

BaBar  $\alpha$  measurement from  $B^0 \rightarrow \rho\pi$   
Dalitz plot analysis and  $\beta$  from  
 $B^0 \rightarrow D^{*+}D^{*-}$  with partial reconstruction

CKM 2014 Workshop - Vienna, Austria

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Representing  
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# Overview

$\alpha$

- “Measurement of  $CP$ -violating asymmetries in  $B^0 \rightarrow (\rho\pi)^0$  decays using a time-dependent Dalitz plot analysis”

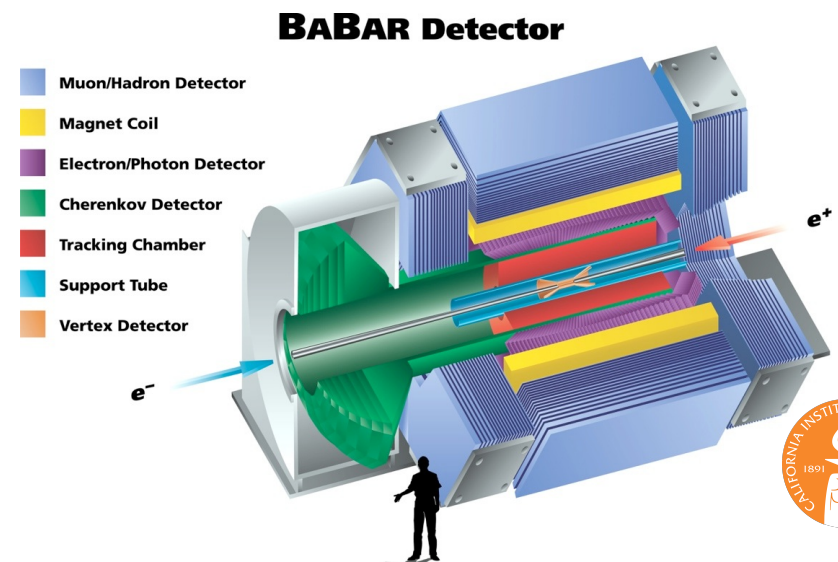
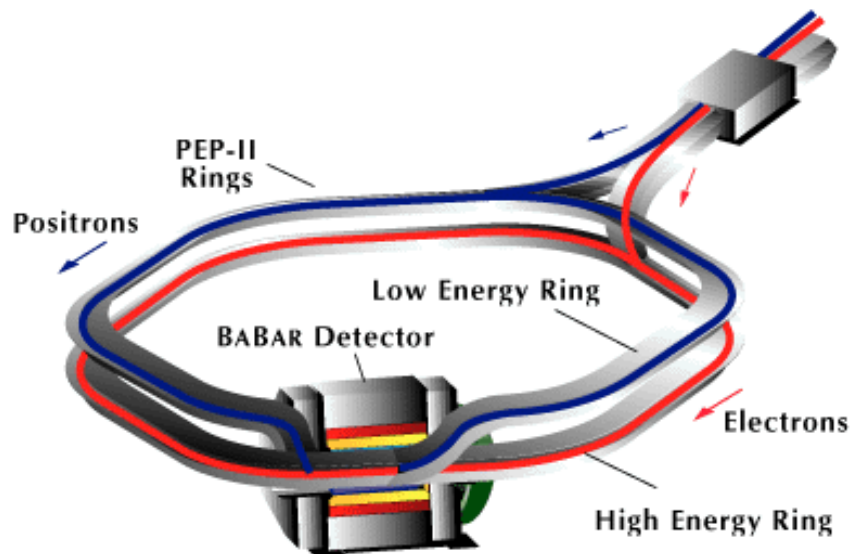
**Phys. Rev. D 88, 012003 (2013)**

$\beta$

- “Measurement of the time-dependent  $CP$  asymmetry of partially reconstructed  $B^0 \rightarrow D^{*+} D^{*-}$  decays”

**Phys. Rev. D 86, 112006 (2012)**

- Both analyses use the full BaBar dataset collected at the  $\Upsilon(4s)$  resonance ( $\sim 470 \times 10^6 B\bar{B}$  pairs)



# $B^0 \rightarrow \rho\pi$ CP Violation Analysis I

- $B^0 \rightarrow \pi^+\pi^-\pi^0$  time-dep CPV measurement

**Phys. Rev. D 88, 012003 (2013)**

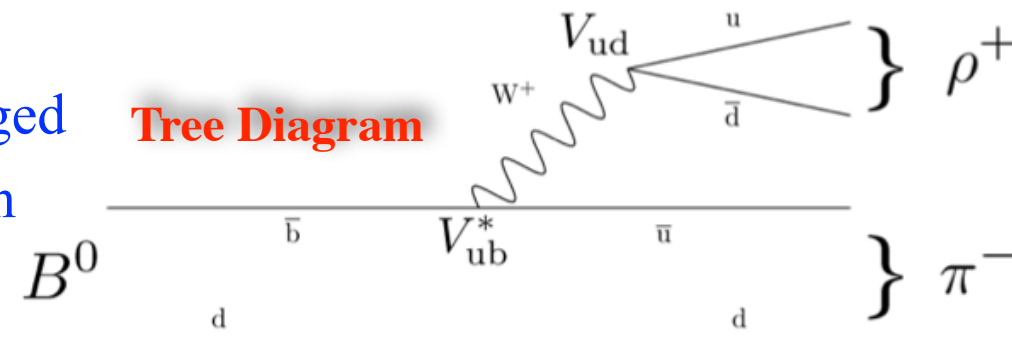
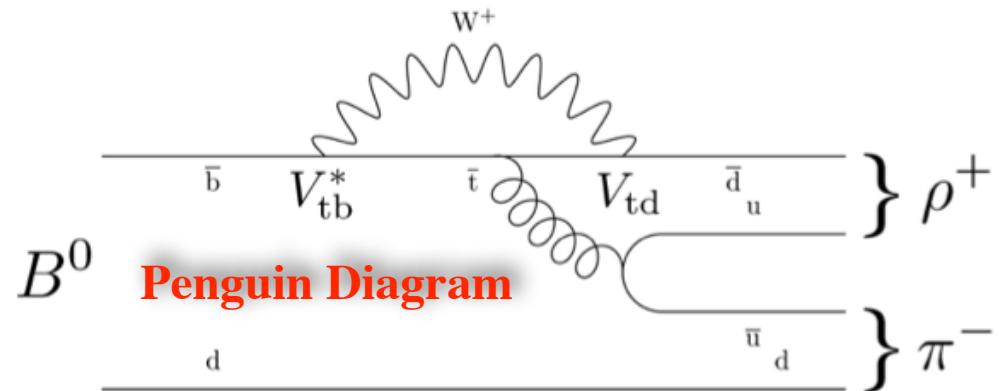
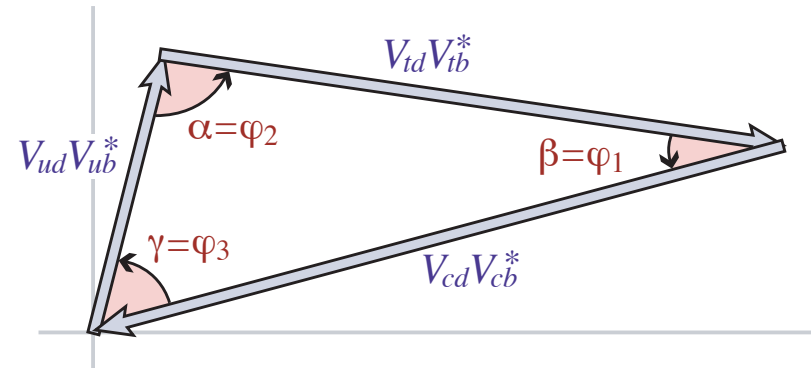
- Dominated by  $B^0 \rightarrow \rho^\pm\pi^\mp$
- Extensive update and reoptimization of a 2007 BaBar analysis\*
- Extracts information about alpha, and other parameters

- Interference between tree and penguin modes and decays w/ and w/o mixing provides sensitivity to alpha

- The use of a full Dalitz plot analysis reduces ambiguities found in analyses that ignore the interference regions

- Isospin relations allow info from charged B decays to be used in alpha extraction

**\*Phys. Rev. D 76, 012004 (2007)**



# $B^0 \rightarrow \rho\pi$ CP Violation Analysis II

- Time-Dependent Probability Distribution

$$|\mathcal{A}_{3\pi}^{\pm}(\Delta t)|^2 = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} \left[ |A_{3\pi}|^2 + |\bar{A}_{3\pi}|^2 \mp (|A_{3\pi}|^2 - |\bar{A}_{3\pi}|^2) \cos(\Delta m_d \Delta t) \pm 2\text{Im} \left[ \frac{q}{p} \bar{A}_{3\pi} A_{3\pi}^* \right] \sin(\Delta m_d \Delta t) \right]$$

$$A_{3\pi} = f_+ A^+ + f_- A^- + f_0 A^0 \quad \text{for } B^0 \rightarrow \pi^+ \pi^- \pi^0$$

$$\bar{A}_{3\pi} = f_+ \bar{A}^+ + f_- \bar{A}^- + f_0 \bar{A}^0 \quad \text{for } \bar{B}^0 \rightarrow \pi^+ \pi^- \pi^0$$

$$f_{\kappa}(m, \theta_{\kappa}) \propto F_{\rho(770)}(m, \theta_{\kappa}) + a_{\rho'} e^{i\phi_{\rho'}} F_{\rho(1450)}(m, \theta_{\kappa})$$

- In the final fit, this distribution is parameterized using 26 “U and I” parameters calculated from resonance amplitudes:

$$U_{\kappa}^{\pm} = |A^{\kappa}|^2 \pm |\bar{A}^{\kappa}|^2$$

$$U_{\kappa\sigma}^{\pm, \text{Re(Im)}} = \text{Re(Im)} \left[ A^{\kappa} A^{\sigma*} \pm \bar{A}^{\kappa} \bar{A}^{\sigma*} \right]$$

$$I_{\kappa} = \text{Im} \left[ \bar{A}^{\kappa} A^{\kappa*} \right]$$

$$I_{\kappa\sigma}^{\text{Re}} = \text{Re} \left[ \bar{A}^{\kappa} A^{\sigma*} - \bar{A}^{\sigma} A^{\kappa*} \right]$$

$$I_{\kappa\sigma}^{\text{Im}} = \text{Im} \left[ \bar{A}^{\kappa} A^{\sigma*} + \bar{A}^{\sigma} A^{\kappa*} \right]$$

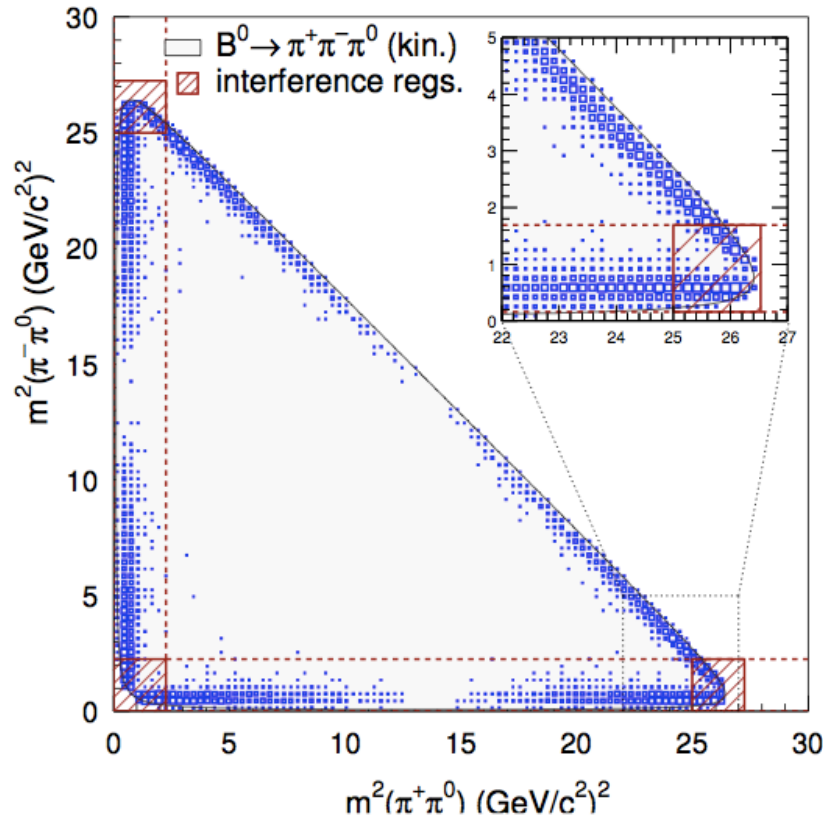
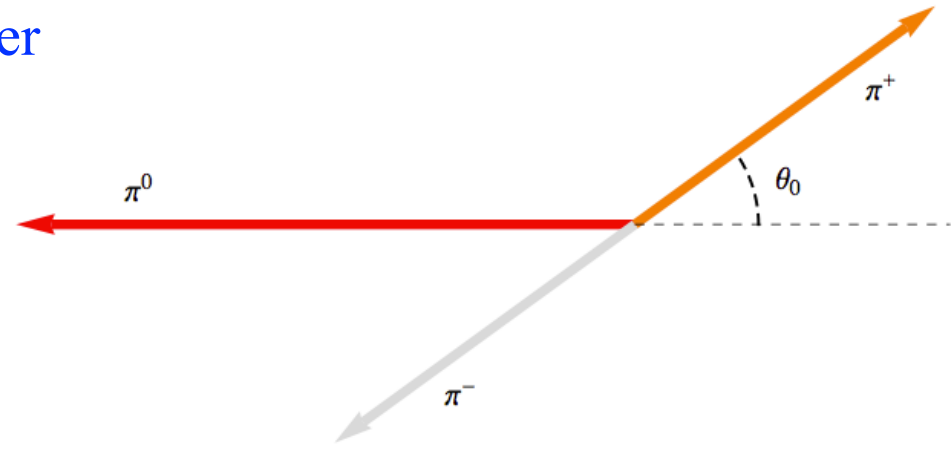


# $B^0 \rightarrow \rho\pi$ CP Violation Analysis III

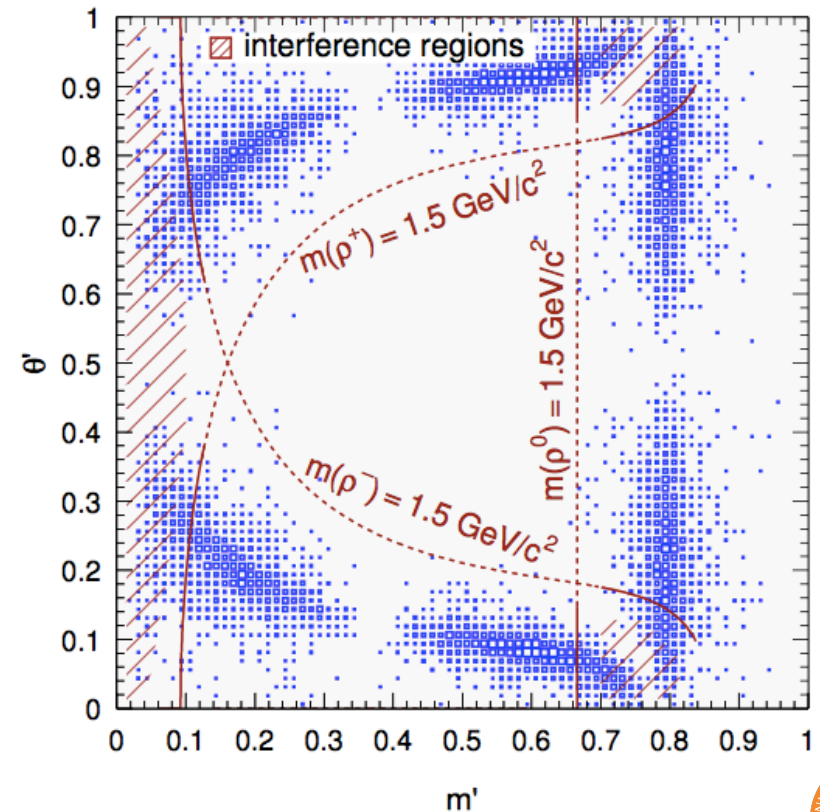
- The Dalitz plot is transformed to cover a unit square before fitting

$$m' \equiv \frac{1}{\pi} \arccos \left( 2 \frac{m_0 - m_0^{\min}}{m_0^{\max} - m_0^{\min}} - 1 \right)$$

$$\theta' \equiv \frac{1}{\pi} \theta_0$$



$\rho\pi$  Toy Dalitz Plot



Square Dalitz Plot (SDP)



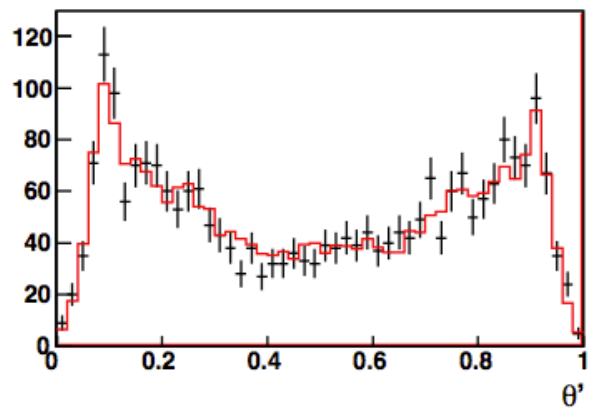
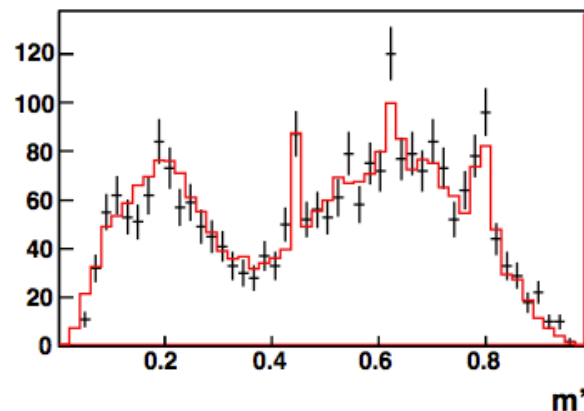
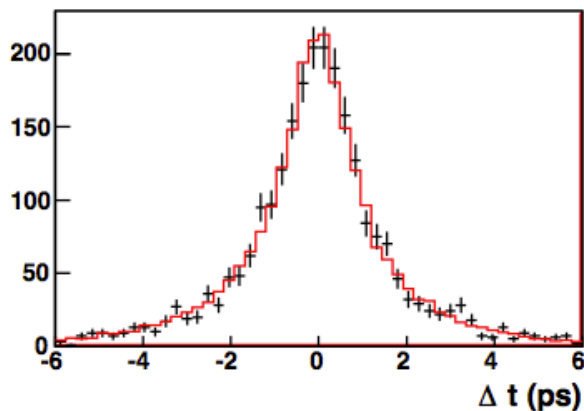
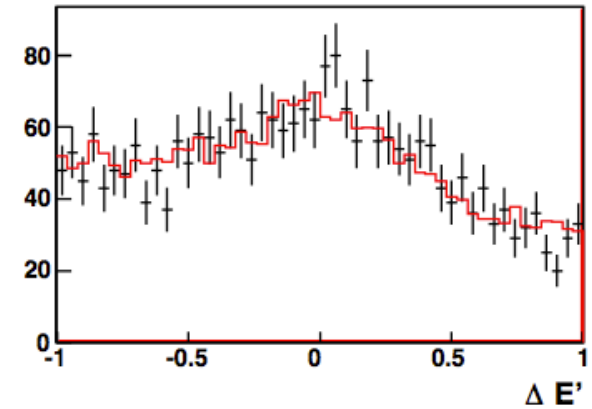
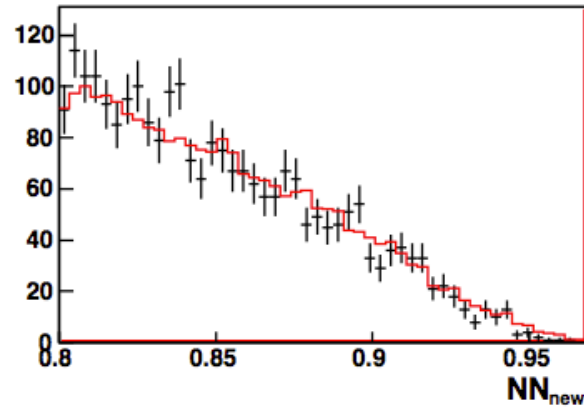
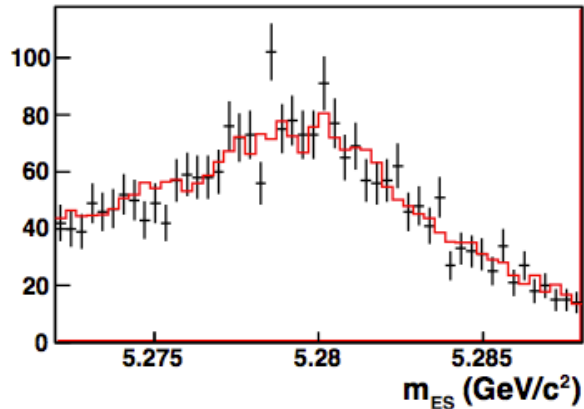
# $B^0 \rightarrow \rho\pi$ CP Violation Analysis IV

- Data is fit using a multi-dimensional extended maximum likelihood fit with 6 input variables:

- $m_{ES}$ ,  $\Delta E$ , NN output
- Time-Dependent SDP:  $\Delta t$ ,  $(m', \theta')$

$$m_{ES} = \sqrt{\left(\frac{\sqrt{s}}{2}\right)^2 - (p_B^*)^2}$$
$$\Delta E = E_B^* - \frac{1}{2}\sqrt{s}$$

— Fit Results  
— Data



Signal-Enhanced Agreement Between Data and Fit



# $B^0 \rightarrow \rho\pi$ CP Violation Analysis V

- Direct  $CPV$  asymmetries extracted in 2D scan:

$$\mathcal{A}_{\rho\pi}^{+-} \equiv \frac{\Gamma(\bar{B}^0 \rightarrow \rho^- \pi^+) - \Gamma(B^0 \rightarrow \rho^+ \pi^-)}{\Gamma(\bar{B}^0 \rightarrow \rho^- \pi^+) + \Gamma(B^0 \rightarrow \rho^+ \pi^-)} = 0.09_{-0.06}^{+0.05} \pm 0.04,$$

$$\mathcal{A}_{\rho\pi}^{-+} \equiv \frac{\Gamma(\bar{B}^0 \rightarrow \rho^+ \pi^-) - \Gamma(B^0 \rightarrow \rho^- \pi^+)}{\Gamma(\bar{B}^0 \rightarrow \rho^+ \pi^-) + \Gamma(B^0 \rightarrow \rho^- \pi^+)} = -0.12 \pm 0.08_{-0.05}^{+0.04}$$

- Origin (no direct  $CPV$ ) is  $\sim 2\sigma$  from central value
- Previous results:

BaBar 2007

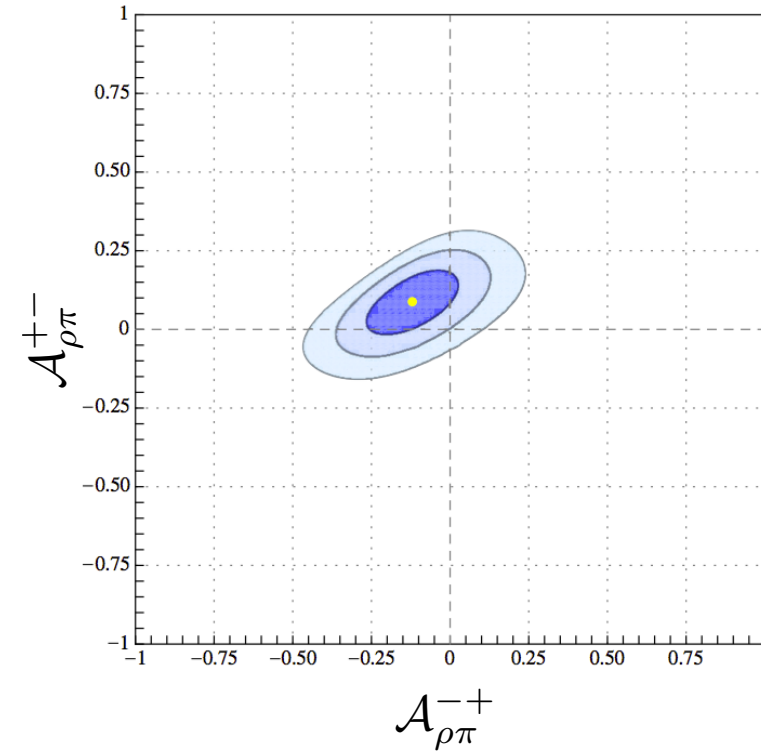
$$\mathcal{A}_{\rho\pi}^{+-} = 0.03 \pm 0.07 \pm 0.04$$

$$\mathcal{A}_{\rho\pi}^{-+} = -0.32 \pm 0.16_{-0.10}^{+0.09}$$

Belle 2008

$$\mathcal{A}_{\rho\pi}^{+-} = 0.21 \pm 0.08 \pm 0.04$$

$$\mathcal{A}_{\rho\pi}^{-+} = 0.08 \pm 0.16 \pm 0.11$$

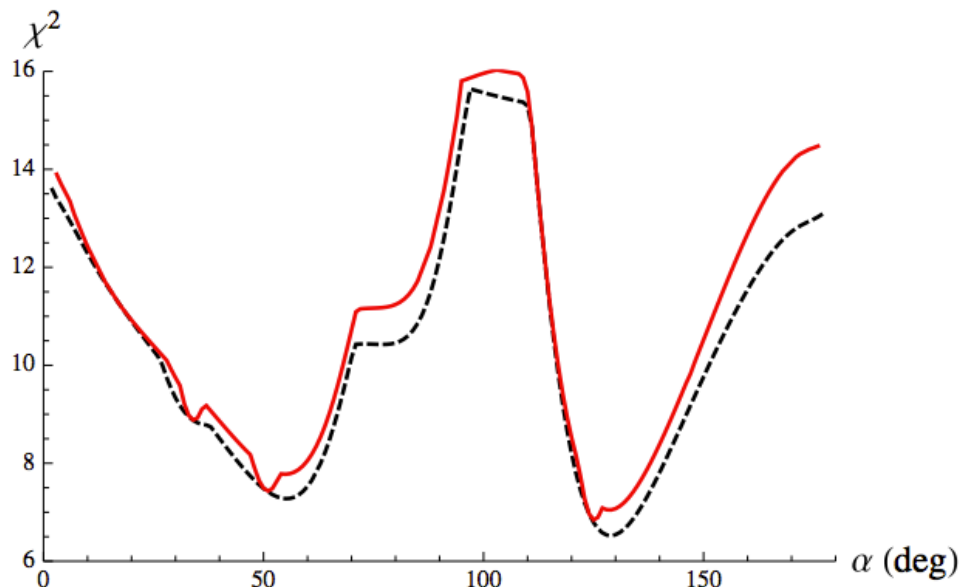


- The 26 physics parameters describing the  $B^0 \rightarrow \rho\pi$  decay are extracted with, on average, 0.47 times the statistical uncertainties from the previous BaBar measurement
- Studies find that the 26 physics parameters are robustly extracted with our current statistical sensitivity

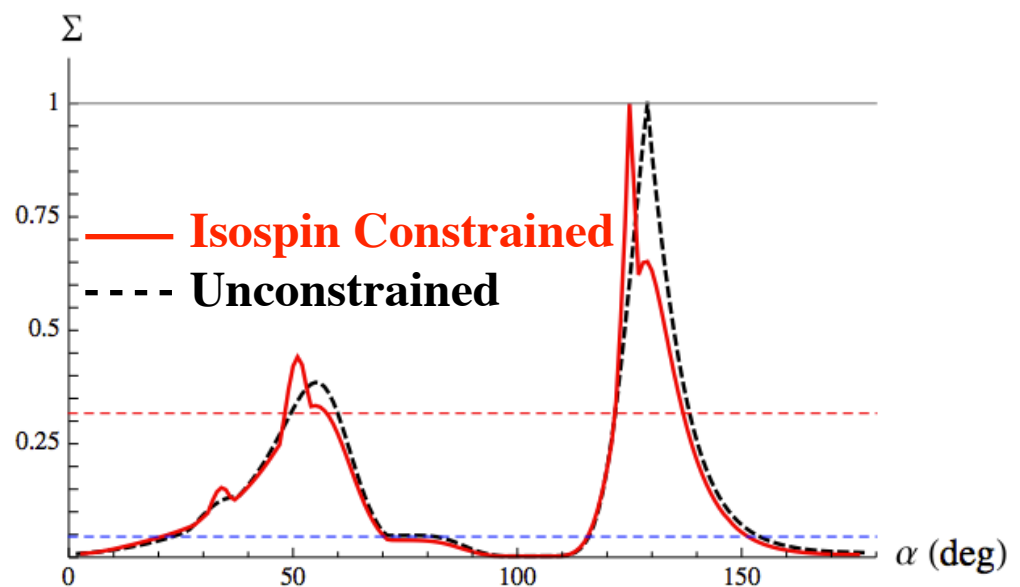


# $B^0 \rightarrow \rho\pi$ CP Violation Analysis VI

- We extract information about  $\alpha$  from a  $\chi^2$  scan
  - For each step in  $\alpha$  between  $0^\circ$  and  $180^\circ$ , we perform a  $\chi^2$  minimization using the U and I parameter values from our nominal fit along with their full covariance matrix



$\chi^2$  Scan



$\Sigma$  Scan

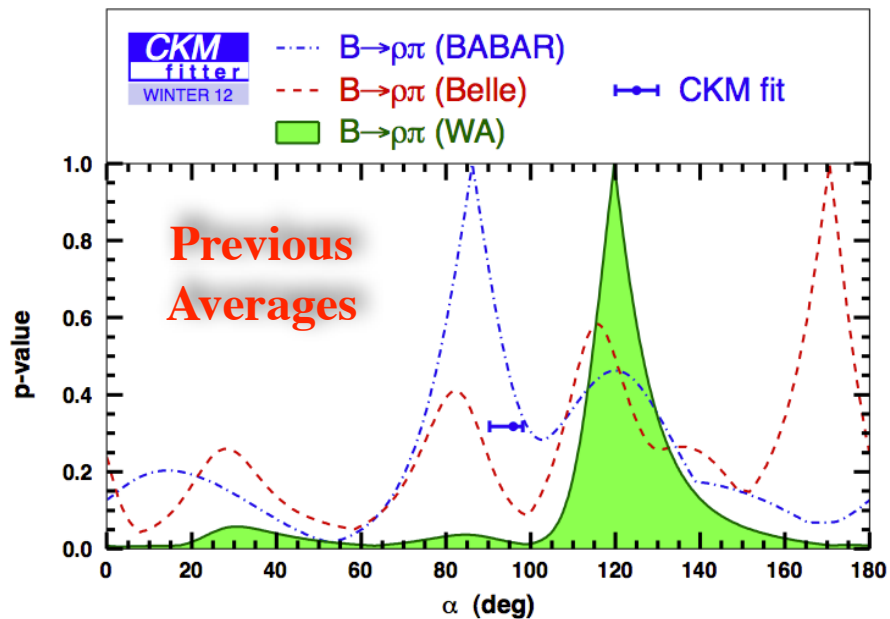
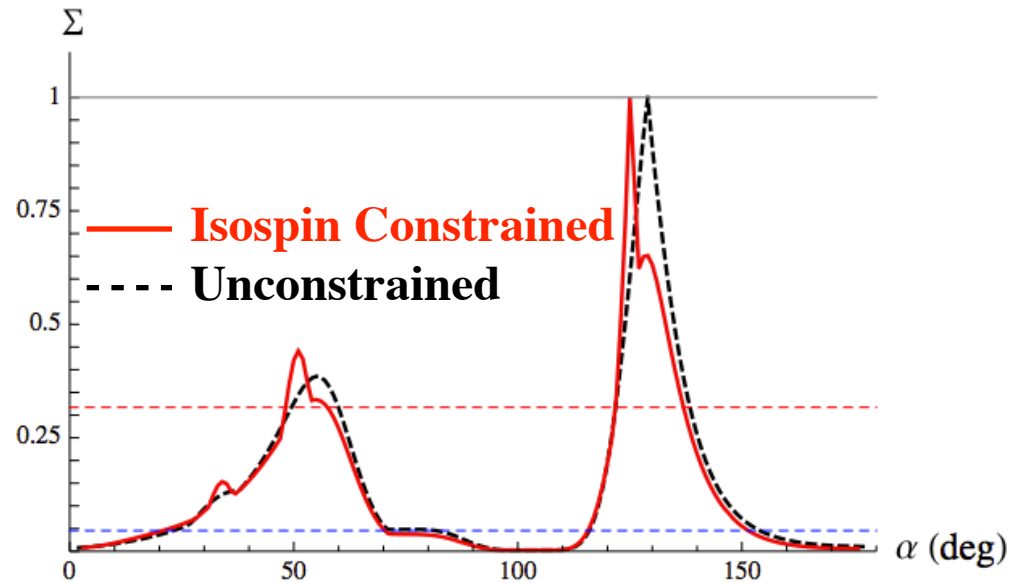
(Commonly called “1-CL”)

- Notably, studies reveal that the alpha scan is not robust with current statistics

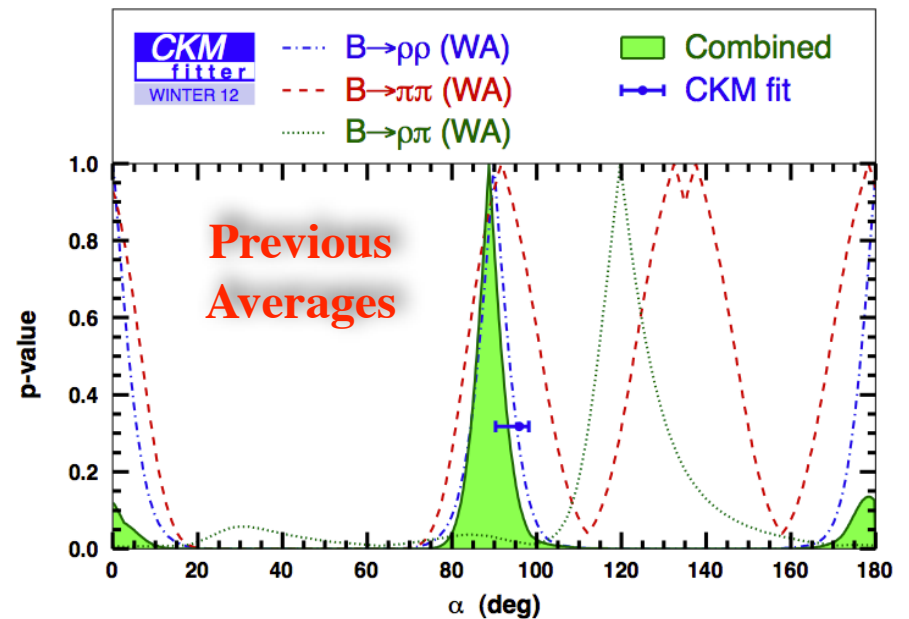


# $B^0 \rightarrow \rho\pi$ CP Violation Analysis VII

- Comparison with previous CKMFitter world averages



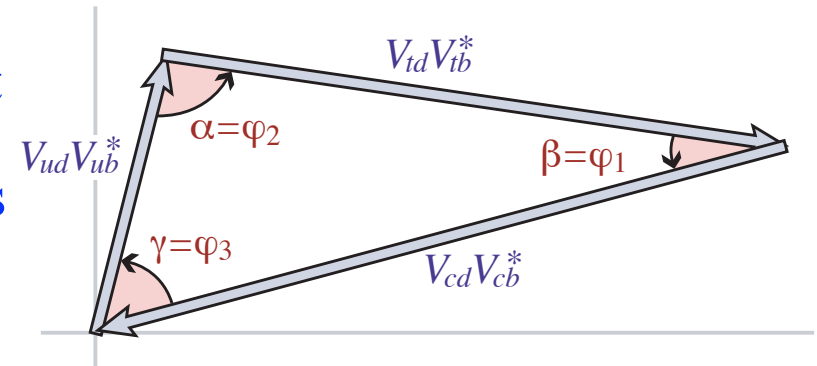
$\rho\pi$  Only



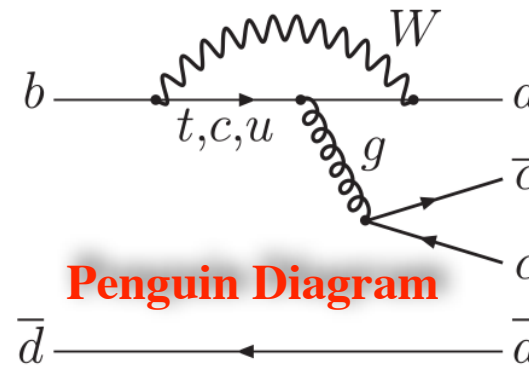
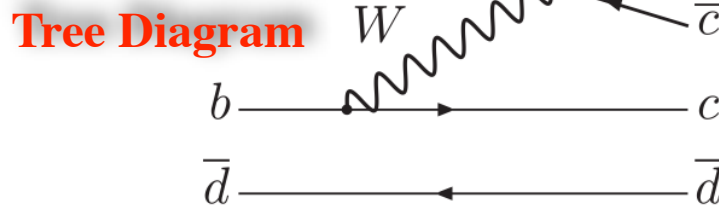
All Modes

# $B^0 \rightarrow D^{*+} D^{*-}$ CP Violation Analysis I

- $b \rightarrow c\bar{c}d$  time-dependent  $CPV$  measurement
- In the absence of penguin contributions, this mode should yield the same measured value for  $\sin 2\beta$  as  $b \rightarrow c\bar{c}s$  ( $J/\psi K$ )



- Only expect correction of a few % due to penguin contributions in the standard model
- A large discrepancy between  $\sin 2\beta$  in the two modes could indicate new physics



# $B^0 \rightarrow D^{*+} D^{*-}$ CP Violation Analysis II

- The Vector-Vector final state is a mixture of  $CP$ -odd and  $CP$ -even states
  - Need an angular analysis to separate  $CP$  states
  - Using fully reconstructed events, BaBar and Belle have both measured the  $CP$ -odd fraction  $R_{\perp}$  and the time-dep  $CP$  asymmetry

$$R_{\perp} = \frac{|A_{\perp}^0|^2}{|A_0^0|^2 + |A_{\parallel}^0|^2 + |A_{\perp}^0|^2}$$

CP=+1 for  $A_{\parallel}, A_0$   
CP=-1 for  $A_{\perp}$

**BaBar Full Reco**

$$R_{\perp} = 0.158 \pm 0.028 \pm 0.006$$

**Phys. Rev. D 79, 032002 (2009)**

- The previously measured  $CP$ -odd fraction reveals that the final state is dominated by the  $CP = +1$  amplitude
- We can forego the angular analysis and use the previously measured  $CP$ -odd fraction to separate the  $CP$ -odd and  $CP$ -even S and C components



# $B^0 \rightarrow D^{*+} D^{*-} \text{ CP Violation Analysis III}$

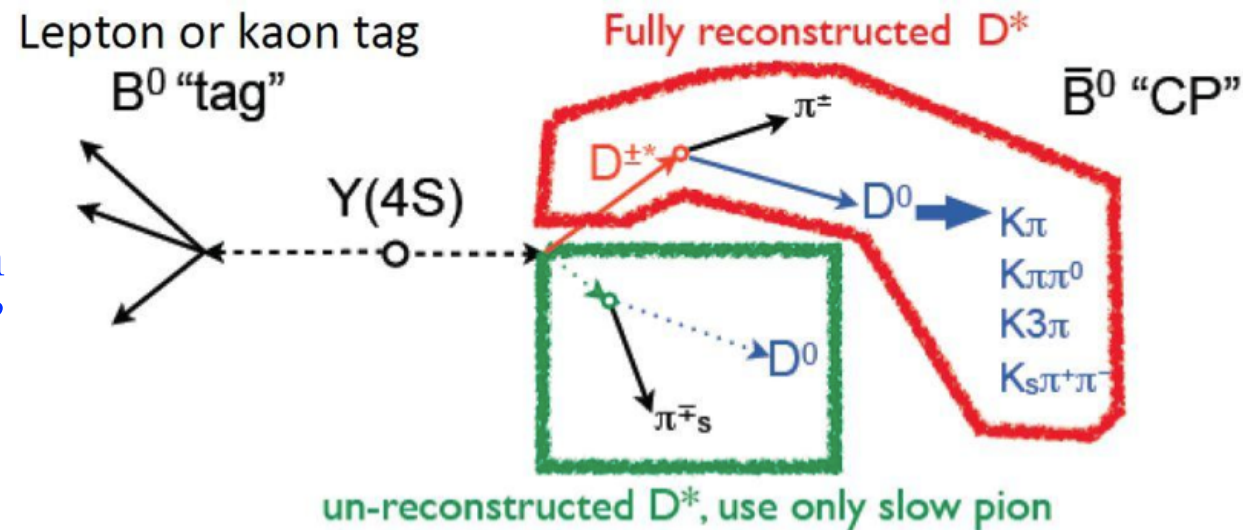
- Use partial reconstruction

- One  $D^*$  is fully reconstructed from  $D^* \rightarrow D^0 \pi$  where the  $D^0$  decays to one of 4 modes
- The fully reconstructed  $D^*$  is matched with a slow pion of opposite charge
- The  $D^*$  candidate is selected if the kinematics are consistent with  $B^0 \rightarrow D^* D^0 \pi$  where the  $D^0$  is missing

$m_{\text{rec}}$  = Mass of recoiling  $D^0$  reconstructed from the  $D^*$  and slow pion momenta

- Partial reconstruction provides  $\sim 5x$  the sig evts from a full reco, but with higher background and larger systematic errors

- The flavor of the other B meson is determined by either “lepton” or “kaon” tagging



# $B^0 \rightarrow D^{*+} D^{*-}$ CP Violation Analysis IV

- PDF for final fit is composed of three components

$$P = f_{B\bar{B}} \frac{\overbrace{[f_{\text{sig}} P_{\text{sig}} + (1 - f_{\text{sig}}) P_{\text{comb}}]}^{\text{signal}}}{\underbrace{B\bar{B}}_{\text{continuum}}} + \underbrace{(1 - f_{B\bar{B}}) P_{q\bar{q}}}_{\text{continuum}}$$

(Peaking background was found to be negligible)

- Each component of the PDF is a product of a kinematic element and a  $\Delta t$  element

$$P_i(m_{\text{rec}}, F, \Delta t, \sigma_{\Delta t}, S_{\text{tag}}) = \frac{\mathcal{M}_i(m_{\text{rec}}) \mathcal{F}_i(F)}{\text{“KIN”}} \frac{T'_i(\Delta t, \sigma_{\Delta t}, S_{\text{tag}})}{\text{“}\Delta t\text{”}}$$

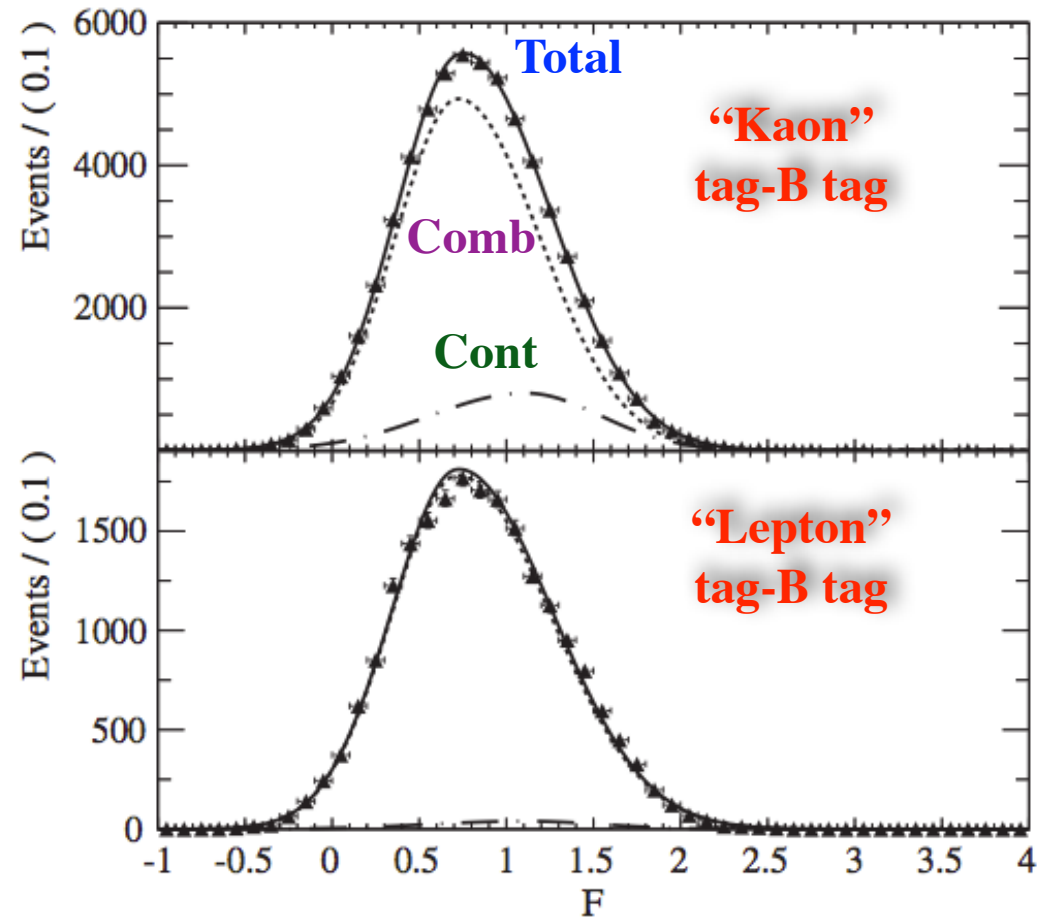
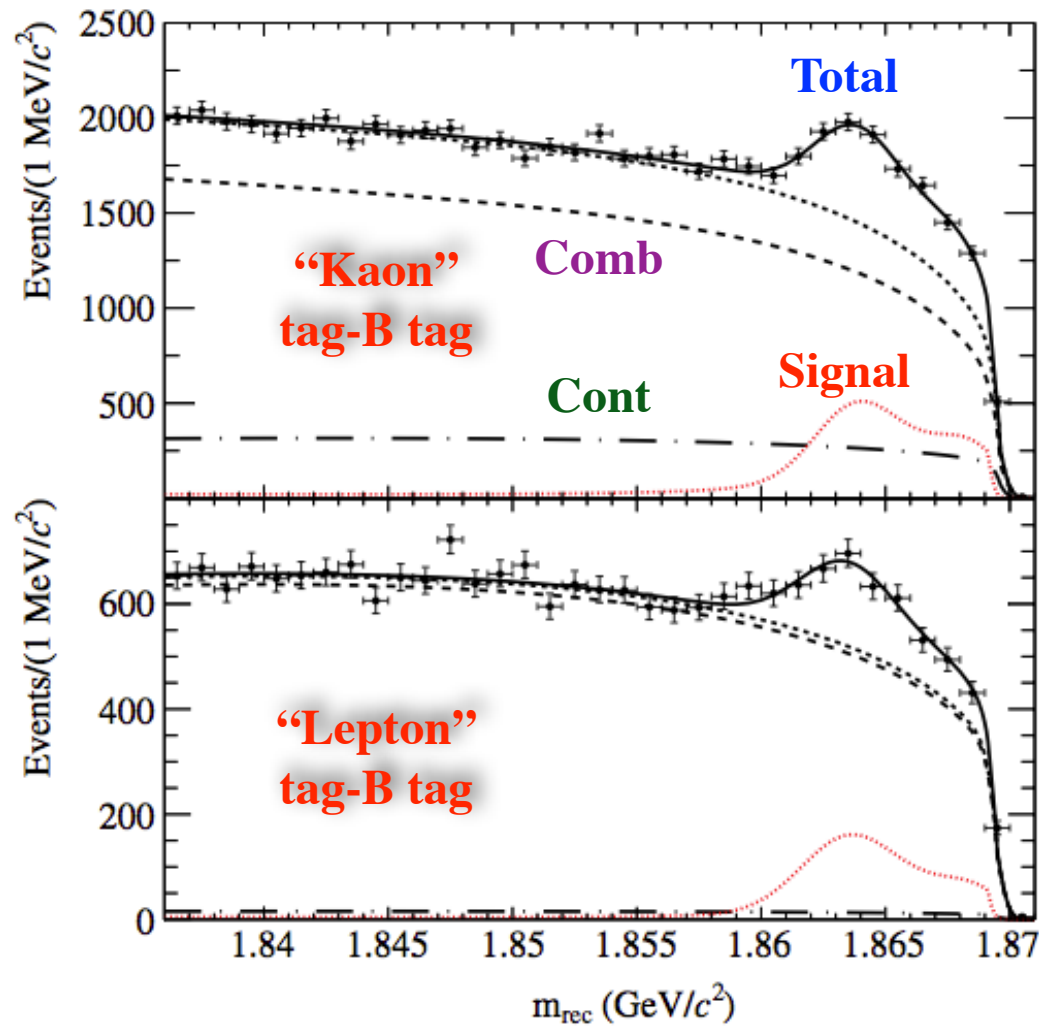
- A Fisher discriminant is used to help distinguish jet-like continuum events from more spherically distributed signal events



# $B^0 \rightarrow D^{*+} D^{*-}$ CP Violation Analysis V

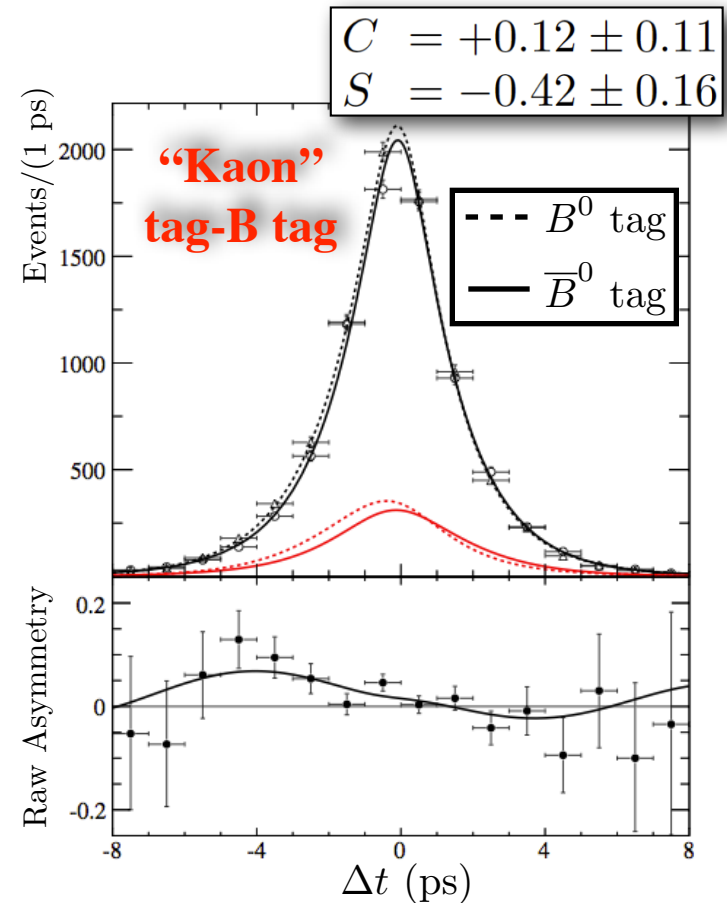
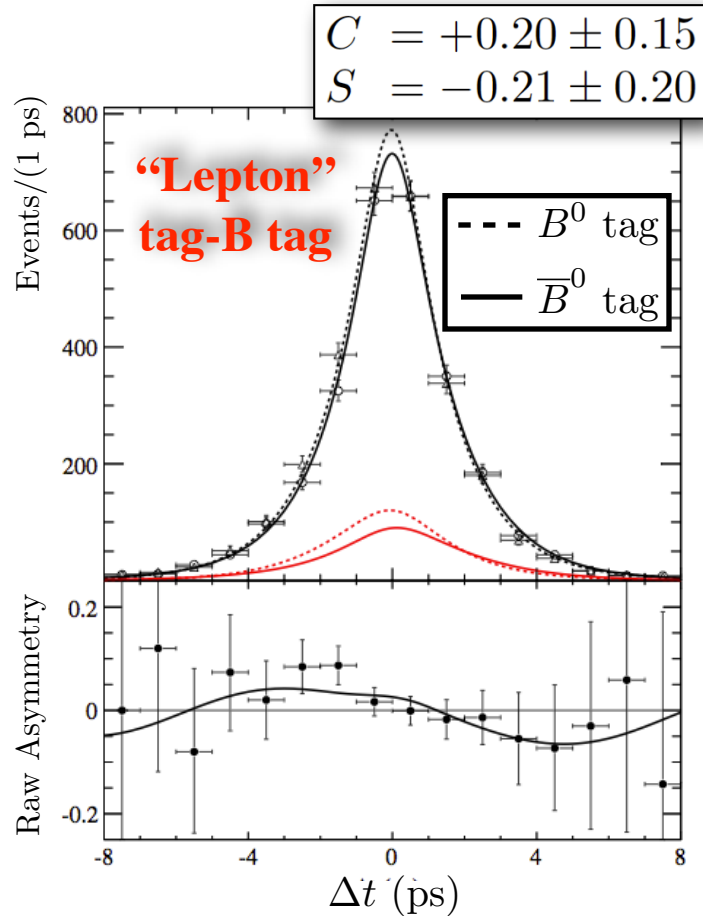
- Kinematic fit distributions

**Phys. Rev. D 86, 112006 (2012)**



# $B^0 \rightarrow D^{*+} D^{*-}$ CP Violation Analysis VI

- Time-dependent fit results:



- Combined parameters:  $C = +0.15 \pm 0.09 \pm 0.05$   
 $S = -0.34 \pm 0.12 \pm 0.09$

for  $R_{\perp} = 0.158 \pm 0.029^*$

**\*Phys. Rev. D 79, 032002 (2009)**

- Neglecting penguin amplitudes:

$$S_+ = -S_-, \quad C_+ = -C_-$$

$$C = C_+ \quad S = S_+(1 - 2R_{\perp}) \implies$$

$$C_+ = +0.15 \pm 0.09 \pm 0.04$$

$$S_+ = -0.49 \pm 0.18 \pm 0.07 \pm 0.04$$





# $B^0 \rightarrow D^{*+} D^{*-}$ CP Violation Analysis VII

- Time-dependent fit result comparison:

- BaBar Partial Reconstruction:

$$\begin{aligned} C &= +0.15 \pm 0.09 \pm 0.05 \\ S &= -0.34 \pm 0.12 \pm 0.09 \end{aligned}$$

$$C_+ = +0.15 \pm 0.09 \pm 0.04$$

$$S_+ = -0.49 \pm 0.18 \pm 0.07 \pm 0.04$$

$$S_+ \approx -\sin 2\beta$$

- Our measured value of  $\sin 2\beta$  is **consistent with the PDG world average** calculated from a variety of modes:

$$\begin{aligned} &\text{PDG 2012 WA} \\ \sin 2\beta &= 0.679 \pm 0.020 \end{aligned}$$

- Our results are **also consistent with the previous Belle and BaBar measurements** performed using full reconstruction:

### Belle Full Reco\*

$$\begin{aligned} C &= 0.15 \pm 0.13 \pm 0.04 \\ S &= -0.96 \pm 0.25^{+0.13}_{-0.16} \end{aligned}$$

\***Phys. Rev. D 80, 111104 (2009)**

### BaBar Full Reco\*\*

$$\begin{aligned} C_+ &= +0.00 \pm 0.12 \pm 0.02 \\ S_+ &= -0.76 \pm 0.16 \pm 0.04 \end{aligned}$$

\*\***Phys. Rev. D 79, 032002 (2009)**



# Conclusions

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- We have performed an update of our alpha measurement in  $B^0 \rightarrow (\rho\pi)^0$  decays using the full BaBar dataset
- Significantly, studies reveal that alpha is not robustly extracted with current statistical significance, though other physics parameters are robust
- A CPV analysis in the mode  $B^0 \rightarrow D^{*+}D^{*-}$  using partial reconstruction has obtained results consistent with the previous BaBar and Belle measurements
- Our result for  $\sin 2\beta$  is consistent with the PDG world average of previous measurements performed in a variety of modes

