



Status of PSB Impedance calculations: Inconel undulated chambers

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Thanks to: E. Benedetto, J. Borburgh

Overview

- Impedance calculations at $\beta < 1$
- Inconel undulated chamber
 - Comparison between Inconel undulated chamber and ceramic chamber
 - Analytical calculation (no corrugation)
 - 3D CST EM simulation
- Summary

Impedance calculations for $\beta < 1$

Analytical calculation (applies only to simple structures)

3D EM simulation (CST Particle Studio: never used for $\beta < 1$)

CST EM simulation are commonly performed in the ultra-relativistic approximation ($\beta = 1$)

$$\beta_{inj}^{PSB} \cong 0.3 \quad \beta_{ext}^{PSB} \cong 0.9$$

The use of 3D EM simulations for $\beta < 1$ has been investigated

Definition of impedance

$$Z_{\parallel}(x, y, x_0, y_0, \omega) [\Omega] = -\frac{1}{q_0} \int_0^L E_s(x, y, s, x_0, y_0, \omega) e^{jks} ds$$

Longitudinal component of the electric field in (x, y) induced by a source charge placed in (x_0, y_0)

$$E_s^{tot} = E_s + E_s^{SC}$$

EM simulator uses the total fields

$$Z(\beta)$$

contribution due to the interaction of beam and accelerator components

Depend only on the source

$$Z_{direct}^{SC}(\beta)$$

3D CST EM simulation for $\beta < 1$

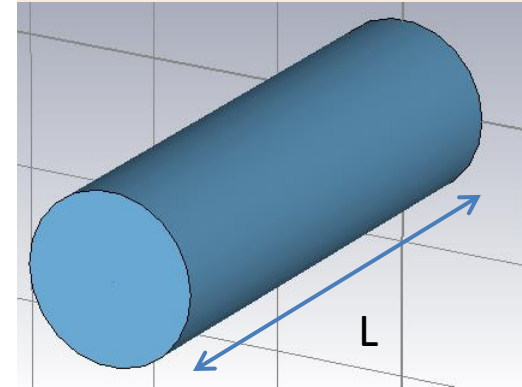
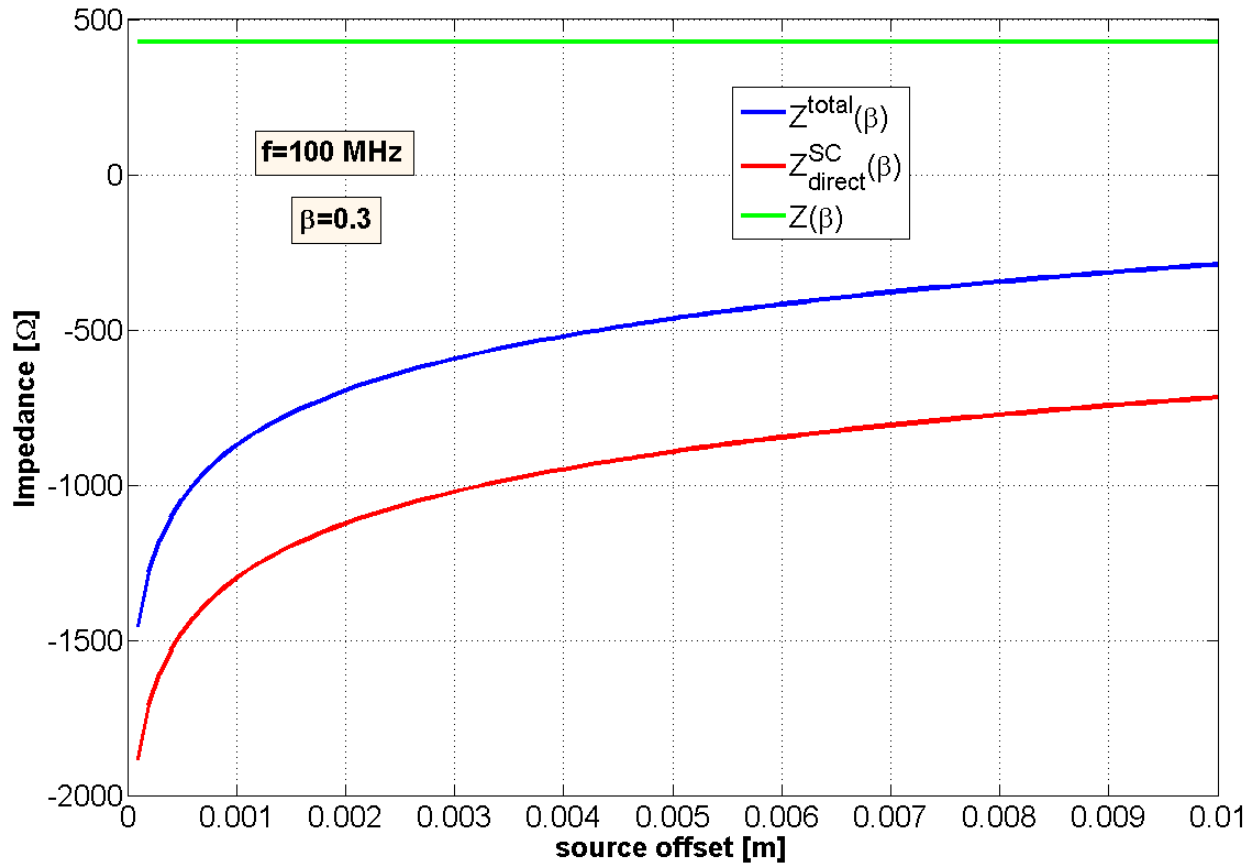
$$Z^{total}(\beta) = Z(\beta) + Z_{direct}^{SC}(\beta)$$

Depend only on the source

contribution due to the interaction of
beam and external surroundings

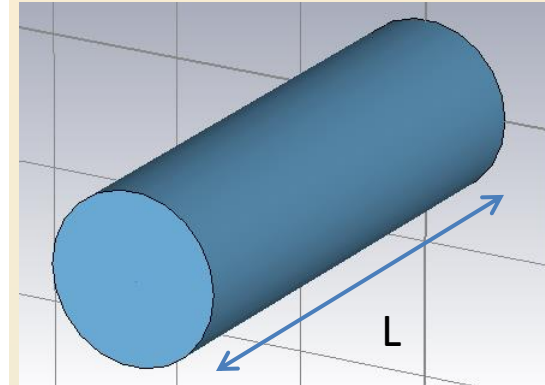
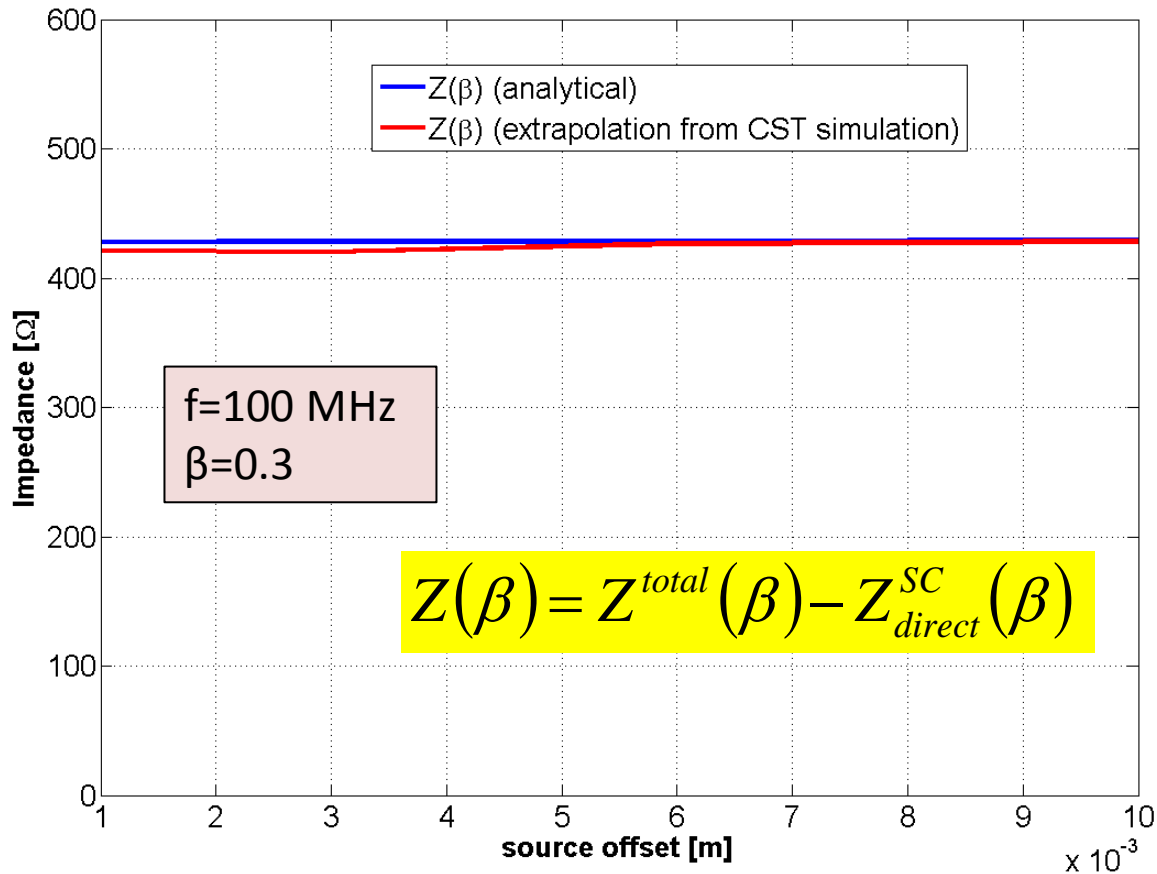
To single out the impedance contribution $Z(\beta)$ the direct space charge is analytically removed

Longitudinal impedance: analytical calculation



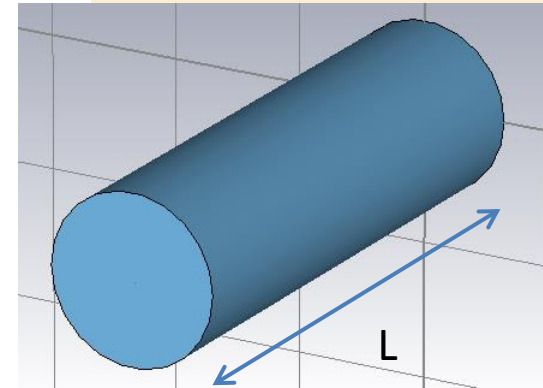
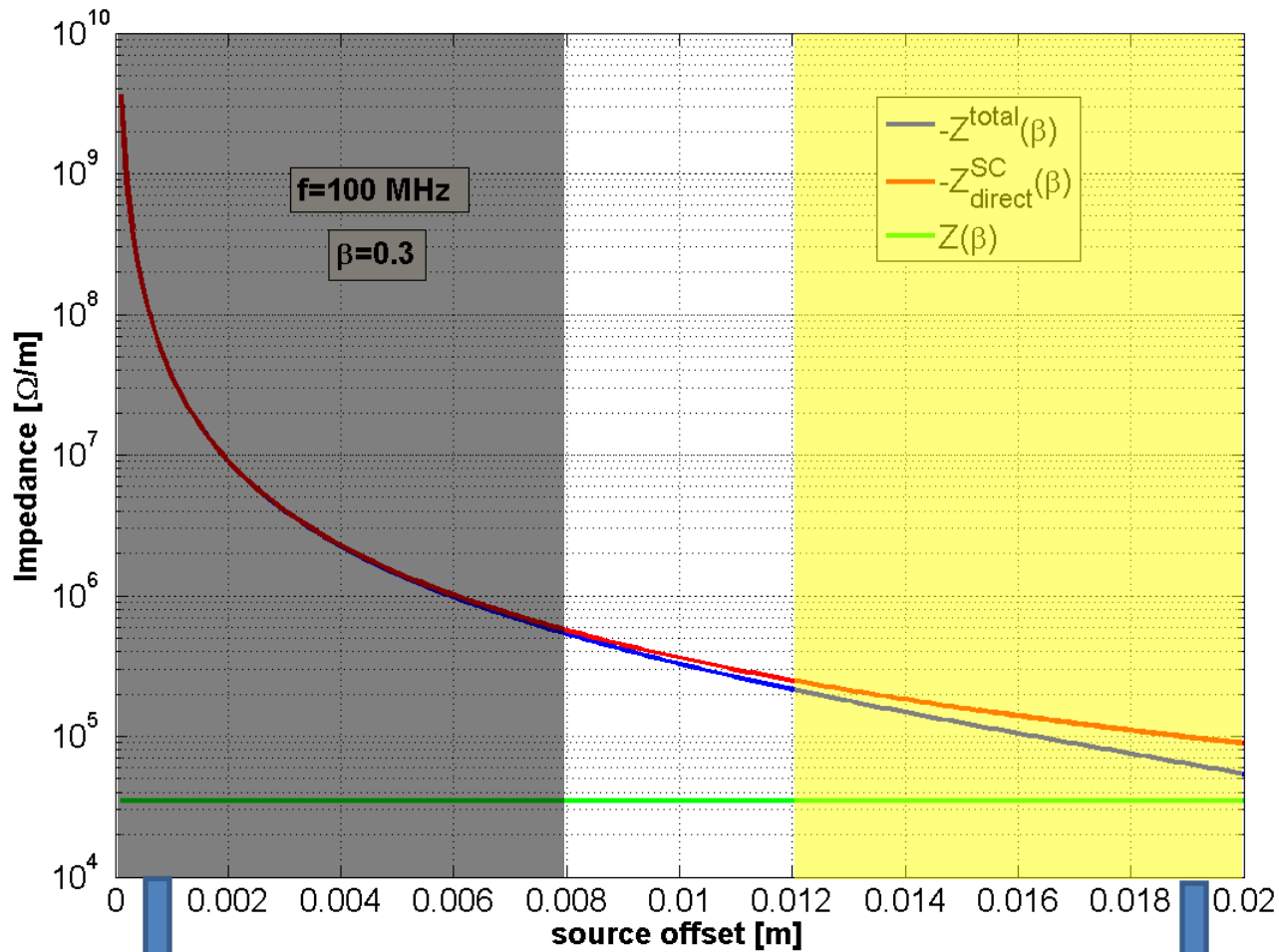
$L = 0.2$ m
Radius = 0.0315 m

Longitudinal impedance: comparison between the analytical calculation and the CST simulation



$L = 0.2$ m
Radius = 0.0315 m

Transverse impedance: analytical calculation

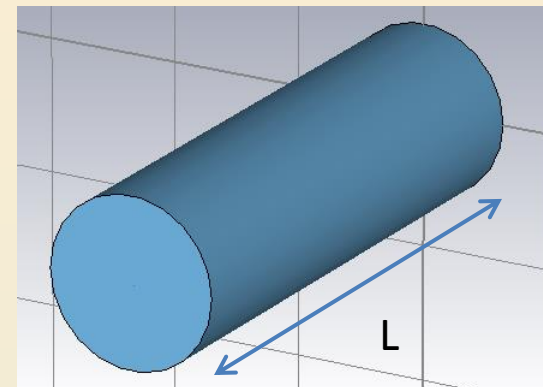
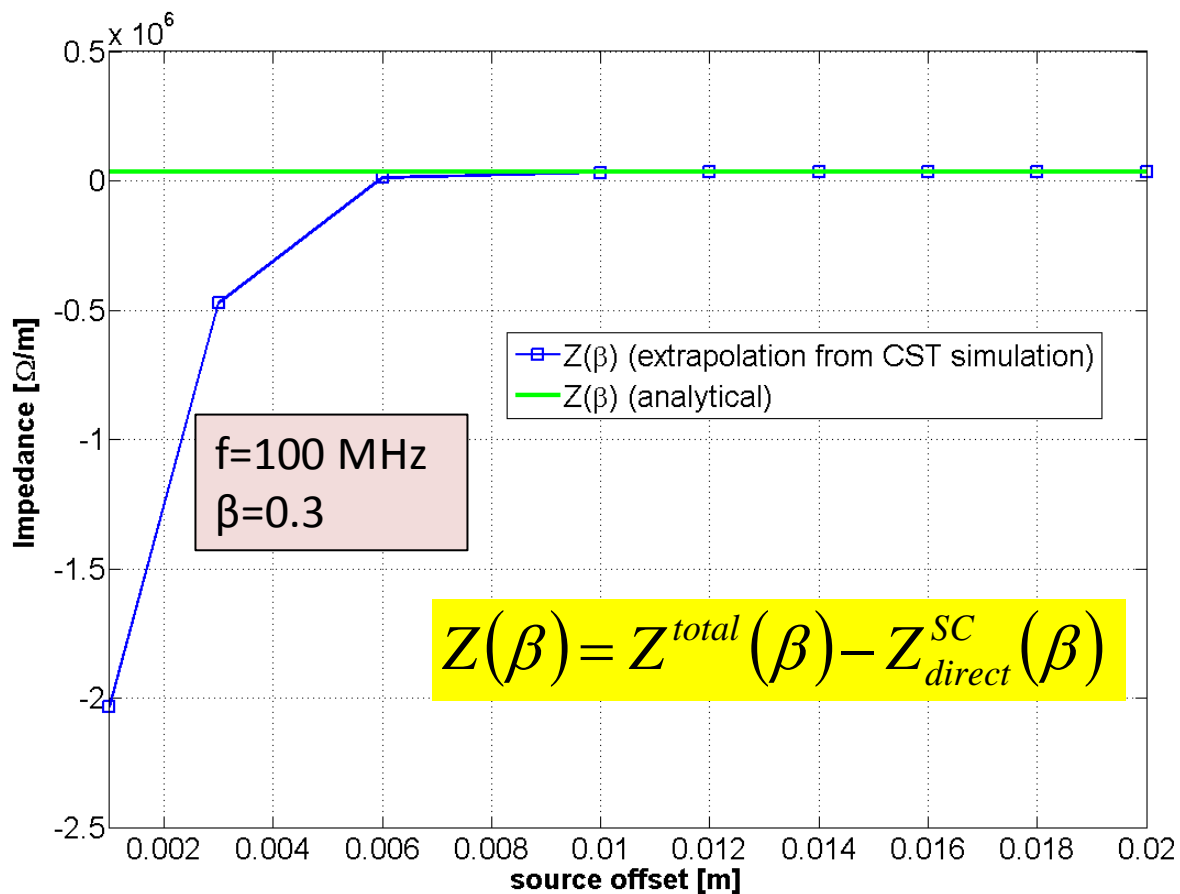


$L = 0.2$ m
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The extrapolation of $Z(\beta)$ would require a very high accuracy of the simulation (impossible to be reached)

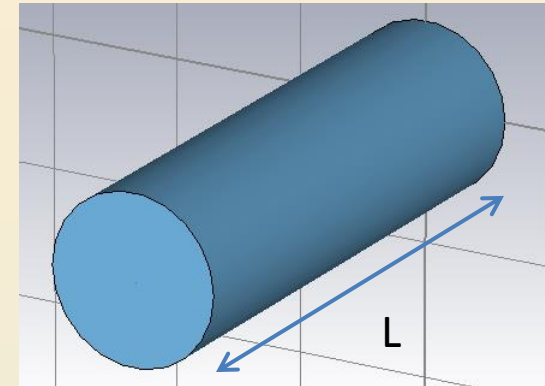
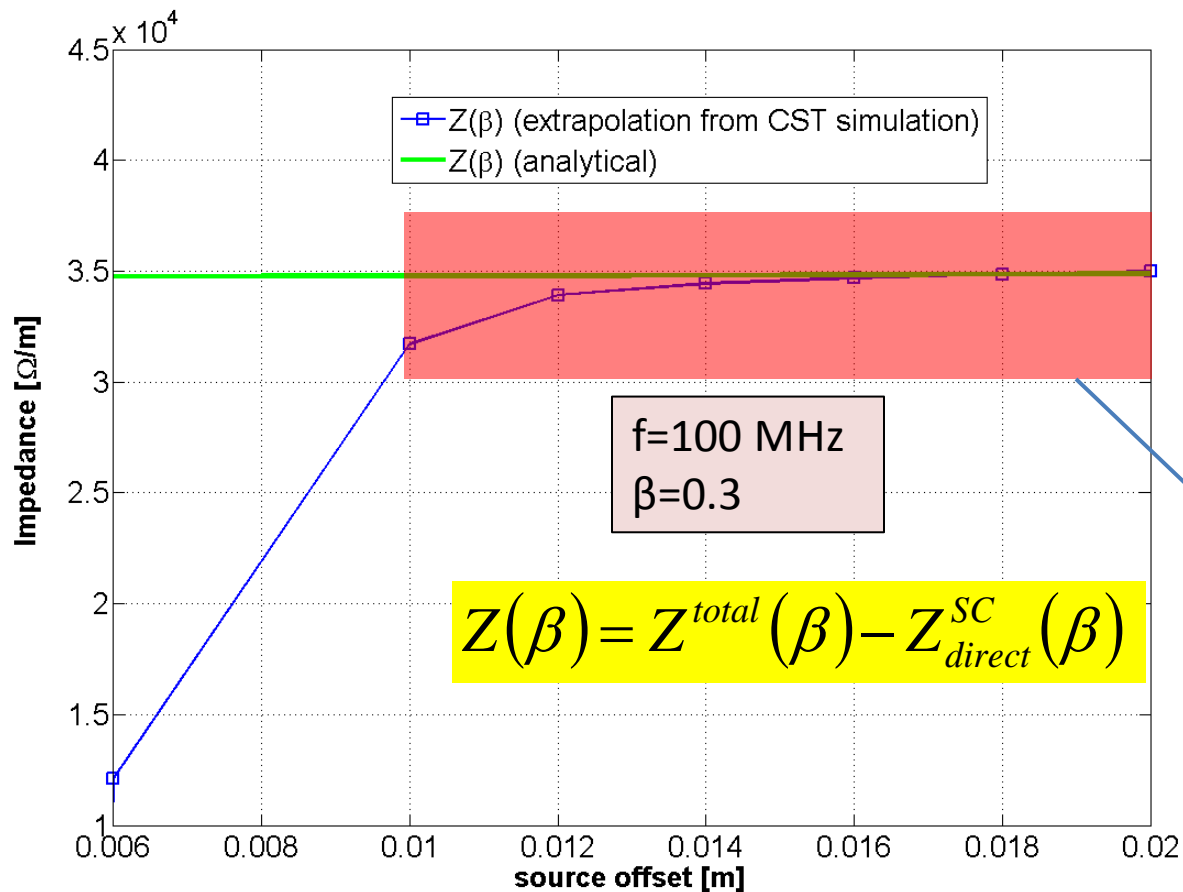
The accuracy of the simulation allow the extrapolation of $Z(\beta)$

Transverse impedance: comparison between the analytical calculation and the CST simulation



$L = 0.2$ m
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Transverse impedance: comparison between the analytical calculation and the CST simulation



$L = 0.2$ m
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Error smaller than 10%

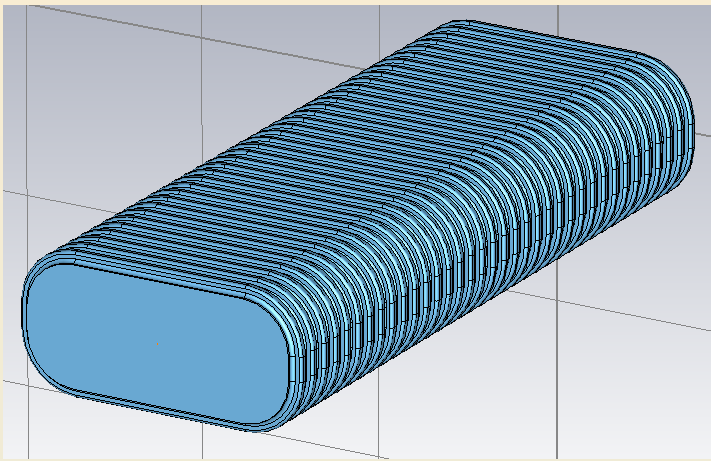
The extrapolation method requires the linearity of the impedance with the offset

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Inconel undulated chamber

Inconel undulated chamber



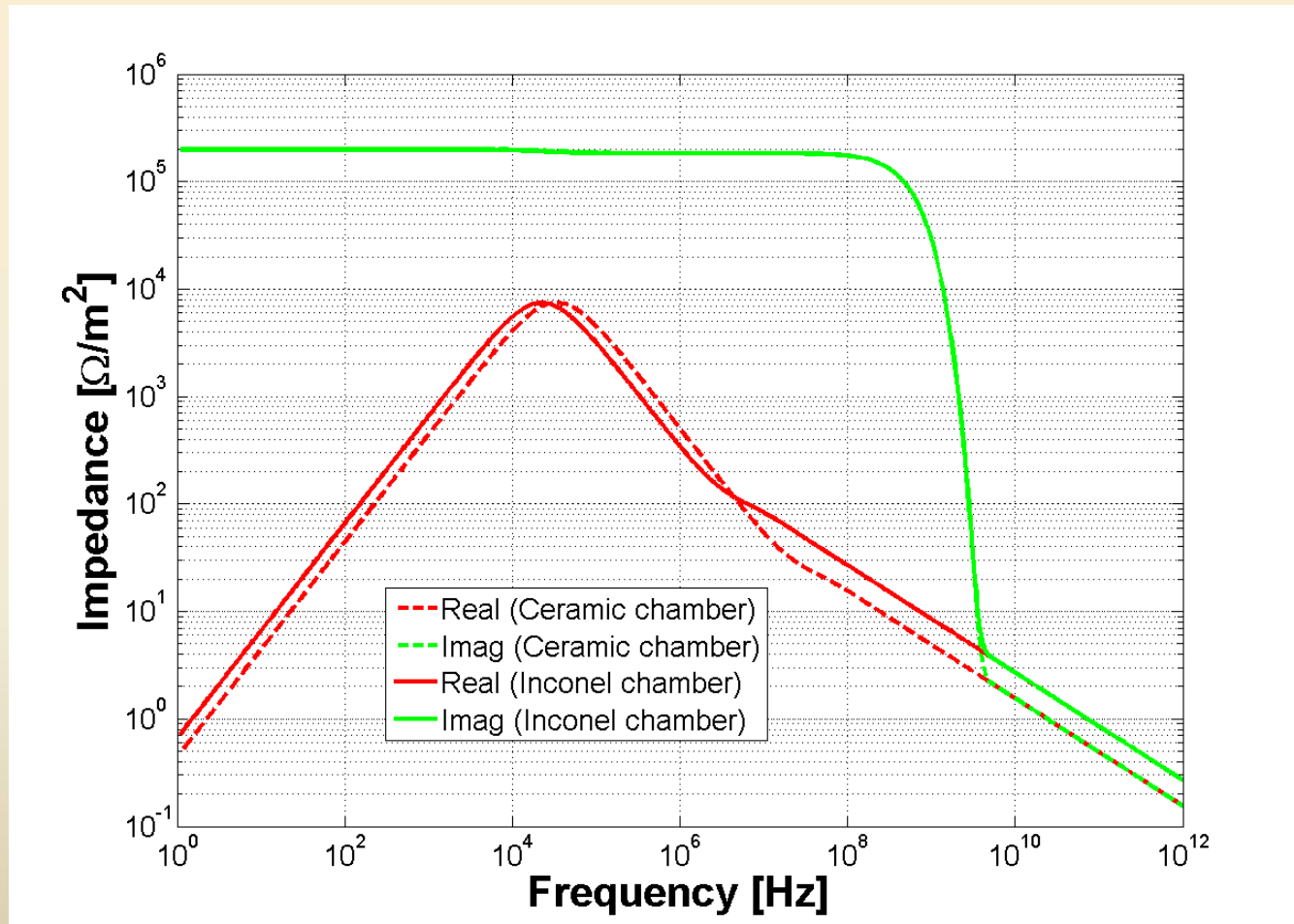
Inconel thickness: 0.45-0.50 mm
Vertical full aperture: 63 mm
Inconel conductivity = $7.89 \cdot 10^5$

Alternative solution

Titanium coated Ceramic (Al_2O_3) chamber
(no corrugation)

Vertical full aperture: 63 mm
Titanium thickness: 100 μm

Analytical calculation (no corrugation): comparison between Inconel and Ceramic chamber

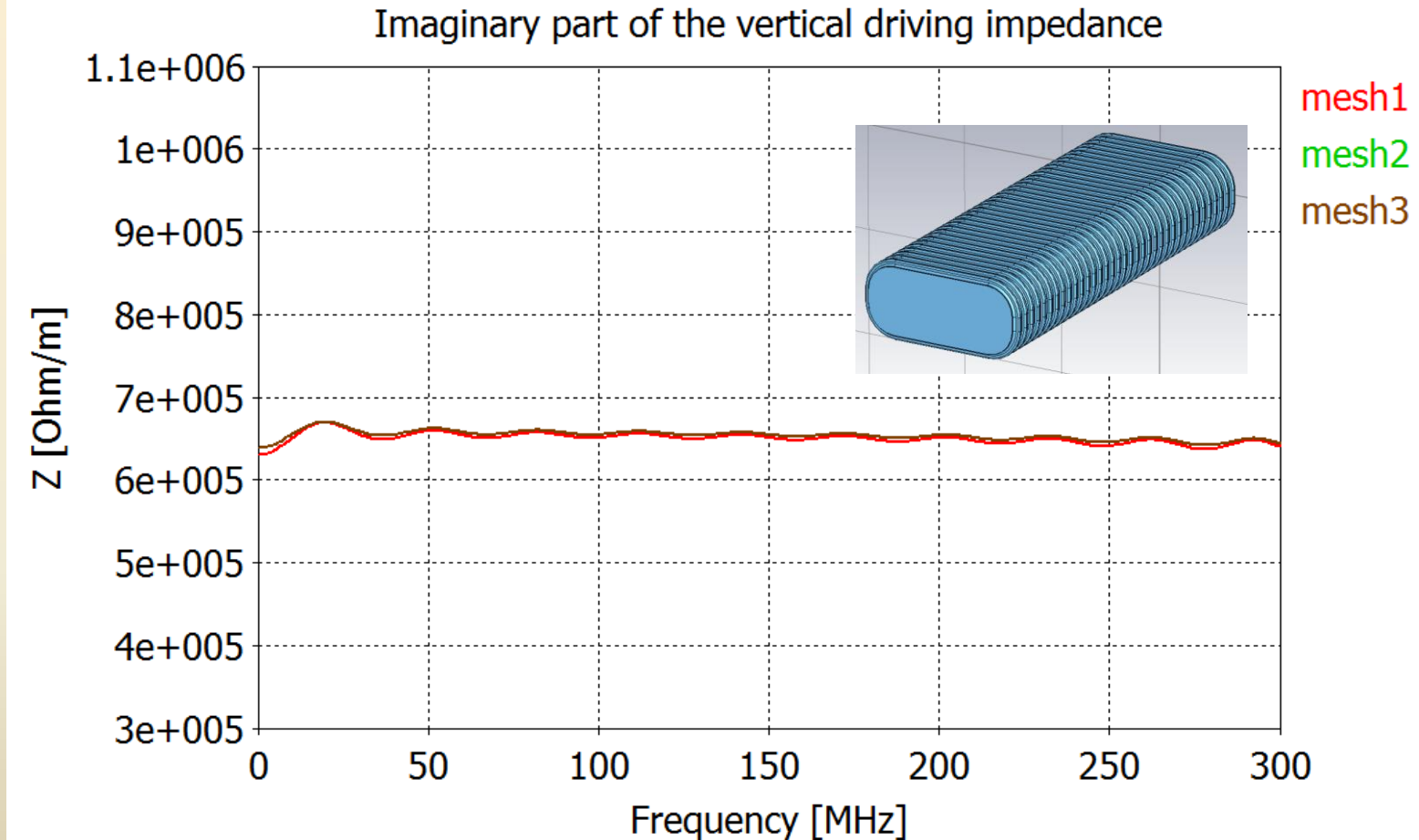


Theoretical calculation made with the TLwall code

Overview

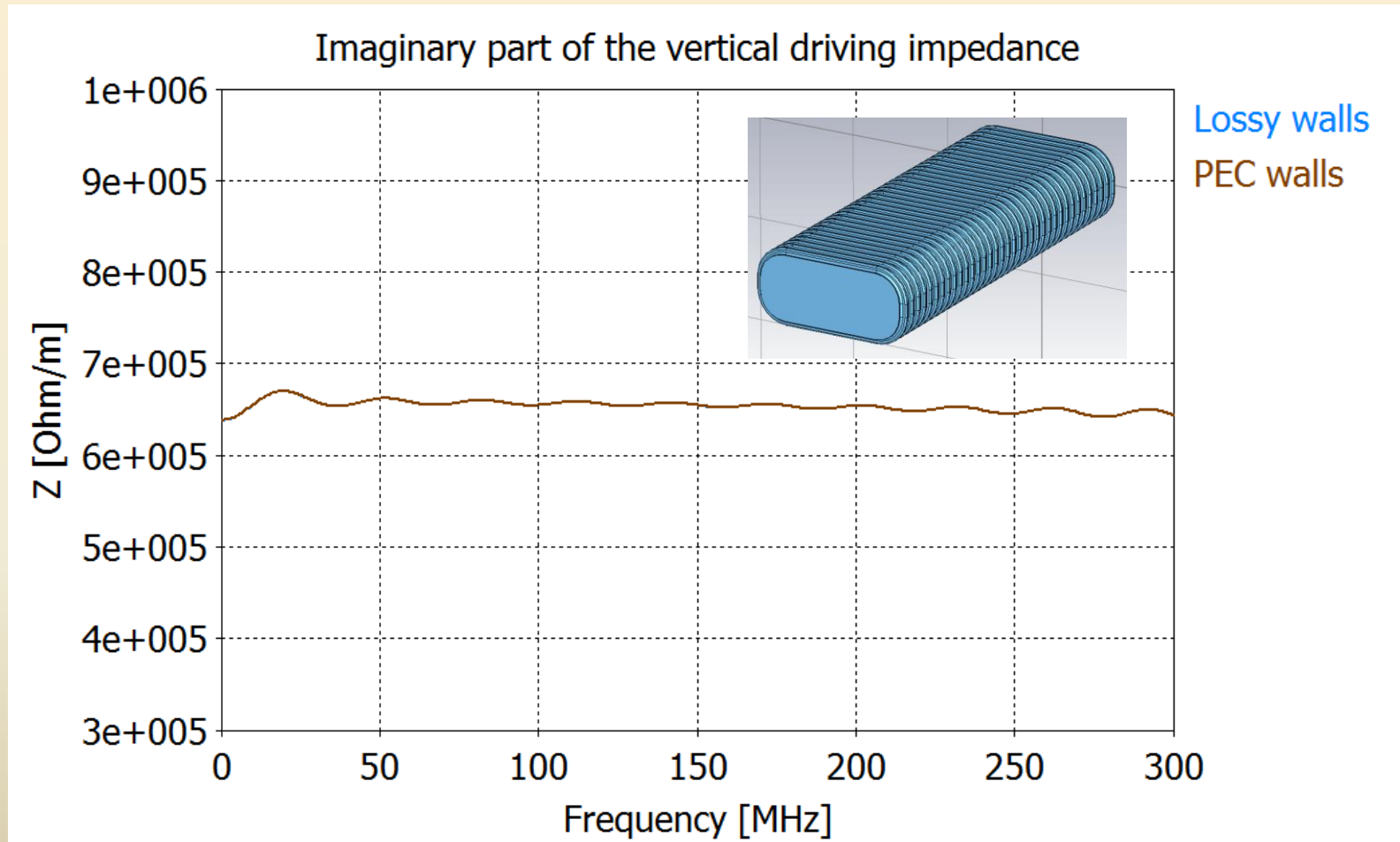
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Inconel undulated chamber: CST Particle Studio simulation



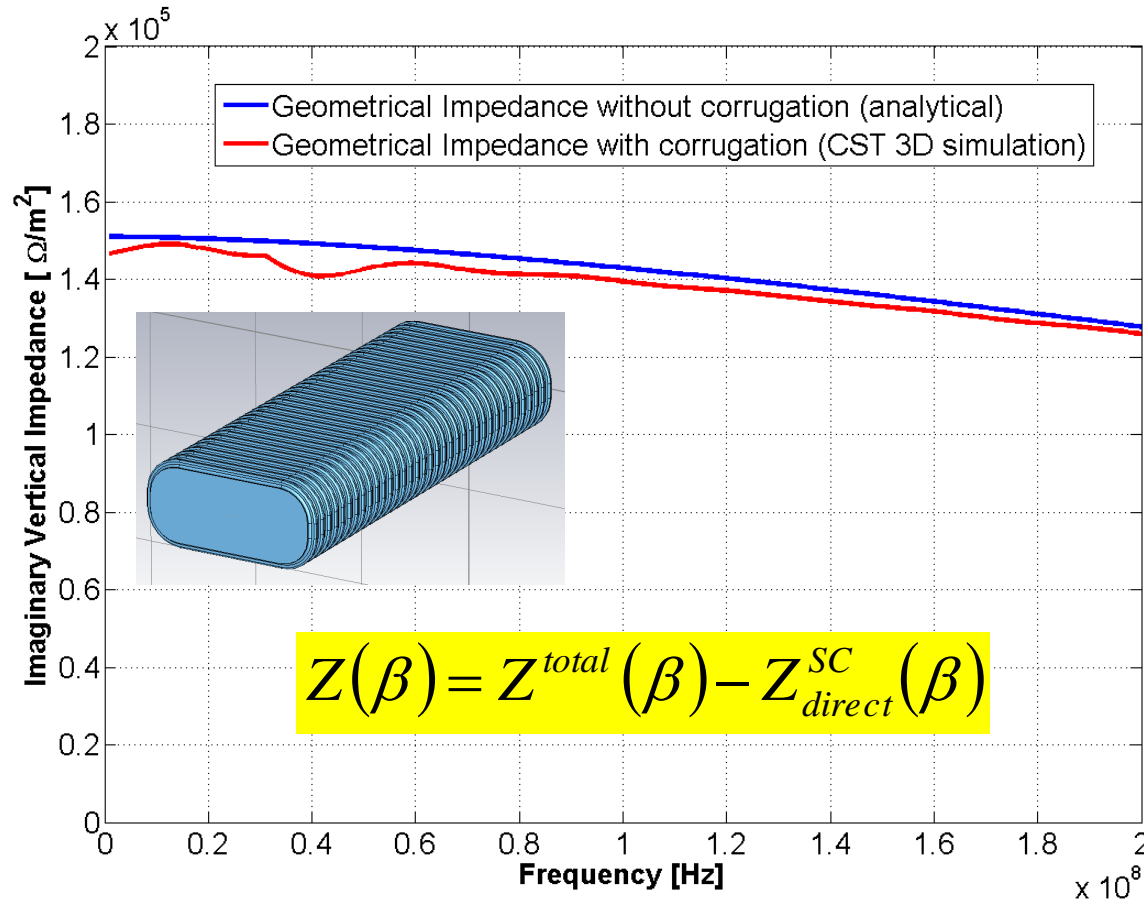
The calculation is stable

Inconel undulated chamber: CST Particle Studio simulation



The resistive wall impedance is insignificant with respect to the total impedance

Inconel undulated chamber: CST Particle Studio simulation



The impedance contribution of the corrugation seems to be negligible

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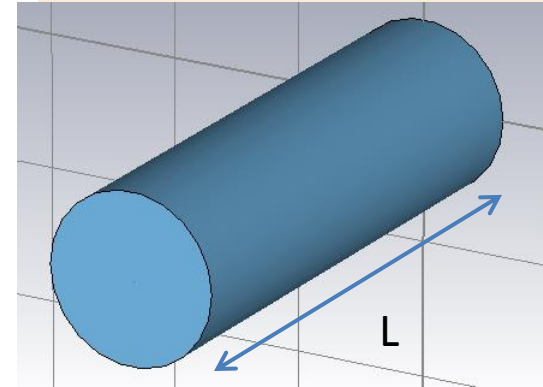
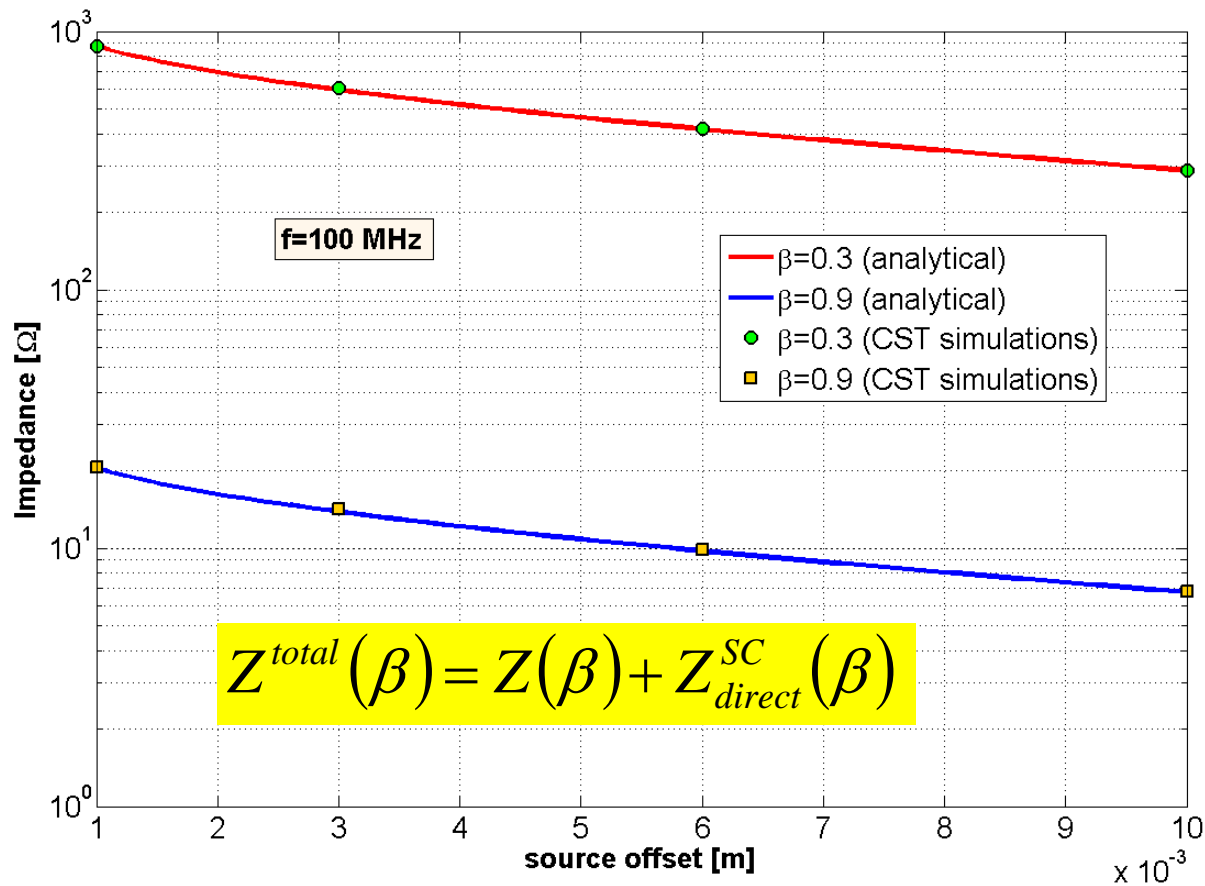
- The use of 3D CST simulation at the PSB energy has been discussed
- From the impedance point of view the Inconel chamber and the ceramic chamber seem to be equivalent

Future plans

- Construction of the PSB impedance model
 - Including all the expected sources of impedance (e.g. kicker)
 - Accurate estimation of the wall impedance
 - I need precise information about the layout of the machine
 - Based on approximate calculations performed by D. Quatraro, the wall impedance represents the 50% of the measured vertical effective impedance at injection ($18 \text{ M}\Omega/\text{m}$)

Thank you very much for your attention

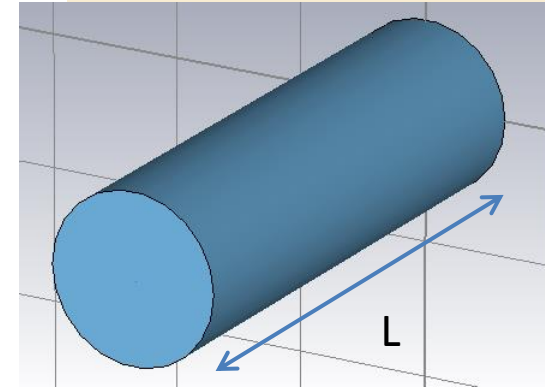
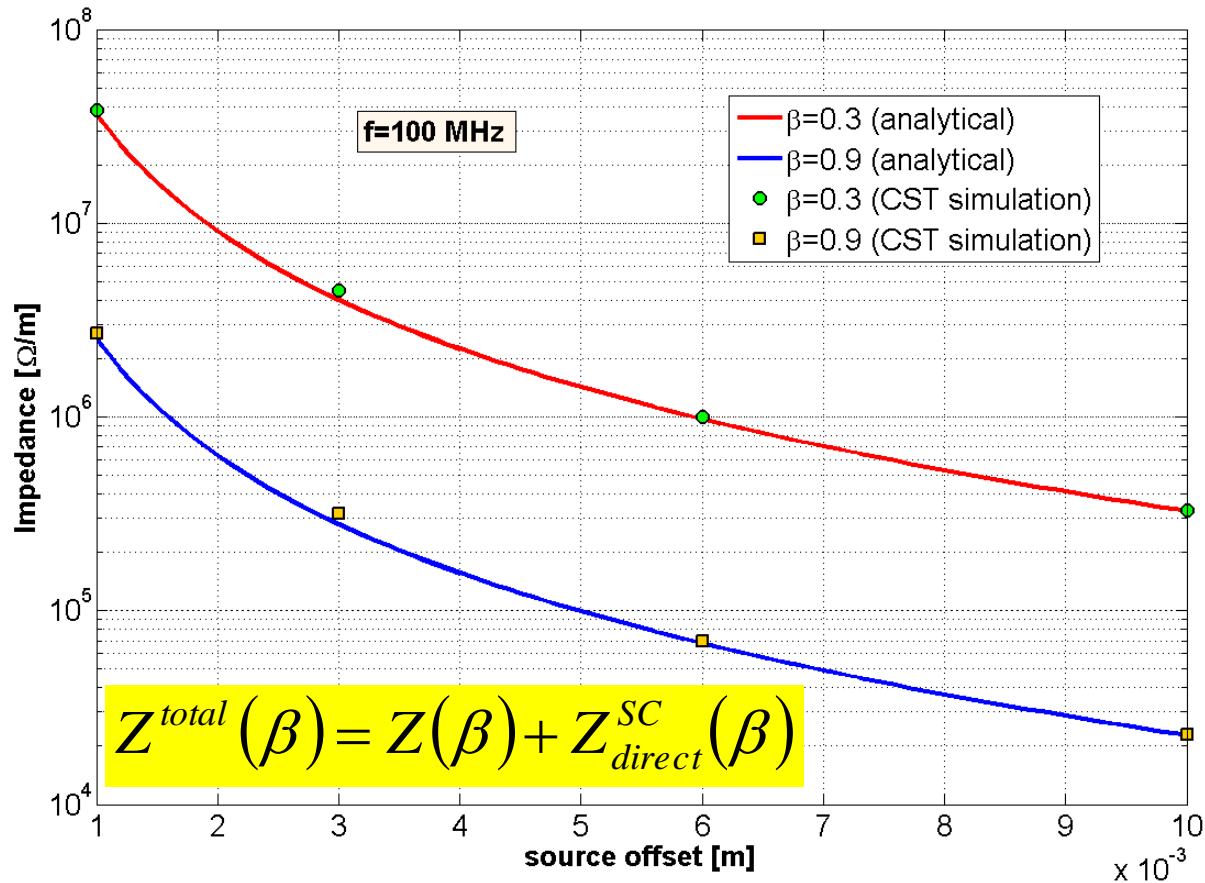
Comparing longitudinal impedance versus source offset



$L = 0.2$ m
Radius = 0.0315 m

CST simulations and analytical model are in very good agreement

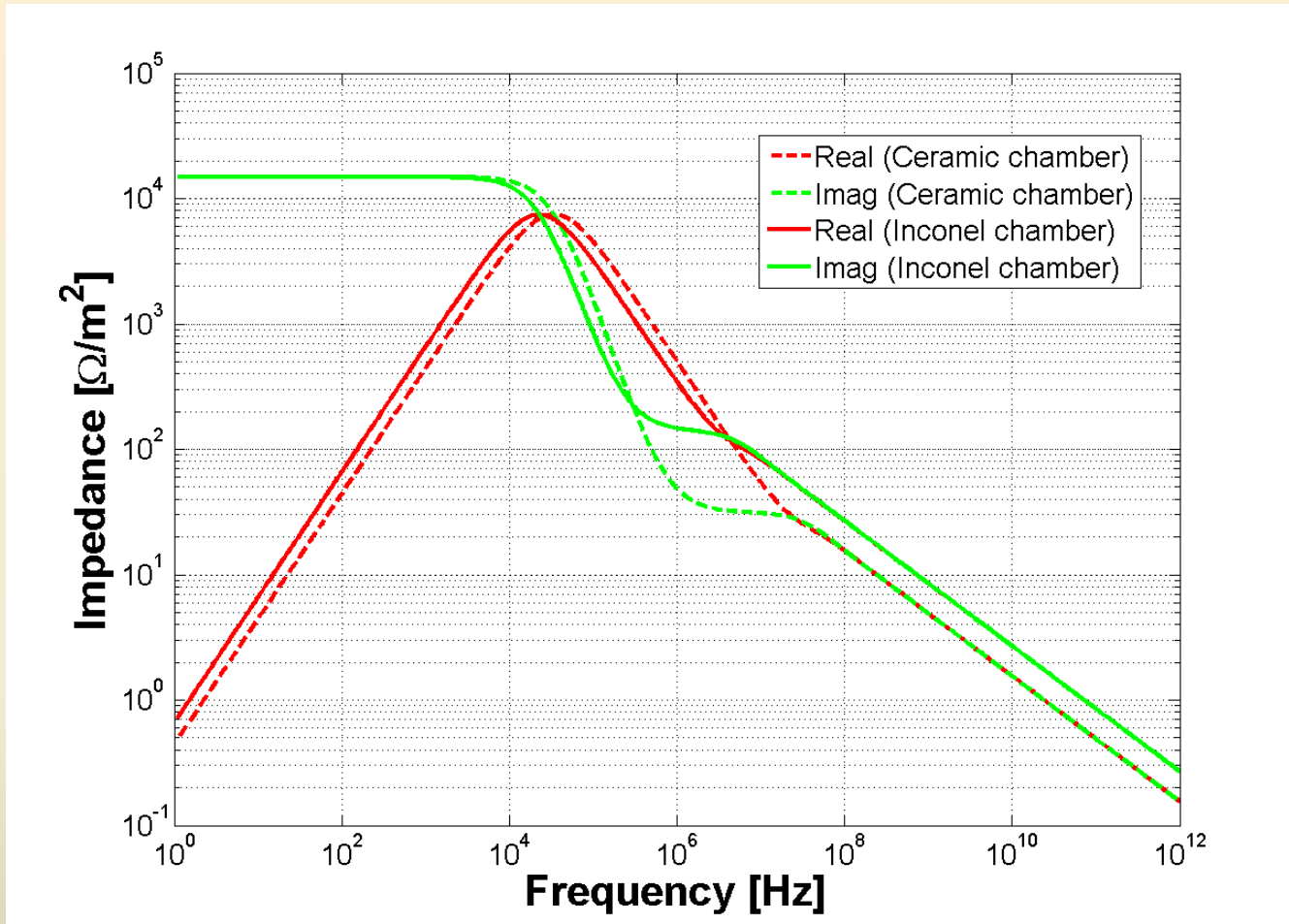
Comparing transverse impedance versus source offset



L = 0.2 m
Radius = 0.0315 m

CST simulations and analytical model are in very good agreement

Resistive wall contribution



Theoretical calculation made with the TLwall code

Impedance contribution of the injection region

