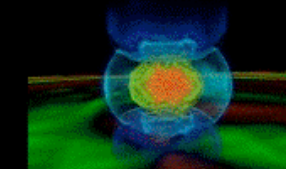
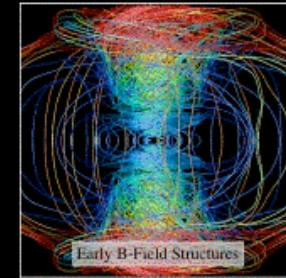
BETHE: Hydro

- Compatible Arbitrary-Lagrangian-Eulerian (ALE) Hydrodynamics for Unstructured Grids using the Support Operator Method
- 2nd-order in space & time
- 2nd-order bound- and sign-preserving Remap for arbitrary polygonal grids
- Arbitrary moving grid
- General EOS
- Iterative Poisson Gravity Solver
- Also discretized using Support Operator Method
- Multi-grid preconditioner, GMRES acceleration

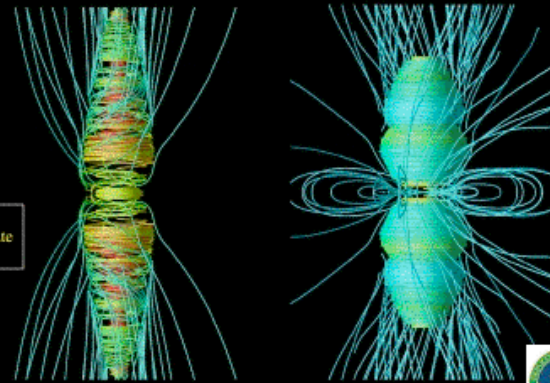
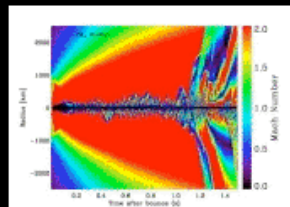
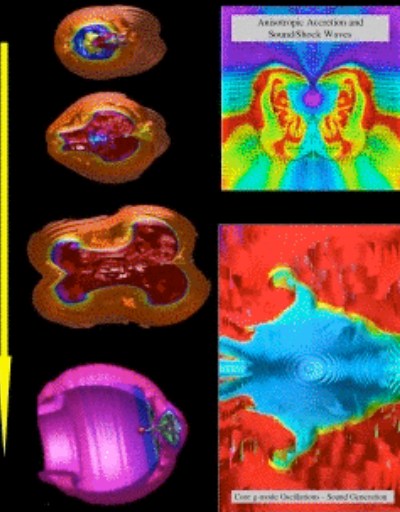
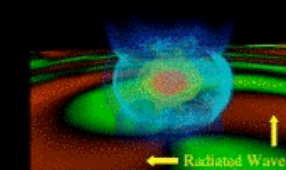
BETHE: Transport

Motivation: a need for a fast and efficient multi-D transport solver for supernovae and other astrophysical simulations

- Full transport
- Time-dependent, implicit
- 2 1/2 D + 2D (axisymmetric + rotation)
- All terms up to $O(v/c)$ included
- Multi-group, Multi-angle
- Anisotropic scattering
- Inelastic scattering
- Hubeny & Burrows 2007

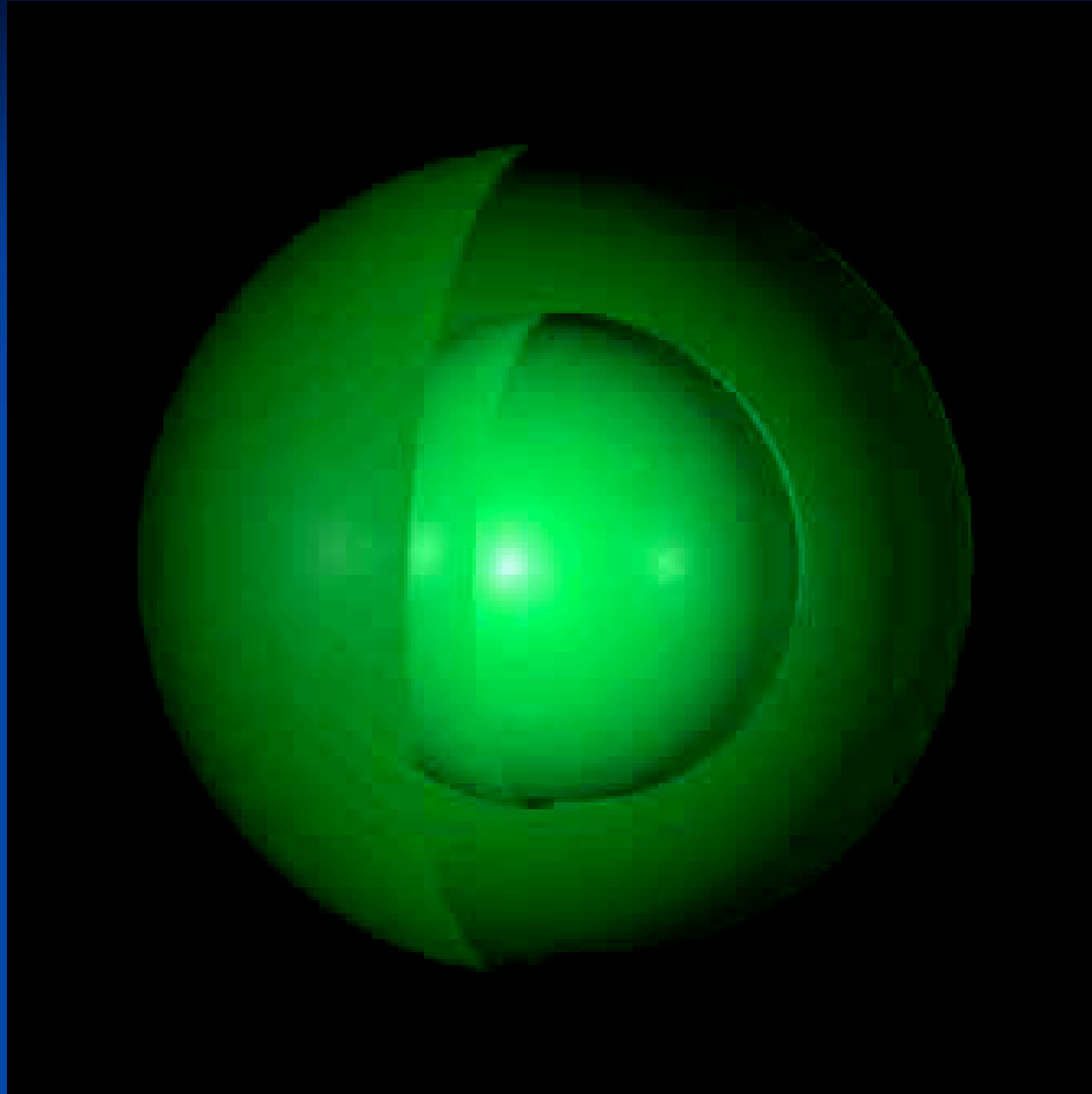


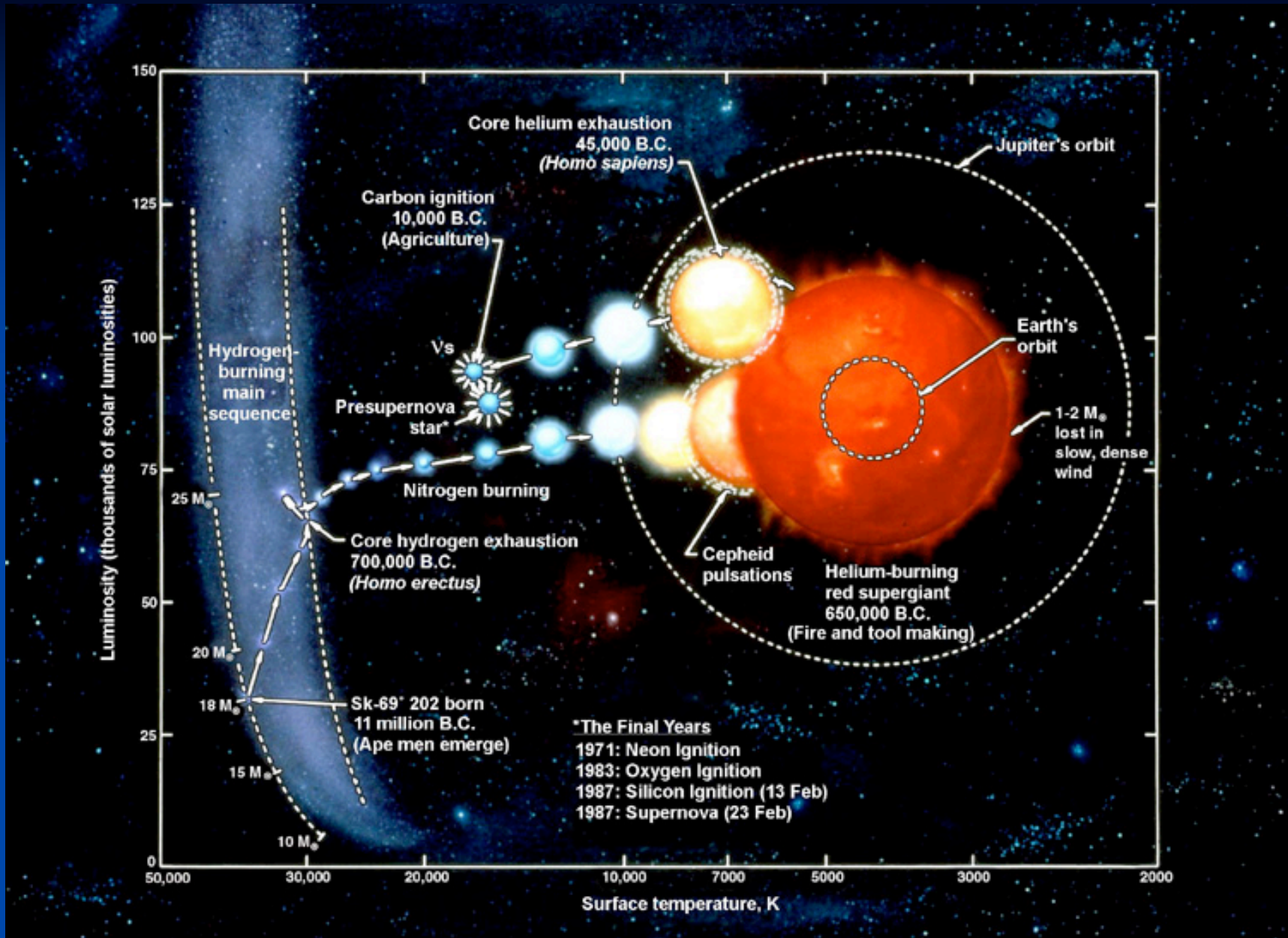
3D General-Relativistic Rotational Collapse:
 Gravitational Radiation



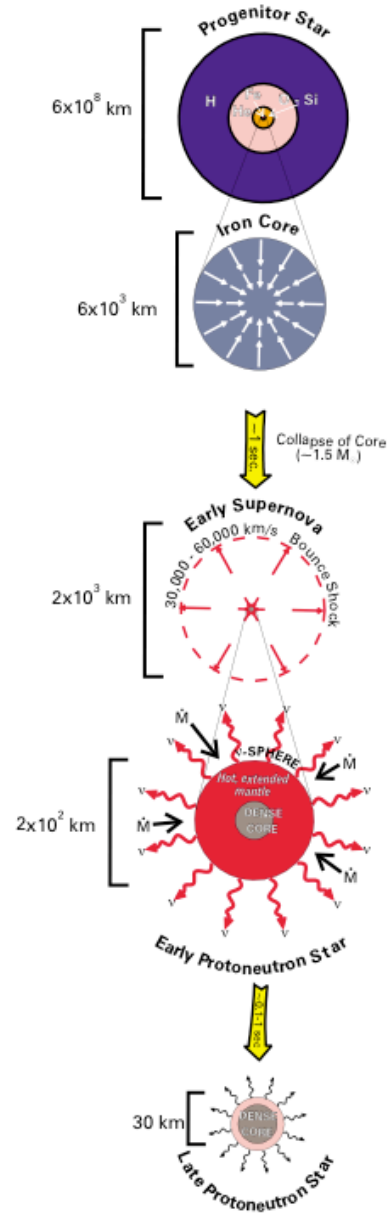
Magneto-Rotational Jet Mechanism

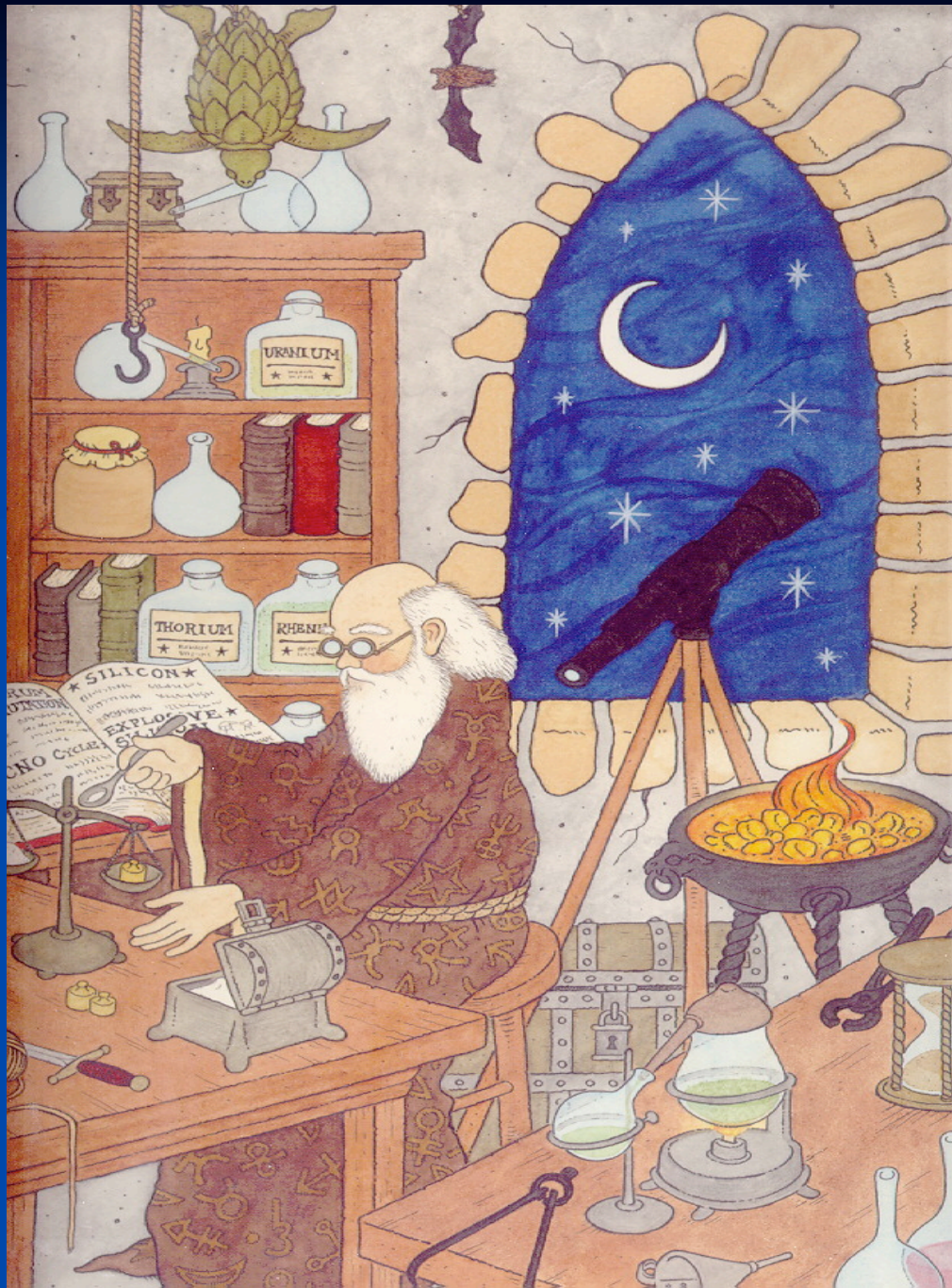
Onion Skin Structure: The Mote in the Eye of the Storm



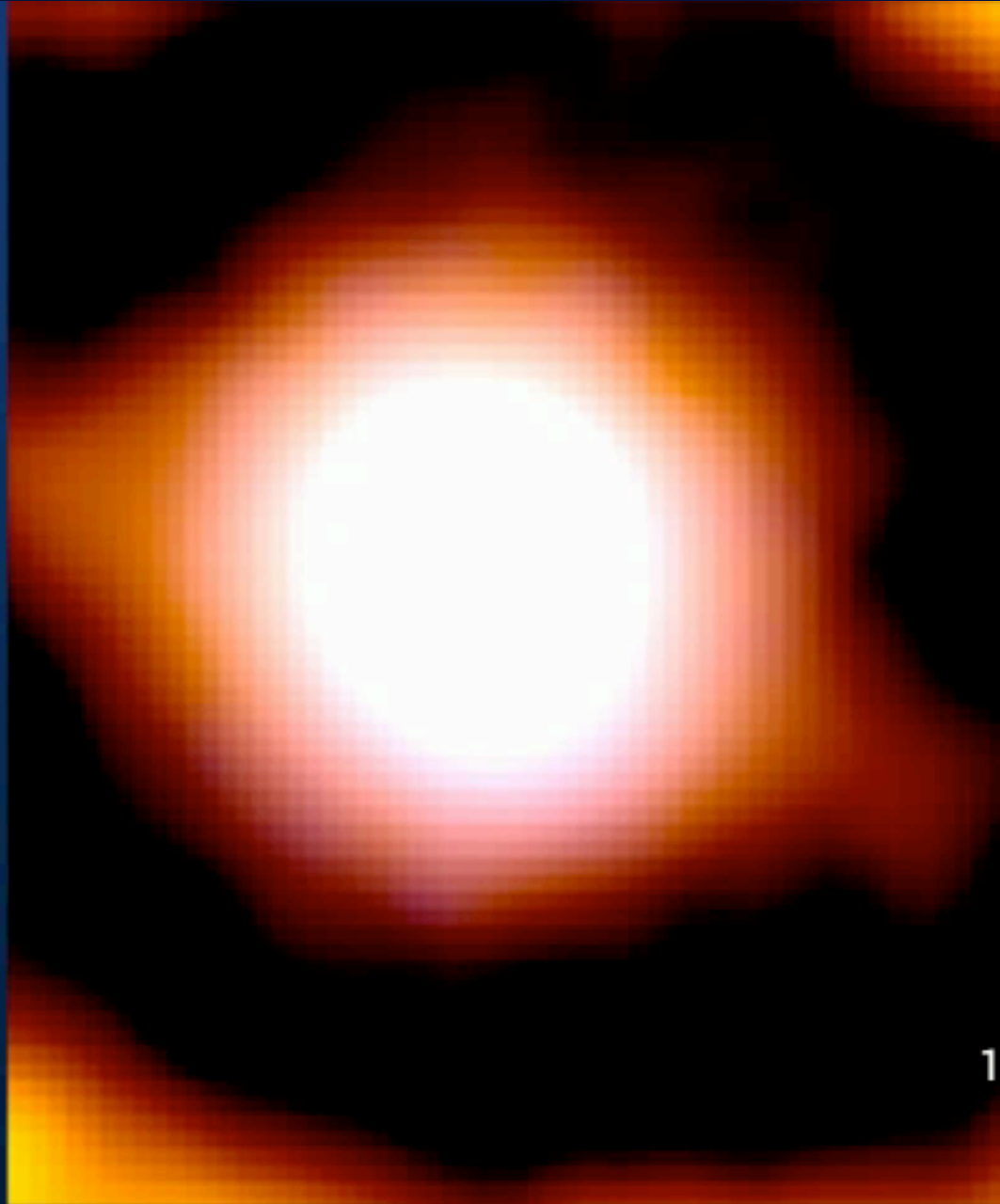


Courtesy of Tom Weaver



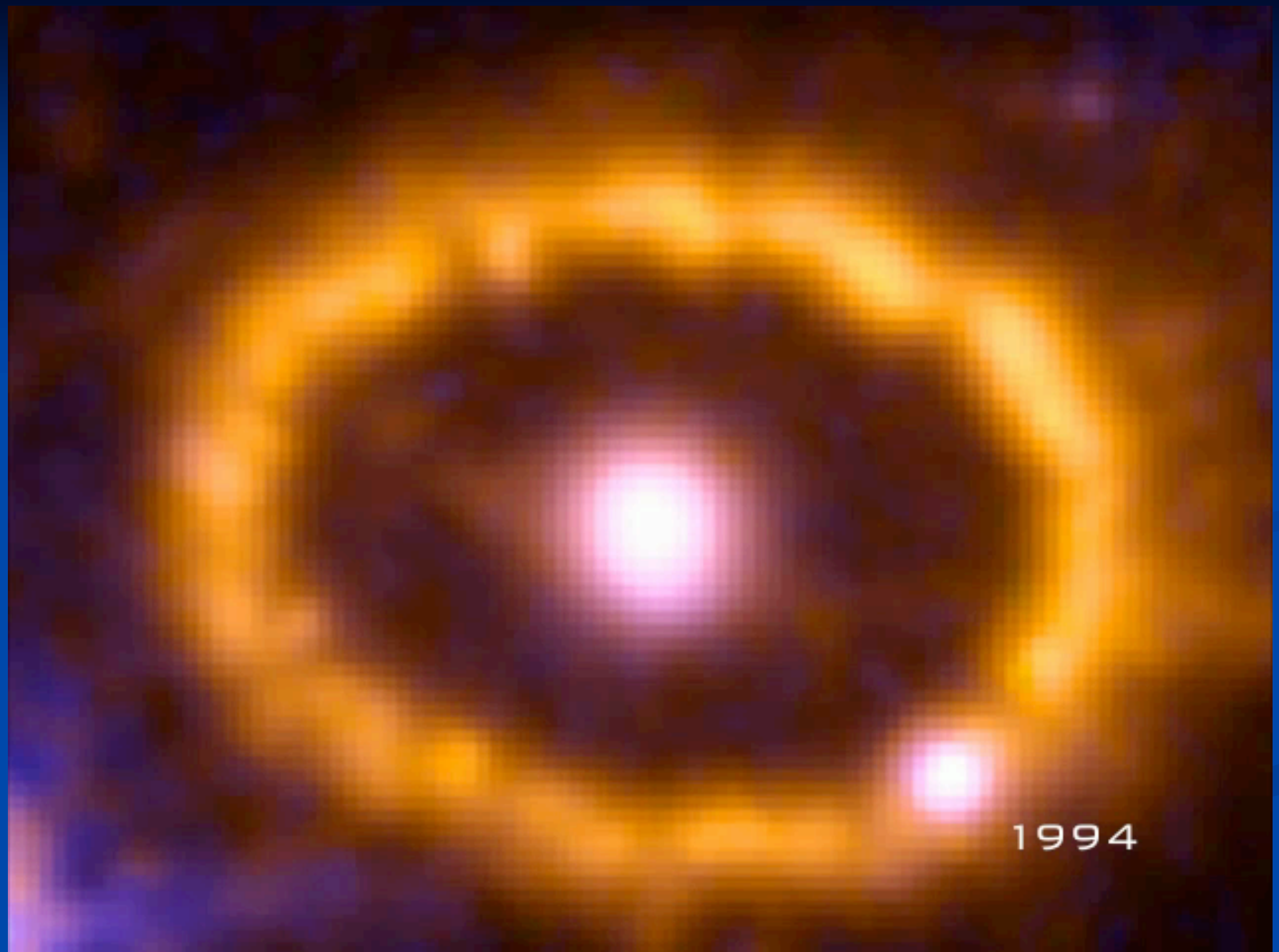


SN1987a (Pete Challis)



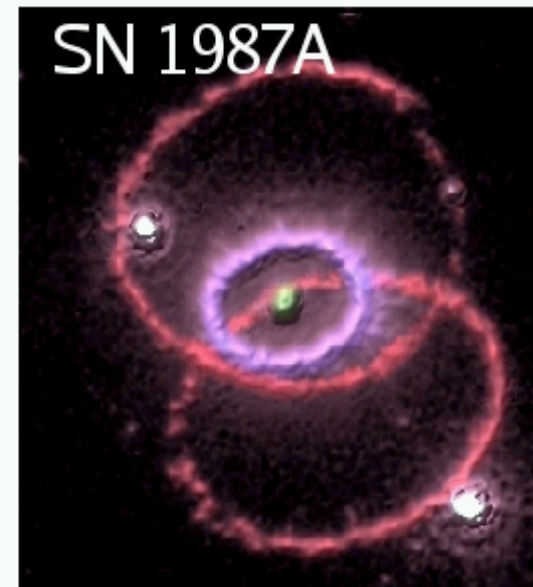
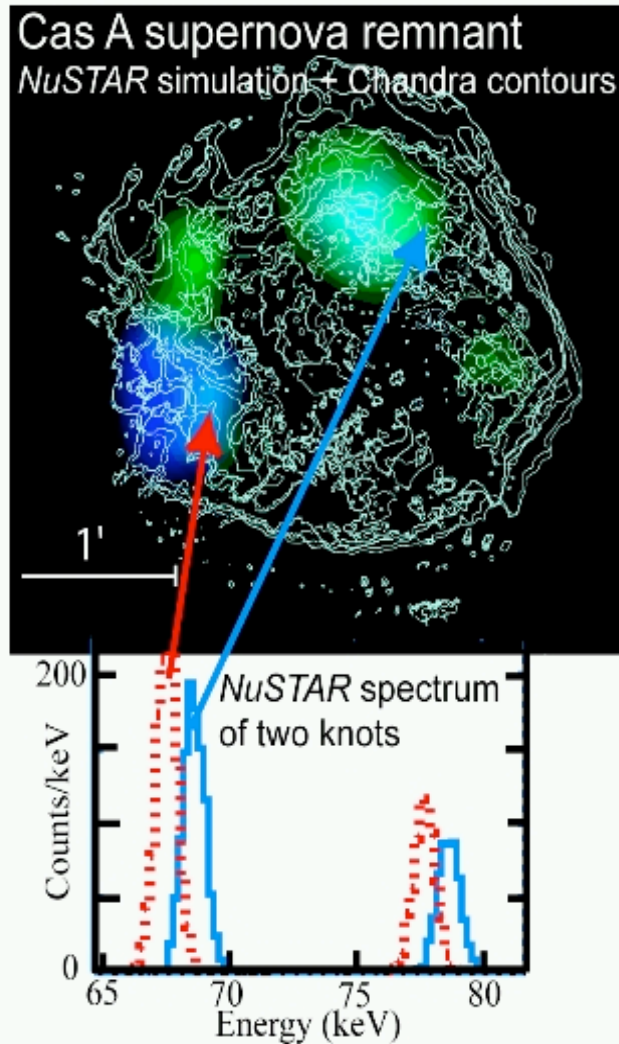
1994

SN1987a (Pete Challis)



1994

NuSTAR will map the remnants of recent supernova explosions, testing theories of where the elements are born



NuSTAR will measure and map the ^{44}Ti lines at 68 and 78 keV in historic remnants:
Tycho, Kepler, Cas A and SN1987A

Important Questions in Supernova Theory

- Mechanism of explosion?
- Pulsar Kicks (proper motions)?
- Nucleosynthesis: Nickel, etc. Yields?
- R-process site?
- Blast Morphology (and polarization)?
- Pulsar Spins?
- Pulsar / AXP / Magnetar B-fields?
- Black Hole formation?
- Systematics with progenitor (and role of rotation / magnetic fields)?
- Connection with GRBs and Hypernovae?

Mechanisms of Explosion

- **Direct Hydrodynamic Mechanism:** always fails?
- **Neutrino-Driven Wind Mechanism, ~1D** (Burrows 1987)
Lowest-mass massive stars, ~spherical (e.g., 8.8 solar masses, [Kitaura et al. 2006](#))
- **SASI-aided (Blondin et al. 2003) Neutrino-Driven Wind Mechanism, 2D** (e.g., 11.2 solar masses, [Buras et al. 2006](#))
- **Neutrino-Driven Jet/Wind Mechanism, Rapidly rotating AIC of White Dwarf** ([Dessart et al. 2006](#))
- **Acoustic Power Mechanism** (after delay), all progenitors explode ([Burrows et al. 2006, 2007a](#))
- Nuclear-burning aided? ([Mezzacappa et al. 2006](#))
- **MHD Jet Explosions** (e.g., [Burrows et al. 2007b](#))
- The **Key feature** of almost all mechanisms is the **Breaking of Spherical Symmetry**

Multi-D: Simultaneous Explosion and Accretion is the Key?

- **Neutrino Mechanism:** Anisotropic $l=1$ explosion --> lower ram pressure at head, larger neutrino heating region, while accretion elsewhere maintains neutrino luminosity to drive the explosion
- **MHD-Rapid rotation:** Explosion along poles, accretion of free rotational energy at equator (engine)
- **Acoustic Mechanism:** Explosion in one direction, accretion funnels from another, powering oscillation to maintain acoustic power

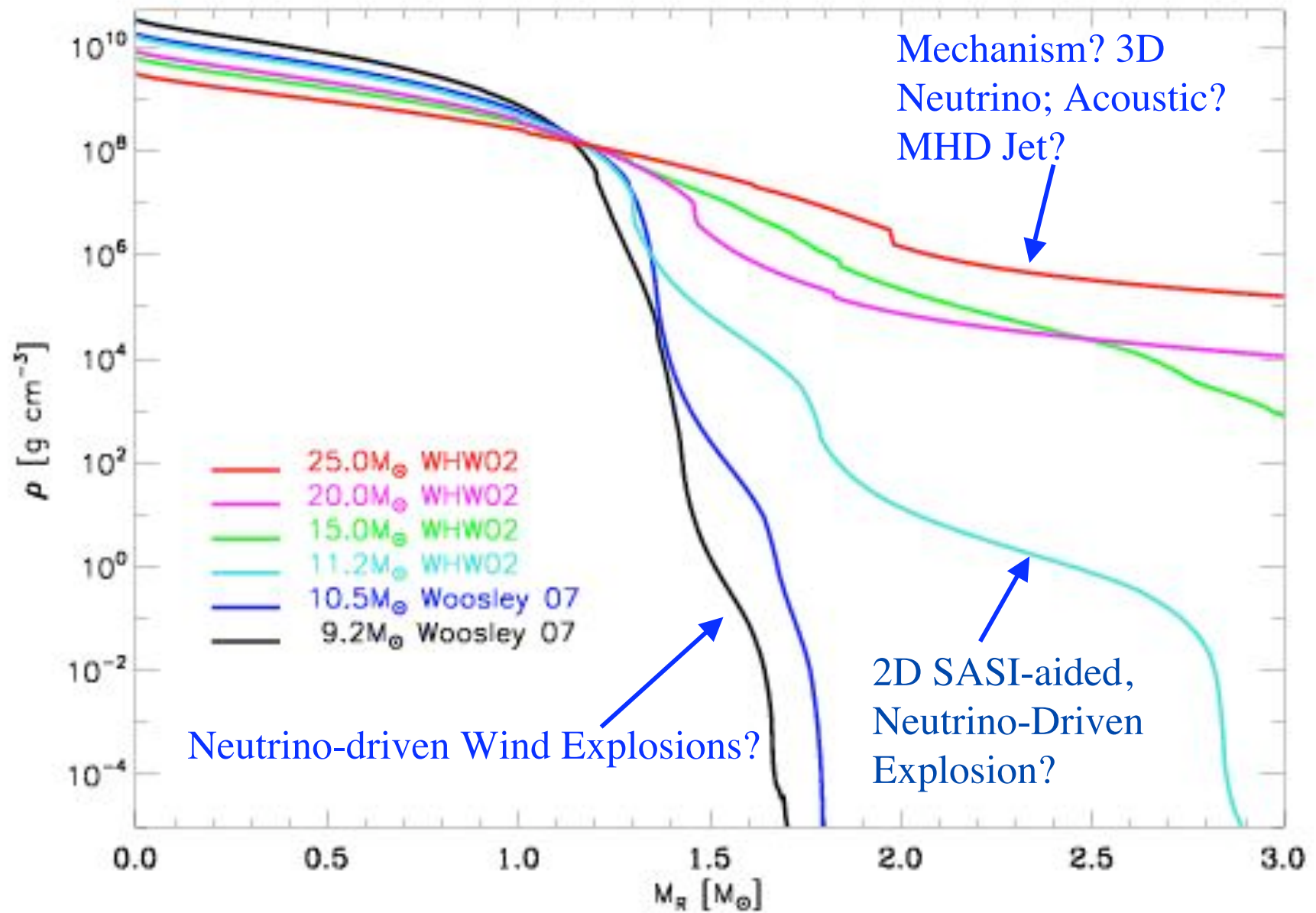
Issues/Problems

- Neutrino-driven wind explosions are “under-energetic”: ~0.05 to 0.2 **Bethes**, or don't work (in 2D): What of $M > \sim 12$ solar masses?
- **3D** effects may be needed to save the day for the neutrino mechanism for most progenitors and to achieve ~1 Bethe energies (last chance?); but note **Janka's 15 solar mass model**; **Better and Multi-D Neutrino Transport?**
- **Long delay** for Core-oscillation/ Acoustic mechanism: Does something else precede it? Can the core modes achieve the required **amplitudes**?
- MHD Jets: **Rapid Rotation** necessary

VULCAN/2D Multi-Group, Multi-Angle, Time-dependent Boltzmann/Hydro (6D)

- Arbitrary Lagrangian-Eulerian (ALE); remapping
- 6 - dimensional (1(time) + 2(space) + 2(angles) + 1(energy-group))
- Moving Mesh, Arbitrary Grid; Core motion (kicks?)
- 2D multi-group, multi-angle, S_n (~150 angles), time-dependent, implicit transport (still slow)
- 2D MGFLD, rotating version (quite fast)
- Poisson gravity solver
- Axially-symmetric; Rotation
- MHD version ("2.5D") - $\text{div } \mathbf{B} = 0$ to machine accuracy; torques
- Flux-conservative; smooth matching to diffusion limit
- Velocity-dependent terms: advection included (Df/dt), but not yet Doppler/Aberation terms
- Parallelized in energy groups; almost perfect parallelism
- Energy redistribution: explicit
- New Implicit Hydro version
- Livne, Burrows et al. (2004,2007)
- Burrows et al. (2006,2007), Ott et al. (2005); Dessart et al. 2005ab

Density Profiles of Supernova Progenitor Cores



**Neutrino-Driven
Wind Explosions:
Low Mass and AIC**

Current Status of the Neutrino Mechanism

- **Spherically-symmetric neutrino mechanism** might work for O/Ne/Mg cores (e.g., 8.8-solar-mass model: [Kitaura et al. 2006](#)), powered by neutrino-driven wind, but underenergetic: $\sim 10^{50}$ ergs
- 11.2-solar-mass model of WHW (2002) might explode by the **convective/SASI (2D) neutrino-driven mechanism** ([Buras et al. 2006](#)), aided by density cliff, but underenergetic: $>10^{49}$ ergs (mantle binding?), other progenitors very problematic (fizzle, but 3D??)
- **Accretion-Induced Collapse (AIC)**: neutrino-driven jet/wind mechanism; underenergetic ($\sim \text{few} \times 10^{50}$ ergs) as well ([Dessart et al. 2006](#))
- **Note**: Janka's recent 15 solar mass model? Neutrino-driven, long timescale (580 ms)
- **3D may be needed to explode other/most progenitors**

8.8-Solar mass Progenitor of Nomoto: Neutrino-driven Wind Explosion

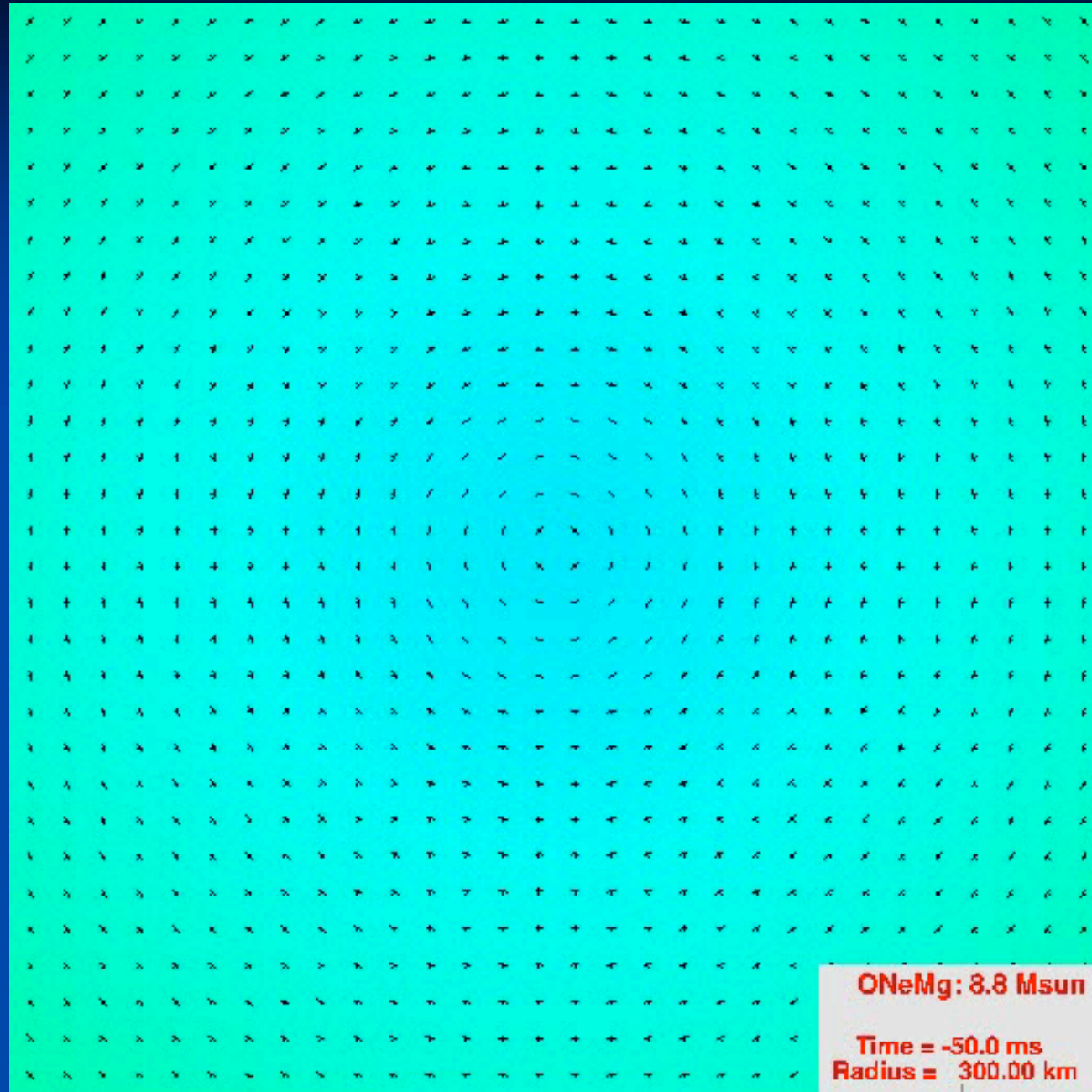
First shown
by Kitaura et
al. 2006

NOTE
WIND
THAT
FOLLOWS:

TWO
SHOCKS!

Dessart,
Burrows et
al. 2007;

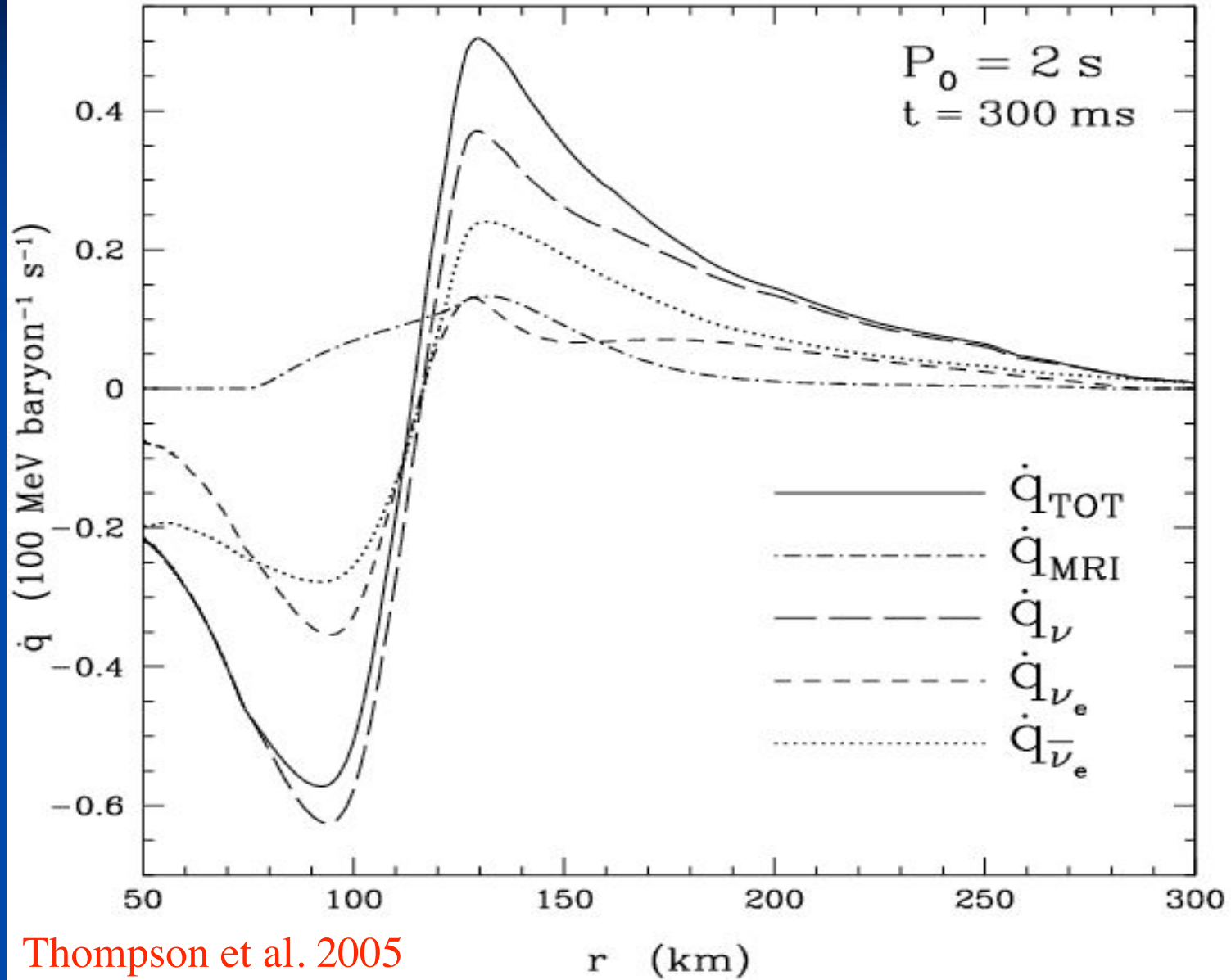
Burrows
1987



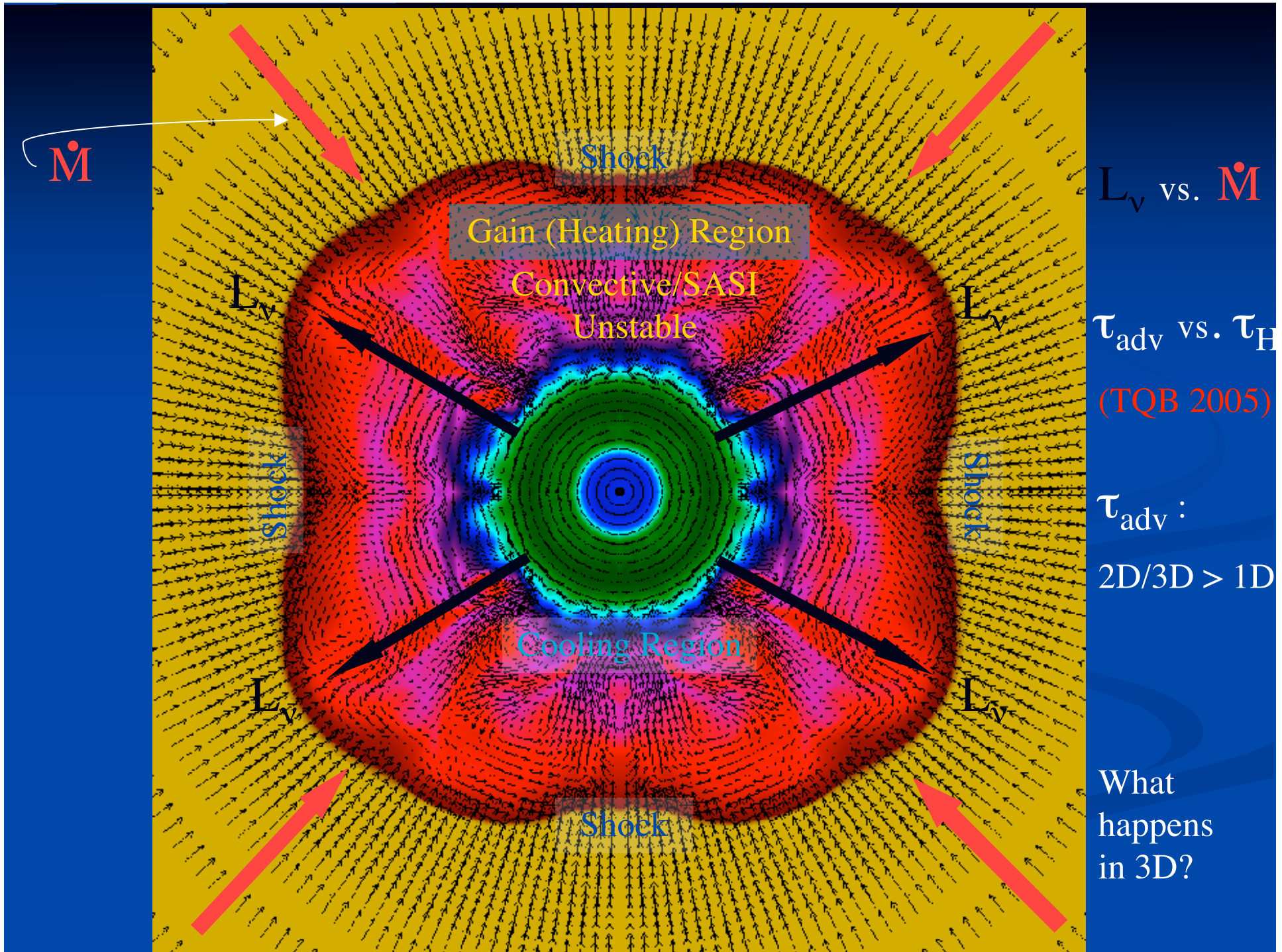
1) What is the Essence of the
Neutrino Mechanism

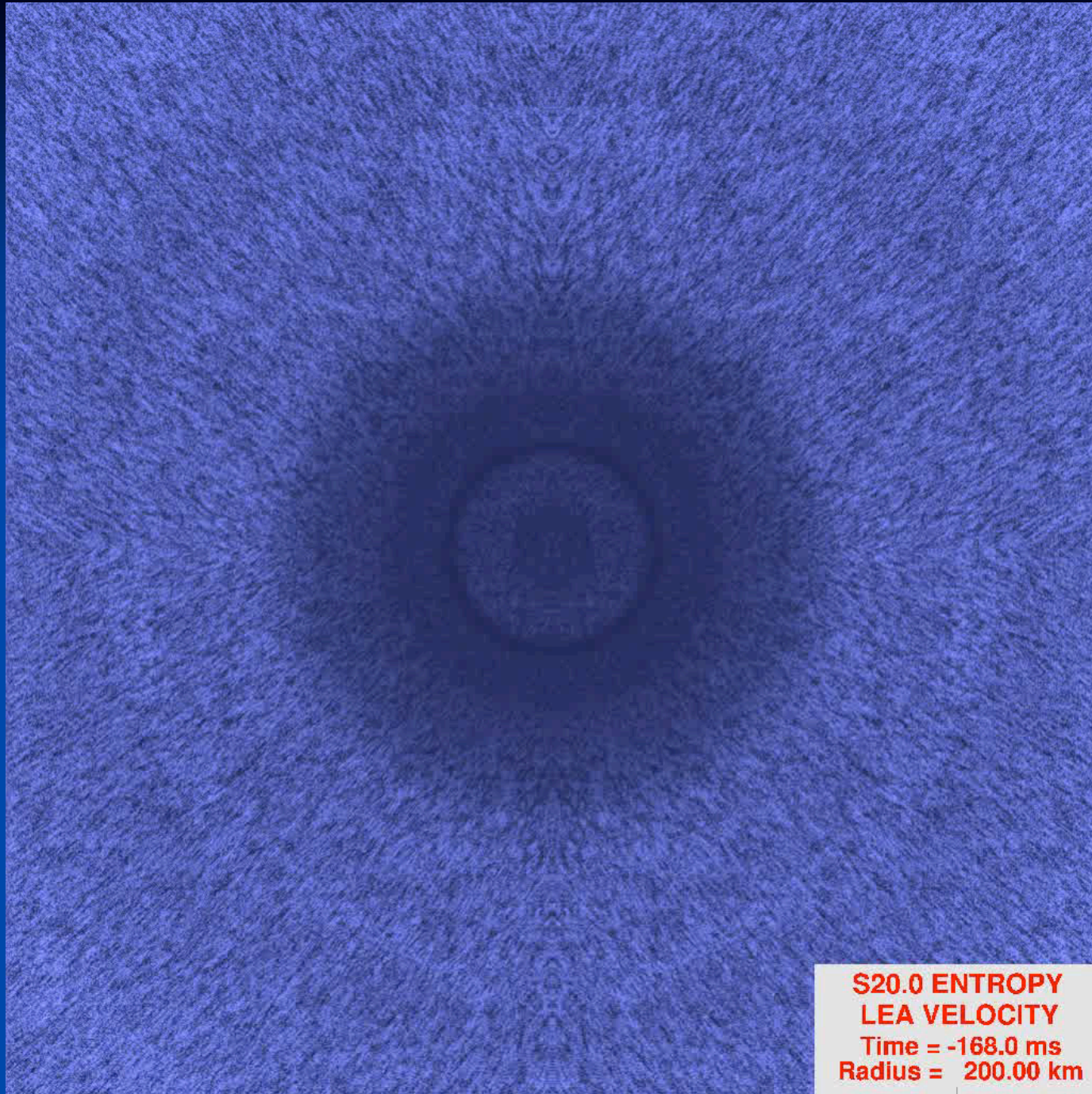
2) How can it “be made” to
work?

Heating and Cooling; The Effect of an Extra Source



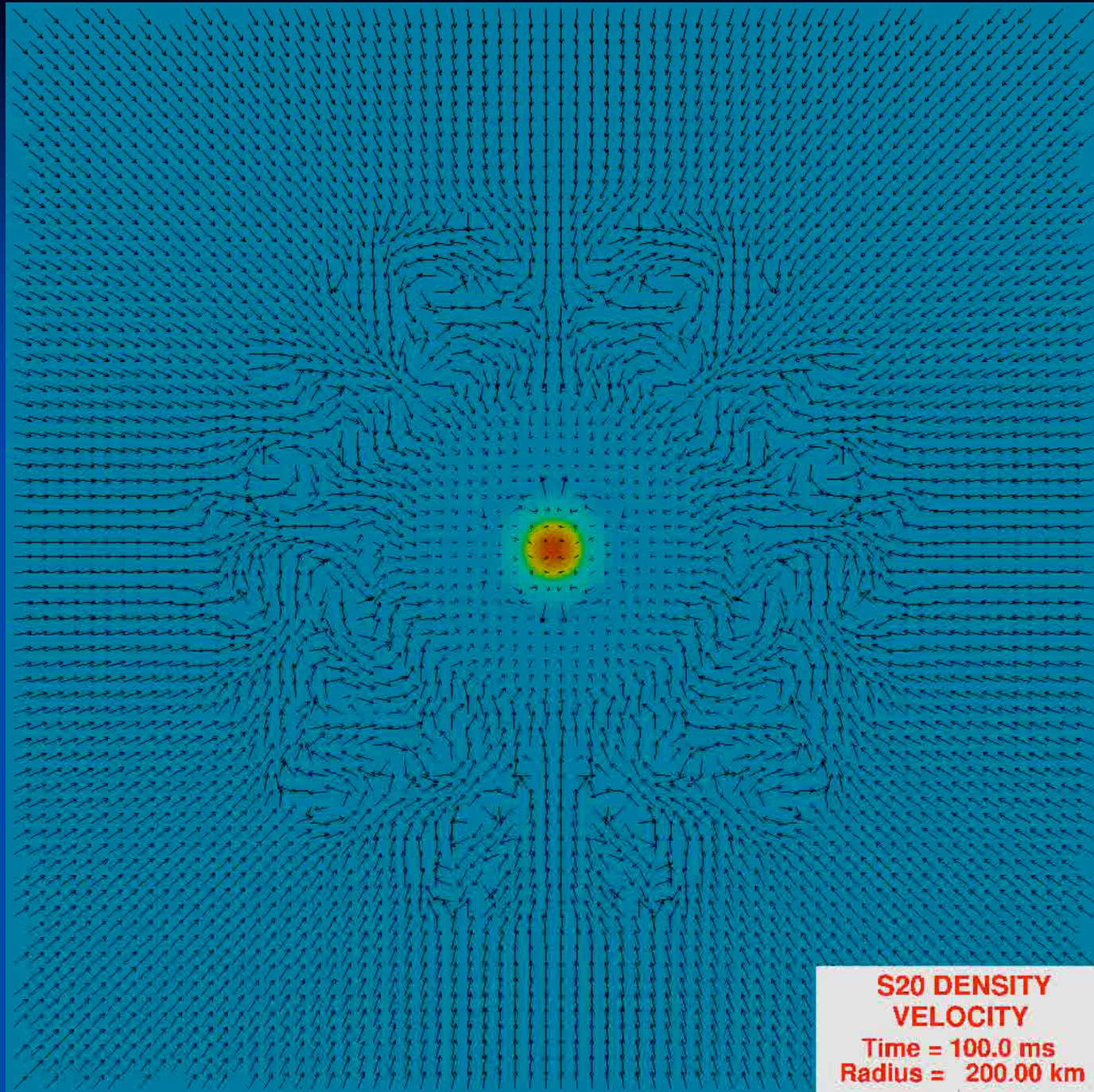
Thompson et al. 2005





S20.0 ENTROPY
LEA VELOCITY
Time = -168.0 ms
Radius = 200.00 km

But,
in
3D?



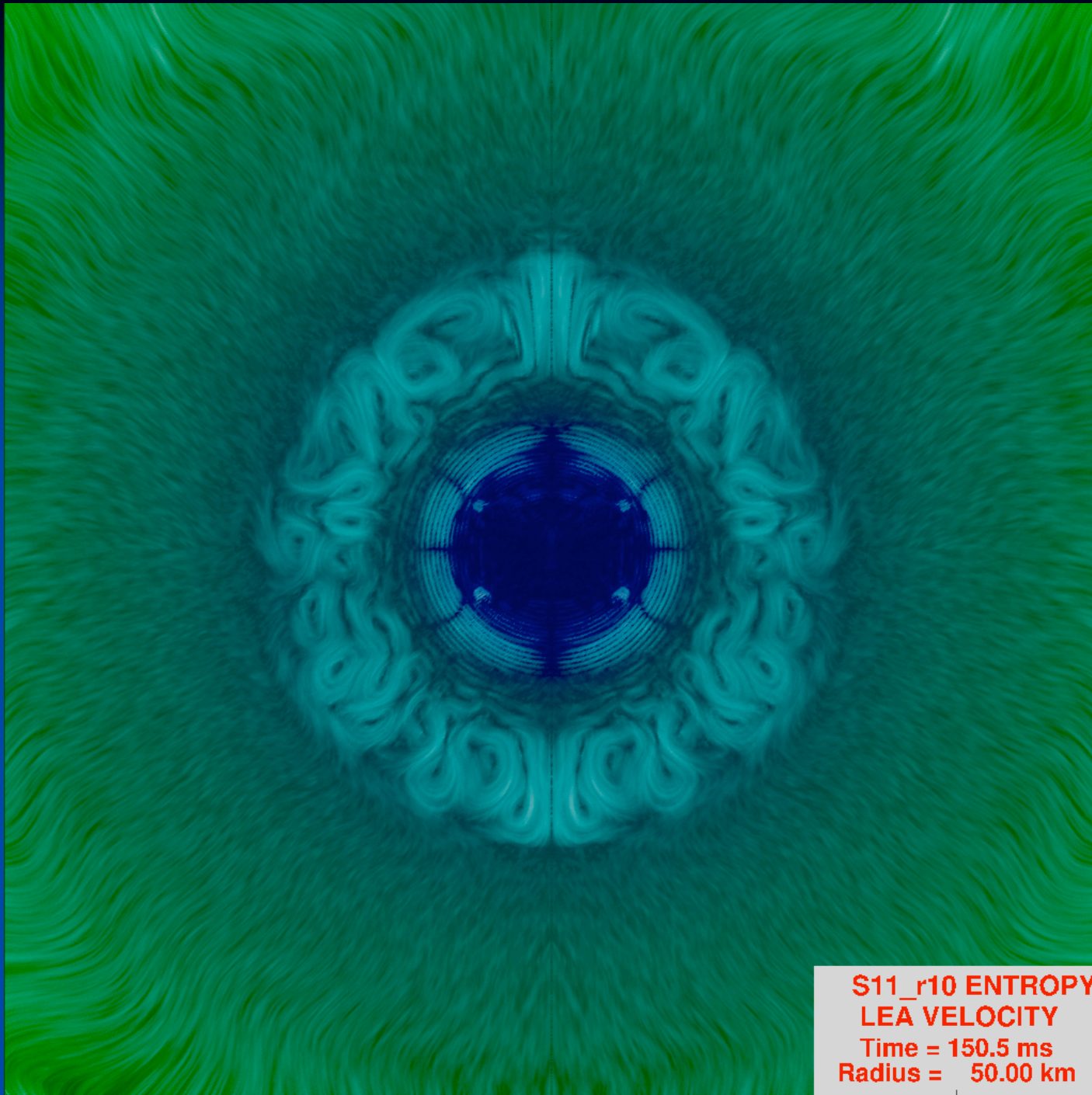
“Protonneutron Star Convection”

Ledoux (S/Y_e ?) and/or Doubly-Diffusive Convection?

Can it Boost the Driving Neutrino Luminosities?

(Wilson & Mayle 1988; Burrows 1987)

New study by Dessart et al. 2005

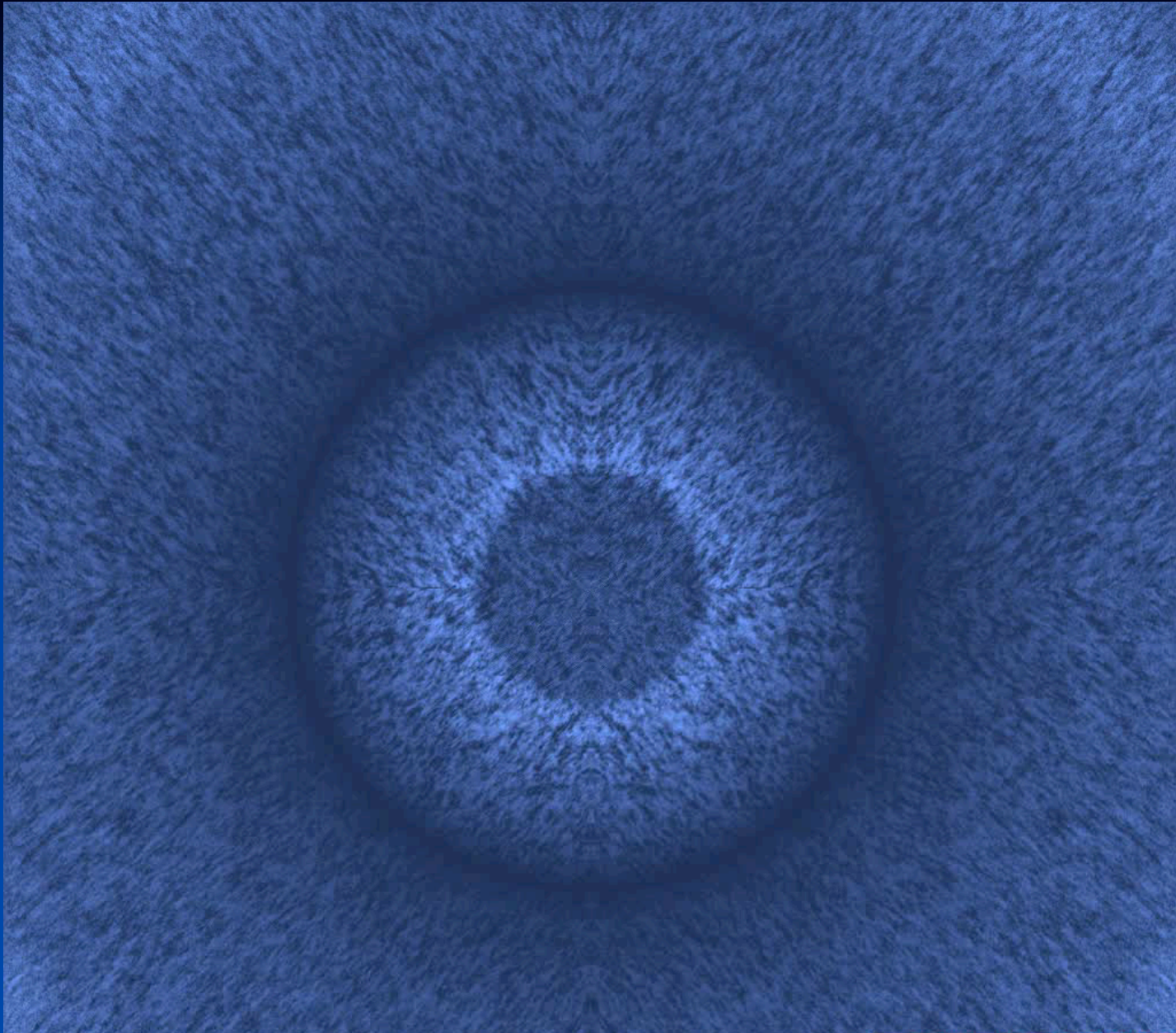


S11_r10 ENTROPY

LEA VELOCITY

Time = 150.5 ms

Radius = 50.00 km



S11_r10 ENTROPY
LEA VELOCITY
Time = -235.0 ms
Radius = 75.00 km
Frame No = 00000

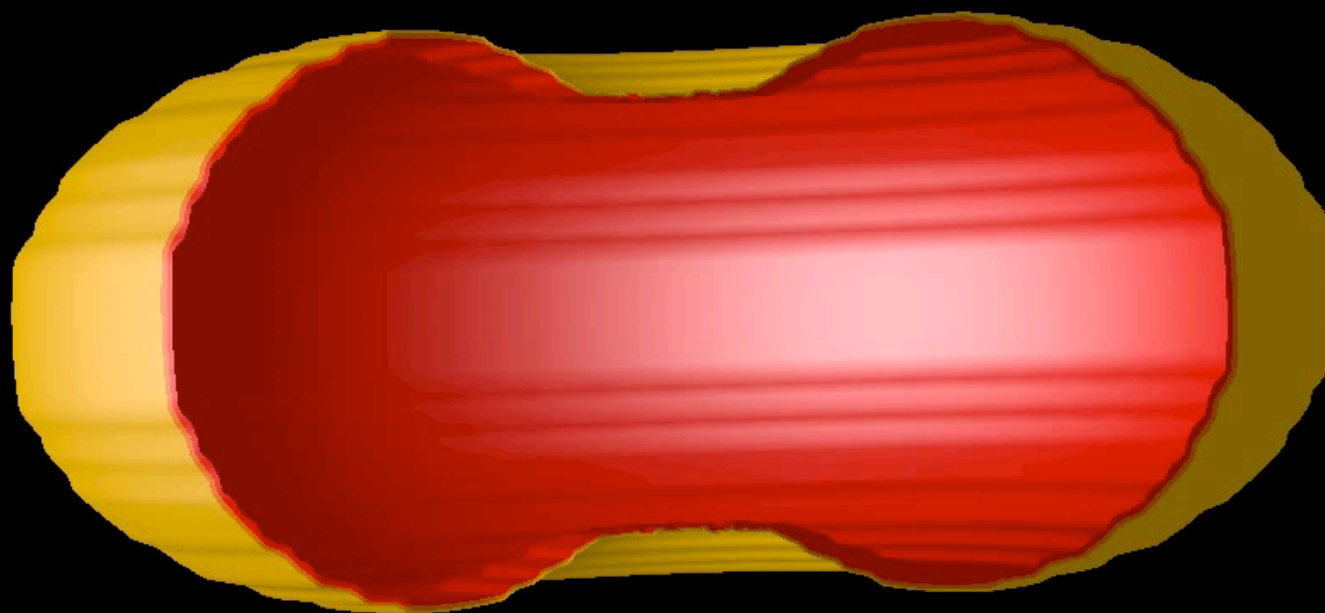
Accretion-Induced Collapse of O-Ne-Mg White Dwarfs

Dessart, Burrows, Ott, Livne, Yoon, & Langer 2006

Rapid Rotation!

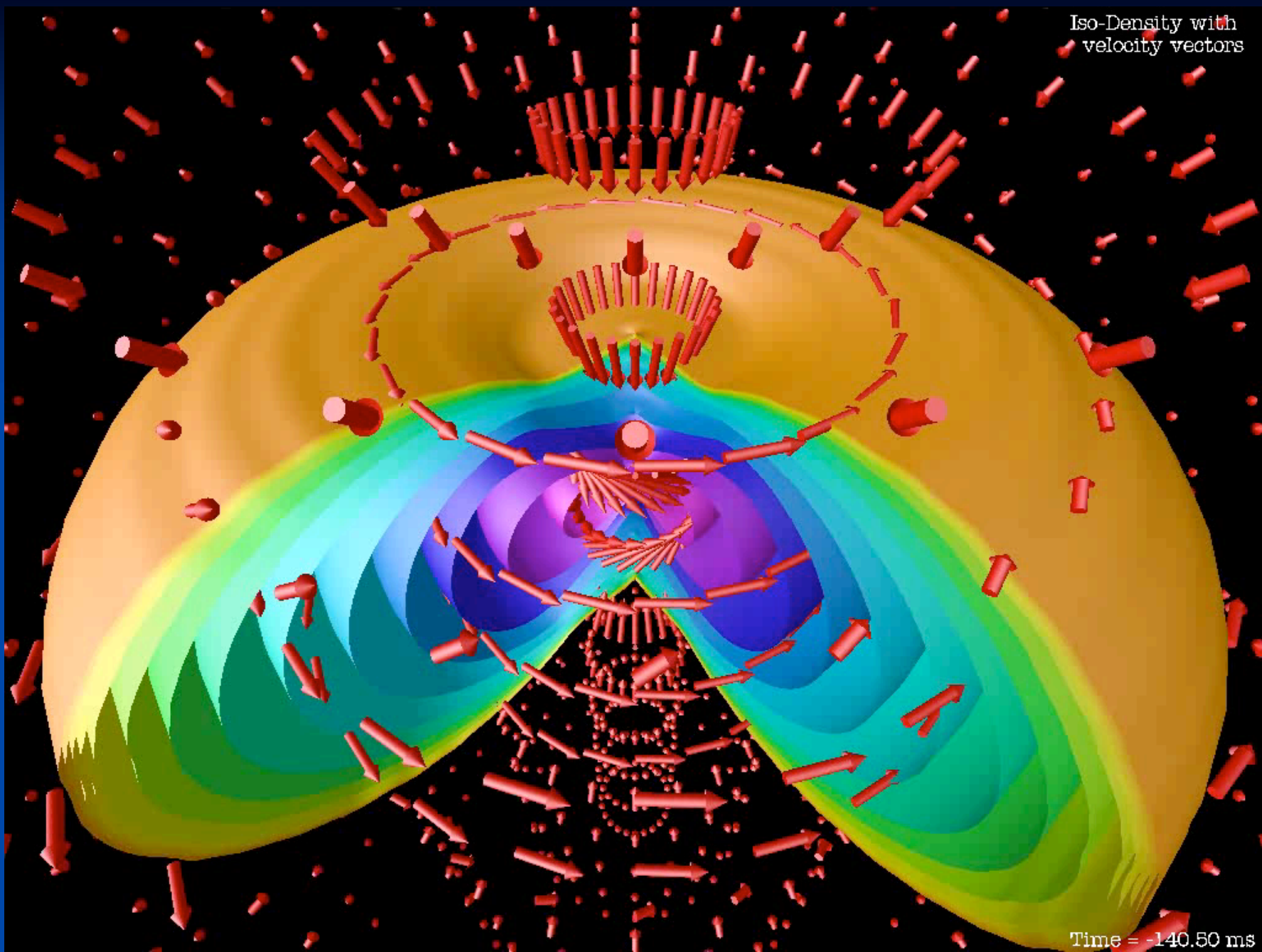
AIC: 1.92 solar masses:

Entropy

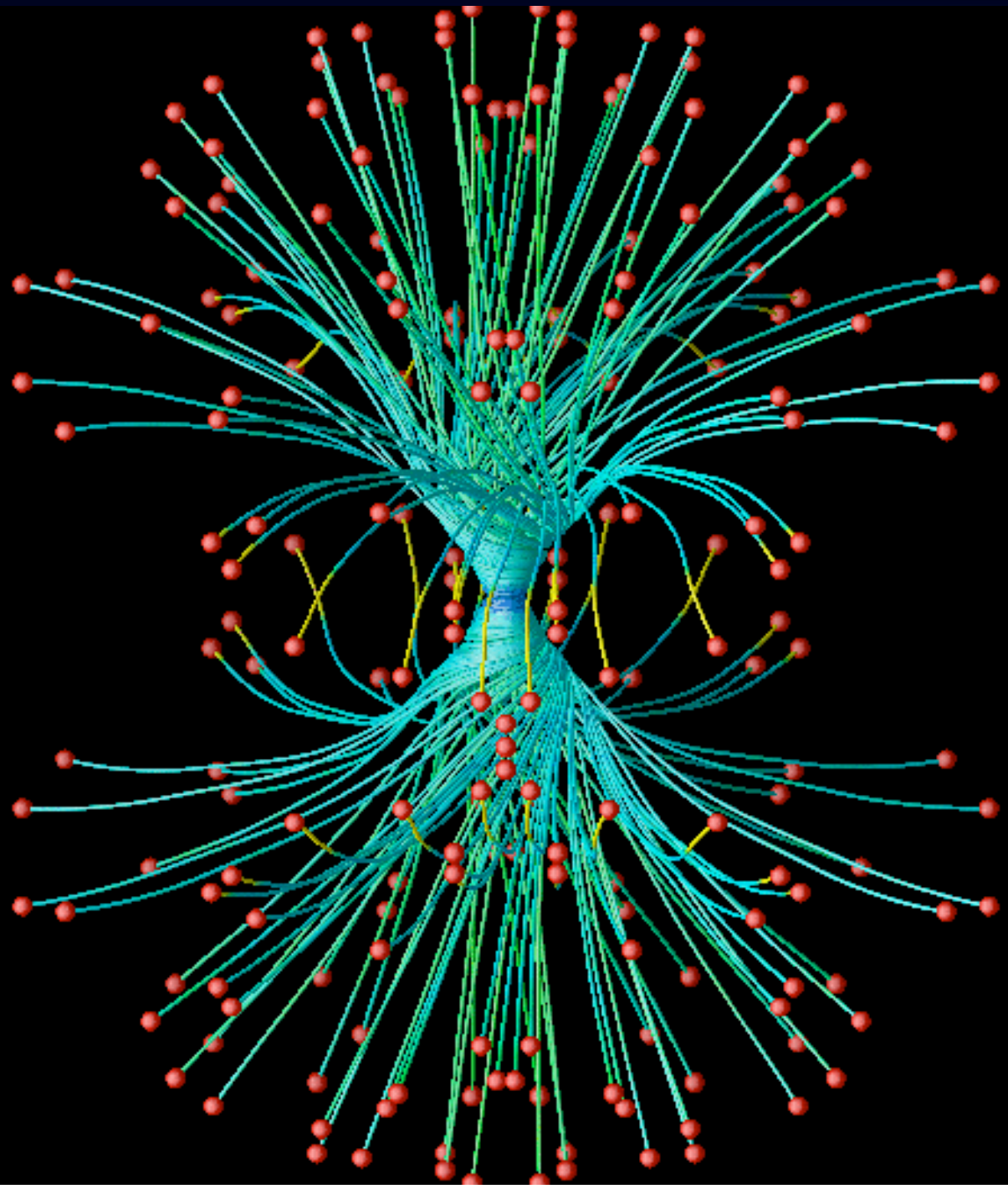


$t = -67.00$ ms

Iso-Density with
velocity vectors



Time = -140.50 ms

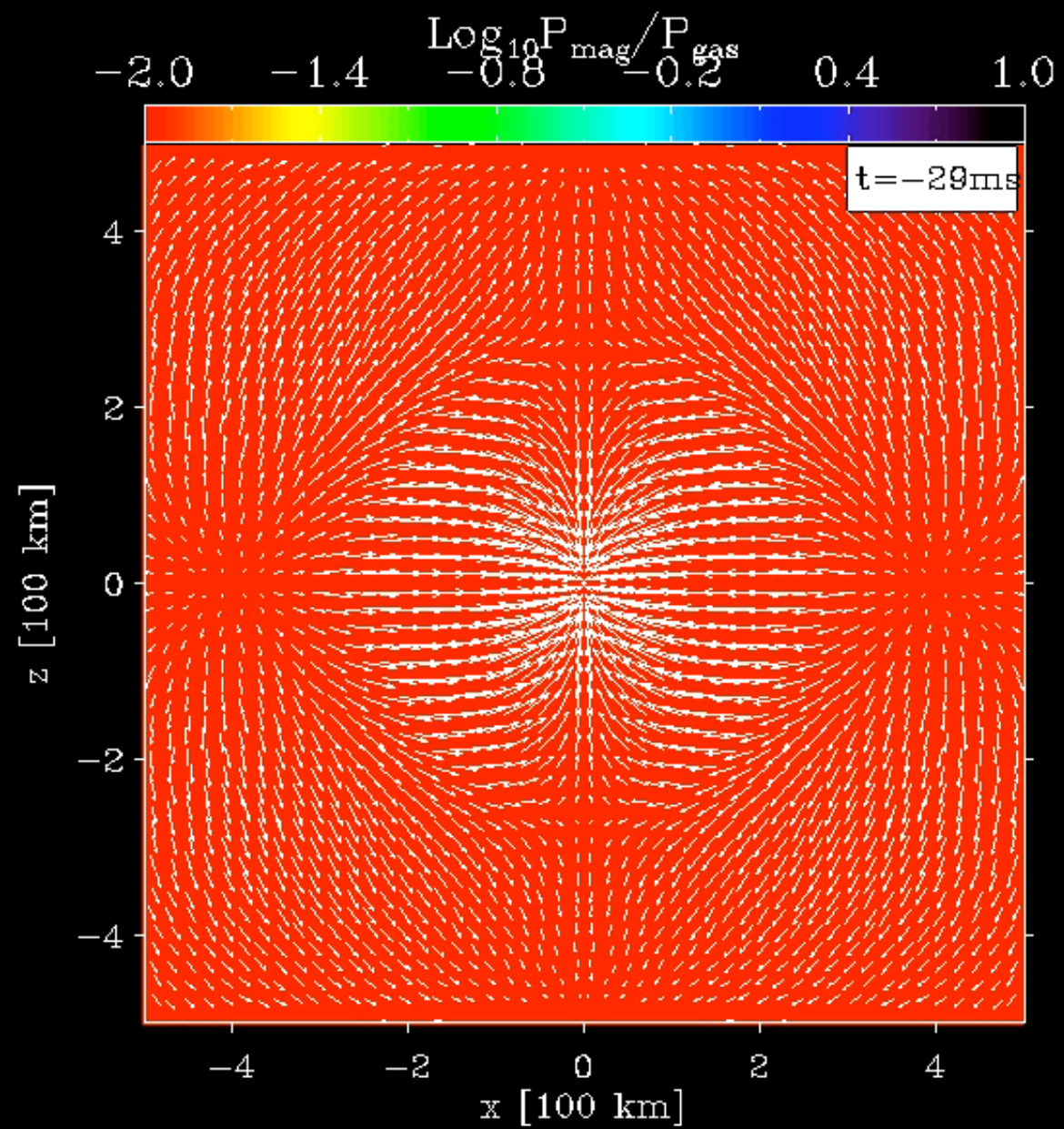


Accretion-Induced Collapse with Magnetic Fields

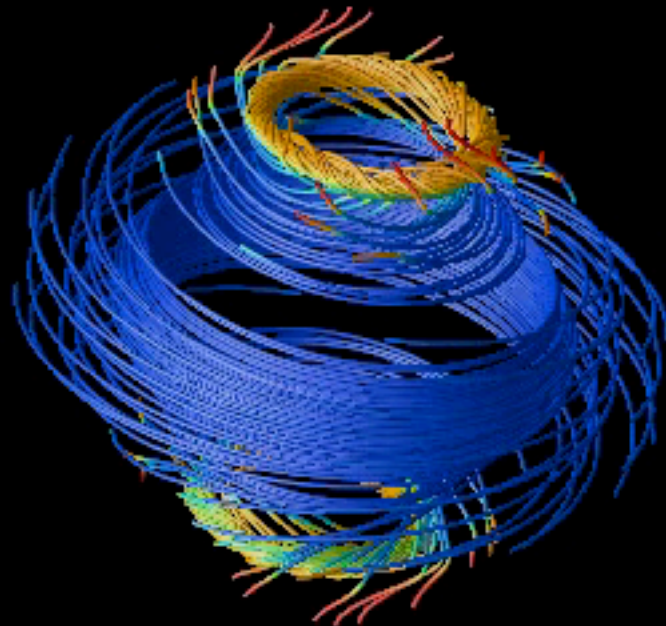
Dessart et al. 2007

Rapid Rotation!

AIC with MHD

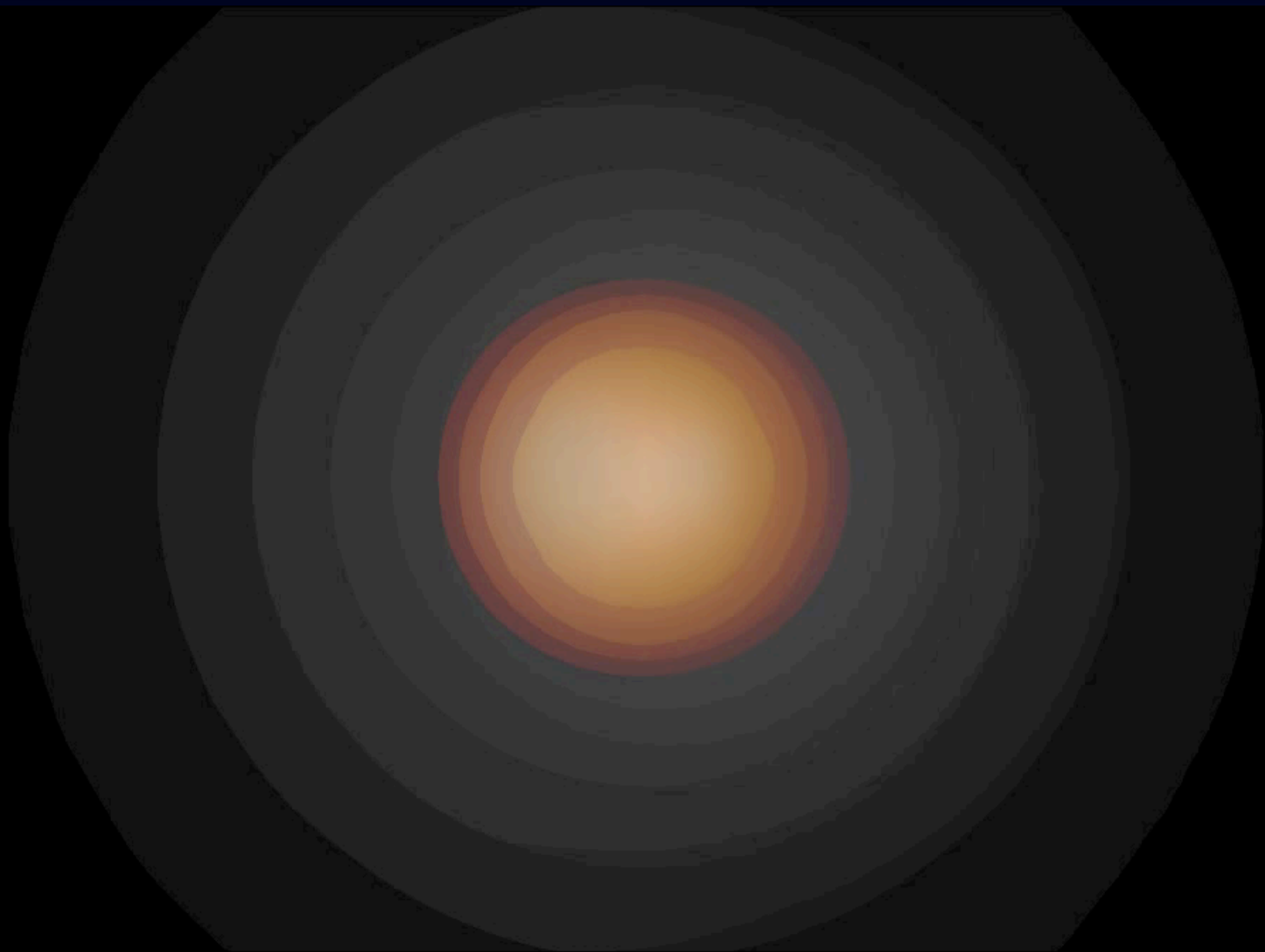


AIC
with
MHD



aic_MHD3
Velocity
Time = 100.0 ms
Radius = 4000.00 km

Core Oscillation/Acoustic Power Mechanism

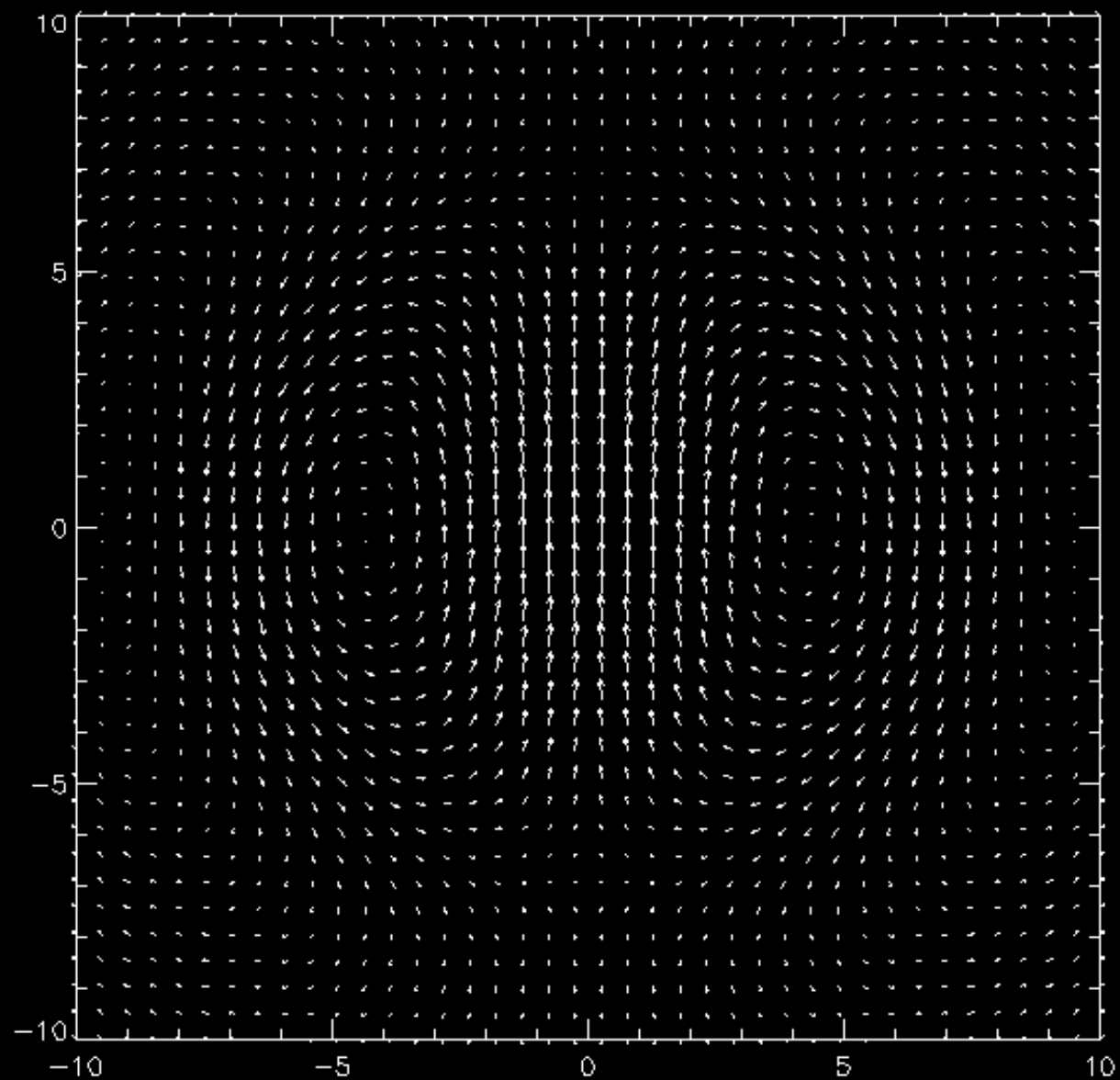


Time = -0.50 ms

Width = 50.00 km

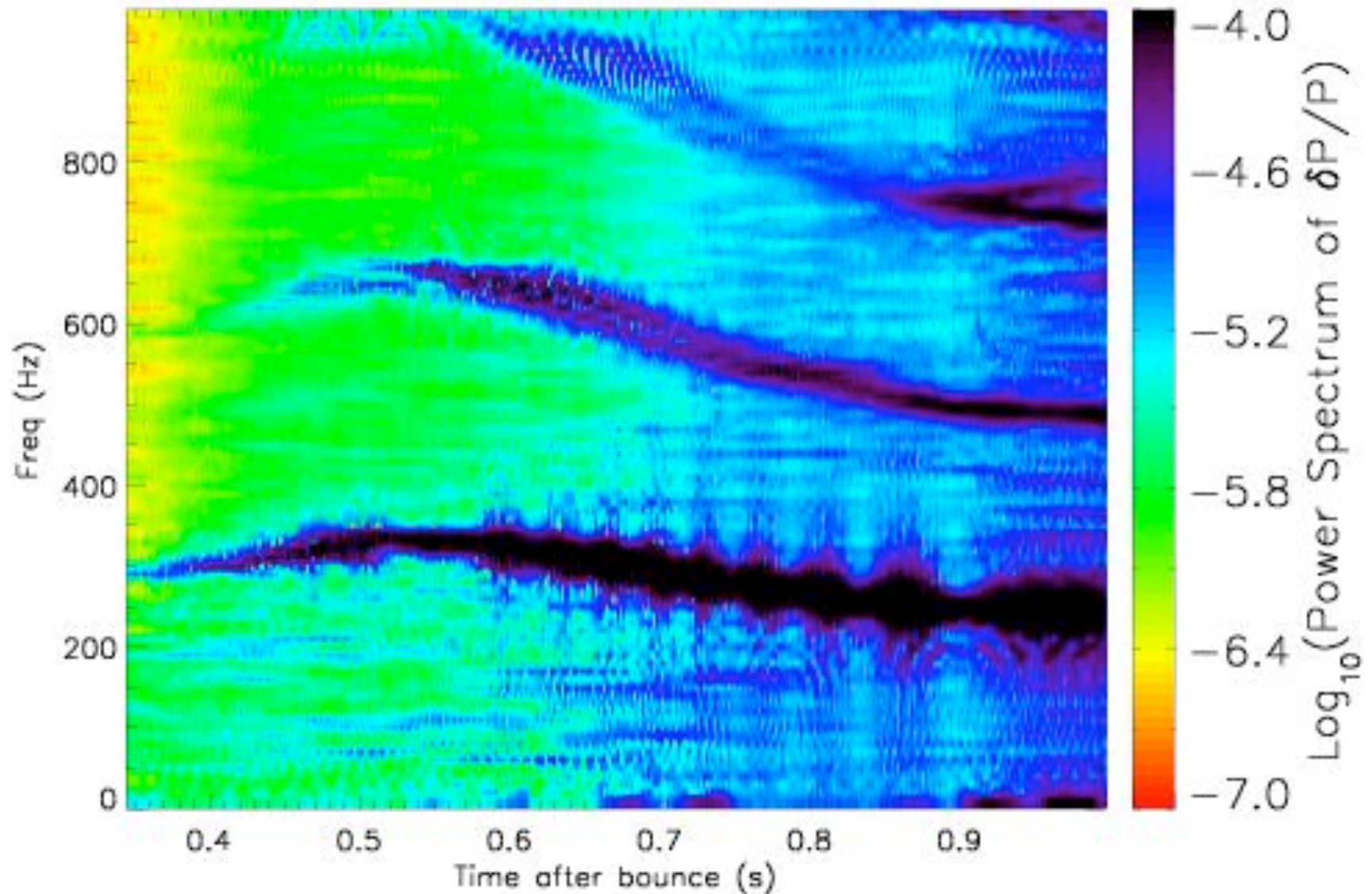
Analytic $l=1$

g -mode oscillation:

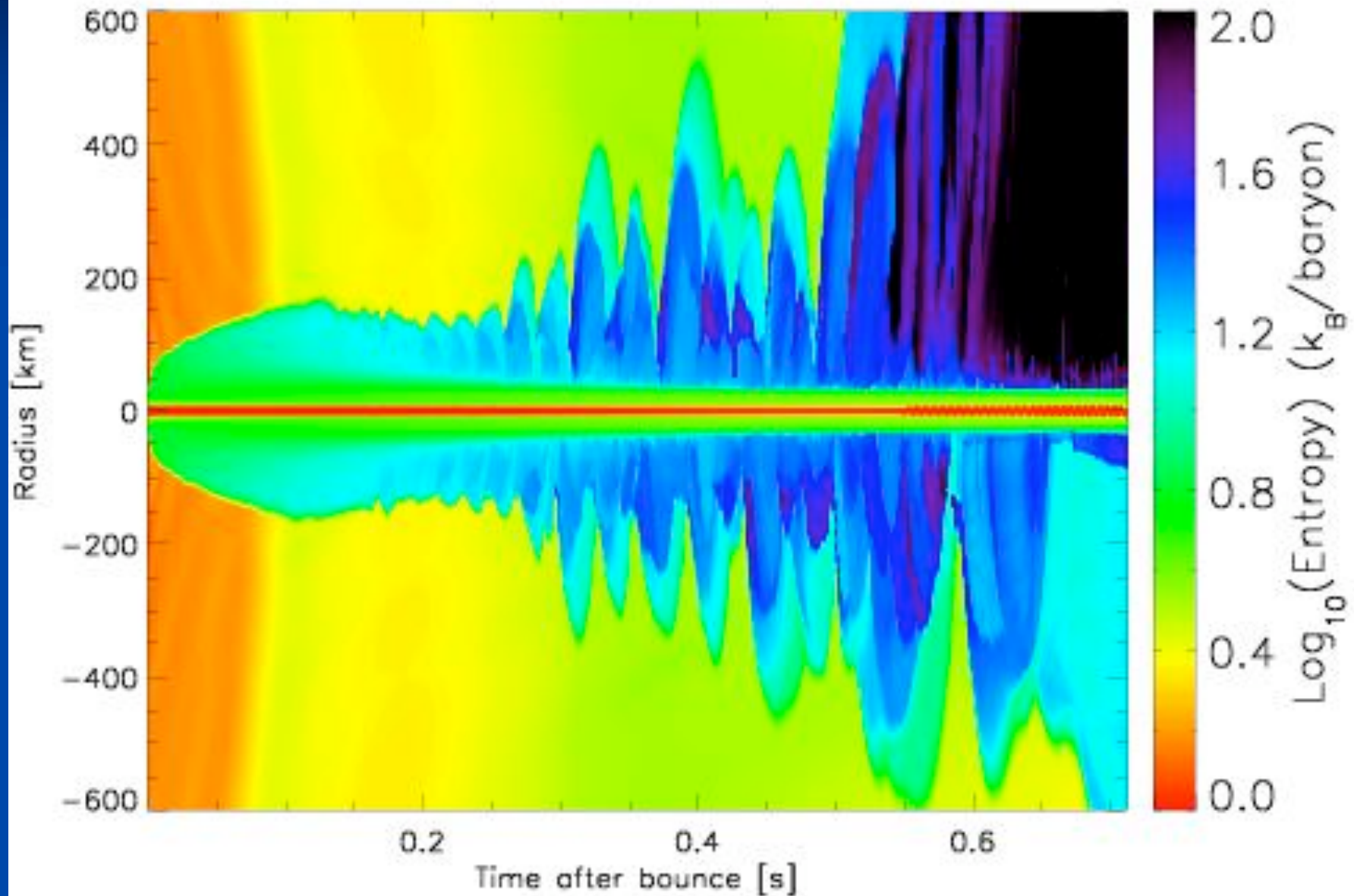




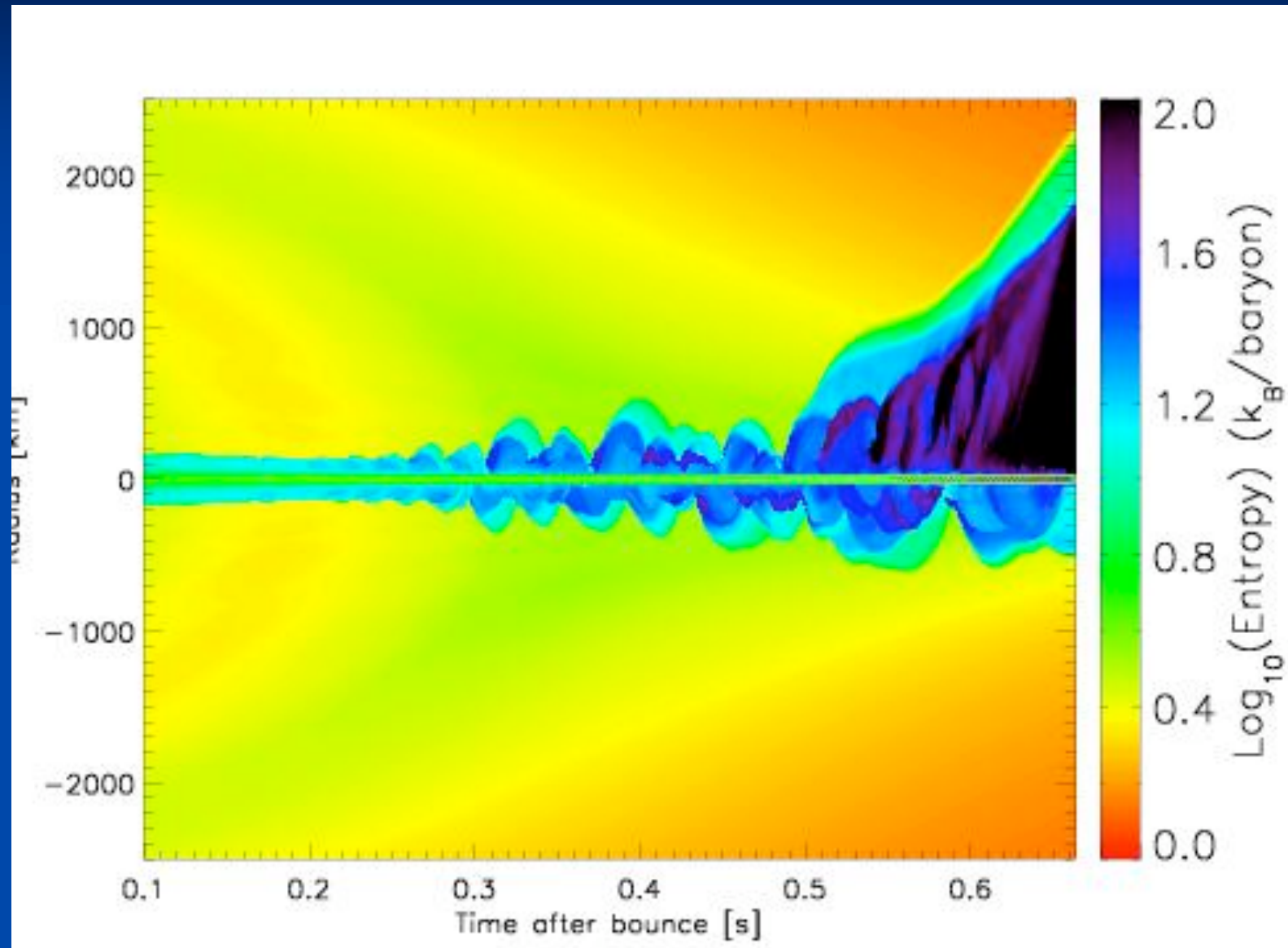
Frequency-Time Evolution of Pulsating Core at 30 km

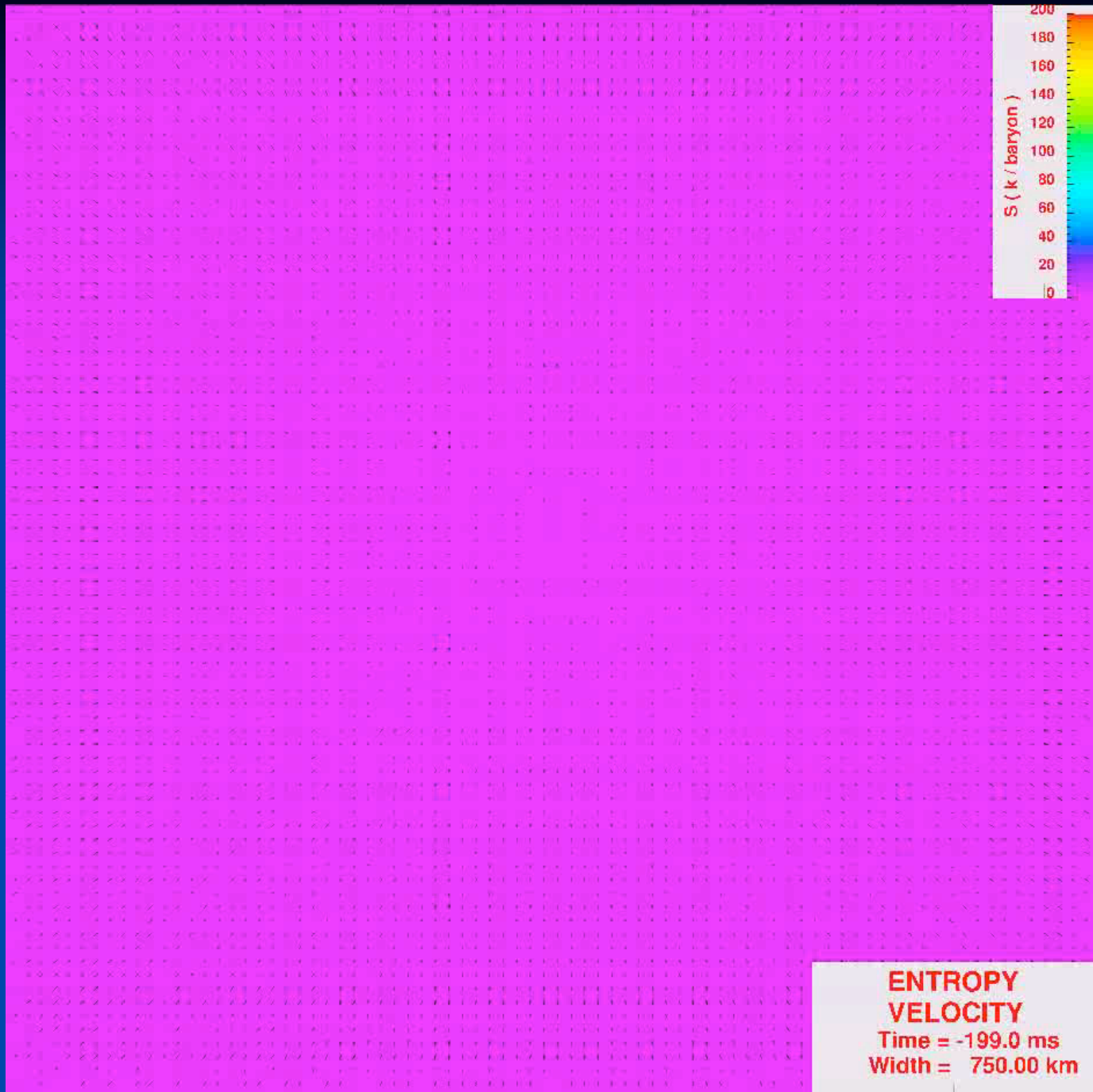


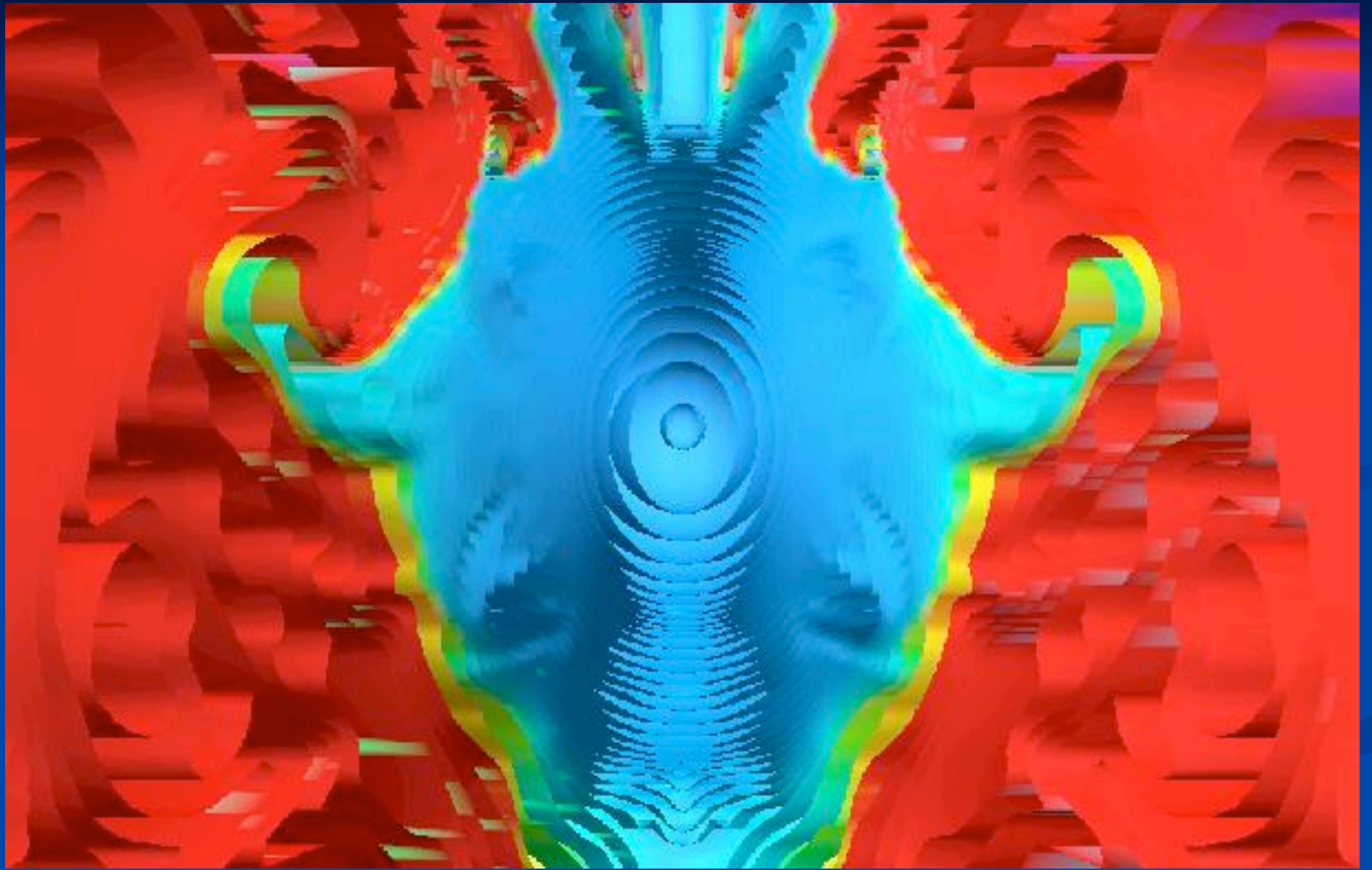
Inner 600-km Look at the Advective-Acoustic Instability



Entropy Profile along Pole versus Time after Bounce



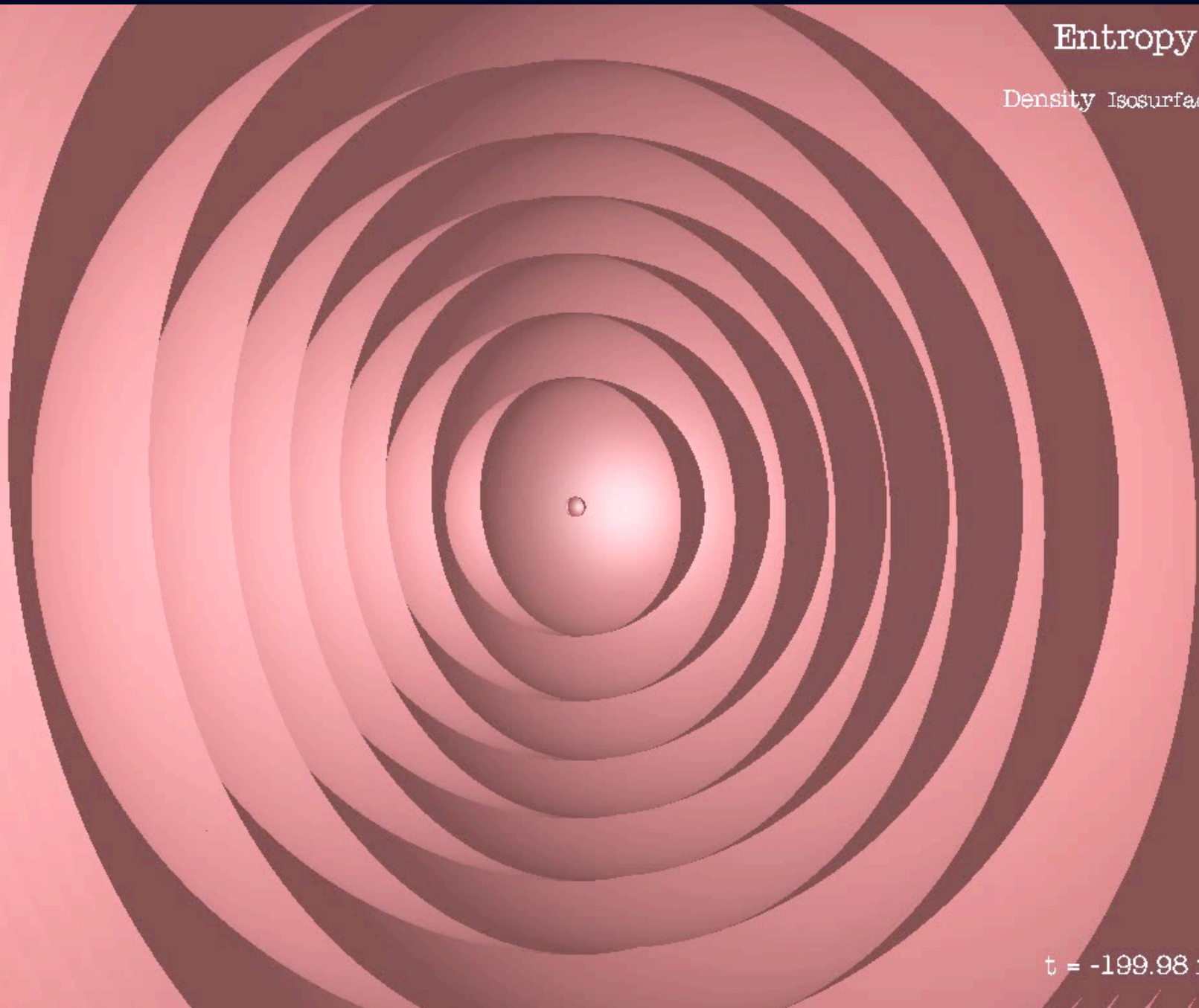




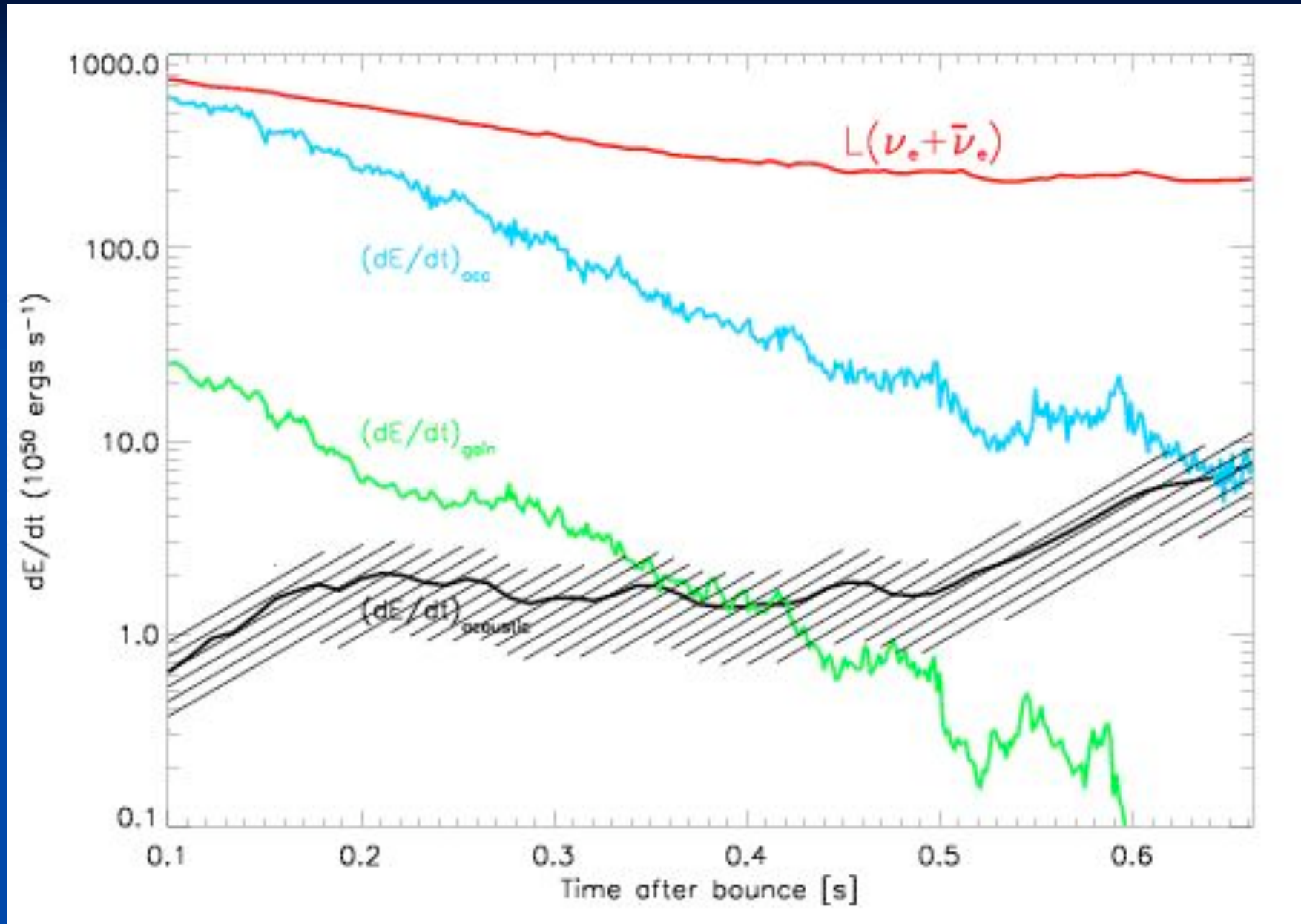
Entropy

Density Isosurfaces

$t = -199.98 \text{ ms}$



Power Comparisons: 11 Solar-Mass model



Computational Context Needed to Explore Acoustic Mechanism

- Most calculations were stopped after 200-300 ms
- Other grid-based codes excised the core, did the calculations on a 90° wedge, or followed the core in 1D, completely suppressing core oscillations
- One key was the computational liberation of the core to execute its natural multi-dimensional motions
- Another key was patience to perform the calculations to very “late” times
- Crucial capabilities: 1) Momentum conservation, 2) “Cartesian-like” grid in the core (Courant condition), 3) High-precision gravity solver, 4) Moving grid (to maintain high-resolution under core)
- But, are the g-mode amplitudes large enough to explode the star?

MHD Jets and RMHD Simulations of Core Collapse: Rapid Rotation

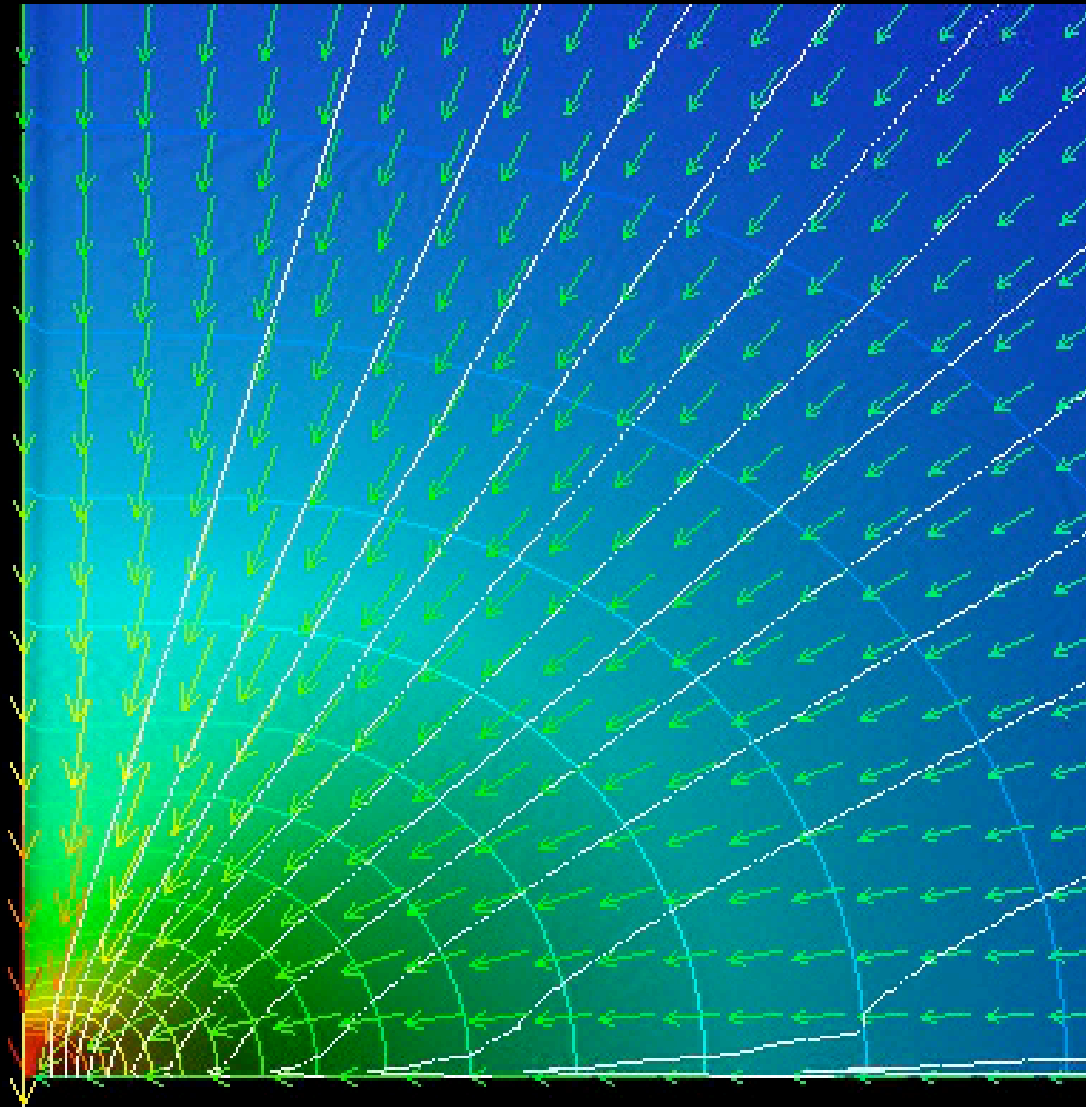
Burrows, Dessart, Livne, Ott, & Murphy 2007; Dessart
et al. 2007

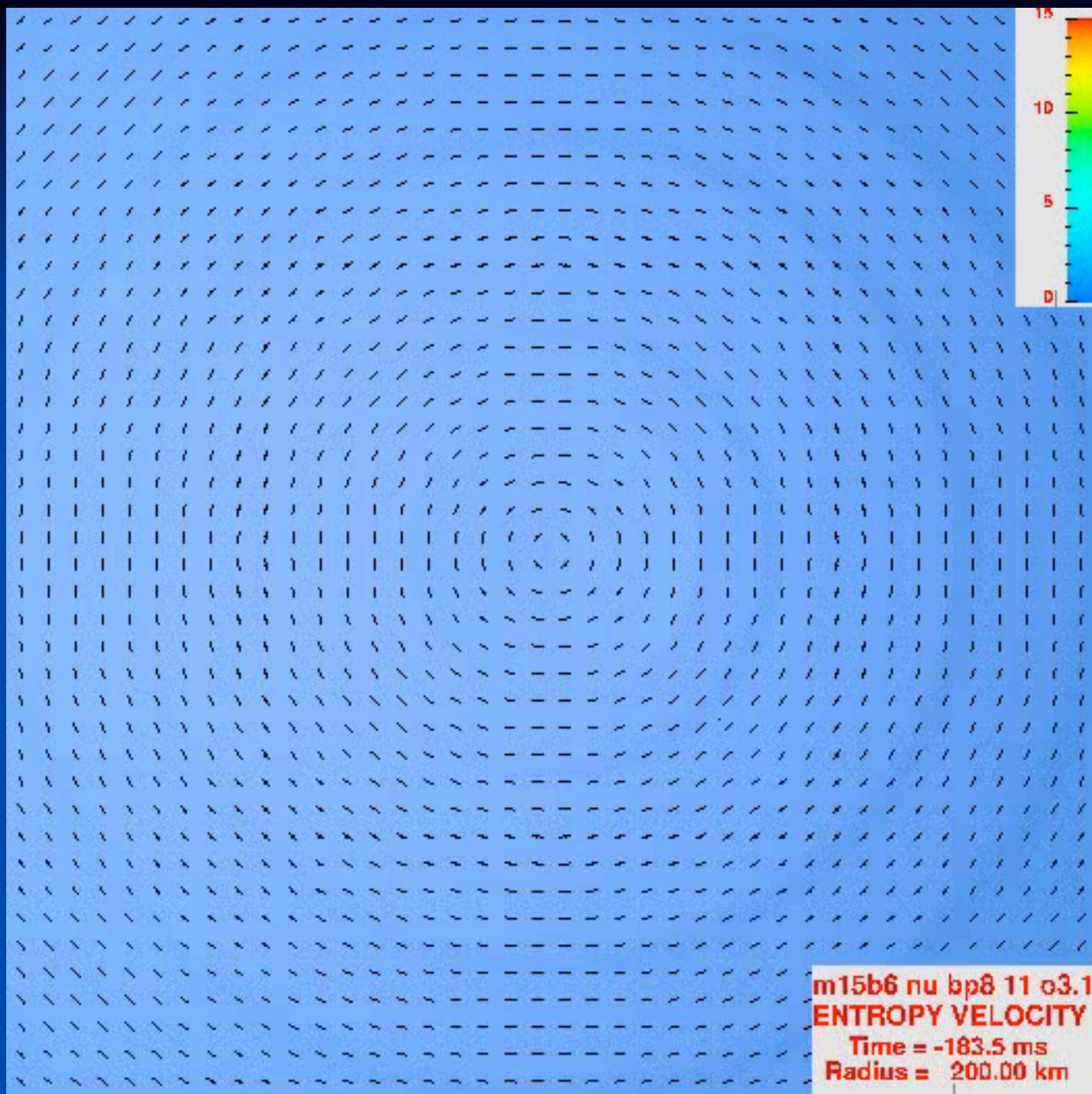
Rotation Winding, the MRI and B-field Stress effects

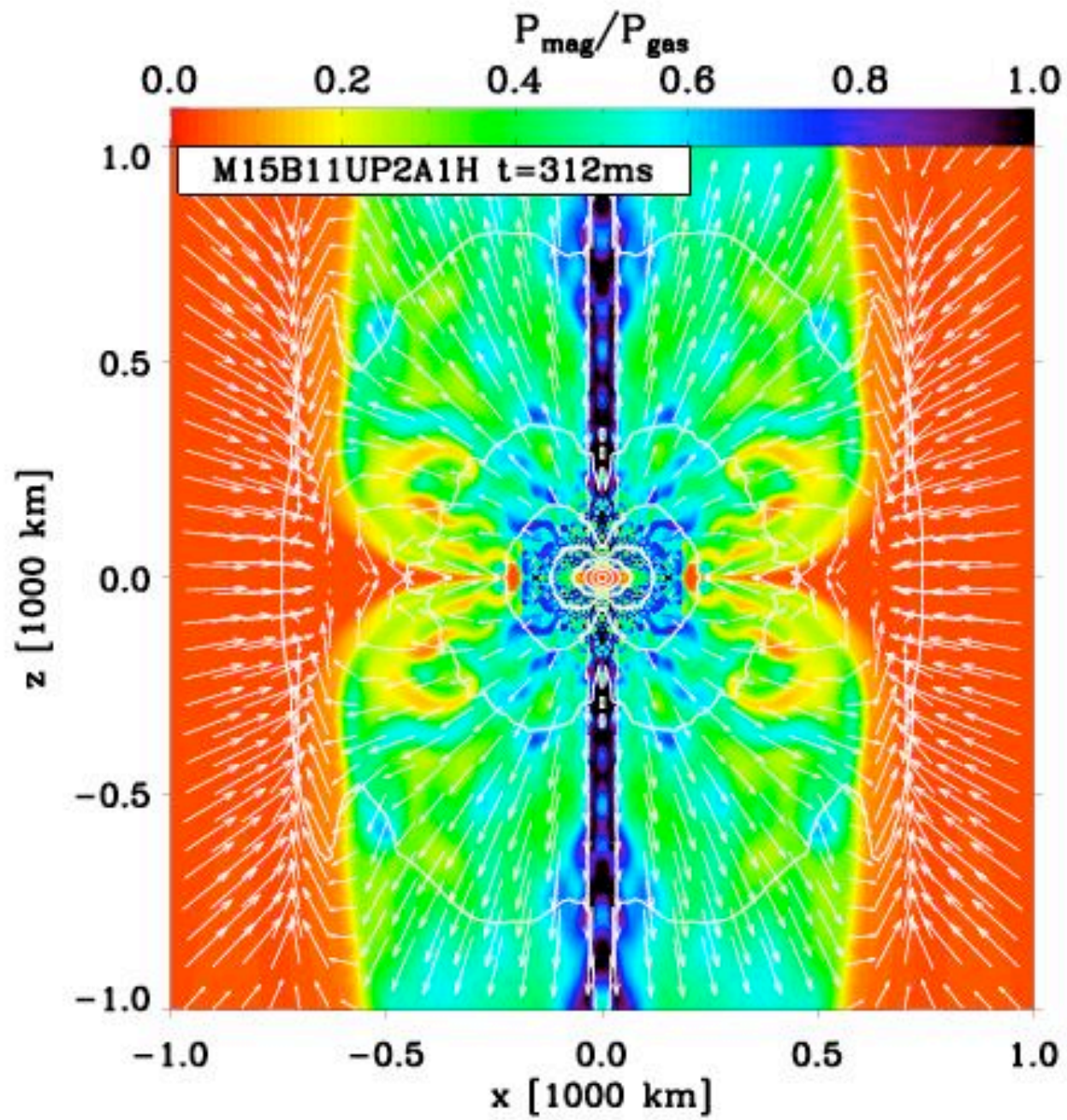
115.01256580000

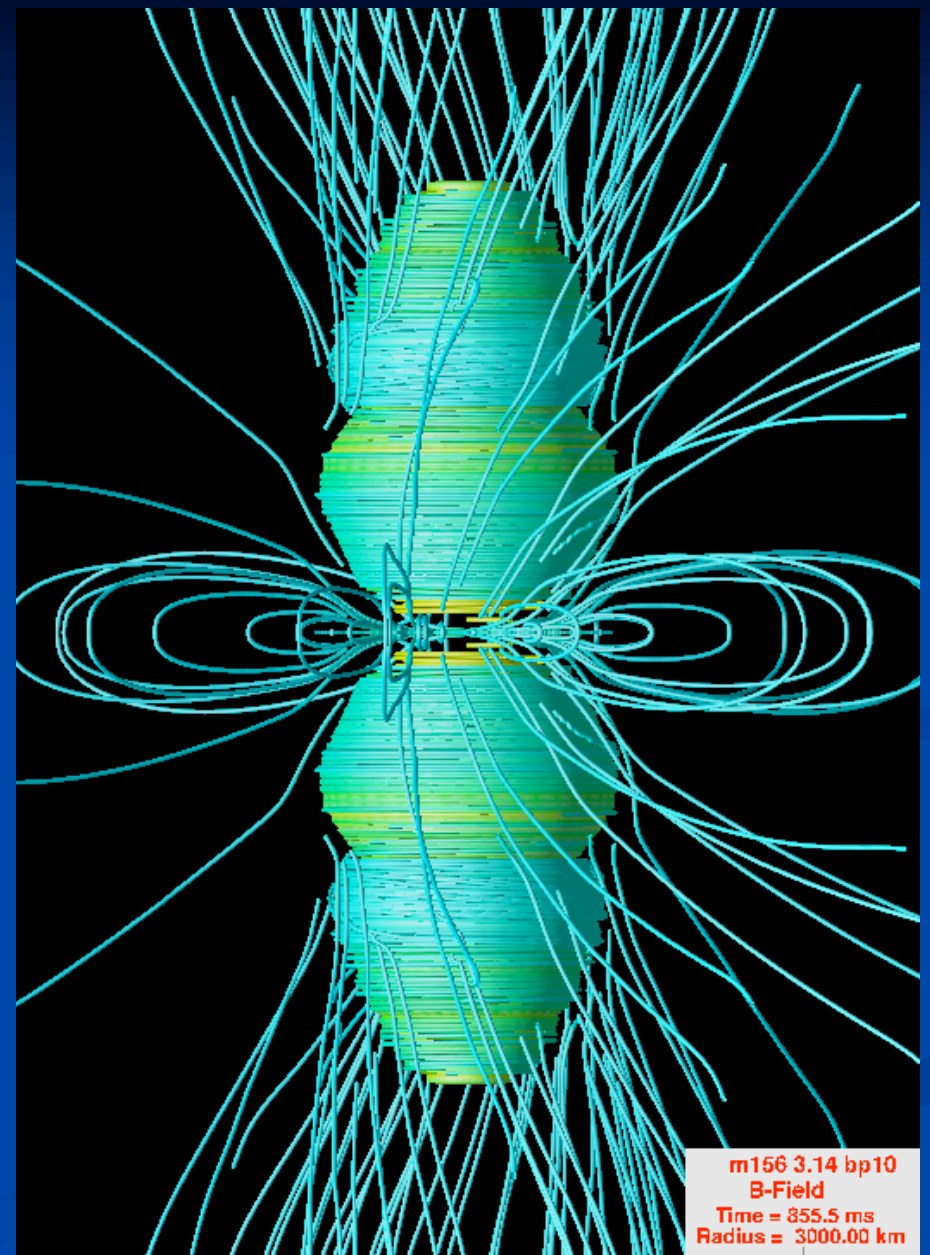
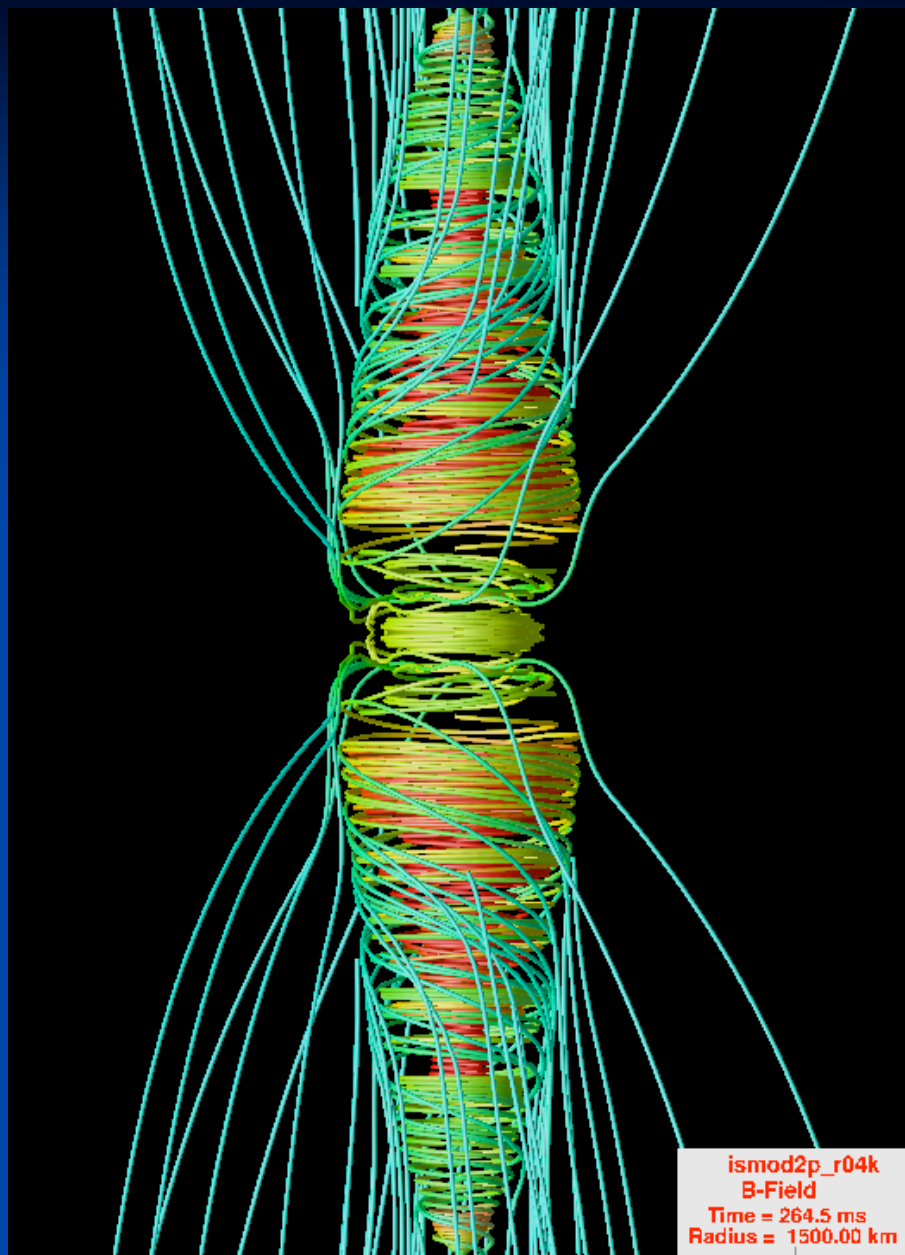
Shibata et
al. 2007

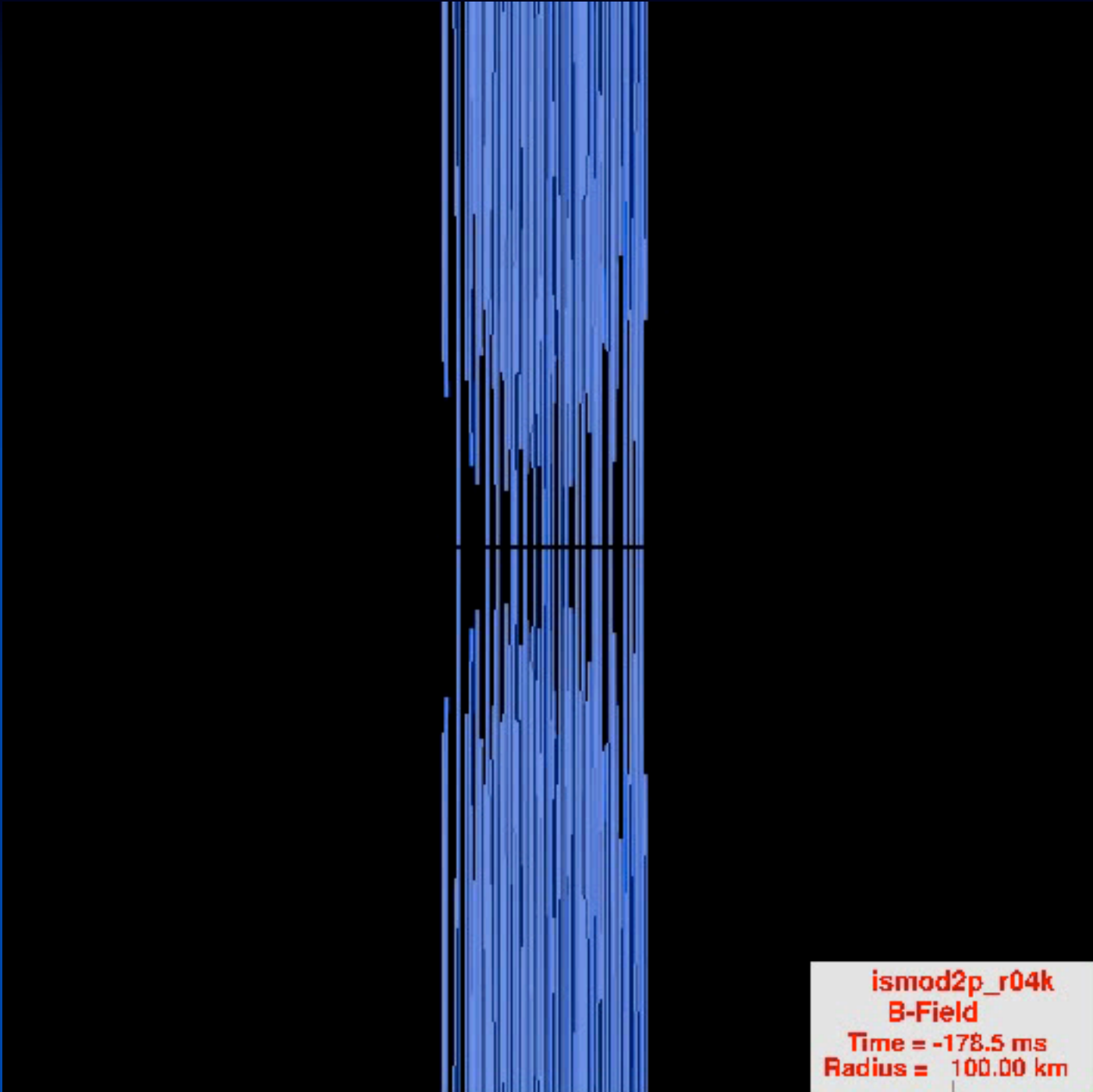
(33 ms of
post-bounce
evolution)











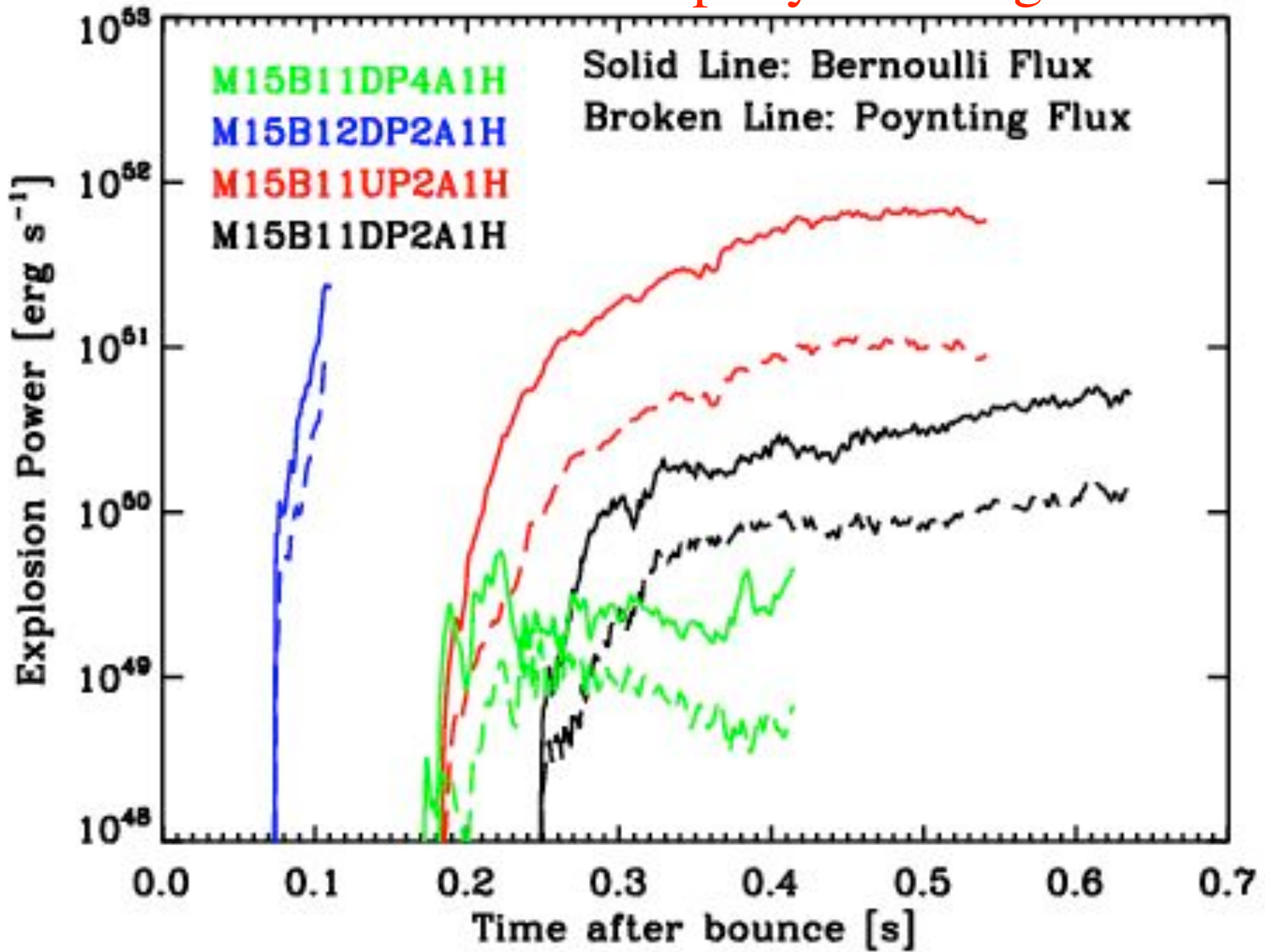
ismod2p_r04k
B-Field
Time = -178.5 ms
Radius = 100.00 km





M15B11UP2A1H
B-Field
Time = 175.5 ms
Radius = 3500.00 km

MHD Jet Powers for Rapidly-Rotating Cores

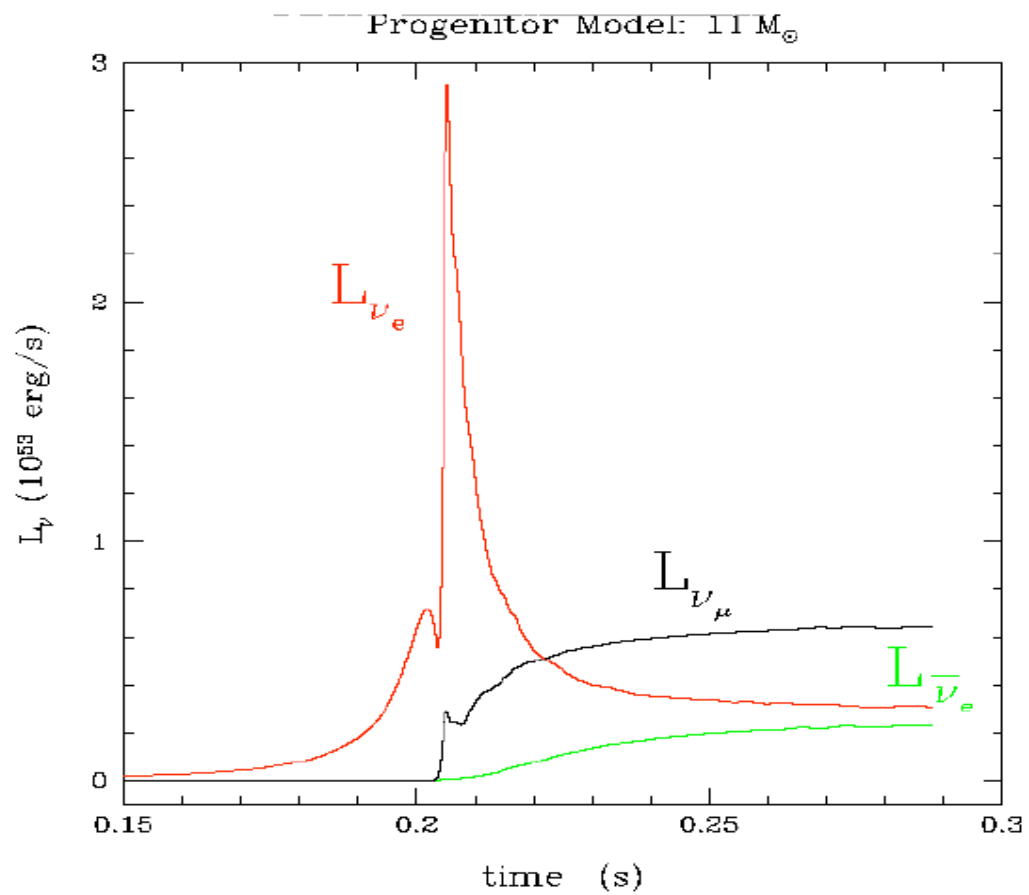


Questions: MHD Jets

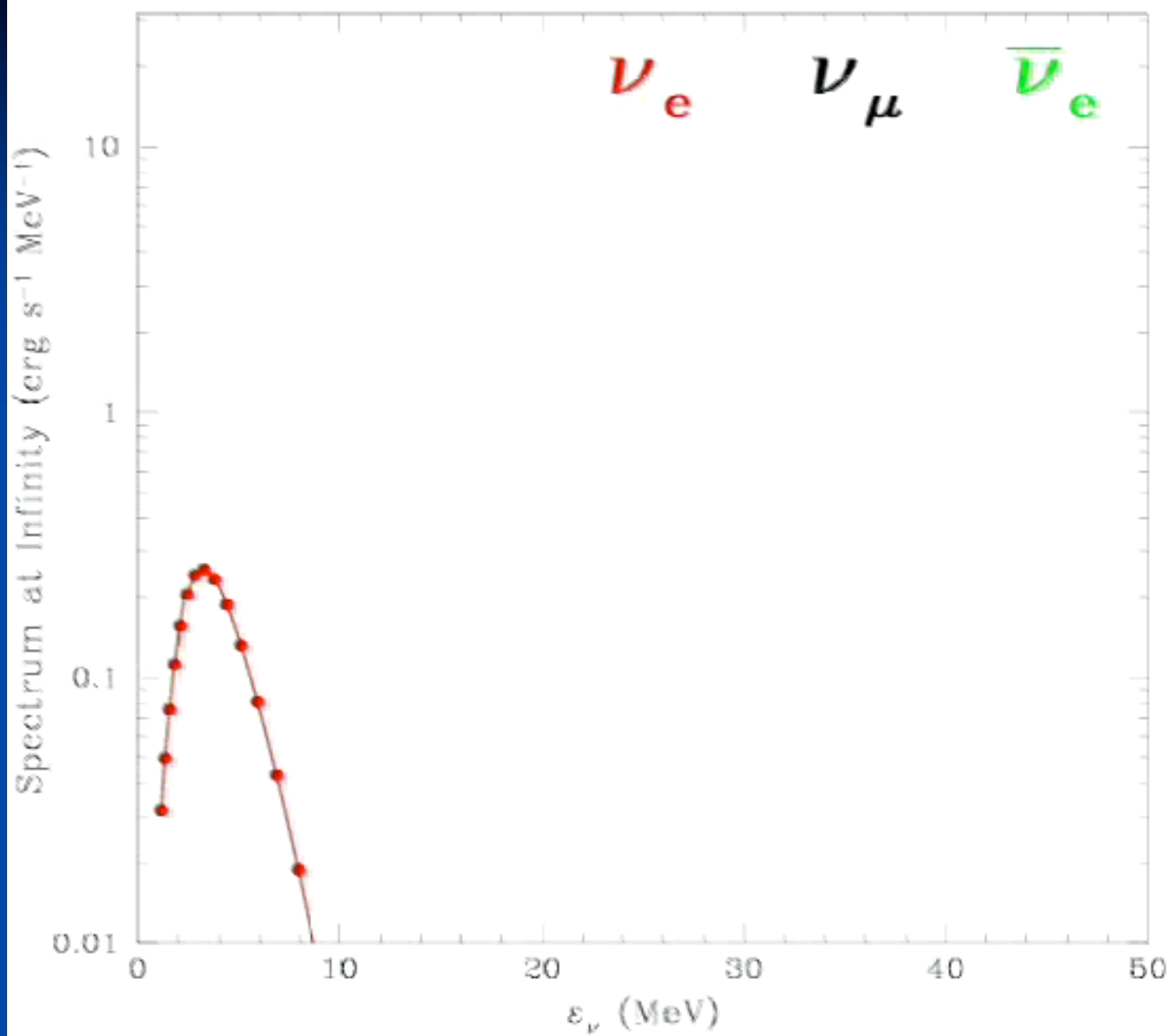
- Initial models: Spin rates and B-fields?
- 3D simulations?
- MRI?
- Dynamo?
- Whither Pulsars / Magnetars? Final spins and B-fields? Spindown?
- Hypernova / GRB connection?
- Secondary MHD Jets / low-energy explosion after other main explosion?

Neutrino Bursts/Signatures

Breakout Burst of Neutrinos: Precision Boltzmann Transfer



Model: $15 M_{\odot}$, time = 0.08823 s



Flux Vectors

ν_e
21.01 MeV

$\Omega = 0$

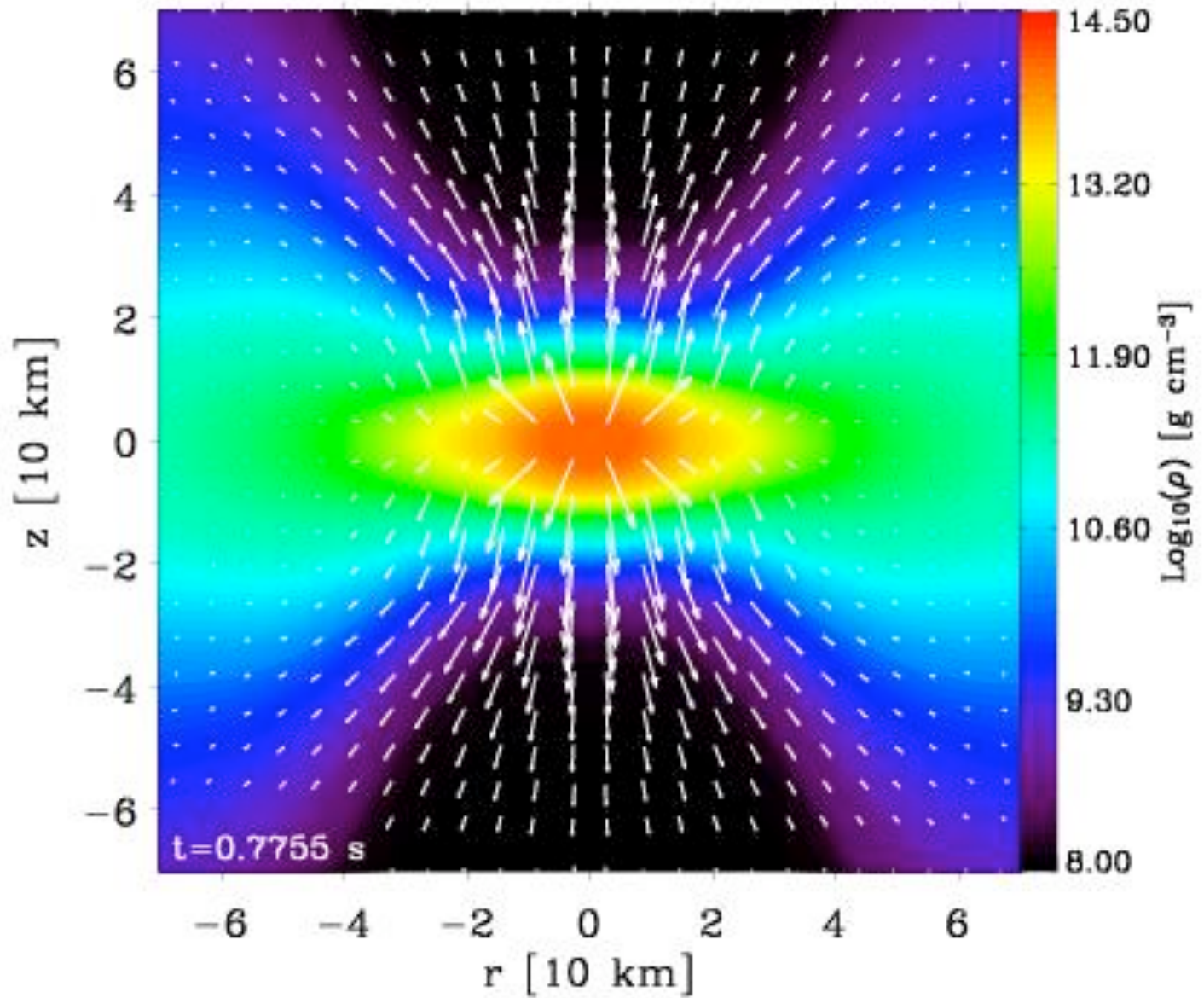
Time = -194.5 ms
Distance = 250.0 km



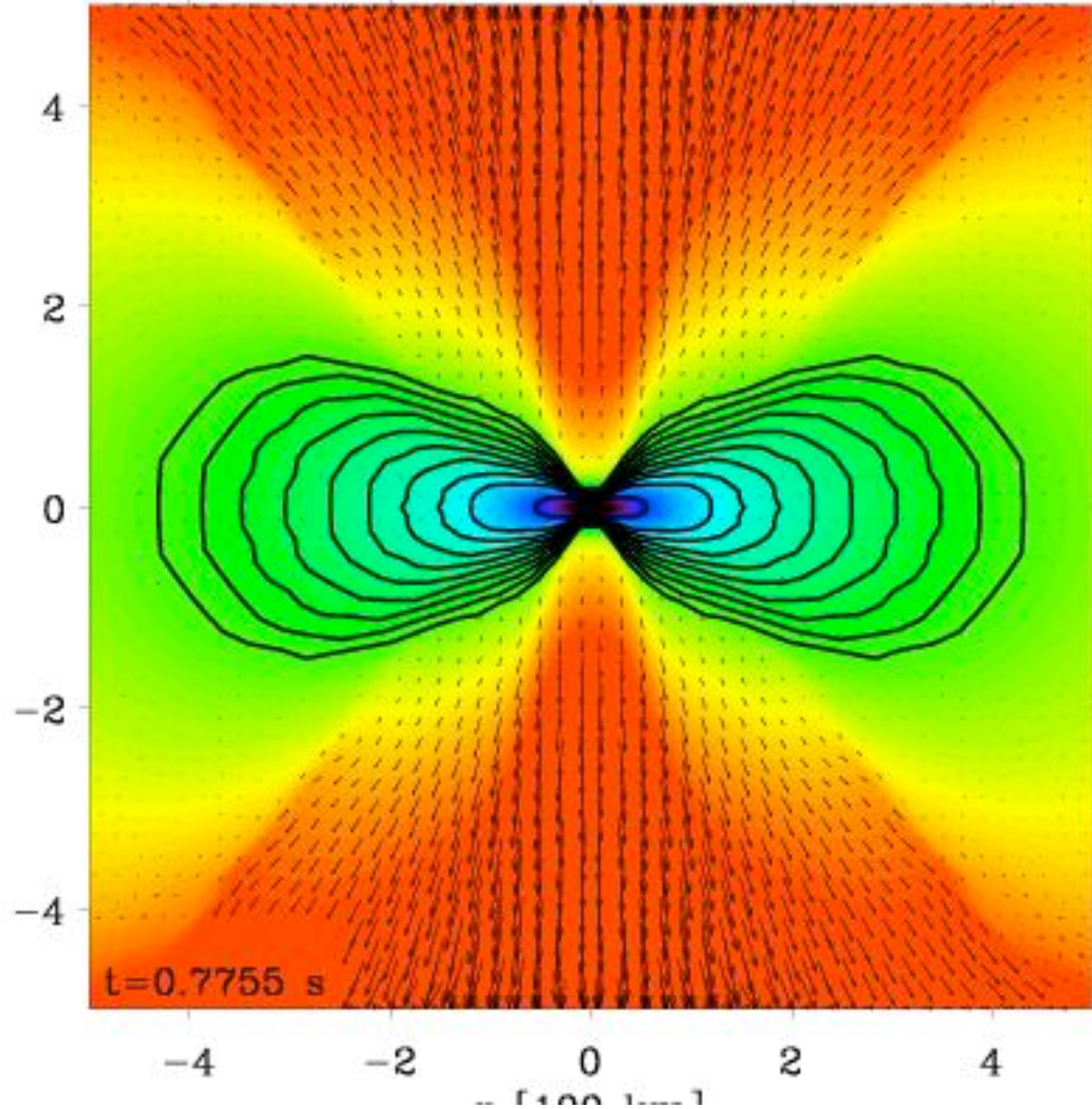
2D Electron
Neutrino Fluxes
for 1.92 solar
mass AIC
model:

Rapid
Rotation!

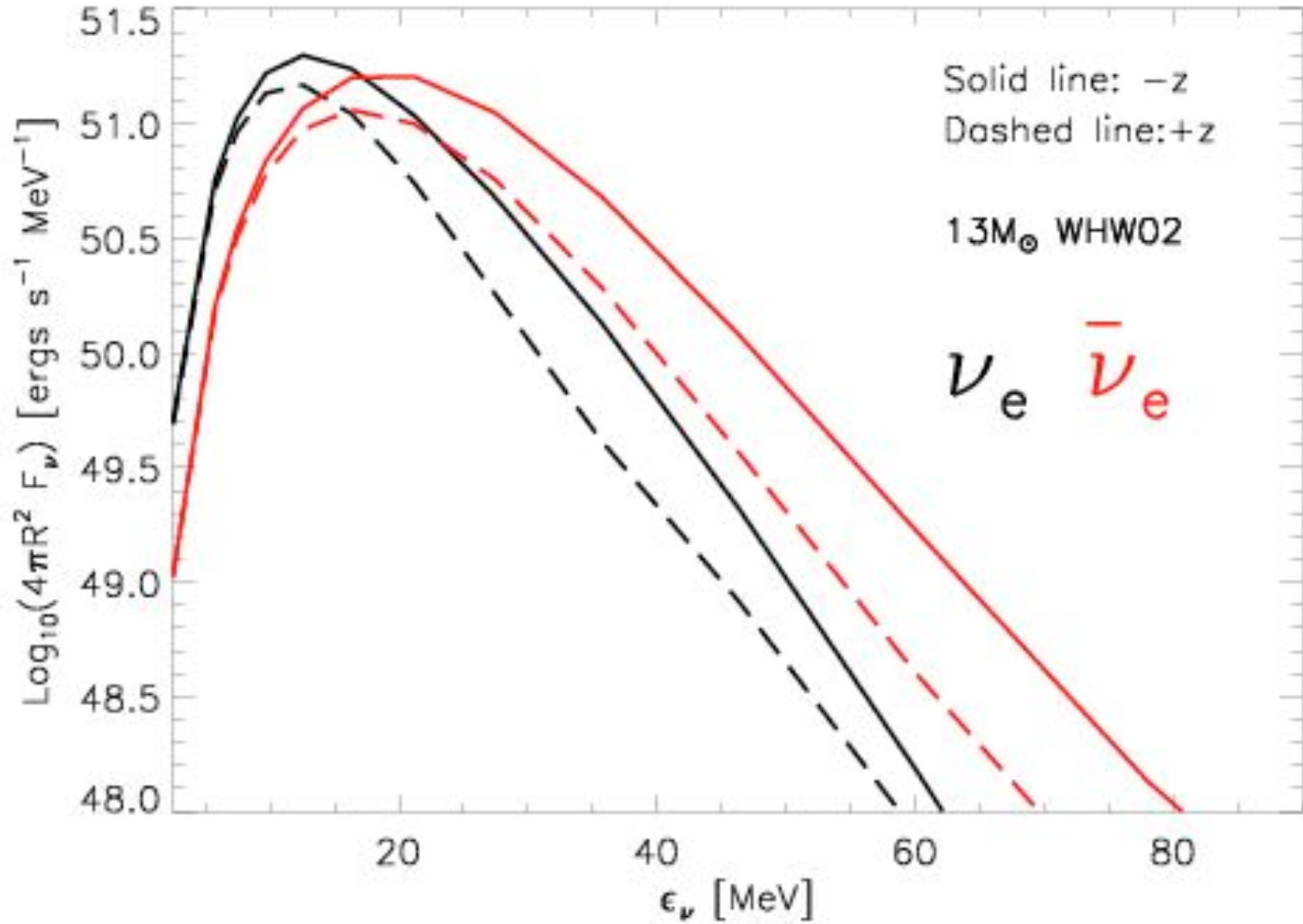
Anisotropic Neutrino Fluxes due to Rotation



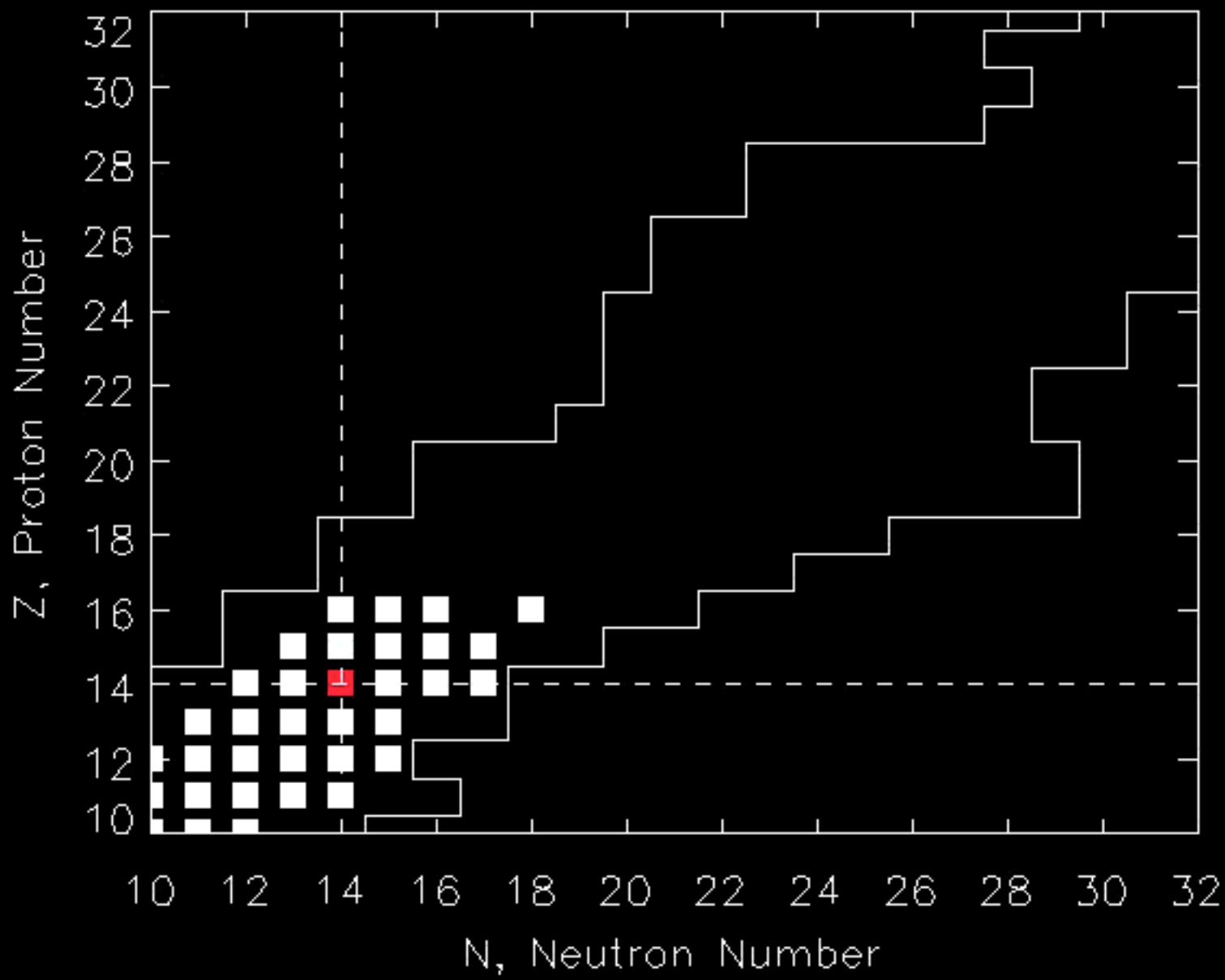
Electron
Neutrinospheres
for 1.92 solar
mass AIC
model:



Top-Bottom Asymmetry in Neutrino Luminosity after Explosion: Kicks!

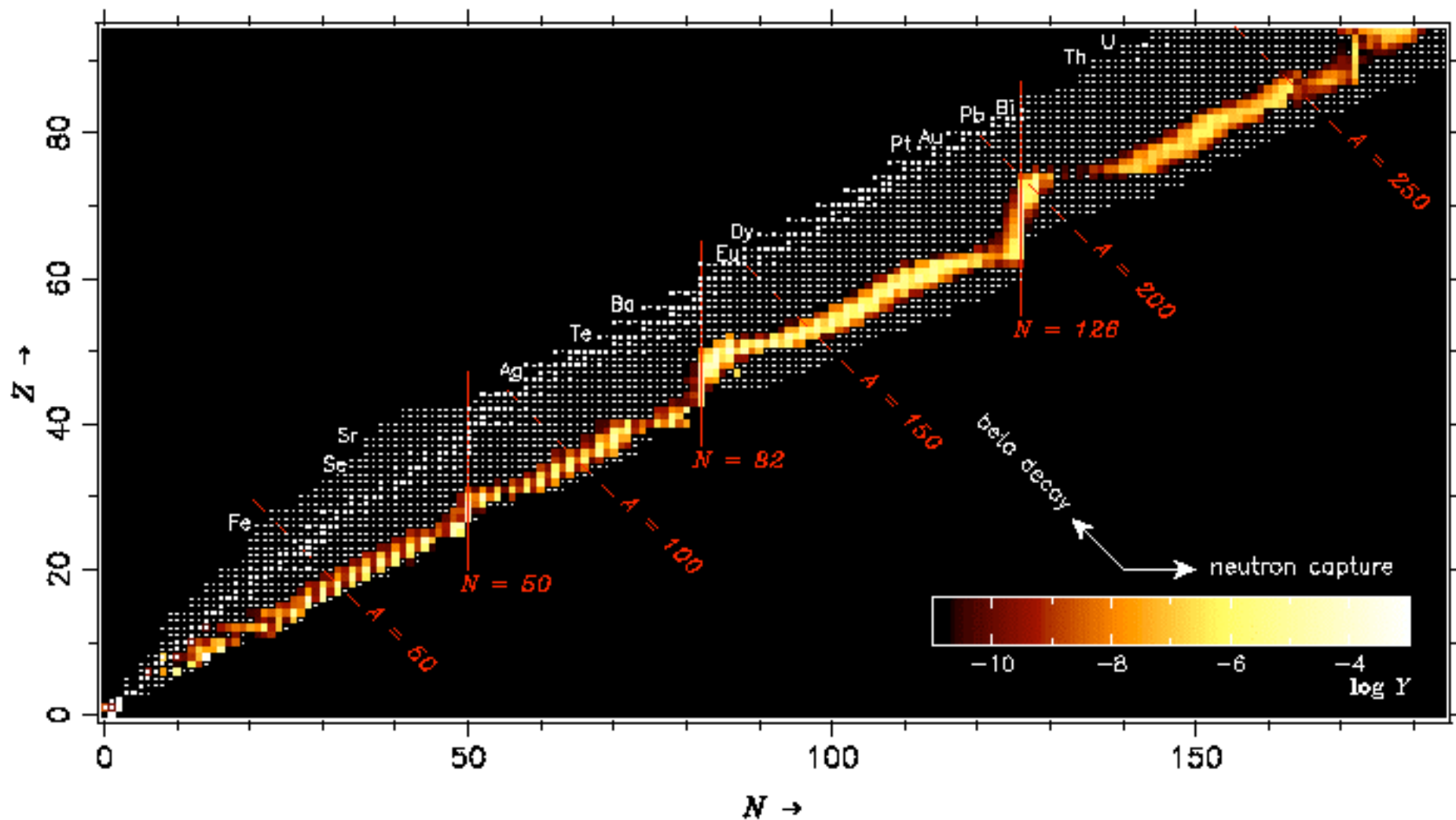


$t \text{ (s)} = 6.74200e-20$ $T_g = 5.50$ $\rho \text{ (g/cc)} = 1.00000e+07$



**“R-process”
Nucleosynthesis?**

R-Process Nucleosynthesis



Nucleosynthesis in the r-process

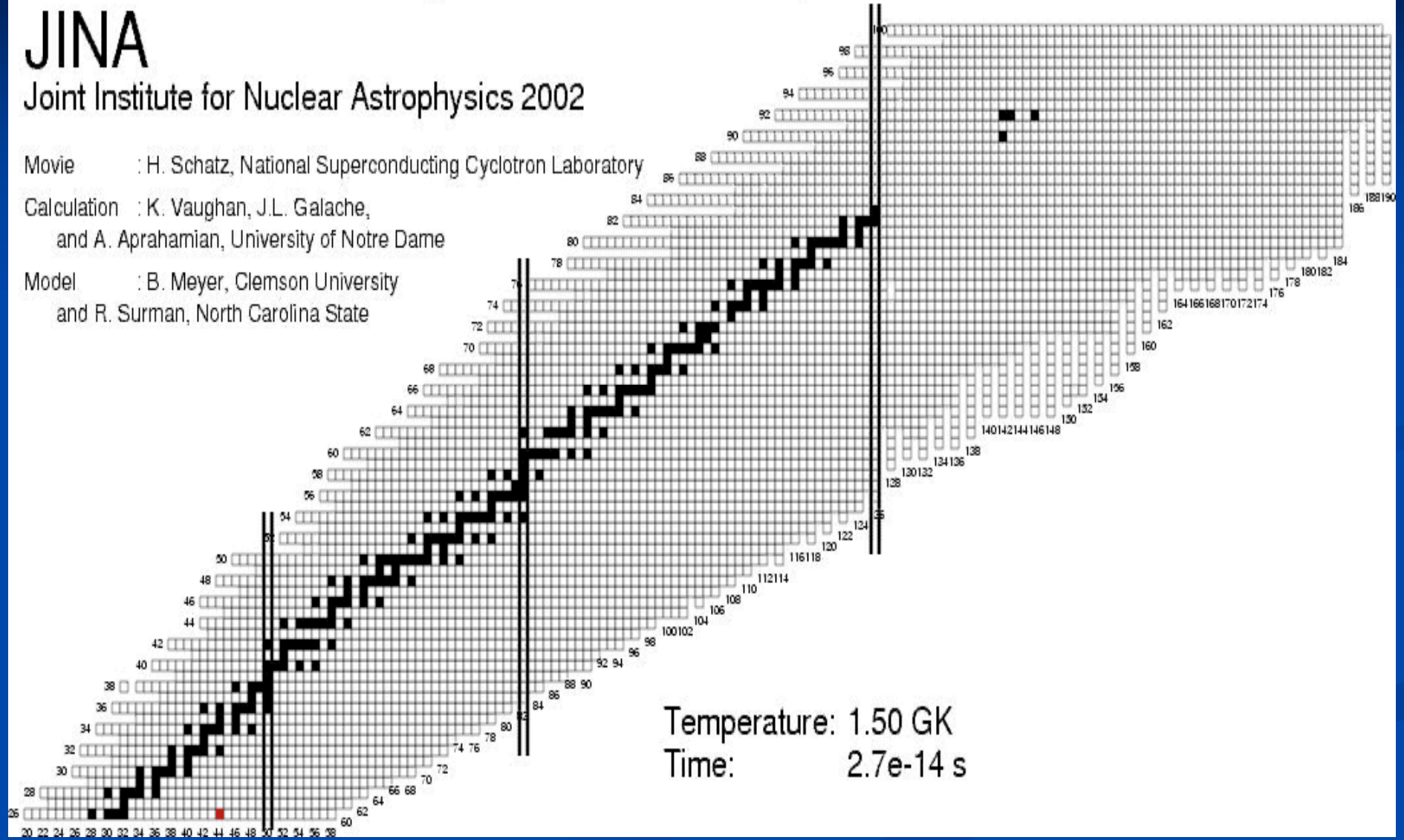
JINA

Joint Institute for Nuclear Astrophysics 2002

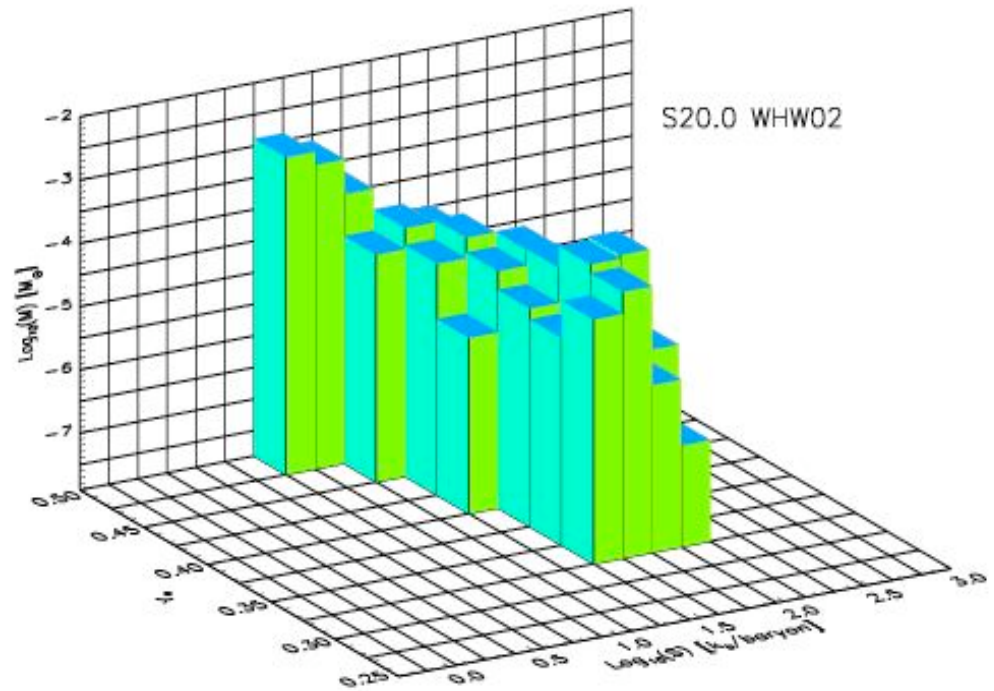
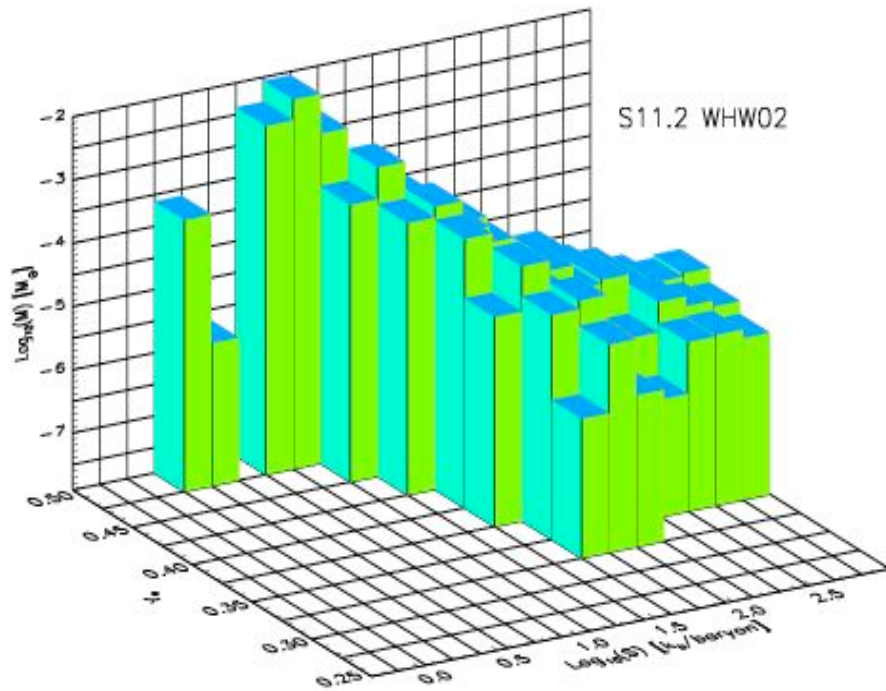
Movie : H. Schatz, National Superconducting Cyclotron Laboratory

Calculation : K. Vaughan, J.L. Galache,
and A. Aprahamian, University of Notre Dame

Model : B. Meyer, Clemson University
and R. Surman, North Carolina State



Ejecta mass versus Entropy and Y_e for Acoustic Mechanism: R-process?

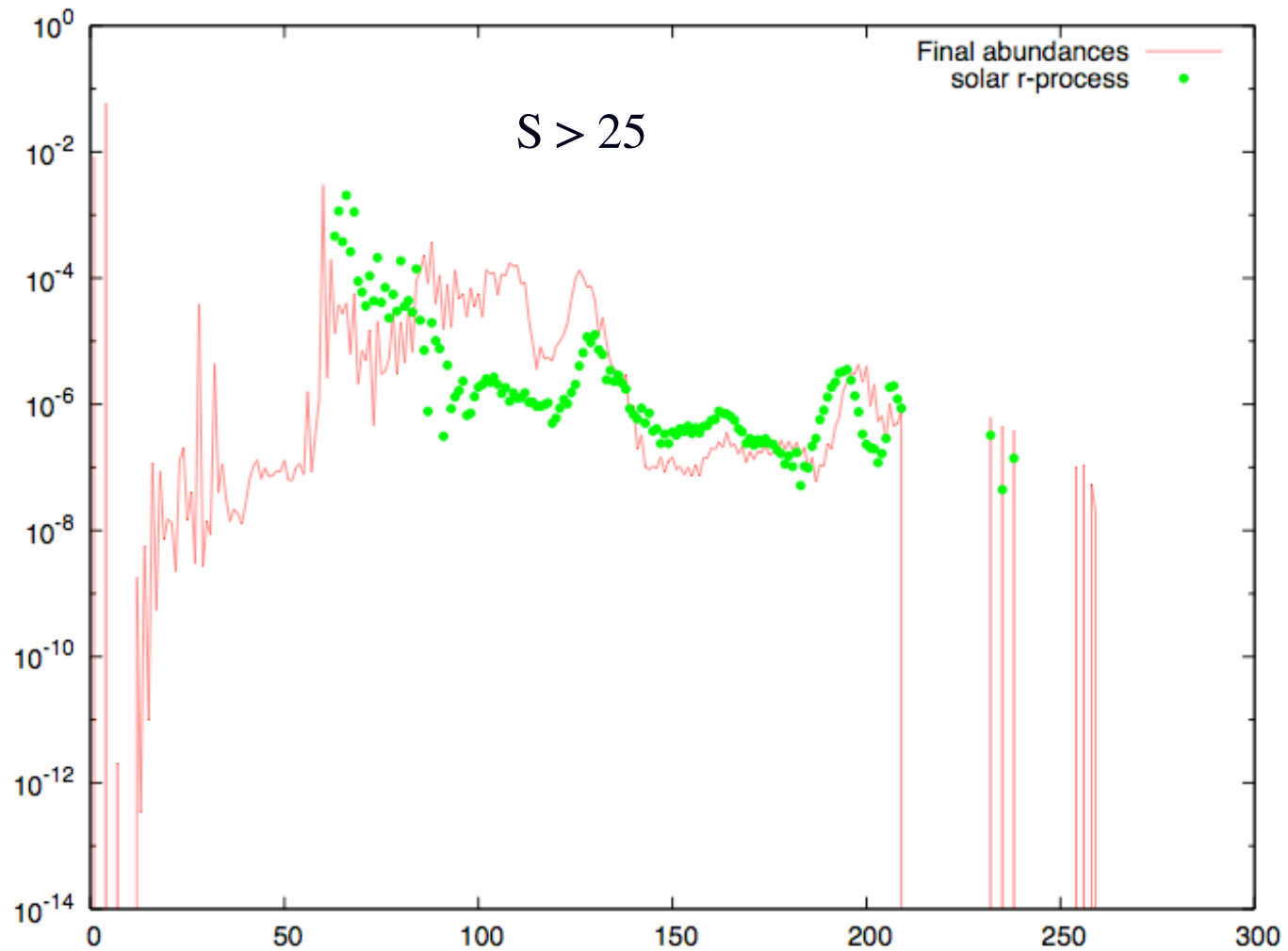


$M (s > 300): 1.25 \times 10^{-4} M_{\odot} ?$

$M (s > 100): 1.07 \times 10^{-5} M_{\odot} ?$

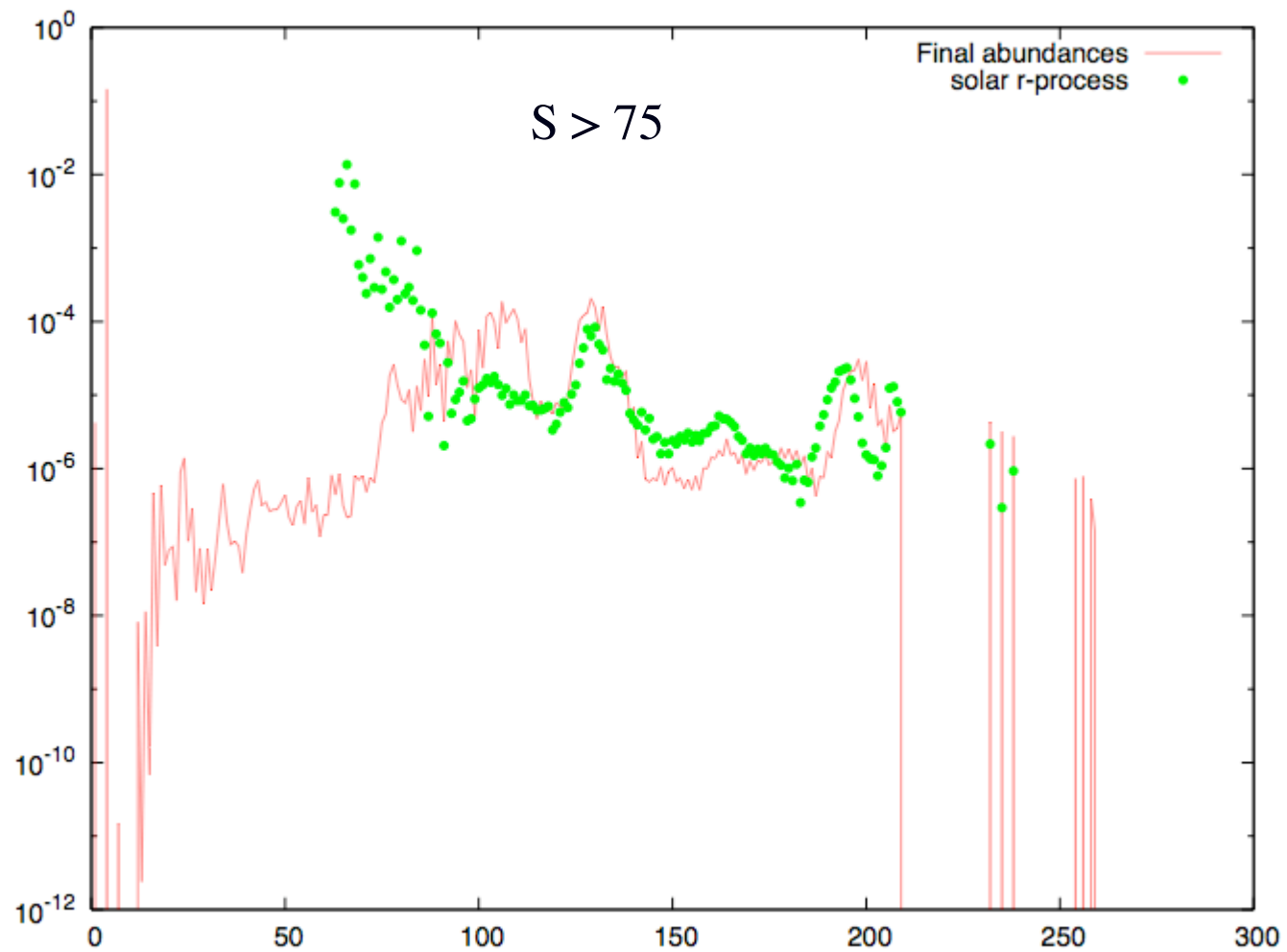
Very Preliminary!!!

Preliminary R-process Calculations for the Long-term Acoustic Mechanism



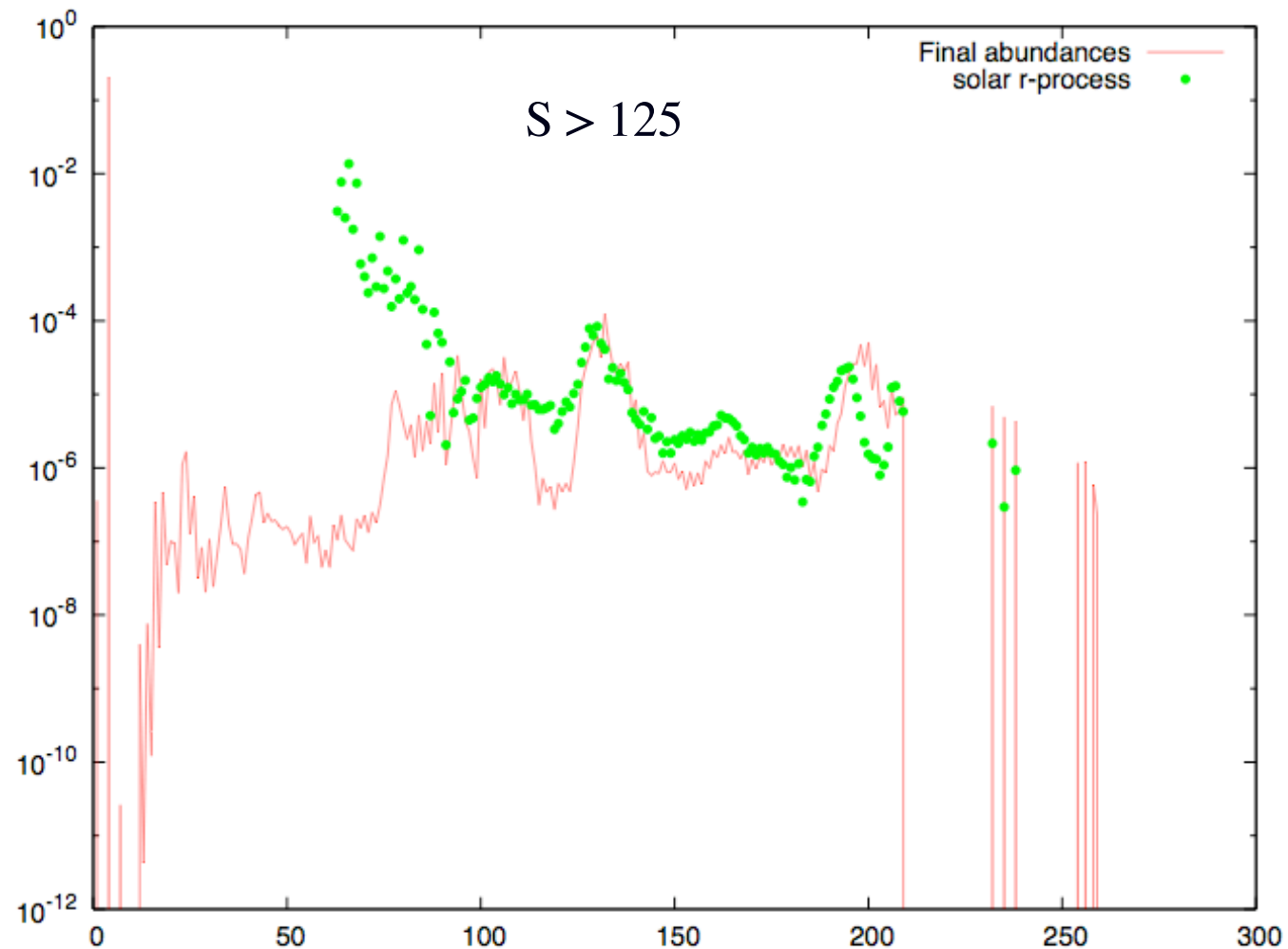
K. Otsuki et al. 2008

Preliminary R-process Calculations for the Long-term Acoustic Mechanism



K. Otsuki et al. 2008

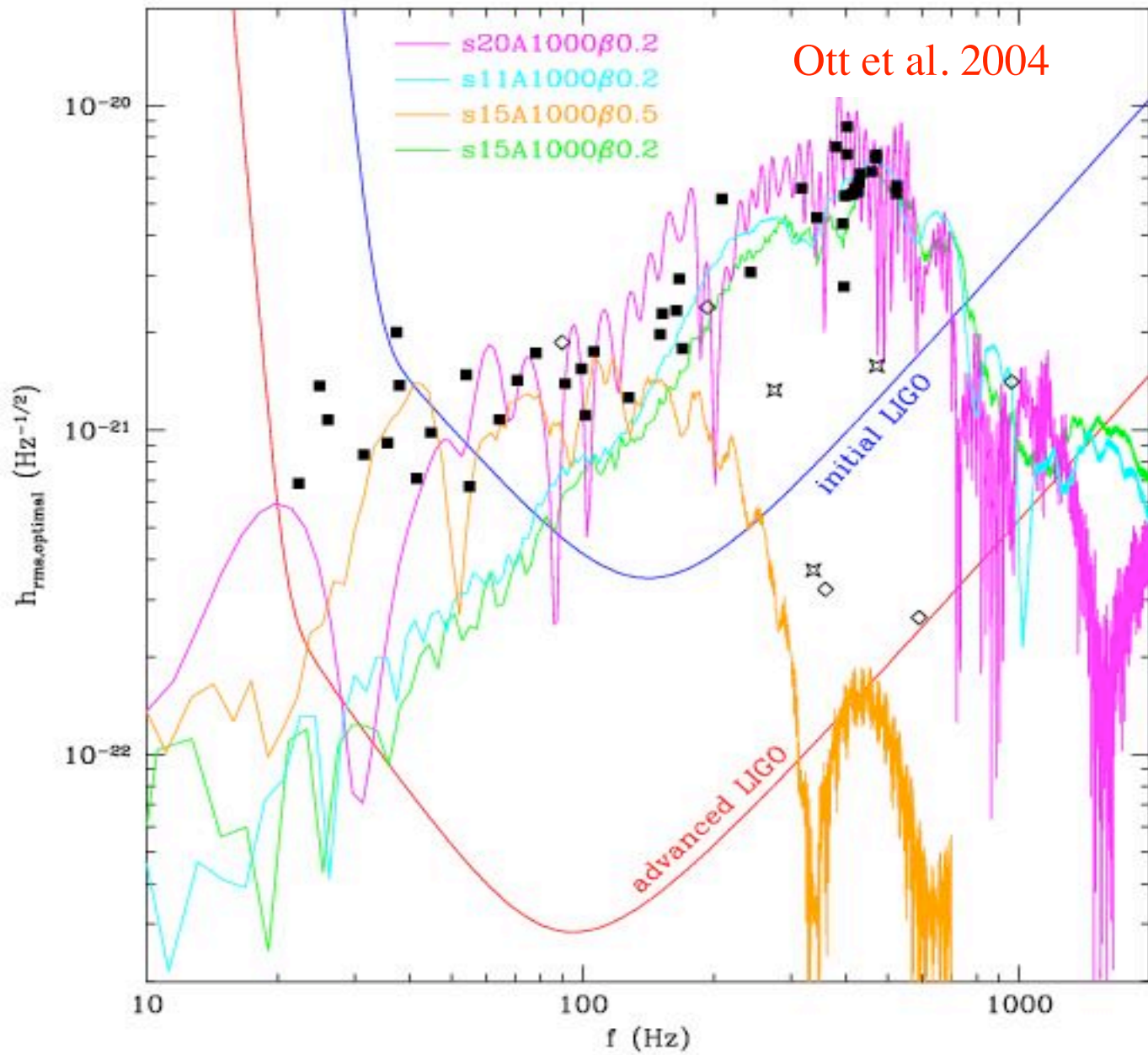
Preliminary R-process Calculations for the Long-term Acoustic Mechanism

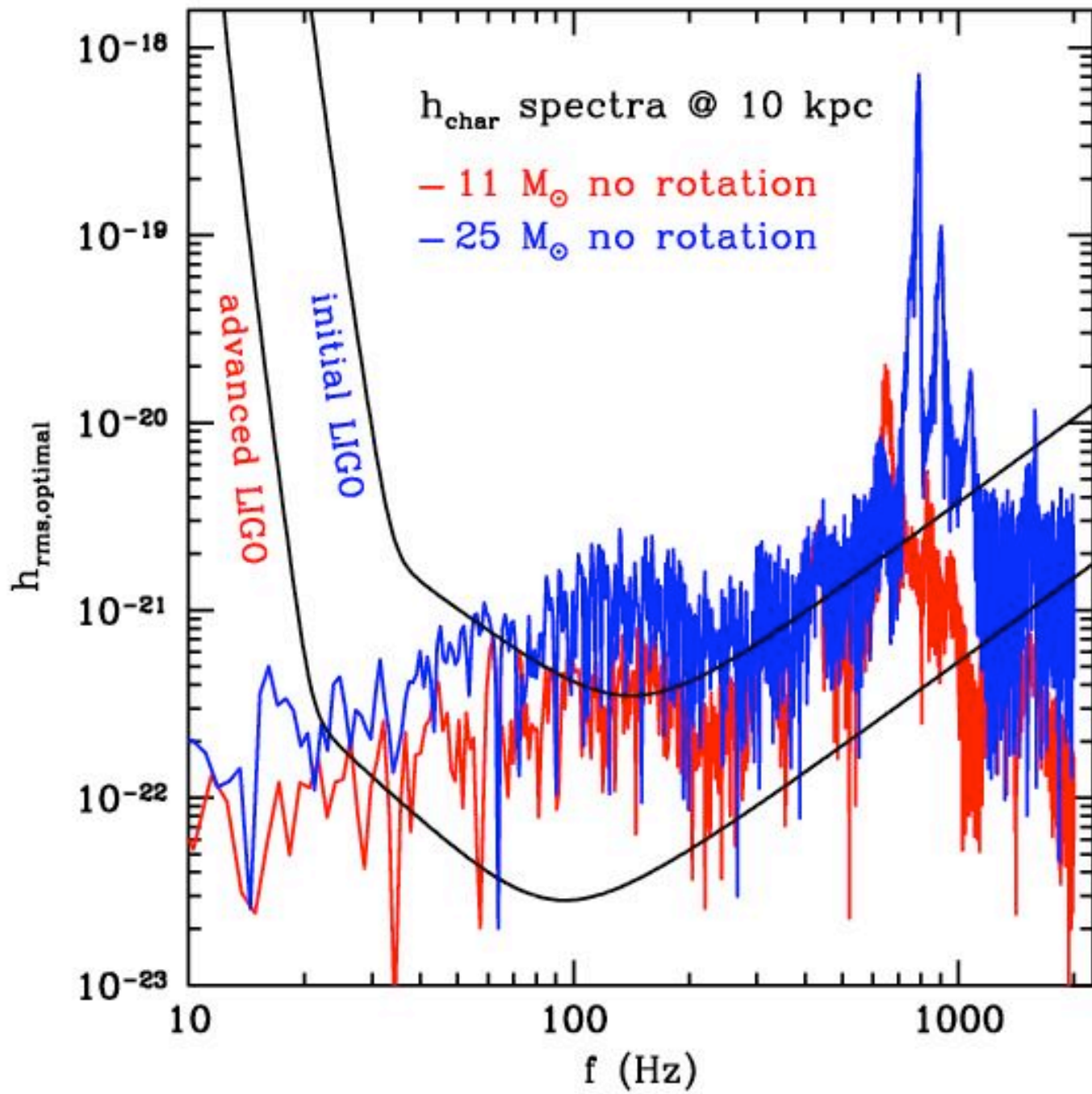


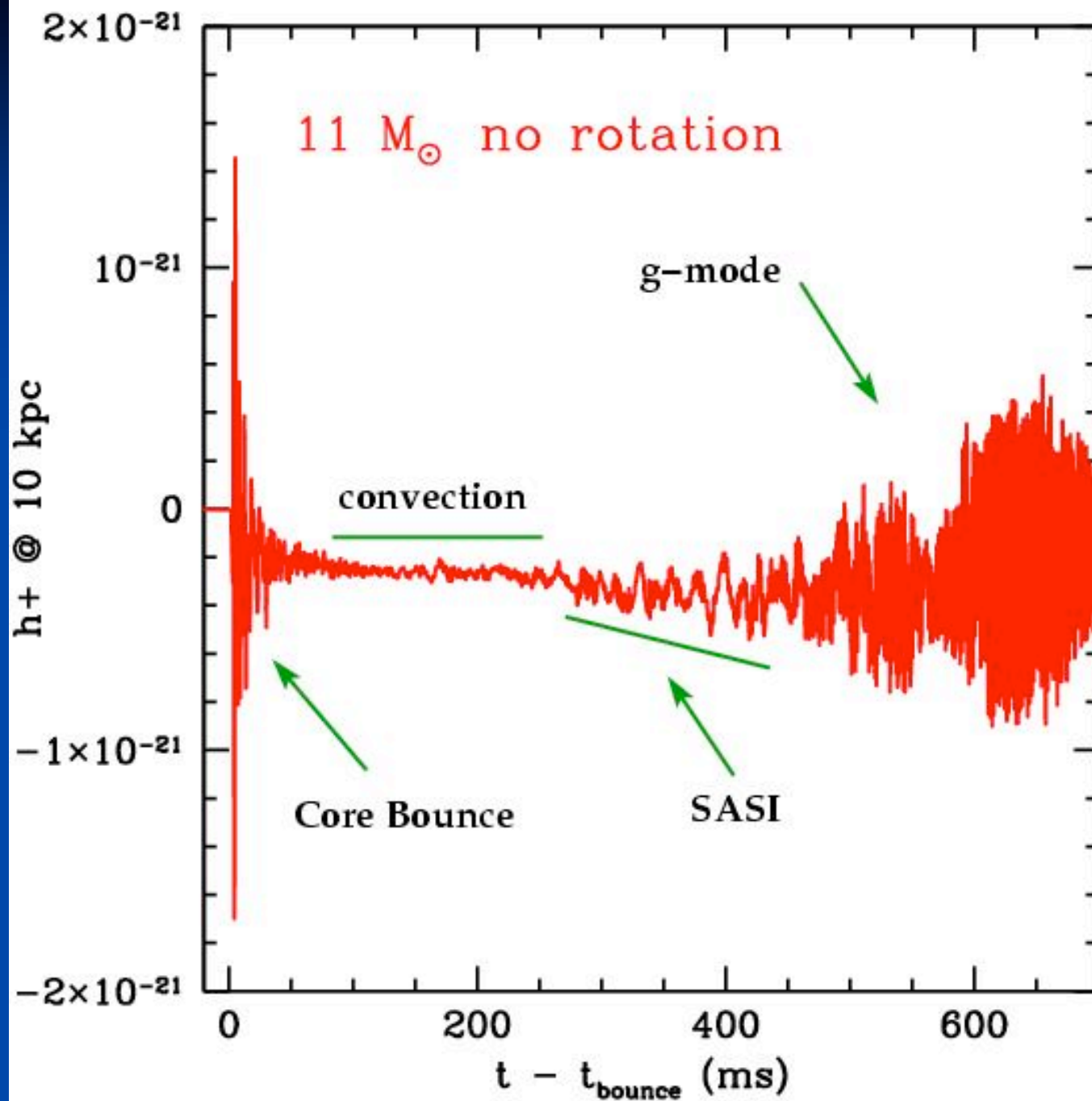
K. Otsuki et al. 2008

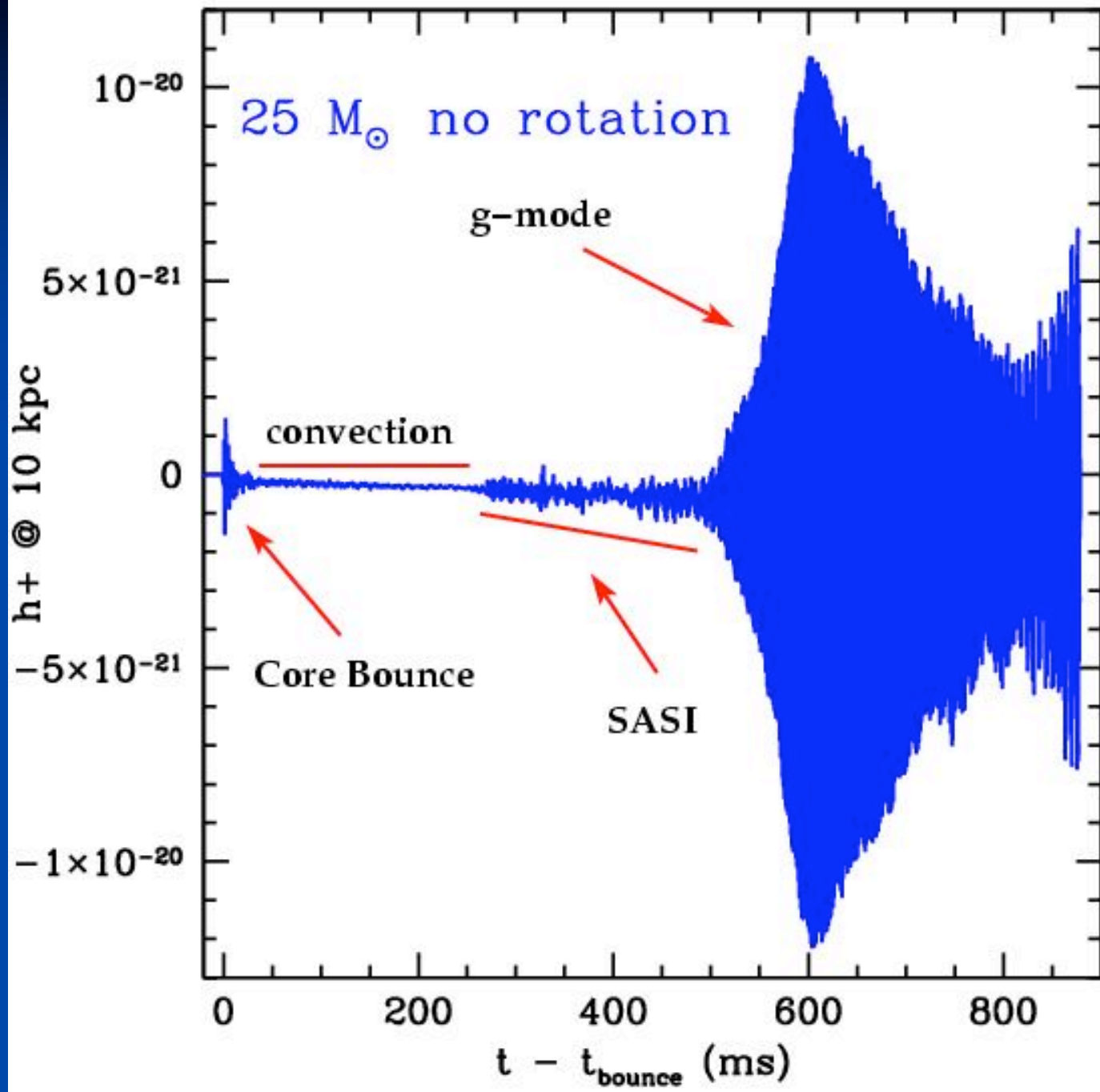
Gravitational Radiation from Supernovae

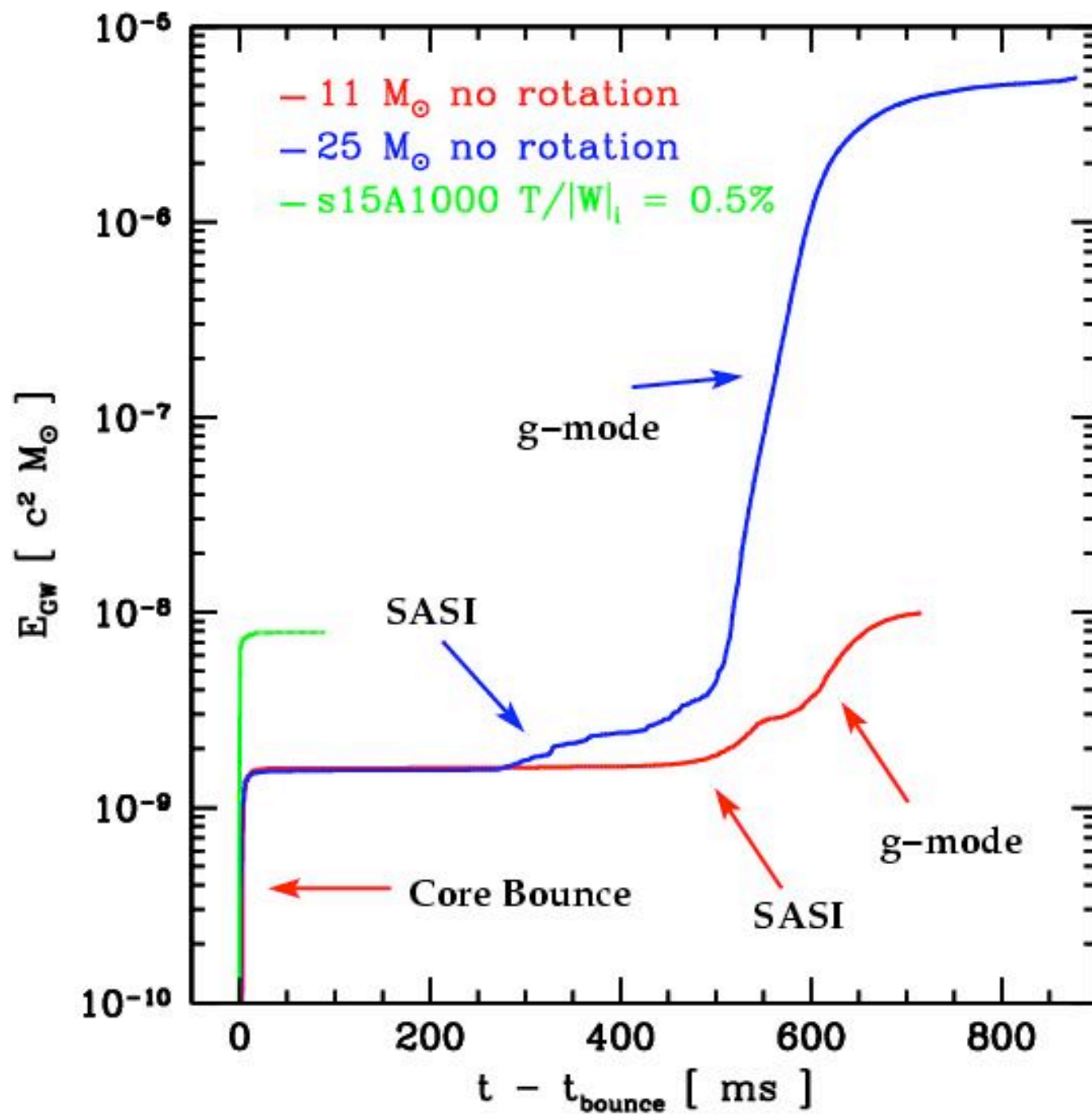
Ott et al. (2004,2006)

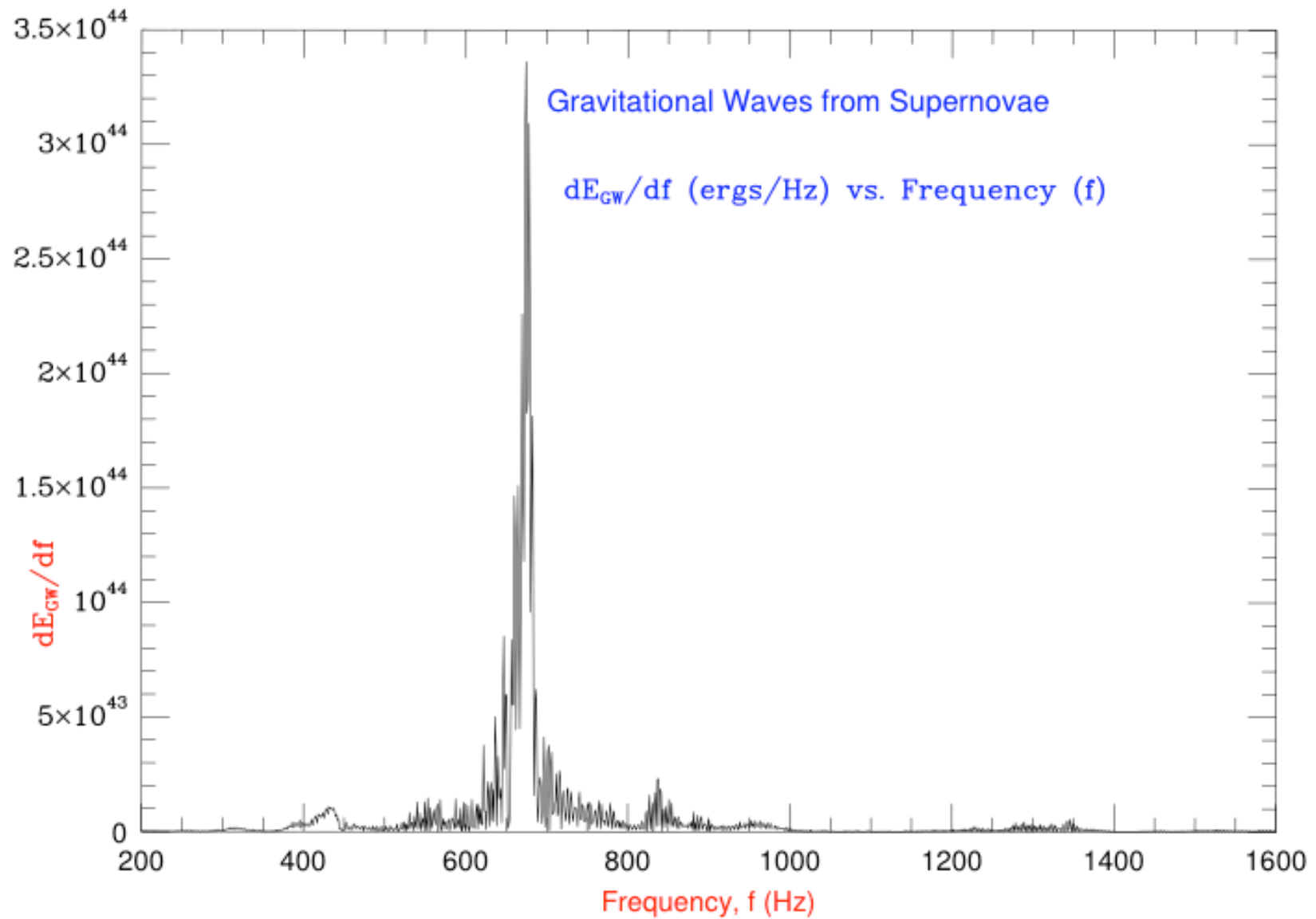


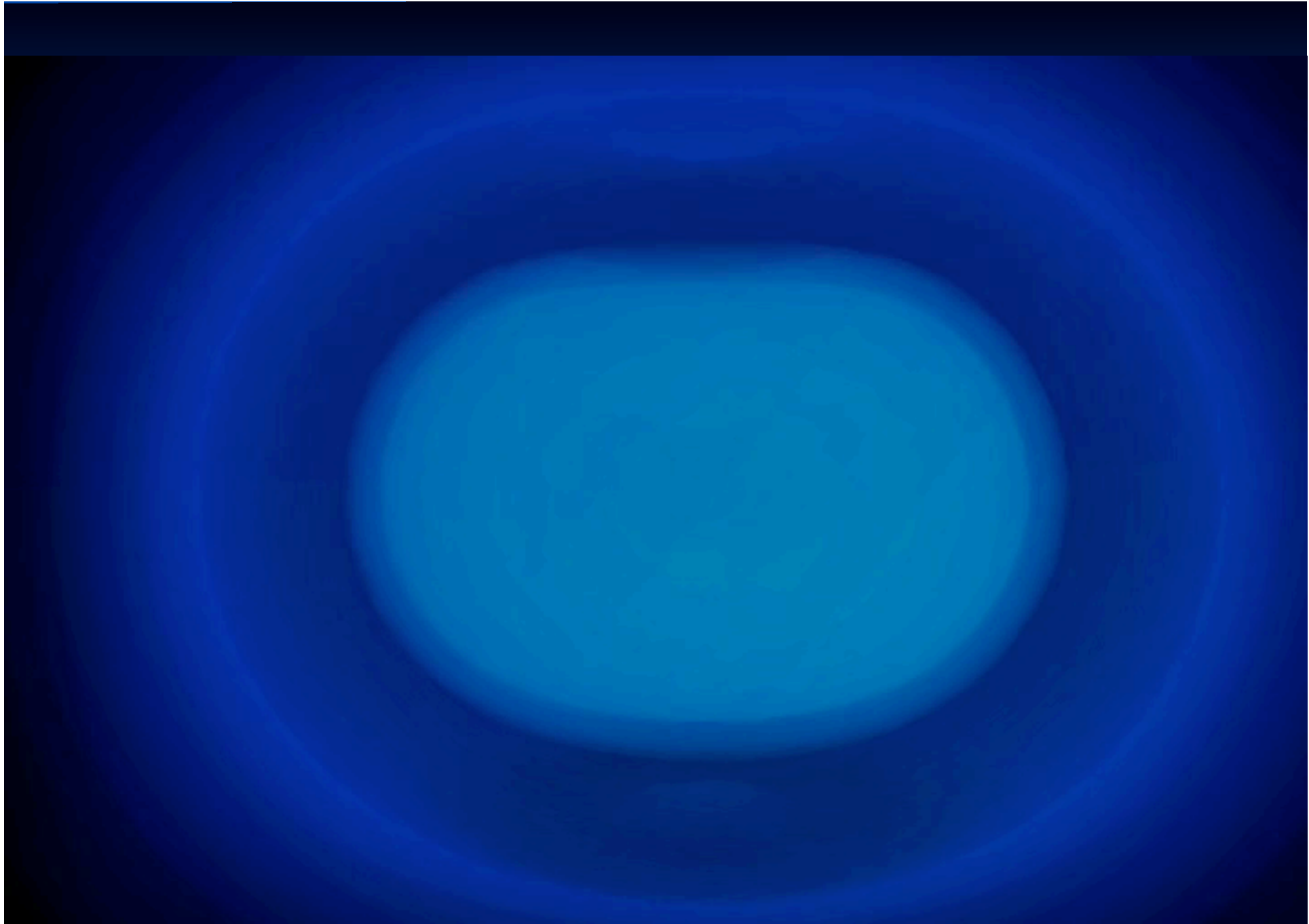








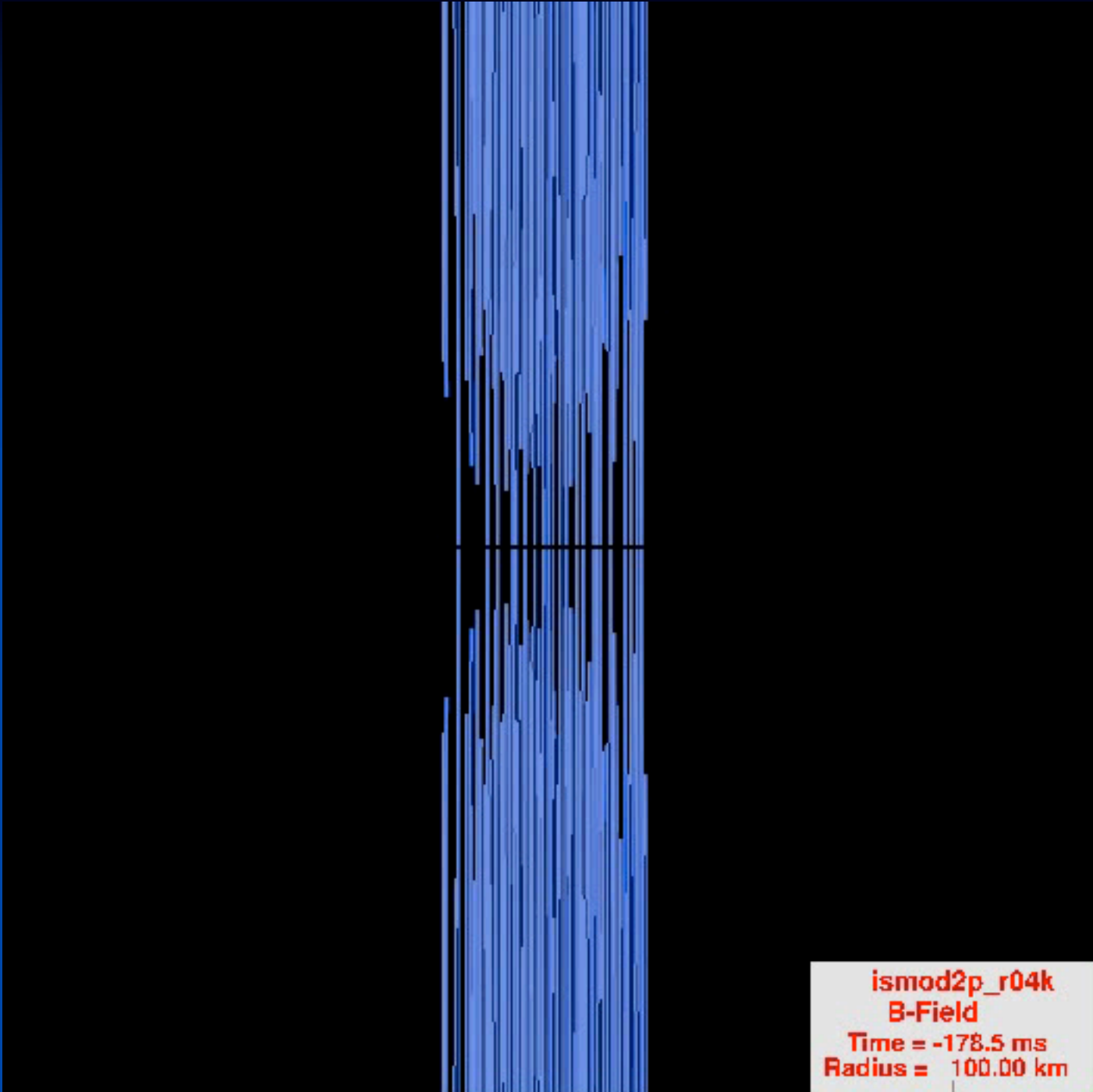




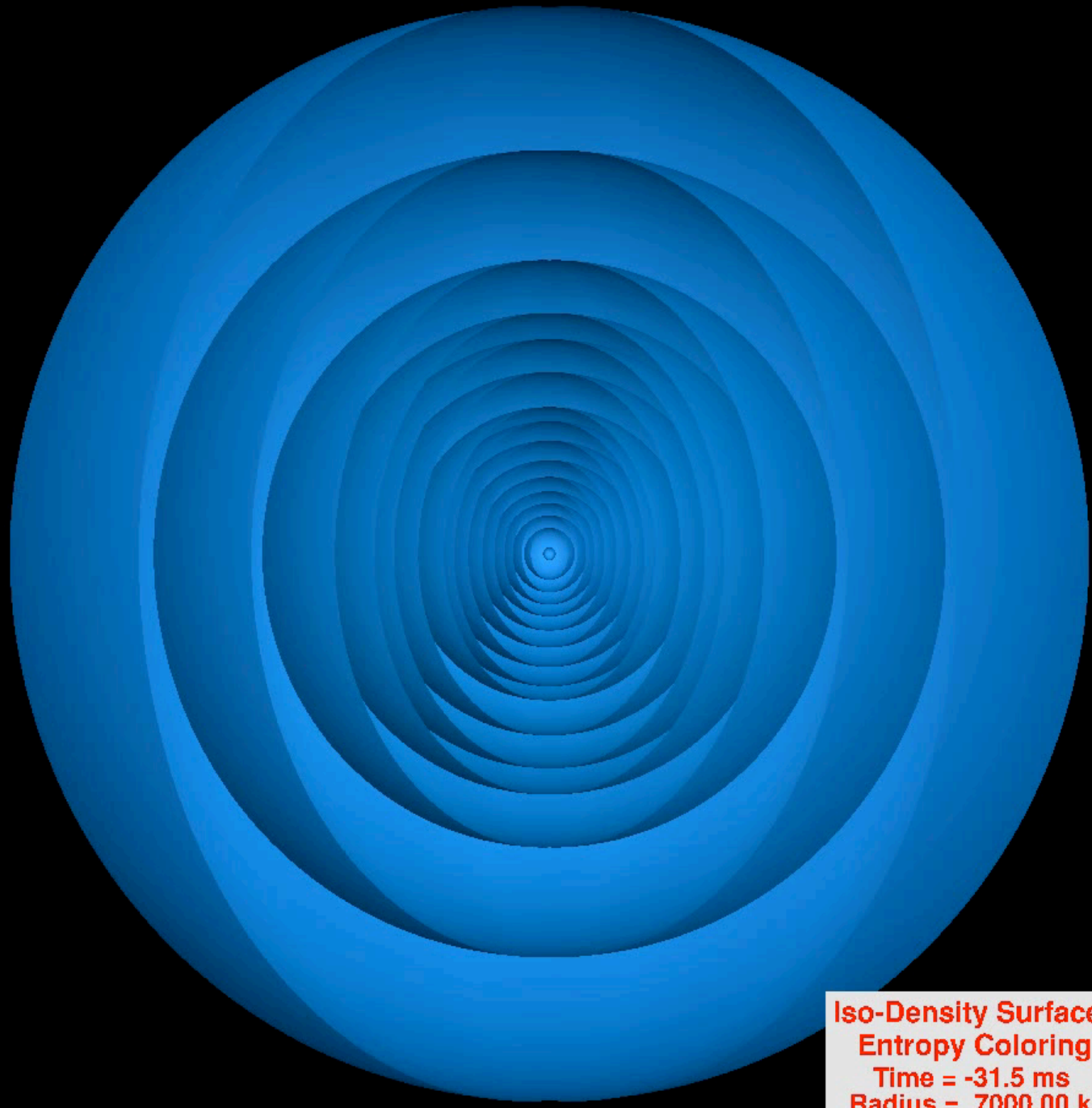
3D; GR; C. Ott et al.

Core-Collapse Supernovae: The Future

- Numerous Explosion Mechanisms identified: **Neutrino-Wind**, **Neutrino/SASI**, **Acoustic/Core-oscillation**, **MHD Jet**, **Hybrids**
- **Symmetry-breaking**, **instabilities** frequently the key to explosion: Simultaneous accretion and explosion
- **Multi-D (2D and 3D) radiation hydrodynamics: 3D effects?**
- Is there an important role for **Rotation**?
- Is there a role for **Magnetic fields**? Pulsar / Magnetar fields?
- **Viscosity?** viscous heating and angular momentum transport
- Equation of state?
- Neutrino physics, rates, neutrino oscillations?
- **Systematics with progenitor:** **kicks**, r-process, SN energy, BH of observables / diagnostics?
- **GRB / hypernova / SN connections!**

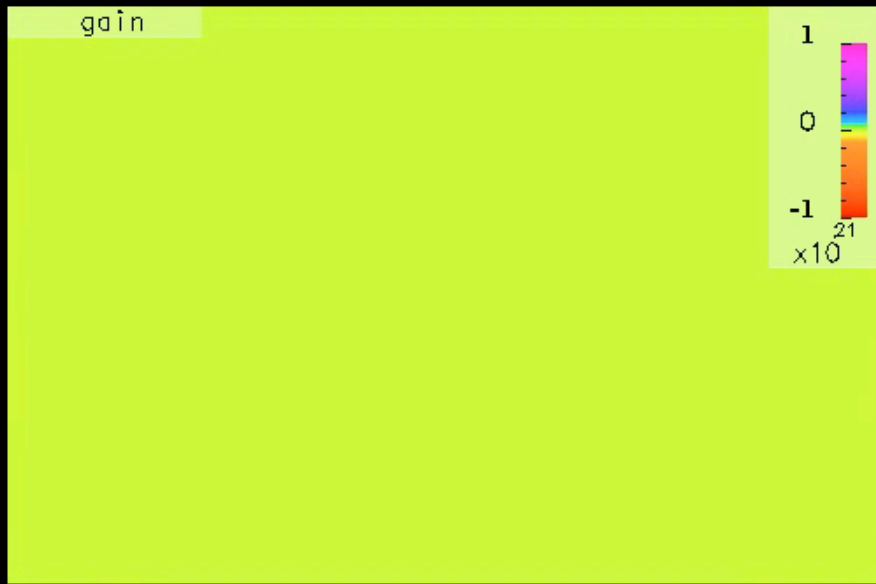
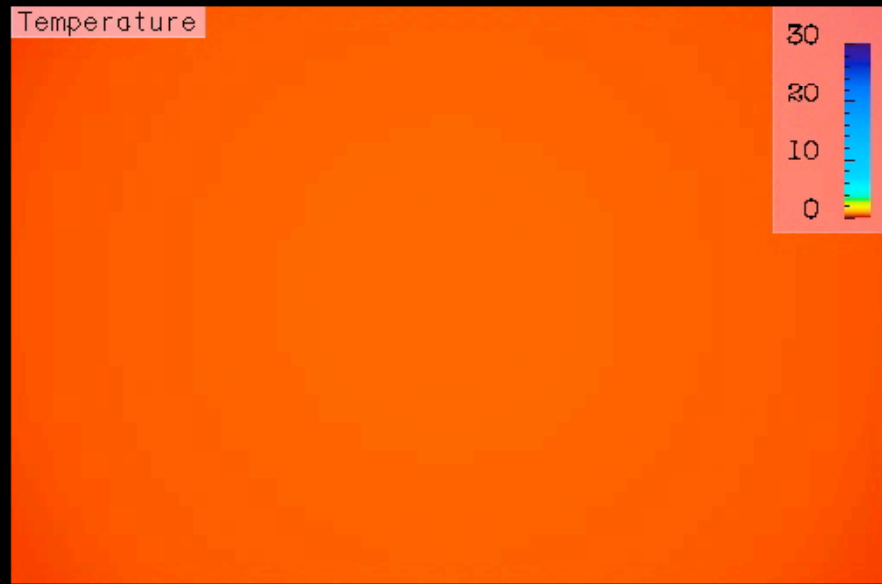


ismod2p_r04k
B-Field
Time = -178.5 ms
Radius = 100.00 km



Iso-Density Surfaces
Entropy Coloring
Time = -31.5 ms
Radius = 7000.00 km

Extra Slides

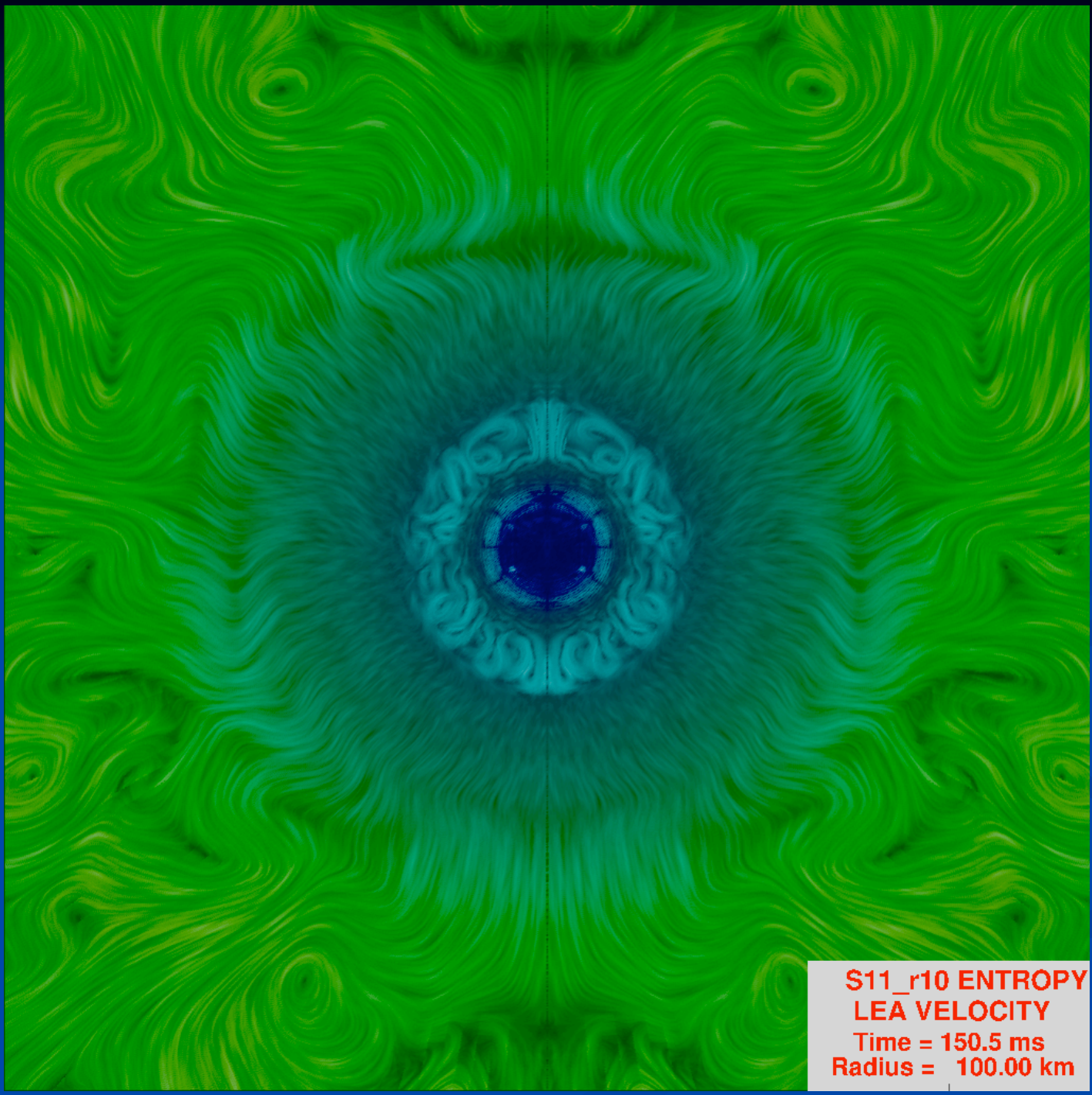


Time = -201.98 ms

Width = 1000.00 km

Summary of Salient Features of Acoustic Mechanism

- All Explosions are Fundamentally Aspherical
- Core $l=1$ g-modes are excited by turbulence and funnel accretion, which persists
- Explosion driven by Acoustic power radiated by Core Oscillations and by neutrino heating (which dominates?)
- Sound pulses steepen into multiple, nested shock waves; r-process entropies possible?
- “Unipolar” / asymmetric-wind explosion: simultaneous explosion and accretion; symmetry breaking is fundamental
- Self-excitation of core oscillation; core is transducer, storage battery?
- Natural mechanism for pulsar proper motions, supernova polarizations, and observed debris morphologies?



S11_r10 ENTROPY
LEA VELOCITY
Time = 150.5 ms
Radius = 100.00 km

A Boltzmann Formalism for Oscillating Neutrinos

P. Strack and A. Burrows

Phys.Rev.D 71:093004,2005 (hep-ph/0504035) & hep-ph/0505056

Quasi-classical Boltzmann equations

- Wigner density matrix, ensemble-averaging \longrightarrow

$$\mathcal{F} = \langle n_i | \rho | n_j \rangle = \begin{pmatrix} f_{\nu e} & f_{e\mu} \\ f_{e\mu}^* & f_{\nu\mu} \end{pmatrix}$$



Diagonal elements: real numbers:
Phase-Space densities



Off-diagonal elements: complex numbers: Macroscopic Overlap densities

$$f_r = \frac{1}{2} (f_{e\mu} + f_{e\mu}^*) \quad (\text{Real part})$$

$$f_i = \frac{1}{2i} (f_{e\mu} - f_{e\mu}^*) \quad (\text{Imaginary part})$$

$$L = \frac{4\pi\hbar c\epsilon}{\Delta m^2 c^4}$$

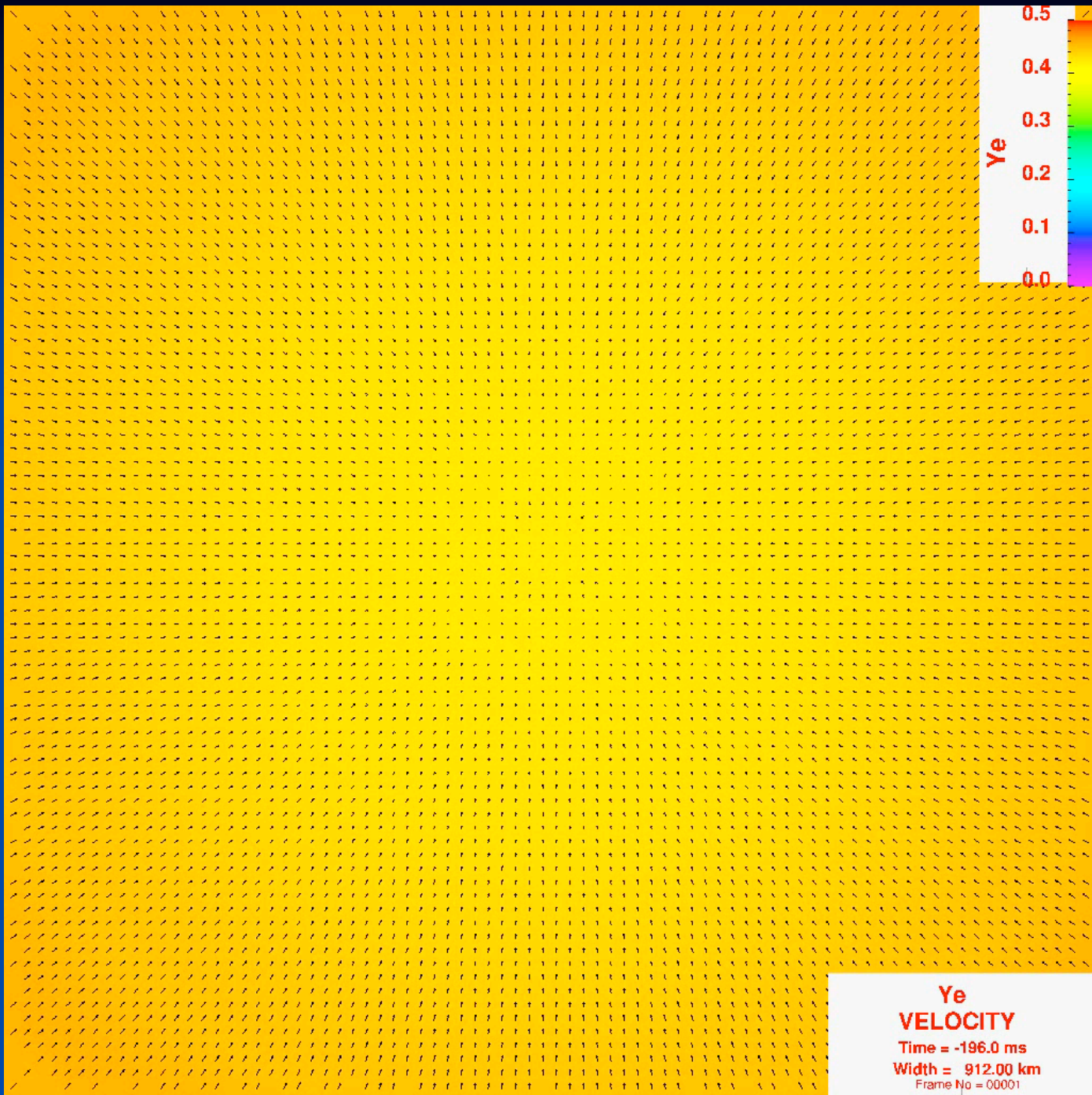
$$A = \left(\frac{L}{\pi c}\right) \frac{2\sqrt{2}G_F}{\hbar} n_e(\mathbf{r})$$

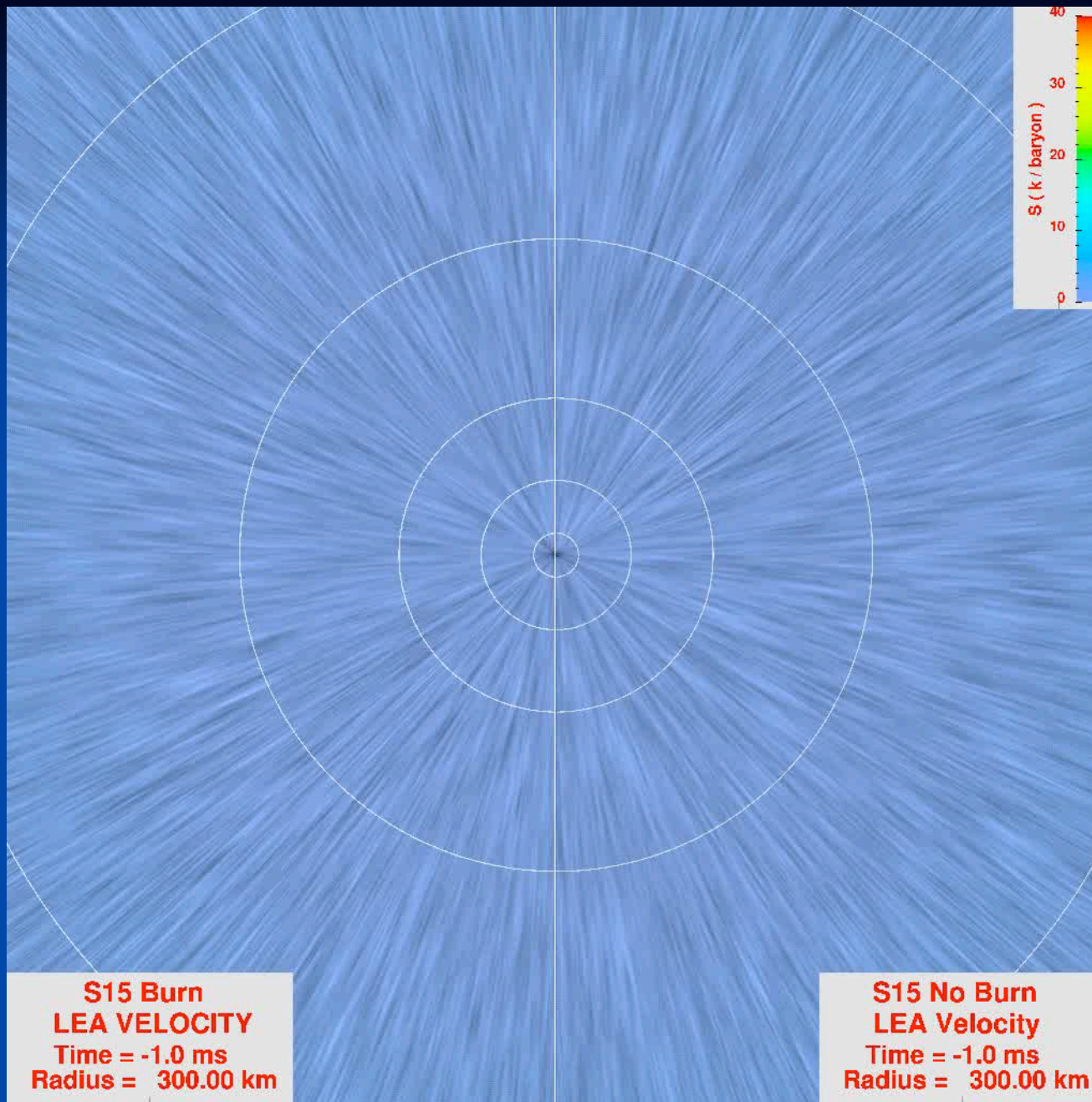
$$\frac{\partial f_{\nu_e}}{\partial t} + \mathbf{v} \cdot \frac{\partial f_{\nu_e}}{\partial \mathbf{r}} + \dot{\mathbf{p}} \cdot \frac{\partial f_{\nu_e}}{\partial \mathbf{p}} = -\frac{2\pi c}{L} f_i \sin 2\theta + C_{\nu_e}$$

$$\frac{\partial f_{\nu_\mu}}{\partial t} + \mathbf{v} \cdot \frac{\partial f_{\nu_\mu}}{\partial \mathbf{r}} + \dot{\mathbf{p}} \cdot \frac{\partial f_{\nu_\mu}}{\partial \mathbf{p}} = \frac{2\pi c}{L} f_i \sin 2\theta + C_{\nu_\mu}$$

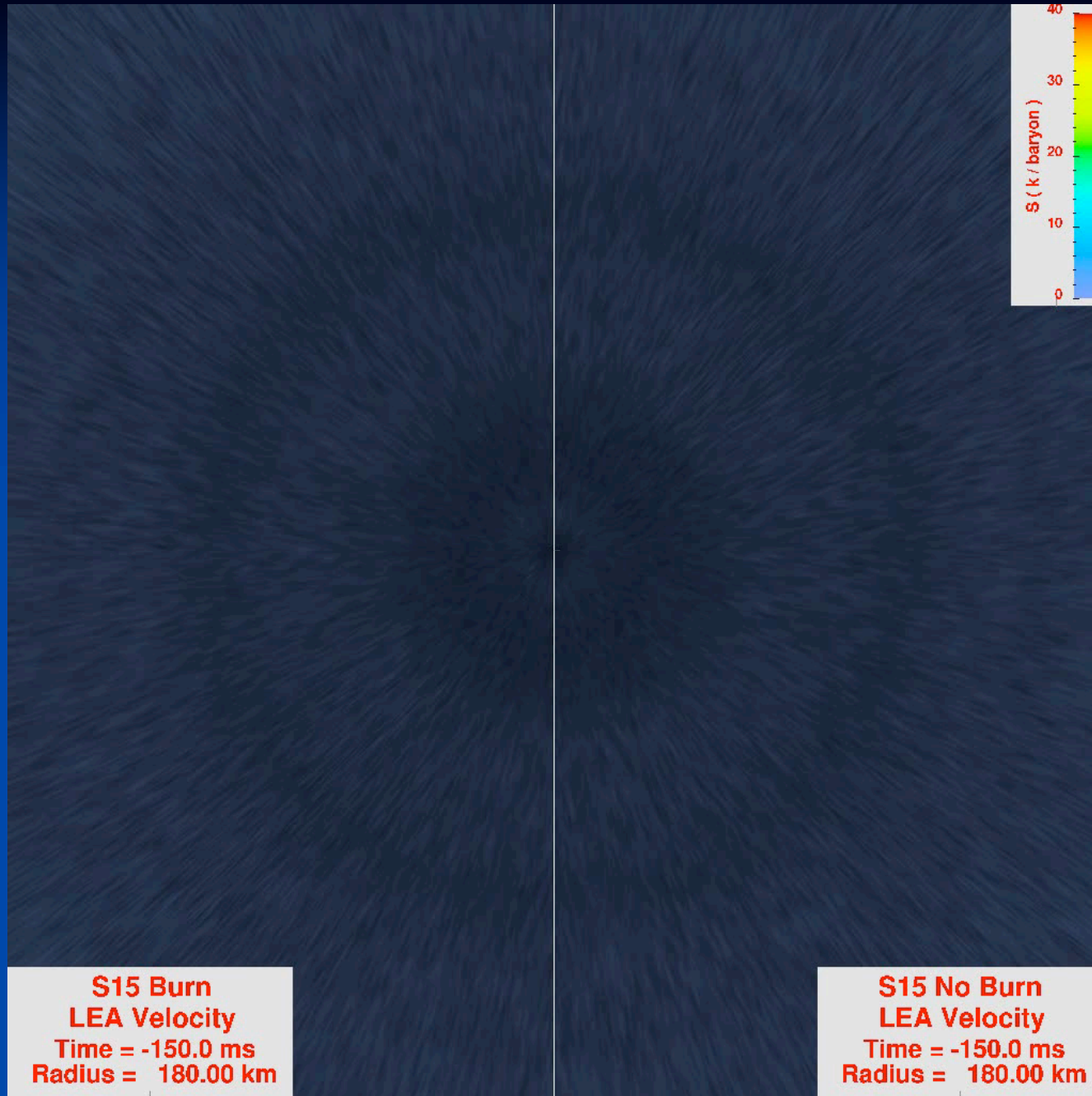
$$\frac{\partial f_r}{\partial t} + \mathbf{v} \cdot \frac{\partial f_r}{\partial \mathbf{r}} + \dot{\mathbf{p}} \cdot \frac{\partial f_r}{\partial \mathbf{p}} = -\frac{2\pi c}{L} f_i (\cos 2\theta - A)$$

$$\frac{\partial f_i}{\partial t} + \mathbf{v} \cdot \frac{\partial f_i}{\partial \mathbf{r}} + \dot{\mathbf{p}} \cdot \frac{\partial f_i}{\partial \mathbf{p}} = \frac{2\pi c}{L} \left(\frac{f_{\nu_e} - f_{\nu_\mu}}{2} \sin 2\theta + f_r (\cos 2\theta - A) \right)$$

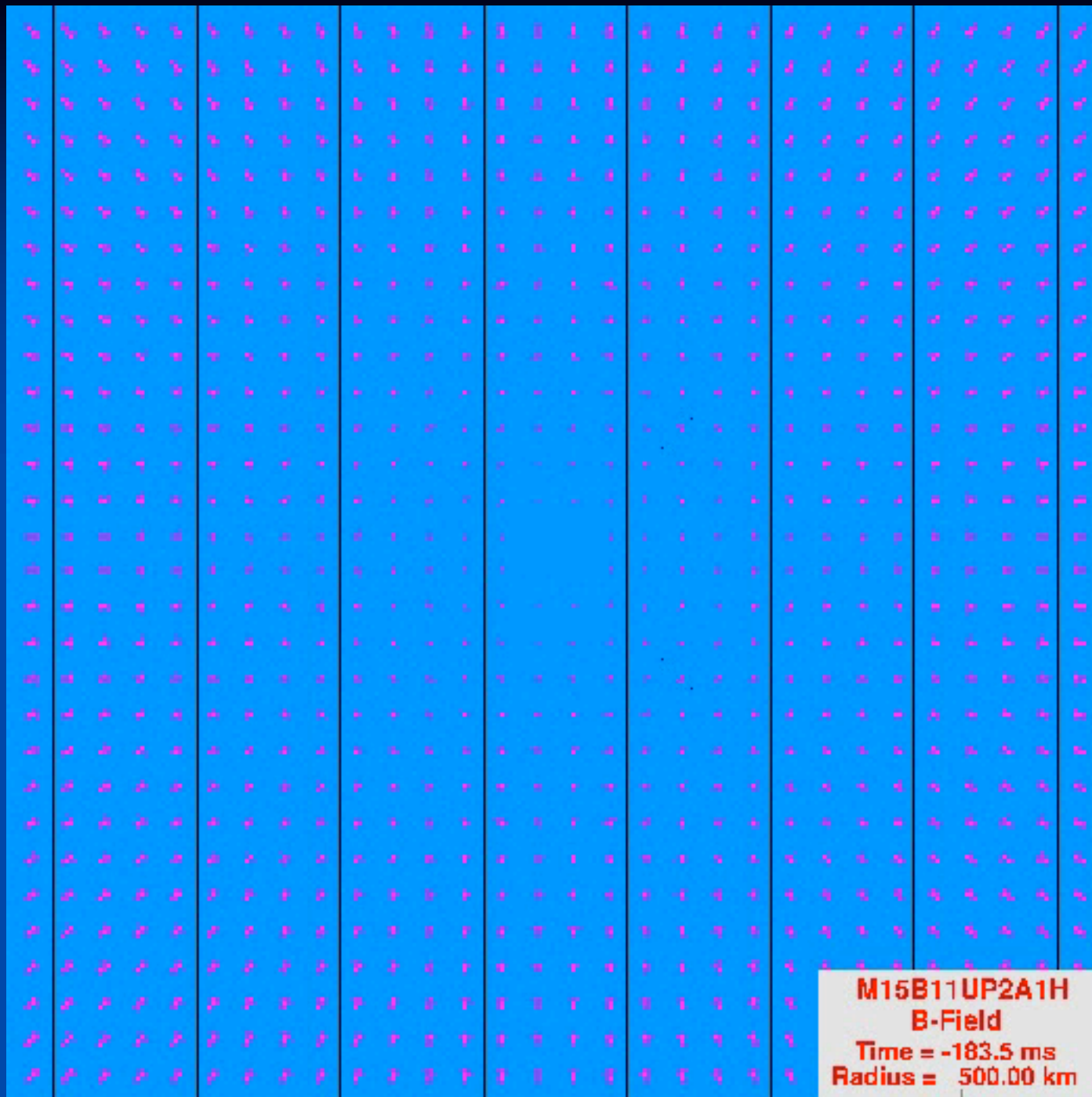




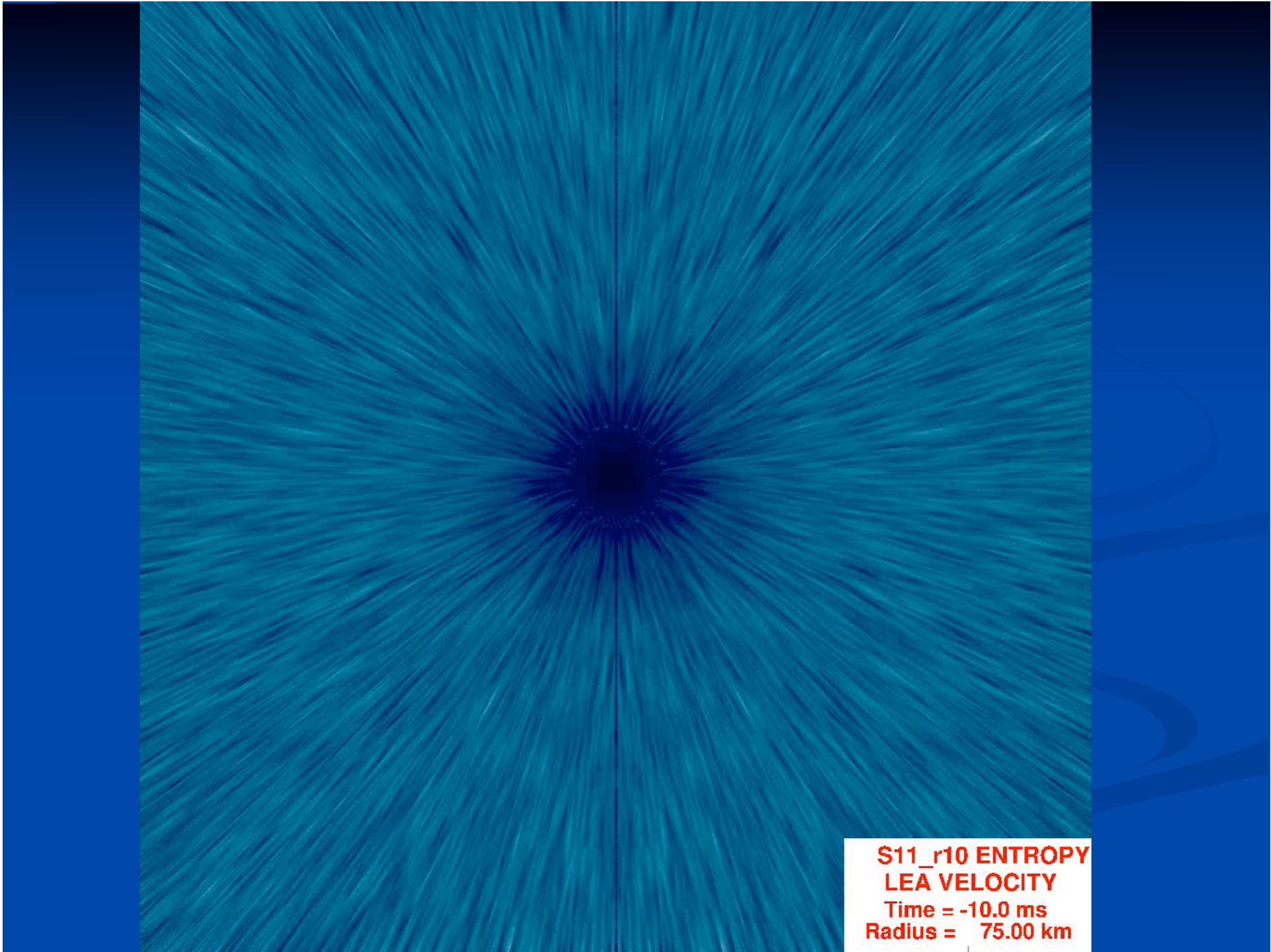
With and Without Burning



With and Without Burning



M15B11UP2A1H
B-Field
Time = -183.5 ms
Radius = 500.00 km



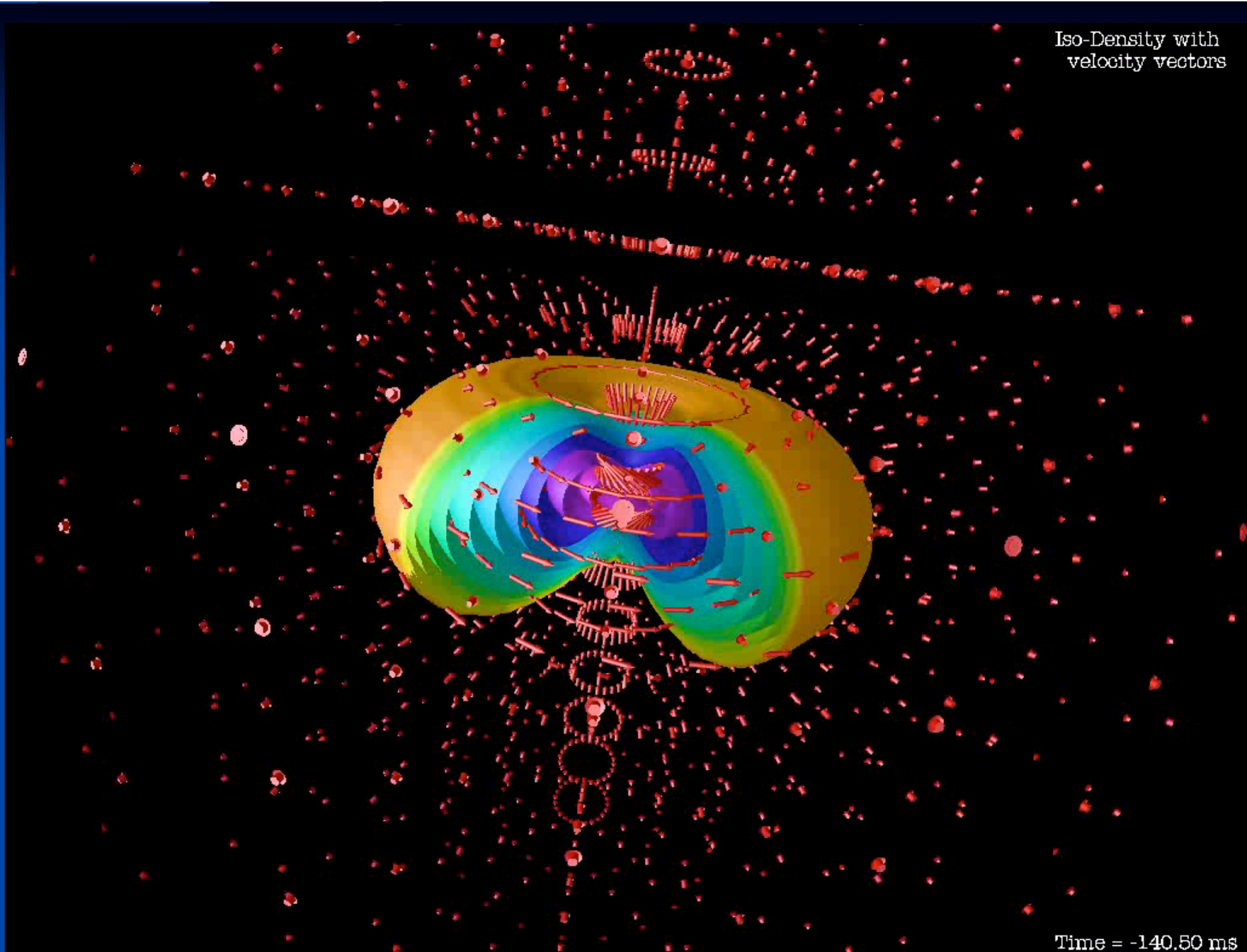
S11_r10 ENTROPY
LEA VELOCITY
Time = -10.0 ms
Radius = 75.00 km

Accretion-Induced Collapse of O-Ne-Mg White Dwarfs

Dessart, Burrows, Ott, Livne, Yoon, & Langer 2005

Rapid Rotation!

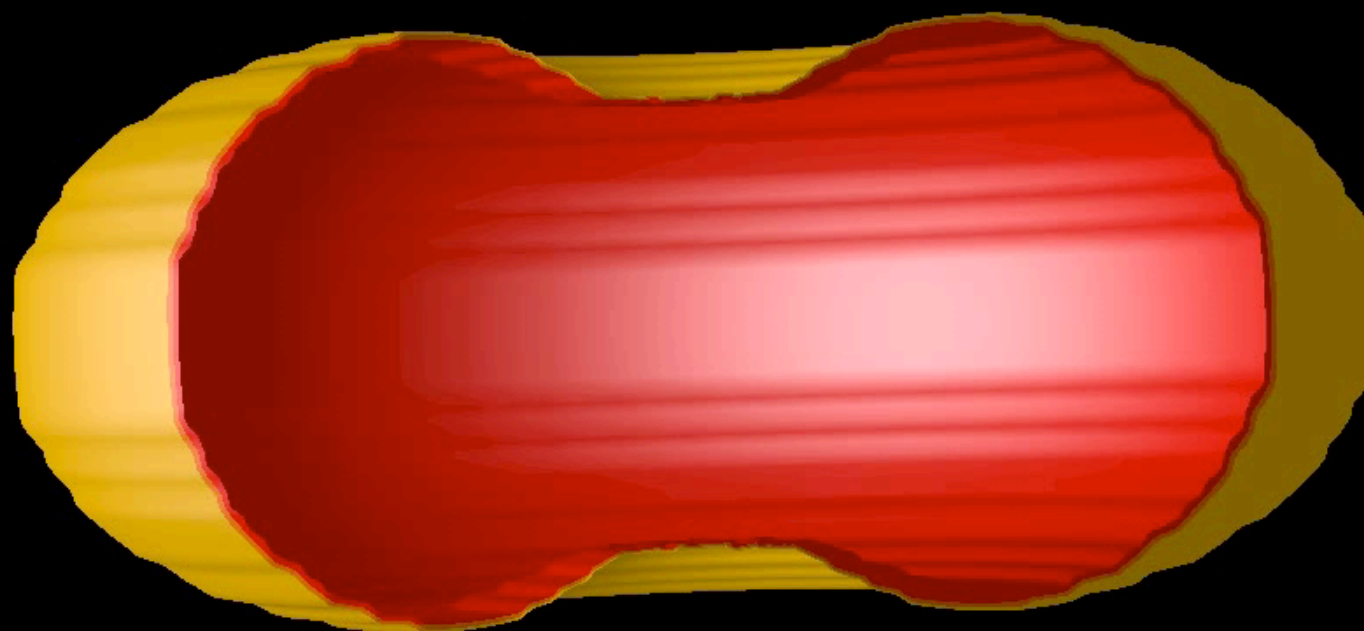
Iso-Density with
velocity vectors



Time = -140.50 ms

AIC: 1.92 solar masses:

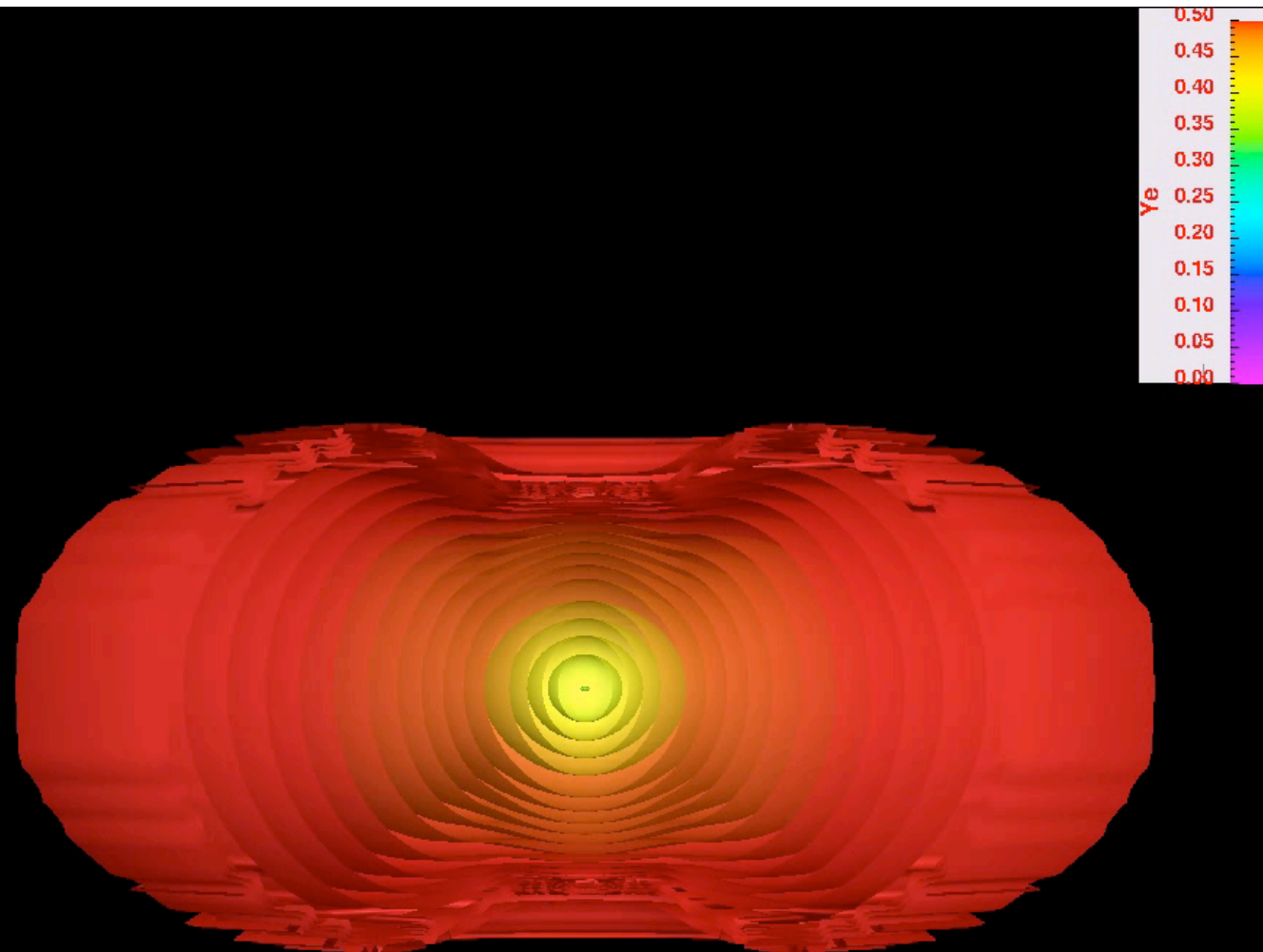
Entropy



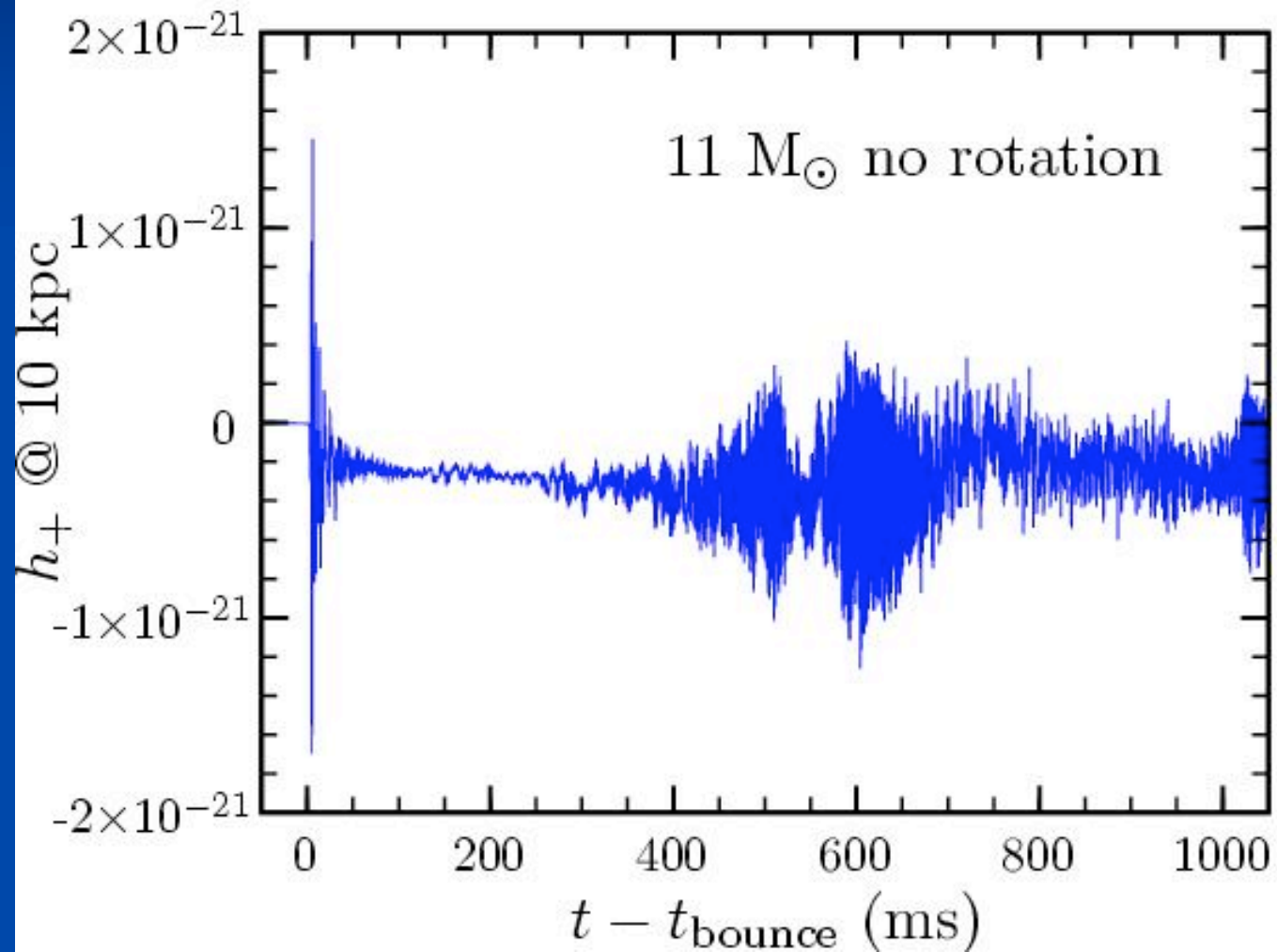
$t = -67.00$ ms

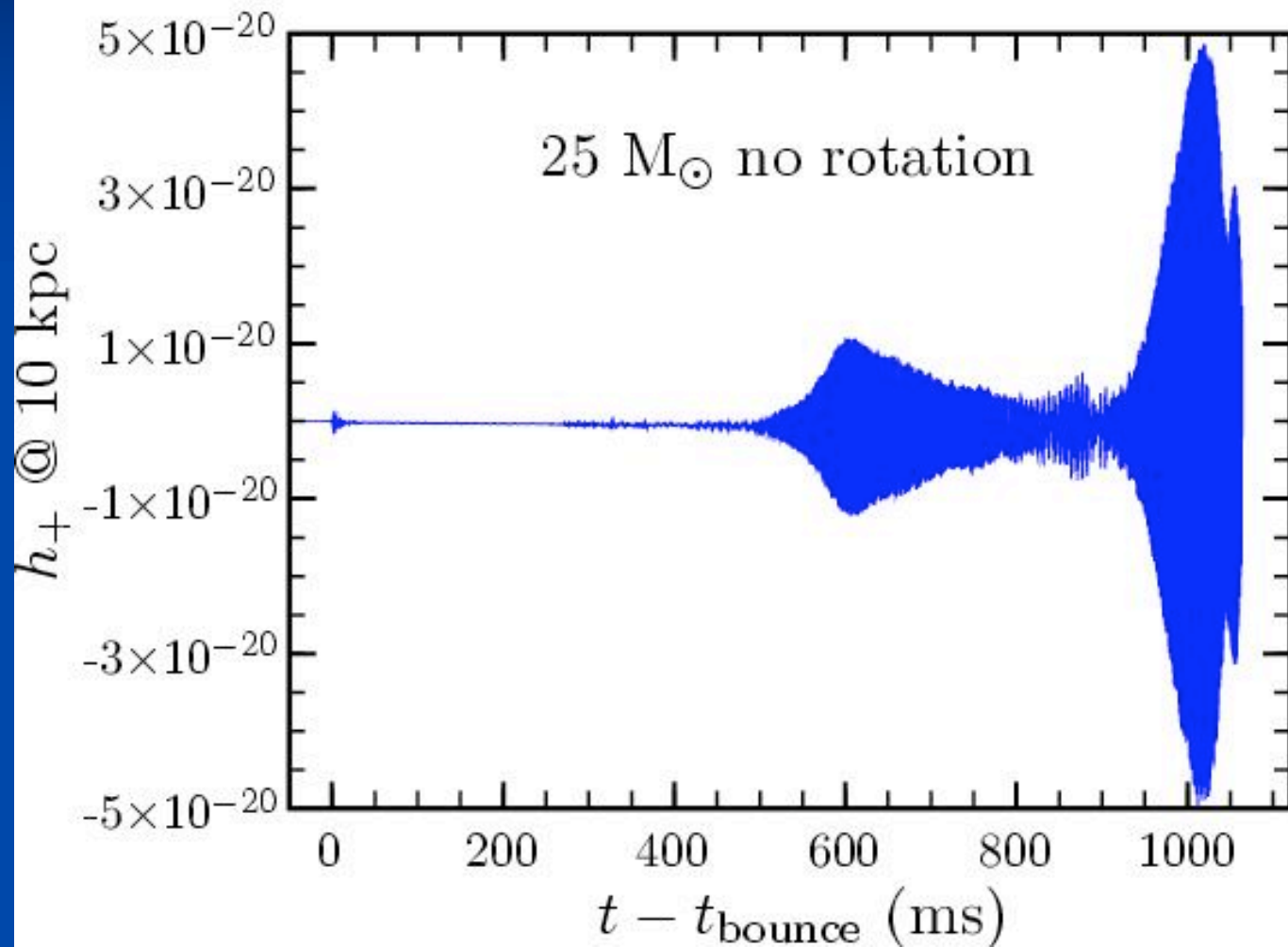
AIC: 1.92 solar
masses:

Iso-Energy/ Y_e
coloring

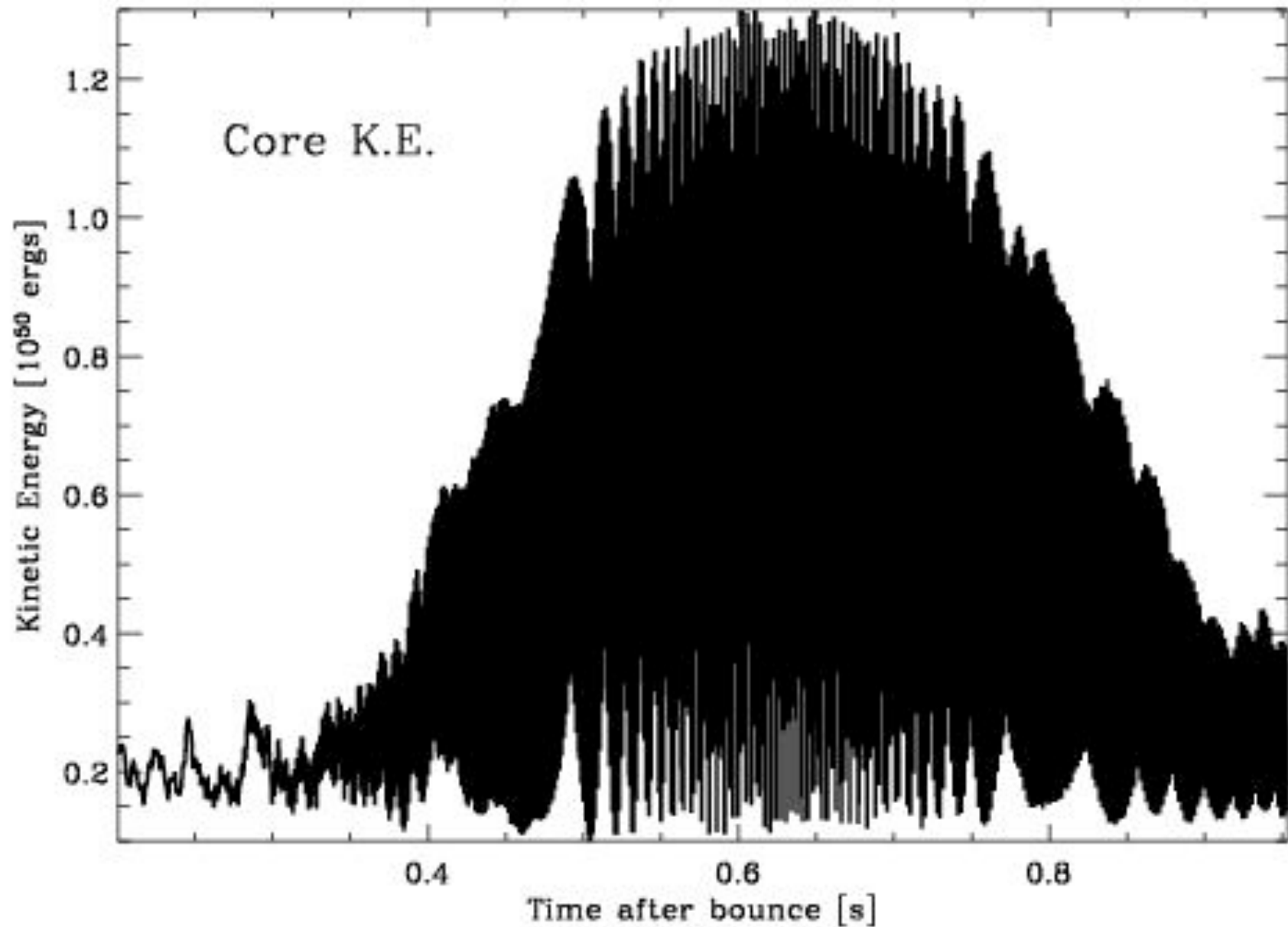


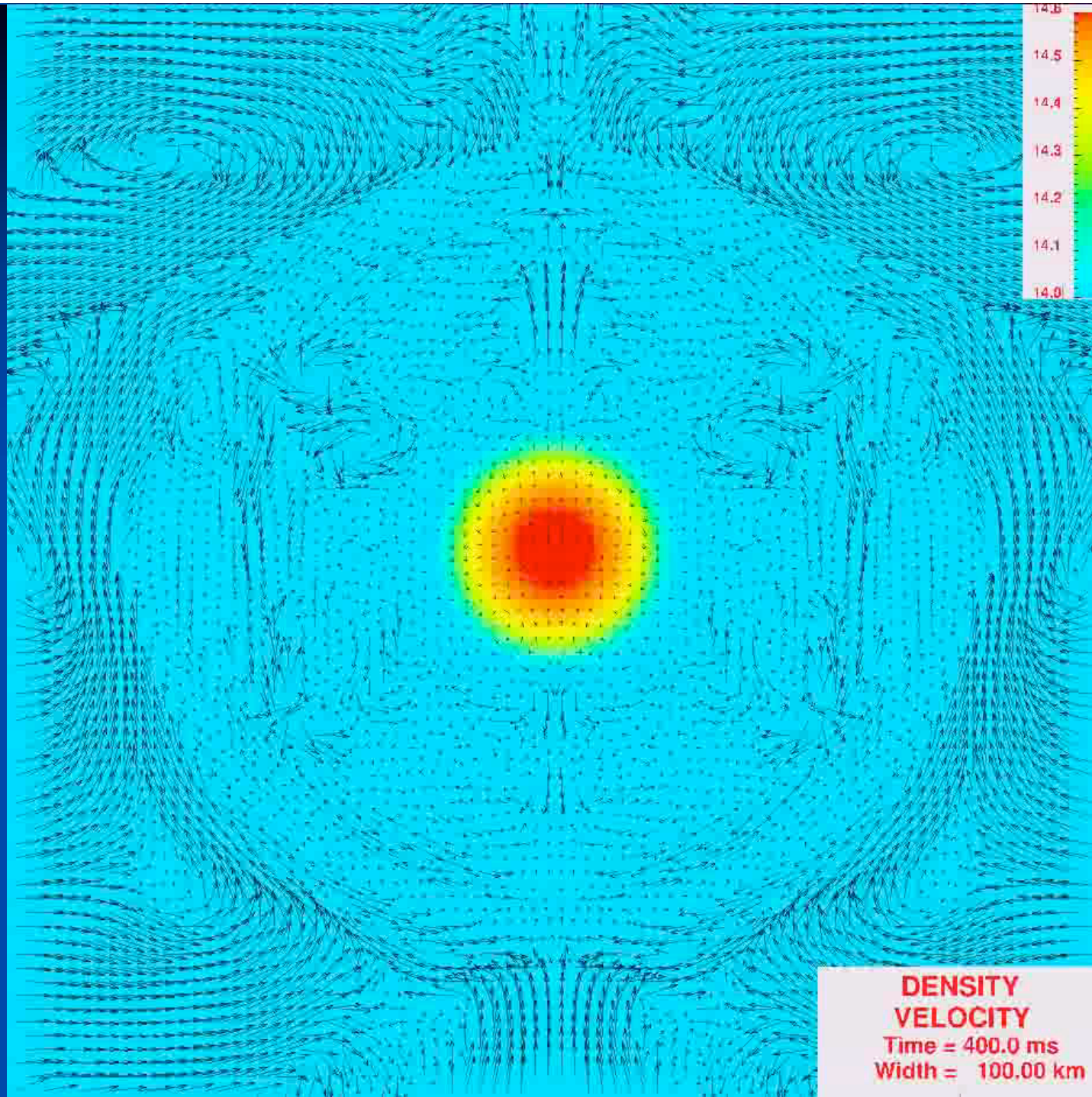
Iso-Energy Surfaces
 Y_e Coloring
Time = -26.5 ms
Radius = 2250.00 km



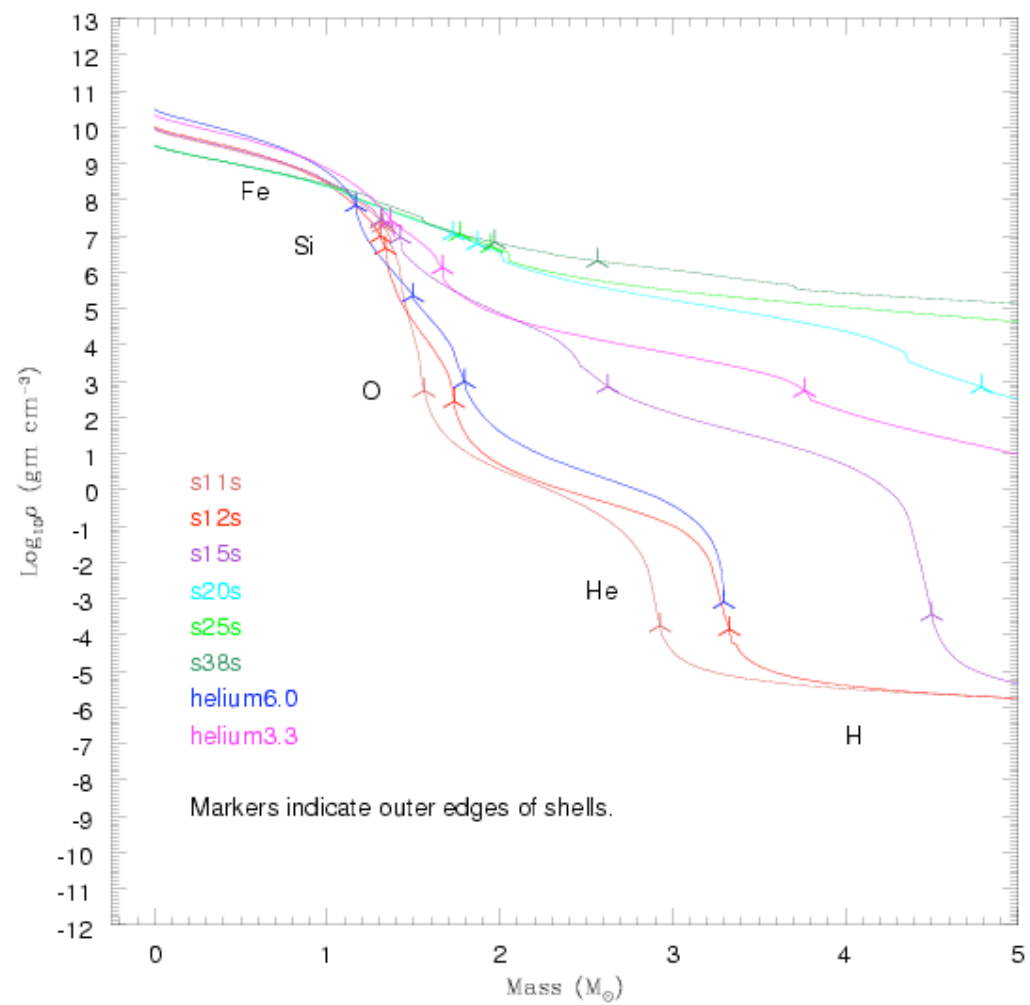


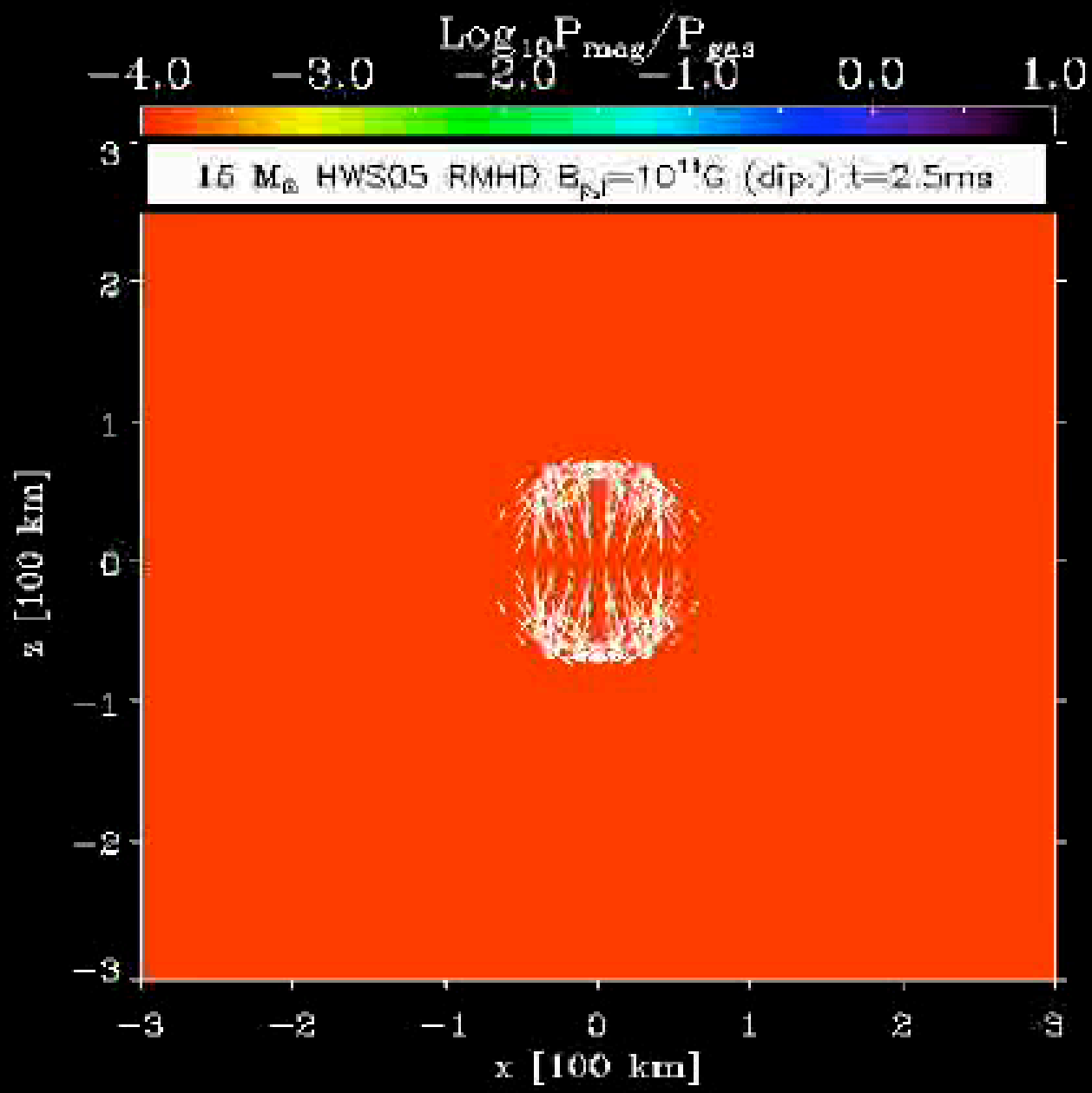
Evolution of Core Kinetic Energy: 11 solar-mass Progenitor



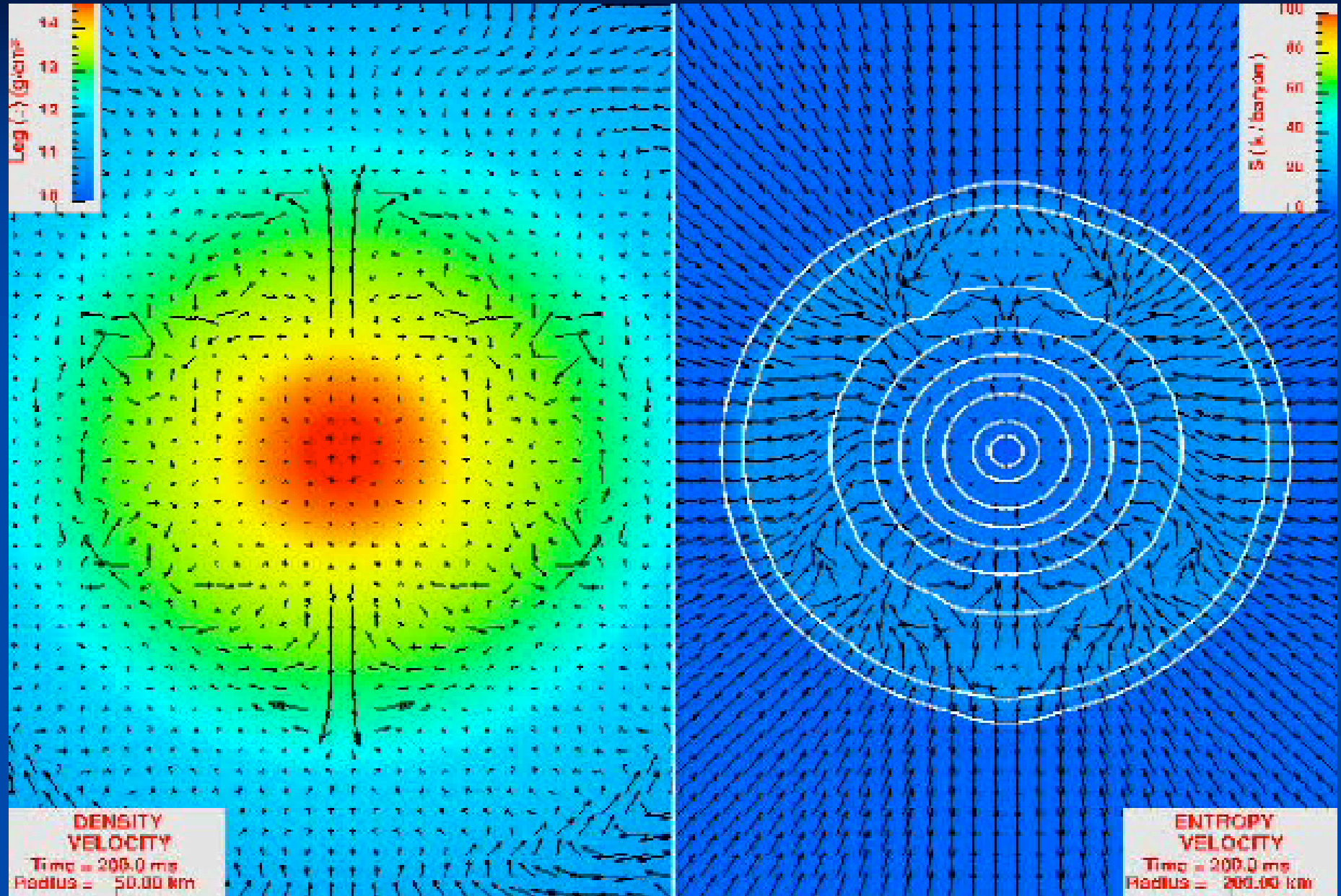


Progenitor Models

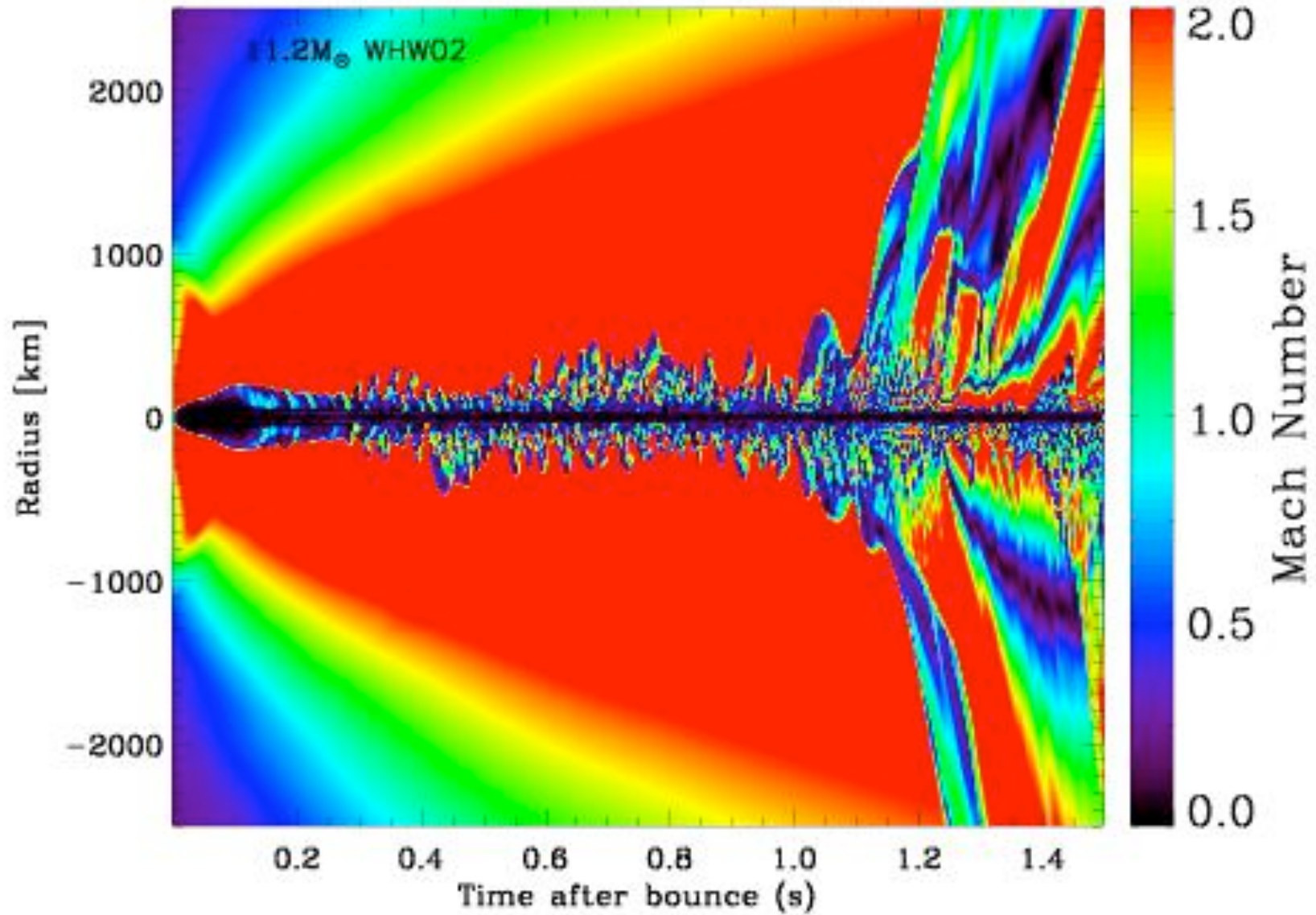


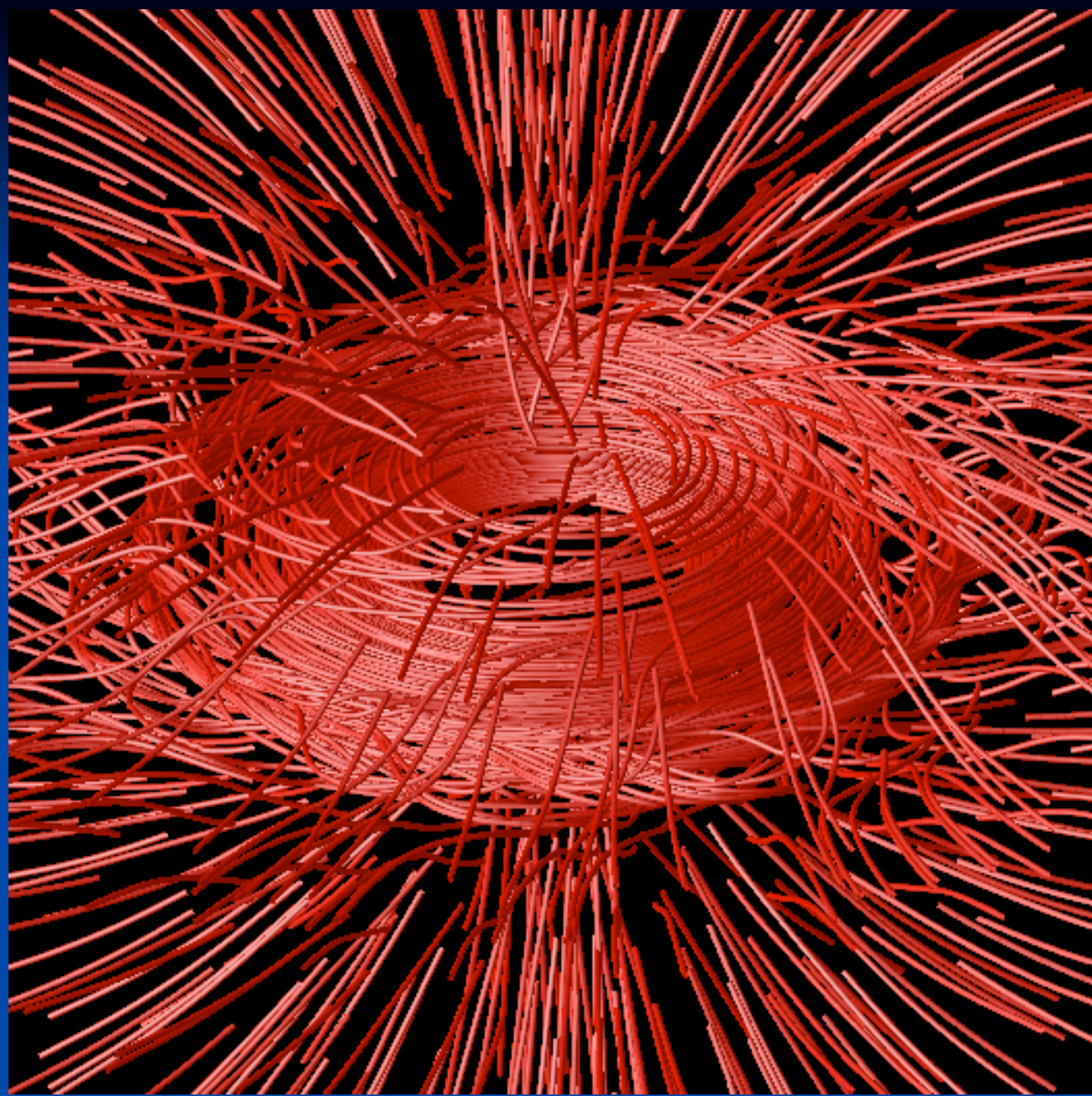


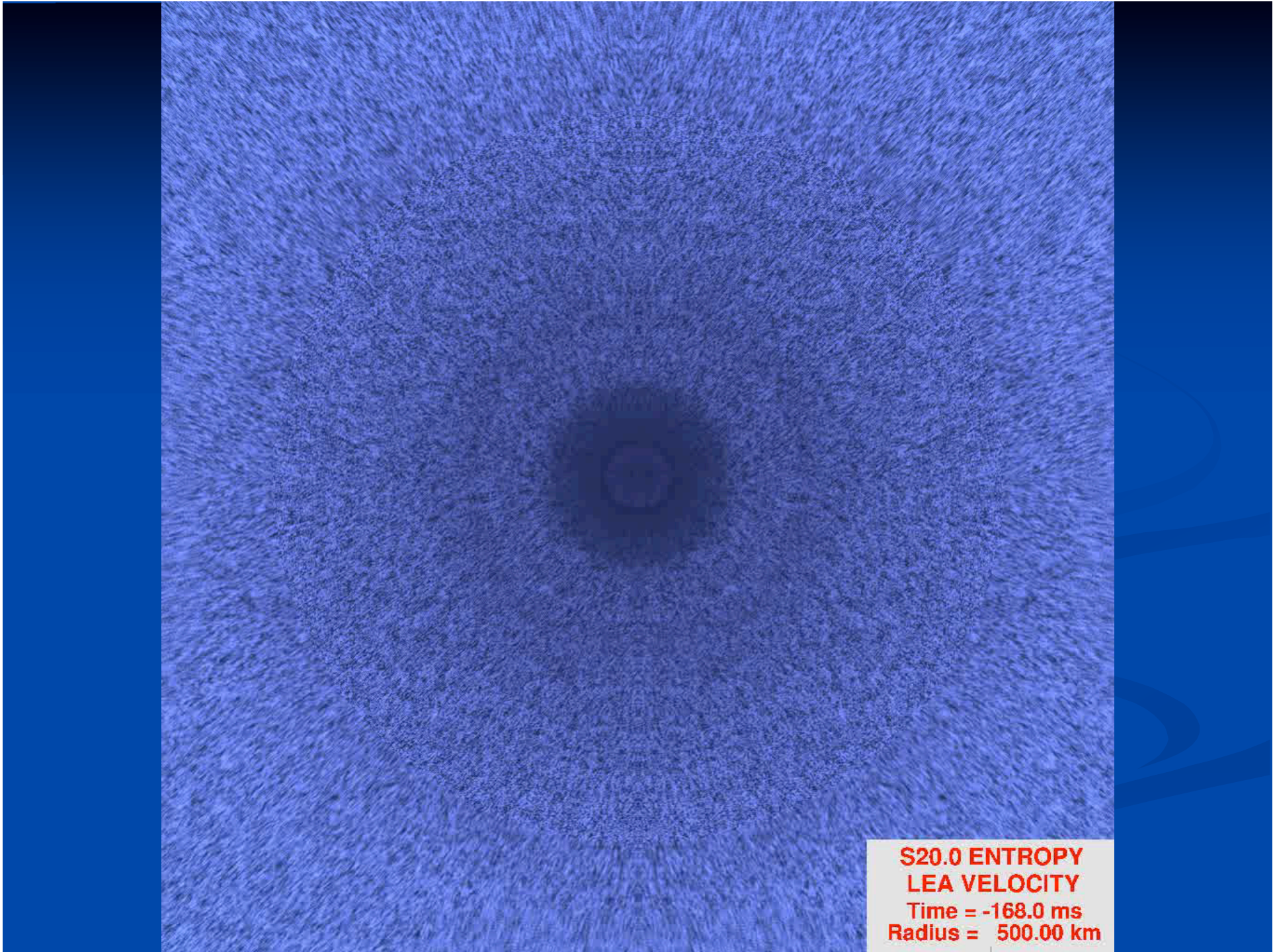
25 Solar Mass Progenitor: Core Oscillation and Shock Evolution



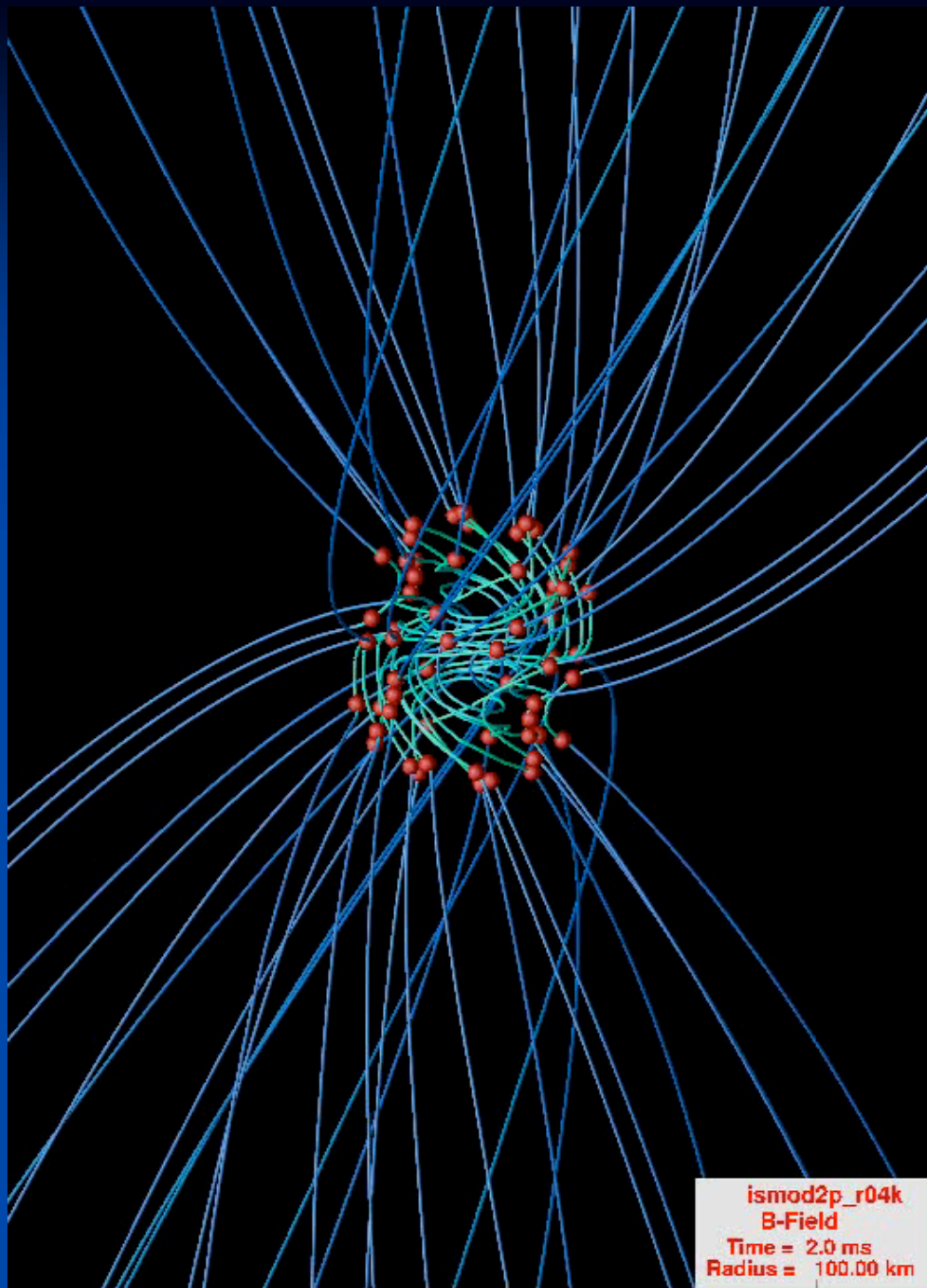
Mach Number along axis versus Time

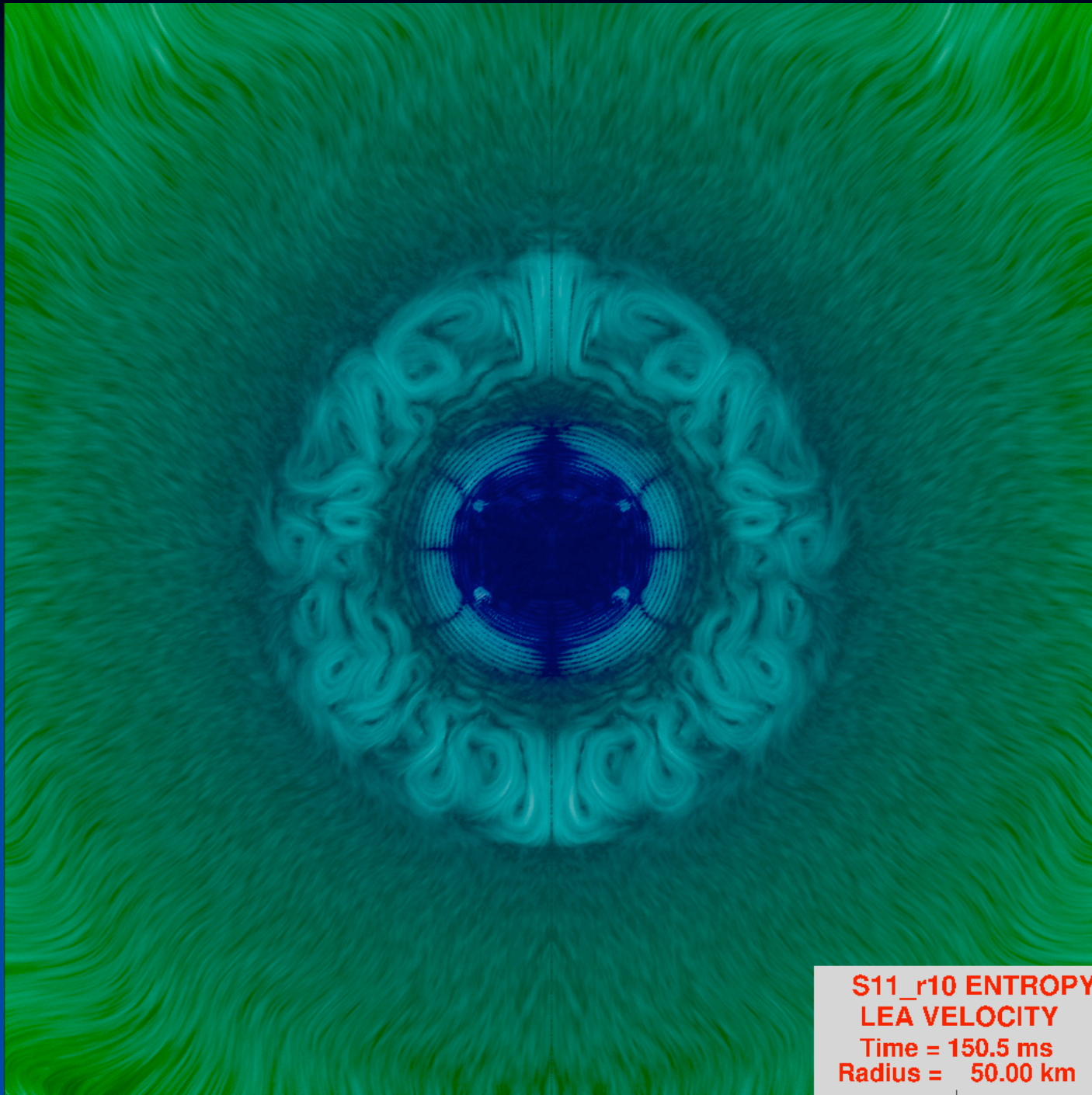






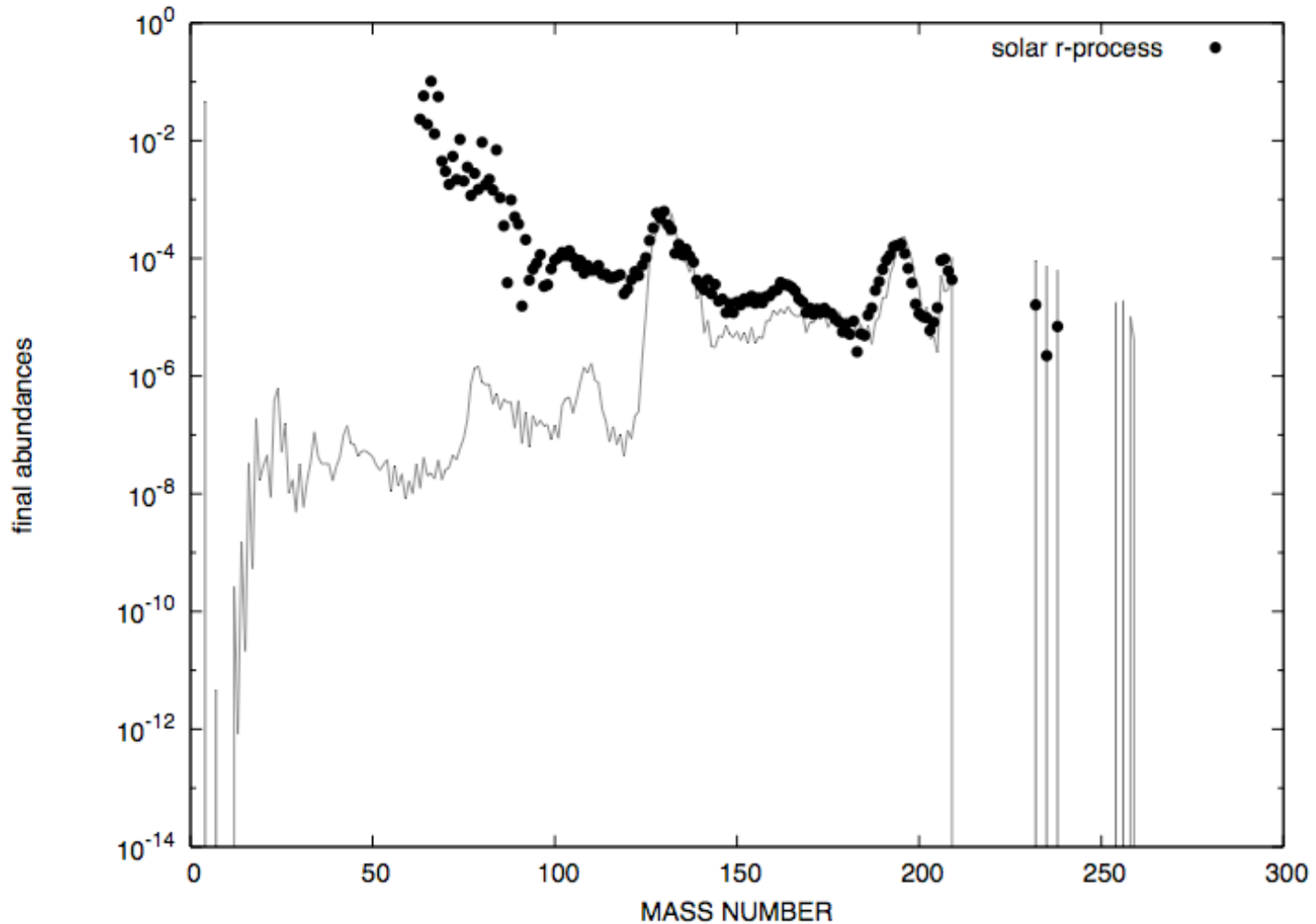
S20.0 ENTROPY
LEA VELOCITY
Time = -168.0 ms
Radius = 500.00 km





S11_r10 ENTROPY
LEA VELOCITY
Time = 150.5 ms
Radius = 50.00 km

Preliminary R-process Calculations for the Long-term Acoustic Mechanism



K. Otsuki et al. 2008

Key Features of Acoustic Mechanism

- “A Tale of Two Instabilities”
- **Shock Instability (SASI)** after bounce (30-80 Hz)
- Rapid **core oscillation** progressively excited: **$l=1$ g-mode** (~ 300 Hz), first by turbulence (that grows with time), then non-linearly by anisotropic downflowing **plumes/streams**
- Core oscillation generates **sound waves** that propagate outward
- Acoustic power and momentum explode the star
- **Hybrid** acoustic/neutrino model?
- **Self-excited oscillations** (very non-linear); transducer
- All models explode, but “late” (0.5-1.0 seconds after bounce)
- Fundamentally **aspherical** explosions: unipolar?
- **R-process** nucleosynthesis?
- **Recoil**: Natural mechanism for pulsar kicks?