

# Allowed parameter region in NMSSM with a long-lived slepton from a 125 GeV Higgs boson and light elements abundances

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— Collaborators —

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based on Phys.Rev. D86 (2012) 095024 and an ongoing project

# Motivation

## MSSM

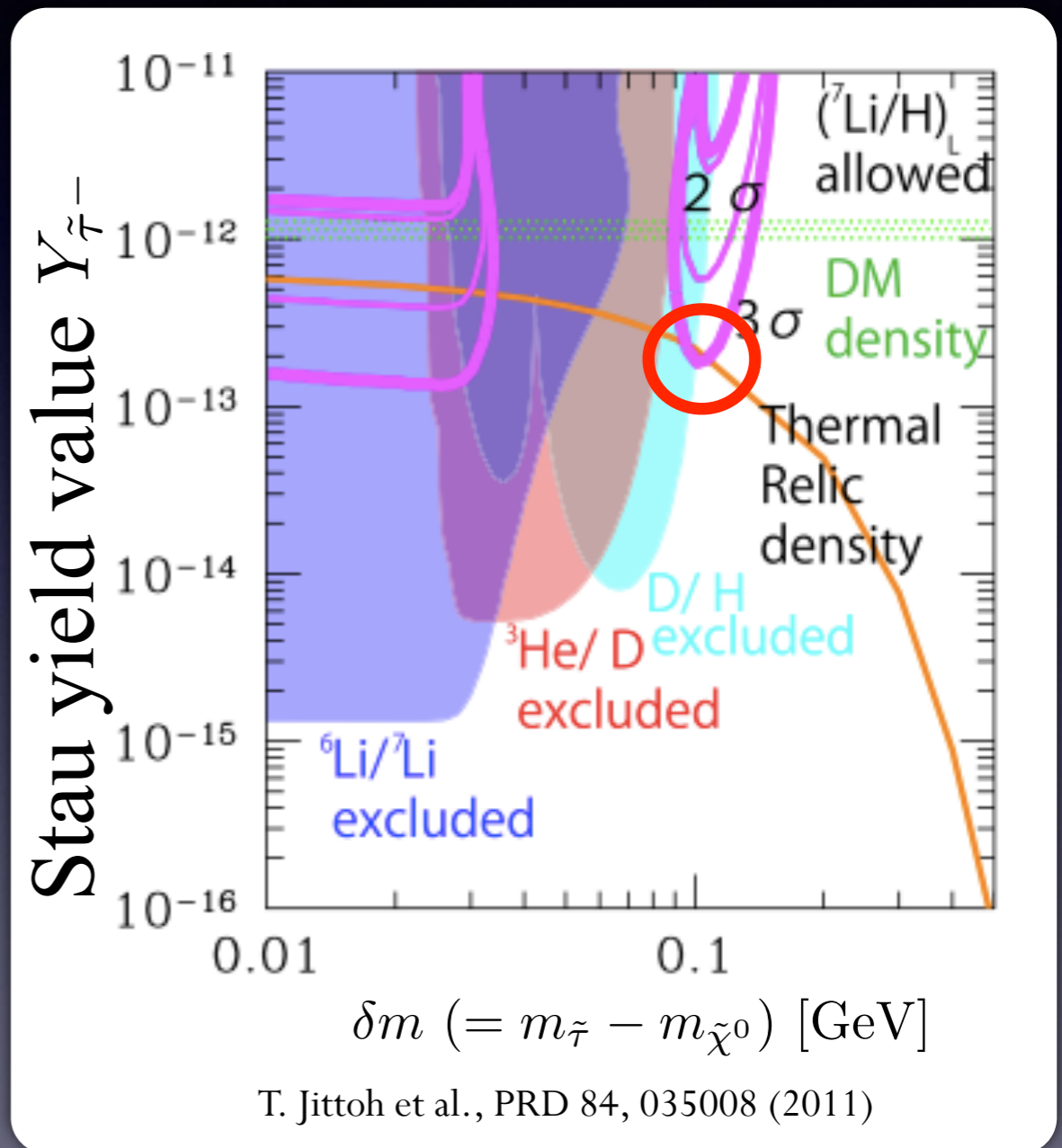
- ✓ Light element abundances
- ✓ Dark Matter relic density

T. Jittoh et al.(2010, 2011), K. Kohri et al.(2012)



## NMSSM

- ✓ Light element abundances
- ✓ Dark Matter relic density
- ✓ Higgs boson mass



# Introduction -DM candidate in MSSM-

## Stau coannihilation

DM candidate

LSP : Bino-like neutralino  $\tilde{\chi}^0 (\simeq \tilde{B}^0)$   
(Lightest SUSY Particle)

NLSP : Stau  $\tilde{\tau}$   
(Next-to-Lightest one)

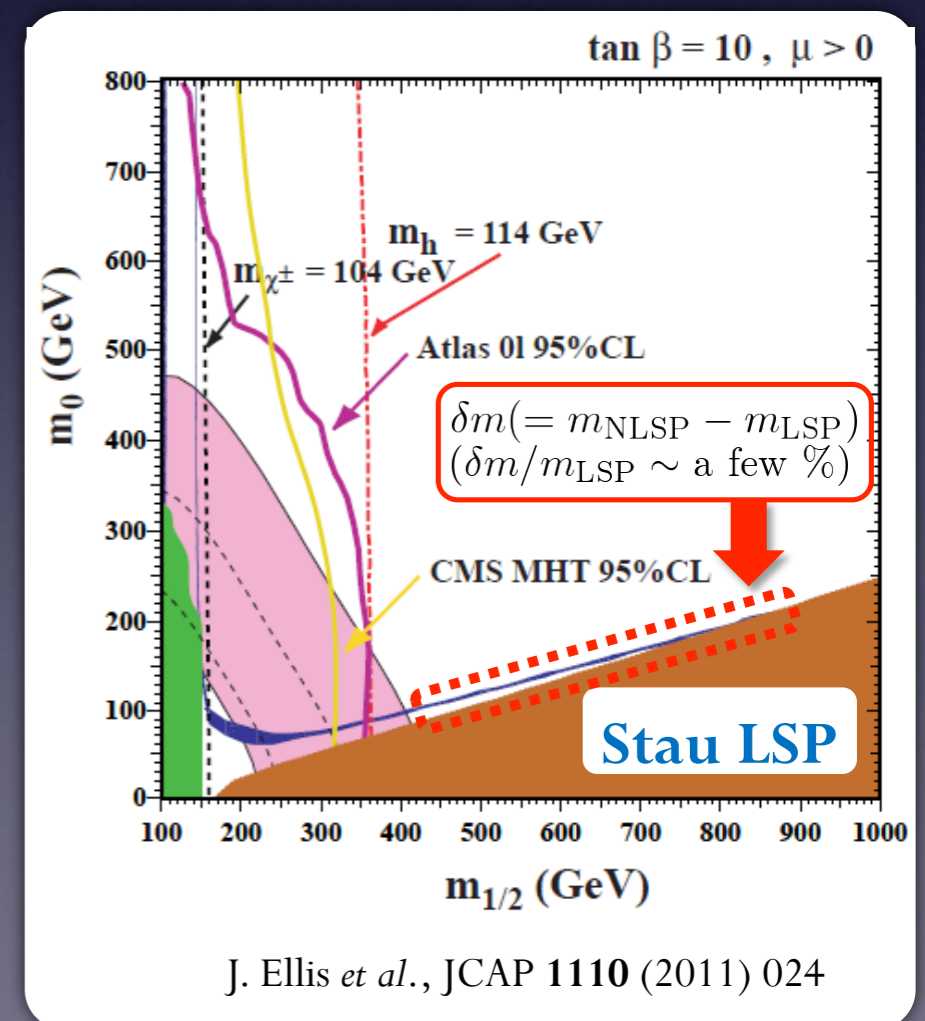
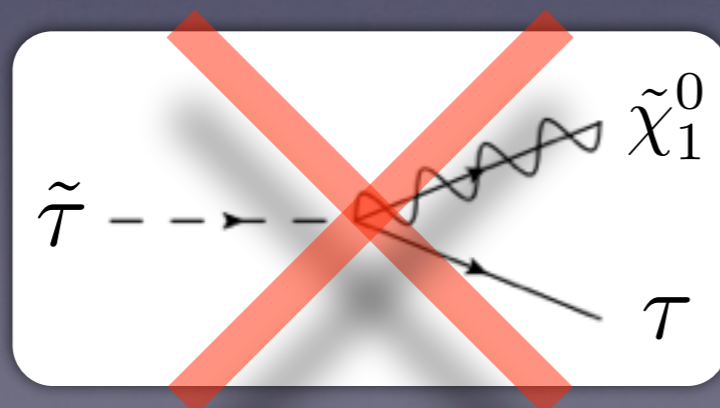
... degenerated in mass

→ NLSP annihilations also contribute to LSP DM annihilation.

→ Suitable relic density can be obtained.

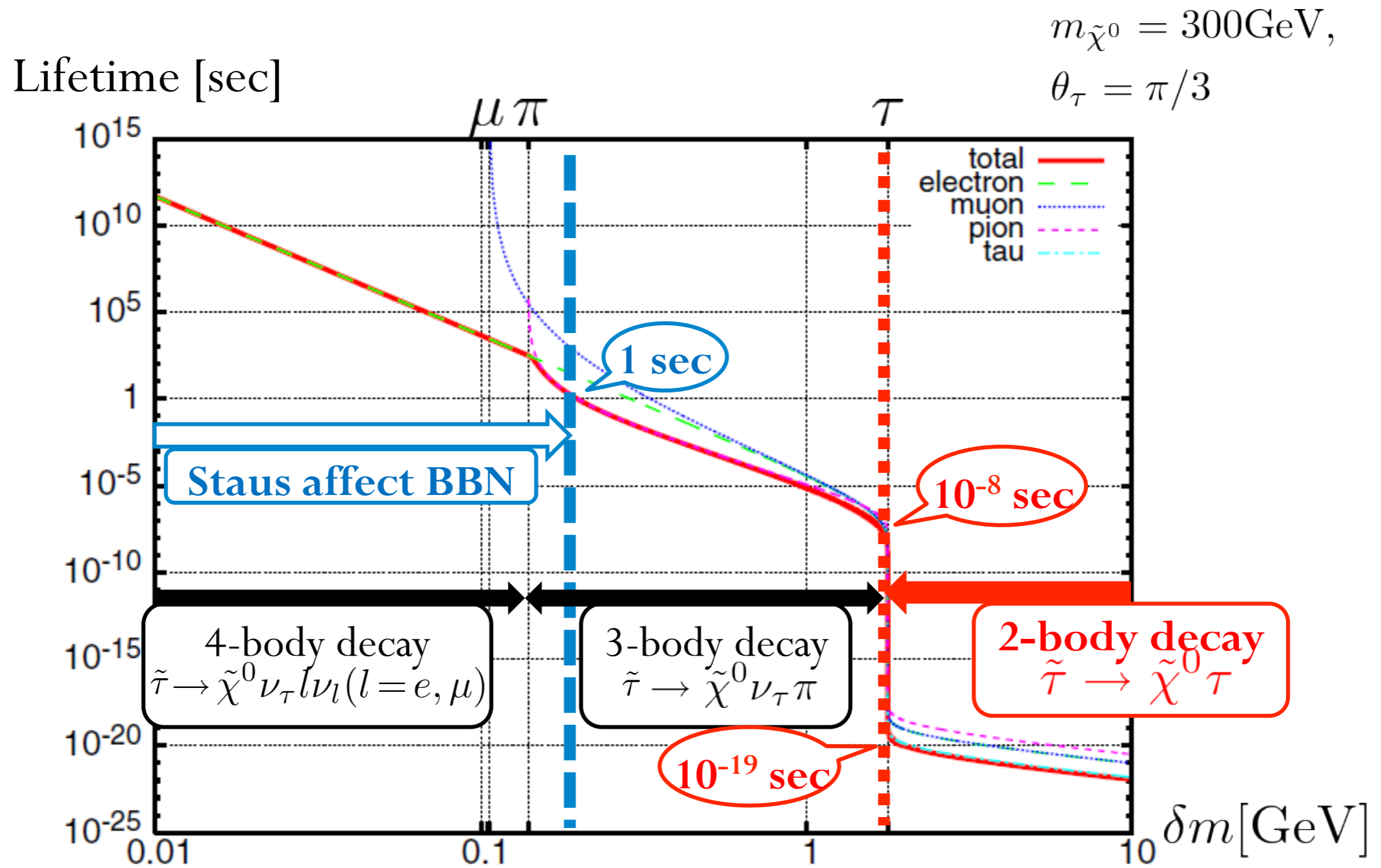
✓  $\delta m$  must satisfy  $\delta m / m_{\tilde{\chi}^0} < 1\%$ .

✓ If  $\delta m < m_\tau$   
stau becomes *long-lived*.





# Introduction - long-lived stau -





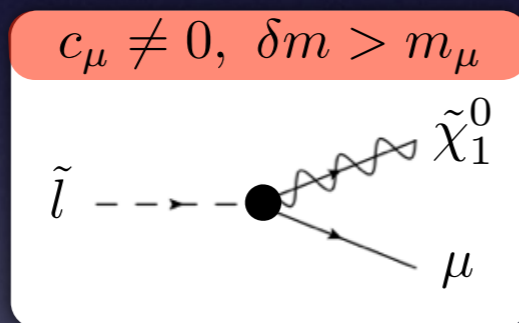
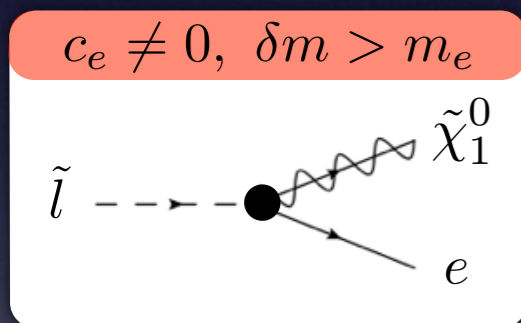
# Introduction - flavor mixing of the stau -

> Generalize the stau to be mixed state, 'slepton'

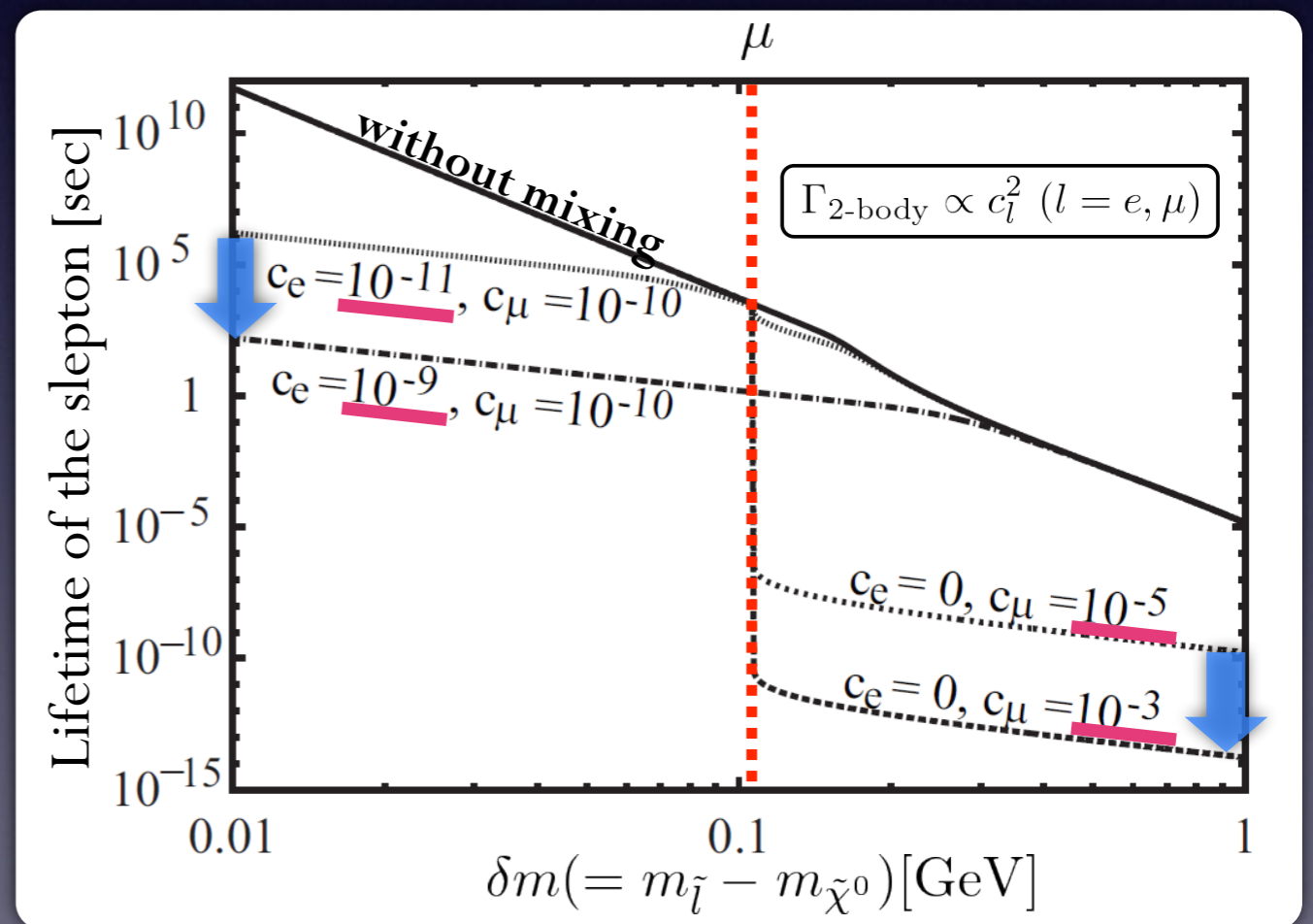
$$\tilde{\tau} \rightarrow \tilde{l} = \sum_{f=e,\mu,\tau} c_f \tilde{f}$$

$$\tilde{f} = \cos \theta_f \tilde{f}_L + \sin \theta_f e^{i\gamma_f} \tilde{f}_R, \quad c_e^2 + c_\mu^2 + c_\tau^2 = 1$$

→ flavor violating 2-body decays are allowed!



shorten the slepton lifetime



larger  $c_\mu$  and/or  $c_e$  → shorter  $\tau_{\tilde{l}}$

# Introduction - ${}^7\text{Li}$ problem and a solution -

## > ${}^7\text{Li}$ problem

... theor. > obs. for  ${}^7\text{Li}$  abundance in the standard BBN



A solution by exotic BBN reaction with long-lived slepton

### Internal Conversion

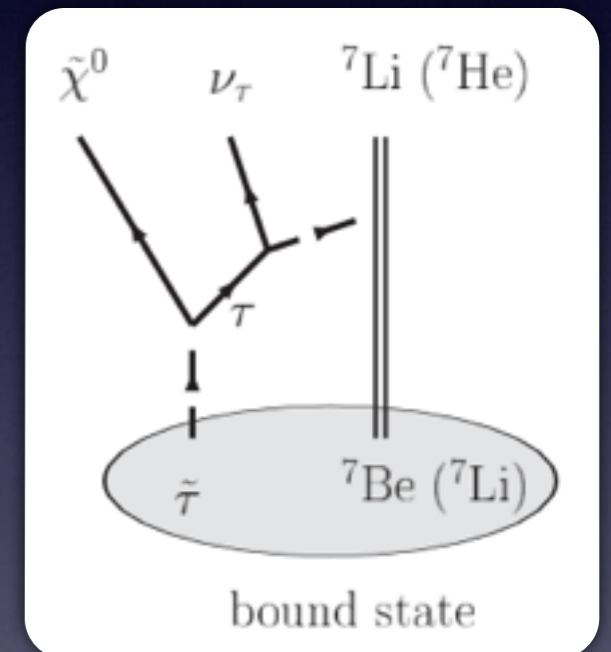
BBN era

$$T \sim (1 - 0.01)\text{MeV}$$

$$\Leftrightarrow t \sim (1 - 10^3)\text{sec}$$



$\sim \mathcal{O}(10^3)$  sec to form bound states



... reduce resultant abundance of  ${}^7\text{Li}$

T. Jittoh et al., PRD76, 125023 (2007)

$\tilde{l}$  must have enough long lifetime and sufficient relic density.  
... at least,  $\tau_{\tilde{l}} \sim 10^3\text{sec}$  and  $Y_{\tilde{l}} = n_{\tilde{l}}/s \sim 10^{-13}$  for  $\delta m \sim 100\text{MeV}$

# Allowed region in MSSM

## MSSM

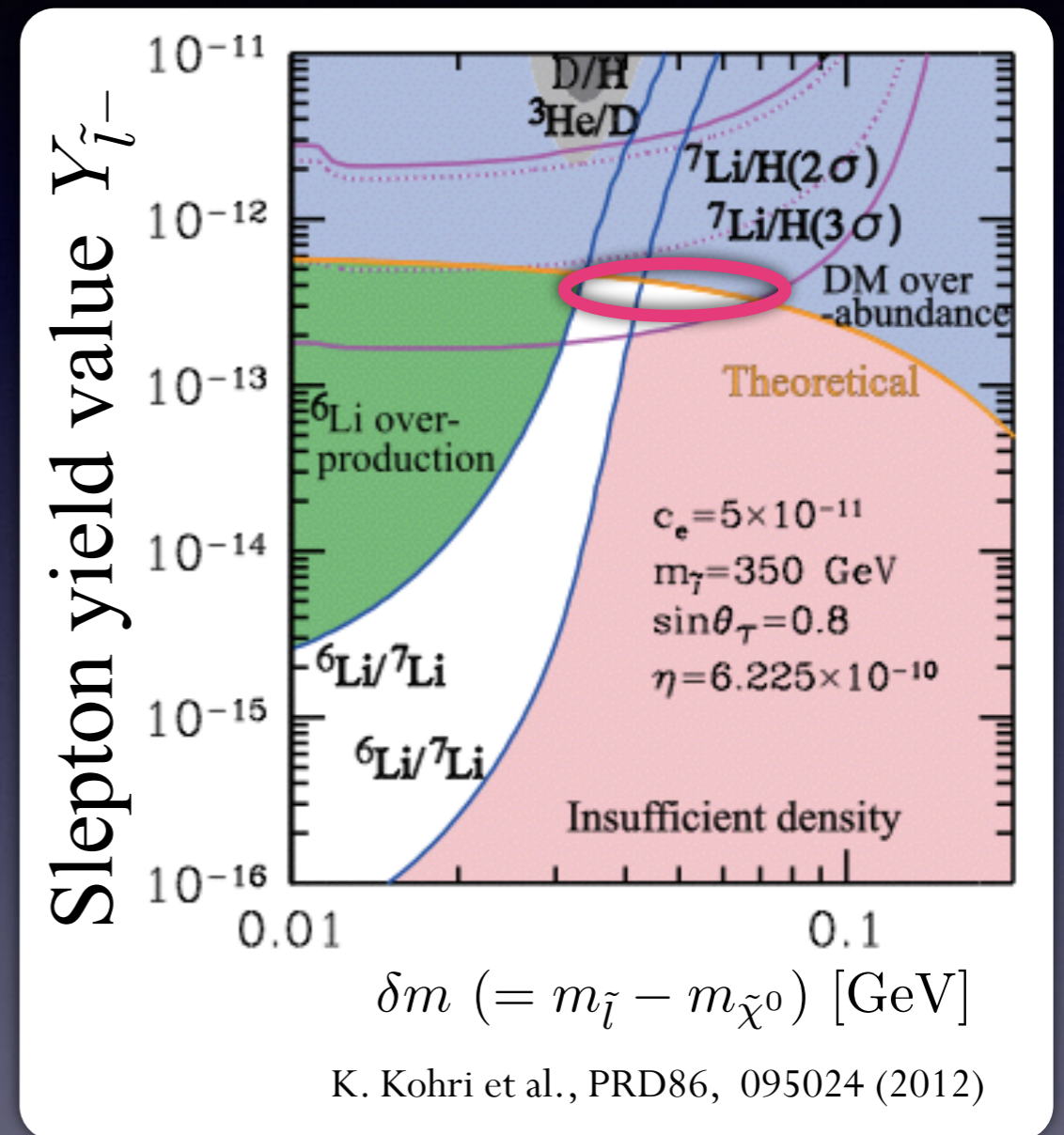
- ✓ Light element abundances
- ✓ Dark Matter relic density

T. Jittoh et al.(2010, 2011), K. Kohri et al.(2012)



## NMSSM

- ✓ Light element abundances
- ✓ Dark Matter relic density
- ✓ Higgs boson mass



With flavor mixing



# NMSSM ( $Z_3$ -invariant)

## ◆ Superpotential and soft SUSY breaking terms

$$W = W_{\text{MSSM}} + \lambda \hat{S} \hat{H}_u \cdot \hat{H}_d + \frac{1}{3} \kappa \hat{S}^3$$
$$-\mathcal{L}_{\text{soft}} = -\mathcal{L}_{\text{soft}}^{\text{MSSM}} + m_S^2 |S|^2 + \lambda A_\lambda H_u \cdot H_d S + \frac{1}{3} \kappa A_\kappa S^3 + h.c.$$

## ★ Higgs boson mass

$$m_h^2 = m_Z^2 \cos^2 2\beta + \lambda^2 v^2 \sin 2\beta - \frac{\lambda^2}{\kappa^2} v^2 (\lambda - \kappa \sin 2\beta)^2$$
$$+ \frac{3m_t^4}{16\pi^2 v^2} \left\{ \log \frac{m_s^2}{m_t^2} + \frac{X_t^2}{m_s^2} \left( 1 - \frac{X_t^2}{12m_s^2} \right) \right\} + \dots$$

(  $X_t \equiv A_t - \mu \cot \beta$ ,  $m_s \equiv \sqrt{m_{\tilde{t}_1} m_{\tilde{t}_2}}$  )

## ✓ Parameters in the Higgs sector

$$\lambda, \kappa, A_\lambda, A_\kappa, \tan \beta \equiv \langle H_u \rangle / \langle H_d \rangle, \mu_{\text{eff}} \equiv \lambda s \quad (s = \langle S \rangle)$$

# Neutralinos in NMSSM

> Mass eigenstates

$$\tilde{\chi}_i^0 = N_{i\tilde{B}^0} \tilde{B}^0 + N_{i\tilde{W}^0} \tilde{W}^0 + N_{i\tilde{H}_d^0} \tilde{H}_d^0 + N_{i\tilde{H}_u^0} \tilde{H}_u^0 + N_{i\tilde{S}^0} \tilde{S}^0$$

> Mass matrix

$$\begin{pmatrix} M_1 & 0 & -\cos\beta \sin\theta_W m_Z & \sin\beta \sin\theta_W m_Z & 0 \\ & M_2 & \cos\beta \cos\theta_W m_Z & -\sin\beta \cos\theta_W m_Z & 0 \\ & & 0 & -\mu_{\text{eff}} & -\mu_\lambda \sin\beta \\ & & & 0 & -\mu_\lambda \cos\beta \\ & & & & \mu_\kappa \end{pmatrix}$$

$$\mu_{\text{eff}} = \lambda s, \quad \mu_\lambda = \lambda v, \quad \mu_\kappa = 2\kappa s$$

✓ We consider two cases;

- **Singlino-like neutralino LSP** ... not exist in MSSM
- **Bino-like neutralino LSP** ... almost same as one in MSSM

# Singlino-like neutralino LSP

## > Interaction relevant to the slepton decay

$$-\mathcal{L}_{\tilde{\chi}_1^0-l-\tilde{l}} = \tilde{l}^* \tilde{\chi}_1^0 (G_{L1} P_L + G_{R1} P_R) l + \text{h.c.}$$

$$G_{L1} = \frac{m_l g_2}{\sqrt{2} m_W \cos \beta} \sin \theta_l e^{i\gamma_l} N_{1\tilde{H}_d^0},$$

$$G_{R1} = \frac{m_l g_2}{\sqrt{2} m_W \cos \beta} \cos \theta_l N_{1\tilde{H}_d^0},$$

●  $G_{L1}$  and  $G_{R1}$  are typically small comparing to those in the case of bino-like neutralino LSP.



⊗ **Longer lifetime of the slepton ( $\tau_{\tilde{l}}$ )**

⊗ **Longer timescale of Internal Conversion ( $\tau_{IC}$ )**

✓ Parameters :  $\lambda, \kappa, \tan \beta$



# Bino-like neutralino LSP

> Interaction relevant to the slepton decay

include NMSSM parameters  
(do not depend on  $\kappa$ )

$$-\mathcal{L}_{\tilde{\chi}_1^0-l-\tilde{l}} = \tilde{l}^* \tilde{\chi}_1^0 (G_{L1} P_L + G_{R1} P_R) l + \text{h.c.}$$

$$G_{L1} = \frac{g_2}{\sqrt{2}} \tan \theta_W \cos \theta_l - \frac{m_l g_2}{\sqrt{2} m_W \cos \beta} \sin \theta_l e^{i\gamma_l} N_{1\tilde{H}_d^0},$$

$$G_{R1} = \sqrt{2} g_2 \tan \theta_W \sin \theta_l e^{i\gamma_l} + \frac{m_l g_2}{\sqrt{2} m_W \cos \beta} \cos \theta_l N_{1\tilde{H}_d^0}$$

● The second terms are typically small comparing to the first terms in  $G_{L1}$  and  $G_{R1}$ .

( $N_{1\tilde{H}_d^0} \rightarrow 0$   $\Rightarrow$  same as in bino neutralino in MSSM)

✓ Parameters :  $\lambda, \tan \beta, s$

# Strategy

## 1. Search for allowed region on $\lambda$ - $\kappa$ plane

### ✓ Theoretical constraints :

- *lifetime of the slepton  $\tau_{\tilde{l}}$*
- *timescale of the internal conversion processes  $\tau_{IC}$*

## 2. Select several points allowed from phenomenology

### ✓ Phenomenological constraints :

- *the Higgs boson mass  $m_h$*
- *DM relic density  $\Omega_{DM}h^2$*
- *etc.*



NMSSMTools

U. Ellwanger, C.Hugonie

## 3. Confirm the points to give suitable light element abundances

- ✓ Nuclear network calculation (show the results on  $\delta m$ - $Y_{\tilde{l}-}$  plane)

### NMSSM

- ✓ Light element abundances
- ✓ Dark Matter relic density
- ✓ Higgs boson mass

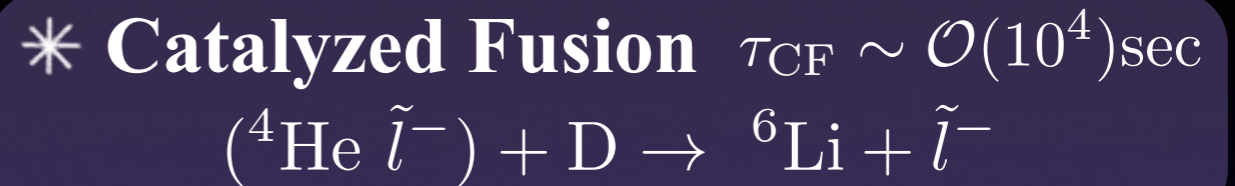
# Theoretical constraints

- **Lifetime of the slepton**

$$10^3 \text{ sec} < \tau_{\tilde{l}} < 10^5 \text{ sec}$$

... to avoid over-production of  ${}^6\text{Li}$ .

... to form bound state with nuclei for IC.



A solution of  
**the  ${}^6\text{Li}$  problem**  
( theor.  $<$  obs. )

- **Timescale of the Internal Conversion**

$$\tau_{\text{IC}} < 0.1 \tau_{\tilde{l}} \quad \dots \text{ to reduce enough amount of } {}^7\text{Li}.$$

- **Rate of dominant component in the LSP neutralino**

$$N_{1\tilde{S}}^2 > 0.9 \quad \dots \text{ for singlino-like LSP}$$

$$N_{1\tilde{B}}^2 > 0.9 \quad \dots \text{ for bino-like LSP}$$



# Phenomenological constraints

- **Dark matter relic density**

$$0.1118 \leq \Omega_{\text{DM}} h^2 \leq 0.1280 \quad (3\sigma)$$

by Planck Collaboration

- **Higgs boson mass**

$$m_h = 125.0 \pm 3 \text{ GeV}$$

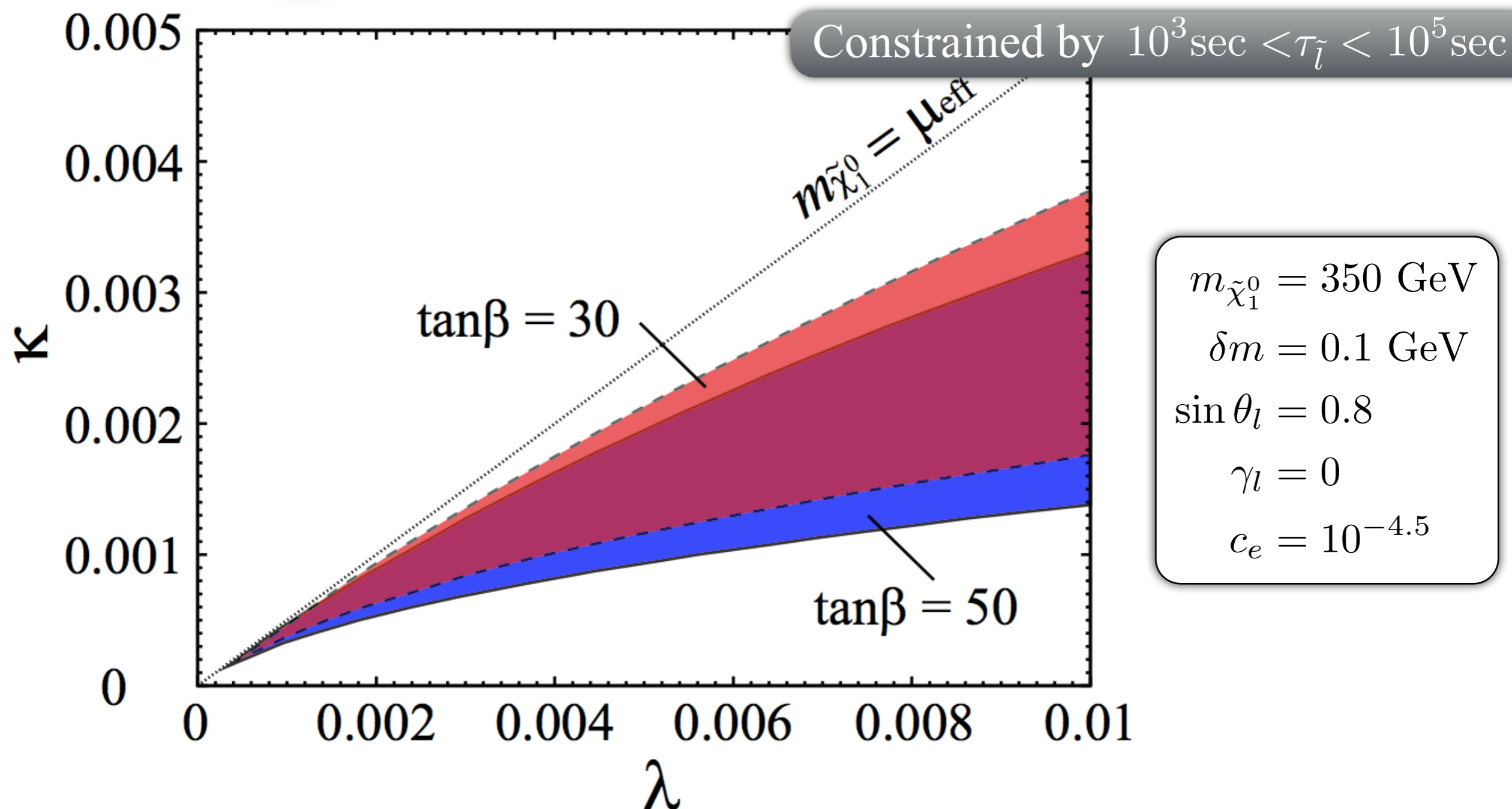
... uncertainty among calculation codes  
( NMSSMTools, SPheno, etc.. )

We also check  $(g - 2)_\mu$ , and branching ratios of rare decays  $B_s \rightarrow \mu^+ \mu^-$  and  $b \rightarrow s\gamma$  calculated by NMSSMTools.

# Results

Case 1. Singlino-like LSP, small  $\lambda$ - $\kappa$  region

# 1. The region allowed from theoretical constraints



✓ Larger  $\kappa$ , and/or  $\tan\beta$ , smaller  $\lambda$

→ larger  $G_{L1}$  → shorter  $\tau_{\tilde{l}}$  and  $\tau_{\text{IC}}$



# 2. The points which satisfy phenomenological constraints

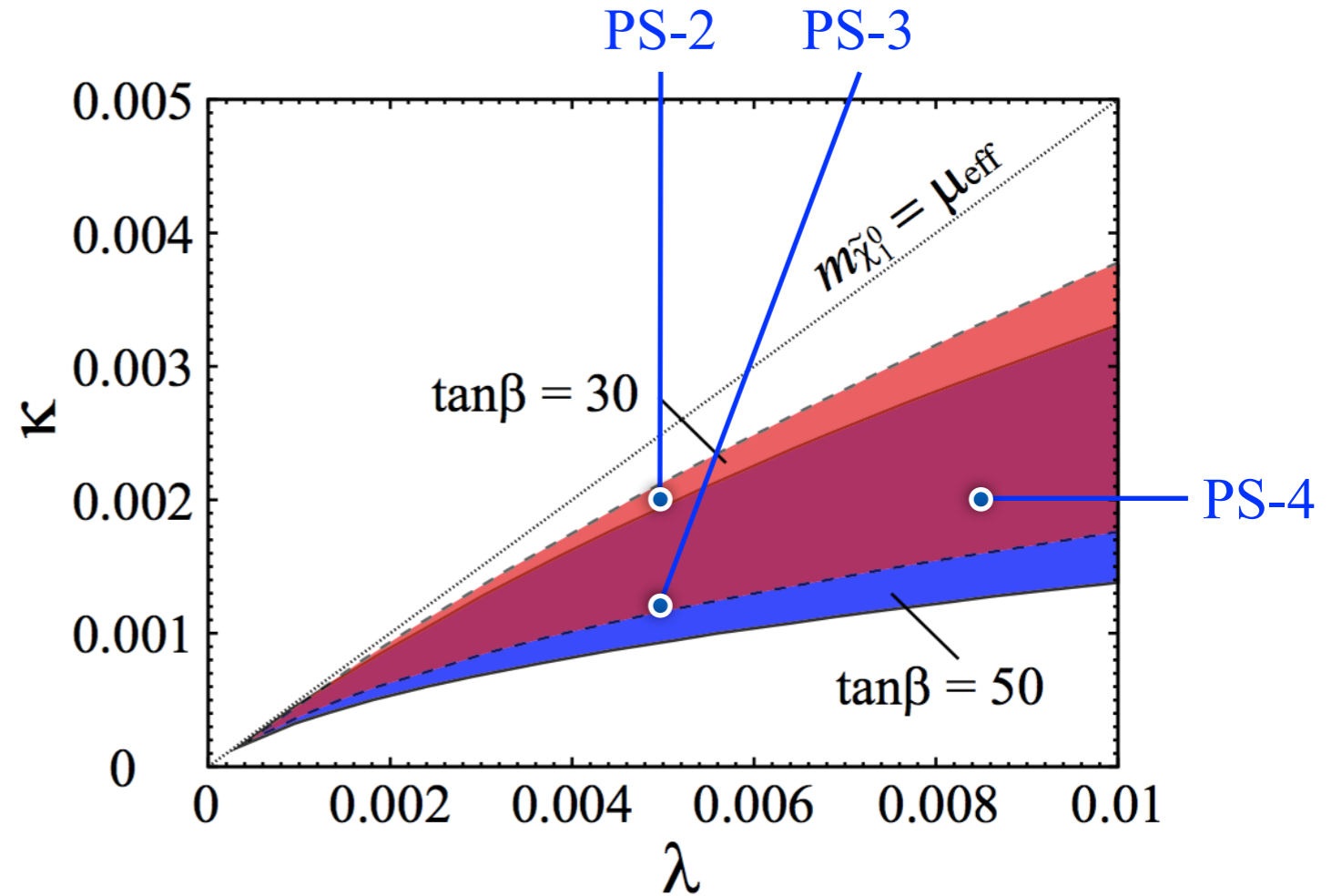
Input	PS-1, PS-2	PS-3	PS-4
$M_2$	1000.0	1000.0	1000.0
$A_t$	-7200.0	-7200.0	-7200.0
$A_\tau$	-7200.0	-1000.0	-400.00
$m_{\tilde{L}_3}$	409.72	416.69	416.16
$m_{\tilde{E}_3}$	383.90	388.08	387.75
$\lambda$	0.0050	0.0050	0.0085
$\kappa$	0.0020	0.0012	0.0020
$A_\lambda$	800.00	800.00	800.00
$A_\kappa$	-100.00	-100.00	-100.00
$\mu_{\text{eff}}$	426.39	714.61	728.81
$\tan\beta$	30.000	30.000	30.000
Output			
$h_1^0$	125.30	124.82	124.55
$h_2^0$	315.13	317.05	317.06
$h_3^0$	3512.5	4512.6	5424.1
$a_1^0$	226.20	226.83	226.81
$a_2^0$	3512.6	4512.6	5424.1
$H^\pm$	3511.2	4501.2	5411.7
$\tilde{b}_1$	3093.1	3089.9	3089.8
$\tilde{b}_2$	3108.0	3111.2	3111.3
$\tilde{t}_1$	2932.3	2932.1	2932.1
$\tilde{t}_2$	3265.3	3265.5	3265.5
$\tilde{\tau}_1$	350.10	350.10	350.10
$\tilde{\tau}_2$	443.35	453.37	452.59
$\tilde{g}$	3193.7	3193.7	3193.7
$\tilde{\chi}_1^0$	350.00	350.00	350.00
$\tilde{\chi}_2^0$	418.18	485.45	485.76
$\tilde{\chi}_3^0$	-440.50	722.15	735.99
$\tilde{\chi}_4^0$	502.72	-731.60	-746.16
$\tilde{\chi}_5^0$	1035.9	1040.8	1041.8
$\tilde{\chi}_1^\pm$	433.78	719.76	733.82
$\tilde{\chi}_2^\pm$	1035.9	1040.8	1041.8
$\Omega_{\tilde{\chi}_1^0} h^2$	0.12306	0.11354	0.11509
$\sigma_{\text{SI}}[\text{cm}^2]$	$4.3172 \times 10^{-51}$	$8.6107 \times 10^{-52}$	$6.0035 \times 10^{-51}$
$\delta a_\mu$	$1.1604 \times 10^{-9} (2\sigma)$	$9.0488 \times 10^{-10} (3\sigma)$	$8.9167 \times 10^{-10} (3\sigma)$
$\text{Br}(B_s^0 \rightarrow \mu^+ \mu^-)$	$3.4352 \times 10^{-9} (1\sigma)$	$3.4450 \times 10^{-9} (1\sigma)$	$3.4727 \times 10^{-9} (1\sigma)$
$\text{Br}(b \rightarrow s\gamma)$	$3.0310 \times 10^{-4} (2\sigma)$	$3.0086 \times 10^{-4} (3\sigma)$	$3.0029 \times 10^{-4} (3\sigma)$

Assumption:

$$m_{Q_{1,2}} = m_{Q_3}, \quad m_{U_{1,2}} = m_{U_3}, \quad m_{D_{1,2}} = m_{D_3},$$

$$m_{L_{1,2}} = m_{L_3}, \quad m_{E_{1,2}} = m_{E_3},$$

$$M_1 = M_2/2, \quad M_3 = 3M_2, \quad A_{e,\mu} = A_\tau$$



... suitable  $m_h$  and  $\Omega_{\text{DM}} h^2$  are obtained.

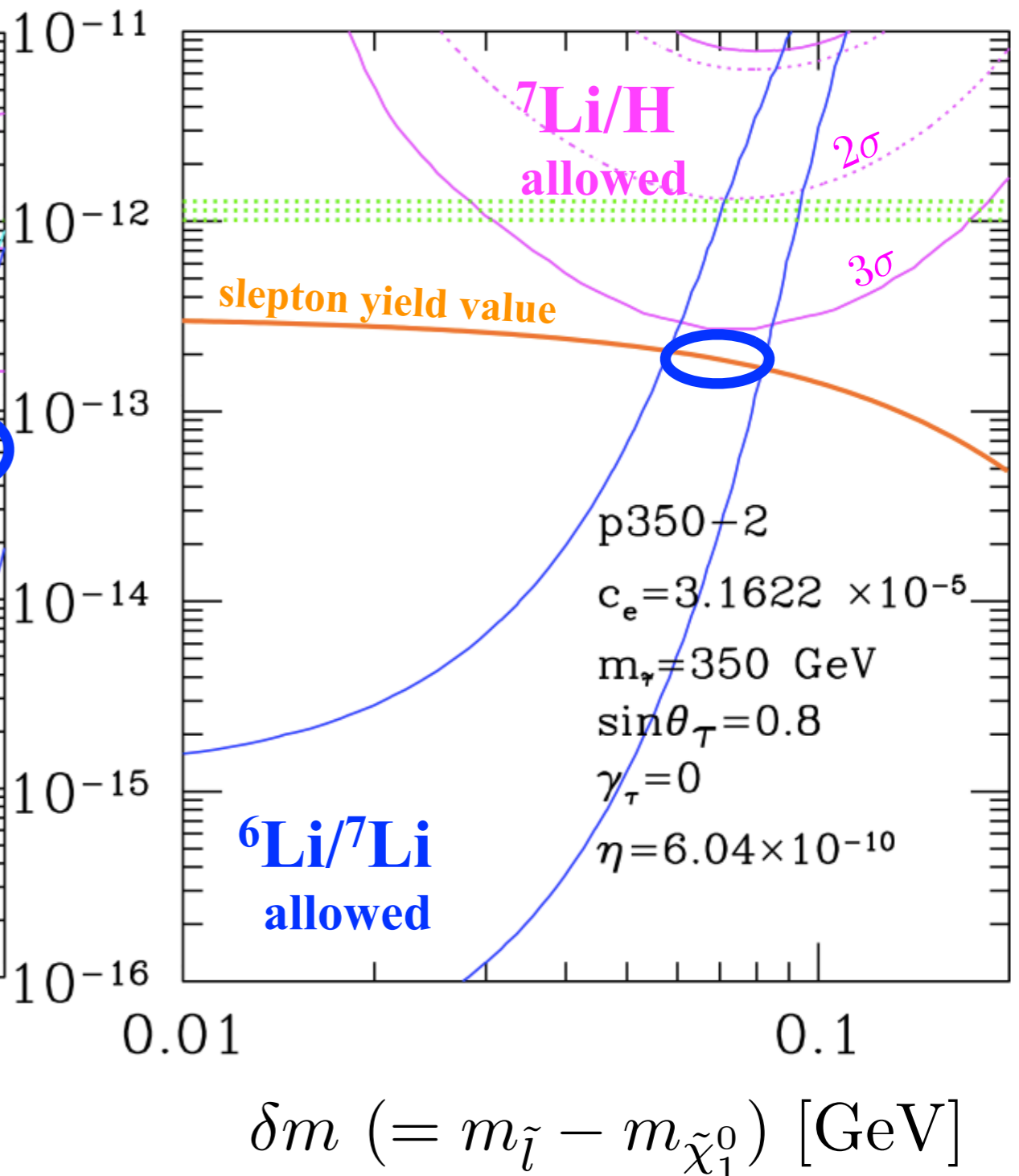
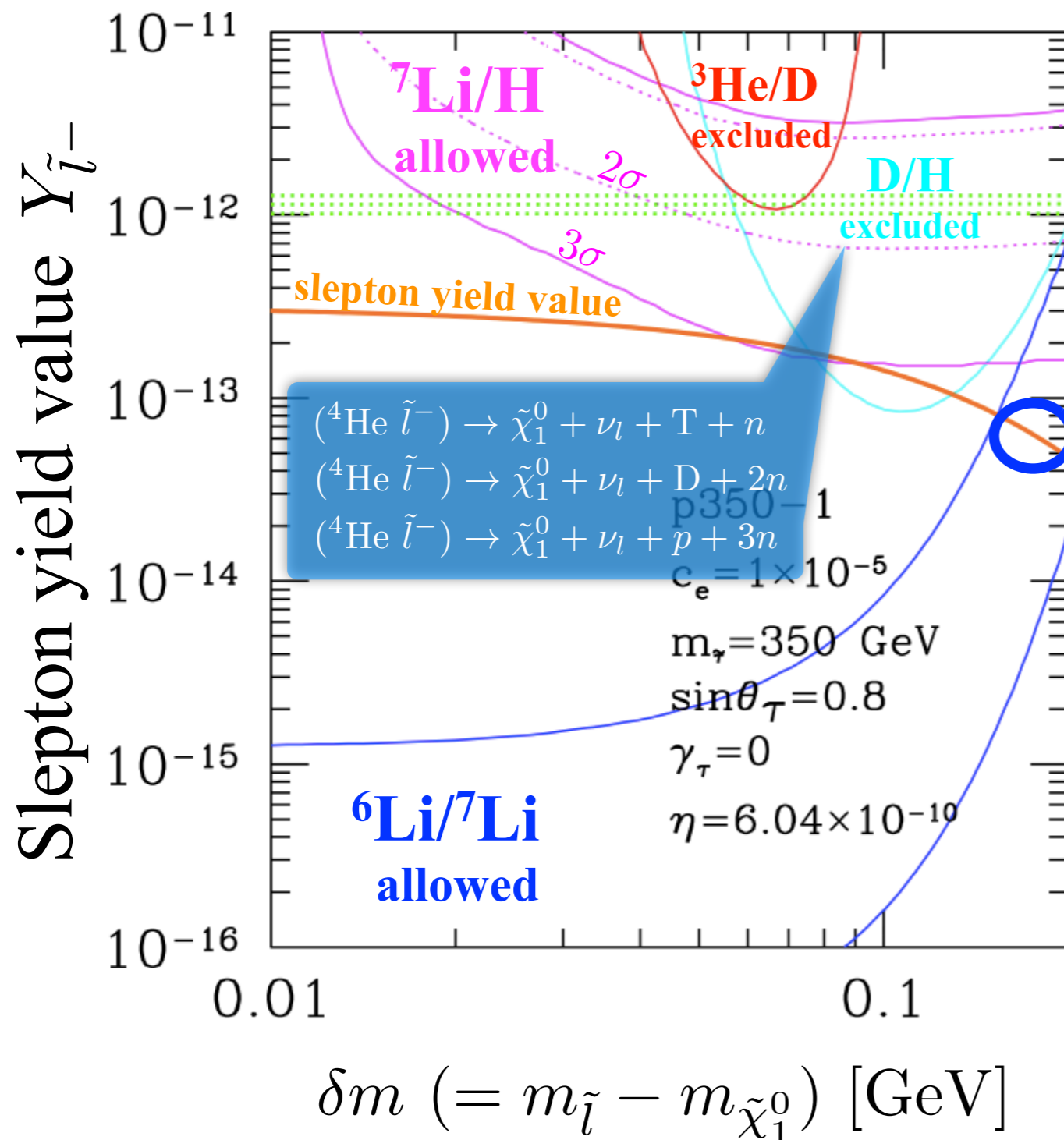
realized by large 1-loop contribution  
(same as MSSM)

\*NMSSMTools ver.4.1.1, \*GeV

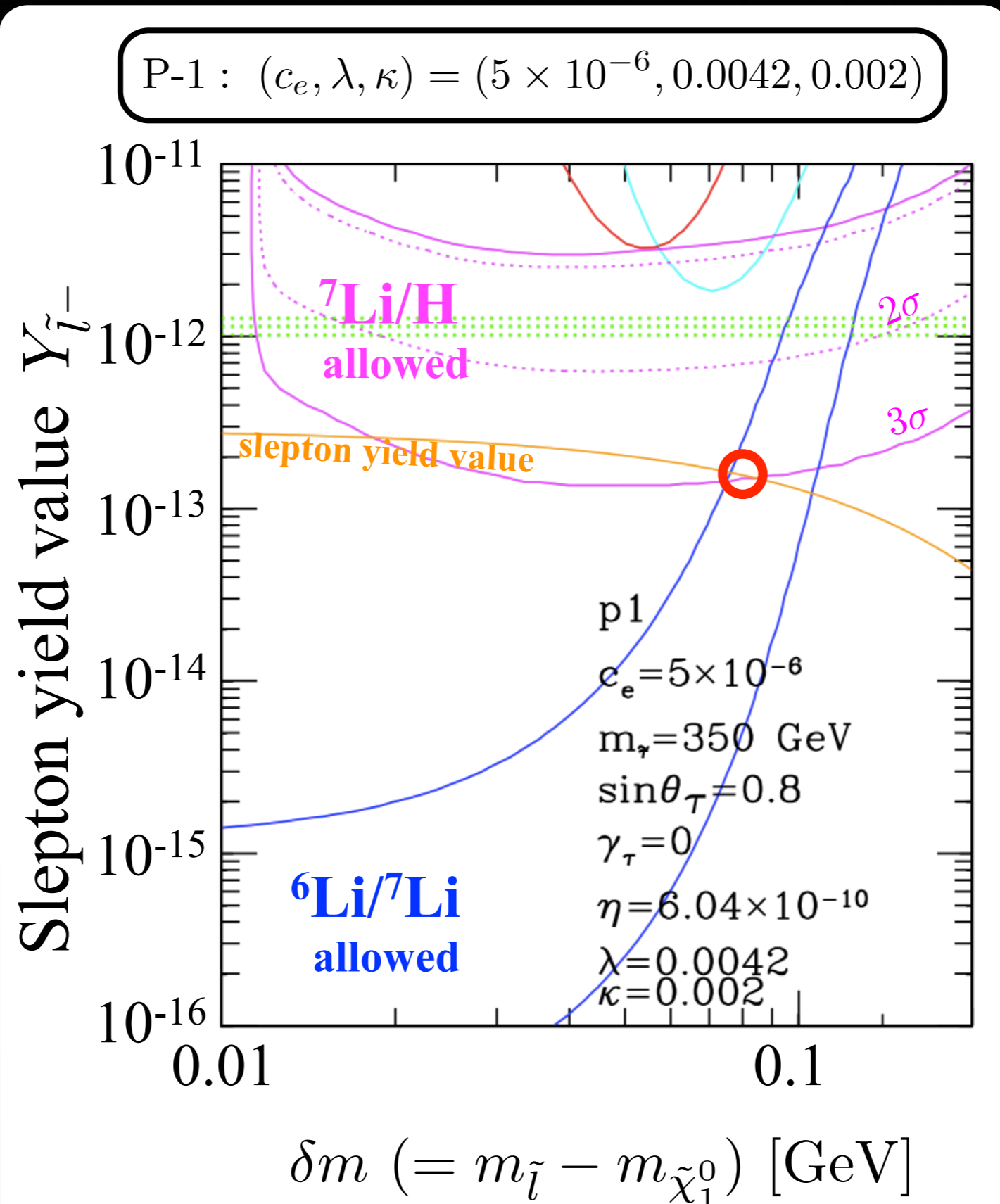
# 3. Results of BBN calculation

PS-1 :  $(c_e, \lambda, \kappa) = (10^{-5}, 0.005, 0.002)$

PS-2 :  $(c_e, \lambda, \kappa) = (10^{-4.5}, 0.005, 0.002)$



# 3. Results of BBN calculation

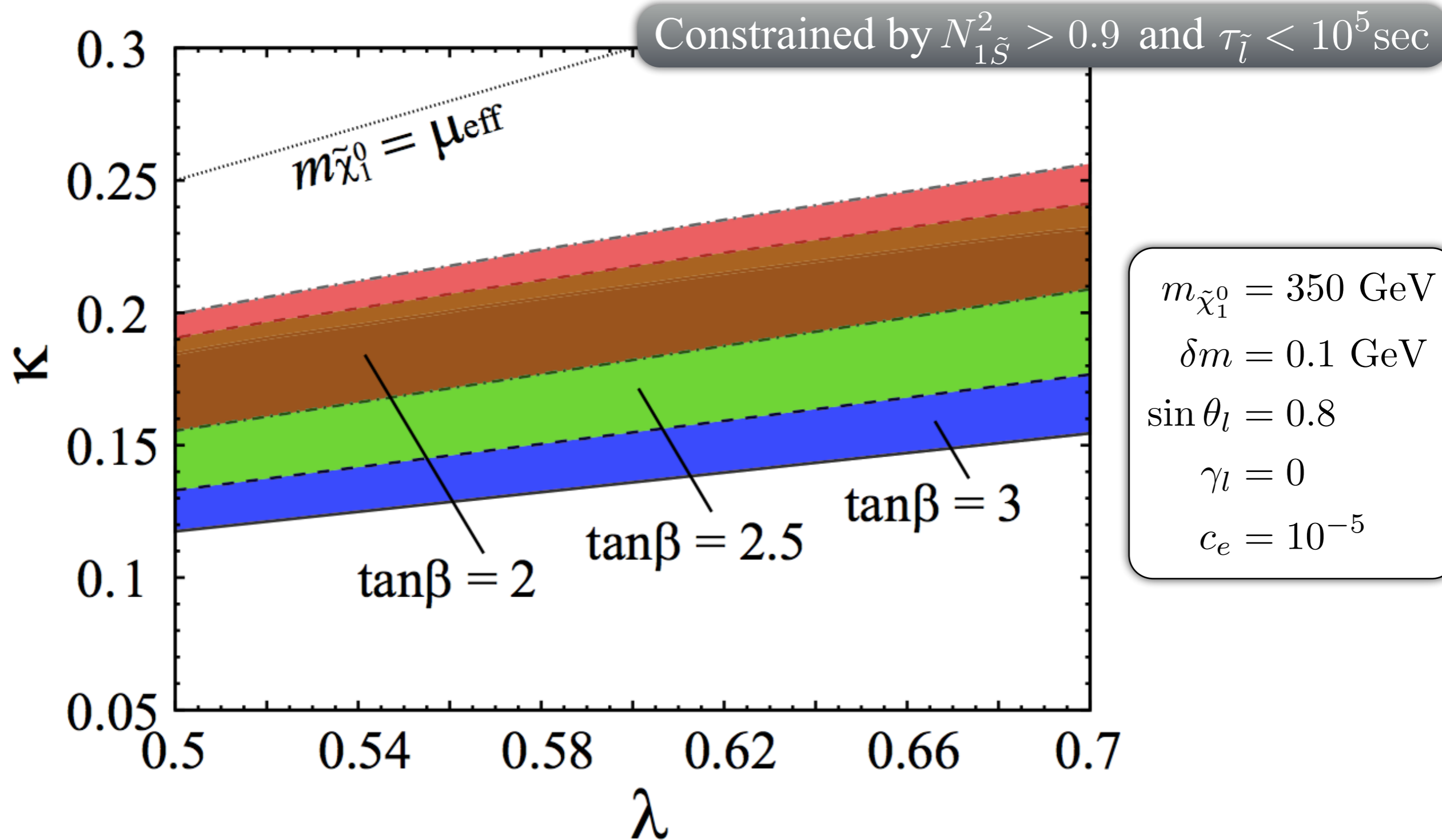




# Results

Case 2. Singlino-like LSP, large  $\lambda$ - $\kappa$  region

# 1. The region allowed from theoretical constraints



# 2. The points which satisfy phenomenological constraints

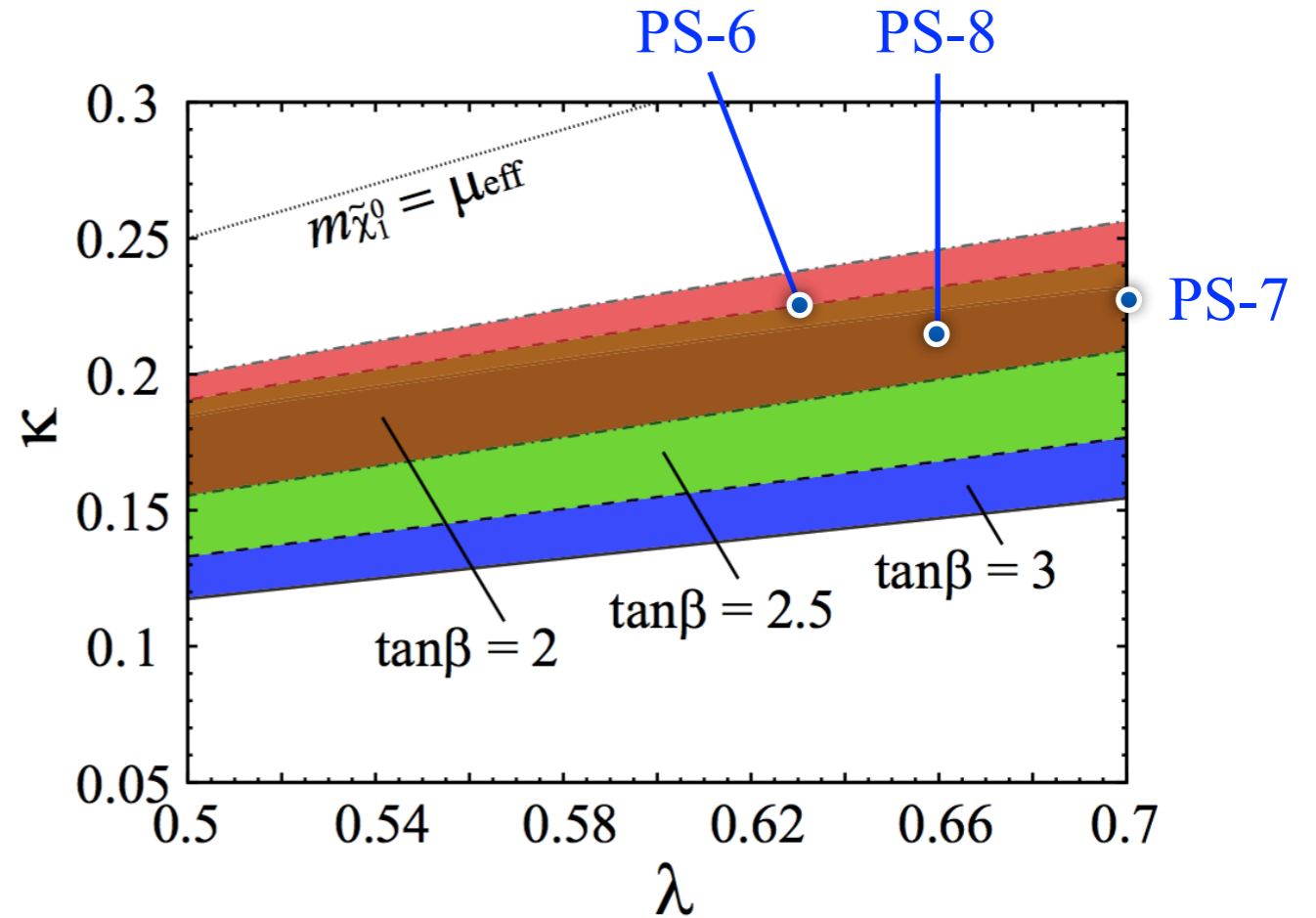
Input	PS-5, PS-6	PS-7	PS-8
$M_2$	1000.0	1000.0	1000.0
$A_t$	-1500.0	-1500.0	-1500.0
$A_\tau$	-1500.0	-1500.0	-1500.0
$m_{\tilde{L}_3}$	356.97	357.38	357.40
$m_{\tilde{E}_3}$	353.31	353.53	353.55
$m_{\tilde{Q}_3}$	1000.0	1000.0	1000.0
$m_{\tilde{U}_3}$	1000.0	1000.0	1000.0
$m_{\tilde{D}_3}$	1000.0	1000.0	1000.0
$\lambda$	0.6300	0.7000	0.6600
$\kappa$	0.2300	0.2300	0.2150
$A_\lambda$	1050.0	1080.0	1150.0
$A_\kappa$	-10.000	-50.000	-100.00
$\mu_{\text{eff}}$	479.78	527.45	531.54
$\tan\beta$	2.5000	2.5000	2.5000
Output			
$h_1^0$	124.33	126.41	125.95
$h_2^0$	365.73	361.55	347.64
$h_3^0$	1306.0	1384.4	1428.4
$a_1^0$	142.35	204.78	256.15
$a_2^0$	1304.6	1383.5	1427.5
$H^\pm$	1299.0	1375.8	1420.7
$\tilde{b}_1$	822.97	822.79	822.77
$\tilde{b}_2$	830.40	830.58	830.60
$\tilde{t}_1$	703.40	701.86	701.68
$\tilde{t}_2$	953.20	954.76	954.89
$\tilde{\tau}_1$	350.10	350.10	350.10
$\tilde{\tau}_2$	364.09	364.70	364.75
$\tilde{g}$	2881.7	2881.7	2881.7
$\tilde{\chi}_1^0$	350.00	350.00	350.00
$\tilde{\chi}_2^0$	456.22	472.39	472.62
$\tilde{\chi}_3^0$	-498.62	-548.29	-550.81
$\tilde{\chi}_4^0$	528.51	556.97	558.88
$\tilde{\chi}_5^0$	1011.7	1013.2	1013.4
$\tilde{\chi}_1^\pm$	476.01	522.67	526.66
$\tilde{\chi}_2^\pm$	1011.7	1013.1	1013.3
$\Omega_{\tilde{\chi}_1^0} h^2$	0.11220	0.11939	0.12643
$\sigma_{\text{SI}} [\text{cm}^2]$	$3.3230 \times 10^{-45}$	$1.9286 \times 10^{-45}$	$6.6097 \times 10^{-46}$
$\delta a_\mu$	$1.2586 \times 10^{-10} (> 3\sigma)$	$1.2364 \times 10^{-10} (> 3\sigma)$	$1.2299 \times 10^{-10} (> 3\sigma)$
$\text{Br}(B_s^0 \rightarrow \mu^+ \mu^-)$	$3.5365 \times 10^{-9} (1\sigma)$	$3.5368 \times 10^{-9} (1\sigma)$	$3.5370 \times 10^{-9} (1\sigma)$
$\text{Br}(b \rightarrow s\gamma)$	$3.1812 \times 10^{-4} (2\sigma)$	$3.1743 \times 10^{-4} (2\sigma)$	$3.1677 \times 10^{-4} (2\sigma)$

Assumption:

$$m_{Q_{1,2}} = m_{Q_3}, m_{U_{1,2}} = m_{U_3}, m_{D_{1,2}} = m_{D_3},$$

$$m_{L_{1,2}} = m_{L_3}, m_{E_{1,2}} = m_{E_3},$$

$$M_1 = M_2/2, M_3 = 3M_2, A_{e,\mu} = A_\tau$$



... suitable  $m_h$  and  $\Omega_{\text{DM}} h^2$  are obtained.

realized by large tree contribution  
(different from MSSM)

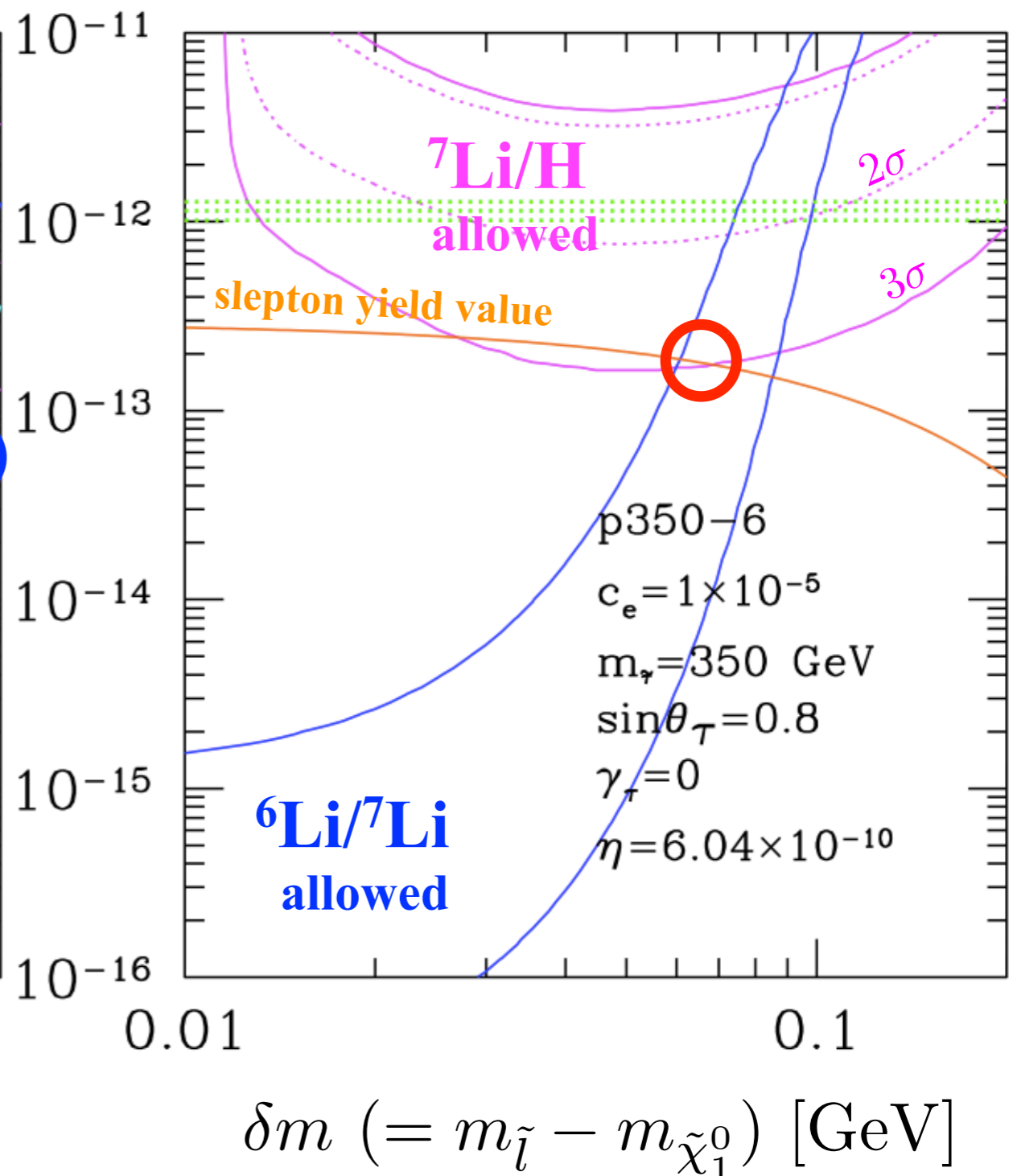
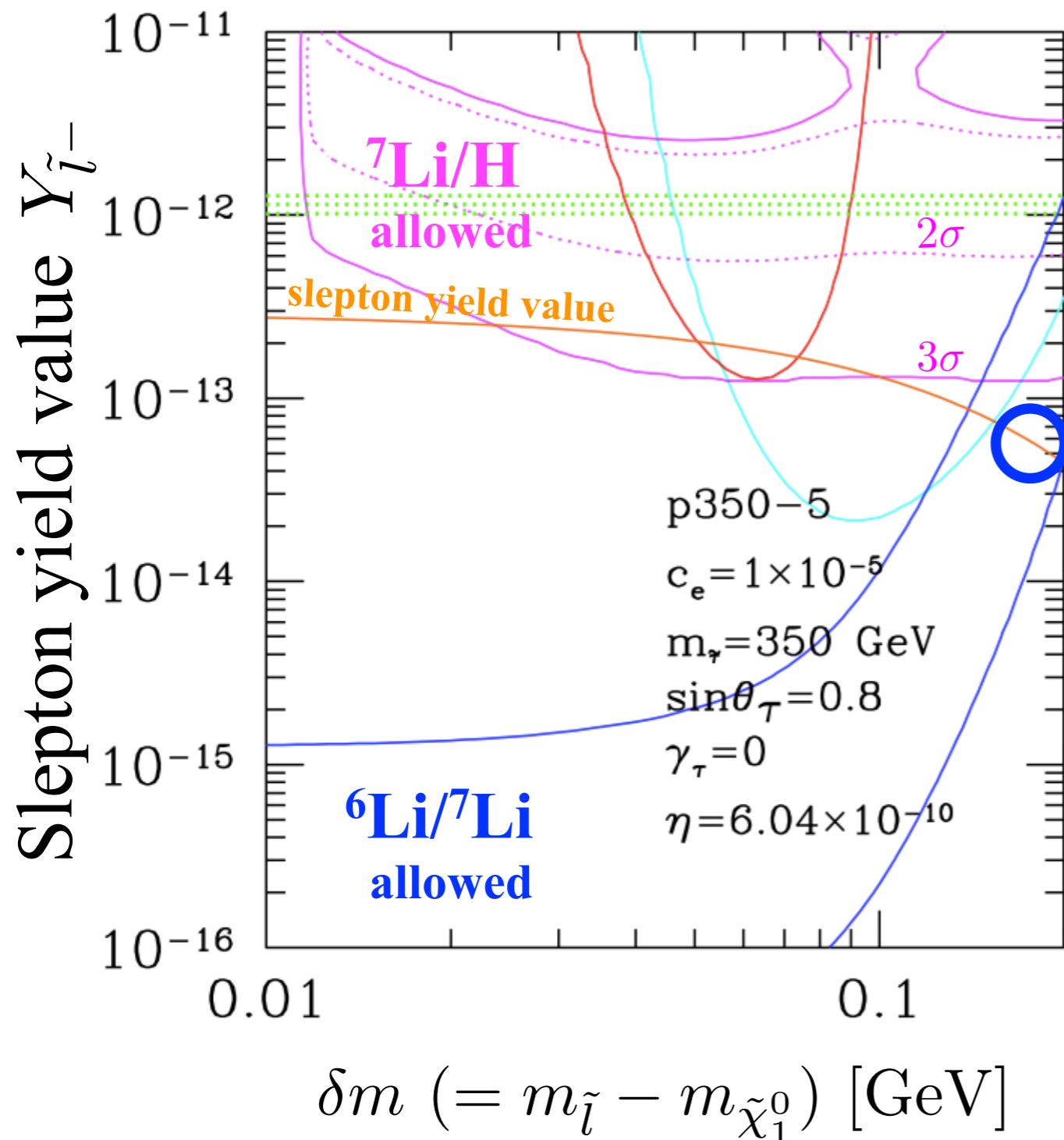
\*NMSSMTools ver.4.1.1, \*GeV



# 3. Results of BBN calculation

PS-5 :  $(c_e, \lambda, \kappa) = (10^{-5.5}, 0.63, 0.23)$

PS-6 :  $(c_e, \lambda, \kappa) = (10^{-5}, 0.63, 0.23)$



# Results

Case 3. Bino-like LSP, large  $\lambda$ - $\kappa$  region

# Results

## Case 3. Bino-like LSP, large $\lambda$ - $\kappa$ region

- ✓  $G_{L1}$  and  $G_{R1}$  are almost independent from  $\lambda$ ,  $\kappa$ , and  $\tan \beta$ .
- ✓ We choose points at which suitable DM relic density and the Higgs boson mass without taking the theoretical conditions into account.



# 2. The points which satisfy phenomenological constraints

Input	PB-1	PB-2	PB-3	PB-4
$M_2$	713.14	713.25	713.36	712.97
$A_t$	-1500.0	-1500.0	-1500.0	-1500.0
$A_\tau$	-1500.0	-1500.0	-1500.0	-1500.0
$m_{\tilde{L}_3}$	359.32	359.32	359.32	359.32
$m_{\tilde{E}_3}$	354.76	354.76	354.76	354.76
$m_{\tilde{Q}_3}$	1000.0	1000.0	1000.0	1000.0
$m_{\tilde{U}_3}$	1000.0	1000.0	1000.0	1000.0
$m_{\tilde{D}_3}$	1000.0	1000.0	1000.0	1000.0
$\lambda$	0.6000	0.6800	0.6800	0.6000
$\kappa$	0.2000	0.2000	0.3200	0.3200
$A_\lambda$	1500.0	1480.0	1000.0	1500.0
$A_\kappa$	-100.00	-100.00	-100.00	-100.00
$\mu_{\text{eff}}$	900.00	900.00	900.00	900.00
$\tan\beta$	2.0000	2.0000	2.0000	2.0000
Output				
$h_1^0$	124.19	126.51	125.23	124.35
$h_2^0$	609.68	552.89	844.57	960.06
$h_3^0$	2014.2	1983.6	1793.5	2115.8
$a_1^0$	304.76	289.22	372.60	379.68
$a_2^0$	2014.3	1983.7	1792.3	2114.5
$H^\pm$	2007.0	1974.3	1783.8	2108.5
$\tilde{b}_1$	988.74	988.71	988.67	988.80
$\tilde{b}_2$	996.89	996.85	996.82	996.95
$\tilde{t}_1$	853.45	853.41	853.37	853.51
$\tilde{t}_2$	1132.2	1132.1	1132.1	1132.2
$\tilde{\tau}_1$	350.10	350.10	350.10	350.10
$\tilde{\tau}_2$	367.13	367.13	367.13	367.13
$\tilde{g}$	2068.2	2068.5	2068.8	2067.7
$\tilde{\chi}_1^0$	350.00	350.00	350.00	350.00
$\tilde{\chi}_2^0$	602.38	534.28	696.36	697.51
$\tilde{\chi}_3^0$	699.76	699.36	842.69	-906.34
$\tilde{\chi}_4^0$	-907.56	-909.78	-908.00	914.24
$\tilde{\chi}_5^0$	934.51	934.66	944.68	984.08
$\tilde{\chi}_1^\pm$	697.54	697.56	697.21	697.60
$\tilde{\chi}_2^\pm$	929.52	929.50	929.28	929.61
$\Omega_{\tilde{\chi}_1^0} h^2$	0.11964	0.11964	0.11956	0.11968
$\sigma_{\text{SI}}[\text{cm}^2]$	$7.7946 \times 10^{-46}$	$7.5748 \times 10^{-46}$	$7.3740 \times 10^{-46}$	$7.4233 \times 10^{-46}$
$\delta a_\mu$	$1.3321 \times 10^{-10} (> 3\sigma)$	$1.3370 \times 10^{-10} (> 3\sigma)$	$1.3398 \times 10^{-10} (> 3\sigma)$	$1.3296 \times 10^{-10} (> 3\sigma)$
$\text{Br}(B_s^0 \rightarrow \mu^+ \mu^-)$	$3.5382 \times 10^{-9} (1\sigma)$	$3.5382 \times 10^{-9} (1\sigma)$	$3.5381 \times 10^{-9} (1\sigma)$	$3.5383 \times 10^{-9} (1\sigma)$
$\text{Br}(b \rightarrow s\gamma)$	$3.1732 \times 10^{-4} (2\sigma)$	$3.1754 \times 10^{-4} (2\sigma)$	$3.1907 \times 10^{-4} (2\sigma)$	$3.1668 \times 10^{-4} (2\sigma)$

Assumption:

$$m_{Q_{1,2}} = m_{Q_3}, m_{U_{1,2}} = m_{U_3}, m_{D_{1,2}} = m_{D_3},$$

$$m_{L_{1,2}} = m_{L_3}, m_{E_{1,2}} = m_{E_3},$$

$$M_1 = M_2/2, M_3 = 3M_2, A_{e,\mu} = A_\tau$$

Parameters	PB-1	PB-2	PB-3	PB-4
$c_e$	0	0	0	0
$\lambda$	0.6	0.68	0.68	0.6
$\kappa$	0.2	0.2	0.32	0.32

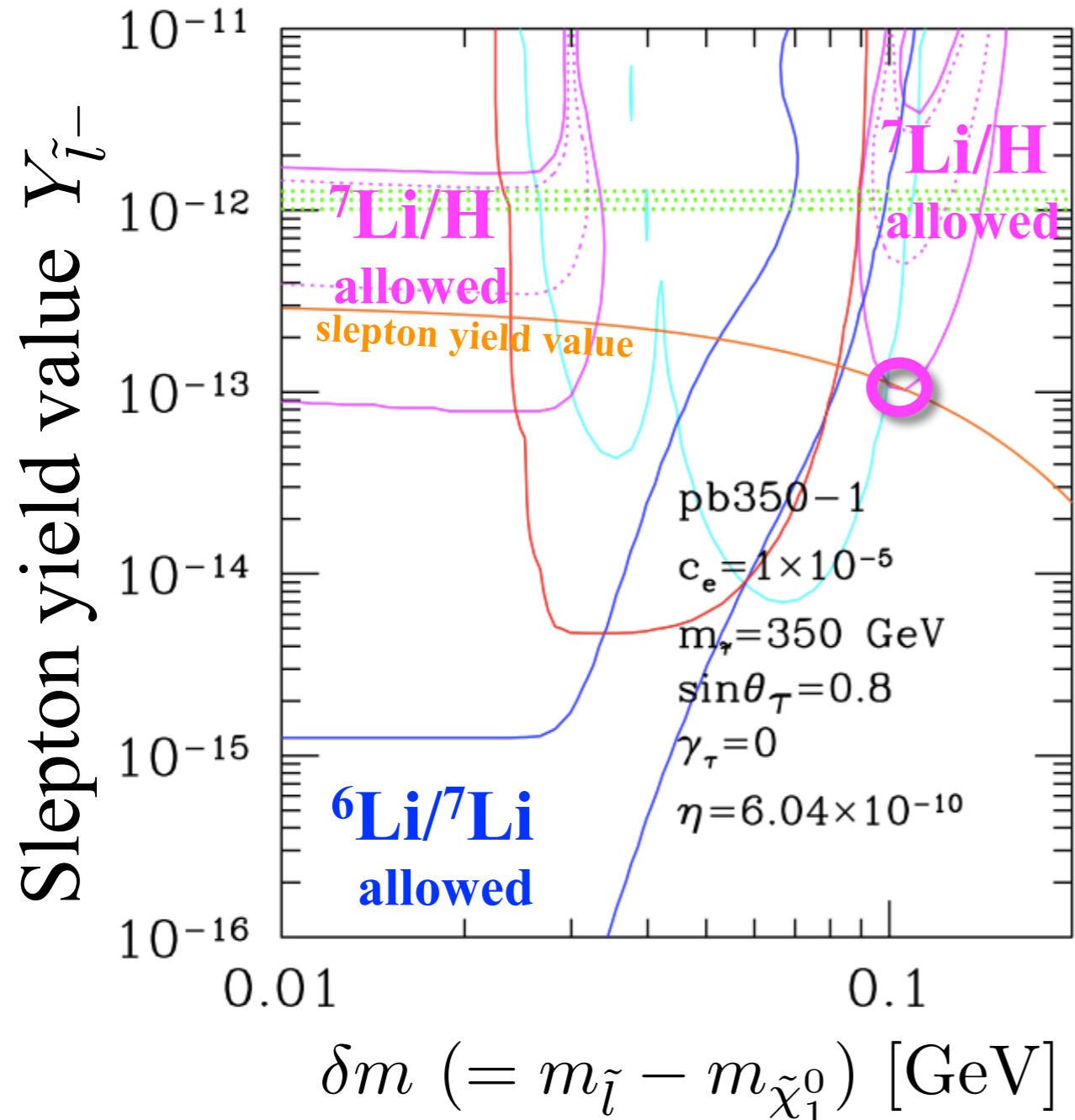
... suitable  $m_h$  and  $\Omega_{\text{DM}} h^2$  are obtained.

realized by large tree contribution  
(different from MSSM)

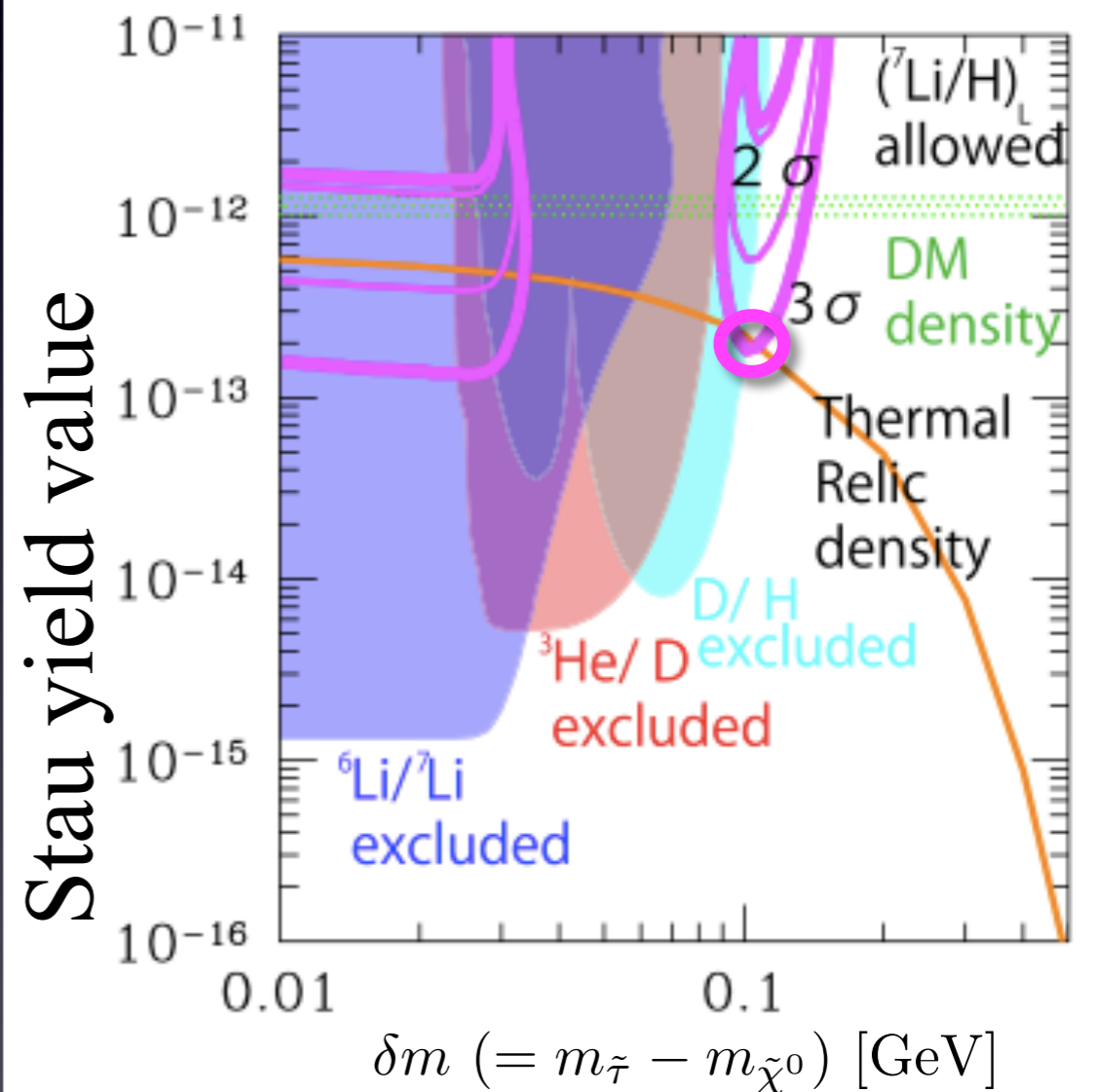
\*NMSSMTools ver.4.1.1, \*GeV

# 3. Results of BBN calculation

PB-1 :  $(c_e, \lambda, \kappa) = (0, 0.6, 0.2)$



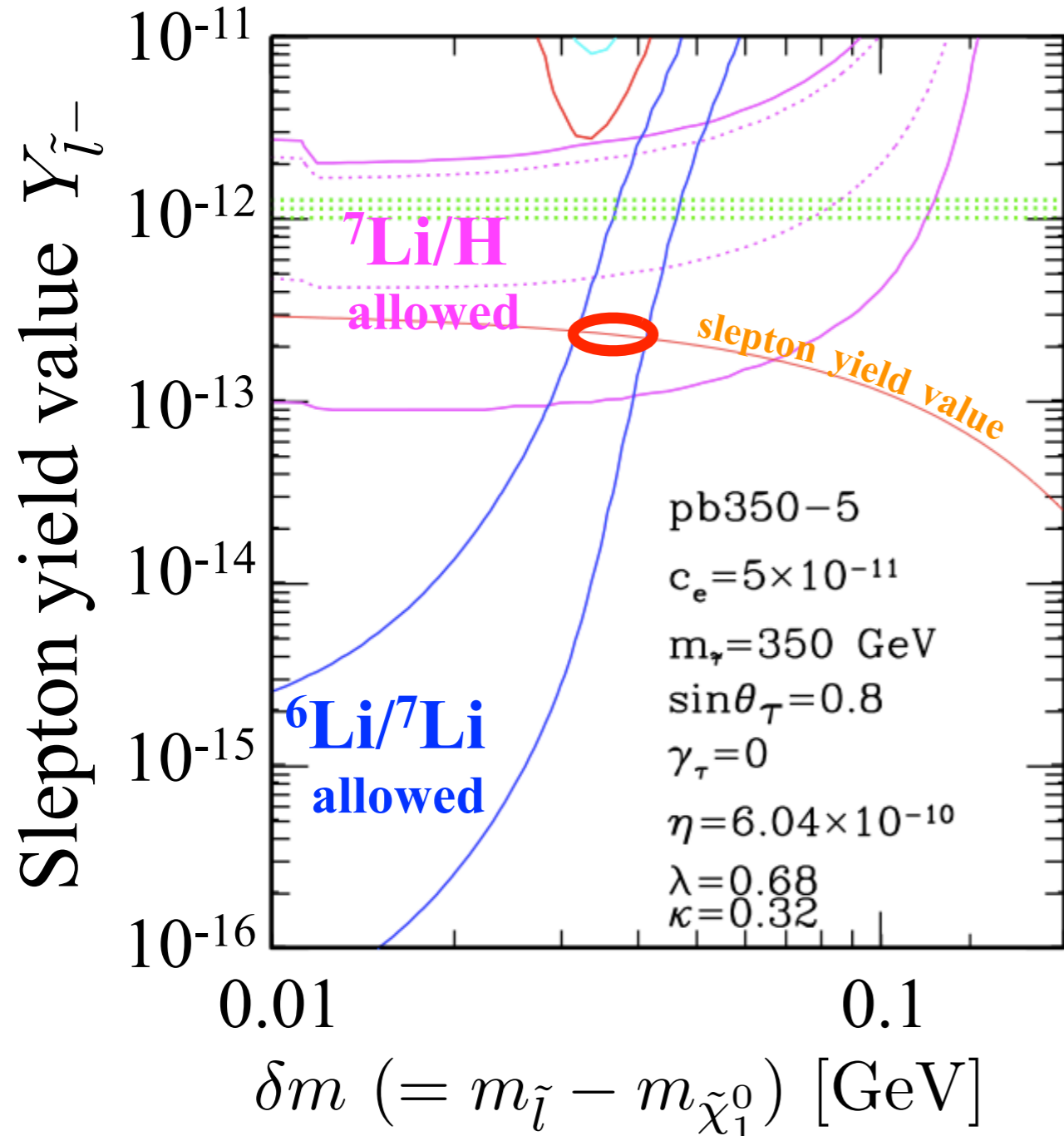
← NMSSM  
 ↓ MSSM



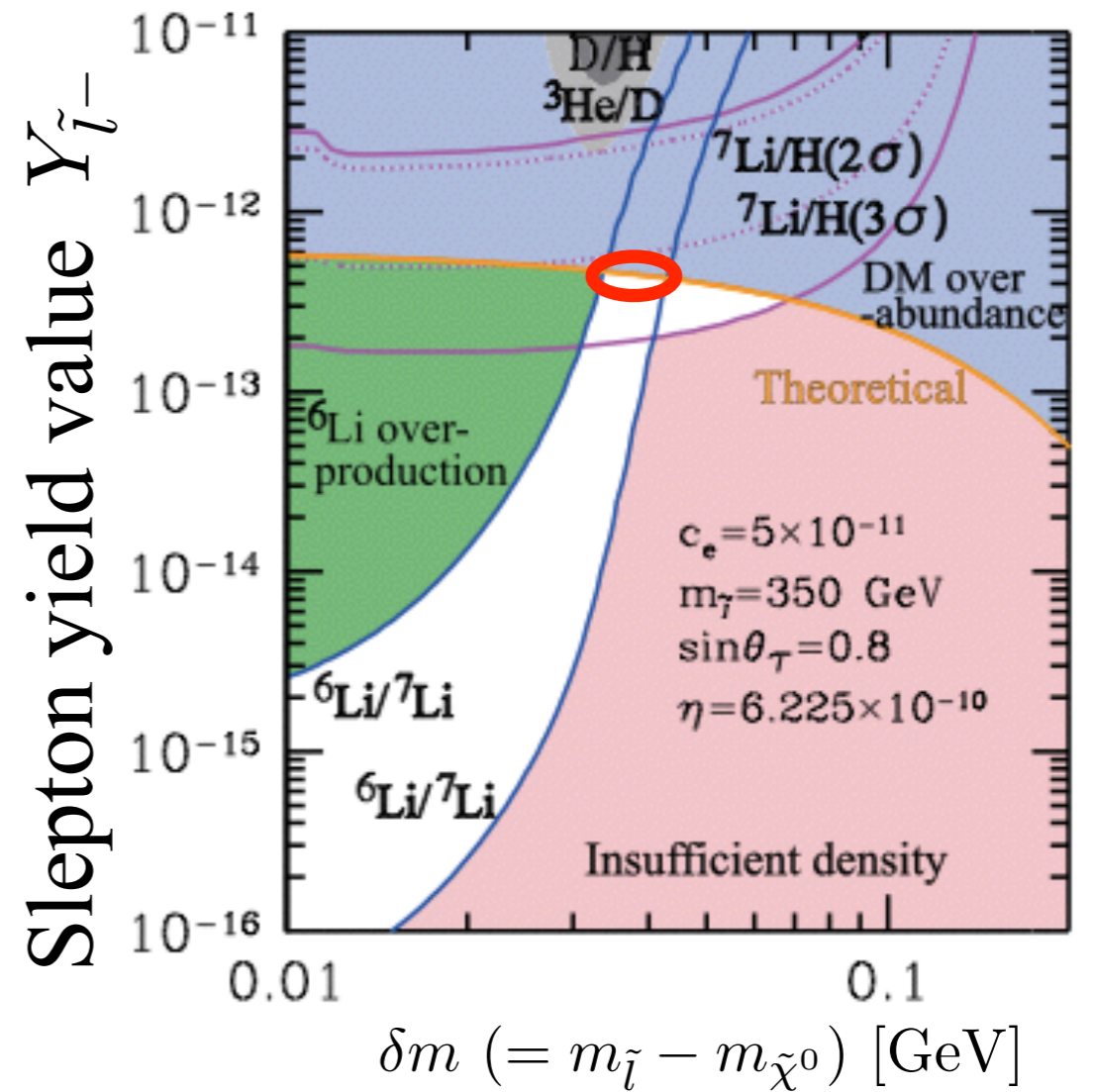
T. Jittoh et al., PRD 84, 035008 (2011)

# 3. Results of BBN calculation

PB-5 :  $(c_e, \lambda, \kappa) = (5 \times 10^{-11}, 0.68, 0.32)$



← NMSSM  
 ↓ MSSSM



K. Kohri et al., PRD86, 095024 (2012)



# Summary

## > Motivation

### MSSM

- ✓ Light element abundances
- ✓ Dark Matter relic density



### NMSSM

- ✓ Light element abundances
- ✓ Dark Matter relic density
- ✓ Higgs boson mass

## > Strategy

- ✓ Search for allowed region on  $\lambda$ - $\kappa$  plane  
(theoretical constraints;  $\tau_{\tilde{l}}$ ,  $\tau_{IC}$ , and  $N_{1\tilde{S}}^2(N_{1\tilde{B}}^2)$ )
- ✓ Select several points allowed from phenomenology ( $\Omega_{\tilde{\chi}_1^0} h^2$  and  $m_h$ )
- ✓ Confirm the points to give suitable light element abundances

## > Results

We have found several points where suitable light element abundances (including  ${}^7\text{Li}$  and  ${}^6\text{Li}$ ), DM relic density, and Higgs boson mass are obtained;

- (1) Singlino-like neutralino LSP, small  $\lambda$ - $\kappa$  ,
- (2) Singlino-like neutralino LSP, large  $\lambda$ - $\kappa$  ,
- (3) Bino-like neutralino LSP, large  $\lambda$ - $\kappa$  .

Backup

# Bing-Bang Nucleosynthesis (BBN)

... primordial synthesis of light elements nuclei.

$$T \sim (1 - 0.01)\text{MeV} \Leftrightarrow t \sim (1 - 10^3)\text{sec}$$

## Standard BBN theory

... based on the SM

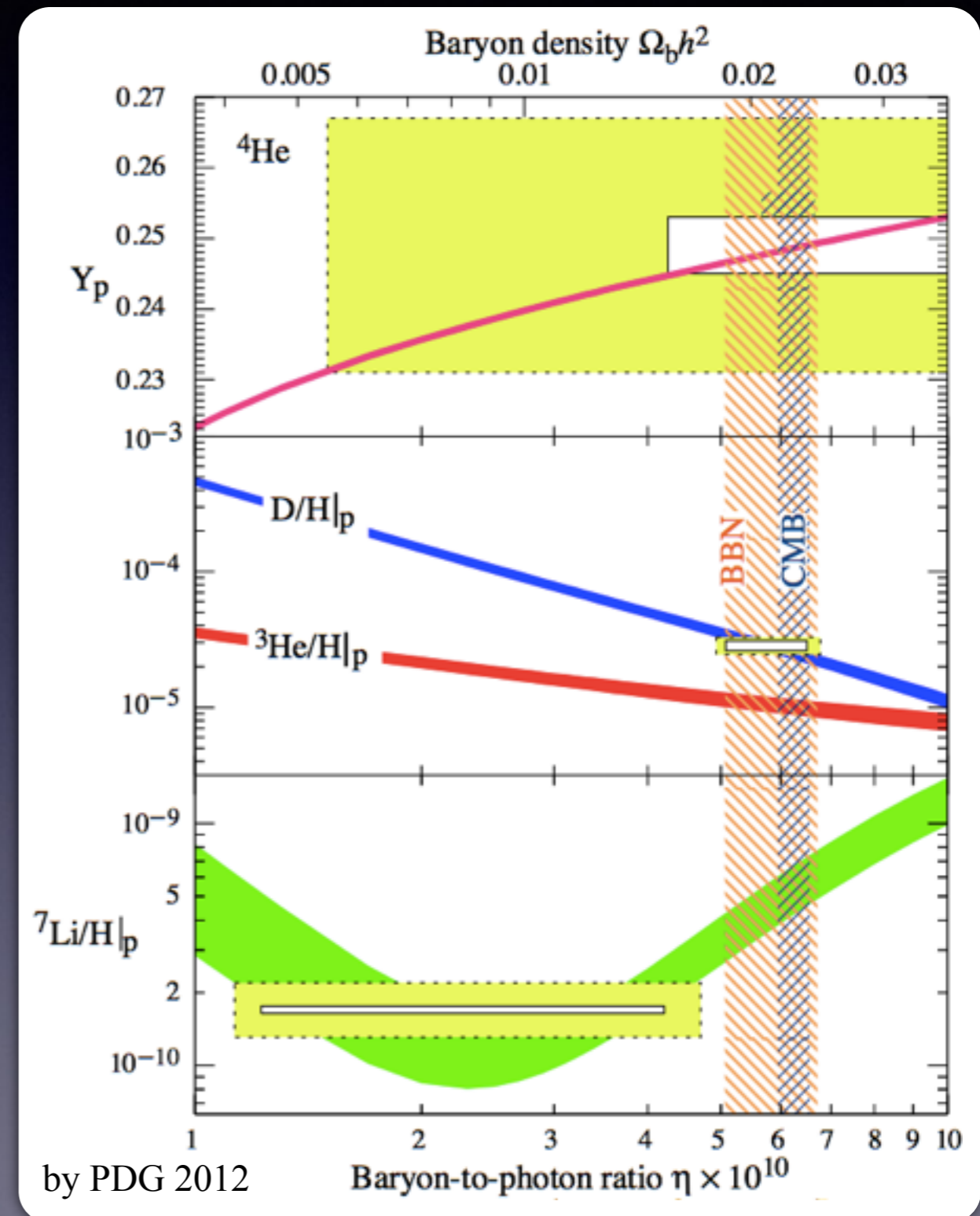
✓ Predicts light element abundances from only one parameter,  $\eta$ .

$$\eta \equiv \frac{n_{\text{baryon}}}{n_{\text{photon}}} = (6.225 \pm 0.170) \times 10^{-10}$$

WMAP9 result

✓ Consistent predictions with obs. in most species of light elements.

D,  $^4\text{He}$  → OK!





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### Lithium problems

#### ✓ Lithium-7 ( ${}^7\text{Li}$ ) problem

theory  $>$  observation

$$\log_{10}({}^7\text{Li}/\text{H}) : -9.35 \pm 0.006 \quad -9.63 \pm 0.06$$

T. Jittoh et al., PRD 84, 035008 (2011),

J. Melendez and I. Ramirez, Astrophys. J. 615, L33 (2004)

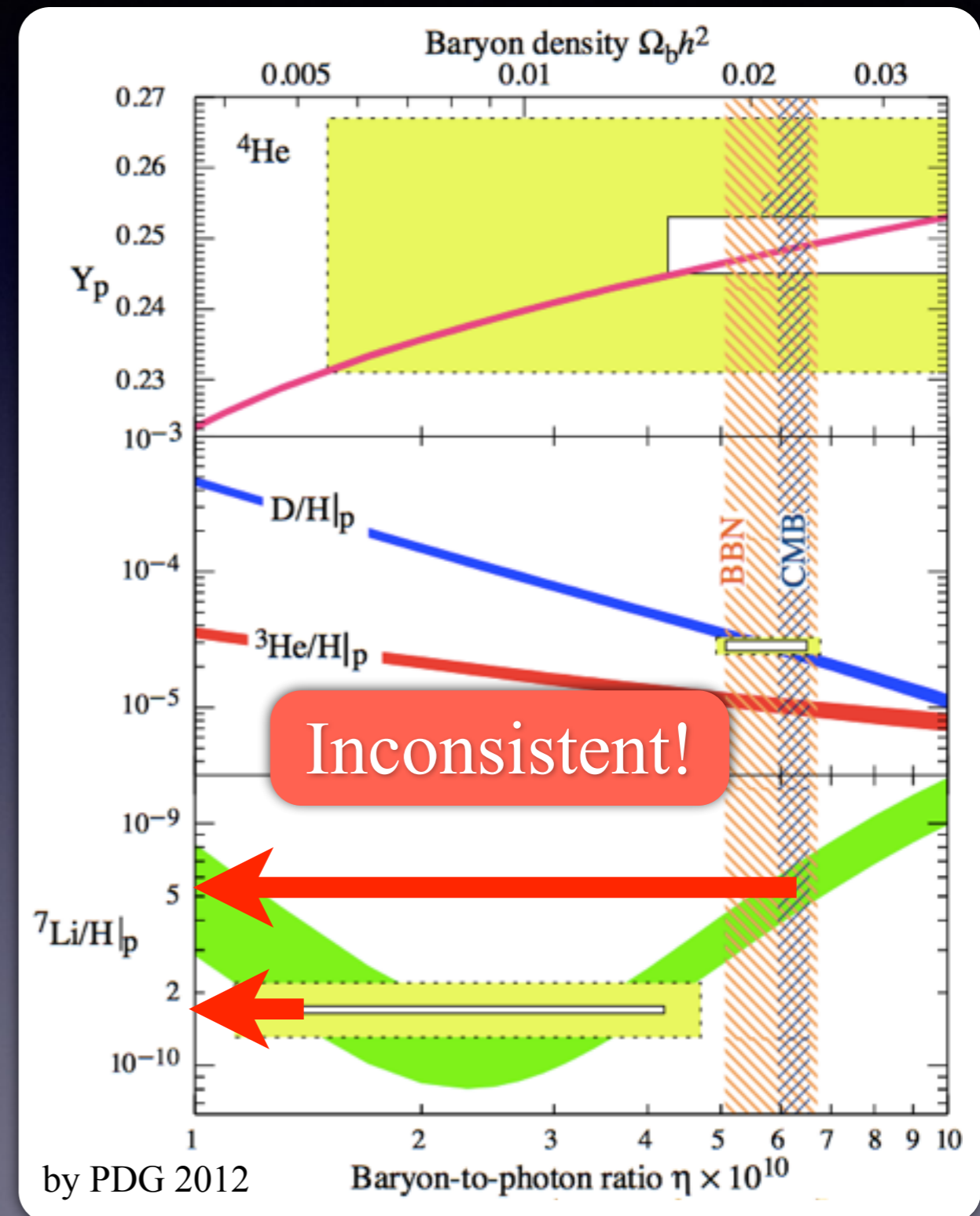
#### ✓ Lithium-6 ( ${}^6\text{Li}$ ) problem

theory  $<$  observation

$${}^6\text{Li}/{}^7\text{Li} : \lesssim 10^{-4} \quad 0.046 \pm 0.022$$

Vangioni-Flam E et al., New Astron 4:245(1999)

M. Asplund et al., Astrophys. J. 644, 229 (2006)



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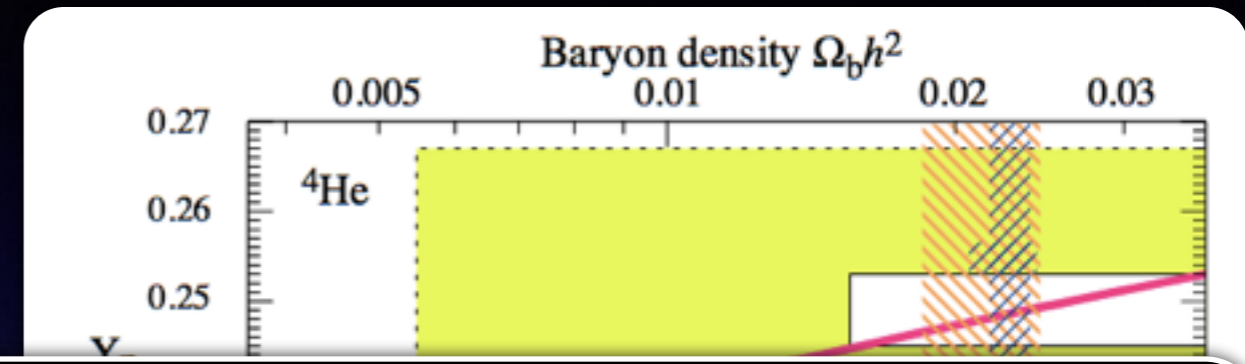
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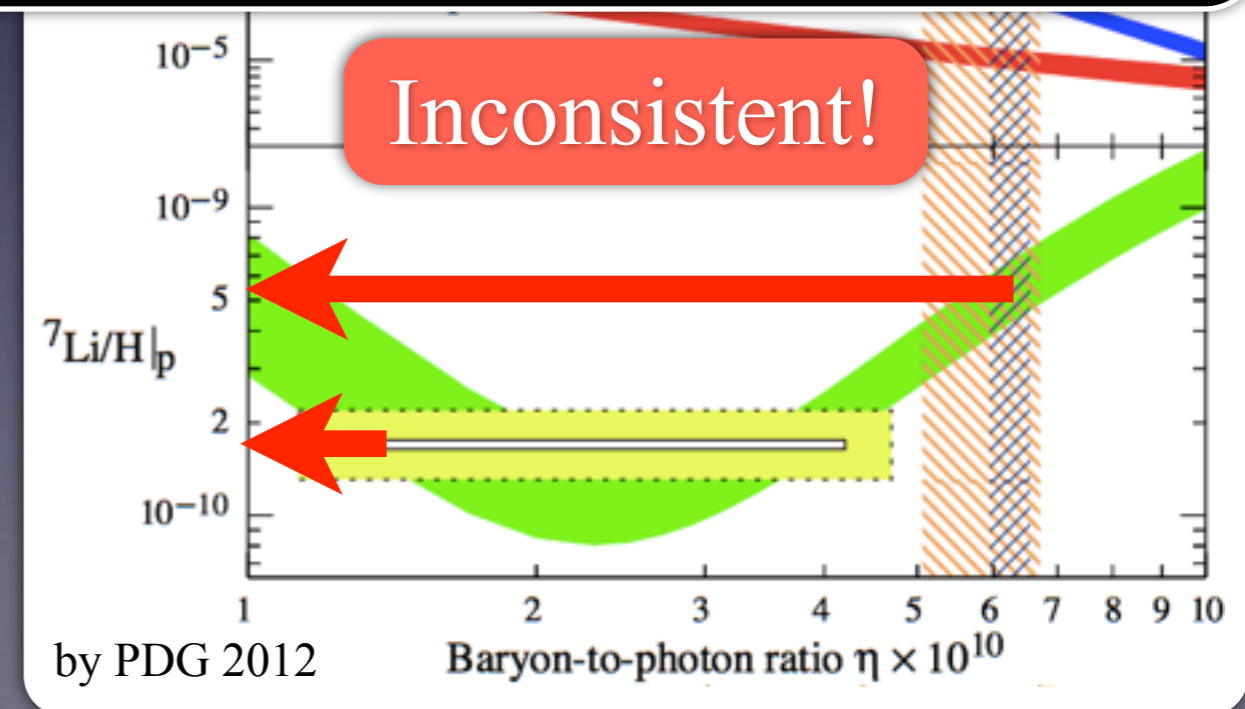
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can be solved by exotic BBN reactions



by PDG 2012



# Relic stau density at the BBN

## ■ Total number density of the SUSY particles

... annihilation and creation processes of SUSY particles,  $\tilde{\chi}^0$  and  $\tilde{\tau}$ , are frozen out at  $T_f$  ( $m_{\tilde{\chi}^0}/T_f \simeq 25$ )

→  $n_{\tilde{\chi}^0} + n_{\tilde{\tau}^\pm}$  is fixed

... this sum is the relic number density of the Dark Matter,  $n_{DM}$ .

\*all SUSY particles eventually decay into the LSP

## ■ Stau relic density

✓ **Even after the freeze out, stau number density is not yet fixed!**

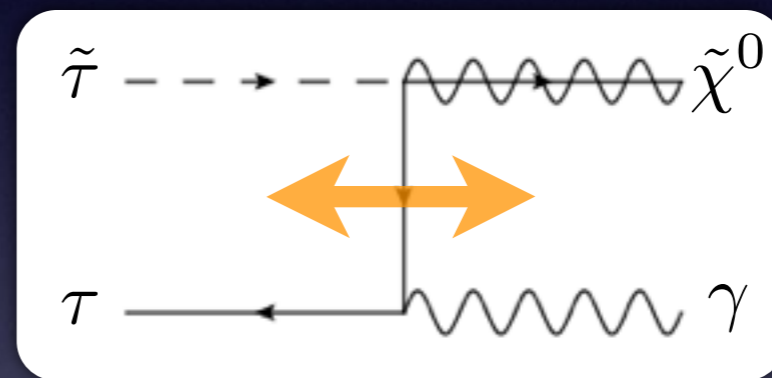
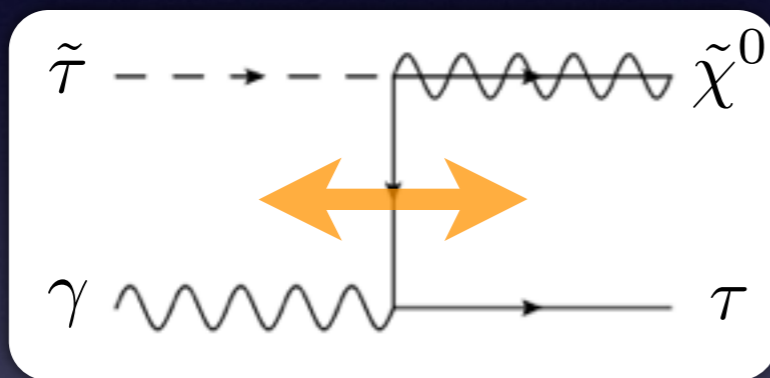
$n_{\tilde{\chi}^0}$ ,  $n_{\tilde{\tau}^-}$  and  $n_{\tilde{\tau}^+}$  are still evolving (with fixed  $n_{DM}$ ) as the temperature of the Universe drops.



# Relic stau density at the BBN

- ✦ Evolution of the stau number density until the BBN era  
... described by Boltzmann equations for the stau

> Exchange processes of  $\tilde{\tau}$  and  $\tilde{\chi}^0$



✓ In thermal equilibrium,  $Y_{\tilde{\tau}}/Y_{\tilde{\chi}^0} \sim e^{-\delta m/T}$  ( $Y_i = n_i/s$ )

✓ The exchange processes are frozen out at  $T_{f(\text{ratio})}$

... compete between the reaction rates and the Hubble expansion rate.

# Relic stau density at the BBN

- Evolution of the stau number density until the BBN era ... described by Boltzmann equations for the stau

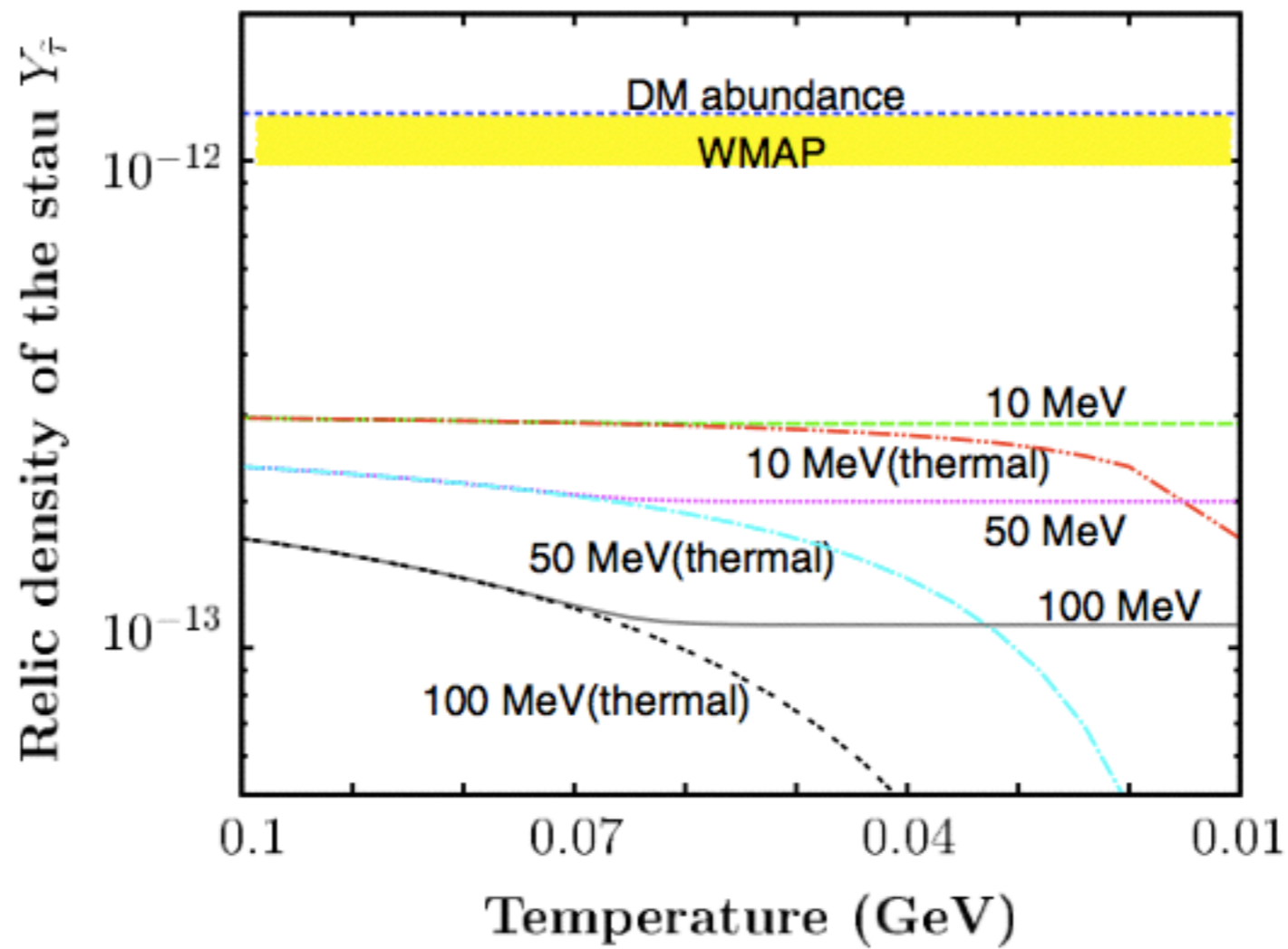
> Exchange

$\tilde{\tau}$  -  
 $\gamma$   $\sim$

✓ In therm

✓ The exch

... compe



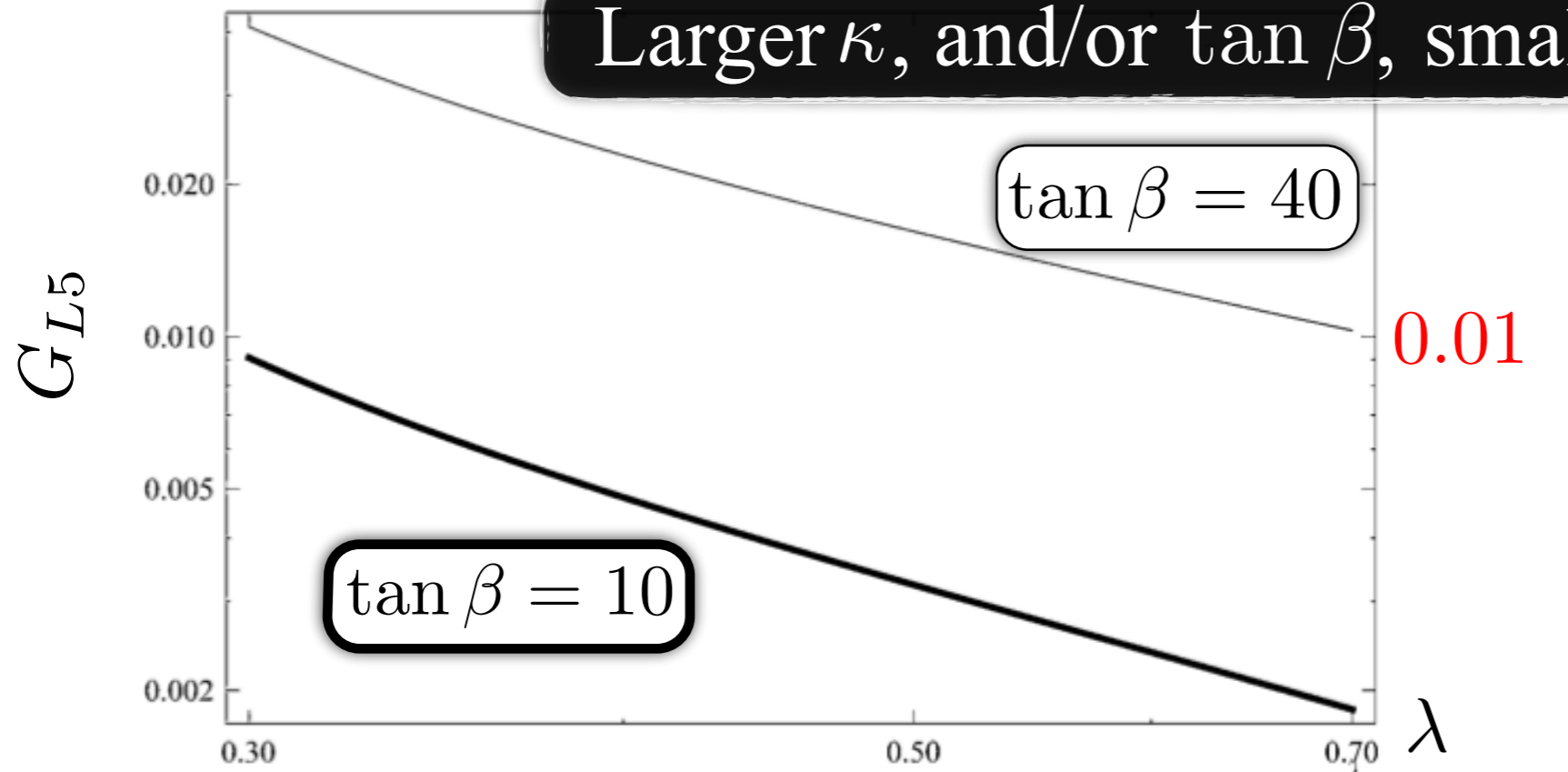
T. Jittoh et al., PRD 82, 115030 (2010)

$\tilde{\tau}$   
 $\gamma$

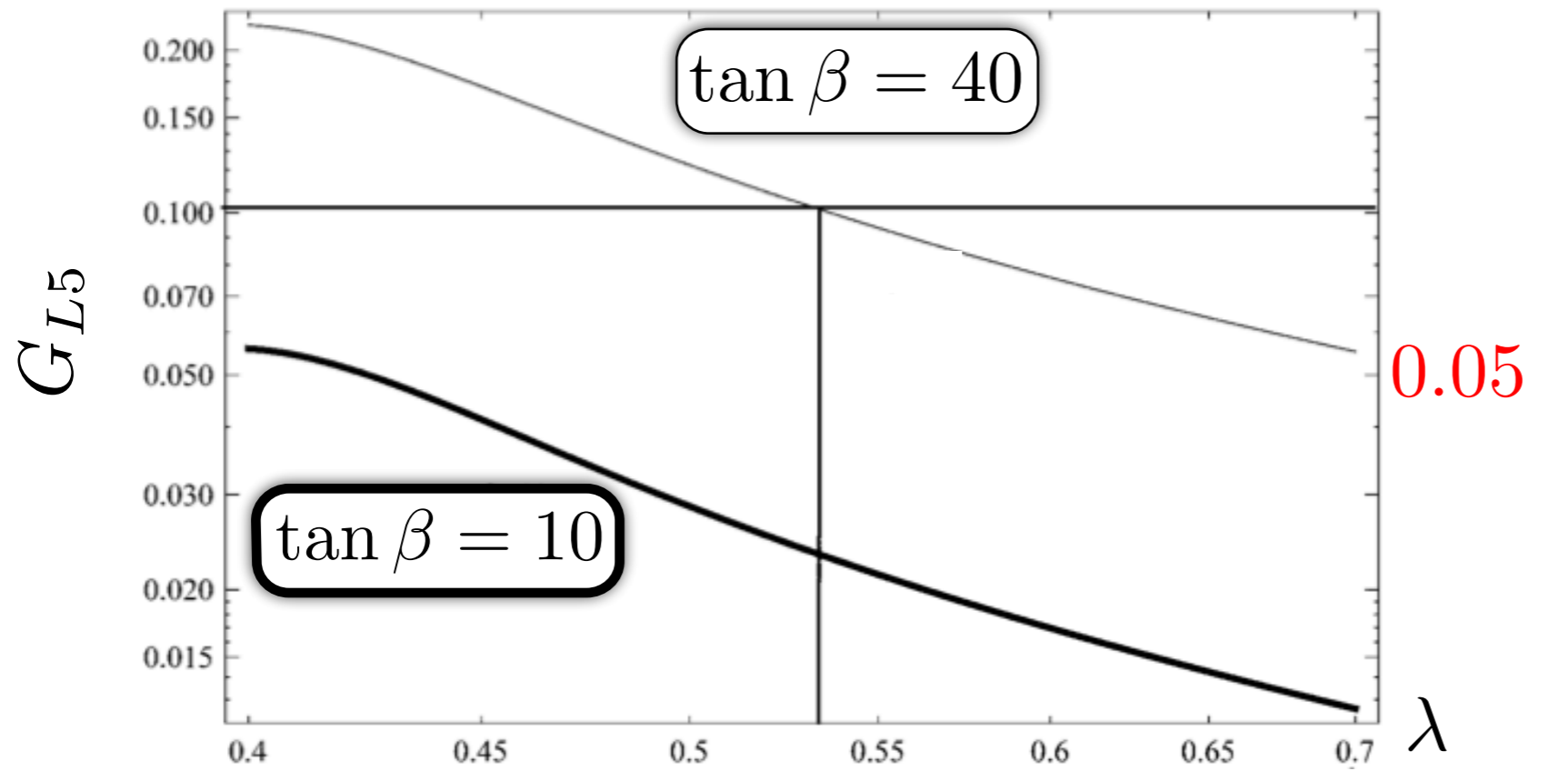
$n_i/s$

the expansion rate.

Larger  $\kappa$ , and/or  $\tan \beta$ , smaller  $\lambda \longrightarrow$  larger  $G_{L5}$

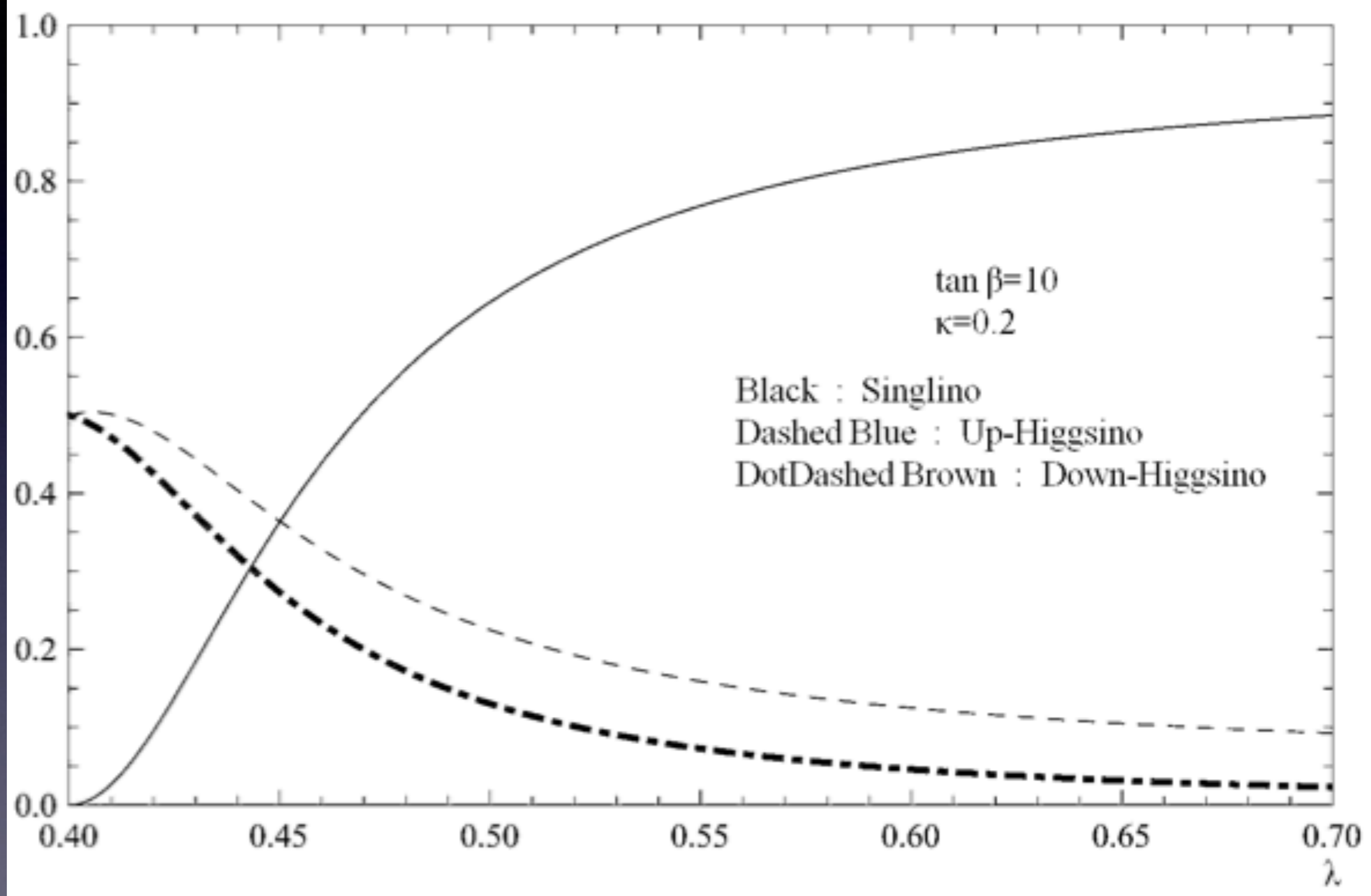


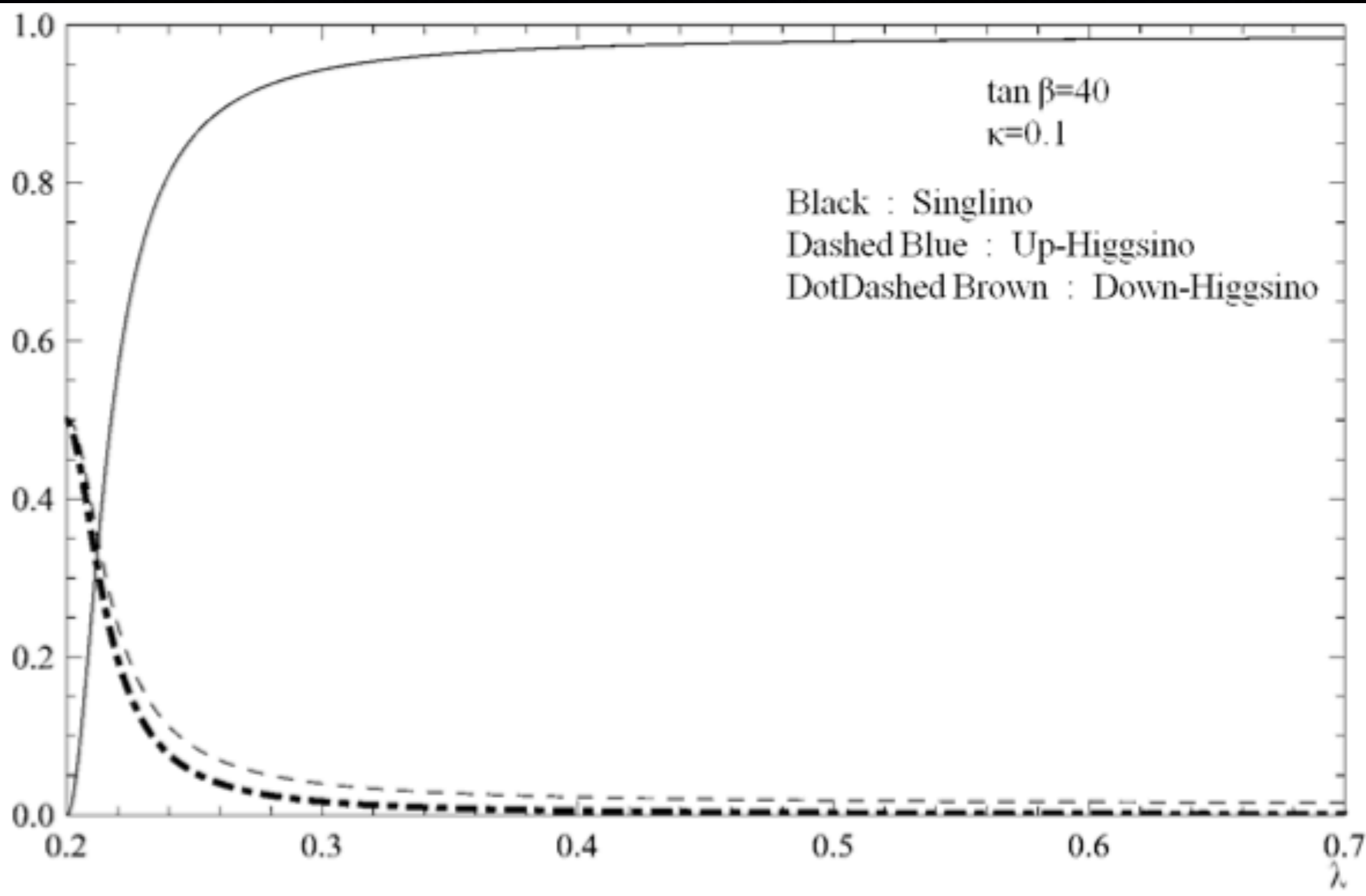
$\kappa = 0.1$

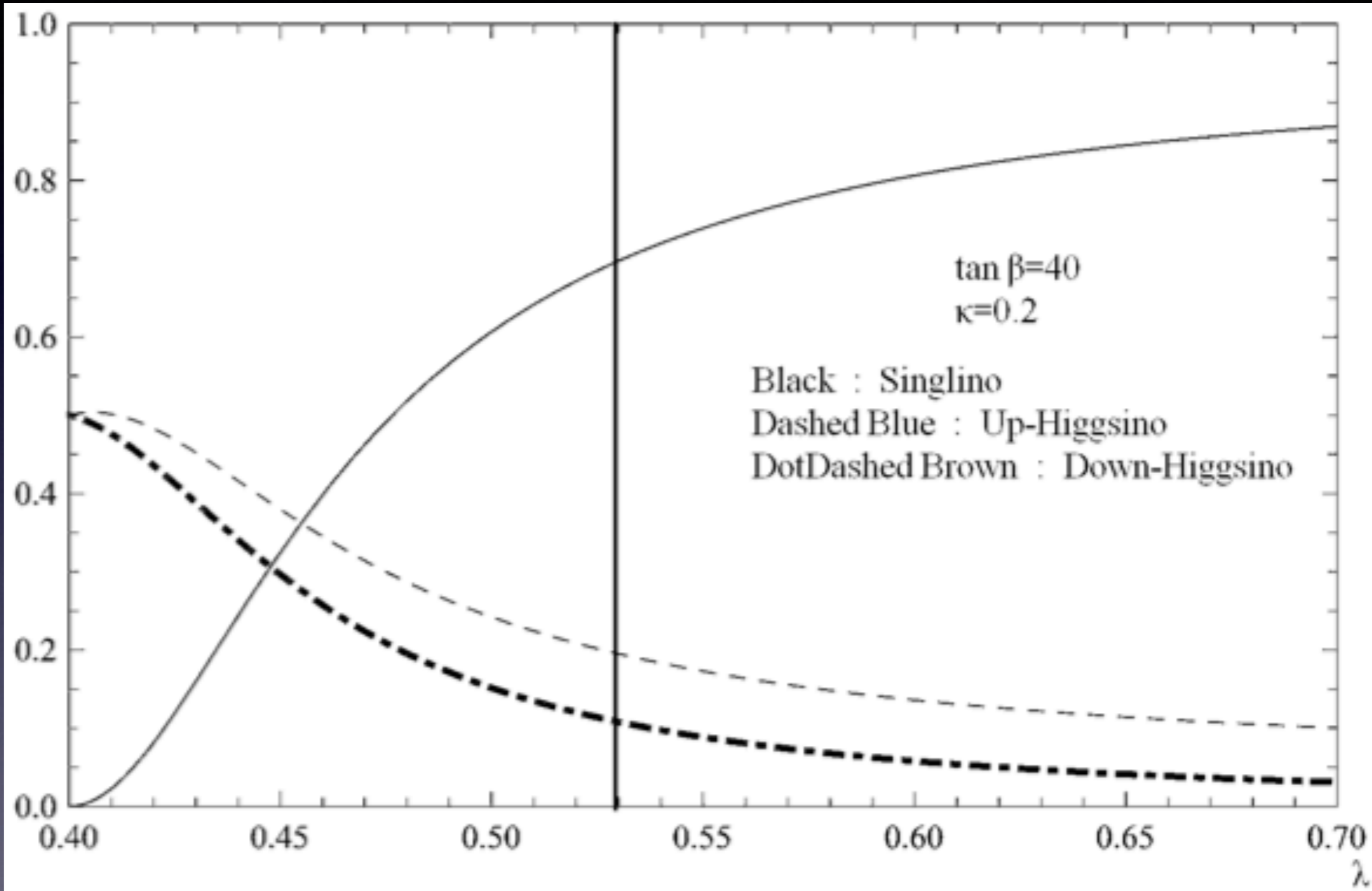


$\kappa = 0.2$

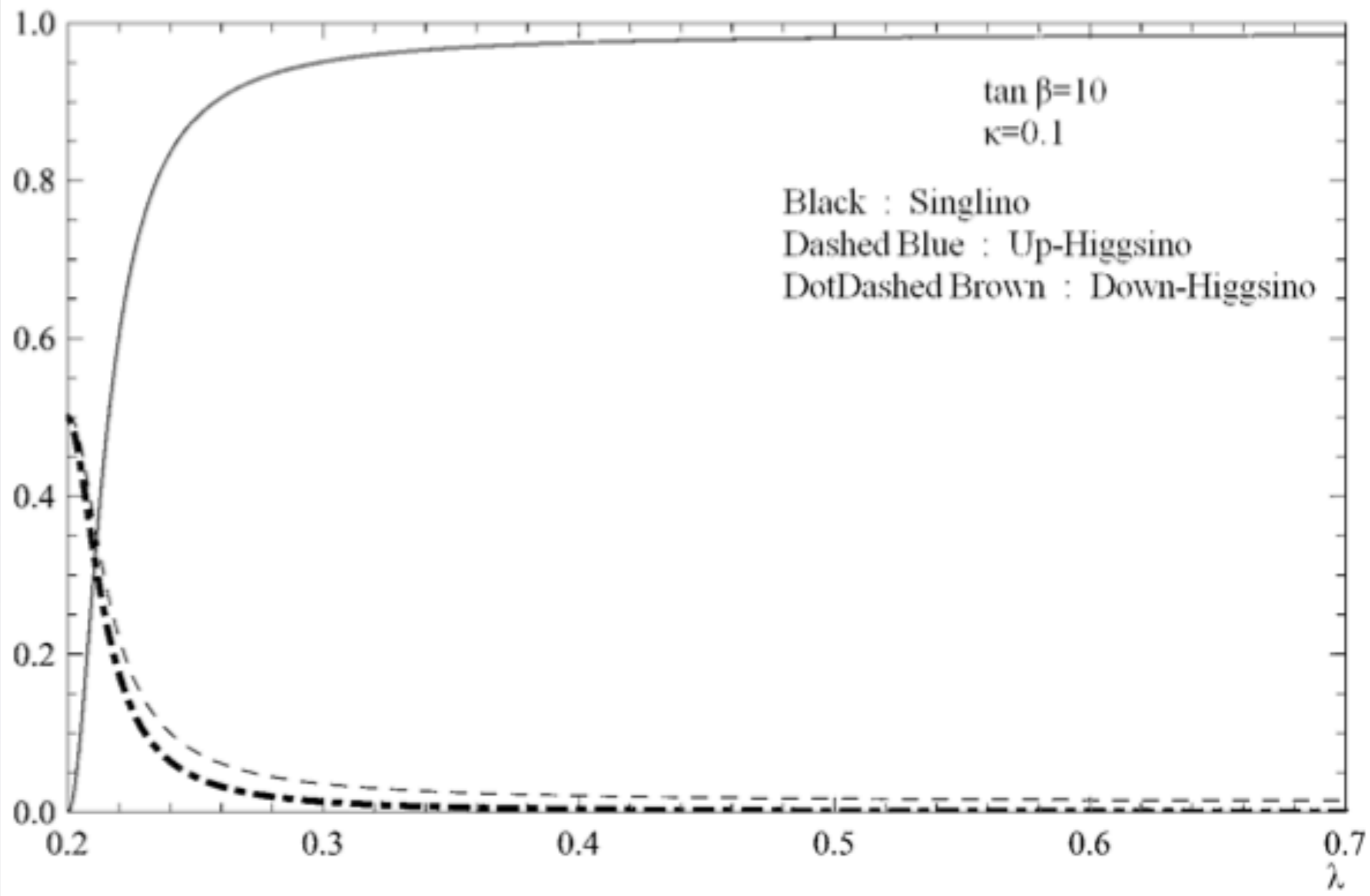




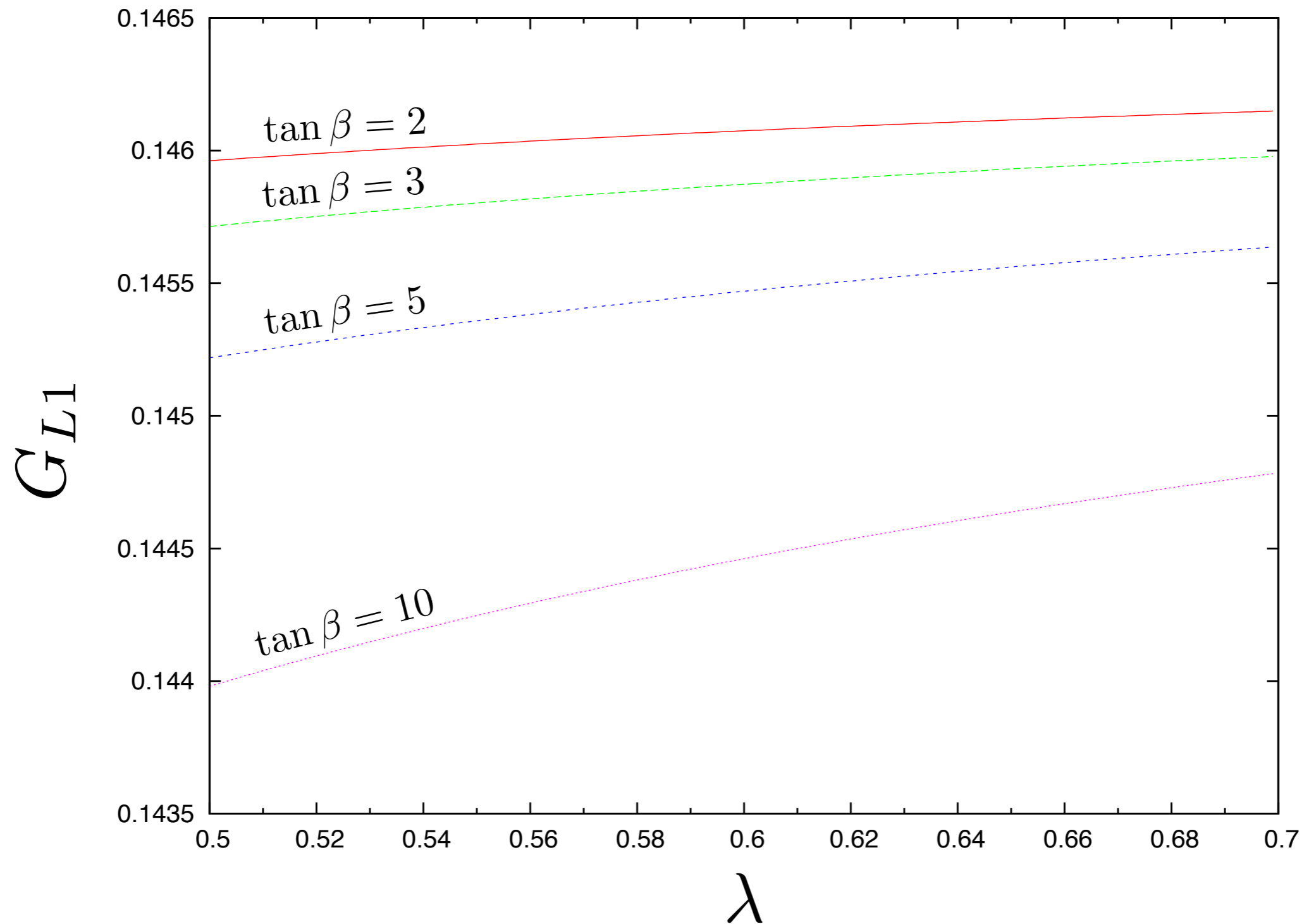




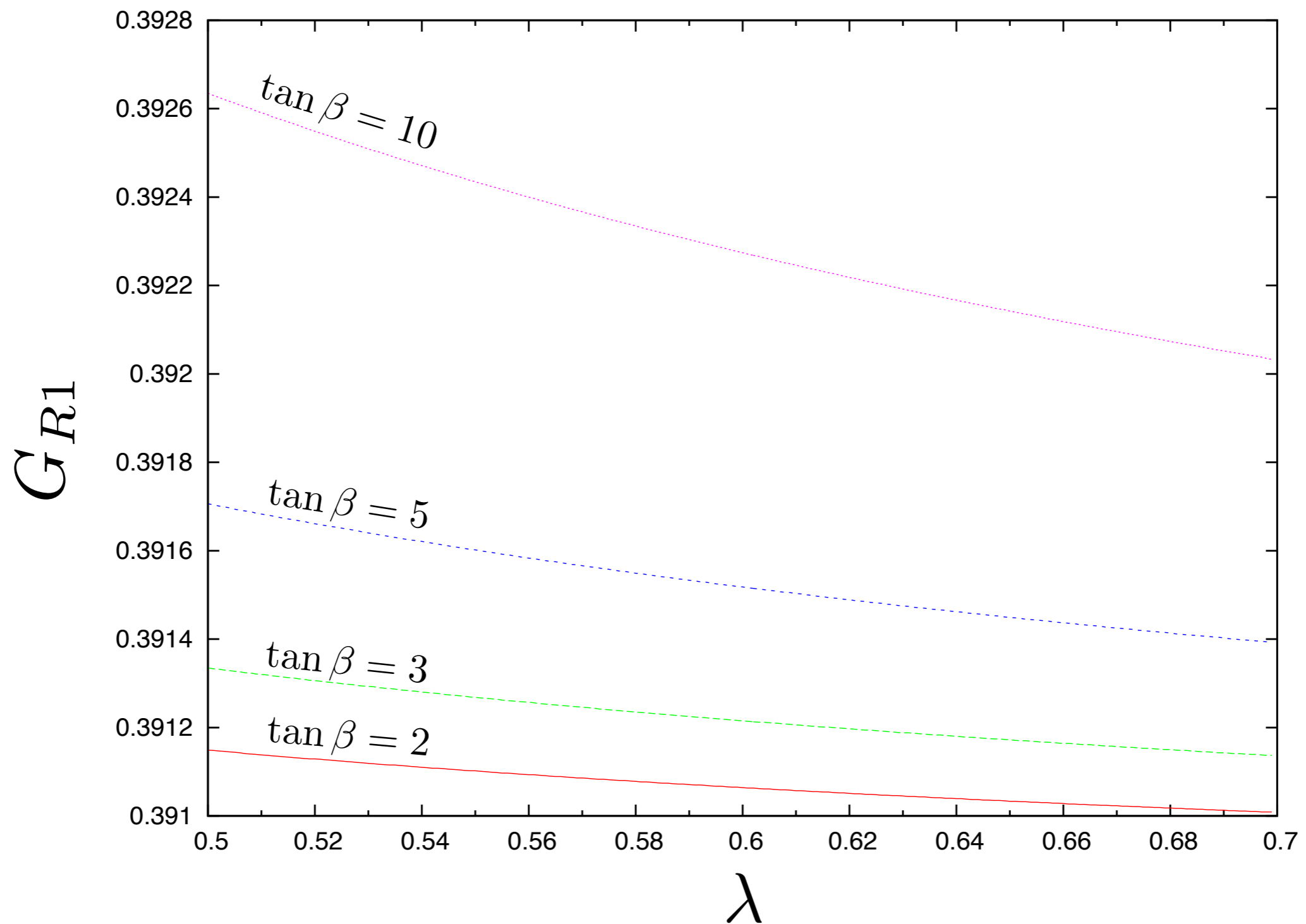




# Parameter dependences of $G_{L1}$ and $G_{R1}$

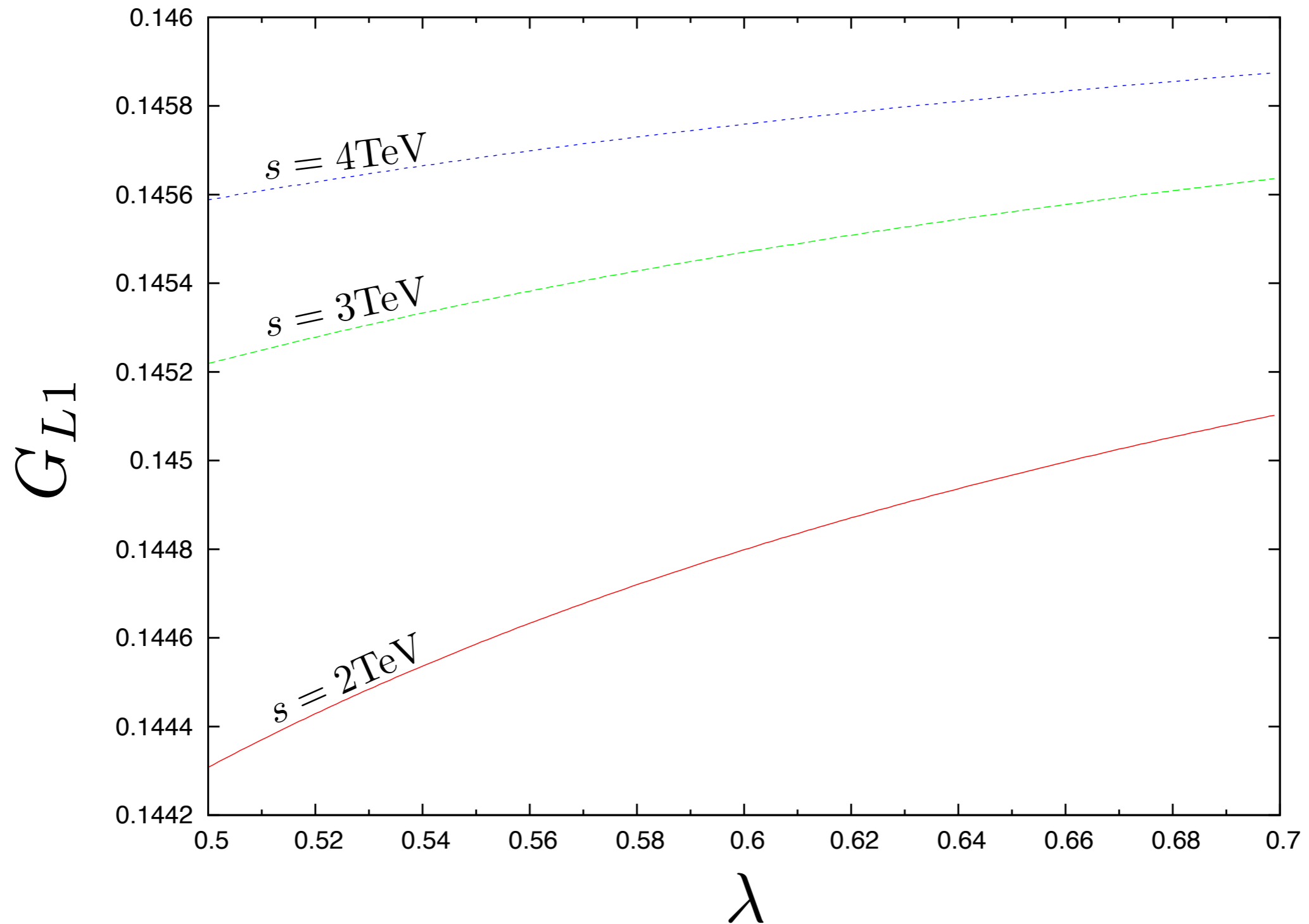


# Parameter dependences of $G_{L1}$ and $G_{R1}$





# Parameter dependences of $G_{L1}$ and $G_{R1}$



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