

# Hard exclusive $J/\Psi$ (and $\Phi$ ) photoproduction off a proton

A.T. Goritschnig<sup>1</sup>, B. Melic<sup>2</sup>,  
K. Passek-Kumerički<sup>2</sup>, W. Schweiger<sup>1</sup>

<sup>1</sup>University of Graz, Graz, Austria

<sup>2</sup>Rudjer-Boškovic-Institute, Zagreb, Croatia

DIS 2014 - Warsaw at the 1<sup>st</sup> of May 2014

# Motivation

We investigate the photoproduction

$$\gamma(p_\gamma) p(p_i) \rightarrow J/\Psi(p_\Psi) p(p_f)$$

at large four-momentum transfer  $|t| = |(p_f - p_i)^2|$ .

- heavy charm-quark mass sets a hard energy scale  
⇒ perturbative QCD can become applicable
- studying quark-mass influences on production mechanism
- comparison to other mechanisms (pomeron, regge, etc...)

# Perturbative Methods in QCD

Perturbative methods in QCD are based on factorization, i.e., separation of the overall process into hard and soft subprocesses.

## Hard subprocess

- dominated by large energy effects
- takes place at short space-time distances
- perturbatively manageable
- calculation of several Feynman graphs

## Soft subprocess

- dominated by low energy effects
- takes place at long space-time distances
- non-perturbative
- parametrized by a priori unknown functions

Basic idea: **Scale separation**  $\Rightarrow$  **quantum-mechanical incoherence**.  
This means the two scales are uncorrelated and will not interfere.

# Hard Scattering Approach (HSA)

[Efremov and Radyushkin, Phys. Lett. B 94, 245 (1980)]

[Lepage and Brodsky, Phys. Rev. D 22, 2157 (1980)]

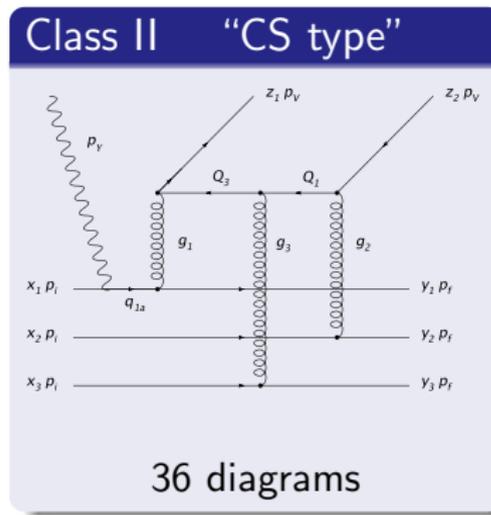
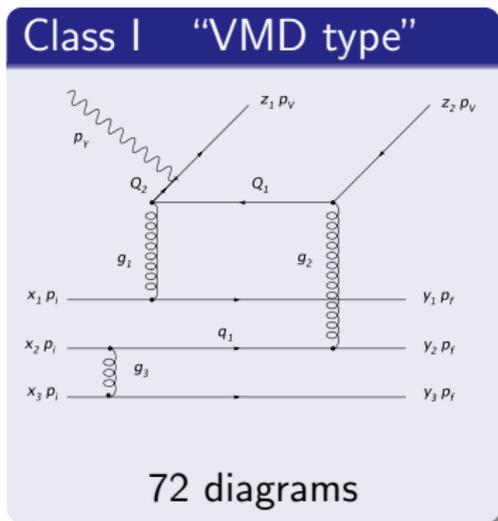
The HSA should be the dominant mechanism for exclusive reactions at very large (infinitely large) four-momentum transfer  $|t|$ .

Problem statement: large  $|t|$  AND specific final state requested.

- In the **hard scattering subprocess** hadrons replaced by on-shell valence quarks (since redistribution of momentum easier when only a few partons involved)
- and minimal number of hard gluons is introduced to connect all quark lines (to redistribute large  $|t|$  and to allow formation of requested final state).
- The **soft subprocess**, i.e., the transitions from quarks to hadronic bound-states, described by distribution amplitudes.

# HSA: hard subprocess & its generic graphs

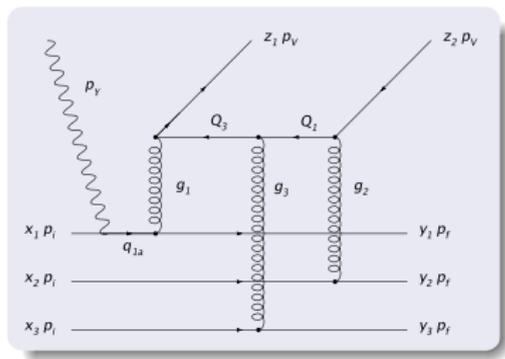
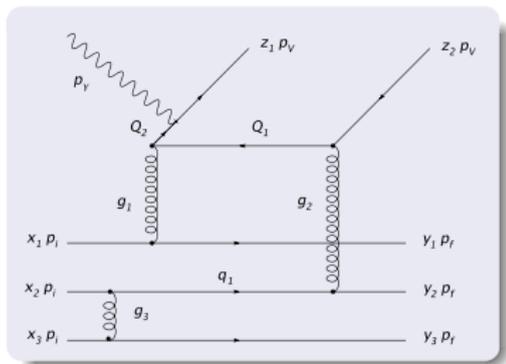
When applying the HSA to  $\gamma p \rightarrow J/\Psi p$  photoproduction, for the **hard subprocess** one has to consider a **coherent sum of altogether 108 tree graphs** with (in principle) different topology. They can be grouped into **two generic classes** according to where  $\gamma$  couples:



# HSA: hard subprocess & collinear approximation

We furthermore work within a **collinear approximation** where...

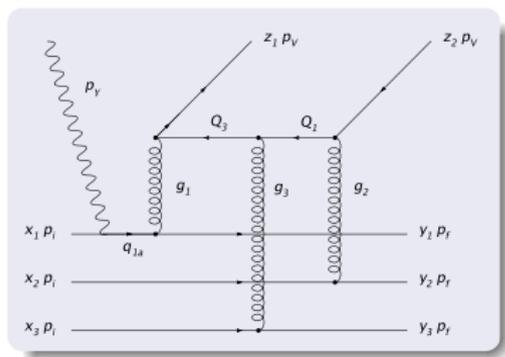
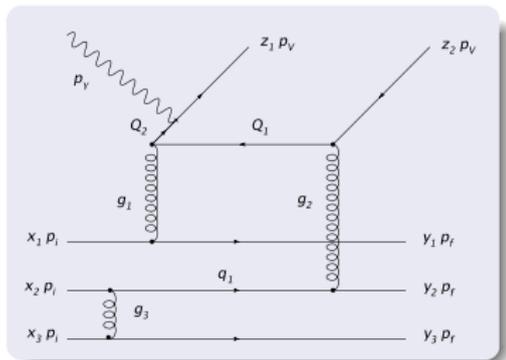
- ...four-momenta of valence quarks **assumed to be collinear** to the four-momenta of their parent hadrons.
- ...for each quark **momentum fractions** are introduced, which then parametrize their relative momenta.



# HSA: hard subprocess & quark masses

Within our approach we treat the **quark masses** as follows...

- ...we **neglect the light** quark-masses of the valence-quarks inside the proton (as it is foreseen in the “pure” HSA).
- ...we **approximate the heavy** quark-mass of the (anti)charm inside the  $J/\Psi$  by  $m_c = z_1 M_{J/\Psi}$  or  $m_c = z_2 M_{J/\Psi}$ .



## HSA: soft subprocess & distribution amplitudes

- **Distribution amplitudes defined** via matrix elements  $\langle 0 | u(r_3) u(r_2) d(r_1) | p \rangle$  and  $\langle 0 | \bar{c}(r) c(0) | J/\Psi \rangle$  for the proton and the  $J/\Psi$ , respectively.
- They incorporate the **soft, non-perturbative transitions** from the quarks to the hadronic bound-states.
- They are **probability amplitudes** for a certain configuration of momentum-fractions of quarks inside parent hadron.

For the distribution amplitudes of the proton and the  $J/\Psi$  we take

$$\phi_p(x_1, x_2, x_3) = 120 x_1 x_2 x_3 \text{ and } \phi_{J/\Psi}(z_1) = \delta(z_1 - 1/2),$$

respectively. ( $\phi_p$  is the so-called “asymptotic” nucleon amplitude.  $\phi_{J/\Psi}$  is helicity independent and essentially non-relativistic.)

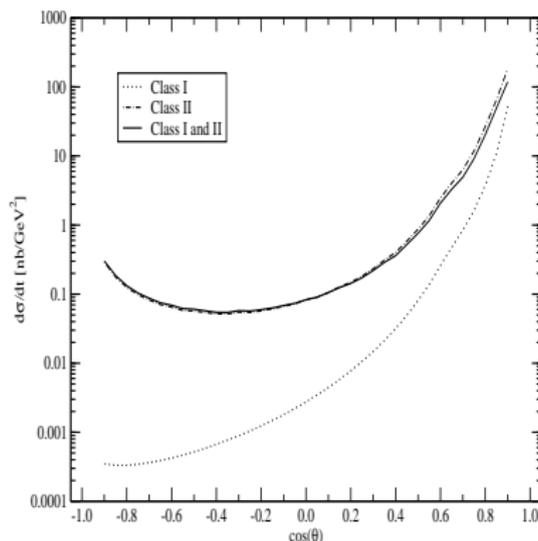
## The $\gamma p \rightarrow J/\Psi p$ Amplitude

Within the HSA the  $\gamma p \rightarrow J/\Psi p$  photoproduction amplitude is a convolution integral between the hard scattering amplitude and the soft distribution amplitudes w.r.t. the momentum fractions:

$$\mathcal{M} = \int_0^1 [dx] \int_0^1 [dy] \int_0^1 [dz] \phi_{J/\Psi}^\dagger(z_i) \phi_P^\dagger(y_i) T_H(x_i, y_i, z_i) \phi_P(x_i) .$$

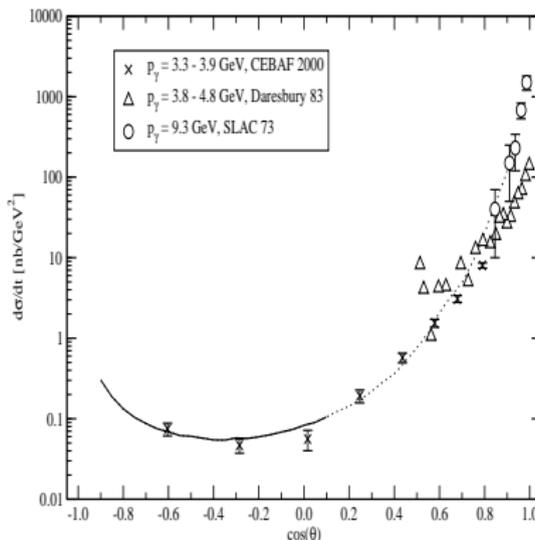
This means that the hard scattering amplitude is weighted with corresponding probability distribution amplitudes of each hadron participating in the scattering process

# $\Phi$ Production



Contribution of class I (dotted) and class II (dashed-dotted) graphs to our predictions for  $d\sigma_{\gamma p \rightarrow \Phi p}/dt$  at  $p_{\gamma}^{(lab)} = 9.3\text{GeV}$ . For comparison the complete calculation (class I and II) is also shown (solid line).

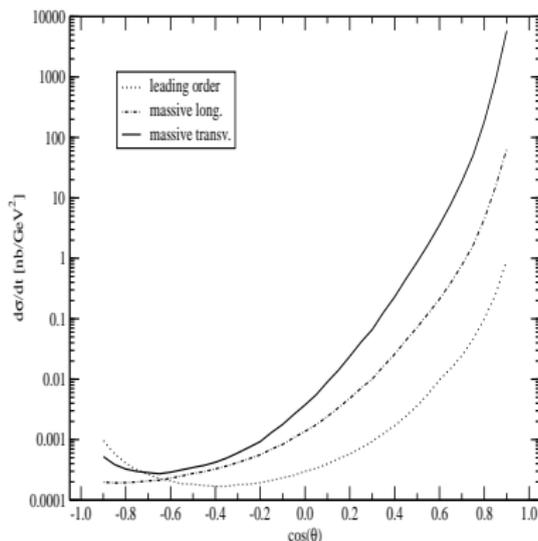
# $\Phi$ Production



Our predictions for  $d\sigma_{\gamma p \rightarrow \Phi p}/dt$  at  $p_\gamma^{(lab)} = 9.3$  GeV in comparison with SLAC, Daresbury and CEBAF data. (Daresbury and CEBAF scaled to  $p_\gamma^{(lab)} = 9.3$  GeV.)

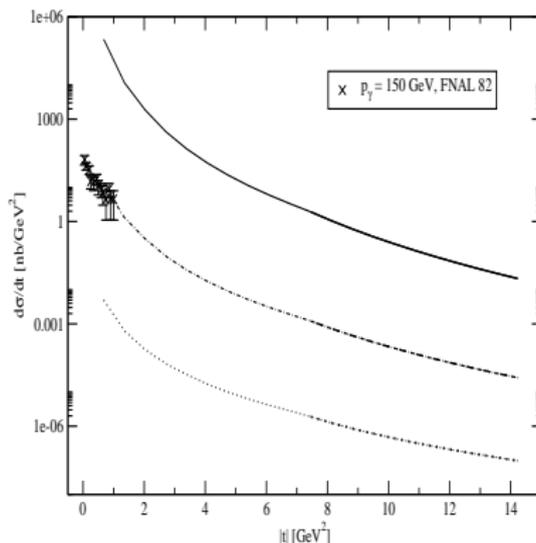
Solid part of the curve corresponds to  $\alpha_S \leq 0.5$ , for the rest  $0.5 < \alpha_S \leq 0.7$ .

# $J/\Psi$ Production



The influence of mass effects over the whole angular range. Calculations performed at  $p_{\gamma}^{(lab)} = 20\text{GeV}$ . Cross section for  $\lambda_{J/\psi} = 0$  without (dotted) and with (dashed-dotted)  $J/\psi$  mass is compared to cross section for  $\lambda_{J/\psi} = \pm 1$  (solid line).

# $J/\Psi$ Production



Our predictions for  $d\sigma_{\gamma p \rightarrow J/\Psi p}/dt$  at  $p_\gamma^{(lab)} = 150$  GeV in comparison with FNAL data. Cross section for  $\lambda_{J/\Psi} = 0$  without (dotted) and with (dashed-dotted)  $J/\Psi$  mass is compared to full cross section (solid line).

# Conclusions

- Good (indirect) reproduction of  $\Phi$  photoproduction data by our perturbative results.
- Photoproduction at large  $|t|$  dominated by class II graphs.
- For  $J/\psi$  the c-quark has been taken into account in the constituents' kinematics.
- Mass effects are crucial and raise the cross section nearly over the whole angular range.
- Finite c-mass  $\rightarrow$  longitudinally and transversely polarized  $J/\psi$ s can be produced.
- $\lambda_{J/\psi} = \pm 1$  amplitudes (which come as mass effects) even dominate.

Thank You!