

# Jets @ high $Q^2$ Status report

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H1 Collaboration Meeting, September 2013  
Liverpool, 11 September 2013

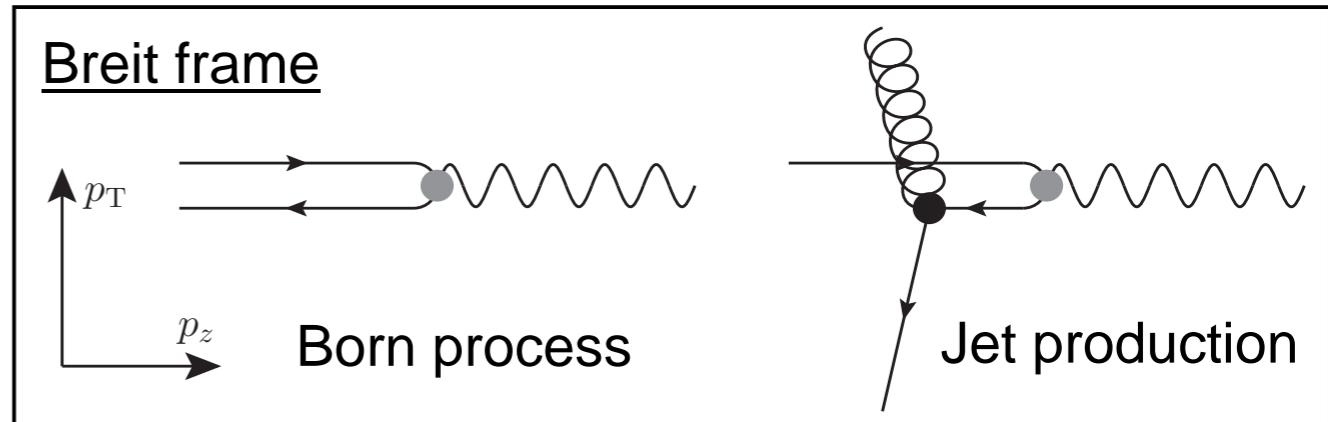


# Jet production in ep scattering

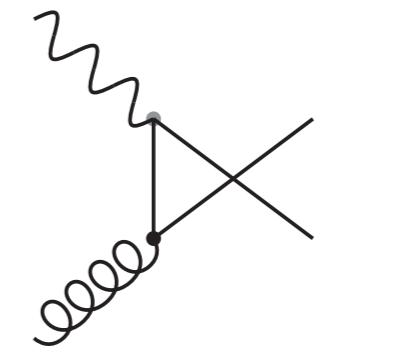
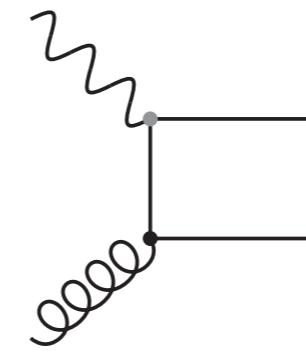
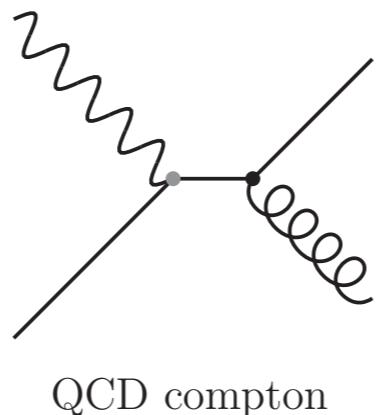
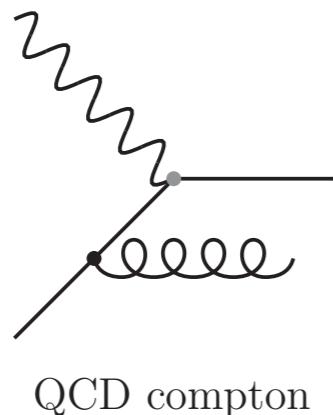
## Breit frame of reference

$$2x_{Bj}p + k = 0$$

- Only hard QCD processes generate considerable  $p_T$  in the Breit frame



## Jet production in DIS in leading-order



## Jet cross section calculable in pQCD

$$\sigma_{\text{jet}} = \sum_n \sum_{a=q,\bar{q},g} [\sigma_{n,a} \otimes f_a] (1 + \delta_{\text{had}})$$

- Expansion in orders of  $\alpha_s(\mu_r)$  with  $n \geq 1$
- Hadronization effects with correction factor
- Coefficients available up to next-to-leading order

Jet production directly sensitive to  $\alpha_s$

# Phase space of measurement

## Measurement phase space (MPS)

### Neutral current phase space

$$150 < Q^2 < 15000 \text{ GeV}^2$$

$$0.2 < y < 0.7$$

### Jet acceptance

$$-1.0 < \eta_{lab} < 2.5$$

### Inclusive Jet

$$7 < p_T^{\text{jet}} < 50 \text{ GeV}$$

### Dijet ( $n_{\text{jet}} \geq 2$ )

$$5 < p_T^{\text{jet}} < 50 \text{ GeV}$$

$$M_{12} > 16 \text{ GeV}$$

### Trijet ( $n_{\text{jet}} \geq 3$ )

$$7 < \langle p_T \rangle_2 < 50 \text{ GeV}$$

$$0.006 < \xi_2 < 0.316$$

## Extended phase space (EPS)

### Neutral current phase space

$$100 < Q^2 < 40000 \text{ GeV}^2$$

$$0.08 < y < 1.0$$

### Jet acceptance

$$-1.5 < \eta_{lab} < 2.75$$

### Inclusive Jet

$$p_T^{\text{jet}} > 3 \text{ GeV}$$

### Dijet ( $n_{\text{jet}} \geq 2$ )

$$3 < p_T^{\text{jet}} < 50 \text{ GeV}$$

### Trijet ( $n_{\text{jet}} \geq 3$ )

$$3 < \langle p_T \rangle_2 < 50 \text{ GeV}$$

$$0.0 < \xi_2 < 1.0$$

$$0.0 < \xi_3 < 1.0$$

Phase space of final data points

Extended phase space used only  
for migrations in unfolding

# Schematic definition of migration matrix

## Simultaneous unfolding

NC DIS, inclusive jet, dijet and trijet

## Covariance matrix $V_y$

takes statistical correlations of observables into account

## Individual unfolding schemes

- $E, J_1, J_2, J_3$  studied in detail
- Are optimized separately using MC

## Matrices $B_i$

Constrain reconstructed but not generated contributions

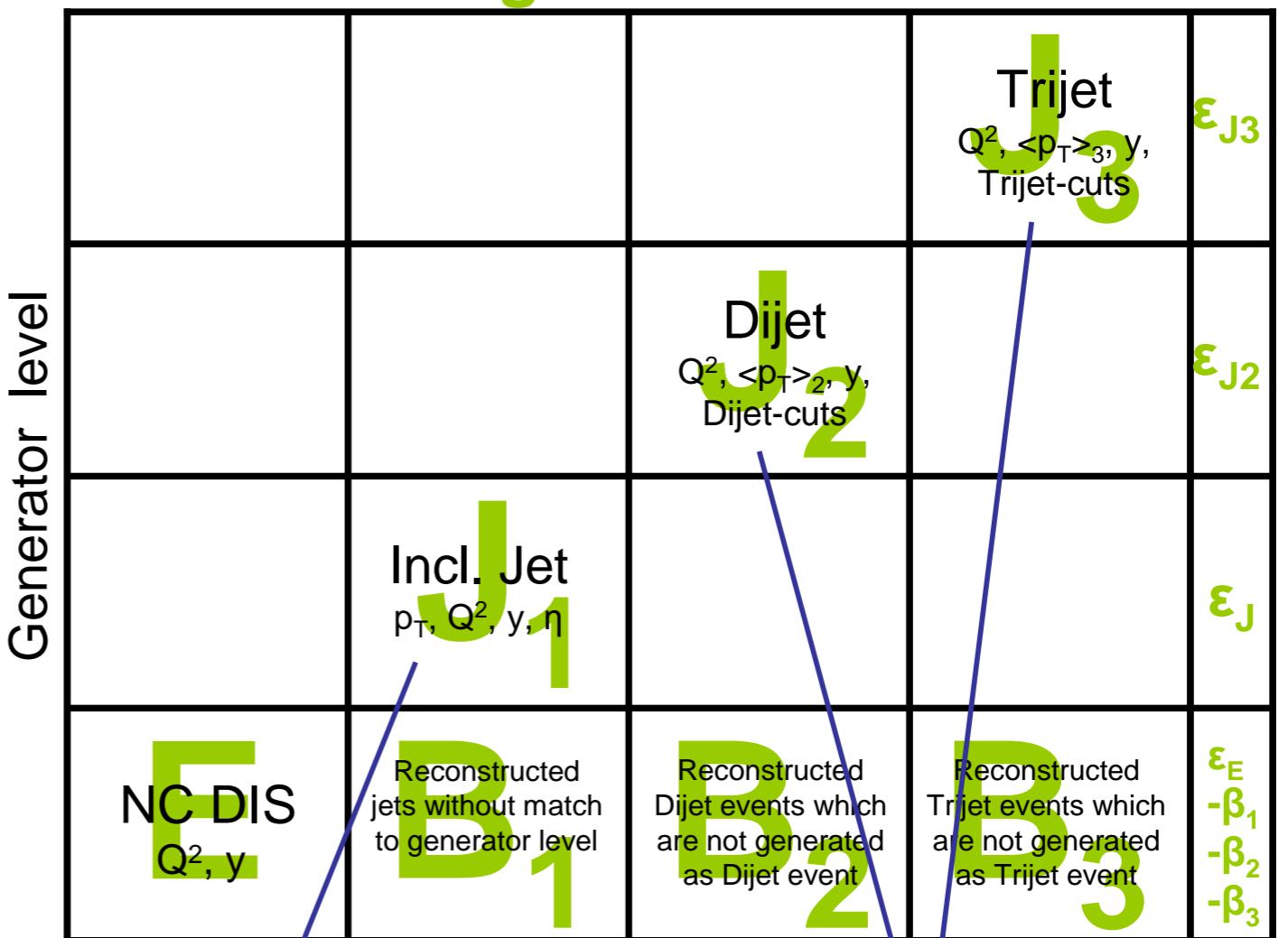
## Two MC generators

Django and Rapgap

## Phase space is enlarged

in all variables where migrations are relevant

## Migration Matrix



4-dimensional  
unfolding in  
 $p_T, Q^2, y, \eta$

Up to 7 observables  
are considered to  
describe migrations

# Problem with uncertainties after unfolding

## Systematic uncertainties

Alternative unfolding matrix is determined for every source of systematic uncertainty

- Jet energy scale (JES)
- Remaining cluster energy scale (RCES)
- Electron angle ( $E_\theta$ )
- Electron energy ( $E_e$ )

Uncertainty is propagated analytically

- using linear error propagation formulae to generator level distribution

Uncertainties show large fluctuations ( $O(\%)$ )

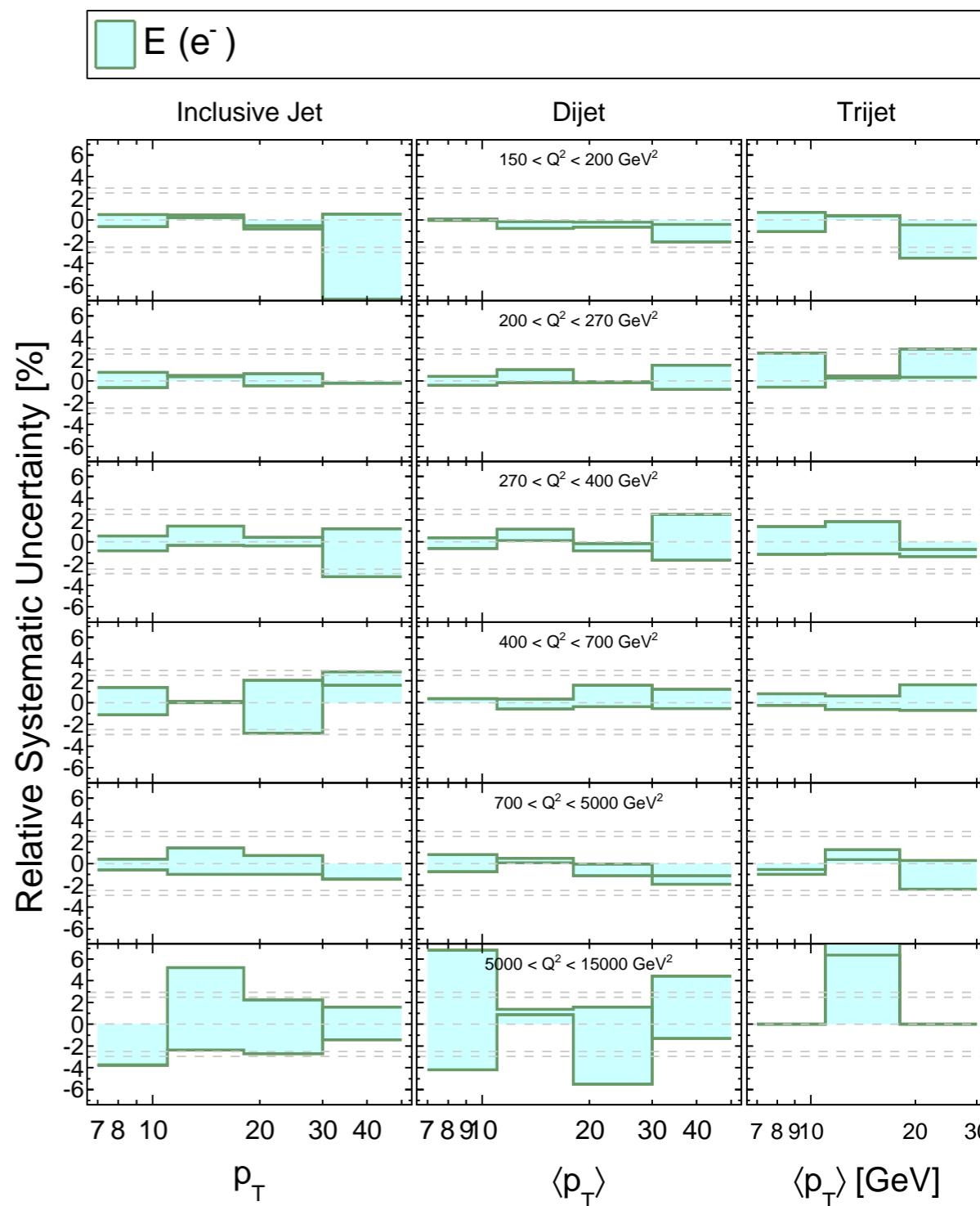
## Unclear

Caused by

- limited data statistics?
- limited MC statistics? -> New MC production

Impact on fit

- Does fluctuation ‘mimic’ statistical fluctuation  
-> Causing large nuisance parameters



# New Monte Carlo production

## New Rapgap and Django MC

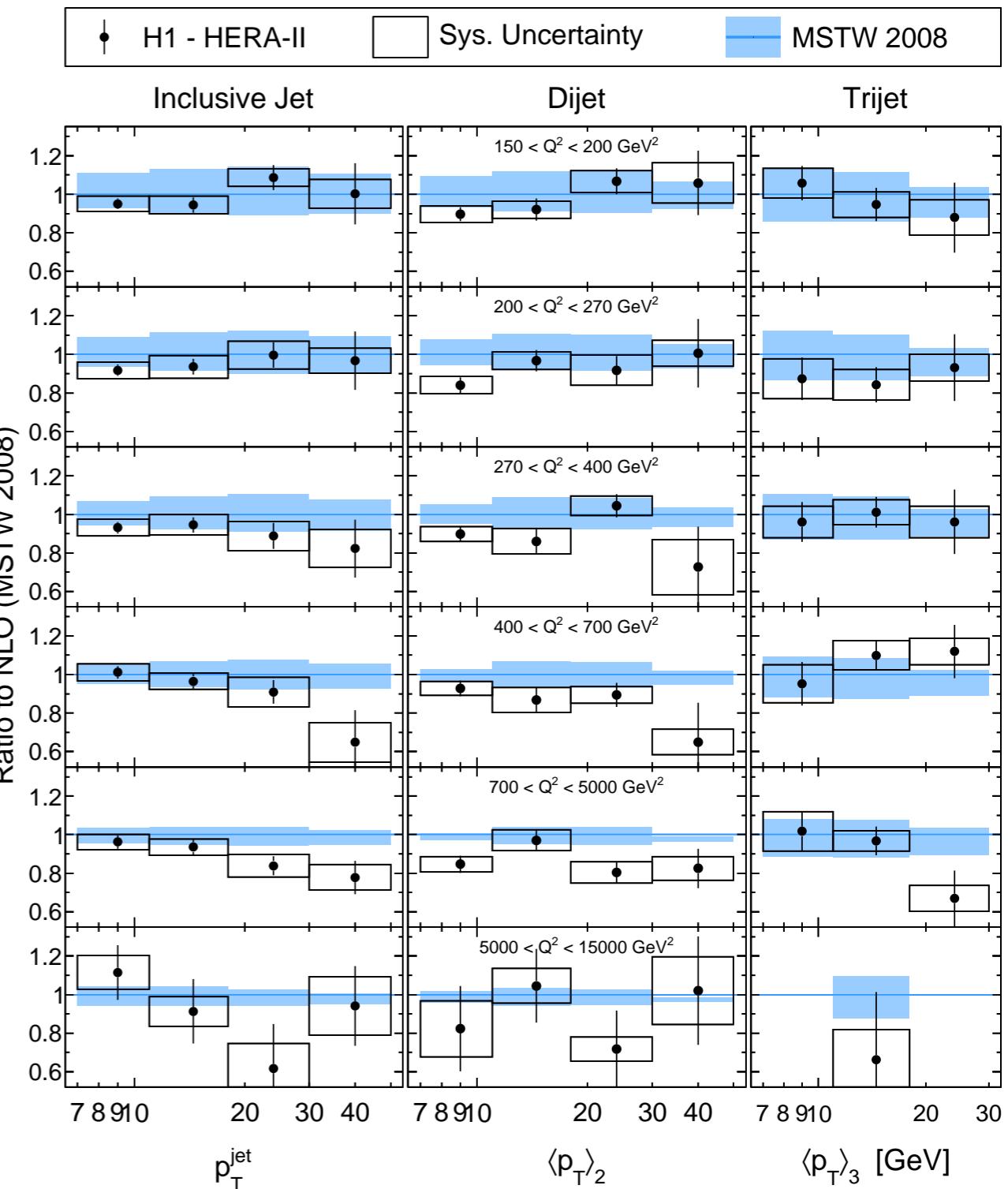
### Huge statistics

- 40  $\text{fb}^{-1}$  of MC data for every generator
- New controlplots very well consistent with old ones

### Two Sim/Rec files corrupt

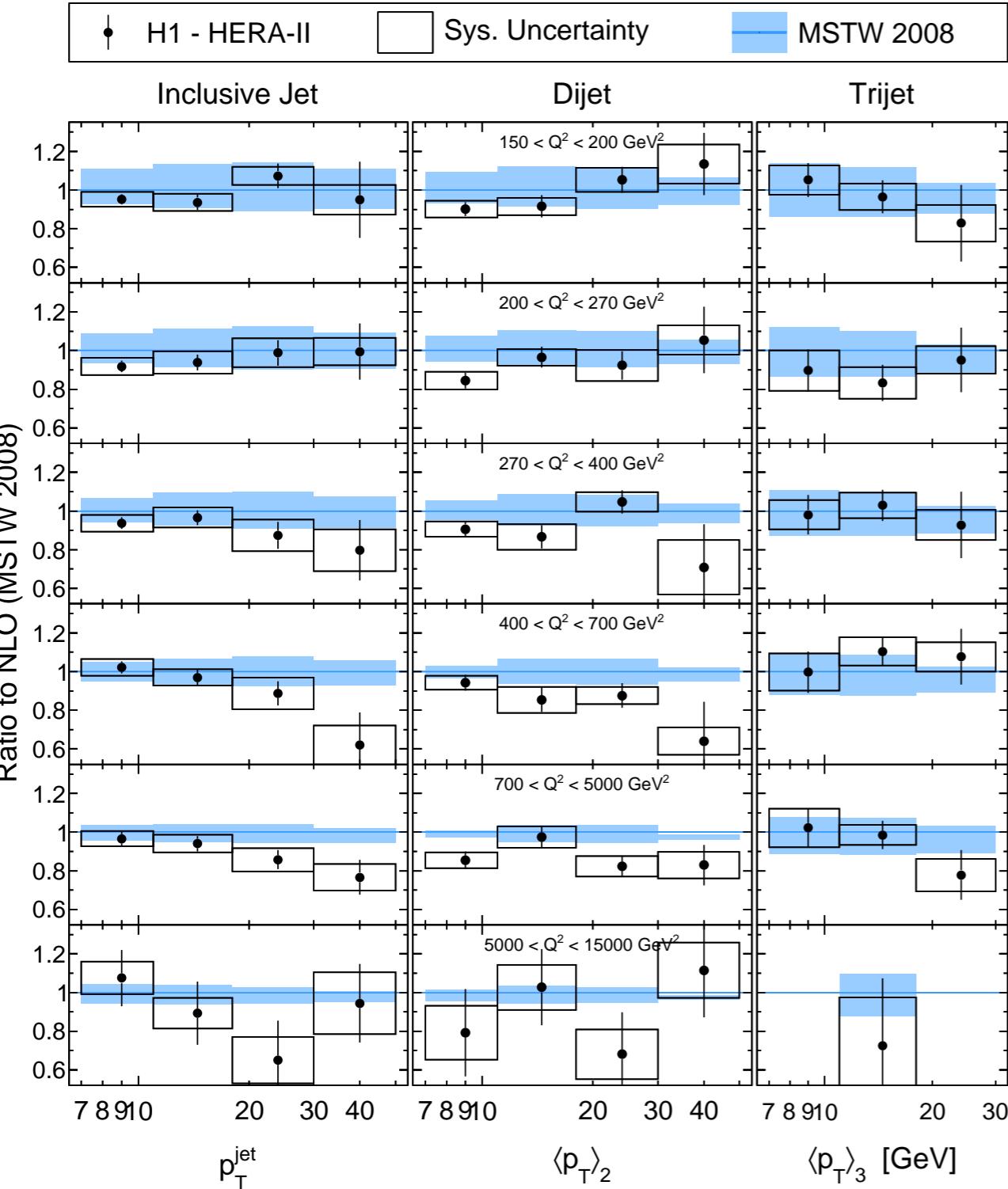
- Therefore today only:  
'almost-almost-close-tovery-finalfinal2\_4'  
cross sections

### Hardly any effect on cross sections or uncertainties

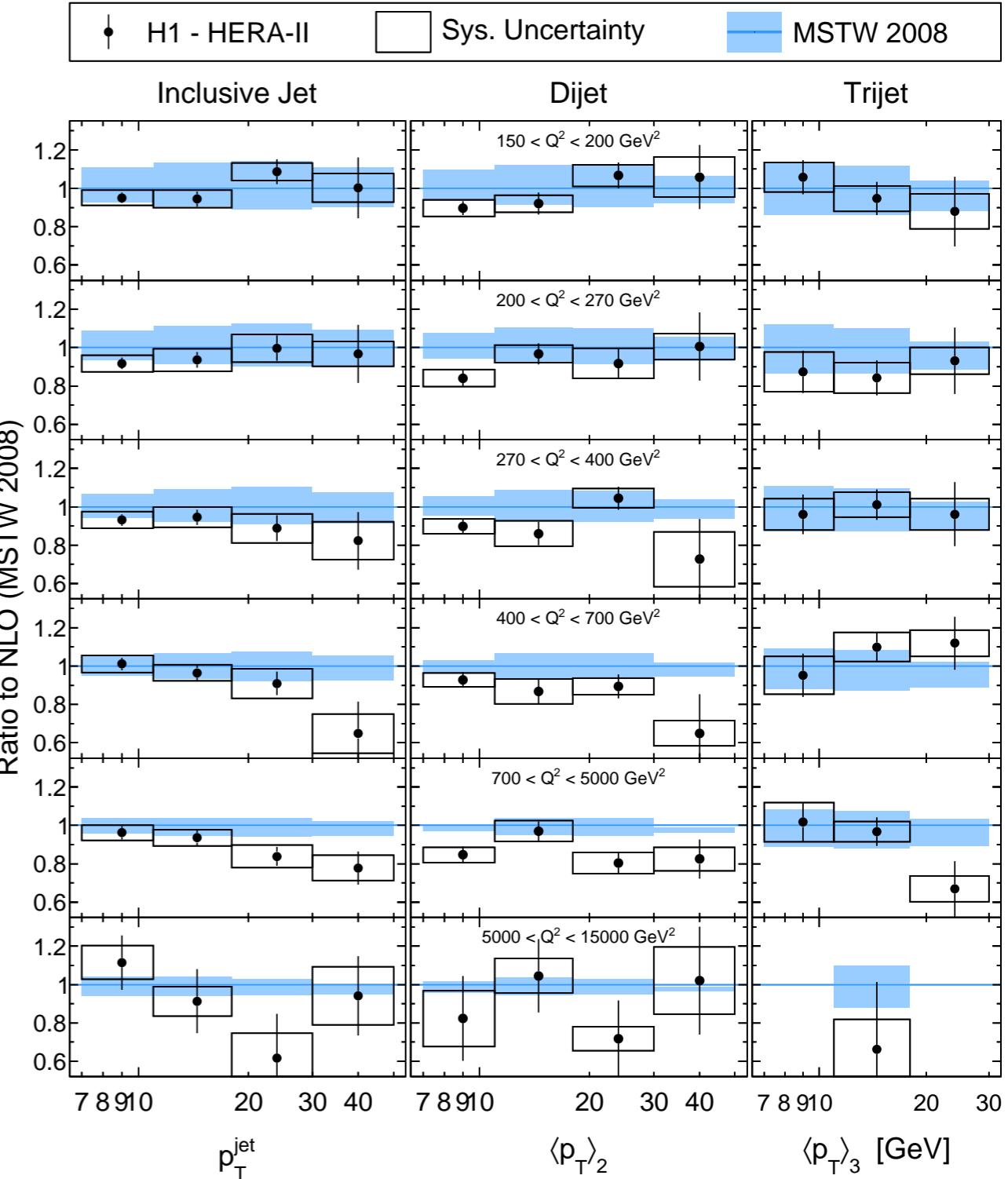


# Comparison to old MCs ( $\tau=10^{-6}$ )

Using 'old MC'



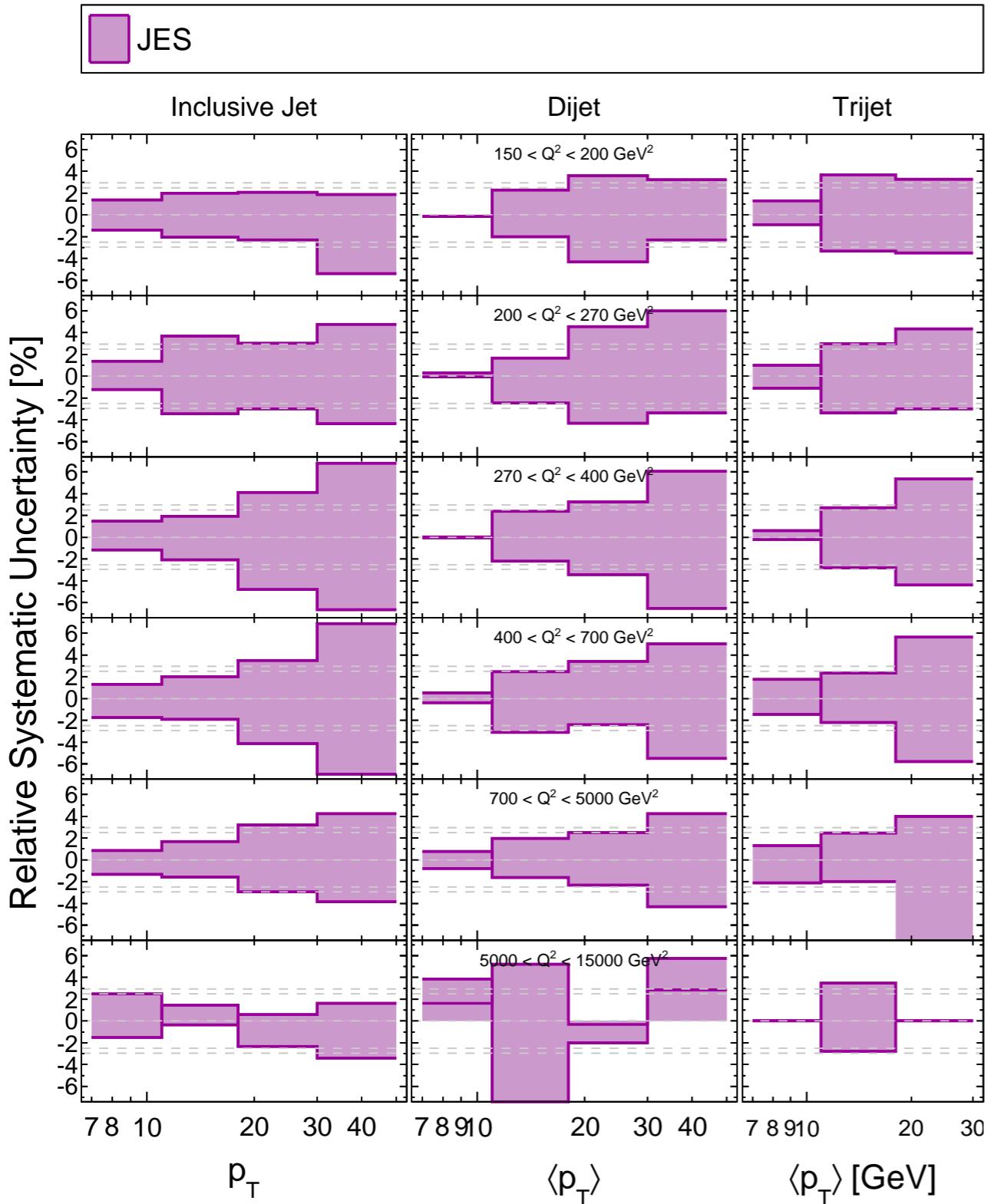
Using 'old+new MC'



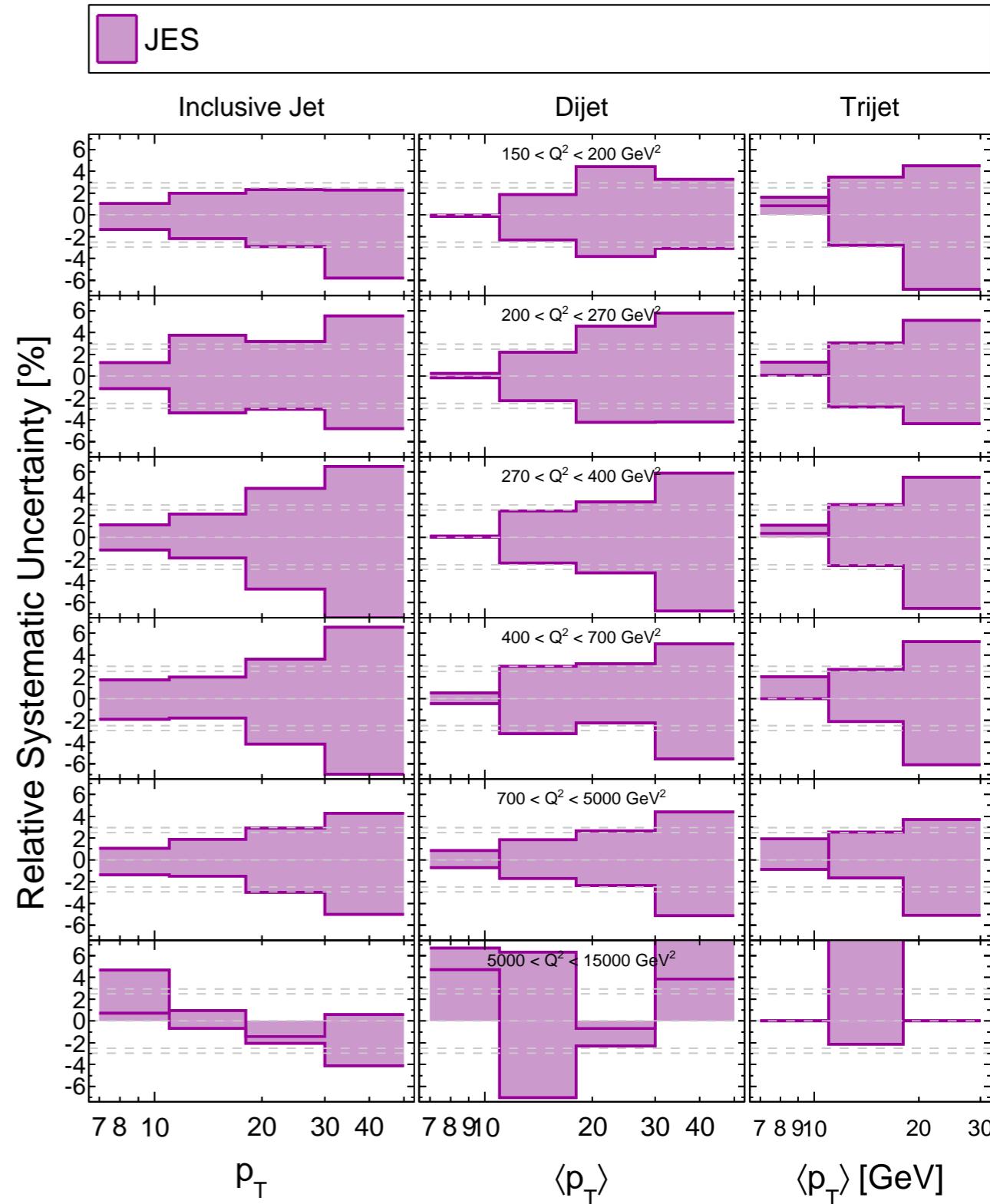
Overall picture does not change

# Comparison of uncertainties

Using ‘old MC’

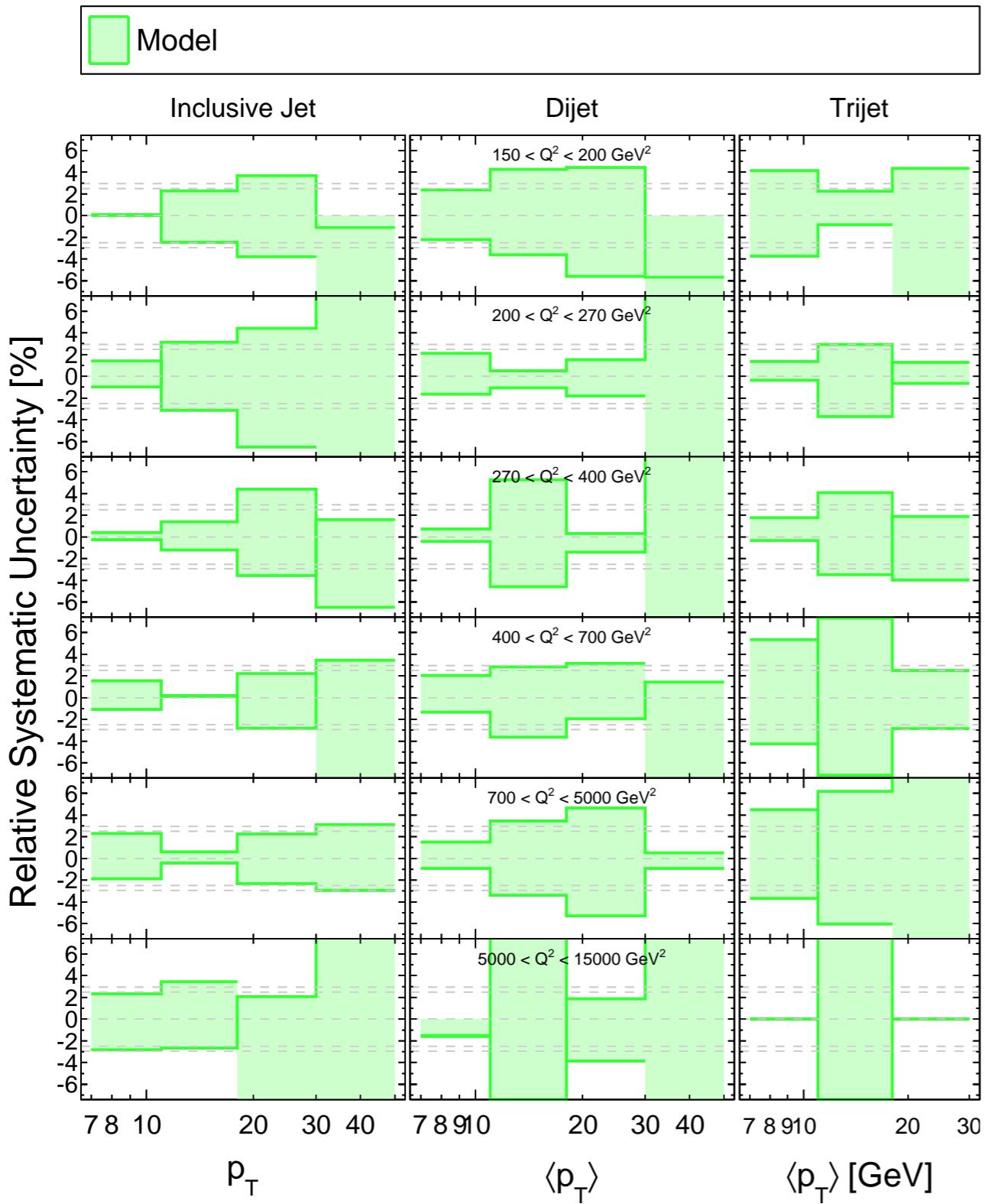


Using ‘old+new MC’

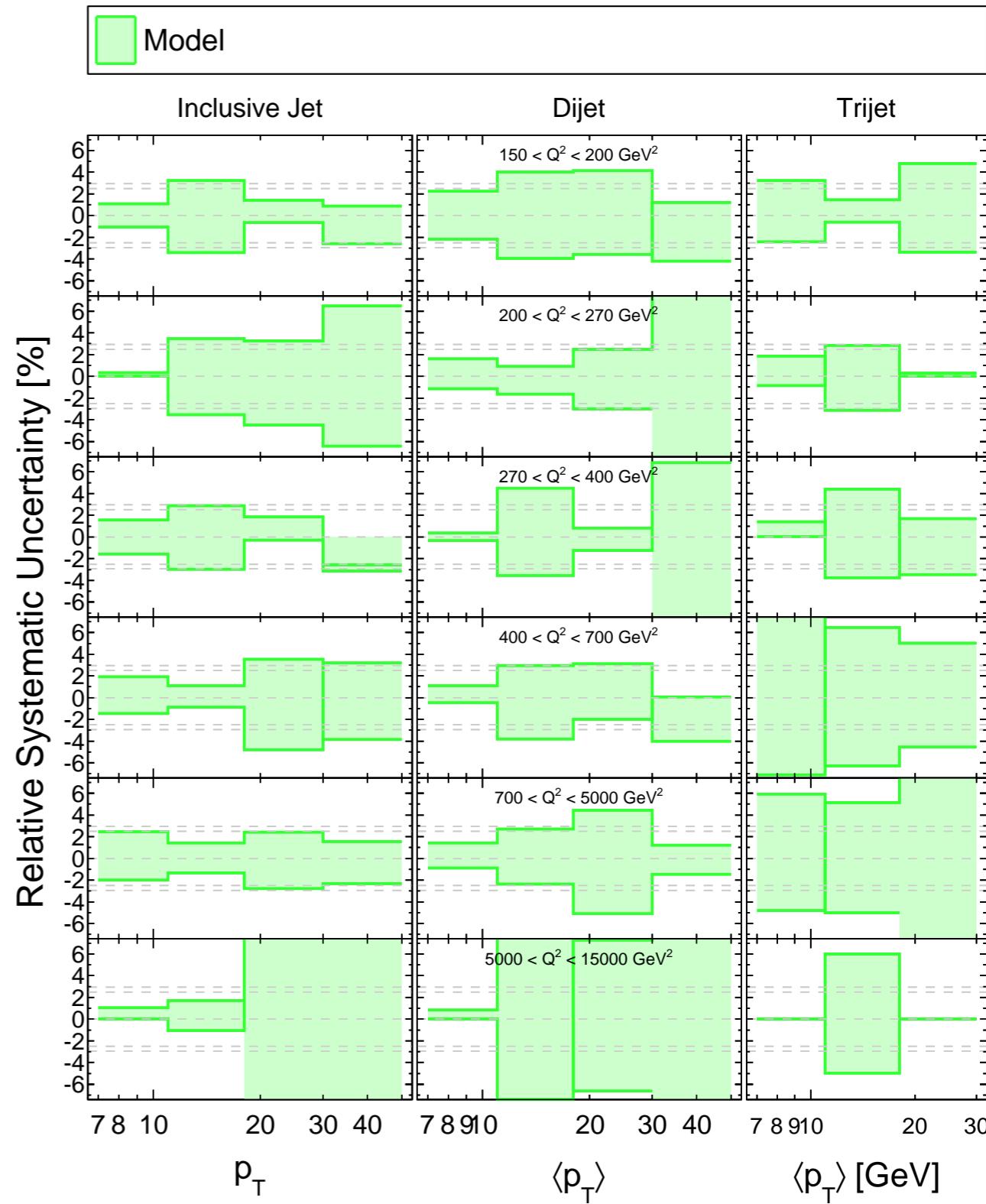


# Model uncertainty

Using ‘old MC’



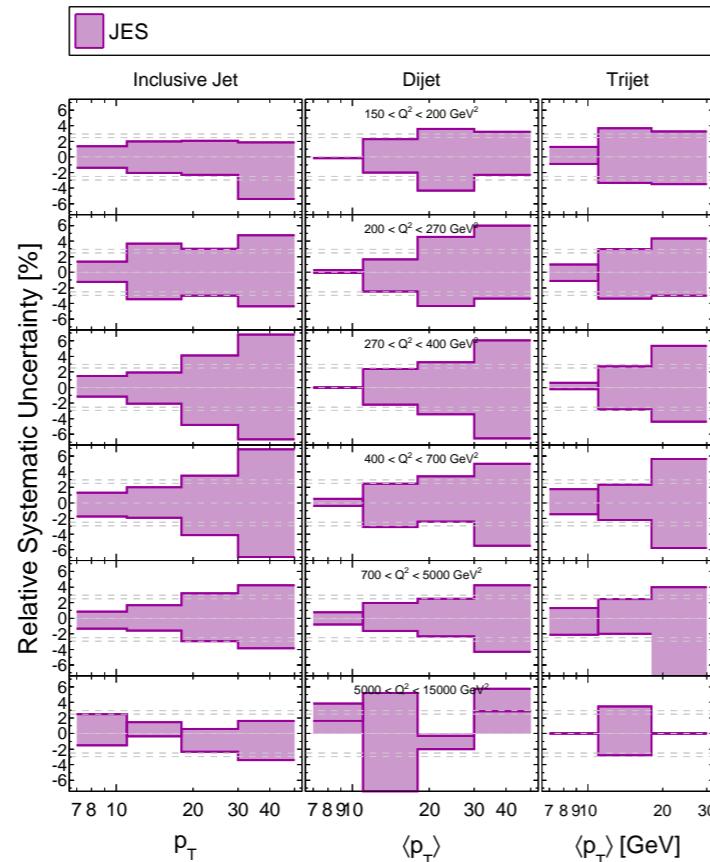
Using ‘old+new MC’



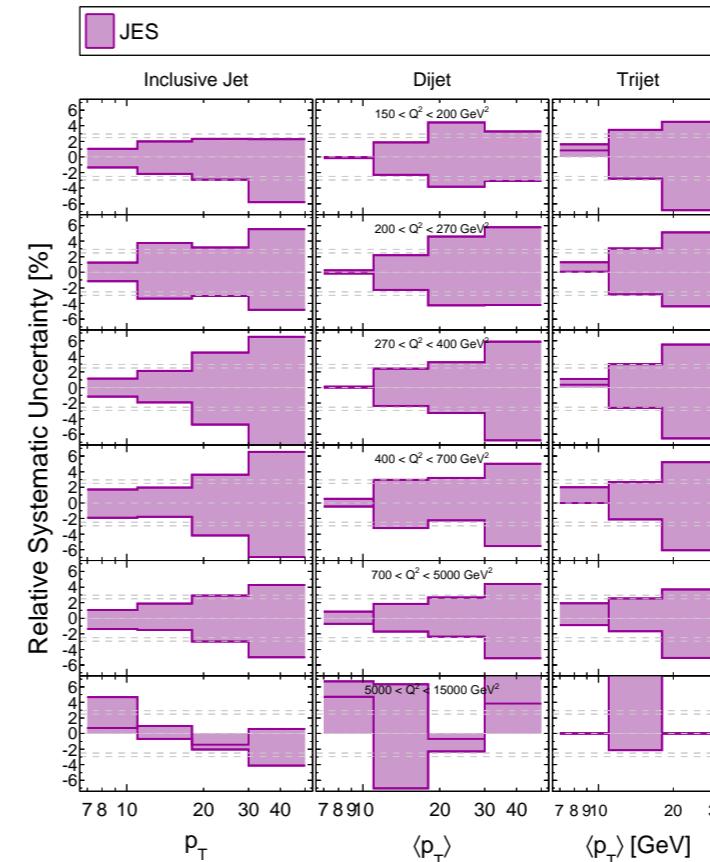
Some bins have quite different model uncertainties, but also large fluctuations/asymmetries

# Conclusion on uncertainties

## Using ‘old MC’



## Using ‘old+new MC’



## Results

Size of systematic uncertainties does not change

‘Fluctuations’ are still present

Quite consistent results (even for some ‘fluctuations’)

Low-statistics bins (e.g. high- $Q^2$ , high  $p_T$  bins) have slight changes

## Open questions

Do we trust these uncertainties ?

What is the potential impact on the fit?

# Careful smoothing of uncertainties (by hand!)

## Previously used ‘smoothing’ algorithm

1. Unfold data (with  $Dj+Rg$ )  $\delta_{Data(Dj+Rg)}$
2. Unfold Django-pseudo-data with Rapgap
  - reduced dependence on limited data statistics
3. Unfold Rapgap-pseudo-data with Django

$$4. \delta\sigma = \frac{\delta\sigma_{Data(Dj+Rg)} + \delta\sigma_{Dj(Rg)} + \delta\sigma_{Rg(Dj)}}{3}$$

Only small effect on ‘fluctuations’

Now:

## CAREFUL(!) smoothing of uncertainties by hand

- e.g. average uncertainty in bins of similar phase space
- Consider  $Q^2$  and  $p_T$  dependence of uncertainties
  - JES and RCES should have small dependence in  $Q^2$
  - Electron uncertainties should hardly differ between different jet  $p_T$  bins
- Consider also uncertainties if bin-by-bin method would be used

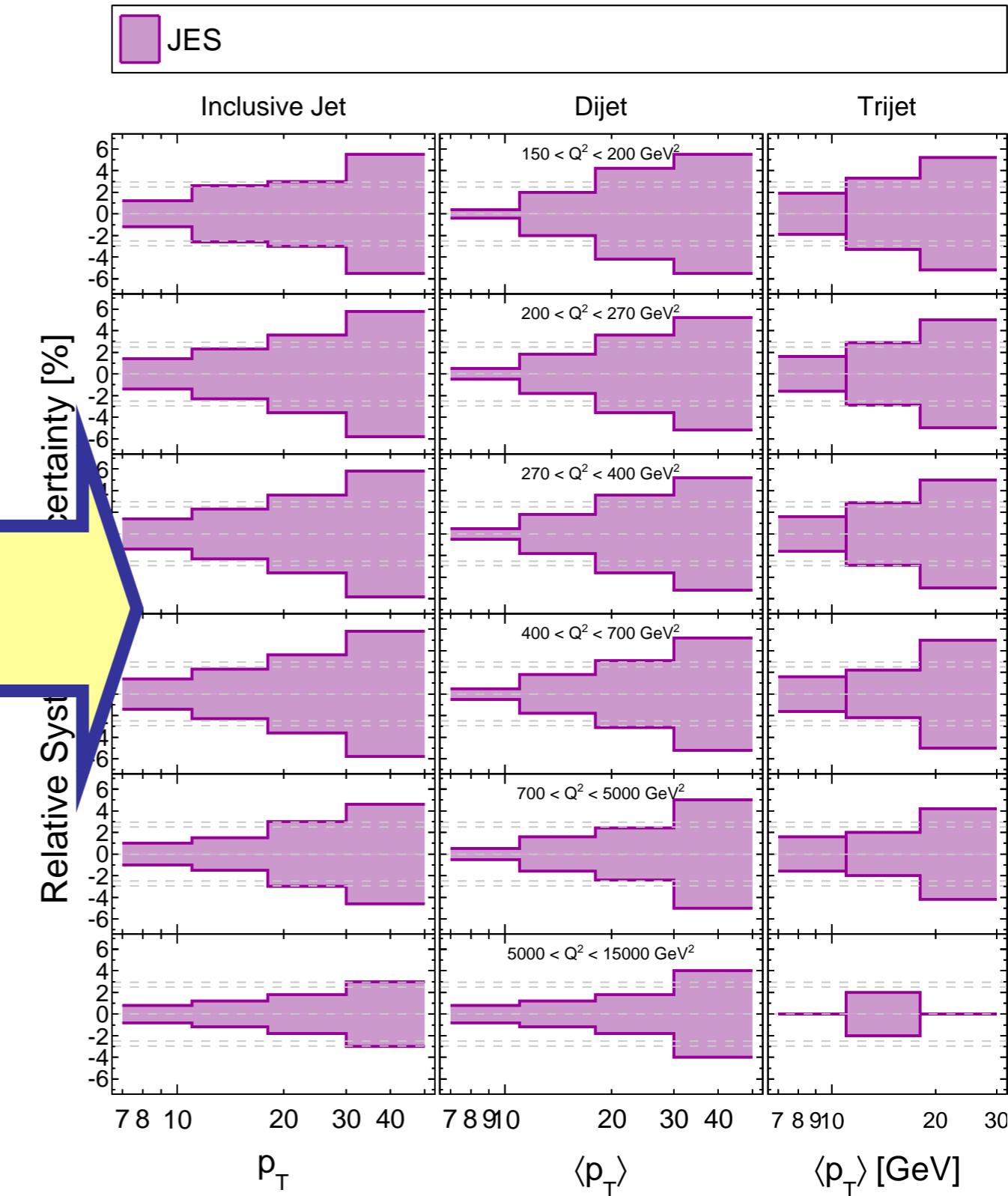
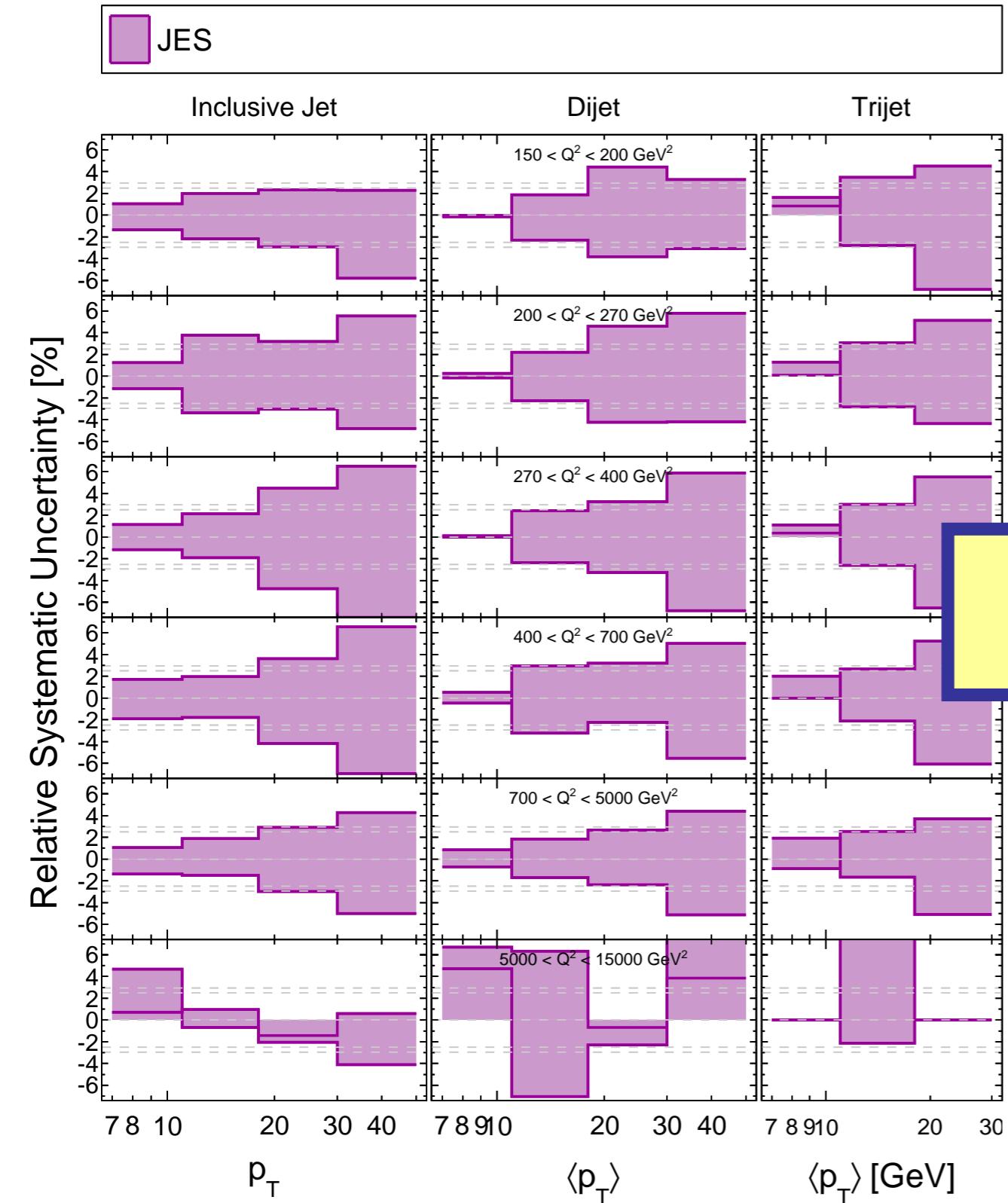




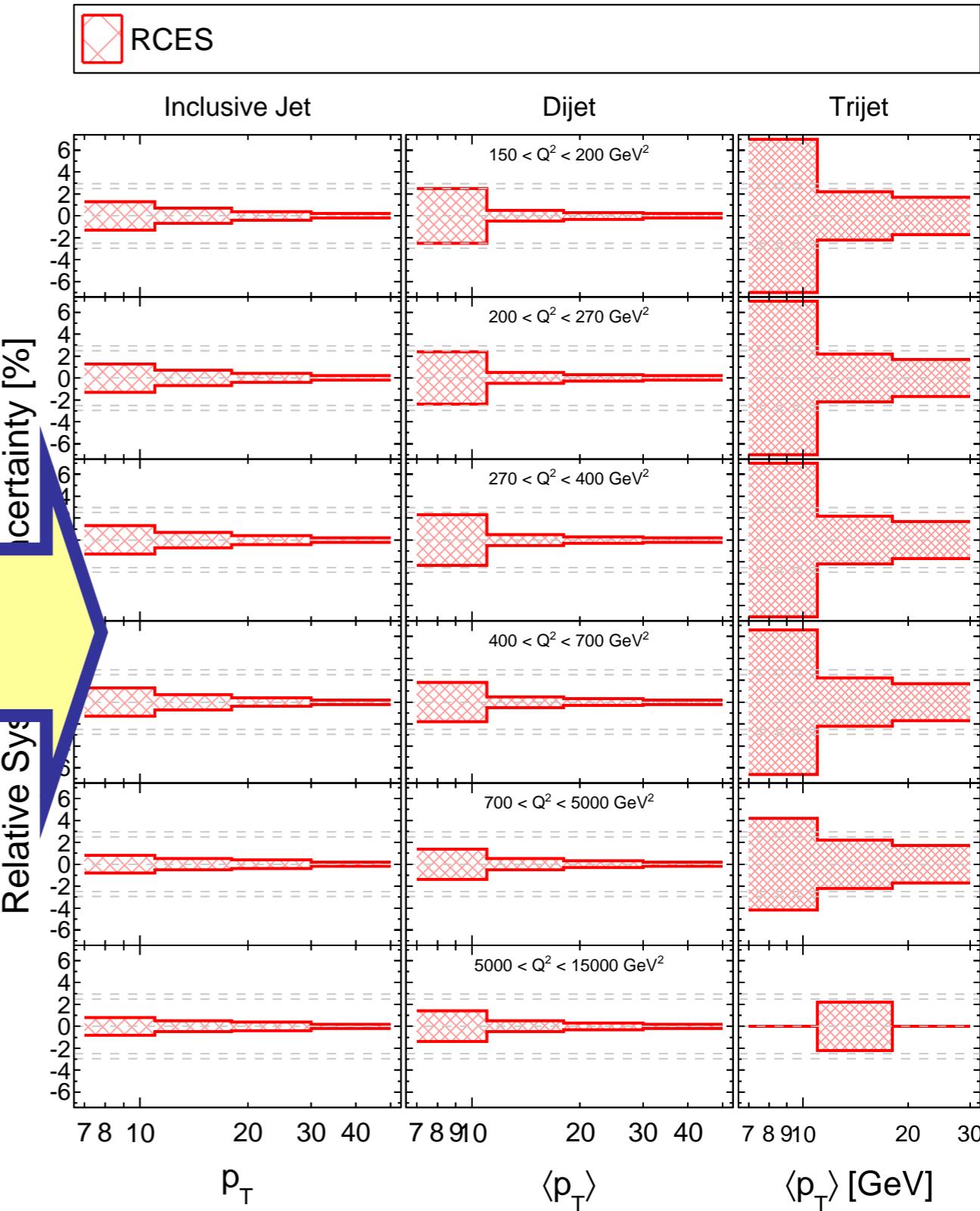
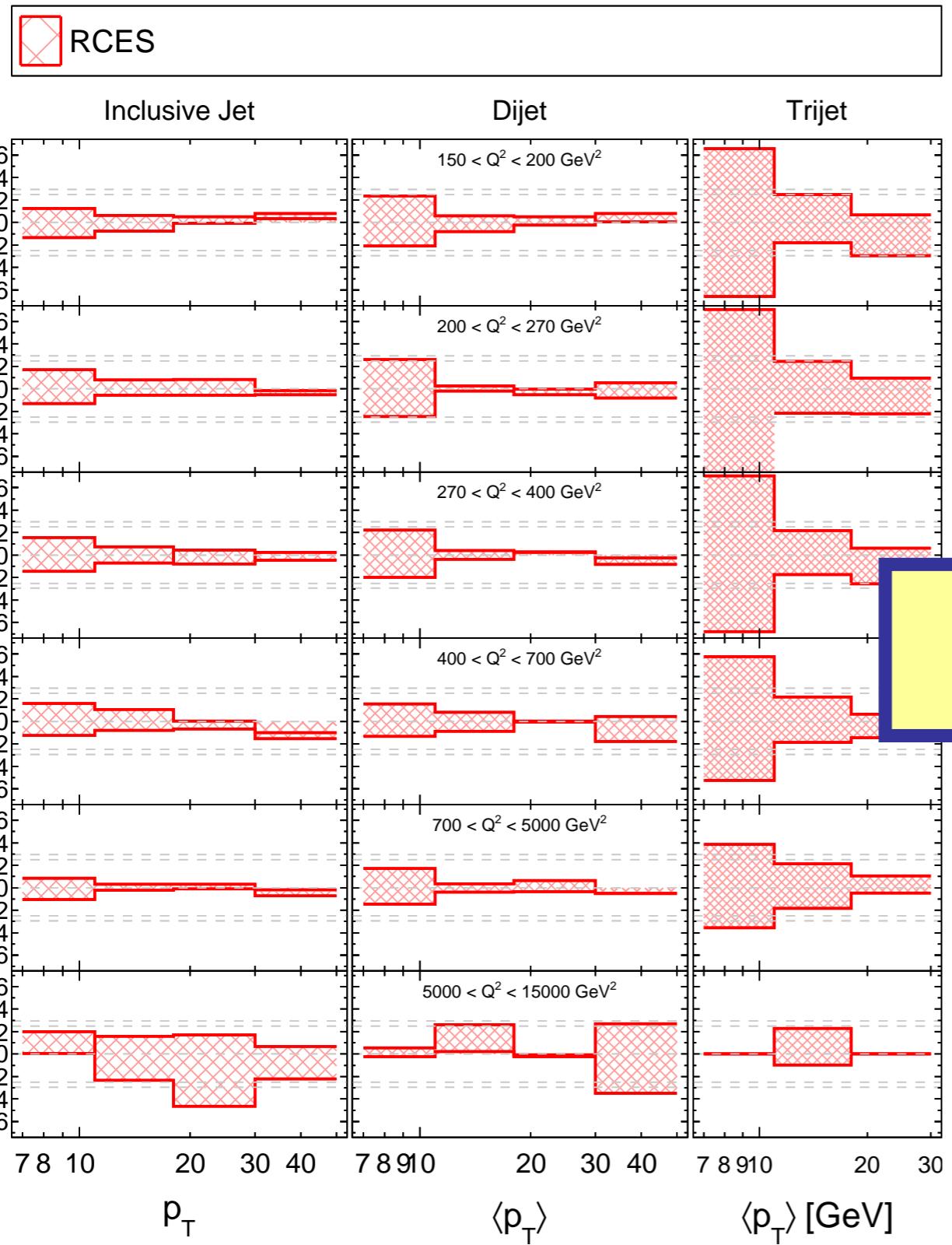
2 x 3 MACHT 4 -  
WIDDEWIDDEWITT UND 3 MACHT 9E !  
ICH MACH' MIR DIE FEHLER -  
WIDDEWIDDE WIE SIE MIR GEFALLEN ...



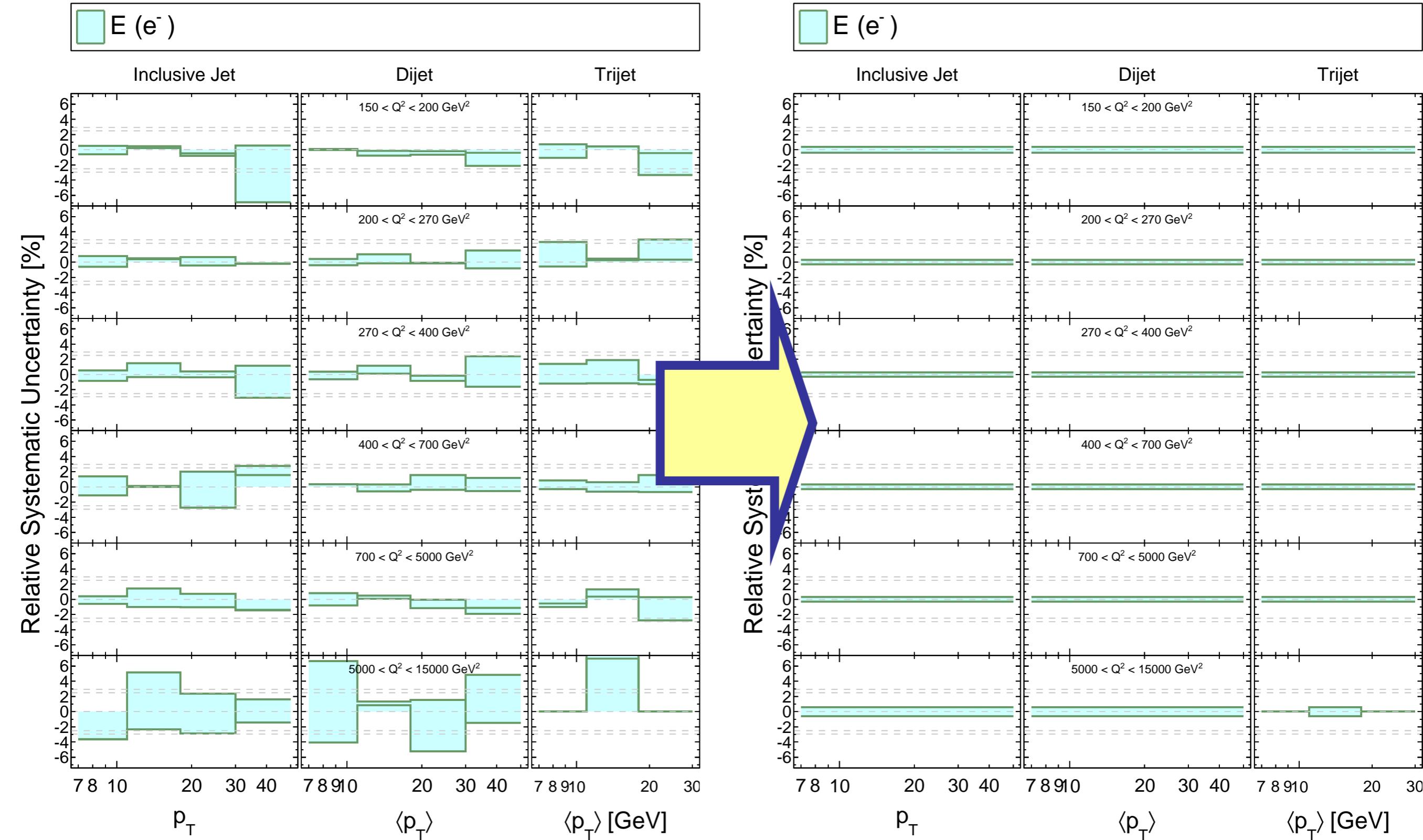
# Before and after ‘smoothing’



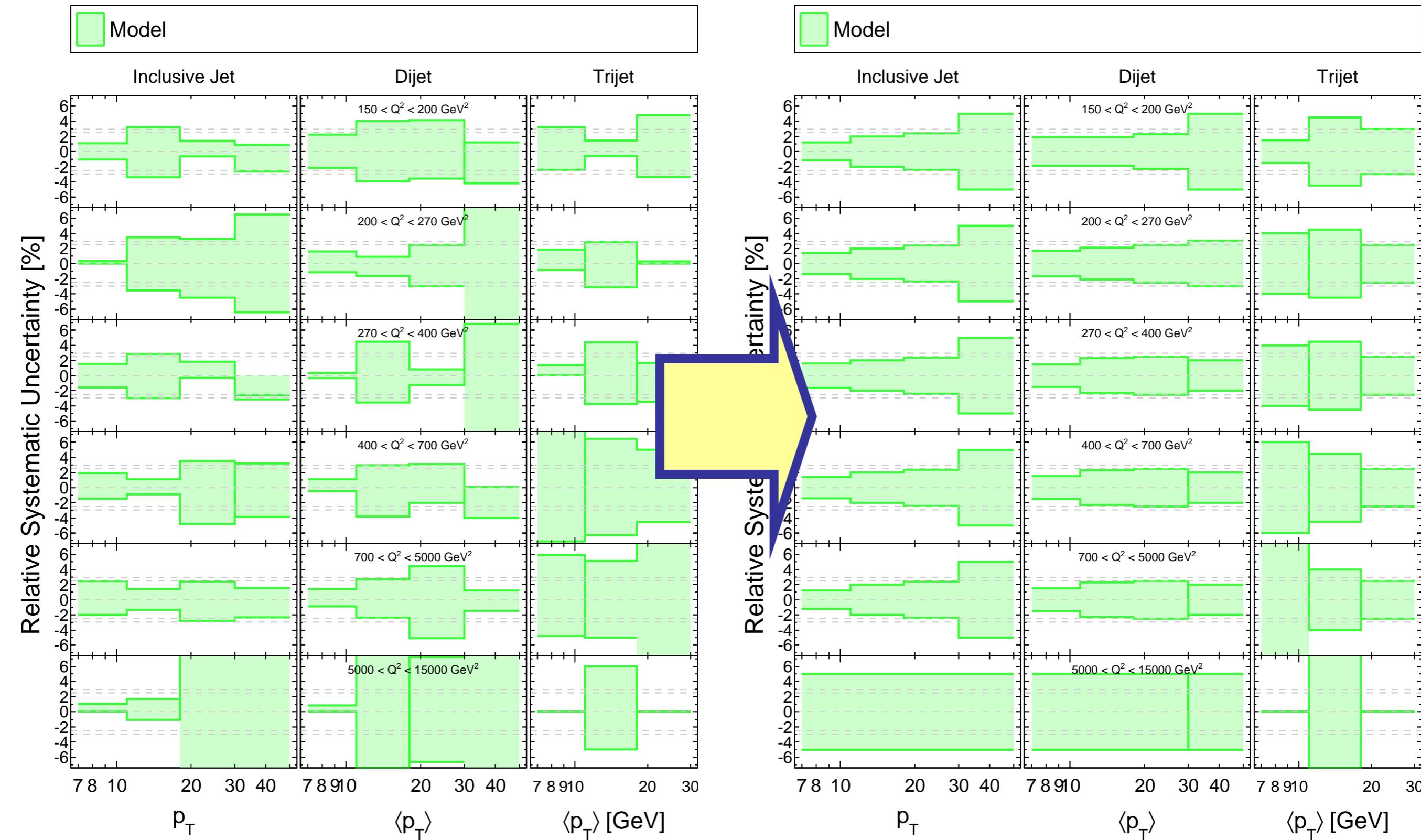
# Before and after ‘smoothing’



# Before and after ‘smoothing’



# Before and after ‘smoothing’



# Impact on alpha\_s

## Unsmoothed data set

### Inclusive Jet

0.1175 +/- 0.0022 (exp) @ chi2/ndf = 1.342

### Dijet

0.1136 +/- 0.0023 (exp) @ chi2/ndf = 1.261

### Trijet

0.1168 +/- 0.0019 (exp) @ chi2/ndf = 1.002

### Multijet

0.1179 +/- 0.0017 (exp) @ chi2/ndf = 1.251

eps(HFS) = 0.202 +/- 0.627

eps(JES) = 0.422 +/- 0.603

eps(LArNoise) = 0.292 +/- 0.933

eps(Norm) = 1.531 +/- 0.759

## Smoothed data set

### Inclusive Jet

0.1176 +/- 0.0022 (exp) @ chi2/ndf = 1.408

### Dijet

0.1137 +/- 0.0024 (exp) @ chi2/ndf = 1.396

### Trijet

0.1165 +/- 0.0019 (exp) @ chi2/ndf = 1.347

### Multijet

0.1182 +/- 0.0018 (exp) @ chi2/ndf = 1.400

eps(HFS) = 0.326 +/- 0.876

eps(JES) = 0.677 +/- 0.739

eps(LArNoise) = 0.347 +/- 0.977

eps(Norm) = 1.517 +/- 0.779

- ‘Smoothing’ has no significant influence on fit
- Large nuisance parameters are not caused by ‘fluctuations of system. uncertainties’
- Results change more significantly if uncertainties are treated as ‘fully correlated’ (backup)

# Study: Include systematic uncertainties in Unfolding Covariance matrix (based on old MC)

## Regularized unfolding using Tunfold

- Find hadron level  $x$  by analytic minimization of  $\chi^2$

$$\chi^2(x, \tau) = (y - Ax)^T V_y^{-1} (y - Ax) + \tau^2 (x - x_0)^T (L^T L)(x - x_0)$$

- Include Systematic uncertainty in

$$V: V \rightarrow V_{\text{stat}} + V_{\text{sys}}$$

- Only JES and RCES (the largest systematic uncertainties) (technical limitations)
- Correlated, uncorrelated, 50:50, ...

## Systematic uncertainty will be included in Covariance matrix of result

Cannot be disentangled from statistical uncertainty

# Systematic uncertainties in unfolding

	Referenz	JES and RCES in V	JES and RCES in V	JES and RCES in V
Uncertainty treatment		Correlated	Uncorrelated	half correlated, half uncorrelated
tau	$10^{-6}$	$10^{-6}$	$10^{-6}$	$10^{-6}$
Chi2a in unfolding	3306.7	3219.8	2685.35	2388.76

Update 11. 09. 13: **WARNING !!!**

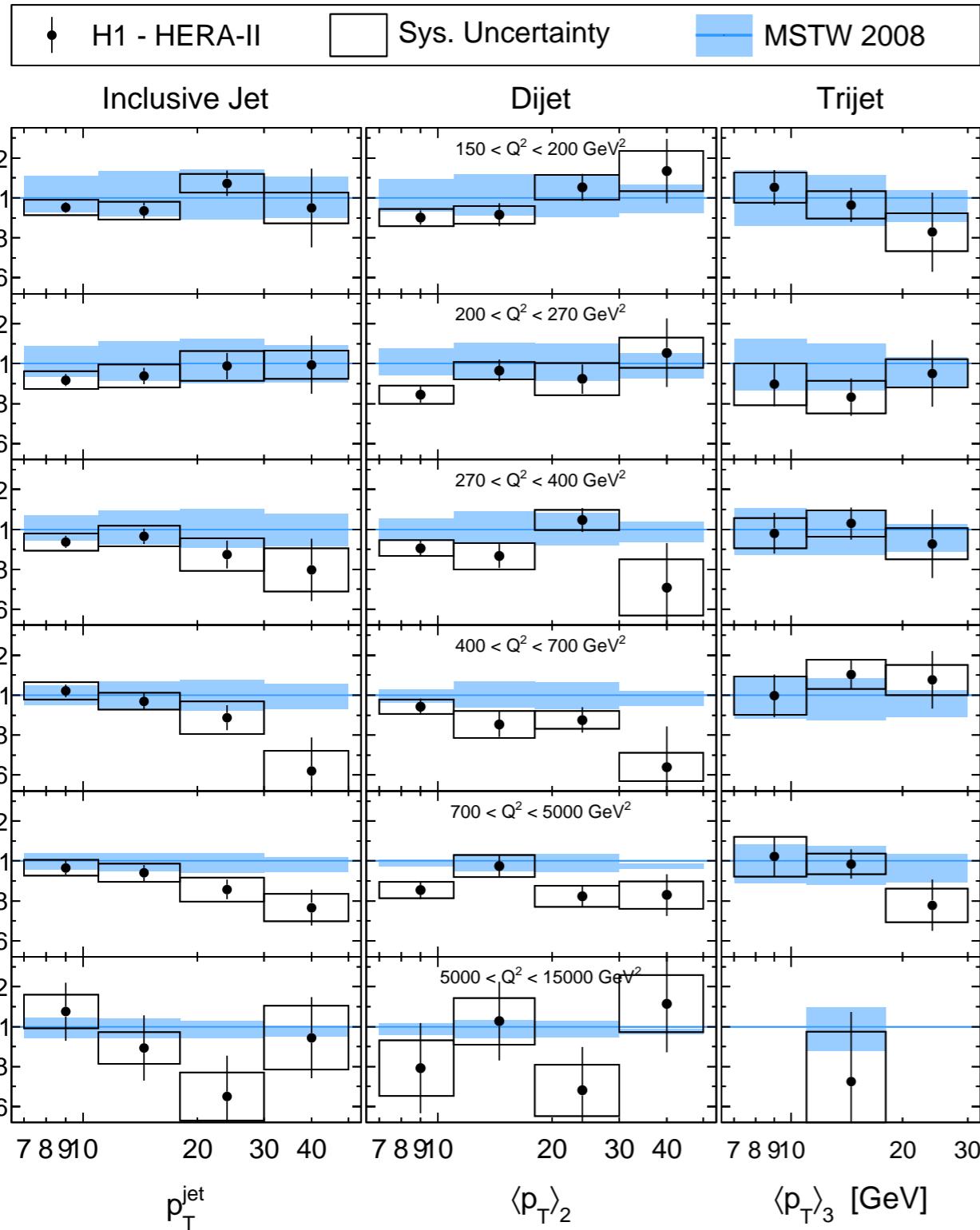
Systematic uncertainty was added twice in unfolding (once for up/down variation)

This gives an increased uncertainty of 1.4142...

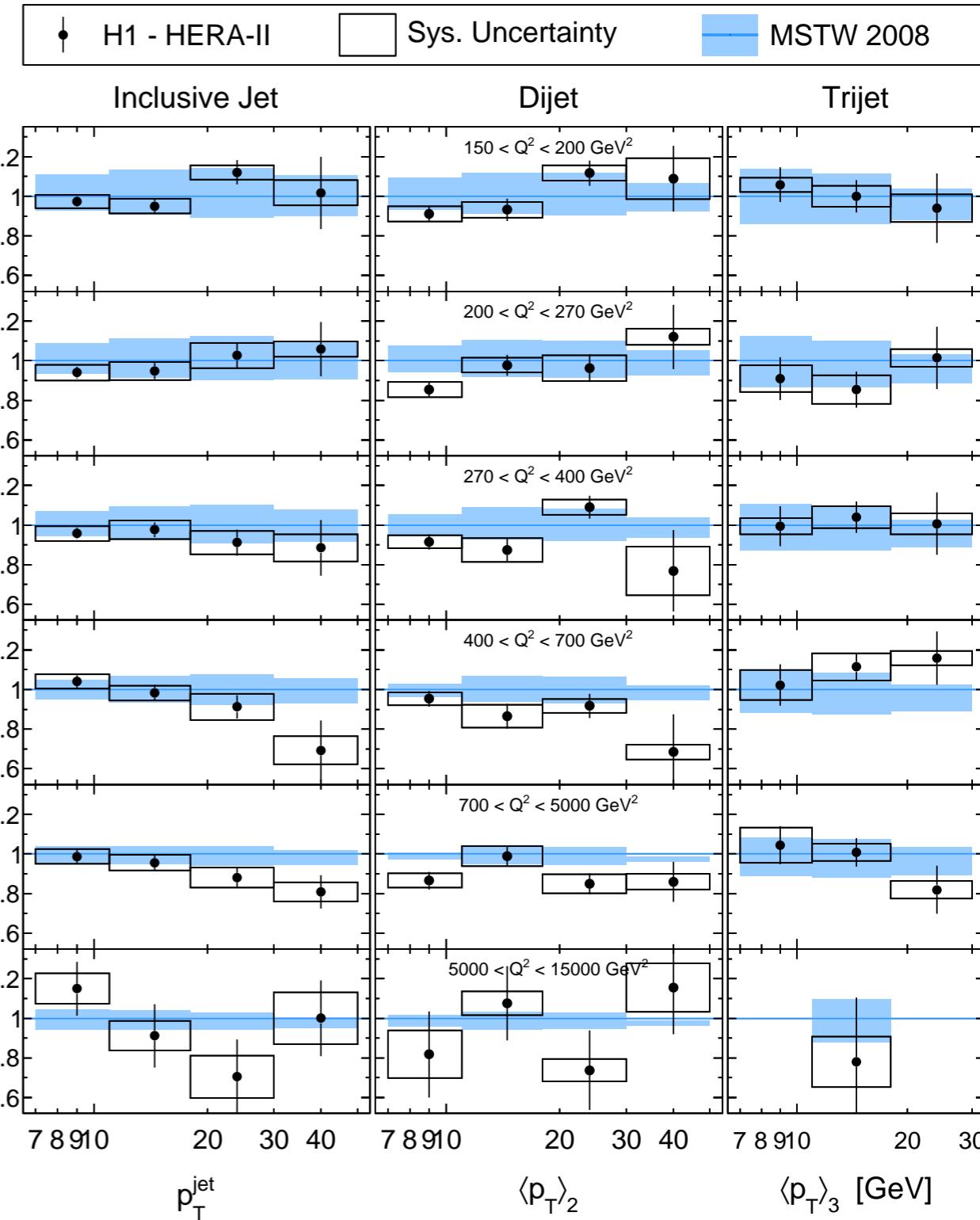
If there is a visible effect, this should be even increased !!!

# Systematic uncertainties in unfolding

## Reference

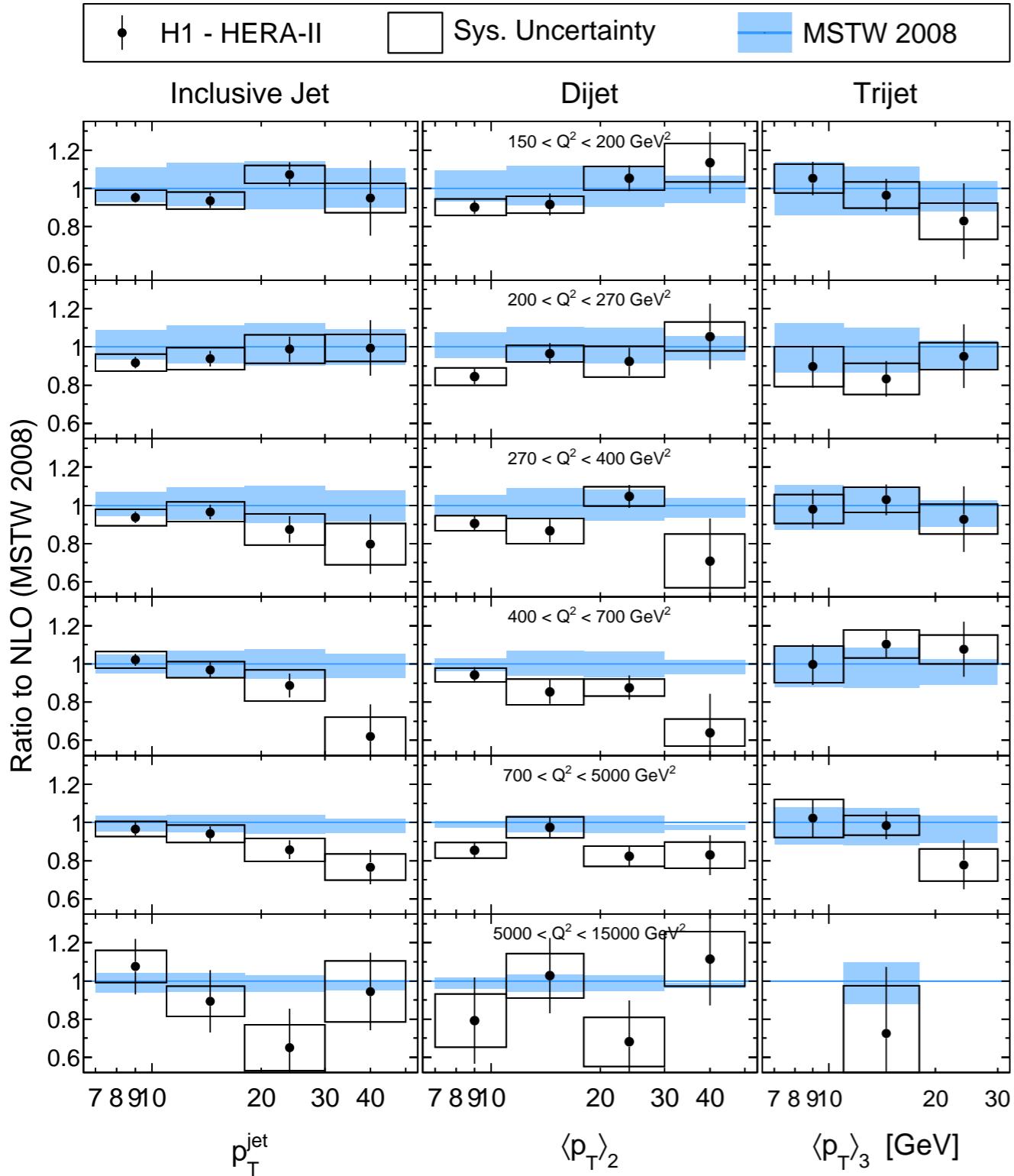


## JES and RCES as correlated

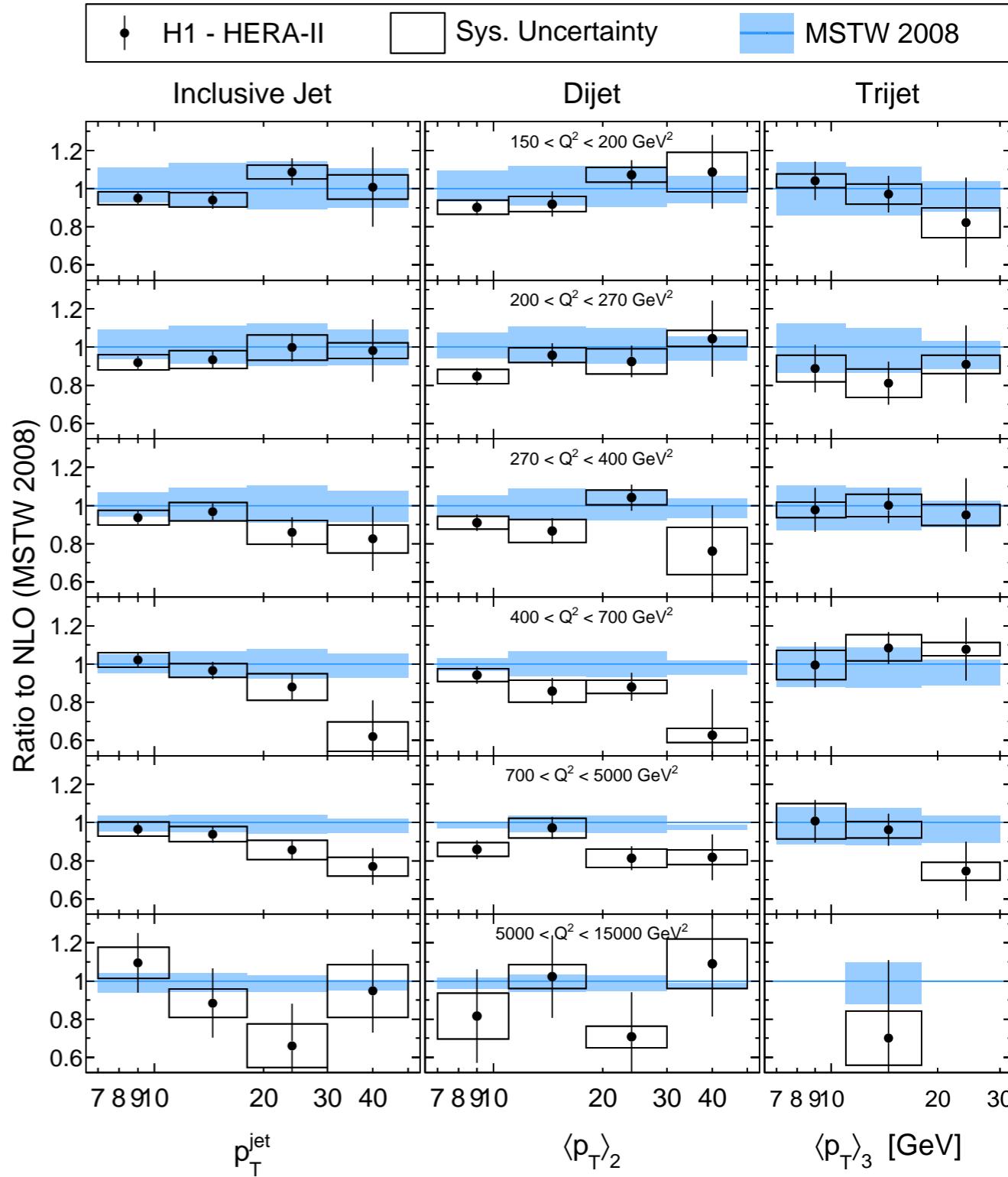


# Systematic uncertainties in unfolding

## Reference



## JES and RCES as uncorrelated



# Effect in $\alpha_s$ -fit

	Sys in $\alpha_s$ -fit uncorrelated	Sys in $\alpha_s$ -fit (50:50)	Sys in $\alpha_s$ -fit correlated (rel.)	Sys in $\alpha_s$ -fit correlated (abs.)
<b>Inclusive Jet</b>	0.1168 +/- 0.0021 chi2/ndf = 1.372	0.1176 +/- 0.0022 chi2/ndf = 1.386	0.1180 +/- 0.0022 chi2/ndf = 1.475	0.1178 +/- 0.0023 chi2/ndf = 1.529
<b>Dijet</b>	0.1135 +/- 0.0022 chi2/ndf = 1.260		0.1134 +/- 0.0023 chi2/ndf = 1.500	0.1129 +/- 0.0024 chi2/ndf = 1.462
<b>Trijet</b>	0.1171 +/- 0.0016 chi2/ndf = 0.748	0.1176 +/- 0.0017 chi2/ndf = 0.797	0.1179 +/- 0.0018 chi2/ndf = 0.878	0.1180 +/- 0.0020 chi2/ndf = 0.892
<b>Multijet</b>	0.1181 +/- 0.0016 chi2/ndf = 1.179	0.1184 +/- 0.0017 chi2/ndf = 1.290	0.1186 +/- 0.0017 chi2/ndf = 1.454	0.1177 +/- 0.0019 chi2/ndf = 1.457
<b>Multijet Norm</b>	0.1165 +/- 0.0006 chi2/ndf = 1.519	0.1165 +/- 0.0007 chi2/ndf = 1.614	0.1166 +/- 0.0007 chi2/ndf = 1.738	0.1164 +/- 0.0007 chi2/ndf = 1.731
	Sys in Unfolding V Uncorrelated	Sys in Unfolding V (50:50)	Sys in Unfolding V Correlated	
<b>Inclusive Jet</b>	0.1168 +/- 0.0021 chi2/ndf = 1.447	0.1180 +/- 0.0021 chi2/ndf = 1.429	0.1183 +/- 0.0020 chi2/ndf = 1.509	
<b>Dijet</b>	0.1137 +/- 0.0022 chi2/ndf = 1.218	0.1148 +/- 0.0022 chi2/ndf = 1.455	0.1151 +/- 0.0022 chi2/ndf = 1.677	
<b>Trijet</b>	0.1167 +/- 0.0016 chi2/ndf = 0.860	0.1178 +/- 0.0015 chi2/ndf = 0.870	0.1182 +/- 0.0015 chi2/ndf = 0.878	
<b>Multijet</b>	0.1177 +/- 0.0015 chi2/ndf = 1.222	0.1188 +/- 0.0015 chi2/ndf = 1.347	0.1194 +/- 0.0014 chi2/ndf = 1.483	
<b>Multijet Norm</b>	0.1164 +/- 0.0006 chi2/ndf = 1.424	0.1175 +/- 0.0006 chi2/ndf = 1.545	0.1179 +/- 0.0006 chi2/ndf = 1.691	

For JES/RCES 50:50 was commonly used: No significant difference there  
 Inclusion of sys. uncertainties in unfolding is an equally valid approach

# Summary

## Status

- Reason for fluctuations in systematic uncertainty remains unclear
  - It is not MC statistics, not Data statistics ...
- Fluctuations of sys. uncertainties do not have bad influence on fit results
  - Some smoothing may be reasonable, but not too much
- Systematic uncertainties can also be included in covariance matrix, which enters unfolding
  - Systematic uncertainties cannot be disentangled after unfolding from statistical uncertainties
  - No visibly preferred effect on cross sections
  - Treatment seems to be equally valid, as using systematic uncertainties in a similar way in  $\alpha_s$ -fit
  - Uncertainties on  $\alpha_s$  may come out to be slightly smaller

## Plans

- As soon as remaining new MCs are sim-rec'd and oo'd, data will be unfold'd, cross-section'd and fitt'd
  - Final cross sections
- Final fits are also ahead
- Writing paper
- T0 planned on 17. October (optimistic, but possible)

# Correction of detector effects using regularized unfolding

## Detector effects

- Acceptance and efficiency
- Migrations due to limited resolution

## Aim

- Cross section on hadron level
- Direct matrix inversion of  $A$  often not possible

## Detector response

$$y = A \cdot x$$

- Measured vector  $y$
- Hadron level vector  $x$
- Detector response matrix  $A$
- Covariance matrix  $V_y$

## Regularized unfolding using Tunfold ([JINST 7 \(2012\) T10003](#))

- Find hadron level  $x$  by analytic minimization of  $\chi^2$

$$\chi^2(x, \tau) = \frac{(y - Ax)^T V_y^{-1} (y - Ax)}{\text{Matrix inversion: } \chi^2_A} + \frac{\tau^2 (x - x_0)^T (L^T L) (x - x_0)}{\text{Regularization: } \chi^2_L}$$

Matrix inversion:  $\chi^2_A$

Regularization:  $\chi^2_L$

- Find stationary point ( $\partial\chi^2/\partial x = 0$ ) by solving analytically as function of  $x$
- ‘True’ hadron level can be determined directly

$$x = (A^T V_y^{-1} A + \tau^2 L^2)^{-1} A^T V_y^{-1} y =: B y$$

- $\tau$  (and  $L$ ) are free parameters

# Correlation matrix

## Covariance matrix

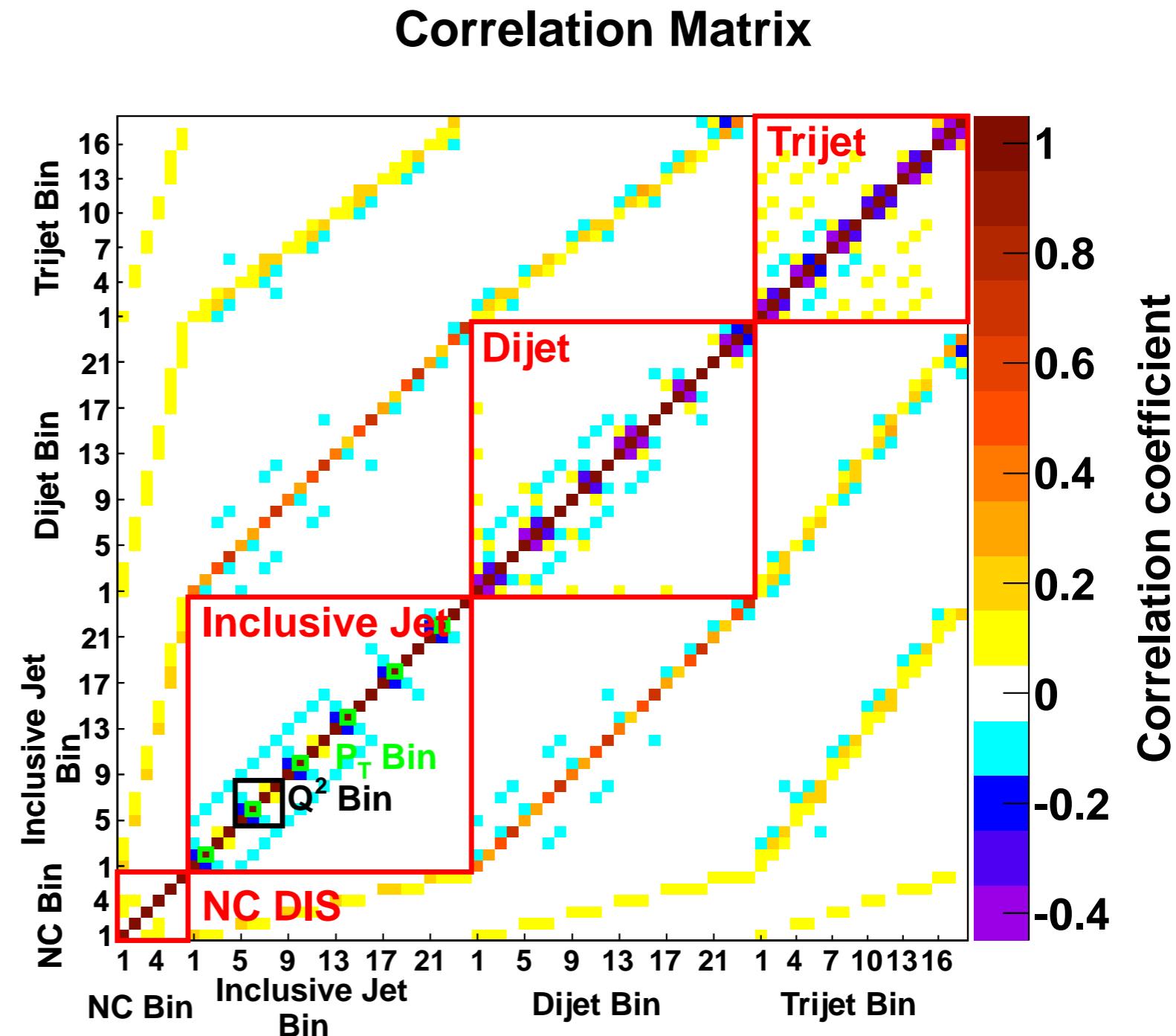
Obtained through linear error propagation of statistical uncertainties

## Correlations

- Resulting from unfolding
- Physical correlations
  - Between measurements
  - Within inclusive jet

## Useful for

- Cross section ratios
- Combined fits
- Normalized cross sections



Correlation matrix is employed for correct error propagation for norm. cross sections

# All sys. uncertainties fully correlated (model 50%:50%)

```
Fit_SysCorrMod05_MC13pre12/log.1.txt:446:xxac alpha_s = 0.1181 +/- 0.0022 (exp) @ chi2/ndf = 1.539
Fit_SysCorrMod05_MC13pre12/log.123.txt:651:xxac alpha_s = 0.1189 +/- 0.0017 (exp) @ chi2/ndf = 1.534
Fit_SysCorrMod05_MC13pre12/log.2.txt:446:xxac alpha_s = 0.1146 +/- 0.0024 (exp) @ chi2/ndf = 1.528
Fit_SysCorrMod05_MC13pre12/log.3.txt:434:xxac alpha_s = 0.1174 +/- 0.0022 (exp) @ chi2/ndf = 1.275

Fit_SysCorrMod05_MC13pre12/log.123.txt:638:xxe-----
Fit_SysCorrMod05_MC13pre12/log.123.txt:639:xxe eps(HFS) = 0.230 +/- 0.537 Corr to as: 0.515
Fit_SysCorrMod05_MC13pre12/log.123.txt:640:xxe eps(JES) = 0.387 +/- 0.456 Corr to as: 0.264
Fit_SysCorrMod05_MC13pre12/log.123.txt:641:xxe eps(LArNoise) = 0.534 +/- 0.992 Corr to as: 0.172
Fit_SysCorrMod05_MC13pre12/log.123.txt:642:xxe eps(Ee) = 1.408 +/- 0.435 Corr to as: 0.029
Fit_SysCorrMod05_MC13pre12/log.123.txt:643:xxe eps(The) = 0.228 +/- 0.940 Corr to as: -0.106
Fit_SysCorrMod05_MC13pre12/log.123.txt:644:xxe eps(IDe) = 1.375 +/- 0.891 Corr to as: 0.020
Fit_SysCorrMod05_MC13pre12/log.123.txt:645:xxe eps(Norm) = 1.790 +/- 0.735 Corr to as: 0.755
Fit_SysCorrMod05_MC13pre12/log.123.txt:648:xxe eps(Model) = -0.027 +/- 0.421 Corr to as: 0.116

Fit_SysCorrMod05_MC13pre12SmoothHand/log.1.txt:446:xxac alpha_s = 0.1191 +/- 0.0023 (exp) @ chi2/ndf = 1.531
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Fit_SysCorrMod05_MC13pre12SmoothHand/log.2.txt:446:xxac alpha_s = 0.1149 +/- 0.0026 (exp) @ chi2/ndf = 1.672
Fit_SysCorrMod05_MC13pre12SmoothHand/log.3.txt:434:xxac alpha_s = 0.1166 +/- 0.0021 (exp) @ chi2/ndf = 1.496

Fit_SysCorrMod05_MC13pre12SmoothHand/log.123.txt:638:xxe-----
Fit_SysCorrMod05_MC13pre12SmoothHand/log.123.txt:639:xxe eps(HFS) = 0.769 +/- 0.799 Corr to as: 0.671
Fit_SysCorrMod05_MC13pre12SmoothHand/log.123.txt:640:xxe eps(JES) = 0.587 +/- 0.627 Corr to as: 0.383
Fit_SysCorrMod05_MC13pre12SmoothHand/log.123.txt:641:xxe eps(LArNoise) = 0.622 +/- 0.991 Corr to as: 0.142
Fit_SysCorrMod05_MC13pre12SmoothHand/log.123.txt:642:xxe eps(Ee) = 0.136 +/- 0.996 Corr to as: 0.061
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Fit_SysCorrMod05_MC13pre12SmoothHand/log.123.txt:644:xxe eps(IDe) = 1.292 +/- 0.901 Corr to as: 0.010
Fit_SysCorrMod05_MC13pre12SmoothHand/log.123.txt:645:xxe eps(Norm) = 1.595 +/- 0.773 Corr to as: 0.666
Fit_SysCorrMod05_MC13pre12SmoothHand/log.123.txt:648:xxe eps(Model) = 0.642 +/- 0.543 Corr to as: 0.041
```