

# Precision QCD in the LHC era

Daniel de Florian  
Dpto. de Física - FCEyN- UBA  
Argentina

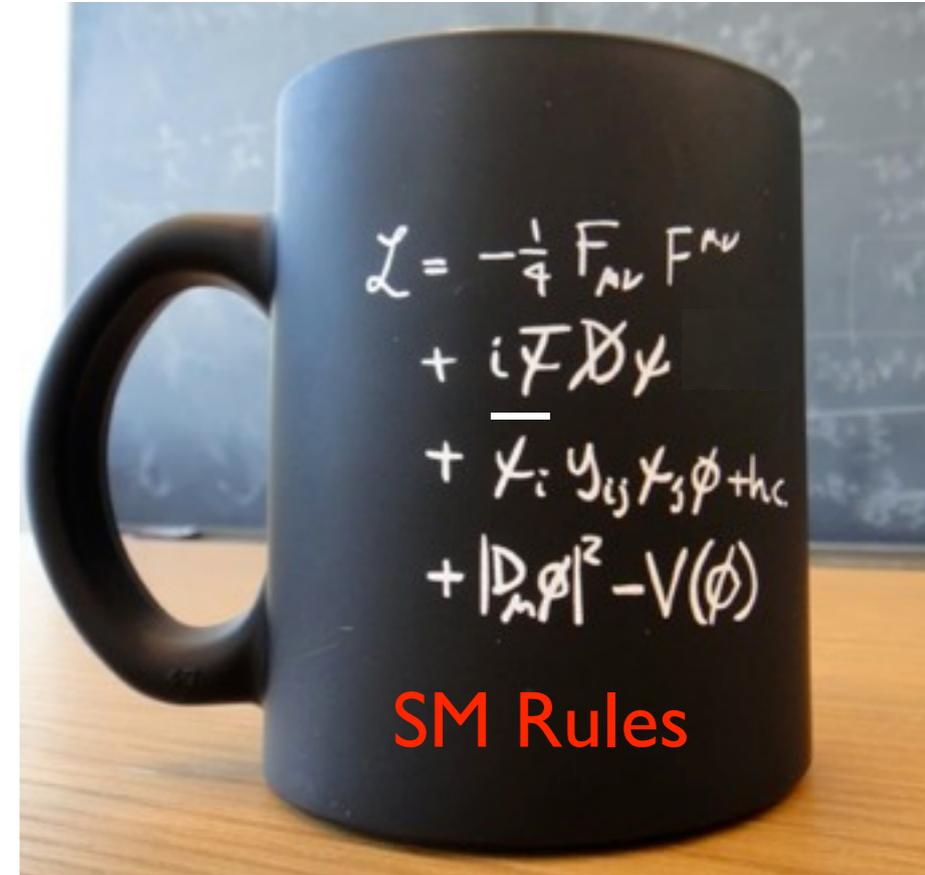


**DIS 2014**  
Warsaw, April 28

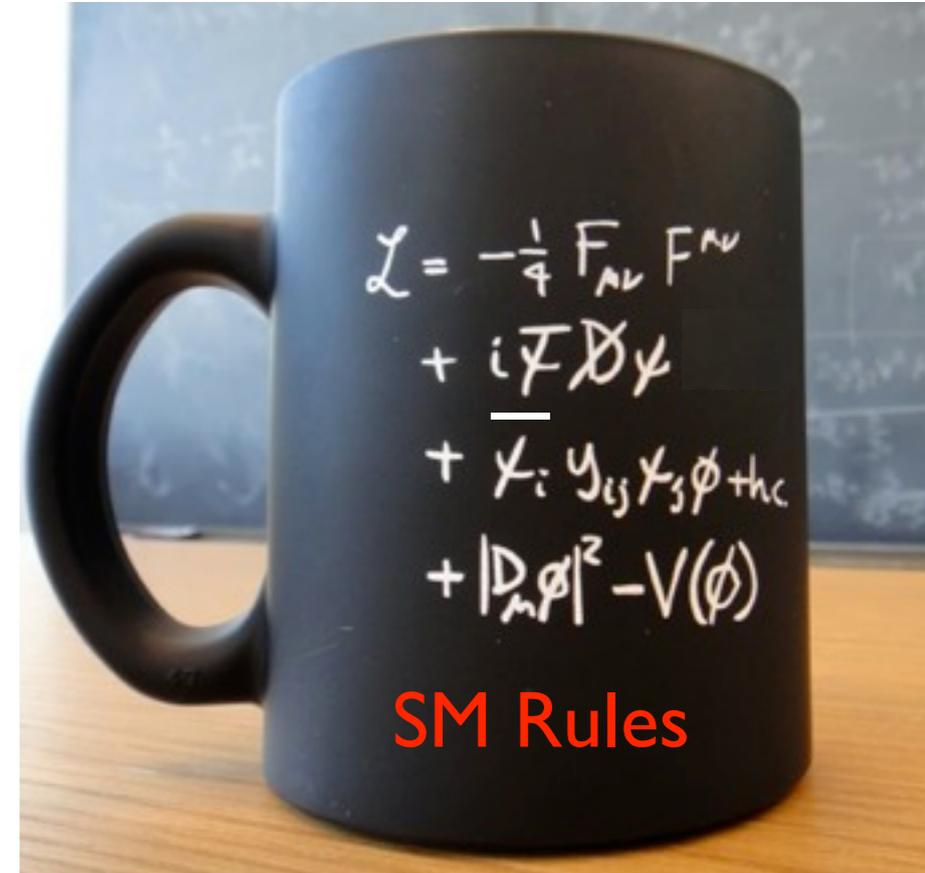
**DIS 2014**

- ▶ LHC was incredibly successful at 7 & 8 TeV
- ▶ Everything SM like (including Higgs)

- ▶ LHC was incredibly successful at 7 & 8 TeV
- ▶ Everything SM like (including Higgs)



- ▶ LHC was incredibly successful at 7 & 8 TeV
- ▶ Everything SM like (including Higgs)
- ▶ New physics might be in the detail
- ▶ Need to be precise on cross-sections and SM parameters



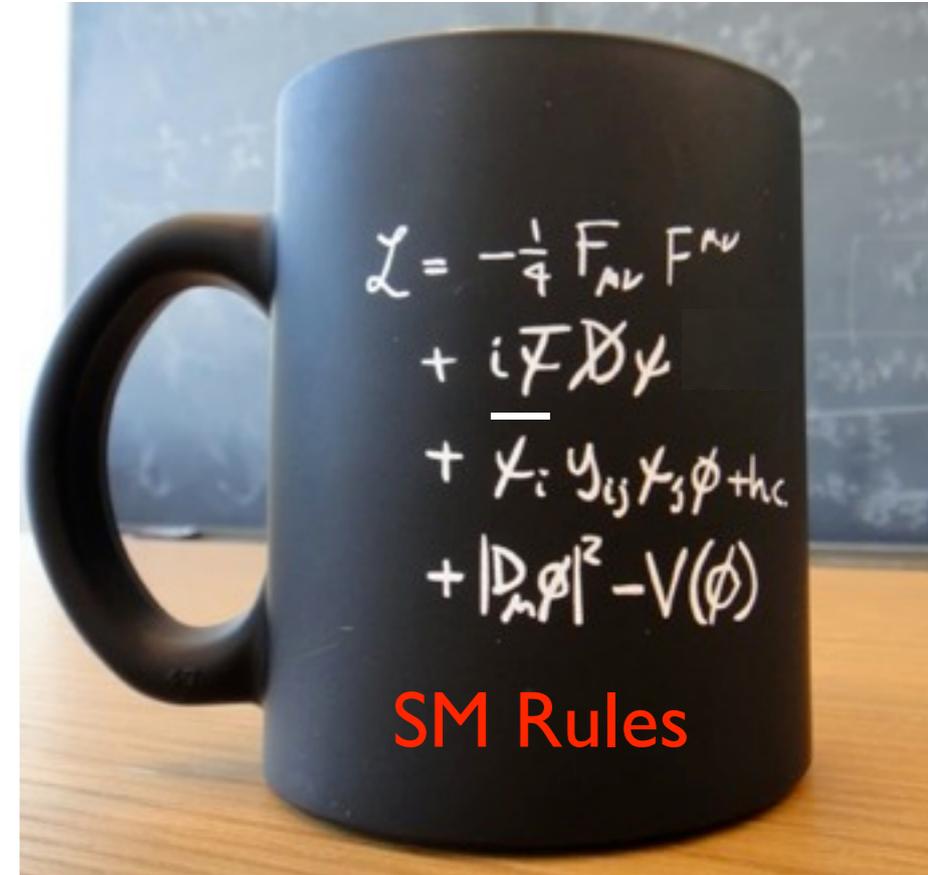
$$m_H, m_t, \alpha_s, \dots$$

Degrassi et al; Bezrukov et al;  
Alekhin, Djouadi, Moch; Masina  
(2012)

Vacuum stability in the SM at NNLO requires

$$m_H \geq 129.2 + 1.8 \times \left( \frac{m_t^{\text{pole}} - 173.2 \text{ GeV}}{0.9 \text{ GeV}} \right) - 0.5 \times \left( \frac{\alpha_s(M_Z) - 0.1184}{0.0007} \right) \pm 1.0 \text{ GeV}$$

- ▶ LHC was incredibly successful at 7 & 8 TeV
- ▶ Everything SM like (including Higgs)
- ▶ New physics might be in the detail
- ▶ Need to be precise on cross-sections and SM parameters



$$m_H, m_t, \alpha_s, \dots$$

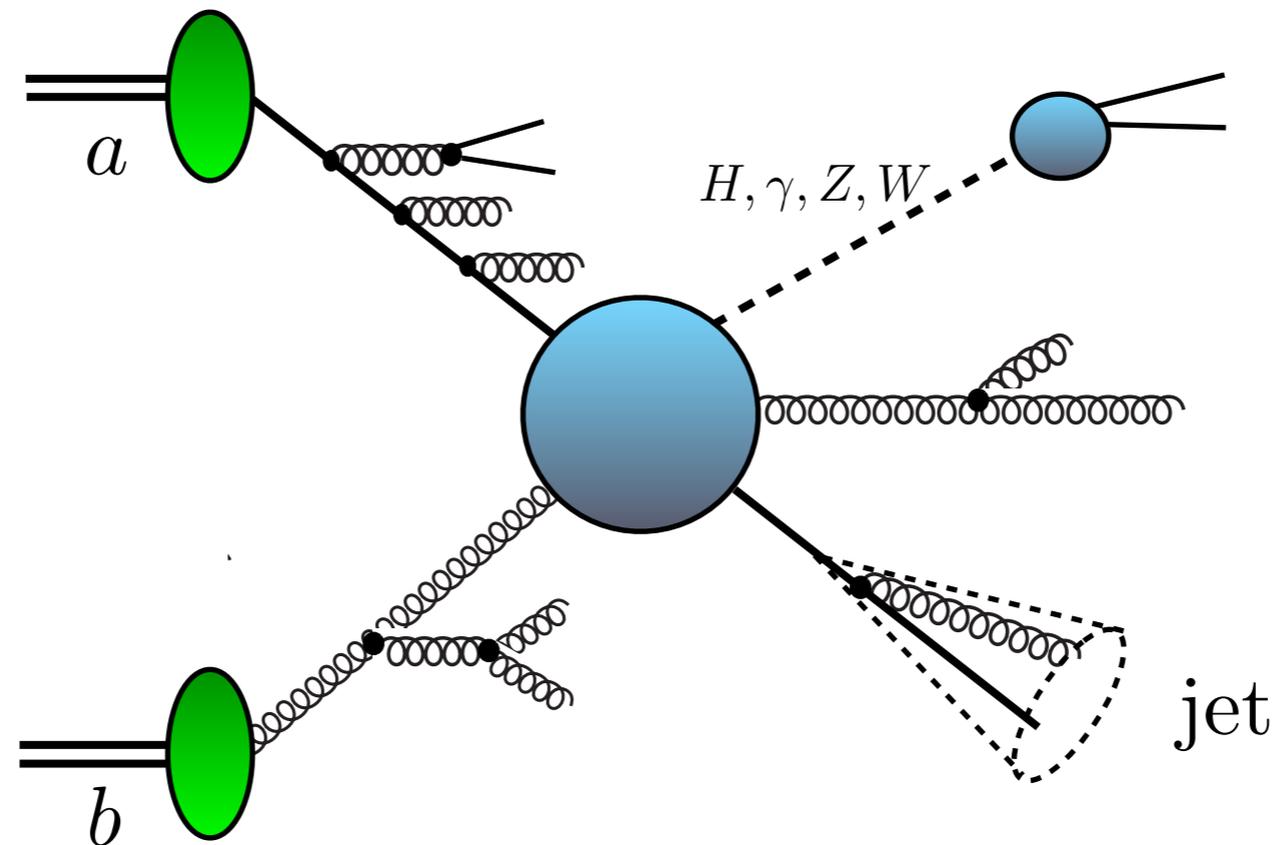
Degrassi et al; Bezrukov et al;  
Alekhin, Djouadi, Moch; Masina  
(2012)

Vacuum stability in the SM at NNLO requires

$$m_H \geq 129.2 + 1.8 \times \left( \frac{m_t^{\text{pole}} - 173.2 \text{ GeV}}{0.9 \text{ GeV}} \right) - 0.5 \times \left( \frac{\alpha_s(M_Z) - 0.1184}{0.0007} \right) \pm 1.0 \text{ GeV}$$

**This Talk**  
**Toolkit for precise TH predictions at the LHC**

► In the LHC era, QCD is everywhere!



non-perturbative parton distributions

$$d\sigma = \sum_{ab} \int dx_a \int dx_b f_a(x_a, \mu_F^2) f_b(x_b, \mu_F^2) \times d\hat{\sigma}_{ab}(x_a, x_b, Q^2, \alpha_s(\mu_R^2)) + \mathcal{O}\left(\left(\frac{\Lambda}{Q}\right)^m\right)$$

perturbative partonic cross-section

Partonic cross-section: expansion in  $\alpha_s(\mu_R^2) \ll 1$   $d\hat{\sigma} = \alpha_s^n d\hat{\sigma}^{(0)} + \alpha_s^{n+1} d\hat{\sigma}^{(1)} + \dots$

► Require precision for perturbative and non-perturbative contribution

# PDFs

- ▶ Several groups provide pdf fits + uncertainties
- ▶ Differ by: data input, TH/bias, HQ treatment, coupling, etc

set	H.O.	data	$\alpha_s(M_Z)$ @NNLO	uncertainty	HQ	Comments
MSTW 2008	NNLO	DIS+DY+Jets	0.1171	Hessian (dynamical tolerance)	GM-VFN (ACOT+TR')	old HERA DIS
CT10	NNLO	DIS+DY+Jets	0.118	Hessian (dynamical tolerance)	GM-VFN (SACOT-X)	New HERA DIS
NNPDF	NNLO	DIS+DY+Jets +LHC	0.1174	Monte Carlo	GM-VFN (FONLL)	New HERA DIS
ABKM	NNLO	DIS+DY(f.t.) +DY-tT(LHC)	0.1132	Hessian	FFN BMSN	New HERA DIS
(G)JR	NNLO	DIS+DY(f.t.)+ some jet	0.1124	Hessian	FFN (VFN massless)	valence like input pdfs
HERA PDF	NNLO	only DIS HERA	0.1176	Hessian	GM-VFN (ACOT+TR')	Latest HERA DIS

# PDFs

- ▶ Several groups provide pdf fits + uncertainties
- ▶ Differ by: data input, TH/bias, HQ treatment, coupling, etc



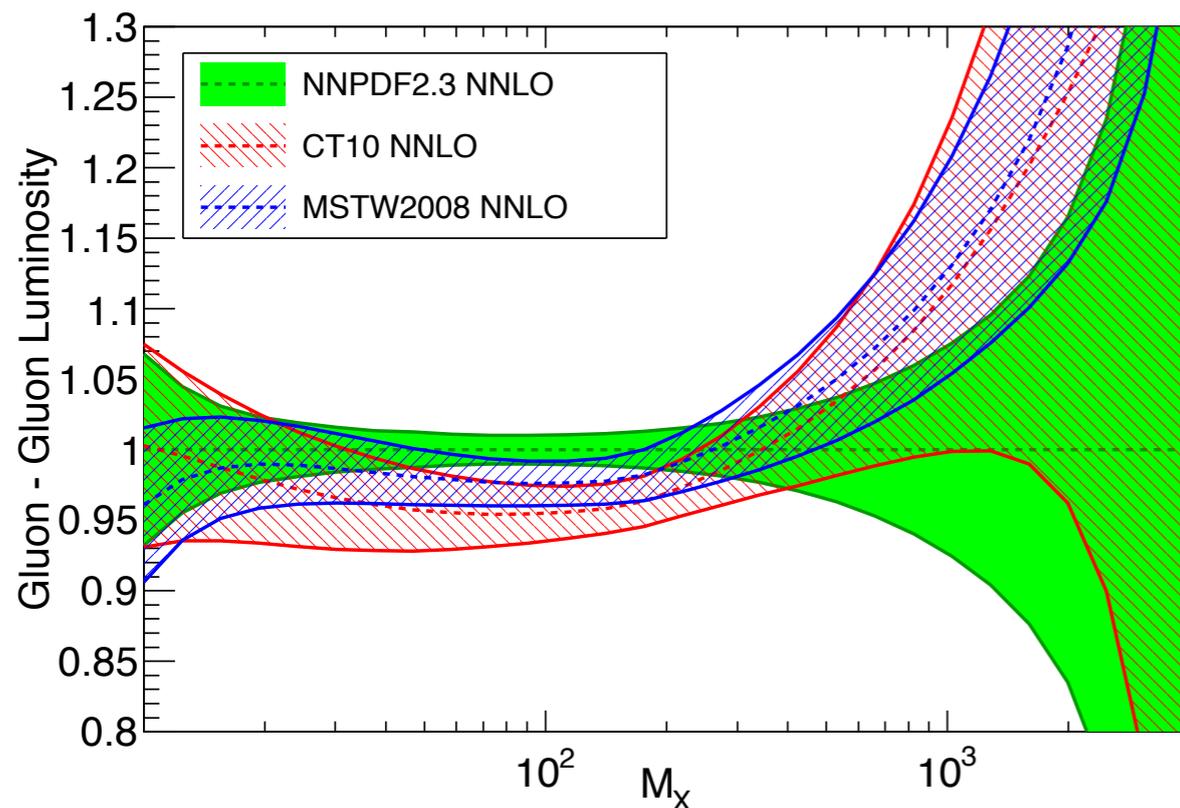
up to 5% ! >15% in Higgs cross section

set	H.O.	data	$\alpha_s(M_Z)$ @NNLO	uncertainty	HQ	Comments
MSTW 2008	NNLO	DIS+DY+Jets	0.1171	Hessian (dynamical tolerance)	GM-VFN (ACOT+TR')	old HERA DIS
CT10	NNLO	DIS+DY+Jets	0.118	Hessian (dynamical tolerance)	GM-VFN (SACOT-X)	New HERA DIS
NNPDF	NNLO	DIS+DY+Jets +LHC	0.1174	Monte Carlo	GM-VFN (FONLL)	New HERA DIS
ABKM	NNLO	DIS+DY(f.t.) +DY-tT(LHC)	0.1132	Hessian	FFN BMSN	New HERA DIS
(G)JR	NNLO	DIS+DY(f.t.)+ some jet	0.1124	Hessian	FFN (VFN massless)	valence like input pdfs
HERA PDF	NNLO	only DIS HERA	0.1176	Hessian	GM-VFN (ACOT+TR')	Latest HERA DIS

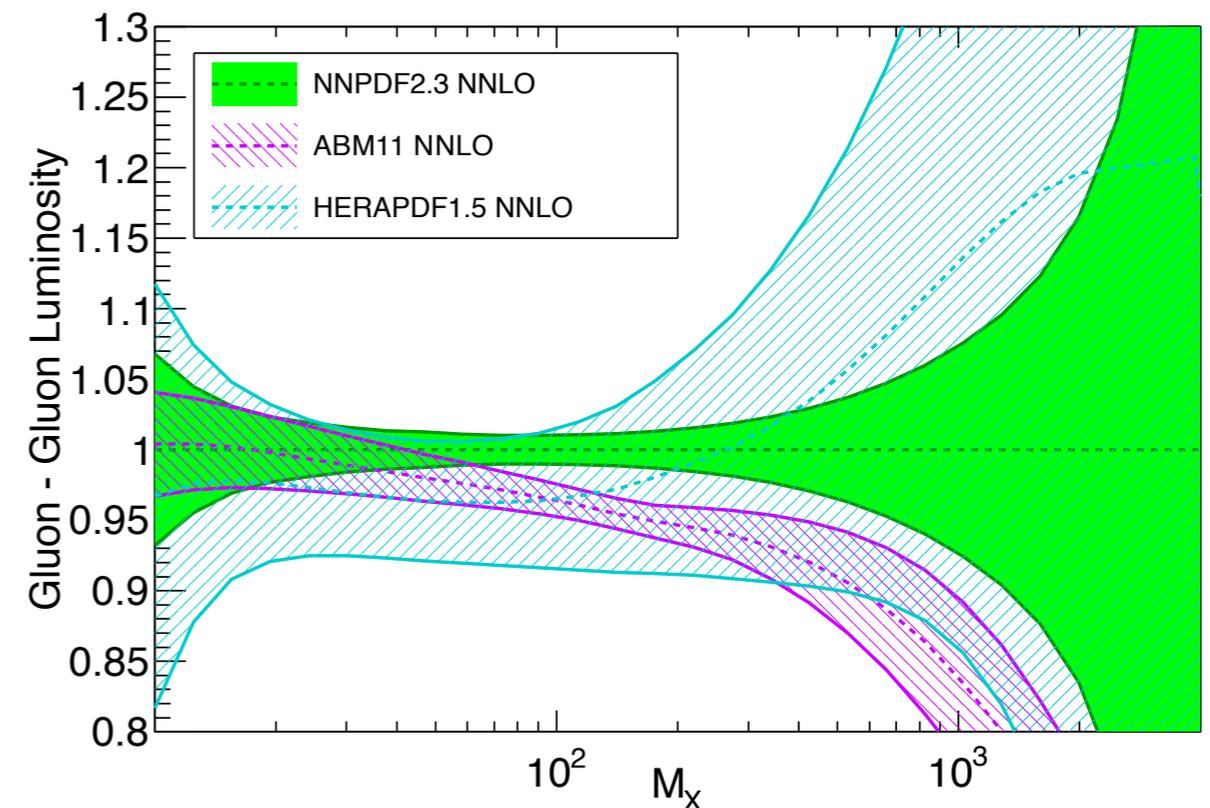
$$\mathcal{L}_{ij}(\tau \equiv M_X^2/S) = \frac{1}{S} \int_{\tau}^1 \frac{dx}{x} f_i(x, M_X^2) f_j(\tau/x, M_X^2)$$

## gluon-gluon

LHC 8 TeV - Ratio to NNPDF2.3 NNLO -  $\alpha_s = 0.118$



LHC 8 TeV - Ratio to NNPDF2.3 NNLO -  $\alpha_s = 0.118$

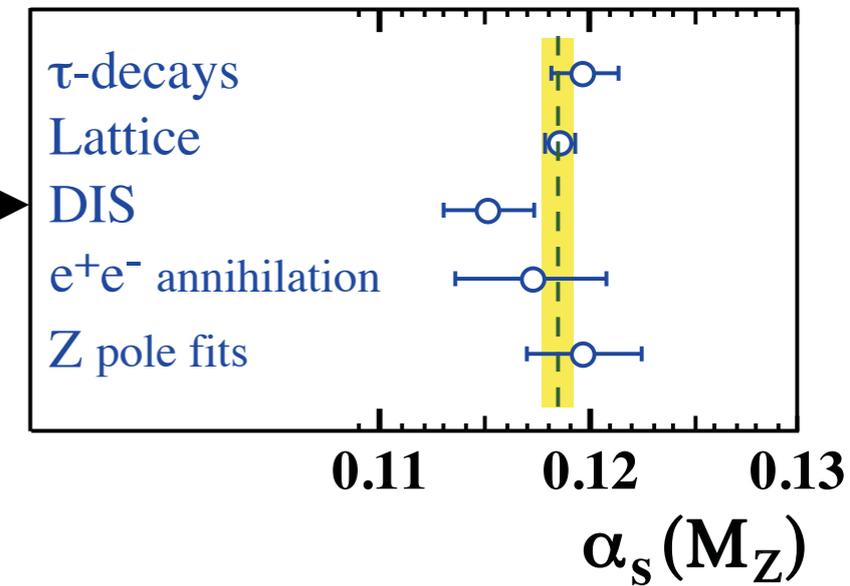


- ▶ Good agreement for global fits but deviations as large as uncertainties
- ▶ Larger differences with “non-global” results
- ▶ 2x larger uncertainties for gluon

► One main issue is the coupling constant

PDG S. Bethke

$$\alpha_s(M_Z) = 0.1184 \pm 0.0007$$



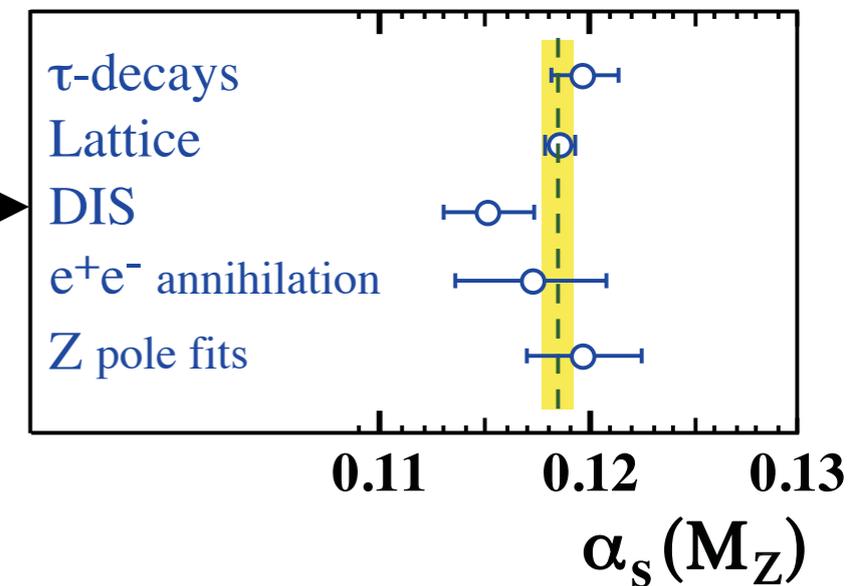
• Optimistic value for the uncertainty at the LHC

• DIS (PDFS) not well covered : some experiments pull value down

- ▶ One main issue is the coupling constant

PDG S. Bethke

$$\alpha_s(M_Z) = 0.1184 \pm 0.0007$$



- Optimistic value for the uncertainty at the LHC
- DIS (PDFS) not well covered : some experiments pull value down

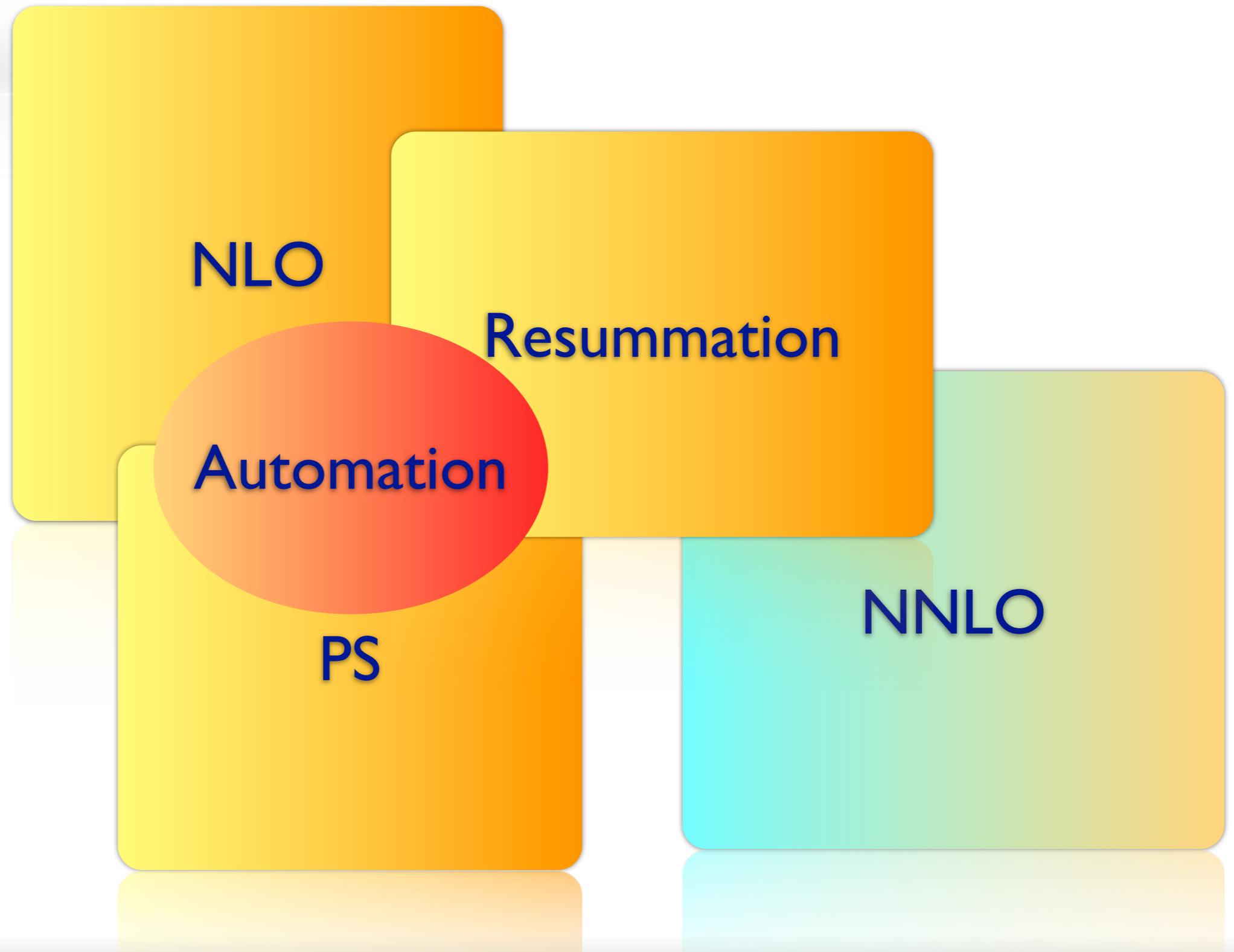
## **PDF4LHC recommendation**

- ▶ Compute pdfs uncertainties using MSTW & CT & NNPDF (68%cl)
- ▶ Obtain the envelope of all bands and use

$$\Delta\alpha_s(M_Z) = \pm 0.0012 (\pm 0.002) \text{ at } 68\% (90\%) \text{ c.l.}$$

- ▶ Precise LHC data will have important effect on validation & improvement

# The perturbative toolkit for precision at colliders



# The NLO revolution

## Why NLO?

- ▶ Accurate Theoretical Predictions
  - shape and normalization
  - first error estimate
- ▶ Large Corrections : check PT Higgs
- ▶ Opening of new channels
- ▶ Effect of extra radiation
  - jet algorithm dependence

Amazing progress in the last few years

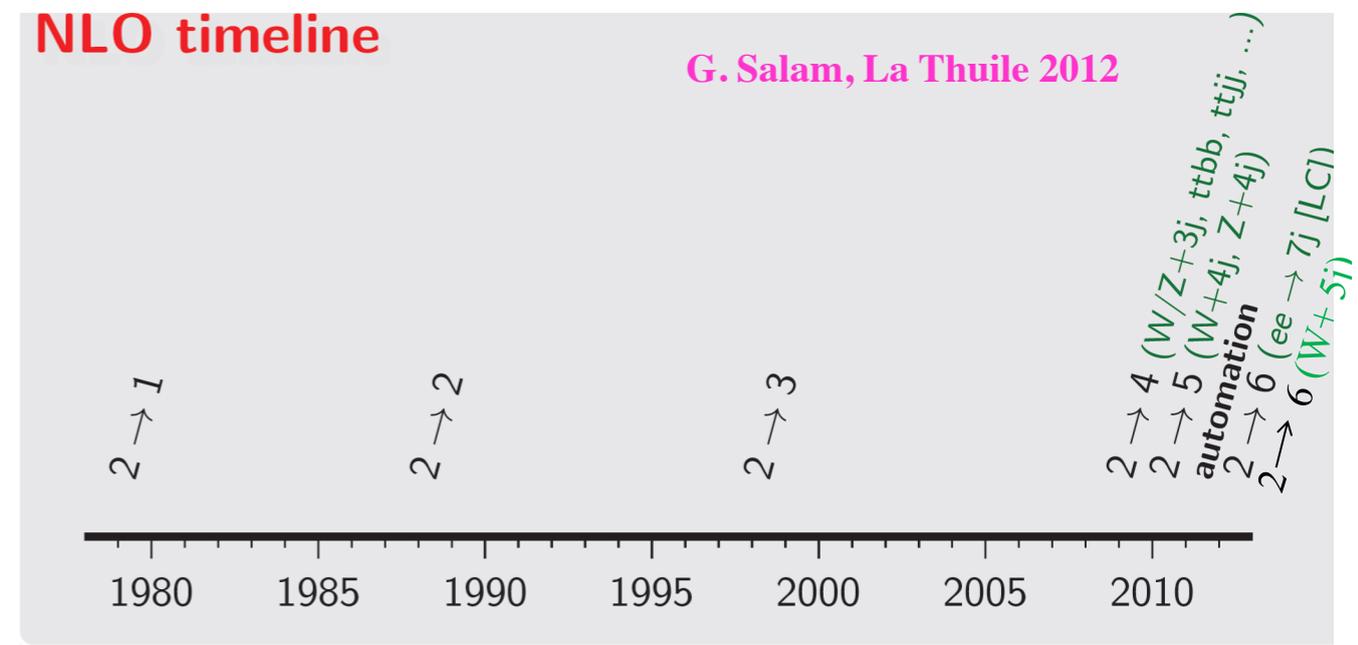
# The NLO revolution

## Why NLO?

- ▶ Accurate Theoretical Predictions
  - shape and normalization
  - first error estimate
- ▶ Large Corrections : check PT **Higgs**
- ▶ Opening of new channels
- ▶ Effect of extra radiation
  - jet algorithm dependence

Amazing progress in the last few years

Large multiplicities  
relevant for LHC



# Revolution in calculation of 1-loop amplitudes

Bottleneck in the virtual contribution : **large multiplicities**

$$\text{Sun diagram} = \sum_i d_i \text{Box} + \sum_i c_i \text{Triangle} + \sum_i b_i \text{Bubble} + \sum_i a_i \text{Circle} + \frac{x}{y}$$

## Feynmanian approach

 Improvements in decomposition and reduction

Denner, Dittmaier; Pozzorini; Binoth, Guillet, Heinrich, Pilon, Schubert + many others

## Unitarian approach

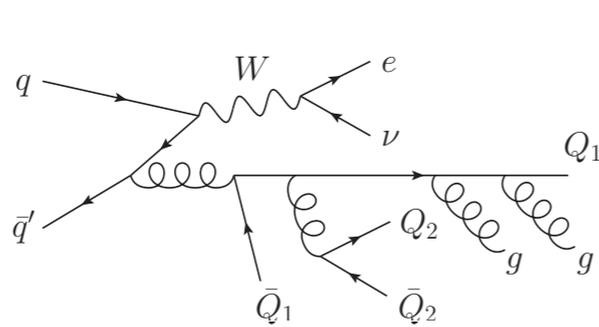
 Use multi-particle **cuts** from generalized **unitarity**

Bern, Dixon, Dunbar, Kosower; Britto, Cachazo, Feng; Mastrolia; Forde; Badger; Ellis, Giele, Kunszt, Melnikov + many others

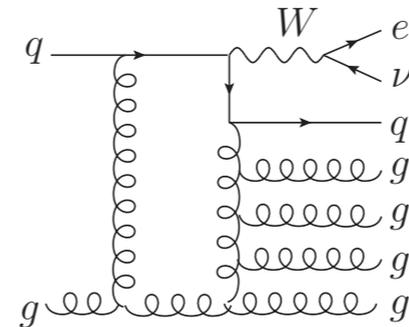
**OPP** Ossola, Papadopoulos, Pittau    decomposition at the *integrand* level

# A very recent example :W+5 jets !!

BlackHat Collaboration, Z.Bern et al

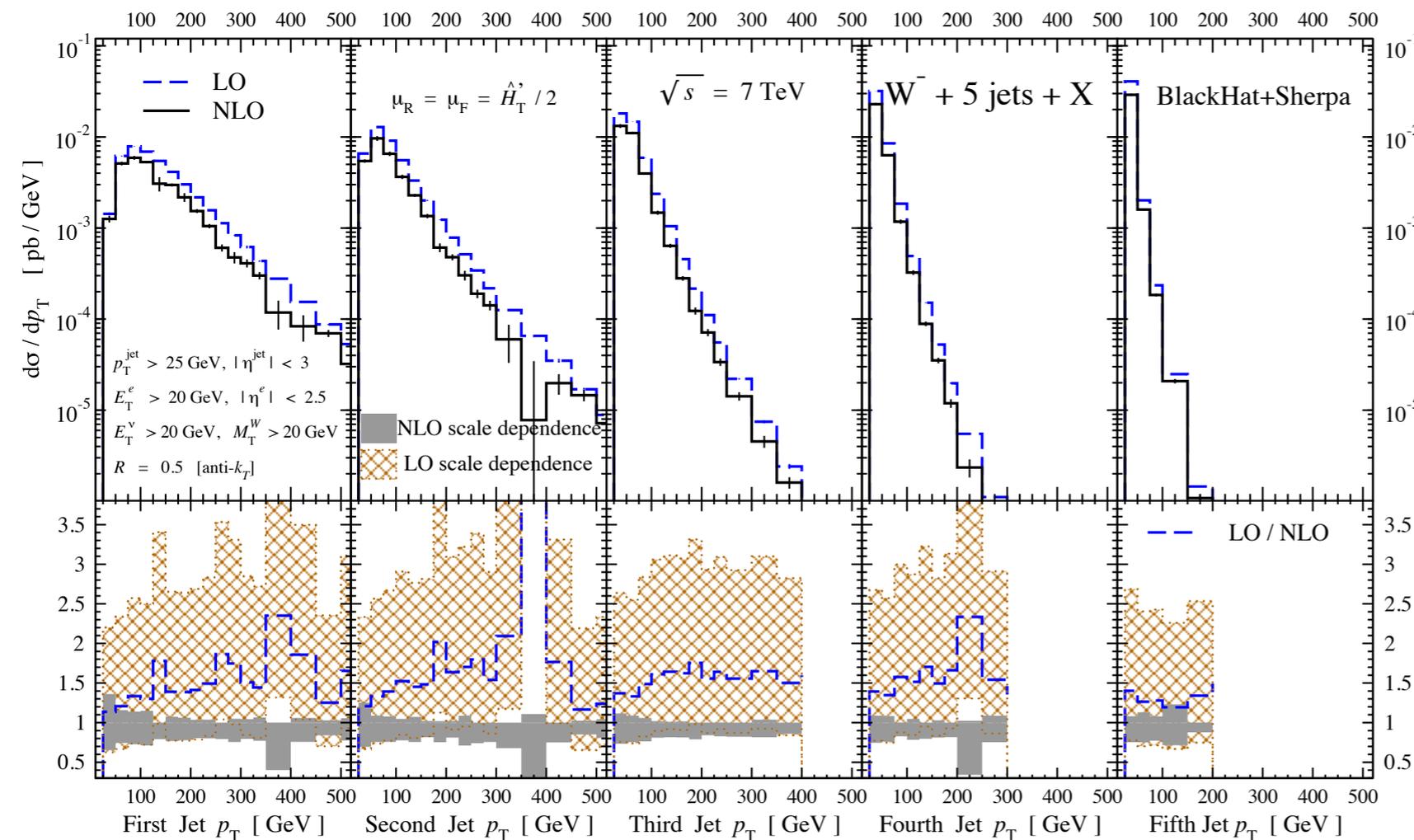


Real 2 → 8 SHERPA



Virtual 2 → 7 BlackHat

Dynamical Scale choice  $\mu_R = \mu_F = \frac{\hat{H}'_T}{2} \equiv \frac{1}{2} \sum_m p_T^m + E_T^W$



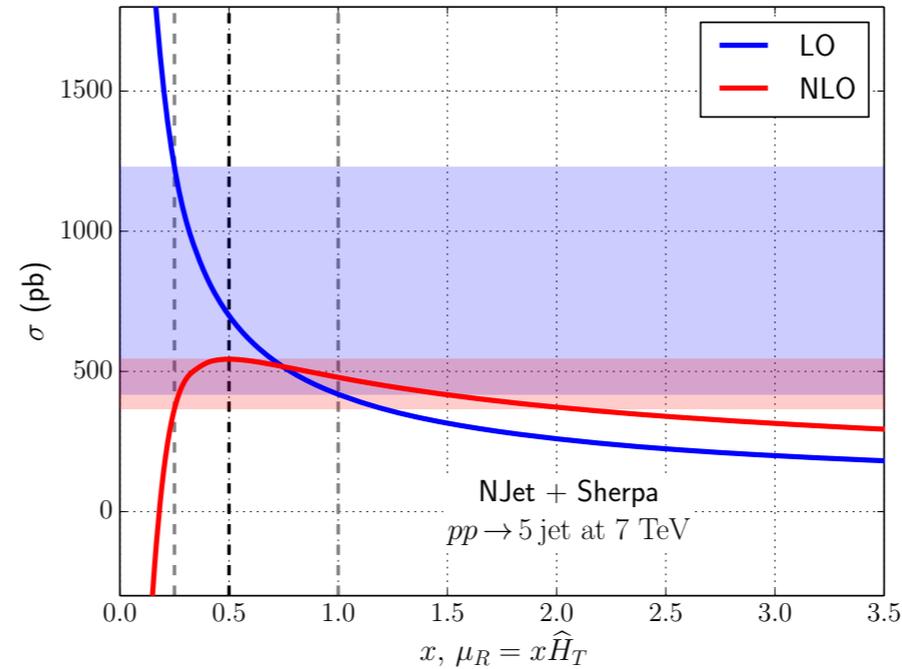
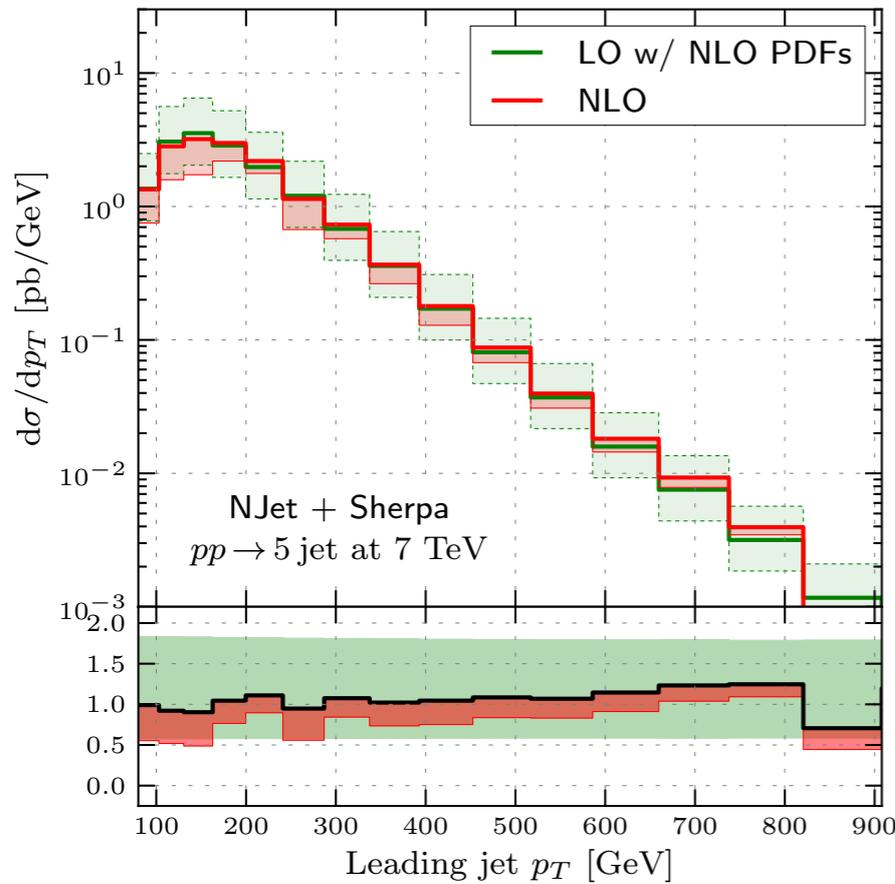
► Dramatic reduction in scale dependence (~20%)

► Up to 50% correction (non-trivial in shape)

# Multi-jet production

$pp \rightarrow 5 \text{ jets at NLO}$

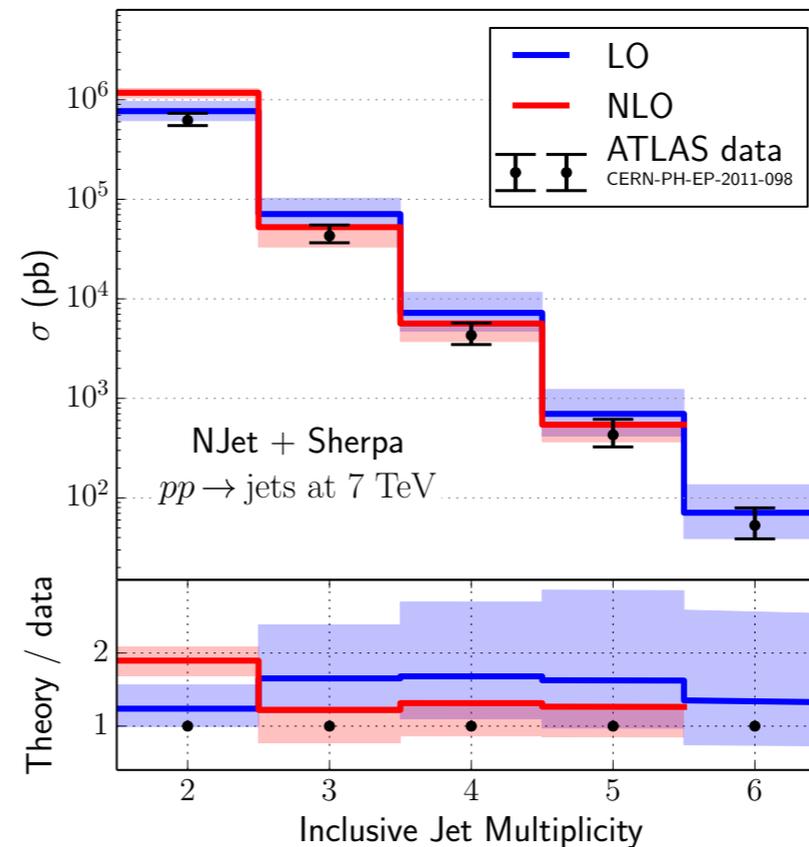
NJet+Sherpa (Badger, Biedermann, Uwer, Yundin)



$$\hat{H}_T = \sum_{i=1}^{N_{\text{parton}}} p_{T,i}^{\text{parton}}$$

► Better stability

► NLO in very good agreement with data!



# Experimenter's wish-list

Process ( $V \in \{Z, W, \gamma\}$ )	Comments
Calculations completed since Les Houches 2005	
1. $pp \rightarrow VV\text{jet}$	$WW\text{jet}$ completed by Dittmaier/Kallweit/Uwer [4,5]; Campbell/Ellis/Zanderighi [6]. $ZZ\text{jet}$ completed by
2. $pp \rightarrow \text{Higgs}+2\text{jets}$	Binoth/Gleisberg/Karg/Kauer/Sanguinetti [7] NLO QCD to the $gg$ channel completed by Campbell/Ellis/Zanderighi [8]; NLO QCD+EW to the VBF channel completed by Ciccolini/Denner/Dittmaier [9,10]
3. $pp \rightarrow VVV$	$ZZZ$ completed by Lazopoulos/Melnikov/Petriello [11] and $WWZ$ by Hankele/Zeppenfeld [12] (see also Binoth/Ossola/Papadopoulos/Pittau [13])
4. $pp \rightarrow t\bar{t}b\bar{b}$	relevant for $t\bar{t}H$ computed by Bredenstein/Denner/Dittmaier/Pozzorini [14,15] and Bevilacqua/Czakon/Papadopoulos/Pittau/Worek [16]
5. $pp \rightarrow V+3\text{jets}$	calculated by the Blackhat/Sherpa [17] and Rocket [18] collaborations
Calculations remaining from Les Houches 2005	
6. $pp \rightarrow t\bar{t}+2\text{jets}$	relevant for $t\bar{t}H$ computed by Bevilacqua/Czakon/Papadopoulos/Worek [19]
7. $pp \rightarrow VVb\bar{b}$ ,	relevant for VBF $\rightarrow H \rightarrow VV, t\bar{t}H$
8. $pp \rightarrow VV+2\text{jets}$	relevant for VBF $\rightarrow H \rightarrow VV$ VBF contributions calculated by (Bozzi/Jäger/Oleari/Zeppenfeld [20–22])
NLO calculations added to list in 2007	
9. $pp \rightarrow b\bar{b}b\bar{b}$	$q\bar{q}$ channel calculated by Golem collaboration [23]
NLO calculations added to list in 2009	
10. $pp \rightarrow V+4\text{ jets}$	top pair production, various new physics signatures
11. $pp \rightarrow Wb\bar{b}j$	top, new physics signatures
12. $pp \rightarrow t\bar{t}t\bar{t}$	various new physics signatures
Calculations beyond NLO added in 2007	
13. $gg \rightarrow W^*W^* \mathcal{O}(\alpha^2\alpha_s^3)$	backgrounds to Higgs
14. NNLO $pp \rightarrow t\bar{t}$	normalization of a benchmark process
15. NNLO to VBF and $Z/\gamma+\text{jet}$	Higgs couplings and SM benchmark
Calculations including electroweak effects	
16. NNLO QCD+NLO EW for $W/Z$	precision calculation of a SM benchmark

# Experimenter's wish-list

Process ( $V \in \{Z, W, \gamma\}$ )	Comments
Calculations completed since Les Houches 2005	
1. $pp \rightarrow VV\text{jet}$	$WW\text{jet}$ completed by Dittmaier/Kallweit/Uwer [4,5]; Campbell/Ellis/Zanderighi [6]. $ZZ\text{jet}$ completed by
2. $pp \rightarrow \text{Higgs}+2\text{jets}$	Binoth/Gleisberg/Karg/Kauer/Sanguinetti [7] NLO QCD to the $gg$ channel completed by Campbell/Ellis/Zanderighi [8]; NLO QCD+EW to the VBF channel completed by Ciccolini/Denner/Dittmaier [9,10]
3. $pp \rightarrow VVV$	$ZZZ$ completed by Lazopoulos/Melnikov/Petriello [11] and $WWZ$ by Hankel-Beppel/Zeppenfeld [12] (see also Binoth/Oleari/Papadopoulos/Pittau [13])
4. $pp \rightarrow t\bar{t}b\bar{b}$	relevant for $t\bar{t}H$ computed by Bredenstein/Denner/Dittmaier/Bozzorini [14,15] and Pavlac/Czakon/Papadopoulos/Pittau/Worek [16]
5. $pp \rightarrow V+3\text{jets}$	calculated by the Blackhat/Sherpa [17] and Rescale [18] collaborations
Calculations remaining from Les Houches 2005	
6. $pp \rightarrow t\bar{t}+2\text{jets}$	relevant for $t\bar{t}H$ computed by Pavlac/Czakon/Papadopoulos/Worek [19]
7. $pp \rightarrow VVb\bar{b}$ ,	relevant for VBF $\rightarrow H \rightarrow VV$ , $t\bar{t}H$
8. $pp \rightarrow VV+2\text{jets}$	relevant for VBF $\rightarrow H \rightarrow VV$ VBF contributions calculated by (Bozzi/Jäger/Oleari/Zeppenfeld [20–22])
NLO calculations added to list in 2007	
9. $pp \rightarrow b\bar{b}b\bar{b}$	$q\bar{q}$ channel calculated by Golem collaboration [23]
NLO calculations added to list in 2009	
10. $pp \rightarrow V+4\text{ jets}$	top pair production, various new physics signatures
11. $pp \rightarrow Wb\bar{b}j$	top, new physics signatures
12. $pp \rightarrow t\bar{t}t\bar{t}$	various new physics signatures
Calculations beyond NLO added in 2007	
13. $gg \rightarrow W^*W^* \mathcal{O}(\alpha^2\alpha_s^3)$	backgrounds to Higgs
14. NNLO $pp \rightarrow t\bar{t}$	normalization of a benchmark process
15. NNLO to VBF and $Z/\gamma+\text{jet}$	Higgs couplings and SM benchmark
Calculations including electroweak effects	
16. NNLO QCD+NLO EW for $W/Z$	precision calculation of a SM benchmark

► Final goal: Really automatic NLO calculations

zero cost for humans

- Specify the process (input card)
- Input parameters
- Define final cuts

► Automatic NLO calculation “conceptually” solved

- in a few years a number of codes (among others)

Blackhat+Sherpa

GoSam + Sherpa/MadGraph

MadLoop+MadFKS

CutTools

OpenLoops+Sherpa

- ✓ compete on precision, flexibility, speed, stability, ...
- ✓ many features : uncertainties, ...

**Best solution still to emerge, but not more NLO wish-list, do it yourself!**

► Individual calculations still relevant! ✓ open the way to new methods

# Resummation

● QCD based on convergence of perturbative expansion

$$\sigma = \mathcal{C}_0 + \alpha_s \mathcal{C}_1 + \alpha_s^2 \mathcal{C}_2 + \alpha_s^3 \mathcal{C}_3 + \dots$$

requires  $\alpha_s \ll 1$  ,  $\mathcal{C}_n \sim \mathcal{O}(1)$

In the boundaries of phase space  $\longrightarrow$  soft and collinear emission

unbalance cancellation of infrared singularities  
between real and virtual contributions

● Convergence spoiled when two scales are very different  $L = \left| \log \frac{E_1}{E_2} \right| \gg 1$

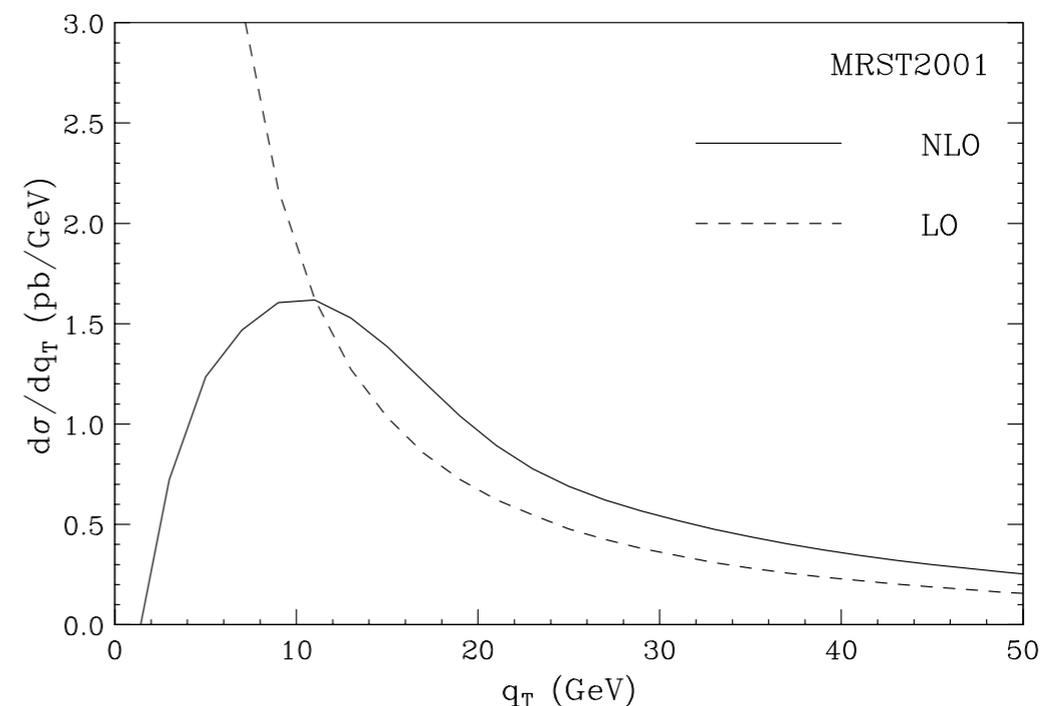
$$\mathcal{C}_m \sim L^n \quad n \leq 2m$$

low transverse momentum  $\log \frac{q_T}{Q}$

Higgs

$$\text{LO: } \frac{d\sigma}{dq_T} \rightarrow +\infty \text{ as } q_T \rightarrow 0$$

$$\text{NLO: } \frac{d\sigma}{dq_T} \rightarrow -\infty \text{ as } q_T \rightarrow 0$$



# ► Resummation achieved by exponentiation of large logs in Sudakov factor

## Most recently: jet vetos

### Jet veto in Higgs @ NNLL

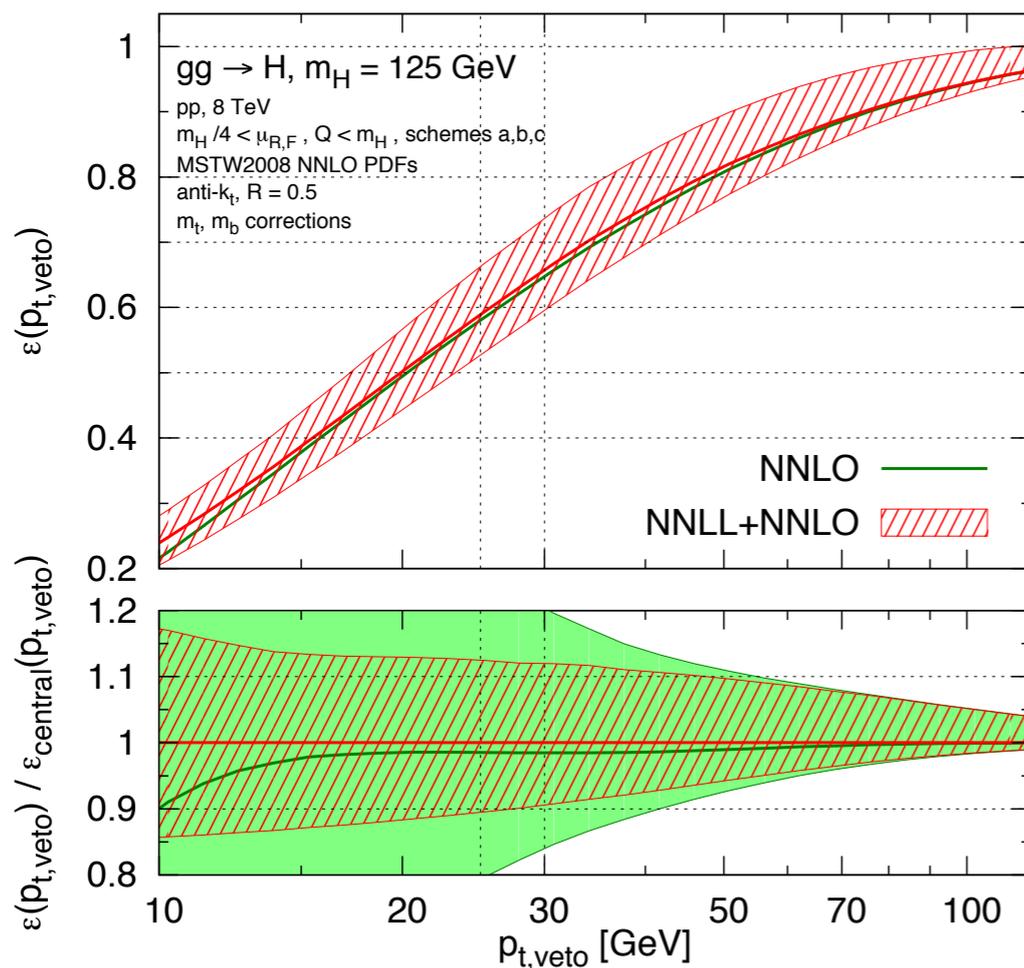
Banfi, Monni, Salam, Zanderighi (2012)

Banfi, Monni, Zanderighi (2013)

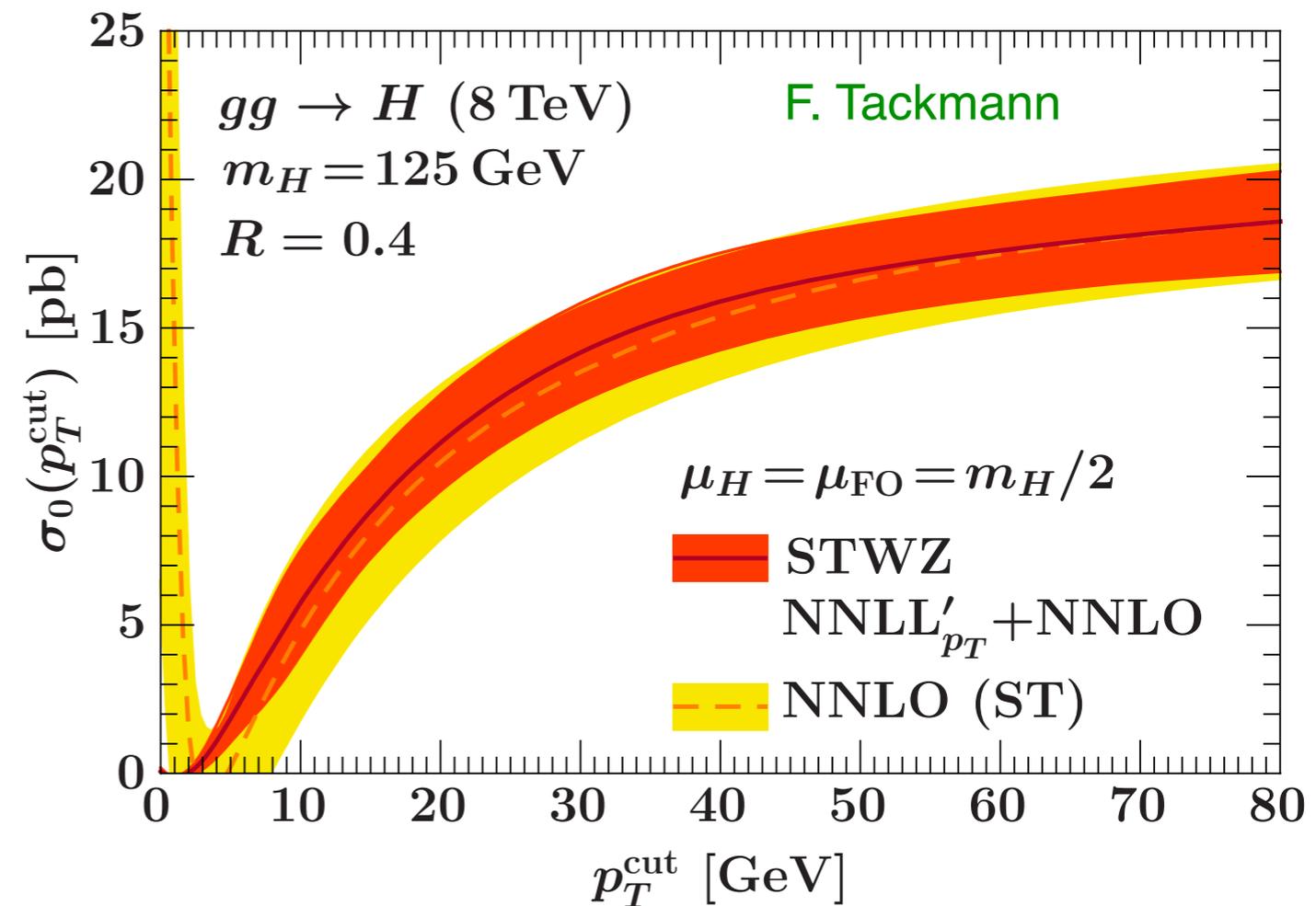
► Reduction in uncertainty

► Validation of tools

Stewart, Tackmann, Walsh, Zuberi (2013)



efficiency 0-jet “QCD”



cross section 0-jet “SCET”

# ► Resummation achieved by exponentiation of large logs in Sudakov factor

## Most recently: jet vetos

### Jet veto in Higgs @ NNLL

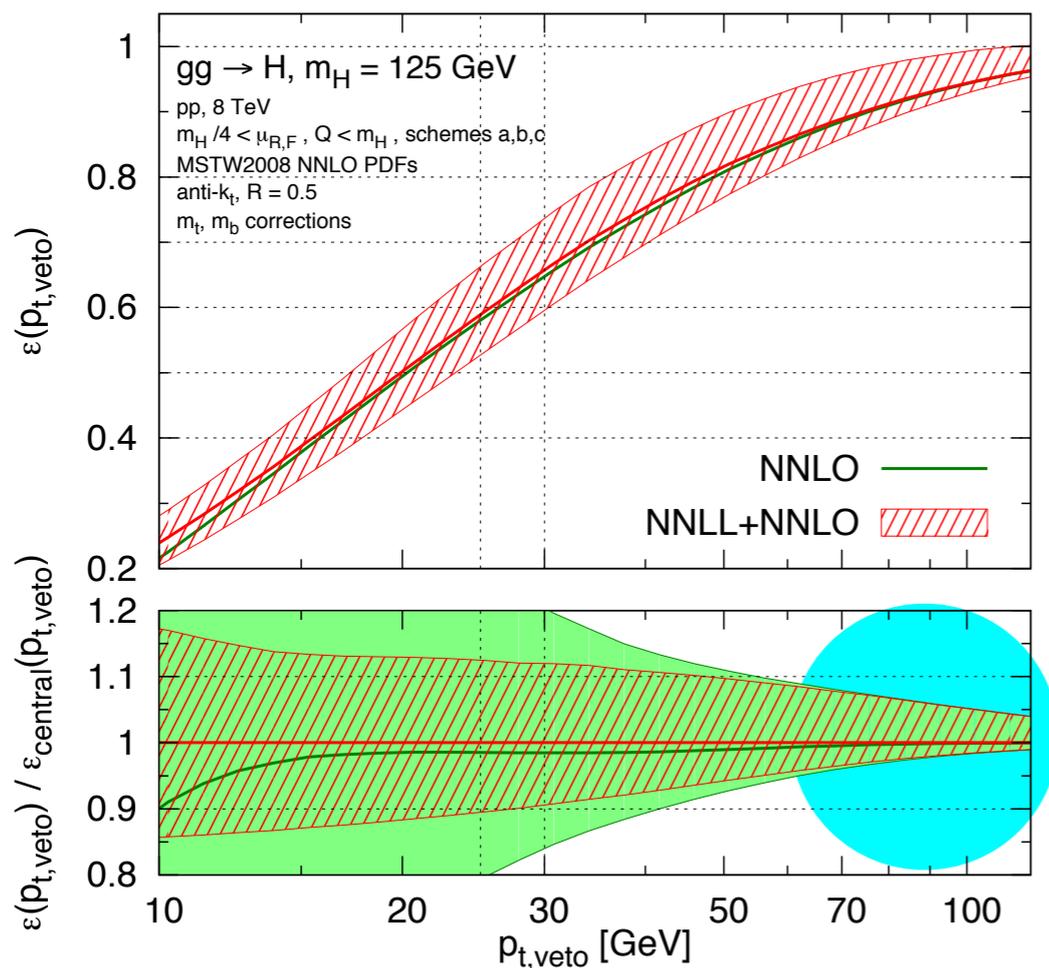
Banfi, Monni, Salam, Zanderighi (2012)

Banfi, Monni, Zanderighi (2013)

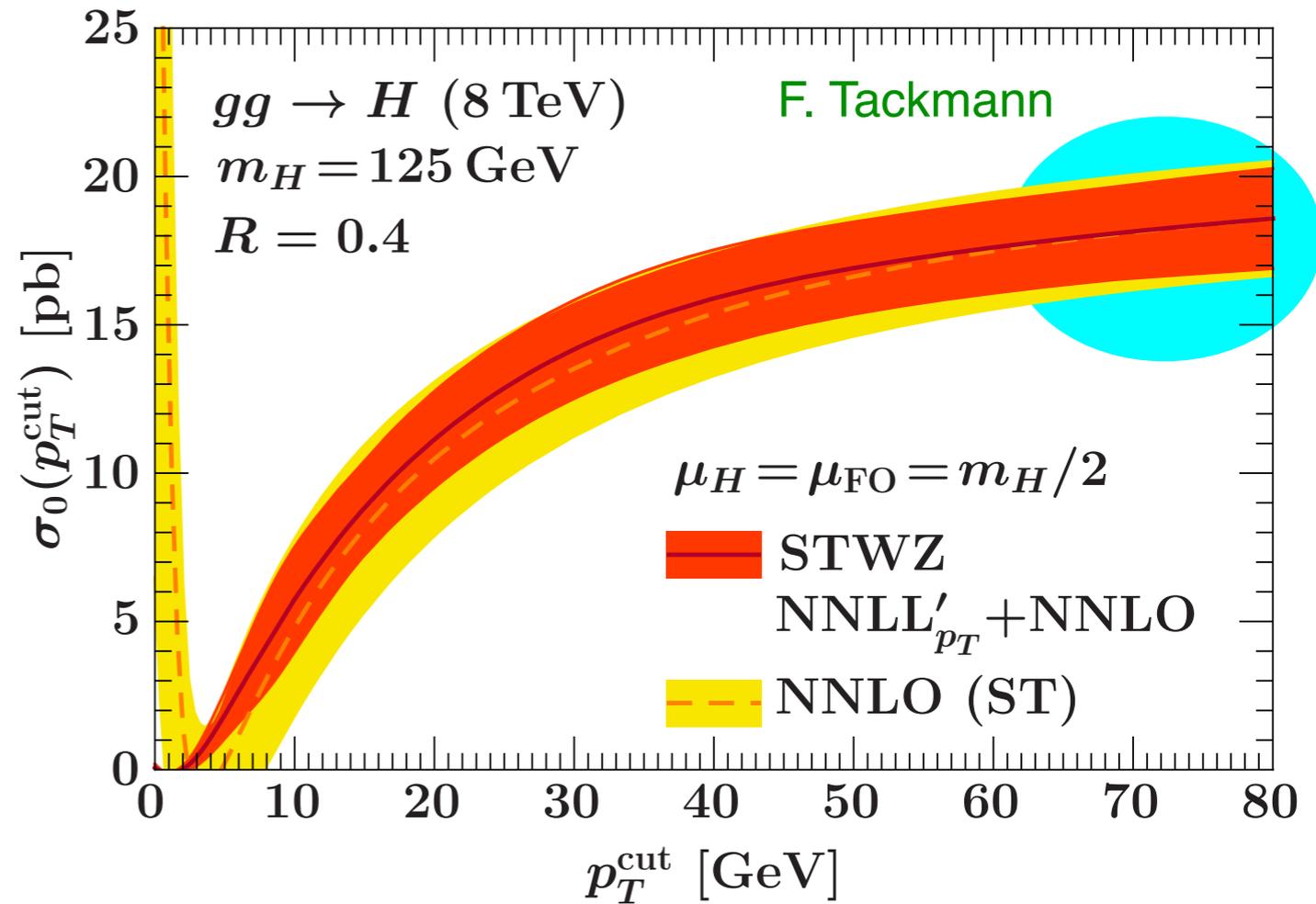
► Reduction in uncertainty

► Validation of tools

Stewart, Tackmann, Walsh, Zuberi (2013)



efficiency 0-jet “QCD”



cross section 0-jet “SCET”

Recover fixed order at large transverse momentum

# Merging NLO with Parton Showers

- ▶ Resummation to NLL accuracy + realistic final states
- ▶ Allow to carry NLO precision to all aspects of experimental analysis

 MC@NLO [Frixione, Webber](#)       POWHEG [Nason; Frixione, Nason, Oleari](#)

- ▶ Can be interfaced to different tools : Herwig, Phytia, Sherpa
- ▶ Treat radiation differently but formally same NL accuracy

# Merging NLO with Parton Showers

- ▶ Resummation to NLL accuracy + realistic final states
- ▶ Allow to carry NLO precision to all aspects of experimental analysis

📌 MC@NLO [Frixione, Webber](#)

📌 POWHEG [Nason; Frixione, Nason, Oleari](#)

- ▶ Can be interfaced to different tools : Herwig, Phytia, Sherpa
- ▶ Treat radiation differently but formally same NL accuracy

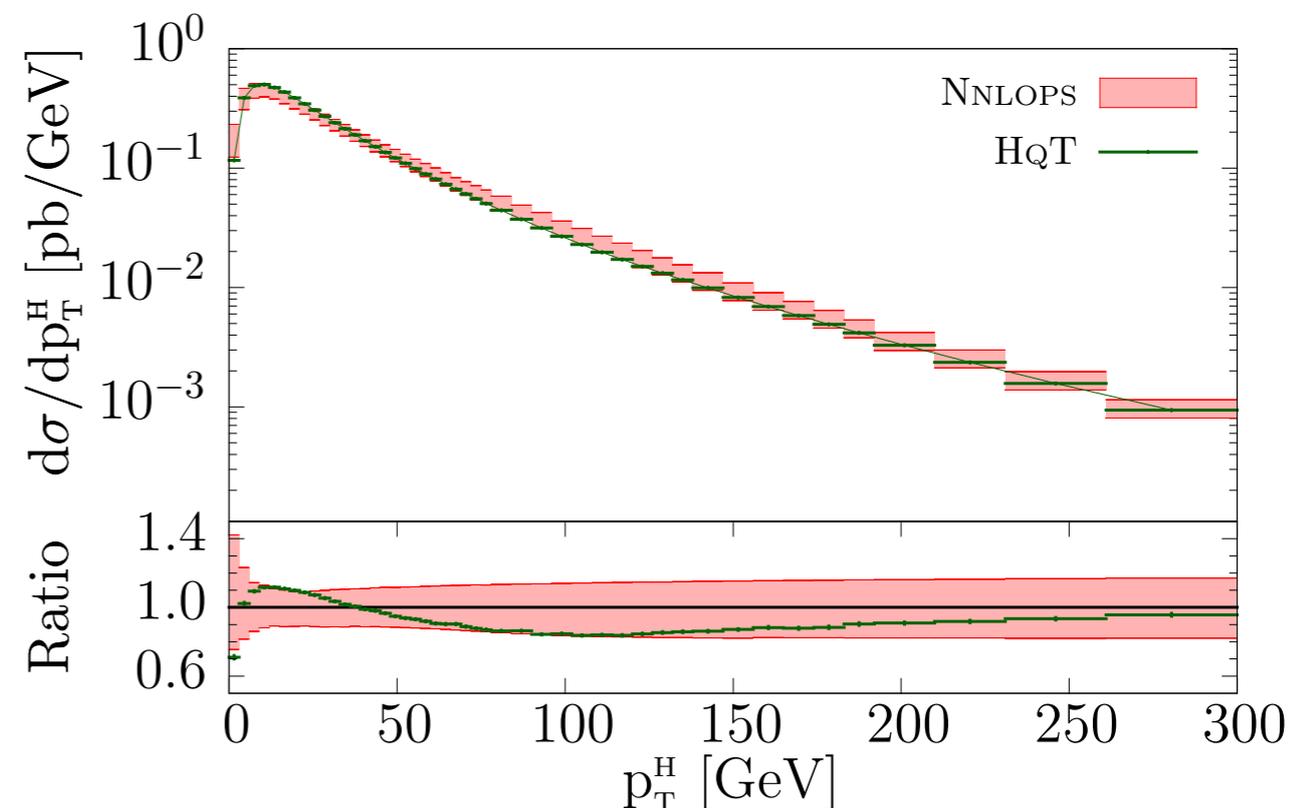
▶ NNLOPS (Higgs) 

[Hamilton, Nason, Re, Zanderighi](#)

POWHEG+MINLO

H+jet at NLO

Inclusive H reweighted to NNLO



# Automation and more

- ▶ Provide large library of processes or different degree of automation
  - ▶ aMC@NLO: full automation of NLO and PS in MC@NLO framework  
Frederix, Frixione, Hirschi, Pittau, Maltoni, Torrelli
  - ▶ POWHEG-BOX framework Aioli, Nason, Oleari, re
  - ▶ Sherpa : real matrix elements matching MC@NLO and POWHEG  
Krauss, Höche, Siebert, Schönher
  - ▶ POWHEL: automation of ME from HELAC with POWHEG-Box  
Papadopoulos, Garzelli, Kardos, Trocsanyi
  - ▶ POWHEG Box + Madgraph4 Campbell, Ellis, Frederix, Nason, Oleari, Williams
  - ▶ MINLO Hamilton, Nason, Oleari, Zanderighi
  - ▶ UNLOPS Lönnbland, Prestel
  - ▶ GENEVA Aioli et al
- + many others**

# NNLO the new frontier

► Some measurements to few percent accuracy

✓  $e^+e^- \rightarrow 3 \text{ jets}$

$e^-p \rightarrow (2 + 1) \text{ jets}$

✓  $pp \rightarrow V$

$pp \rightarrow \text{jets}$       **partial**

$pp \rightarrow V + \text{jets}$

✓  $pp \rightarrow t\bar{t}$

$$\mathcal{O}(\alpha_s^2)$$

Match experimental accuracy  
Extract accurate information

► Some processes with still (potentially) large NNLO corrections

✓  $pp \rightarrow H$        $pp \rightarrow HH$

✓  $pp \rightarrow \gamma\gamma$        $pp \rightarrow Z\gamma$        $pp \rightarrow VH$

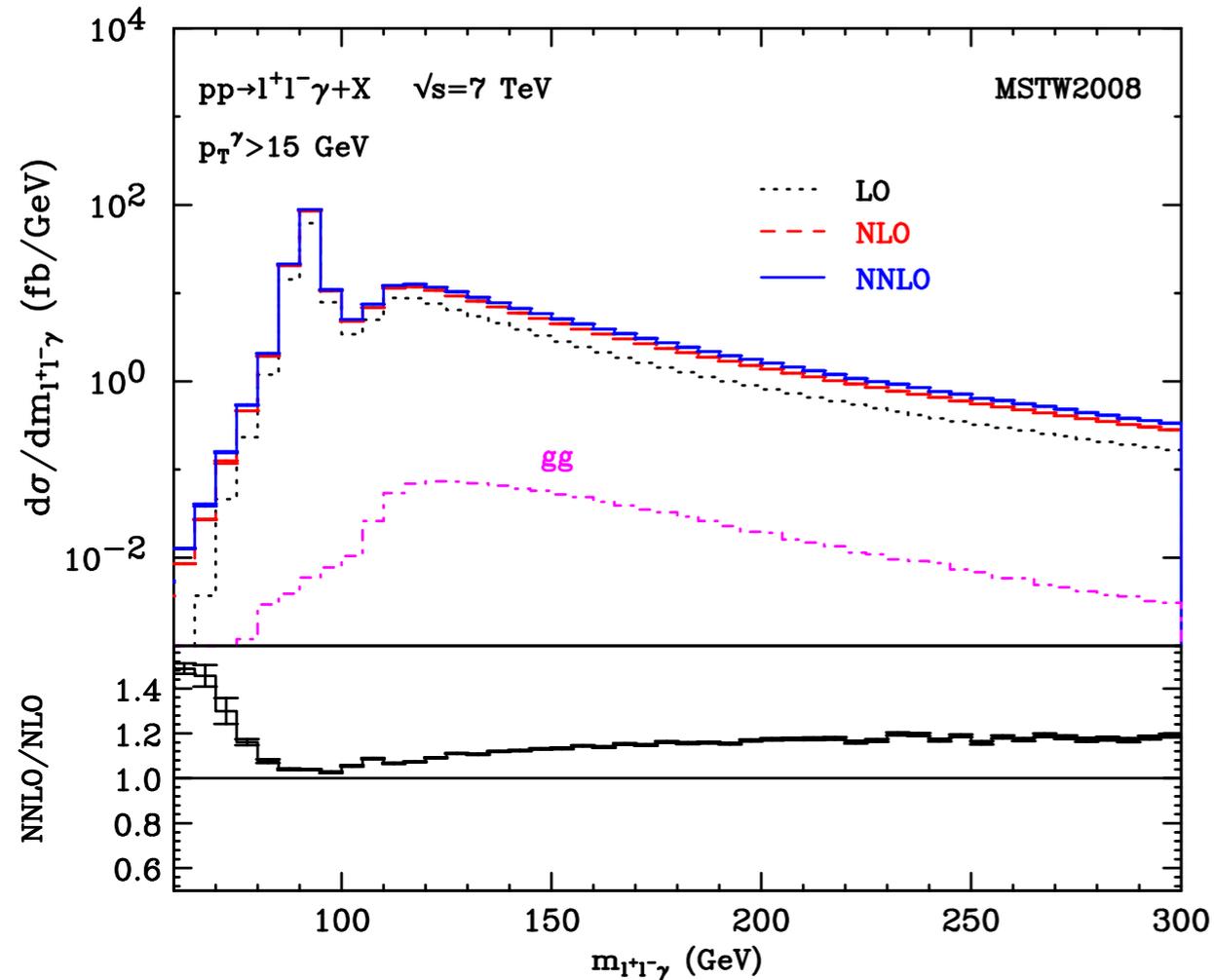
$pp \rightarrow VV$

$pp \rightarrow H + \text{jets}$       **partial**

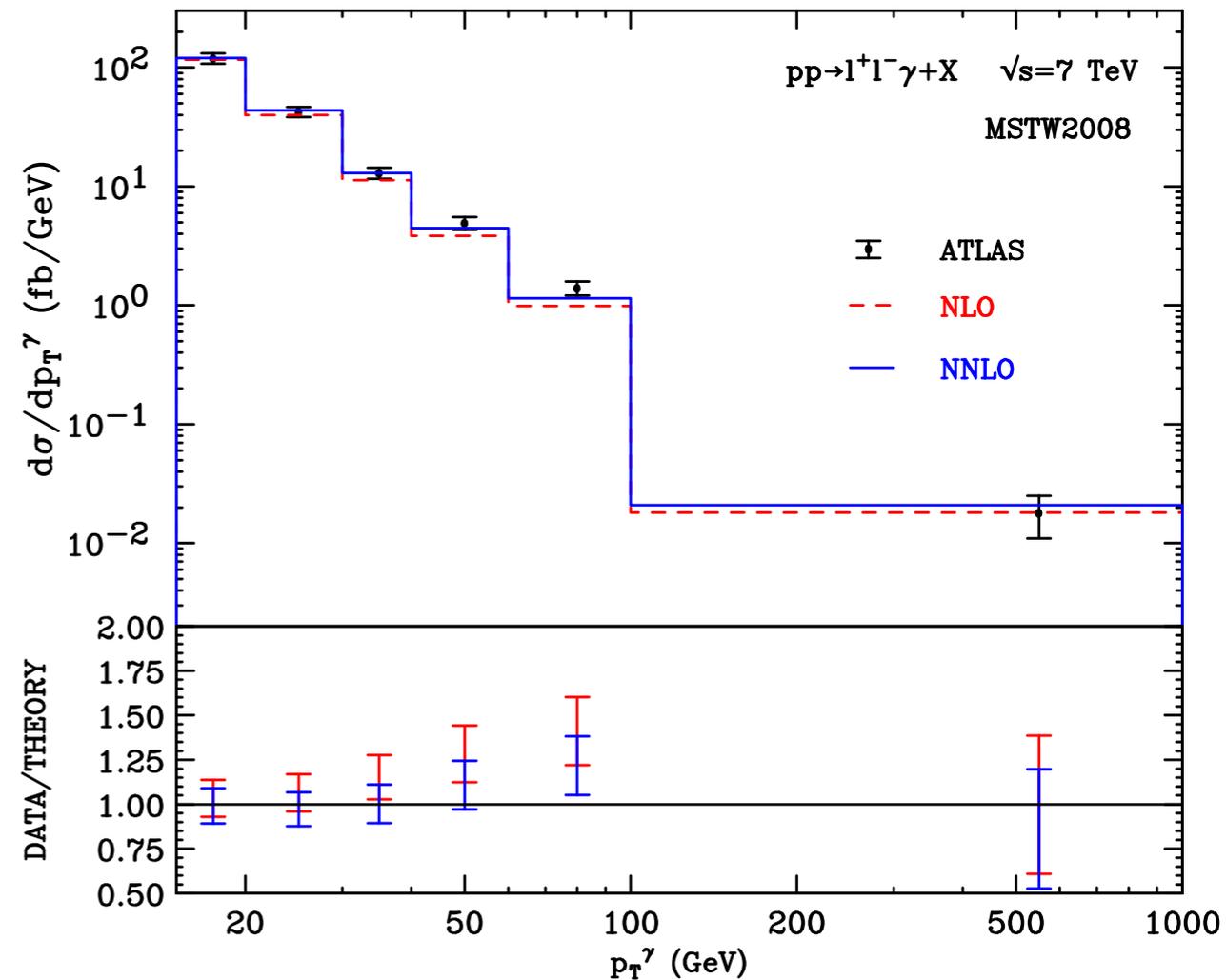
meaningful comparison  
solid estimate of uncertainties

$$pp \rightarrow Z\gamma$$

M.Grazzini, S.Kallweit, D.Rathlev, A.Torre (2013)



- NNLO ~16% at LHC
- Improvement in data/TH



- Triple gauge boson couplings
- **OpenLoops** for amplitude generation
- First step towards automation

➔ **VV** in general

$$pp \rightarrow t\bar{t}$$

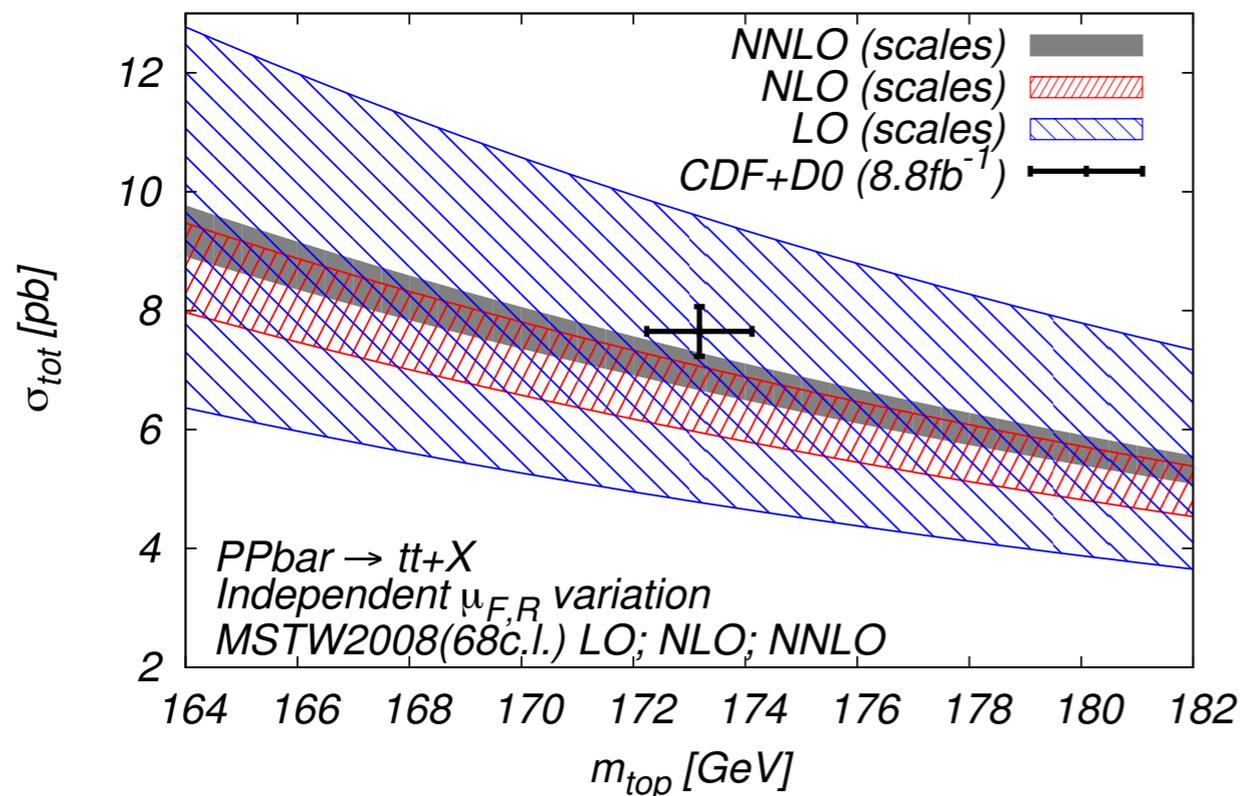
- ▶ Very relevant observable at colliders
- ▶ LHC will reach better than 5% accuracy
- ▶ top mass, pdfs, new physics

(inclusive) Full NNLO available  
 <5% TH uncertainties

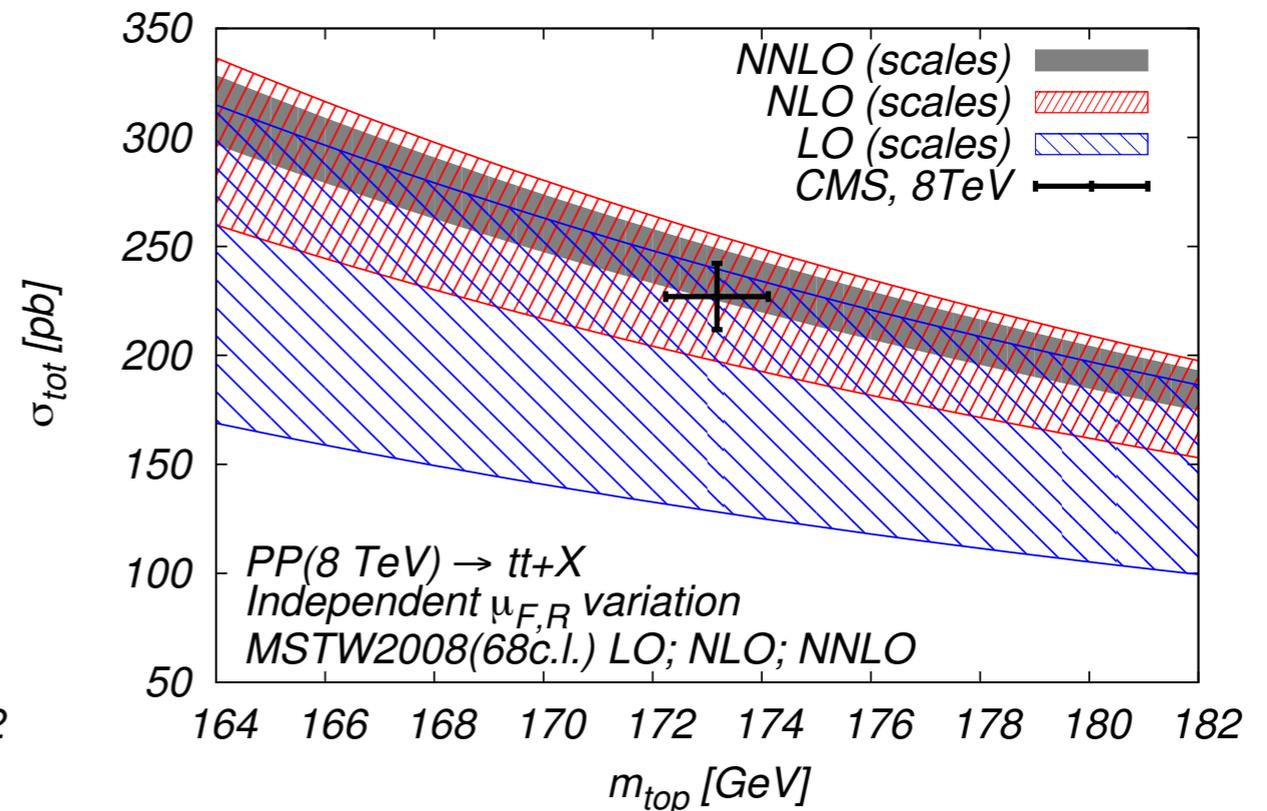
Czakon, Fiedler, Mitov (2013)

Collider	$\sigma_{\text{tot}}$ [pb]	scales [pb]	pdf [pb]
Tevatron	7.164	+0.110(1.5%) -0.200(2.8%)	+0.169(2.4%) -0.122(1.7%)
LHC 7 TeV	172.0	+4.4(2.6%) -5.8(3.4%)	+4.7(2.7%) -4.8(2.8%)
LHC 8 TeV	245.8	+6.2(2.5%) -8.4(3.4%)	+6.2(2.5%) -6.4(2.6%)
LHC 14 TeV	953.6	+22.7(2.4%) -33.9(3.6%)	+16.2(1.7%) -17.8(1.9%)

## • Precision for mass



M. Czakon, P. Fiedler, A. Mitov, J. Rojo (2013)

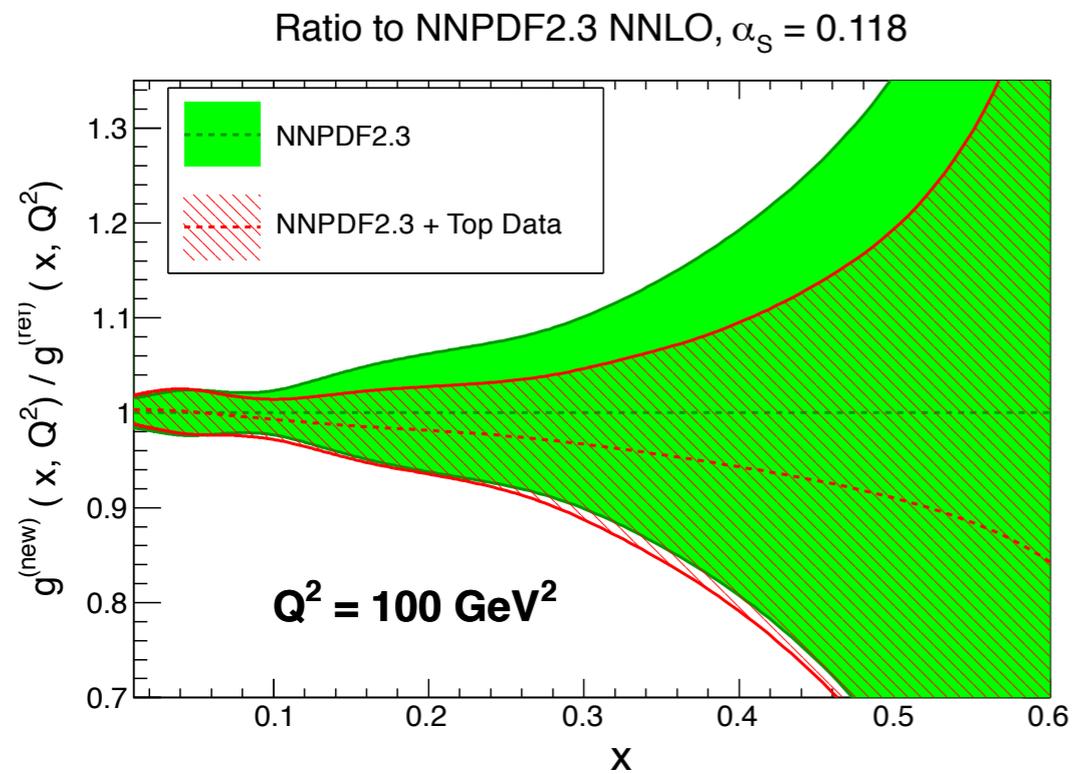


$$pp \rightarrow t\bar{t}$$

## • Precision for gluon pdf

M. Czakon, M. Mangano, A. Mitov, J. Rojo (2013)

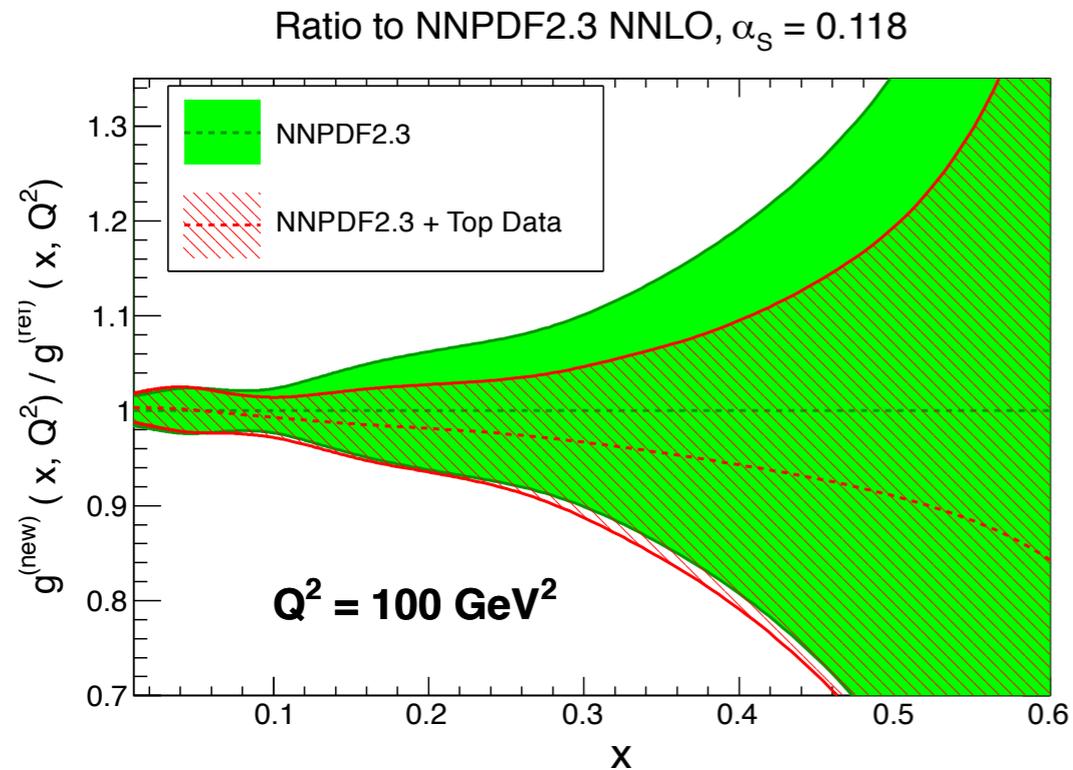
~20% reduction  $x=0.1$  to  $0.5$



- data used in ABM 2013

# $pp \rightarrow t\bar{t}$

## • Precision for gluon pdf

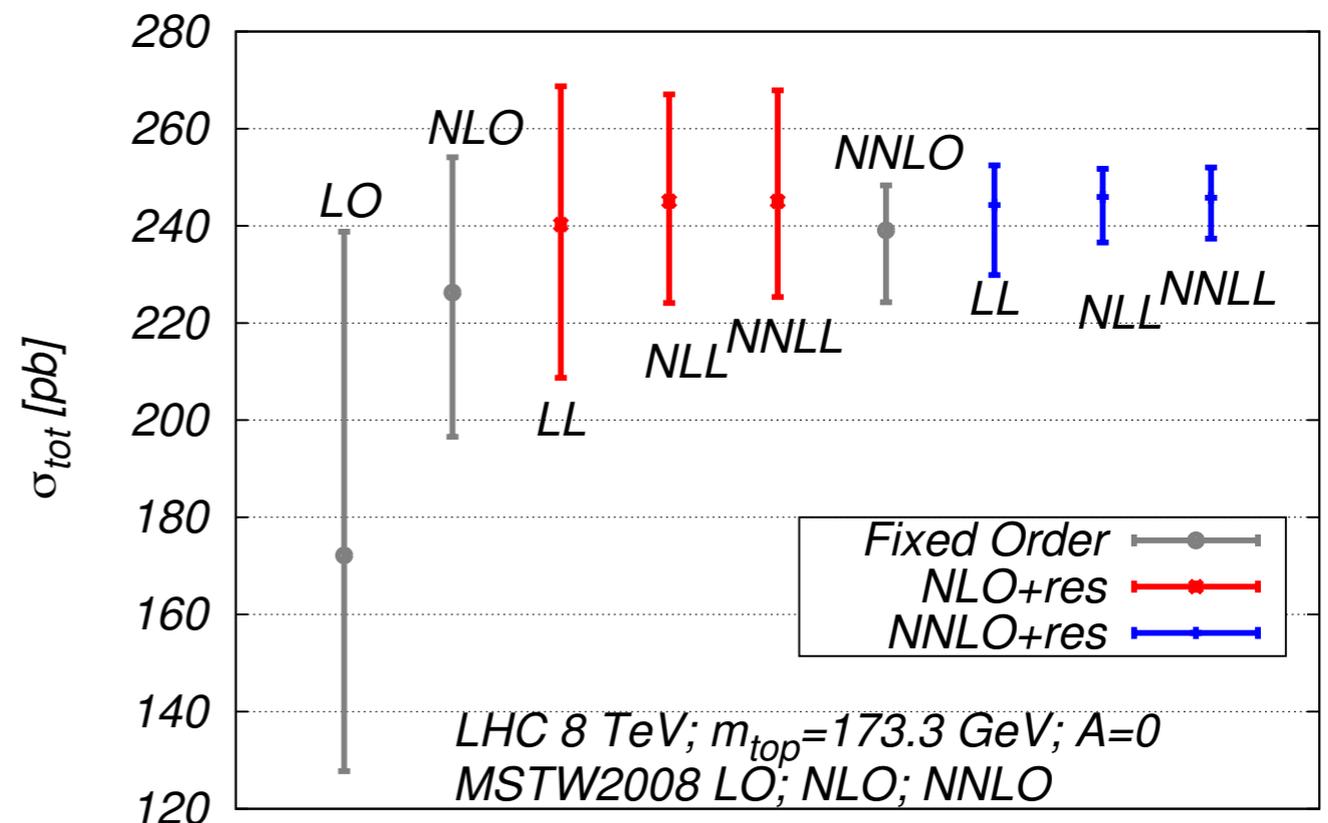


## • Even higher precision: threshold resummation

M. Czakon, M. Mangano, A. Mitov, J. Rojo (2013)

~20% reduction  $x=0.1$  to 0.5

- data used in ABM 2013

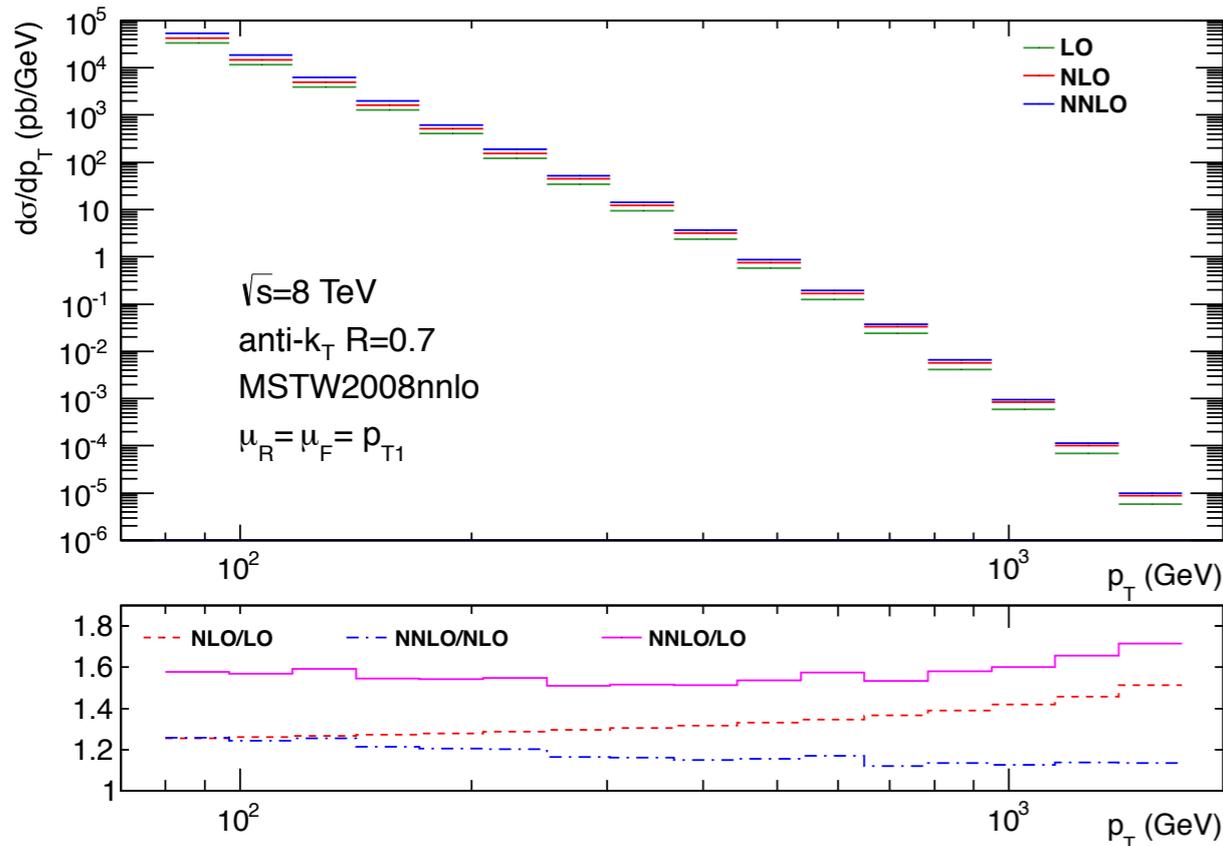


# $pp \rightarrow 2 \text{ jets}$

A. Gehrmann-De Ridder, T. Gehrmann, E.W.N. Glover, J.Pires (2013)

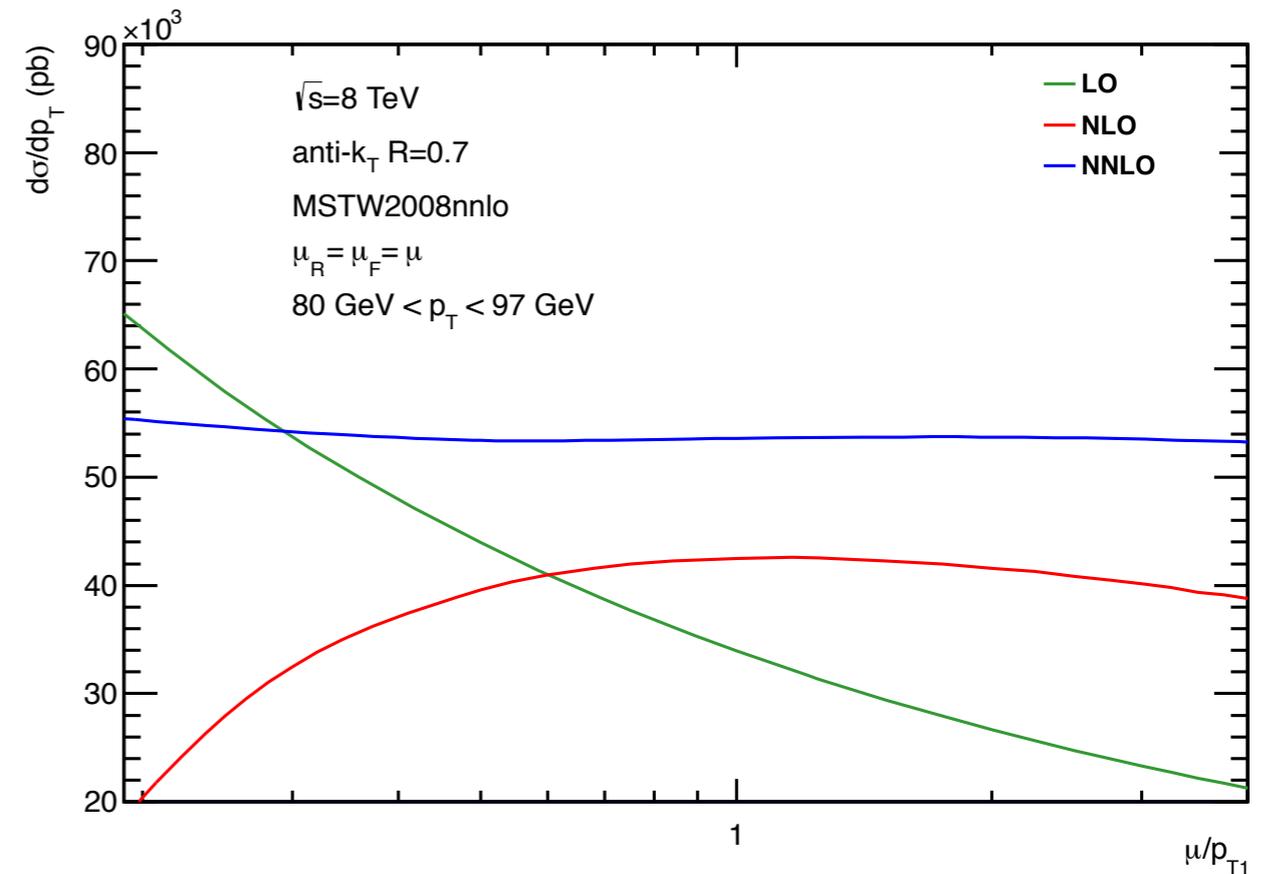
J.Curry, A. Gehrmann-De Ridder, E.W.N. Glover, J.Pires (2013)

## ► Pure gluon using antenna subtraction : NNLOJET



- 15-25% increase

Similar results expected for other partonic channels (gg dominant at low  $p_T$ )

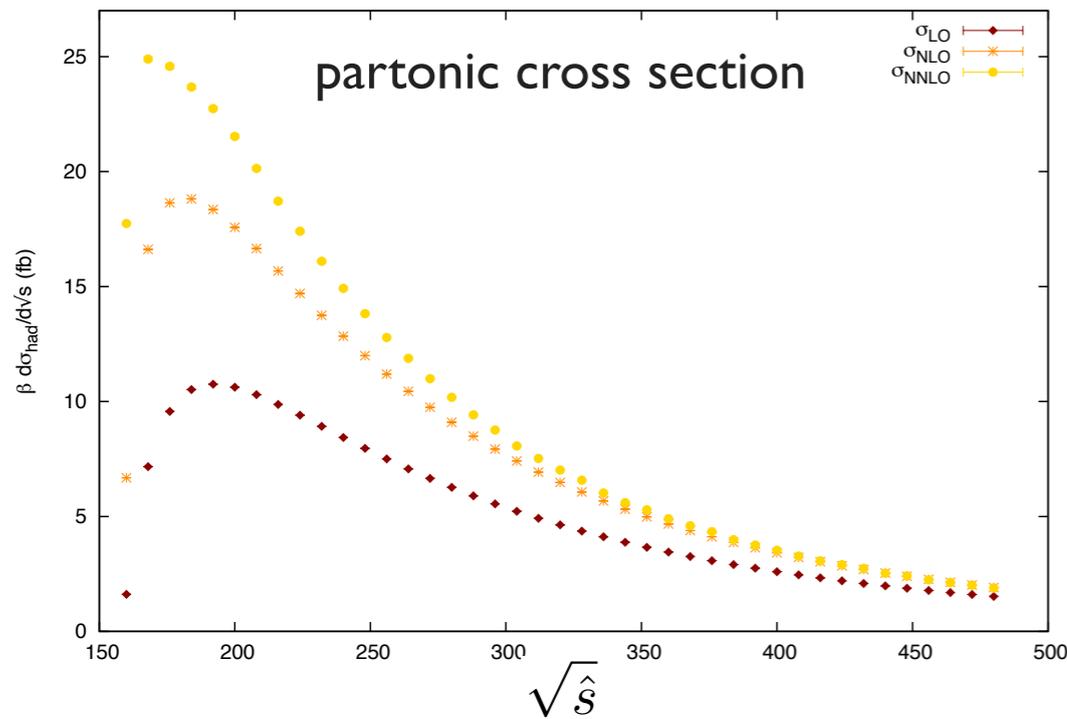


- Amazing reduction in scale dependence : **precision for LHC**

- **But** NNLO can not be predicted by NLO scale variations..

# $pp \rightarrow H + \text{jet}$

R.Boughezal, F.Caola, K.Melnikov, F.Petriello, M.Schulze (2013)



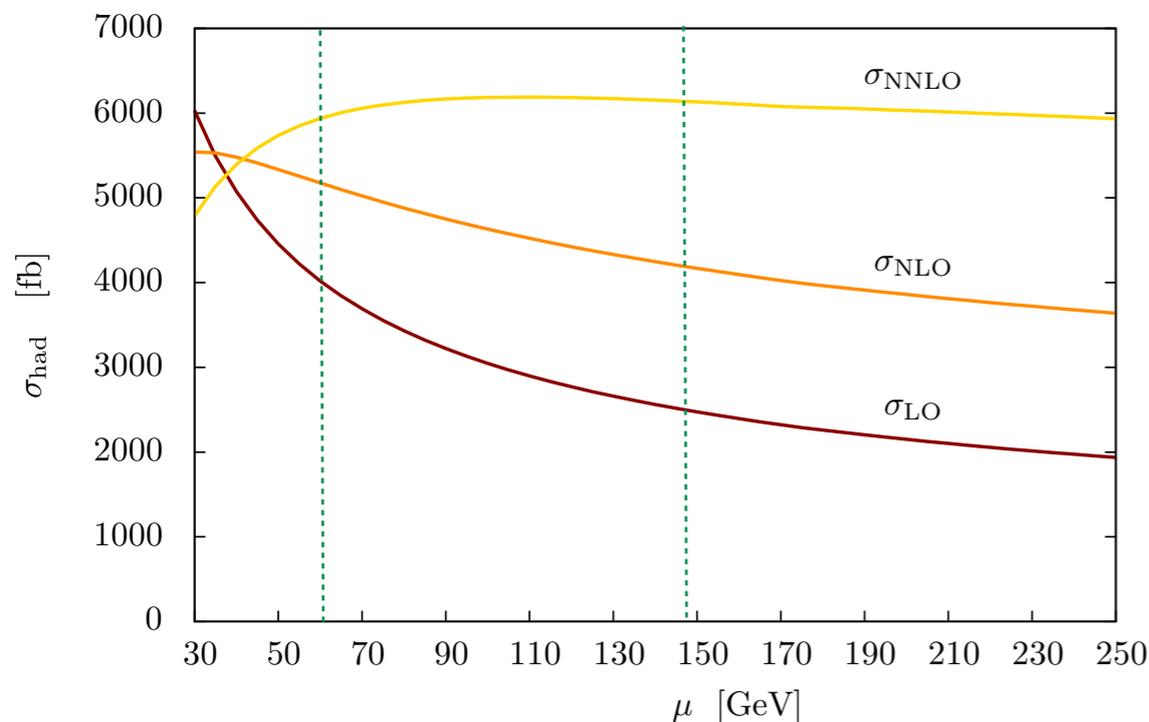
► Pure gluon only  $p_T^{\text{jet}} > 30 \text{ GeV}$

$$\sigma_{\text{LO}}(pp \rightarrow H j) = 2713_{-776}^{+1216} \text{ fb},$$

$$\sigma_{\text{NLO}}(pp \rightarrow H j) = 4377_{-738}^{+760} \text{ fb},$$

$$\sigma_{\text{NNLO}}(pp \rightarrow H j) = 6177_{+242}^{-204} \text{ fb}.$$

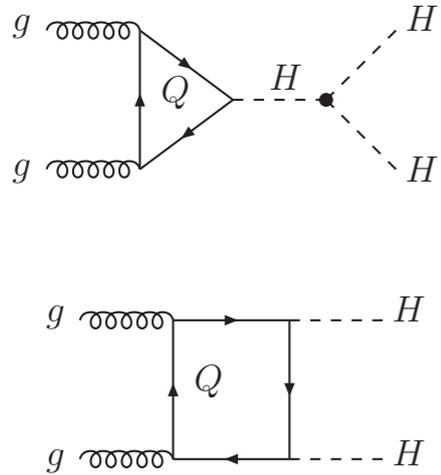
+60% NLO  
+30-40% NNLO



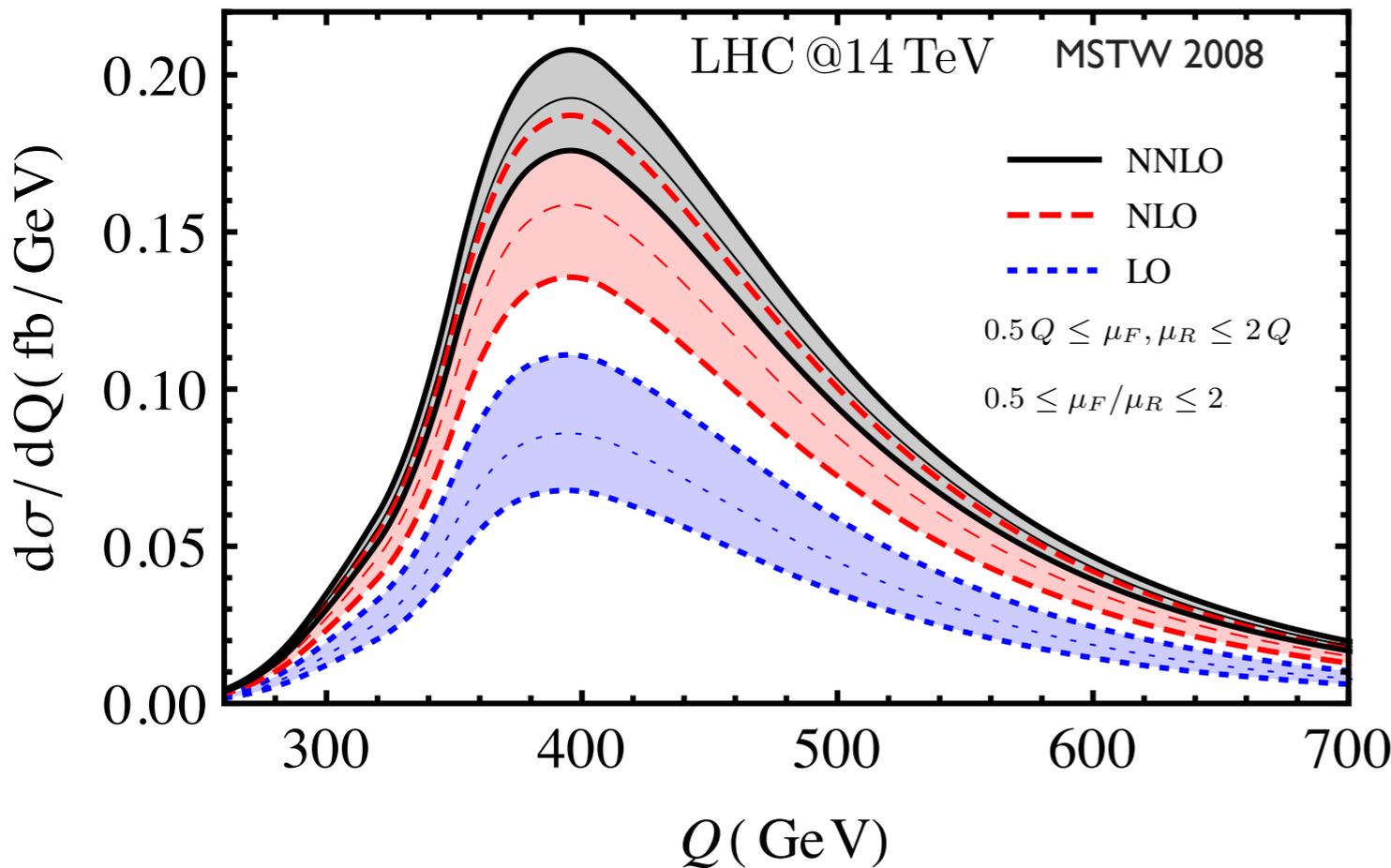
► Another case of significantly reduced scale dependence  $\sim 4\%$

# $pp \rightarrow HH$

DdeF., J.Mazzitelli (2013)



- ▶ Triple Higgs coupling : Higgs potential
- ▶ Expect large corrections (single Higgs)
- ▶ Use large top mass limit



$$M_H = 126 \text{ GeV}$$

**$K$**

$$\sigma_{\text{LO}} = 17.8^{+5.3}_{-3.8} \text{ fb}$$

$$\sigma_{\text{NLO}} = 33.2^{+5.9}_{-4.9} \text{ fb} \quad \mathbf{1.86}$$

$$\sigma_{\text{NNLO}} = 40.2^{+3.2}_{-3.5} \text{ fb} \quad \mathbf{2.26}$$

$\pm 8\%$

$\mathcal{O}(\pm 20\%)$  at NLO.

**21%**  $\updownarrow$

# Les Houches NNLO wish-list (2013)

- ▶ Many of them **doable** in the next few years
- ▶ More realistic final states (V, top with decays)
- ▶ Larger multiplicities not possible yet
- ▶ Automation far away
- ▶ Shower requires increase in accuracy
- ▶ NLO EW corrections needed

Process	known	desired	details
V	$d\sigma(\text{lept. V decay}) @ \text{NNLO QCD}$ $d\sigma(\text{lept. V decay}) @ \text{NLO EW}$	$d\sigma(\text{lept. V decay}) @ \text{NNNLO QCD} + \text{NLO EW}$ MC@NNLO	precision EW, PDFs
V + j	$d\sigma(\text{lept. V decay}) @ \text{NLO QCD}$ $d\sigma(\text{lept. V decay}) @ \text{NLO EW}$	$d\sigma(\text{lept. V decay}) @ \text{NNLO QCD} + \text{NLO EW}$	Z + j for gluon PDF W + c for strange PDF
V + jj	$d\sigma(\text{lept. V decay}) @ \text{NLO QCD}$	$d\sigma(\text{lept. V decay}) @ \text{NNLO QCD} + \text{NLO EW}$	study of systematics of H + jj final state
VV'	$d\sigma(\text{V decays}) @ \text{NLO QCD}$ $d\sigma(\text{stable V}) @ \text{NLO EW}$	$d\sigma(\text{V decays}) @ \text{NNLO QCD} + \text{NLO EW}$	off-shell leptonic decays TGCs
gg → VV	$d\sigma(\text{V decays}) @ \text{LO QCD}$	$d\sigma(\text{V decays}) @ \text{NLO QCD}$	bkg. to $H \rightarrow VV$ TGCs
V $\gamma$	$d\sigma(\text{V decay}) @ \text{NLO QCD}$ $d\sigma(\text{PA, V decay}) @ \text{NLO EW}$	$d\sigma(\text{V decay}) @ \text{NNLO QCD} + \text{NLO EW}$	TGCs
Vb $\bar{b}$	$d\sigma(\text{lept. V decay}) @ \text{NLO QCD}$ massive b	$d\sigma(\text{lept. V decay}) @ \text{NNLO QCD}$ massless b	bkg. for $VH \rightarrow b\bar{b}$
VV' $\gamma$	$d\sigma(\text{V decays}) @ \text{NLO QCD}$	$d\sigma(\text{V decays}) @ \text{NLO QCD} + \text{NLO EW}$	QGCs
VV'V''	$d\sigma(\text{V decays}) @ \text{NLO QCD}$	$d\sigma(\text{V decays}) @ \text{NLO QCD} + \text{NLO EW}$	QGCs, EWSB
VV' + j	$d\sigma(\text{V decays}) @ \text{NLO QCD}$	$d\sigma(\text{V decays}) @ \text{NLO QCD} + \text{NLO EW}$	bkg. to H, BSM searches
VV' + jj	$d\sigma(\text{V decays}) @ \text{NLO QCD}$	$d\sigma(\text{V decays}) @ \text{NLO QCD} + \text{NLO EW}$	QGCs, EWSB
$\gamma\gamma$	$d\sigma @ \text{NNLO QCD}$		bkg to $H \rightarrow \gamma\gamma$

Process	known	desired	details
t $\bar{t}$	$\sigma_{\text{tot}} @ \text{NNLO QCD}$ $d\sigma(\text{top decays}) @ \text{NLO QCD}$ $d\sigma(\text{stable tops}) @ \text{NLO EW}$	$d\sigma(\text{top decays}) @ \text{NNLO QCD} + \text{NLO EW}$	precision top/QCD, gluon PDF, effect of extra radiation at high rapidity, top asymmetries
t $\bar{t}$ + j	$d\sigma(\text{NWA top decays}) @ \text{NLO QCD}$	$d\sigma(\text{NWA top decays}) @ \text{NNLO QCD} + \text{NLO EW}$	precision top/QCD top asymmetries
single-top	$d\sigma(\text{NWA top decays}) @ \text{NLO QCD}$	$d\sigma(\text{NWA top decays}) @ \text{NNLO QCD} (\text{t channel})$	precision top/QCD, $V_{tb}$
dijet	$d\sigma @ \text{NNLO QCD} (\text{g only})$ $d\sigma @ \text{NLO weak}$	$d\sigma @ \text{NNLO QCD} + \text{NLO EW}$	Obs.: incl. jets, dijet mass → PDF fits (gluon at high x) → $\alpha_s$ CMS <a href="http://arxiv.org/abs/1212.6660">http://arxiv.org/abs/1212.6660</a>
3j	$d\sigma @ \text{NLO QCD}$	$d\sigma @ \text{NNLO QCD} + \text{NLO EW}$	Obs.: $R3/2$ or similar → $\alpha_s$ at high scales dom. uncertainty: scales CMS <a href="http://arxiv.org/abs/1304.7498">http://arxiv.org/abs/1304.7498</a>
$\gamma$ + j	$d\sigma @ \text{NLO QCD}$ $d\sigma @ \text{NLO EW}$	$d\sigma @ \text{NNLO QCD} + \text{NLO EW}$	gluon PDF $\gamma$ + b for bottom PDF

Process	known	desired	details
H	$d\sigma @ \text{NNLO QCD}$ $d\sigma @ \text{NLO EW}$ finite quark mass effects @ NLO	$d\sigma @ \text{NNNLO QCD} + \text{NLO EW}$ MC@NNLO finite quark mass effects @ NNLO	H branching ratios and couplings
H + j	$d\sigma @ \text{NNLO QCD} (\text{g only})$ $d\sigma @ \text{NLO EW}$ finite quark mass effects @ LO	$d\sigma @ \text{NNLO QCD} + \text{NLO EW}$ finite quark mass effects @ NLO	H $p_T$
H + 2j	$\sigma_{\text{tot}}(\text{VBF}) @ \text{NNLO}(\text{DIS}) \text{QCD}$ $d\sigma(\text{gg}) @ \text{NLO QCD}$ $d\sigma(\text{VBF}) @ \text{NLO EW}$	$d\sigma @ \text{NNLO QCD} + \text{NLO EW}$	H couplings
H + V	$d\sigma @ \text{NNLO QCD}$ $d\sigma @ \text{NLO EW}$	with $H \rightarrow b\bar{b}$ @ same accuracy	H couplings
t $\bar{t}$ H	$d\sigma(\text{stable tops}) @ \text{NLO QCD}$	$d\sigma(\text{top decays}) @ \text{NLO QCD} + \text{NLO EW}$	top Yukawa coupling
HH	$d\sigma @ \text{LO QCD} (\text{full } m_t \text{ dependence})$ $d\sigma @ \text{NLO QCD} (\text{infinite } m_t \text{ limit})$	$d\sigma @ \text{NLO QCD} (\text{full } m_t \text{ dependence})$ $d\sigma @ \text{NNLO QCD} (\text{infinite } m_t \text{ limit})$	Higgs self coupling

# Electroweak corrections at large energies

## ► Sudakov logarithms induced by soft gauge-boson exchange

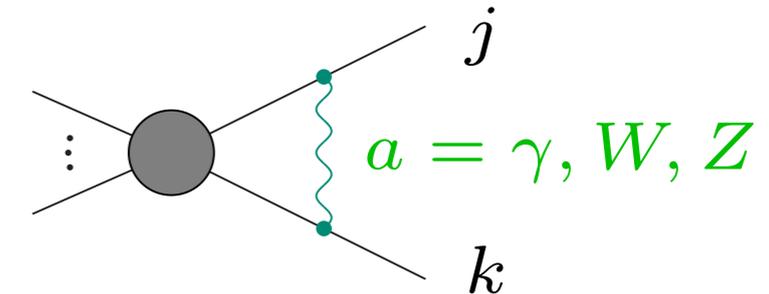
at  $\sqrt{s} \sim 1 \text{ TeV}$

S. Dittmaier

$$\delta_{\text{LL}}^{1\text{-loop}} \sim -\frac{\alpha}{\pi s_W^2} \ln^2\left(\frac{s}{M_W^2}\right) \simeq -26\%$$

$$\delta_{\text{LL}}^{2\text{-loop}} \sim +\frac{\alpha^2}{2\pi^2 s_W^4} \ln^4\left(\frac{s}{M_W^2}\right) \simeq 3.5\%$$

• still sizable at 2-loops

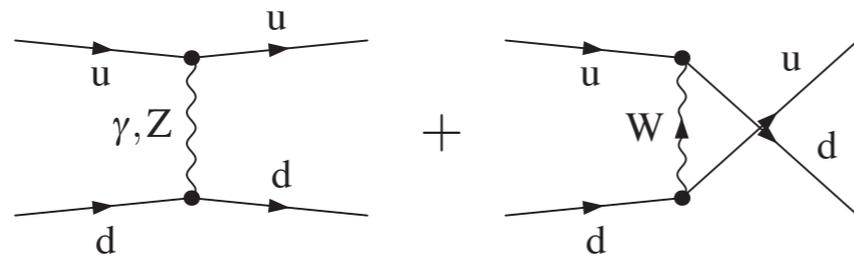


$$s, |t|, |u| \gg M_W^2$$

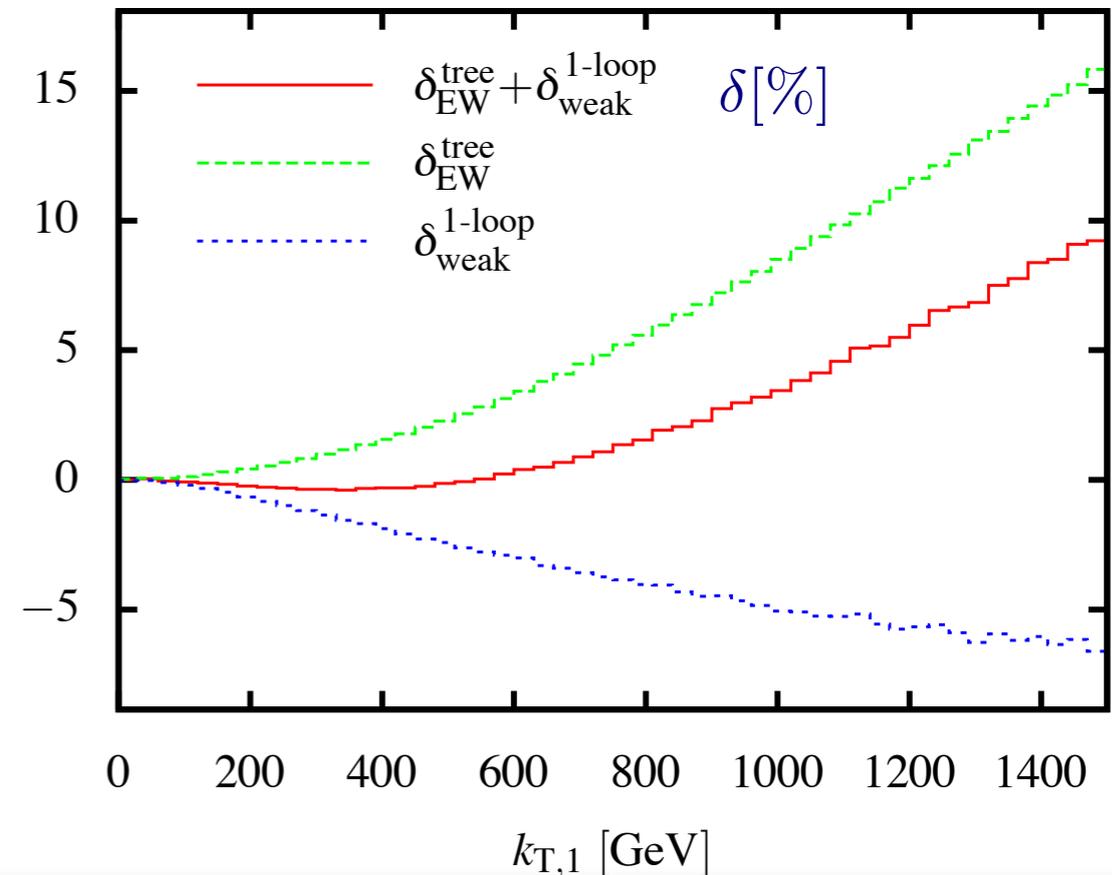
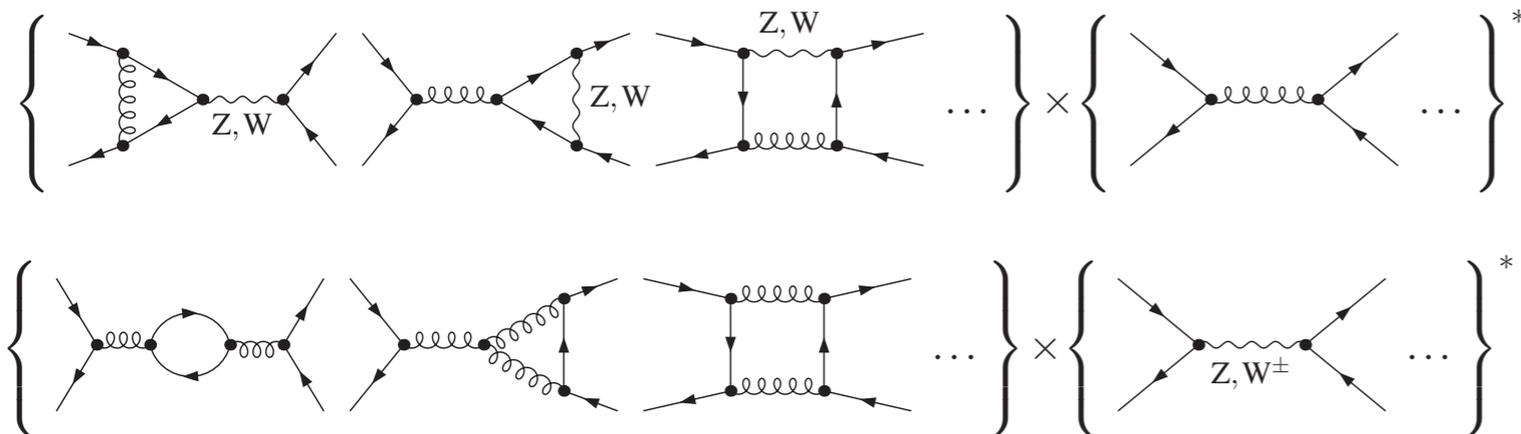
## Dijet production

Dittmaier, Huss, Speckner

tree EW

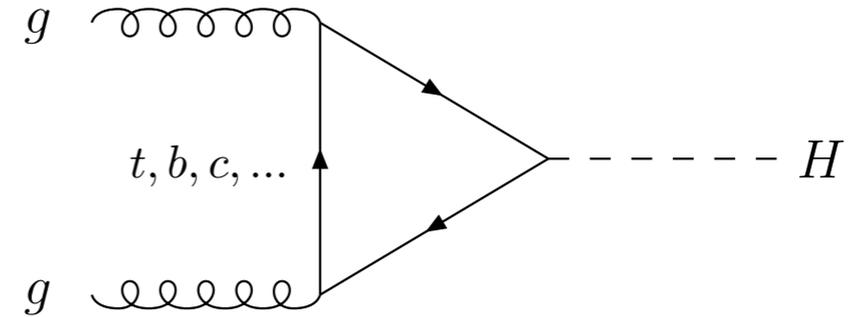


1-loop EW

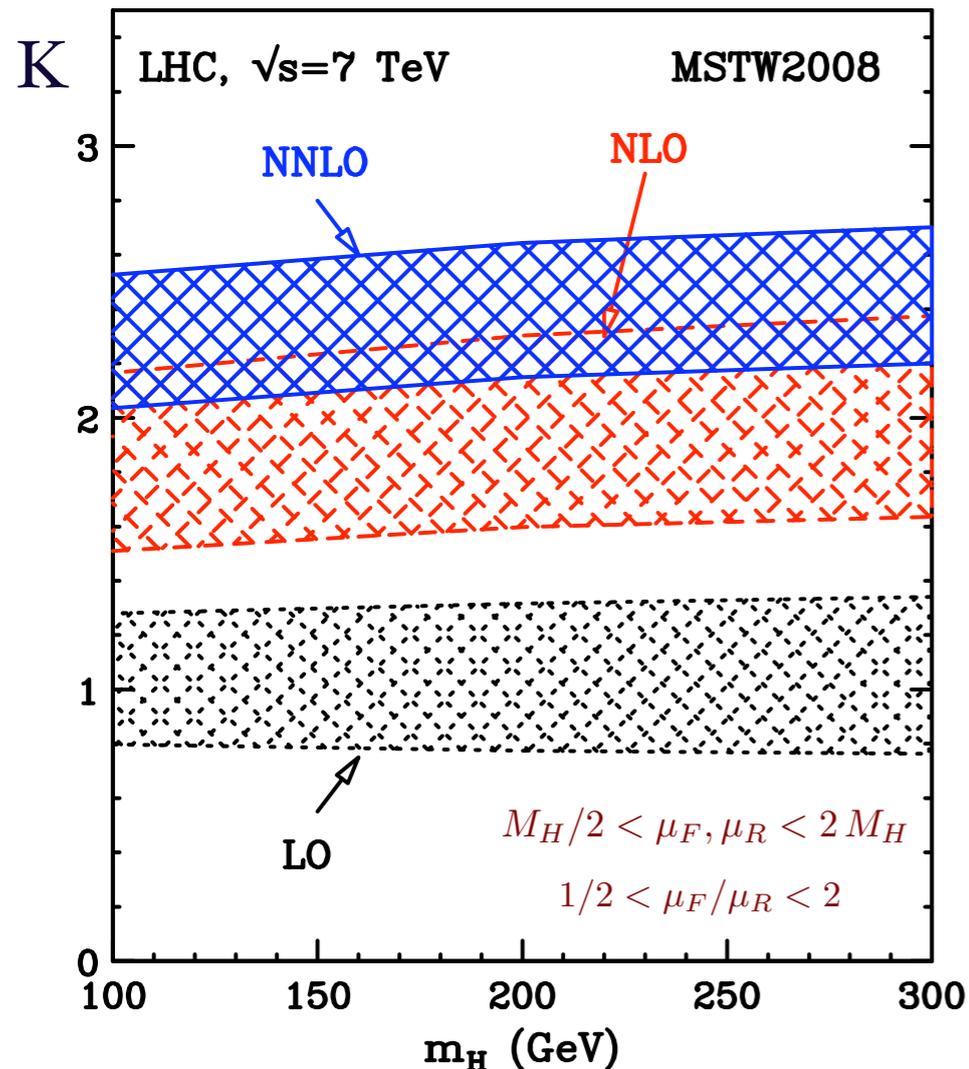


# Higgs Boson

► Gluon-gluon fusion dominates due to large gluon luminosity



► QCD corrections are huge!



$$K = \frac{\sigma^{NNLO(NLO)}}{\sigma^{LO}}$$

**NLO** Dawson (1991); Djouadi, Spira, Zerwas (1991)  
Graudenz, Spira, Zerwas (1993)

**NNLO** Harlander, Kilgore (2002)  
Anastasiou, Melnikov (2002)  
Ravindran, Smith, van Neerven (2003)

# Improved Higgs Cross-section @ LHC

- ▶ NNLL Resummation 9% at 7 TeV [Catani, deF., Grazzini, Nason \(2003\)](#)
- ▶ Two loop EW corrections not negligible ~ 5%  
[Aglietti, Bonciani, Degrassi, Vicini \(2004\)](#)  
[Degrassi, Maltoni \(2004\)](#)  
[Actis, Passarino, Sturm, Uccirati \(2008\)](#)
- ▶ Mixed EW-QCD effects evaluated in EFT approach [Anastasiou et al \(2008\)](#)
- ▶ + Mass effects, Line-shape, interferences, ... [Higgs Cross-Section WG](#)

scale pdf +  $\alpha_S$

$$\sigma(m_H = 125 \text{ GeV}) = 19.27^{+7.2\%}_{-7.8\%} \begin{matrix} +7.5\% \\ -6.9\% \end{matrix} \text{ pb} \quad \text{deF, Grazzini}$$

- ▶ Still sizable uncertainties but great improvement over the last years
- ▶ And more precise results just arriving!!

# Improved Higgs Cross-section @ LHC

- ▶ NNLL Resummation 9% at 7 TeV Catani, deF., Grazzini, Nason (2003)
- ▶ Two loop EW corrections not negligible ~ 5% Aglietti, Bonciani, Degrassi, Vicini (2004)  
Degrassi, Maltoni (2004)  
Actis, Passarino, Sturm, Uccirati (2008)
- ▶ Mixed EW-QCD effects evaluated in EFT approach Anastasiou et al (2008)
- ▶ + Mass effects, Line-shape, interferences, ... Higgs Cross-Section WG

$$\sigma(m_H = 125 \text{ GeV}) = 19.27^{+7.2\%}_{-7.8\%} \overset{\text{scale}}{+7.5\%} \overset{\text{pdf} + \alpha_S}{-6.9\%} \text{ pb} \quad \text{deF, Grazzini}$$

Higher orders      LHC data and more observables

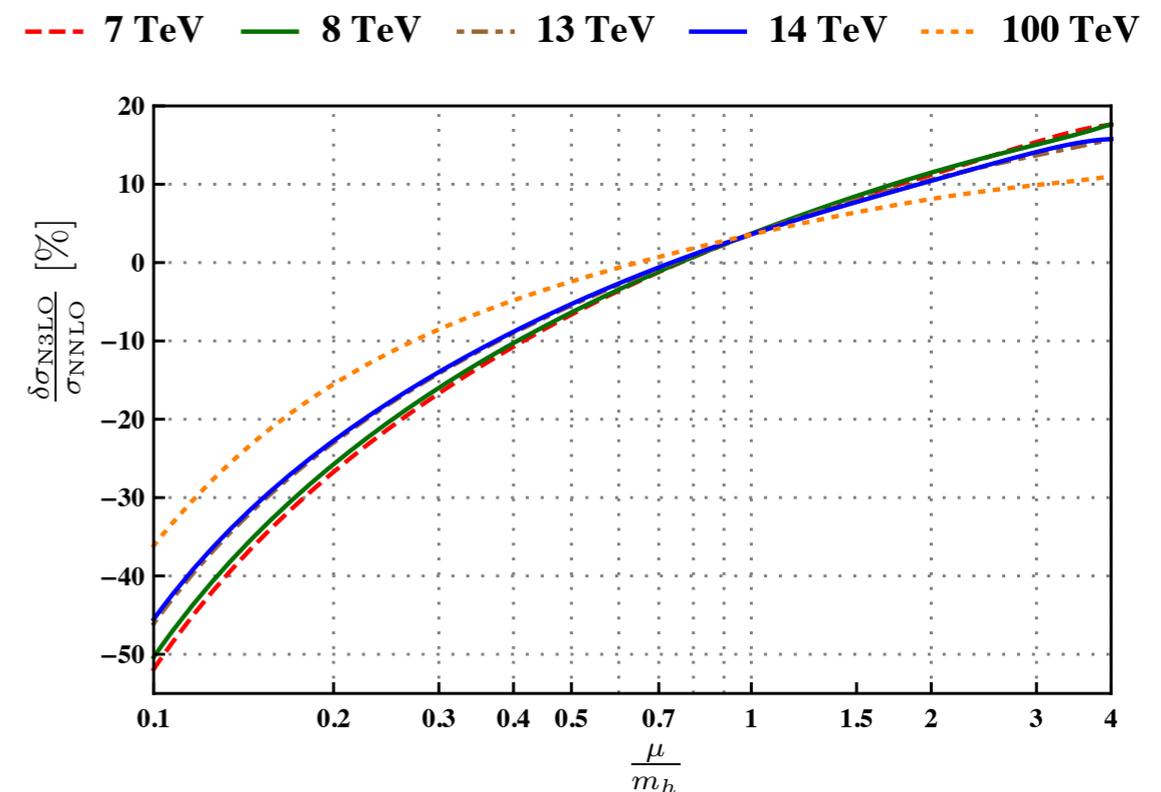
- ▶ Still sizable uncertainties but great improvement over the last years
- ▶ And more precise results just arriving!!

# Even Higher orders : N<sup>3</sup>LO

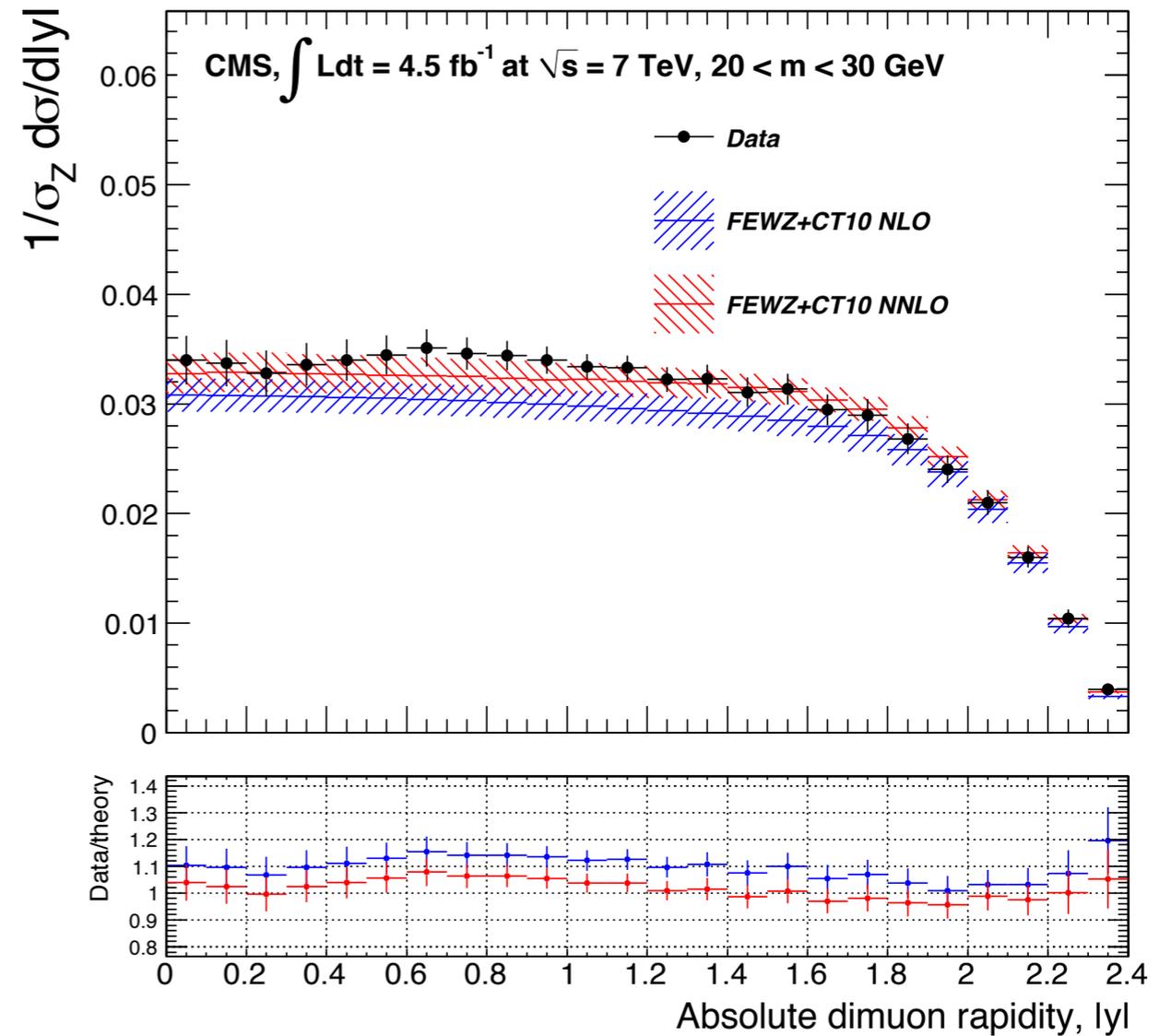
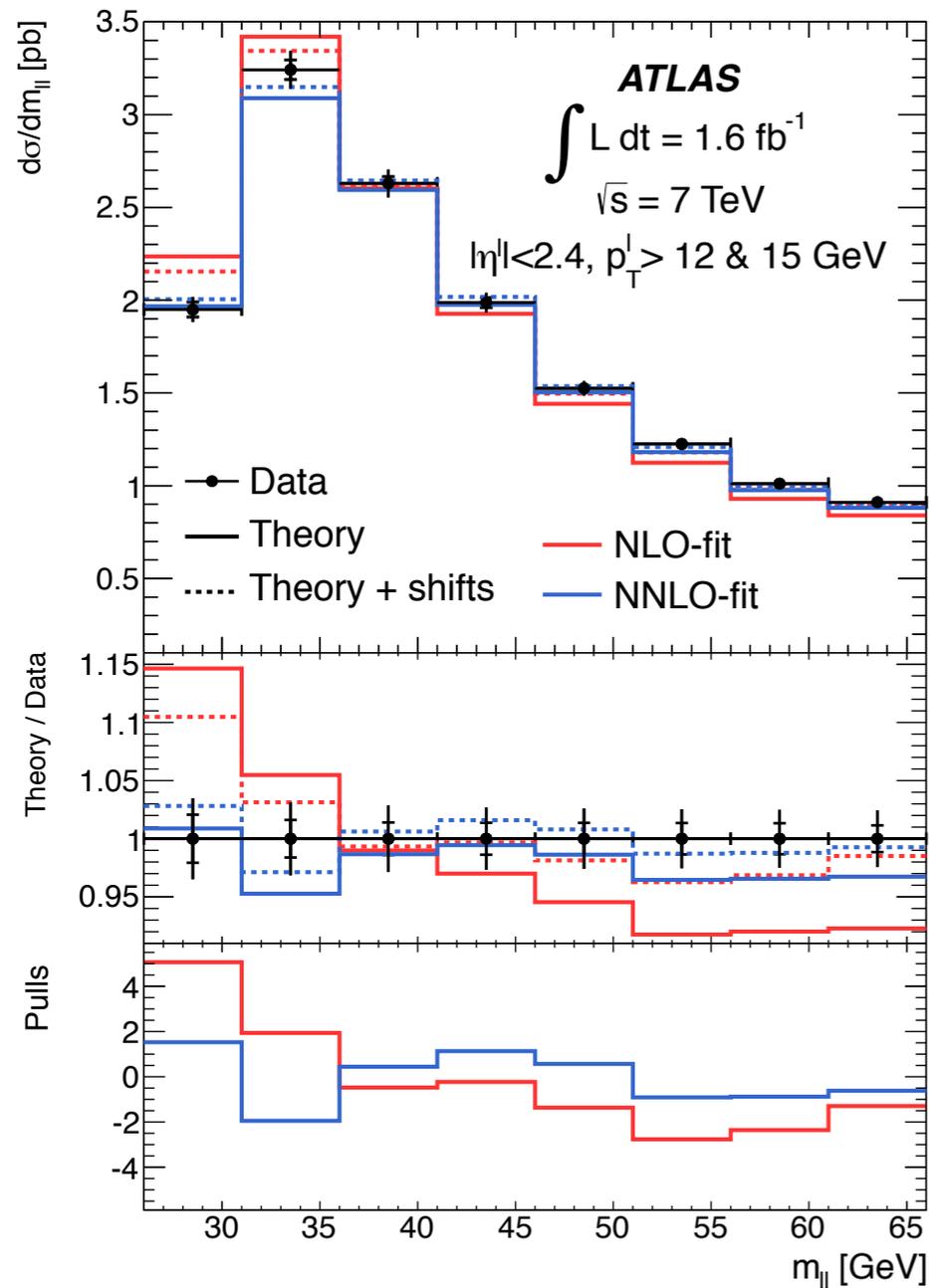
- ▶ 3 loop form factor      Baikov et al (2009)  
   Gehrman et al (2010)  
   Lee, Smirnov, Smirnov (2010)
- ▶ Triple real emission : threshold expansion      Anastasiou, Duhr, Dulat, Mistlberger (2013)
- ▶ 2 loop + single emission      Duhr, Gehrman (2013); Li, Zu (2013);  
   Gehrman, Jaquier, Glover, Koukoutsakis (2012)
- ▶ 1 loop + double emission      Anastasiou, Duhr, Dulat, Herzog, Mistlberger (2013)
- ▶ Subtraction terms      Höschele, Hoff, Pak, Steinhauser, Ueda (2013)  
   Buehler, Lazopoulos (2013)
- ▶ NNNLO Soft-Virtual approximation

Anastasiou, Duhr, Dulat, Furlan, Gehrman,  
Herzog, Mistlberger (2014)

**New era in precision**  
**Further improvements expected**



# DATA vs TH : Drell-Yan

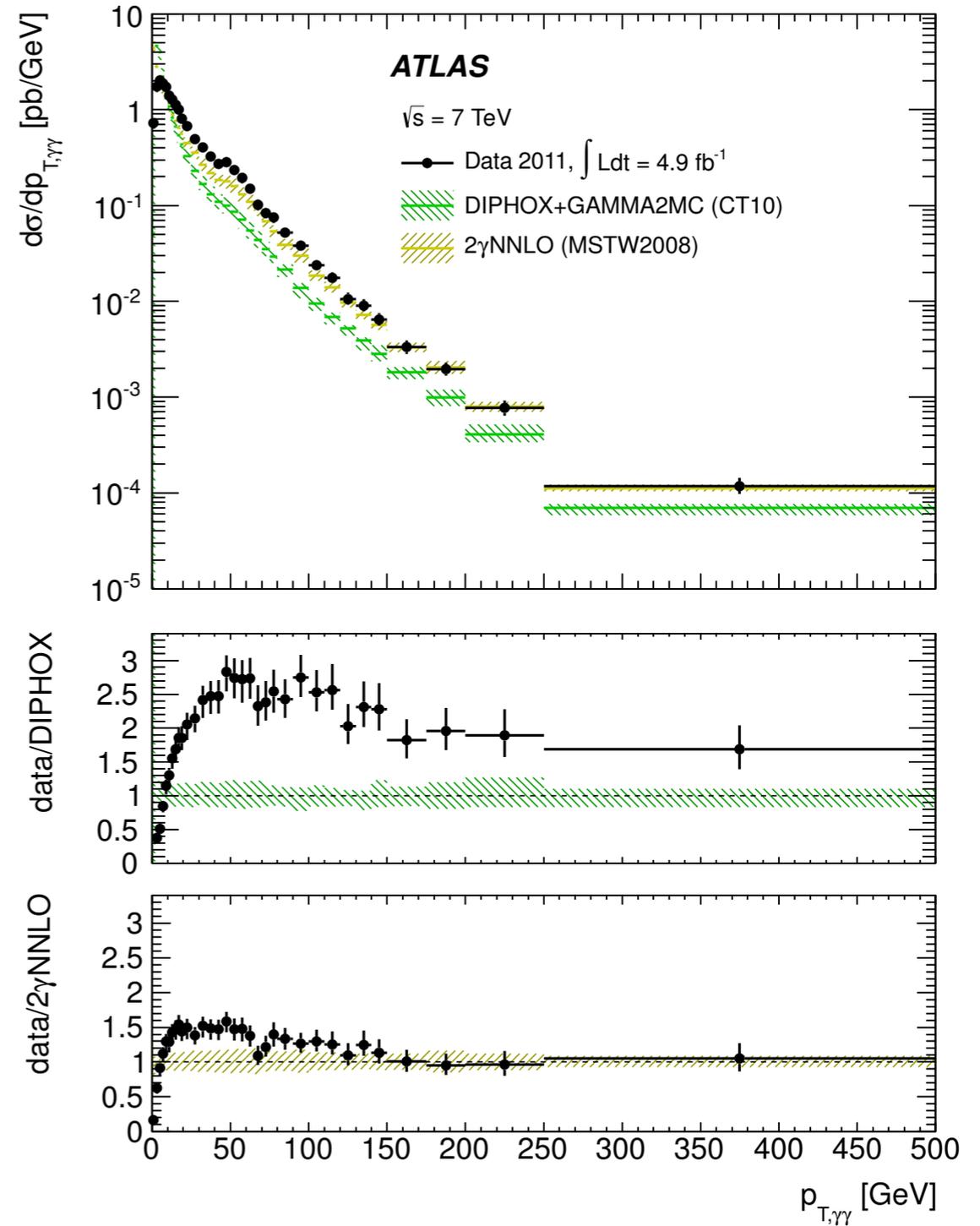
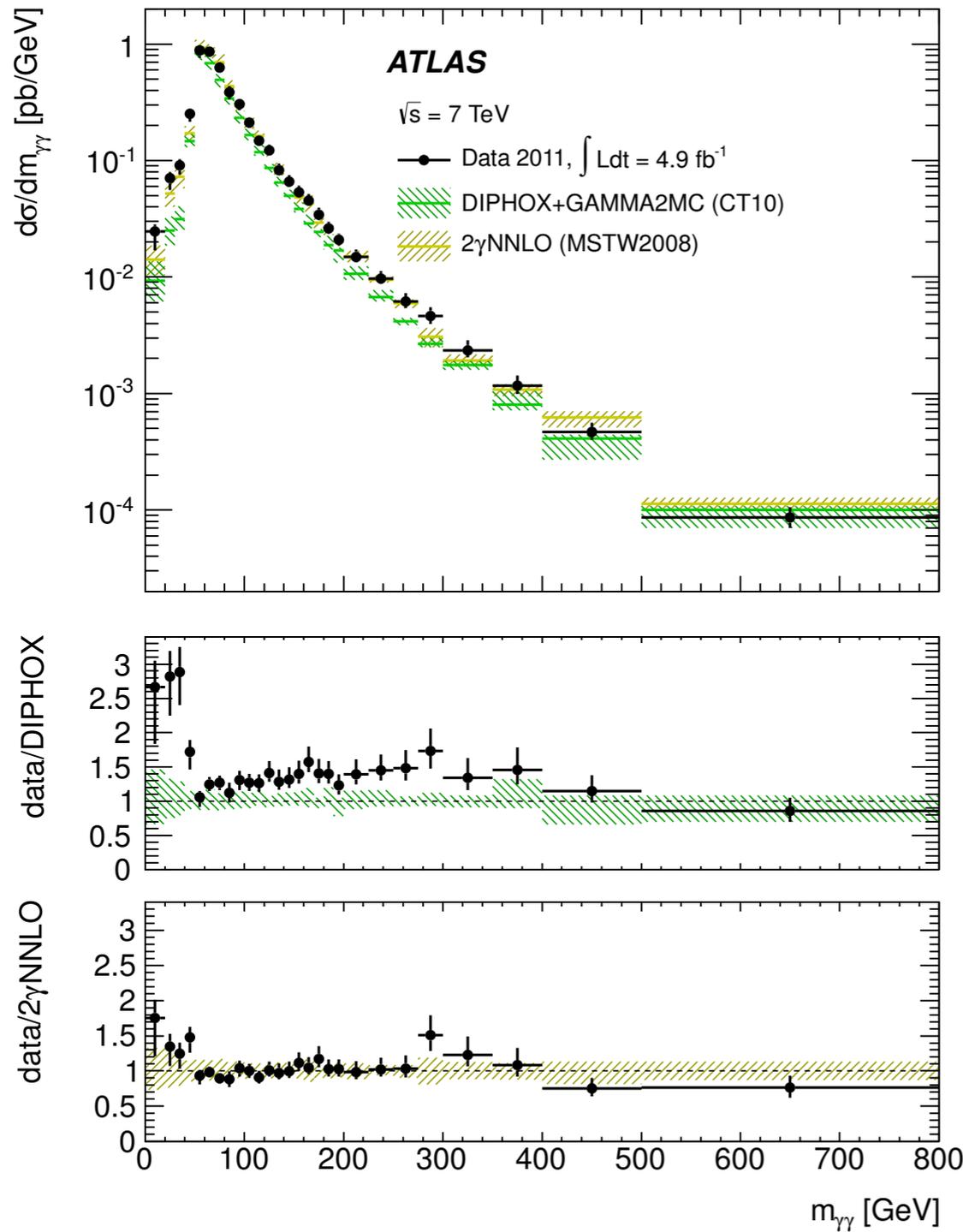


Precision in data sensitive to NNLO effects

TH vs EXP : detailed comparison just began at LHC

# DATA vs TH : DiPhotons

$$pp \rightarrow \gamma\gamma$$



# Conclusions

Amazing work in the last few years  direct consequence of LHC

- 📌 PDFs: precision and uncertainties
- 📌 NLO : multileg processes and automatic!
- 📌 NNLO finally reaching  $2 \rightarrow 2$  processes
- 📌 Resummation setting NNLL as new standard
- 📌 Improvements for NLO+PS and high degree of automation
- 📌 Higgs moving towards N3LO
- 📌 + many other issues not discussed (including jet structure)!

# Conclusions

Amazing work in the last few years  direct consequence of LHC

- 📌 PDFs: precision and uncertainties
- 📌 NLO : multileg processes and automatic!
- 📌 NNLO finally reaching  $2 \rightarrow 2$  processes
- 📌 Resummation setting NNLL as new standard
- 📌 Improvements for NLO+PS and high degree of automation
- 📌 Higgs moving towards N3LO
- 📌 + many other issues not discussed (including jet structure)!

Thanks to Sven Moch, Frank Tackmann, Stefan Dittmaier, Massimiliano Grazzini and Joey Huston for discussions

# Thanks!