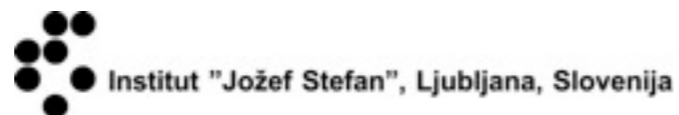


# Theory implications from rare charm decays

Nejc Košnik



Univerza v Ljubljani  
Fakulteta za *matematiko in fiziko*



# Rare charm decays

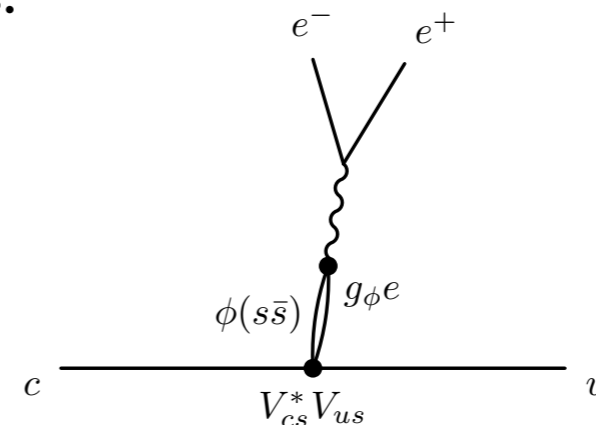
- Small and almost CP conserving short distance FCNCs due to effective GIM cancellation

$$m_d, m_s, m_b \ll M_W \quad \text{CKM} \sim \begin{pmatrix} 1 & \lambda & \lambda^3 \\ \lambda & 1 & \lambda^2 \\ \lambda^3 & \lambda^2 & 1 \end{pmatrix}$$

- Sensitive to NP in up-quarks FCNC
- FCNCs in the up sector are few:  $D\bar{D}$  mixing, rare charm decays, rare t decays

## However ...

- GIM broken by nonperturbative effects. Resonances distinguish s and d quarks. Large long distance contributions obscure FCNCs.



# Plan

- $c \rightarrow u \mu^+ \mu^-$  probing SUSY-RPV, leptoquarks ... in
  - $D^+ \rightarrow \pi^+ \mu^+ \mu^-$
  - $D^0 \rightarrow \mu^+ \mu^-$
- Direct CP Vs. Rare decay (in  $\text{Im}[C_7]$  ).
  - $\Delta A_{\text{CP}} \equiv A_{\text{CP}}(D^0 \rightarrow K^+ K^-) - A_{\text{CP}}(D^0 \rightarrow \pi^+ \pi^-)$
  - direct CP of on the  $\Phi$  peak in  $D^+ \rightarrow \pi^+ \mu^+ \mu^-$
  - large  $q^2$  region of  $D^+ \rightarrow \pi^+ \mu^+ \mu^-$
- Many other interesting decays, LFV, LNV, *not* covered here

$$D^0 \rightarrow \mu^+ e^-, \tau^+ e^- \quad D \rightarrow PP' \ell^+ \ell^-$$

$$D \rightarrow P \mu^+ e^- \quad D_{(s)} \rightarrow V \ell^+ \ell^-$$

$$D_{(s)}^+ \rightarrow P^- \mu^+ \mu^+$$

# Effective Hamiltonian for

$$D \rightarrow P \ell^+ \ell^-$$

$$\mathcal{H}_{\text{eff}} = \lambda_d \mathcal{H}^d + \lambda_s \mathcal{H}^s + \lambda_b \mathcal{H}^{\text{peng}}$$

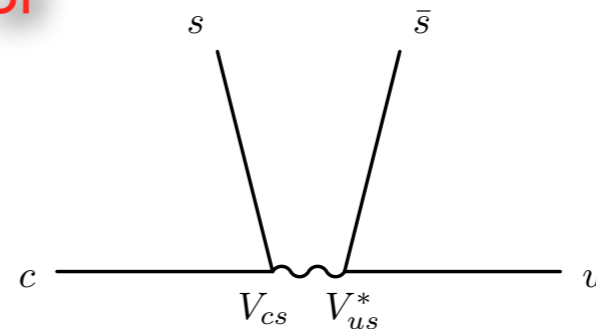
$$\mathcal{H}^{q=d,s} = -\frac{4G_F}{\sqrt{2}} (C_1 \mathcal{O}_1^q + C_2 \mathcal{O}_2^q)$$

$$\lambda_i = V_{ci}^* V_{ui}$$

$$\lambda_d \approx -\lambda_s \approx \lambda$$

Singly Cabibbo suppressed,  
real up to  $\mathcal{O}(\lambda^5)$

nonlocal contributions of  
d and s quarks



$$\mathcal{O}_1^q = (\bar{q}_L^\alpha \gamma^\mu c_L^\alpha) (\bar{u}_L^\beta \gamma_\mu q_L^\beta)$$

$$\mathcal{O}_2^q = (\bar{q}_L^\alpha \gamma^\mu c_L^\beta) (\bar{u}_L^\beta \gamma_\mu q_L^\alpha)$$

$$C_1^{\text{SM,tree}} = 1, C_2^{\text{SM,tree}} = 0$$

# Effective Hamiltonian for

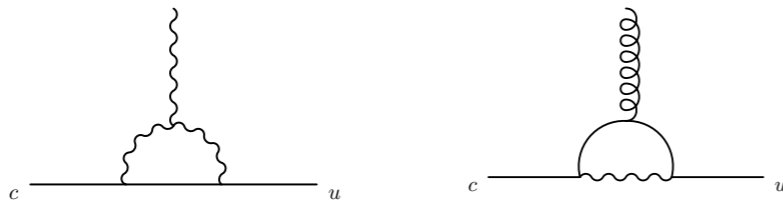
$$D \rightarrow P \ell^+ \ell^-$$

$$\mathcal{H}_{\text{eff}} = \lambda_d \mathcal{H}^d + \lambda_s \mathcal{H}^s + \lambda_b \mathcal{H}^{\text{peng}}$$

$$\mathcal{H}^{\text{peng}} = -\frac{4G_F}{\sqrt{2}} \sum_{i=3,\dots,10} C_i \mathcal{O}_i,$$

QCD penguins  $\mathcal{O}_{3\dots 6}$

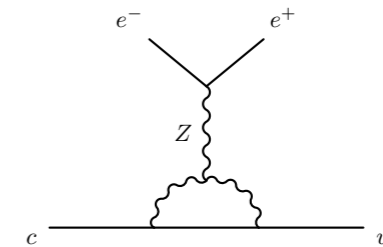
Magnetic penguins  $\mathcal{O}_7, \mathcal{O}_8$



$\lambda_b \sim \lambda^5$  suppressed

$$\mathcal{O}_7 = \frac{em_c}{(4\pi)^2} \bar{u} \sigma_{\mu\nu} P_{RC} F^{\mu\nu}$$

EW penguins  $\mathcal{O}_{9,10}$



$$\mathcal{O}_9 = \frac{e^2}{(4\pi)^2} (\bar{u} \gamma^\mu P_L c) (\bar{\ell} \gamma_\mu \ell),$$

$$\mathcal{O}_{10} = \frac{e^2}{(4\pi)^2} (\bar{u} \gamma^\mu P_L c) (\bar{\ell} \gamma_\mu \gamma_5 \ell)$$

# Effective Hamiltonian for

$$D \rightarrow P \ell^+ \ell^-$$

- MSSM with R-parity

Burdman et al, 2002

$$C_{10}^{\tilde{g}} = -\frac{1}{9} \frac{\alpha_s}{\alpha} (\delta_{22}^u)_{LR} (\delta_{12}^u)_{LR} P_{032}(u) = -\frac{C_9^{\tilde{g}}}{1 - 4 \sin^2 \theta_W}$$

$$C_7^{\tilde{g}} = -\frac{8}{9} \frac{\sqrt{2}}{G_F M_{\tilde{q}}^2} \pi \alpha_s \left\{ (\delta_{12}^u)_{LL} \frac{P_{132}(u)}{4} + (\delta_{12}^u)_{LR} P_{122}(u) \frac{M_{\tilde{g}}}{m_c} \right\}, \quad +\text{chirally flipped operators}$$

- MSSM without R-parity / leptoquarks, e.g. (3,2,7/6)

$$\delta C_9 = -\delta C_{10} = \frac{\sin^2 \theta_W}{2\alpha^2} \left( \frac{M_W}{m_{\tilde{d}_R^k}} \right)^2 \tilde{\lambda}'_{i2k} \tilde{\lambda}'_{i1k}$$

$$C'_S = -C'_P \sim \frac{y_{22} y_{12}^*}{m_S^2}$$

$$D \rightarrow P \ell^+ \ell^-$$

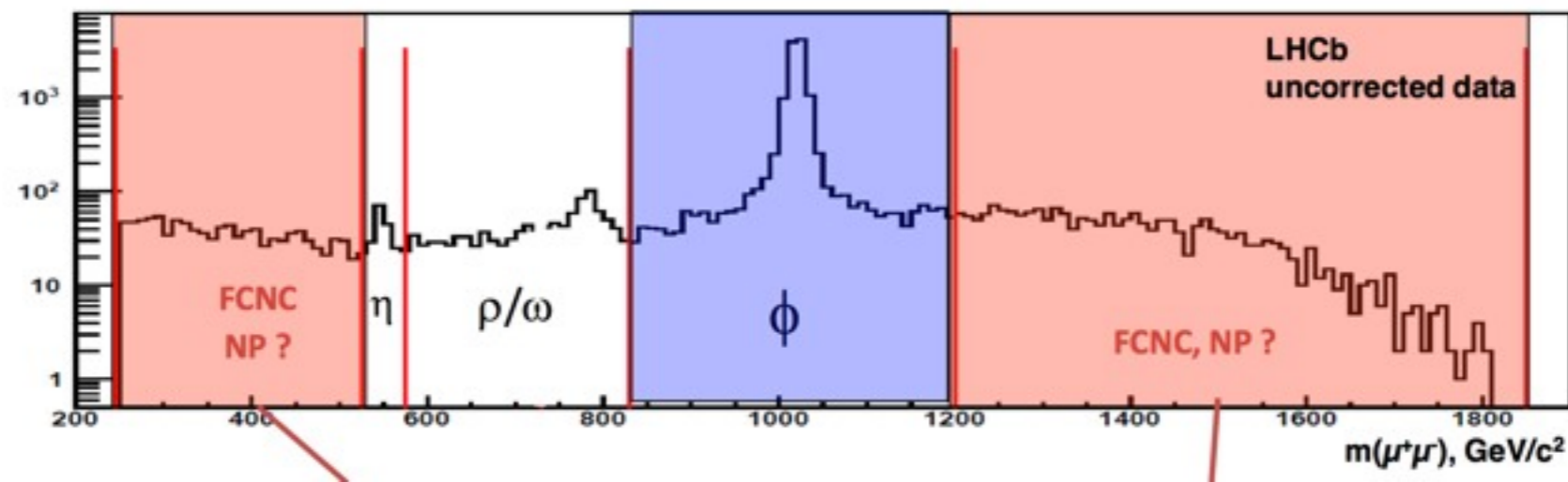
$$\mathcal{A}_{\text{SD}} = -i \frac{4\pi\alpha G_F}{\sqrt{2}} V_{cb}^* V_{ub} \left[ \left( \frac{C_7}{2\pi^2} \frac{m_c}{m_D} + \frac{C_9}{16\pi^2} \right) \bar{u}(p_-) \not{p} v(p_+) + \frac{C_{10}}{16\pi^2} \bar{u}(p_-) \not{p} \gamma_5 v(p_+) \right] f_+(q^2)$$

LD amplitudes include t-channel vector resonances ( $\Phi$ ,  $\omega$ ,  $\rho$ )

$q^2$  spectrum

$D_{(s)}^+ \rightarrow \pi^+ \mu^+ \mu^-$  at LHCb

1 fb<sup>-1</sup>  
2011 data



O. Kochebina, EPS '13

1) For the rate measurements, focus on low or high  $m^2_{\mu\mu}$  ( $= q^2$ )

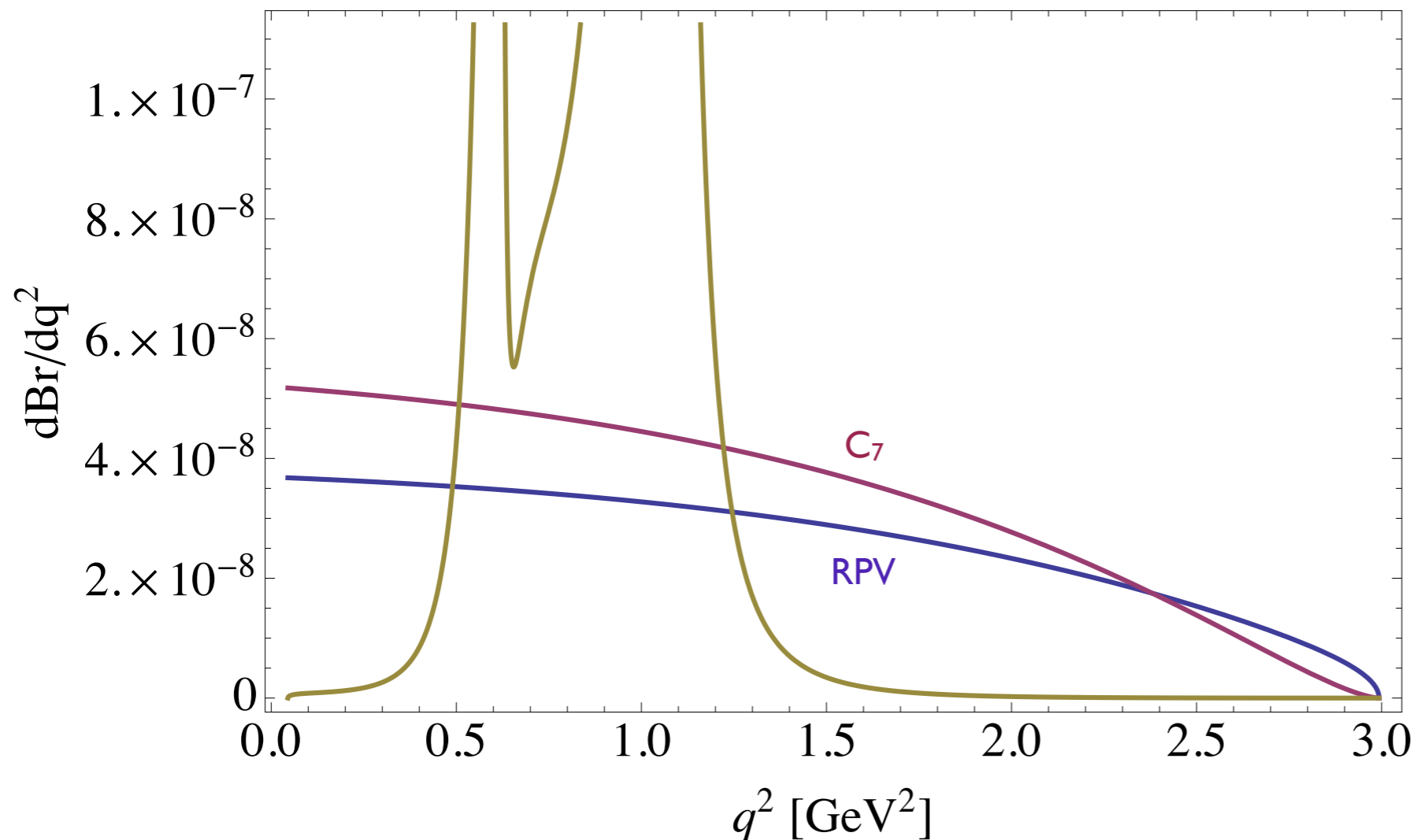
2) No reliable predictions for rate in the resonant region. Short distance effects are overwhelmed.

$$D \rightarrow P \ell^+ \ell^-$$

Decay	Bin	90% [ $\times 10^{-8}$ ]
$D^+ \rightarrow \pi^+ \mu^+ \mu^-$	low- $m(\mu^+ \mu^-)$	2.0
	high- $m(\mu^+ \mu^-)$	2.6
	Total	7.3

LHCb, Physics Letters  
B 724 (2013) 203

Constraints from the  
high- $q^2$  region:



$$|\lambda_b \delta C_{9,10}^{\text{RPV}}| < 2.5$$

One order improvement in  
few years.

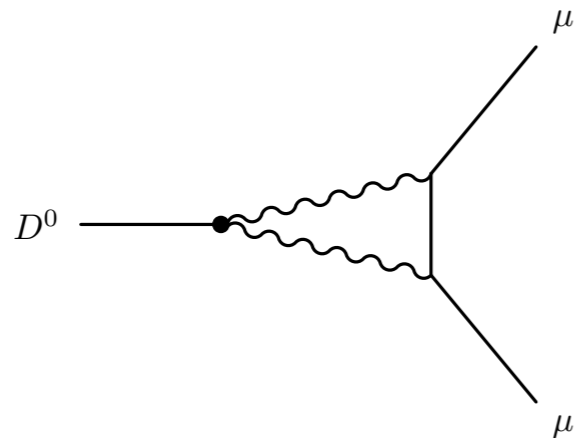
$$|\lambda_b \delta C_7| < 0.8$$

Close to what is required  
for direct CP in 2 body  
decays



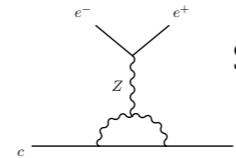
$$D^0 \rightarrow \ell^+ \ell^-$$

Long distance effects in  $D^0 \rightarrow \gamma\gamma$  dominate



$$\text{Br}(D^0 \rightarrow \mu^+ \mu^-) \simeq 2.7 \cdot 10^{-5} \times \text{Br}(D^0 \rightarrow \gamma\gamma)$$

Burdman et al, 2002



SM short-distance contribution is negligible, GIM!

Combined with experimentally bounded  $\gamma\gamma$  branching fraction,  $< 2.2 \times 10^{-6}$  at 90% CL :

BaBar, 2012

$$\text{Br}(D^0 \rightarrow \mu^+ \mu^-)^{\text{SM}} \lesssim 10^{-10}$$

Almost null test of the SM

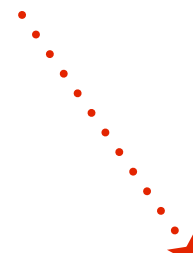
$$\text{Br}(D^0 \rightarrow \mu^+ \mu^-)^{\text{LHCb}} < 6.2 \times 10^{-9}$$

LHCb, Physics Letters  
B 725 (2013) 15

$$D^0 \rightarrow \ell^+ \ell^-$$

Neglect SM contribution, insert a New physics (NP) candidate:

$$\text{Br}_{\text{th}}^{\text{NP}} (D^0 \rightarrow \mu^+ \mu^-) = \tau_D f_D^2 m_D^3 \frac{G_F^2 \alpha^2}{64\pi^3} |V_{ub} V_{cb}^*|^2 \beta_\ell(m_D^2) \left[ \frac{m_D^2}{m_c^2} |C_S - C'_S|^2 \left(1 - \frac{4m_\ell^2}{m_D^2}\right) + \left| \frac{m_D}{m_c} (C_P - C'_P) + 2 \frac{m_\ell}{m_D} (C_{10} - C'_{10}) \right|^2 \right]$$



$$\text{Br}_{\text{th}}^{\text{NP}} (c_i, m_i, \dots) < \text{Br}^{\text{exp}}$$

Three combinations enter

$$C_{10} - C'_{10}, \quad C_S - C'_S, \quad C_P - C'_P$$

Helicity suppression of axial lepton current operator, nevertheless better bound than from semileptonic decay

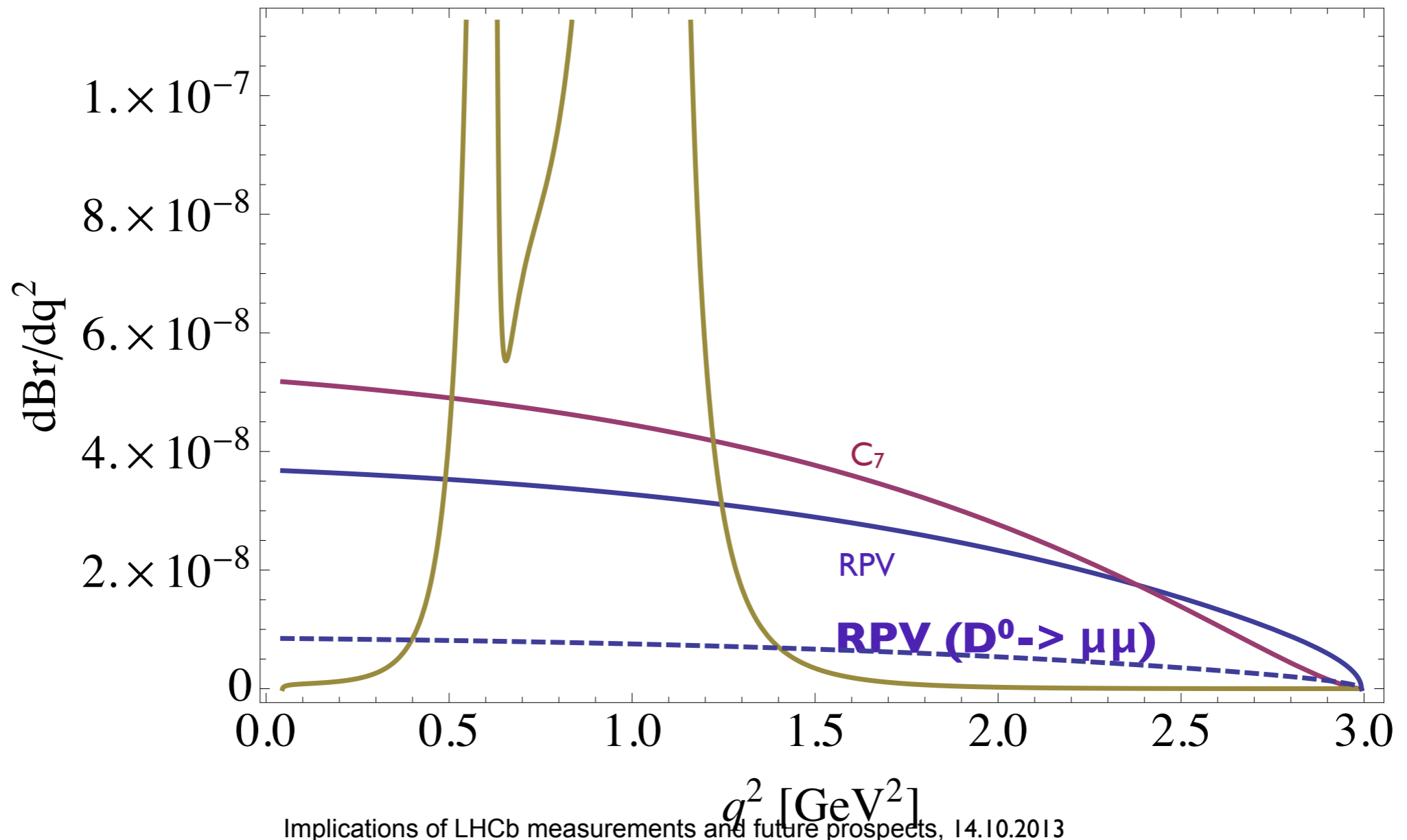
$$|\lambda_b \delta C_9^{\text{RPV}}|, |\lambda_b \delta C_{10}^{\text{RPV}}| < 1.2$$

$$D^0 \rightarrow \ell^+ \ell^-$$

$$|\lambda_b \delta C_9^{\text{RPV}}|, |\lambda_b \delta C_{10}^{\text{RPV}}| < 1.2$$

Stronger than from semileptonic decay!

Repercussions for  $D \rightarrow P \ell^+ \ell^-$

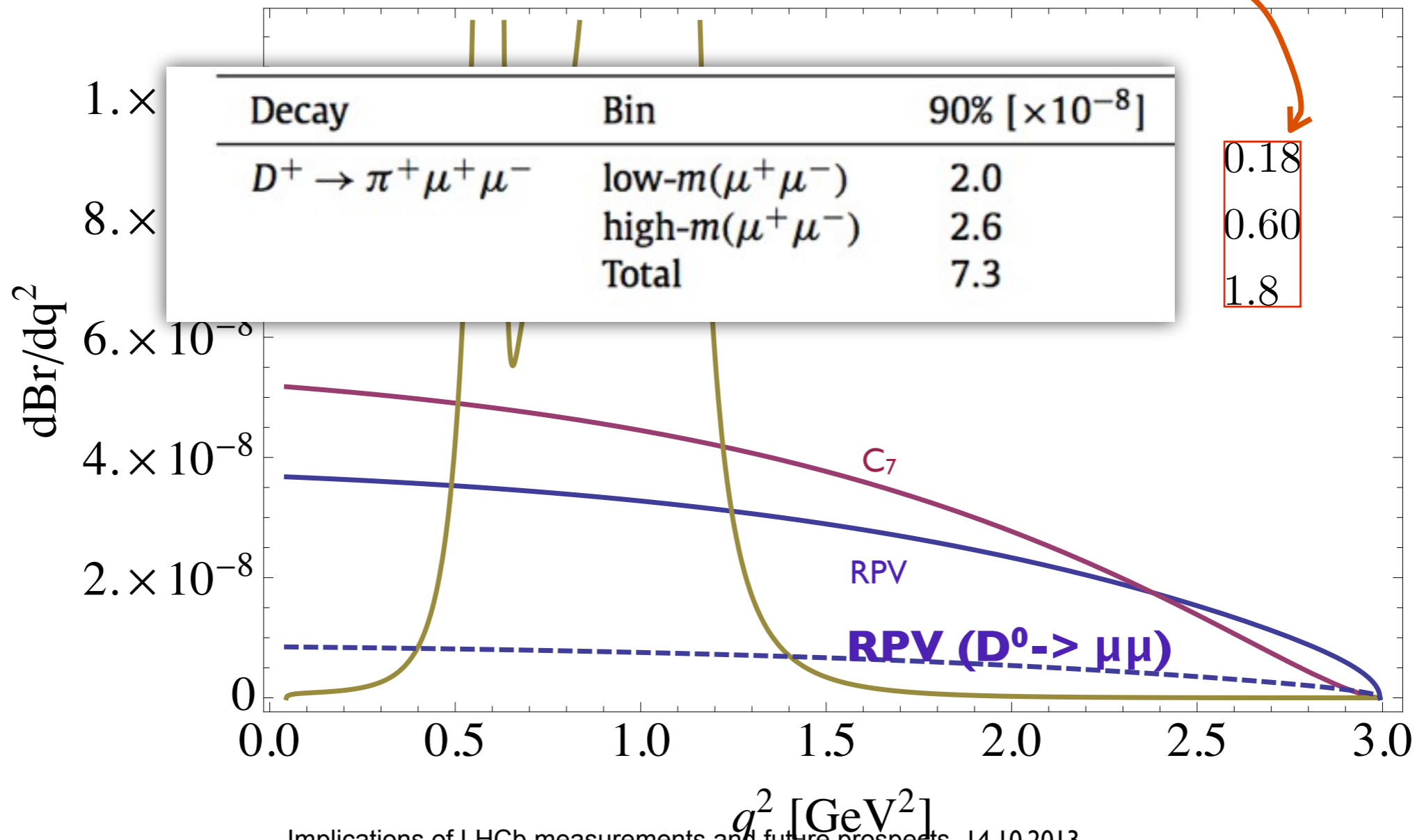


$$D^0 \rightarrow \ell^+ \ell^-$$

$$|\lambda_b \delta C_9^{\text{RPV}}|, |\lambda_b \delta C_{10}^{\text{RPV}}| < 1.2$$

Stronger than from semileptonic decay!

Repercussions for  $D \rightarrow P \ell^+ \ell^-$

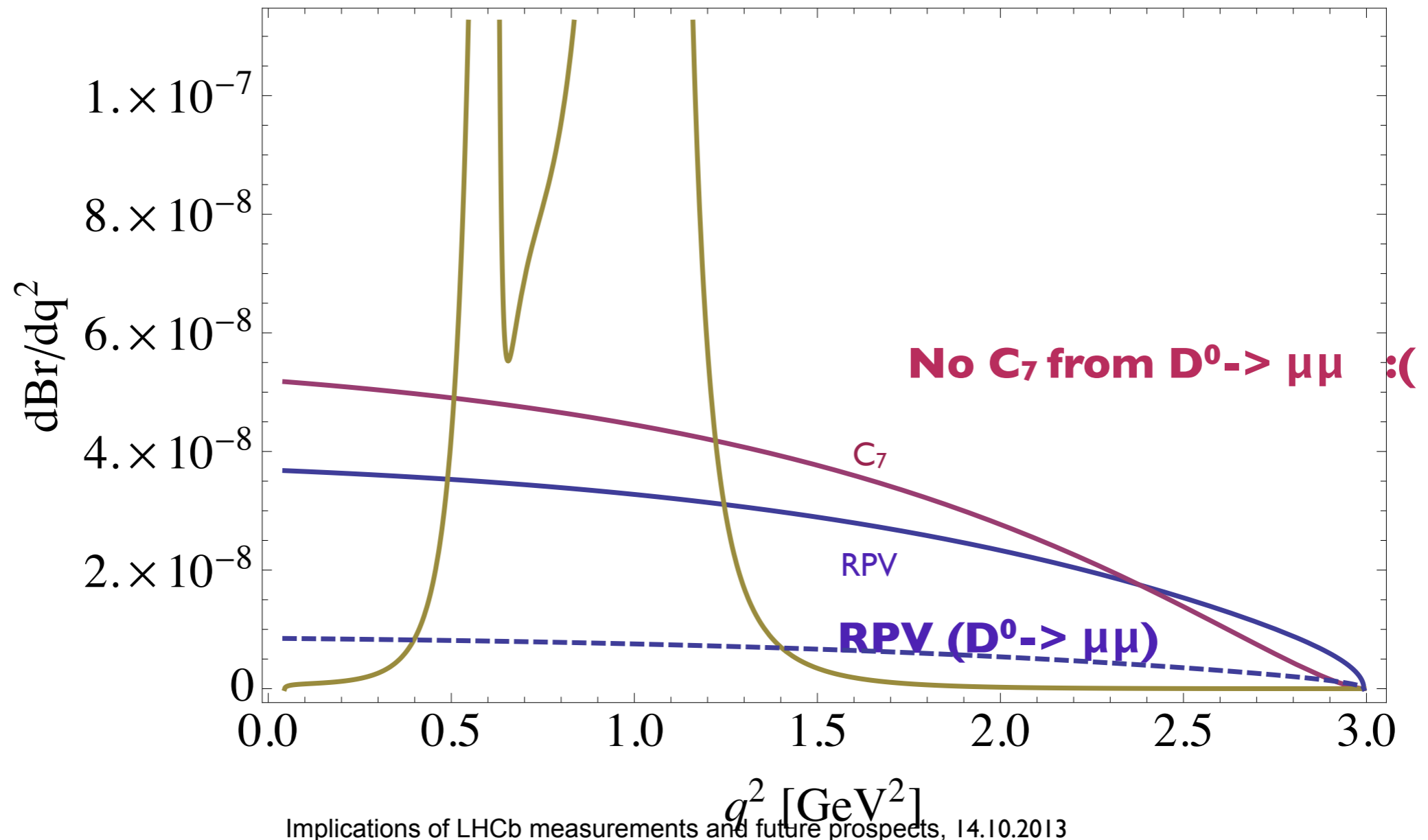


$$D^0 \rightarrow \ell^+ \ell^-$$

$$|\lambda_b \delta C_9^{\text{RPV}}|, |\lambda_b \delta C_{10}^{\text{RPV}}| < 1.2$$

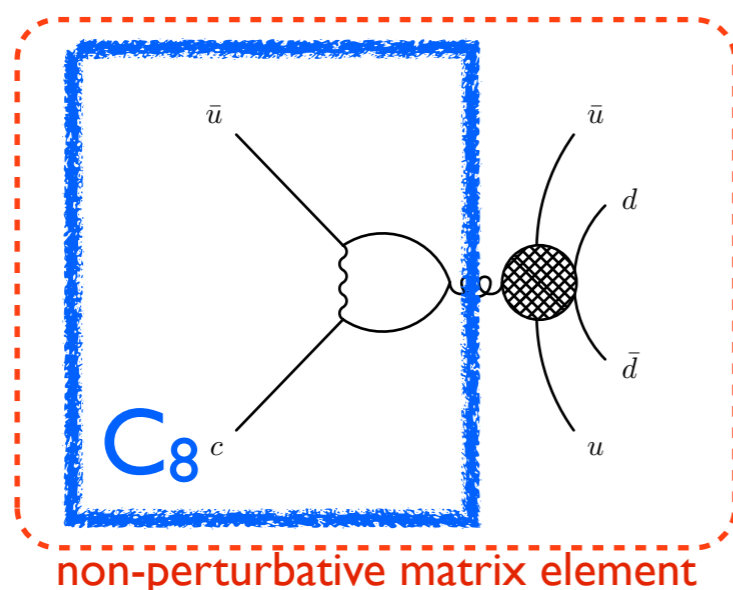
Stronger than from semileptonic decay!

Going back to  $D \rightarrow P \ell^+ \ell^-$



# Motivation for NP phase in $C_7$

- Natural explanation of CPV observed in  $D \rightarrow \pi\pi$  and  $D \rightarrow KK$  via non-standard phase in  $C_8$



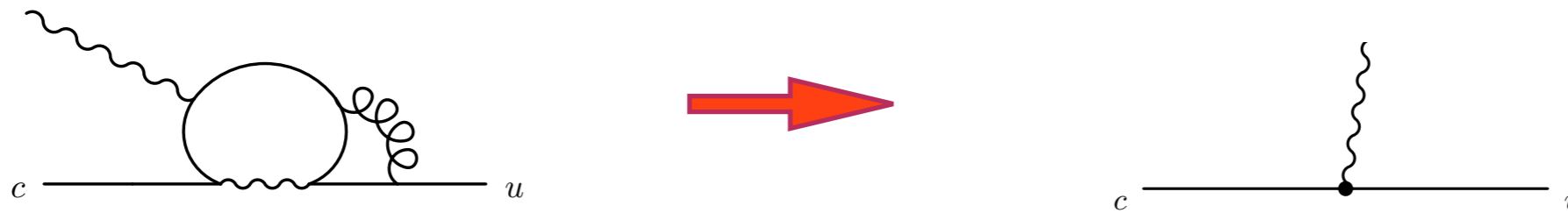
$$\begin{aligned} \Delta A_{\text{CP}} &\equiv A_{\text{CP}}(D^0 \rightarrow K^+ K^-) - A_{\text{CP}}(D^0 \rightarrow \pi^+ \pi^-) \\ &= \begin{cases} (-0.34 \pm 0.15 \pm 0.10) \% & ; \text{ LHCb '13} \\ (-0.62 \pm 0.21 \pm 0.10) \% & ; \text{ CDF '12} \end{cases} \end{aligned}$$

- Gluonic penguin ( $C_8$ ) usually present together with photonic penguin ( $C_7$ ) in concrete NP models (e.g. gluino loop in SUSY)
- Even if  $C_7 = 0$  at high scale, QCD renormalization mixes  $C_8$  into  $C_7$

Isidori et al, '11  
Giudice et al, '12

# Motivation for NP phase in $C_7$

QCD renormalization



$$C_7(m_c) = \tilde{\eta} [\eta C_7(M) + 8(\eta - 1)C_8(M)]$$

$$\eta = \left[ \frac{\alpha_s(M)}{\alpha_s(m_t)} \right]^{2/21} \left[ \frac{\alpha_s(m_t)}{\alpha_s(m_b)} \right]^{2/23} \left[ \frac{\alpha_s(m_b)}{\alpha_s(m_c)} \right]^{2/25}$$

$$\tilde{\eta} = \left[ \frac{\alpha_s(M)}{\alpha_s(m_t)} \right]^{14/21} \left[ \frac{\alpha_s(m_t)}{\alpha_s(m_b)} \right]^{14/23} \left[ \frac{\alpha_s(m_b)}{\alpha_s(m_c)} \right]^{14/25}$$

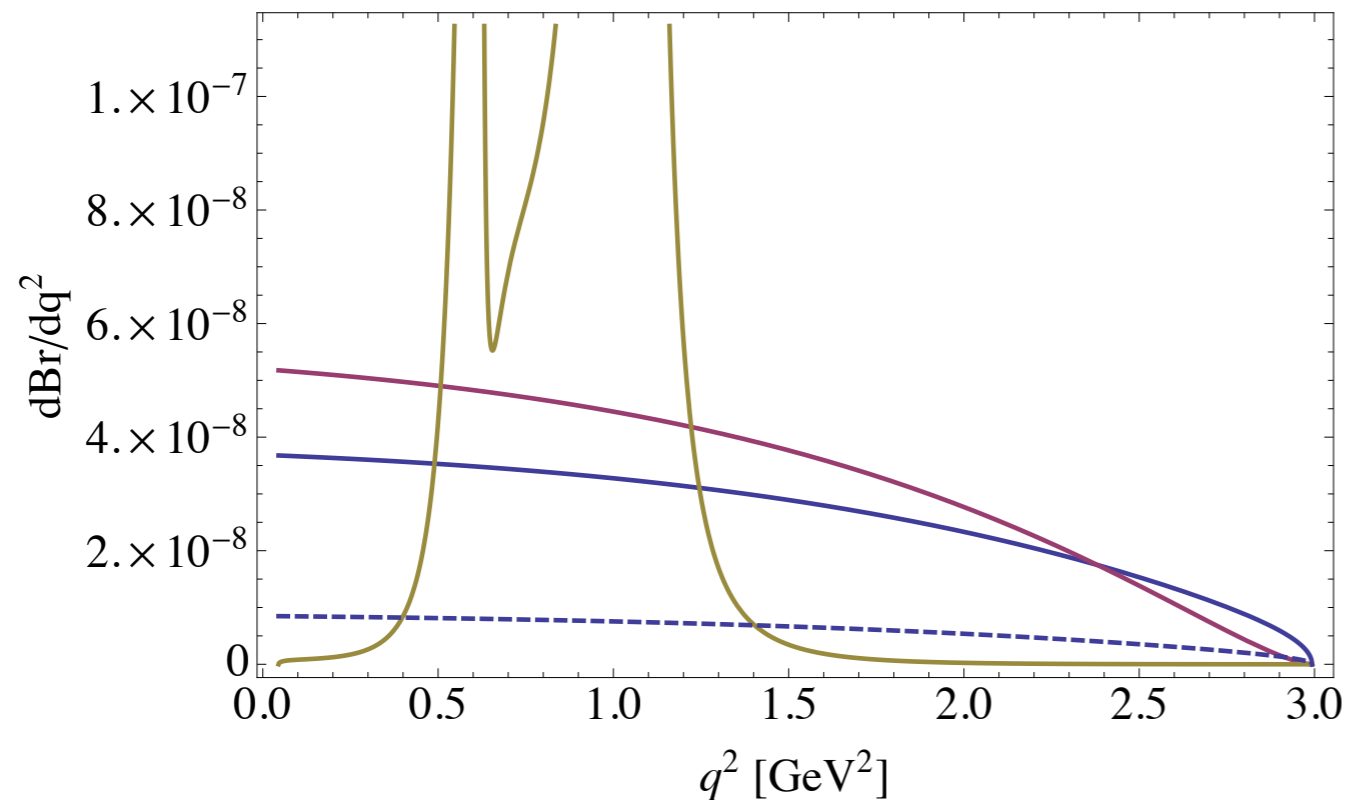
If  $C_7(1 \text{ TeV}) \ll C_8(1 \text{ TeV})$

$$\text{Im}[\lambda_b C_7(m_c)] \approx \text{Im}[\lambda_b C_8(m_c)] \approx (0.2 - 0.8) \times 10^{-2}$$

$\Delta A_{CP}$

**Independently test CP phase in  $C_7$  sensitive processes!**

# Test: direct CP on $\Phi$ resonance



$$|\mathcal{A}_{LD} + \mathcal{A}_{SD}|^2 \approx |\mathcal{A}_{LD}|^2 + 2\Re[\mathcal{A}_{LD}\mathcal{A}_{SD}^*]$$

$$a_{CP} \sim \text{Im}[\mathcal{A}_{SD}]/|\mathcal{A}_{LD}|$$

- Linear effect (interference)
- If the LD amplitude is CP even, measuring CPV is a null-test



# Direct CP

$$\mathcal{A}(D^+ \rightarrow \pi^+ \ell^+ \ell^-) = \mathcal{A}_{\text{LD}}^\phi + \mathcal{A}_{\text{SD}}^{\text{CPV}},$$

$$\bar{\mathcal{A}}(D^- \rightarrow \pi^- \ell^+ \ell^-) = \mathcal{A}_{\text{LD}}^\phi + \bar{\mathcal{A}}_{\text{SD}}^{\text{CPV}}$$

$$a_{\text{CP}}(q^2) \equiv \frac{|\mathcal{A}|^2 - |\bar{\mathcal{A}}|^2}{|\mathcal{A}|^2 + |\bar{\mathcal{A}}|^2}$$

$$= \frac{-3}{2\pi^2} \frac{m_c}{m_D + m_\pi} \text{Im} \left[ \frac{\lambda_b}{\lambda_s} C_7 \right] \frac{f_T(q^2)}{a_\phi} \left[ \cos \delta_\phi - \frac{q^2 - m_\phi^2}{m_\phi \Gamma_\phi} \sin \delta_\phi \right]$$

Fajfer, NK, '12

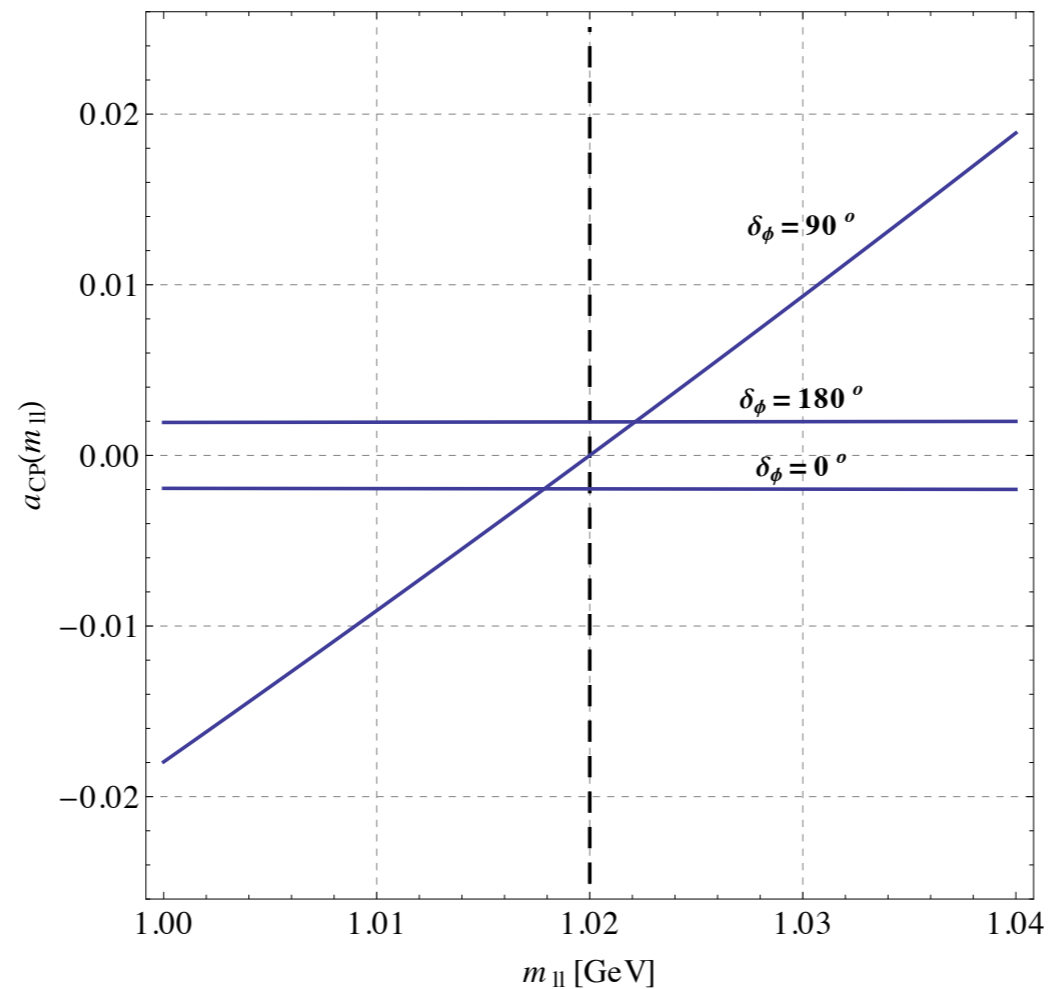
resonance and form  
factor dependence

$$\text{Im} \left[ \frac{\lambda_b}{\lambda_s} C_7 \right] \approx \frac{\text{Im}[\lambda_b C_7]}{\text{Re}[\lambda_s]}$$

- Behaviour around the peak crucially depends on the value of  $\delta_\phi$

# Direct CP

$$a_{CP}(q^2) = \frac{-3}{2\pi^2} \frac{m_c}{m_D + m_\pi} \text{Im} \left[ \frac{\lambda_b}{\lambda_s} C_7 \right] \frac{f_T(q^2)}{a_\phi} \left[ \cos \delta_\phi - \frac{q^2 - m_\phi^2}{m_\phi \Gamma_\phi} \sin \delta_\phi \right]$$

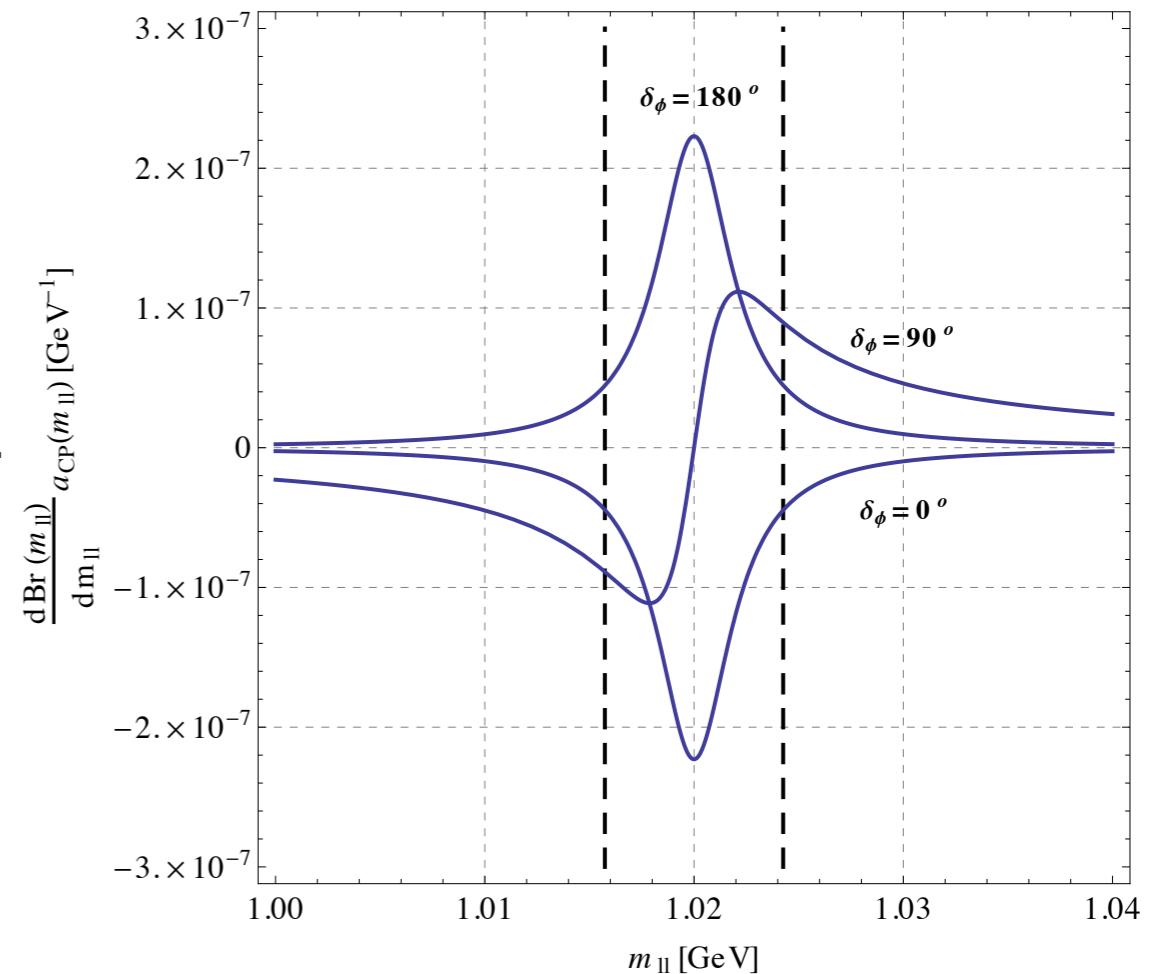
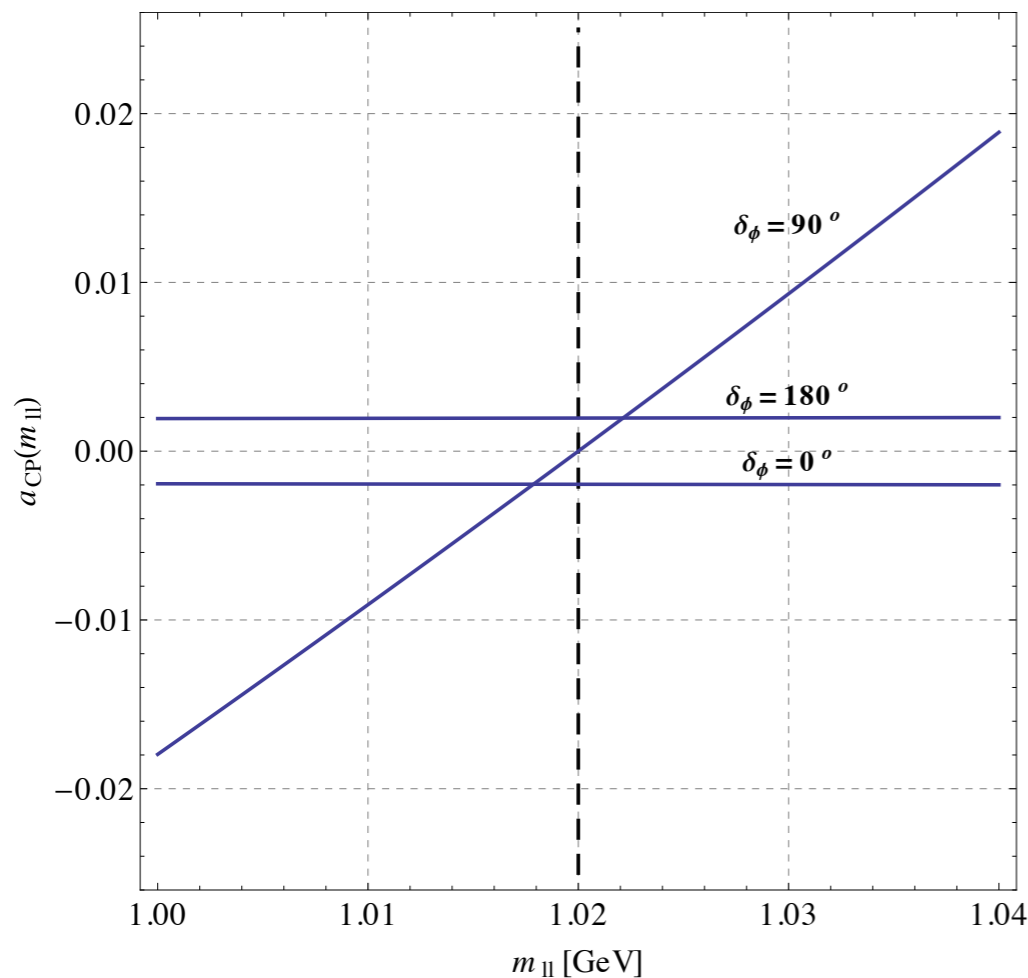


few %  
for  $\text{Im}[\lambda_b C_7] = 0.8 \times 10^{-2}$   
(needed for  $\Delta A_{CP}$ )

- $a_{CP}(q^2)$  antisymmetric around  $\Phi$  for  $\delta_\phi = \pm\pi/2$
- “ symmetric around  $\Phi$  for  $\delta_\phi = 0, \pi$

# Direct CP, sensitivity

- However, event decay rate is tiny



- Not very promising, constraint from decay rate at low/high  $q^2$  will be more revealing

$$\text{Im}[\lambda_b C_7] = 0.8 \times 10^{-2}$$

(needed for  $\Delta A_{CP}$ )

**Vs**

$$|\lambda_b \delta C_7| < 0.8$$

From semileptonic

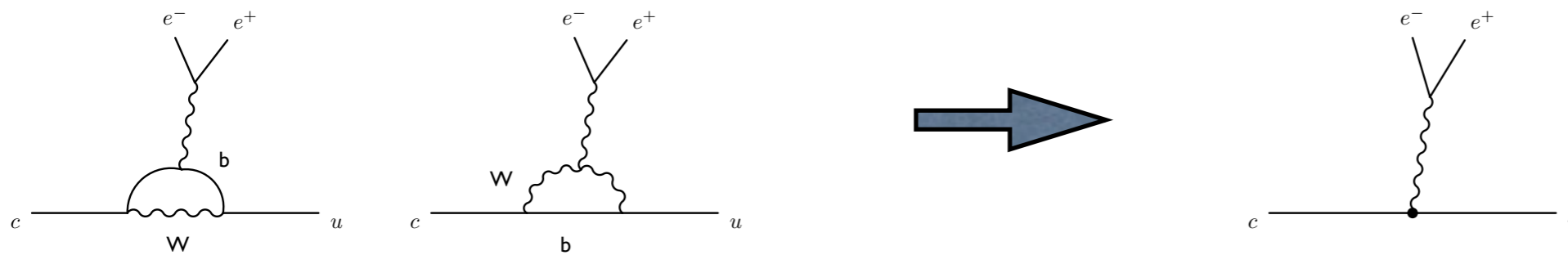
# Summary and conclusion

- Semileptonic  $D \rightarrow P\ell^+\ell^-$  offers windows into short-distance physics
- Leptonic decay  $D^0 \rightarrow \ell^+\ell^-$  is Standard Model free (not for long)
  - ▶ Future: important interplay with  $D^0 \rightarrow \gamma\gamma$
- Example I, we have constrained RPV trilinear terms
  - ▶ Huge improvement in last few years, thanks to new experimental bounds
  - ▶ Leptonic decay slightly more powerful probe
- Example II,  $C_7$  with CPV phase, required by  $\Delta A_{CP}$ 
  - ▶ Independent test: direct CP on the  $\Phi$  resonance. Tiny.
  - ▶ Affects semileptonic decay, not leptonic. Constraint is 2 orders of magnitude short of testing  $\Delta A_{CP}$

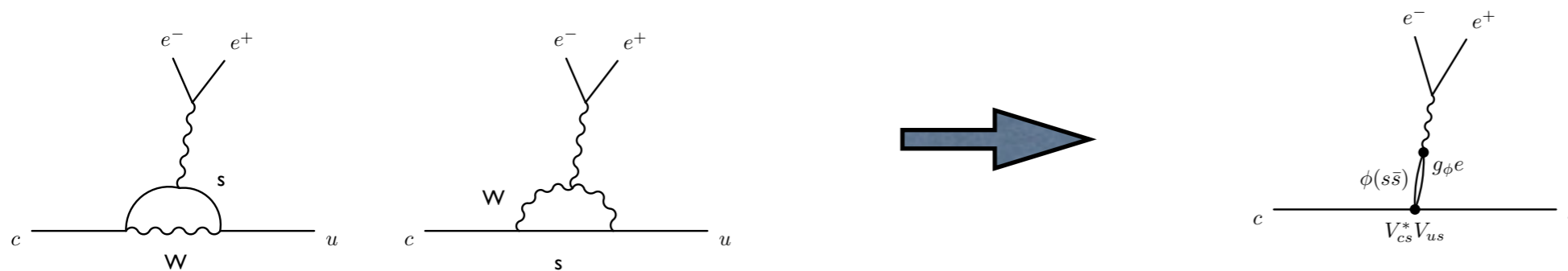
# Backup

# Definition (of short and long distance amplitudes)

SD amplitude := of local Hamiltonian (and nonlocal propagation of colorless particles)



LD contribution\* := not SD

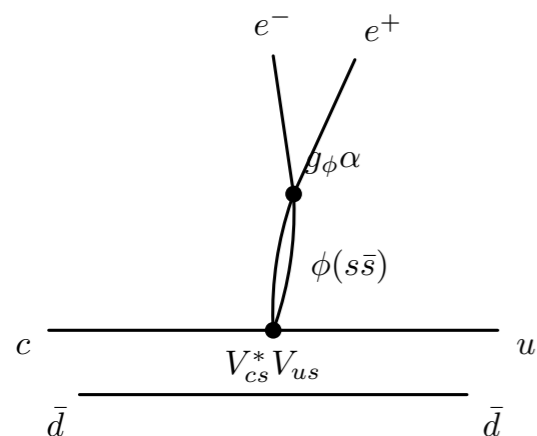


\*limited to resonant in this talk

# Pole model for $\Phi$ resonance

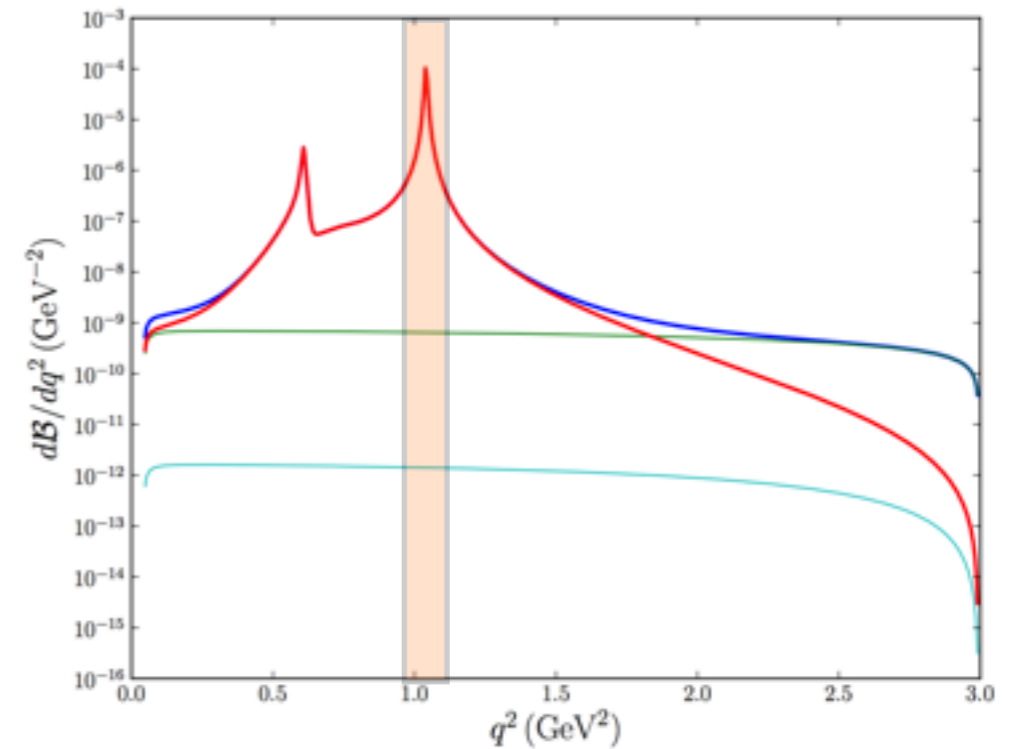
$$\mathcal{H}_{\text{eff}} = \lambda_d \mathcal{H}^d + \lambda_s \mathcal{H}^s + \lambda_b \mathcal{H}^{\text{peng}}$$

$$\mathcal{A}_{\text{LD}}^\Phi = \langle \phi \pi^+ | - \frac{4G_F}{\sqrt{2}} \lambda_s (\bar{s}_L \gamma^\mu c_L) (\bar{u}_L \gamma_\mu s_L) | D^+ \rangle$$



×  
Breit-Wigner propagator

×  
 $\mathcal{A}(\Phi \rightarrow \mu\mu)$



$\Phi$

$$\mathcal{A}_{\text{LD}}^\Phi [D \rightarrow \pi \phi \rightarrow \pi \ell^- \ell^+] = \frac{iG_F}{\sqrt{2}} \lambda_s \frac{8\pi\alpha}{3} a_\phi e^{i\delta_\phi} \frac{m_\phi \Gamma_\phi}{q^2 - m_\phi^2 + im_\phi \Gamma_\phi} \bar{u}(k_-) \not{p} v(k_+)$$

# Pole model for $\Phi$ resonance

$$\mathcal{A}_{\text{LD}}^\phi [D \rightarrow \pi\phi \rightarrow \pi\ell^-\ell^+] = \frac{iG_F}{\sqrt{2}} \lambda_s \frac{8\pi\alpha}{3} a_\phi e^{i\delta_\phi} \frac{m_\phi \Gamma_\phi}{q^2 - m_\phi^2 + im_\phi \Gamma_\phi} \bar{u}(k_-) \not{p} v(k_+)$$

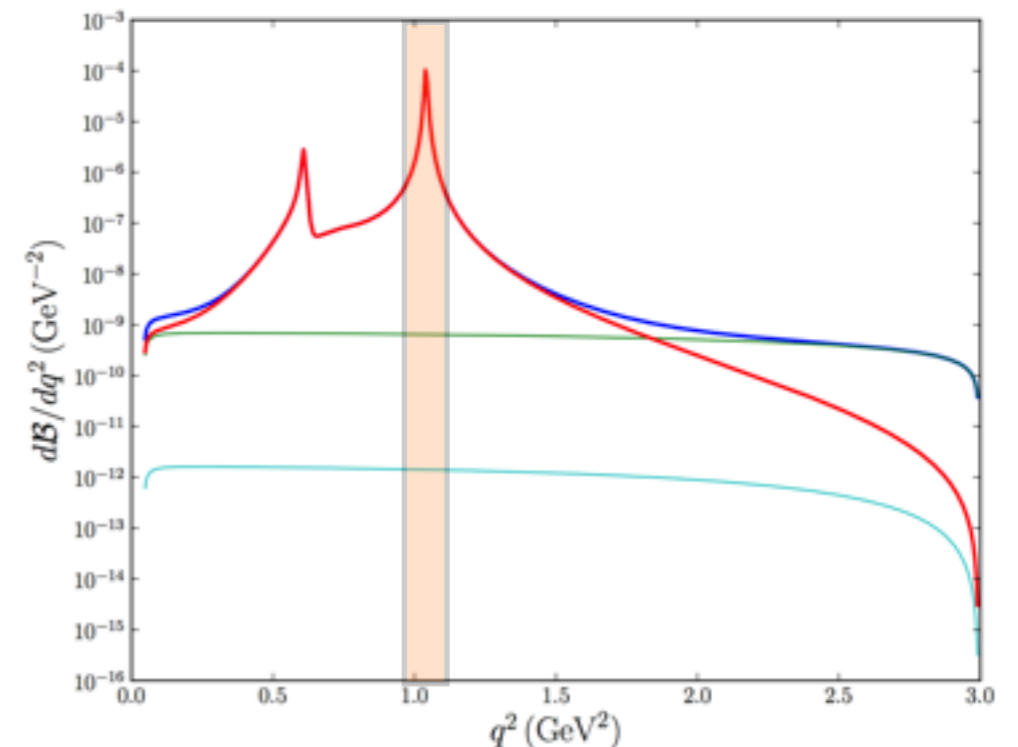
$a_\phi, \delta_\phi$  real parameters

$$\begin{aligned} \text{Br}(D^+ \rightarrow \phi\pi^+) &= (2.65 \pm 0.09) \times 10^{-3}, \\ \text{Br}(\phi \rightarrow \mu^+\mu^-) &= (0.287 \pm 0.019) \times 10^{-3} \end{aligned}$$

$$a_\phi = 1.23 \pm 0.05$$

$\delta_\phi$  = strong phase, smoothly varying

**Caveat:** We neglect CPV  $C_8$  contributions to the LD amplitude. Perturbatively, they are loop suppressed w.r.t. to the  $C_7$  contribution.



$\Phi$



# Short distance amplitude

- $C_7, C_9, C_{10}$  ( $\lambda^4$  suppressed w.r.t. LD in the SM)
- $C_7$  carries non-standard CP phase,  $C_9, C_{10}$  are SM-like

$$\mathcal{A}_{\text{SD}}^{\text{CPV}} = -\frac{i\sqrt{2}G_F\alpha}{\pi} \lambda_b C_7(m_c) \frac{m_c}{m_D + m_\pi} f_T(q^2) \bar{u}(k_-) \not{p} v(k_+)$$

tensor form factor

$$\tilde{f}_T(q^2) \equiv \frac{m_{D^*}}{m_D + m_\pi} \frac{f_{D^*}^V}{f_{D^*}^T(\mu)} f_T(q^2; \mu) \quad \langle \pi(p') | \bar{u} \sigma_{\mu\nu} c | D(p) \rangle = -i (p_\mu p'_\nu - p_\nu p'_\mu) \frac{2f_T(q^2)}{m_D + m_\pi}$$

$$\tilde{f}_T(q^2) = \frac{\tilde{f}_T(0)}{\left(1 - \frac{q^2}{m_{D^*}^2}\right) \left(1 - a_T \frac{q^2}{m_{D^*}^2}\right)}$$

$$\tilde{f}_T(0) = 0.56(5), \quad a_T = 0.18(16)$$

Quenched lattice calculation

Abada et al 2001, Becirevic 2012

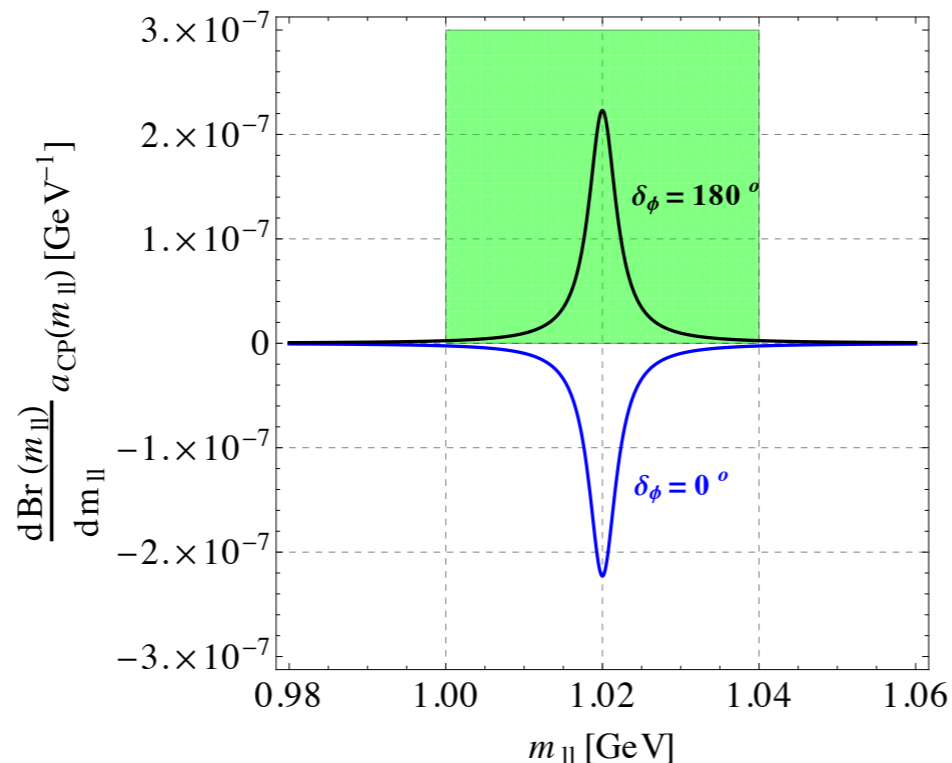
# Direct CP observables

- Partial width asymmetry

$$A_{CP}(m_1, m_2) = \frac{\Gamma(m_1 < m_{\ell\ell} < m_2) - \bar{\Gamma}(m_1 < m_{\ell\ell} < m_2)}{\Gamma(m_1 < m_{\ell\ell} < m_2) + \bar{\Gamma}(m_1 < m_{\ell\ell} < m_2)}$$

$$= \frac{\int_{m_1^2}^{m_2^2} dq^2 R(q^2) a_{CP}(\sqrt{q^2})}{\int_{q_{\min}^2}^{q_{\max}^2} dq^2 R(q^2)}$$

- Defined on a symmetric bin around  $m_\phi$  ( $\pm 20$  MeV)

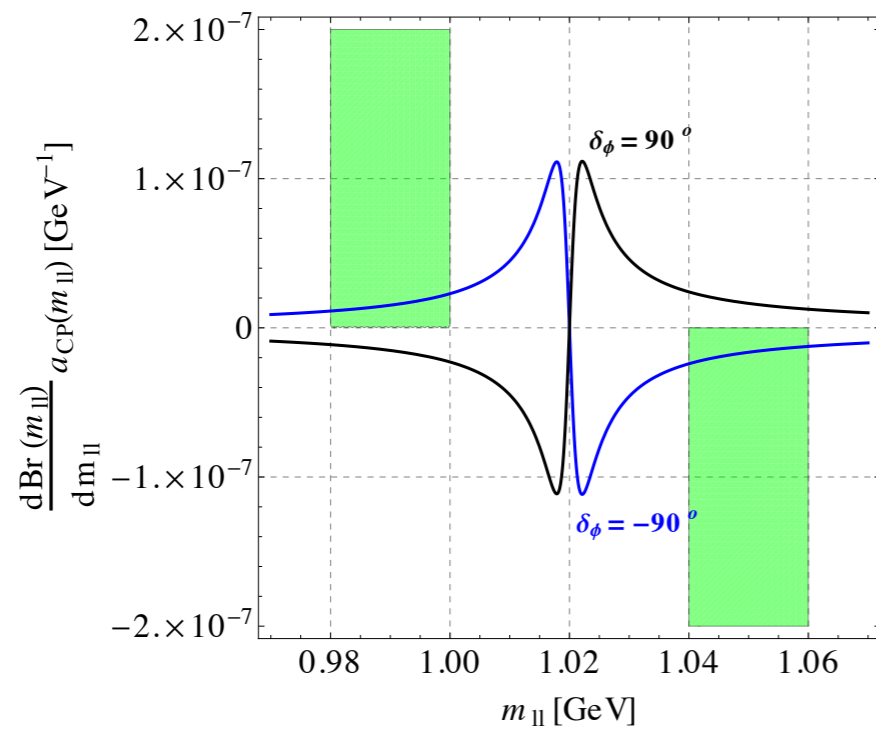


$$C_{CP}^\phi \equiv A_{CP}(m_\phi - 20 \text{ MeV}, m_\phi + 20 \text{ MeV})$$

Sensitive to scenarios with  $\delta_\phi \approx 0, \pi$

# Direct CP observables

How to detect cases with  $\delta_\phi \approx \pi/2, -\pi/2$  ?

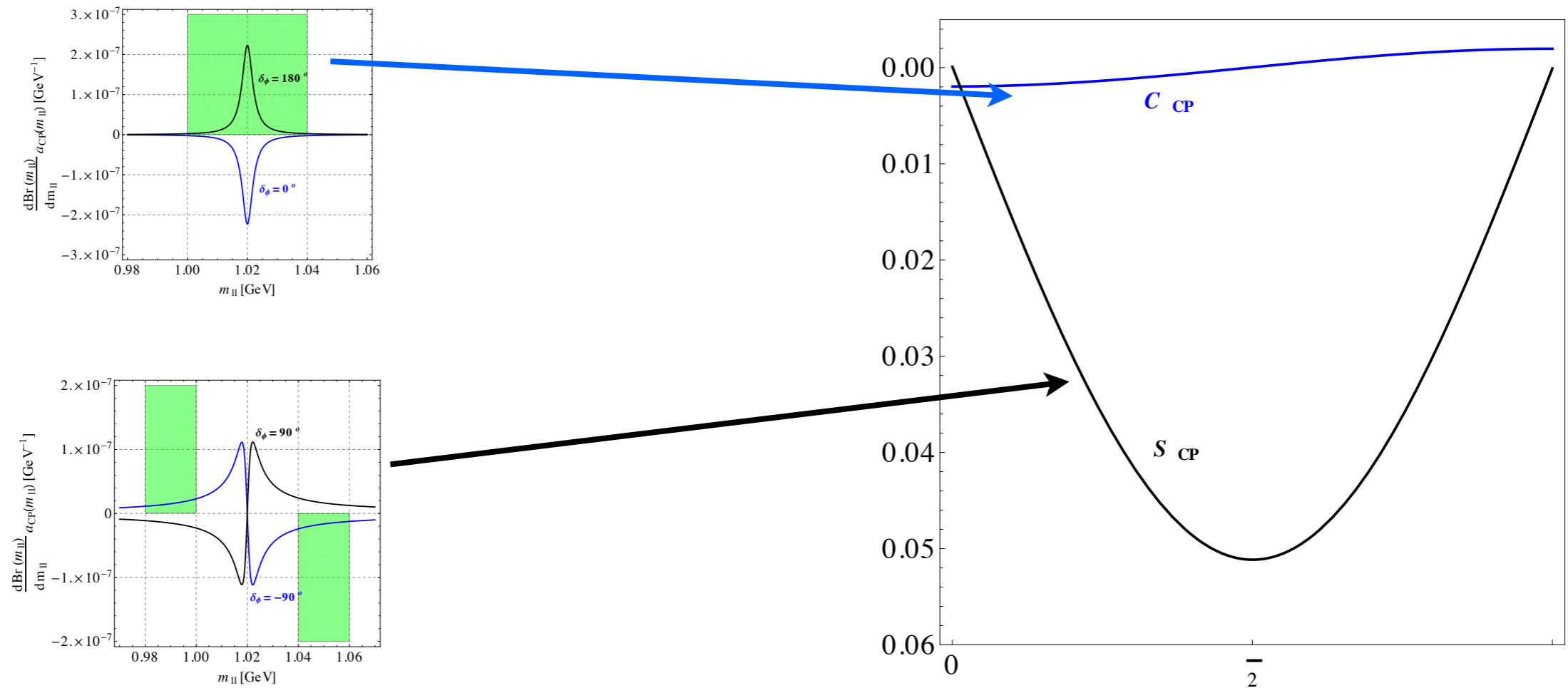


Difference of two asymmetries, above and below the peak

$$S_{CP}^\phi \equiv A_{CP}(m_\phi - 40 \text{ MeV}, m_\phi - 20 \text{ MeV}) - A_{CP}(m_\phi + 20 \text{ MeV}, m_\phi + 40 \text{ MeV})$$

# Direct CP observables

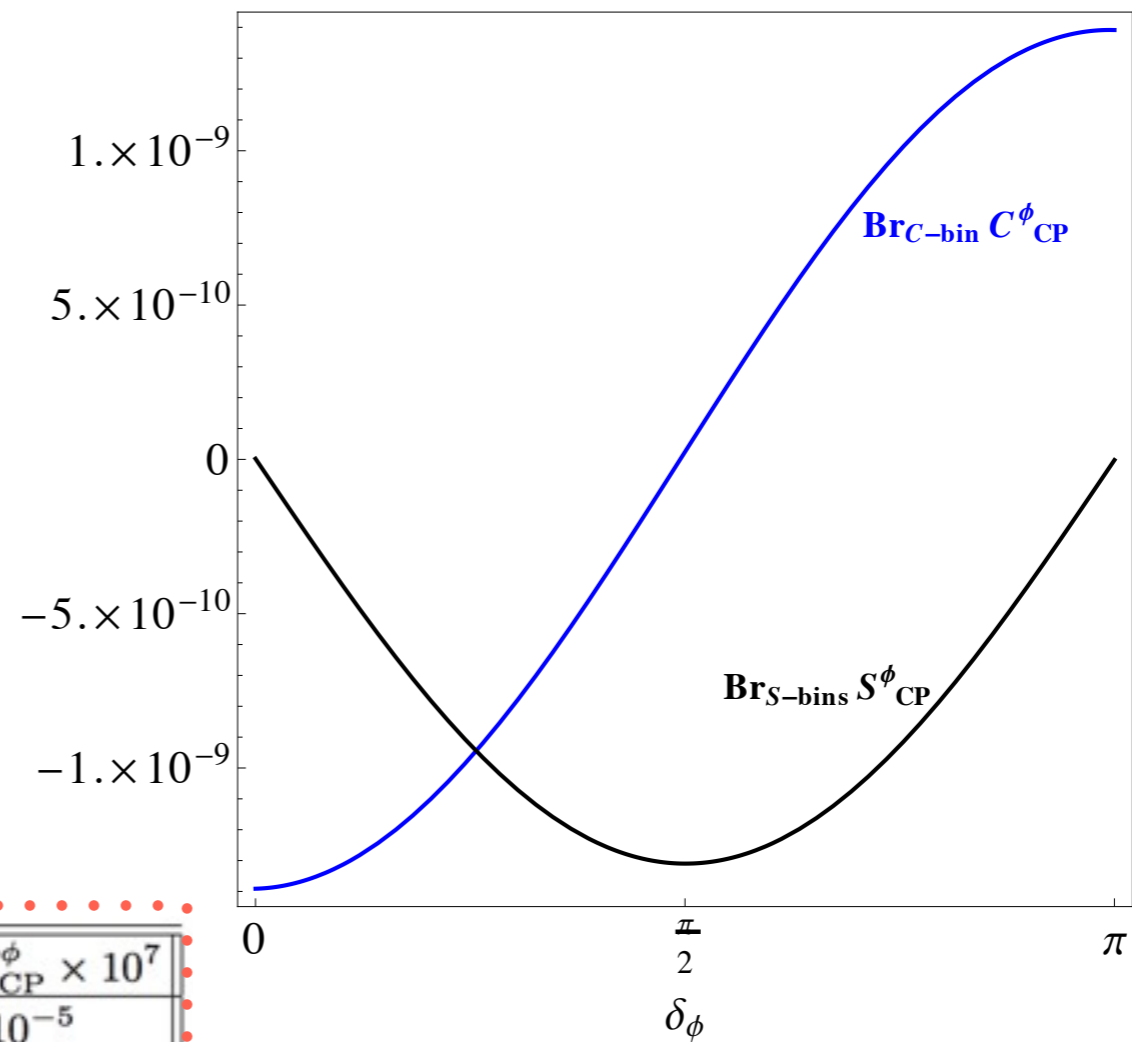
Scan over the strong phase



# Sensitivity

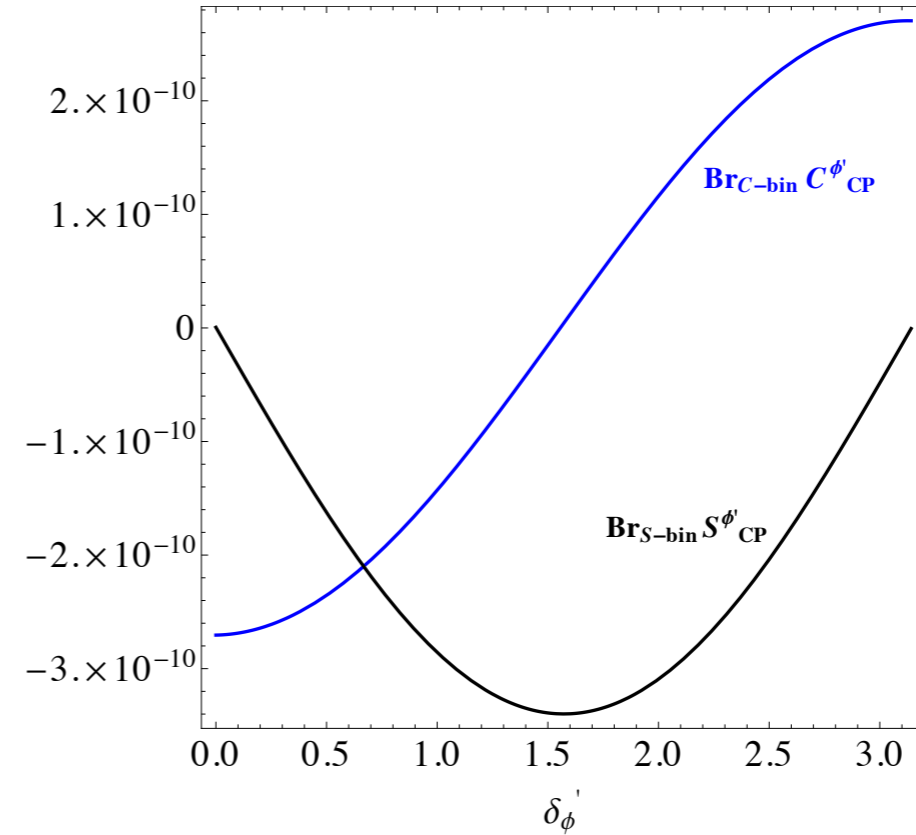
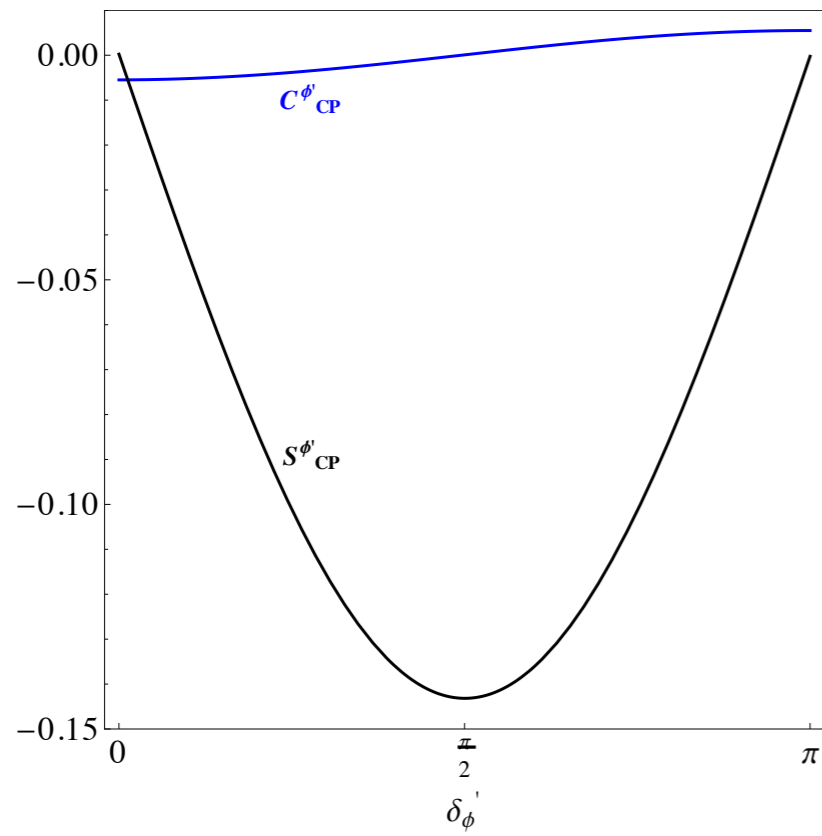
:= Branching ratio  $\times$  CP asymmetry

Even coverage over  $\delta_\phi$ .



$\delta_\phi$	$C_{\text{CP}}^\phi \times 10^2$	$S_{\text{CP}}^\phi \times 10^2$	$\text{Br}(\text{C-bin}) C_{\text{CP}}^\phi \times 10^7$	$\text{Br}(\text{S-bin}) S_{\text{CP}}^\phi \times 10^7$
$0, \pi$	$\mp 0.20$	$\pm 0.008$	$\mp 0.014$	$\pm 2 \times 10^{-5}$
$\pm \pi/2$	$\pm 0.003$	$\mp 5.1$	$\pm 2.4 \times 10^{-4}$	$\mp 0.013$

# Sensitivity ( $D_s \rightarrow K^+ \mu^+ \mu^-$ )



$\delta_{\phi'}$	$C_{CP}^{\phi'} \times 10^2$	$S_{CP}^{\phi'} \times 10^2$	$\text{Br}(C\text{-bin}) C_{CP}^{\phi'} \times 10^7$	$\text{Br}(S\text{-bin}) S_{CP}^{\phi'} \times 10^7$
$0, \pi$	$\mp 0.55$	$\pm 0.024$	$\mp 0.0027$	$\pm 1 \times 10^{-5}$
$\pm \pi/2$	$\pm 0.008$	$\mp 14$	$\pm 4 \times 10^{-5}$	$\mp 0.007$