

TLEP: Part of a Vision for the Future

Exploration of the 10 TeV scale

Direct (VHE-LHC) + Indirect (TLEP)

Need major effort to develop the physics case

Work together

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The Twin Pillars of TLEP Physics

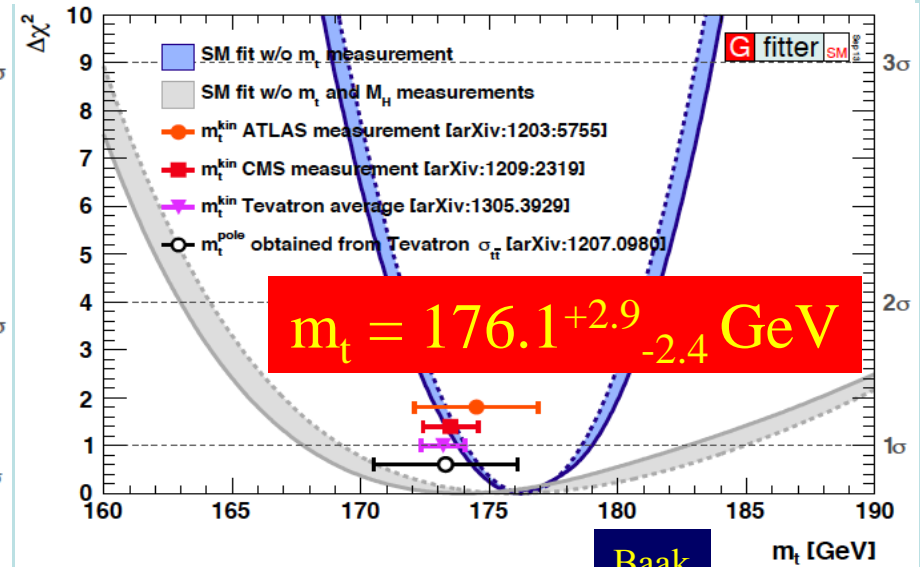
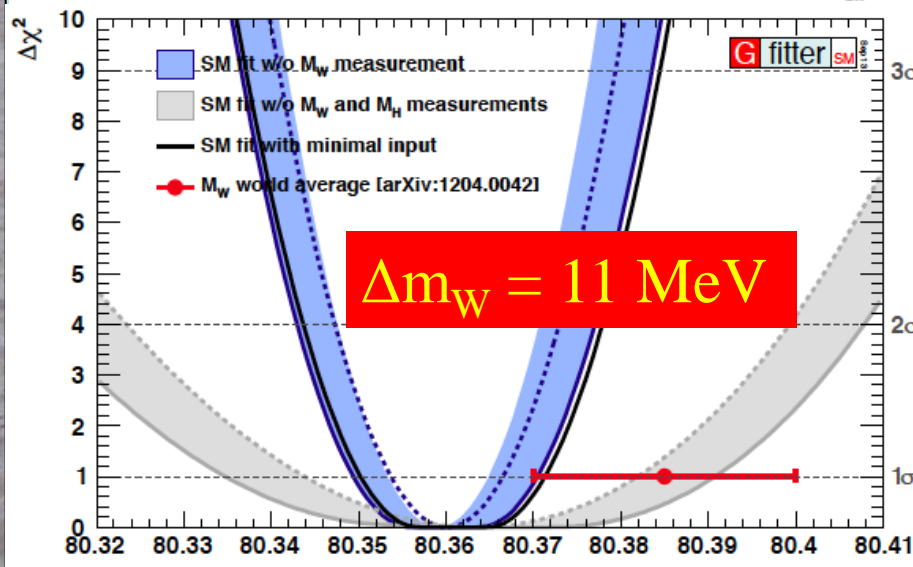
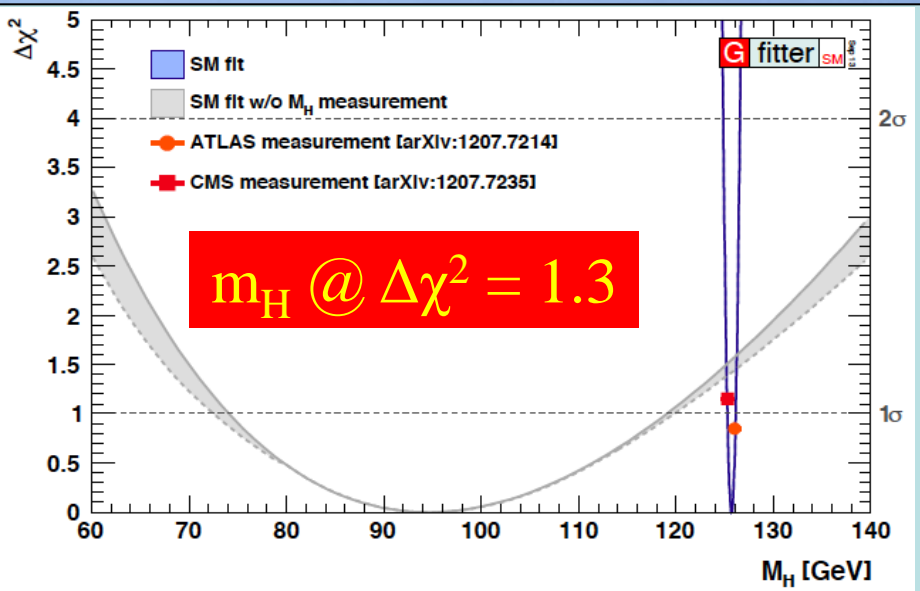
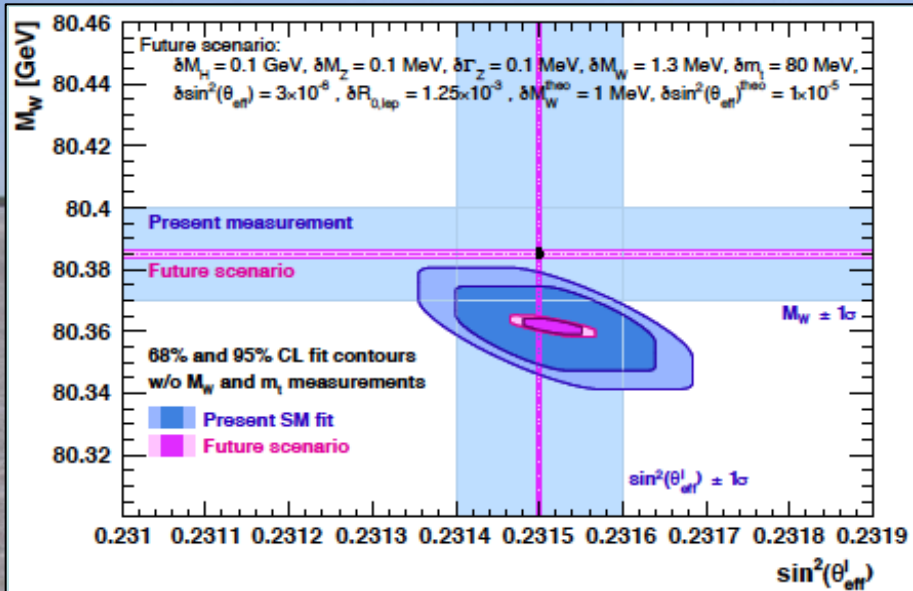
Precision Measurements

- Springboard for sensitivity to new physics
- Theoretical issues:
 - Higher-order QCD
 - Higher-order EW
 - Mixed QCD + EW
- Experimental issues
 - Patrick

Rare Decays

- Direct searches for new physics
- Many opportunities
- Z: 10^{12}
- b, c, τ : 10^{11}
- W: 10^8
- H: 10^6
- t: 10^6

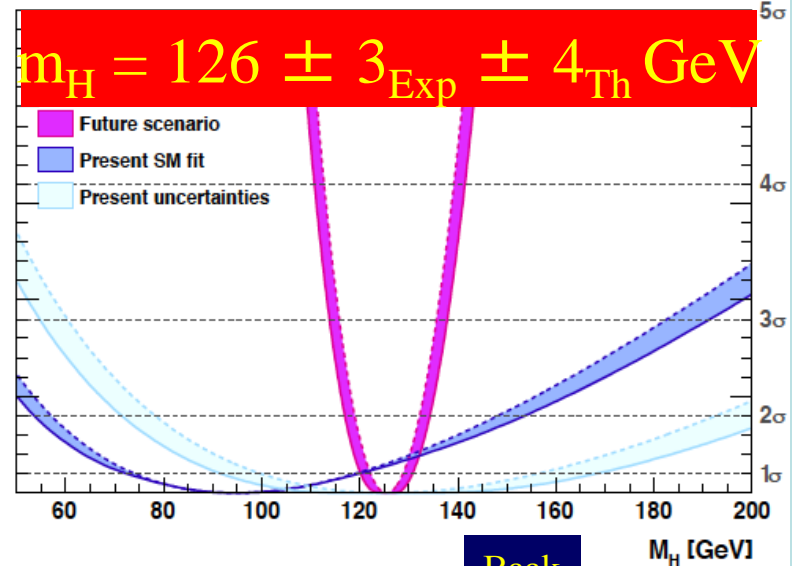
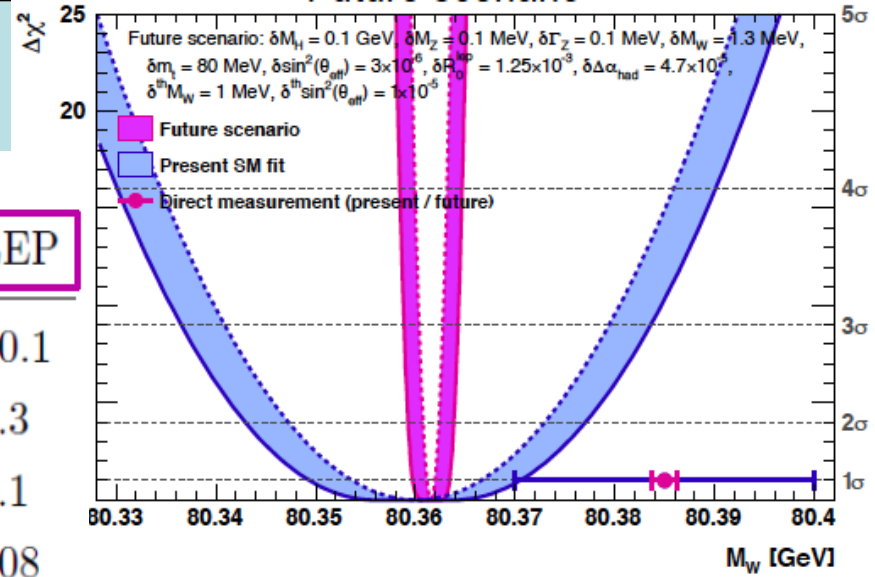
Present Predictions from Gfitter



Future Predictions from Gfitter

- Assumed inputs

| Parameter | Experimental input [$\pm 1\sigma$] | | | |
|--|--------------------------------------|-----------------|-------------------|-------------------|
| | Present | LHC | ILC/GigaZ | TLEP |
| M_H [GeV] | 0.4 \Rightarrow < 0.1 | < 0.1 | < 0.1 | < 0.1 |
| M_W [MeV] | 15 \Rightarrow 8 | \Rightarrow 5 | \Rightarrow 1.3 | |
| M_Z [MeV] | 2.1 | 2.1 | 2.1 | \Rightarrow 0.1 |
| m_t [GeV] | 0.9 \Rightarrow 0.6 | 0.1 | 0.08 | |
| Γ_Z [MeV] | 2.3 | 2.3 | \Rightarrow 0.8 | \Rightarrow 0.1 |
| $\sin^2\theta_{\text{eff}}^\ell$ [$\cdot 10^{-5}$] | 16 | 16 | \Rightarrow 1.3 | \Rightarrow 0.3 |
| R_l^0 [$\cdot 10^{-3}$] | 25 | 25 | \Rightarrow 4 | \Rightarrow 1.3 |
| $\Delta\alpha_{\text{had}}^5(M_Z^2)$ [$\cdot 10^{-5}$] | 10 \Rightarrow 4.7 | 4.7 | 4.7 | |
| $\alpha_S(M_Z^2)$ [$\cdot 10^{-4}$] | - | - | - | - |
| $\delta_{\text{th}}M_W$ [MeV] | 4 \Rightarrow 1 | 1 | 1 | |
| $\delta_{\text{th}}\sin^2\theta_{\text{eff}}^\ell$ [$\cdot 10^{-5}$] | 4.7 \Rightarrow 1 | 1 | 1 | |



TLEP Measurements & New Physics

- Assumed future measurements

| | Current data | before TLEP | TLEP-Z | TLEP-Z (pol.) | TLEP-W | TLEP-t |
|--|-----------------------|-------------------|---------------|----------------|---------------|-------------|
| $\alpha_s(M_Z^2)$ | 0.1184 ± 0.0006 | ??? | | | | |
| $\Delta\alpha_{\text{had}}^{(5)}(M_Z^2)$ | 0.02750 ± 0.00033 | ± 0.00005 (?) | | | | |
| M_Z [GeV] | 91.1875 ± 0.0021 | | ± 0.0001 | | | |
| m_t [GeV] | 173.2 ± 0.9 | ± 0.5 (?) | | | | ± 0.016 |
| m_h [GeV] | 125.6 ± 0.3 | ± 0.15 (?) | | | | |
| M_W [GeV] | 80.385 ± 0.015 | ± 0.010 (?) | | | ± 0.00064 | |
| Γ_W [GeV] | 2.085 ± 0.042 | | | | ??? | |
| Γ_Z [GeV] | 2.4952 ± 0.0023 | | ± 0.0001 | | | |
| σ_h^0 [nb] | 41.540 ± 0.037 | | ??? | | | |
| $\sin^2 \theta_{\text{eff}}^{\text{lept}}(Q_{\text{FB}}^{\text{had}})$ | 0.2324 ± 0.0012 | | ??? | | | |
| P_{τ}^{pol} | 0.1465 ± 0.0033 | | ??? | | | |
| \mathcal{A}_e | 0.1513 ± 0.0021 | | | ± 0.000021 | | |
| \mathcal{A}_c | 0.670 ± 0.027 | | | ??? | | |
| \mathcal{A}_b | 0.923 ± 0.020 | | | ??? | | |
| $A_{\text{FB}}^{0,\ell}$ | 0.0171 ± 0.0010 | | ??? | | | |
| $A_{\text{FB}}^{0,c}$ | 0.0707 ± 0.0035 | | ??? | | | |
| $A_{\text{FB}}^{0,b}$ | 0.0992 ± 0.0016 | | ??? | | | |
| R_{ℓ}^0 | 20.767 ± 0.025 | | ± 0.001 | | | |
| R_c^0 | 0.1721 ± 0.0030 | | ??? | | | |
| R_b^0 | 0.21629 ± 0.00066 | | ± 0.00006 | | | |

Theoretical Uncertainties

- We assume that theoretical uncertainties will be reduced by calculating three-loop contributions of $O(\alpha^2\alpha_s)$ and $O(\alpha^3)$.

| | TLEP direct | Parametric uncertainty | | | | | | Theoretical uncertainty | |
|--------------------------------------|-------------|------------------------|-----------------------------------|------------|------------|------------|------------|-------------------------|------------|
| | | α_s | $\Delta\alpha_{\text{had}}^{(5)}$ | M_Z | m_t | m_h | Total | current | future |
| δM_W [MeV] | ± 0.64 | ± 0.36 | ± 0.91 | ± 0.13 | ± 0.10 | ± 0.14 | ± 1.00 | ± 4 | ± 1 |
| $\delta \Gamma_Z$ [MeV] | ± 0.1 | ± 0.3 | ± 0.0 | ± 0.0 | ± 0.0 | ± 0.0 | ± 0.3 | ± 0.5 | ± 0.1 |
| $\delta \mathcal{A}_e$ [10^{-5}] | ± 2.1 | ± 1.6 | ± 13.7 | ± 0.6 | ± 0.4 | ± 0.9 | ± 13.9 | ± 37.0 | ± 11.8 |

$$\delta \sin^2 \theta_{\text{eff}}^{\text{lept}} = 4.7 \times 10^{-5} \rightarrow 1.5 \times 10^{-5}$$

Hadronic contribution to α :

At present: $\Delta\alpha_{\text{had}}^{(5)}(M_Z^2) = 0.02750 \pm 0.00033$

measured with inclusive processes.

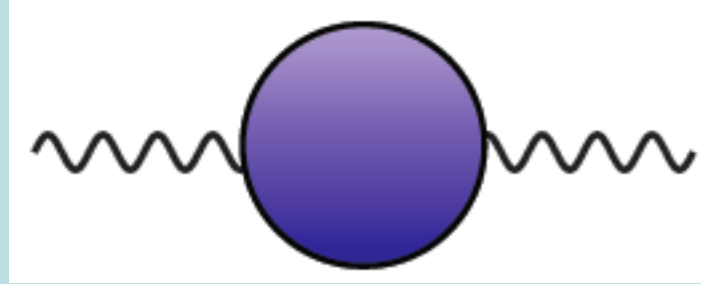
smaller uncertainty (~ 0.00010) if using exclusive processes with pQCD, etc.

Burkhardt & Pietrzyk (11)
 (see also Davier et al(11);
 Hagiwara et al(11); Jegerlehner(11))

➔ assume $\delta(\Delta\alpha_{\text{had}}^{(5)}(M_Z^2)) \sim 0.00005$ from low-energy exp's

Sensitivity to New Physics

- Oblique Parameters
- (vacuum polarizations)



$$\delta M_W, \delta \Gamma_W \propto -S + 2c_W^2 T + \frac{(c_W^2 - s_W^2) U}{2s_W^2}$$

$$\delta \Gamma_Z \propto -10(3 - 8s_W^2) S + (63 - 126s_W^2 - 40s_W^4) T$$

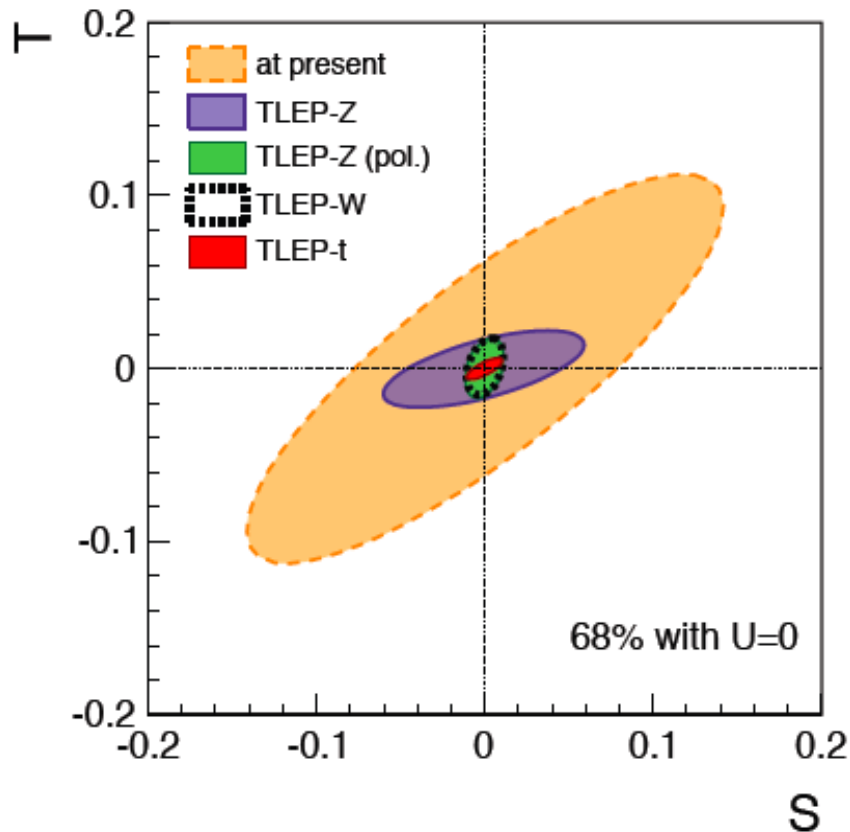
$$\text{others} \propto S - 4c_W^2 s_W^2 T$$

- Expect $U \ll S, T$
- Will need effort to reduce theoretical uncertainties to realize sensitivities $< 10^{-2}$

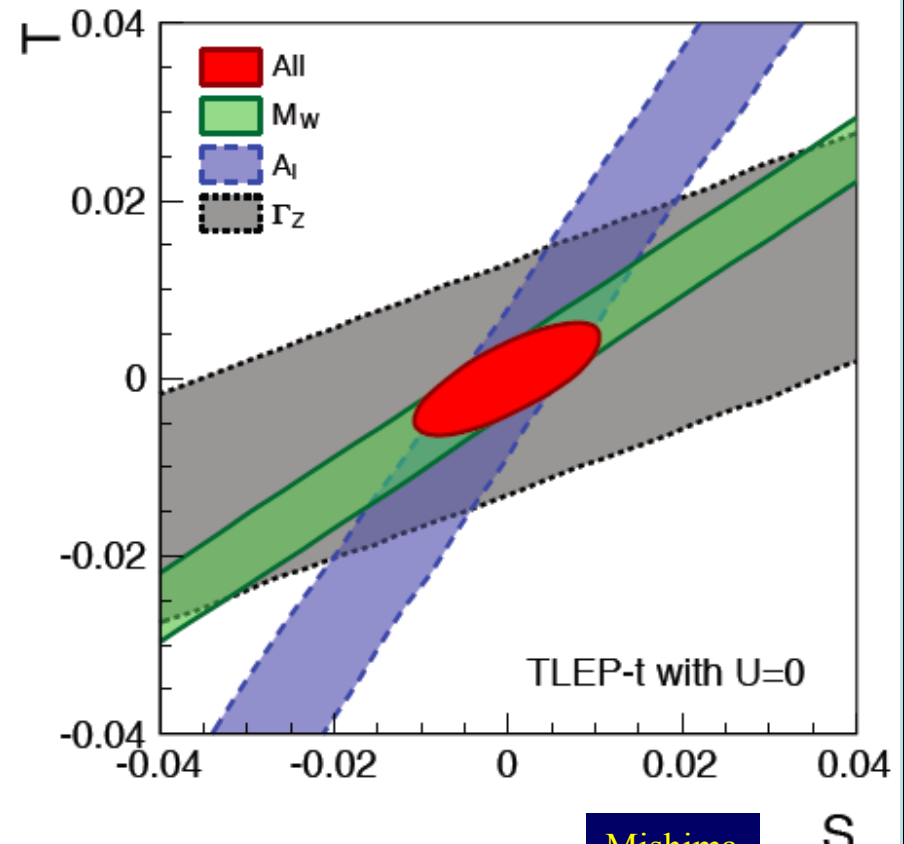
Sensitivity to Oblique Parameters

$$\delta S \sim 7 \times 10^{-3}, \quad \delta T \sim 4 \times 10^{-3}$$

SM scenario



Contributions to fit



Sensitivity to New Physics

- Higher-dimensional operators induced by high-E physics

$$\mathcal{O}_{WB} = (H^\dagger \tau^a H) W_{\mu\nu}^a B^{\mu\nu}$$

$$\mathcal{O}_H = |H^\dagger D_\mu H|^2$$

$$\mathcal{O}_{LL} = \frac{1}{2} (\bar{L} \gamma_\mu \tau^a L)^2$$

$$\mathcal{O}'_{HL} = i(H^\dagger D_\mu \tau^a H) (\bar{L} \gamma^\mu \tau^a L)$$

$$\mathcal{O}'_{HQ} = i(H^\dagger D_\mu \tau^a H) (\bar{Q} \gamma^\mu \tau^a Q)$$

$$\mathcal{O}_{HL} = i(H^\dagger D_\mu H) (\bar{L} \gamma^\mu L)$$

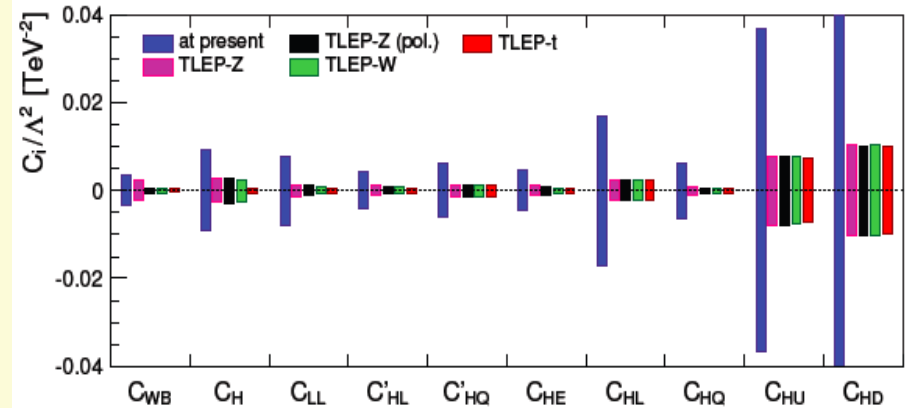
$$\mathcal{O}_{HQ} = i(H^\dagger D_\mu H) (\bar{Q} \gamma^\mu Q)$$

$$\mathcal{O}_{HE} = i(H^\dagger D_\mu H) (\bar{E} \gamma^\mu E)$$

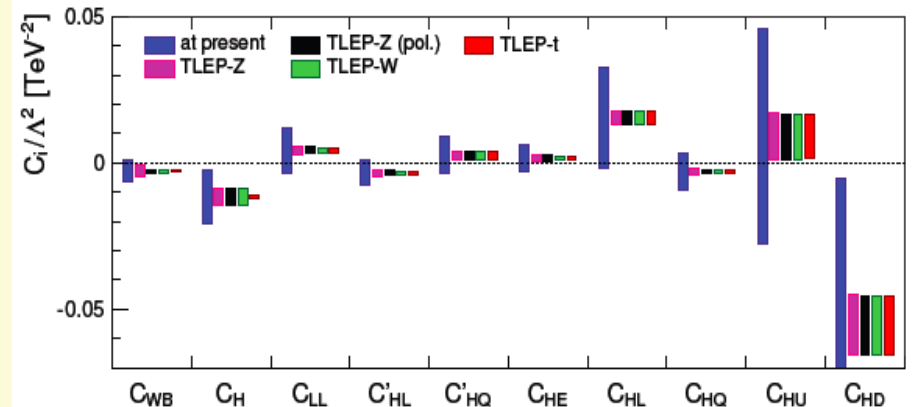
$$\mathcal{O}_{HU} = i(H^\dagger D_\mu H) (\bar{U} \gamma^\mu U)$$

$$\mathcal{O}_{HD} = i(H^\dagger D_\mu H) (\bar{D} \gamma^\mu D)$$

SM scenario



NP scenario



Mishima

Sensitivity to New Physics

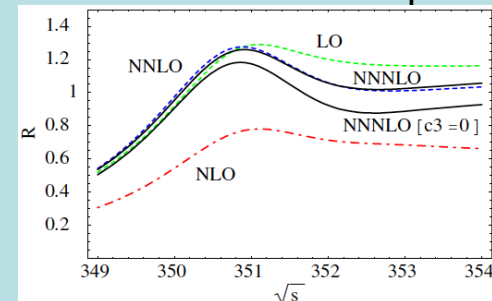
- Sensitivity to coefficients of possible higher-dimensional operators induced by high-E physics (in TeV units)

| Coefficient | at present | | TLEP-Z | | TLEP-Z (pol.) | | TLEP-W | | TLEP-t | |
|-------------|------------|-----------|------------|-----------|---------------|-----------|------------|-----------|------------|-----------|
| | $C_i = -1$ | $C_i = 1$ | $C_i = -1$ | $C_i = 1$ | $C_i = -1$ | $C_i = 1$ | $C_i = -1$ | $C_i = 1$ | $C_i = -1$ | $C_i = 1$ |
| C_{WB} | 12.0 | 12.0 | 15.2 | 15.2 | 31.3 | 31.1 | 31.3 | 31.5 | 38.3 | 38.9 |
| C_H | 7.4 | 7.4 | 13.6 | 13.6 | 13.9 | 13.7 | 14.0 | 14.1 | 27.9 | 27.8 |
| C_{LL} | 8.1 | 8.1 | 19.3 | 19.3 | 19.9 | 19.9 | 25.4 | 25.5 | 27.6 | 27.7 |
| C'_{HL} | 10.9 | 10.9 | 21.2 | 21.1 | 25.9 | 25.7 | 25.8 | 25.8 | 31.2 | 30.9 |
| C'_{HQ} | 9.0 | 9.1 | 19.5 | 19.3 | 19.5 | 19.4 | 19.4 | 19.2 | 19.6 | 19.6 |
| C_{HL} | 10.4 | 10.4 | 21.5 | 21.5 | 21.5 | 21.9 | 28.6 | 28.5 | 28.3 | 28.4 |
| C_{HQ} | 5.4 | 5.5 | 14.9 | 14.9 | 15.0 | 14.9 | 15.1 | 15.0 | 15.0 | 15.0 |
| C_{HE} | 8.9 | 8.9 | 22.2 | 22.2 | 30.2 | 30.0 | 30.1 | 30.3 | 31.2 | 31.2 |
| C_{HU} | 3.7 | 3.7 | 8.0 | 8.0 | 8.1 | 8.1 | 8.1 | 8.1 | 8.3 | 8.3 |
| C_{HD} | 3.2 | 3.2 | 7.1 | 7.0 | 7.1 | 7.1 | 7.0 | 7.1 | 7.1 | 7.1 |

- Substantial improvement in sensitivity
- Reach well into multi-TeV range

(Mainly) QCD Uncertainties

- Γ_b : Higgs WG: $\Delta\Gamma_b = 7.5\%$ should be 1.7%
 - Higher-order QCD 0.25%
 - m_b uncertainty overstated by factor 4
 - Error could be reduced by running SuperKEK-B above Υ
 - 5-loop running underway
 - Need inputs from LE: m_b , m_c , α_{EM} , α_s
 - 0.3% possible
- M_W :
 - 4-loop uncertainty of 2.1 MeV insufficient: use \overline{MS} m_t
 - Could do 4-loop mixed EW/QCD
- m_t :
 - calculation of σ at NNNLO underway



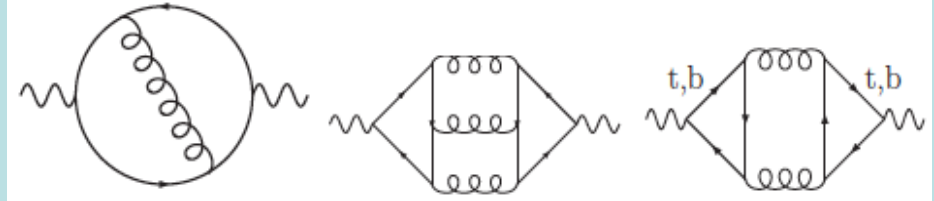
(Mainly) QCD Uncertainties

- Γ_Z :

- $\Delta(\text{non-singlet}) = 101 \text{ KeV}$

- $\Delta(\text{singlet}) V(3g) = 2.7 \text{ KeV}, A(2g) = 42 \text{ KeV}$

- Difficult to do next order

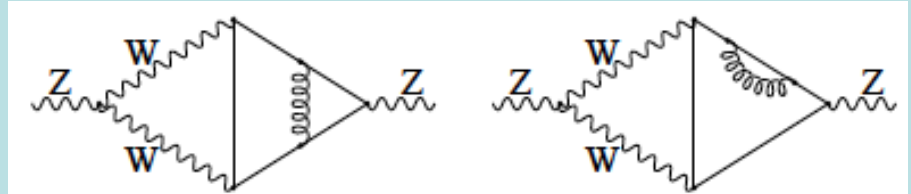


- Γ_b :

- Correction @ $G_F m_t^2 \alpha_s^2 = 0.1 \text{ MeV}$

- Smaller corrections if use MSbar m_t , but need to know 4-loop conversion (underway)

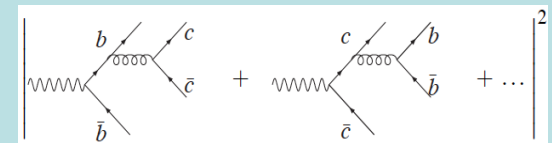
- Not well-defined at higher order: $b\bar{b}c\bar{c}$ final states!



- Γ_W :

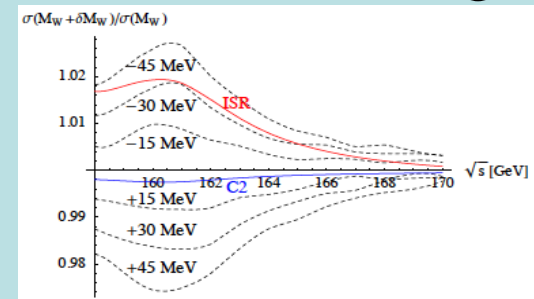
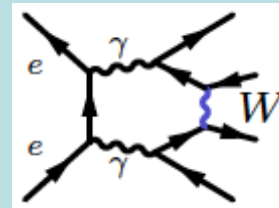
- Mixed EW/QCD calculated @ 2-loop: -0.55 MeV

- 3-loop $\alpha_W \alpha_s^2$ difficult but feasible



WW Production at Threshold

- Aim at $\Delta m_W < 1 \text{ MeV}$: need $\Delta\sigma \ll 0.1\%$
- Current $\Delta m_W < 4 \text{ MeV}$
 - Should make off-shell treatment:
 - 4-fermion production known @ NLO and leading NNLO
 - Threshold corrections included
 - Need more understanding of ISR
 - NNLO EW calculation of on-shell WW within reach
 - Sufficient for $\Delta m_W < 1 \text{ MeV}$
 - NNLO off-shell calculation beyond current reach

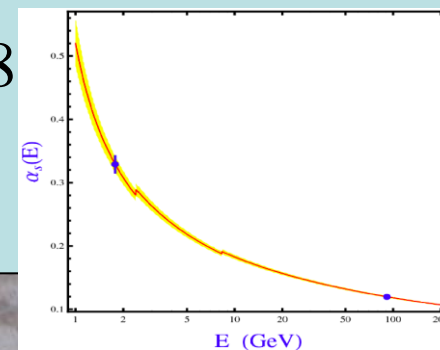
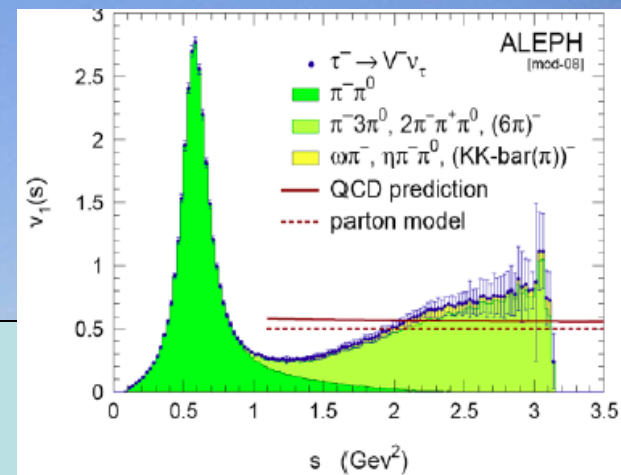


High-Energy Measurements of α_s

- TLEP study quotes $\Delta\alpha_s = 0.0002$ from Z decays based on NNNLO calculation
- W decays could yield $\Delta\alpha_s = 0.00015$?
- Important CKM uncertainty, mainly due to ΔV_{cs}
 - Assume unitarity? Measure V_{cs} better?
- Possible strategy: Use Z value @ W to measure V, use @ τ to constrain non-perturbative effects
- Need to study uncertainty in running

Measurement of α_s in τ Decays

- LEP data still dominate τ analyses
 - Systematic uncertainties at B factories
- Assume charged-current universality OK, but check W to $\tau\nu/\mu\nu$
- QCD predicts moments of spectral function
 - Expect small non-perturbative piece, can be fitted from data
- 2 ways of summing QCD give estimate of error:
 - $\alpha_s(m_\tau) = 0.339$ vs 0.318 , $\alpha_s(m_Z) = 0.1210$ vs 0.1198
- Uncertainty due to running: c threshold!

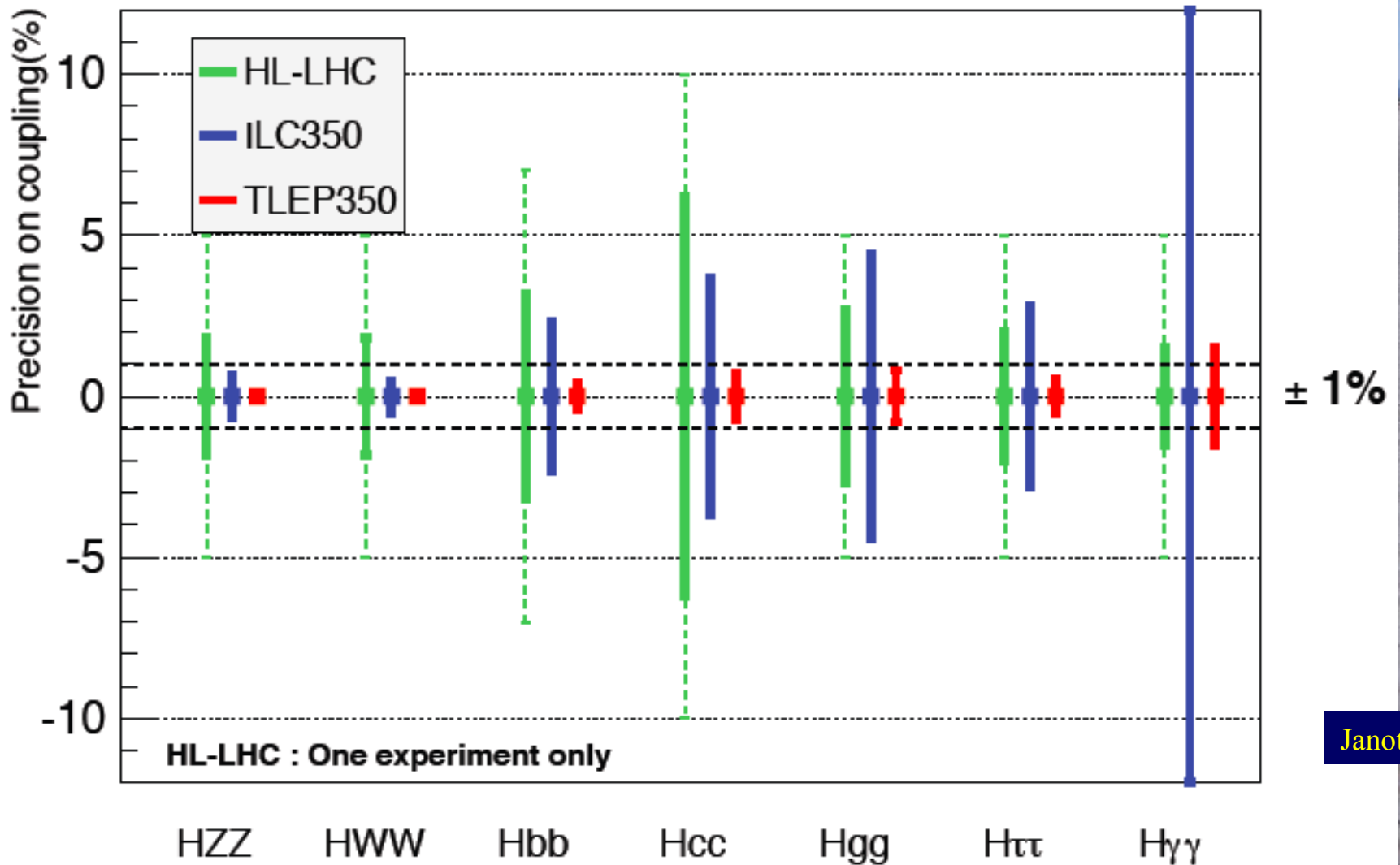


Possible Future Higgs Measurements

| Facility | | ILC | | ILC(LumiUp) | | TLEP (4 IP) | | CLIC | |
|-------------------------------------|--------------|--------------|--------------|---------------------------|--------|-------------|-----------|-----------|-----------|
| \sqrt{s} (GeV) | 250 | 500 | 1000 | 250/500/1000 | 240 | 350 | 350 | 1400 | 3000 |
| $\int \mathcal{L} dt$ (fb $^{-1}$) | 250 | +500 | +1000 | 1150+1600+2500 † | 10000 | +2600 | 500 | +1500 | +2000 |
| $P(e^-, e^+)$ | (-0.8, +0.3) | (-0.8, +0.3) | (-0.8, +0.2) | (same) | (0, 0) | (0, 0) | (-0.8, 0) | (-0.8, 0) | (-0.8, 0) |
| Γ_H | 12% | 5.0% | 4.6% | 2.5% | 1.9% | 1.0% | 9.2% | 8.5% | 8.4% |
| κ_γ | 18% | 8.4% | 4.0% | 2.4% | 1.7% | 1.5% | – | 5.9% | <5.9% |
| κ_g | 6.4% | 2.3% | 1.6% | 0.9% | 1.1% | 0.8% | 4.1% | 2.3% | 2.2% |
| κ_W | 4.9% | 1.2% | 1.2% | 0.6% | 0.85% | 0.19% | 2.6% | 2.1% | 2.1% |
| κ_Z | 1.3% | 1.0% | 1.0% | 0.5% | 0.16% | 0.15% | 2.1% | 2.1% | 2.1% |
| κ_μ | 91% | 91% | 16% | 10% | 6.4% | 6.2% | – | 11% | 5.6% |
| κ_τ | 5.8% | 2.4% | 1.8% | 1.0% | 0.94% | 0.54% | 4.0% | 2.5% | <2.5% |
| κ_c | 6.8% | 2.8% | 1.8% | 1.1% | 1.0% | 0.71% | 3.8% | 2.4% | 2.2% |
| κ_b | 5.3% | 1.7% | 1.3% | 0.8% | 0.88% | 0.42% | 2.8% | 2.2% | 2.1% |
| κ_t | – | 14% | 3.2% | 2.0% | – | 13% | – | 4.5% | <4.5% |
| BR_{inv} | 0.9% | < 0.9% | < 0.9% | 0.4% | 0.19% | < 0.19% | | | |

- Interpretation?
- Theoretical uncertainties and new physics interpretations

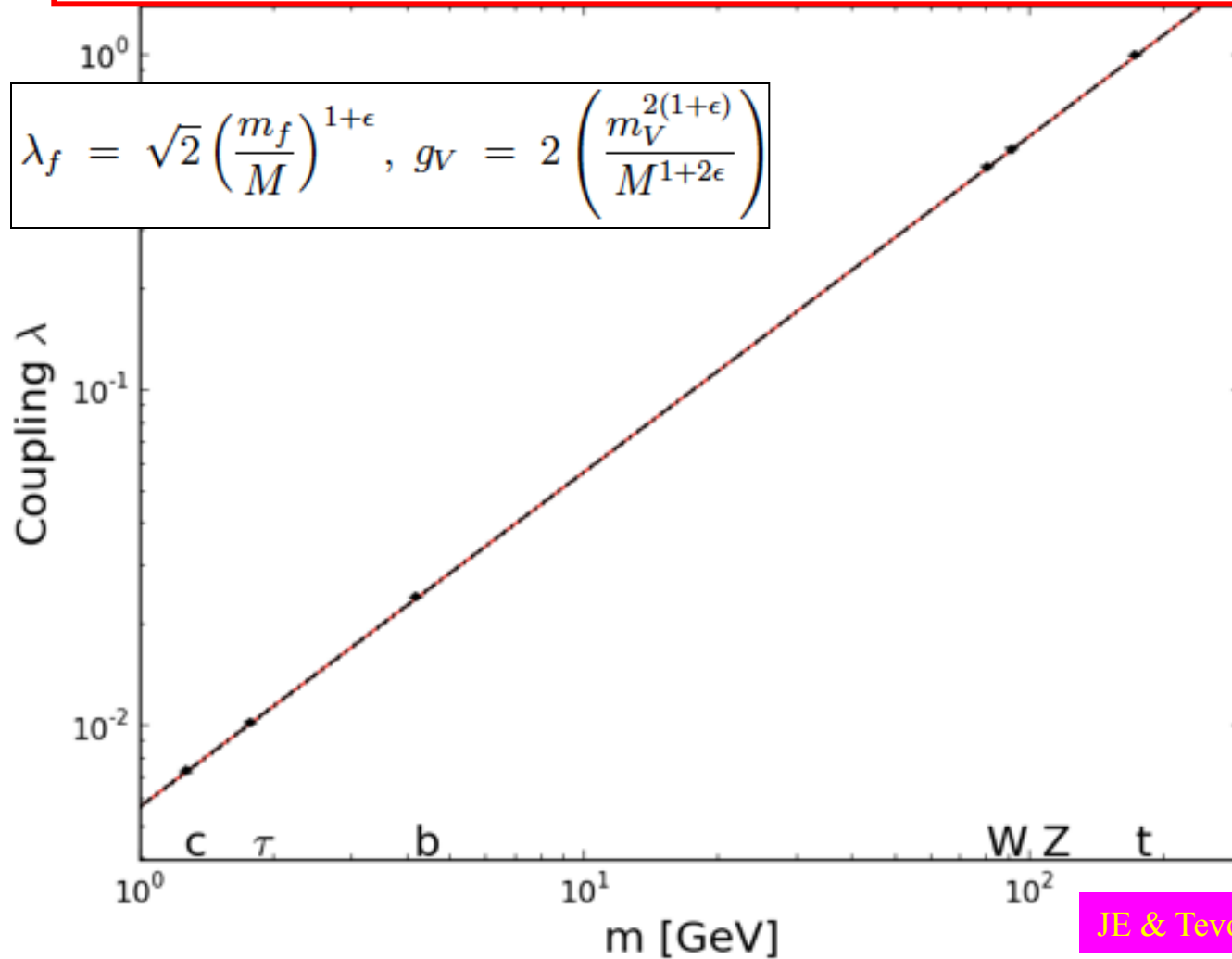
Possible Future Higgs Measurements



H Coupling Measurements @TLEP

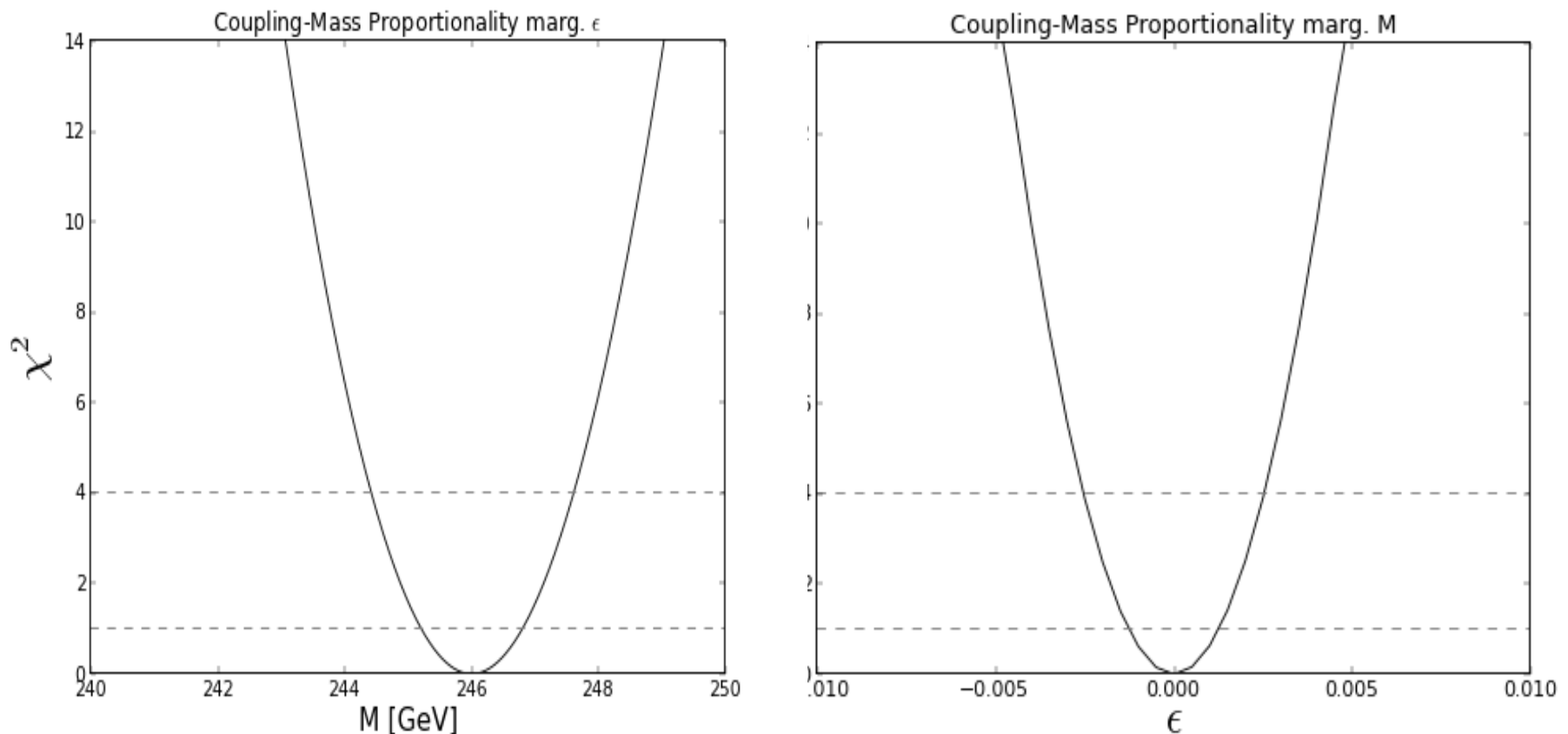
$$M = 246.0 \pm 0.8 \text{ GeV}, \quad \varepsilon = 0.0000^{+0.0015}_{-0.0010}$$

$$\lambda_f = \sqrt{2} \left(\frac{m_f}{M} \right)^{1+\varepsilon}, \quad g_V = 2 \left(\frac{m_V^{2(1+\varepsilon)}}{M^{1+2\varepsilon}} \right)$$



Global Analysis of Higgs @ TLEP

- One-dimensional χ^2 for M , ϵ



$$M = 246.0 \pm 0.8 \text{ GeV}, \epsilon = 0.0000^{+0.0015}_{-0.0010}$$

Rare Leptonic Z Decays?

Silvestrini

- Upper limits from flavour-changing neutral currents (FCNC)

- **Current and future** bounds on LFV μ and τ decays:
 - $BR(\mu \rightarrow eee) < 10^{-12}$
 - $BR(\tau \rightarrow \mu\mu\mu) < 2 \cdot 10^{-8}$ (10^{-9})
 - $BR(\tau \rightarrow eee) < 3 \cdot 10^{-8}$ (10^{-9})
- These bounds imply:
 - $BR(Z \rightarrow \mu e) < 3 \cdot 10^{-13}$
 - $BR(Z \rightarrow \tau\mu) < 4 \cdot 10^{-8}$ ($2 \cdot 10^{-9}$)
 - $BR(Z \rightarrow \tau e) < 6 \cdot 10^{-8}$ ($2 \cdot 10^{-9}$)

Opportunities

- Measuring $BR(Z \rightarrow \tau e)$ & $BR(Z \rightarrow \tau\mu)$ better than 10^{-9} would overcome future bounds on LFV decays

Rare Hadronic Z Decays?

Silvestrini

- Upper limits from flavour-changing neutral currents (FCNC)

- From present expts in B physics one gets

$$|U_{bs}| < \sim 4 \cdot 10^{-4} \text{ and } |U_{bd}| < \sim 10^{-4} \quad \text{Buras et al.}$$

$$\Rightarrow \text{BR}(Z \rightarrow bd) < \sim 10^{-9}, \text{BR}(Z \rightarrow bs) < \sim 2 \cdot 10^{-8}$$

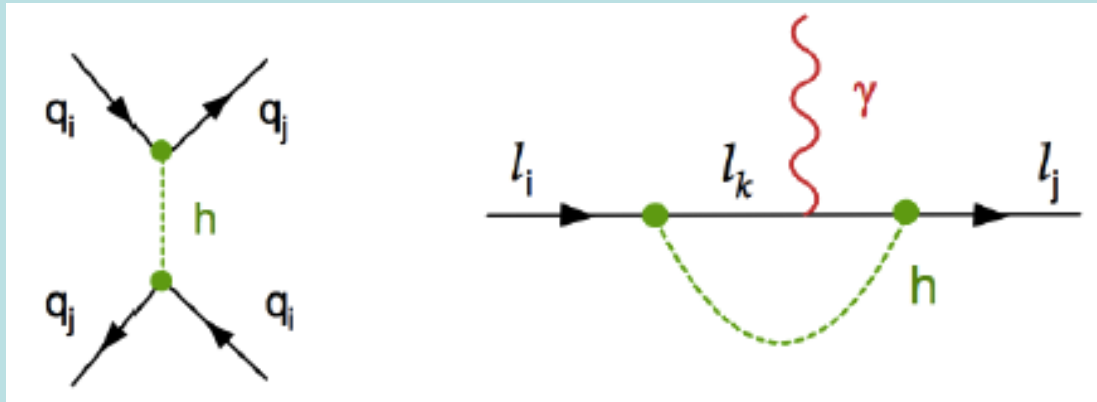
- How far can TLEP go? How will b id perform?
- From D mixing one gets $|U_{uc}| < \sim 2 \cdot 10^{-3}$

$$\Rightarrow \text{BR}(Z \rightarrow cu) < \sim 5 \cdot 10^{-7}$$

Opportunities

Rare Higgs Decays?

- Upper limits from FCNC, EDMs, ...



- Quark FCNC bounds exclude observability of quark-flavour-violating h decays
- Lepton-flavour-violating h decays could be large:
 $BR(\tau\mu)$ or $BR(\tau e)$ could be $O(10)\%$

Flavour-Changing Higgs Couplings?

- Constraints on quark-flavour-changing couplings from FCNC

- Constraints on lepton-flavour-changing couplings

| Operator | Eff. couplings | 95% C.L. Bound | | Observables |
|--|----------------------|-----------------------|-------------------------------|--|
| | | $ c_{\text{eff}} $ | $ \text{Im}(c_{\text{eff}}) $ | |
| $(\bar{s}_R d_L)(\bar{s}_L d_R)$ | $c_{sd} c_{ds}^*$ | 1.1×10^{-10} | 4.1×10^{-13} | $\Delta m_K; \epsilon_K$ |
| $(\bar{s}_R d_L)^2, (\bar{s}_L d_R)^2$ | c_{ds}^2, c_{sd}^2 | 2.2×10^{-10} | 0.8×10^{-12} | |
| $(\bar{c}_R u_L)(\bar{c}_L u_R)$ | $c_{cu} c_{uc}^*$ | 0.9×10^{-9} | 1.7×10^{-10} | $\Delta m_D; q/p , \phi_D$ |
| $(\bar{c}_R u_L)^2, (\bar{c}_L u_R)^2$ | c_{uc}^2, c_{cu}^2 | 1.4×10^{-9} | 2.5×10^{-10} | |
| $(\bar{b}_R d_L)(\bar{b}_L d_R)$ | $c_{bd} c_{db}^*$ | 0.9×10^{-8} | 2.7×10^{-9} | $\Delta m_{B_d}; S_{B_d \rightarrow \psi K}$ |
| $(\bar{b}_R d_L)^2, (\bar{b}_L d_R)^2$ | c_{db}^2, c_{bd}^2 | 1.0×10^{-8} | 3.0×10^{-9} | |
| $(\bar{b}_R s_L)(\bar{b}_L s_R)$ | $c_{bs} c_{sb}^*$ | 2.0×10^{-7} | 2.0×10^{-7} | Δm_{B_s} |
| $(\bar{b}_R s_L)^2, (\bar{b}_L s_R)^2$ | c_{sb}^2, c_{bs}^2 | 2.2×10^{-7} | 2.2×10^{-7} | |

| Operator | Eff. couplings | Bound | Constraint |
|--|--|----------------------|---|
| $(\bar{\mu}_R e_L)(\bar{q}_L q_R), (\bar{\mu}_L e_R)(\bar{q}_L q_R)$ | $ c_{\mu e} ^2, c_{e\mu} ^2$ | 3.0×10^{-8} | $\mathcal{B}(\mu \rightarrow e(\text{Ti})) < 4.3 \times 10^{-12}$ |
| $(\bar{\tau}_R \mu_L)(\bar{\mu}_L \mu_R), (\bar{\tau}_L \mu_R)(\bar{\mu}_L \mu_R)$ | $ c_{\tau\mu} ^2, c_{\mu\tau} ^2$ | 2.0×10^{-1} | $\Gamma(\tau \rightarrow \mu\bar{\mu}\mu) < 2.1 \times 10^{-8}$ |
| $(\bar{\tau}_R e_L)(\bar{\mu}_L \mu_R), (\bar{\tau}_L e_R)(\bar{\mu}_L \mu_R)$ | $ c_{\tau e} ^2, c_{e\tau} ^2$ | 4.8×10^{-1} | $\Gamma(\tau \rightarrow e\bar{\mu}\mu) < 2.7 \times 10^{-8}$ |
| $(\bar{\tau}_R e_L)(\bar{\mu}_L e_R), (\bar{\tau}_L e_R)(\bar{\mu}_L e_R)$ | $ c_{\mu e} c_{e\tau}^* , c_{\mu e} c_{\tau e} $ | 0.9×10^{-4} | $\Gamma(\tau \rightarrow \bar{\mu}ee) < 1.5 \times 10^{-8}$ |
| $(\bar{\tau}_R e_L)(\bar{\mu}_R e_L), (\bar{\tau}_L e_R)(\bar{\mu}_R e_L)$ | $ c_{e\mu}^* c_{e\tau}^* , c_{e\mu}^* c_{\tau e} $ | | |
| $(\bar{\tau}_R \mu_L)(\bar{e}_L \mu_R), (\bar{\tau}_L \mu_R)(\bar{e}_L \mu_R)$ | $ c_{e\mu} c_{\mu\tau}^* , c_{e\mu} c_{\tau\mu} $ | 1.0×10^{-4} | $\Gamma(\tau \rightarrow \bar{e}\mu\mu) < 1.7 \times 10^{-8}$ |
| $(\bar{\tau}_R \mu_L)(\bar{e}_R \mu_L), (\bar{\tau}_L \mu_R)(\bar{e}_R \mu_L)$ | $ c_{\mu e}^* c_{\mu\tau}^* , c_{\mu e}^* c_{\tau\mu} $ | | |

| Eff. couplings | Bound | Constraint |
|---|---|--|
| $ c_{e\tau} c_{\tau e} $ ($ c_{e\mu} c_{\mu e} $) | 1.1×10^{-2} (1.8×10^{-1}) | $ \delta m_e < m_e$ |
| $ \text{Re}(c_{e\tau} c_{\tau e}) $ ($ \text{Re}(c_{e\mu} c_{\mu e}) $) | 0.8×10^{-2} (1.4×10^{-1}) | $ \delta a_e < 6 \times 10^{-12}$ |
| $ \text{Im}(c_{e\tau} c_{\tau e}) $ ($ \text{Im}(c_{e\mu} c_{\mu e}) $) | 1.1×10^{-7} (1.9×10^{-6}) | $ d_e < 1.6 \times 10^{-27} \text{ ecm}$ |
| $ c_{\mu\tau} c_{\tau\mu} $ | 2 | $ \delta m_\mu < m_\mu$ |
| $ \text{Re}(c_{\mu\tau} c_{\tau\mu}) $ | 2×10^{-2} | $ \delta a_\mu < 4 \times 10^{-9}$ |
| $ \text{Im}(c_{\mu\tau} c_{\tau\mu}) $ | 8 | $ d_\mu < 1.2 \times 10^{-19} \text{ ecm}$ |
| $ c_{e\tau} c_{\tau\mu} , c_{\tau e} c_{\mu\tau} $ | 2.4×10^{-6} | $\mathcal{B}(\mu \rightarrow e\gamma) < 2.4 \times 10^{-12}$ |
| $ c_{\mu\tau} ^2, c_{\tau\mu} ^2$ | 6.6×10^{-1} | $\mathcal{B}(\tau \rightarrow \mu\gamma) < 4.4 \times 10^{-8}$ |
| $ c_{e\tau} ^2, c_{\tau e} ^2$ | 4.7×10^{-1} | $\mathcal{B}(\tau \rightarrow e\gamma) < 3.3 \times 10^{-8}$ |

Blankenburg, JE, Isidori: arXiv:1202.5704

Neutrino Counting?

Blondel

- Z line shape
- Jarlskog's theorem

Theorem.

In the standard model, with n left-handed lepton doublets and $N - n$ right-handed neutrinos, the effective number of neutrinos, $\langle n \rangle$, defined by

$$\Gamma(Z \rightarrow \text{neutrinos}) \equiv \langle n \rangle \Gamma_0,$$

where Γ_0 is the standard width for one massless neutrino, satisfies the inequality

$$\langle n \rangle \leq n.$$

(15)

“Neutrino Counting”

Blondel

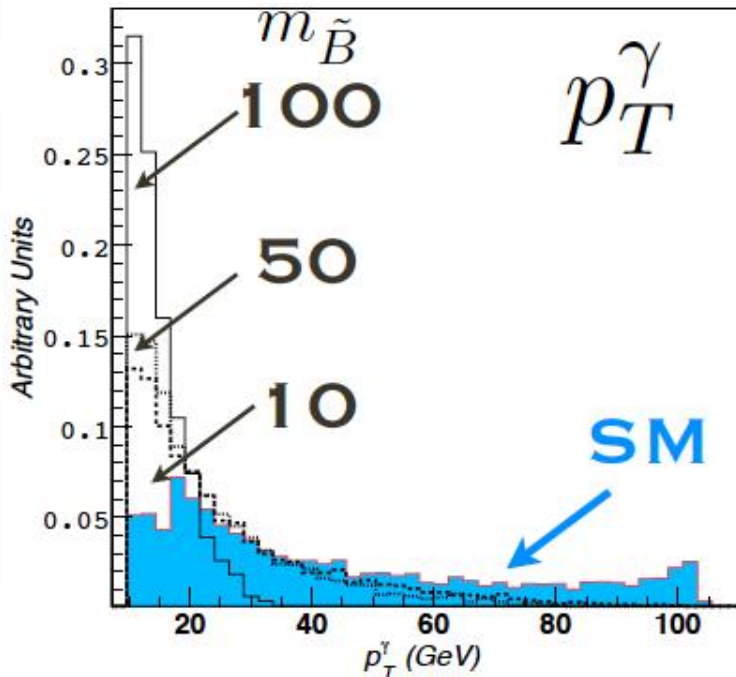
- **On Z peak:** $N_\nu = 2.984 \pm 0.008$
- 2 σ :^) !!
- Error ΔN_ν dominated by ΔL , theory dominated:
- Bhabha uncertainty ± 0.0046
- Building blocks available to bring perturbative error $< 0.1\%$
- **Radiative return:** $N_\nu = 2.92 \pm 0.05$
- EW corrections!
- Useful to study $WW\gamma$ vertex: EW NLO

Piccinini

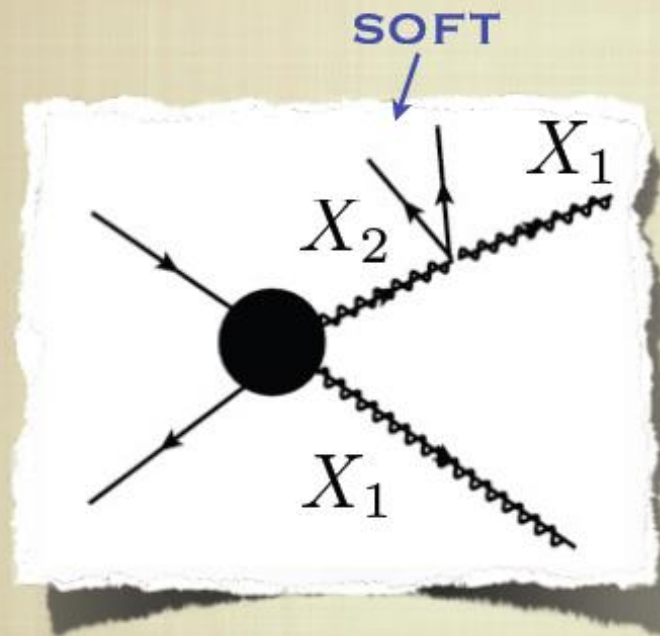
Direct Searches for New Particles?

- Best chance may be pair-production of dark matter particles + soft γ , ...
- Way to get “ $N_\nu > 3$ ” Compressed spectra

Sanz

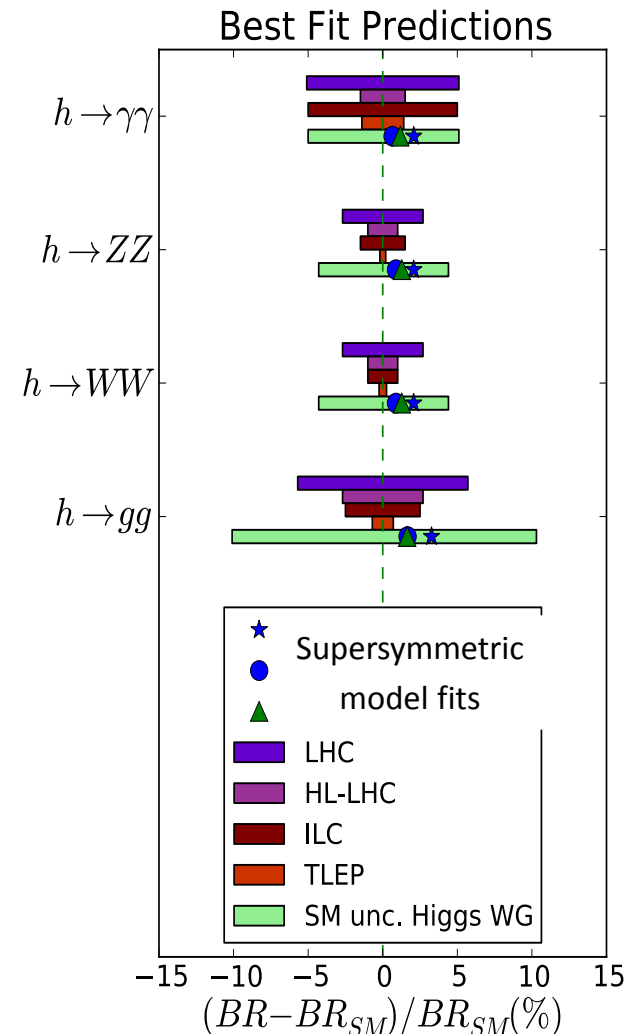


$$\Delta m = m_{X_2} - m_{X_1} \ll m_{X_1}$$



Impact of Higgs Measurements

- Predictions of current best fits in **simple SUSY models**
- **Current uncertainties** in SM calculations [LHC Higgs WG]
- Comparisons with
 - **LHC**
 - **HL-LHC**
 - **ILC**
 - **TLEP**
- **Don't decide before LHC 13/4**



cf, LEP and LHC

- *“Those who don't know history are doomed to repeat it...”*
 - Edmund Burke
- *“... and maybe also those who do.”*
- LEP: Precision ✓ Z studies, $W+W-$, search for ✗ Higgs, anything else
- LHC: search for ✓ Higgs, anything else
- **Do not decide anything until LHC 13/4**