

3rd MCNet Meeting / Göstafest, Lund, January 2008

Time-like Showers and Matching with Antennae

Peter Skands

CERN & Fermilab

In collaboration with R. Frederix, W. Giele, D. Kosower, T. Sjöstrand



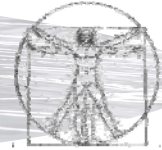
Parton Showers

- ▶ **The final answer depends on:**
 - The choice of evolution variable
 - The splitting functions (finite/subleading terms not fixed)
 - The phase space map ($d\Phi_{n+1}/d\Phi_n$)
 - The renormalization scheme (argument of α_s)
 - The infrared cutoff contour (hadronization cutoff)
- ▶ **Step 1, Quantify uncertainty:** vary all of these (within reasonable limits)
- ▶ **Step 2, Systematically improve:** Understand the importance of each and how it is canceled by
 - Matching to fixed order matrix elements
 - Higher logarithms, subleading color, etc, are included
- ▶ **Step 3, Write a generator:** Make the above explicit (while still tractable) in a Markov Chain context → matched parton shower MC algorithm



VINCIA

VIRTUAL NUMERICAL COLLIDER WITH INTERLEAVED ANTENNAE



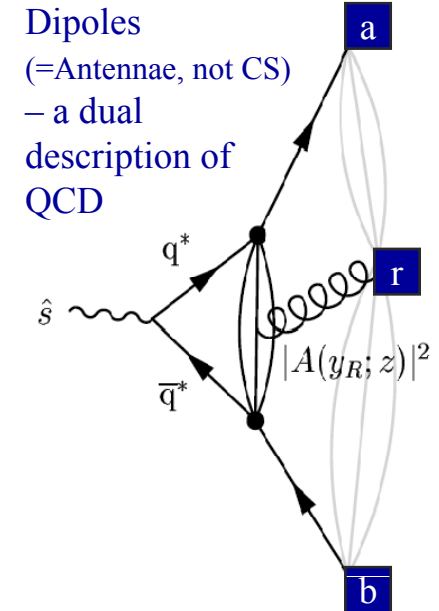
Gustafson, PLB175(1986)453; Lönnblad (ARIADNE), CPC71(1992)15.
Azimov, Dokshitzer, Khoze, Troyan, PLB165B(1985)147
Kosower PRD57(1998)5410; Campbell, Cullen, Glover EPJC9(1999)245

► Based on Dipole-Antennae

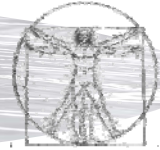
- Shower off color-connected pairs of partons
- Plug-in to PYTHIA 8.1 (C++)

► So far: Giele, Kosower, PS : hep-ph/0707.3652 + Les Houches 2007

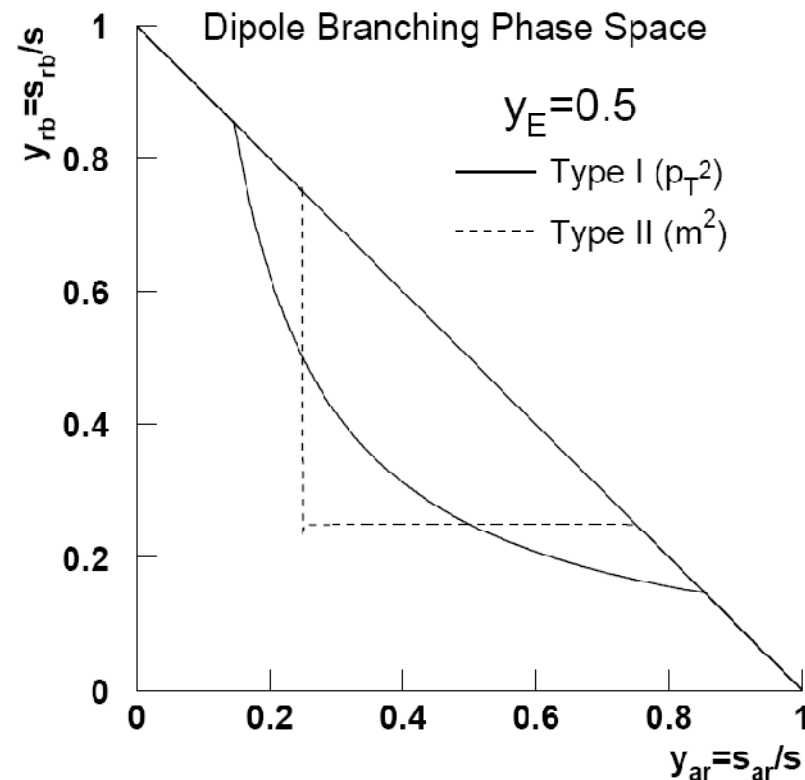
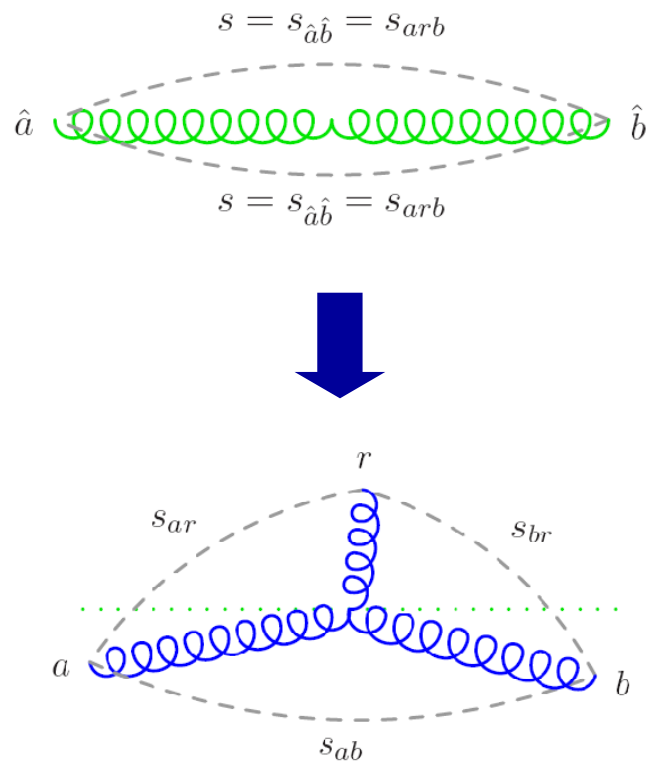
- Time-like QCD cascades (with massless quarks)
- 2 different shower evolution variables:
 - pT-ordering (= ARIADNE ~ PYTHIA 8)
 - Dipole-mass-ordering (~ Thrust ≠ PYTHIA 6, SHERPA)
- For each: an infinite family of antenna functions
 - Laurent series in branching invariants with arbitrary finite terms
- Shower cutoff contour: independent of evolution variable
 - IR factorization “universal”
- Several different choices for α_s (evolution scale, p_T , mother antenna mass, 2-loop, ...)
- Phase space mappings: 2 different choices implemented
 - Antenna-like (ARIADNE angle) or Parton-shower-like: Emitter + longitudinal Recoiler



Dipole-Antenna Showers

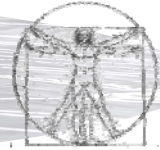


► Dipole branching and phase space



(→ Most of this talk, including matching by antenna subtraction, should be applicable to ARIADNE as well)

Example: Z decays



► **VINCIA and PYTHIA8** (using identical settings to the max extent possible)

$$\alpha_s(p_T),$$

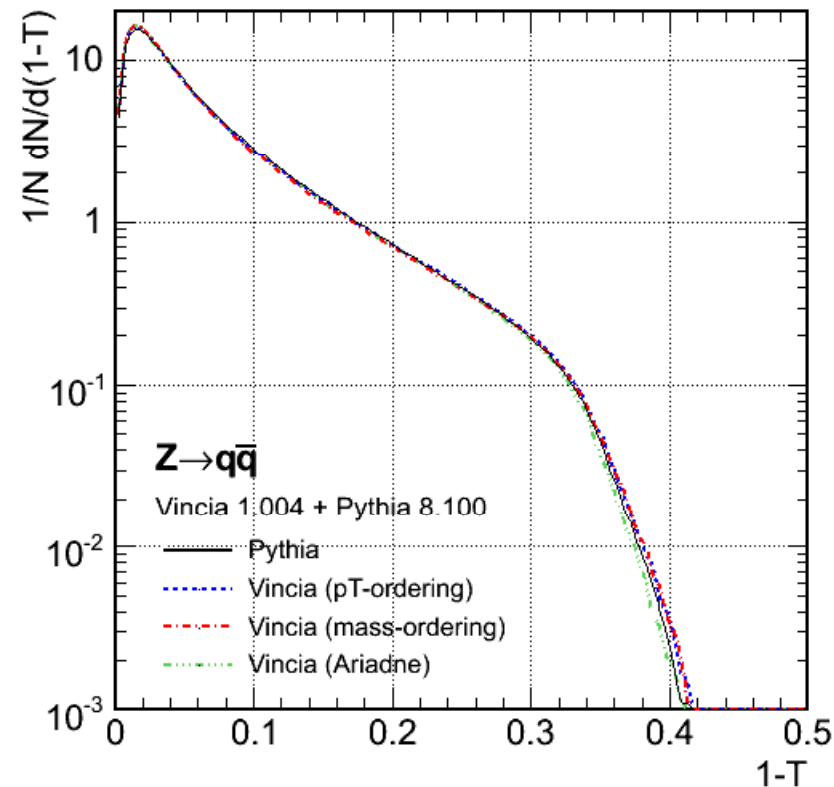
$$p_{\text{Thad}} = 0.5 \text{ GeV}$$

$$\alpha_s(m_Z) = 0.137$$

$$N_f = 2$$

Note: the default Vincia antenna functions reproduce the $Z \rightarrow 3$ parton matrix element;

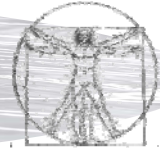
Pythia8 includes matching to $Z \rightarrow 3$



Frederix, Giele, Kosower, PS : Les Houches Proc., in preparation



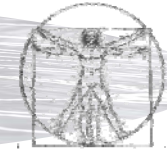
Example: Z decays



- ▶ Why is the dependence on the evolution variable so small?
 - Conventional wisdom: evolution variable has huge effect
 - Cf. coherent vs non-coherent parton showers, mass-ordered vs p_T -ordered, etc.
- ▶ Dipole-Antenna showers resum radiation off *pairs* of partons
 - → interference between 2 partons included in radiation function
 - If radiation function = dipole formula → intrinsically coherent
 - → angular ordering there by construction [Gustafson, PLB175\(1986\)453](#)
 - Remaining dependence on evolution variable much milder than for conventional showers
- ▶ The main uncertainty in this case lies in the choice of radiation function away from the collinear and soft regions
 - → dipole-antenna showers under the hood ...



Dipole-Antenna Functions



Giele, Kosower, PS : hep-ph/0707.3652

- ▶ Starting point: “GGG” antenna functions, e.g., $gg \rightarrow ggg$:

Gehrmann-De Ridder, Gehrmann, Glover, JHEP 09 (2005) 056

$$f_3^0(p_a, p_r, p_b) = \frac{1}{s^{[i]}} \left[(1 - y_{ar} - y_{rb}) \left(\underbrace{\frac{2}{y_{ar}y_{rb}}}_{\text{“soft”}} + \underbrace{\frac{y_{ar}}{y_{rb}} + \frac{y_{rb}}{y_{ar}}}_{\text{“collinear”}} \right) + \frac{8}{3} \right]$$

$$y_{ar} = s_{ar} / s_i$$

s_i = invariant mass of i 'th dipole-antenna

- ▶ Generalize to arbitrary Laurent series:

$$A(s_{ar}, s_{rb}) = \frac{4\pi\alpha_s(\mu_R)N_C}{s_{arb}} \sum_{\alpha, \beta \geq -1} C_{\alpha\beta} \frac{s_{ar}^\alpha s_{rb}^\beta}{s_{arb}^{\alpha+\beta}}$$

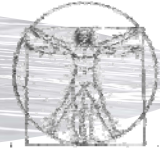
Singular parts fixed, finite terms arbitrary

- ➔ Can make shower systematically “softer” or “harder”

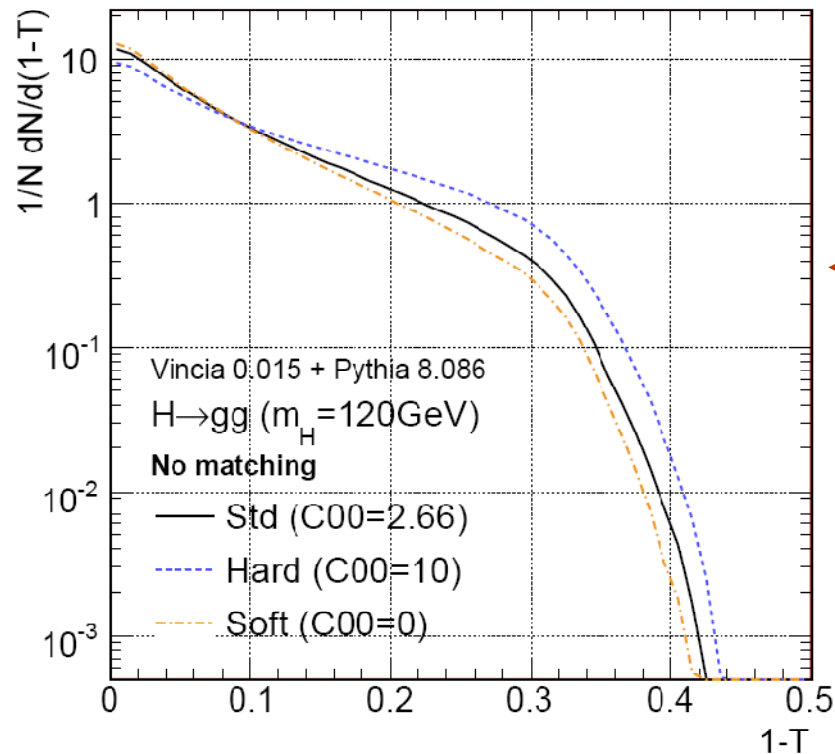
- Will see later how this variation is explicitly canceled by matching
- ➔ quantification of uncertainty
- ➔ quantification of improvement by matching



Quantifying Matching



- ▶ The unknown finite terms are a major source of uncertainty
 - DGLAP has some, GGG have others, ARIADNE has yet others, etc...
 - They are arbitrary (and in general process-dependent)



← Varying finite terms only

with

$$\alpha_s(M_Z) = 0.137,$$
$$\mu_R = 1/4 m_{\text{dipole}},$$
$$p_{\text{Thad}} = 0.5 \text{ GeV}$$

Giele, Kosower, PS : hep-ph/0707.3652



Matching



Pure Shower
(all orders)

$$\left. \frac{d\sigma_X}{d\mathcal{O}} \right|_{\text{PS}} = \int d\Phi_X w_X S(\{p\}_X, \mathcal{O})$$

$$w_X : |M_X|^2$$

S : Evolution operator

$\{p\}$: momenta

$$S(\{p\}_X, \mathcal{O}) = \underbrace{\delta(\mathcal{O} - \mathcal{O}(\{p\}_X)) \Delta(t_X, t_{\text{had}})}_{X + 0 \text{ exclusive above } 1/t_{\text{had}}} \leftarrow \begin{array}{l} \text{“X + nothing”} \\ \text{“X+something”} \end{array}$$

$$+ \underbrace{\int_{t_X}^{t_{\text{had}}} dt_{X+1} \sum_i \int \frac{d\Phi_{X+1}^{[i]}}{d\Phi_X} \delta(t_{X+1} - t^{[i]}(\{p\}_{X+1})) \Delta(t_X, t_{X+1}) A_i(\dots) S(\{p\}_{X+1}, \mathcal{O})}_{X + 1 \text{ inclusive above } 1/t_{\text{had}}}$$

A: splitting function



Matched shower (including simultaneous tree- and 1-loop matching for any number of legs)

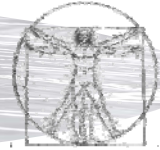
$$\left. \frac{d\sigma}{d\mathcal{O}} \right|_{\text{MS}} = \sum_{k=0}^n \int d\Phi_{X+k} \left(w_{X+k}^{(R)} + w_{X+k}^{(V)} \right) S(\{p\}_{X+k}, \mathcal{O})$$

Tree-level “real”
matching term for X+k
Loop-level “virtual+unresolved”
matching term for X+k

Giele, Kosower, PS : hep-ph/0707.3652



Tree-level matching to X+1



1. **Expand parton shower to 1st order** (real radiation term)

PS :
$$\int d\Phi_X |M_{X+0}^{(0)}|^2 \int_{t_{X+0}}^{t_{\text{had}}} dt_{X+1} \sum_i \int \frac{d\Phi_{X+1}^{[i]}}{d\Phi_X} \delta(t_{X+1} - t^{[i]}(\{p\}_{X+1})) A_i(\dots) \delta(\mathcal{O} - \mathcal{O}(\{p\}_{X+1}))$$

2. **Matrix Element** (Tree-level X+1 ; above t_{had})

ME :
$$\int_{t < t_{\text{had}}} d\Phi_{X+1} |M_{X+1}^{(0)}|^2 \delta(\mathcal{O} - \mathcal{O}(\{p\}_{X+1}))$$

Inverse phase space
map \sim clustering

$$\{\hat{p}_i\}_X = \{\kappa_i^{-1}(\{p\}_{X+1})\}_X$$

→ Matching Term:

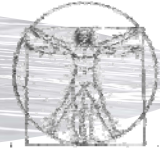
MT :
$$w_{X+1}^{(R)} = |M_{X+1}^{(0)}|^2 - \sum_{i \in X \rightarrow X+1} A_i(\dots) |M_{X+0}^{(0)}(\{\hat{p}_i\}_{X+0})|^2$$

- → variations in finite terms (or dead regions) in A_i **canceled** (at this order)
- (If A too hard, correction can become negative → **negative weights**)

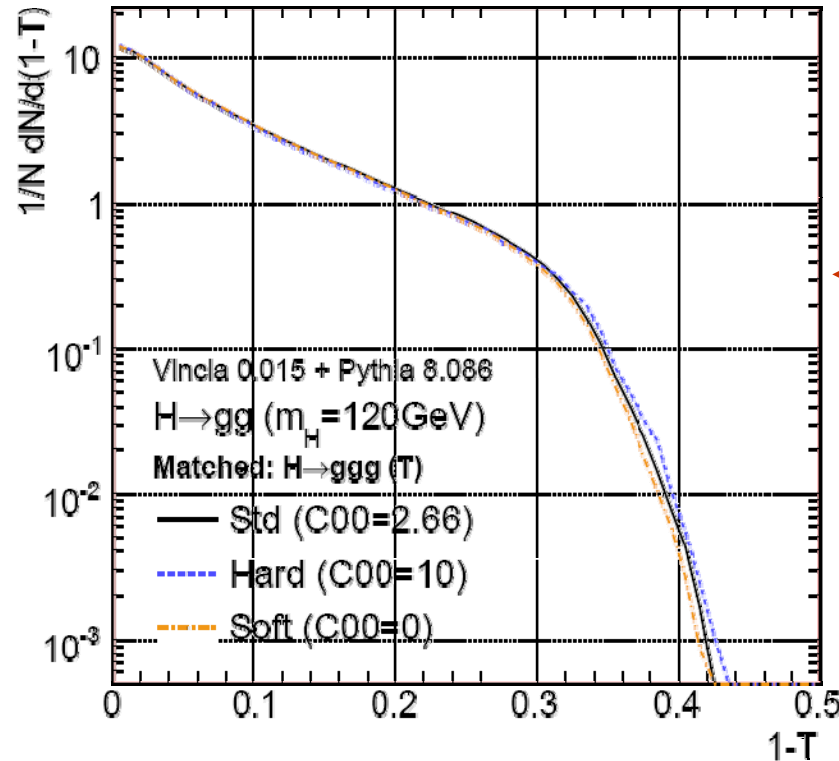
$$= \frac{8\pi\alpha_s(\mu_R)N_c}{M_H^2} \left(8 - 3C_{00} - (C_{10} + C_{01}) - C_{11} (y_{12}y_{23} + y_{23}y_{31} + y_{31}y_{12}) + \dots \right) |M_2^{(0)}|^2$$



Quantifying Matching



- ▶ The unknown finite terms are a major source of uncertainty
 - DGLAP has some, GGG have others, ARIADNE has yet others, etc...
 - They are arbitrary (and in general process-dependent)



← Varying finite terms only

with

$$\alpha_s(M_Z) = 0.137,$$

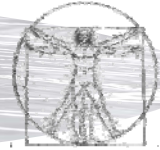
$$\mu_R = 1/4 m_{\text{dipole}},$$

$$p_{\text{Thad}} = 0.5 \text{ GeV}$$

Giele, Kosower, PS : hep-ph/0707.3652



1-loop matching to X



- ▶ NLO “virtual term” from parton shower (= expanded Sudakov: $\exp=1 - \dots$)

$$\text{PS} : - \int d\Phi_X |M_X^{(0)}|^2 \delta(\mathcal{O} - \mathcal{O}(\{p\}_X)) \int_{t_X}^{t_{\text{had}}} dt_{X+1} \sum_i \int \frac{d\Phi_{X+1}^{[i]}}{d\Phi_X} \delta(t_{X+1} - t^{[i]}(\{p\}_{X+1})) A_i(\dots)$$

- ▶ Matrix Elements (unresolved real plus genuine virtual)

$$\text{ME} : \int_{t > t_{\text{had}}} d\Phi_{X+1} |M_{X+1}^{(0)}|^2 \delta(\mathcal{O} - \mathcal{O}(\{p\}_{X+1})) + \int d\Phi_X 2 \text{Re}[M_X^{(0)} M_X^{(1)*}] \delta(\mathcal{O} - \mathcal{O}(\{p\}_X))$$

- ▶ Matching condition same as before (almost):

$$\begin{aligned} \text{MT: } w_X^{(V)} &= 2 \text{Re}[M_X^{(0)} M_X^{*(1)}] + |M_X^{(0)}|^2 \sum_i \int_{\text{all } t} \frac{d\Phi_{X+1}^{[i]}}{d\Phi_X} A_i(\dots) + \int_{t > t_{\text{had}}} d\Phi_{X+1} w_{X+1}^{(R)} \\ &= 2 \text{Re}[M_X^{(0)} M_X^{*(1)}] + |M_X^{(0)}|^2 \sum_i \int_{\text{all } t} \frac{d\Phi_{X+1}^{[i]}}{d\Phi_X} A_i(\dots) + \mathcal{O}(t_X/t_{\text{had}}), \end{aligned}$$

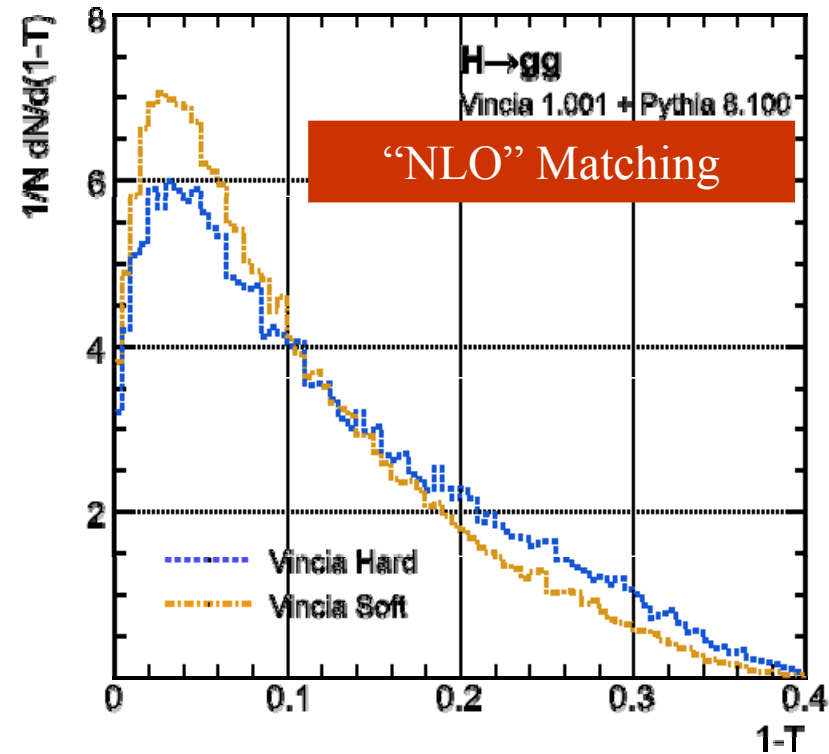
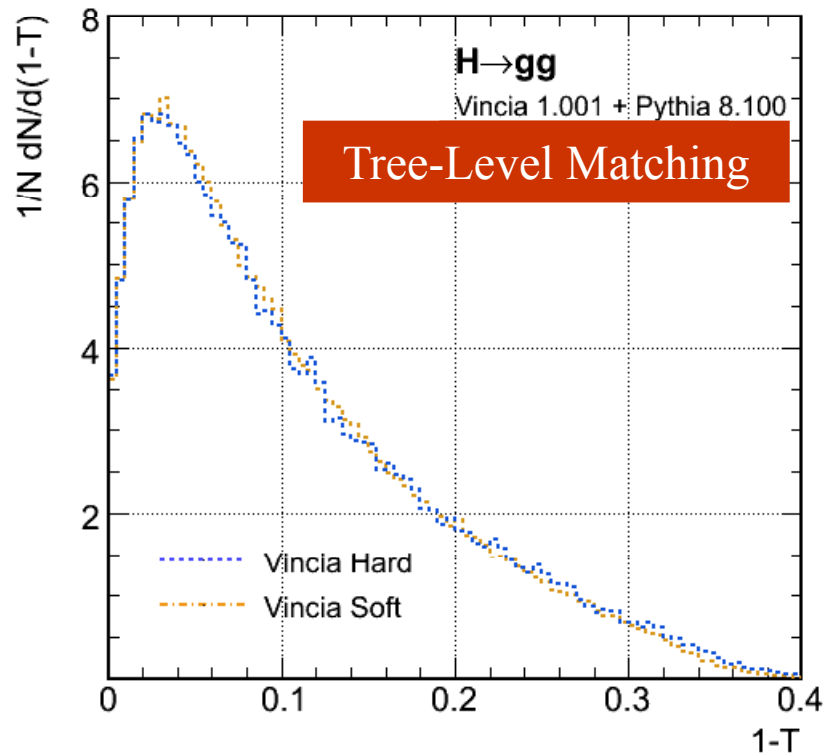
• (This time, too small A \rightarrow correction negative)

Tree-level matching just corresponds to using zero

- ▶ You can choose anything for A_i (different subtraction schemes) as long as you use the same one for the shower

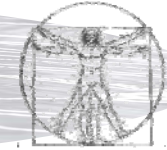
Note about “NLO” matching

- ▶ Shower off virtual matching term \rightarrow unmatched $O(\alpha^2)$ contribution to 3-jet observables (only canceled by 1-loop 3-parton matching)
- ▶ While normalization is improved, most shapes are not



Using $\alpha_s(M_Z)=0.137$, $\mu_R=1/4m_{\text{dipole}}$, $p_{\text{Thad}}=0.5 \text{ GeV}$

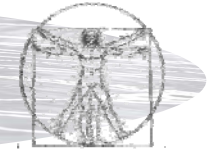
What happened?



- ▶ Brand new code, so bear in mind possibility of bugs
- ▶ Naïve conclusion: tree-level matching “better” than NLO?
 - No, first remember that the shapes we look at are not “NLO”
 - E.g., 1-T appears at $O(\alpha)$ below $1-T=2/3$, and at $O(\alpha^2)$ above
 - An “NLO” thrust calculation would have to include *at least* 1-loop corrections to $Z \rightarrow 3$
 - So: both calculations are LO/LL from the point of view of 1-T
- ▶ What is the difference then?
 - Tree-level $Z \rightarrow 3$ is the same (LO)
 - The $O(\alpha)$ corrections to $Z \rightarrow 3$, however, **are different**
 - The first non-trivial corrections to the shape!
 - So there *should* be a large residual uncertainty \rightarrow the 1-loop matching is “honest”
 - The real question: **why did the tree-level matching not tell us?**
 - I haven't completely understood it yet ... but speculate it's to do with detailed balance
 - In tree-level matching, unitarity \rightarrow **Virtual = - Real** \rightarrow cancellations. Broken at 1 loop
 - **+ the tree-level curves had different normalizations (covering the shape uncertainty?)**



What to do next?



▶ Further shower studies

- Interplay between shower ambiguities and hadronization “tuning”
- Shower+hadronization tuning in the presence of matching

▶ Go further with tree-level matching

- Demonstrate it beyond first order (include H,Z \rightarrow 4 partons)
- Automated tree-level matching (automated subtractions)

▶ Go further with one-loop matching

- Demonstrate it beyond first order (include 1-loop H,Z \rightarrow 3 partons)
 - Should start to see genuine stabilization of shapes as well as normalizations

▶ Extend to the initial state

▶ Extend to massive particles

- Massive antenna functions, phase space, and evolution

We're only a few people working part-time, so plenty of room for collaboration



Extra Material

Frederix, Giele, Kosower, PS : Les Houches Proc., in preparation

► Number of partons and number of quarks

- N_q shows interesting dependence on ordering variable

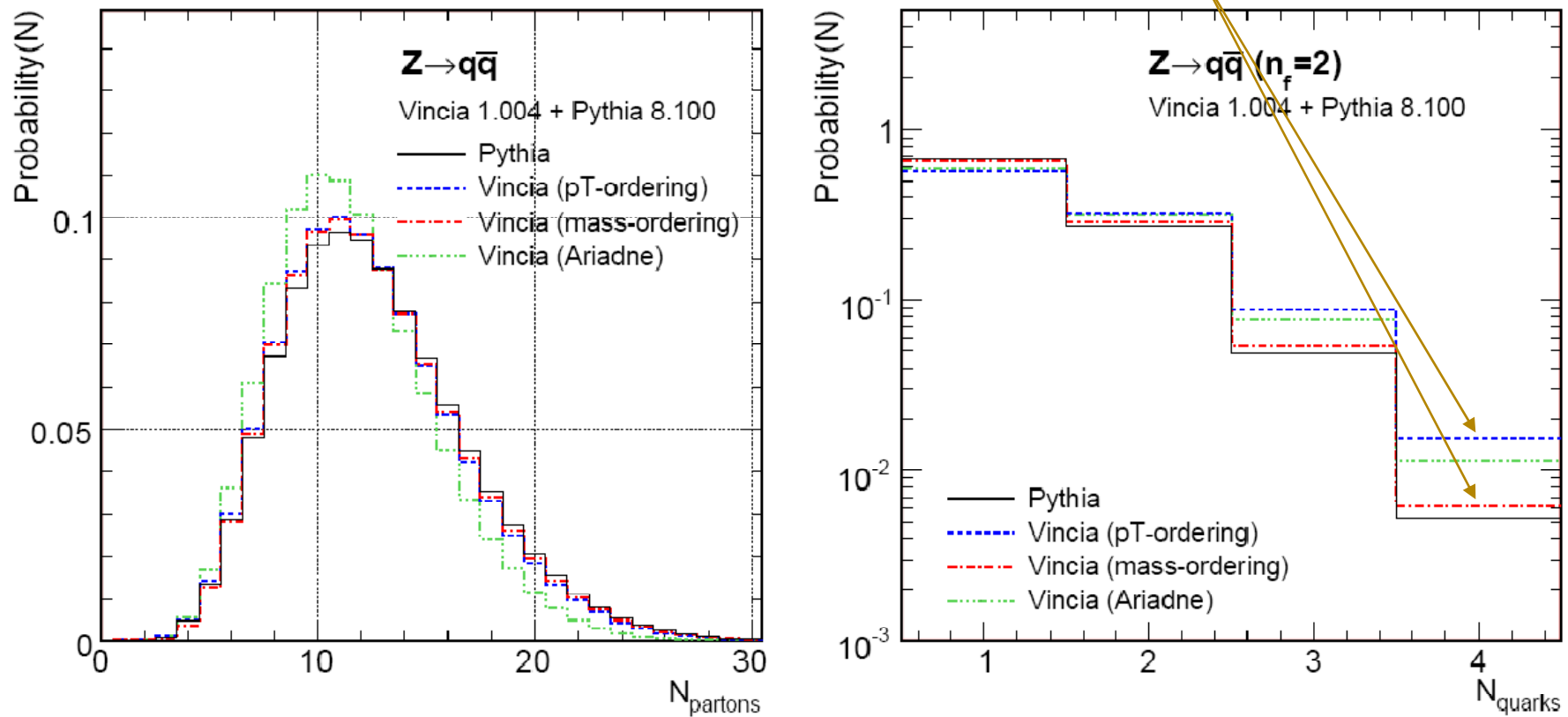


Fig. 3: Number of partons (left) and number of quarks (right) at shower termination, with 2 massless quark flavors.

Comparison

$$A(s_{ar}, s_{rb}) = \frac{4\pi\alpha_s(\mu_R)N_C}{s_{arb}} \sum_{\alpha, \beta \geq -1} C_{\alpha\beta} \frac{s_{ar}^\alpha s_{rb}^\beta}{s_{arb}^{\alpha+\beta}}$$

	C_{-1-1}	C_{-10}	C_{0-1}	C_{-11}	C_{1-1}	C_{-12}	C_{2-1}	C_{00}	C_{10}	C_{01}
G G G										
$q\bar{q} \rightarrow qg\bar{q}$	2	-2	-2	1	1	0	0	0	0	0
$qg \rightarrow qgg$	2	-2	-2	1	1	0	-1	$\frac{5}{3}$	-1	$\frac{3}{2}$
$gg \rightarrow ggg$	2	-2	-2	1	1	-1	-1	$\frac{5}{3}$	-1	-1
$qg \rightarrow q\bar{q}'q'$	0	0	$\frac{1}{2}$	0	-1	0	1	$-\frac{1}{2}$	1	0
$gg \rightarrow g\bar{q}q$	0	0	$\frac{1}{2}$	0	-1	0	1	-1	1	$\frac{1}{2}$
ARIADNE										
$q\bar{q} \rightarrow qg\bar{q}$	2	-2	-2	1	1	0	0	0	0	0
$qg \rightarrow qgg$	2	-2	-3	1	3	0	-1	0	0	0
$gg \rightarrow ggg$	2	-3	-3	3	3	-1	-1	0	0	0
$qg \rightarrow q\bar{q}'q'$	0	0	$\frac{1}{2}$	0	-1	0	1	-1	1	$\frac{1}{2}$
$gg \rightarrow g\bar{q}q$	0	0	$\frac{1}{2}$	0	-1	0	1	-1	1	$\frac{1}{2}$
ARIADNE2 (reparametrization of ARIADNE functions à la GGG, for comparison)										
$q\bar{q} \rightarrow qg\bar{q}$	2	-2	-2	1	1	0	0	0	0	0
$qg \rightarrow qgg$	2	-2	-2	1	1	0	-1	-1	0	0
$gg \rightarrow ggg$	2	-2	-2	1	1	-1	-1	$-\frac{4}{3}$	-1	-1

Table 1: Laurent coefficients for massless LL QCD antennae ($\hat{a}\hat{b} \rightarrow arb$). The coefficients with at least one negative index are universal (apart from a reparametrization ambiguity for gluons). For “GGG” (the defaults in VINCIA), the finite terms correspond to the specific matrix elements considered in [4]. In particular, the $q\bar{q}$ antenna absorbs the tree-level $Z \rightarrow qg\bar{q}$ matrix element [5] and the qg antennae absorb the tree-level $h^0 \rightarrow qg \rightarrow qgg$ and $h^0 \rightarrow qg \rightarrow q\bar{q}q$ matrix elements [6]. The

MC4BSM



Monte Carlo Tools for Beyond the Standard Model Physics

ORGANIZERS:
mc4bsm.AT.phys.ufl.edu

RESOURCES:

- [Video Lectures on Monte Carlo for the LHC](#)
- [BSM tool repository](#)
- [Summary of MC4BSM-1](#)

3rd workshop: **MARCH 10-11, 2008 (CERN)**

Note: both days will be full days. Participants who don't want to miss anything should plan on arriving Mar 9 and leaving Mar 12.

Organizing committee: Georges Azuelos, Christophe Grojean, Jay Hubisz, Borut Kersevan, Joe Lykken, Fabio Maltoni, Konstantin Matchev, Filip Moortgat, Steven Mrenna, Maxim Perelstein, Peter Skands :
mc4bsm.AT.phys.ufl.edu

Main Focus: Alternative (non-MSSM) TeV scale physics models