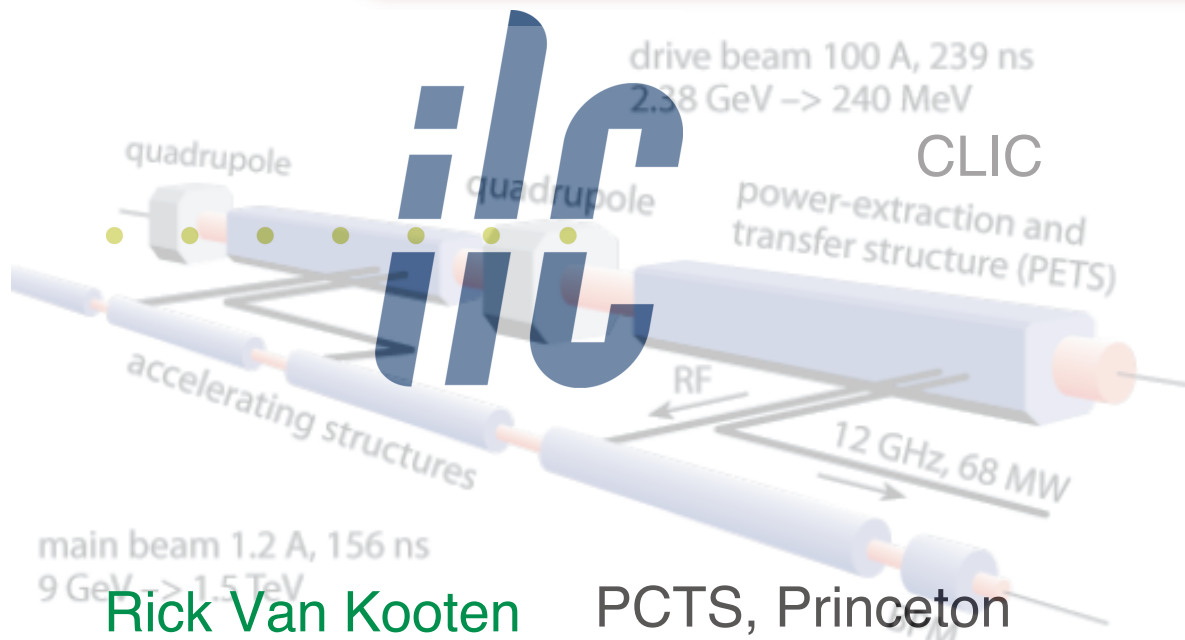


Implications of Higgs Discovery on LC/ e^+e^- Factories



Outline:

- Implications
- Physics
- Facilities
- Organization
- Property measurements
- Some comparisons

Rick Van Kooten
Indiana University

PCTS, Princeton
April 25 – 26, 2013

What we know

Implications for ILC/ e^+e^-

- Scalar Mass ~ 125 GeV
- SM-like couplings to WW and ZZ
 - major production reactions present in e^+e^-

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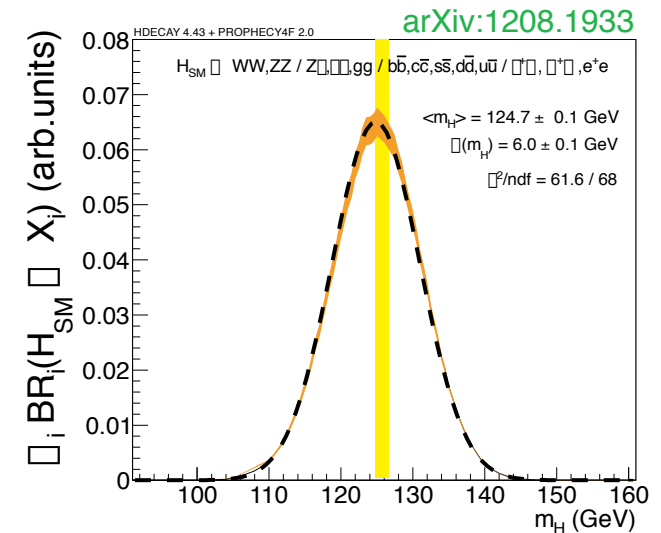
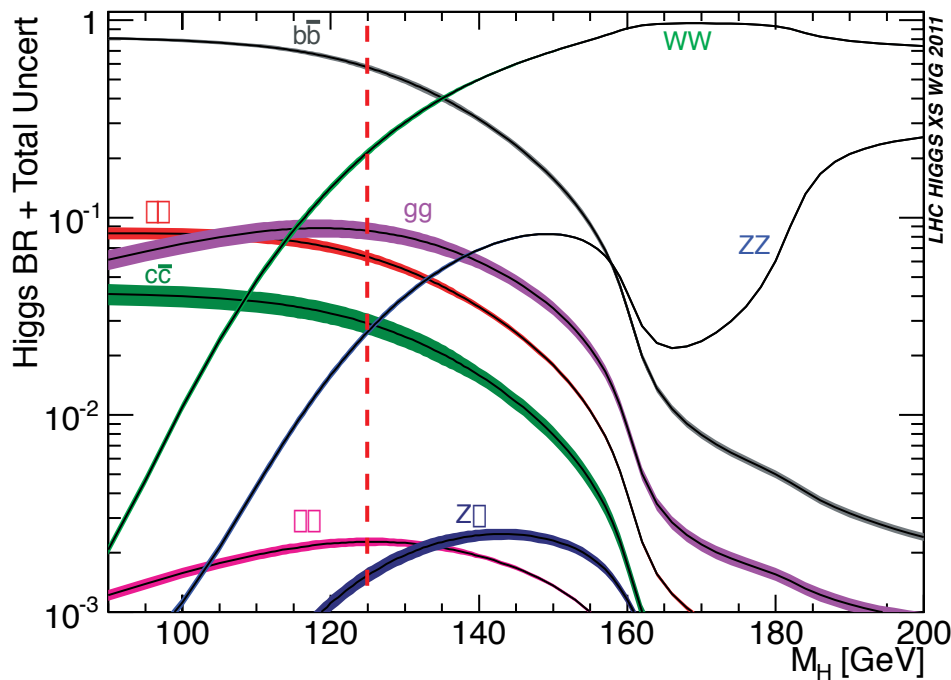
accessible to
 $E_{cm} \geq 250$ GeV
 e^+e^-

What we know

Implications for ILC/ e^+e^-

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- SM-like Br 's expected

accessible to
 $E_{cm} \geq 250$ GeV
 e^+e^-



Mass of "maximum opportunity"
in terms of the study of its decays
and couplings to other particles

What we know

- Scalar Mass ~ 125 GeV
- SM-like couplings to WW and ZZ
→ major production reactions present in
- SM-like Br 's expected

Implications for ILC/ e^+e^-

accessible to
 $E_{cm} \geq 250$ GeV
 e^+e^-

flurry of machine
options being
considered

political trigger, particularly
for ILC in Japan

What we know

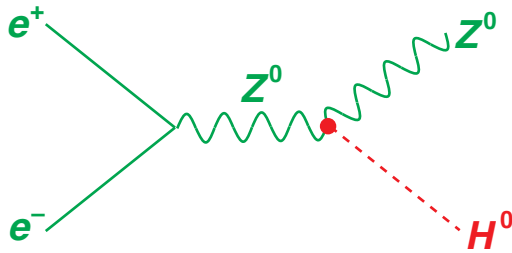
- Scalar Mass ~ 125 GeV
- SM-like couplings to WW and ZZ
 - major production reactions present in
- SM-like Br 's expected
- $t\bar{t}H$ coupling exists ($gg \rightarrow H, H \rightarrow \gamma\gamma$)
 - direct $e^+e^- \rightarrow t\bar{t}H$ exists (need higher collision energies)
- J^{PC} mainly 0^{++} (but want sensitive tests of small admixtures)

Implications for ILC/ e^+e^-

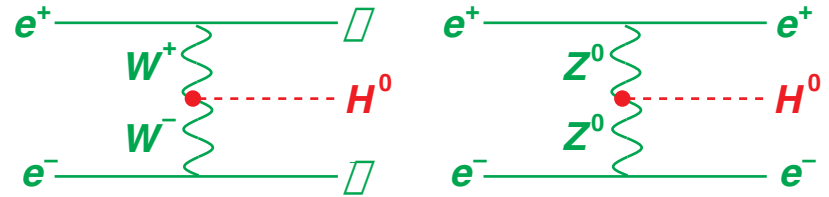
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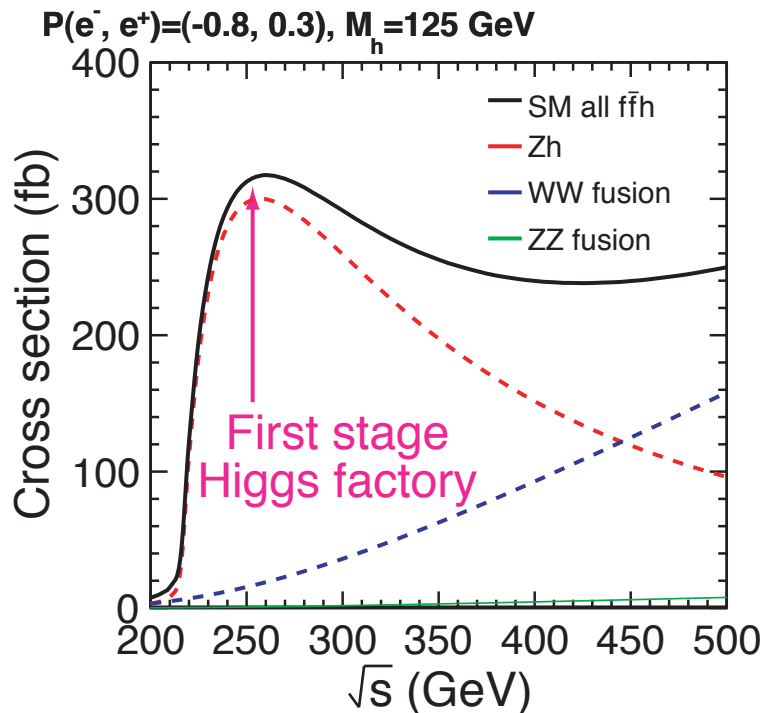
Higgs Production



- "Higgs"strahlung

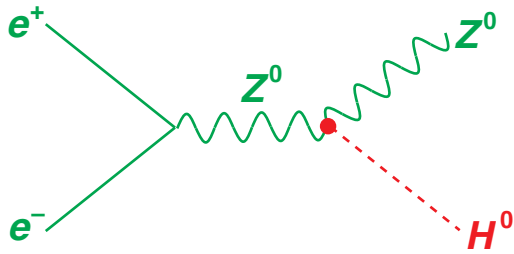


- Fusion

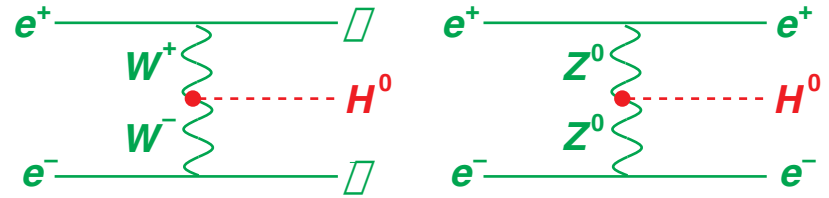


- Clean
- Democratic
 - 1 Higgs in $\sim 10^9 - 10^{12}$ pp collisions
 - 1 Higgs in 1% of all e^+e^- collisions
- Calculable
- Longitudinal Polarization
 - (linear colliders): can boost signal, control SM backgrounds
 - (unpolarized cross section at ~ 200 fb for circular colliders, transverse polarization available)

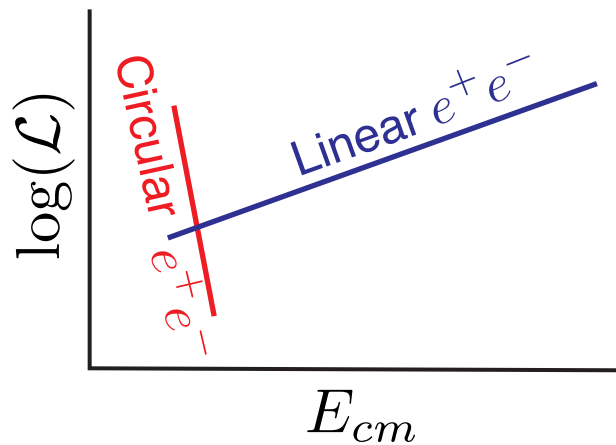
Higgs Production



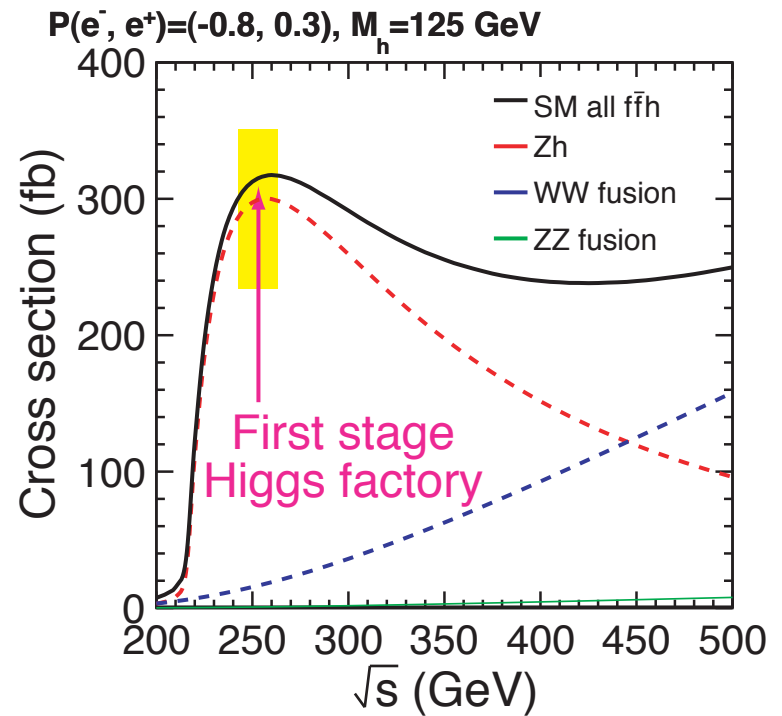
- "Higgs"strahlung



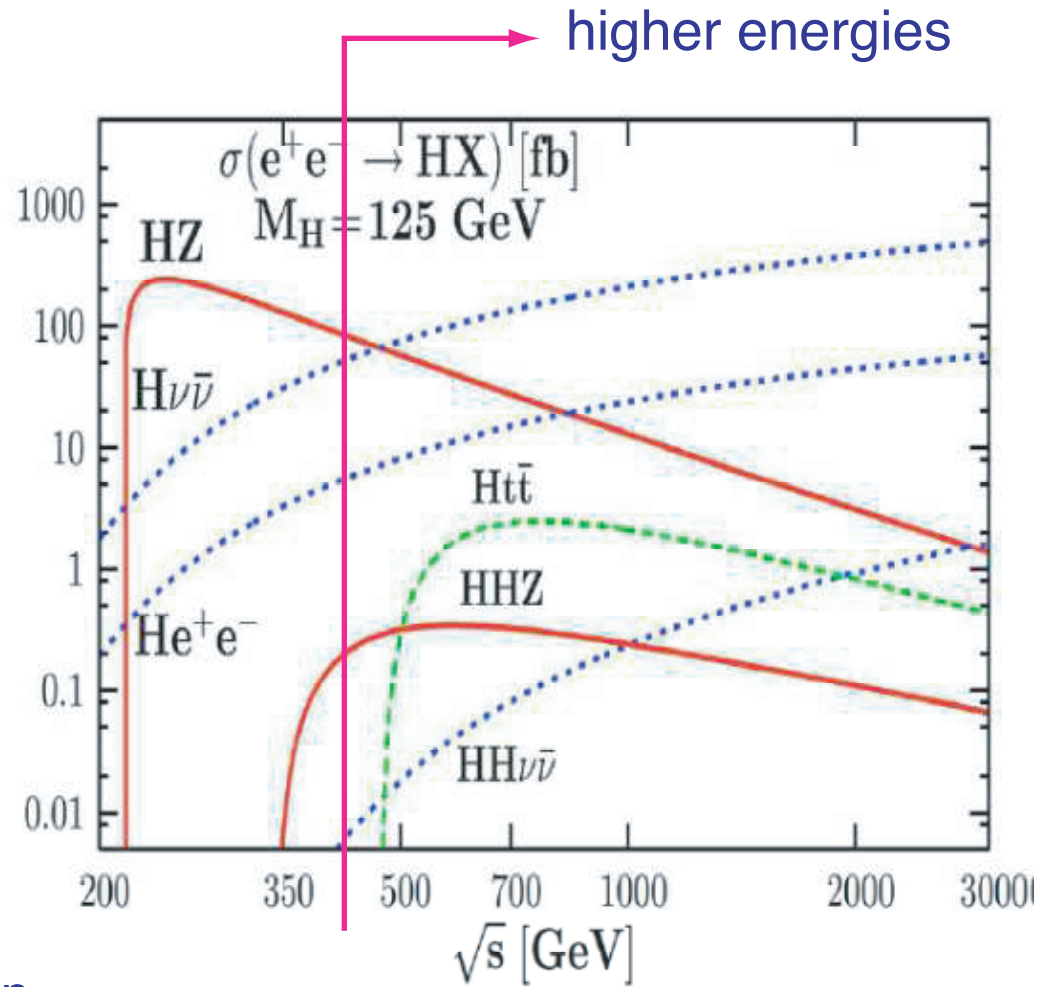
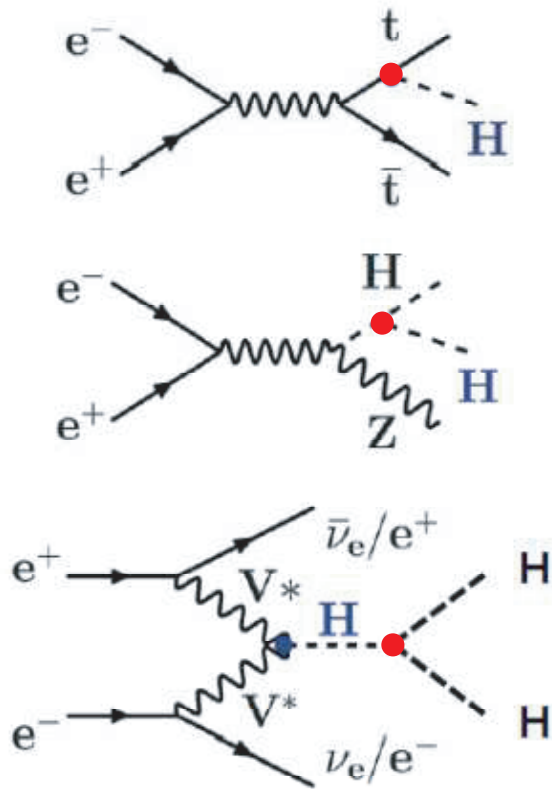
- Fusion



→ circular machines usually
 $E_{cm} \simeq 240 \text{ GeV}$

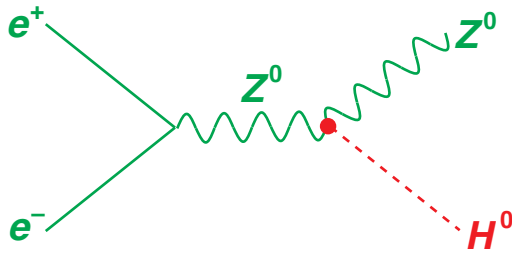


Higgs Production

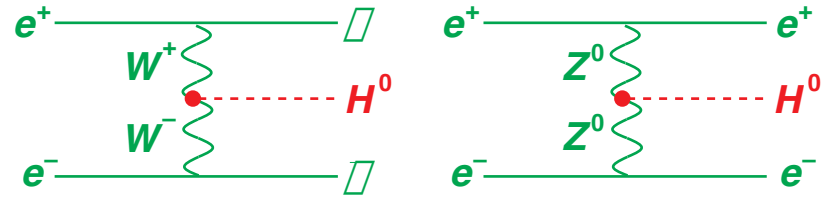


- (direct) coupling to top
- self-coupling

Higgs Production



• "Higgs"strahlung



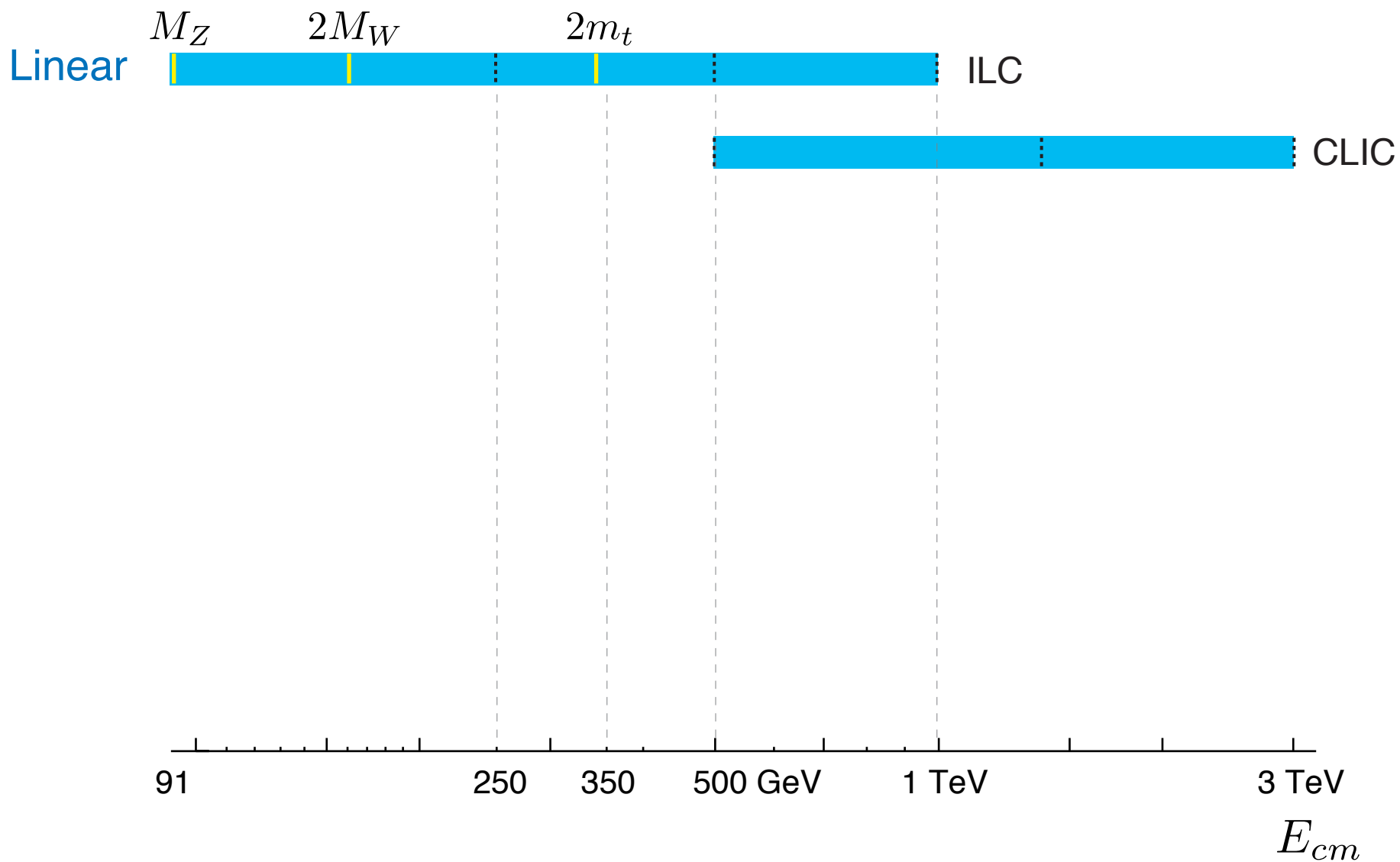
• Fusion

Typical ILC program, 3 – 5 years each energy:

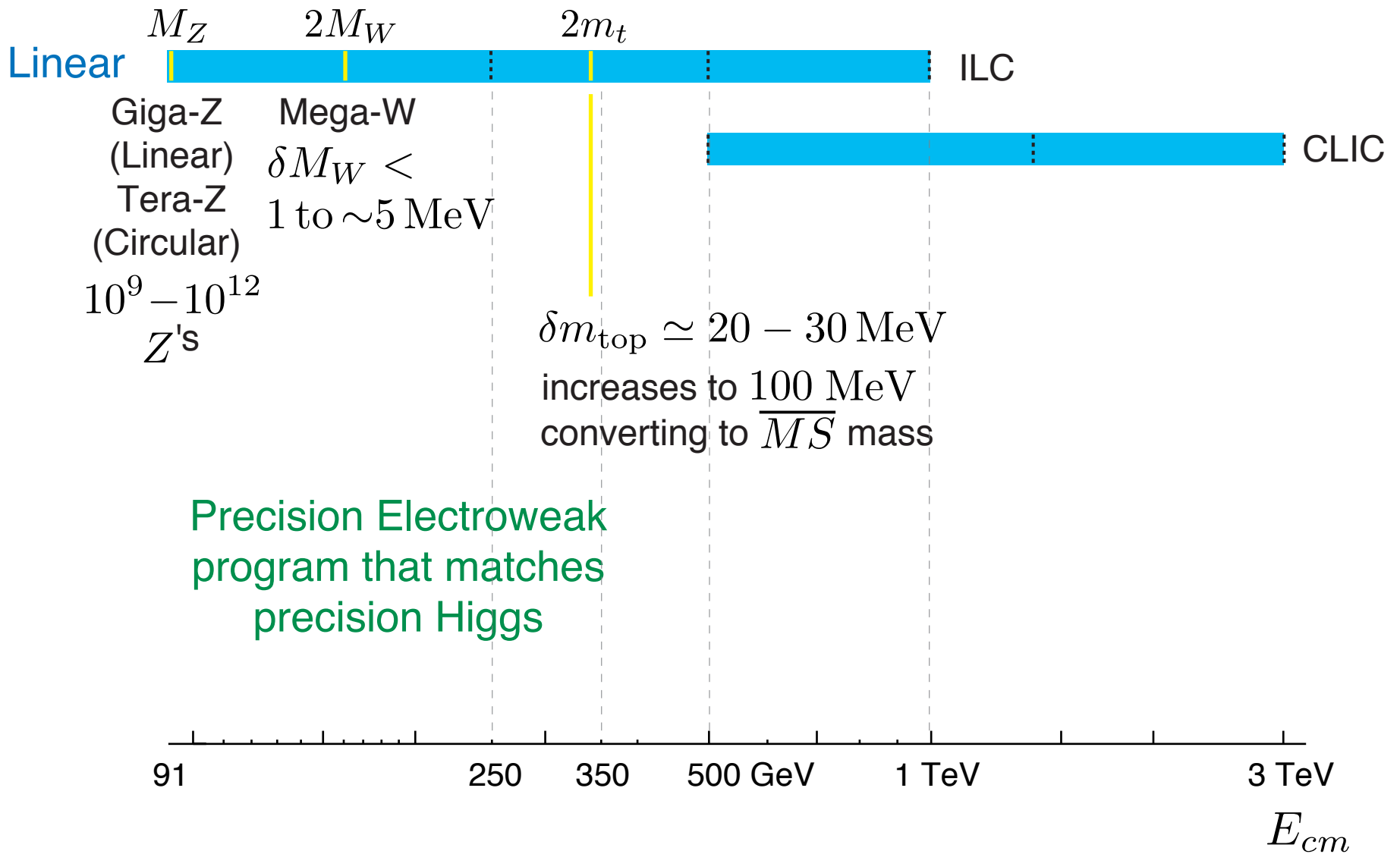
	250 GeV	350 GeV	500 GeV	1 TeV	1.5 TeV	3 TeV
$\sigma(e^+e^- \rightarrow ZH)$	300 fb	129 fb	57 fb	13 fb	6 fb	1 fb
$\sigma(e^+e^- \rightarrow \nu\nu H)$	18 fb	30 fb	75 fb	210 fb	309 fb	484 fb
Int. Luminosity	250 fb ⁻¹	350 fb ⁻¹	500 fb ⁻¹	1 ab ⁻¹	1.5 ab ⁻¹	2 ab ⁻¹
# ZH events	75,000	45,500	28,500	13,000	7,500	2,000
# $\nu\nu H$ events	4,500	10,500	37,500	210,000	460,000	970,000

Polarized

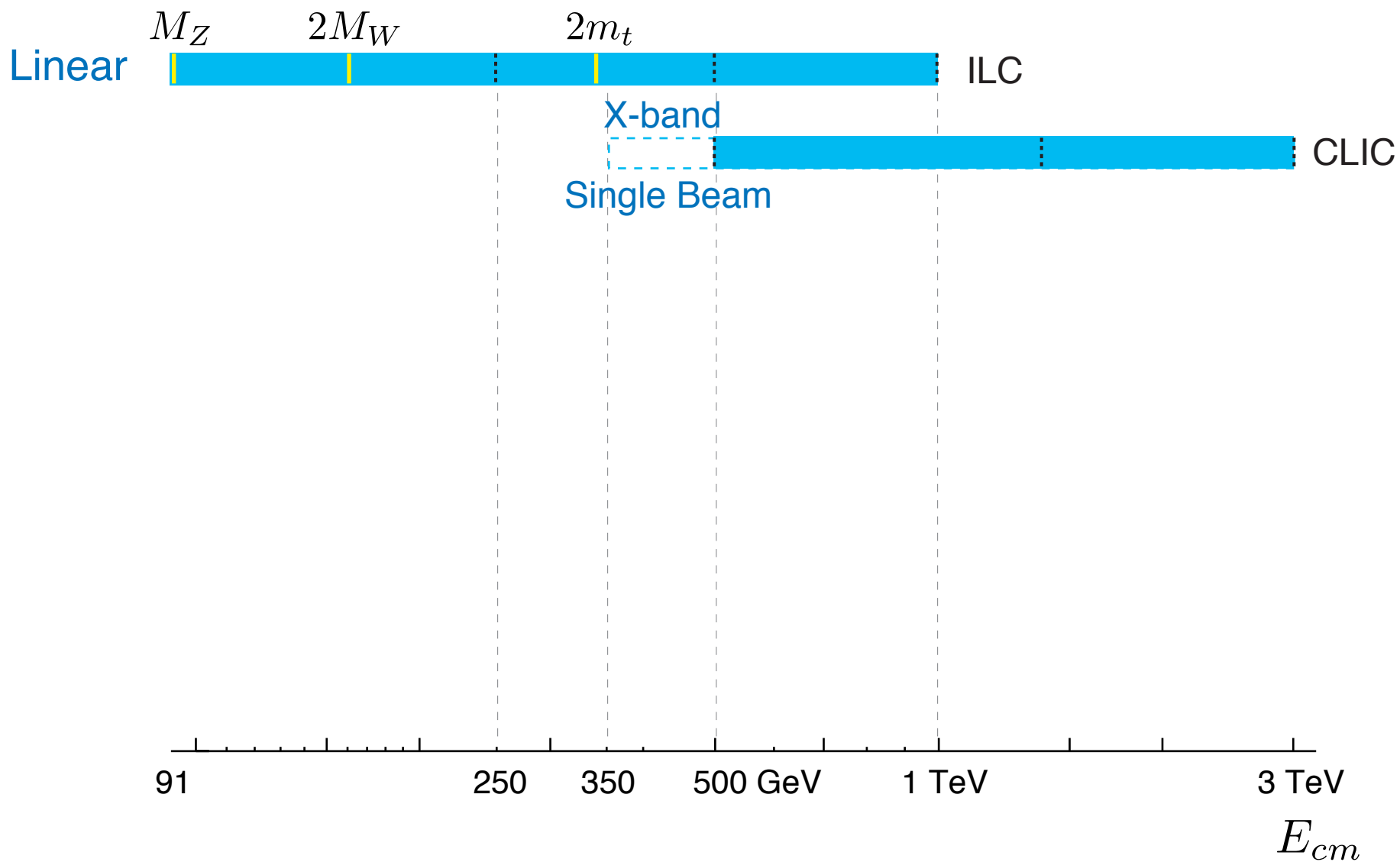
e^+e^- Facilities



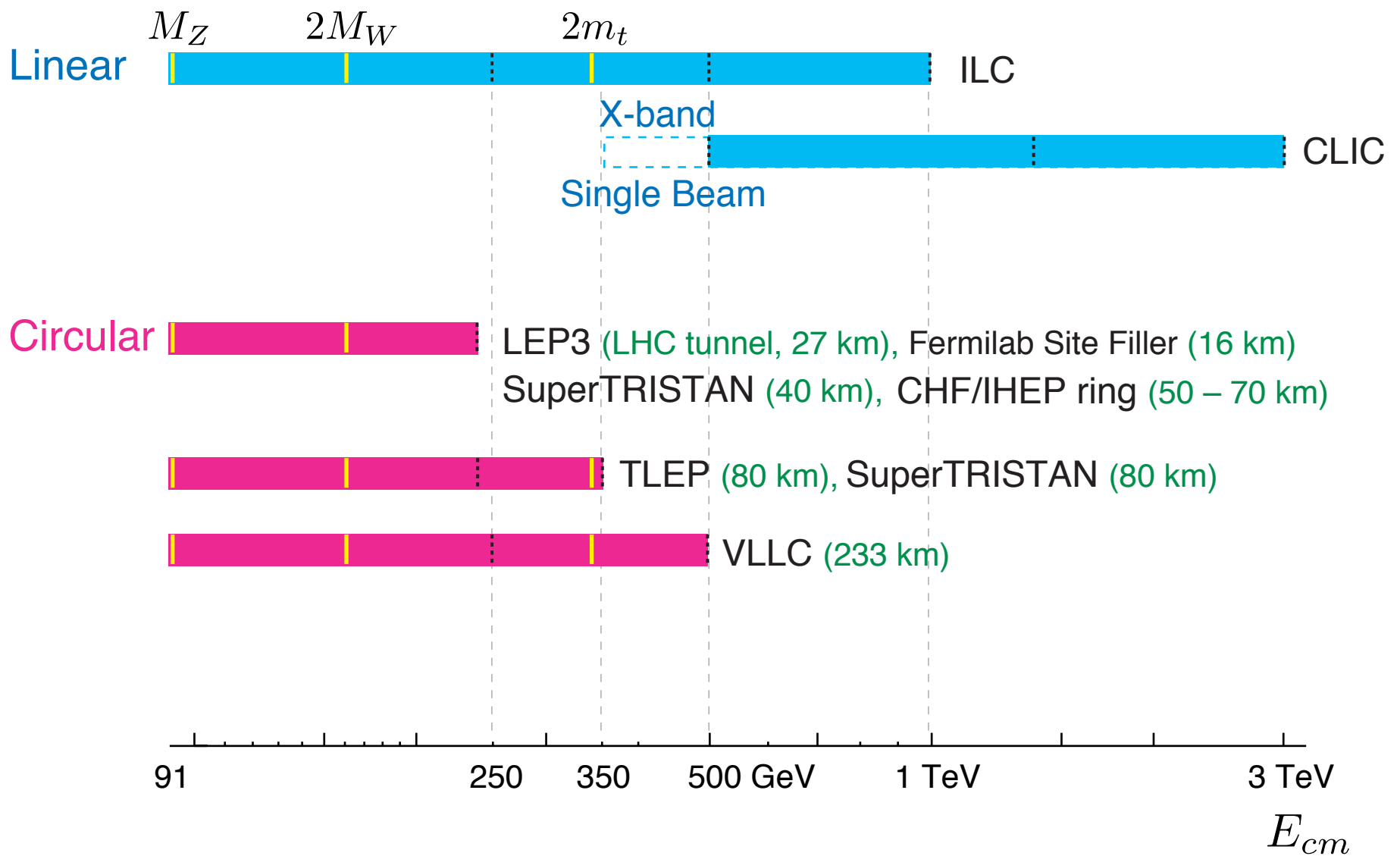
e^+e^- Facilities



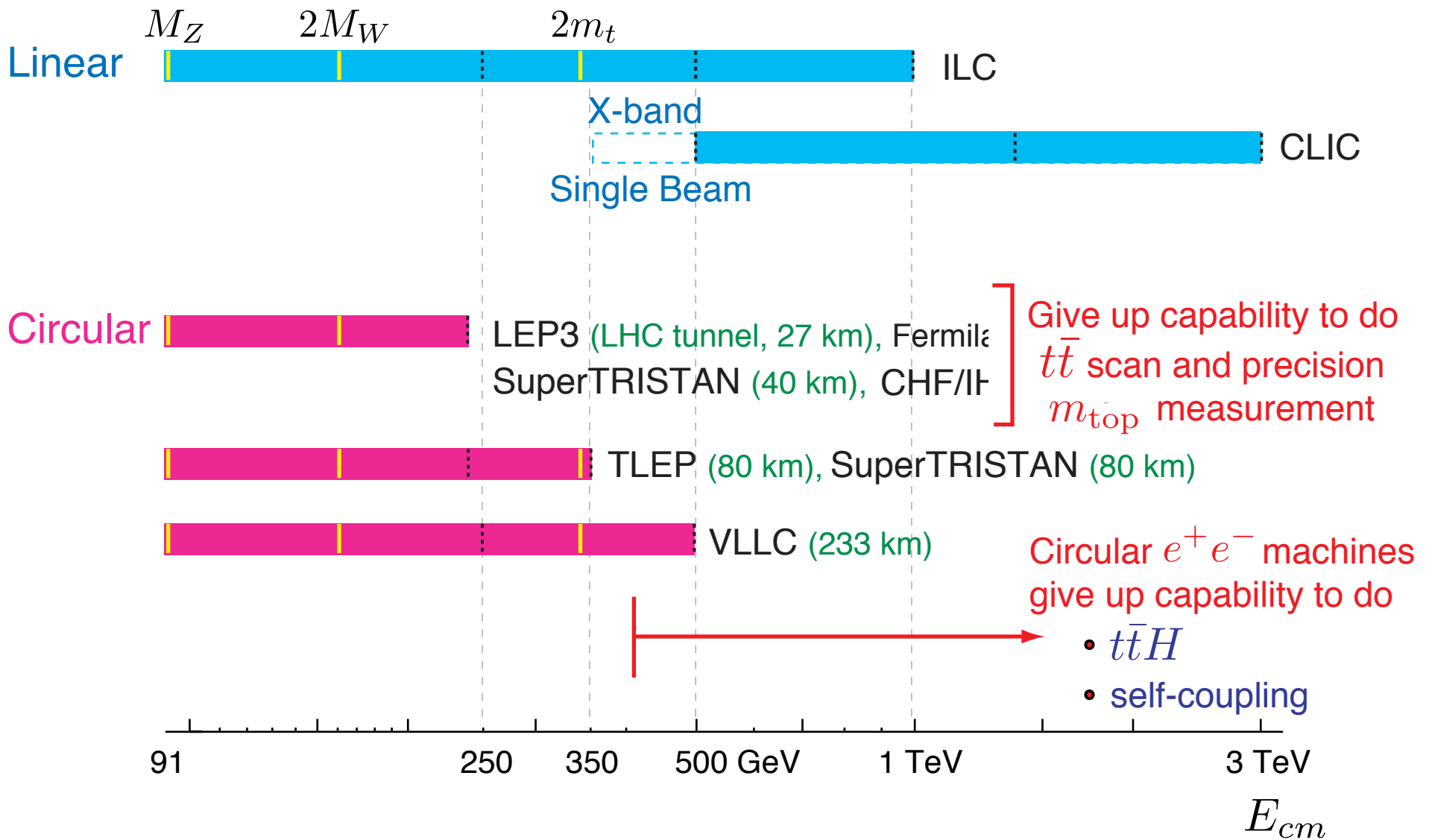
e^+e^- Facilities



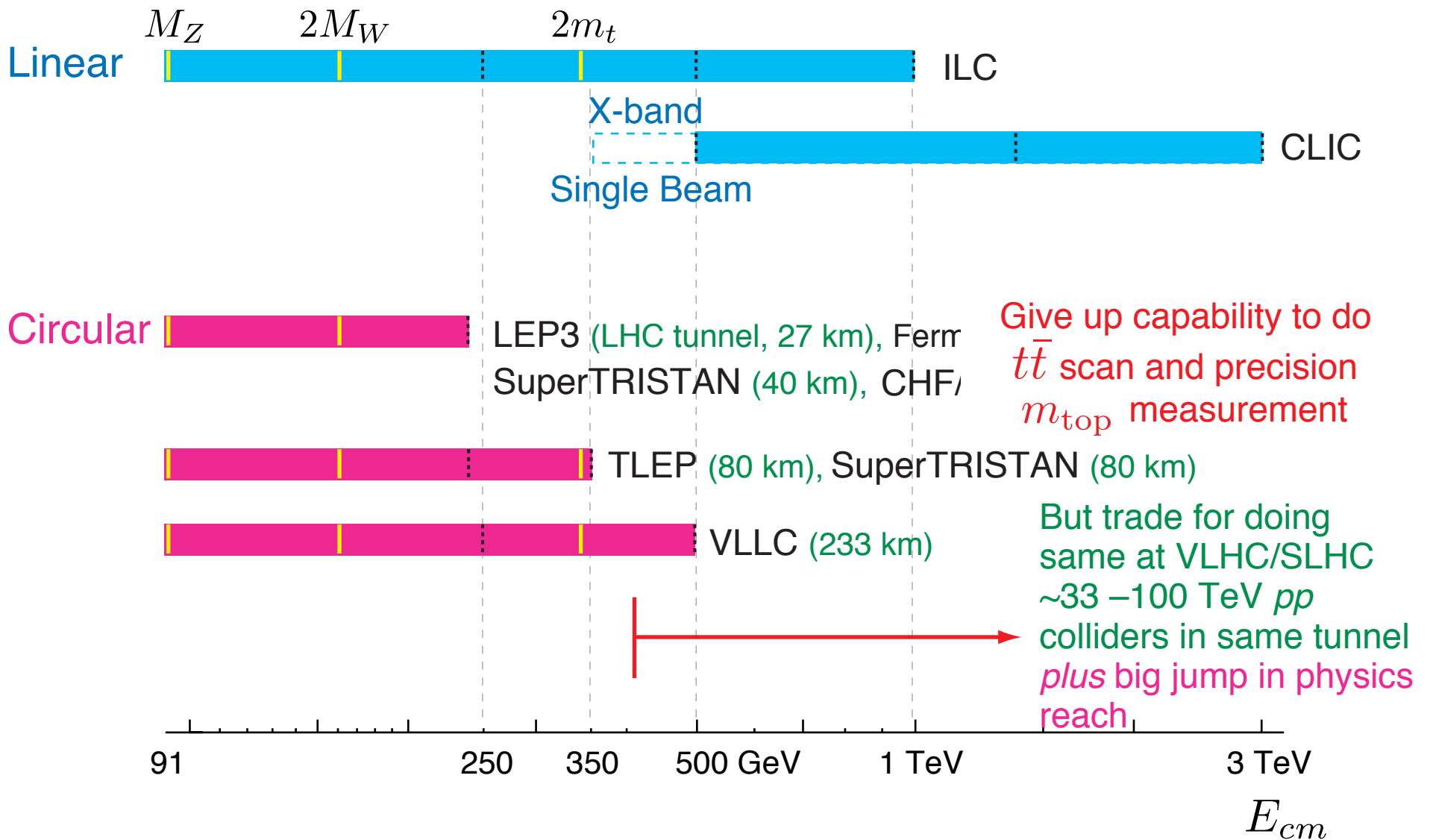
e^+e^- Facilities



e^+e^- Facilities



e^+e^- Facilities

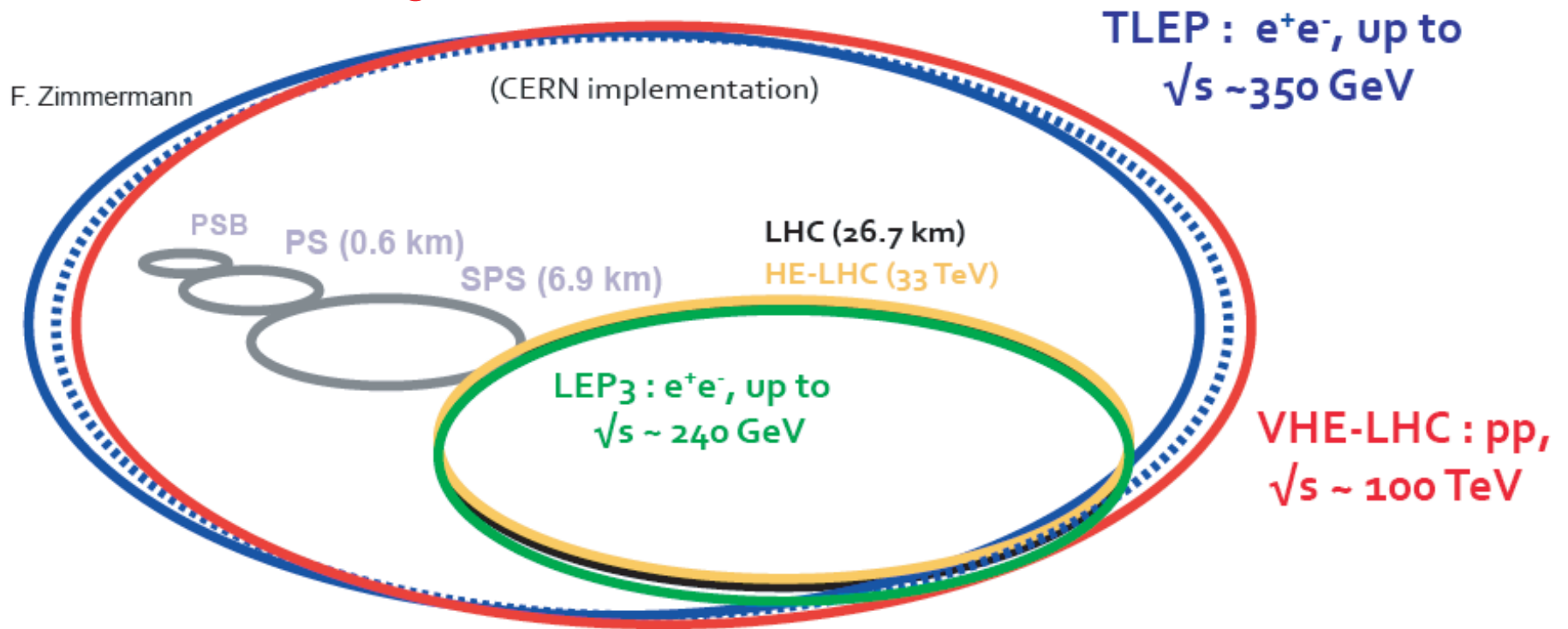


Circular

(~no beamstrahlung: full \sqrt{s} , recirculating beams,
multiple detectors, no energy upgrade)

Short beam lifetime (minutes), top-up injection from separate
accelerating ring

New ~80 km ring:



- At White Paper stage, planning Conceptual Design Report

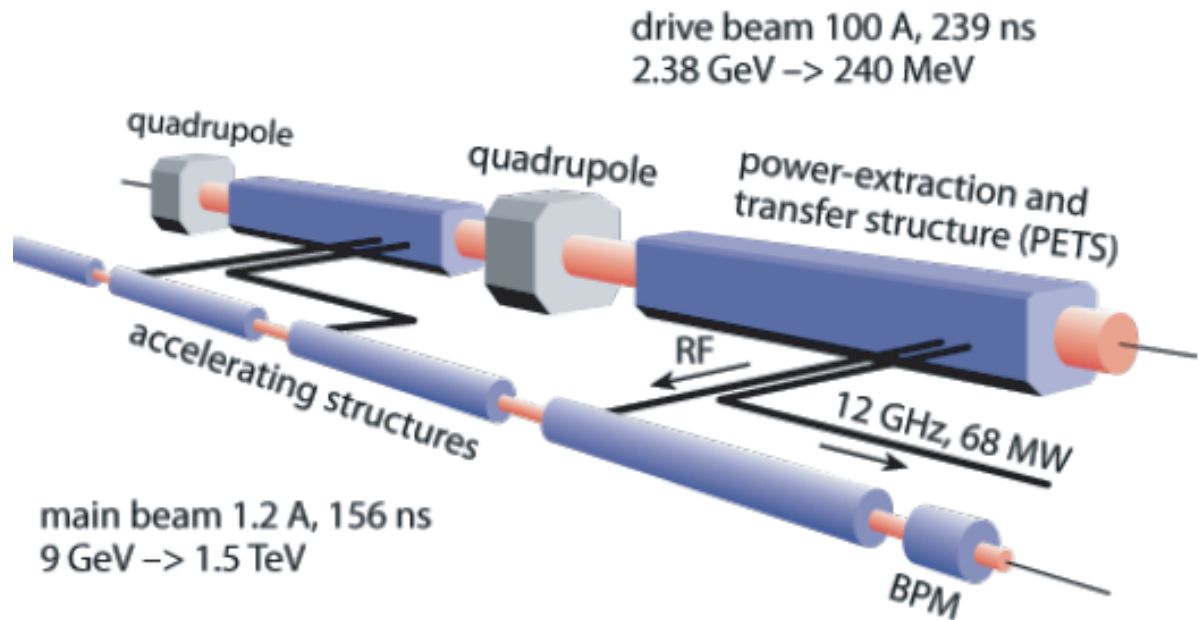
Linear

$$\begin{aligned}\sqrt{s} &= 500 \text{ GeV} \\ &= 1.5 \text{ TeV} \\ &= 3 \text{ TeV}\end{aligned}$$

(looking at lower energy options)

CLIC (Compact Linear Collider)

Two beams: low E, high current drive; ~48 km long



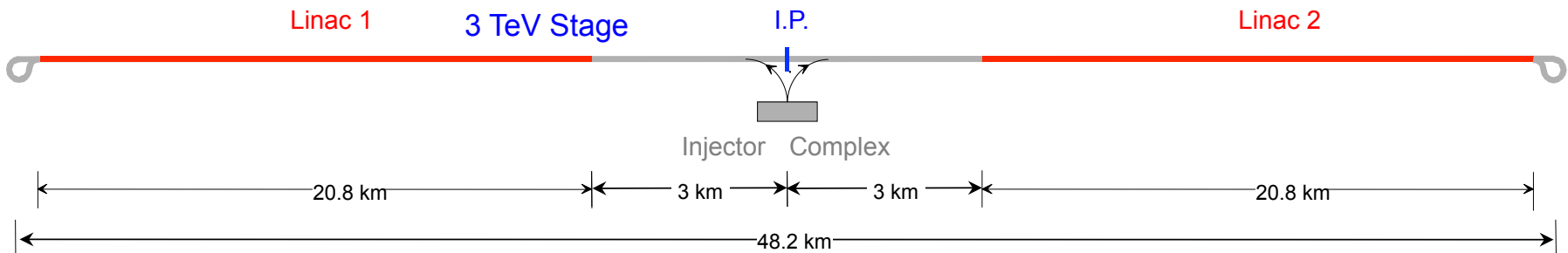
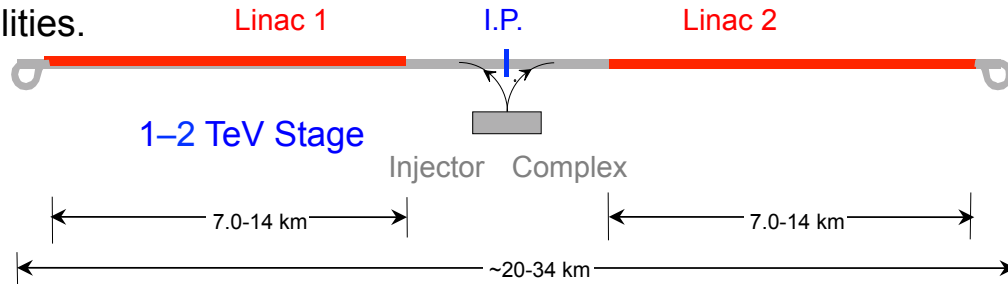
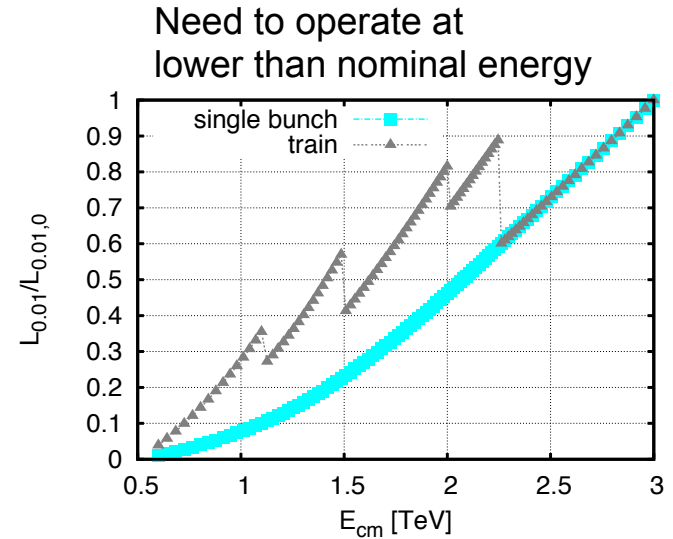
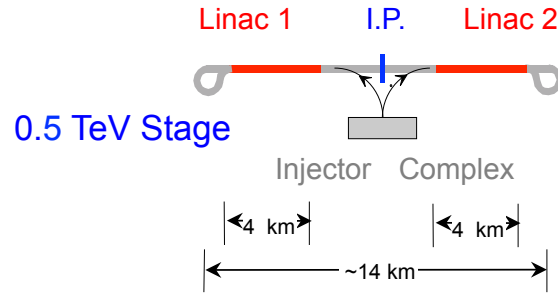
- Conceptual Design Report completed in 2012

<http://clic-study.org/accelerator/CLIC-ConceptDesignRep.php>

CLIC two-beam scheme compatible with energy staging to provide the optimal machine for a large energy range.

Lower energy machine can run most of the time during the construction of the next stage.

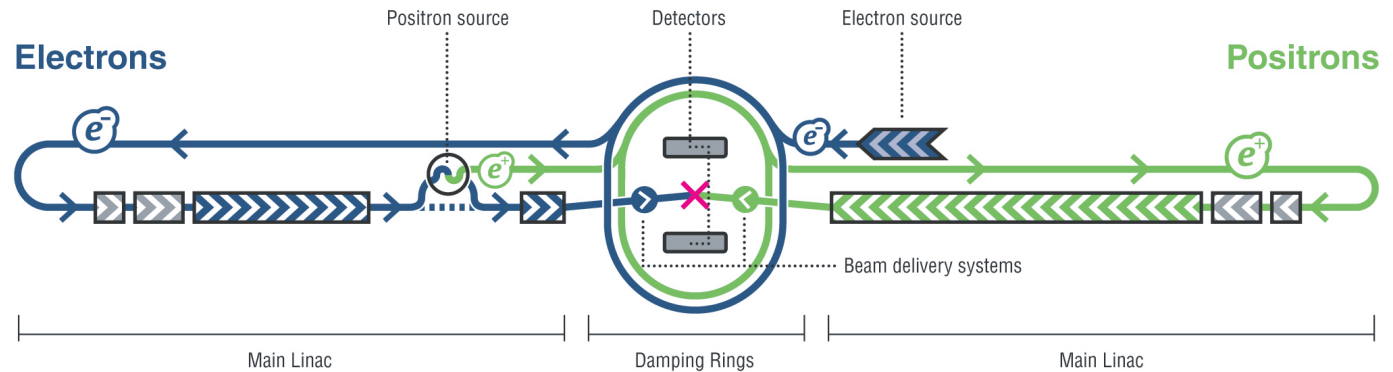
Recently studies have begun on a **~375 GeV first stage** with single beam, switching to two-beam at higher energies which reuses the low energy facilities.



Linear

$\sqrt{s} = 250 \text{ GeV}^\dagger$ ILC (International Linear Collider)
= 500 GeV Superconducting cavities, ~30 km long
= 1 TeV

† cost does not scale linearly!



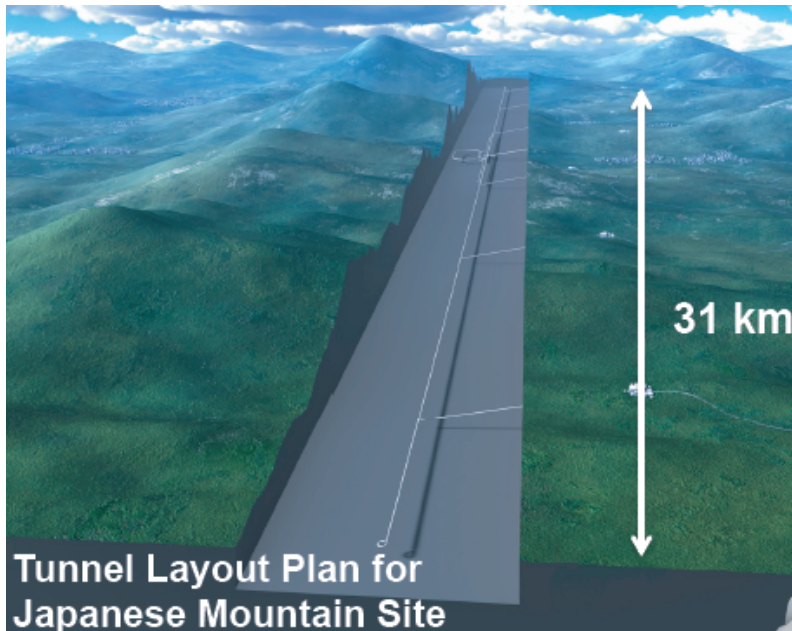
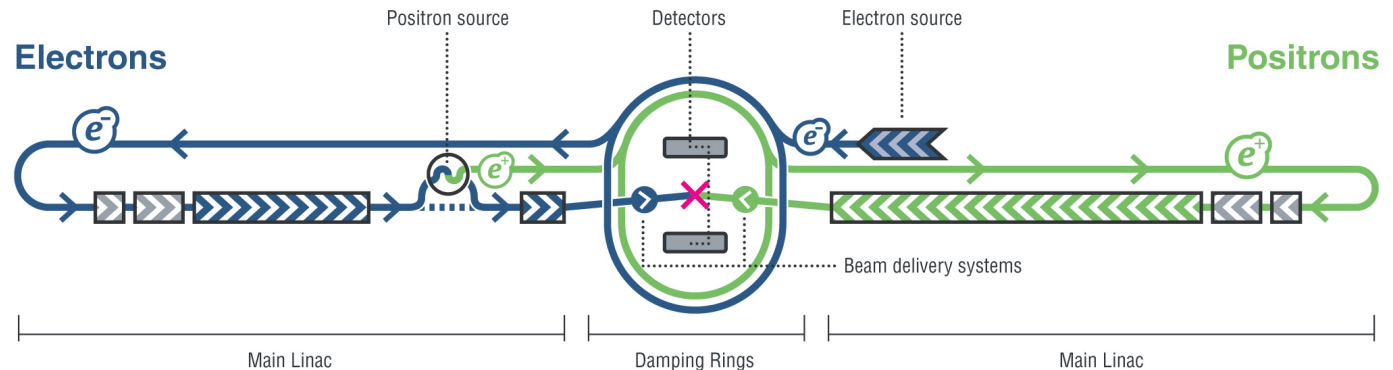
- ILC Technical Design Report (2013) (including full costing)
Draft versions of Detailed Baseline Design Report, Physics & Detectors:
<http://ific.uv.es/~fuster/DBD-Chapters/>
Final version
(including Accelerator via multi-year Global Design Effort)
will be available in 2013

Linear

$$\begin{aligned}\sqrt{s} &= 250 \text{ GeV}^\dagger \\ &= 500 \text{ GeV} \\ &= 1 \text{ TeV}\end{aligned}$$

† cost does not scale linearly!

ILC (International Linear Collider)
Superconducting cavities, ~30 km long



Implication of Higgs discovery:
political trigger point

Hitoshi Muryama, BNL Energy
Frontier Meeting

[https://indico.bnl.gov/materialDisplay.py?
contribId=57&sessionId=11&materialId=slides&confId=571](https://indico.bnl.gov/materialDisplay.py?contribId=57&sessionId=11&materialId=slides&confId=571)

Tomohiko Tanabe, Princeton
Snowmass Higgs Meeting

[http://physics.princeton.edu/indico/contributionDisplay.py?
contribId=13&sessionId=7&confId=127](http://physics.princeton.edu/indico/contributionDisplay.py?contribId=13&sessionId=7&confId=127)

Situation in Japan

- March 2012: Japan Association of High Energy Physicists:

"Should a new particle such as a Higgs boson with a mass below approximately 1~TeV be confirmed at LHC, Japan should take the leadership role in an early realization of an e^+e^- linear collider. In particular, if the particle is light, experiments at low collision energy should be started at the earliest possible time."

- Oct. 2012: Japan Association of High Energy Physicists:

"On the basis of these developments and following the subcommittee's recommendation on ILC, JAHEP proposes that ILC be constructed in Japan as a global project with the agreement of and participation by the international community.

Staging:

- A Higgs factory with a CM energy of ~250 GeV to start*
- Upgraded in stages to ~500 GeV (ILC baseline)*
- Technical expandability to ~1 TeV to be secured*

Situation in Japan

- KEK 2013 Roadmap:
"aims at starting the construction under international framework within the duration of this roadmap (5 years from 2014)."
- Guideline for cost sharing
The host country to cover 50% of the expenses (construction) of the overall project of the 500 GeV machine.
The actual contribution, however, should be left to negotiations among the governments.

Situation in Japan



Dec. 2012: new political party elected, new prime minister Shinzo Abe

ILC explicitly mentioned twice in campaign policy document

In his State of the Union equivalent speech

Answered questions on it in parliament

'Federation of Diet Members for Promotion of the ILC', two ministers to be visiting D.C.

Situation in Japan



Dec. 2012:
prime min

ILC explicit
policy doc

In his State

Answered

'Federation
of the IL



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D.C.

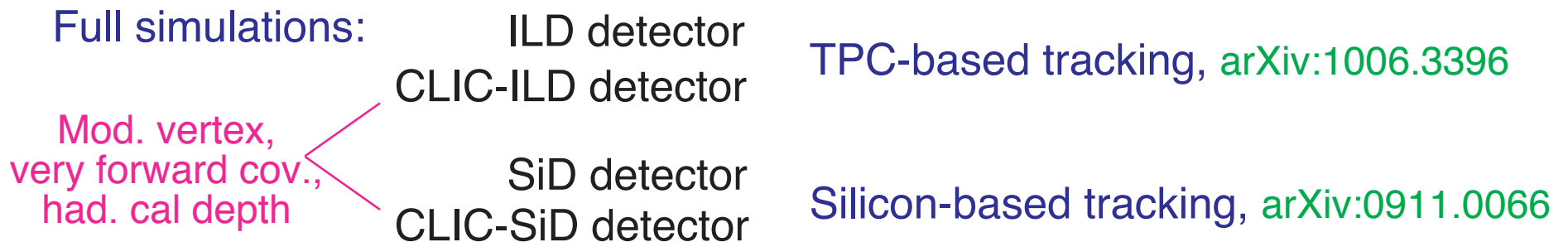
LC Organization

Studies of measurements of mass, J^{PC} , couplings, etc., going on for ~20 years so generally mature, in decent shape, and fairly up-to-date, *but still holes, always room for improvements, and now responding to 125 GeV state: white papers for Snowmass*



Recent documents:

- *ILC Reference Design Report V2: Physics*, [arXiv:0709.1893](https://arxiv.org/abs/0709.1893)
- *ILC Detailed Baseline Design Report/Physics*, lcsim.org/papers/DBDPhysics.pdf (draft)
- *CLIC Conceptual Design Report*, [arXiv:1202.5940](https://arxiv.org/abs/1202.5940)



e^+e^- Higgs Factories

LHC already and likely to continue doing a spectacular job!

Necessary increased precision on:

- Mass
- CP admixture
- Separate cross sections
- Separate branching fractions
- Total width

Complementary to LHC

Remember: if expect deviations of only a few %,
need $\frac{\text{few \%}}{5}$ for a 5 σ "discovery" ...

e^+e^- Higgs Factories

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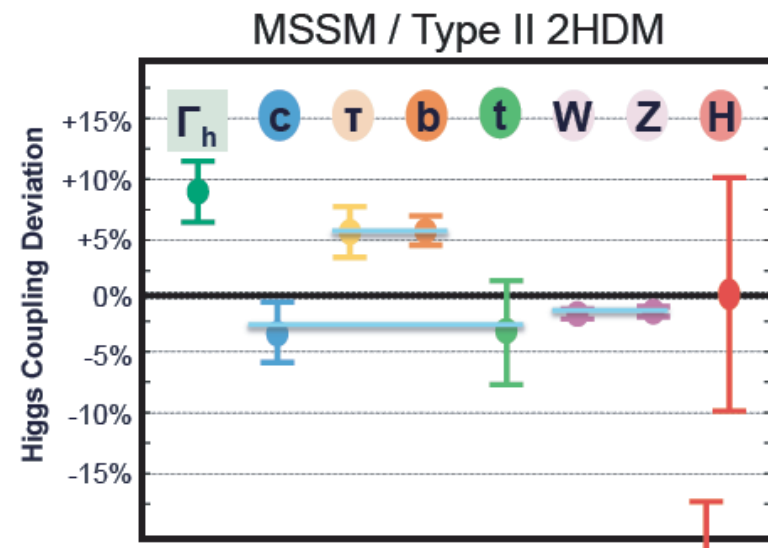
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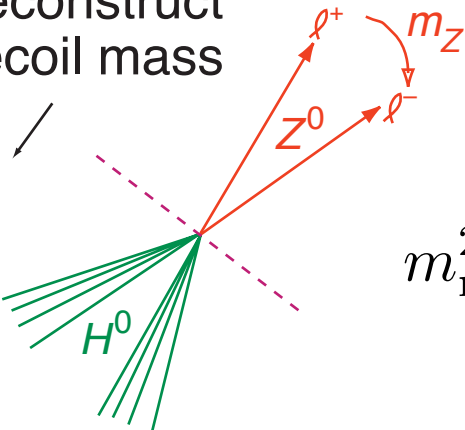
...although there may be patterns:



$\sqrt{s} \simeq 250 \text{ GeV}$, Cross Section

The first step...

Reconstruct recoil mass

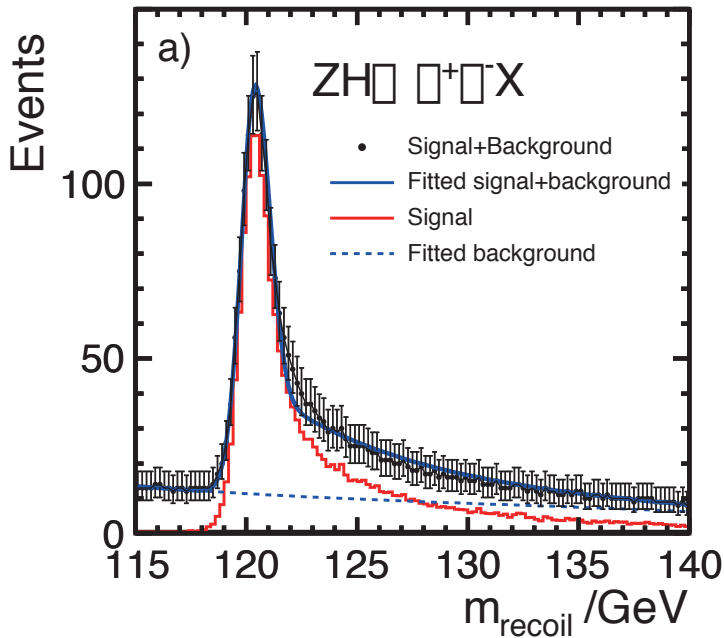


$$m_{\text{recoil}}^2 = (\sqrt{s} - E_{\ell\ell})^2 - |\vec{p}_{\ell\ell}|^2$$

- $\sigma(ZH)$ measurement independent of Higgs decay mode

$$\Delta m_H \simeq 32 \text{ MeV}$$

ILD@ILC, $E_{cm} = 250 \text{ GeV}$, 250 fb^{-1}



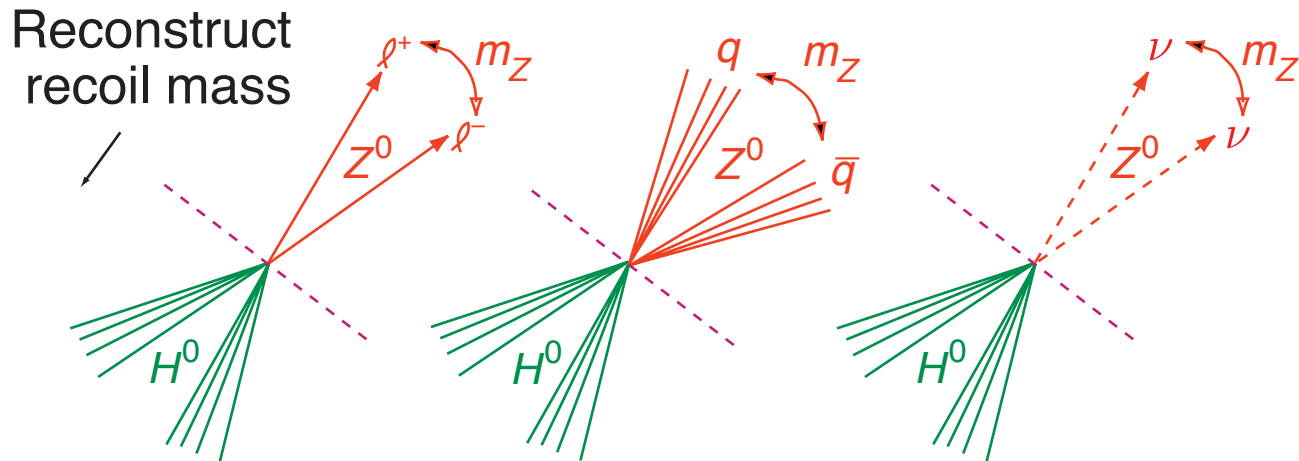
\sqrt{s}	250 GeV	350 GeV
Int. \mathcal{L}	250 fb^{-1}	350 fb^{-1}
$\Delta\sigma_{ZH}/\sigma_{ZH}$	2.5%	4%
$\Delta g_{HZZ}/g_{HZZ}$	1.3%	2%

So important

→ Can we do better than this?

(small systematics, e.g., lumi syst., understanding of isolated leptons)

$\sqrt{s} \simeq 250 \text{ GeV}$, ***Br's***



- Completely model independent measurements of *Br's*/couplings (instead of $\sigma \cdot Br$ as LHC)

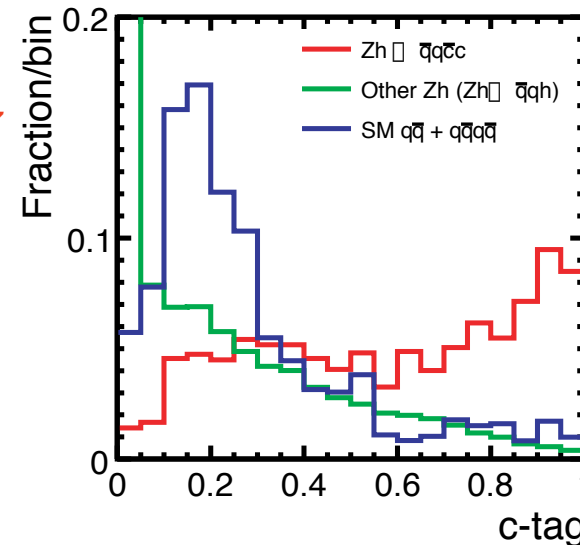
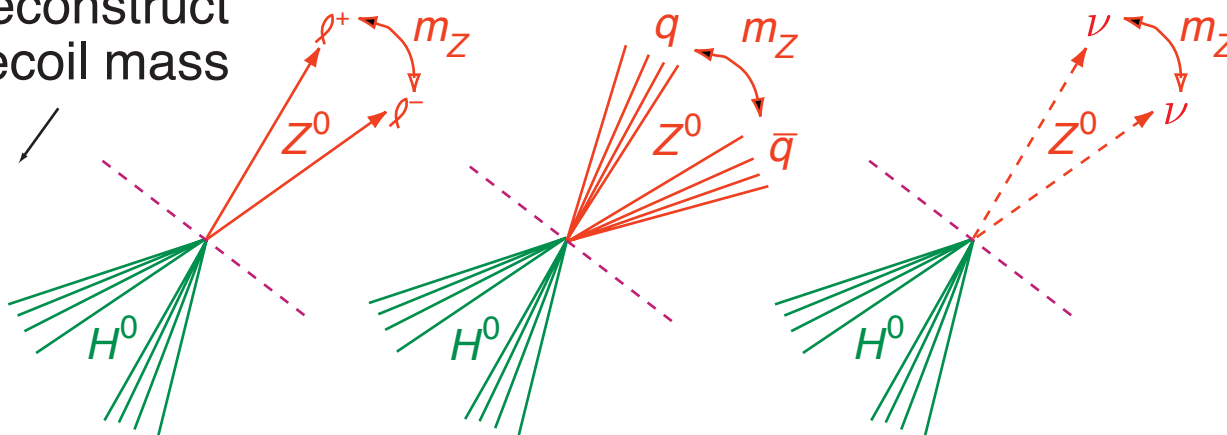
including to invisible/dark matter or *exotic* decays

$$\mathcal{B}(H \rightarrow \text{invis.}) < 0.8\% \text{ (95\% C.L.)}$$

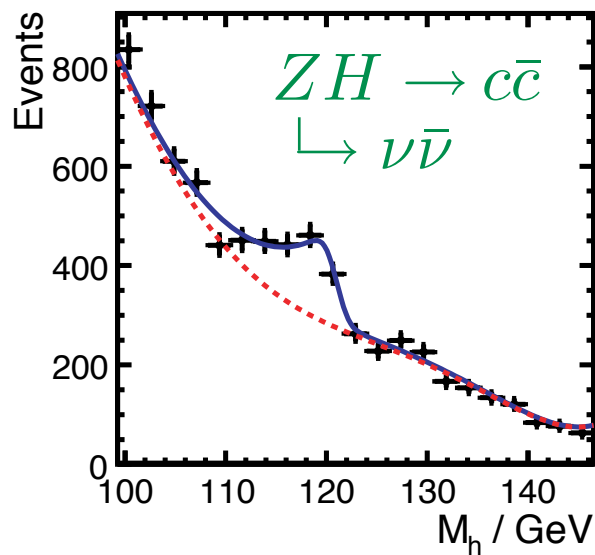
Essential! Could be happening at LHC and we would not know

$\sqrt{s} \simeq 250 \text{ GeV}, Br's$

Reconstruct
recoil mass



ILC, $E_{cm} = 250 \text{ GeV}, 250 \text{ fb}^{-1}$



- Completely model independent measurements of $Br's/couplings$ (instead of $\sigma \cdot Br$ as LHC) including to invisible/dark matter or *exotic* decays

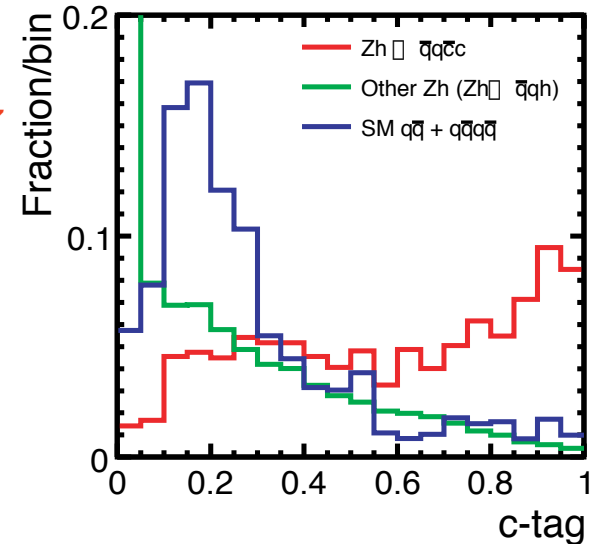
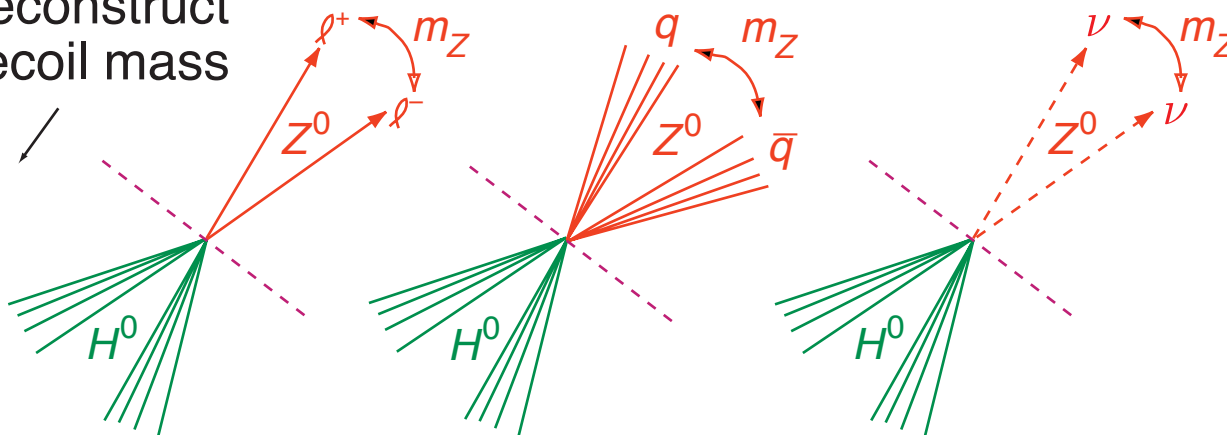
$$\Delta(\sigma \cdot \mathcal{B}(H \rightarrow c\bar{c})) / (\sigma \cdot \mathcal{B}) = 6.9\%$$

Similarly:

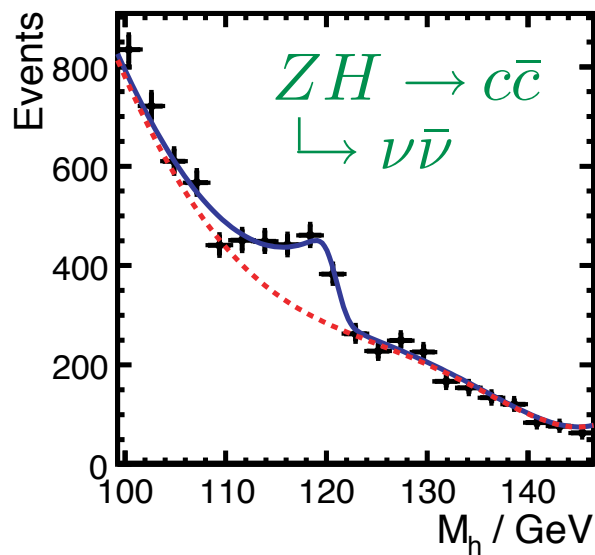
$$\Delta(\sigma \cdot \mathcal{B}(H \rightarrow b\bar{b})) / (\sigma \cdot \mathcal{B}) = 1.0\%$$

$\sqrt{s} \simeq 250 \text{ GeV}, Br's$

Reconstruct
recoil mass



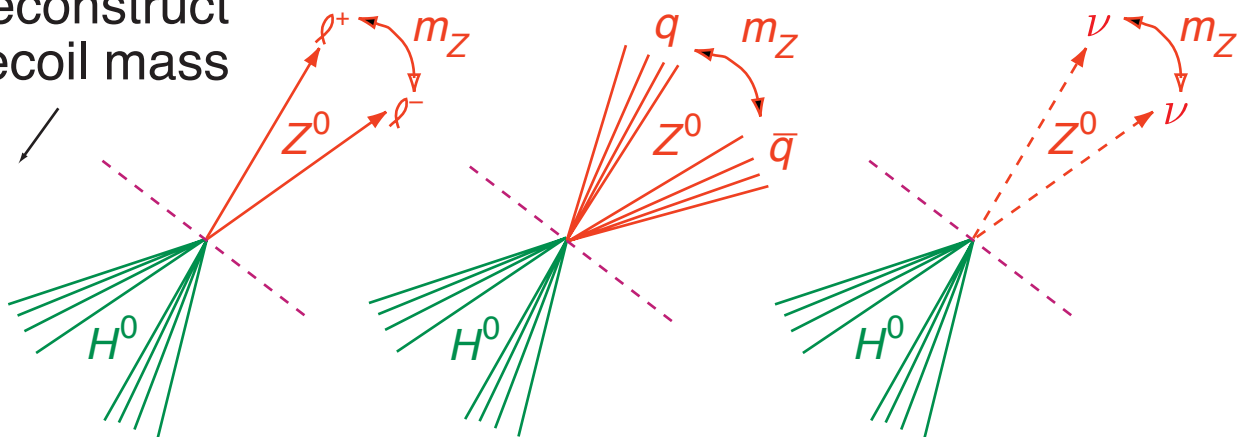
ILD@ILC, $E_{cm} = 250 \text{ GeV}, 250 \text{ fb}^{-1}$



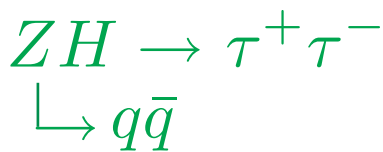
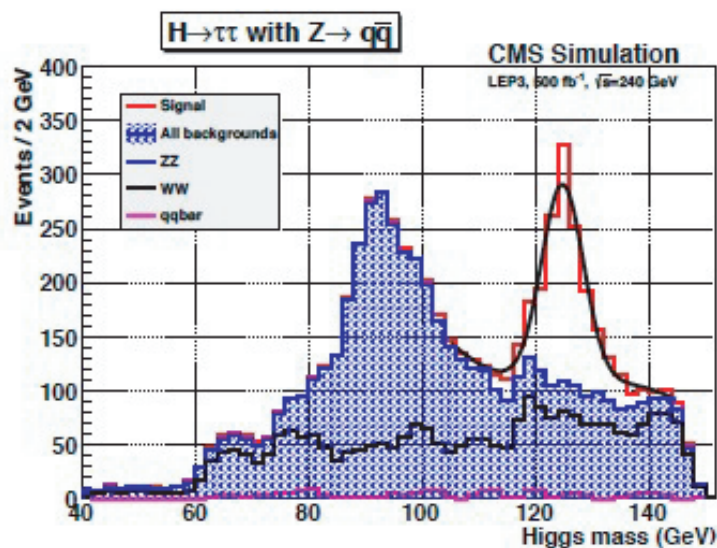
- Completely model independent measurements of $Br's/couplings$ (instead of $\sigma \cdot Br$ as LHC) including to invisible/dark matter or *exotic* decays
- extraction of $Br's$ will always include $\oplus \Delta(\sigma_{ZH})$ (e.g., $\pm 2.5\%$) (although correlated across all $Br's$)

$\sqrt{s} \simeq 250 \text{ GeV}, Br's$

Reconstruct
recoil mass



CMS@LEP3, $E_{cm} = 240 \text{ GeV}, 500 \text{ fb}^{-1}$



- Completely model independent measurements of $Br's/couplings$ (instead of $\sigma \cdot Br$ as LHC) including to invisible/dark matter or exotic decays

- Experimentally, not much difference between circular and linear machines

$\sqrt{s} \simeq 250 \text{ GeV}, Br's$

ILC, $E_{cm} = 250 \text{ GeV}, 250 \text{ fb}^{-1}$, polarization $(e^-, e^+) = (-0.8, +0.3)$

mode	BR	$\sigma \cdot BR$ (fb)	$N_{evt}/250 \text{ fb}^{-1}$	$\Delta(\sigma BR)/(\sigma BR)$	$\Delta BR/BR$
$h \rightarrow b\bar{b}$	65.7%	232.8	58199	1.0%	2.7%
$h \rightarrow c\bar{c}$	3.6%	12.7	3187	6.9%	7.3%
$h \rightarrow gg$	5.5%	19.5	4864	8.5%	8.9%
$h \rightarrow WW^*$	15.0%	53.1	13281	8.1%	8.5%
$h \rightarrow \tau^+\tau^-$	8.0%	28.2	7050	3.6%	4.4%
$h \rightarrow ZZ^*$	1.7%	6.1	1523	26%	26%
$h \rightarrow \gamma\gamma$	0.29%	1.02	255	23-30%	23-30%

Physics Volume, Technical Design Report (DBD), updated March 31



$\oplus 2.5\%$
fully correlated
across all $Br's$

$\sqrt{s} \simeq 250 \text{ GeV}$, Total Width

$$\Gamma_{\text{tot}} = \frac{\Gamma(H \rightarrow ZZ^*)}{\mathcal{B}(H \rightarrow ZZ^*)}$$

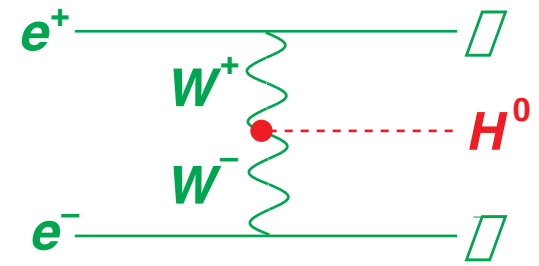
prop. to $\sigma(ZH), g_{HZZ}^2$
small, large error

Instead:

$$\Gamma_{\text{tot}} = \frac{\Gamma(H \rightarrow WW^*)}{\mathcal{B}(H \rightarrow WW^*)}$$

prop. to $\sigma(\nu\bar{\nu}H), g_{HWW}^2$
↑
smallish

$\Delta\Gamma_{\text{tot}}/\Gamma_{\text{tot}} \simeq 11\%$



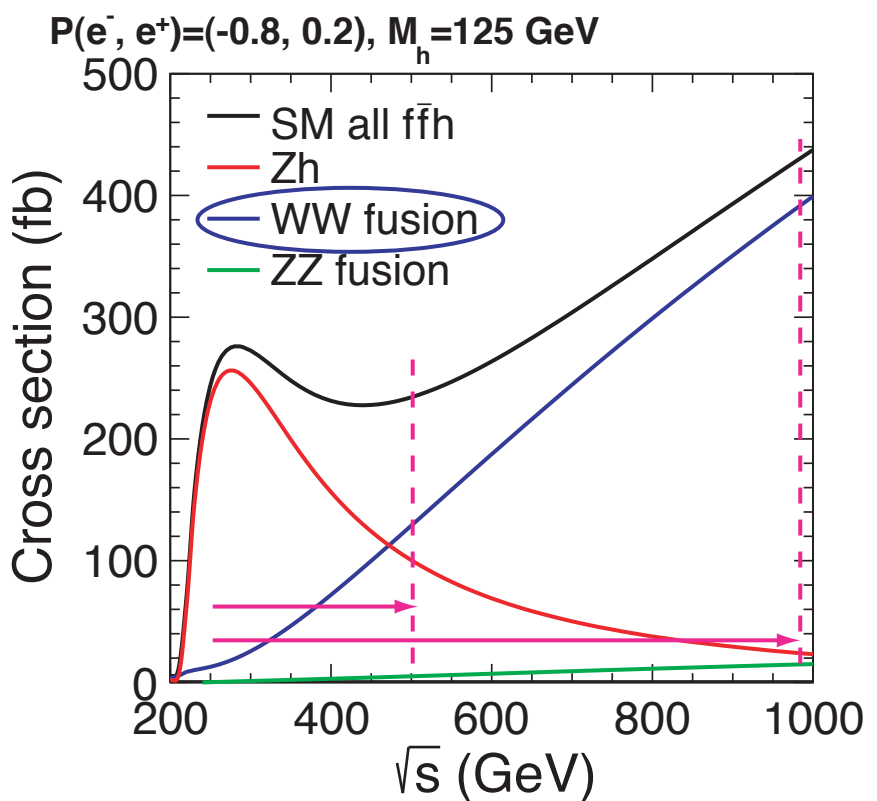
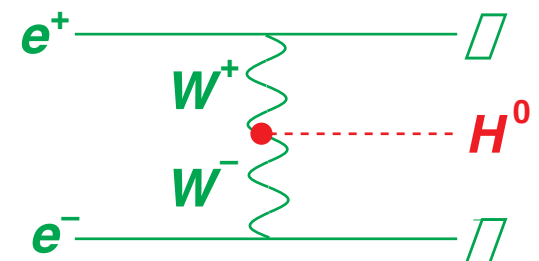
How to do better??

$\sqrt{s} \simeq 500 \text{ GeV}$, Total Width

Instead:

$$\Gamma_{\text{tot}} = \frac{\Gamma(H \rightarrow WW^*)}{\mathcal{B}(H \rightarrow WW^*)}$$

prop. to $\sigma(\nu\bar{\nu}H), g_{HWW}^2$



Move to higher energies,
e.g., $\sqrt{s} = 500 \text{ GeV}$

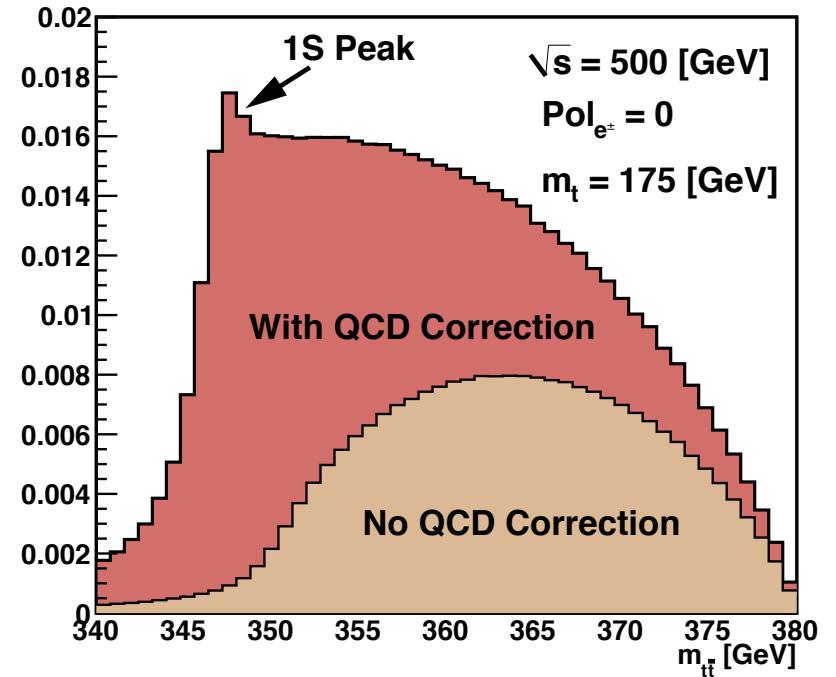
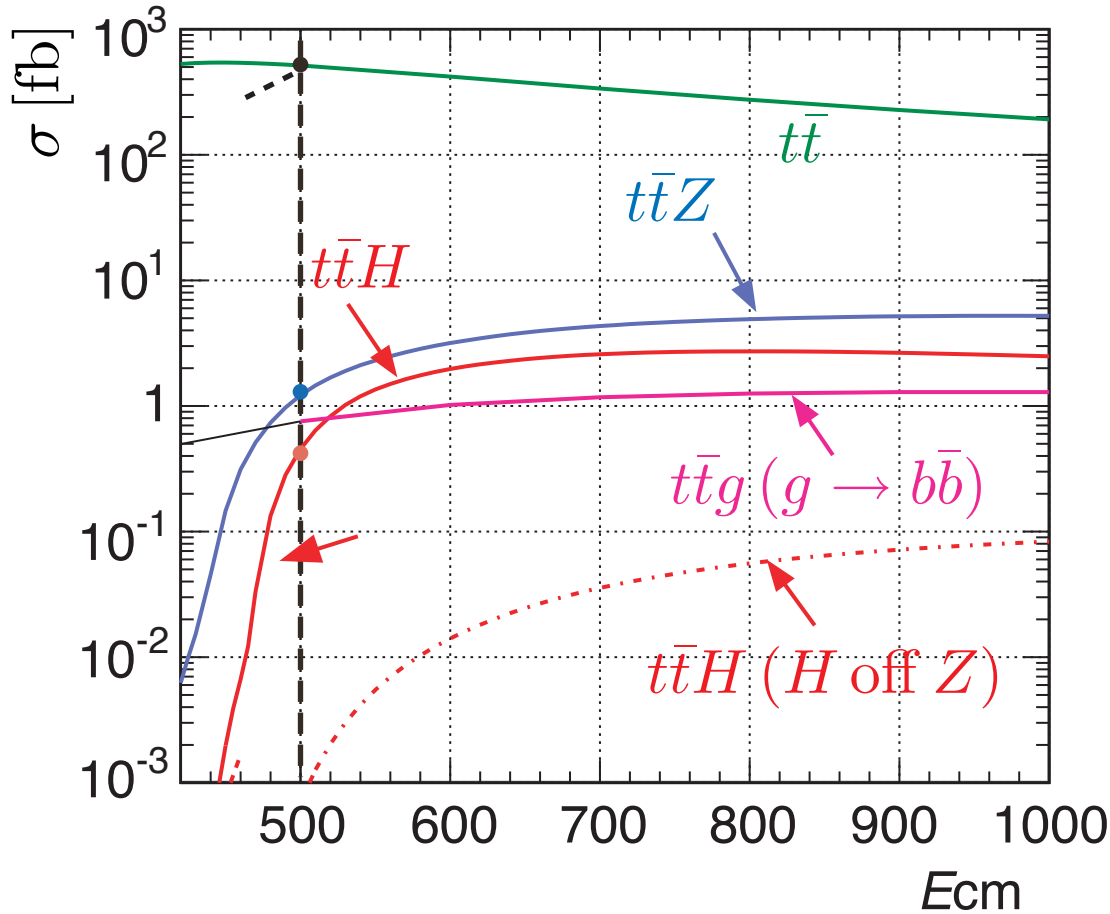
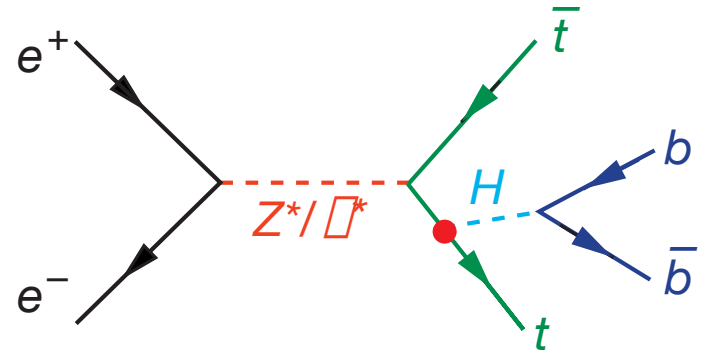
$$\Delta\Gamma_{\text{tot}}/\Gamma_{\text{tot}} \simeq 6\%$$

Keep measuring *Br*'s!

...and now the stuff that is tough for most machines...

$t\bar{t}H$

- 6-jet and 8-jet modes:

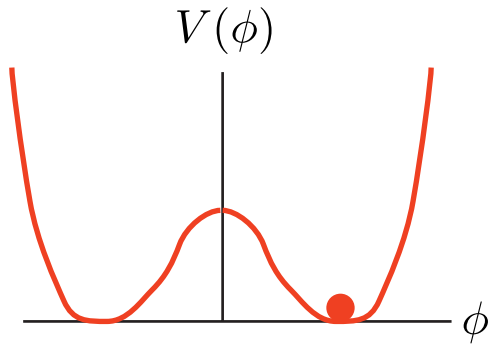
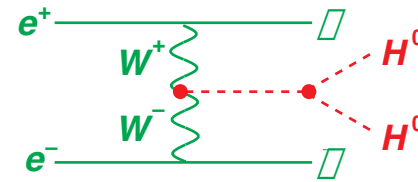
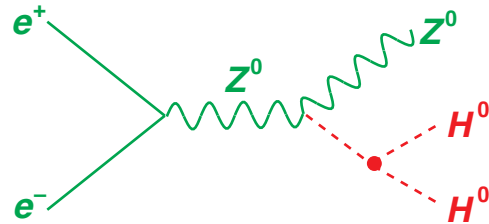


- Now feasible at 500 GeV! Complicated, multi-jet system, four b jets

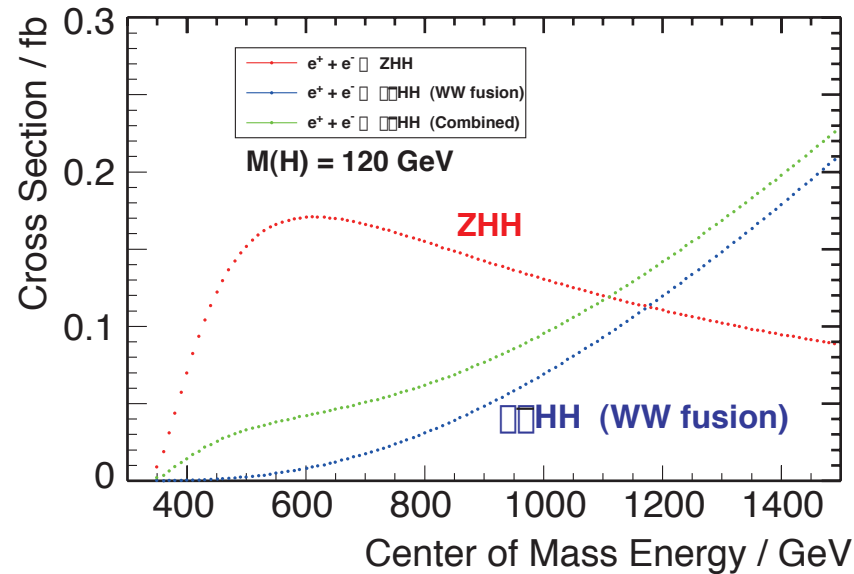
$$\Delta g_{ttH} / g_{ttH} = 10\% \quad (1 \text{ ab}^{-1})$$

- Better at higher energies (aside from larger fraction of non- $t\bar{t}H$ components)

Self-Coupling



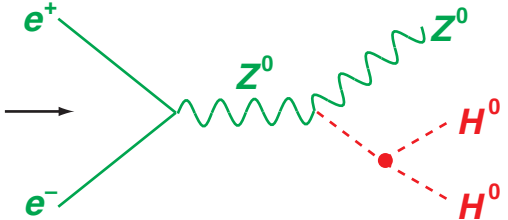
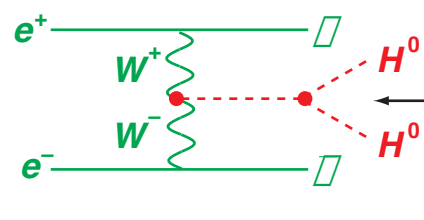
$$V(\phi) = \mu^2 \phi^\dagger \phi + \lambda (\phi^\dagger \phi)^2$$



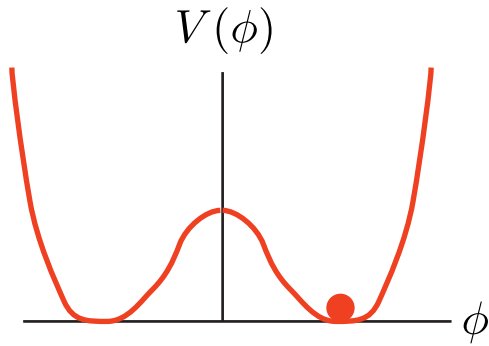
- Tough analysis, low rate
- Separate non-self-coupling contributions by HH invariant mass

- Uses $H \rightarrow b\bar{b}$; b-jet "color singlet" assignment is tough

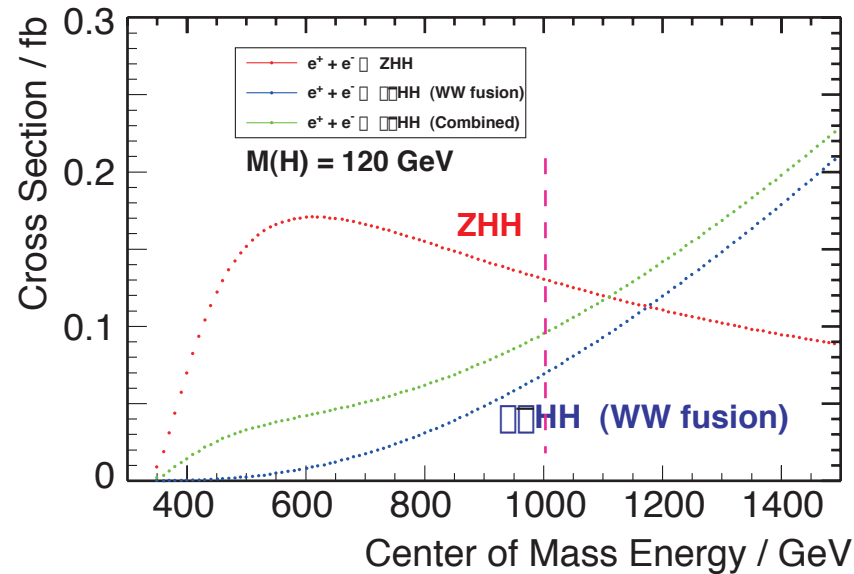
Self-Coupling

$$\frac{\Delta\lambda}{\lambda} = 1.66 \frac{\Delta\sigma}{\sigma} \rightarrow$$



$$\frac{\Delta\lambda}{\lambda} = 0.76 \frac{\Delta\sigma}{\sigma}$$



$$V(\phi) = \mu^2 \phi^\dagger \phi + \lambda (\phi^\dagger \phi)^2$$



- Tough analysis, low rate
- Separate non-self-coupling contributions by HH invariant mass

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Tough Stuff

process	\sqrt{s} [GeV]	\mathcal{L} [ab^{-1}]	(P_{e^-}, P_{e^+})	$(\Delta\sigma \cdot BR)/(\sigma \cdot BR)$	$\Delta g/g$
$t\bar{t}h$	500	1	$(-0.8, +0.3)$	25%	13%
Zhh	500	2	$(-0.8, +0.3)$	32% →	53%
$t\bar{t}h$	1000	1	$(-0.8, +0.2)$	8.7%	4.5%
$\nu\bar{\nu}hh$	1000	2	$(-0.8, +0.2)$	26% →	21%

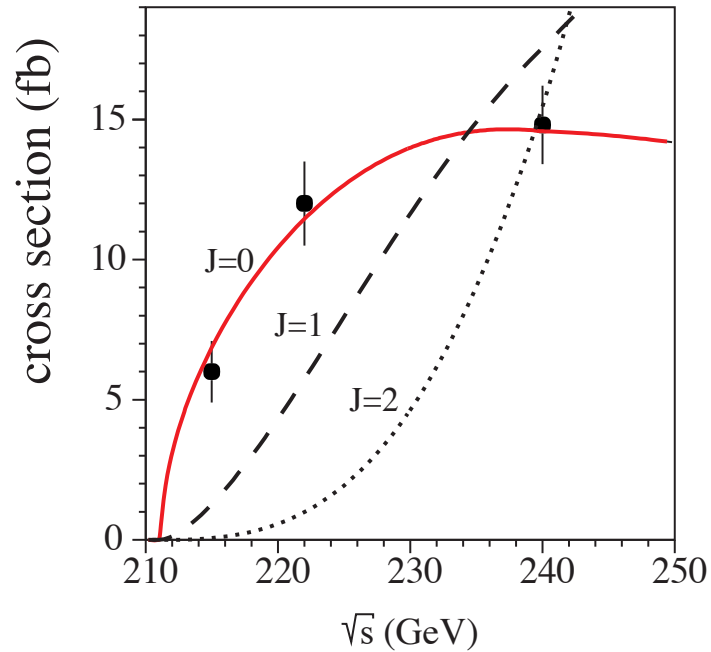
Collecting...

\sqrt{s} and \mathcal{L} (P_{e^-}, P_{e^+})	$\Delta(\sigma \cdot BR)/(\sigma \cdot BR)$				
	250 fb ⁻¹ at 250 GeV (-0.8,+0.3)		500 fb ⁻¹ at 500 GeV (-0.8,+0.3)		1 ab ⁻¹ at 1 TeV (-0.8,+0.2)
mode	Zh	$\nu\bar{\nu}h$	Zh	$\nu\bar{\nu}h$	$\nu\bar{\nu}h$
$h \rightarrow b\bar{b}$	1.1%	10.5%	1.8%	0.66%	0.47%
$h \rightarrow c\bar{c}$	7.4%	-	12%	6.2%	7.6%
$h \rightarrow gg$	9.1%	-	14%	4.1%	3.1%
$h \rightarrow WW^*$	6.4%	-	9.2%	2.6%	3.3%
$h \rightarrow \tau^+\tau^-$	4.2%	-	5.4%	14%	3.5%
$h \rightarrow ZZ^*$	19%	-	25%	8.2%	4.4%
$h \rightarrow \gamma\gamma$	29-38%	-	29-38%	20-26%	7-10%
$h \rightarrow \mu^+\mu^-$	100%	-	-	-	32%

...input to global analysis

Spin & CP

- scan $e^+e^- \rightarrow ZH$:

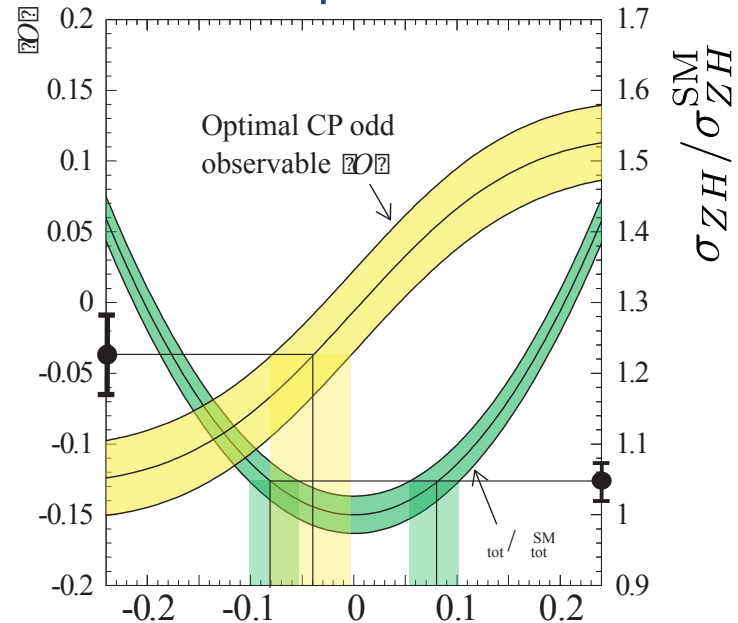


Spin (will be) moot aside from "conspiracy theories"?

Fermions:

- Angular analysis of decay products of polarized taus in $H \rightarrow \tau^+\tau^-$, CP-odd admixture to $\sim 6^\circ$

- total rate + optimal observable



η : *Bosons:*
CP-odd admixture to $\sim 4\%$

Combination Assumptions

- $\sum_i \mathcal{B}_i = 1$
- $|g_{HWW}| < g_{HWW}|_{\text{SM}}$
 $|g_{HZZ}| < g_{HZZ}|_{\text{SM}}$
- $g_{HWW}/g_{HZZ} = \cos^2 \theta_w$
- No invisible or undetectable Higgs decays

More constrained



Combination Assumptions



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Global Analysis

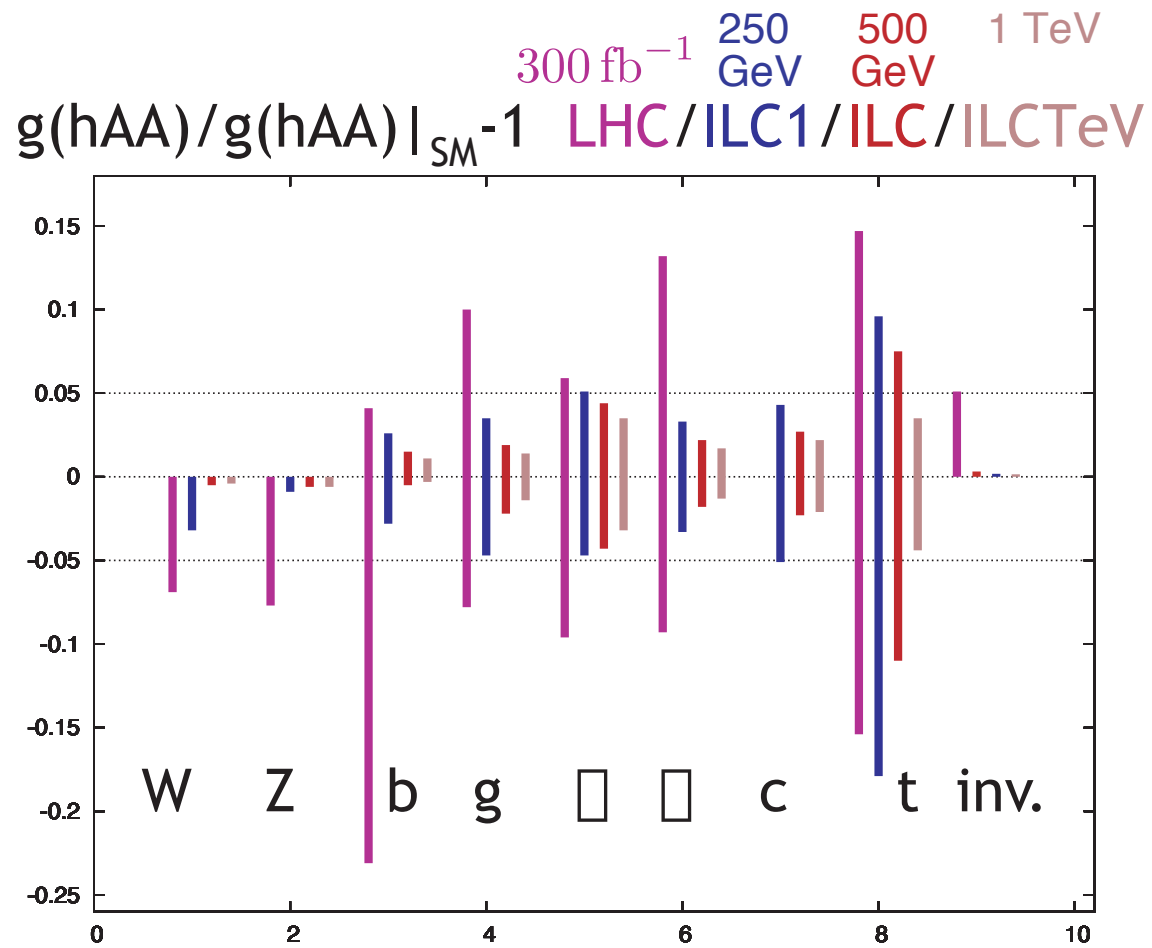
Expected Higgs boson coupling precisions in %:

Mode	300 fb ⁻¹	250 fb ⁻¹	500 fb ⁻¹	1000 fb ⁻¹
	LHC	ILC(250)	ILC(500)	ILC(1000)
WW	4.1	1.9	0.24	0.17
ZZ	4.5	0.44	0.30	0.27
$b\bar{b}$	13.6	2.7	0.94	0.69
gg	8.9	4.0	2.0	1.4
$\gamma\gamma$	7.8	4.9	4.3	3.3
$\tau^+\tau^-$	11.4	3.3	1.9	1.4
$c\bar{c}$	–	4.7	2.5	2.1
$t\bar{t}$	15.6	14.2	9.3	3.9
$\mu^+\mu^-$	–	–	–	16.
self	–	–	–	20.
BR(invis.)	< 9	< 0.44	< 0.30	< 0.26
Γ_{tot}	20.3	4.8	1.6	1.2

Physics Volume, ILC Technical Design Report (DBD), updated March 31

arXiv:1207.2516 [hep-ph]

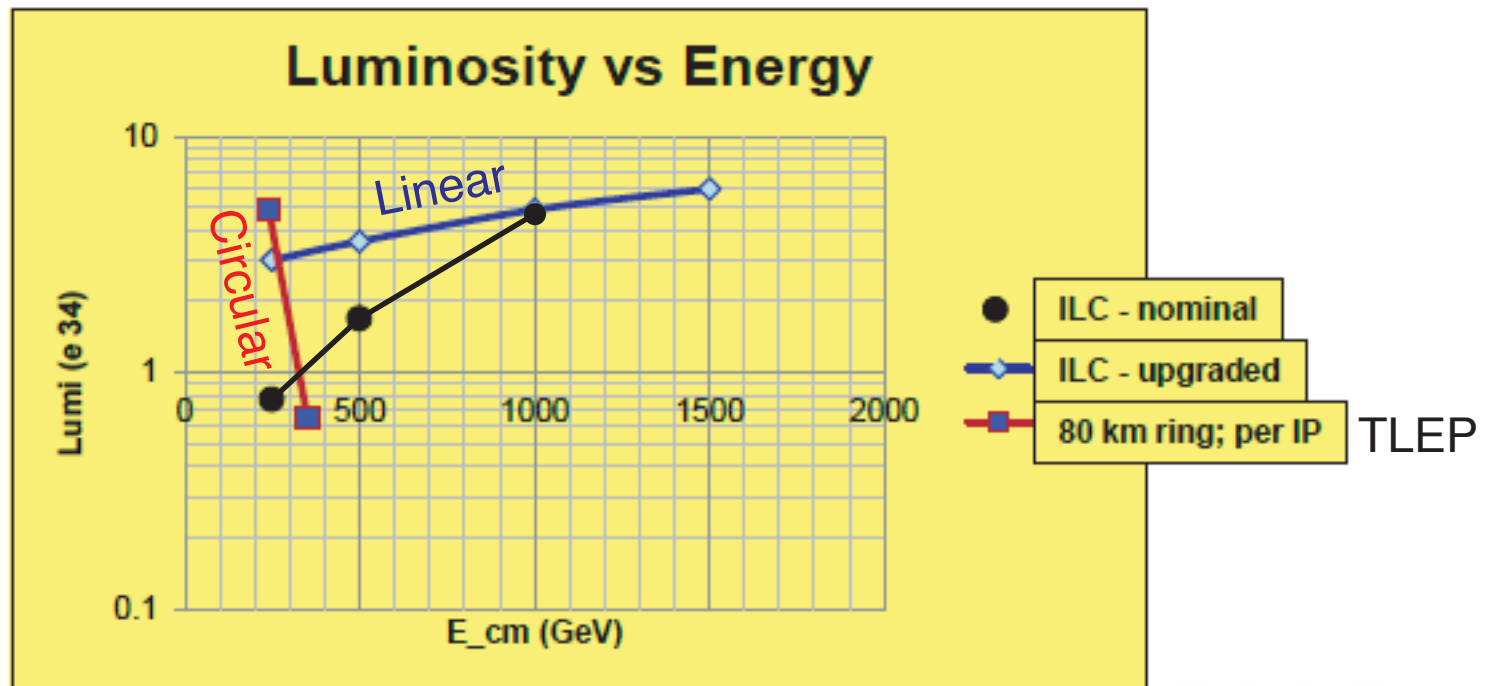
Global Analysis



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[arXiv:1207.2516 \[hep-ph\]](https://arxiv.org/abs/1207.2516)

e^+e^- Linear and Circular Comparisons

$$\int \mathcal{L} dt \begin{array}{l} + \text{ optimistic} \\ - \text{ pessimistic} \end{array}$$



- In consultation with accelerator physicists, proponents investigating luminosity upgrades and their impact

$$\mathcal{L} = 0.75 \rightarrow 3.0 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$$

e^+e^- Linear and Circular Comparisons

Example Apples and Oranges:

- Assumptions going into global analyses of Higgs couplings
- Ignoring multiple IP's/detectors of circular machines
- Beam-beam effects of multiple IP's tend to reduce luminosity
- Not including correlated uncertainties into table entries (e.g., σ_{ZH})
- What's a year?

Snowmass year = 1×10^7 sec (usually to take into account uptime)

ILC	LEP3
$\mathcal{L} = 0.75$	$1.0 \times 10^{34} \text{cm}^{-2} \text{s}^{-1}$

"The integrated luminosities for the ILC and CLIC were based on a model with slow initial build-up for machine operation."

Physics case as a Higgs Factory (1)

- Number of Higgs bosons produced at $\sqrt{s} = 240\text{-}250$ GeV

	ILC-250	LEP ₃ -240	TLEP-240
Lumi / IP / 5 years	250 fb ⁻¹	500 fb ⁻¹	2.5 ab ⁻¹
# IP	1	2 - 4	2 - 4
Lumi / 5 years	250 fb ⁻¹	1 - 2 ab ⁻¹	5 - 10 ab ⁻¹
Beam Polarization	80%, 30%	–	–
L _{0.01} (beamstrahlung)	86%	100%	100%
Number of Higgs	70,000	400,000	2,000,000
Upgradeable to	ILC 1TeV CLIC 3TeV ?	HE-LHC 33 TeV	VHE-LHC 100 TeV

- In a given amount of time, Higgs coupling precisions scale like
 - e.g., for g_{HZZ} : 1.5% for ILC : 0.65% for LEP₃ : 0.2% for TLEP

e^+e^- Linear and Circular Comparisons

My personal take:

- LHC is where Higgs properties are being measured, so fully exploit!
- Taking uncertainties into account, for direct Higgs properties:

ILC (at only 250) ~ 240 GeV Circular (e.g., LEP)

(but lose top threshold scan!!)

- ILC at higher energies is essential; momentum in Japan

Circular machine luminosity roughly prop. to circumference

- For sheer luminosity and follow-up physics reach, hard to beat TLEP + pp collider, *but what about time scales and total cost?*

(both sizes deserve CDR...)

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- ILC at higher energies is essential; momentum in Japan
- For sheer luminosity and follow-up physics reach, hard to beat TLEP + HE pp collider, *but what about time scales and total cost?*
(deserves CDR...)

Discussion welcome!