

HERE BE DRAGONS: THE UNEXPLORED CONTINENTS OF THE CMSSM

Jay Wacker
(SLAC)

with Tim Cohen

[arXiv:13XX.soon](#)

PCTS After the Higgs Workshop
April 25, 2013

Disclaimer

This is not a talk on the Higgs boson,

but

the Higgs boson mass plays a central role.

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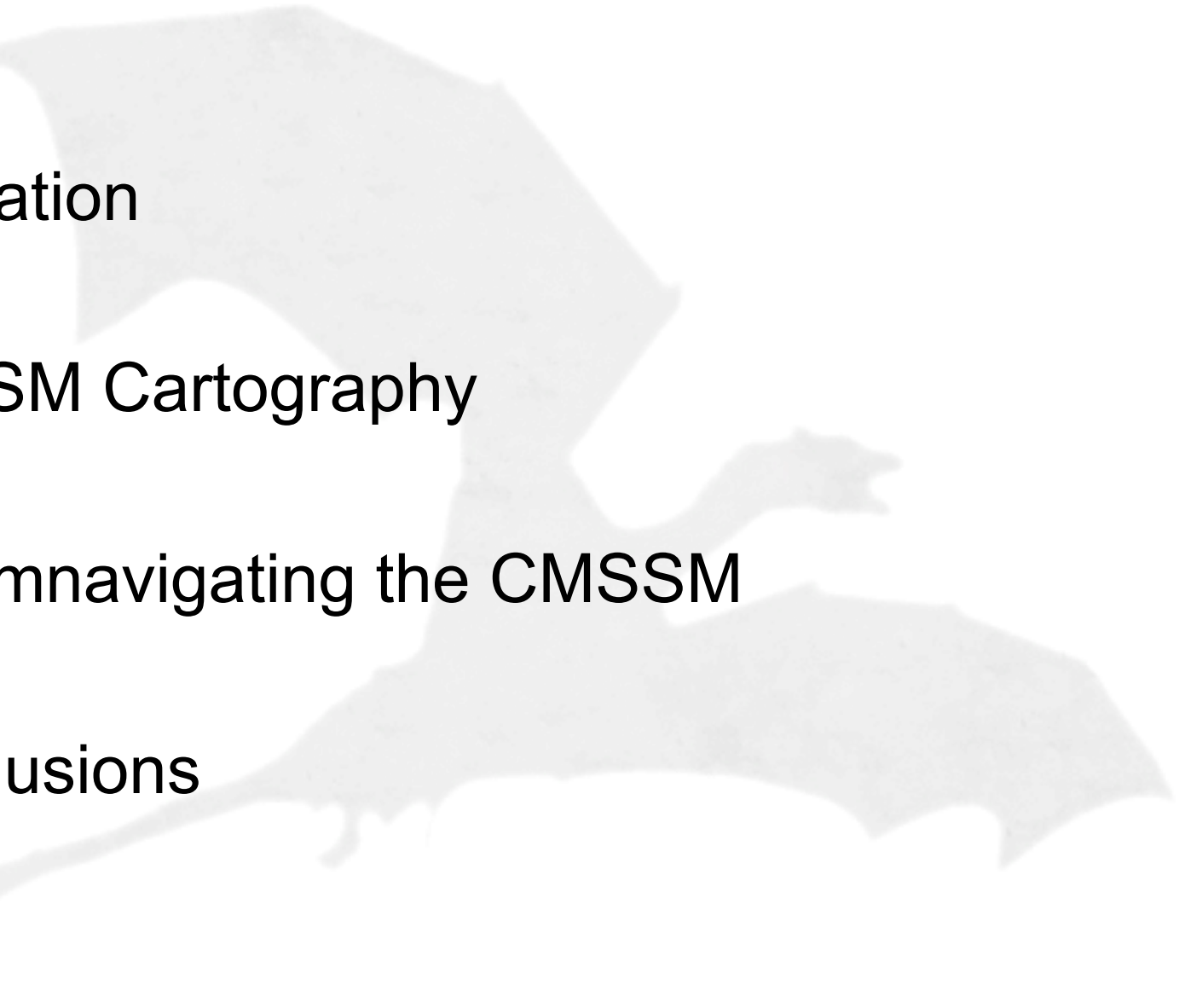
but

the Higgs boson mass plays a central role.

The 8 TeV LHC just began to exploring
CMSSM

Need 13 TeV (and beyond)

Outline

- I) Motivation
 - II) CMSSM Cartography
 - III) Circumnavigating the CMSSM
 - IV) Conclusions
- 



MOTIVATION

The MSSM in the Era of Higgs Discovery

- A SM-like Higgs has been discovered at 125 GeV.
 - Profound implications for spectrum

ATLAS [arXiv:1207.7214]
CMS [arXiv:1207.7235]

$$m_{h^0}^2 \simeq m_{Z^0}^2 \cos^2 2\beta + \frac{3g^2 m_t^4}{8\pi^2 m_{W^\pm}^2} \left(\log \frac{m_{\tilde{t}_1} m_{\tilde{t}_2}}{m_t^2} + \frac{A_t^2}{m_{\tilde{t}_1} m_{\tilde{t}_2}} \left(1 - \frac{A_t^2}{12 m_{\tilde{t}_1} m_{\tilde{t}_2}} \right) \right)$$

$$m_{h^{0'}} - m_{h^0} \simeq \frac{3g^2 m_t^4}{16\pi^2 m_{W^\pm}^2 m_{h^0}} \log \frac{m_{\tilde{t}'_1} m_{\tilde{t}'_2}}{m_{\tilde{t}_1} m_{\tilde{t}_2}} \implies m_{\tilde{t}'_1} m_{\tilde{t}'_2} \simeq m_{\tilde{t}_1} m_{\tilde{t}_2} 2^{\frac{\Delta m_h}{5.6 \text{ GeV}}}$$

- This measurement is “consistent” with MSSM.
 - Stops 500 GeV to 100 TeV - 4x heavier than pre-Higgs
- The motivation for weak-scale superpartners remains:
 - Solves the hierarchy problem;
 - Explains the dark matter;
 - Predicts gauge coupling unification.

The MSSM in the Era of Higgs Discovery

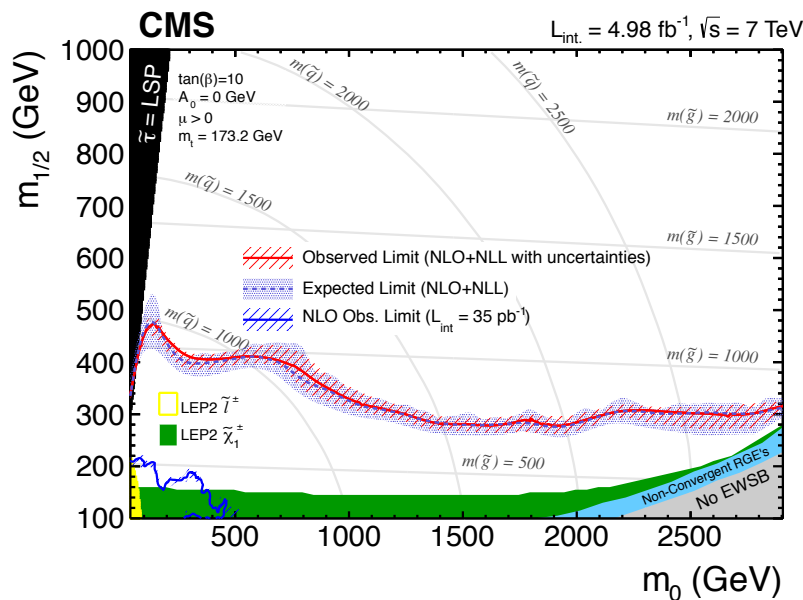
- The parameter space of the MSSM is enormous.
 - The soft supersymmetry breaking Lagrangian includes more than 120 new parameters.
- How can we map out all possible signatures?
 - Simplified models: isolate particles for specific signature. Parameter space is tractable; only a few masses and branching ratios to specify.
 - pMSSM: phenomenologically motivated reduction to 19 parameters.
[Berger, Gainer, Hewett, Rizzo \[arXiv:0812.0980\]](#)
 - CMSSM/mSUGRA: 4 parameters.
[Chamseddine, Arnowitt, Nath \[PRL 49 \(1982\)\]; Barbieri, Ferrara, Savoy \[PLB \(1982\)\]; Hall, Lykken, Weinberg \[PRD \(1983\)\]](#)
- 4 parameters is potentially tractable.
- Can we understand all predictions of this ansatz?

A Simple Ansatz - a wide range of dynamics

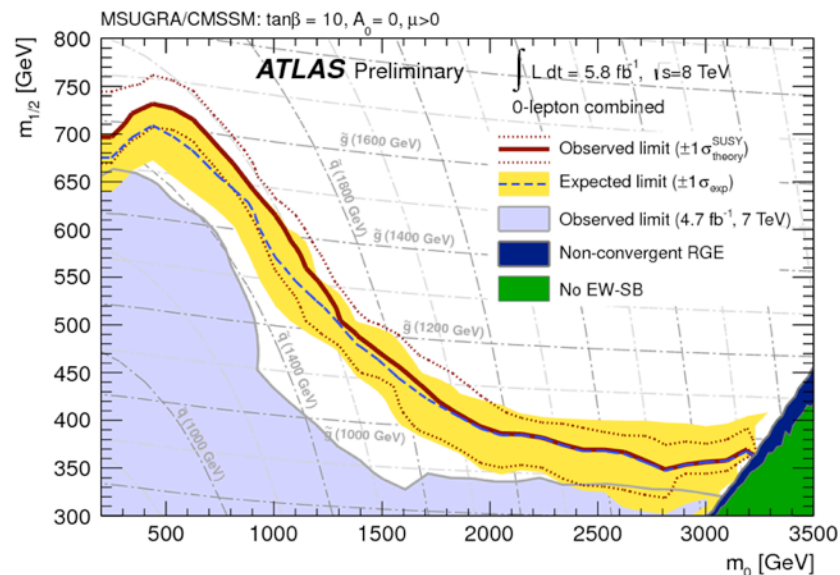
- CMSSM is 4-dimensional subspace of the R -parity conserving MSSM.
- Defined at the GUT scale by the following (real) inputs:
 - The unified scalar soft mass M_0
 - The unified gaugino mass $M_{1/2}$
 - The unified A -term A_0
 - The ratio of the Higgs vevs $\tan \beta$ (traded for B_μ term).
- Parameters are evolved to M_W using the RGEs.
- μ -term determined by requiring m_Z
- 19 coupled RGEs integrated over 32 e-folds \Rightarrow relation between input parameters & low energy spectrum is non-linear.

The State of the Art

- Both ATLAS and CMS put limits on the CMSSM:



CMS [arXiv:1205.6615]



ATLAS-CONF-2012-109

- Exclusions are regions of the $M_{1/2}$ versus M_0 plane at fixed A_0 & $\tan \beta$
- What is the Higgs mass?
- Does the neutralino overclose the Universe?

Classification

- “Quadrants” defined by sign A_0 & sign μ with $M_{1/2} > 0$.

- Schematically RGEs for A and B terms are

$$16 \pi^2 \frac{d}{dt} A = A (|y|^2 - g^2) + y g^2 M,$$

$$16 \pi^2 \frac{d}{dt} B = B (|y|^2 - g^2) + \mu (A y^\dagger + g^2 M),$$

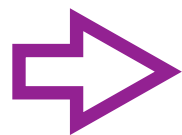
- Low energy spectrum is different depending quadrant.
- What process determines the relic abundance?

Classification

- What process determines the relic abundance?
 - “light $\tilde{\chi}^0$ ”: annihilation is dominated by the Z^0 and h poles.
 - “well-tempered”: annihilation via Higgsino/Bino mixing to $W^+ W^-$.
 - “ A^0 pole”: annihilation is dominated by an s-channel A^0 resonance.
 - “stau coannihilation”
 - “stop coannihilation”

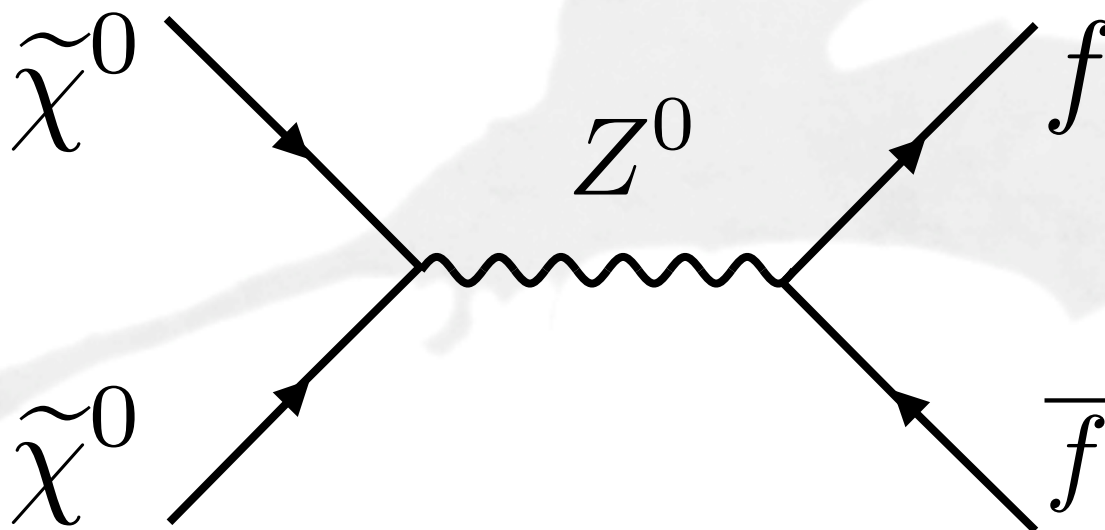
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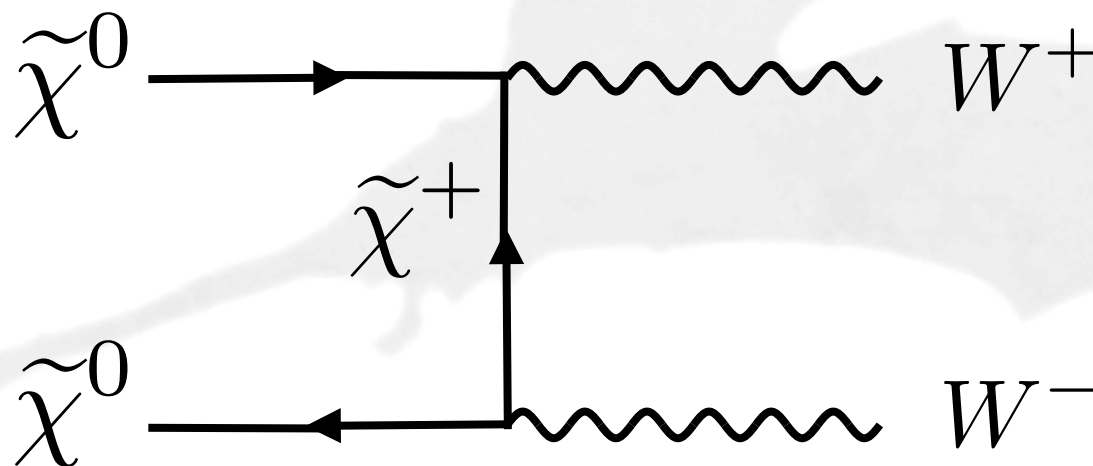
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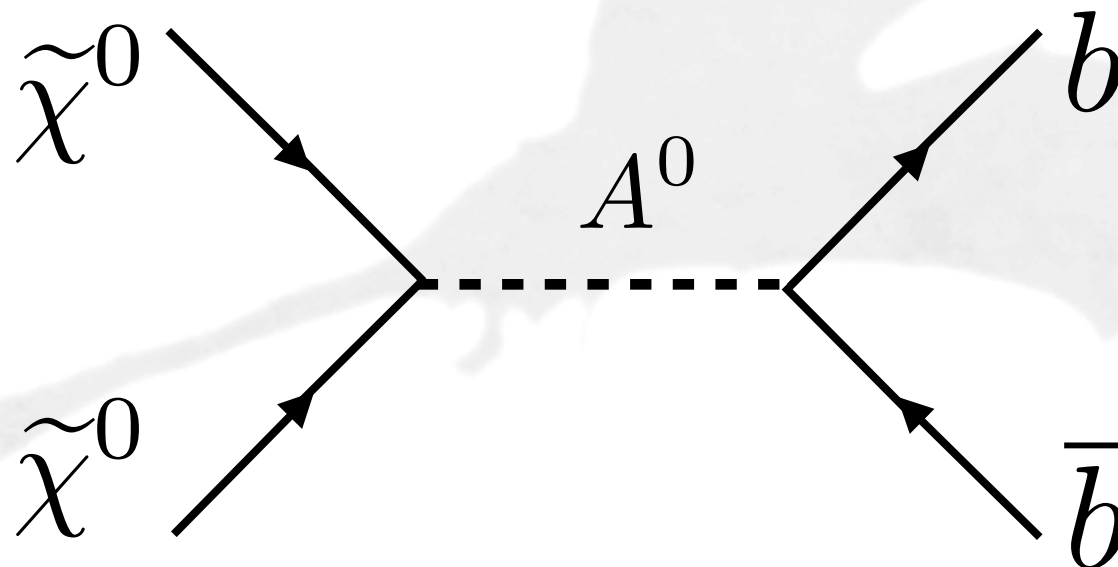
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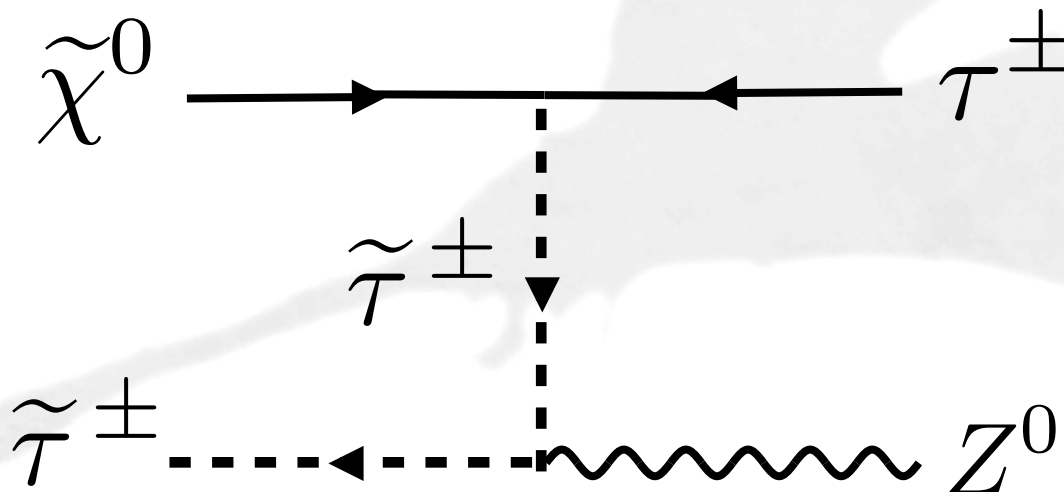
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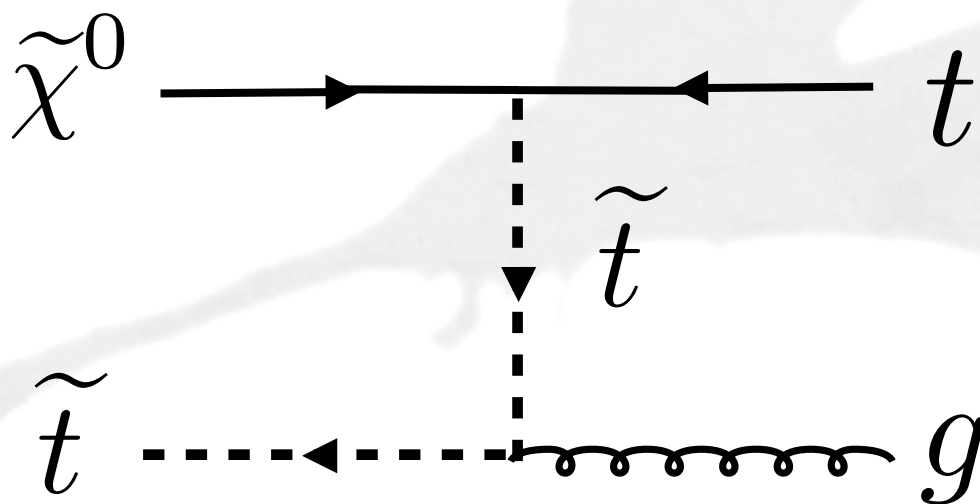
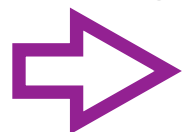
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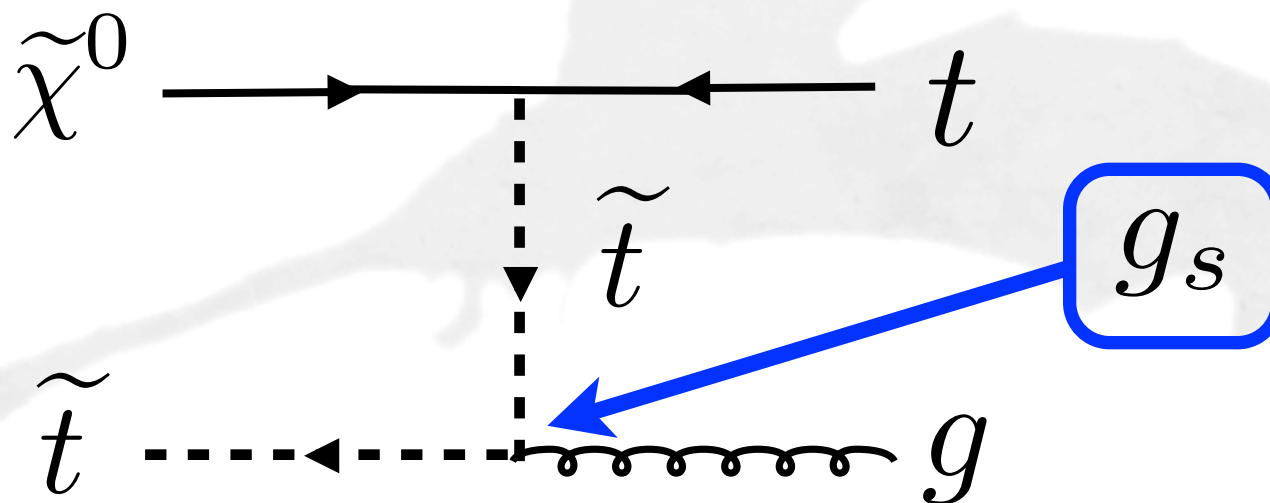
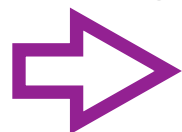
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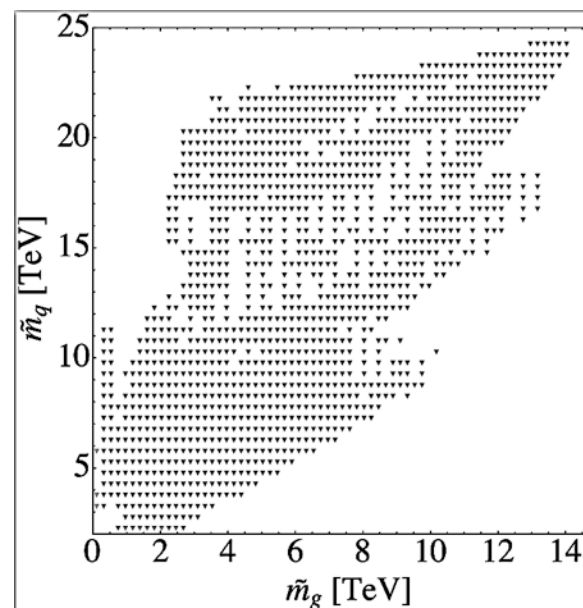
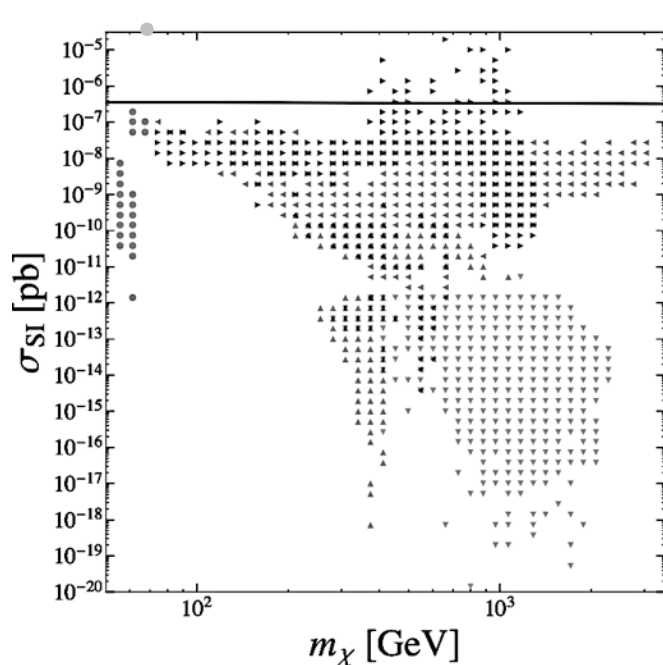
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Grading The Post- h^0 Discovery CMSSM Literature

- Light χ^0
- Well Tempered
- A^0 -pole
- Stau Coannihilation
- Stop Coannihilation
- A (Excluded by LHC gluinos)
- B- (“will be excluded by DD soon”)
- D (nothing said recently)
- B (“will be excluded by LHC soon”)
- F (Last paper in 2001)





CMSSM CARTOGRAPHY

The CMSSM is compact

- 125 GeV Higgs mass means M_0 not arbitrarily large.
- Relic density: not overclosing
 - Bounds $M_{1/2}$ from being too large
- Lifetime of vacuum being longer than 14Gyr bounds A_0 .
- Perturbativity of bottom Yukawa coupling bounds $\tan \beta$.

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Consequence

Every MSSM particle discoverable
by a human-buildable accelerator

Tools

- SoftSUSY v3.3.7 computes low energy spectrum from CMSSM inputs. [Allanach \[arXiv:hep-ph/0104145\]](#)
 - Two loop MSSM RGEs (leading log decoupling is accounted for by the inclusion of all 1-loop finite terms).
 - The two loop contributions to the Higgs potential are included.
- DarkSUSY v5.1.1 computes the relic density and direct detection cross sections.
 - All 2-2 scattering processes are included. [Gondolo, Edsjo, Ullio, Bergstrom, Schelke \[arXiv:astro-ph/0406204\]](#)
- SUSY-HIT v1.3 computes the decay tables. [Djouadi, Muhlleitner, Spira \[arXiv:hep-ph/0609292\]](#)

Constraints

- 3 GeV error for the theoretical prediction for the Higgs mass:

$$122 \text{ GeV} < m_h < 128 \text{ GeV}$$

Allanach, Djuadi, Kneur, Porod, Slavich [arXiv:hep-ph/0406166]

- Require the relic density be in the range:

$$0.08 < \Omega h^2 < 0.14$$

- Require that the lifetime of vacuum decay to a charge/color breaking minimum be longer than 14Gyr:

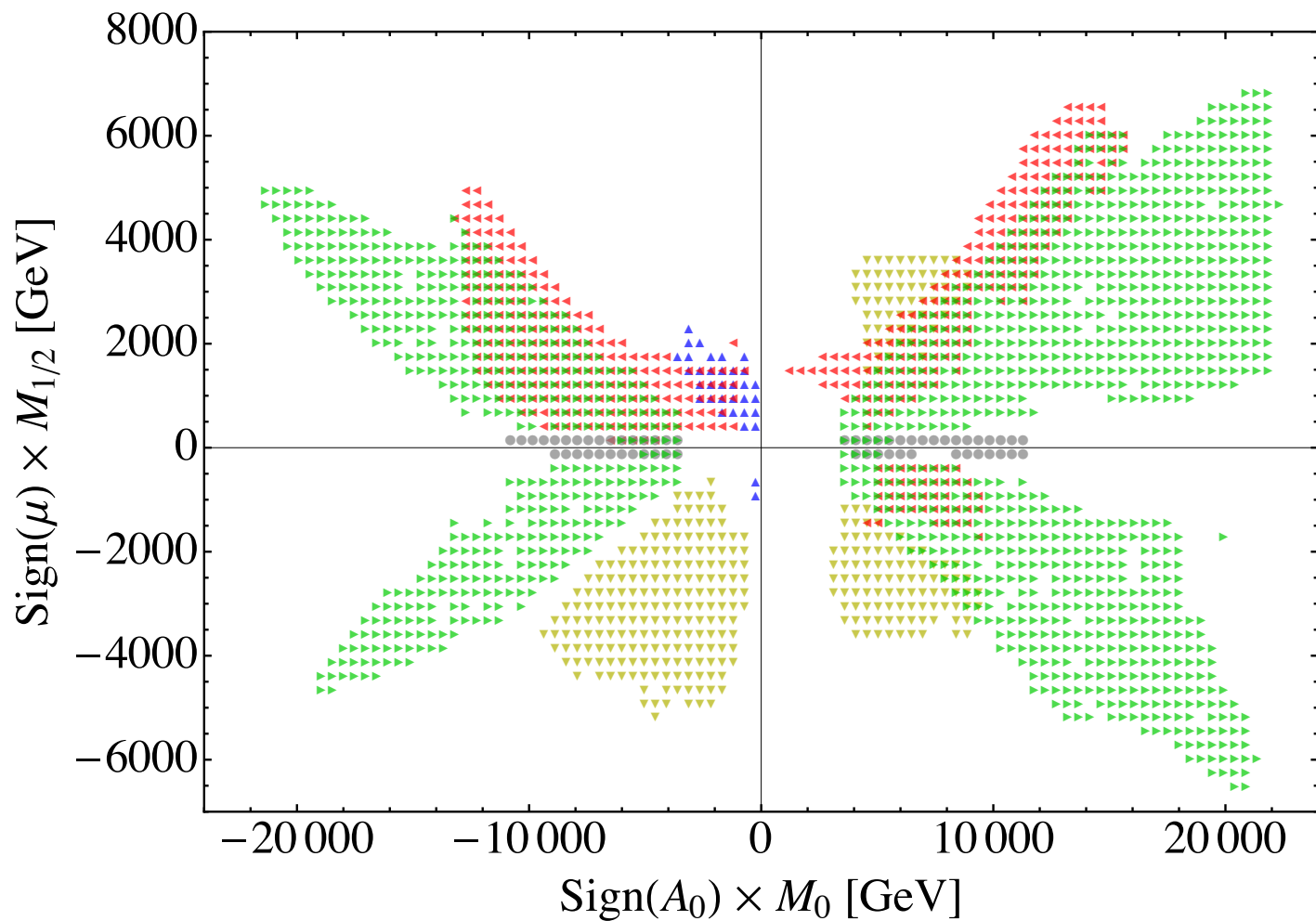
$$|a_t|^2 < (7.5 m_{q_3}^2 + 7.5 m_{u_3^c}^2 + 3 (m_{H_u}^2 + |\mu|^2))$$

Kusenko, Langacker, Segre [arXiv:hep-ph/9602414]

- Require that the chargino mass satisfy LEP bound:

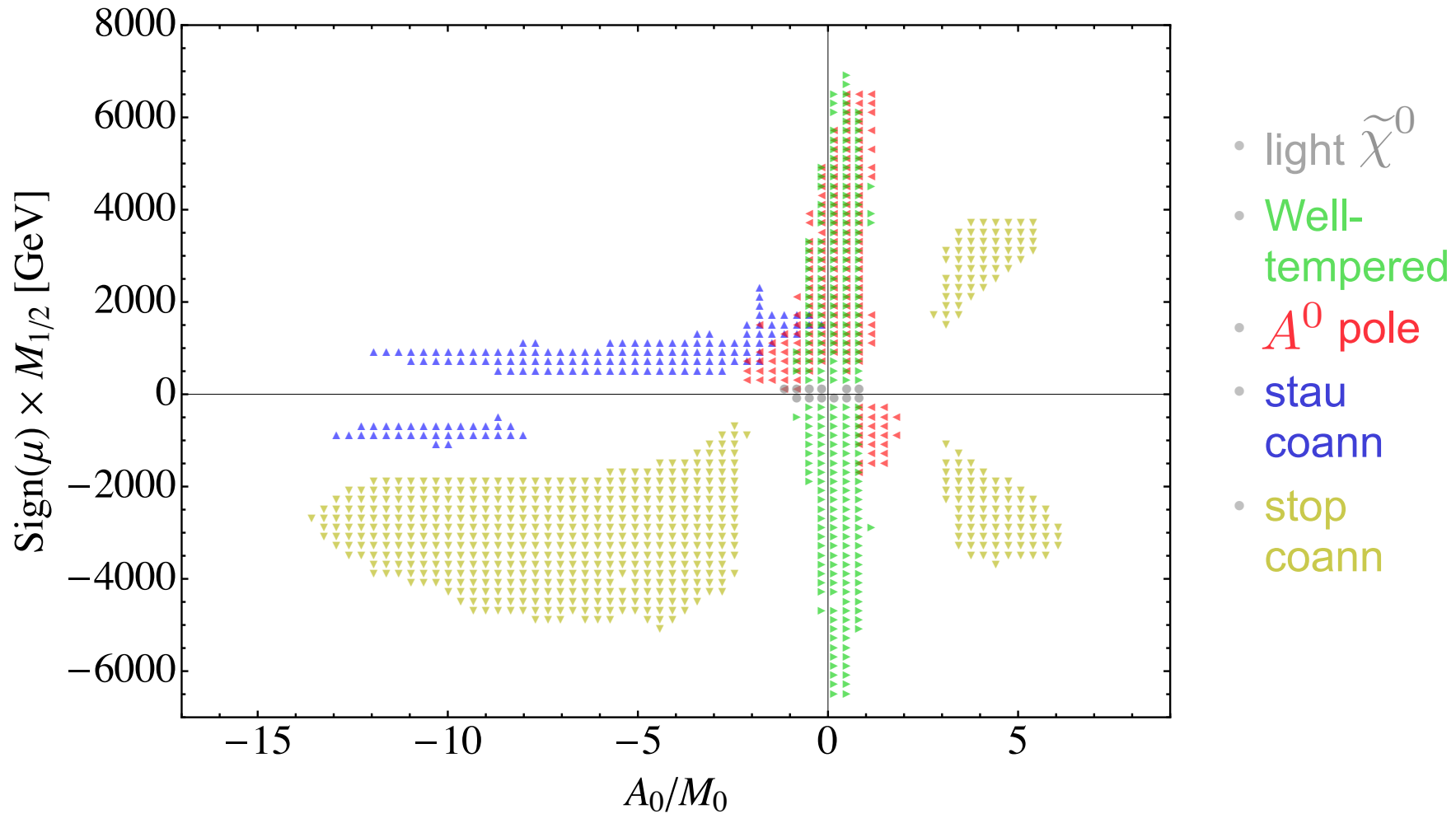
$$\tilde{m}_{\chi^+} > 100 \text{ GeV}$$

Charting the CMSSM

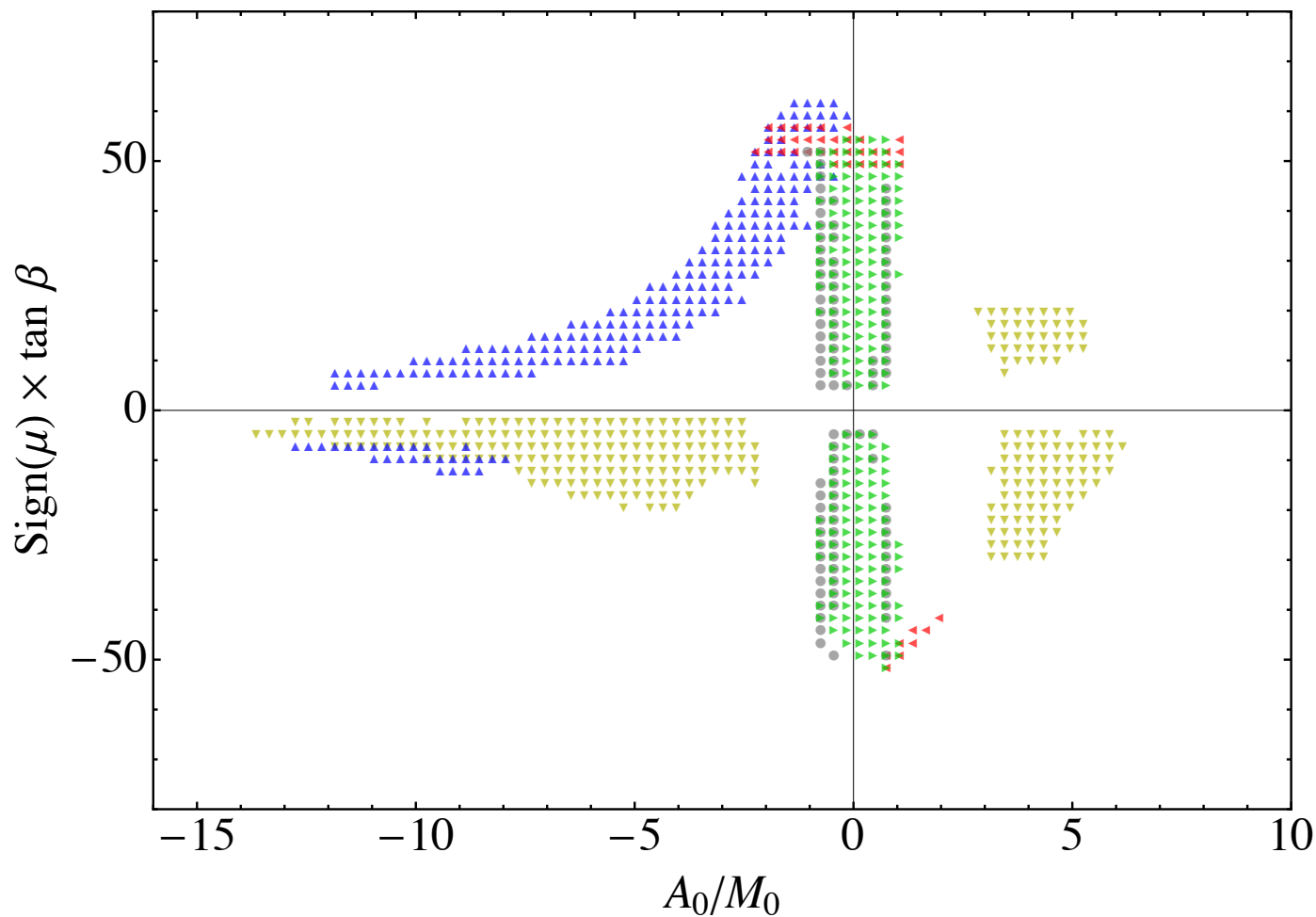


- light $\tilde{\chi}^0$
- Well-tempered
- A^0 pole
- stau coann
- stop coann

Charting the CMSSM



Charting the CMSSM

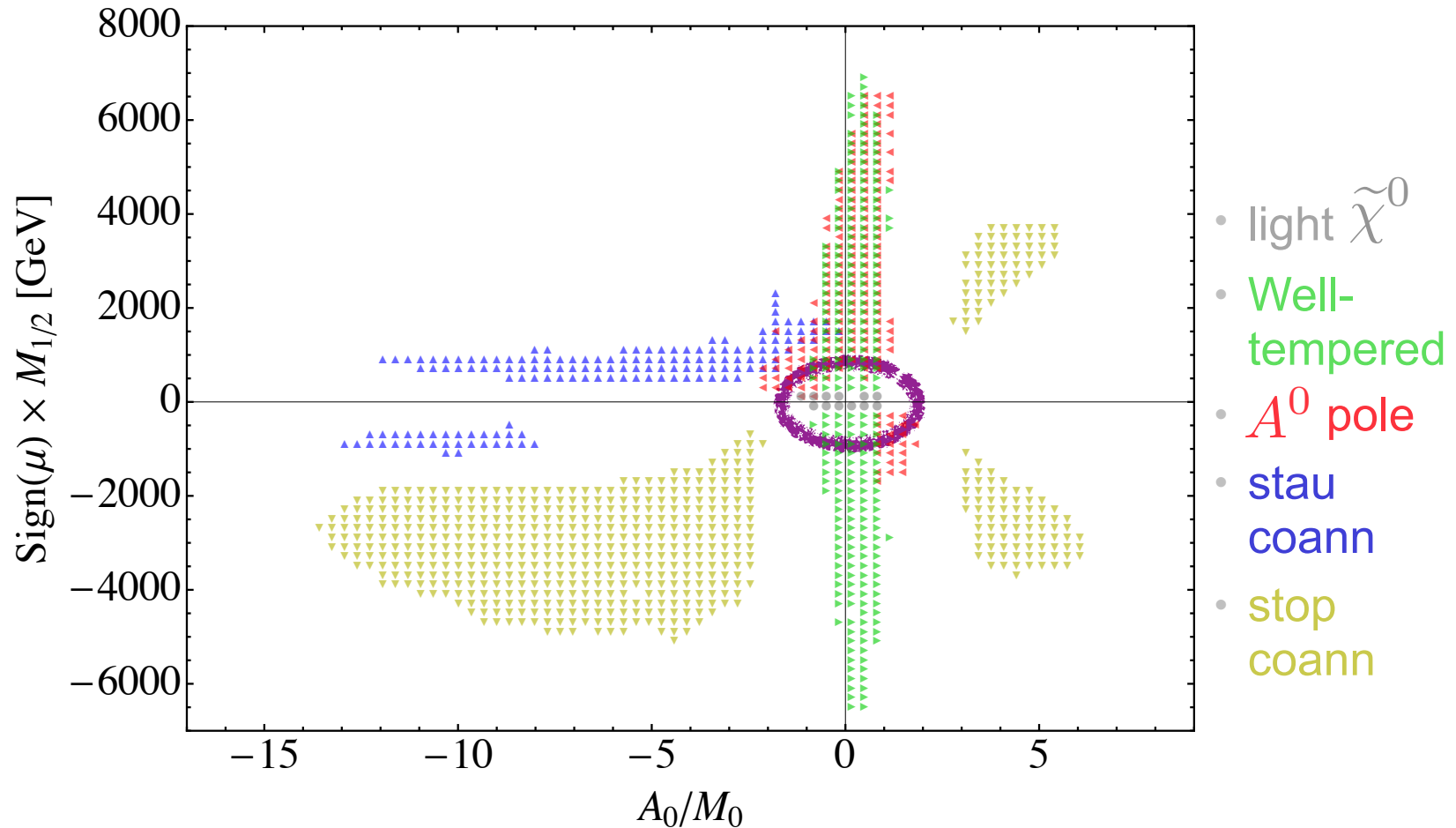


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CIRCUMNAVIGATING THE CMSSM

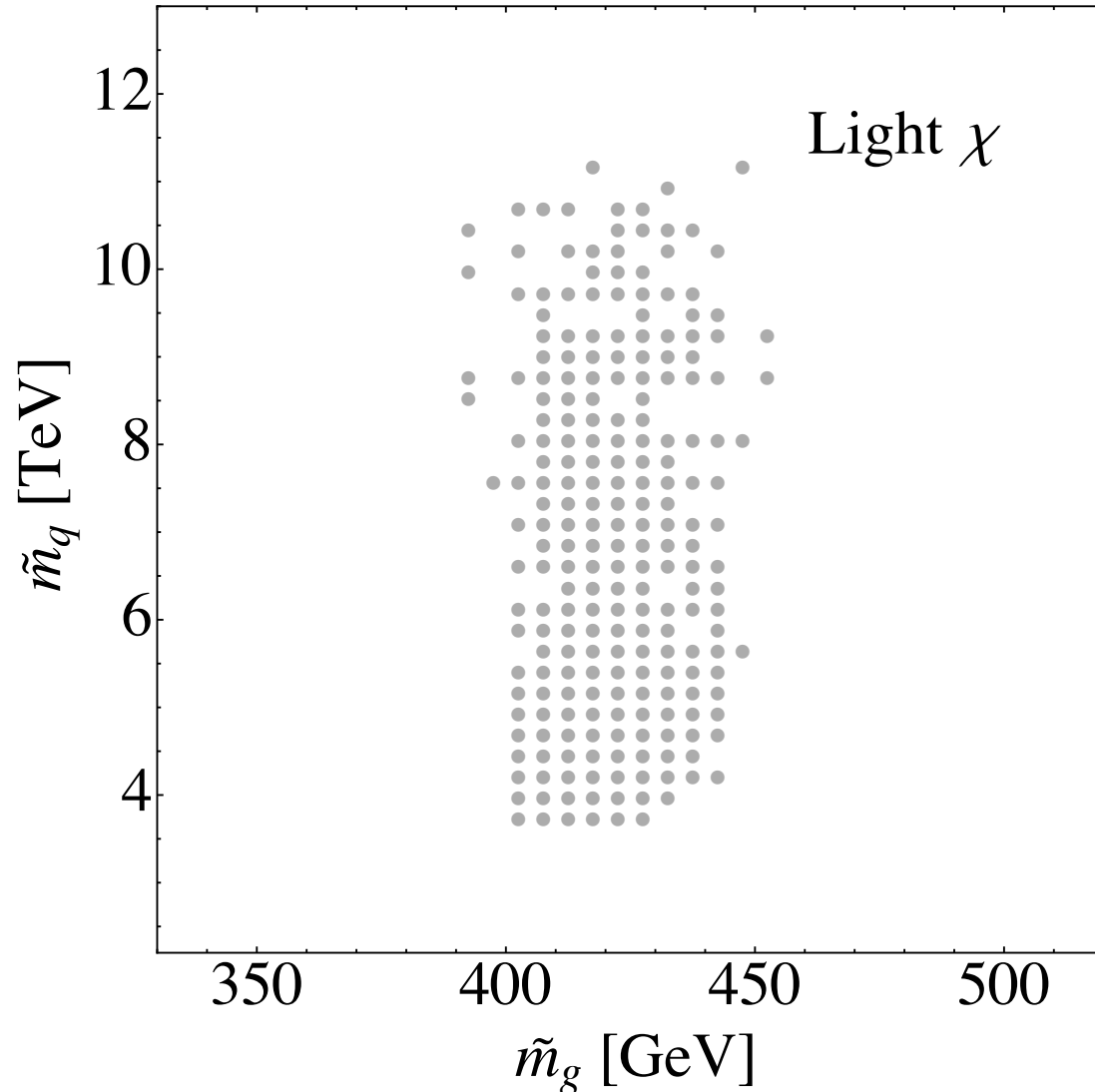
Light $\tilde{\chi}^0$

Setting sail for light $\tilde{\chi}^0 \iff \tilde{m}_{\chi^0} < 75 \text{ GeV}$



- $2 \text{ TeV} \lesssim M_0 \lesssim 12 \text{ TeV}$
- $5 \lesssim \tan \beta \lesssim 50$

Light $\tilde{\chi}^0$ implies light gluinos



\tilde{m}_g	\tilde{m}_q	\tilde{m}_{t_1}	\tilde{m}_{τ_1}	m_χ	m_{χ^\pm}	m_h	m_{A^0}
409.28	5393.5	3098.7	5327.3	57.139	111.1	124.14	5214.8

Probably Excluded

$$\begin{aligned} \tilde{g} &\rightarrow \tilde{B} q \bar{q} & 1.9\% \\ \tilde{g} &\rightarrow \tilde{W}^\pm q \bar{q} \rightarrow \tilde{B} W^\pm q \bar{q} & 46\% \\ \tilde{g} &\rightarrow \tilde{W}^0 q \bar{q} \rightarrow \tilde{B} Z^0 q \bar{q} & 34\% \end{aligned}$$

Have separate searches for

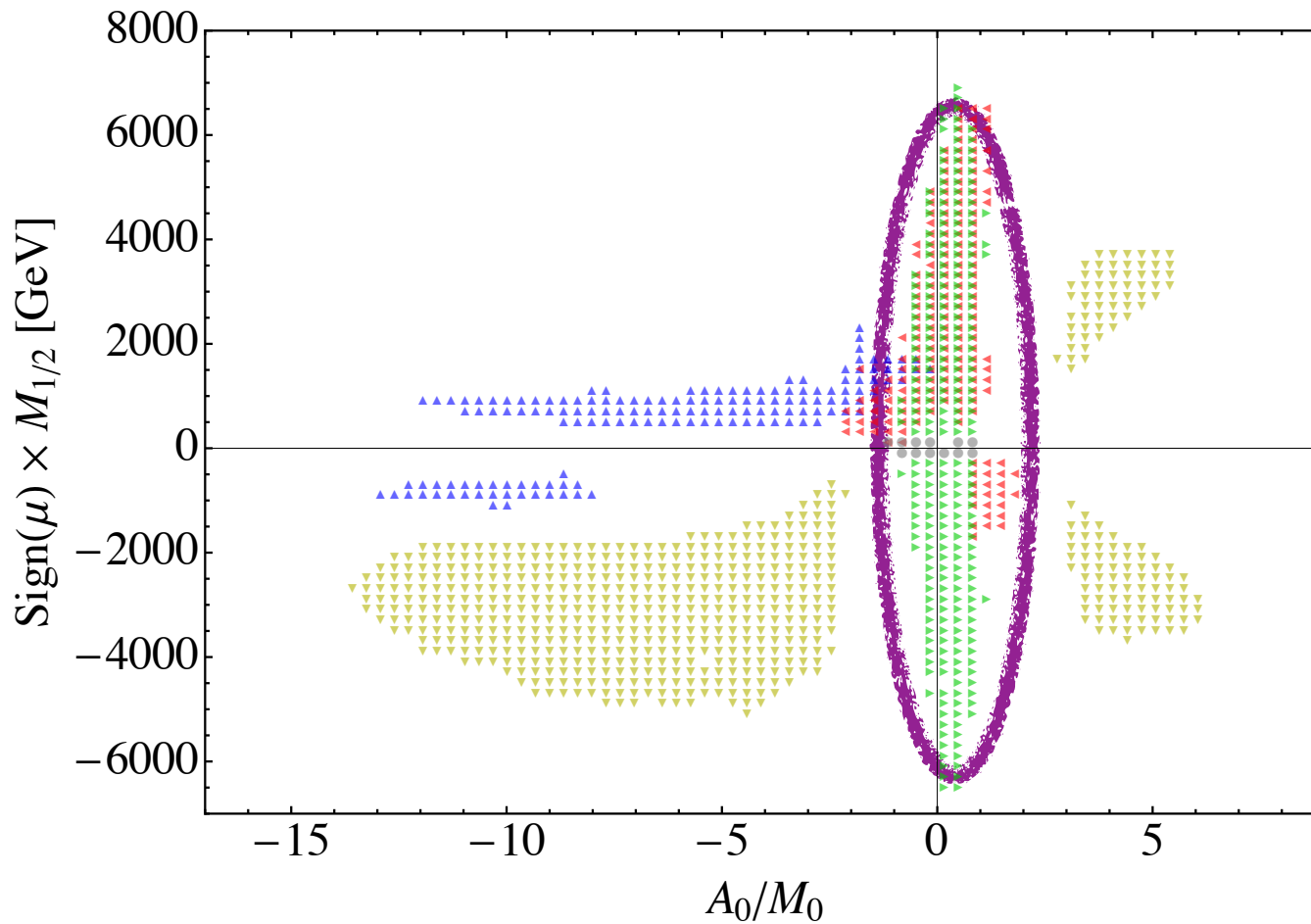
$$\begin{aligned} \tilde{g} \tilde{g} &\rightarrow W^\pm W^\pm q \bar{q} q \bar{q} \chi \chi \\ \tilde{g} \tilde{g} &\rightarrow Z^0 Z^0 q \bar{q} q \bar{q} \chi \chi \\ \tilde{g} \tilde{g} &\rightarrow q \bar{q} q \bar{q} \chi \chi \end{aligned}$$

Don't provide efficiencies of alternate simplified models

CIRCUMNAVIGATING THE CMSSM

Well-tempered

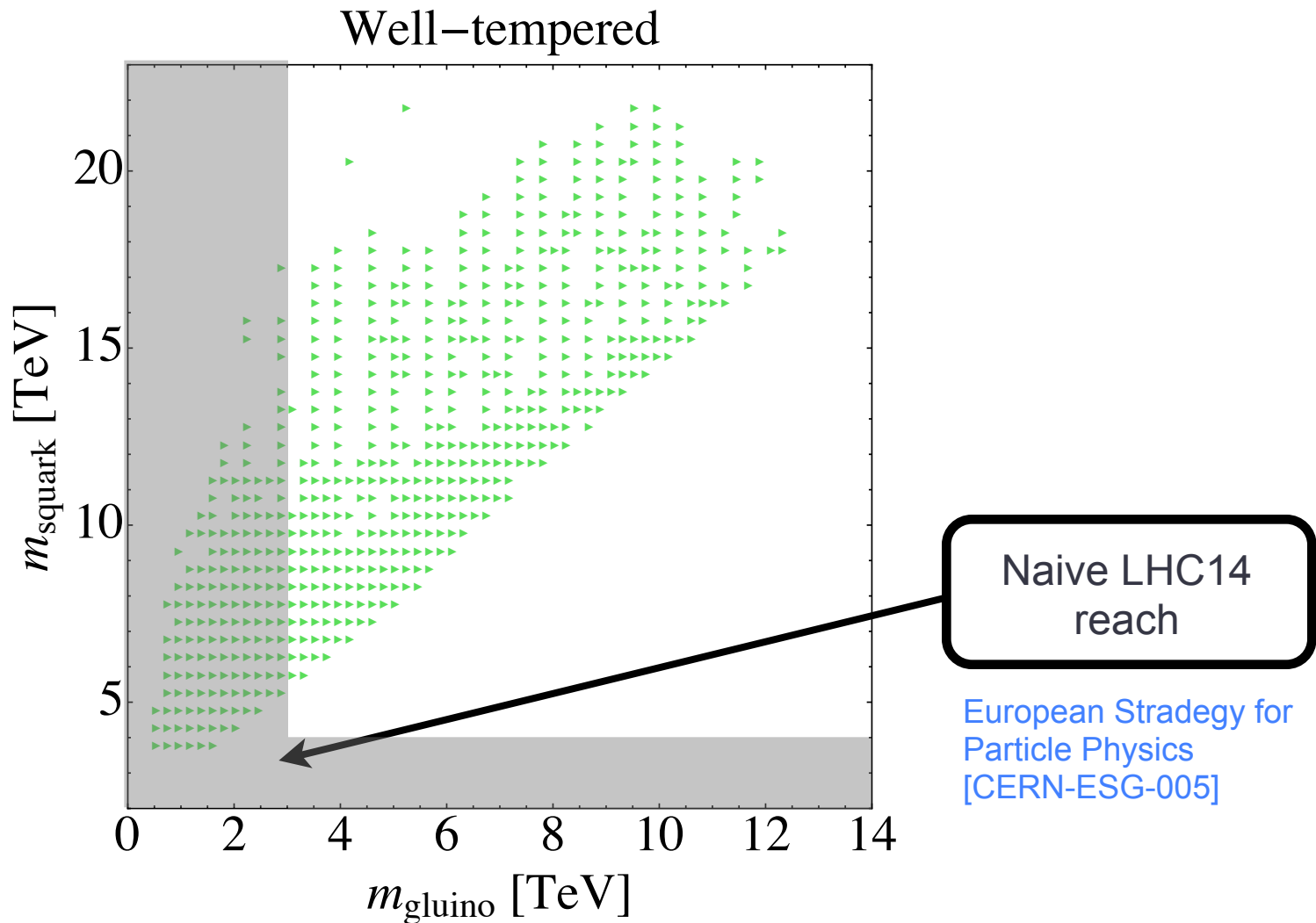
Setting sail for well-tempered



- light $\tilde{\chi}^0$
- Well-tempered
- A^0 pole
- stau coann
- stop coann

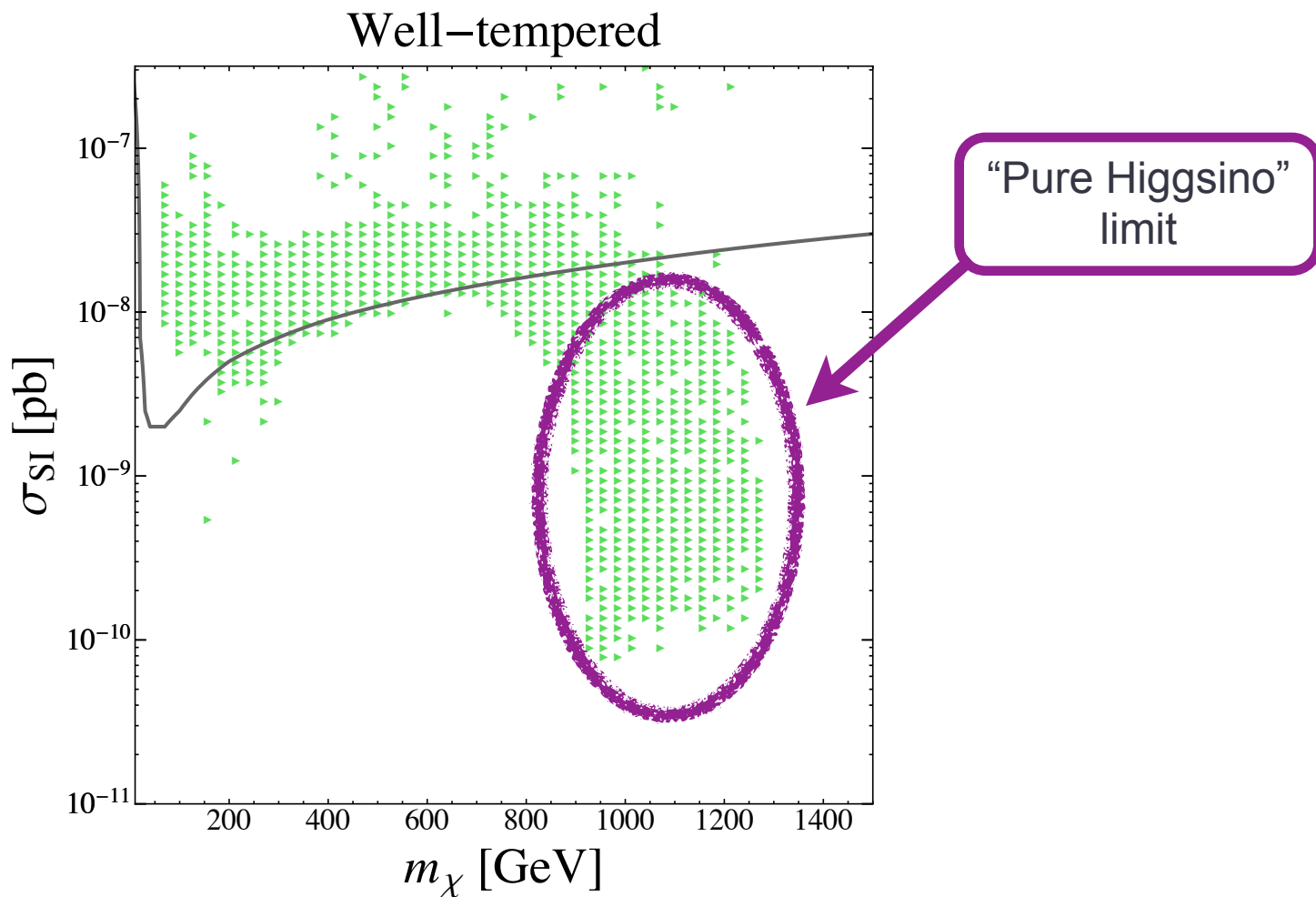
- $4 \text{ TeV} \lesssim M_0 \lesssim 20 \text{ TeV}$
- $5 \lesssim \tan \beta \lesssim 50$

What about the LHC?



- The LHC will have little impact on the well-tempered spectra.

Will direct detection exclude this region?

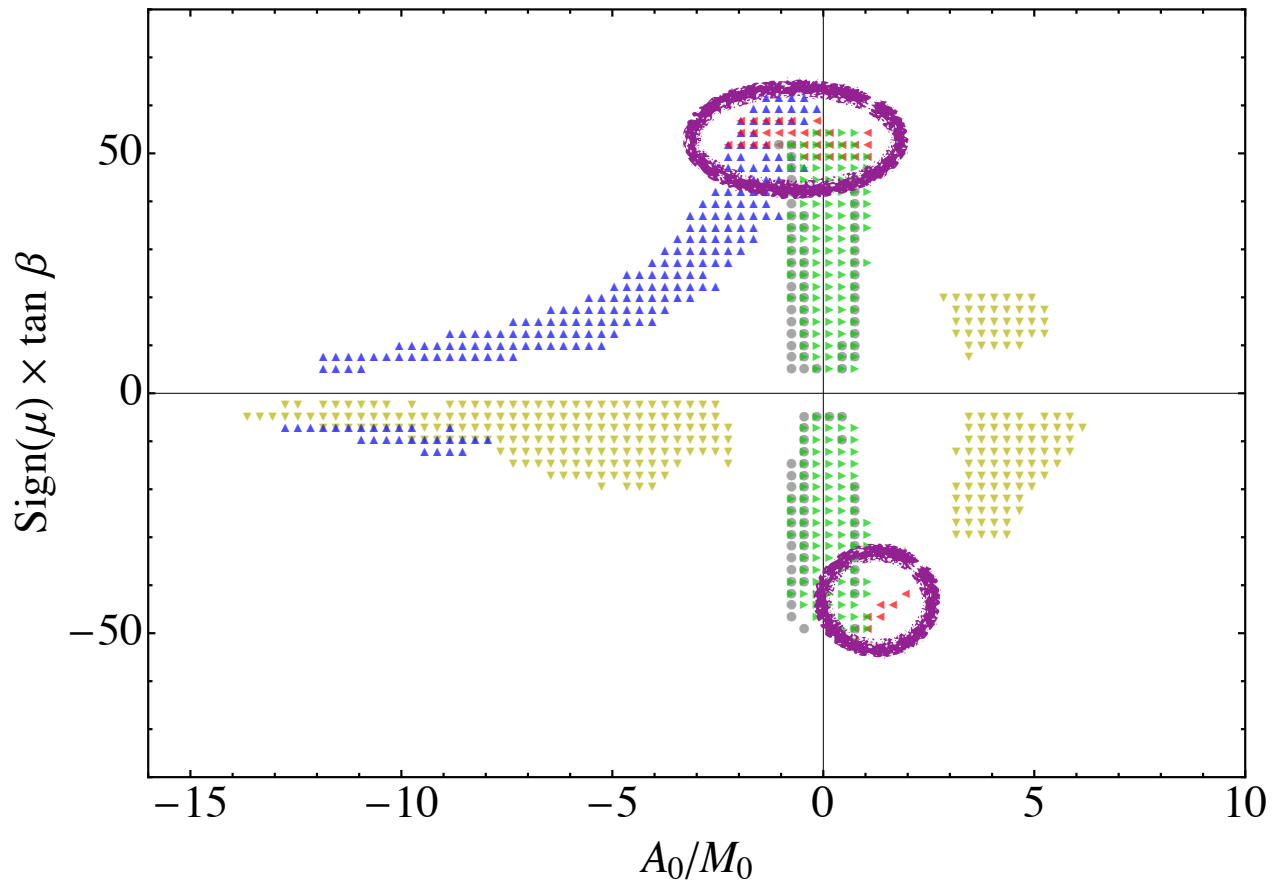


- A 1-ton Xenon experiment can reach spin-independent cross sections of 5×10^{-12} pb at 300 GeV.

CIRCUMNAVIGATING THE CMSSM

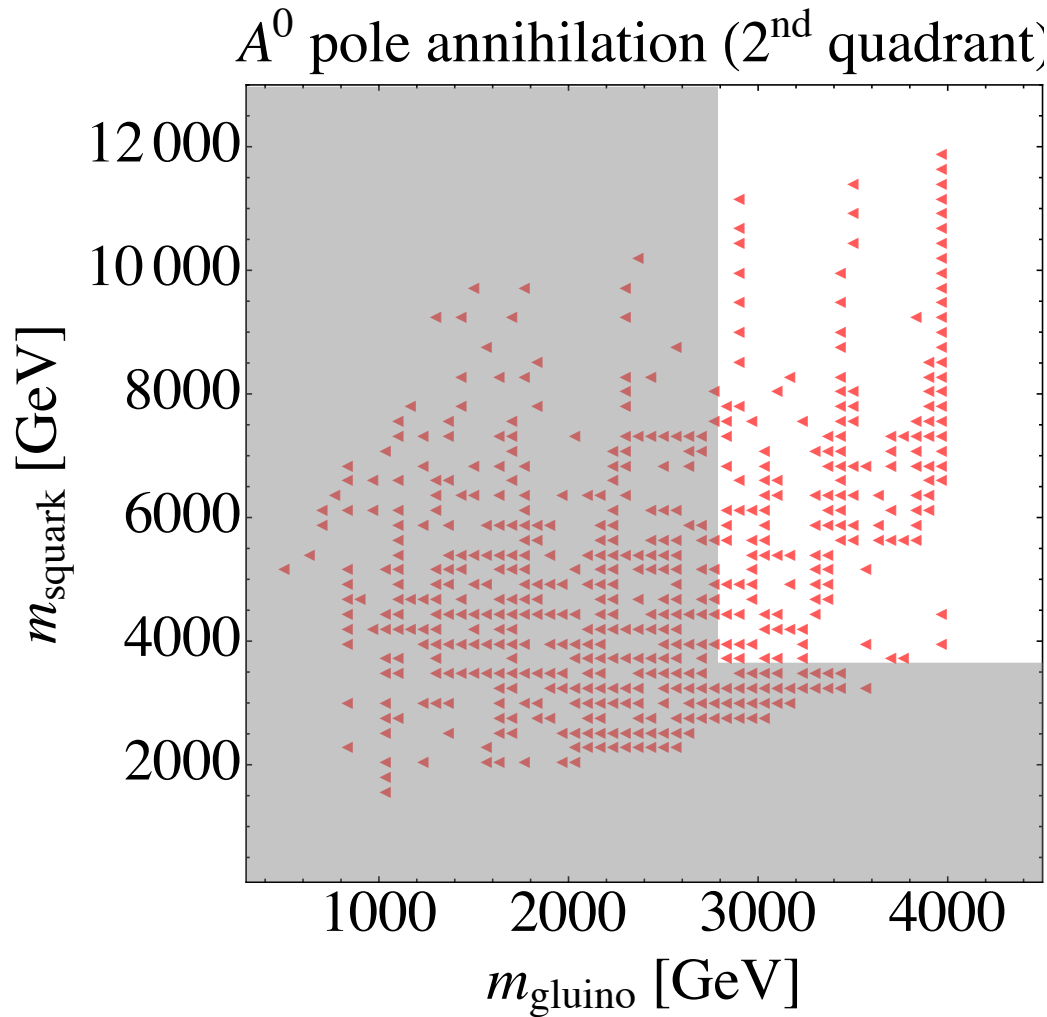
A^0 pole annihilation

Setting sail for A^0 pole annihilation



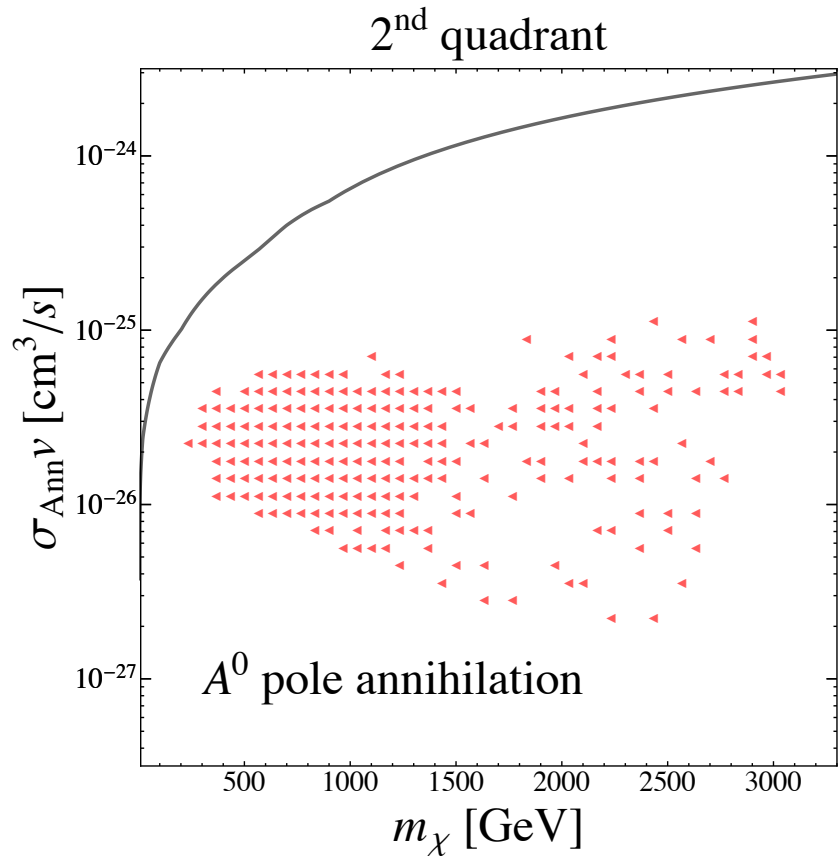
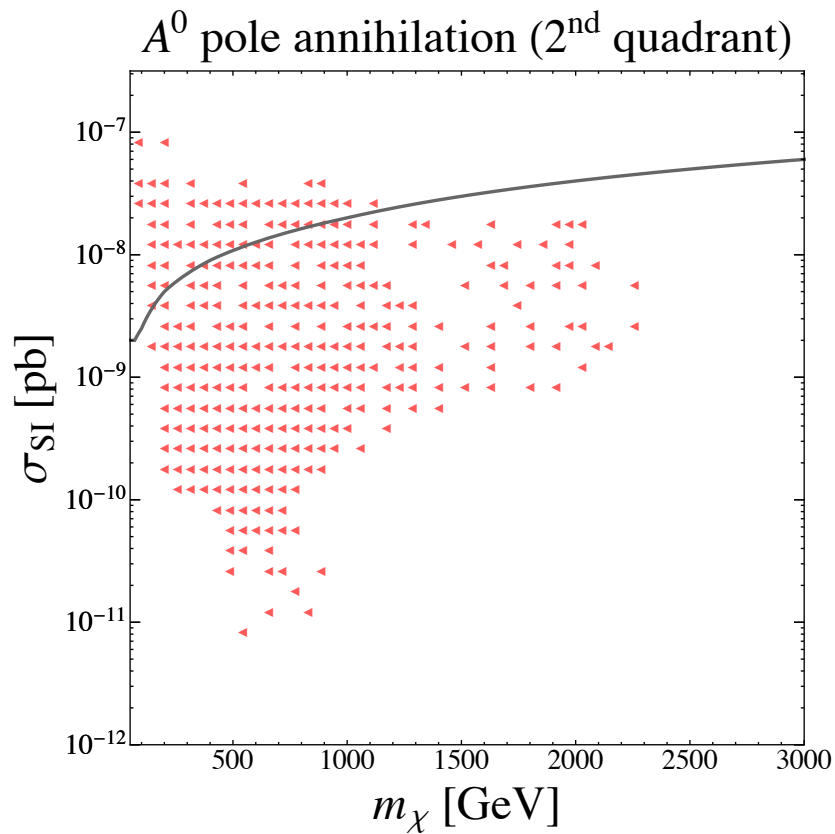
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The squark-gluino plane



- 1st quadrant is similar.

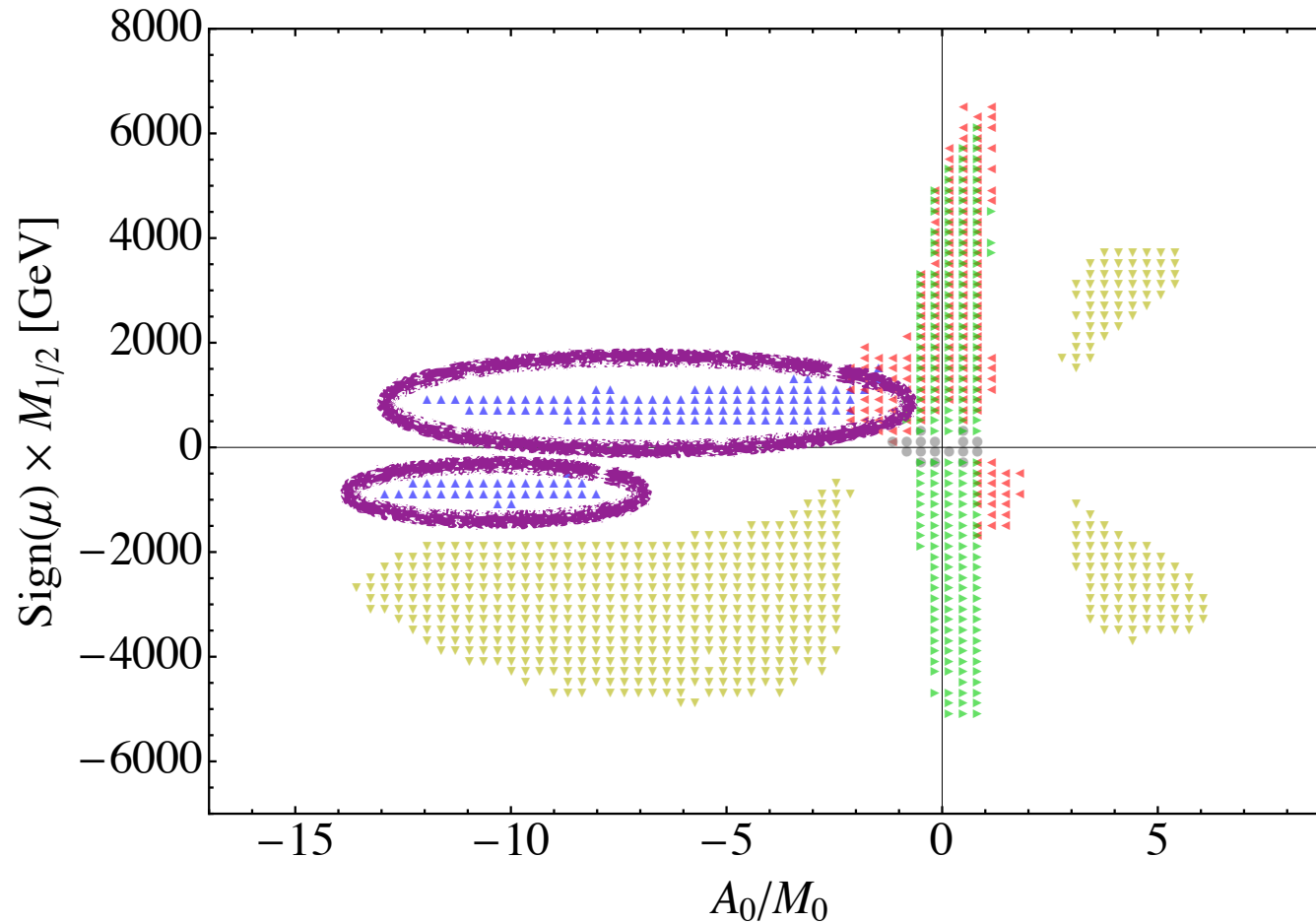
Direct & Indirect Detection



CIRCUMNAVIGATING THE CMSSM

Stau coannihilation

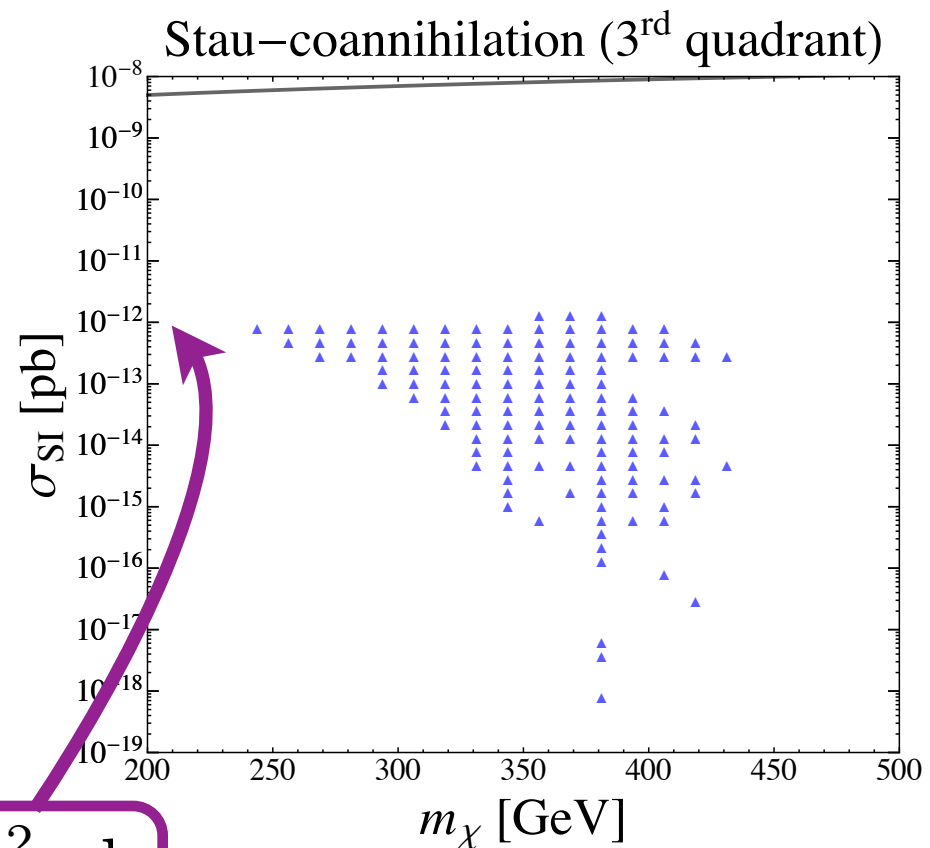
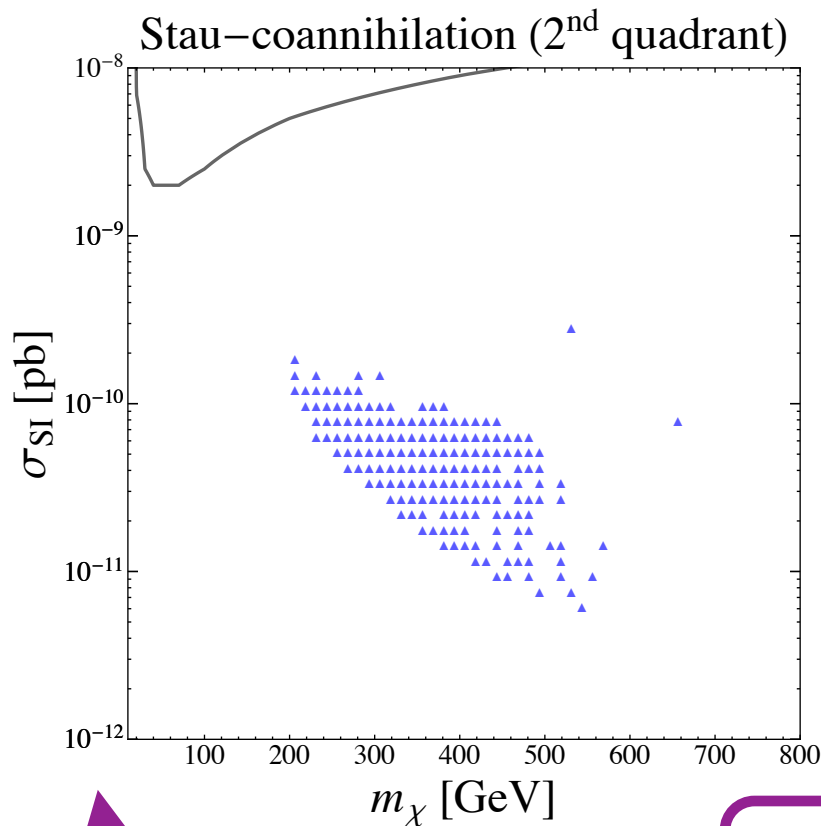
Setting sail for stau coannihilation



- light $\tilde{\chi}^0$
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- $200 \text{ GeV} \lesssim M_0 \lesssim 3 \text{ TeV}$
- $5 \lesssim \tan \beta \lesssim 60$

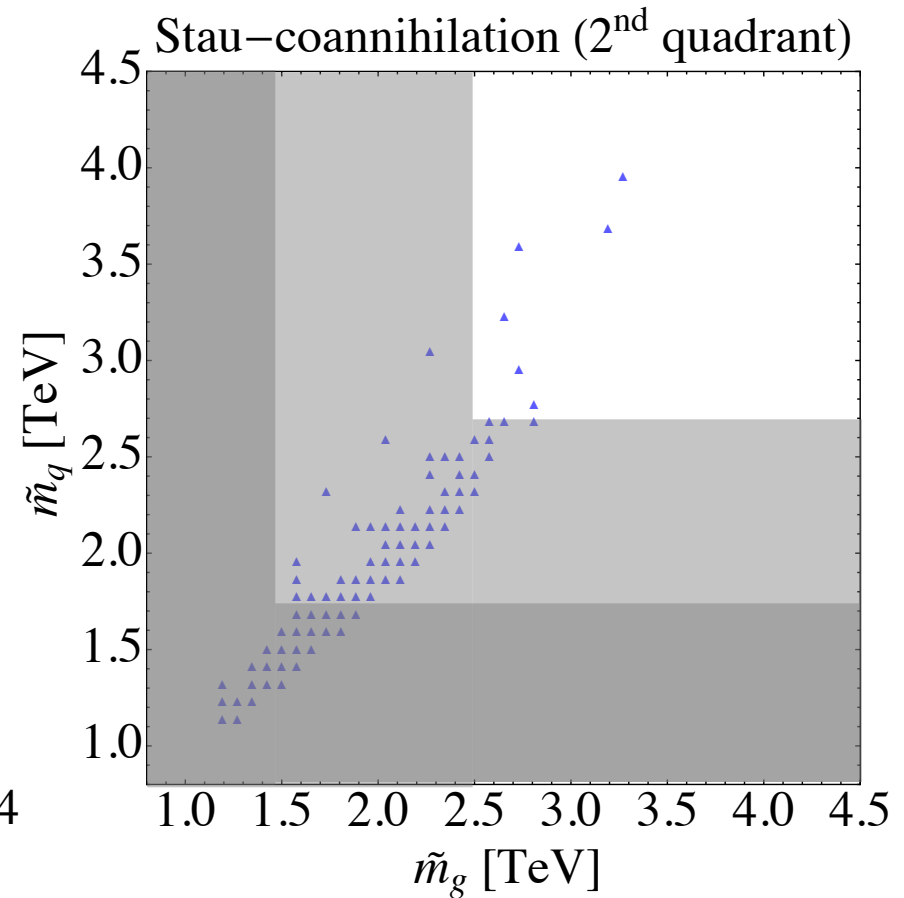
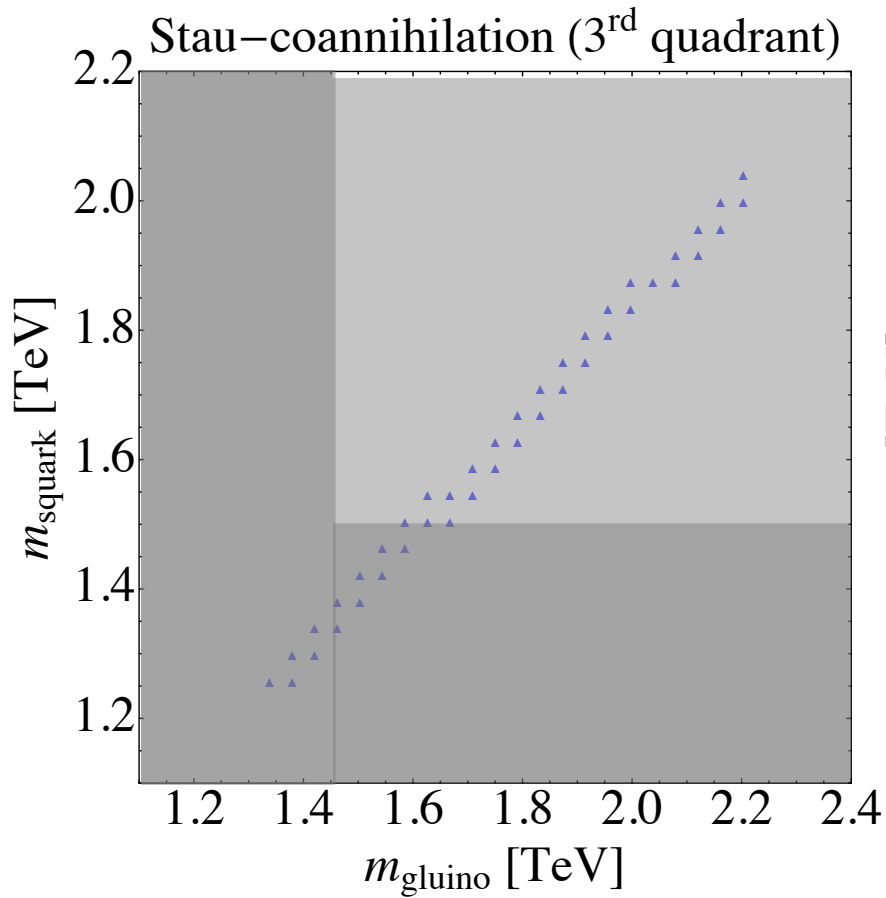
Stau-coann: direct detection



10^{-12} pb

- A 1-ton Xenon experiment can reach spin-independent cross sections of 5×10^{-12} pb at 300 GeV. [Dark matter limit plotter \[http://dmtools.brown.edu/\]](http://dmtools.brown.edu/)
- Direct detection can probe all of the 2nd quadrant.

Stau-coann: squark-gluino plane



- Are these spectra discoverable at the LHC?

A stau-coann benchmark (3rd quad)

Input parameters						
M_0	$M_{1/2}$	A_0	$\tan \beta$	$\text{sign}(\mu)$	$ \mu $	B_μ
259.515	900.862	-2296.71	9.23077	-1	-1555.68	7.574×10^7

- The LSP is 383.52 GeV; the stau is 383.8 GeV.
 - The stau lifetime is $O(10^{-2} \text{ s})$. Probed via long-lived stau searches?
Citron, Ellis, Luo, Marrouche, Olive, Vries [arXiv:1212.2886]
- The gluino is 1980 GeV.

- The squark masses are

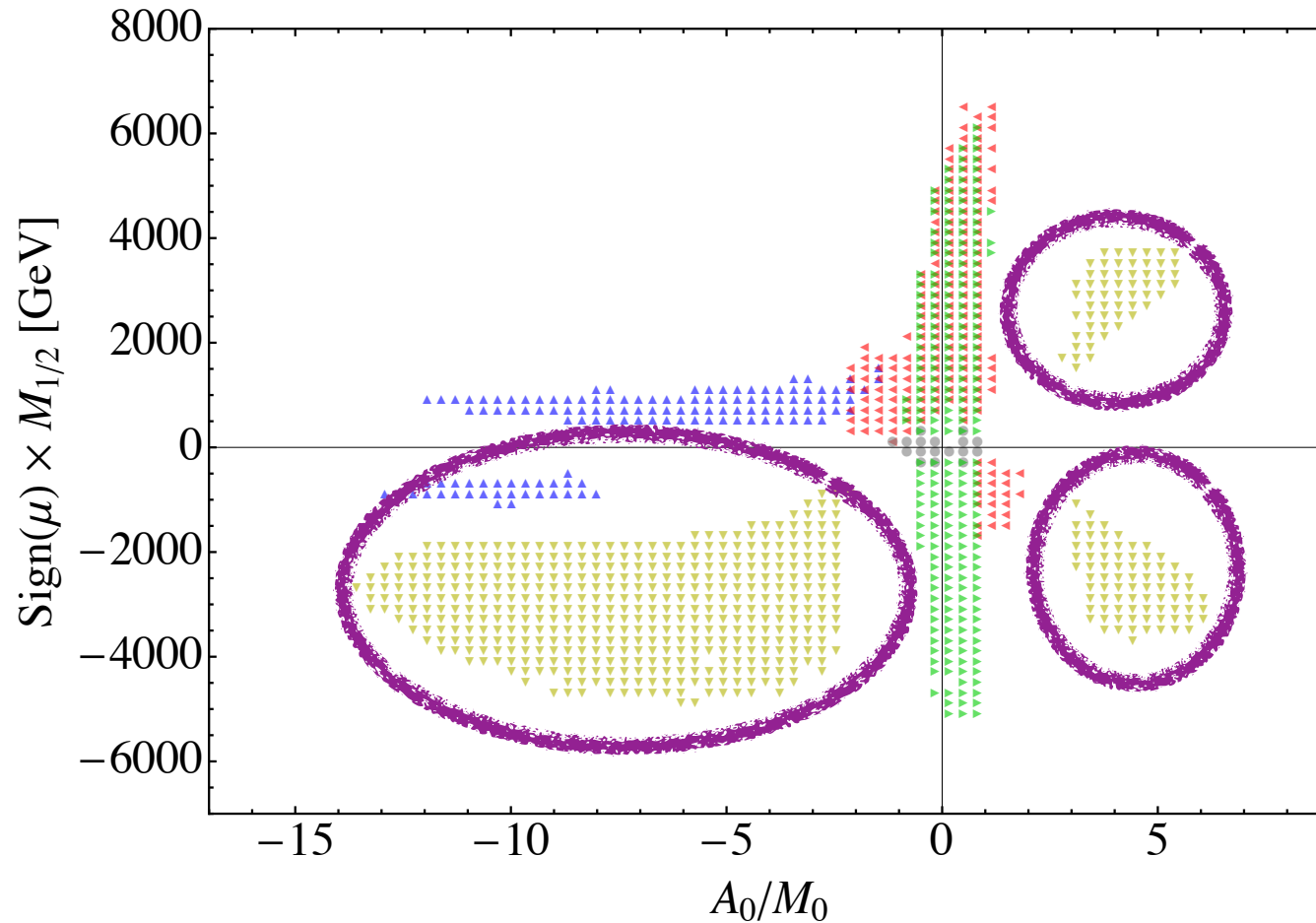
	\tilde{q}	\tilde{b}_1	\tilde{b}_2	\tilde{t}_1	\tilde{t}_2
m [GeV]	1780.8	1529.9	1715.3	1067.2	1562.9

- The gluino branching ratios are
 - $\tilde{g} \rightarrow \tilde{t}_{1,2} + \bar{t}$ [52%]
 - $\tilde{g} \rightarrow \tilde{b}_{1,2} + \bar{b}$ [20%]
 - $\tilde{g} \rightarrow \tilde{q} + \bar{q}$ [28%]
- Probed via gluino pair production?

CIRCUMNAVIGATING THE CMSSM

Stop coannihilation

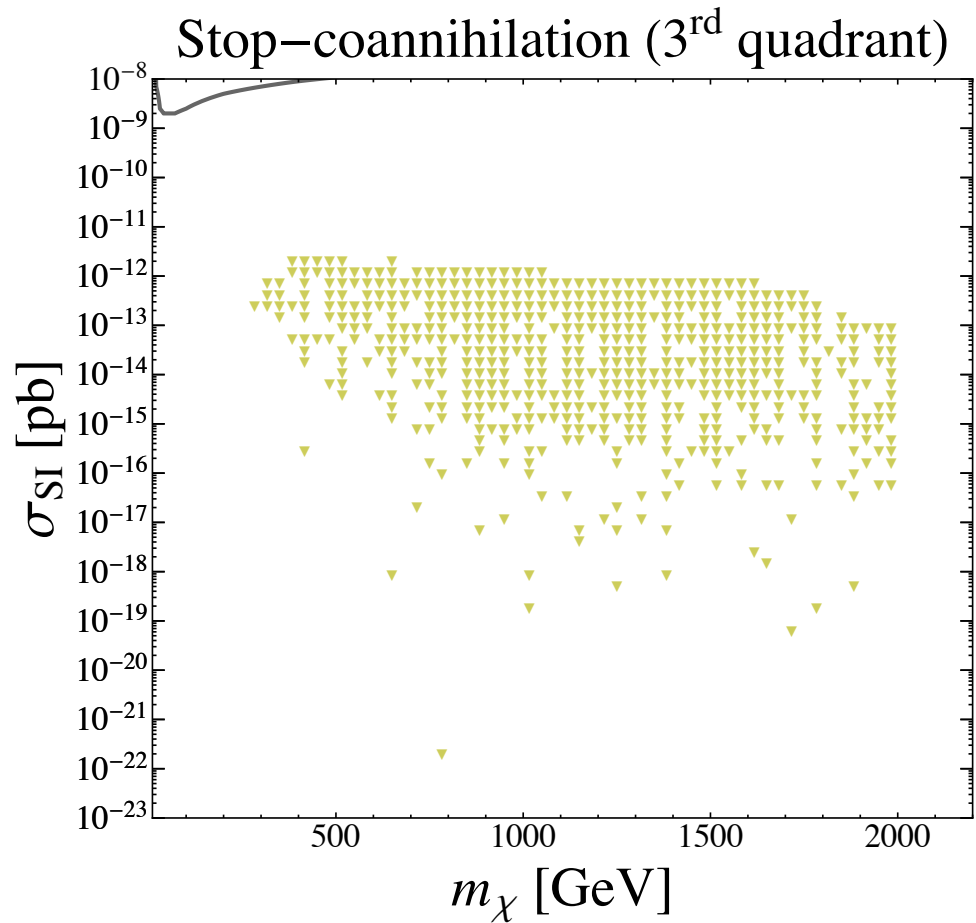
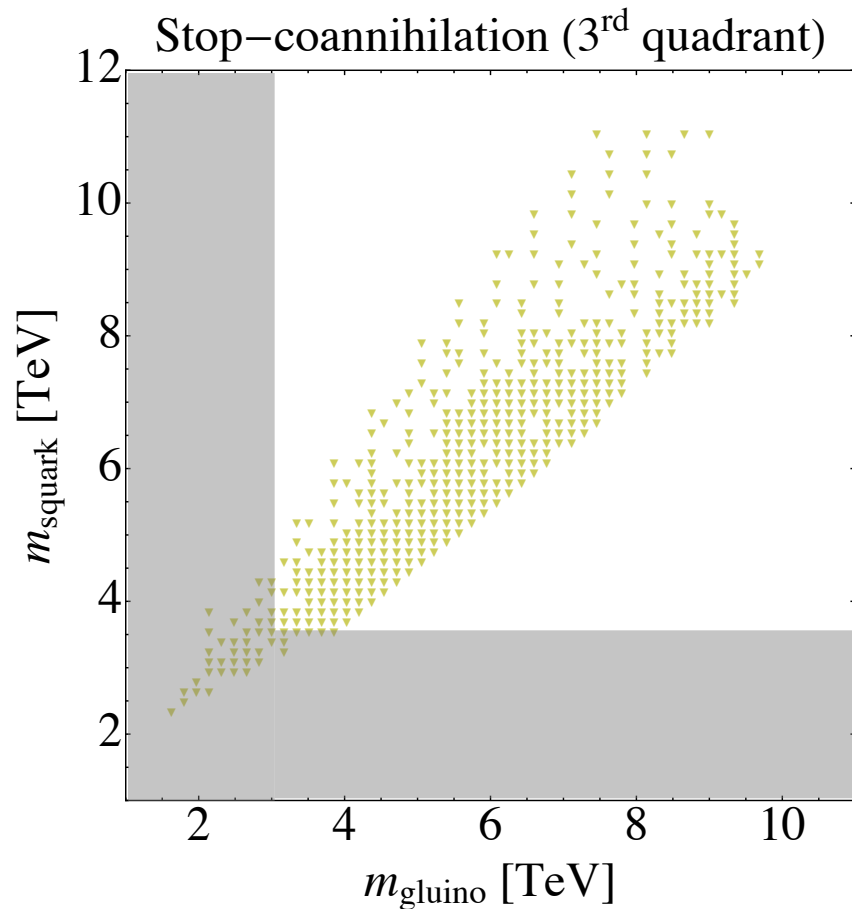
Setting sail for stop coannihilation



- light $\tilde{\chi}^0$
- Well-tempered
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- stop coann

- $2 \text{ TeV} \lesssim M_0 \lesssim 12 \text{ TeV}$
- $\tan \beta \lesssim 50$

Stop-coannihilation phenomenology



- A large portion of these spectra will require a machine beyond the 14 TeV LHC.

A Missing Simplified Model

- A new simplified model appears in stop coannihilation

\tilde{m}_g	\tilde{m}_q	\tilde{m}_{t_1}	\tilde{m}_{τ_1}	m_χ	$m_{\chi_1^\pm}$
2174.1	3200.3	445.51	2636.4	410.64	790.82

$$\tilde{t}_1 \rightarrow \begin{cases} c \chi_1^0 & 69\% \\ b (W^+)^* \chi_1^0 & 31\% \end{cases} \quad \sigma(pp \rightarrow \tilde{t}_1 \tilde{t}_1) = 1.21 \text{ pb.}$$

$$\tilde{g} \rightarrow \bar{t} \tilde{t}_1 + \text{c.c.} \quad 100\% \quad \sigma(pp \rightarrow \tilde{g} \tilde{g}) = 0.42 \text{ fb}$$

$$\tilde{q}_R \rightarrow q \tilde{g} \quad 100\% \quad \sigma(pp \rightarrow \tilde{g} \tilde{q}) = 0.43 \text{ fb.}$$

$$\tilde{q}_L \rightarrow \begin{cases} q \tilde{g} & 88\% \\ q' \chi_1^+ & 8\% \\ q \chi_2^0 & 4\% \end{cases}$$

$$\sigma(pp \rightarrow t \bar{t} \cancel{E}_T X) = 0.41 \text{ fb}$$

$$\sigma(pp \rightarrow t \bar{t} \cancel{E}_T X) = 0.42 \text{ fb}$$

Same Sign Tops
(boosted)



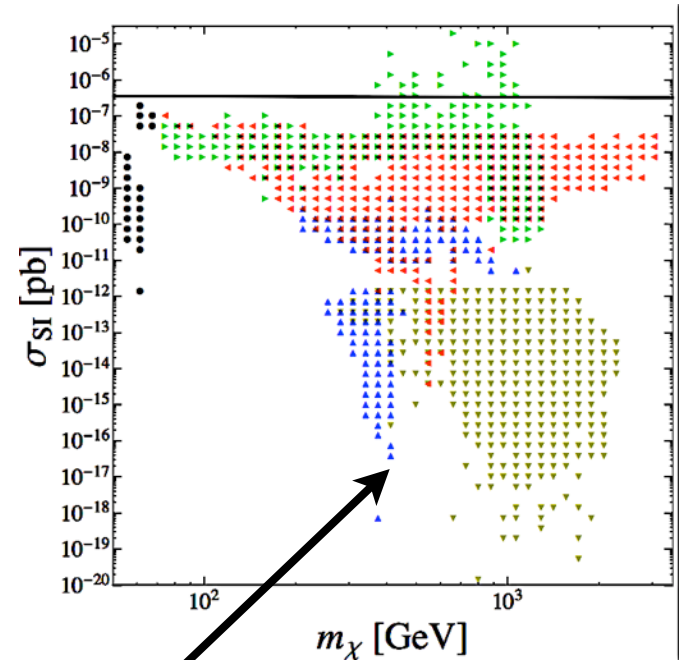
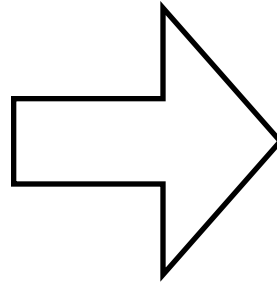
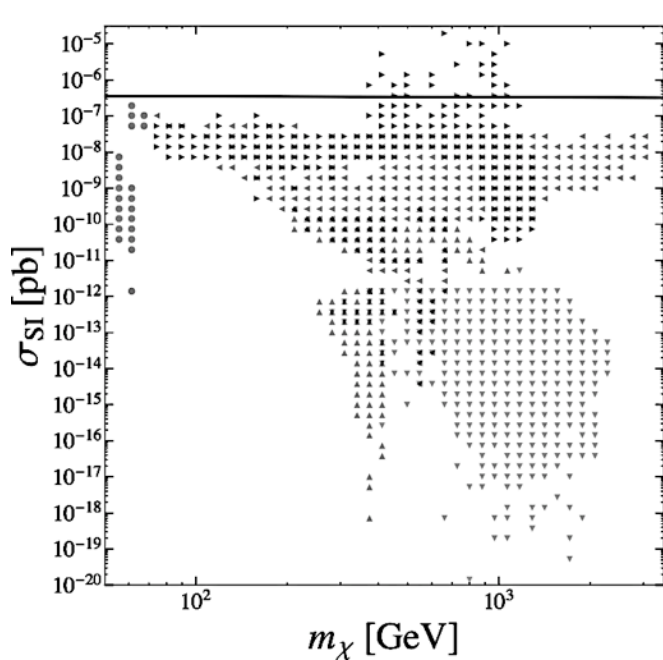
ALMOST HOME

Conclusions

Conclusions

- CMSSM provides tractable ansatz & allows study of full parameter space.
- Provided a map of the CMSSM consistent with Higgs mass & thermal dark matter.
- Demonstrated that parameter space is compact.
- Regions will remain unconstrained after LHC14 and Ton scale spin-independent direct detection?
 - Large portions of the stop coannihilation regions.
- LHC results to be presented as generally as possible so it is easy to interpret bound for non-trivial models
 - More Simplified Model efficiency plots needed.

Colors in the CMSSM



HERE BE DRAGONS