

$B \rightarrow D$  and  $B_s \rightarrow D_s^{(*)}$   
semileptonic decays  
on the lattice

Francesco Sanfilippo



In collaboration with M.Atoui, V.Morénas, D.Bečirevic

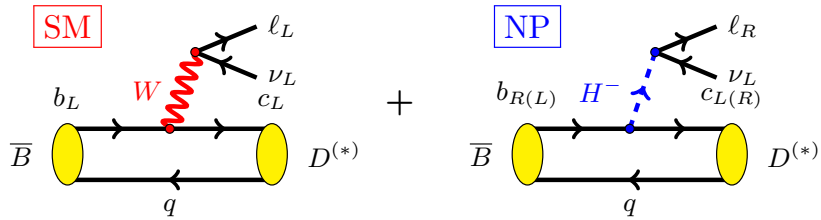
## Introduction

- 1 Physical motivation
- 2 Lattice QCD for  $b$ -physics
- 3 Ratio method

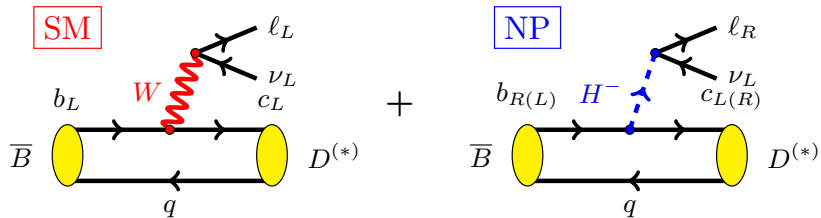
## Semileptonic form factors

- 1  $B_{(s)} \rightarrow D_{(s)}$  - based on Eur.Phys.J. C74 (2014)
- 2  $B_{(s)} \rightarrow D_{(s)}^*$  - fresh new for this conference

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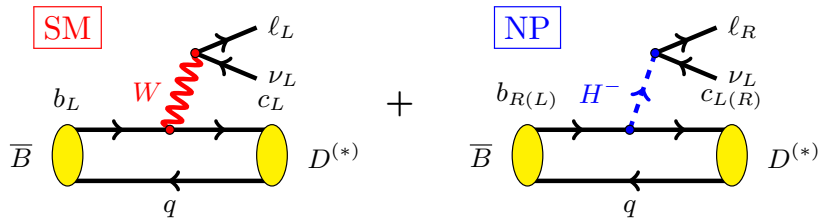


## Popular test of New Physics

$$R(D) = \frac{\mathcal{B}(B \rightarrow D\tau\nu_\tau)}{\mathcal{B}(B \rightarrow D\ell\nu)}, \quad R(D^*) = \frac{\mathcal{B}(B \rightarrow D^*\tau\nu_\tau)}{\mathcal{B}(B \rightarrow D^*\ell\nu)}, \quad (\ell = e, \mu)$$

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## BaBar ('12)

$$R(D) = 0.440 \pm 0.058 \pm 0.042, \quad R(D)^{SM} = 0.31 \pm 0.02$$

$$R(D^*) = 0.332 \pm 0.024 \pm 0.018, \quad R(D^*)^{SM} = 0.252 \pm 0.003$$

- Larger than the SM expectations! **New Physics?**
- Need form factors  $f_{+,0,T}^{B \rightarrow D}$  to check SM and constraint the NP contribution
- Would be nice to check also the unmeasured  $B_s \rightarrow D_s \ell \nu$  process (easier on the lattice)

## Form factors relevant for $B_{(s)} \rightarrow D_{(s)}$

Embeds the **non-perturbative dynamics** entering  $d\Gamma(B_{(s)} \rightarrow D_{(s)}\ell\nu_\ell)/dq^2$

- Convenient parameterization (HQET motivated) in terms of  $\mathcal{G}(\omega)$  [ $\omega = v_B \cdot v_D$  rel.velocity]

$$\frac{1}{\sqrt{m_{B_{(s)}} m_{D_{(s)}}}} \langle D_{(s)}(k) | V_\mu | B_{(s)}(p) \rangle \propto \mathcal{G}(\omega) + \text{corr.}$$

- $\mathcal{G}$  can be expressed in terms of the standard form factors  $f_+(q^2)$  and  $f_-(q^2)$
- $\mathcal{G}(1) = 1$  up to radiative and  $1/m_h$  corrections, **important** to compute  $\mathcal{G}(1)$  on the lattice

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### Other form factors

- Scalar form factor  $f_0$ : necessary in the SM in the case of **heavy lepton** and to check on a non-zero contribution from the diagram mediated by a **charged Higgs boson**
- Tensor form factor  $f_T$ : **leptoquark** scenarios, NP with vector bosons allowing **tensor couplings**
- Need to move away from zero recoil  $\omega = 1$  [i.e.  $q_{max}^2 = (m_{B_{(s)}} - m_{D_{(s)}})^2$ ]

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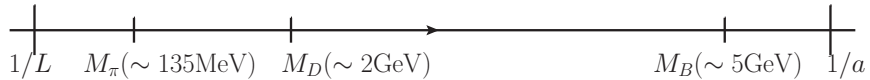
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### Results of our study

- Central result: form factor for unmeasured  $B_s \rightarrow D_s \ell \nu$  close to zero recoil, **easier on the lattice**
- Error for  $B \rightarrow D$  form factor **large: no impact** on  $V_{cb}$  with current lattice statistics
- New results at this conference:  $B_s \rightarrow D_s^*$  axial and tensor form factors at zero recoil
- Results by Fermilab collaboration much more precise but subjects to different systematic errors



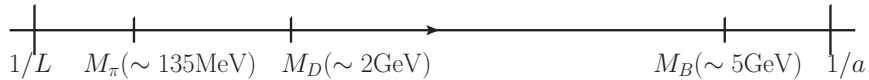
# Approaching $b$ physics



$$M_B/M_\pi \sim 50 \quad \rightarrow \quad L/a \gg 50 \quad \rightarrow \quad N_{points} \gg 50^4 \quad \rightarrow \quad \text{too many points!}$$

Moreover: technical problems in going to too-small lattice spacings (breaking of ergodicity?)

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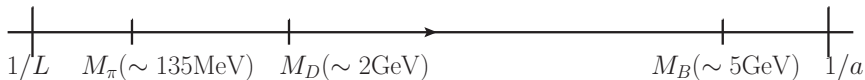
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- Nonrelativistic QCD (expansion in **quark velocity** and in  $1/am_b$ ): HPQCD coll.
- Heavy Quark Effective Theory (continuum expansion in  $\Lambda_{\text{QCD}}/m_b$ ): ALPHA coll.
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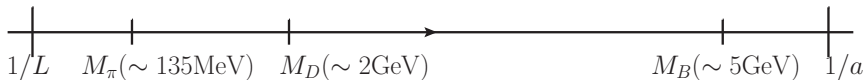
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### Separation of scales, Special actions

- Use of step scaling function to **separate various scales** ( $a$ ,  $m_b$ ,  $L$ ): ALPHA coll.
- **Special actions** have been designed to deal with  $b$  quarks (HISQ, ...): HPQCD coll.

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## This Work: Extrapolate results from the charm to the bottom region

- Scaling laws **often known** in effective theories
- Use **exact** information coming from the **static limit**
- Results become more reliable as lattice spacings get smaller

Consider a series of masses  $m^{(0)} = m_c$ ,  $m^{(1)} = \lambda m_c$ , ...  $m^{(n)} = \lambda^n m_c$

- Define:  $\sigma_i = \frac{\mathcal{G}(1, \lambda m_h, m_c)}{\mathcal{G}(1, m_h, m_c)}$  ratio of form factors at consecutive masses
- Form factor decomposes as:  $\mathcal{G}(1, m_b, m_c) = \sigma_n \sigma_{n-1} \dots \sigma_1 \sigma_0 \mathcal{G}(1, m_c, m_c)$  → 1 (charge conservation)
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## Reconstructing the form factor at physical $b$

- Compute  $\sigma(m_h^{(n)}, \lambda; m_l, a)$ , extrapolate to the continuum & physical  $m_l$
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## Advantages of the ratio approach: double constraint

### Elastic case constraint

- Requires only to interpolate ratios  $\sigma(m_h)$
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**Home message:** we study the scaling toward the static limit taking advantage of **all symmetries**



## Desired features

**Continuum:** Several lattice spacings to take continuum limit

**Renormalization:** Non perturbative

***b*-quark:** Work directly with a relativistic *b* quark at physical mass

**Unquenching:** Include 2 physical light, strange and charm dynamical quarks

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Wilson regularization of QCD with twisted mass term (tmQCD)

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## Salient features (why are we different from next speaker?)

- Consider smart ratios to **interpolate** relativistic data to  $m_b^{phys}$  between  $m_c$  and  $m_h \rightarrow \infty$
- Possible to determine **fully non-perturbatively** form factors different from vector one

$$\langle H_2(\vec{p}_2) | V_\mu | H_1(\vec{p}_1) \rangle = p_\mu f_+^{H_1 \rightarrow H_2}(q^2) + q_\mu \frac{M_{H_1}^2 - M_{H_2}^2}{q^2} f_0^{H_1 \rightarrow H_2}(q^2) \quad \begin{cases} p = p_1 + p_2 \\ q = p_1 - p_2 \end{cases}$$

# Form factor computation

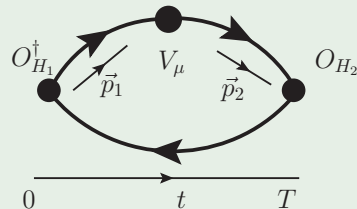
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## Three point correlation functions

$$C_\mu^{(3)}(t) = \langle \sum_{\vec{x}, \vec{y}} O_{H_2}^\dagger(\vec{x}, T) e^{-i\vec{p}_2 \vec{x}} V_\mu(\vec{y}, t) O_{H_1}(0) \rangle$$

at intermediate times:

$$\underset{0 \ll t \ll T}{\simeq} \frac{Z_{H_1} Z_{H_2} \exp[(E_{H_1} - E_{H_2})t] \langle H_1 | V_\mu | H_2 \rangle}{4 E_{H_1} E_{H_2}}$$



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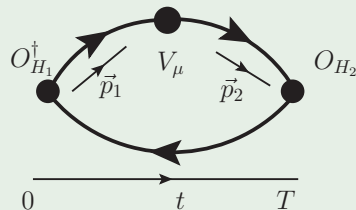
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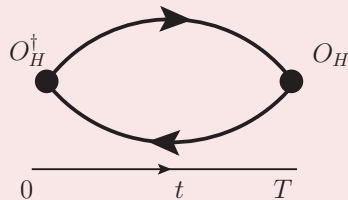


## Two points correlation functions: used to remove the sources

$$C^{(2)}(t) = \sum_{\vec{x}} \langle O_H(\vec{x}, t) O_H^\dagger(\vec{0}, 0) \rangle$$

at large times:

$$\underset{t \rightarrow \infty}{\approx} \frac{Z_H^2 \exp(-E_H t)}{2E_H}$$



## Correlation functions (two point ones)

Choose a lattice discretization of QCD, in Euclidean space

$$a^4 S_{lat}^{QCD} = \bar{\psi}_n D_{n,m} \psi_m + S_{lat}^{gauge} \xrightarrow{a \rightarrow 0} S_{cont}^{QCD} = \bar{\psi} (\not{D} + m) \psi + \frac{1}{4} G_{\mu\nu} G_{\mu\nu}$$

Sample **numerically** (with Monte Carlo methods) the configuration space:

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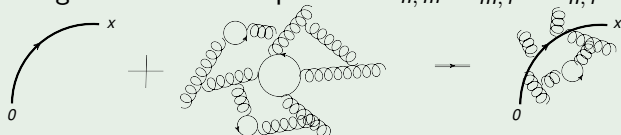
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Compute full quark propagator

- Compute propagator solving discrete Dirac equation:  $D_{n,m} \cdot S_{m,l} = \delta_{n,l}$



- Propagator  $S$  embeds all non perturbative QCD dynamics in the scales  $\sim [1/L, 1/a]$



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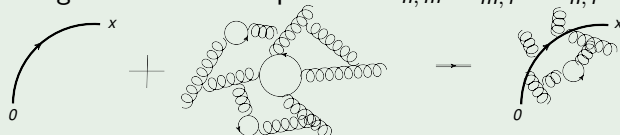
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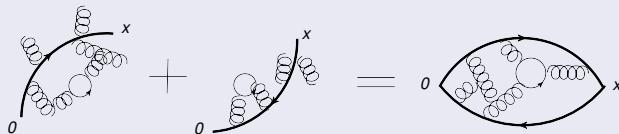
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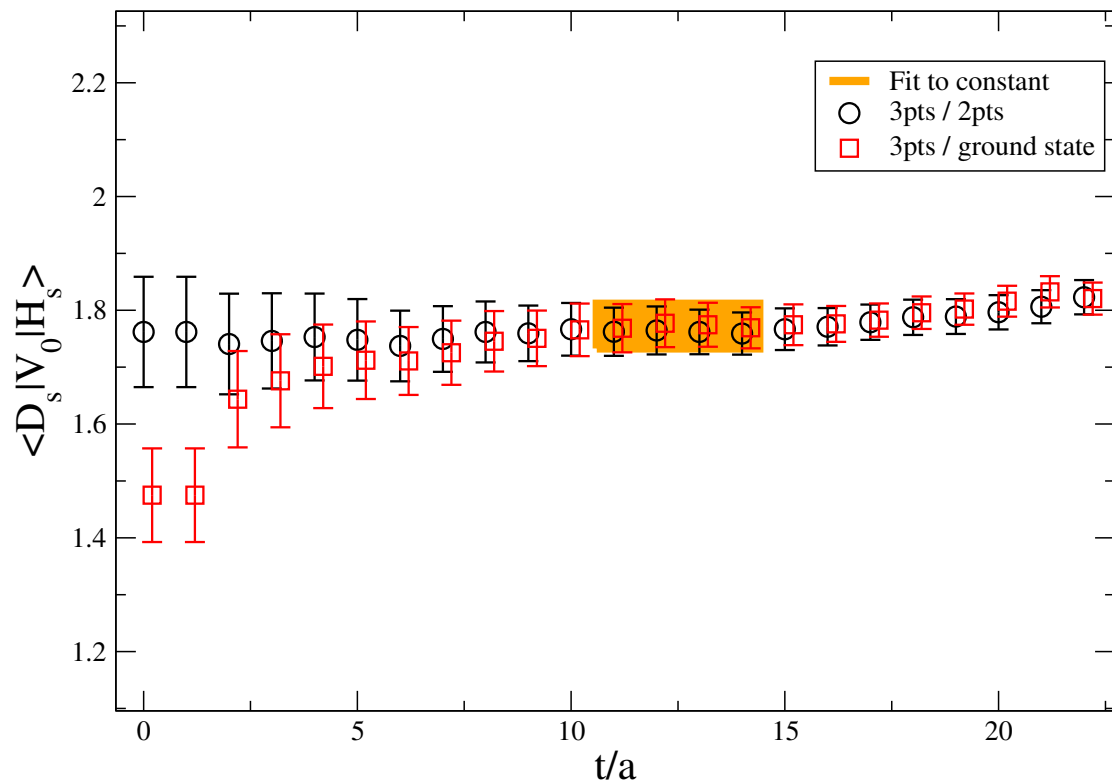
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Combine 2 propagators with suitable Dirac structures

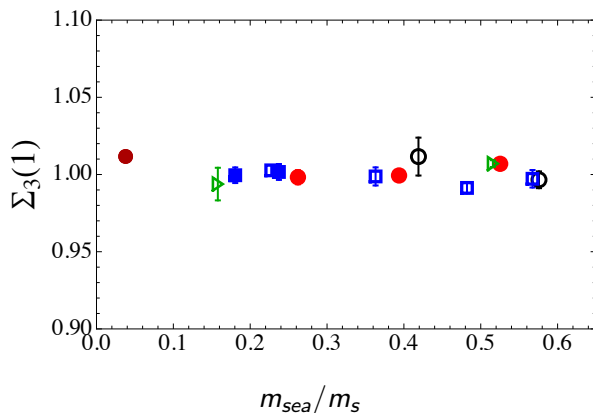
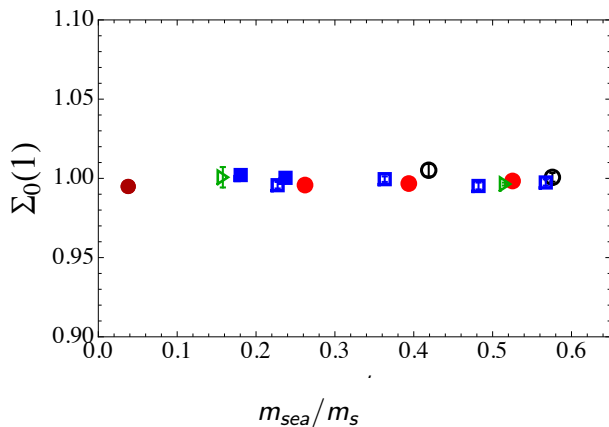


$\langle \bar{\psi}(0) \Gamma_1 \psi(0) \cdot \bar{\psi}(x) \Gamma_2 \psi(x) \rangle \rightarrow$  Fully non-perturbative correlation function

# Example of determination of $\langle D_s | V_0 | H_s(\sim 2m_c) \rangle$



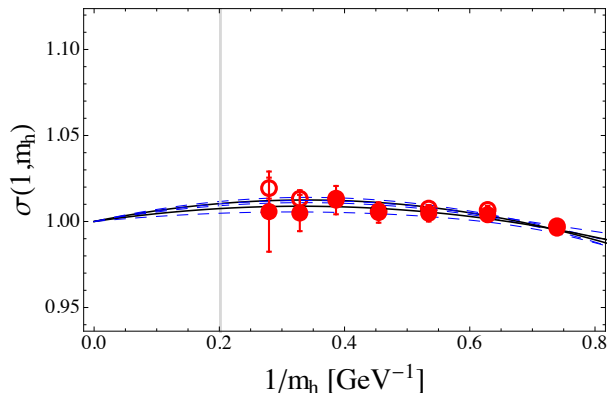
# Chiral and continuum limit extrapolation for ratios



## Chiral continuum extrapolation

- Fit ansatz:  $\Sigma_k(1) = \alpha_k + \beta_k \frac{m_{sea}}{m_s} + \gamma_k a^2$
- Very smooth continuum extrapolation
- Negligible dependence in  $m_{sea}$  (perfectly fitted if  $\beta_k = 0$ )  
(expected since  $m_{sea}$  dependence occurs only through loop effects)
- Chiral logarithms cancel between numerator and denominator of the ratios

# Interpolation to $b$ quark mass



## $B_s \rightarrow D_s$ vector form factor

- Final Results:  $\mathcal{G}^{B_s \rightarrow D_s}(1) = 1.052(46)$ . If no chiral extrapolation included: 1.073(17)  
M.Atoui, V.Morénas, D.Bečirevic, FS, Eur.Phys.J. C74 (2014)
- De Divitiis et al. (Phys.Lett.B '07):  $\mathcal{G}^{B \rightarrow D}(1) = 1.026(17)$  ✓ Step scaling method ✗ Quenched
- MILC+Fermilab: 1.074(24), Preliminary results at Lattice '04

## Other form factors (first computation of $f_T$ ) near zero recoil

$$f_0(q_0^2)/f_+(q_0^2) = 0.77(2), \quad f_T(q_0^2)/f_+(q_0^2) = 1.08(7) \quad \text{at } q_0^2 = 11.5 \text{ GeV}^2$$

## The case of $B_s \rightarrow D_s^* \ell \nu$ (new results)

### Non-perturbative quantities [hadronic matrix elements]

- Possible currents inducing this process:  $T_{\mu\nu} = \bar{c}\sigma_{\mu\nu}b$ ,  $A = \bar{c}\gamma_\mu\gamma_5b$ ,  $V = \bar{c}\gamma_\mu b$
- In total 7 form factors: Axial ( $A_1, A_2, A_3$ ), Tensor ( $T_1, T_2, T_3$ ) and Vector ( $V$ )
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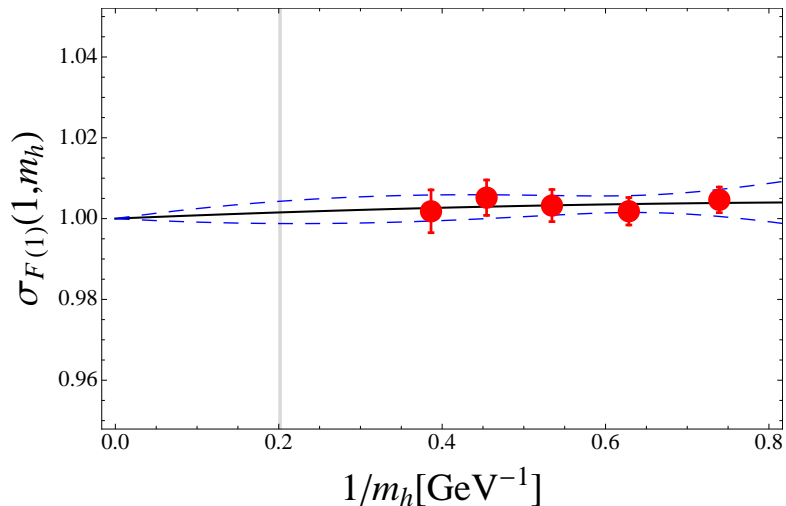
### Ratio of Tensor/Axial form factor

- Same external fields that couple to  $B_s$  and  $D_s^*$
- Determine  $T_2/A_1$  directly from ratio of correlators, together with  $Z_T(\mu)/Z_A$

$$\frac{T_2}{A_1} = \frac{Z_T}{Z_A} \frac{C_{3pts}^T(t)}{C_{3pts}^A(t)}$$

- Allow **high precision** determination of  $T_2/A_1$

# Interpolation of $B_s \rightarrow D_s^*$ to $b$ quark mass



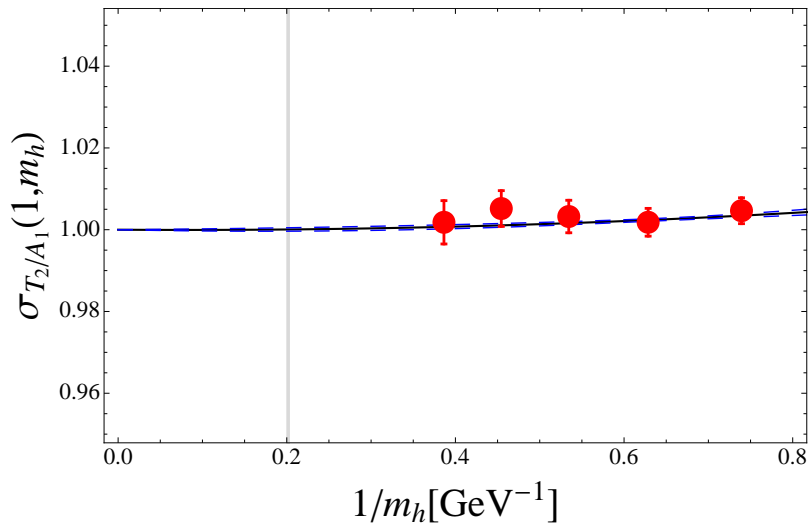
## $B_s \rightarrow D_s^*$ axial form factor

- PRELIMINARY Result:  $\mathcal{F}^{B_s \rightarrow D_s^*}(1) = 0.953(35)$
- Very recently Fermilab + MILC reported:  $\mathcal{F}^{B \rightarrow D^*}(1) = 0.906(4)(12)$ , PRD 89 114504 (2014)

(see next talk for more info!)



# Tensor to axial form factor ratio



## Considerations

- In HQET static limit the matrix element of Tensor and Axial currents are equal
- $1/M_h^2$  corrections to the relation could be large in the charm region
- It turns out they are instead VERY small!!!
- $T_2^{B_s \rightarrow D_s^*} / A_1^{B_s \rightarrow D_s^*} (\omega = 1; \mu = 2\text{GeV}) = 1.073(5)$  (PRELIMINARY!)

### $B_s \rightarrow D_s$ near zero recoil

- First unquenched determination of  $\mathcal{G}^{B_s \rightarrow D_s}(1) = 1.052(46)$ : compatible with previous results
- Determination of  $f_T/f_+$  and  $f_0/f_+$  important to constraint BSM low energy couplings
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## $B_s \rightarrow D_s^*$ at zero recoil

- Determination of  $\mathcal{F}^{B_s \rightarrow D_s^*}(1) = 0.953(35)$
- The first computation of the ratio  $T_2/A_1$  at zero recoil: very close to 1 (at  $\mu = 2$  GeV)
  - important to constraint new physics models from  $B_s \rightarrow D_s^* \ell \nu$
  - reveal the smallness of  $1/M_{\tilde{h}}^2$ -corrections to the static limit provided the QCD renormalization scale is  $\mu \sim 2$  GeV

# Conclusions & future perspectives

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## Non-strange decay

- $B_s \rightarrow D_s^{(*)} \ell \nu$  decays still to be measured
- Invitation to experimentalists to measure these processes
- Strategy presented here can also be used to study the non-strange case
- Commitment to improve statistics and get a more accurate valued of  $B \rightarrow D^{(*)} \ell \nu$  form factors

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Stay tuned!