

# Probing anomalous $ttZ$ interactions with rare meson decays

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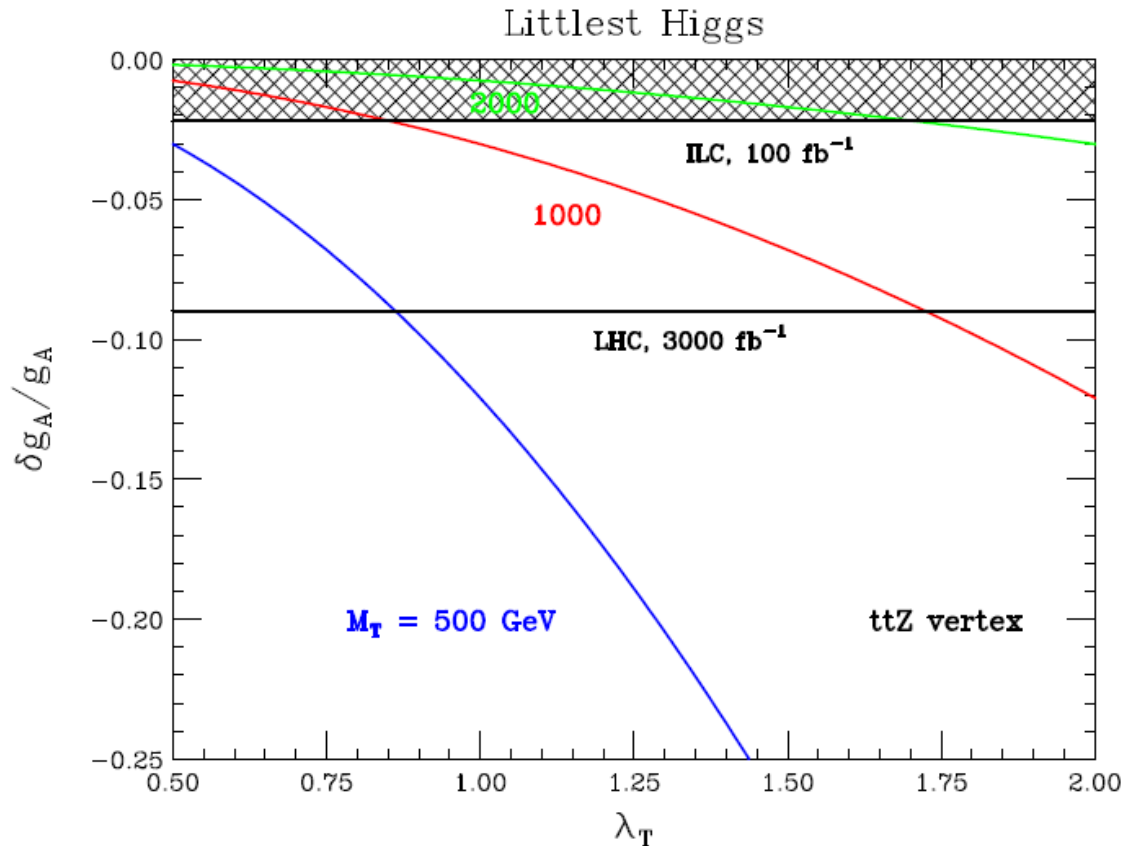
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# Outline

- Motivation
- Anomalous  $ttZ$  in the Effective Field Theory
- Indirect searches
  - Electroweak precision observables
  - Rare meson decays
- Direct searches
  - $ttZ$  production at the LHC
- Conclusions

# Why deviations in $ttZ$ coupling?

- Top quark – special role in EWSB
- Example of natural theories: Little Higgs Models



[Berger, Perelstein, Petriello]

# Effective field theory

- SM + dimension six operators

$$\mathcal{L}^{\text{eff}} = \mathcal{L}^{\text{SM}} + \sum_k \frac{1}{\Lambda^2} C_k Q_k$$

- The operators

$$Q_{\phi q,33}^{(3)} \equiv (\phi^\dagger i \overleftrightarrow{D}_\mu^a \phi) (\bar{Q}_{L,3} \gamma^\mu \sigma^a Q_{L,3}),$$

$$Q_{\phi q,33}^{(1)} \equiv (\phi^\dagger i \overleftrightarrow{D}_\mu \phi) (\bar{Q}_{L,3} \gamma^\mu Q_{L,3}),$$

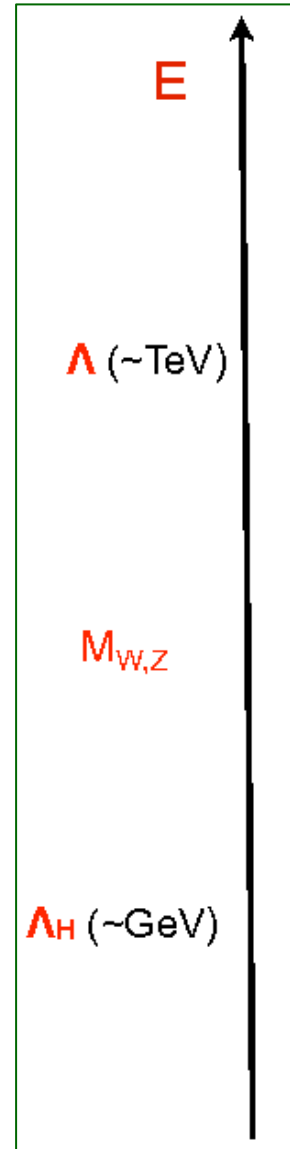
$$Q_{\phi u,33} \equiv (\phi^\dagger i \overleftrightarrow{D}_\mu \phi) (\bar{t}_R \gamma^\mu t_R).$$

$$Q_{L,3} \equiv \begin{bmatrix} t_L \\ \sum_j V_{3j} d_{L,j} \end{bmatrix}$$

- Anomalous  $ttZ$  at tree level

$$\delta g_L^t = \frac{v^2}{2\Lambda^2} (C_{\phi q,33}^{(3)} - C_{\phi q,33}^{(1)}), \quad \delta g_R^t = -\frac{v^2}{2\Lambda^2} C_{\phi u,33},$$

$$\delta g_L^b = -\frac{v^2}{2\Lambda^2} \sum_{i=1,2,3} V_{i3}^* V_{i3} (C_{\phi q,ii}^{(3)} + C_{\phi q,ii}^{(1)}).$$



# Effective field theory - Mixings

- Electroweak and top Yukawa corrections induce mixing into

$$\begin{aligned}
 Q_{\phi q,ii}^{(3)} &\equiv (\phi^\dagger i \overleftrightarrow{D}_\mu^a \phi) (\bar{Q}_{L,i} \gamma^\mu \sigma^a Q_{L,i}), \\
 Q_{\phi q,ii}^{(1)} &\equiv (\phi^\dagger i \overleftrightarrow{D}_\mu \phi) (\bar{Q}_{L,i} \gamma^\mu Q_{L,i}), \\
 Q_{lq,33jj}^{(3)} &\equiv (\bar{Q}_{L,3} \gamma_\mu \sigma^a Q_{L,3}) (\bar{L}_{L,j} \gamma^\mu \sigma^a L_{L,j}), \\
 Q_{lq,33jj}^{(1)} &\equiv (\bar{Q}_{L,3} \gamma_\mu Q_{L,3}) (\bar{L}_{L,j} \gamma^\mu L_{L,j}), \\
 Q_{\phi WB} &\equiv (\phi^\dagger \sigma^a \phi) W_{\mu\nu}^a B^{\mu\nu}, \\
 Q_{\phi D} &\equiv |\phi^\dagger D_\mu \phi|^2,
 \end{aligned}$$

- Assumptions for the initial conditions at the scale  $\Lambda$ :

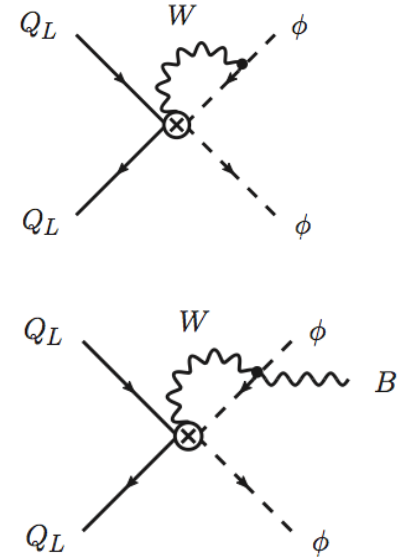
- Non-zero Wilson coefficients:  $C_{\phi q,33}^{(3)}$ ,  $C_{\phi q,33}^{(1)}$ ,  $C_{\phi u,33}$
- $C_{\phi q,33}^{(3)} + C_{\phi q,33}^{(1)} = 0$  - for example, models with VLQs

[Aguila, Perez-Victoria, Santiago]

# Electroweak precision observables: $Z \rightarrow b\bar{b}$

- The relevant part of the RGE-s:

$$\begin{aligned}\mu \frac{d}{d\mu} C_{\phi q,33}^{(3)} &= \frac{y_t^2}{16\pi^2} \left( 8C_{\phi q,33}^{(3)} - 3C_{\phi q,33}^{(1)} \right) - \frac{g_2^2}{16\pi^2} \frac{11}{3} C_{\phi q,33}^{(3)}, \\ \mu \frac{d}{d\mu} C_{\phi q,33}^{(1)} &= \frac{y_t^2}{16\pi^2} \left( -9C_{\phi q,33}^{(3)} + 10C_{\phi q,33}^{(1)} - C_{\phi u} \right) + \frac{g_1^2}{16\pi^2} \frac{1}{9} \left( 5C_{\phi q,33}^{(1)} + 4C_{\phi u} \right), \\ \mu \frac{d}{d\mu} C_{\phi q,11}^{(3)} &= \mu \frac{d}{d\mu} C_{\phi q,22}^{(3)} = \frac{g_2^2}{16\pi^2} 2C_{\phi q,33}^{(3)}, \\ \mu \frac{d}{d\mu} C_{\phi q,11}^{(1)} &= \mu \frac{d}{d\mu} C_{\phi q,22}^{(1)} = \frac{g_1^2}{16\pi^2} \frac{2}{9} \left( C_{\phi q,33}^{(1)} + 2C_{\phi u} \right),\end{aligned}$$



- In the leading-log approximation at the electroweak scale

$$\begin{aligned}\delta g_L^b &= -\frac{e}{2s_w c_w} \frac{v^2}{\Lambda^2} \frac{\alpha}{4\pi} \left\{ V_{33}^* V_{33} \left[ \frac{x_t}{2s_w^2} \left( 8C_{\phi q,33}^{(1)}(\Lambda) - C_{\phi u}(\Lambda) \right) + \frac{17c_w^2 + s_w^2}{3s_w^2 c_w^2} C_{\phi q,33}^{(1)}(\Lambda) \right] \right. \\ &\quad \left. + \left[ \frac{2s_w^2 - 18c_w^2}{9s_w^2 c_w^2} C_{\phi q,33}^{(1)}(\Lambda) + \frac{4}{9c_w^2} C_{\phi u}(\Lambda) \right] \right\} \log \frac{\mu_W}{\Lambda}.\end{aligned}$$

# Electroweak precision observables: T-parameter

- The relevant part of the RGE-s:

$$16\pi^2\mu\frac{d}{d\mu}C_{\phi WB} = 0,$$
$$16\pi^2\mu\frac{d}{d\mu}C_{\phi D} = \frac{8}{3}g_1^2\left(C_{\phi q,33}^{(1)} + 2C_{\phi u,33}\right) + 24y_t^2\left(C_{\phi q,33}^{(1)} - C_{\phi u,33}\right)$$

- In the leading-log approximation at the electroweak scale

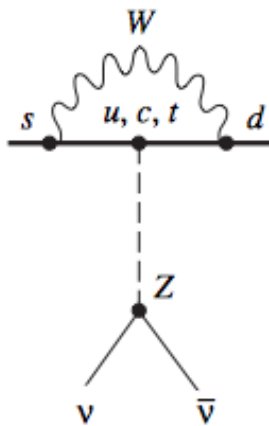
$$S = 0,$$
$$T = -\frac{v^2}{2\alpha\Lambda^2}C_{\phi D}$$
$$= -\frac{v^2}{\Lambda^2}\left[\frac{1}{3\pi c_w^2}\left(C_{\phi q,33}^{(1)} + 2C_{\phi u,33}\right) + \frac{3x_t}{2\pi s_w^2}\left(C_{\phi q,33}^{(1)} - C_{\phi u,33}\right)\right]\log\frac{\mu_W}{\Lambda}$$

# Rare meson decays

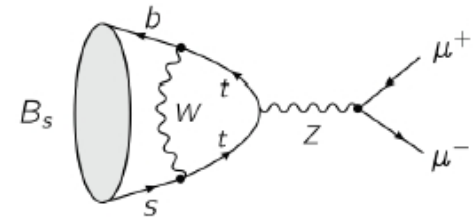
- The relevant part of the RGE-s:

$$\mu \frac{d}{d\mu} C_{lq}^{(3)} = -\frac{g_2^2}{16\pi^2} \frac{1}{3} C_{\phi q,33}^{(3)}, \quad \mu \frac{d}{d\mu} C_{lq}^{(1)} = \frac{g_1^2}{16\pi^2} \frac{1}{3} C_{\phi q,33}^{(1)}$$

- The observables:



$$\text{Br}(B_q \rightarrow \mu^+ \mu^-) = \frac{|N|^2 M_{B_q}^3 f_{B_q}^2 \beta_{q\mu} r_{q\mu}^2 |-2Y_t|^2}{8\pi\Gamma_H^q}$$



$$\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu}(\gamma))$$

$$= \kappa_+(1 + \Delta_{\text{EM}}) \left[ \left( \frac{\text{Im}\lambda_t}{\lambda^5} X_t \right)^2 + \left( \frac{\text{Re}\lambda_c}{\lambda} (P_c + \delta P_{c,u}) + \frac{\text{Re}\lambda_t}{\lambda^5} X_t \right)^2 \right]$$

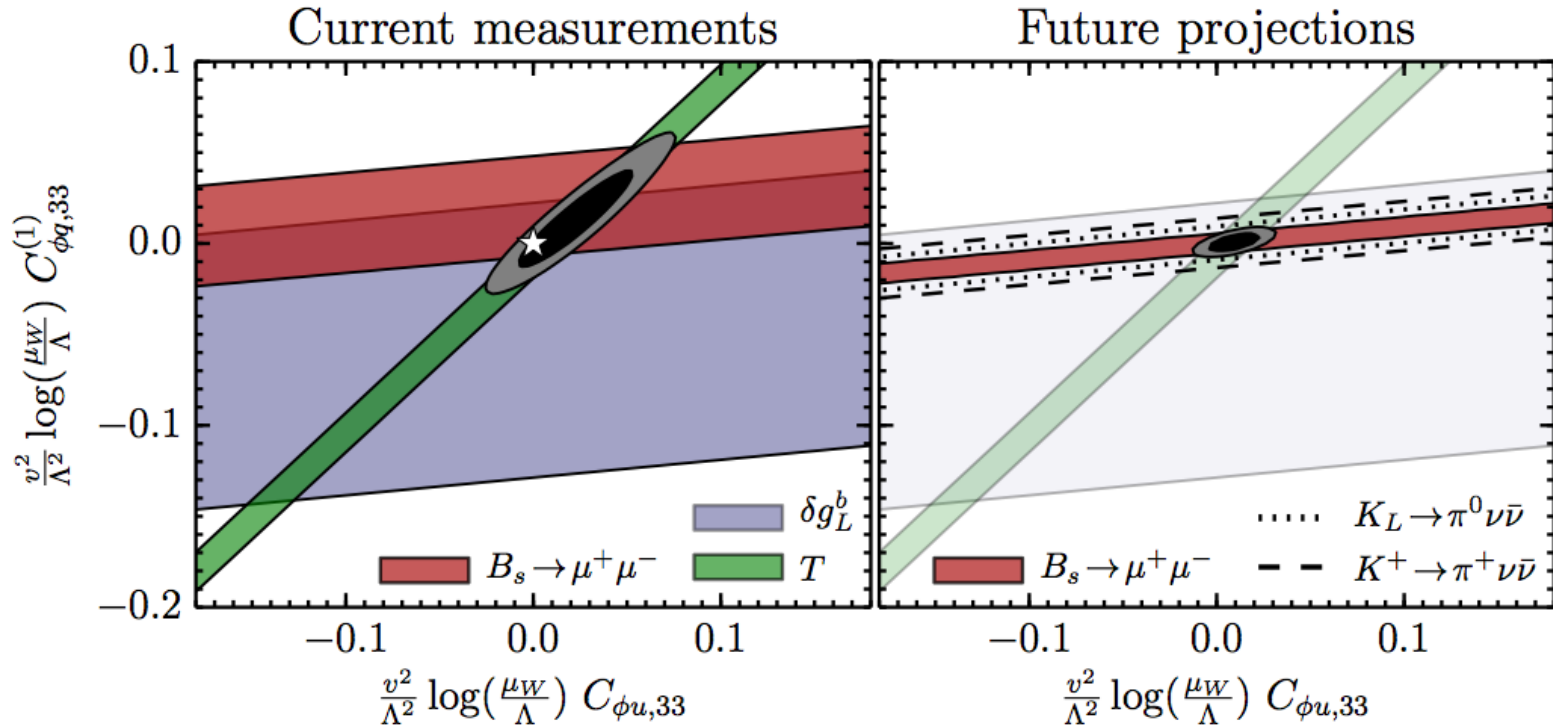
$$\text{Br}(K_L \rightarrow \pi^0 \nu \bar{\nu}) = \kappa_L \left( \frac{\text{Im}\lambda_t}{\lambda^5} X_t \right)^2$$

- The modification due to the anomalous  $ttZ$

$$\delta Y^{\text{NP}} = \delta X^{\text{NP}} = \frac{x_t}{8} \left( C_{\phi u}(\Lambda) - \frac{12 + 8x_t}{x_t} C_{\phi q,33}^{(1)} \right) \frac{v^2}{\Lambda^2} \log \frac{\mu_W}{\Lambda}$$



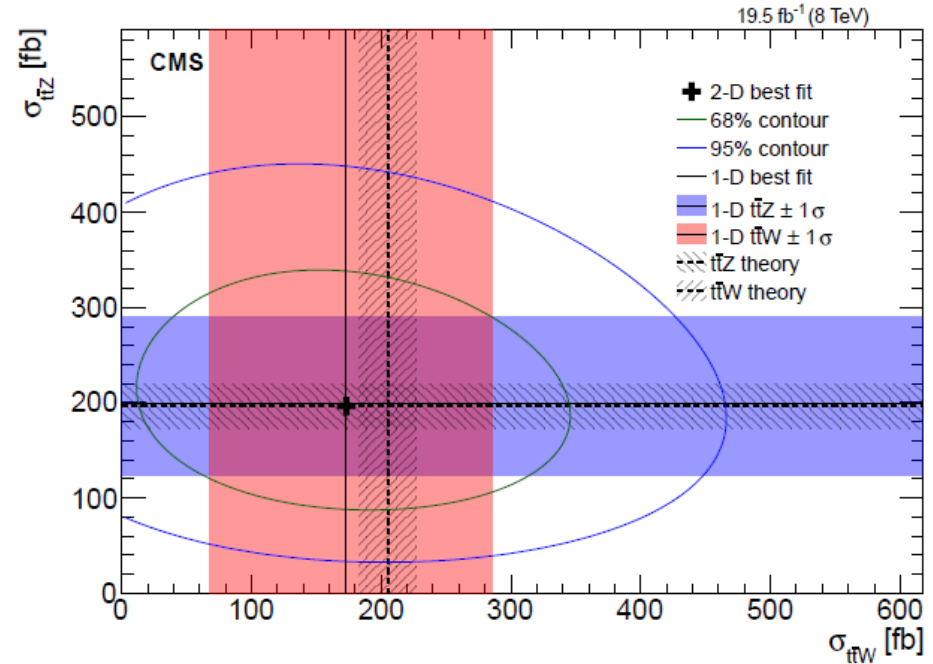
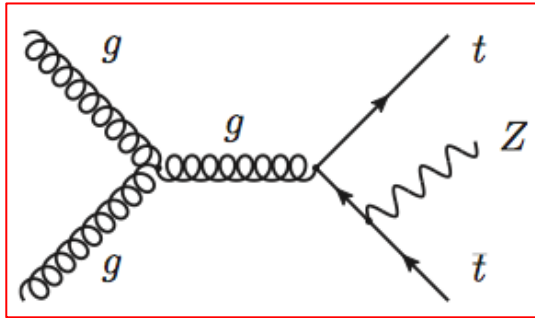
# Indirect constraints: Results



Observable	Value	Ref.
$T$	$0.08 \pm 0.07$	[14]
$\delta g_L^b$	$0.0016 \pm 0.0015$	[14]
$\text{Br}(B_s \rightarrow \mu^+ \mu^-)$ [CMS]	$(3.0_{-0.9}^{+1.0}) \times 10^{-9}$	[29]
$\text{Br}(B_s \rightarrow \mu^+ \mu^-)$ [LHCb]	$(2.9_{-1.0}^{+1.1}) \times 10^{-9}$	[30]
$\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$	$(1.73_{-1.05}^{+1.15}) \times 10^{-10}$	[51]

# Direct searches

- **CMS-TOP-12-036:**  $pp \rightarrow t\bar{t} + Z \rightarrow t(\rightarrow l\nu b) \bar{t}(\rightarrow jj\bar{b}) Z(\rightarrow \ell\ell)$



- **Current and future-projected LHC limits** [Rontsh,Schulze]

$$\begin{aligned} -0.50 &\leq \frac{v^2}{\Lambda^2} \text{Re} [C_{\phi q}^{(3,33)}] \leq 0.68, \\ -0.82 &\leq \frac{v^2}{\Lambda^2} \text{Re} [C_{\phi u}^{33}] \leq 1.59. \end{aligned}$$

$$\begin{aligned} \left. \begin{array}{l} -0.25 \\ -0.22 \\ -0.19 \end{array} \right\} &\leq \frac{v^2}{\Lambda^2} \text{Re} [C_{\phi q}^{(3,33)}] \leq \begin{cases} 0.26 & \text{with } 30 \text{ fb}^{-1} \\ 0.10 & \text{with } 300 \text{ fb}^{-1} \\ 0.04 & \text{with } 3000 \text{ fb}^{-1} \end{cases}, \\ \left. \begin{array}{l} -0.27 \\ -0.19 \\ -0.13 \end{array} \right\} &\leq \frac{v^2}{\Lambda^2} \text{Re} [C_{\phi u}^{33}] \leq \begin{cases} 0.67 & \text{with } 30 \text{ fb}^{-1} \\ 0.47 & \text{with } 300 \text{ fb}^{-1} \\ 0.32 & \text{with } 3000 \text{ fb}^{-1} \end{cases}. \end{aligned}$$

# Conclusions

- ✓ Indirect probes are powerful - Direct searches not competitive
- ✓ Future rare meson decay measurements - route to discovery
- ✓ Disclaimer: Indirect searches depend on the assumptions about UV completion