

The differential neutron-deuteron scattering cross section from 100 keV to 600 keV measured using a proportional counter

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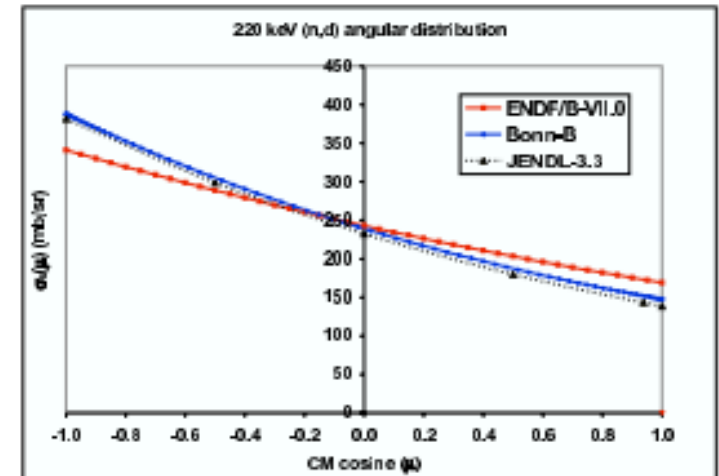
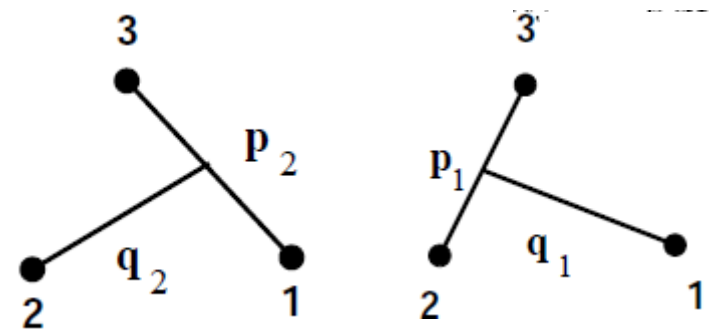
- **Motivation: Why is n-d scattering still of interest?**
- **Experimental and evaluated data**
- **Detour: Experiment at higher energies at nELBE**
- **The recoil proton prop. counter P2 of PTB**
- **MC modelling of the P2 reponse**
- **Measurements**
- **Results and future work**

⇒ **Remind: Work in progress!**



Quantum-mechanical N -body problems:

- $N = 2$: n-p scattering
 - $N = 3$: n-d scattering
 - Three-body problem described by Fadeev equations
 - Nucleon-nucleon potentials required as input
- ⇒ **Advanced theory makes precise predictions of cross sections and spin observables**



Ref. : J.P. Svenne *et al.*, Proc. ND2007, 07208

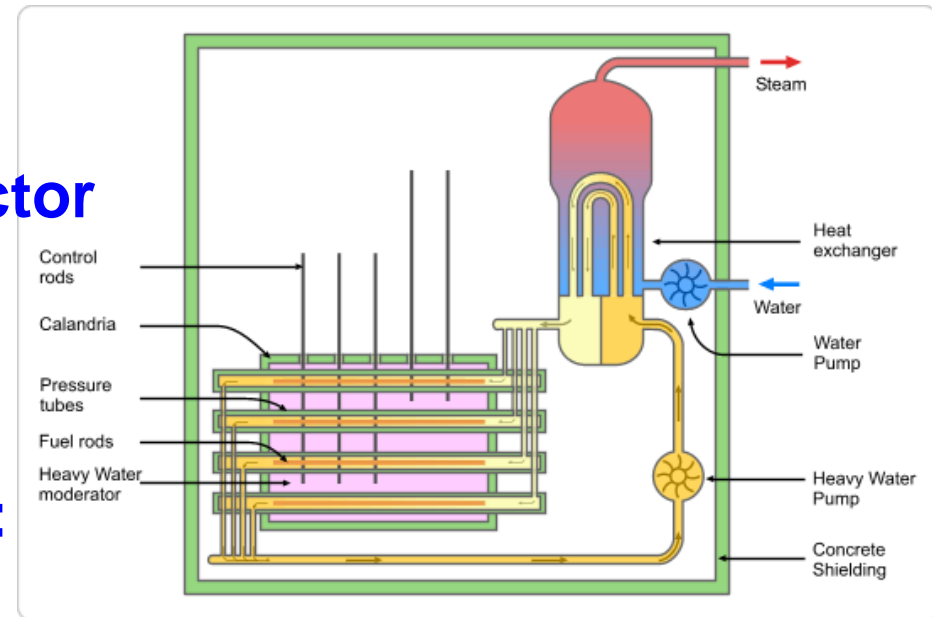
CANDU reactor:

- D₂O moderated and cooled reactor
- 28 operating units worldwide
- GenIII+: Advanced CANDU

Heavy-water solution benchmark:

- LANL HEU/D₂O experiment
- AECL coolant void reactivity critical experiment (NU/D₂O)
- Replacement of ENDF/B-VI.3 by ENDF/B-VII.1:

Calculated k_{eff} shows sensitivity to DX of D(n,n)D



Narrow Energy (optional), eV: Min: 100000.0 Max: 2000000.0
 Apply Data re-normalization (for advanced users, results in: C4, TAB and Plots)

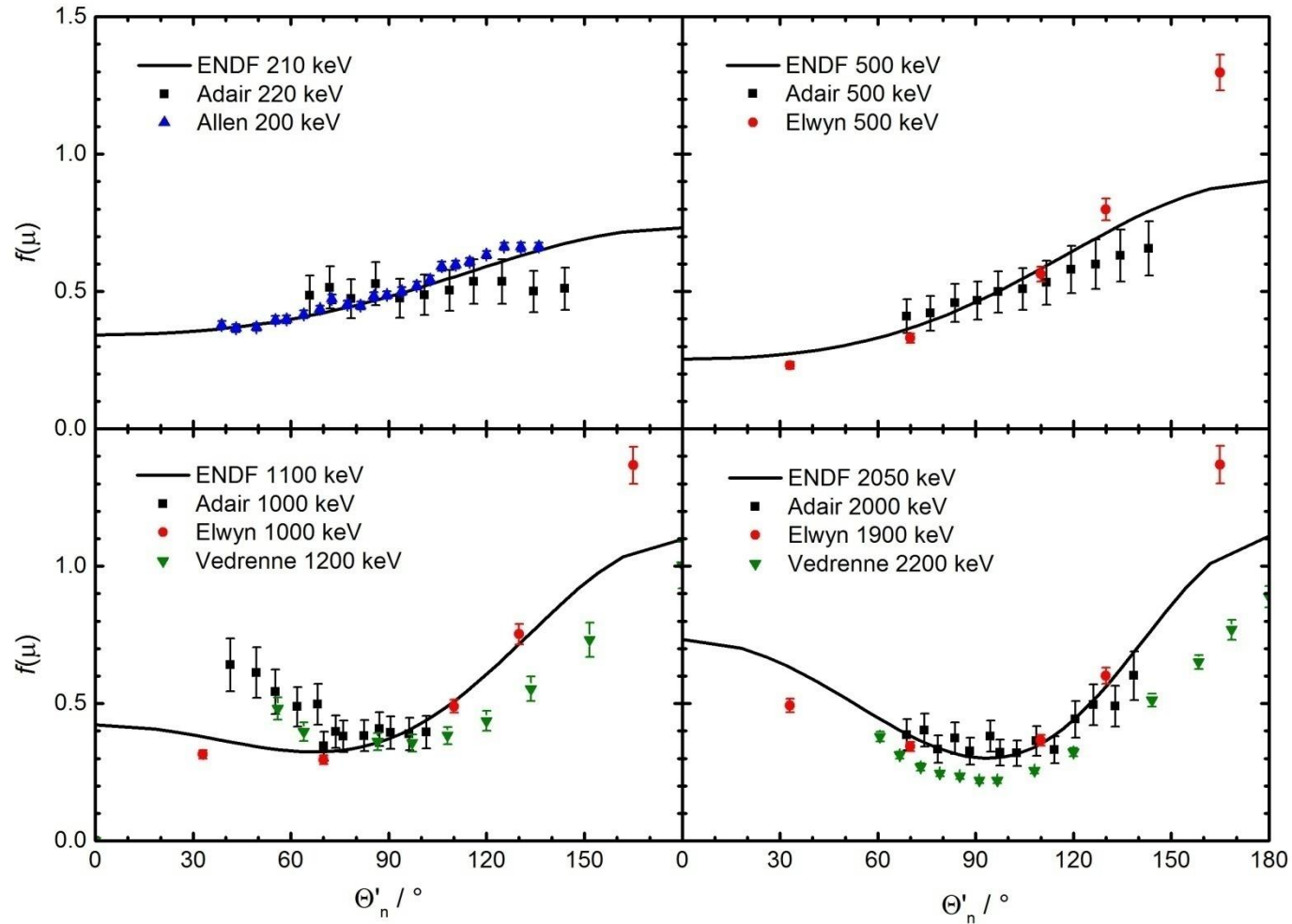
n	Display	Year	Author-1	Energy range, eV	Points
1)	1-H-2 (N,EL) 1-H-2,, DA C4: MF4 MT2				
Quantity: [DA] Differential c/s with respect to angle					
1	<input type="checkbox"/> Info X4+ X4± T4	1966	G.Vedrenne	1.20e6 1.42e7	98
2	<input type="checkbox"/> Info X4+ X4± T4	1962	A.J.Elwyn+	5.00e5 1.95e6	15
3	<input type="checkbox"/> Info X4+ X4± T4	1953	R.K.Adair+	2.20e5 2.50e6	88
2)	1-H-2 (N,EL) 1-H-2,, DA,, LEG C4: MF154 MT2				
Quantity: [DA] Legendre coef. $d/dA=a(0)+\text{Sum}(a(L)*P(L))$					
4	<input type="checkbox"/> Info X4+ X4± T4	1966	G.Vedrenne	1.20e6 1.42e7	35
3)	1-H-2 (N,EL) 1-H-2,, DA,D C4: MF=4 MT=?				
Quantity: [DA] Angular distribution of particle specified					
5	<input type="checkbox"/> Info X4+ X4± T4	1955	W.D.Allen+	1.00e5 2.00e5	44

Detection method:

- Recoil deuteron: Tunncliffe 1953, Adair 1955, Allen 1955
- Scattered neutron: Elwyn 1962, Vedrenne 1966

... Is this list complete ??

Experimental Data: Overview



ENDF: ENDF/B-VII.0

[Data Bank](#) > [Nuclear Data Services](#)

NEA Nuclear Data High Priority Request List, HPRL

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[Related references](#)

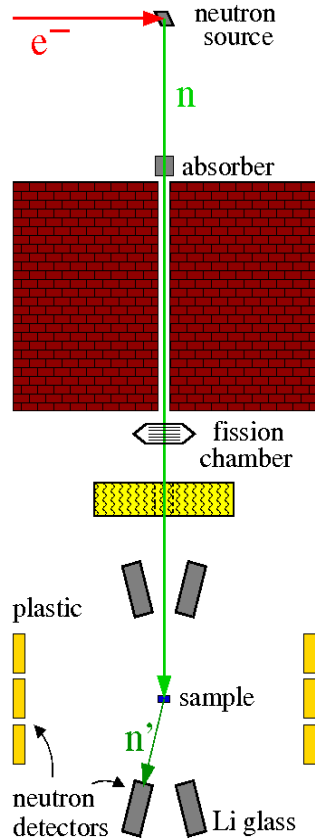
Request ID	8		Status of the request	High Priority request	
Target	Reaction and process	Incident Energy	Secondary energy or angle	Target uncertainty	Covariance
1-H-2	(n,ela) dA/dE	0.1 MeV-1 MeV	0-180 Deg	5	Y
Field	Subfield	Date Request created	Date Request accepted	Ongoing action	
Fission	Heavy Water Reactors	25-JUL-06	16-APR-07		

⇒ two ERINDA proposals by A.J.M. Plompen *et al.*:

Measurement of D(n,n)D angular distribution

- nELBE: neutron detection using LiGlas detectors
- PTB: deuteron detection in a proportional counter

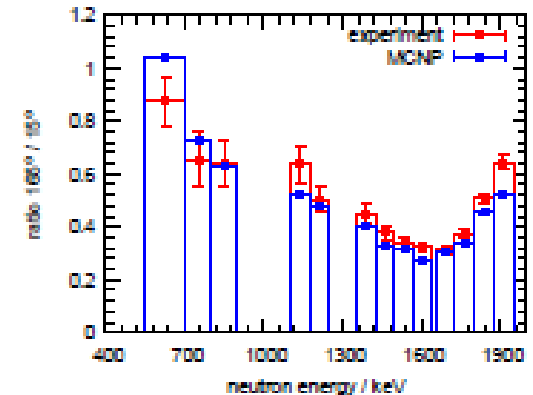
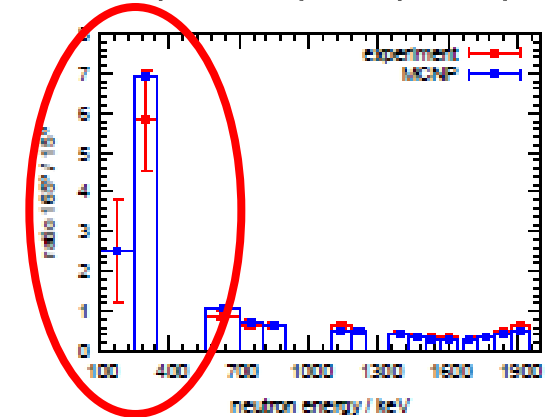
Detour: The experiment at nELBE



- ${}^6\text{Li}$ -glass detectors
51 mm \varnothing x 12.7 mm thick
- CD_2 target supplied by AECL
- Ratio $15^\circ/165^\circ$ measured
- Corrections for multiple scattering and background calculated using MCNP



$$N(165^\circ)/N(15^\circ)$$



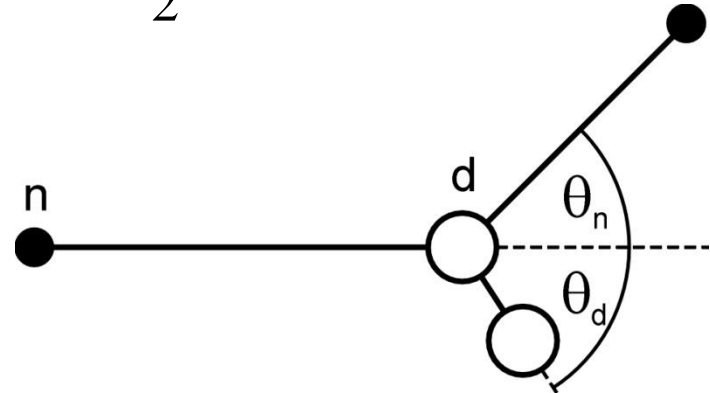
Ref: N. Nankov et al., 'The angular distribution of neutrons scattered from deuterium below 2 MeV', Proceedings of the conference ND2013 , PR80

Elastic scattering of neutrons:

$$E_{\text{rec}} = E_n \frac{4A}{(A+1)^2} \cos^2 \Theta_{\text{rec}}^{\text{LAB}} = E_n \frac{4A}{(A+1)^2} \frac{1 + \cos \Theta_{\text{rec}}^{\text{CM}}}{2}$$

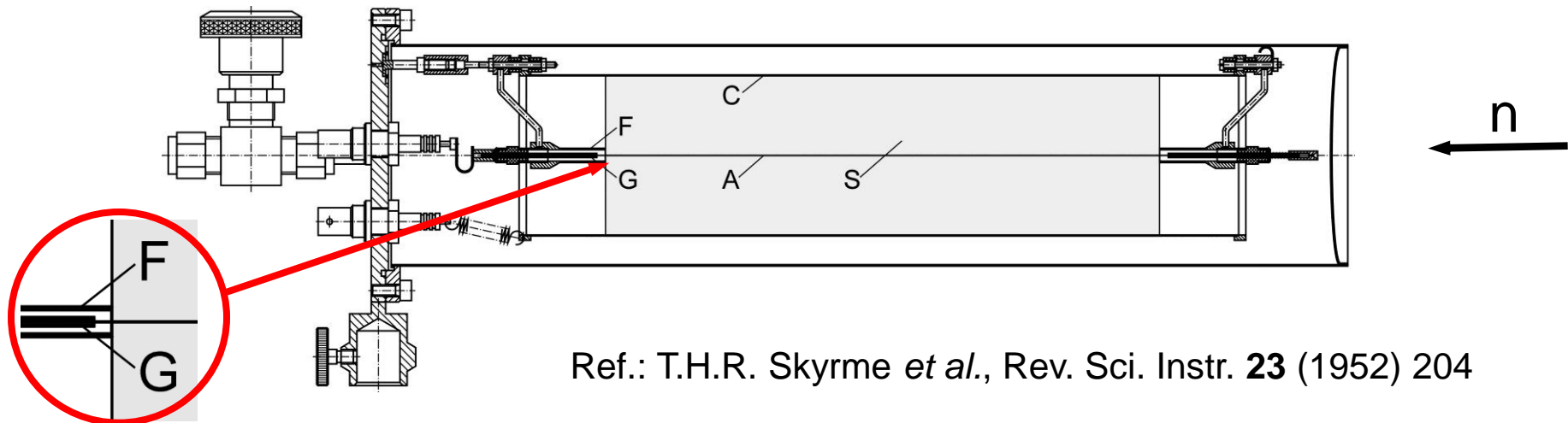
$$\frac{d\sigma}{dE_{\text{rec}}} = \frac{1}{\Phi} \frac{dN}{dE_{\text{rec}}} = \frac{1}{\Phi} \frac{dN}{d\Omega_{\text{rec}}^{\text{CM}}} \frac{2\pi d\cos \Theta_{\text{rec}}^{\text{CM}}}{dE_{\text{rec}}}$$

$$\Rightarrow \frac{d\sigma}{dE_{\text{rec}}} = \frac{4\pi}{E_n} \frac{(A+1)^2}{4A} \left(\frac{d\sigma}{d\Omega_{\text{rec}}^{\text{CM}}} \right) (E_{\text{rec}})$$



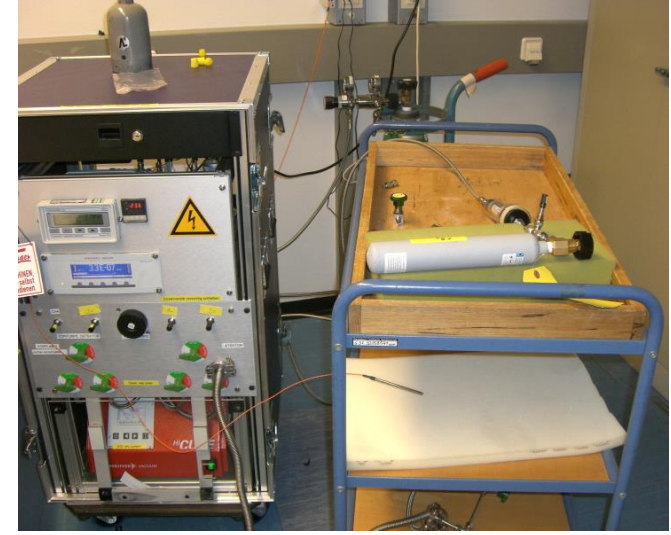
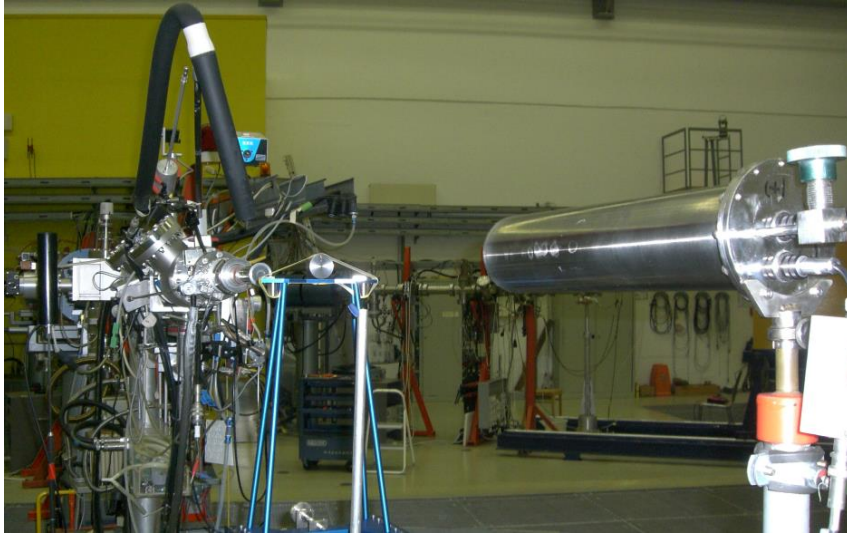
Ideal recoil detectors yield the angular distribution, but:

- incomplete energy deposition: wall effects
- conversion of deposited energy to detected signal: light yield, W -value
- non-linearity of the detection process: gas amplification
- competing reactions: n - ^{12}C scattering
- photon interactions



Ref.: T.H.R. Skyrme *et al.*, Rev. Sci. Instr. **23** (1952) 204

- **total volume: $\approx 1.6 \text{ dm}^3$**
- **active volume: $\varnothing 55.5 \text{ mm}$, $l = 193.3 \text{ mm}$**
- **el. field: defined by $\varnothing 4 \text{ mm}$ field tubes at ground potential**
- **anode: $\varnothing 100 \mu\text{m}$ gold-plated tungsten wire (selected)**
- **counting gas: H_2/CH_4 (3.5 vol.%), C_3H_8**
- **energy range: 20 keV – 2 MeV**



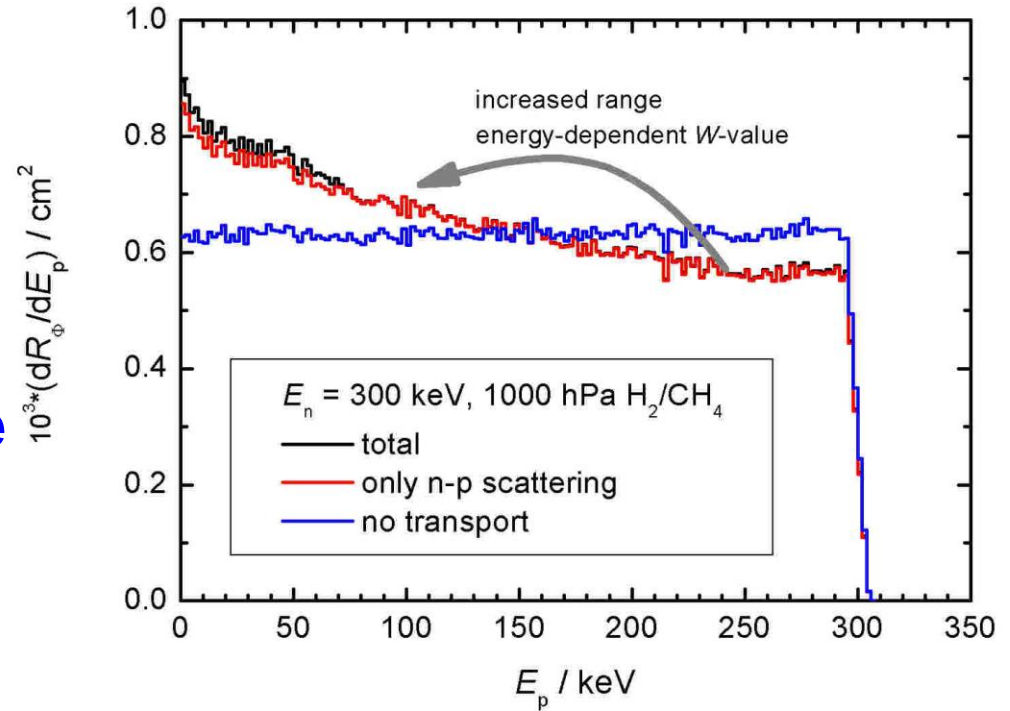
- deuterated gases: $H/D \approx 0.01$
 - D_2
 - CD_4 , C_3D_8 : purified using OxiSorb cartridges
- ${}^7Li(p,n)$: metallic Li target, Ta backing, $I_p = 3 \mu A$,
 $E_n = 150, 200, 250, 300, 500$ keV
- room-return neutrons: shadow-cone technique
- target scattering: MC calculation

MCNPX:

- dedicated PTRAC filter
- new ACE files required

Dedicated MC code:

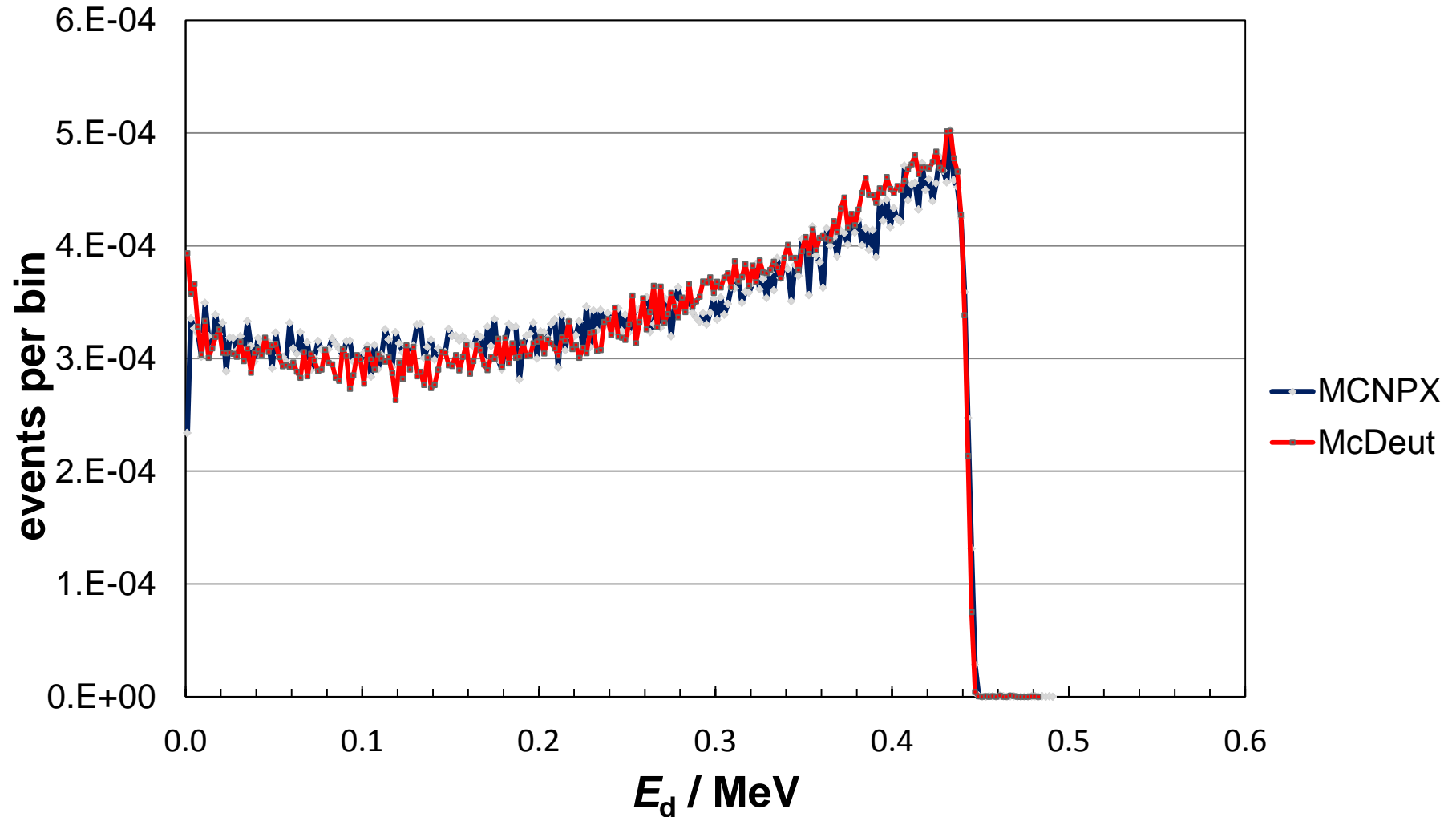
- energy-dependent W -value
- carbon recoils included
- exchange of range and DX data possible
- single $P_\ell(\cos \Theta)$ distributions
- fully analogue simulation

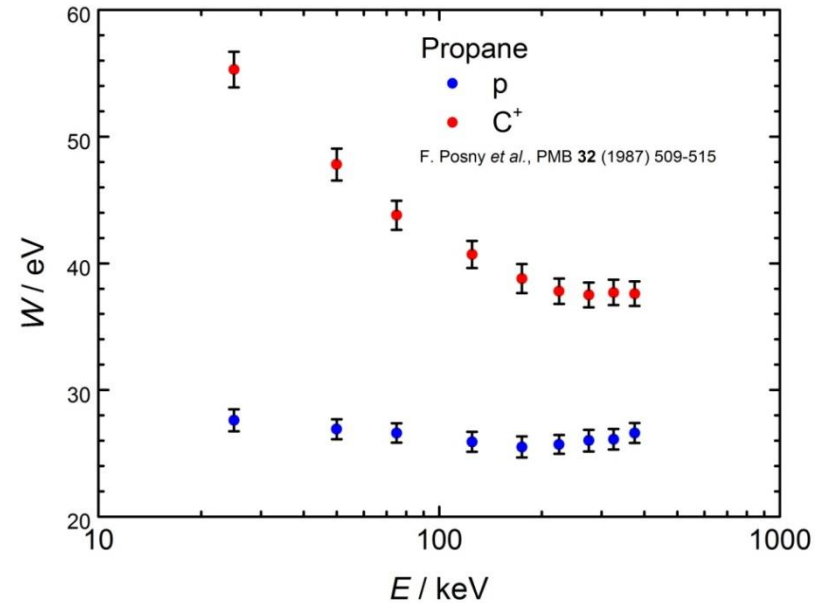
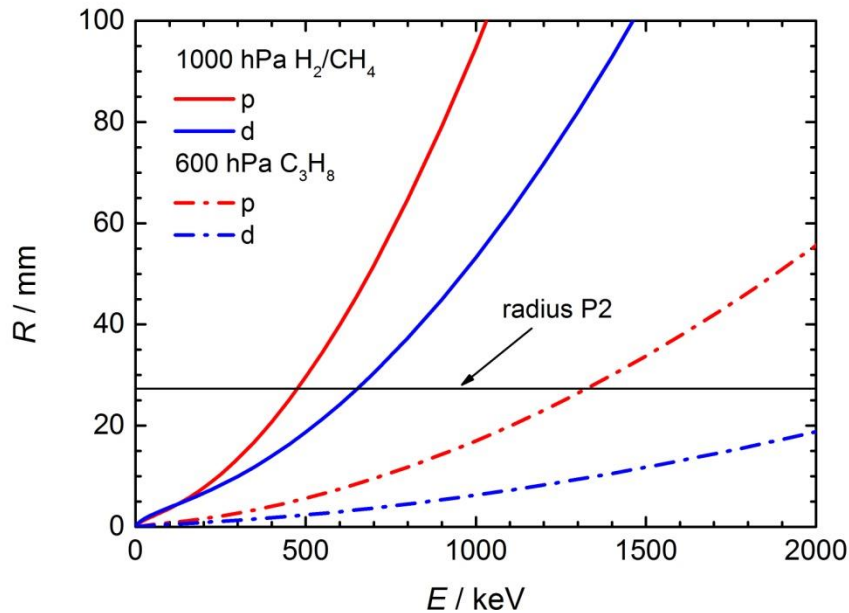


PH resolution:

Gaussian broadening, $\sigma/E = \text{const}$

498 keV



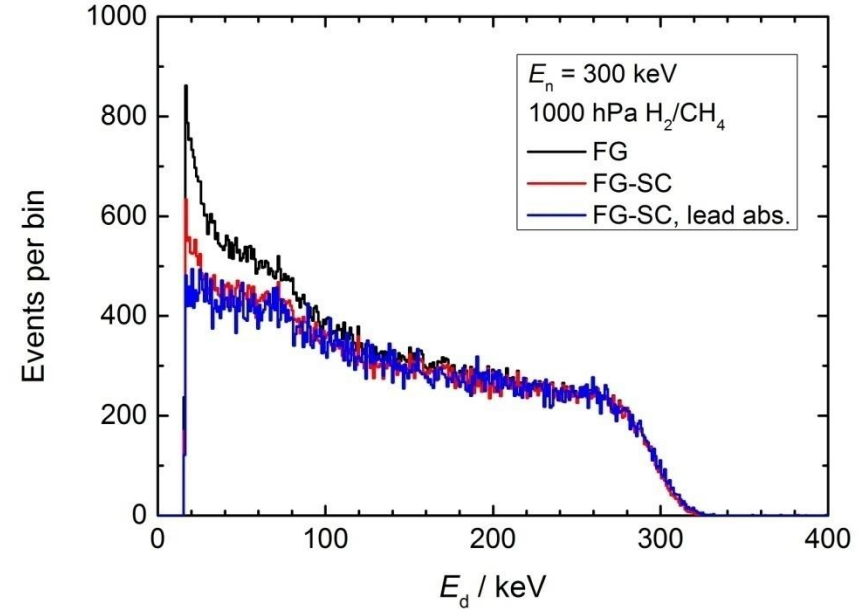
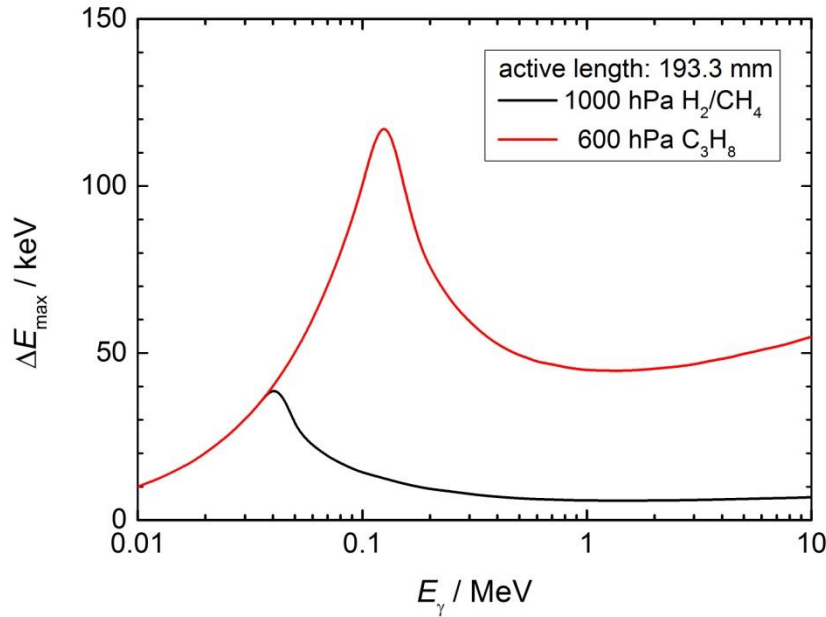


Range data: SRIM2012

Uncertainty: $u_S/S \approx 3\%$
 $u_R/R > 3\%$?

Rel. W -values: $W(Z_T, z_p, v_p)/W(Z_T, 1, \infty)$

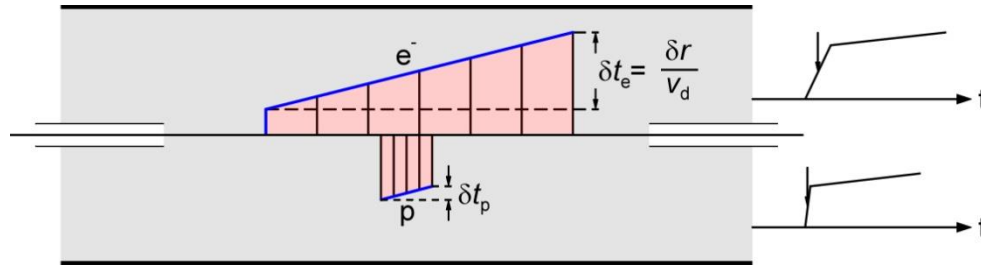
- p, d in H_2 : $W_r = 1$ for $E > 10$ keV
- p, d in C_3H_8 : $W_r = 1$?
- C^+ in H_2, C_3H_8 : $W_r = a \cdot \log(E) + b$



Photon interference suppressed by:

- metallic Li/Ta target: only ${}^7\text{Li}(p,p'\gamma)$, $\text{Ta}(p,p'\gamma)$, ${}^7\text{Be}$ decay
- 20 mm lead absorber: only el. scattering below 570 keV
- subtraction of a sub-threshold measurement
- electronic discrimination

Risetime Discrimination



Risetime:

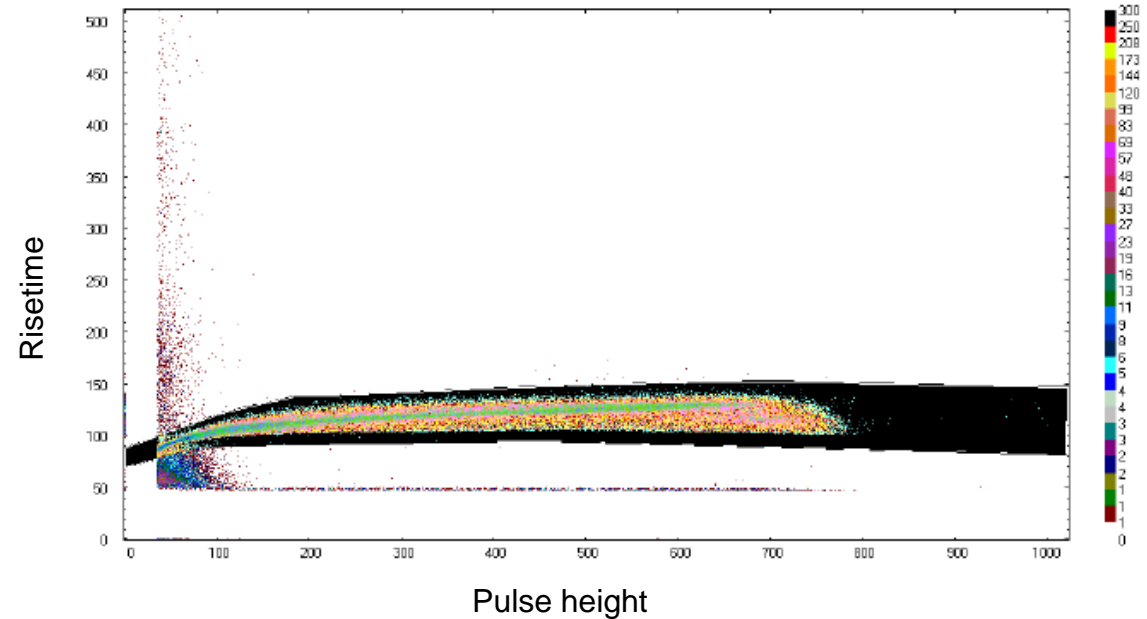
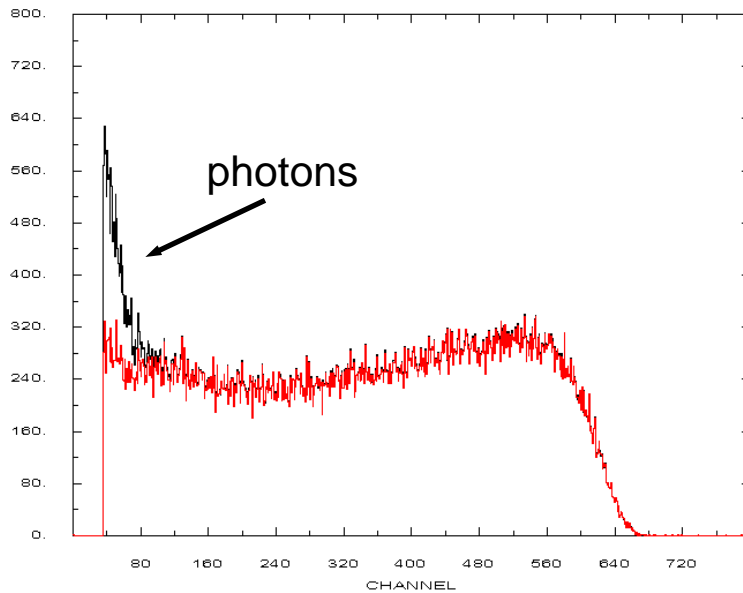
fast filter amp. : $t_{diff} = 50 \text{ ns}$, $t_{int} = 500 \text{ ns}$

- start: LE-disc. close to noise
- stop: CF-disc. ($f = 0.4$)

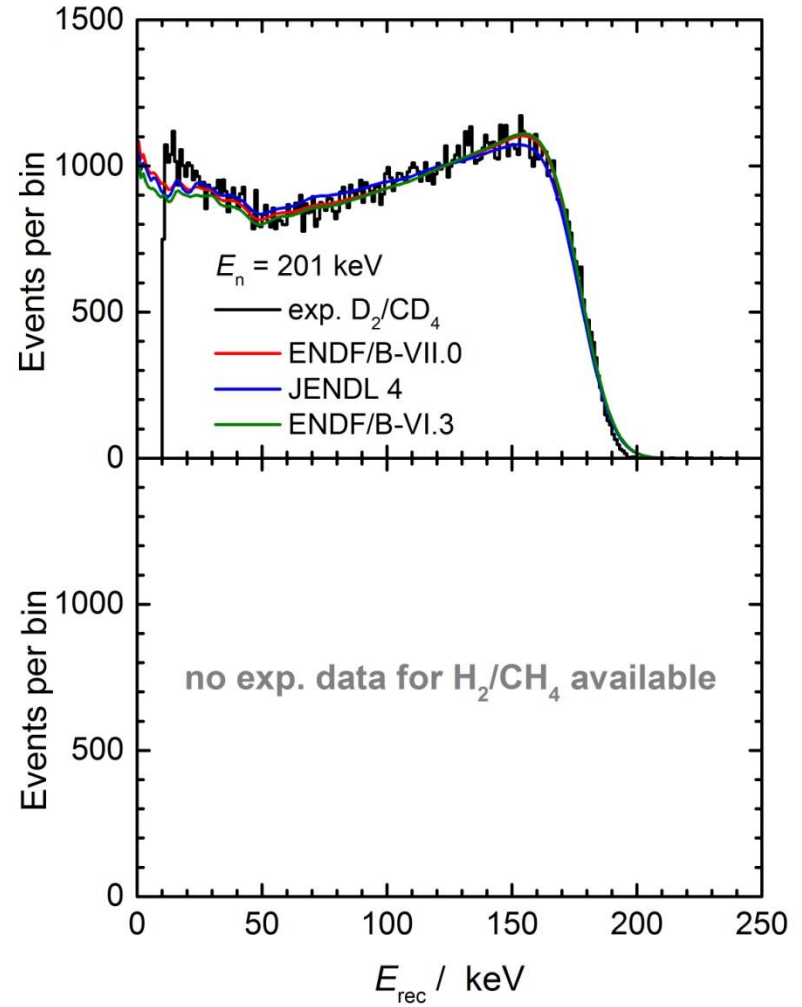
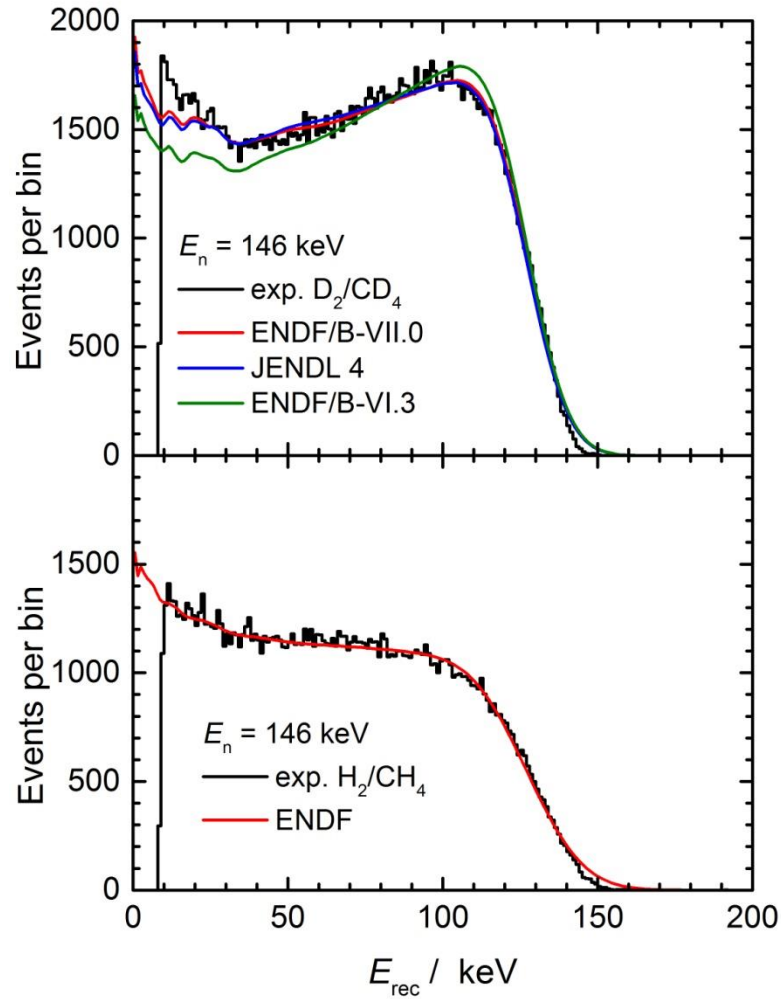
Pulse height:

shaping amp.: $t_s = 2 \mu\text{s}$

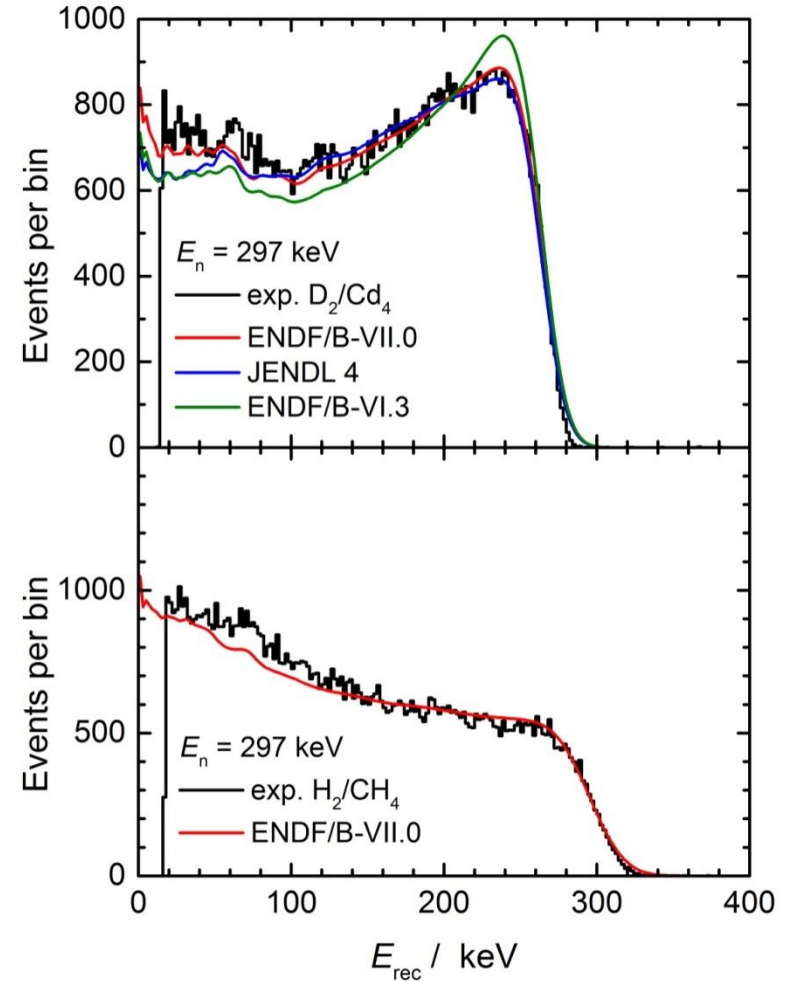
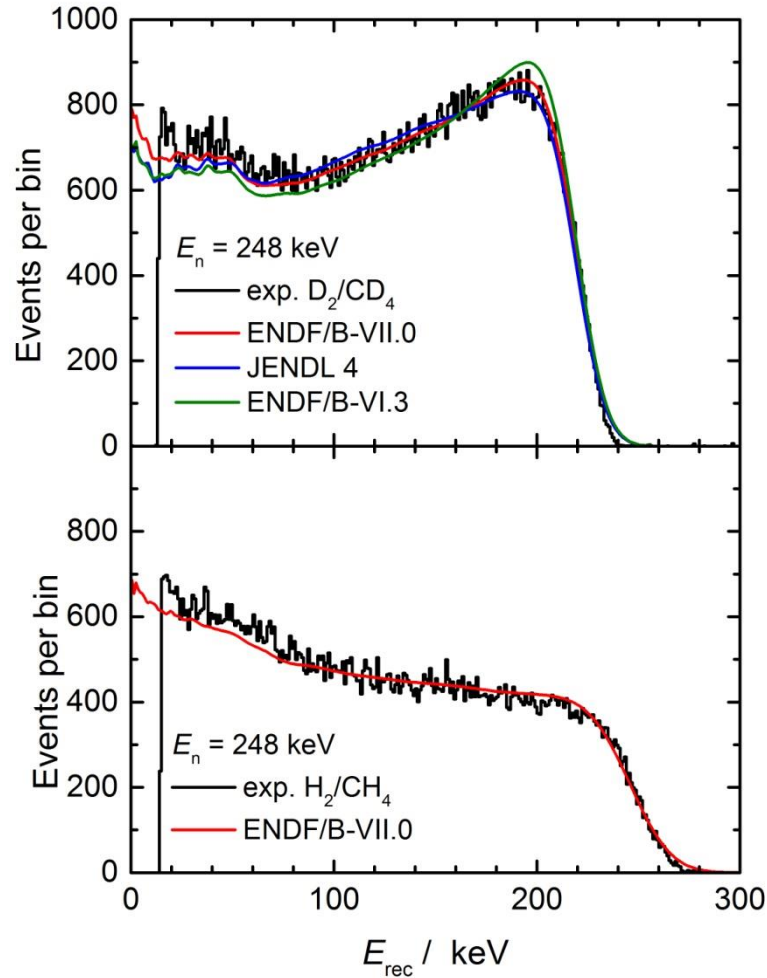
300 keV D_2/CD_4

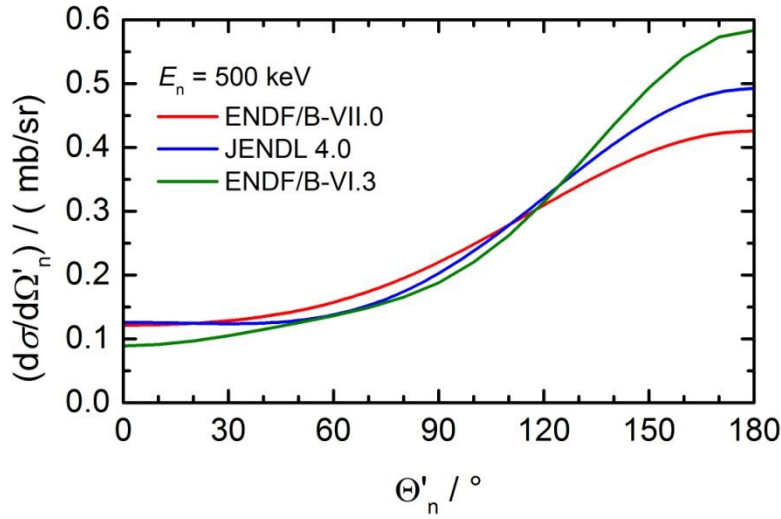
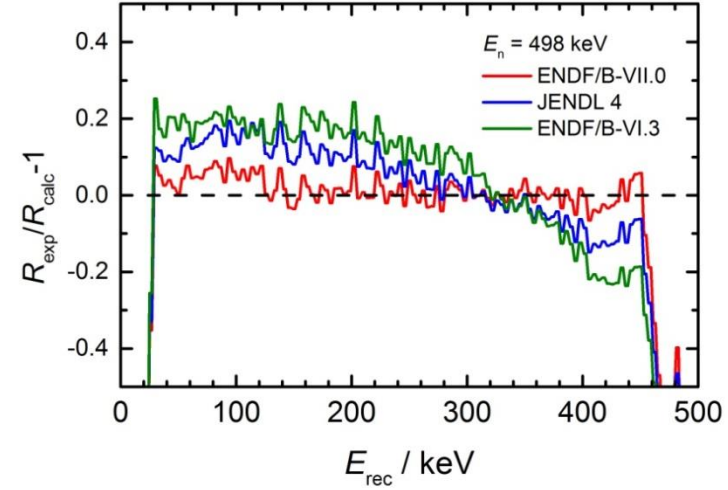
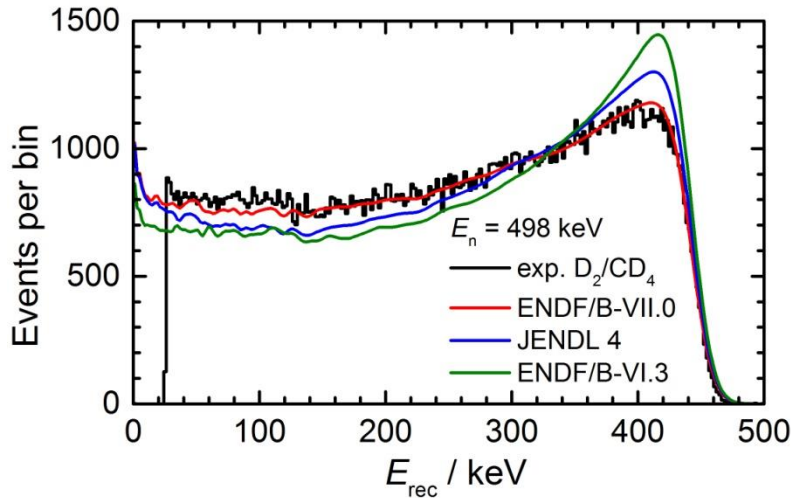


Results: 150 keV, 200 keV

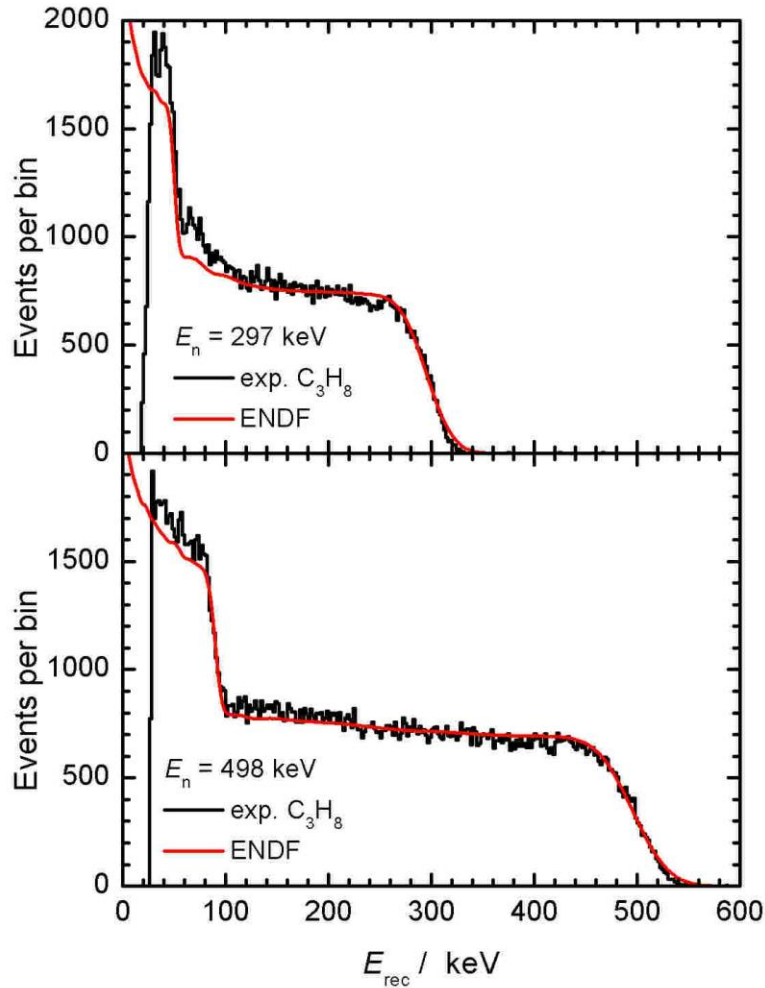


Results: 250 keV, 300 keV





- Still discrepancies at low pulse height
- ENDF/B-VI.3 and JENDL 4.0 are too anisotropic
- ENDF/B-VII.0: fair agreement
- Uncertainty: still $> 5\%$ at backward angles



- Same discrepancies below 100 keV as for hydrogen
- Energy dependence of W -value?
- So far no data for C_3D_8

- **Measurements of DX for D(n,n)D using a recoil counter were revisited:**
 - Reduced photon interference
 - Response from realistic MC simulations
 - Uncertainties from *W*-values and range data remained
 - Still residual photon interference at low pulse-heights
- ⇒ **ENDF/B-VII.0 evaluation is consistent with present results, ENDF/B-VI.3 is too anisotropic**
- ⇒ **Results relevant for a re-analysis of U/D₂O benchmarks**
- **Future work:**
 - Elimination of the photon interference
 - Extension to higher energies using C₃D₈ gas