

Quantum Correlated Charm @ Threshold

*and $\phi_3 = \gamma$
from B Decays*

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*Full disclosure: member of
CLEO-c / BESIII / BelleII

Outline

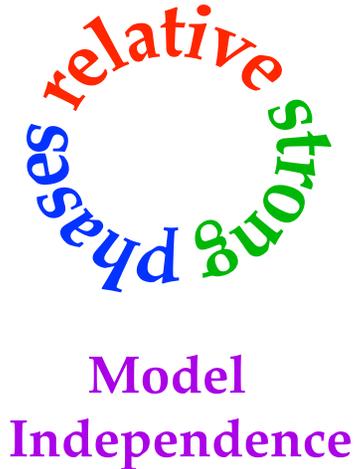
Introduction: Essentials

Overview of Results

Recent Published Results

Preliminary $K_S \pi^+ \pi^-$ Results

Conclusion



- Access to relative $D^0, D^{0\text{bar}}$ *strong phase differences*
 - Directly measure what B analyses need with *no models*
 - Useful inputs to *CKM γ extractions w/ $B \rightarrow D^{(*)} K^{(*)}, D^{(*)} \pi$*
 - Also relevant for *D mixing*
- (*and just plain fun to see EPR-like correlations in HEP experiment!)*

Introduction

Threshold production of charm with $e^+e^- \rightarrow \psi$ (3770)

Decays to *coherent* pair of D mesons

$$\psi(3770) \rightarrow [D^0 \quad D^{0\text{bar}} - D^{0\text{bar}} \quad D^0] / \sqrt{2} \quad (\text{Eq 1})$$

$$= - [D_{\text{CP}^+} \quad D_{\text{CP}^-} - D_{\text{CP}^-} \quad D_{\text{CP}^+}] / \sqrt{2} \quad (\text{Eq 2})$$

$$D_{\text{CP}^\pm} = [D^0 \pm D^{0\text{bar}}] / \sqrt{2}$$

Measure various combination of rates for:

one decay mode only \rightarrow “single tags”

two decay modes \rightarrow “double tags”

Naïve Get interference with CP tags since they project
2nd meson into a $D^0, D^{0\text{bar}}$ superposition (Eq 2)

Truth Yes, but we get interference even *without* CP tags:
Terms in Eq 1 already interfere ...
(1st vs. 2nd D means +z vs. -z along decay axis)

Decay Modes

Flavored

Flavored semileptonic	$K^-e^+\nu, K^-\mu^+\nu$	Pure CF
Flavored hadronic	$K^-\pi^+, K^-\pi^+\pi^0, K^-\pi^+\pi^+\pi^-$	CF + DCSD

Self-conjugate

2-body CP eigenstate	$K^-K^+, \pi^+\pi^-, K_S\pi^0, \dots$	SCS
Multi body	$K_S h^+h^-, K_L h^+h^-$	CF + DCSD
Multi body	$K^+K^-\pi^+\pi^-, \pi^+\pi^-\pi^0$	SCS

Neither

$K_S K^-\pi^+$ SCS

Both

* not possible *

Blue modes: already used for γ green : future? [black: tag only]

“h” = K, π

CF : Cabibbo-Favored

SCS : Singly-Cabibbo-Suppressed

DCSD : Double-Cabibbo-Suppressed (Decay)

Multi-Body “Coherence Factors”

Simplified Two body:

$$|A_1 + A_2|^2 = |A_1|^2 + |A_2|^2 + 2 A_1 A_2 e^{-i\delta} \quad | \quad 1, 2 = \text{CF, DCSD}$$

Generalization \rightarrow Atwood-Soni :

Integrate over Dalitz plot; define real average amplitudes
[$\mathcal{A} \rightarrow A$ below]

BUT this requires a “fudge factor” of $\text{Re}^{-i\delta}$ for interference term

Simplified Multi body:

$$\int d \text{Dalitz} | \mathcal{A}_1 + \mathcal{A}_2 |^2 = | A_1 |^2 + | A_2 |^2 + 2 R e^{-i\delta} A_1 A_2 |$$

Define: $R e^{-i\delta} = (\text{true cross-term}) / (\text{naïve} = A_1 A_2)$

Note: $R < 1$ due to two reasons: varying phase & “ $|r(x)| \neq 1$ ”

$$A_{K^\pm \pi^\mp \pi^0}^2 = \int | \mathcal{A}_{K^\pm \pi^\mp \pi^0}(\mathbf{x}) |^2 d\mathbf{x}$$

$$R_{K\pi\pi^0} e^{-i\delta_D^{K\pi\pi^0}} = \frac{\int \mathcal{A}_{K^- \pi^+ \pi^0}(\mathbf{x}) \mathcal{A}_{K^+ \pi^- \pi^0}(\mathbf{x}) d\mathbf{x}}{A_{K^- \pi^+ \pi^0} A_{K^+ \pi^- \pi^0}}$$

QC for Pedestrians I

Simplest effect:

$$\psi(3770) \rightarrow [D_{CP+} D_{CP-} - D_{CP-} D_{CP+}] / \sqrt{2}$$

Like CP (++, --): cancels *Unlike CP* (+-, -+): doubled

My favorite general form:

* Ignore mixing for now *

$$\Gamma_{FG} / A_F^2 A_G^2 = [r_F^2 + r_G^2 + 2 r_F r_G R_F R_G \cos(\delta_G - \delta_F)]$$

or $1 + r_F^2 r_G^2 + \dots$: factor out A_i such that $r < 1$

→ $r_{F,G}$ (averaged) amplitude ratios: $\sim A(D^{0\text{bar}} \rightarrow F,G) / A(D^0 \rightarrow F,G)$

1 for CP eigenstates

$\sim \tan^2(\theta_C)$ for hadronic K^- modes [DCSD/CF]

0 for semileptonic → no interference

→ R, δ : Atwood-Soni coherence factors

$R=1; \delta = 0, \pi$ for CP eigenstates;

$R=1; \delta = ?$ for $K^- \pi^+$

Both non-trivial for multi-body hadronic

QC for Pedestrians II

Need some double-tag rate with two “non-trivial” modes to fully separate parameters

→ If not, get only $\text{Re}[R e^{-i\delta}] = R \cos \delta$, not separate (R, δ)
[Or, only c_i , not both c_i, s_i]

The reason this works is simple trigonometry:

$$\cos(\delta_2 - \delta_1) = \cos\delta_1 \cos\delta_2 - \sin\delta_1 \sin\delta_2$$

With this, one has enough observables to separate
(& can still use modes where one $\delta_i = 0$)

Two “non-trivial” modes ?

- Can be different values of n in $K^-(n\pi)^+$ analyses
- Can even be different bins (i) in $K_S \pi^+ \pi^- c_i, s_i$ analyses

From Tags to Physics

CP+ & CP- tags:

Switch of +- flips sign of interference term

Used for γ , but trivial: no need to study w/ charm [GLW]

Semileptonic flavor tags:

No interference; clean normalization [but pesky v...]

Hadronic flavor tags:

Normalization, modulo DCSD [easier than semilep for exp.]

Also modes we want to study [ADS]

Multi-body self-conjugate

Modes we want to under study [GGSZ]

Different analyses use different numbers of tag modes

CLEO $K^-\pi^+$ & CLEO-c, BESIII $K_S\pi^+\pi^-$ use *many* tags

BESIII $K^-\pi^+$ uses only signal and CP tags

Experimental Output

$K^-K^+, \pi^+\pi^-$	GLW	$\delta = 0, \pi$	
$K^- \pi^+$	ADS	δ (R=1)	get from threshold charm...
$K^- \pi^+ \pi^0, K^- \pi^+ \pi^+ \pi^-, K_S K^- \pi^+$	ADS+	R, δ	
$K_S \pi^+ \pi^-, K_S K^+ K^-$	GGSZ	c_i, s_i	

R, δ are Atwood-Soni coherence factors for ADS modes

→ *No relative D^0 - $D^{0\text{bar}}$ phase* in separate $D^0, D^{0\text{bar}}$ Dalitz fits

e.g., if one fits N amplitudes to $D^0, D^{0\text{bar}}$ separately: [D^* -tagged @ B factory]
only gets $2(N-1) = 2N-2$ out of $2N-1$ relative phases

→ Also *avoid Dalitz models*

c_i, s_i are “Cartesian R, δ in Dalitz bins” for GGSZ modes

→ Here, relative D^0 - $D^{0\text{bar}}$ phase is trivial

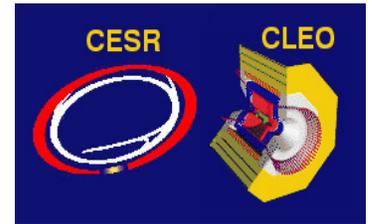
(distinction due to self-conjugate modes, not changing basis to c_i, s_i !)

→ But we still *avoid Dalitz models*

CLEO-c Results

CLEO-c Data : 0.8 fb⁻¹ @ $\Psi(3770)$ & 0.6 fb⁻¹ @ 4170 MeV 2003 - 08

$K^-\pi^+$	281 pb ⁻¹ (updated below)	PRL 100, 221801 (2008); PRD, 78, 012001 (2008) [= more details]	
$K^-\pi^+\pi^0, K^-\pi^+\pi^+\pi^-$	818 pb ⁻¹	PRD 80, 031105(R) (2009)	
$K_S\pi^+\pi^-$	818 pb ⁻¹	PRD 80, 032002 (2009)	
$K_{S,L}h^+h^-$	818 pb ⁻¹	PRD 82, 112006 (2010)	
$K_S K^+\pi^-$	818 pb ⁻¹ *	PRD 85, 092016 (2012)	
$K^-\pi^+$	→ 818 pb ⁻¹	PRD 86, 112001 (2012)	
$K^+K^-\pi^+\pi^-$	818 pb ⁻¹ **	PRD 85, 122002 (2012)	{ isobar analysis; but <i>first D, D^{bar}</i>



also use high-E continuum { * + 15 fb⁻¹ ~10 GeV
** + 24 fb⁻¹ ~10 GeV & 600 pb⁻¹ 4.17 GeV

Today's Main Topics

BESIII Results

Dataset : 2.92 fb^{-1} 2010 - 11 (1 $\frac{2}{3}$ years) \rightarrow 3.5x CLEO-c
Future ability : $\sim 4 \text{ fb}^{-1}$ / running year [note: $\mathcal{L}_{2011} \gg \mathcal{L}_{2010}$]

The logo for BESIII, with 'B' in blue, 'E' in red, 'S' in green, and 'III' in black.

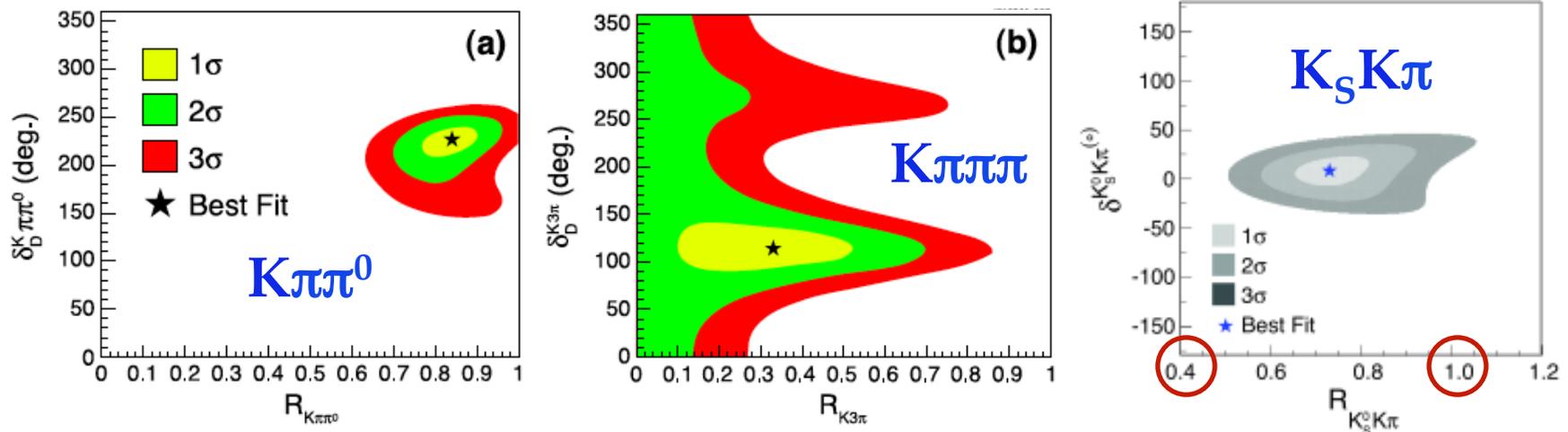
$K^-\pi^+$	2.92 fb^{-1}	PLB 734, 227 (2014)
$K_S^0\pi^+\pi^-$	2.92 fb^{-1}	Preliminary @ APS, Apr 2014
Y_{CP}	2.92 fb^{-1}	Preliminary; will submit soon

[Y_{CP} : see slides by X.R. Lyu; talk running in parallel now !]

CLEO-c "Legacy" Result

$K^-\pi^+\pi^0, K^-\pi^+\pi^+\pi^-$ 818 pb^{-1} PLB 731, 197 (2014)
[CLEO-c data analyzed by past members, after collaboration disbanded]

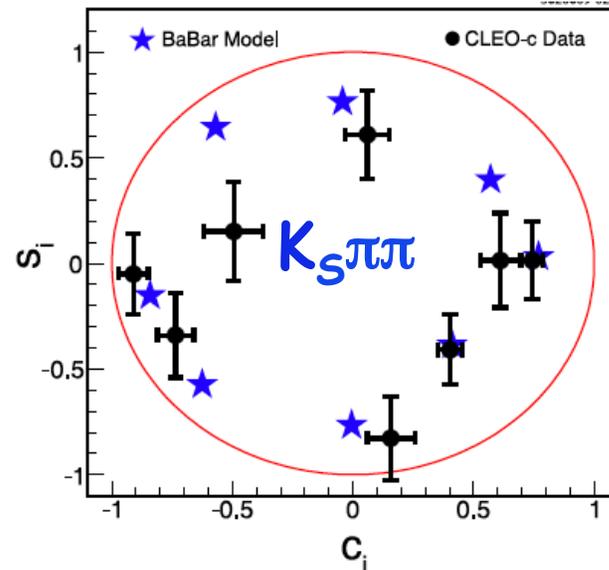
CLEO-c Coherence Factors



Small R for $K\pi\pi$: still useful for r_B !

Or, we could bin across Dalitz plot

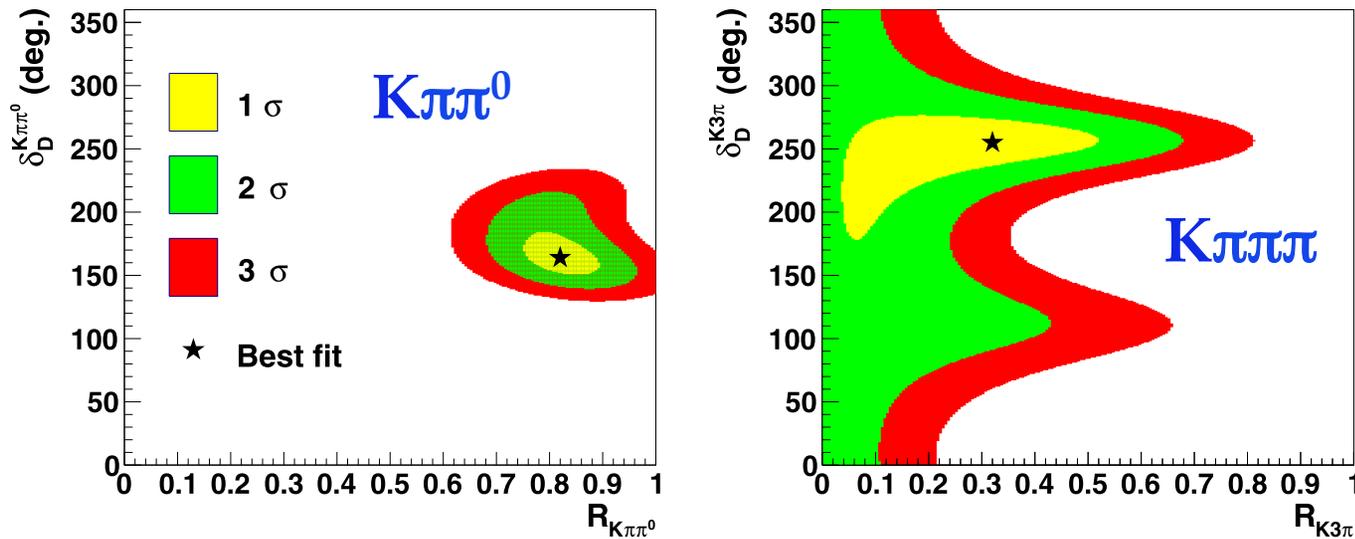
c_i and s_i : bin-averaged
 $\langle R \cos \delta \rangle$ and $\langle R \sin \delta \rangle$



$K^- (n\pi)^+$ Update

PLB 731, 197
(2014) 818 pb⁻¹

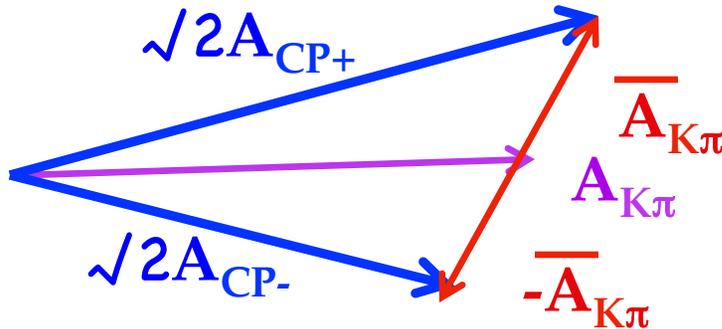
CLEO-c “Legacy data” publication \rightarrow not a collaboration result
(but I personally believe it to be of equal quality)



Note:
 $K\pi\pi\pi$ best fit
now in other
lobe...

- \rightarrow Now includes $K_S\pi^+\pi^-$ tags
- \rightarrow Updated external inputs (BF, mixing, $K\pi$)

Simplified Picture: (simple = no mixing)



Amplitude triangle:

$$CP_{\pm} = CF \pm DCSD$$

[DCSD enhanced for visibility !]

Complex ratio
 DCSD/CF amplitude

$$\frac{\langle K^- \pi^+ | \overline{D}^0 \rangle}{\langle K^- \pi^+ | D^0 \rangle} = -r e^{-i\delta_{K\pi}}$$

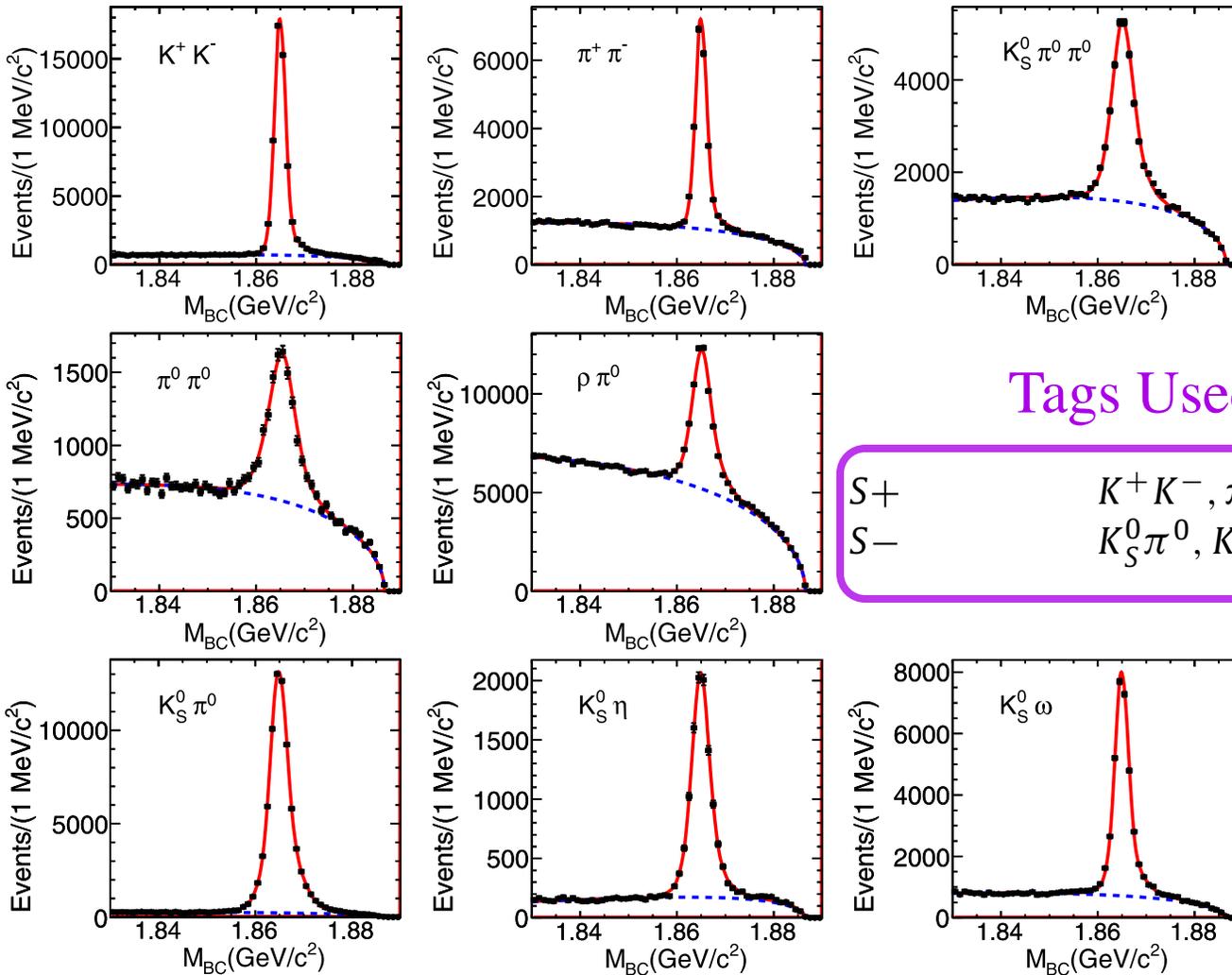
Flip CP of tag: reverses interference term

CP-tagged rate asymmetry (essentially) measures $r \cos \delta$

$$\begin{aligned} \mathcal{A}_{CP} &= [|A_{CP-}|^2 - |A_{CP+}|^2] / [|A_{CP-}|^2 + |A_{CP+}|^2] \\ &= r \cos \delta \quad (+ D \text{ mixing corrections: } y, R_{WS}) \end{aligned}$$

← measure
 ← extract

First BESIII Quantum Coherence result : *straightforward analysis*



Tags Used: 5 CP+, 3 CP-

$S+$	$K^+K^-, \pi^+\pi^-, K_S^0\pi^0\pi^0, \pi^0\pi^0, \rho^0\pi^0$
$S-$	$K_S^0\pi^0, K_S^0\eta, K_S^0\omega$

$$\mathcal{A}_{K\pi}^{CP} \equiv \frac{\mathcal{B}_{D^{S-} \rightarrow K^- \pi^+} - \mathcal{B}_{D^{S+} \rightarrow K^- \pi^+}}{\mathcal{B}_{D^{S-} \rightarrow K^- \pi^+} + \mathcal{B}_{D^{S+} \rightarrow K^- \pi^+}}$$

$S+$ ($S-$) denotes the CP -even (CP -odd) eigenstate.

Direct result : *

$$\mathcal{A}_{CP} = (12.7 \pm 1.3 \pm 0.7)\%$$

$$2r \cos \delta_{K\pi} + y = (1 + R_{WS}) \cdot \mathcal{A}_{K\pi}^{CP}$$

Using external inputs for $r_{K\pi}$, R_{WS} , y , we extract :

$$\cos \delta_{K\pi} = 1.02 \pm 0.11 \pm 0.06 \pm 0.01$$

Compare to CLEO-c:

$$\cos \delta_{K\pi} = 0.81^{+0.22}_{-0.18} {}^{+0.07}_{-0.06} \quad (\text{no external inputs})$$

$$\cos \delta_{K\pi} = 1.15^{+0.19}_{-0.17} {}^{+0.00}_{-0.08} \quad (\text{w/ external inputs})$$

* HFAG can use this, I believe: they now omit final $\delta_{K\pi}$ due to external inputs ...

Classic “GGSZ mode”; better precision than CLEO-c
Preliminary results presented @ APS meeting, Apr 2014

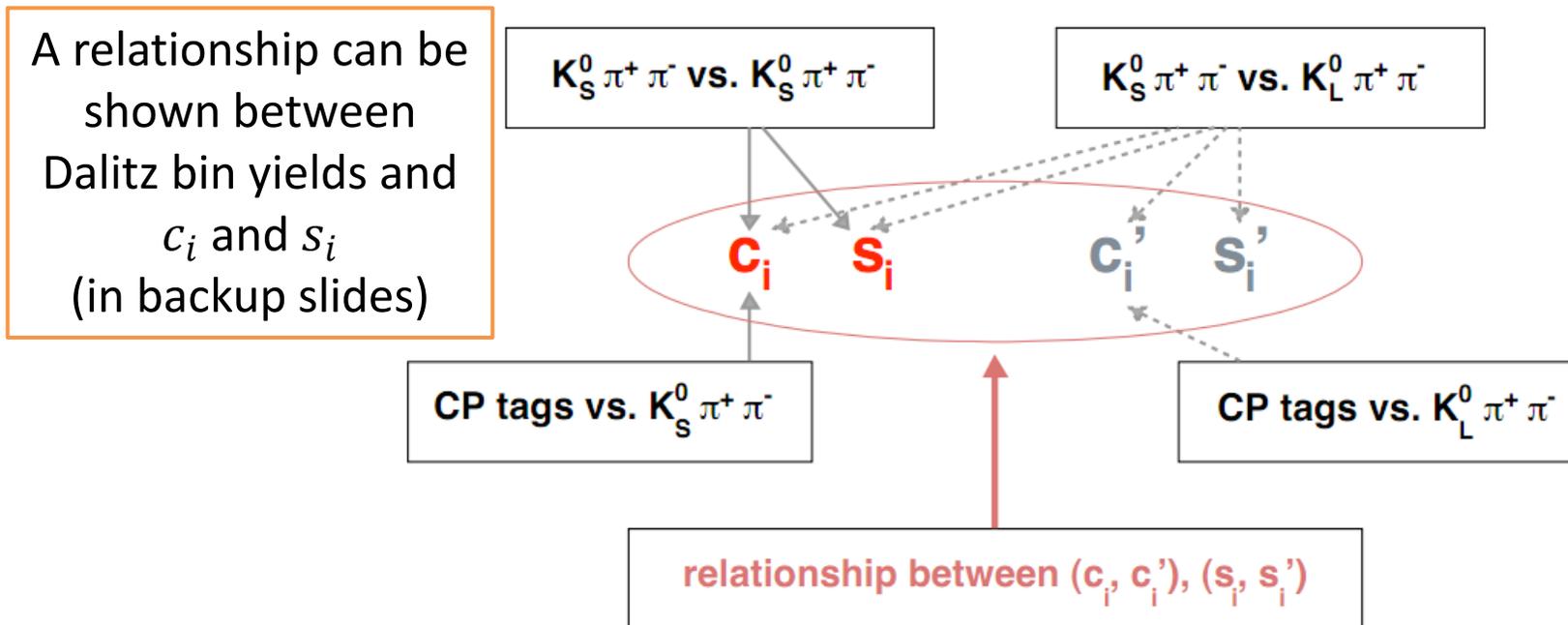
$K_S\pi^+\pi^-$ is the main topic: extract c_i, s_i
 $K_L\pi^+\pi^-$ is also used: extract c'_i, s'_i
relate to c_i, s_i with model corrections.

Aggressive use of tags, including partial reconstruction

All results preliminary; as presented at April 2014 AP meeting

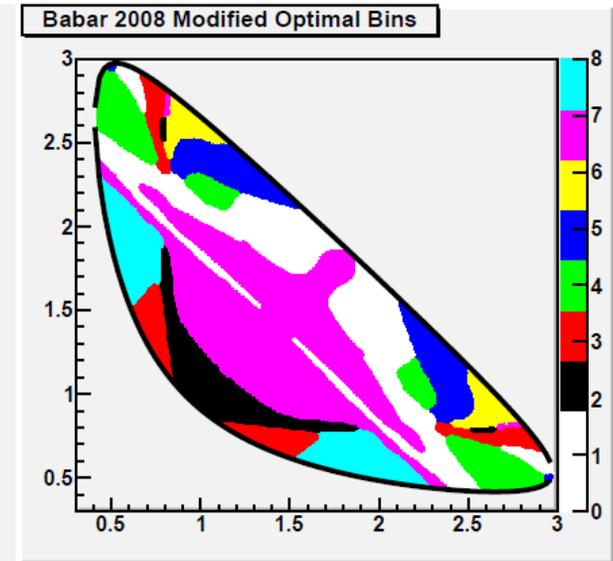
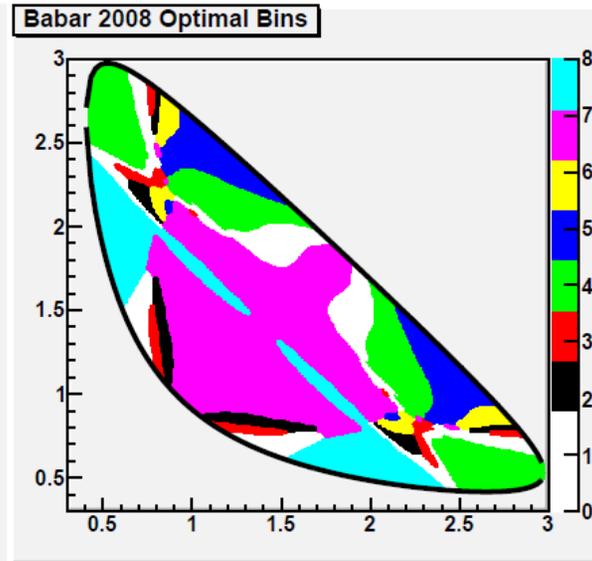
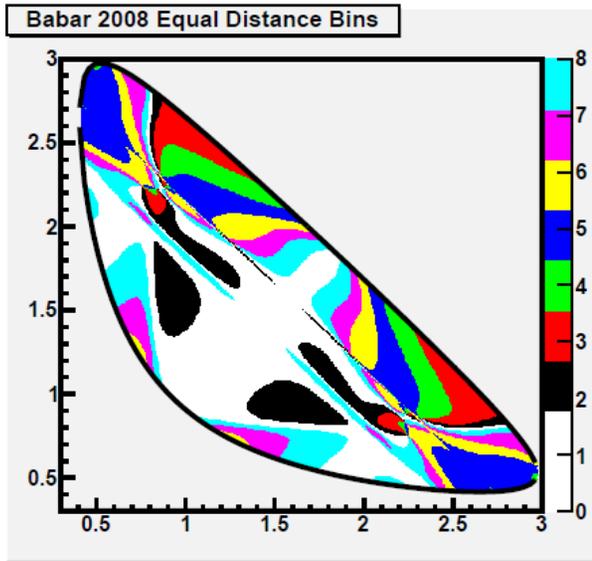
New $K_S \pi^+ \pi^-$ Results

We can calculate c_i and s_i from double tags of $D^0 \rightarrow K_S \pi^+ \pi^-$ vs $D^0 \rightarrow (K_{S,L} \pi^+ \pi^-$ or CP eigenstates)



Only c_i, s_i from $K_S \pi^+ \pi^-$ is used to calculate γ .

However adding in $D^0 \rightarrow K_L \pi^+ \pi^-$ we can calculate c'_i, s'_i and use how they relate to c_i, s_i to further constrain our results in a Global fit.



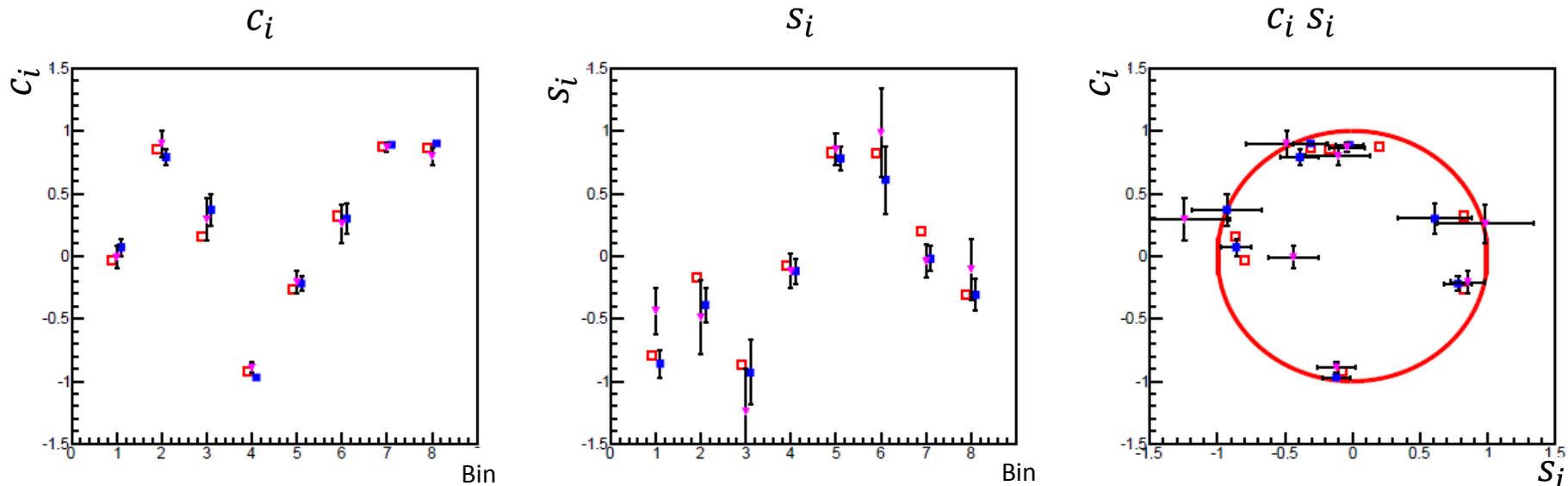
Result of splitting the Dalitz phase space into 8 equally spaced phase bins based on the BaBar 2008 Model.

Starting with the equally spaced bins, bins are adjusted to optimize the sensitivity to γ . A secondary adjustment smooths binned areas smaller than detector resolution.

Similar to the “optimal binning” except the expected background is taken into account before optimizing for γ sensitivity.

Source: CLEO Collaboration, *Physical Review D*, vol 82., pp. 112006 - 112035

Slide from Dan Ambrose, APS 2014



Bins	C_i		S_i	
	BES-III	CLEO-c	BES-III	CLEO-c
1	0.066 ± 0.066	-0.009 ± 0.088	-0.843 ± 0.119	-0.438 ± 0.184
2	0.796 ± 0.061	0.900 ± 0.106	-0.357 ± 0.148	-0.490 ± 0.295
3	0.361 ± 0.125	0.292 ± 0.168	-0.962 ± 0.258	-1.243 ± 0.341
4	-0.985 ± 0.017	-0.890 ± 0.041	-0.090 ± 0.093	-0.119 ± 0.141
5	-0.278 ± 0.056	-0.208 ± 0.085	0.778 ± 0.092	0.853 ± 0.123
6	0.267 ± 0.119	0.258 ± 0.155	0.635 ± 0.293	0.984 ± 0.357
7	0.902 ± 0.017	0.869 ± 0.034	-0.018 ± 0.103	-0.041 ± 0.132
8	0.888 ± 0.036	0.798 ± 0.070	-0.301 ± 0.140	-0.107 ± 0.240

***Only statistical uncertainty is listed

BESIII Preliminary

- Model prediction
- BESIII
- ▼ CLEO-c

Consistent agreement with CLEO-c measurements.

Source: CLEO Collaboration, Physical Review D, vol 82., pp. 112006 - 112035

Improved errors w.r.t. CLEO-c

Slide from Dan Ambrose, APS 2014

My Selected Issues

BaBar $K\pi\pi^0$ mixing result uses an isobar fit; gets rotated x'' , y''
Can't this be done in a model-independent way, using charm
threshold data if needed ??? ("Atwood-Soni for mixing")

Efficiencies vary across D Dalitz plots

Charm and B factories differ; traffic in corrected variables

Current methods accurate ? Need Dalitz models to do well ?

Are studies of D mixing, D CPV, K_S CPV effects complete?

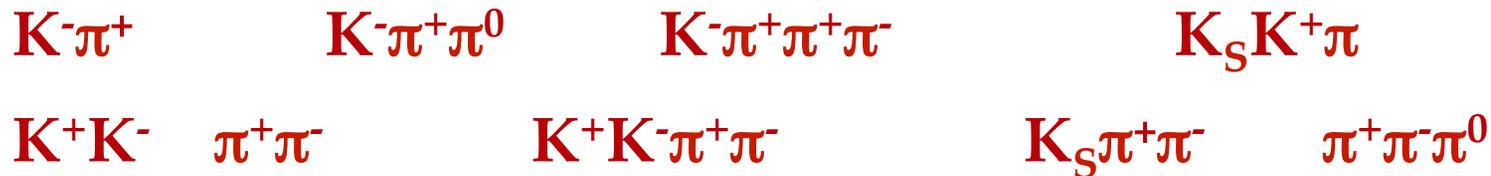
Assumptions of SM re: CPV could be more explicit

e.g., GGSZ assumes no weak phase between CF & DCSD (I think!)

Maintain a lively $D \leftrightarrow B$ interchange & forge ahead !

Everything is a Special Case ! (almost)

so if you were confused, you're probably not alone...



$K^- \pi^+$ only δ ; $K^- \pi^+ \pi^0$, $K^- \pi^+ \pi^+ \pi^-$ have both R & δ

Multi-body Self-conjugate modes:

If no CPV, only $2(n-1)$ isobar phases, not $2n-1$
threshold data only to avoid model dependence;
no “essential” D^0 - $D^{0\text{bar}}$ phase

4-body: more complicated angular momenta than 3-body

K_S modes: CF and DCSD give K^0 , $K^{0\text{bar}}$, not K_S directly

Extracting CKM γ

without charm



with charm



Conclusions

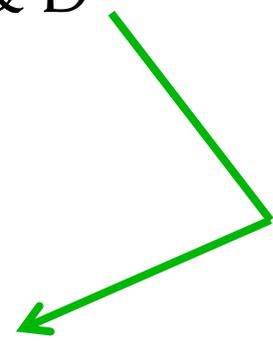
Unique access to strong phases & ability to extract model-independent results with charm at threshold

- Started with many CLEO-c Results
- Still some activity with CLEO-c “legacy data” [≥ 1 more paper?]
- Now, the 3.5x larger BESIII dataset is producing results

Interest of B physics users remains high

- LHCb is a huge addition to older B-factory data
- But e^+e^- will return soon with BelleII
- Important to keep active interaction between B & D

Future prospects are bright

- More precision, new modes, new variables !
 - Need to maintain threshold analysis manpower
- 

Selected Theory References

Quantum Correlations

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Selected Theory References

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