Motivation for an LO version of the HERAPDF

PDFs at LO are used for the simulation of parton showers, underlying event, minimum bias and pile-up.
A set of LO PDFs together with a ‘matching’ set of NLO PDFs is useful for NLO+PS calculations such as MC@NLO OR POWHEG.

The LHC at 13 or 14TeV will extend kinematic coverage to lower values of Bjorken $x$.

The HERAPDF has a special emphasis on low $x$ because it fits only HERA data.
HERAPDF uses the combined H1 and ZEUS data on:

- Inclusive Neutral and Charged Current processes for $e^+p$ and $e^-p$ scattering at 820,920 GeV proton beam energy from HERA-I (HERAPDF1.0) published and HERA I+II (HERAPDF1.5) still preliminary- soon to be superceded – see other talks

This means that HERAPDF uses purely proton data

- No need for deuterium corrections, or heavy target corrections
- No assumption on strong isospin needed to get the d-quark
- A very well understood consistent data set JHEP 1001 (2010) 109 + updates

The HERA data combination gives us a well understood, consistent and accurate data set with systematic errors which are smaller than the statistical errors across most of the kinematic plane. The total errors are ~1% for $Q^2$ ~20-100 GeV$^2$ and less than 2% for most of the rest of kinematic plane.

This allows us to use the $\chi^2$ tolerance $\Delta\chi^2 =1$ to set 68% limits on the PDFs from experimental sources
Where does the information on parton distributions come from?

**CC e-p**
\[
d^2 \sigma(e^- p) = \frac{G_F^2 M^4_W}{2\pi x (Q^2 + M^2_W)^2} \left[ x (u+c) + (1-y)^2 x (d+s) \right]
\]

**CC e+p**
\[
d^2 \sigma(e^+ p) = \frac{G_F^2 M^4_W}{2\pi x (Q^2 + M^2_W)^2} \left[ x (u+c) + (1-y)^2 x (d+s) \right]
\]

- The charged currents give us flavour information for high-\(x\) valence PDFs

**NC e+ and e-**
\[
d^2 \sigma(e^\pm N) = \frac{2\pi \alpha_s^2 s}{Q^4} Y^+ \left[ F_2(x, Q^2) - y^2 \frac{F_L(x, Q^2)}{Y^+} \right] \pm \frac{Y^- x F_3(x, Q^2)}{Y^+}, \quad Y^\pm = 1 \pm (1-y)^2
\]

\[
F_2 = F_2^y - v_e P_Z^y F_2^y Z + (v_e^2 + a_e^2) P_Z^2 F_2^Z
\]

\[
xF_3 = - a_e P_Z^y x F_3^y Z + 2 v_e a_e P_Z^2 x F_3^Z
\]

Where \(P_Z^2 = Q^2/(Q^2 + M^2_Z)\), and at LO

\[
[F_2, F_2^y Z, F_2^Z] = \sum_i [e_i^2, 2e_i v_i, v_i^2 + a_i^2][x q_i(x, Q^2) + x \bar{q}_i(x, Q^2)]
\]

\[
[x F_3^y Z, x F_3^Z] = \sum_i 2[e_i a_i, v_i a_i][x q_i(x, Q^2) - x \bar{q}_i(x, Q^2)]
\]

So that \(xF_3^y Z = 2x[e_u a_u u_v + e_d a_d d_v] = x/3 (2u_v + d_v)

Where \(xF_3^y Z\) is the dominant term in \(xF_3\)

The neutral current \(F_2\) gives the low-\(x\) Sea

The difference between e- and e+ also gives a valence PDF for \(x > 0.01\) - not just at high-\(x\)

And of course the scaling violations give the gluon PDF
This page shows NC e+ combined data

Above: Results of the combination compared to the separate data sets

Right: the full NC e+ data

Note the kinematic coverage to very low x
HERAPDF1.0 at NLO is published (JHEP 1001 -109). It has been updated to HERAPDF1.5 NLO and NNLO: this is an update of data AND fit.

Uses preliminary HERA I+II data combination

The HERAPDF1.5 LO is based on these data

Soon to be superseded. See other HERA talks.
Reminder of released PDF sets from HERA

- In LHAPDF:
  - HERAPDF1.0 NLO: based on published HERA I data (with Uncertainties)
  - HERAPDF1.5 NLO: based on preliminary HERA I+II data (with Uncertainties)
  - HERAPDF1.5 NNLO: based on preliminary HERA I+II data (with Uncertainties)

- Studies
  - HERAPDF1.0 NNLO: based on published HERA I data (2 central lines with different alphas)
  - HERAPDF1.6 NLO: based on preliminary HERA I+II and inclusive jets
  - HERAPDF1.7 NLO: based on preliminary HERA I+II, inclusive jets, charm, low energy runs

And HERAPDF2.0(prel.) to be presented at THIS Conference
The QCD fit was performed using the HERAFitter. 
As far as possible the same settings are used as for HERAPDF1.5 NLO.

- **Data:**
  - Use HERA 1+2 preliminary data as used for HERAPDF1.5 series.
  - 130 sources uncorrelated, 3 procedural (arising from the procedure of data combination) correl.
  - HERAPDF chi-square style, with $\Delta \chi^2 = 1$ criterion.

\[
\chi^2 = \sum_i \left[ \frac{\mu_i - m_i \left(1 - \sum_j \gamma^b_j\right)}{\delta_{i,\text{unc}}^2 m_i^2 + \delta_{i,\text{stat}}^2 \mu_i m_i \left(1 - \sum_j \gamma^b_j\right)} \right]^2 + \sum b_j^2
\]

- **Theory:**
  - Use 10p fit as done for HERAPDF1.5NLO (parametrisation with positive defined PDFs).

\[
\begin{align*}
ux_v(x) &= A_{uv} x^{B_{uv}(1-x)} C_{uv}(1 + E_{uv} x^2) \\
xd_v(x) &= A_{dv} x^{B_{dv}(1-x)} C_{dv} \\
x\bar{u}(x) &= A_{\bar{u}} x^{B_{\bar{u}}(1-x)} C_{\bar{u}} \\
x\bar{D}(x) &= A_{\bar{D}} x^{B_{\bar{D}}(1-x)} C_{\bar{D}} \\
xg(x) &= A_g x^{B_g(1-x)} C_g.
\end{align*}
\]

At $Q^2_0=1.9$ GeV$^2$

$A_{uv}, A_{dv}, A_g$ from the number and momentum sum-rules.

$B_{uv} = B_{dv}, B_{\bar{u}bar} = B_{d\bar{a}r}$

$A_{d\bar{a}r}, A_{\bar{u}bar}$ such that $u\bar{a}r = d\bar{a}r$ as $x \to 0$

Strangeness fraction suppressed such that $s\bar{a}r \sim d\bar{a}r/2$

$Q^2 > 3.5$ GeV$^2$, $m_c=1.4$ GeV, $m_b=4.75$ GeV,

Heavy quarks from the Thorne-Roberts variable Flavour Number Scheme at LO.

Note FL at LO is considered to be $O(\alpha_s)$ not zero.
The value of $\alpha_S(M_Z)$ at LO is not held the same as the NLO value. A $\chi^2$ scan is performed to determine the best value $\alpha_S(M_Z) = 0.13$

This is similar to the LO value used by CTEQ6

The $\chi^2$ of the fit is 762 for 664 degrees of freedom. This is only somewhat worse than the NLO fit which has $\chi^2 = 736$

THE LO PDFS are provided with experimental uncertainties in the eigenvector format.

Compare the LO, NLO and NNLO gluons at the starting scale and at the mass$^2$ of the W
Differences are less in the valence and sea sectors
Note the good description of low x data – even below the $Q^2$ cut of the fit
Data/ Fit comparison for high $Q^2$ NC e+ and e-
Data/ Fit comparison for high $Q^2$ CC $e^+$ and $e^-$
The HERAPDF1.5 at LO – PDF distributions

H1 and ZEUS HERA I+II Combined PDF Fit

\[ Q^2 = 1.9 \text{ GeV}^2 \]

\[ Q^2 = 10000 \text{ GeV}^2 \]

HERAPDF1.5 LO (prel.)
exp. uncert.
Comparisons with other LO PDFs at the starting scale $Q^2=1.9 \text{ GeV}^2$
Comparisons with other LO PDFs at the starting scale $Q^2=M_w^2$
Comparison on $J/\psi$ data

Using photoproduction $J/\psi$ to probe small $x$ gluons

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August 28th 2013
USE of HERAPDF1.5 LO in tuning

CTEQ6L used for comparison
checks done with and w/o simulation of multiparton interactions

1. Inclusive jets (in central and forward region)
   (important cross check, since these measurements are used also for PDF determination and NP&PS corrections determined from shower MCs are applied to NLO predictions used in the PDF fits)
2. Energy flow in forward region

3. Underlying Event (charged particle multiplicity in transverse region as function of leading jet or leading track pt)
Inclusive jets

- MC describes measurements without MPI:
  - HERAPDF1.5LO agrees with CTEQ6L (Z2* is a PYTHIA tune tuned to CTEQ6L)

- significant effect from MPI
  - gluon at small x very important
  - POWHEG is better with MPI included
Energy flow

- without MPI, predictions agree but are too low compared to data
- with MPI, CTEQ6L and HERAPDF1.5LO both agree with measurement
Underlying event

- With MPI predictions agree with each other
- Without MPI data are not described

- With MPI, HERAPDF1.5LO gives better description of UE measurements (even without further tuning) compared to CTEQ6L
HERAPDF1.5LO describes measurements similarly to CTEQ6L

HERAPDF1.5LO gives better agreement with UE measurements than CTEQ6L, although parameters were tuned to CTEQ6L.

description can be further improved with tuning MPI parameters

HERAPDF1.5LO can be used for MC simulation:

for non-perturbative (hadronization +MPI) correction

for parton shower corrections, which are essential for jets, vector-boson, Higgs etc if measurements to be compared to NLO parton level calcs


simulation of min-bias events (50 – 100 pileup events expected)
A LO PDF is particularly useful for Monte Carlo event generators and the simulation of higher order corrections via parton showers.

Presented a LO HERAPDF1.5 PDF set based on preliminary HERA I+II combined data including experimental uncertainties.

- Based on identical settings as HERAPdf1.5 NLO (different alphas)
- Initial tests show that HERAPDF LO set describes measurements similarly to CTEQ 6LO (even if parameters were tuned for CTEQ!)

The set is presented with 10 EIG to express the experimental precision
The set is readily formatted for the LHAPDFv5 style.

And for LHAPDFv6
EXTRAS