



# *D-mixing and indirect CPV at Belle, and prospects for Belle II*

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CKM Unitarity Triangle**

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- *motivation*
- $D^0(t) \rightarrow K^+\pi^-$
- $D^0(t) \rightarrow K_S \pi^+\pi^-$
- $D^0(t) \rightarrow K^+K^-, \pi^+\pi^-$
- *HFAG fit results*
- *Belle II prospects*



## *Why study...*

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### *... CP Violation in D Decays?*

- *SM rates are very low  $\Rightarrow$  a good place to search for new physics [Most promising: singly Cabibbo-suppressed decays, see Grossman, Kagan, Nir, PRD 75, 036008 (2007) ]*
- *Now established that  $D^0/D^0$ bar mesons mix  $\Rightarrow$  is there CPV in the mixing? or CPV due to interference between mixed and direct decay amplitudes?*

### *... CPV in D Decays at an $e^+e^-$ machine (Belle/BaBar/Belle II)?*

- *Final states with neutral particles ( $\gamma, K_S, \pi^0$ ) can be reconstructed that are difficult/impractical to reconstruct at a hadron machine*
- *Low backgrounds, high trigger/reconstruction efficiencies, minimal decay time bias, roughly flat acceptance over Dalitz plots, several control samples*

## “Wrong-sign” $D^0(t) \rightarrow K^+\pi^-$

[Ko et al., PRL 112, 111801 (2014);  
Zhang et al., PRL 96, 151801 (2006);  
Li et al., PRL 94, 071801 (2005)]

Fit for  $x'^2, y', |q/p|, \phi = \text{Arg}(q/p)$

[ $x' = x \cos \delta + y \sin \delta, y' = y \cos \delta - x \sin \delta$ ]

## $D^0(t) \rightarrow K^0 \pi^+ \pi^-$ Dalitz plot analysis

[Peng et al., PRD 89, 091103(R) (2014);  
Zhang et al., PRL 99, 131803 (2007)]

Fit for  $x, y, |q/p|, \phi = \text{Arg}(q/p)$

## Time-dependent $D^0(t) \rightarrow K^+K^-, \pi^+\pi^-$

[Staric arXiv:1212.3478 (2012);  
Staric et al., PRL 98, 211803 (2007);  
Abe et al., hep-ex/0308034 (2003)]

Fit for  $y_{CP}, A_\Gamma$

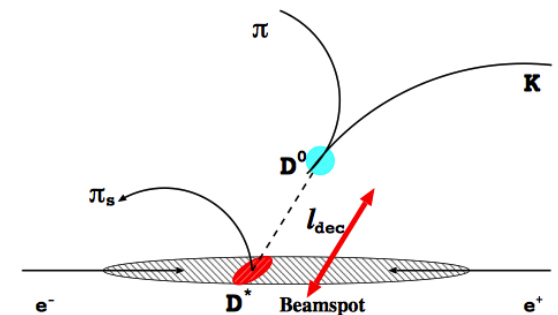
$$2 y_{CP} = (|q/p| + |p/q|) y \cos \phi - (|q/p| - |p/q|) x \sin \phi$$

$$2 A_\Gamma = (|q/p| - |p/q|) y \cos \phi - (|q/p| + |p/q|) x \sin \phi$$

## 3 features in common:

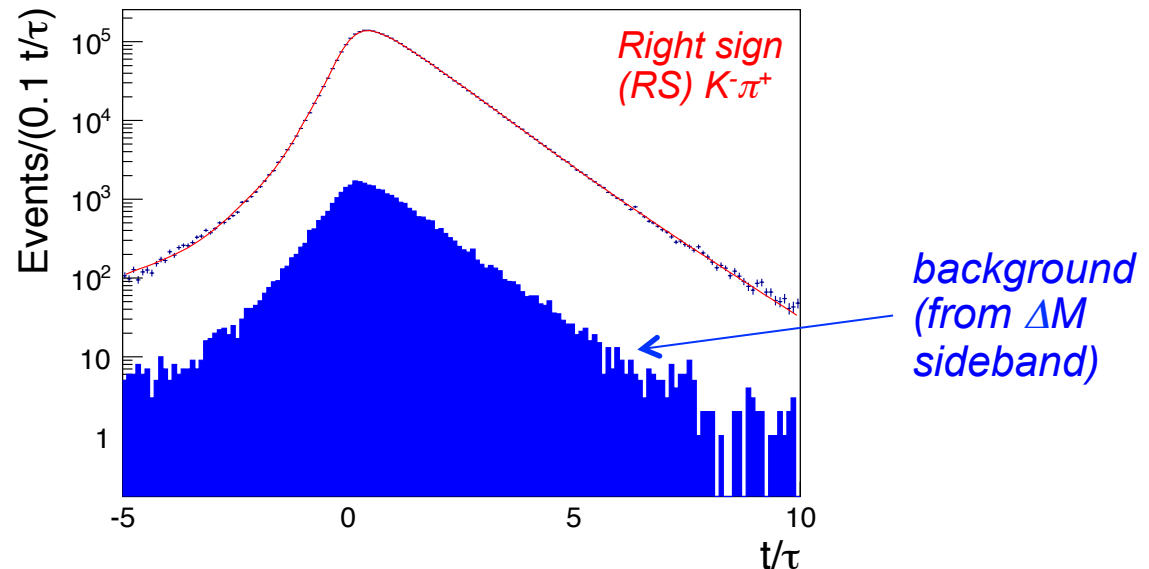
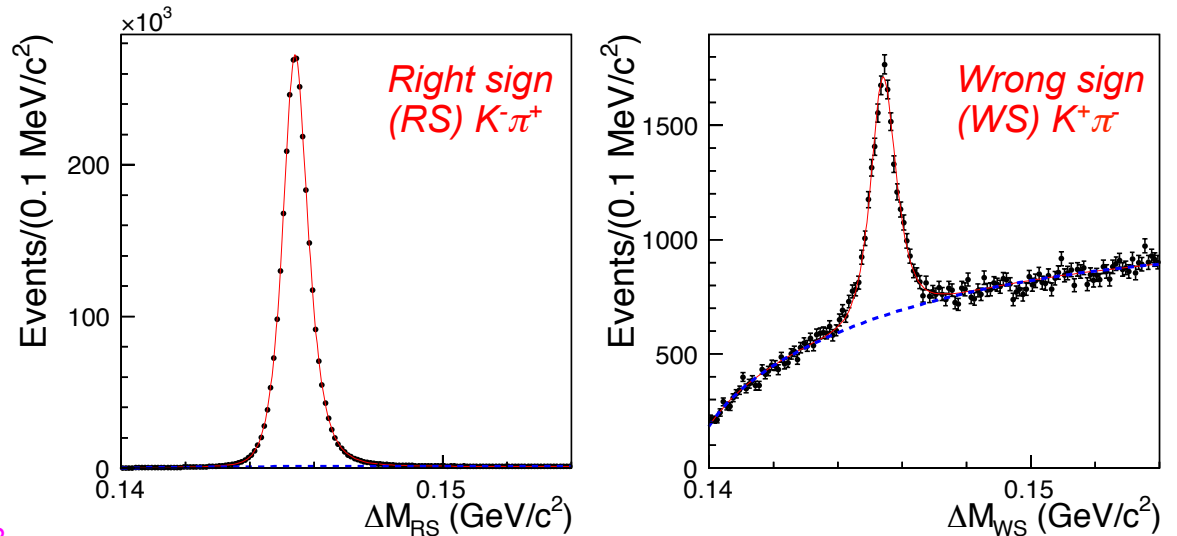
- flavor is tagged via  $D^{*-} \rightarrow \bar{D}^0 \pi_{\text{slow}}$  or  $D^{*+} \rightarrow D^0 \pi_{\text{slow}}$
- dominant background is typically “random  $\pi_{\text{slow}}$ ” – include PDF for this in fits
- decay time  $t$  calculated via

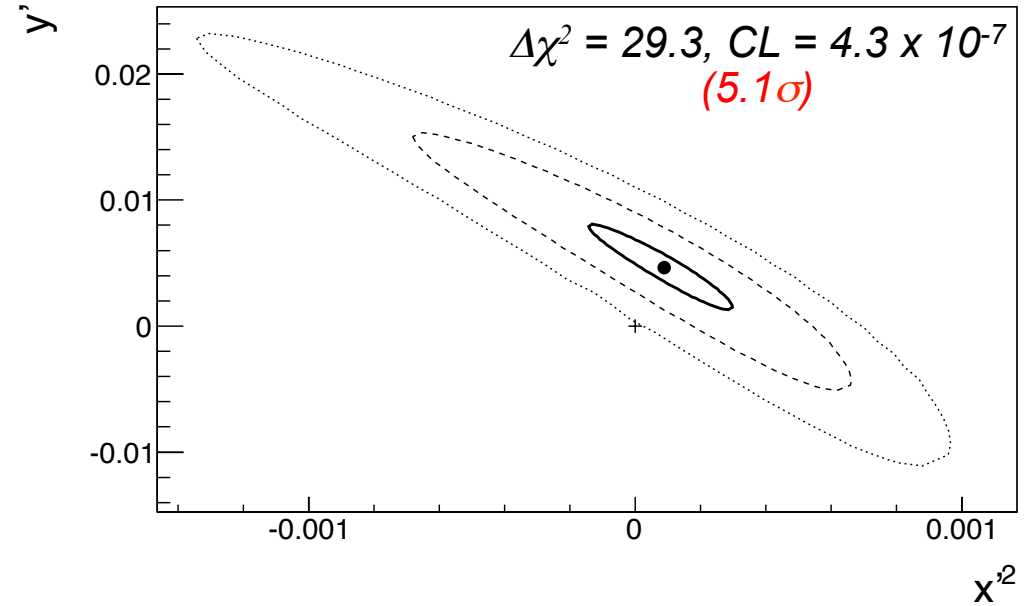
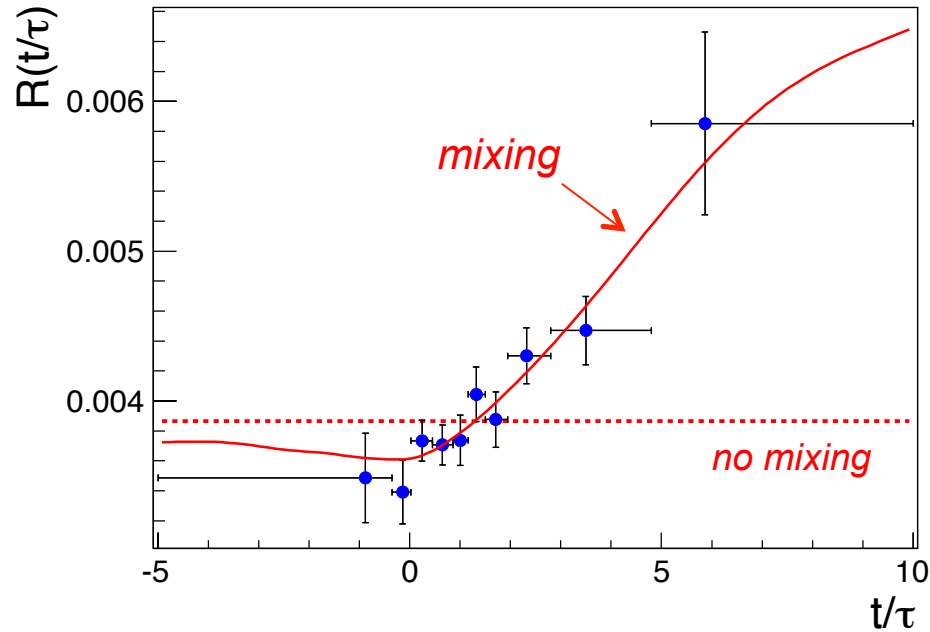
$$t = \left( \frac{m_D}{p_D} \right) \vec{\ell} \cdot \hat{p}_D$$



- 976  $fb^{-1}$ , full data set
- double mis-ID background reduced with tight PID cuts if  $|M_{swapped} - M_D| < 25 \text{ MeV}/c^2$
- Method (opposite the usual):
  - a) WS and RS samples are selected:  $|M_{K\pi} - M_D| < 20 \text{ MeV}/c^2$
  - b) Divide samples into 10 bins of decay time. For each bin, determine event yields by fitting  $\Delta M = M_{K\pi\pi} - M_{K\pi}$  distribution
  - c) plot ratio of event yields, fit this distribution for  $R_D$ ,  $x^2$ ,  $y'$

Advantage: as one fits to ratios of event yields, less sensitive to resolution function





Test hypothesis ( $\chi^2/\text{d.o.f.}$ )	Parameters	Fit results ( $10^{-3}$ )
Mixing (4.2/7)	$R_D$ $y'$ $x'^2$	$3.53 \pm 0.13$ $4.6 \pm 3.4$ $0.09 \pm 0.22$
No Mixing (33.5/9)	$R_D$	$3.864 \pm 0.059$

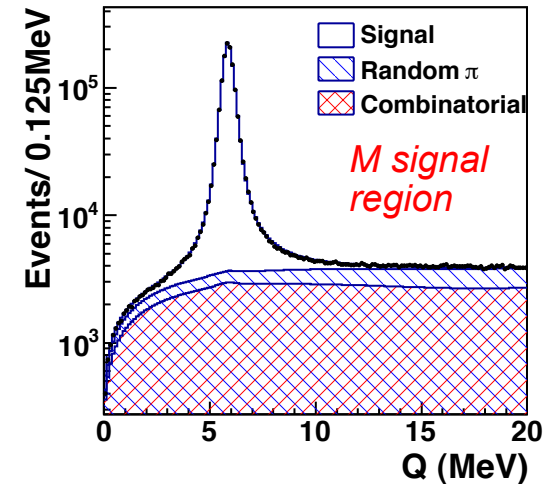
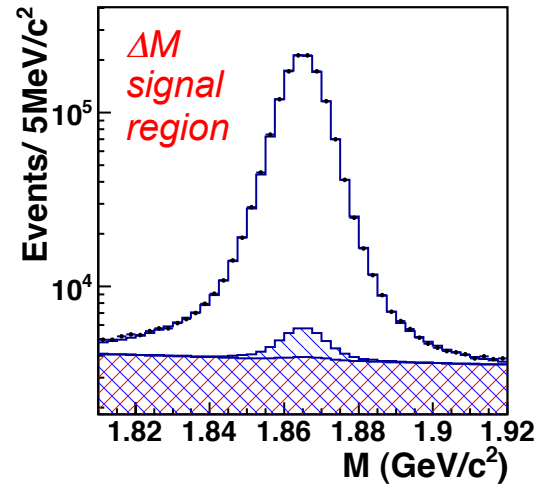
Most precise results from  $e^+e^-$  experiments, But LHCb obtains:

$$\left. \begin{aligned} R_D &= 3.568 \pm 0.066 \\ y' &= 4.8 \pm 1.0 \\ x'^2 &= 0.055 \pm 0.049 \end{aligned} \right\} \times 10^{-3}$$



Fitting the time-dependent Dalitz plot yields  $x$ ,  $y$ ,  $|q/p|$  and  $\phi = \text{Arg}(q/p)$

- 976  $\text{fb}^{-1}$ , full data set
- Signal yield determined from 2-dim. fit to  $M_{K\pi\pi}$  and  $\Delta M = M_{K\pi\pi} - M_{K\pi}$ . Yield is  $1.2 \times 10^6$  events with a purity of 96%.
- Select events in signal region  $|M_{K\pi\pi} - M_D| < 15 \text{ MeV}/c^2$  and  $\Delta M = (5.75, 5.95) \text{ MeV}$ .
- For events in signal region, do unbinned ML fit to  $m^+ = M(K\pi^+)^2$ ,  $m^- = M(K\pi^-)^2$ , and decay time  $t$ . Fit parameters are  $x$ ,  $y$ ,  $\tau$ , resolution function parameters (2-3 Gaussians), and decay model: magnitudes and phases of 13 intermediate resonances.
- Do fit separately (+ simultaneously) for  $D^0$  and  $D^0$ bar samples to obtain  $|q/p|$ ,  $\phi$  parameters.



$$R_{D^0} = \frac{e^{-\Gamma t}}{2} \left\{ \left( |\mathcal{A}_f|^2 + \left| \frac{q}{p} \right|^2 |\overline{\mathcal{A}}_f|^2 \right) \cosh(yt) + \left( |\mathcal{A}_f|^2 - \left| \frac{q}{p} \right|^2 |\overline{\mathcal{A}}_f|^2 \right) \cos(xt) \right. \\ \left. + 2\text{Re} \left( \frac{q}{p} \overline{\mathcal{A}}_f \mathcal{A}_f^* \right) \sinh(yt) - 2\text{Im} \left( \frac{q}{p} \overline{\mathcal{A}}_f \mathcal{A}_f^* \right) \sin(xt) \right\}$$

$$R_{\overline{D}^0} = \frac{e^{-\Gamma t}}{2} \left\{ \left( |\overline{\mathcal{A}}_f|^2 + \left| \frac{p}{q} \right|^2 |\mathcal{A}_f|^2 \right) \cosh(yt) + \left( |\overline{\mathcal{A}}_f|^2 - \left| \frac{p}{q} \right|^2 |\mathcal{A}_f|^2 \right) \cos(xt) \right. \\ \left. + 2\text{Re} \left( \frac{p}{q} \mathcal{A}_f \overline{\mathcal{A}}_f^* \right) \sinh(yt) - 2\text{Im} \left( \frac{p}{q} \mathcal{A}_f \overline{\mathcal{A}}_f^* \right) \sin(xt) \right\}$$

If no CPV :  $\mathcal{A}_f(m_+^2, m_-^2) = \overline{\mathcal{A}}_f(m_-^2, m_+^2)$

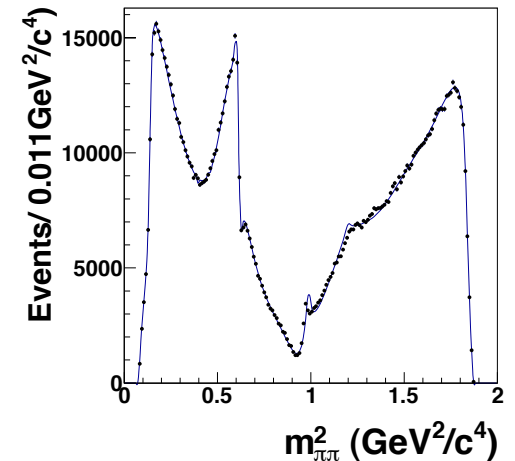
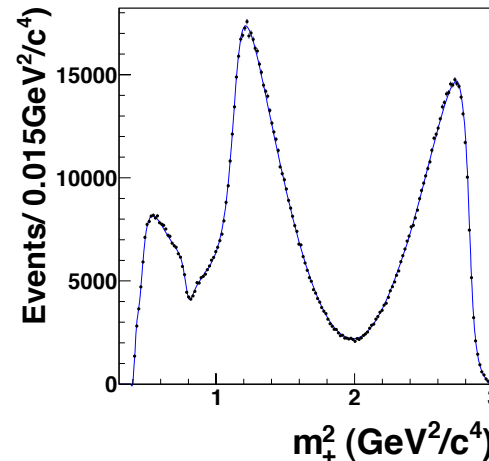
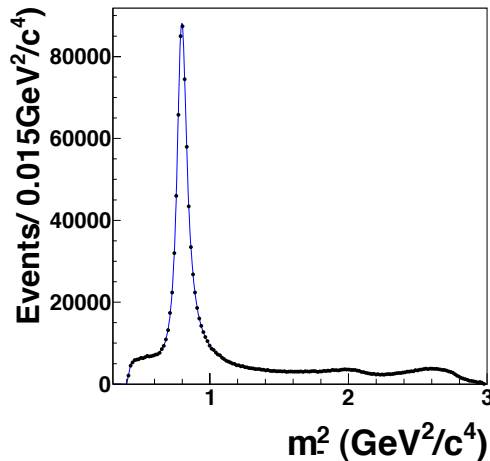


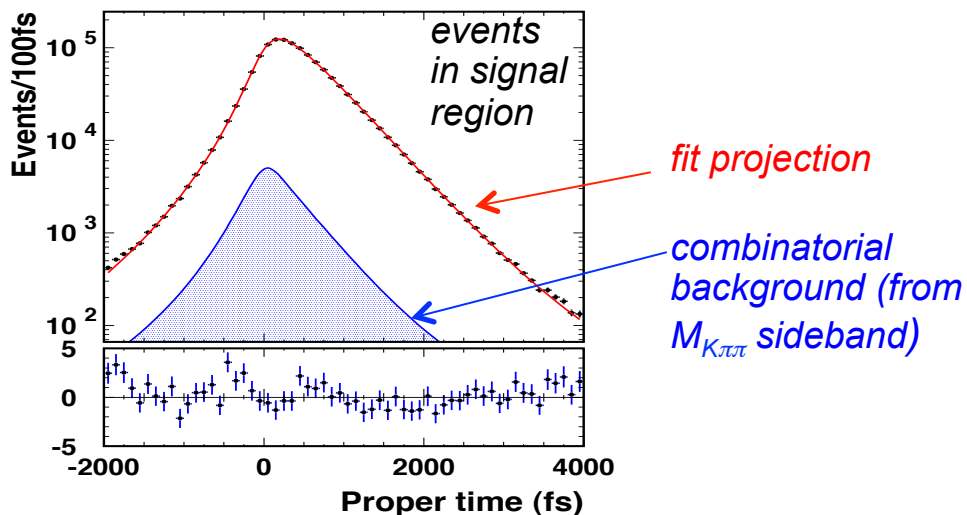
# $D^0(t) \rightarrow K_S \pi^+ \pi^-$ : time-dependent Dalitz plot fit

Resonance	Amplitude	Phase (deg)	Fit fraction
$K^*(892)^-$	$1.590 \pm 0.003$	$131.8 \pm 0.2$	0.6045
$K_0^*(1430)^-$	$2.059 \pm 0.010$	$-194.6 \pm 1.7$	0.0702
$K_2^*(1430)^-$	$1.150 \pm 0.009$	$-41.5 \pm 0.4$	0.0221
$K^*(1410)^-$	$0.496 \pm 0.011$	$83.4 \pm 0.9$	0.0026
$K^*(1680)^-$	$1.556 \pm 0.097$	$-83.2 \pm 1.2$	0.0016
$K^*(892)^+$	$0.139 \pm 0.002$	$-42.1 \pm 0.7$	0.0046
$K_0^*(1430)^+$	$0.176 \pm 0.007$	$-102.3 \pm 2.1$	0.0005
$K_2^*(1430)^+$	$0.077 \pm 0.007$	$-32.2 \pm 4.7$	0.0001
$K^*(1410)^+$	$0.248 \pm 0.010$	$-145.7 \pm 2.9$	0.0007
$K^*(1680)^+$	$1.407 \pm 0.053$	$86.1 \pm 2.7$	0.0013
$\rho(770)$	1 (fixed)	0 (fixed)	0.2000
$\omega(782)$	$0.0370 \pm 0.0004$	$114.9 \pm 0.6$	0.0057
$f_2(1270)$	$1.300 \pm 0.013$	$-31.6 \pm 0.5$	0.0141
$\rho(1450)$	$0.532 \pm 0.027$	$80.8 \pm 2.1$	0.0012

Resonance	Amplitude	Phase (deg)
$\pi\pi$ S-wave		
$\beta_1$	$4.23 \pm 0.02$	$164.0 \pm 0.2$
$\beta_2$	$10.90 \pm 0.02$	$15.6 \pm 0.2$
$\beta_3$	$37.4 \pm 0.3$	$3.3 \pm 0.4$
$\beta_4$	$14.7 \pm 0.1$	$-8.9 \pm 0.3$
$f_{11}^{\text{prod}}$	$12.76 \pm 0.05$	$-161.1 \pm 0.$
$f_{12}^{\text{prod}}$	$14.2 \pm 0.2$	$-176.2 \pm 0.$
$f_{13}^{\text{prod}}$	$10.0 \pm 0.5$	$-124.7 \pm 2.$
$K\pi$ S-wave	<b>Parameters</b>	
$M(\text{MeV}/c^2)$	$1461.7 \pm 0.8$	
$\Gamma(\text{MeV}/c^2)$	$268.3 \pm 1.1$	
F	$0.4524 \pm 0.005$	
$\phi_F(\text{rad})$	$0.248 \pm 0.003$	
R	1 (fixed)	

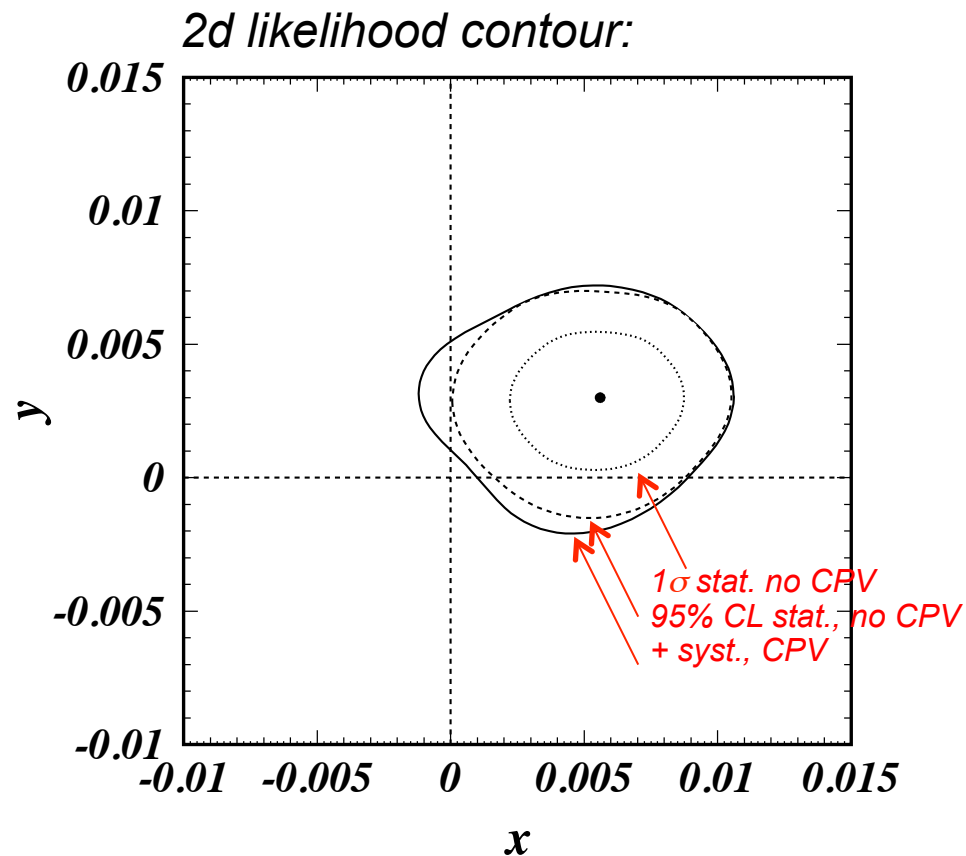
Fit projections:  
(fitted function describes the data well)





Fit type	Parameter	Fit result
No CPV	$x$ (%)	$0.56 \pm 0.19^{+0.03+0.06}_{-0.09-0.09}$
	$y$ (%)	$0.30 \pm 0.15^{+0.04+0.03}_{-0.05-0.06}$
CPV	$x$ (%)	$0.56 \pm 0.19^{+0.04+0.06}_{-0.08-0.08}$
	$y$ (%)	$0.30 \pm 0.15^{+0.04+0.03}_{-0.05-0.07}$
	$ q/p $	$0.90^{+0.16+0.05+0.06}_{-0.15-0.04-0.05}$
	$\arg(q/p)$ ( $^\circ$ )	$-6 \pm 11 \pm 3^{+3}_{-4}$

$$\tau = (410.3 \pm 0.6) \text{ fs}$$



$\Delta\chi^2 \Rightarrow$  mixing significance =  $2.5\sigma$  but no evidence for indirect or direct CPV



Source	No CPV		CPV			
	$\Delta x/10^{-4}$	$\Delta y/10^{-4}$	$\Delta x/10^{-4}$	$\Delta y/10^{-4}$	$ q/p /10^{-2}$	$\arg(q/p)/^\circ$
Best candidate selection	+1.0	+1.9	+1.3	+2.0	-2.3	+2.2
Signal and background yields	$\pm 0.3$	$\pm 0.3$	$\pm 0.4$	$\pm 0.4$	$\pm 1.2$	$\pm 0.8$
Fraction of wrong tagged events	-0.7	-0.4	-0.5	+0.4	+1.1	+0.8
Time resolution of signal	-1.4	-0.9	-1.2	-0.8	+0.8	-1.2
Efficiency	-1.1	-2.1	-1.4	-2.2	+3.1	+1.3
Combinatorial PDF	+1.9 -4.8	+2.3 -3.9	+2.4 -4.1	+2.0 -4.4	+1.2 -2.9	+2.8 -2.3
$K^*(892)$ DCS/CF reduced by 5%	-7.3	+2.3	-6.9	+3.1	+3.3	-1.4
$K_2^*(1430)$ DCS/CF reduced by 5%	+1.7	-0.7	+2.2	-0.2	+1.1	+0.4
Total	+2.8 -8.9	+3.7 -4.6	+3.6 -8.3	+4.3 -5.1	+5.0 -4.0	+3.3 -3.0

→

Systematics due to decay model:

Source	No CPV		CPV			
	$\Delta x/10^{-4}$	$\Delta y/10^{-4}$	$\Delta x/10^{-4}$	$\Delta y/10^{-4}$	$ q/p /10^{-2}$	$\arg(q/p)/^\circ$
Resonance M & $\Gamma$	$\pm 1.4$	$\pm 1.2$	$\pm 1.2$	$\pm 1.3$	$\pm 2.1$	$\pm 1.0$
$K^*(1680)^+$ removal	-1.8	-3.0	-2.2	-2.8	+2.1	-1.2
$K^*(1410)^\pm$ removal	-1.2	-3.6	-1.7	-3.9	-1.3	+1.4
$\rho(1450)$ removal	+2.1	+0.3	+2.1	+0.5	-1.9	+0.9
Form factors	+4.0	+2.4	+4.3	+2.0	-2.4	-1.0
$\Gamma(q^2) = \text{constant}$	+3.3	-1.6	+4.1	-2.3	-1.6	+1.3
Angular dependence	-8.5	-3.9	-7.4	-3.6	+5.6	-3.2
K-matrix formalism	-2.2	+1.8	-3.5	+2.4	-3.6	+1.1
Total	+5.8 -9.1	+3.2 -6.4	+6.4 -8.4	+3.4 -6.9	+6.4 -5.1	+2.5 -3.7



# Belle time-dependent $D^0(t) \rightarrow K^+K^-, \pi^+\pi^-$

presented by Staric at CHARM 2012 (arXiv:1212.3478); update of Staric et al., PRL 98, 211803 (2007)

$$y_{CP} = \frac{\tau(K^-\pi^+)}{\tau(K^+K^-)} - 1 = (|q/p| + |p/q|)y \cos \phi - (|q/p| - |p/q|)x \sin \phi$$

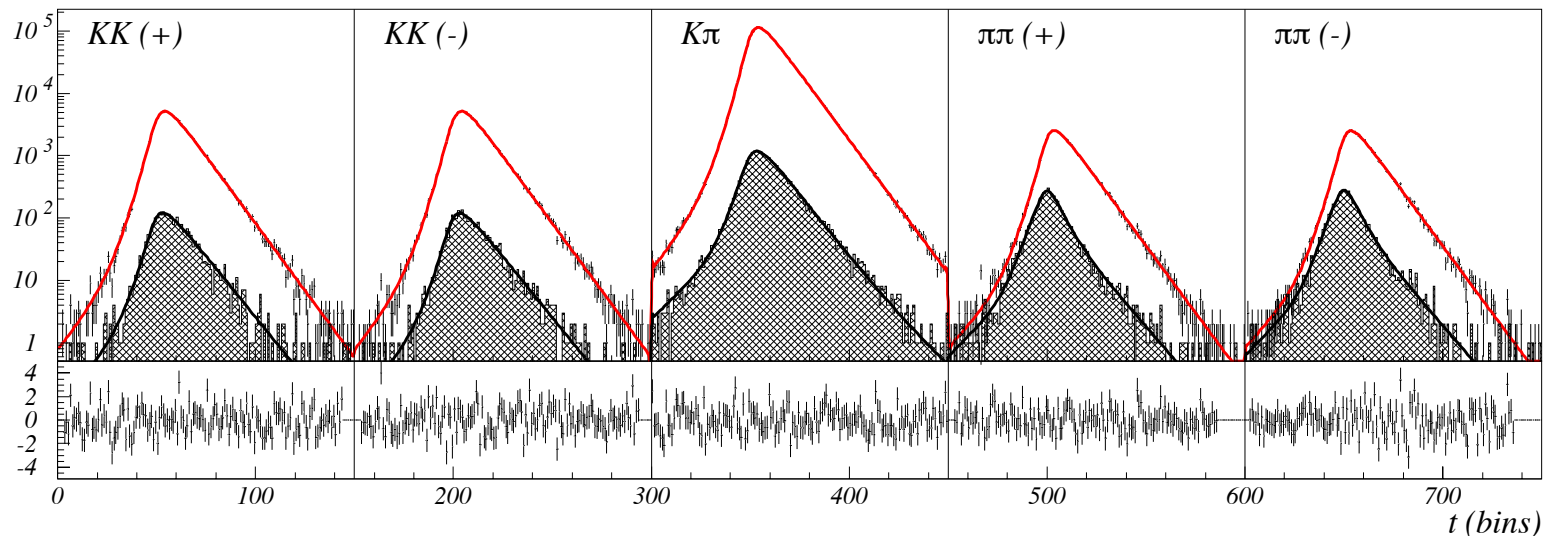
$$A_{\Gamma} = \frac{\tau(\bar{D}^0 \rightarrow K^+K^-) - \tau(D^0 \rightarrow K^+K^-)}{\tau(\bar{D}^0 \rightarrow K^+K^-) + \tau(D^0 \rightarrow K^+K^-)} = (|q/p| - |p/q|)y \cos \phi - (|q/p| + |p/q|)x \sin \phi$$

$= -a_{int} - a_{indirect}$  contribution to  $A_{CP}$

## Method:

- 1) tag flavor via  $D^{*+} \rightarrow D^0\pi^+$
- 2) determine resolution function from MC/data studies
- 3) do simultaneous binned fit to  $K^+K^-, K^-\pi^+, \pi^+\pi^-$  samples

$\chi^2/ndf = 792.9/684$  (CL= 0.2%)



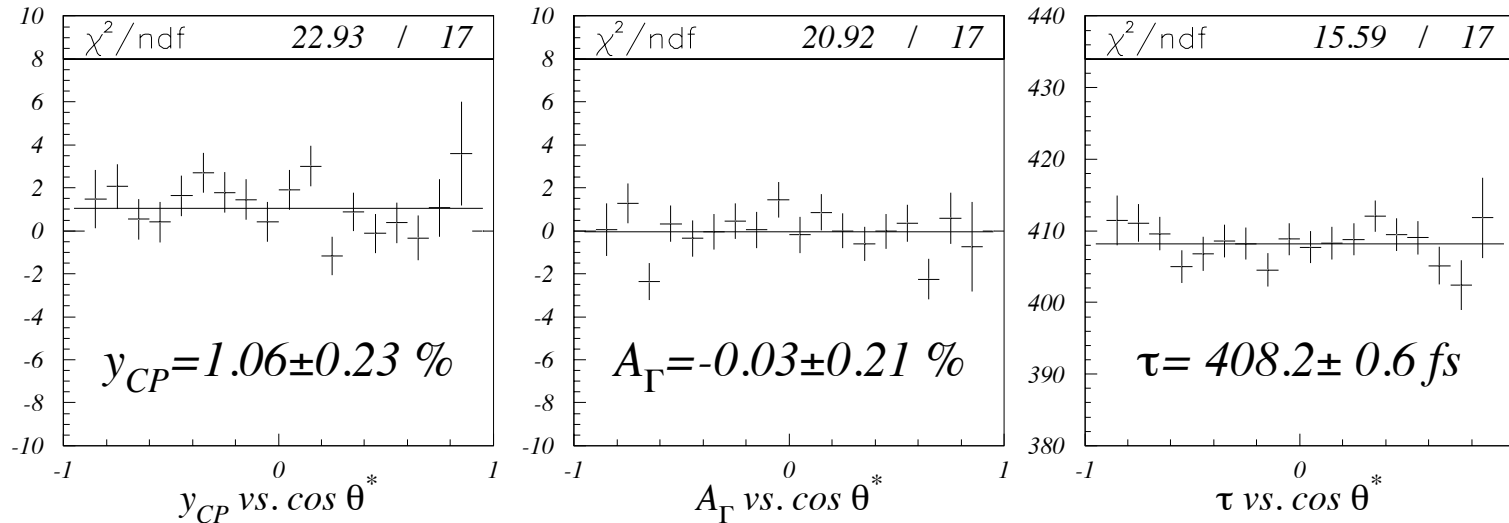


# Belle time-dependent $D^0(t) \rightarrow K^+K^-, \pi^+\pi^-$ (cont'd)

arXiv:1212.3478; update of Staric et al., PRL 98, 211803 (2007)

**Note:** as resolution function depends on  $D^0$  CMS angle ( $\theta^*$ ), fit is performed in bins of  $\cos \theta^*$

**977 fb<sup>-1</sup> preliminary:**



$$y_{CP} = (+1.11 \pm 0.22 \pm 0.11)\%$$

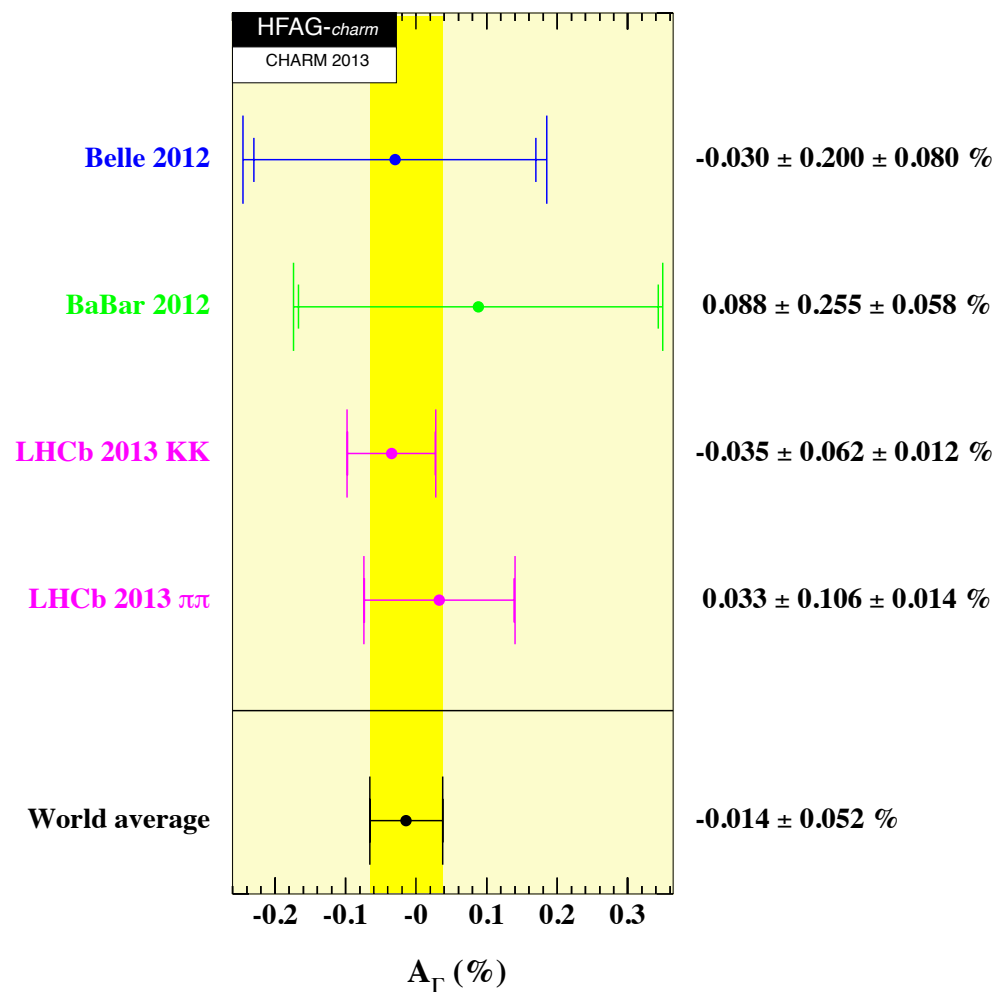
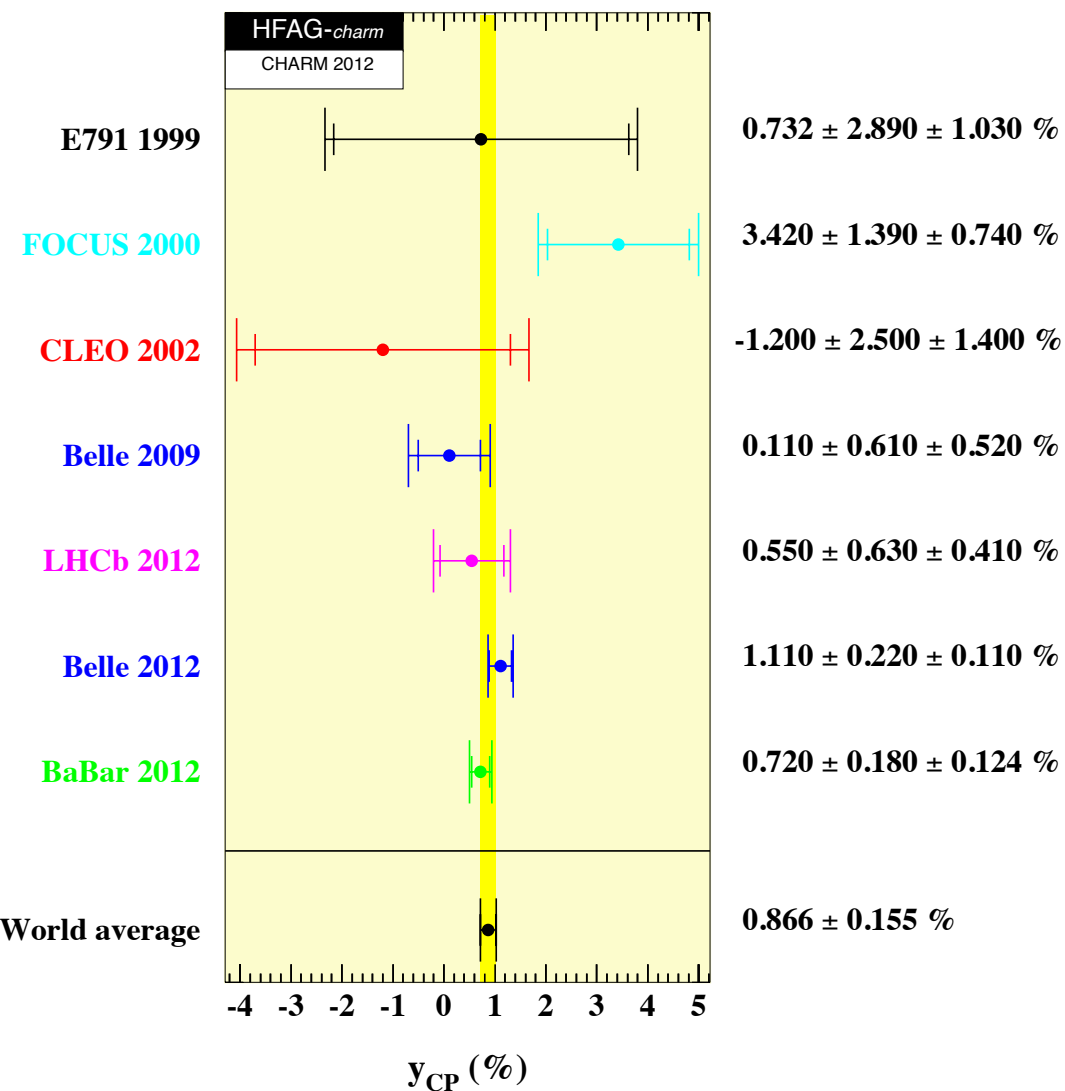
$$A_\Gamma = (-0.03 \pm 0.20 \pm 0.08)\%$$

*was*  
(world's most precise to-date)



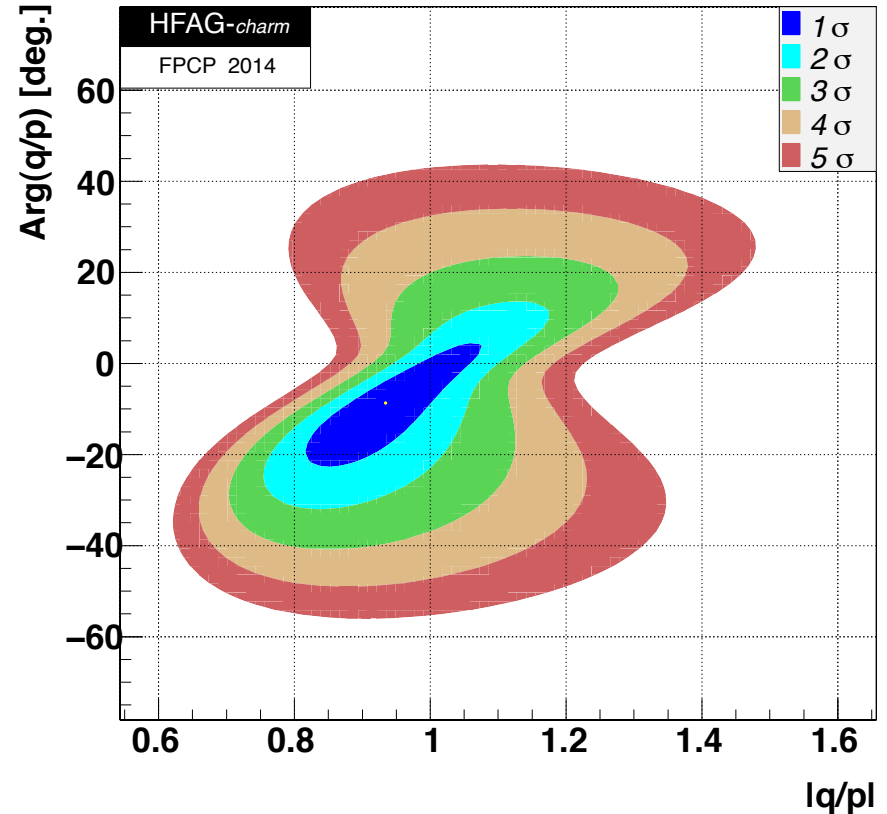
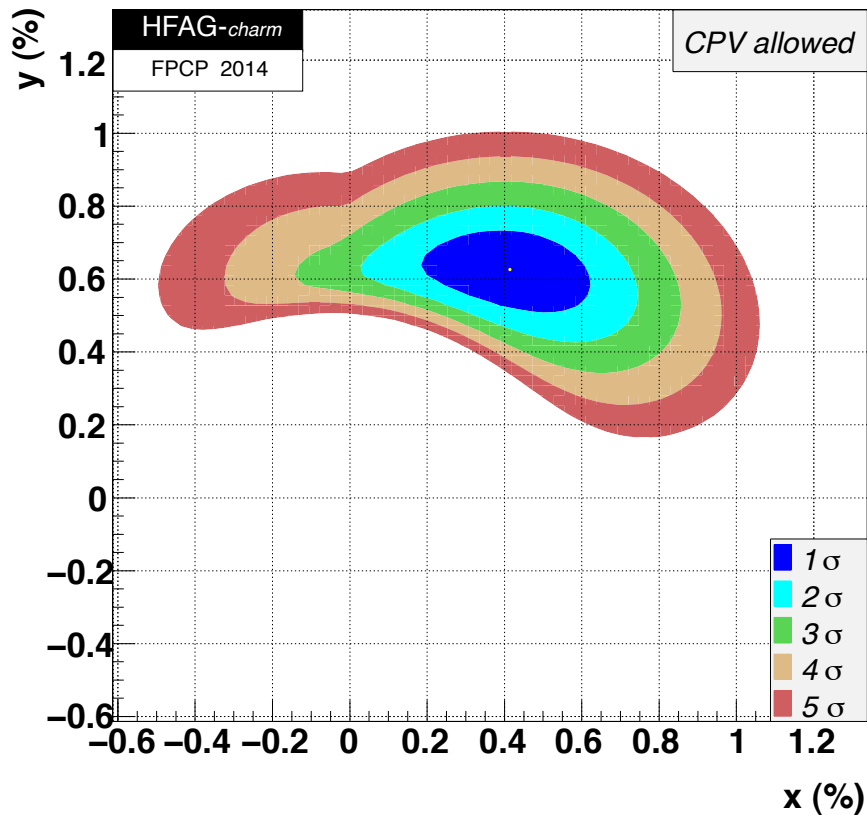
# HFAG World Averages

[www.slac.stanford.edu/xorg/hfag/charm/index.html](http://www.slac.stanford.edu/xorg/hfag/charm/index.html)



# HFAG global fit to all available data

45 measured observables, 10 theoretical fitted parameters:  $x, y, \delta, \delta_{K\pi\pi}, R_D, A_D, |q/p|, \phi, A_K, A_\pi$   
 (for details see Marco Gersabeck's talk & [www.slac.stanford.edu/xorg/hfag/charm/index.html](http://www.slac.stanford.edu/xorg/hfag/charm/index.html))



$\Delta\chi^2$  at no mixing point  $(x,y) = (0,0) > 420$  ( $>12\sigma$ ) [ $x: > 2.4\sigma, y: > 9.4\sigma$ ]  
 No CPV ( $|q/p|, \phi) = (1,0)$  point:  $\Delta\chi^2 = 1.32, CL = 0.48$ , consistent with no CPV



# Belle II expectations for $\bar{D}^0$ - $D^0$ mixing and CPV

**Expected Uncertainties** (M. Staric, KEK FFW14):

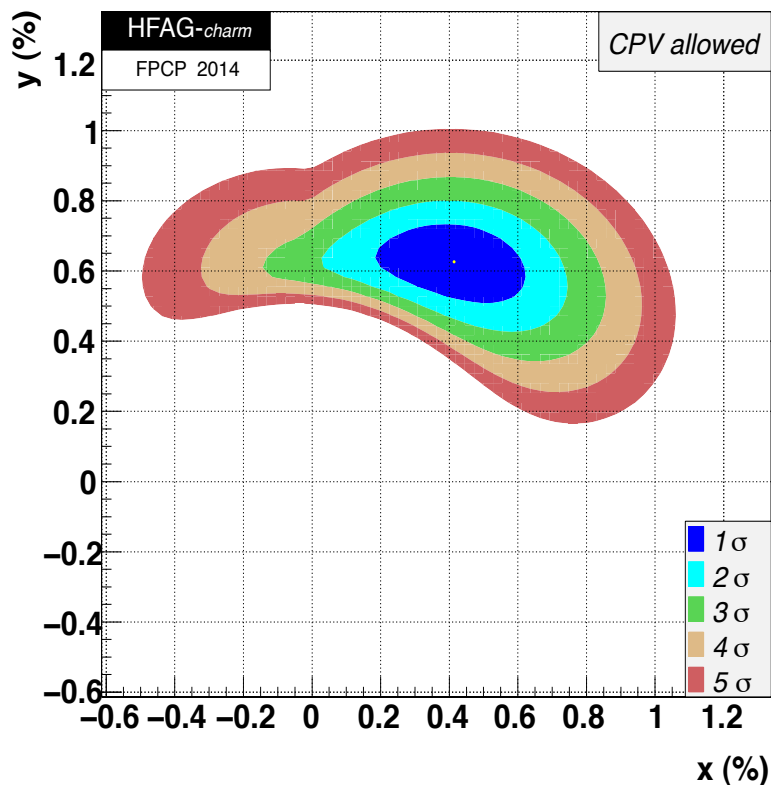
Analysis	Observable	Uncertainty (%)		
		Now ( $\sim 1 \text{ ab}^{-1}$ )	$\mathcal{L} = 50 \text{ ab}^{-1}$	
$K_S^0 \pi^+ \pi^-$	$x$	0.19	0.08	<i>factor of ~3 better</i>
	$y$	0.15	0.05	
	$ q/p $	16	6	
	$\phi$	$11^\circ$	$4^\circ$	
$\pi^+ \pi^-, K^+ K^-$	$y_{CP}$	0.22	0.04	<i>factor of ~6 better</i>
	$A_\Gamma$	0.20	0.03	
$K^+ \pi^-$	$x'^2$	0.022	0.003	<i>factor of 8-10 better</i>
	$y'$	0.34	0.04	
	$ q/p $	0.6	0.06	
	$\phi$	$25^\circ$	$2.3^\circ$	

**Note:** statistical error and some systematics scale by luminosity, but other systematics do not.

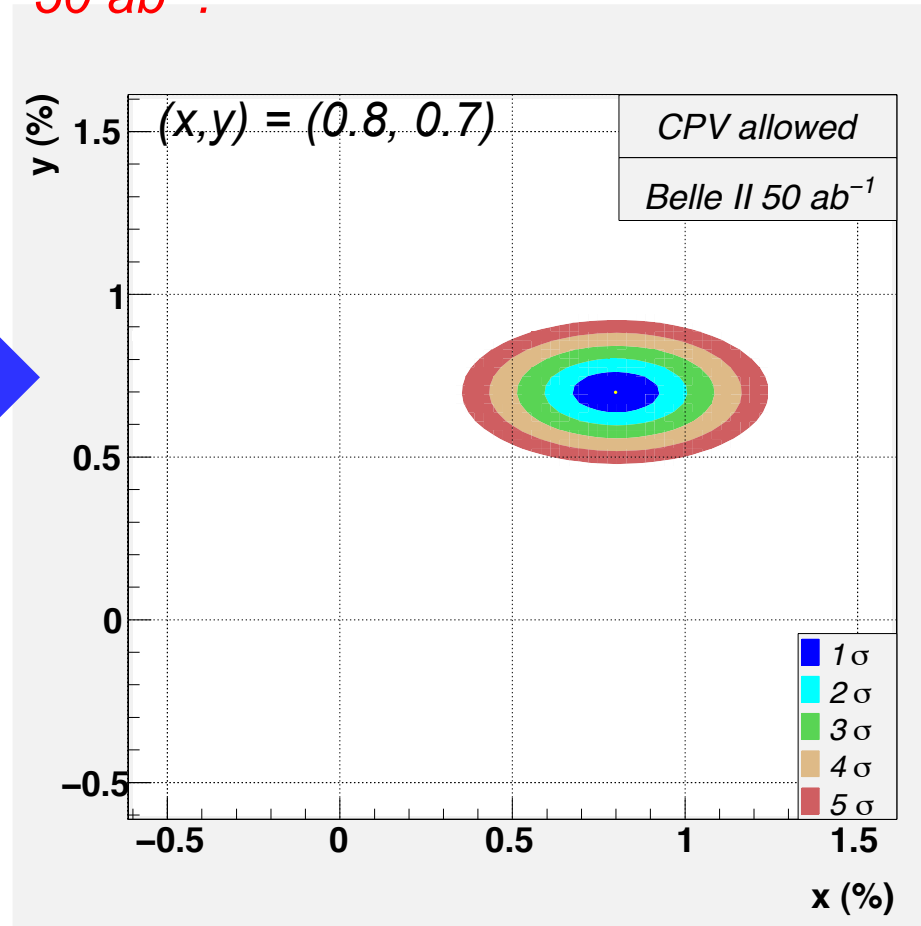


# Belle II expectations for $\bar{D}^0$ - $D^0$ mixing

Now:



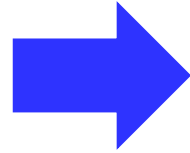
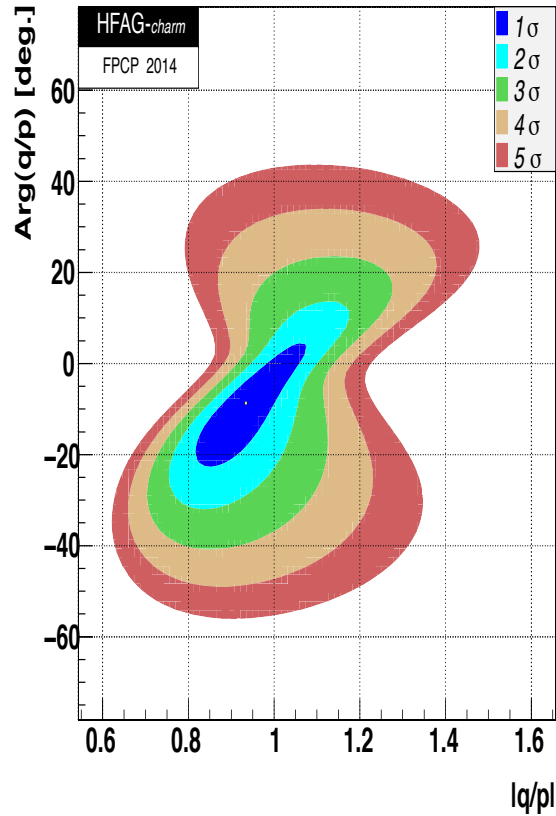
50  $ab^{-1}$ :



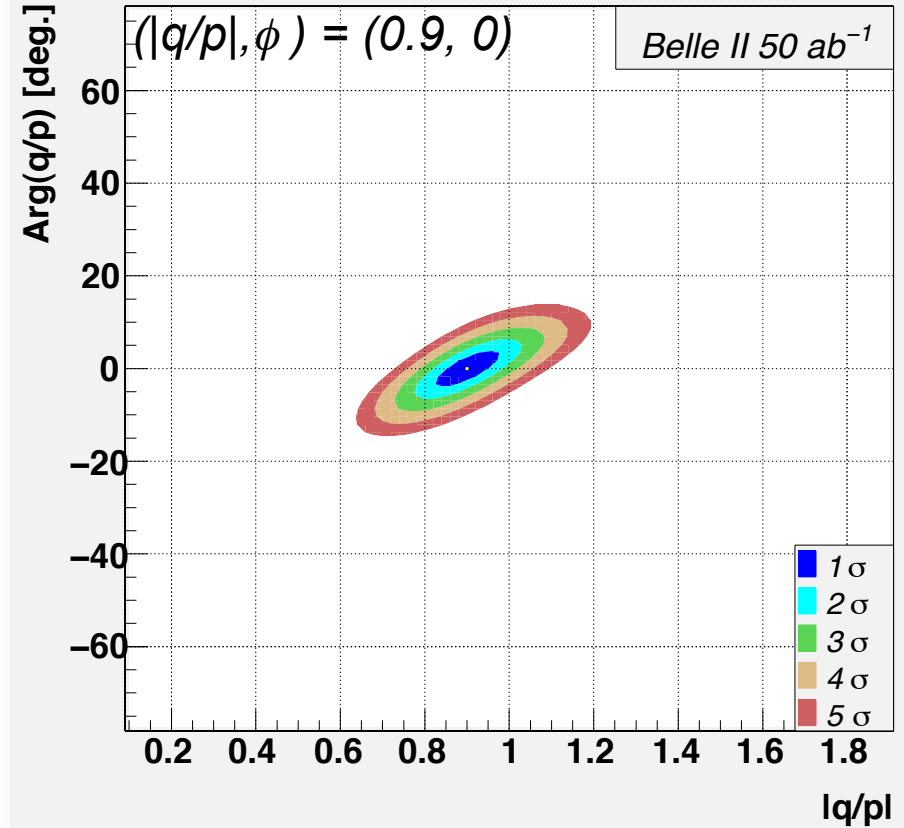
**Current measurements of  $x, y$  give many constraints on NP models**

[see Golowich et al., PRD76, 095009 (2007); 21 models considered, e.g., 2-Higgs doublets, left-right models, little Higgs, extra dimensions, of which 17 give constraints]

Now:



50  $ab^{-1}$ :



**Note:** LHCb will dominate most of these measurements, but Belle II should be competitive in  $y_{CP}$  and possibly in  $x'^2$ ,  $y'$ ,  $|q/p|$ ,  $\phi$  (see Staric, KEK FFW14). *If LHCb sees new physics, it would be important for Belle II to independently confirm.*



# Summary

## time-dependent $D^0(t) \rightarrow K^+\pi$

976  $\text{fb}^{-1}$  published:  $R_D = (3.53 \pm 0.13) \times 10^{-3}$   
 $x'^2 = (0.09 \pm 0.22) \times 10^{-3}$   
 $y' = (0.46 \pm 0.34)\%$

## time-dependent $D^0(t) \rightarrow K_S \pi^+\pi$

921  $\text{fb}^{-1}$  published:  $x = (0.56^{+0.20}_{-0.22})\%$   
 $y = (0.30^{+0.16}_{-0.17})\%$   
 $|q/p| = (0.90^{+0.18}_{-0.16})\%$   
 $\phi = (-6 \pm 12)^\circ$

## time-dependent $D^0(t) \rightarrow K^+K^-, \pi^+\pi$

977  $\text{fb}^{-1}$  preliminary:  $y_{\text{CP}} = (1.11 \pm 0.22 \pm 0.11)\%$   
 $A_{\text{F}} = (-0.03 \pm 0.20 \pm 0.08)\%$



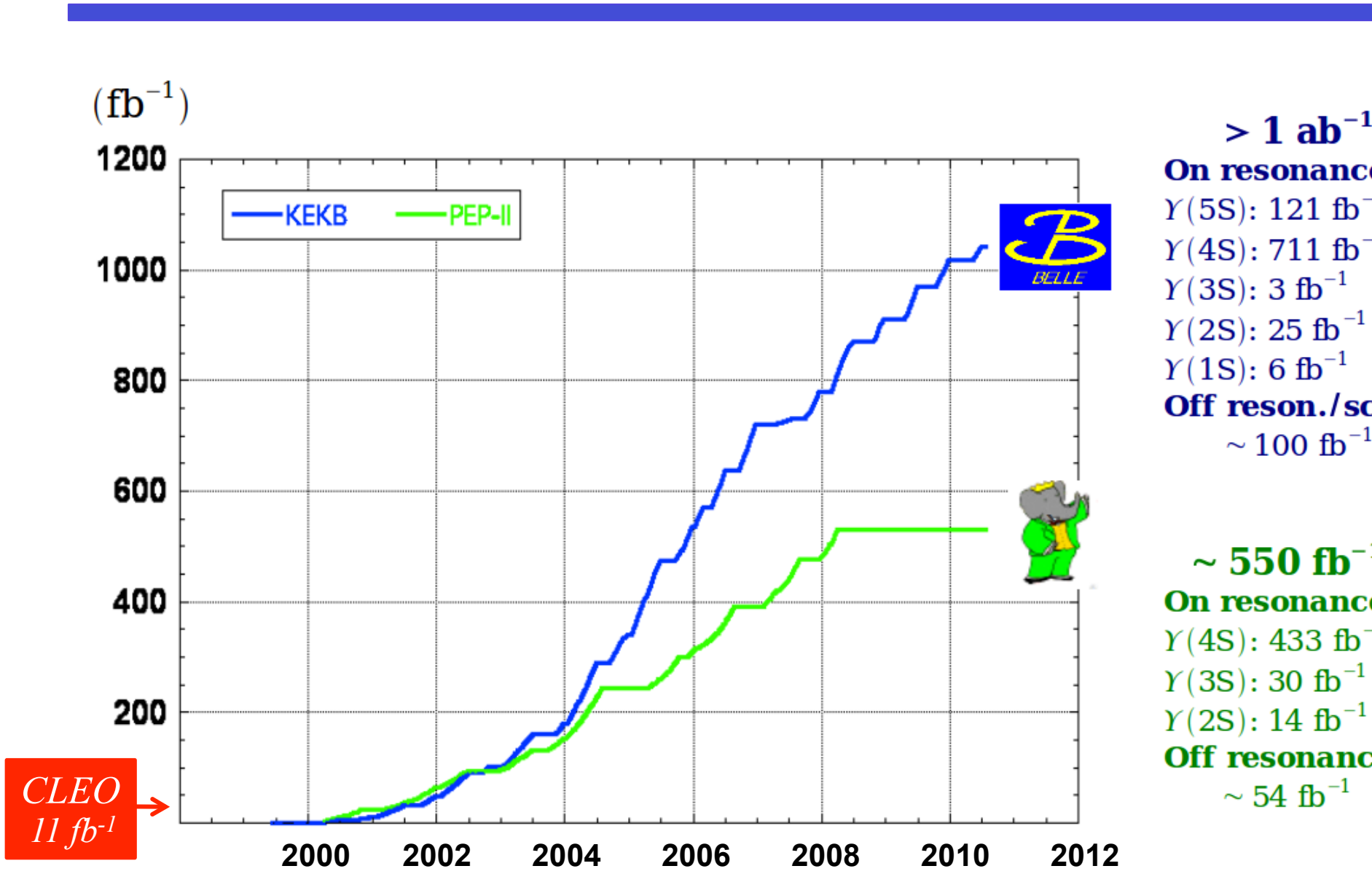
Evidence for mixing is unequivocal:  $K^+\pi$  alone is  $5.1\sigma$ ; combined with all other world data is  $>12\sigma$ . No sign yet of indirect CPV. However, the sensitivity of these searches will greatly improve (factor of  $\sim 50$  statistics) at Belle II



# Extra/Backup



# B factory performance – final tally:



**> 1 ab<sup>-1</sup>**

**On resonance:**

Y(5S): 121 fb<sup>-1</sup>

Y(4S): 711 fb<sup>-1</sup>

Y(3S): 3 fb<sup>-1</sup>

Y(2S): 25 fb<sup>-1</sup>

Y(1S): 6 fb<sup>-1</sup>

**Off reson./scan:**

~ 100 fb<sup>-1</sup>

**~ 550 fb<sup>-1</sup>**

**On resonance:**

Y(4S): 433 fb<sup>-1</sup>

Y(3S): 30 fb<sup>-1</sup>

Y(2S): 14 fb<sup>-1</sup>

**Off resonance:**

~ 54 fb<sup>-1</sup>

**CLEO**  
11 fb<sup>-1</sup>