

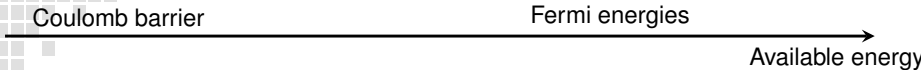
# Probing the decay mechanism of hot nuclei by Coulomb chronometry

Diego Gruyer for the INDRA Collaboration

Grand Accélérateur National d'Ions Lourds, and  
Université de Caen Basse-Normandie



# Collisions between Coulomb and Fermi energies

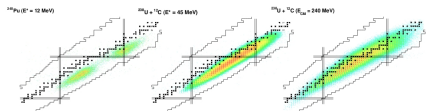
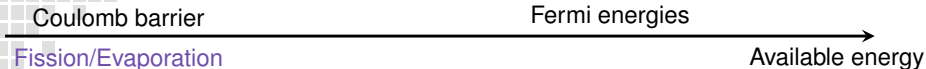


Coulomb barrier

Fermi energies

Available energy

# Collisions between Coulomb and Fermi energies



O.Delaune, PhD Thesis (2012)

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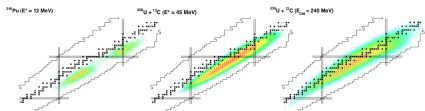
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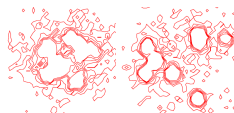
Fission/Evaporation

Multifragmentation

Available energy

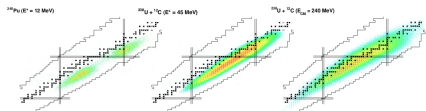
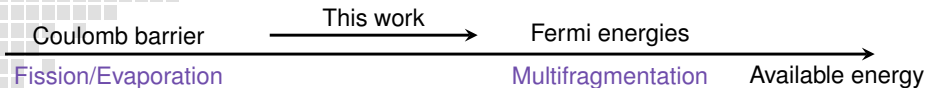


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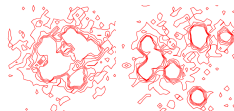


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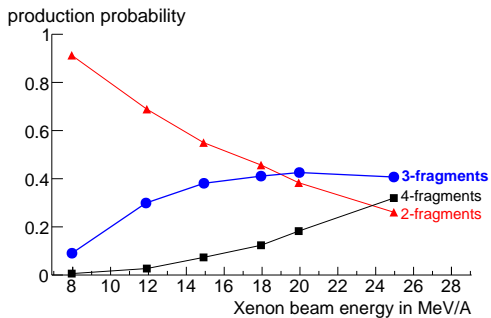


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## Multifragment production in Xe+Sn central collisions

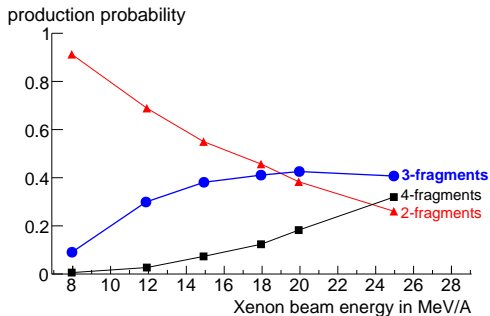


A.Chbihi et al. J.Phys. : Conf.Ser. **420**, 012099 (2012)

# Multifragment production in Xe+Sn central collisions

## Exit channel probabilities

- 8 MeV/A : two fragments

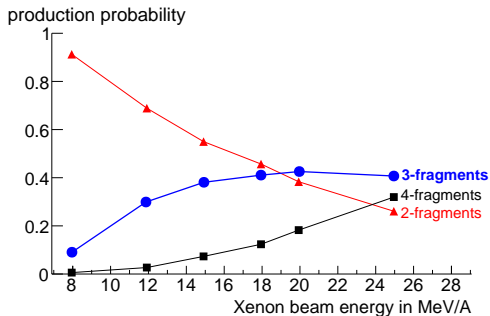


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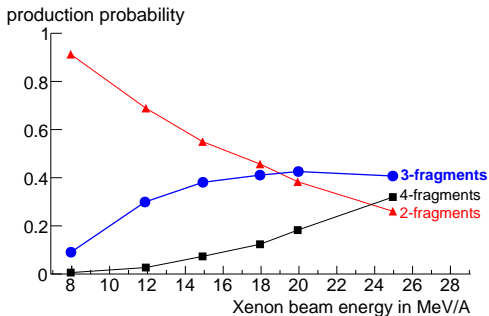
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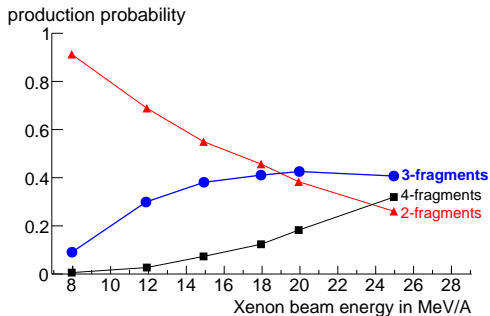
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## Mechanism of three-fragment production

# Multifragment production in Xe+Sn central collisions

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A.Chbihi et al. J.Phys. : Conf.Ser. **420**, 012099 (2012)

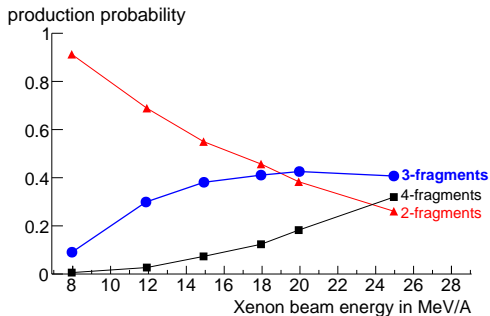
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- Is it the continuation of low energy fission or the precursor of high energy simultaneous fragmentation ?

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## Mechanism of three-fragment production

- Is it the continuation of low energy fission or the precursor of high energy simultaneous fragmentation ?
- Estimation of the time scale can distinguish different mechanisms.

- 1 Introduction
- 2 Experimental details
- 3 Qualitative evolution of the reaction mechanism
- 4 Time scale estimation by Coulomb chronometry
- 5 Summary and prospects

## Experimental details

### Experimental data

- Xe+Sn at 12, 15, 18, 20, 25 MeV/A

# Experimental details

## INDRA $4\pi$ multidetector

- High granularity with 336 cells
- Charge identification from proton to Uranium up to 250 MeV/A
- Low identification thresholds

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- Three heavy fragments with  $Z > 10$  in the exit channel ( $Z_1 > Z_2 > Z_3$ )



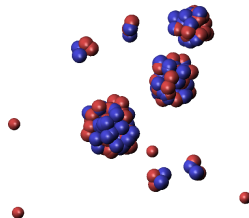
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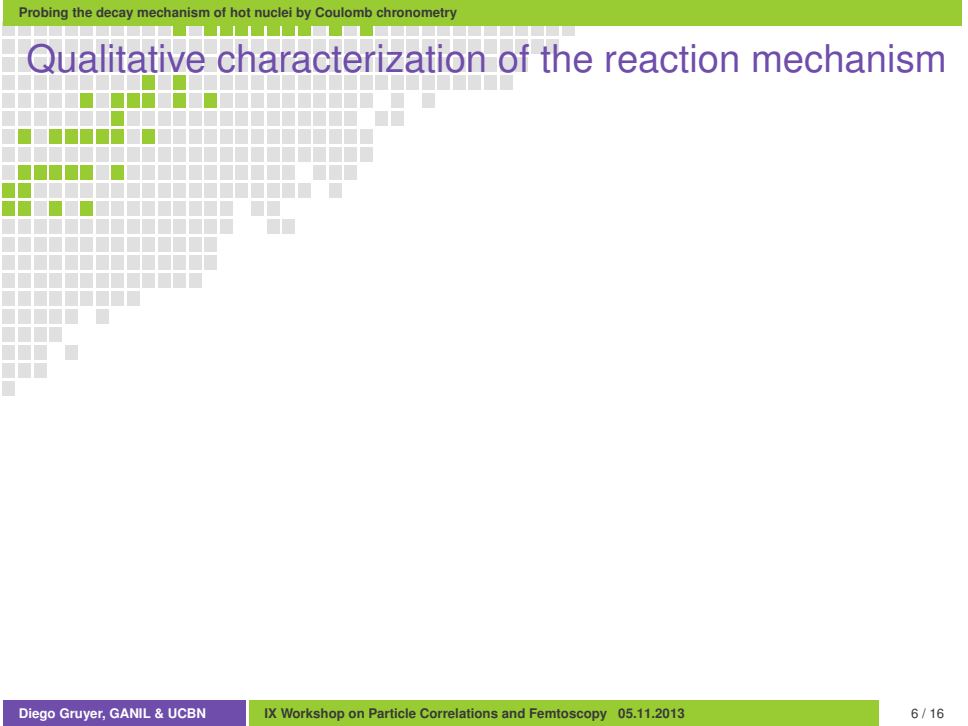
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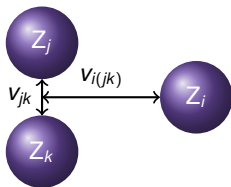
# Qualitative characterization of the reaction mechanism



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## Relative velocity versus fission

$$\bullet P_i = \underbrace{(v_{i(jk)}^{exp} - v_{i(jk)}^{fission})^2}_{1^{st} \text{ step}} + \underbrace{(v_{jk}^{exp} - v_{jk}^{fission})^2}_{2^{nd} \text{ step}}$$



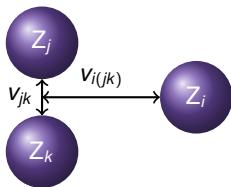
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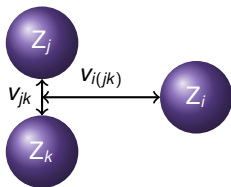
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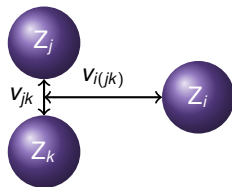
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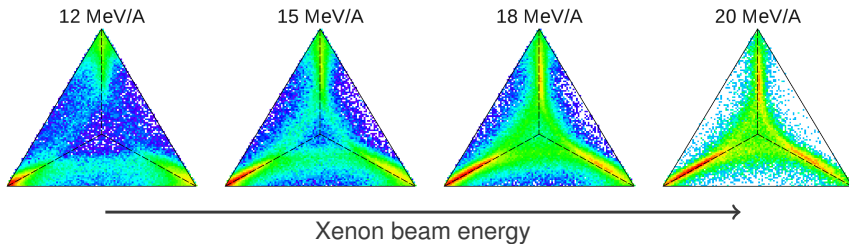
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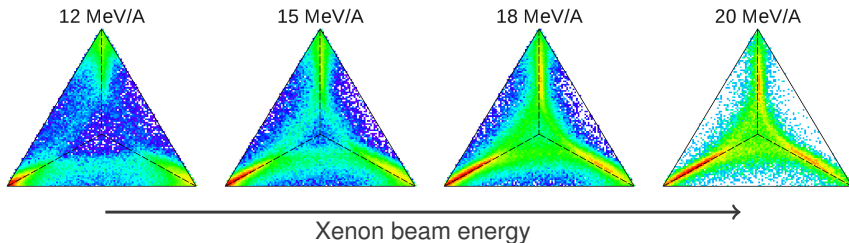
## From sequential to simultaneous break-up



## From sequential to simultaneous break-up

## Lowest beam energy

- Three branches parallel to the edges of the Dalitz plot
- Few events close to the center
- Sequential break-up dominates





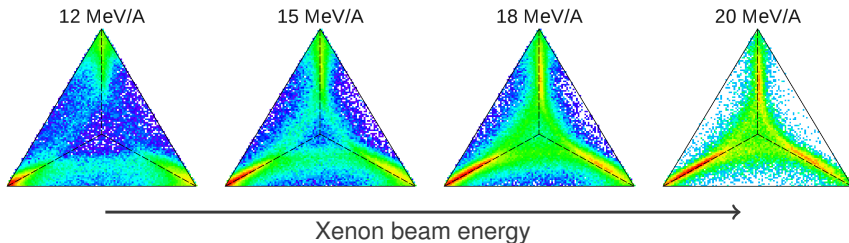
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- Three branches still present
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- Evolution from successive splittings to simultaneous fragmentation



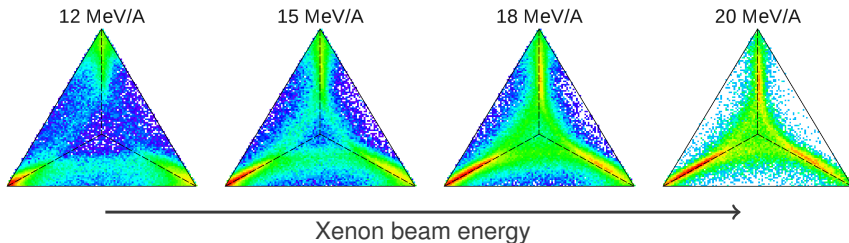
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## Evolution of the involved time scale

- To estimate the time scale we must establish the sequence of splittings

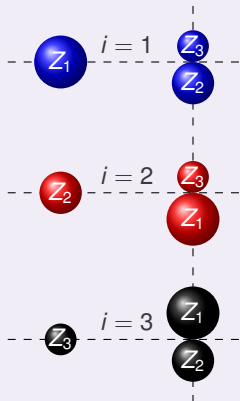
# Identification of the sequence of splittings

## Hypothesis

- Fragments production : 2 successive splittings

# Identification of the sequence of splittings

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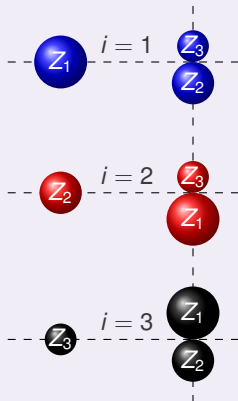


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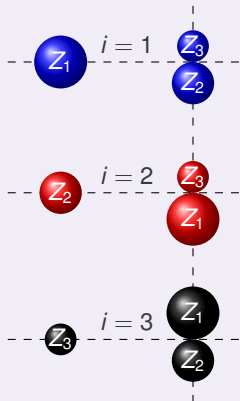
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- Relative velocity of each pair of fragments compared to fission from Viola systematics

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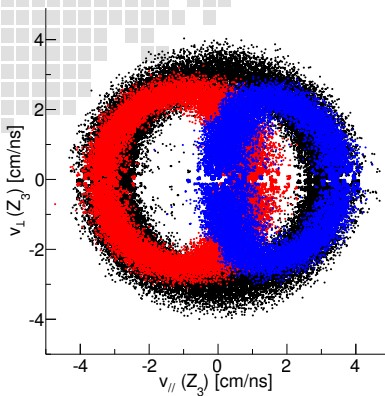
## Minimization procedure

- $\chi_i = (v_{jk}^{exp} - v_{jk}^{viola})^2$  : measure the compatibility of an event with the sequence  $i$  ( $\chi_1, \chi_2, \chi_3$ )
- The smallest  $\chi_i$  determines the sequence  $i$

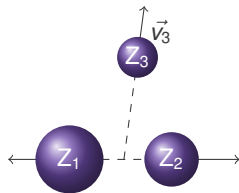
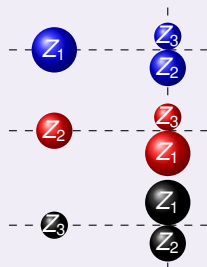
Now we know what happened event by event !



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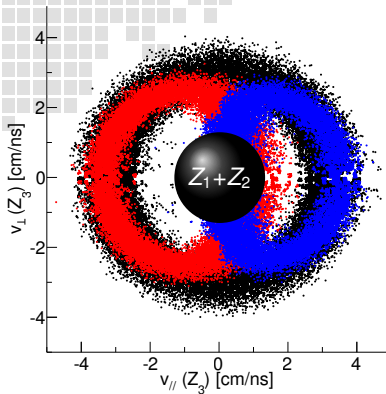


## Sequences

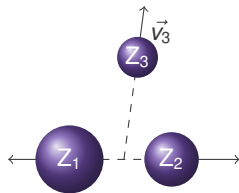
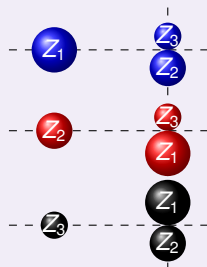




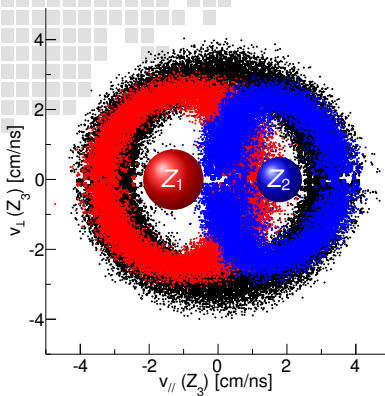
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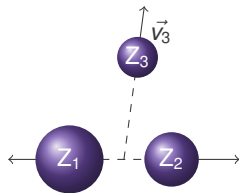
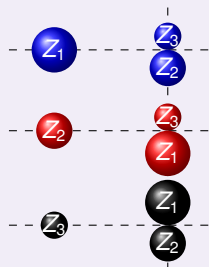
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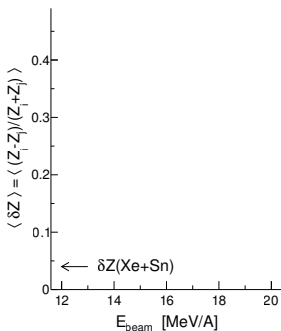
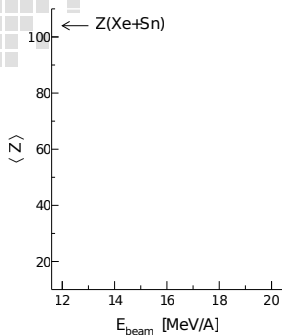
## Sequences



## Reconstruction of the two steps

## Fragment sorting and incomplete fusion

- Fragments sorted according to the sequence and the two steps are reconstructed

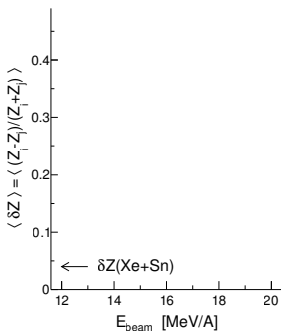
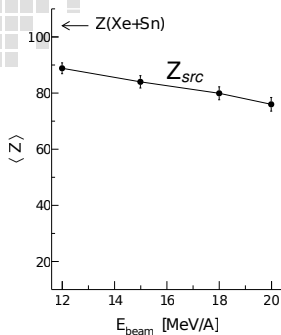


## Scenario

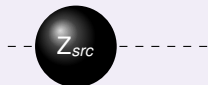
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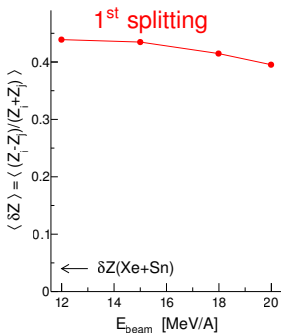
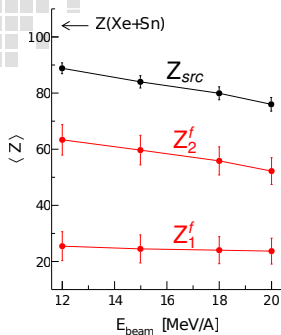
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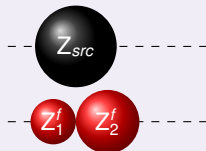
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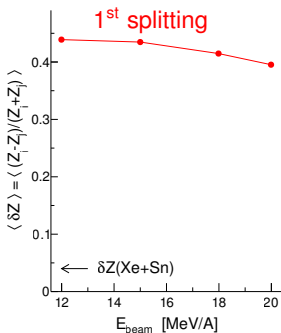
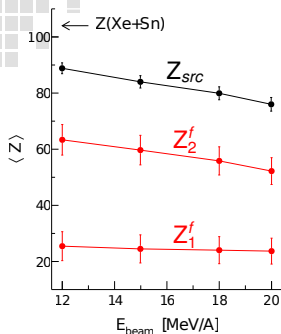
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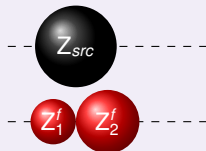
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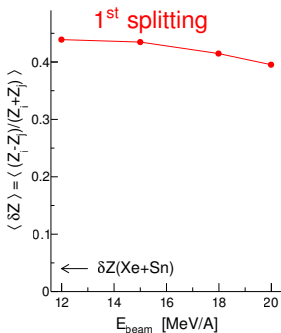
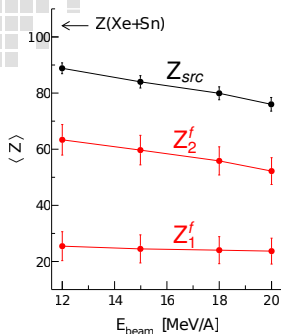
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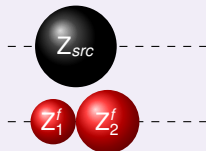
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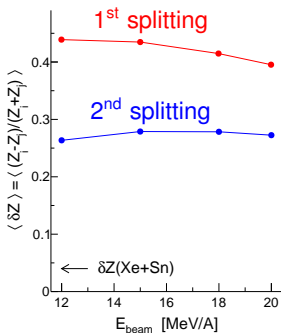
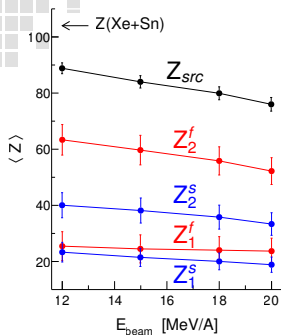
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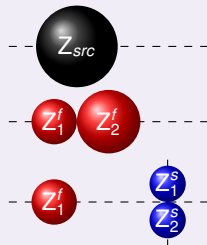
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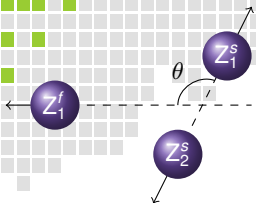


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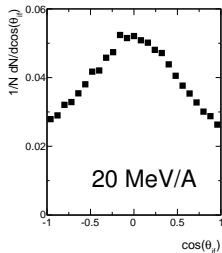
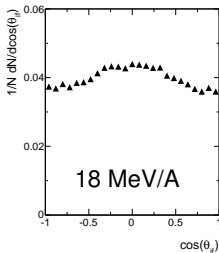
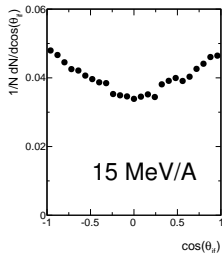
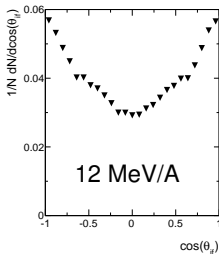




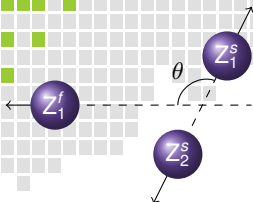
# Coulomb proximity effects : angular distribution



Inter-splitting angle

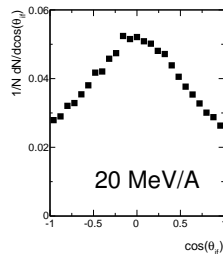
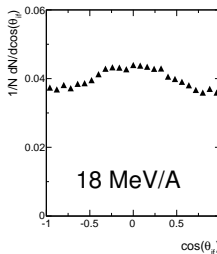
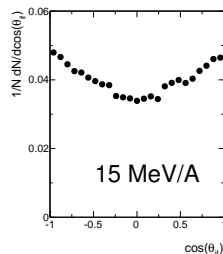
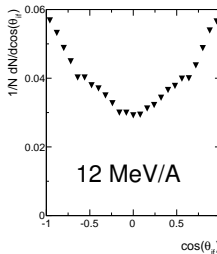


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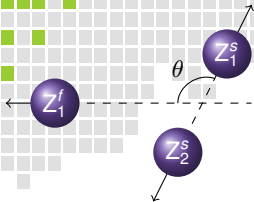


## Inter-splitting angle

- 12-15 MeV/A : “U” shape characteristic of fission with angular momentum,

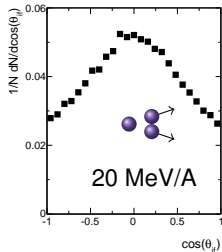
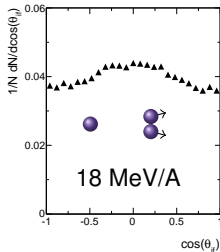
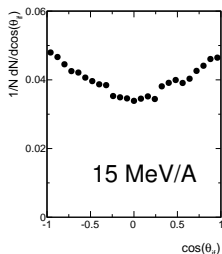
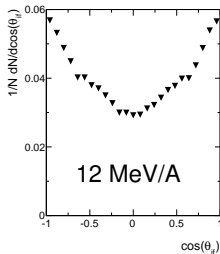


## Coulomb proximity effects : angular distribution

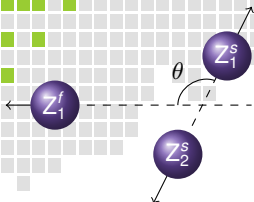


## Inter-splitting angle

- 12-15 MeV/A : “U” shape characteristic of fission with angular momentum,
- 18-20 MeV/A :  $\theta \sim 90^\circ$  due to the coulomb field of  $Z_1^f$

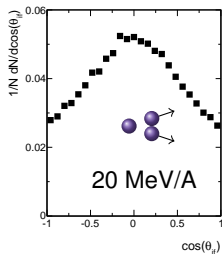
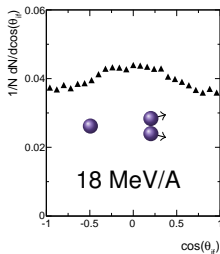
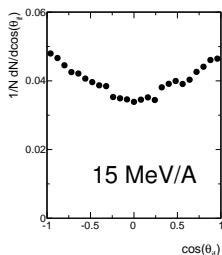
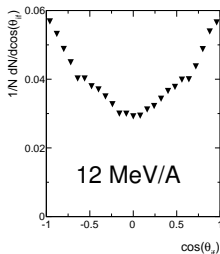


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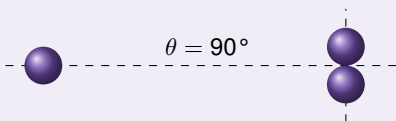


## Inter-splitting angle

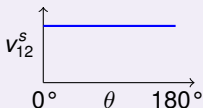
- 12-15 MeV/A : “U” shape characteristic of fission with angular momentum,
- 18-20 MeV/A :  $\theta \sim 90^\circ$  due to the coulomb field of  $Z_1^f$
- It indicates a shortening of the inter-splitting time



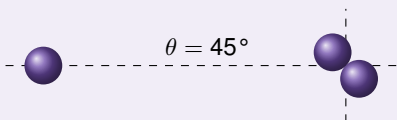
## Inter-splitting time by Coulomb chronometry

Long  $\delta t$ 

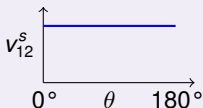
- Second splitting far away from the first emitted fragment
- Relative velocity independent of the inter-splitting angle  $\theta$



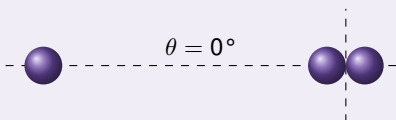
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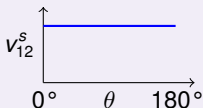
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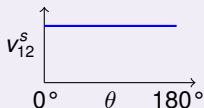
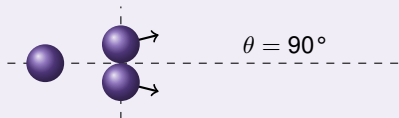
- Second splitting far away from the first emitted fragment
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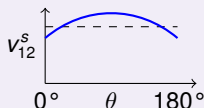
## Inter-splitting time by Coulomb chronometry

Long  $\delta t$ 

- Second splitting far away from the first emitted fragment
- Relative velocity independent of the inter-splitting angle  $\theta$

Short  $\delta t$ 

- Trajectories are modified by the Coulomb field of the first emitted fragment
- Relative velocity depend on  $\theta$

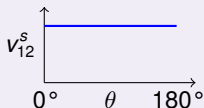
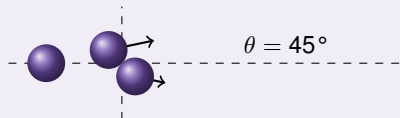




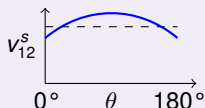
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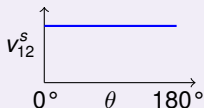
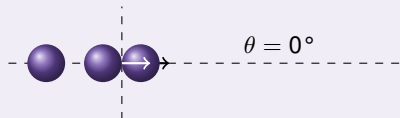
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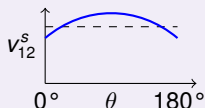
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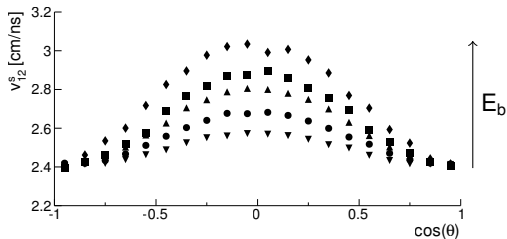
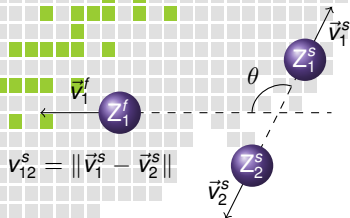
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Short  $\delta t$ 

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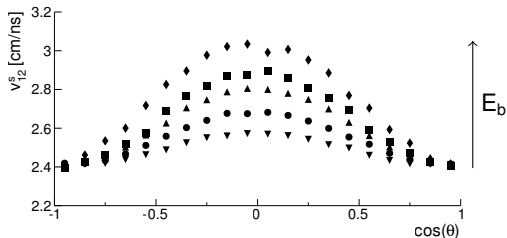
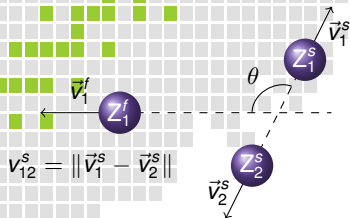


## Use of the Coulomb chronometer



## Experimental correlations

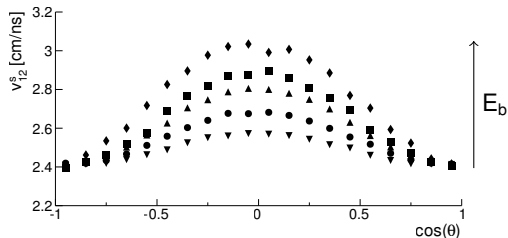
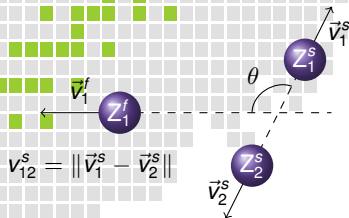
## Use of the Coulomb chronometer



## Experimental correlations

- $\langle v_{12}^s \rangle$  maximum for  $\theta \sim 90^\circ$

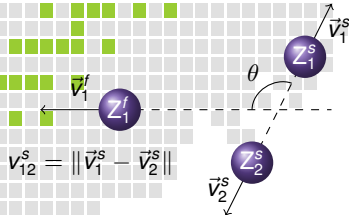
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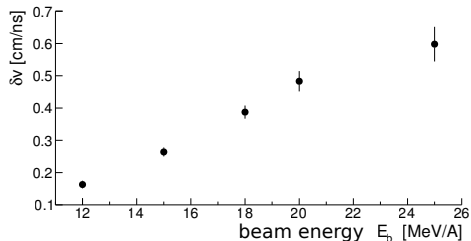
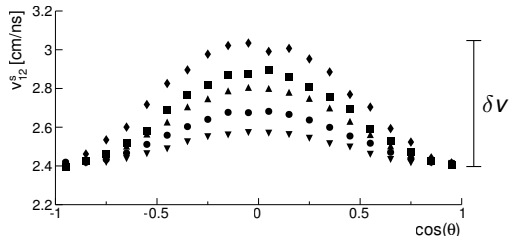
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- This maximum increases when increasing beam energy

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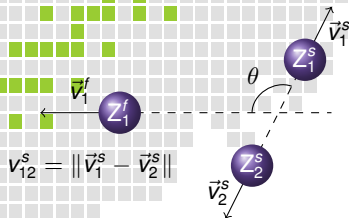


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 $\delta v = v_{12}^s(90^\circ) - v_{12}^s(0^\circ)$

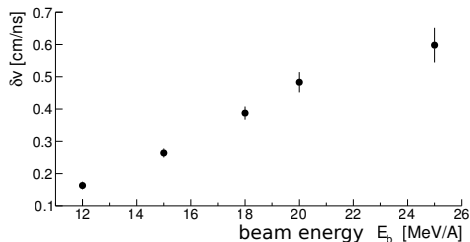
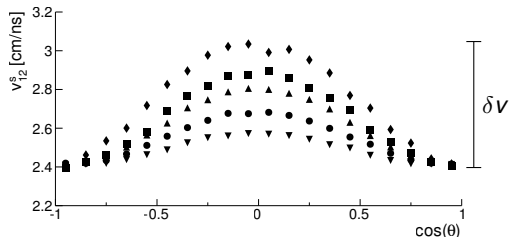


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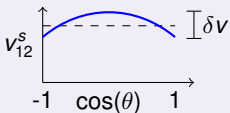
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- Coulomb distortion parameter :  $\delta v = v_{12}^s(90^\circ) - v_{12}^s(0^\circ)$
- $\delta v$  and  $\delta t$  can be related with Coulomb trajectory calculation



# Calibration of the inter-splitting time

## Coulomb trajectory calculations

- We calculate  $\delta v$  for different values of the inter-splitting time  $\delta t$ .

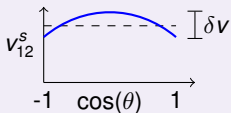




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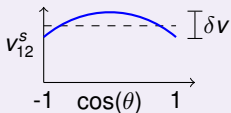
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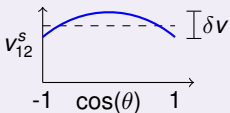
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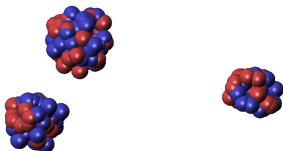
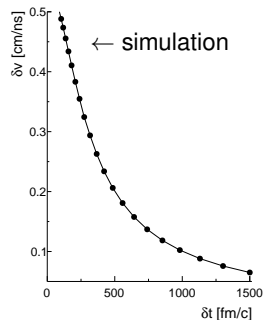
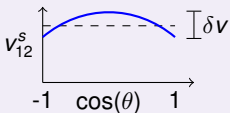
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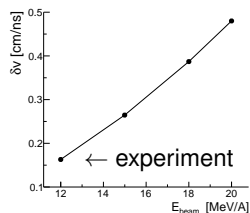
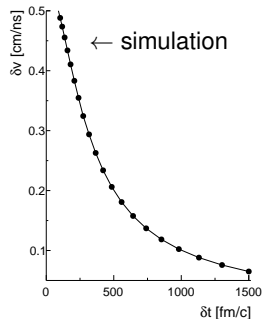
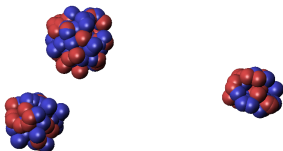
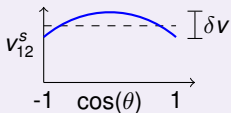
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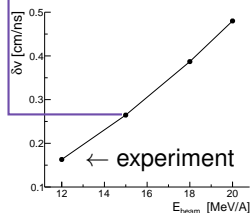
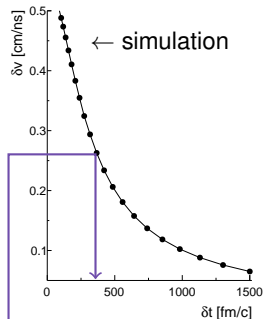
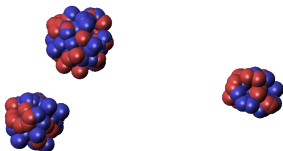
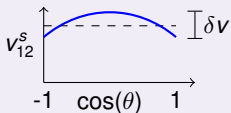
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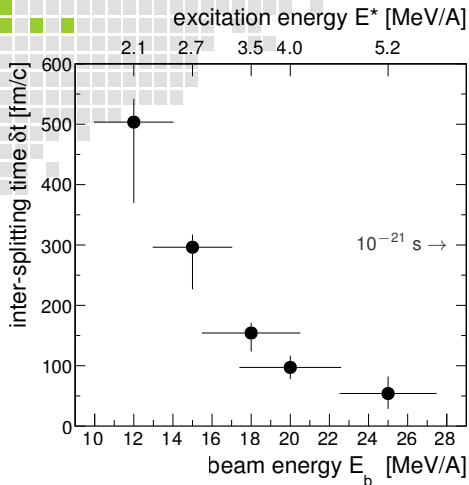
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# From hot sequential fission to multifragmentation

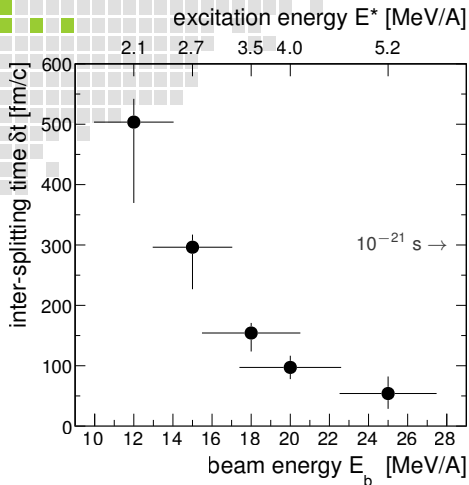


## Inter-splitting time evolution

- $\delta t$  decreases with increasing available or excitation energy

## Reaction mechanism

# From hot sequential fission to multifragmentation



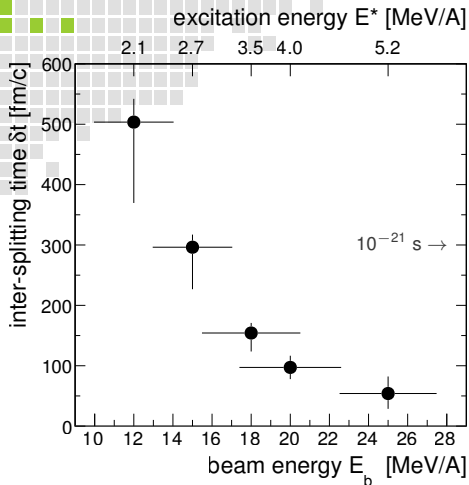
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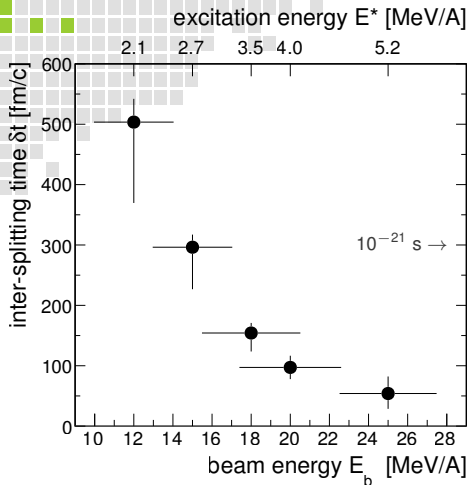
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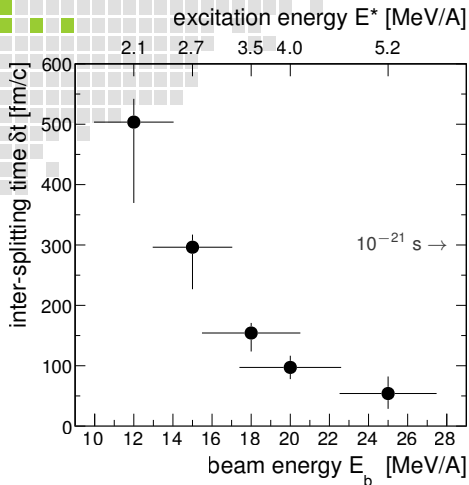
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# Summary and prospects

## Evolution of the decay mechanism : 3-fragment exit channel

- $^{129}\text{Xe} + ^{nat}\text{Sn}$  central collisions measured with INDRA at  $E_{\text{beam}} = 12\text{-}25 \text{ MeV/A}$

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D. Gruyer et al. (INDRA collaboration) arXiv :1309.7779 submitted to Phys. Rev. Let.

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- Chronometer : transport properties of nuclear matter (isospin diffusion, etc.)

Thank you for your attention !

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 M.Pârlog<sup>5</sup>, P.Pawłowski<sup>8</sup>, M.F.Rivet<sup>3</sup>,  
 R.Roy<sup>4</sup>, E.Rosato<sup>9</sup>, G.Spadaccini<sup>9</sup>,  
 G.Verde<sup>12</sup>, E.Vient<sup>5</sup>, M.Vigilante<sup>9</sup>,  
 and J.P.Wieleccko<sup>1</sup>  
**(INDRA Collaboration)**



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