

Mesh transparency and gas gain studies in micromegas detectors

Fabian Kuger

University of Würzburg, Germany

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- Simulation of a micromegas
- Experimental setup
- Macroscopic Results:
 - Transparency
 - Gas gain curves
 - Temperature behavior
- Microscopic Results:
 - Development time of an avalanche
 - Spatial extent of an avalanche
- Statistics of gas amplification

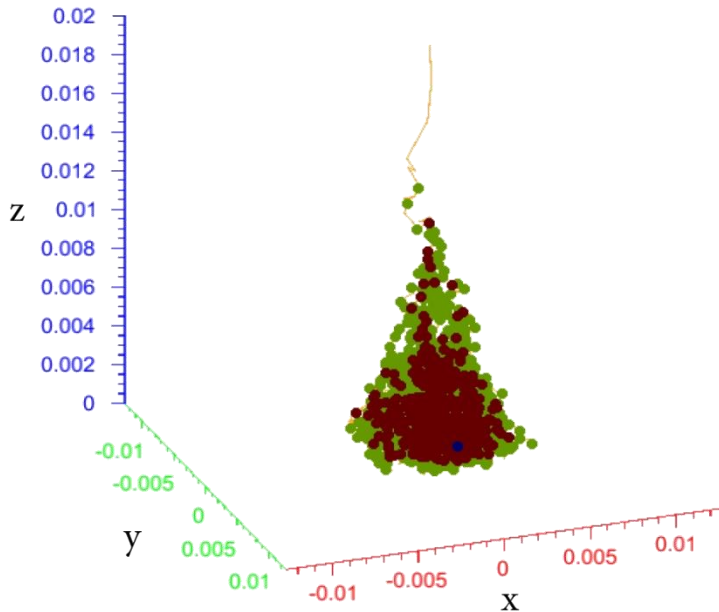
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Simulation of electron drift, scattering processes and avalanche formation is

- done by using the *microscopic avalanche* method in **Garfield++**,
- interfacing **Magboltz 9** for gas properties (Ar CO₂ 93:7, 1 atm, 20°C),
- taking into account penning-transfer
 [Sahin, Ö. ; et al: Penning transfer in argon-based gas mixtures. In: Journal of Instrumentation 5 (2010)]
- Using field maps computed with **ANSYS 12.1**



1-5 10³ avalanches have been simulated per run, relevant information:



- number of electrons per avalanche n_e
- starting z- coordinate of secondary electrons
- end coordinates: Center of gravity, total width, gauss-fit parameters, Z_{min}
- timing information of the electrons

Approximation of the electrical field is done by using a *FiniteElementMethod (FEM)*, utilizing the *smartmeshing* option of **ANSYS 12.1**.

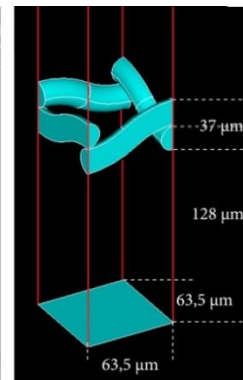
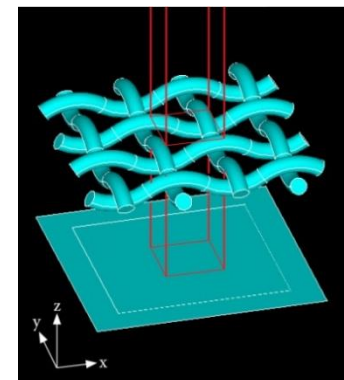
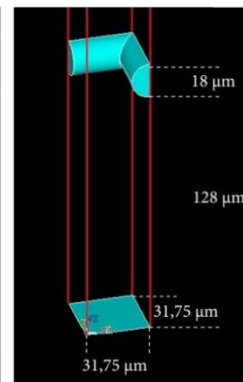
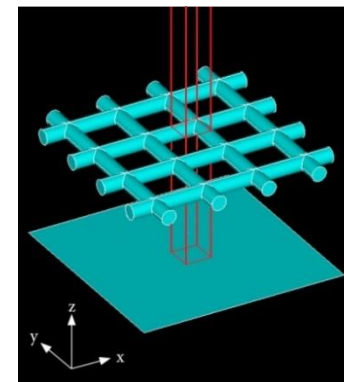
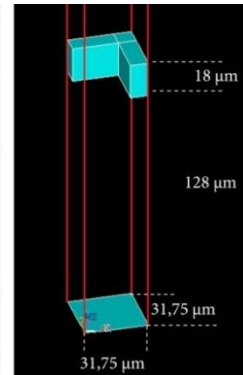
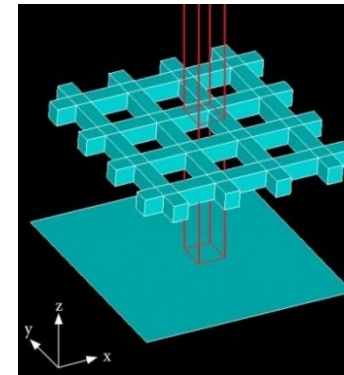
- Only unit cell is calculated, with mirror conditions on all vertical borders applied.

- ✓ Periodicity of the mesh
- ✗ Periodicity of the readout and pillars

- 3 different layout with rising complexity have been under study.

- Layout 1 (L1): flat, rectangular wires
- Layout 2 (L2): flat, cylindrical wires
- Layout 3 (L3): woven, toroidal wire-pieces

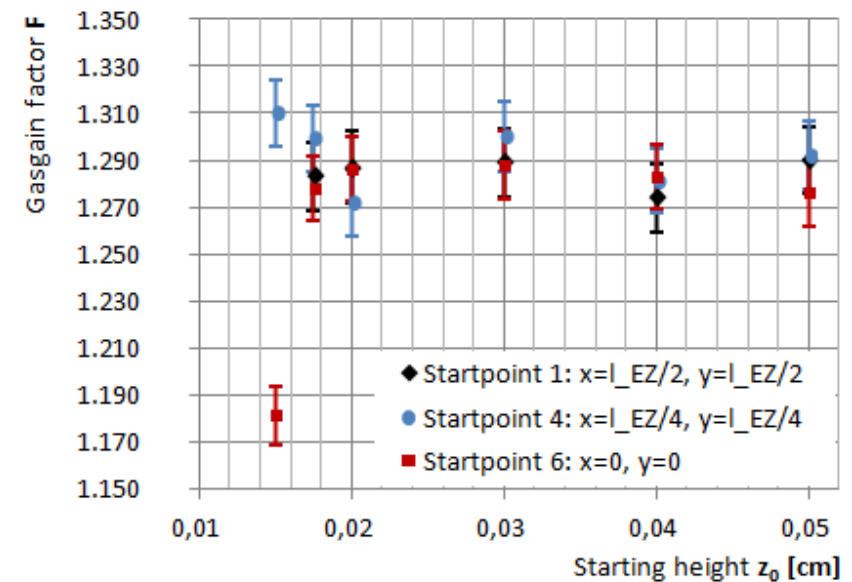
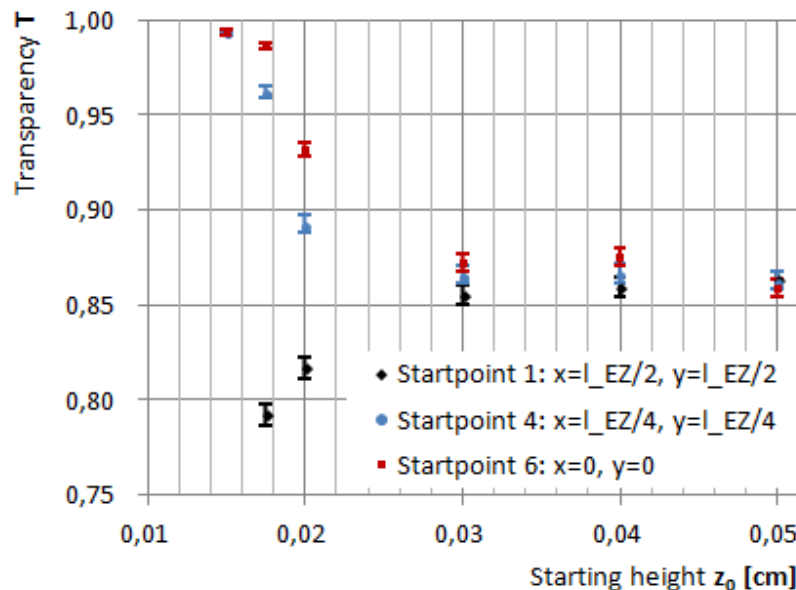
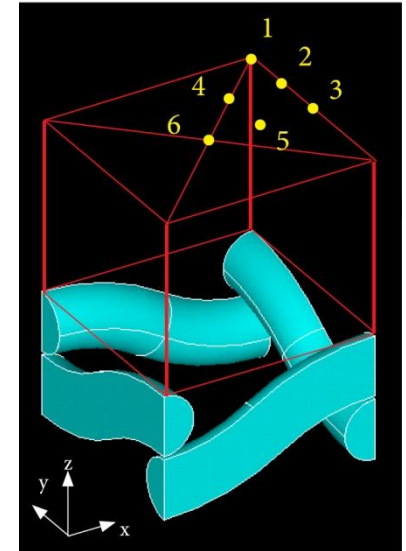
- ✓ Cylindrical wires and woven structure
- ✗ Calendering of the mesh



Elimination of systematic errors due to starting position:

- x-y coordinates at random
- precedent study on starting height dependence for transparency and gas gain.

→ $z_0=400 \mu\text{m}$ ($\sim 250 \mu\text{m}$ above mesh upper border)

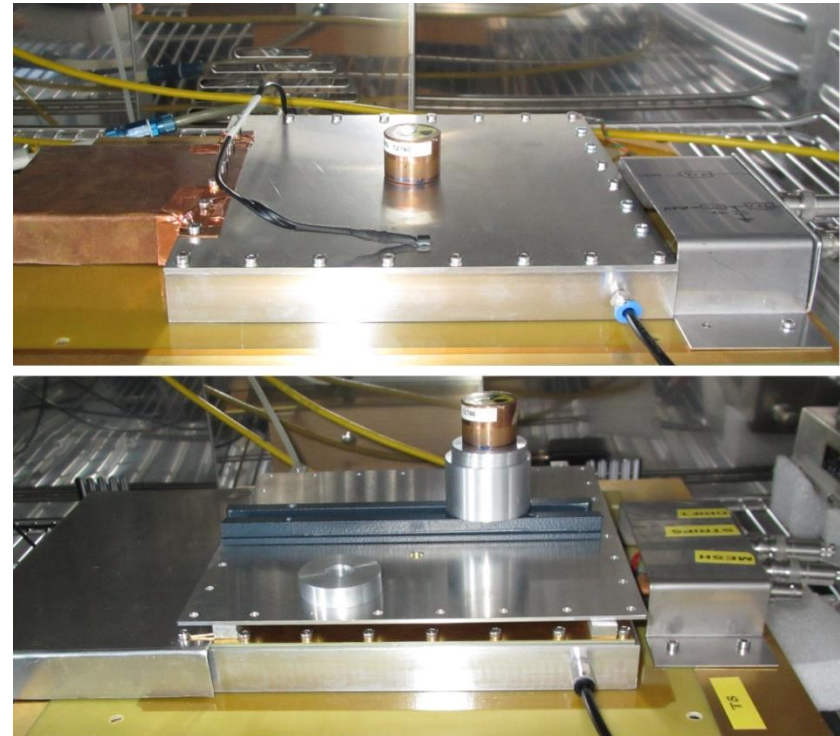


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Measurements taken in February 2013 in collaboration with the experimental particle physics group at the LMU Munich.



- two chambers tested:
 Standard (STD) & Resistive (RES)
- using an ^{55}Fe source
- temperature controlled measurement
- pressure controlled to $\pm 0,3$ mbar,
 self mixed Ar-CO₂ 93:7 gas
- accumulated charge on 18 readout
 strips has been measured



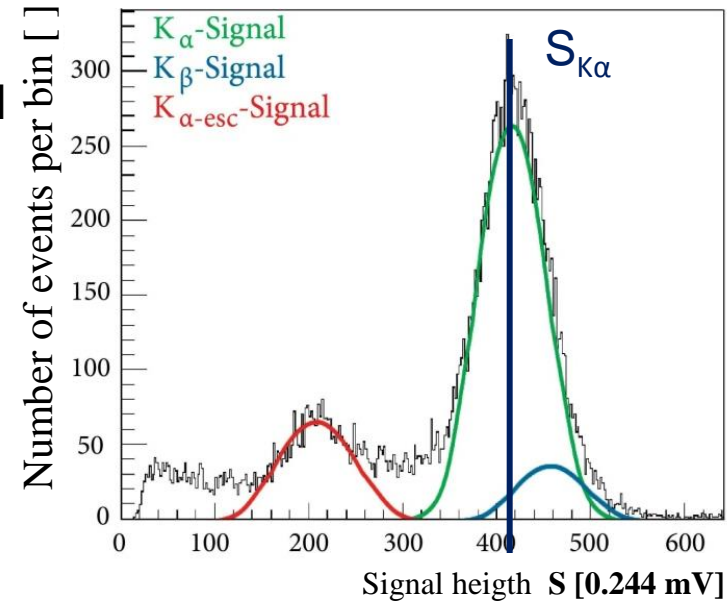


Measure the gas gain: Spectra of the ^{55}Fe source was recorded using $\sim 20\text{K}$ events.

Signal Position of the K_α -Peak $S_{K\alpha}$ is related to the signal of $n_{K\alpha} \approx 230$ primary electrons produced by the 5,9 keV photon.

The mean gas gain F can be calculated by:

$$F(E_{amp}) = \frac{Q_{real}}{n_T \cdot e} = \frac{S_{K\alpha}(E_d, E_{amp}) \cdot \frac{1}{f_{Cor}}}{n_{K\alpha} \cdot T(E_d, E_{amp}) \cdot e}$$



Simulate the gas gain: Avalanche size of single primary electron.

$$F = \overline{n_e}$$

f_{Cor} refers to studies in:

[Bortfeldt, J.: Development of Micro-Pattern Gaseous Detectors - Micromegas, LMU Munich, Diplomarbeit, 2010].

Measure the transparency T : indirectly by observation of the shift in the peak-Position ($S_{K\alpha}$) under variation of E_d at constant E_{amp} , assuming $\lim_{E_d \rightarrow 0} T = 100\%$.

$$F(E_{amp}) = \frac{Q_{real}}{n_T \cdot e} = \frac{S_{K\alpha}(E_d, E_{amp}) \cdot \frac{1}{f_{cor}}}{n_{K\alpha} \cdot T(E_d, E_{amp}) \cdot e}$$

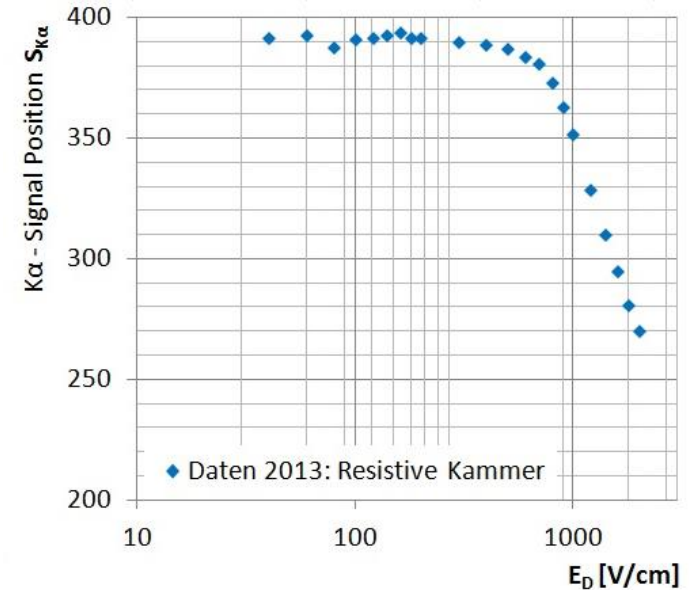
Normalization of the Data to 99%-100% at
 $E_{drift} < 400$ V/cm

Simulate the transparency T :

$$T = \frac{n_T}{n_T + n_A}$$

n_T = Number of events with $z_{min} < 120 \mu\text{m}$, n_A = Number of events with $z_{min} > 120 \mu\text{m}$ *

*(other definition of n_T and n_A has been tested using the number of electrons per event, yielding the same transparency at $< 1\%$ – Level.)



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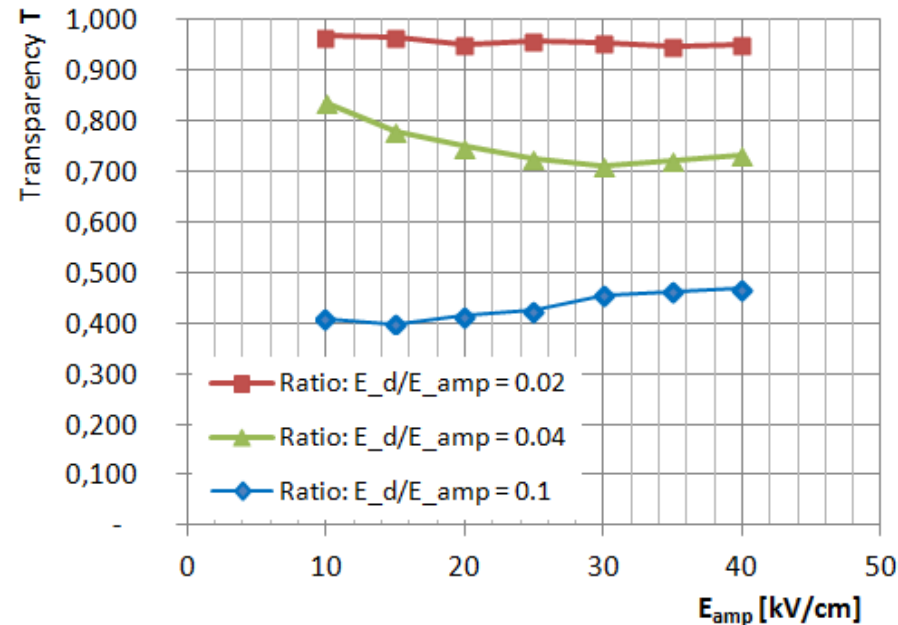


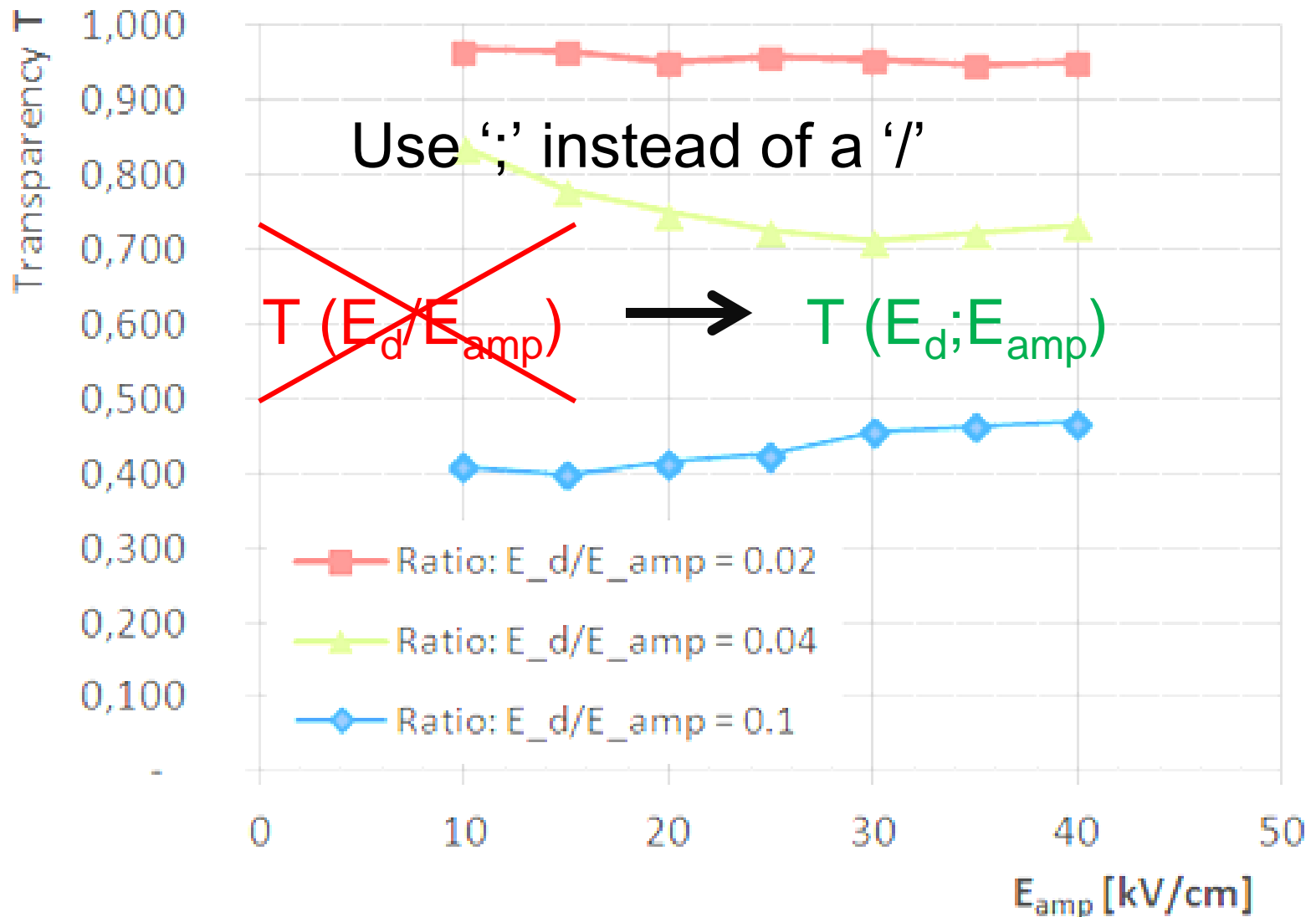
Transparency depends on various parameters:

- **mesh geometry** (woven & calendared or electroformed, wire diameter, wire periodicity, optical transparency)
- **gas mixture**
- gas parameters (**pressure**, **temperature**)
- **electric configuration (voltages)**

In literature, often you can find $T (E_d/E_{amp})$ without any theoretical or experimental justification for this parameter reduction.

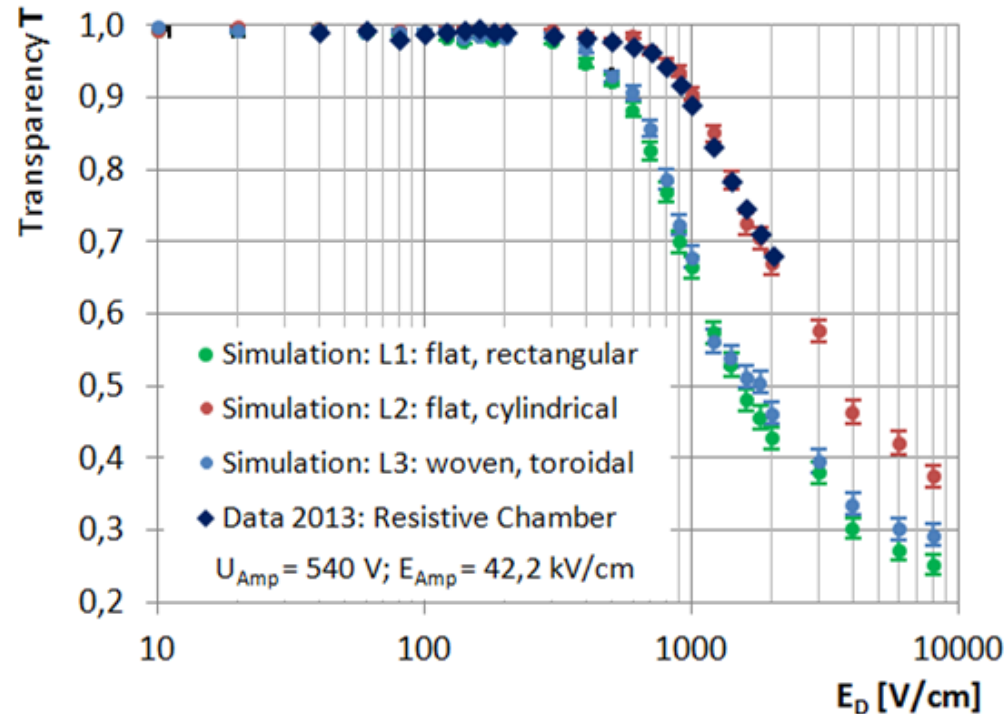
→ Simulation study with fixed
Ratio $E_d/E_{amp} = 0.1; = 0.04; = 0.02$







Comparison of the measured and simulated transparency with constant amplification field and varied drift field.

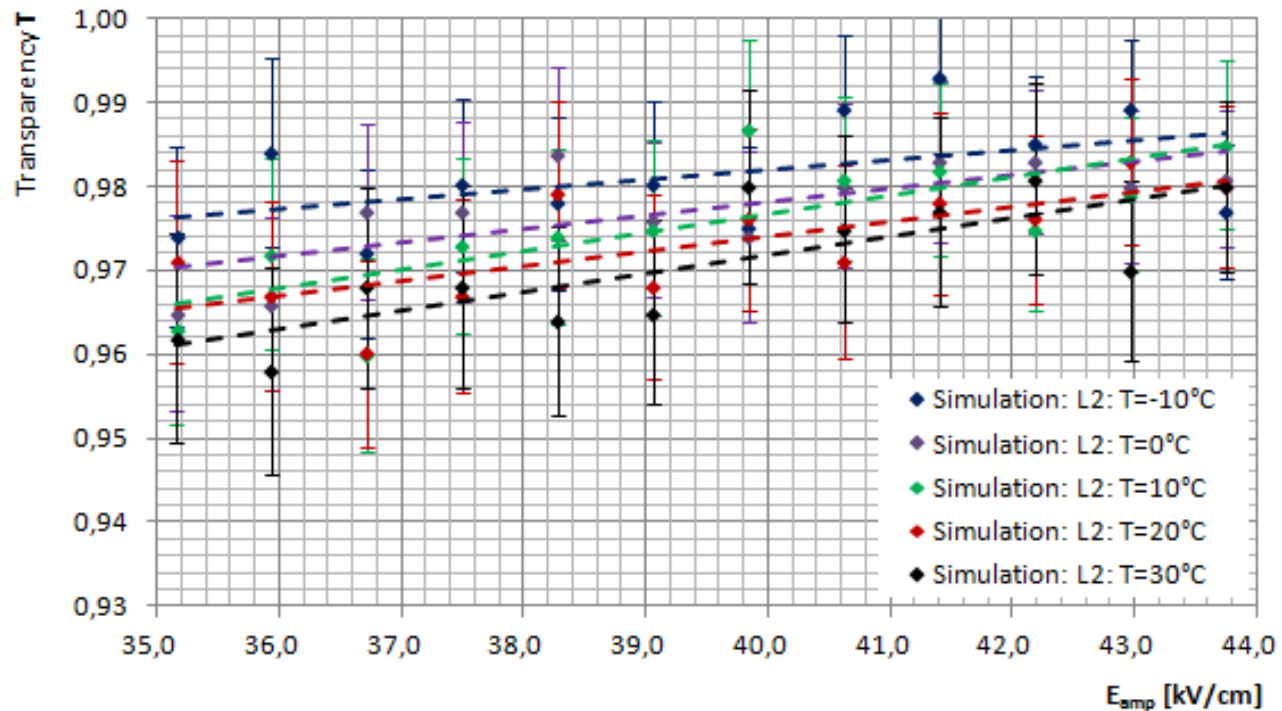


- Experimental and simulation data are in very good agreement for Layout 2
- Layout 3 shows a reduced transparency compared to L2 simulation and data
- Layout 1 transparency underestimates data, in agreement with previous studies

[K. Nikolopoulos, et al: *Electron transparency of a Micromegas mesh*; Journal of Instrumentation 6 (2011)]



The simulated transparency of the mesh with constant driftfield and varied amplification field is shown for different temperatures (-10°C to 30°C).
 (including linear fits as dashed lines)



- Increase of the transparency with the amplification voltage can be observed
- Decrease of the transparency with growing temperature is noticeable

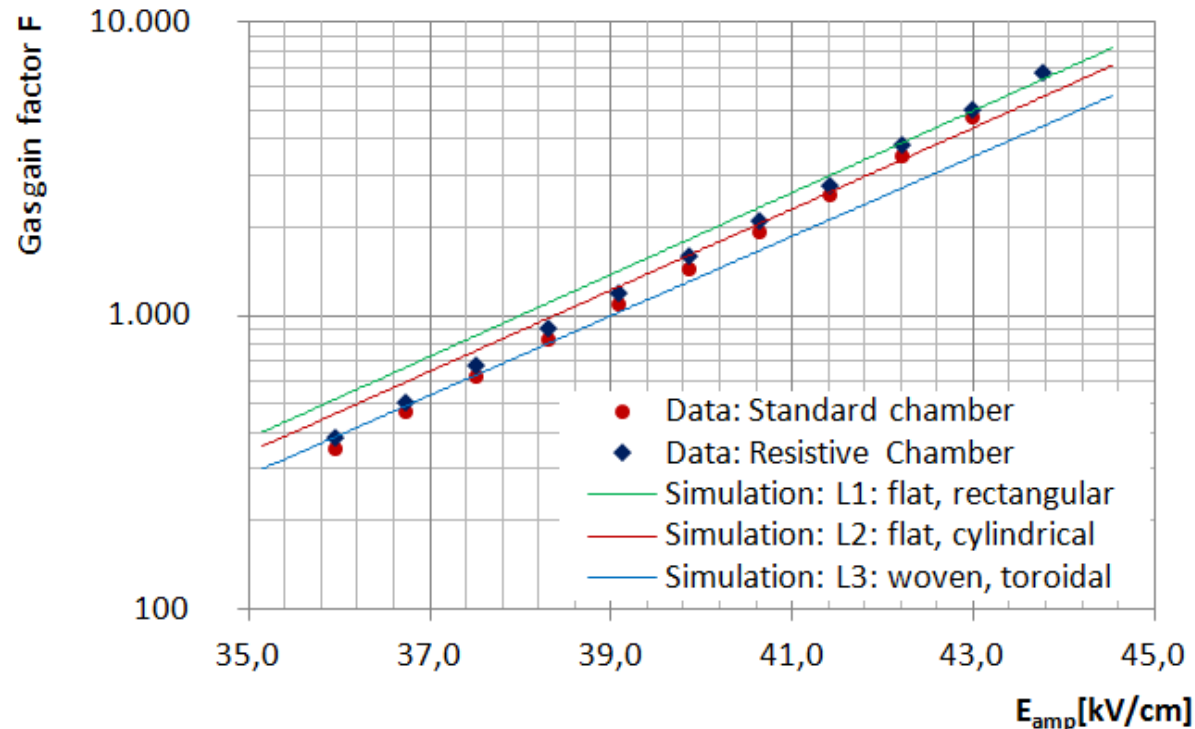


Gas gain also depends on a set of parameters:

- electric configuration: E_{amp} ; (E_d)
- gas mixture
- gas parameters (pressure, temperature)
- height of the amplification gap
- ? mesh geometry ?



The amplification factor for a single electron F , the gas gain, with exponential fit:

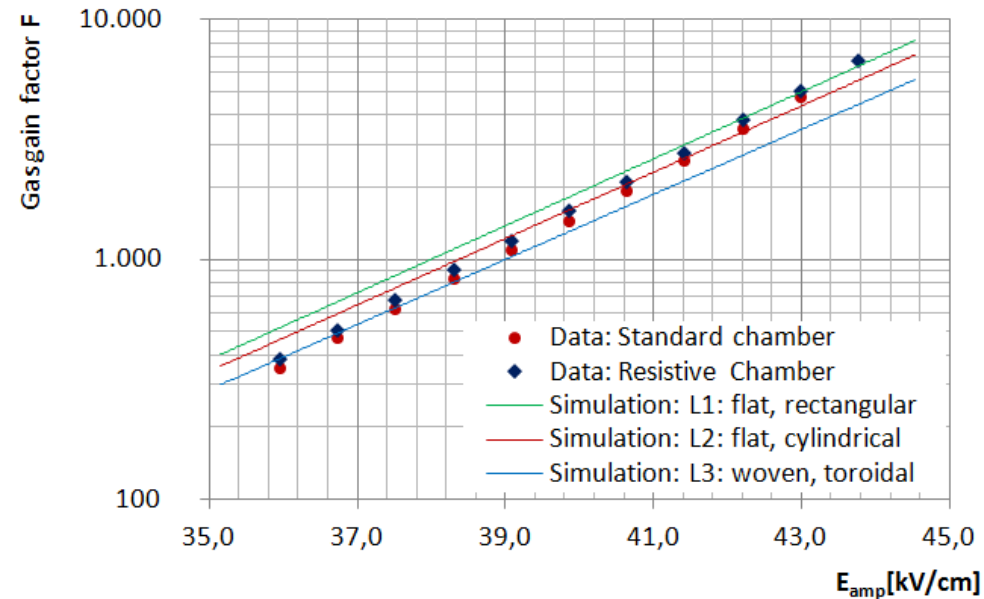


- All data (simulated and experimental) show the exponential behavior
- Good agreement in order of magnitude between simulation and experiment
- Experimental data grow faster



Experimental data:

- Resistive chamber shows an slightly higher amplification behavior of approx. 8,5 %
- Unexpected behavior, signal loss due to resistive strips would be expected



- But: Comparison of the lines assumes equal thickness of the amplification

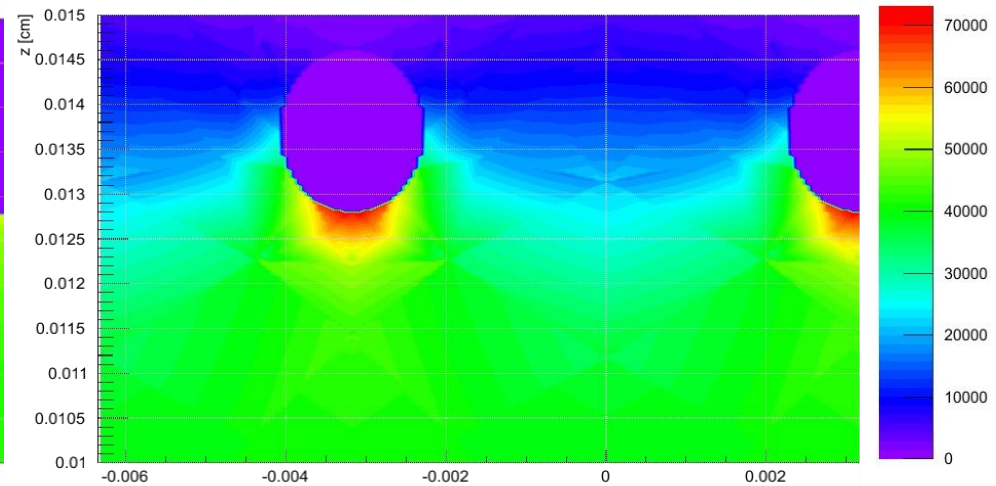
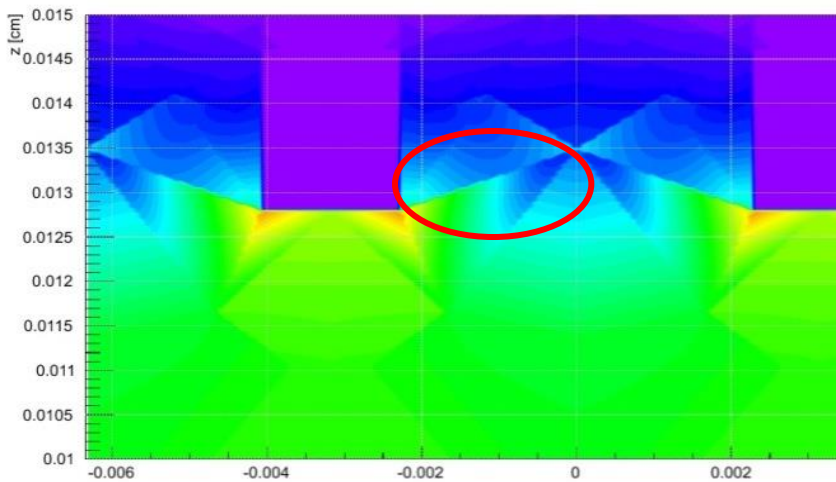
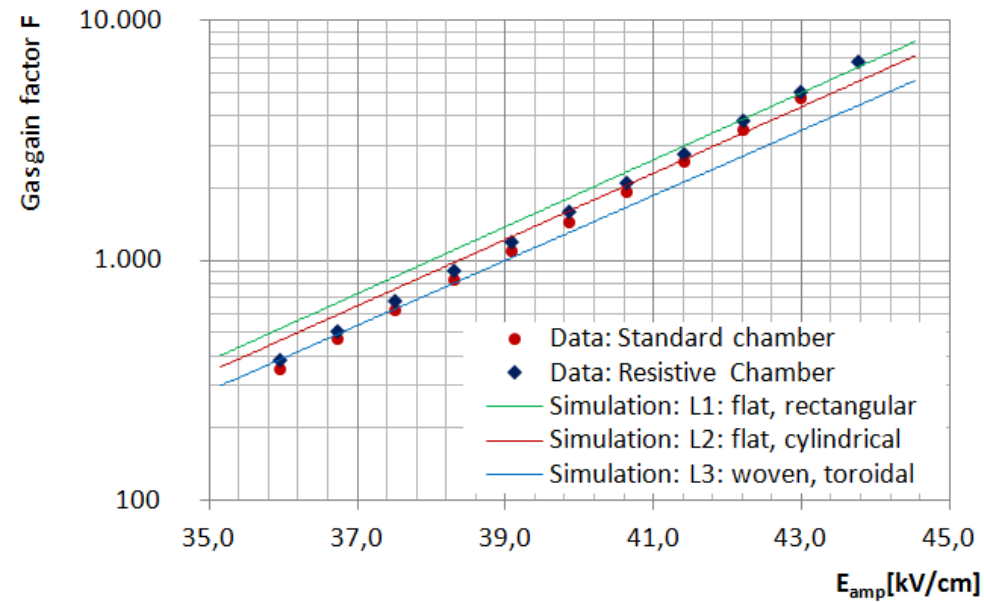
gap ($d_{amp}=128 \mu m$), which is used to determine
$$E_{amp} = \frac{U_m - U_a}{d_{amp}}$$

- Only a deviation of $\pm 1 \mu m$ in this thickness leads to an agreement of the data.



Simulated data:

- **Layout 1** simulation results show the highest gas gain.
- This results from an artifact in the field maps, created by the FEM using the ANSYS *smartmeshing*.

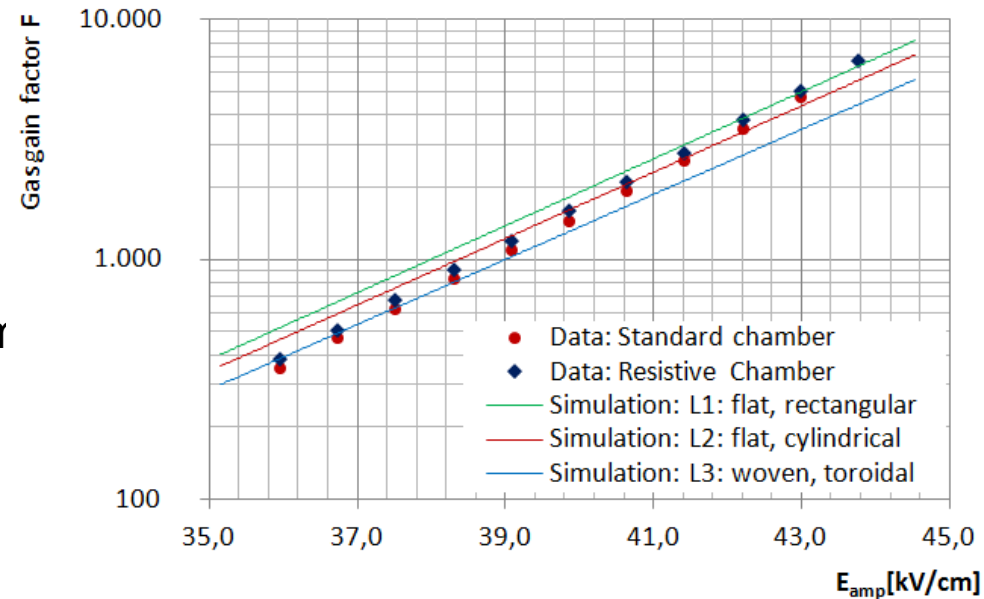


A screenshot of an ANSYS simulation showing a stress distribution on a complex, multi-faceted geometry. The color scale ranges from blue (low stress) to red (high stress). A red oval highlights a specific region of high stress concentration at a sharp corner or junction. The background is a grid of blue and purple, with the object's surfaces in shades of cyan, green, and yellow.

Be aware when dealing with
ANSYS *smart meshing*
+ simple geometries with flat surfaces

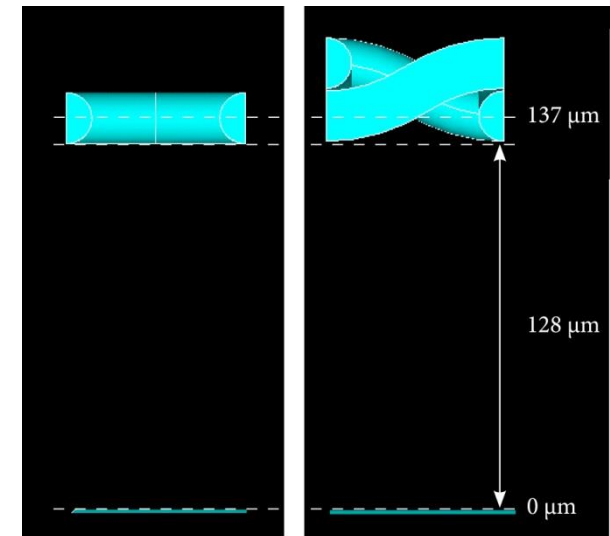
Simulated data:

- **Layout 3** simulation results show the lowest gain values
- This discrepancy again results from the calculation of E_{amp} .



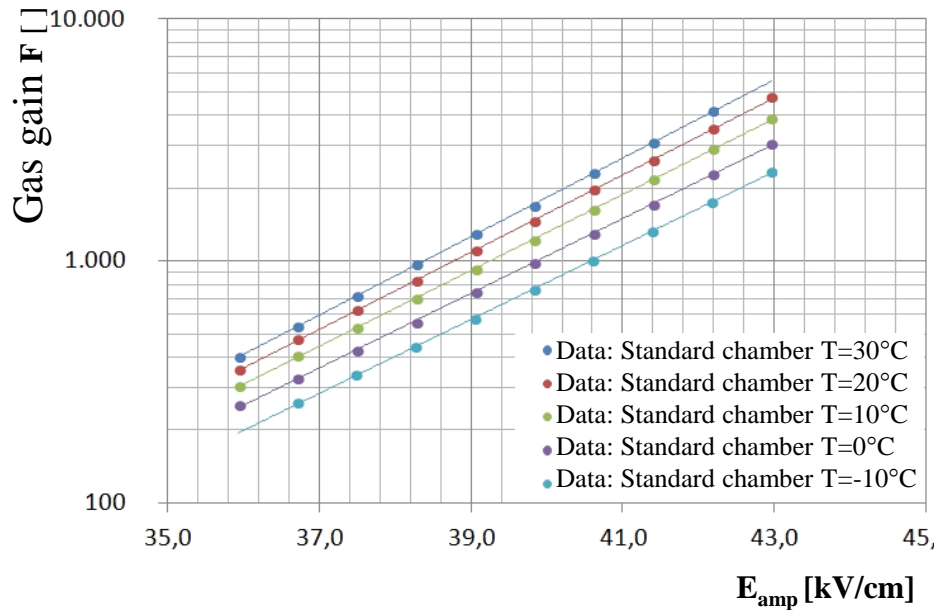
- Using the ,flat' Layout 1 and 2 the lower edge of the mesh is fixed at 128 μm above the anode.
- In Layout 3 only the lower edge of the curved wire is between 128 to 137 μm , thus the mean height of the gap is $>128 \mu\text{m}$.

- Electric field is overestimated by $E_{amp} = \frac{U_m - U_a}{d_{amp}}$

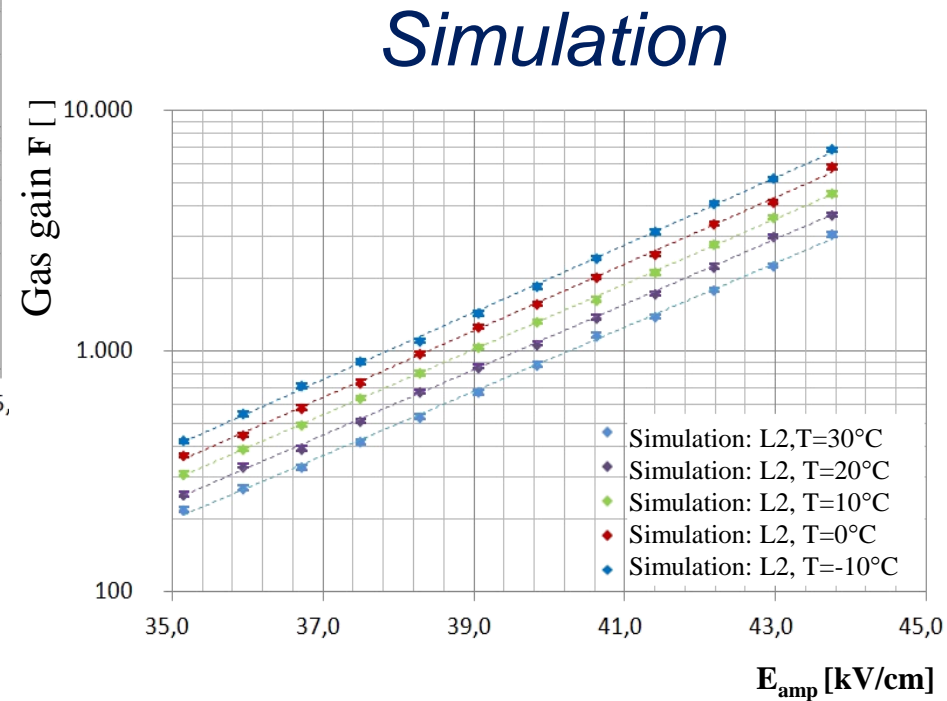




Gas gain ,voltage scan‘ for different temperatures in a range from -10°C to 30°C.



Experiment

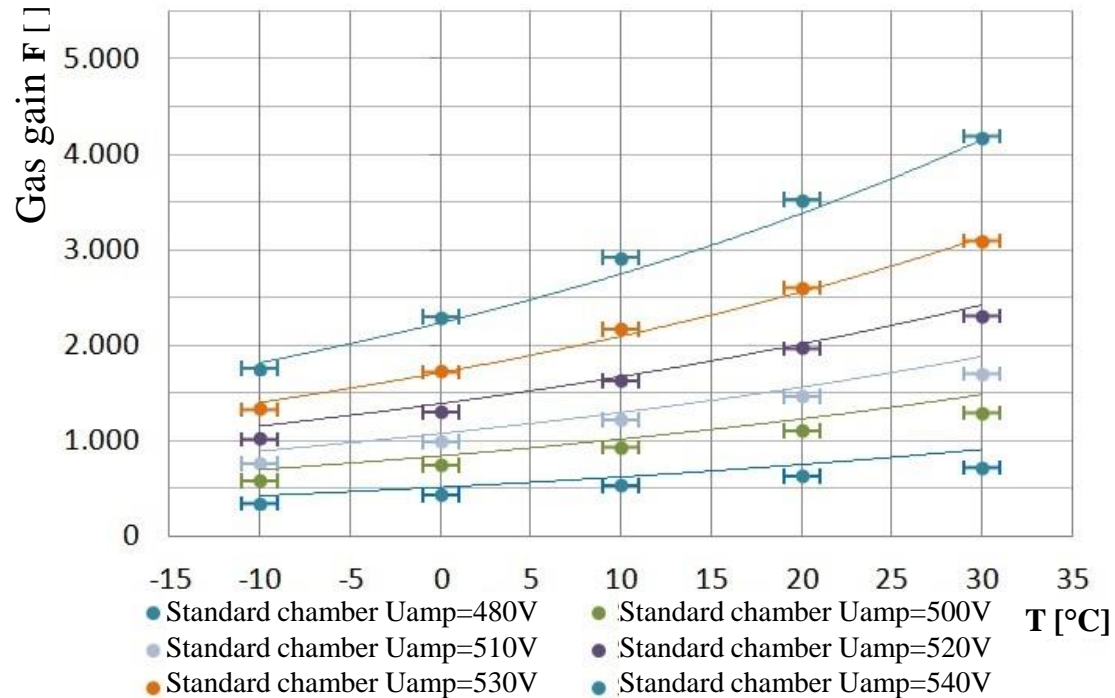


Simulation

→ Same behavior for different chambers / layouts at all temperatures



Agreement between STD chamber data and L2 simulation:



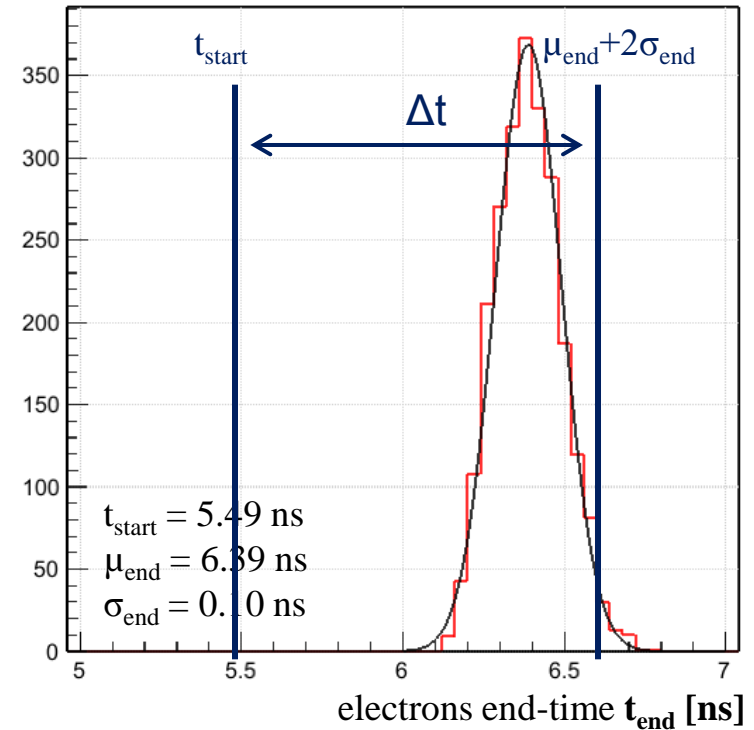
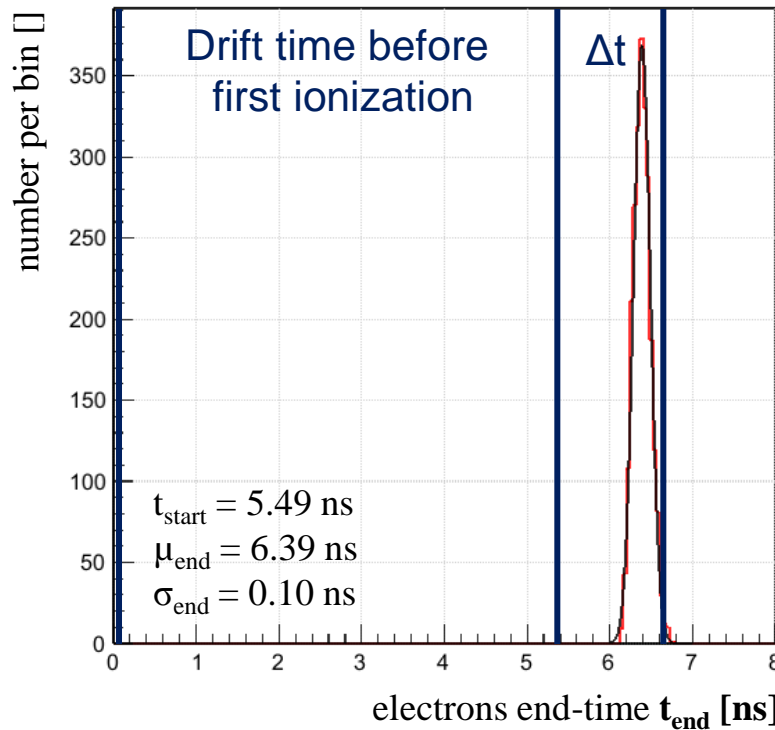
Comparison between gain factors in simulation (lines = exponential fit to simulated data) and experimental data (dots + errors) over growing temperature for different amplification voltages.

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Calculation of the development time of an electron avalanche Δt :

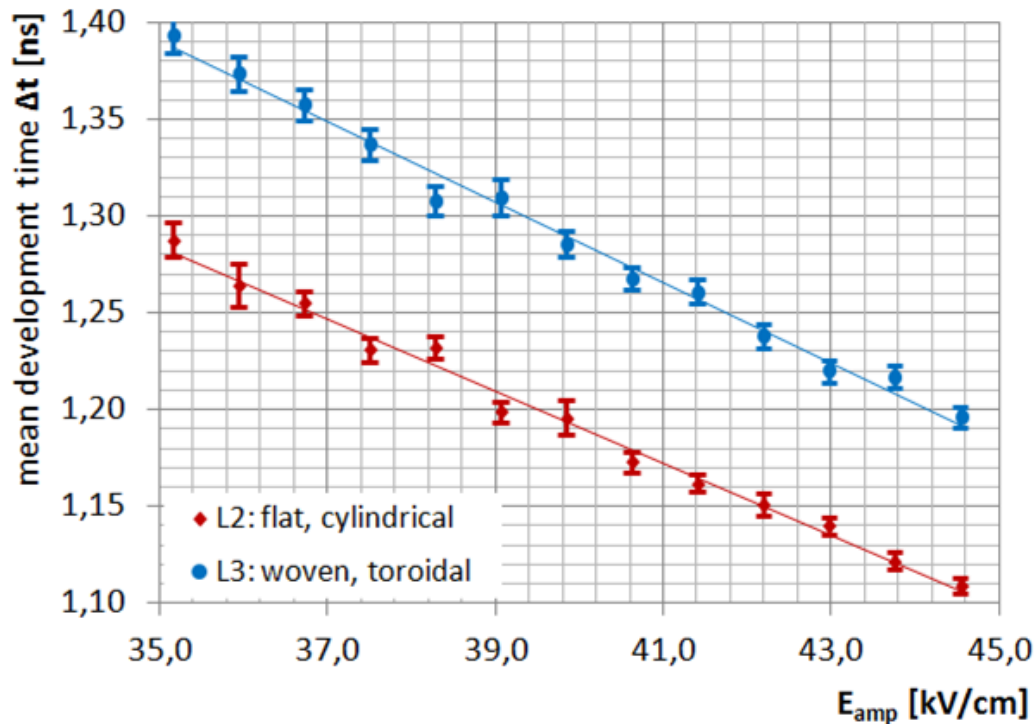
$$\Delta t = \mu_{end} + 2 \sigma_{end} - t_{start}$$



Time span from the production of the first secondary electron (=first ionization) until 97,5% of the avalanche-electrons reached the anode.



Dependency of the development time of an electron avalanche Δt on the electric field in the amplification gap.

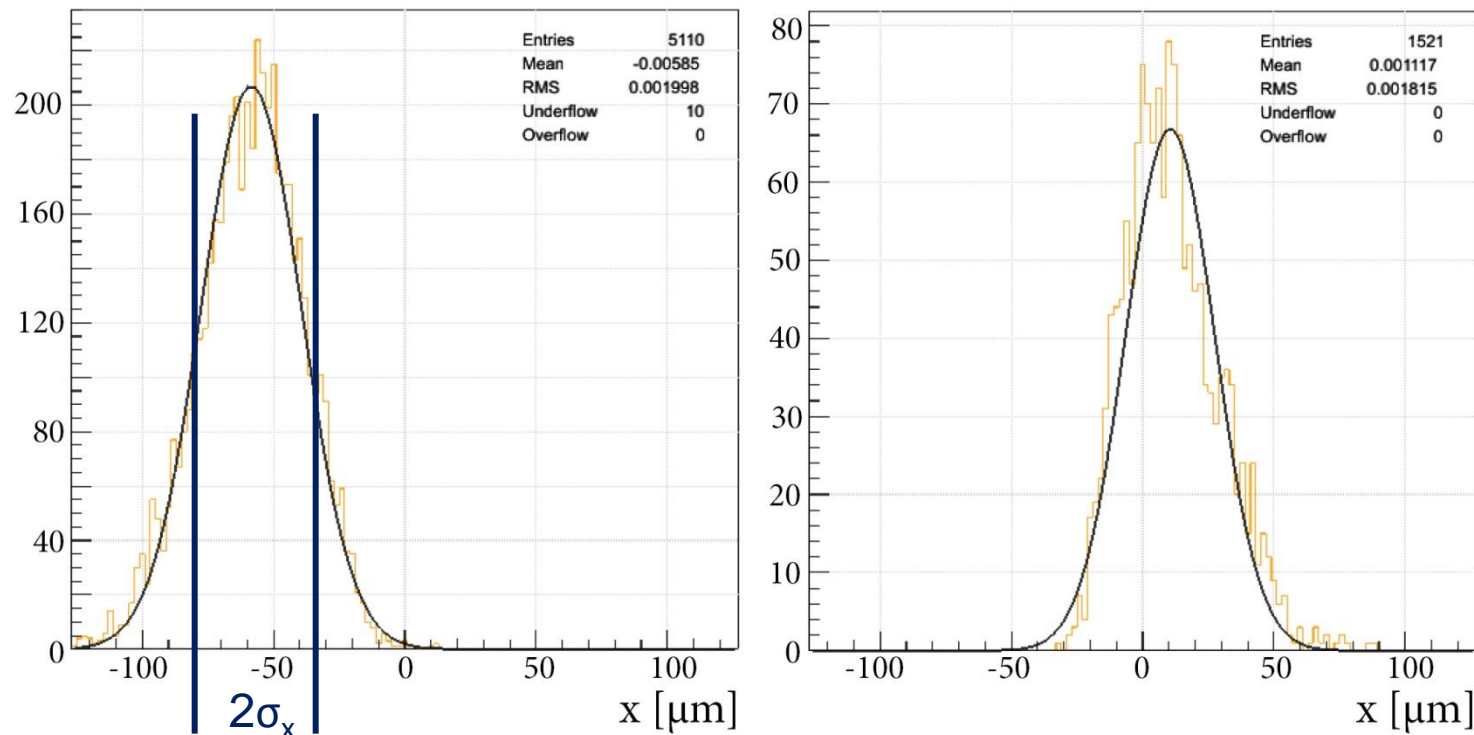


- Linear decrease of Δt with growing E_{amp} , due to higher mean electron velocity
- Systematical greater Δt for the toroidal Layout (L3), due to greater distance between anode and location of first amplification process

Microscopic results – *Spatial extent of an electron avalanche*



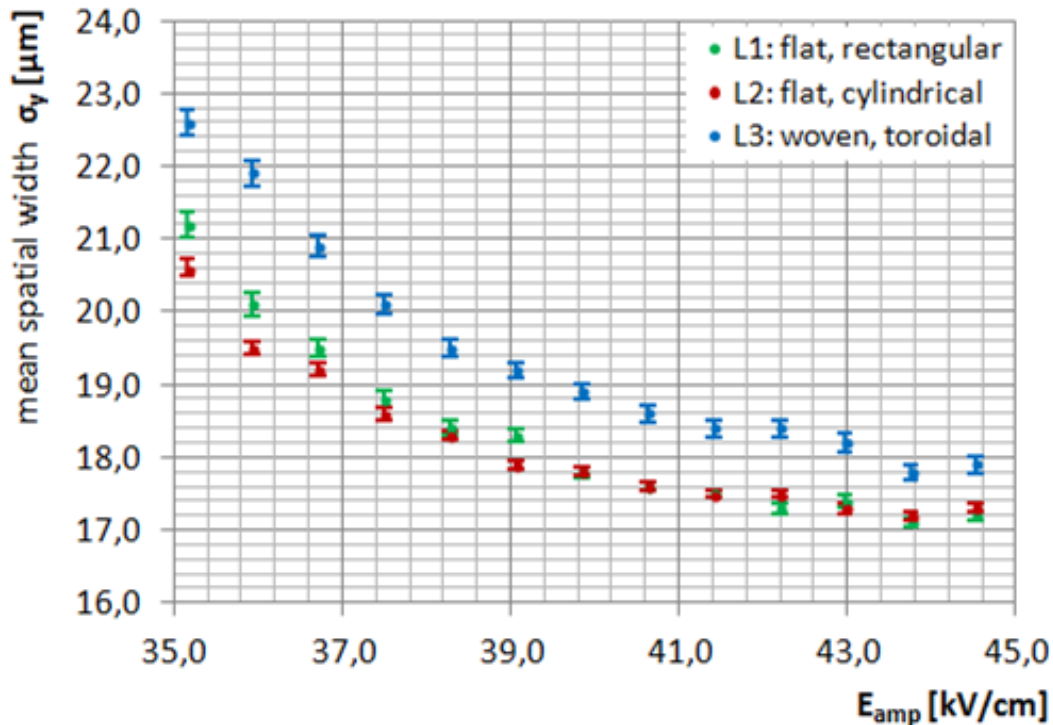
Gauss-function fit proved to be a good form-estimator for large avalanches, less good for small avalanches. Mean spatial extent measured by the sigma along the direction σ_x . (y – direction yields similar results)



The extent of 68% of the electrons can be estimated by $2\sigma_x$.



Electric field dependancy of the mean spatial extent measured by fitting a gauss-function, shown is the sigma along the x-direction σ_x .



- Decrease of spatial extent as expected, due to transversal diffusion $\sigma_x = \sqrt{2D \Delta t}$
- $\sim 50\%$ results from the decrease of Δt , thus $\sim 50\%$ influence on $D(E_{amp})$
- Again systematic offset for L3, according to longer diffusion time

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The number of electrons n_e in one avalanche is statistically distributed. For the parameterization of amplification often the Polya-distribution is used:

$$P(n_e) = \frac{1}{\bar{n}} \frac{(\Theta + 1)^{\Theta+1}}{\Gamma(\Theta + 1)} \left(\frac{n_e}{\bar{n}}\right)^{\Theta} e^{-(\Theta+1)\frac{n_e}{\bar{n}}}$$

Normalized two parameter function with mean electron number \bar{n} and form parameter Θ , which e.g. yields the most probable number of electrons:

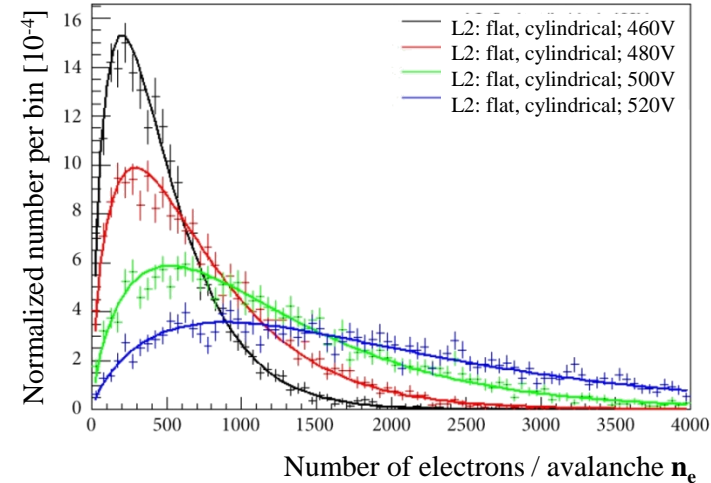
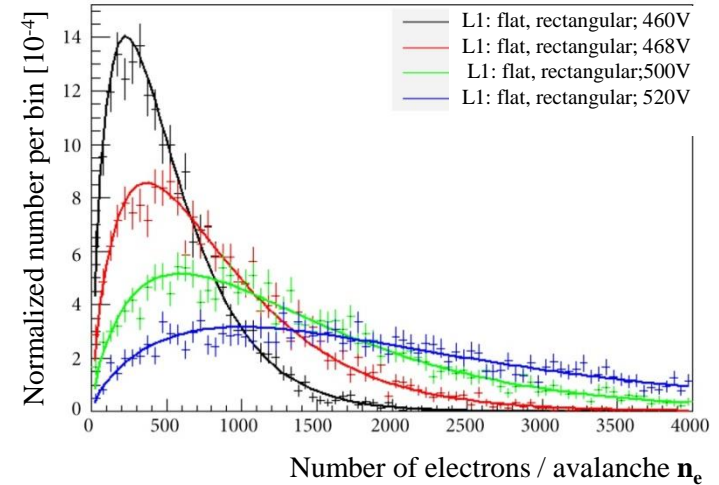
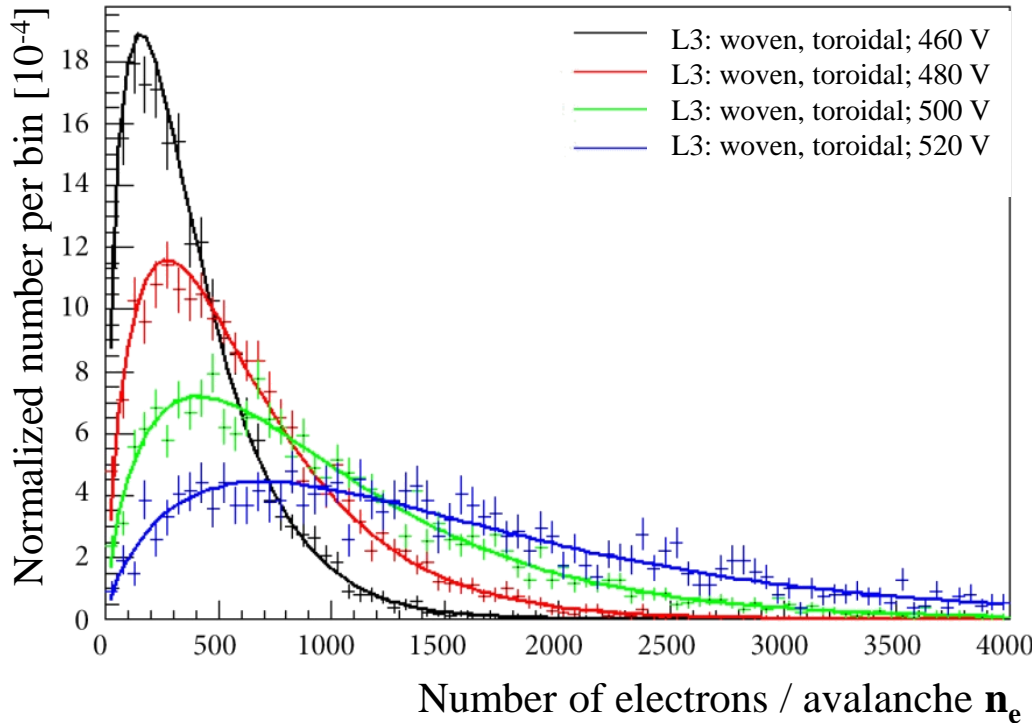
$$n_{mp} = \frac{\bar{n} \Theta}{\Theta + 1}$$

And the width of the distribution:

$$f = \frac{1}{\theta + 1}$$

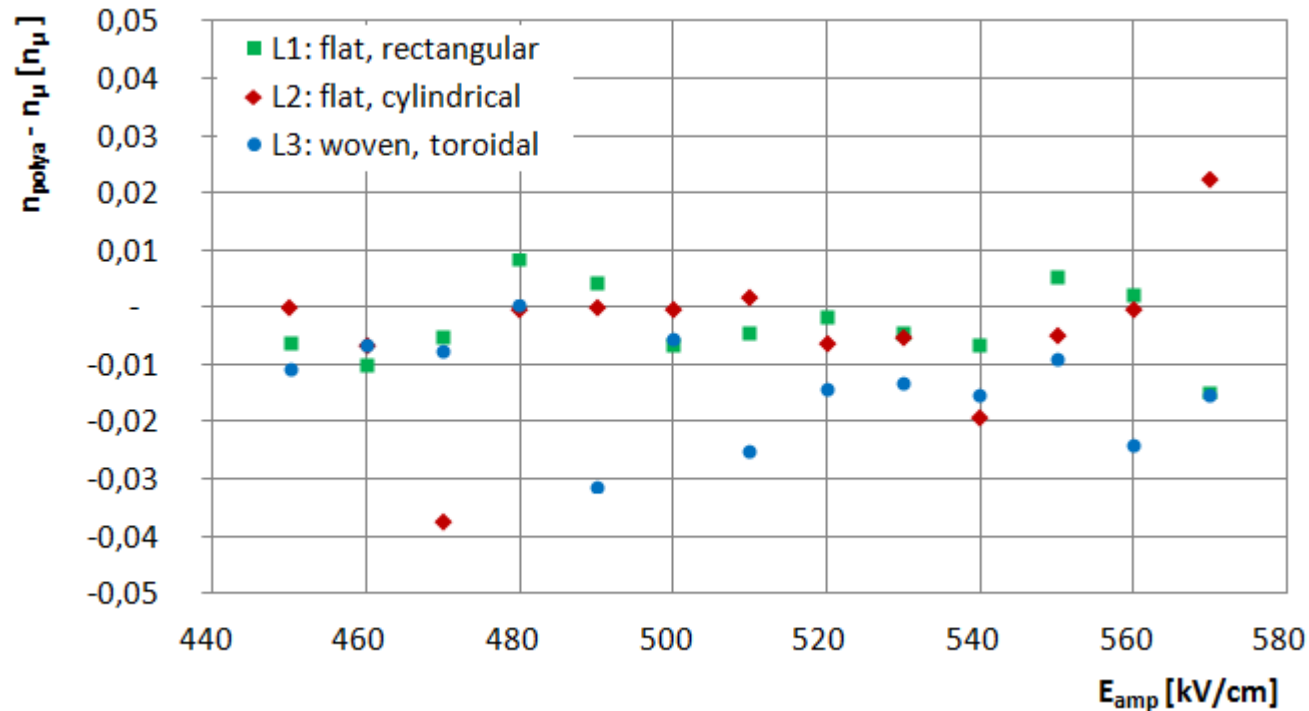


Using Polya distribution to describe gain fluctuations in micromegas simulation





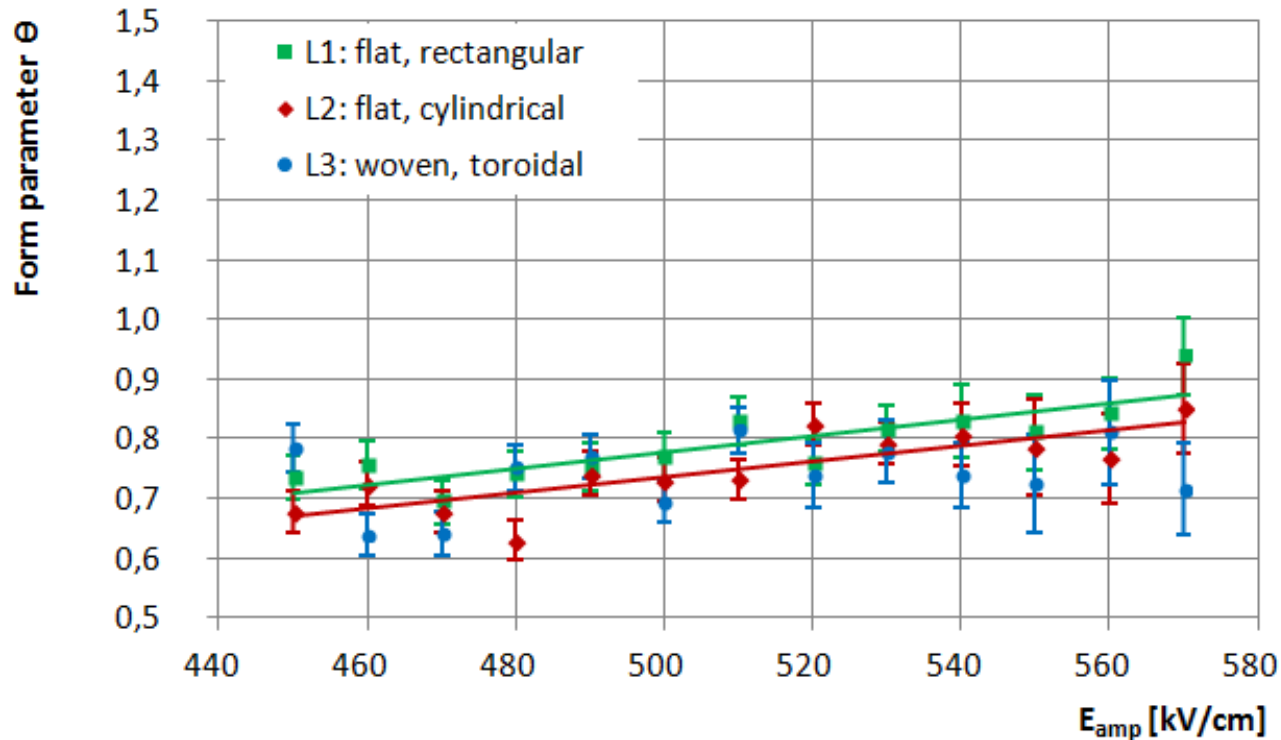
Comparison of mean electron numbers from raw-simulation results n_μ and the numbers taken from the polya fits n_{polya} for different amplification voltages.



This yields a very small underestimation of the ‘real’ value by the fit in Layout 1 (0,3%) and Layout 2 (0,4%) and a noticeable underestimation for the results simulated with Layout 3 (1,4%).



Observation of the form parameter Θ within typical parameter range.



The data produced by L1 and L2 favor a slight growth in Θ

→ Study has to be optimized to reduce to errors



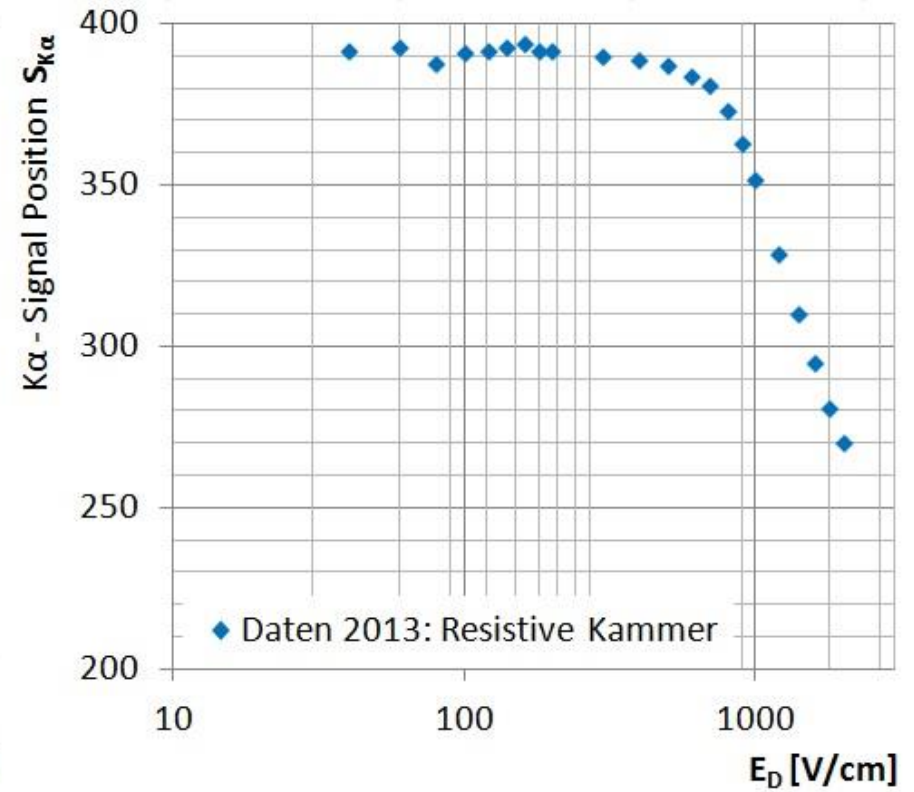
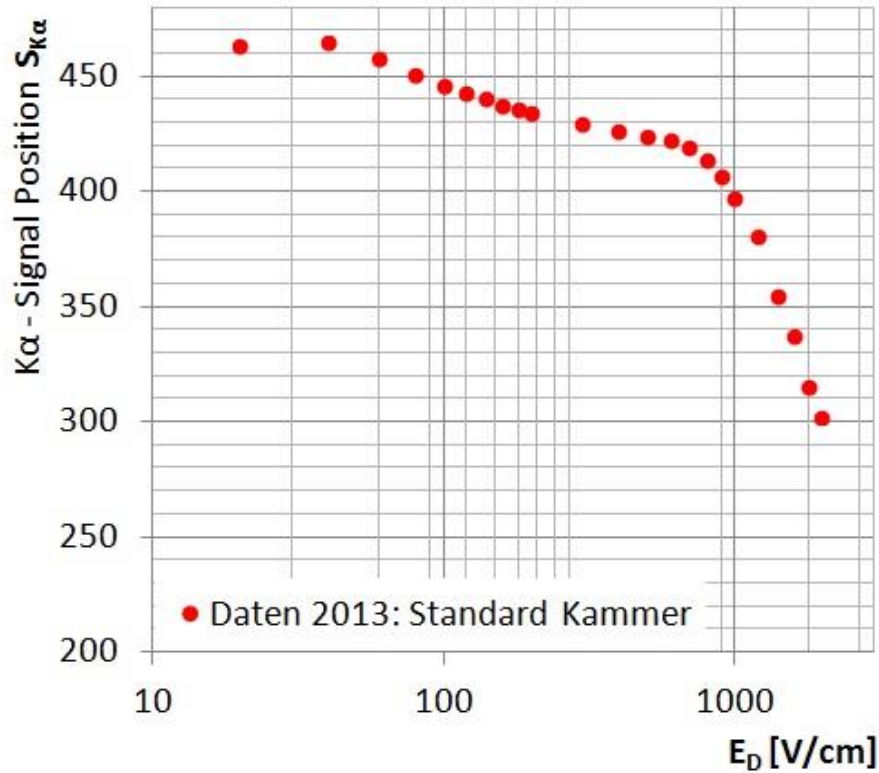
- The mean electron number seems to be slightly underestimated by the Polya-fit function (not significant for L1 and L2).
- The form parameter shows a slight growth with the amplification voltage, further studies on dependencies on gas parameters are to be done.
- A list of parameters (\bar{n} and Θ) for different amplification voltages with the given gas mixture and environmental conditions has been provided for further use.

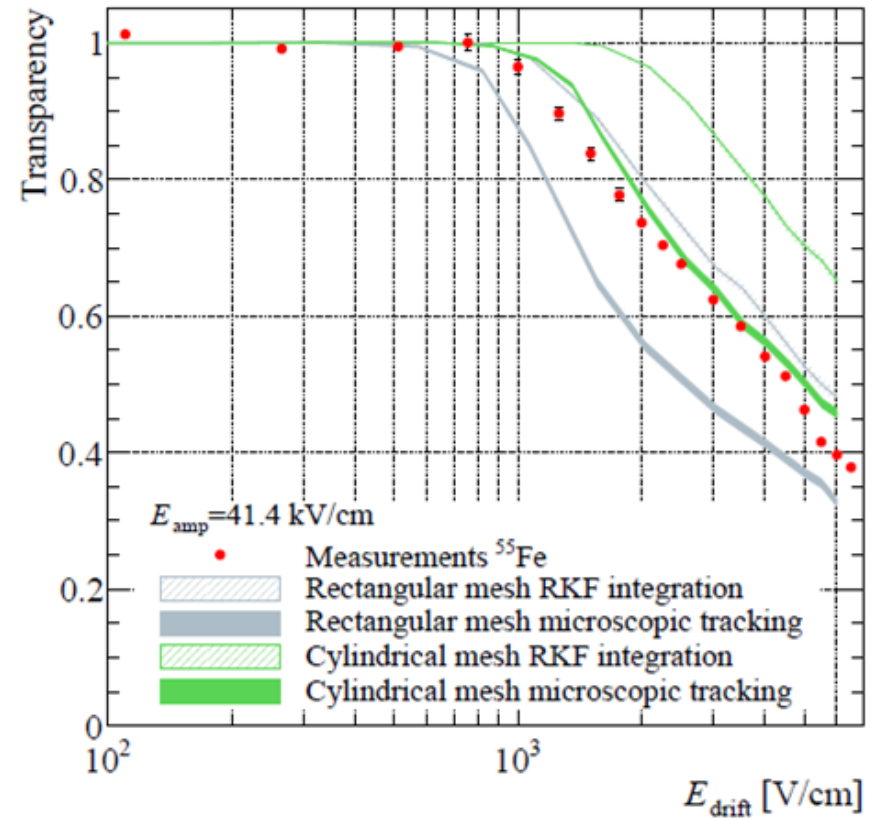
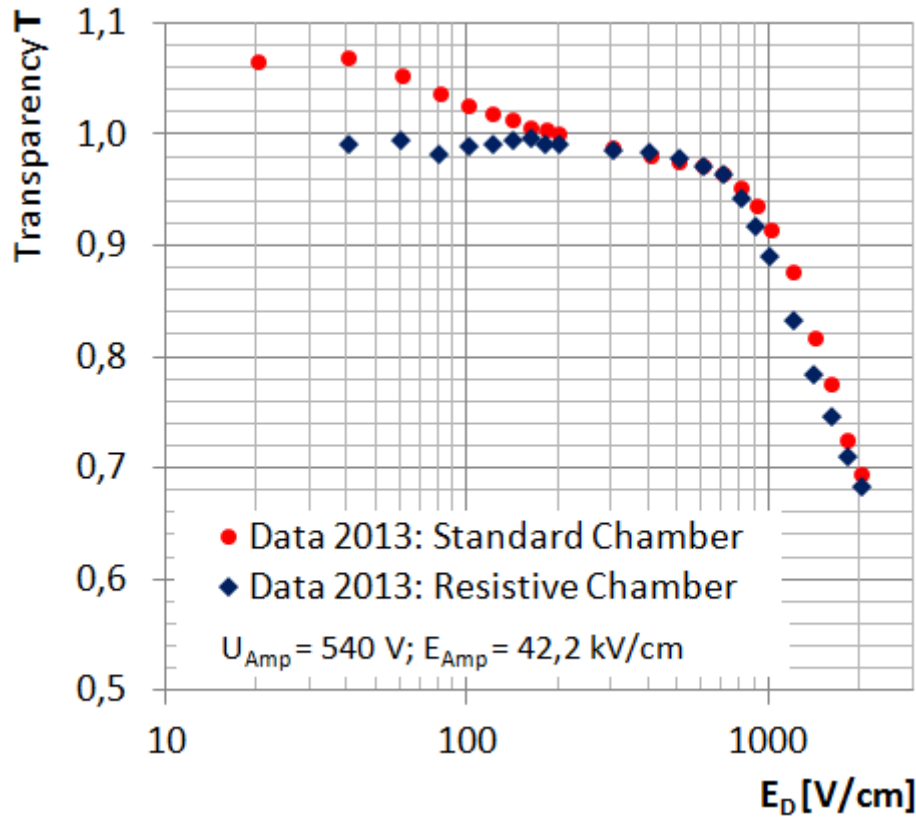


- All experimental accessible macroscopic results (Transparency, Gas gain incl. temperature scan) are in good agreement with the simulation, favoring Layout 2 results.
- Microscopic values of the avalanche process have been studied and guide values could be derived. ($\Delta t = 1,2 - 1,4$ ns; $2\sigma_x = 35 - 45$ μm).
- The statistic of single electron amplification has been successfully described by using Polya-distribution, Form parameter shows a slight dependence on the amplification voltage.
- Layout 3, taking the woven structure of the mesh into account, did not yield better simulation results, since the mesh thickness is clearly overestimated.
- The validated simulation could be use to study different gas mixtures and / or pressure behavior.
- A further improved Layout, taking the calendering process into account, should be studied and compared to Layout 2.

Thank you for your attention!

*Questions, remarks and comments are
highly welcome.*







Merkmal	Symbol	Standard MM	Resistive MM
Innere Abmessungen			
Höhe des Driftbereichs	d_D	5,0 mm	5,0 mm
Höhe des Verstärkungsbereichs	d_V	128 μm	128 μm
Parameter des Netzes			
Drahtdurchmesser	$\varnothing_{\text{Draht}}$	18 μm	18 μm
Drahtdichte	n_{Draht}	400 lpi	400 lpi
Periodizität	p_{Netz}	63,5 μm	63,5 μm
Optische Transparenz	T_{Opt}	51,3 %	51,3 %
Parameter der Streifenelektrode			
Streifenlänge	l_{Streifen}	100 mm	100 mm
Streifenbreite	b_{Streifen}	150 μm	250 μm
Streifenperiodizität	p_{Streifen}	250 μm	400 μm
Gesamte aktive Fläche	A_{gesamt}	90 cm^2	100 cm^2
# der ausgelesenen Streifen	$\#_{\text{Streifen}}$	18	18
Parameter der Pfeilerstruktur			
Pfeilerdurchmesser	$\varnothing_{\text{Pfeiler}}$	300 μm	300 μm
Pfeilerperiodizität	p_{Pfeiler}	2,5 mm	2,5 mm
Inaktiver Flächenanteil	A_{Pfeiler}	1,1 %	1,1 %

Backup – Capaticity Correction Factor

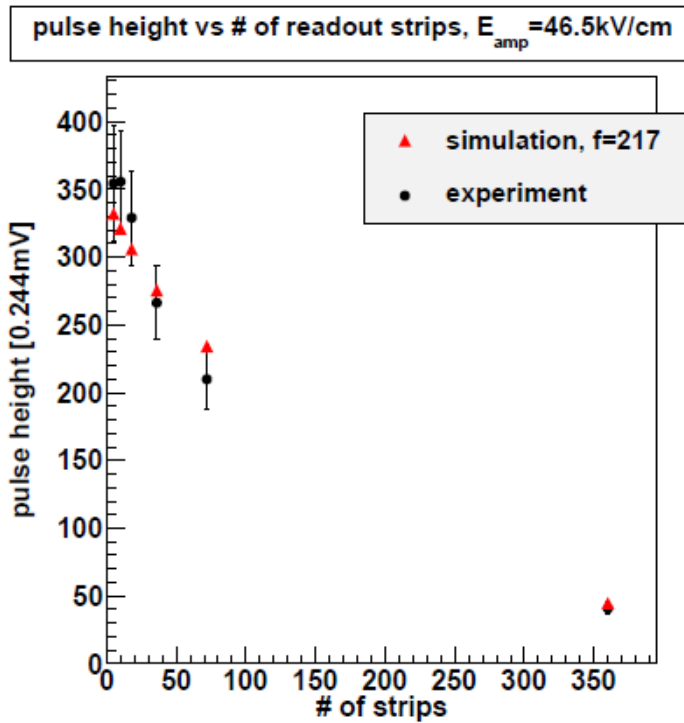


Figure 8.11: Pulse height of 5.9 keV X-rays as a function of the number of readout strips.

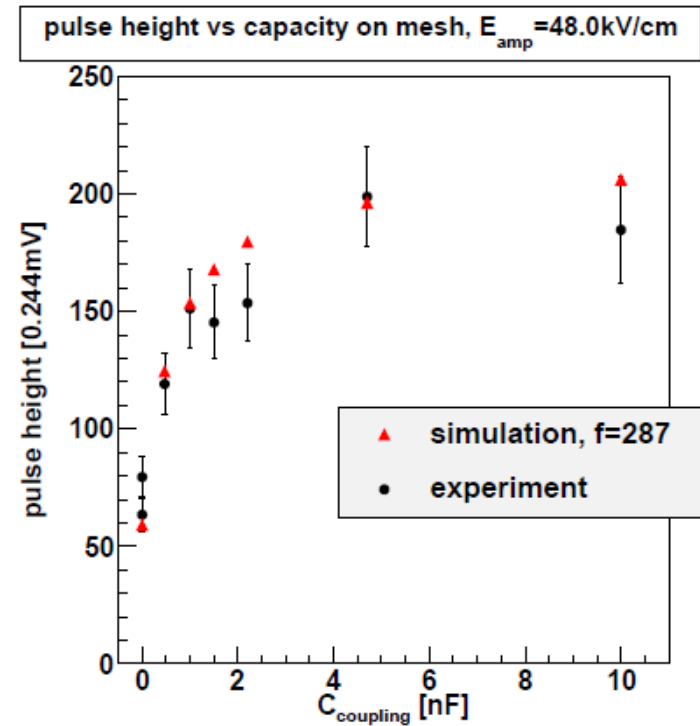


Figure 8.12: Pulse height of 5.9 keV X-rays as a function of the additional capacitor between mesh and ground.

Number of strips	5	10	18	36	72	360
Q_{preamp}/Q_{total}	0.88	0.85	0.81	0.73	0.62	0.12

taken from [Bor11]

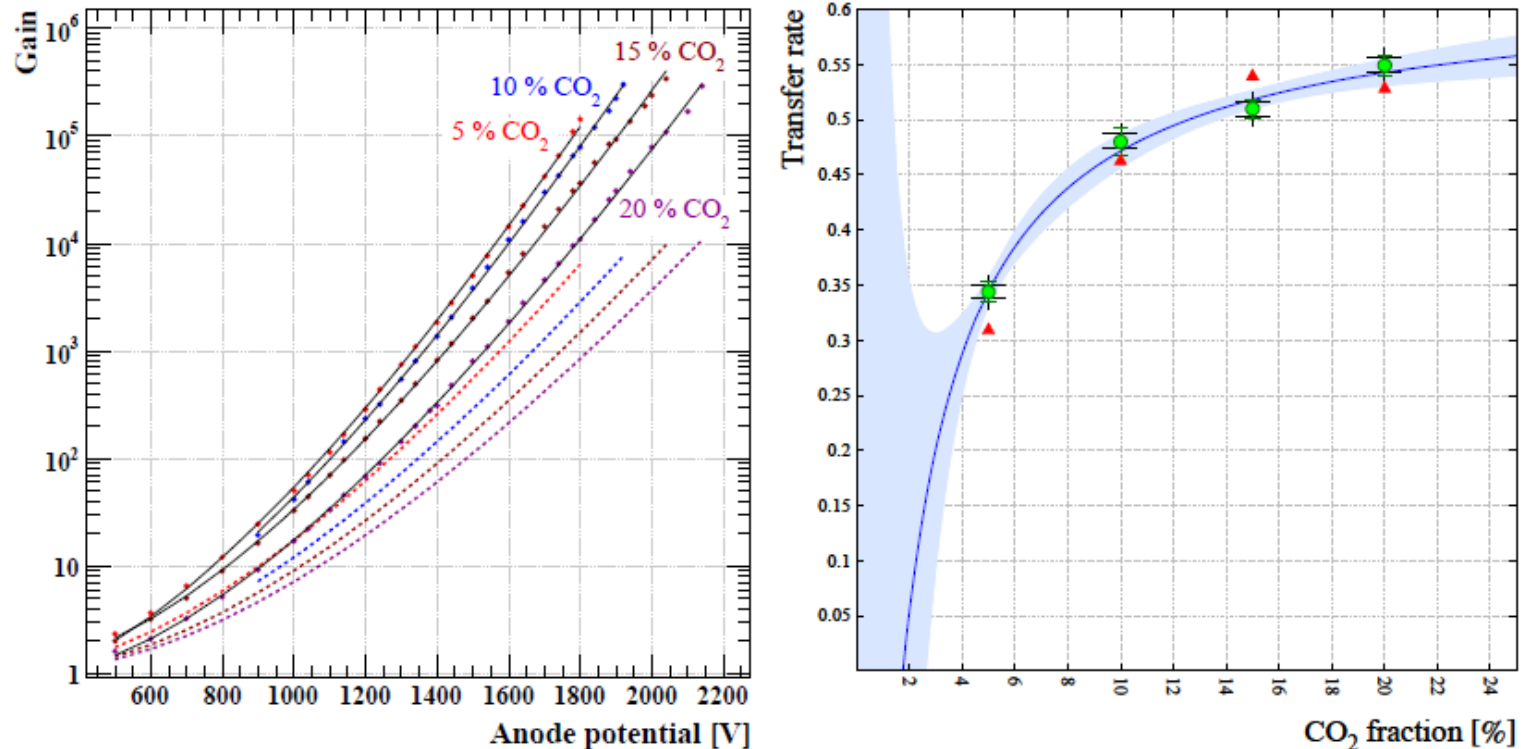


Figure 10. Left: Measured gain curves for Ar-CO₂ mixtures from T.Z. Kowalski et al. [58] (red dots) with fits of the transfer rates (black lines). For comparison, dashed purple lines show the calculated gain curves without transfer. Right: Transfer rates fitted with $(a_1c + a_3)/(c + a_2)$ (blue curve) and the uncertainty on this parametrisation (blue error band). The a_3 parameter is outside the physical range (by 1.2σ). The larger error bars are obtained leaving gain scalings and transfer fractions free, while the broader and smaller error bars correspond to fits with fixed gain scalings. The triangles indicate the transfer rates found when using the weighted average of the gain scaling factor in all fits.

taken from [Sah11]