

Status of Lepton Flavor Violation

Paride Paradisi

University of Padua

Implications of LHCb measurements and future prospects
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- **High-energy frontier**: A unique effort to determine the NP scale
- **High-intensity frontier** (flavor physics): A collective effort to determine the flavor structure of NP

Where to look for **New Physics** at the low energy?

- Processes very **suppressed** or even **forbidden** in the SM
 - ▶ FCNC processes ($\mu \rightarrow e\gamma$, $\tau \rightarrow \mu\gamma$, $B_{s,d}^0 \rightarrow \mu^+\mu^-$, $K \rightarrow \pi\nu\bar{\nu}$)
 - ▶ CPV effects in the electron/neutron EDMs, $d_{e,n}\dots$
 - ▶ FCNC & CPV in $B_{s,d}$ & D decay/mixing amplitudes
- Processes predicted with **high precision** in the SM
 - ▶ EWPO as $(g-2)_{\mu,e}$: $a_{\mu}^{exp} - a_{\mu}^{SM} \approx (3 \pm 1) \times 10^{-9}$, a discrepancy at 3σ !
 - ▶ LU in $R_M^{e/\mu} = \Gamma(M \rightarrow e\nu)/\Gamma(M \rightarrow \mu\nu)$ with $M = \pi, K$

- **Neutrino Oscillation** $\Rightarrow m_{\nu_i} \neq m_{\nu_j} \Rightarrow$ **LFV**
- **see-saw**: $m_\nu = \frac{(m_\nu^D)^2}{M_R} \sim \text{eV}$, $M_R \sim 10^{14-16} \Rightarrow m_\nu^D \sim m_{\text{top}}$
- **LFV** transitions like $\mu \rightarrow e\gamma$ @ 1 loop with exchange of

- ▶ W and ν in the **SM** framework (**GIM**) with $\Lambda_{NP} \equiv M_R$

$$\text{Br}(\mu \rightarrow e\gamma) \sim \frac{m_\nu^D{}^4}{M_R^4} \leq 10^{-50}$$

- ▶ \tilde{W} and $\tilde{\nu}$ in the **MSSM** framework (**SUPER-GIM**) with $\Lambda_{NP} \equiv \tilde{m}$

$$\text{Br}(\mu \rightarrow e\gamma) \sim \frac{m_\nu^D{}^4}{\tilde{m}^4} \quad [\text{Borzumati \& Masiero '86}]$$

⇓

- **LFV** signals are undetectable (**detectable**) in the SM (**MSSM**)

Experimental status

process	current exp.	future exp.
K^0 mixing	$\epsilon_K = (2.228 \pm 0.011) \times 10^{-3}$	—
D^0 mixing	$A_\Gamma = (-0.02 \pm 0.16)\%$	$\pm 0.007\%$ LHCb $\pm 0.06\%$ Belle II
B_d mixing	$\sin 2\beta = 0.68 \pm 0.02$	± 0.008 LHCb ± 0.012 Belle II
B_s mixing	$\phi_s = 0.01 \pm 0.07$	± 0.008 LHCb
d_{Hg}	$< 3.1 \times 10^{-29}$ ecm	—
d_{Ra}	—	$\lesssim 10^{-29}$ ecm
d_n	$< 2.9 \times 10^{-26}$ ecm	$\lesssim 10^{-28}$ ecm
d_p	—	$\lesssim 10^{-29}$ ecm
d_e	$< 1.05 \times 10^{-27}$ ecm YbF	$\lesssim 10^{-30}$ ecm YbF, Fr
$\mu \rightarrow e\gamma$	$< 5.4 \times 10^{-13}$ MEG	$\lesssim 6 \times 10^{-14}$ MEG upgrade
$\mu \rightarrow 3e$	$< 1.0 \times 10^{-12}$ SINDRUM I	$\lesssim 10^{-16}$ Mu3e
$\mu \rightarrow e$ in Au	$< 7.0 \times 10^{-13}$ SINDRUM II	—
$\mu \rightarrow e$ in Al	—	$\lesssim 6 \times 10^{-17}$ Mu2e

Table: Summary of current and selected future expected experimental limits on CP violation in meson mixing, EDMs and lepton flavor violating processes.

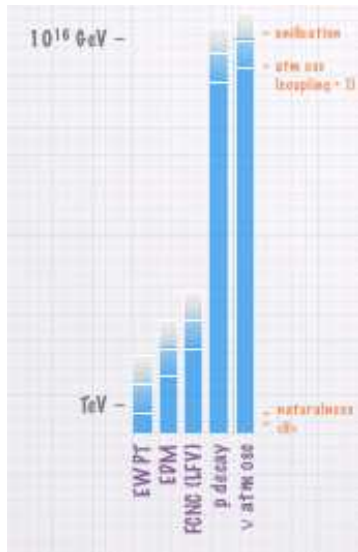
The NP “scale”

- **Gravity** $\implies \Lambda_{\text{Planck}} \sim 10^{18-19}$ GeV
- **Neutrino masses** $\implies \Lambda_{\text{see-saw}} \lesssim 10^{15}$ GeV
- **BAU**: evidence of CPV beyond SM
 - ▶ Electroweak Baryogenesis $\implies \Lambda_{\text{NP}} \lesssim \text{TeV}$
 - ▶ Leptogenesis $\implies \Lambda_{\text{see-saw}} \lesssim 10^{15}$ GeV
- **Hierarchy problem**: $\implies \Lambda_{\text{NP}} \lesssim \text{TeV}$
- **Dark Matter** $\implies \Lambda_{\text{NP}} \lesssim \text{TeV}$

SM = effective theory at the EW scale

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \sum_{d \geq 5} \frac{c_{ij}^{(d)}}{\Lambda_{\text{NP}}^{d-4}} O_{ij}^{(d)}$$

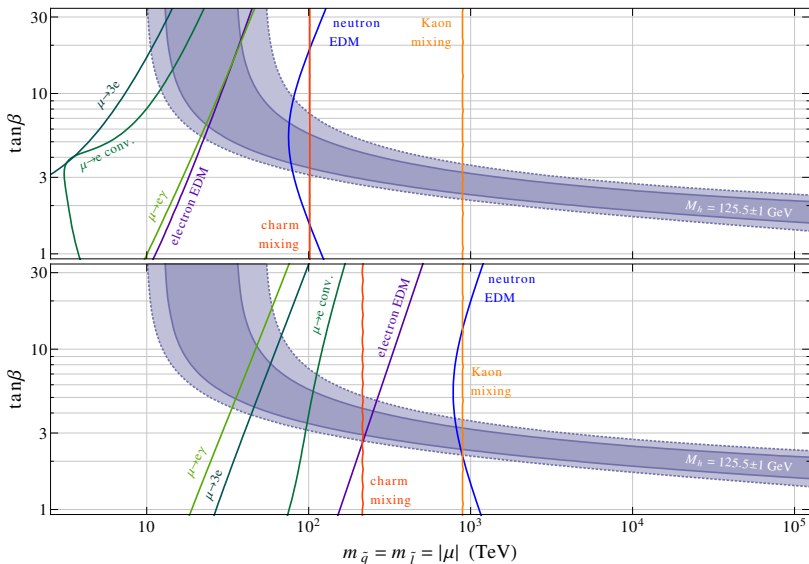
- $\mathcal{L}_{\text{eff}}^{d=5} = \frac{y_{\nu}^{ij}}{\Lambda_{\text{see-saw}}} L_i L_j \phi \phi$,
- $\mathcal{L}_{\text{eff}}^{d=6}$ generates FCNC operators



$$\text{BR}(l_i \rightarrow l_j \gamma) \sim \frac{1}{\Lambda_{\text{NP}}^4}$$

SUSY Flavour after the Higgs discovery

$$|m_{\tilde{B}}| = |m_{\tilde{W}}| = 3 \text{ TeV}, |m_{\tilde{g}}| = 10 \text{ TeV}$$



Low energy constraints fixing $(\delta_A)_{ij} = 0.3$. The upper (lower) plot gives the reach of current (projected future) experimental results [Altmannshofer, Harnik, & Zupan, '13]

- **NP effects are encoded in the effective Lagrangian**

$$\mathcal{L} = e \frac{m_\ell}{2} (\bar{\ell}_R \sigma_{\mu\nu} A_{\ell\ell'} \ell'_L + \bar{\ell}'_L \sigma_{\mu\nu} A_{\ell\ell'}^* \ell_R) F^{\mu\nu} \quad \ell, \ell' = e, \mu, \tau,$$

$$A_{\ell\ell'} = \frac{1}{(4\pi \Lambda_{\text{NP}})^2} \left[\left(g_{\ell k}^L g_{\ell' k}^{L*} + g_{\ell k}^R g_{\ell' k}^{R*} \right) f_1(x_k) + \frac{v}{m_\ell} \left(g_{\ell k}^L g_{\ell' k}^{R*} \right) f_2(x_k) \right],$$

- ▶ **Δa_ℓ and leptonic EDMs are given by**

$$\Delta a_\ell = 2m_\ell^2 \text{Re}(A_{\ell\ell}), \quad \frac{d_\ell}{e} = m_\ell \text{Im}(A_{\ell\ell}).$$

- ▶ **The branching ratios of $\ell \rightarrow \ell' \gamma$ are given by**

$$\frac{\text{BR}(\ell \rightarrow \ell' \gamma)}{\text{BR}(\ell \rightarrow \ell' \nu_\ell \bar{\nu}_{\ell'})} = \frac{48\pi^3 \alpha}{G_F^2} \left(|A_{\ell\ell'}|^2 + |A_{\ell'\ell}|^2 \right).$$

- **“Naive scaling”:**

$$\Delta a_{\ell_i} / \Delta a_{\ell_j} = m_{\ell_i}^2 / m_{\ell_j}^2, \quad d_{\ell_i} / d_{\ell_j} = m_{\ell_i} / m_{\ell_j}.$$

(for instance, if the new particles have an underlying SU(3) flavor symmetry in their mass spectrum and in their couplings to leptons, which is the case for gauge interactions).

- $(g-2)_\ell$ assuming “Naive scaling” $\Delta a_{\ell_i}/\Delta a_{\ell_j} = m_{\ell_i}^2/m_{\ell_j}^2$

$$\Delta a_e = \left(\frac{\Delta a_\mu}{3 \times 10^{-9}} \right) 0.7 \times 10^{-13}, \quad \Delta a_\tau = \left(\frac{\Delta a_\mu}{3 \times 10^{-9}} \right) 0.8 \times 10^{-6}.$$

- EDMs assuming “Naive scaling” $d_{\ell_i}/d_{\ell_j} = m_{\ell_i}/m_{\ell_j}$

$$d_e \simeq \left(\frac{\Delta a_e}{7 \times 10^{-14}} \right) 10^{-24} \tan \phi_e \text{ e cm},$$

$$d_\mu \simeq \left(\frac{\Delta a_\mu}{3 \times 10^{-9}} \right) 2 \times 10^{-22} \tan \phi_\mu \text{ e cm},$$

$$d_\tau \simeq \left(\frac{\Delta a_\tau}{8 \times 10^{-7}} \right) 4 \times 10^{-21} \tan \phi_\tau \text{ e cm},$$

- $\text{BR}(\ell_i \rightarrow \ell_j \gamma)$ vs. $(g-2)_\mu$

$$\text{BR}(\mu \rightarrow e \gamma) \approx 3 \times 10^{-13} \left(\frac{\Delta a_\mu}{3 \times 10^{-9}} \right)^2 \left(\frac{\theta_{e\mu}}{10^{-5}} \right)^2,$$

$$\text{BR}(\tau \rightarrow \mu \gamma) \approx 4 \times 10^{-8} \left(\frac{\Delta a_\mu}{3 \times 10^{-9}} \right)^2 \left(\frac{\theta_{\ell\tau}}{10^{-2}} \right)^2.$$

[Giudice, P.P., & Passera, '12]

A concrete SUSY scenario: “Disoriented A-terms”

- **Challenge:** Large effects for $g-2$ keeping under control $\mu \rightarrow e\gamma$ and d_e
- **“Disoriented A-terms”** [Giudice, Isidori & P.P., '12]:

$$(\delta_{LR}^{ij})_f \sim \frac{A_f \theta_{ij}^f m_{f_j}}{m_{\tilde{f}}} \quad f = u, d, \ell,$$

- ▶ Flavor and CP violation is restricted to the trilinear scalar terms.
 - ▶ Flavor bounds of the down-sector are naturally satisfied thanks to the smallness of down-type quark/lepton masses.
 - ▶ This ansatz arises in scenarios with partial compositeness (where a natural prediction is $\theta_{ij}^\ell \sim \sqrt{m_i/m_j}$ [Rattazzi et al.,'12]) or, as shown in [Calibbi, P.P. and Ziegler,'13], in Flavored Gauge Mediation models [Shadmi and collaborators].
- $\mu \rightarrow e\gamma$ and d_e are generated only by $U(1)$ interactions

$$\text{BR}(\mu \rightarrow e\gamma) \sim \left(\frac{\alpha}{\cos^2 \theta_W} \right)^2 |\delta_{LR}^{\mu e}|^2, \quad \frac{d_e}{e} \sim \frac{\alpha}{\cos^2 \theta_W} \text{Im} \delta_{LR}^{ee}.$$

- $(g-2)_\mu$ is generated by $SU(2)$ interactions and is $\tan \beta$ enhanced

$$\Delta a_\ell \sim \frac{\alpha}{\sin^2 \theta_W} \tan \beta$$

- $(g-2)_\mu$ is enhanced by $\approx 100 \times (\tan \beta/30)$ w.r.t. $\mu \rightarrow e\gamma$ and d_e amplitudes

- Numerical example:** $\tilde{m} = |A_e| = 1 \text{ TeV}$, $\sin \phi_{A_e} = 1$, $M_2 = \mu = 2M_1 = 0.2 \text{ TeV}$, and $\tan \beta = 30$ [Giudice, P.P., & Passera, '12]

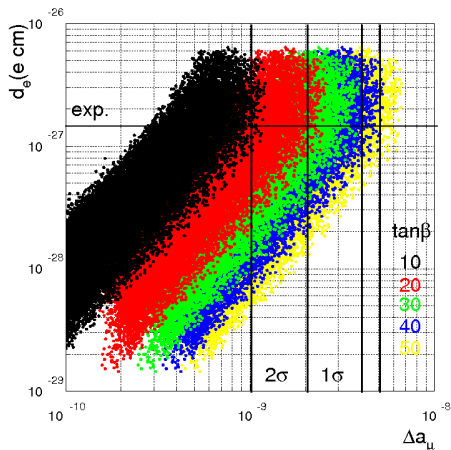
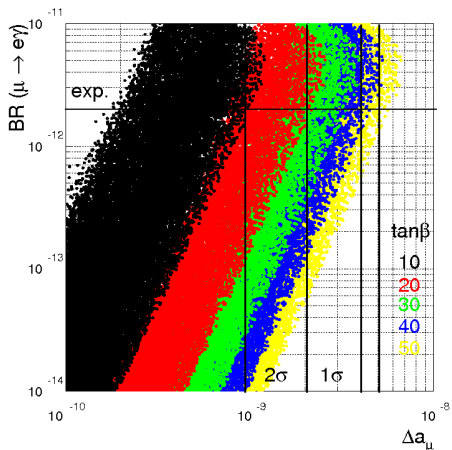
$$\text{BR}(\mu \rightarrow e\gamma) \approx 6 \times 10^{-13} \left| \frac{A_\ell}{\text{TeV}} \frac{\theta_{12}^\ell}{\sqrt{m_e/m_\mu}} \right|^2 \left(\frac{\text{TeV}}{m_{\tilde{\ell}}} \right)^4,$$

$$d_e \approx 4 \times 10^{-28} \text{Im} \left(\frac{A_\ell \theta_{11}^\ell}{\text{TeV}} \right) \left(\frac{\text{TeV}}{m_{\tilde{\ell}}} \right)^2 e \text{ cm},$$

$$\Delta a_\mu \approx 1 \times 10^{-9} \left(\frac{\text{TeV}}{m_{\tilde{\ell}}} \right)^2 \left(\frac{\tan \beta}{30} \right).$$

- ▶ Disoriented A-terms can account for $(g-2)_\mu$, satisfy the bounds on $\mu \rightarrow e\gamma$ and d_e , while giving predictions for $\mu \rightarrow e\gamma$ and d_e within experimental reach.
- ▶ The electron $(g-2)$ follows “naive scaling”.
- ▶ The Higgs boson mass $m_h \approx 126 \text{ GeV}$ is a natural prediction (even for stops at 1 TeV) thanks to the large A-terms [Giudice, Isidori, P.P., '12].

A concrete SUSY scenario: “Disoriented A-terms”



Predictions for $\mu \rightarrow e\gamma$, Δa_μ and d_e in the disoriented A-term scenario with $\theta_{ij}^\ell = \sqrt{m_i/m_j}$. Left: $\mu \rightarrow e\gamma$ vs. Δa_μ . Right: d_e vs. Δa_μ [Giudice, P.P., & Passera, '12]

- LFV processes with an undelying $\tau - \mu$ and $\tau - e$ are unobservable

- LFV operators up to dimension-six

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda_{\text{LFV}}^2} \mathcal{O}^{\text{dim-6}} + \dots$$

$$\mathcal{O}^{\text{dim-6}} \ni \bar{\mu}_R \sigma^{\mu\nu} H e_L F_{\mu\nu}, (\bar{\mu}_L \gamma^\mu e_L) (\bar{f}_L \gamma^\mu f_L), (\bar{\mu}_R e_L) (\bar{f}_R f_L), f = e, u, d$$

- the dipole-operator leads to $\ell \rightarrow \ell' \gamma$ while 4-fermion operators generate processes like $\ell_i \rightarrow \ell_j \bar{\ell}_k \ell_k$ and $\mu \rightarrow e$ conversion in Nuclei.
- When the dipole-operator is dominant:

$$\frac{\text{BR}(\ell_i \rightarrow \ell_j \ell_k \bar{\ell}_k)}{\text{BR}(\ell_i \rightarrow \ell_j \bar{\nu}_j \nu_i)} \simeq \frac{\alpha_{e\ell}}{3\pi} \left(\log \frac{m_{\ell_i}^2}{m_{\ell_k}^2} - 3 \right) \frac{\text{BR}(\ell_i \rightarrow \ell_j \gamma)}{\text{BR}(\ell_i \rightarrow \ell_j \bar{\nu}_j \nu_i)},$$

$$\text{CR}(\mu \rightarrow e \text{ in N}) \simeq \alpha_{\text{em}} \times \text{BR}(\mu \rightarrow e \gamma).$$

- $\text{BR}(\mu \rightarrow e \gamma) \sim 10^{-12}$ implies $\text{BR}(\mu \rightarrow eee) \leq 0.5 \times 10^{-14}$ and $\text{CR}(\mu \rightarrow e \text{ in N}) \leq 0.5 \times 10^{-14}$.
- A combined analysis of $\mu \rightarrow e$ conversion on different target nuclei can discriminate among the underlying operators since the sensitivity of different processes to these operators is not the same [Okada et al. 2004].
- For three body LFV decays as $\mu \rightarrow eee$, an angular analysis of the signal would be crucial to shed light on the operator which is at work.

- Ratios like $Br(\mu \rightarrow e\gamma)/Br(\tau \rightarrow \mu\gamma)$ probe the NP flavor structure
- Ratios like $Br(\mu \rightarrow e\gamma)/Br(\mu \rightarrow eee)$ probe the NP operator at work

ratio	LHT	MSSM	SM4
$\frac{Br(\mu \rightarrow eee)}{Br(\mu \rightarrow e\gamma)}$	0.02... 1	$\sim 2 \cdot 10^{-3}$	0.06... 2.2
$\frac{Br(\tau \rightarrow eee)}{Br(\tau \rightarrow e\gamma)}$	0.04... 0.4	$\sim 1 \cdot 10^{-2}$	0.07... 2.2
$\frac{Br(\tau \rightarrow \mu\mu\mu)}{Br(\tau \rightarrow \mu\gamma)}$	0.04... 0.4	$\sim 2 \cdot 10^{-3}$	0.06... 2.2
$\frac{Br(\tau \rightarrow e\mu\mu)}{Br(\tau \rightarrow e\gamma)}$	0.04... 0.3	$\sim 2 \cdot 10^{-3}$	0.03... 1.3
$\frac{Br(\tau \rightarrow \mu ee)}{Br(\tau \rightarrow \mu\gamma)}$	0.04... 0.3	$\sim 1 \cdot 10^{-2}$	0.04... 1.4
$\frac{Br(\tau \rightarrow eee)}{Br(\tau \rightarrow e\mu\mu)}$	0.8... 2	~ 5	1.5... 2.3
$\frac{Br(\tau \rightarrow \mu\mu\mu)}{Br(\tau \rightarrow \mu ee)}$	0.7... 1.6	~ 0.2	1.4... 1.7
$\frac{R(\mu Tl \rightarrow e Tl)}{Br(\mu \rightarrow e\gamma)}$	$10^{-3} \dots 10^2$	$\sim 5 \cdot 10^{-3}$	$10^{-12} \dots 26$

[Buras et al., '07, '10]

- **Longstanding muon $g - 2$ anomaly**

$$\Delta a_\mu = a_\mu^{\text{EXP}} - a_\mu^{\text{SM}} = 2.90(90) \times 10^{-9}, \quad \mathbf{3.5\sigma \text{ discrepancy}}$$

- **NP effects are expected to be of order $a_\ell^{\text{NP}} \sim a_\ell^{\text{EW}}$**

$$a_\mu^{\text{EW}} = \frac{m_\mu^2}{(4\pi v)^2} \left(1 - \frac{4}{3} \sin^2 \theta_W + \frac{8}{3} \sin^4 \theta_W \right) \approx 2 \times 10^{-9}.$$

- **Main question: how could we check if the a_μ discrepancy is due to NP?**
- **Answer: testing new-physics effects in a_e** [Giudice, P.P. & Passera, '12]
- **“Naive scaling”:** $\Delta a_{\ell_i} / \Delta a_{\ell_j} = m_{\ell_i}^2 / m_{\ell_j}^2$

$$\Delta a_e = \left(\frac{\Delta a_\mu}{3 \times 10^{-9}} \right) 0.7 \times 10^{-13}.$$

- ▶ a_e has never played a role in testing beyond SM effects. From $a_e^{\text{SM}}(\alpha) = a_e^{\text{EXP}}$, we extract α which is the most precise value of α available today!
- ▶ The situation has now changed thanks to progresses both on the th. and exp. sides.

- **Using the second best determination of α from atomic physics $\alpha(^{87}\text{Rb})$**

$$\Delta a_e = a_e^{\text{EXP}} - a_e^{\text{SM}} = -10.6 (8.1) \times 10^{-13},$$

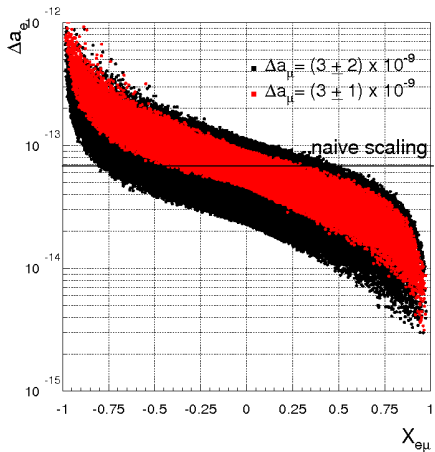
- ▶ Beautiful test of QED at four-loop level!
- ▶ $\delta \Delta a_e = 8.1 \times 10^{-13}$ is dominated by δa_e^{SM} through $\delta \alpha(^{87}\text{Rb})$.

- **Future improvements in the determination of Δa_e**

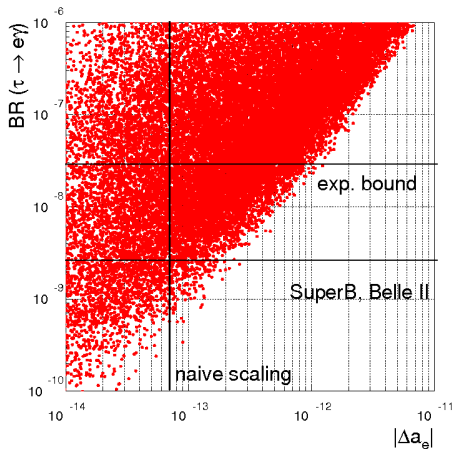
$$\underbrace{(0.6)_{\text{QED4}}, (0.4)_{\text{QED5}}, (0.2)_{\text{HAD}}, (7.6)_{\delta\alpha}, (2.8)_{\delta a_e^{\text{EXP}}}}_{(0.7)_{\text{TH}}}$$

- ▶ The first error, 0.6×10^{-13} , stems from numerical uncertainties in the four-loop QED. It can be reduced to 0.1×10^{-13} with a large scale numerical recalculation [Kinoshita]
 - ▶ The second error, from five-loop QED term may soon drop to 0.1×10^{-13} .
 - ▶ Experimental uncertainties 2.8×10^{-13} (δa_e^{EXP}) and 7.6×10^{-13} ($\delta \alpha$) dominate. We expect a reduction of the former error to a part in 10^{-13} (or better) [Gabrielse]. Work is also in progress for a significant reduction of the latter error [Nez].
- **Δa_e at the 10^{-13} (or below) is not too far! This will bring a_e to play a pivotal role in probing new physics in the leptonic sector.**

- SUSY contributions to a_ℓ comes from loops with exchange of chargino/sneutrino or neutralino/charged slepton.
- **Violations of “naive scaling”** can arise through sources of non-universalities in the slepton mass matrices in two possible ways
 - ▶ **Lepton flavor conserving (LFC) case.** The charged slepton mass matrix violates the global non-abelian **flavor symmetry**, but preserves $U(1)^3$. This case is characterized by non-degenerate sleptons ($m_{\tilde{e}} \neq m_{\tilde{\mu}} \neq m_{\tilde{\tau}}$) but vanishing mixing angles because of an exact alignment.
 - Interesting interplay with collider physics: slepton mass splittings from kinematic edges [Allanach, Colon, Lester, '08, Buras, Calibbi, P.P., '09, see talk by Shadmi]
 - ▶ **Lepton flavor violating (LFV) case.** The slepton mass matrix fully breaks **flavor symmetry** up to $U(1)$ lepton number, generating mixing angles that allow for flavor transitions. Lepton flavor violating processes, such as $\mu \rightarrow e\gamma$, provide stringent constraints on this case. However, because of flavor transitions, a_e and a_μ can receive new large contributions proportional to m_τ (from a chiral flip in the internal line of the loop diagram) [Girrbach, Nierste, '09], giving a new source of non-naive scaling.



$$\Delta a_e \text{ vs. } X_{e\mu} = (m_\theta^2 - m_\mu^2)/(m_\theta^2 + m_\mu^2)$$



$$BR(\tau \rightarrow e\gamma) \text{ vs. } |\Delta a_e|$$

- **LFV Higgs decays** are interesting probes of LFV: $\text{BR}(h \rightarrow \tau\mu) \lesssim 0.1$ is allowed by all low-energy constraints [see talks by Zupan, Harnik], "What if $\text{BR}(h \rightarrow \mu\mu)/\text{BR}(h \rightarrow \tau\tau) \neq m_\mu^2/m_\tau^2$?" [Nir and collaborators, '13]

- **How large can be $\text{BR}(B_s \rightarrow \tau\mu)$?** A crude estimate: assuming $\text{BR}(B_s \rightarrow \mu\mu) \sim 3 \times 10^{-9}$ to be saturated by NP effect

$$\text{BR}(B_s \rightarrow \tau\mu) \lesssim \text{BR}(B_s \rightarrow \mu\mu) \times \left| \frac{Y_{\tau\mu}}{Y_{\mu\mu}} \right|^2$$

- ▶ In the Cheng-Sher ansatz $Y_{\tau\mu}/Y_{\mu\mu} \sim \sqrt{m_\tau/m_\mu}$ and therefore $\text{BR}(B_s \rightarrow \tau\mu) \lesssim 5 \times 10^{-8}$.
 - ▶ In SUSY $Y_{\tau\mu}$ is loop-induced by non-holomorphic Yukawa couplings $Y_{\tau\mu}/Y_{\mu\mu} \sim \epsilon \tan\beta \times (m_\tau/m_\mu) \times \delta_{\tau\mu}$. For $\epsilon \tan\beta \sim 0.2$ and $\delta_{\tau\mu} \sim 0.5$ $\text{BR}(B_s \rightarrow \tau\mu) \lesssim 10^{-8}$.
- **τ -LFV channels @ Belle II & LHCb** and $B \rightarrow K(K^*)\tau\mu$ **at LHCb** are interesting probes of LFV as they are complementary to $\mu \rightarrow e$ processes.
 - LFV at collider: [see the talk by Shadmi]

- **Important questions in view of ongoing/future experiments are** [Isidori, Nir & Perez, '10]:
 - ▶ What are the expected deviations from the SM predictions induced by TeV NP?
 - ▶ Which observables are not limited by theoretical uncertainties?
 - ▶ In which case we can expect a substantial improvement on the experimental side?
 - ▶ What will the measurements teach us if deviations from the SM are [not] seen?
- **Answers:**
 - ▶ The expected deviations from the SM predictions induced by NP at the TeV scale with generic flavor structure are already ruled out by many orders of magnitudes.
 - ▶ On general grounds, we can expect any size of deviation below the current bounds.
 - ▶ The cleanest th. observables are cLFV processes, leptonic EDMs, LFU observables, rare B and K decays (especially $B_{s,d} \rightarrow \mu^+ \mu^-$, $K \rightarrow \pi \nu \bar{\nu}$), CPV in meson mixing
 - ▶ On the exp. side there are still excellent prospects of improvements in several clean channels: $\mu \rightarrow e \gamma$, $\mu N \rightarrow e N$, $\mu \rightarrow e e e$, τ -LFV, EDMs, leptonic $(g-2)_\mu$, $B_{s,d} \rightarrow \mu^+ \mu^-$, $K \rightarrow \pi \nu \bar{\nu}$, CPV in B_s and D systems, γ from $B \rightarrow DK$.
 - ▶ The the origin of the $(g-2)_\mu$ discrepancy can be understood testing new-physics effects in the electron $(g-2)_e$. This would require improved measurements of $(g-2)_e$ and more refined determinations of α in atomic-physics experiments.

Irrespectively of whether the LHC will discover or not new particles, flavor physics will continue to teach us a lot!