

Taming QCD issues in gluon fusion with $gg \rightarrow VV$

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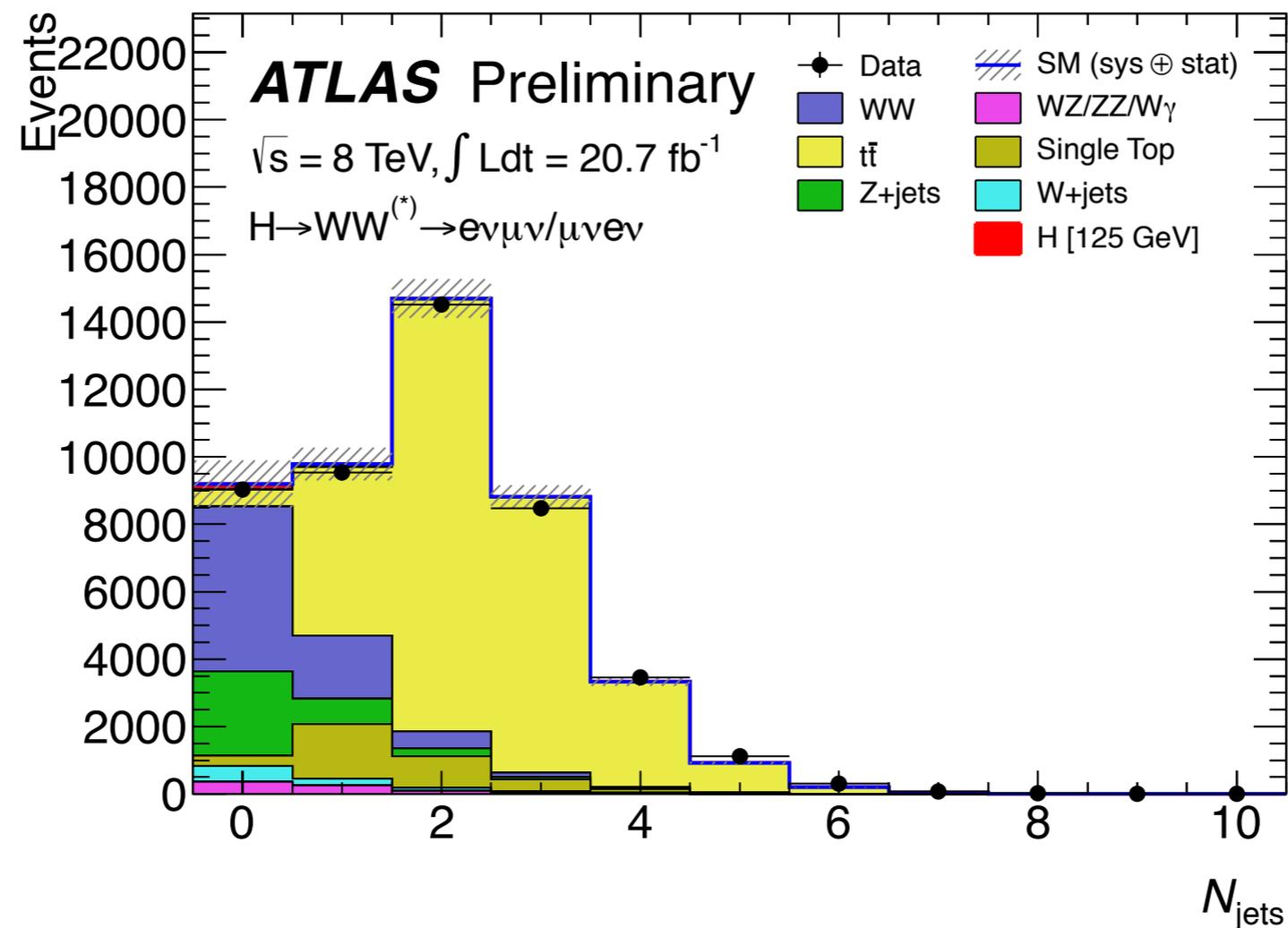


QCD TOOLS FOR LHC PHYSICS: FROM 8 TO 14 TEV - WHAT'S NEEDED AND WHY?

FERMILAB, NOV. 15TH 2013

WW production and
Higgs searches:
why it is interesting

VV production and Higgs physics: vector bosons as a background



Inclusive searches, coupling measurements, channel separation... **mostly $qq \rightarrow VV$ ($\sim 90\%$)**

VV production and Higgs physics: vector bosons as probes for Higgs properties

[Martin; Dixon, Li; Passarino, Kauer; Kauer; FC, Melnikov]

Use **off-shell effects** to probe the Higgs nature

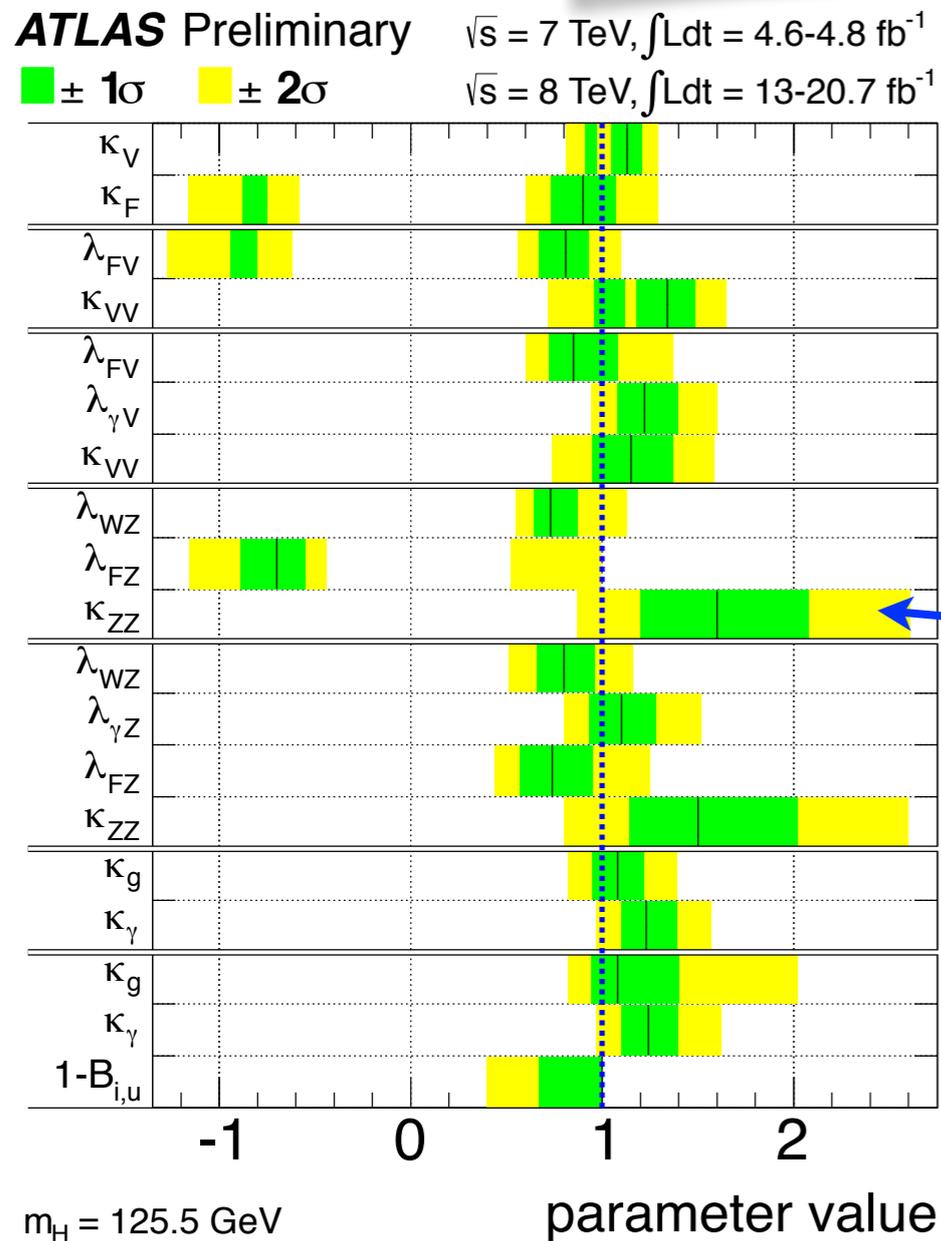
Off-shell effects:

- negligible for the **fiducial rate** for $m_H \sim 126$ GeV SM Higgs
[Ellis, Campbell, Williams (2011); Kauer, Passarino (2012); Kauer (2013)]
- can provide **complementary information** wrt traditional on-shell measurements \rightarrow model-independent Higgs properties
- may become **large for non standard Higgs** (e.g. high-mass SM-like Higgs)

SENSITIVE TO GG \rightarrow VV PROCESSES

Two examples: Higgs coupling determination

$$\sigma_{i \rightarrow H \rightarrow f} \approx \frac{\sigma_{i \rightarrow H} \Gamma_{H \rightarrow f}}{\Gamma_H} \approx \frac{g_i^2 g_f^2}{\Gamma_H}$$



Naively, we only have access to coupling ratios

A pragmatic approach:

1. take cross-section ratios to isolate desired production/decay mode
 2. fit assuming SM-like behavior
- [see e.g. Giardino et al.; Djouadi, Moreau (2013)]

Ideally:

MODEL-INDEPENDENT results

Higgs couplings: the problem

$$\sigma_{i \rightarrow H \rightarrow f} \approx \frac{\sigma_{i \rightarrow H} \Gamma_{H \rightarrow f}}{\Gamma_H} \approx \frac{g_i^2 g_f^2}{\Gamma_H}$$

σ is invariant under $g \rightarrow \xi g$, $\Gamma_H \rightarrow \xi^4 \Gamma_H$

For a model-independent determination,
we must break this degeneracy

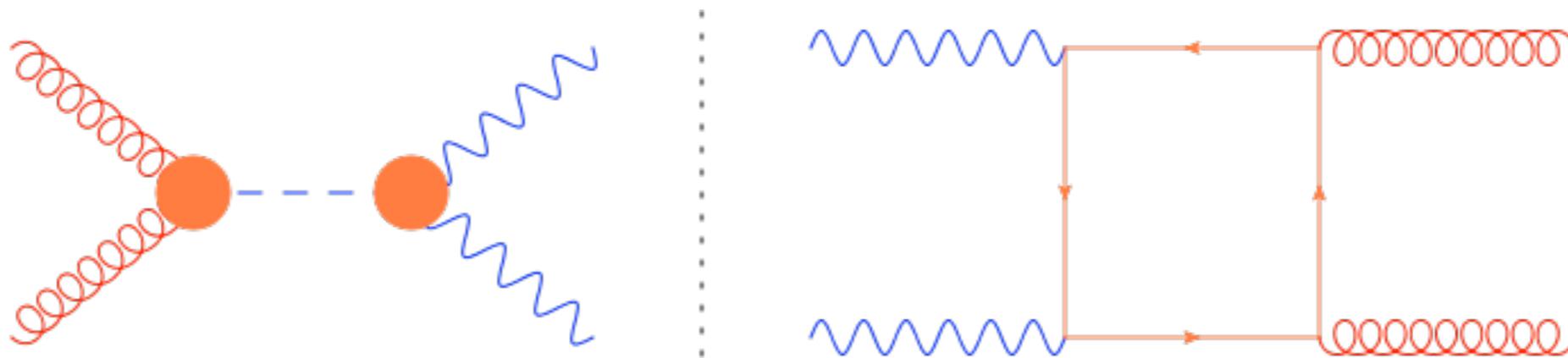
DIRECT MEASUREMENT OF THE HIGGS WIDTH?

- LHC sensitivity: $\sim 1-5$ GeV
- SM width: ~ 4 MeV !!!

WE NEED AN INDIRECT WAY OF MEASURING Γ_H

The key point: search for an observable with different dependence on $g_{i,f}$ and Γ_H

First example: use the mass-shift coming from $H \rightarrow \gamma\gamma$ interference [Dixon, Li (2013)]



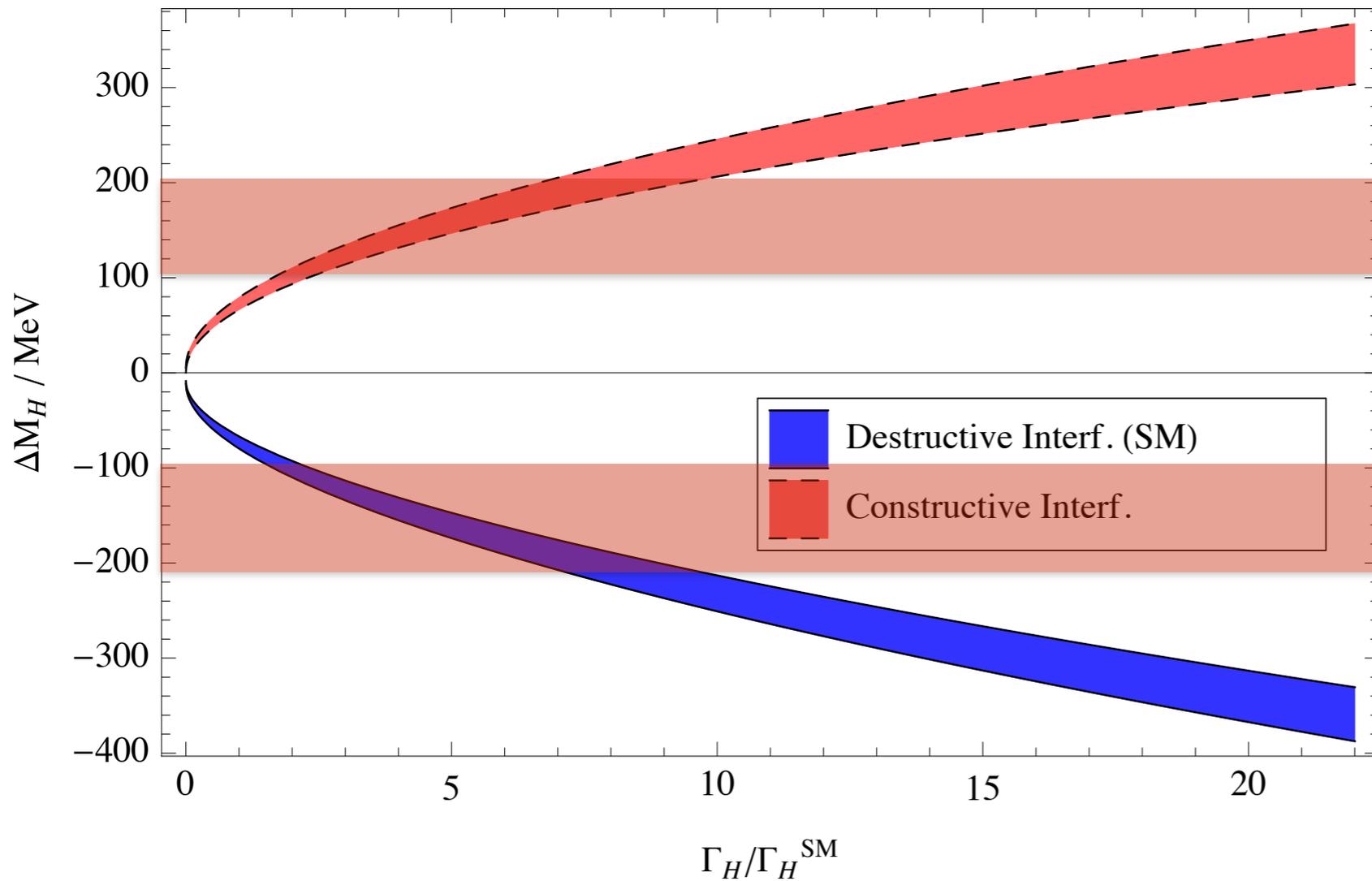
$$\sigma_{gg \rightarrow H \rightarrow \gamma\gamma} \sim \frac{g_{Hgg}^2 g_{H\gamma\gamma}^2}{\Gamma_H}$$

$$\sigma_{gg \rightarrow H \rightarrow \gamma\gamma}^{int} \sim g_{Hgg} g_{H\gamma\gamma}$$

Observable effect from the interference: $\Delta M_{ZZ,\gamma\gamma}$

[Martin (2012)]

Measurement of $\Delta M_{ZZ,\gamma\gamma}$: model-independent determination of Γ_H

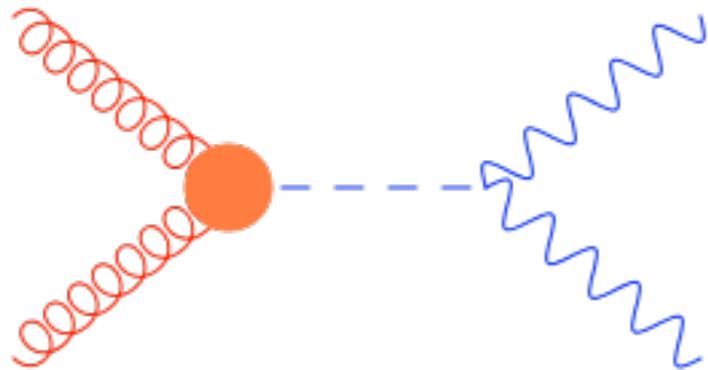


LHC estimated reach

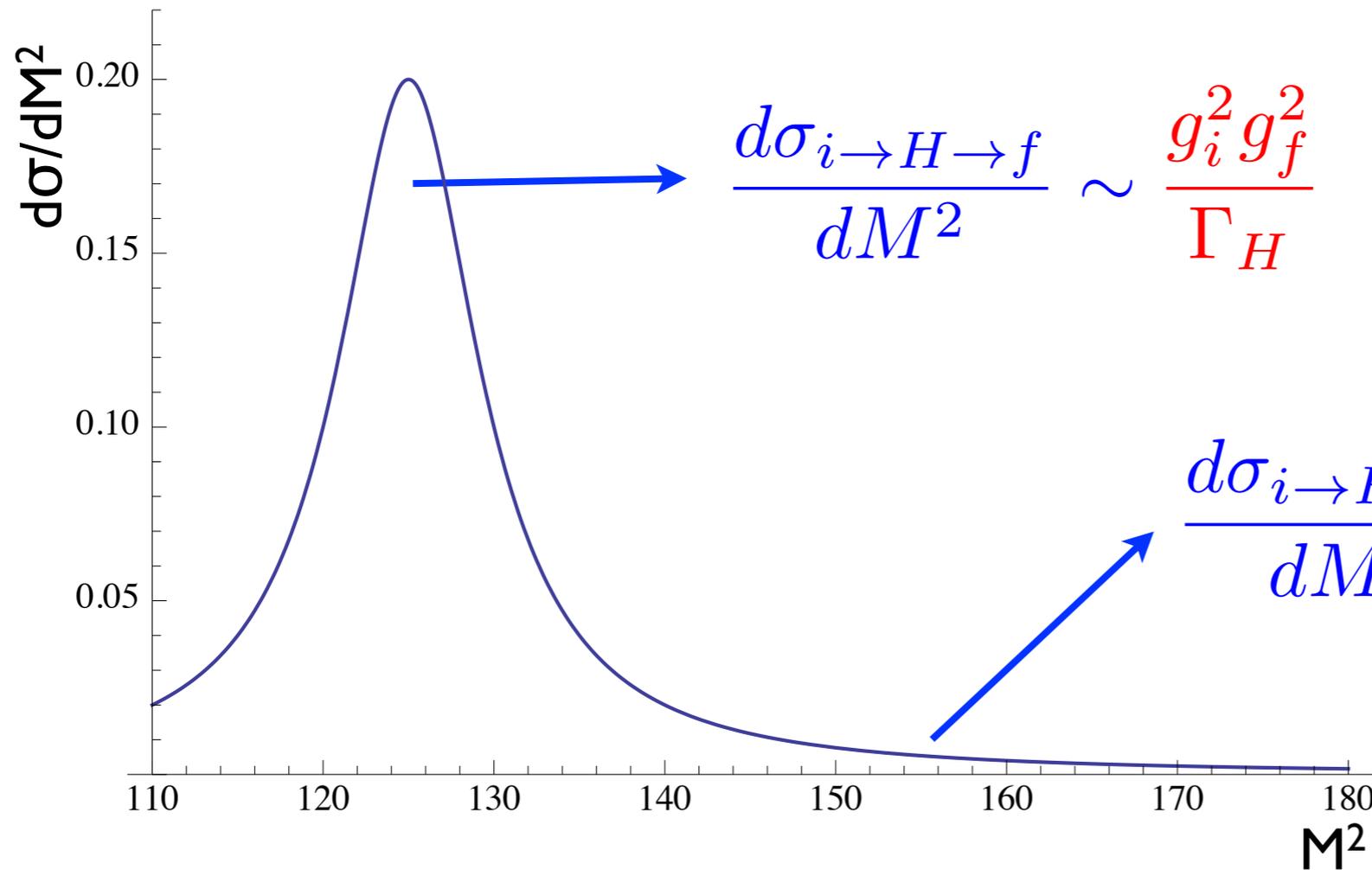
PROMISING, UNDER EXPERIMENTAL STUDY
Similar effects can be used to determine J^{+-} properties
[Dixon, talk at Radcor 2013]

Second example: use the cross-section itself

[FC, Melnikov (2013)]



$$\frac{d\sigma_{i \rightarrow H \rightarrow f}}{dM^2} \sim \frac{g_i^2 g_f^2}{(M^2 - m_H^2)^2 + m_H^2 \Gamma_H^2}$$



$$\frac{d\sigma_{i \rightarrow H \rightarrow f}}{dM^2} \sim \frac{g_i^2 g_f^2}{\Gamma_H}$$

$$\frac{d\sigma_{i \rightarrow H \rightarrow f}}{dM^2} \sim \frac{g_i^2 g_f^2}{(M^2 - m_H^2)^2}$$

OFF THE MASS SHELL, σ DOES NOT DEPEND ON Γ_H

LHC results: on the Higgs peak, the number of events is compatible with the SM expectation

$$\frac{g_i^2 g_f^2}{\Gamma_H} = \frac{g_{i,\text{SM}}^2 g_{f,\text{SM}}^2}{\Gamma_{H,\text{SM}}} \longrightarrow g = \xi g_{\text{SM}}, \Gamma_H = \xi^4 \Gamma_{H,\text{SM}}$$

Look for off-peak events: $\sigma_{off} \sim g_i^2 g_f^2$

$$N_{obs}^{off} \propto g_i^2 g_f^2 = \xi^4 g_{i,\text{SM}}^2 g_{f,\text{SM}}^2 \propto \xi^4 N_{\text{SM}}^{off} = \frac{\Gamma_H}{\Gamma_{H,\text{SM}}} N_{\text{SM}}^{off}$$

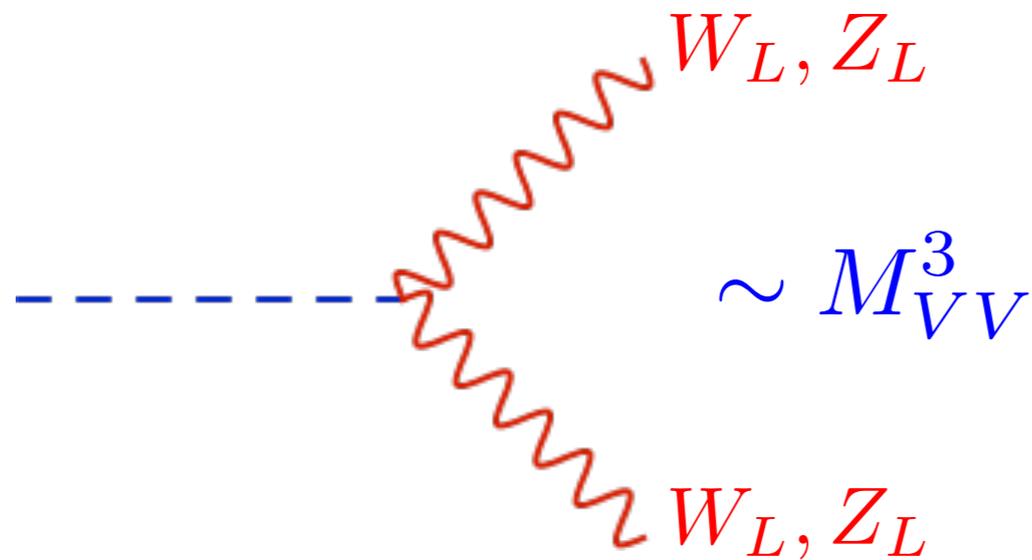
DIRECT ACCESS TO THE WIDTH

$$\Gamma_H = \frac{N_{obs}^{off}}{N_{\text{SM}}^{off}} \Gamma_{H,\text{SM}}$$

The role of vector bosons: enhanced off-shell tail of the cross section

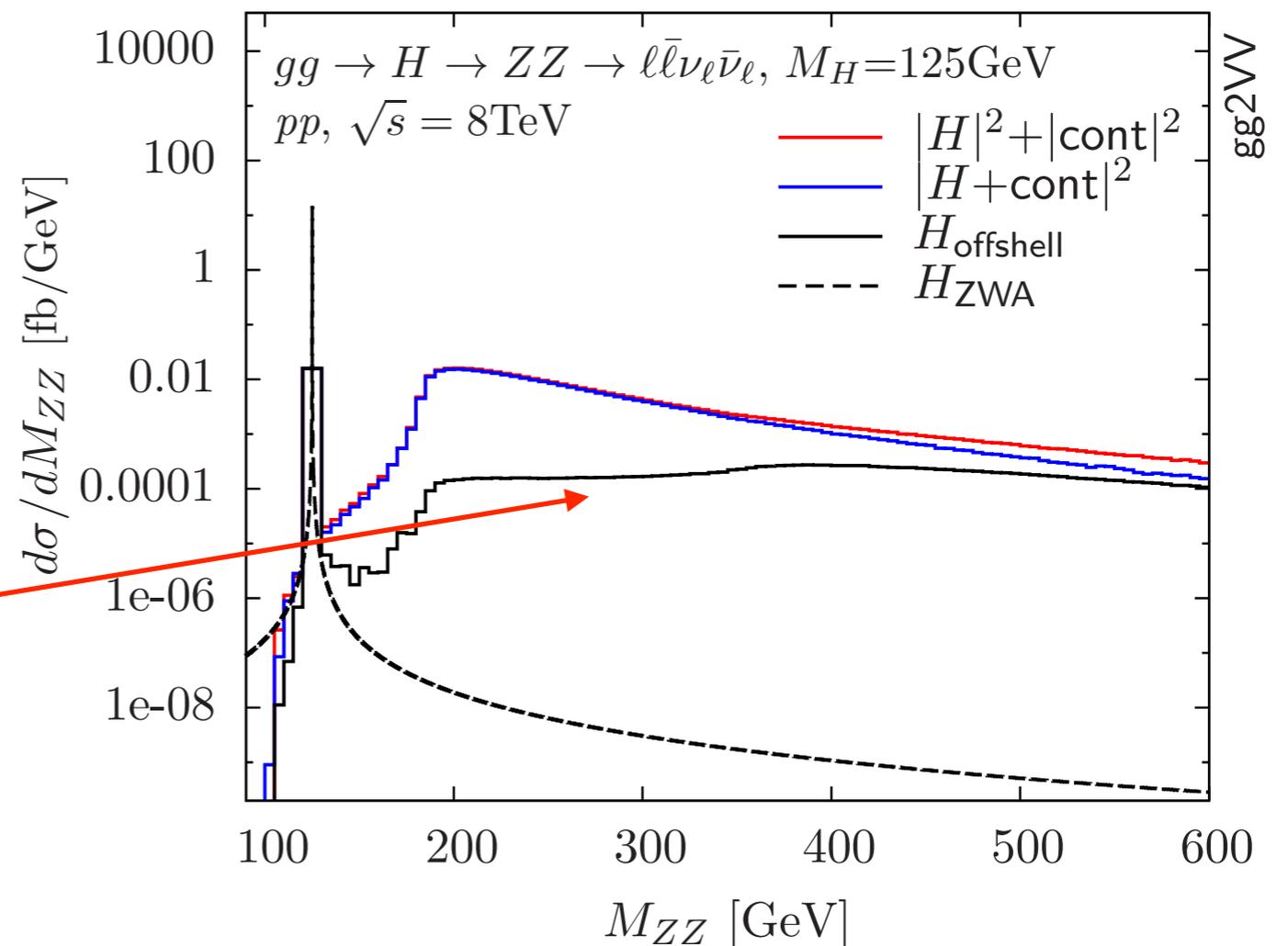
[Kauer, Passarino (2012)]

Above the VV threshold:
enhanced decay into
longitudinal gauge bosons

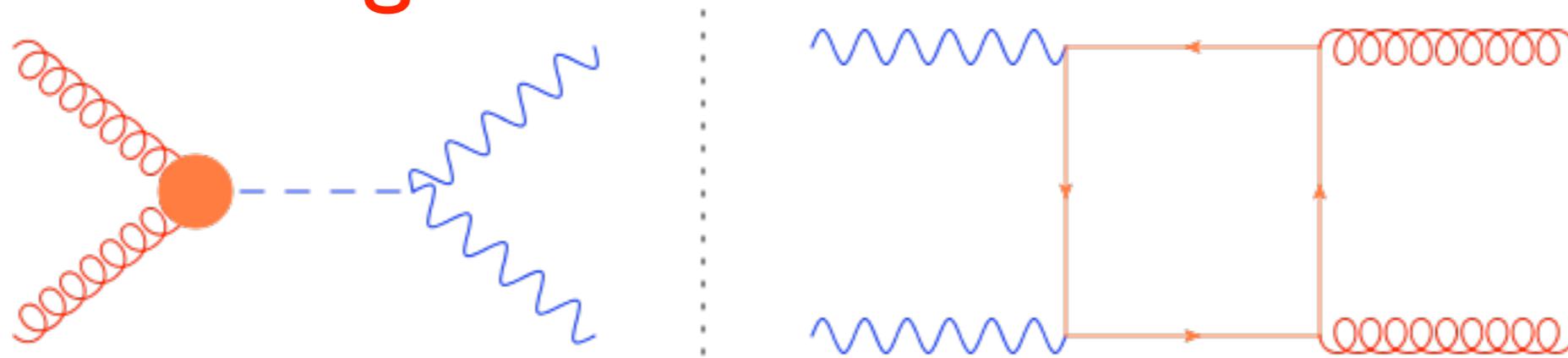


Large plateau,
eventually washed away
by parton luminosities

Large $O(10\%)$ effect



The role of vector bosons: large interference effects



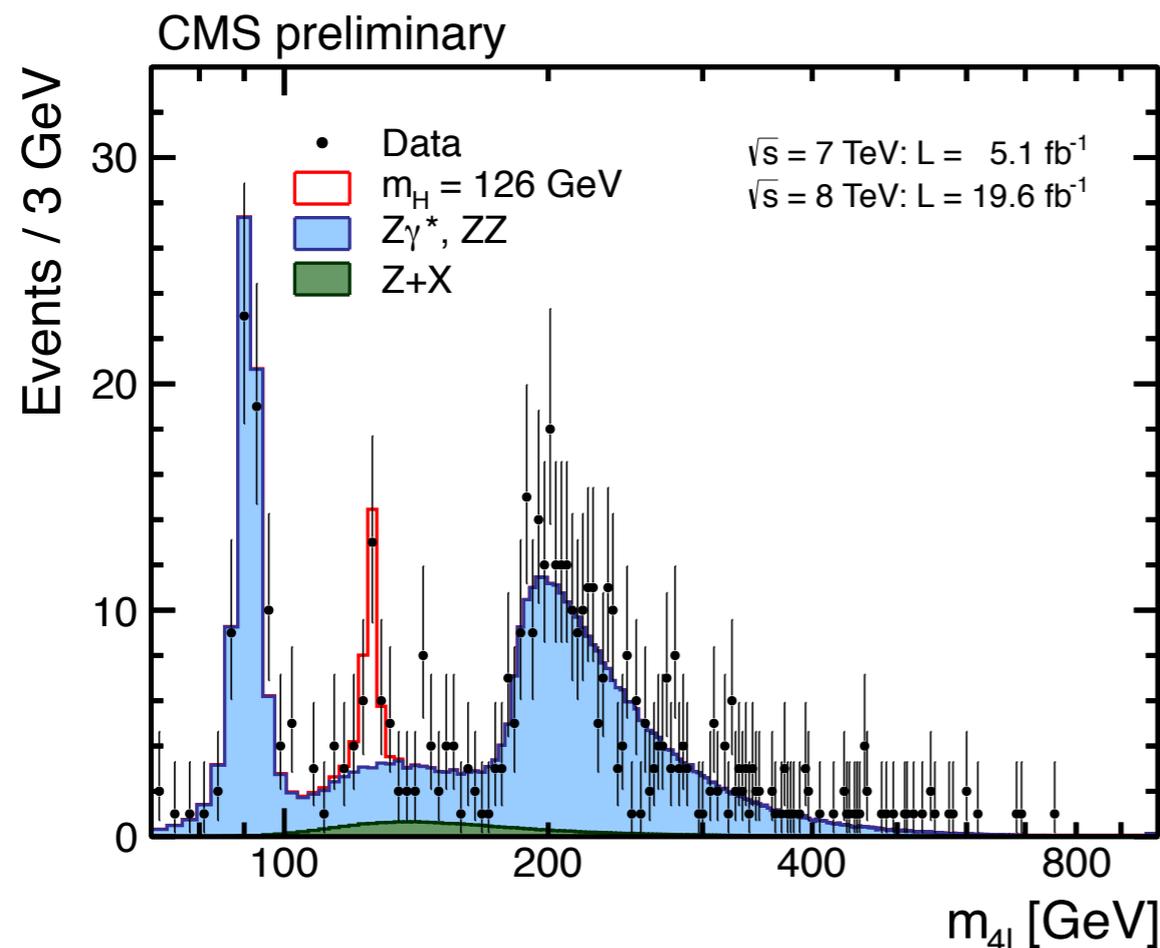
In the SM: $\sigma^{int} \sim -50\%$ off peak [Kauer, Passarino (2012)]

$$\sigma^{int} \sim g_{Hgg}g_{HV V} = [e^{i\theta}] \sqrt{\frac{\Gamma_H}{\Gamma_{H,SM}}} \sigma_{SM}^{int}$$

PUTTING EVERYTHING TOGETHER:

$$N^{off} = \frac{\Gamma_H}{\Gamma_{H,SM}} N_{SM}^{off} - [e^{i\theta}] \sqrt{\frac{\Gamma_H}{\Gamma_{H,SM}}} N_{SM}^{int}$$

Phenomenological results: Γ_H from $H \rightarrow ZZ$ decays



Very crude analysis,
current CMS dataset:

$$\Gamma_H \leq 21 \Gamma_{H,sm}$$

$$\Gamma_H \leq 88 \text{ MeV}$$

[FC, Melnikov (2013)]

More refined analysis, matrix element method:

$$\Gamma_H \leq (15.7_{-2.9}^{+3.9}) \cdot \Gamma_{H,sm} \text{ at } 95\% \text{ CL}$$

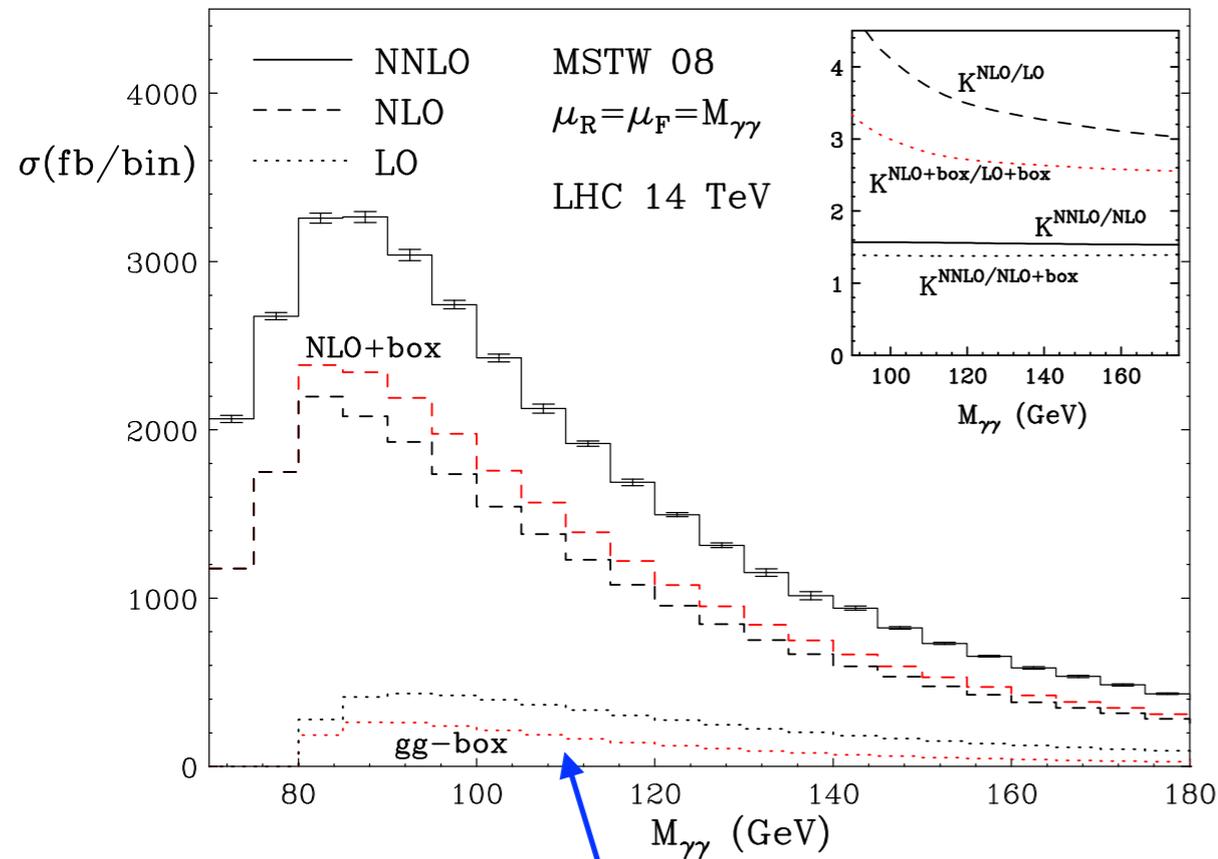
[Campbell, Ellis, Williams arXiv:1311.3589]

Estimated reach of this method at the LHC:

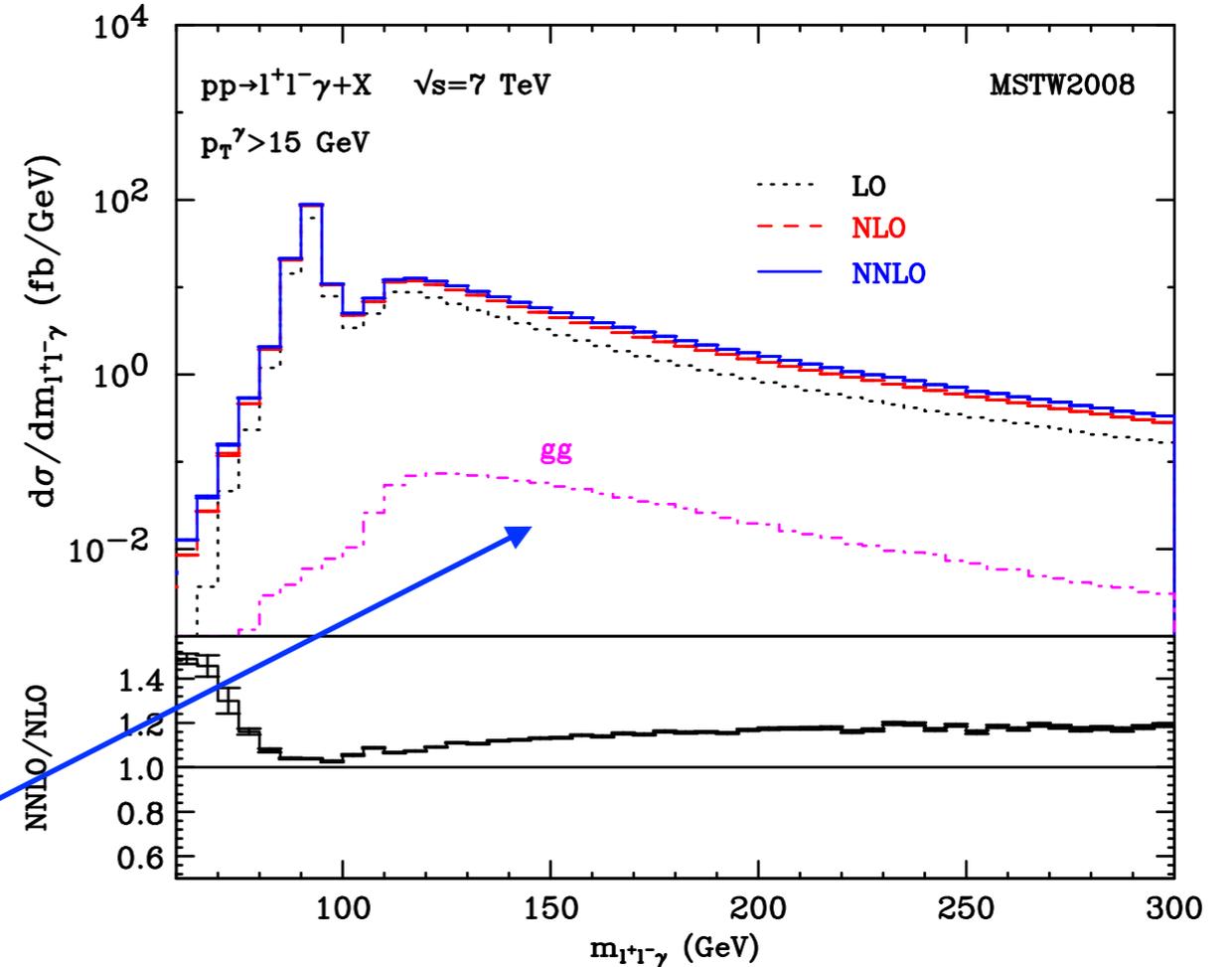
$$\Gamma_H \leq 5 - 10 \text{ MeV}$$

WW production and
Higgs searches:
where do we stand

qq->γγ, qq->Zγ is known @ NNLO



[Catani et al (2011)]

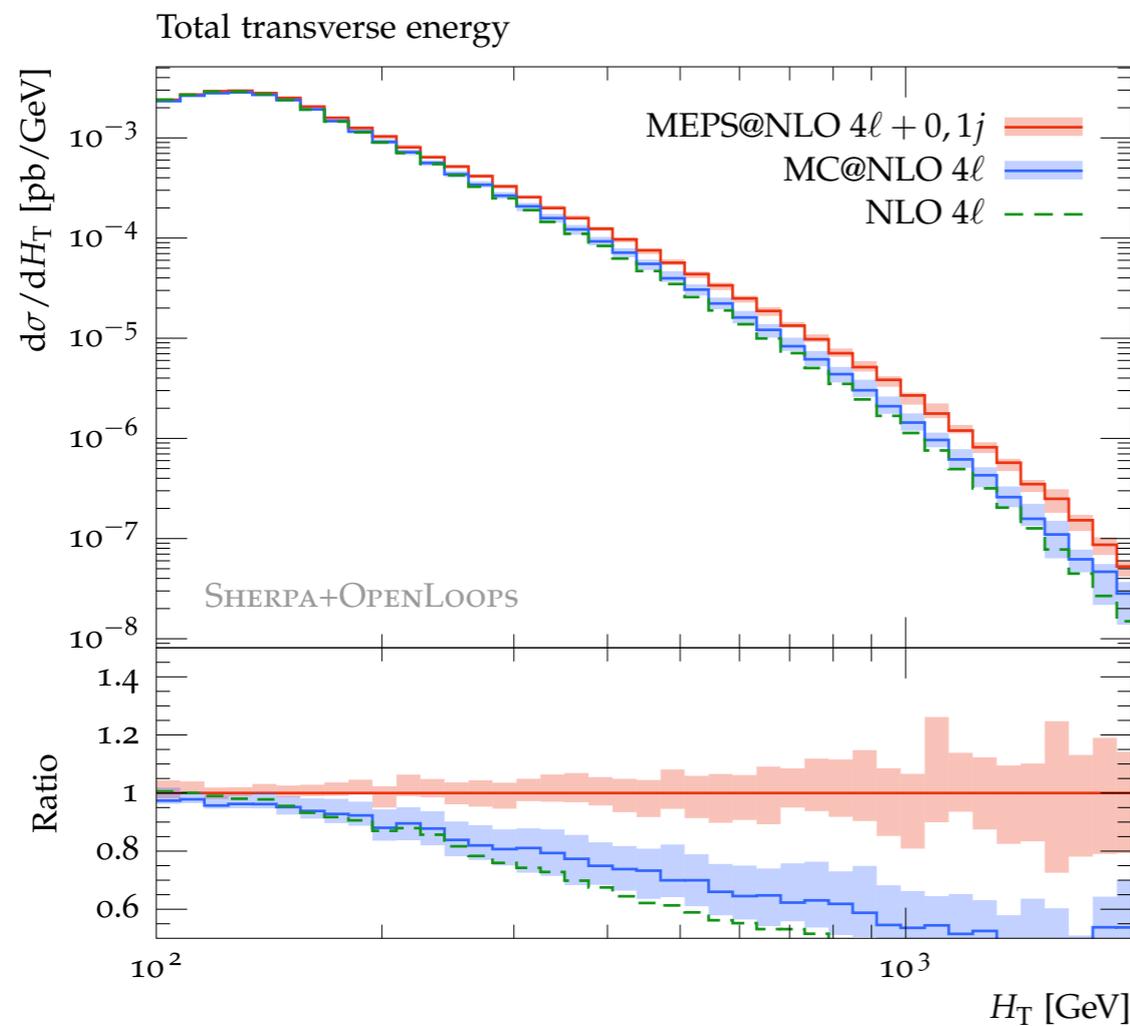


[Grazzini et al (2013)]

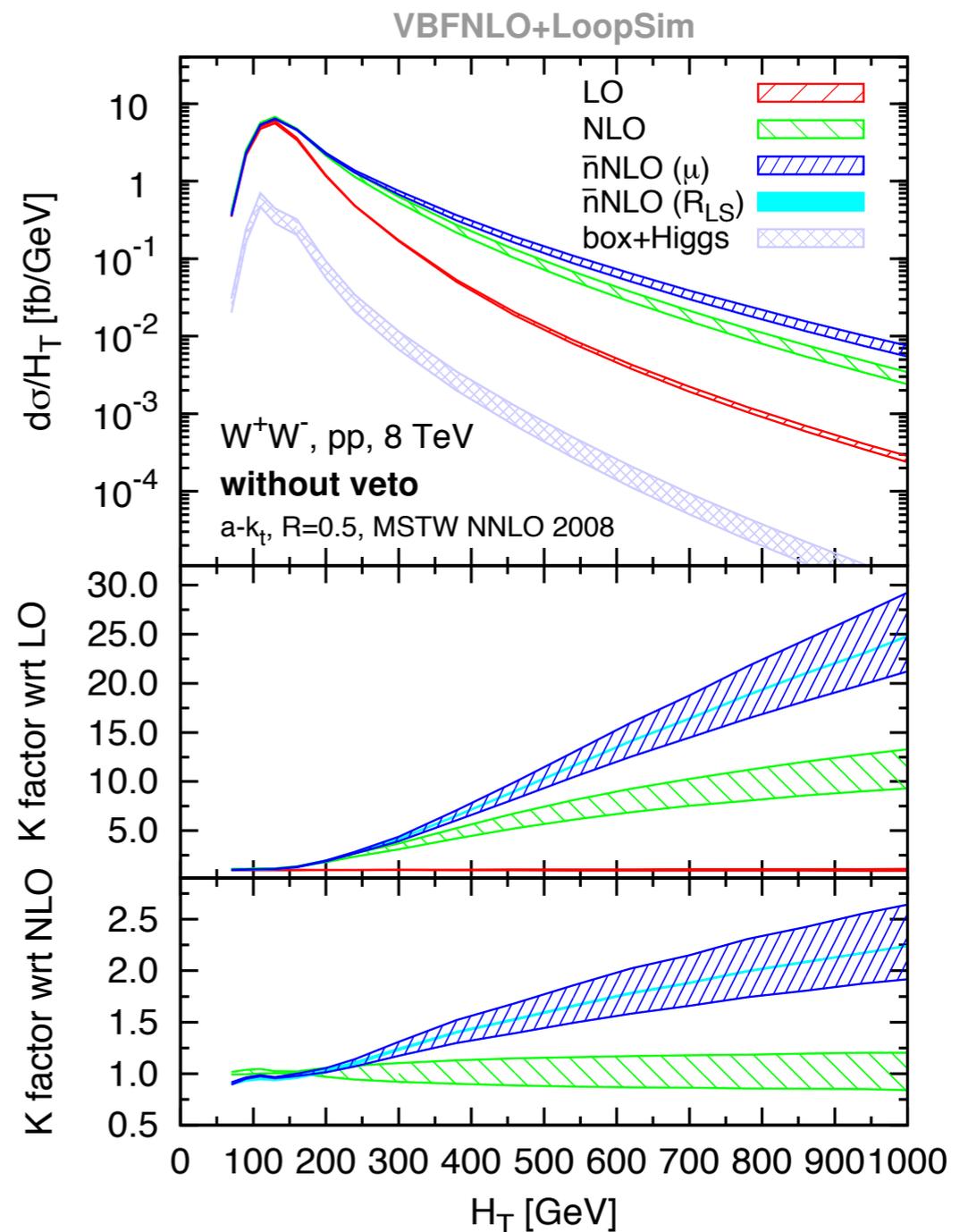
- contains **LO** $gg \rightarrow \gamma\gamma/Z\gamma$
- expect NNLO $qq \rightarrow W\gamma$ soon?

A lot of recent developments for $qq \rightarrow VV$

Matching/merging: sizable part of NNLO corrections



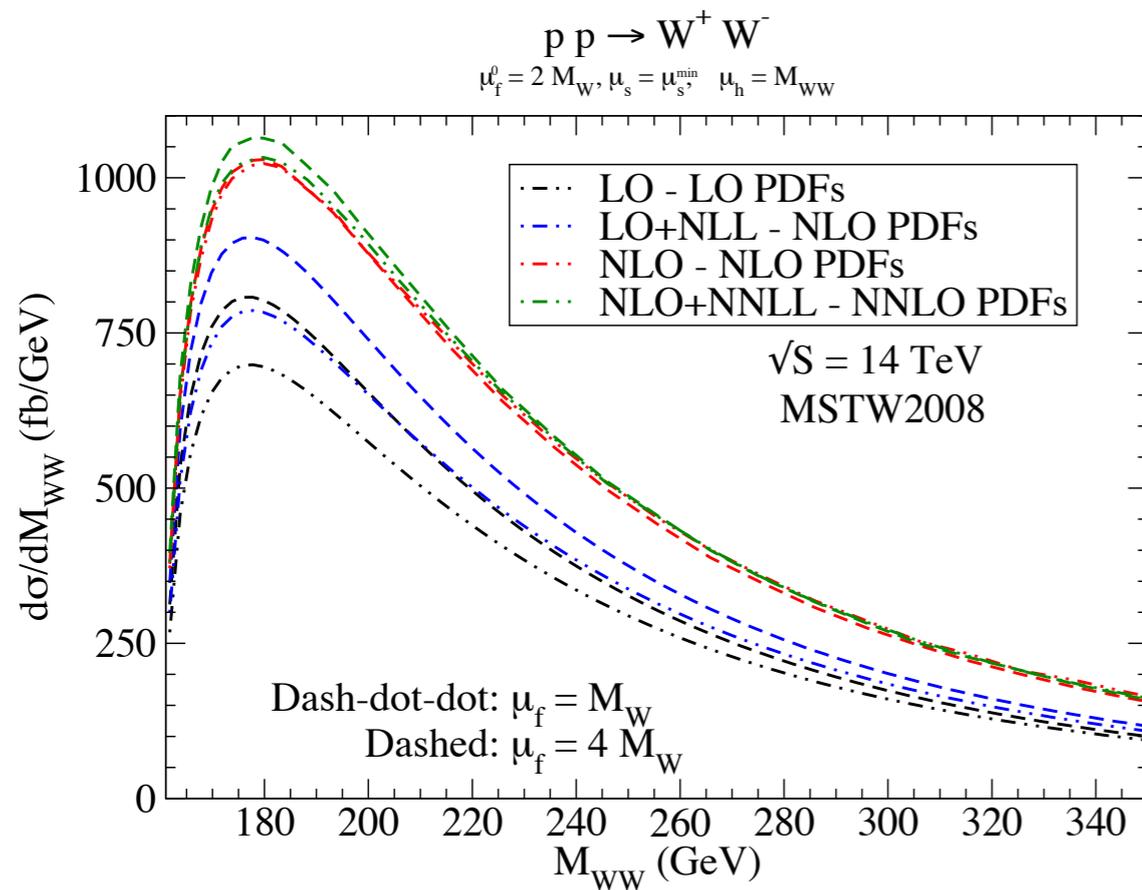
[Cascioli et al (2013), SHERPA+OPENLOOPS]



[Campanario et al (2013), LOOPSIM+VBF@NLO]

Approximate NNLO from resummation

[S. Dawson et al (2013)]



$\sigma(\text{pb})$	$\sqrt{S} = 7 \text{ TeV}$	$\sqrt{S} = 8 \text{ TeV}$	$\sqrt{S} = 13 \text{ TeV}$	$\sqrt{S} = 14 \text{ TeV}$
σ^{NLO}	$45.7^{+1.5}_{-1.1}$	$55.7^{+1.7}_{-1.2}$	$110.6^{+2.5}_{-1.6}$	$122.2^{+2.5}_{-1.8}$
σ^{gg}	$1.0^{+0.3}_{-0.2}$	$1.3^{+0.4}_{-0.3}$	$3.5^{+0.9}_{-0.7}$	$4.1^{+0.9}_{-0.7}$
$\sigma^{NLO+NNLL}$	$44.9^{+0.6}_{-0.6}$	$54.8^{+0.7}_{-0.8}$	$108.2^{+1.3}_{-1.5}$	$119.5^{+1.5}_{-1.6}$
$\sigma^{NLO+NNLL}$	$45.9^{+0.5}_{-0.6}$	$56.1^{+0.7}_{-0.8}$	$111.7^{+1.8}_{-1.6}$	$123.6^{+2.0}_{-1.8}$
σ_{approx}^{NNLO}	$45.0^{+0.4}_{-0.1}$	$54.9^{+0.5}_{-0.05}$	$108.3^{+1.0}_{-0.4}$	$119.6^{+1.2}_{-0.5}$
σ_{approx}^{NNLO}	$46.0^{+0.4}_{-0.047}$	$56.2^{+0.6}_{-0.1}$	$111.8^{+1.7}_{-1.1}$	$123.7^{+1.8}_{-1.2}$

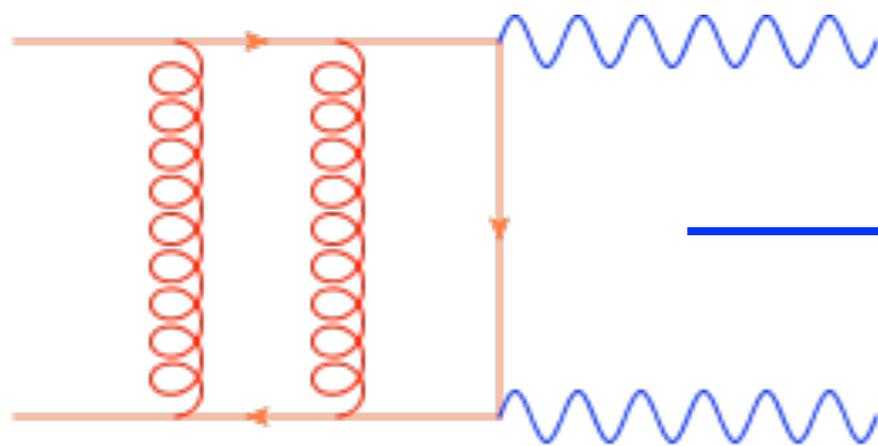
- approximate NNLO: few percent effect
- beyond NNLO, tiny resummation effect (\sim Higgs N^3LO)

Towards the **exact NNLO** for $qq \rightarrow VV$

All $qq \rightarrow VV$ loop amplitudes known numerically

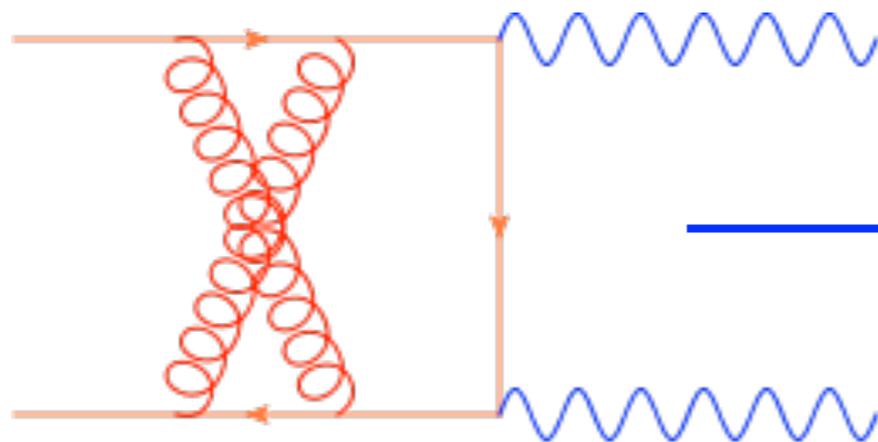
[Chachamis, talk at EPS-HEP 2013]

Analytical results:



VV : [Gehrmann et al (2013)]

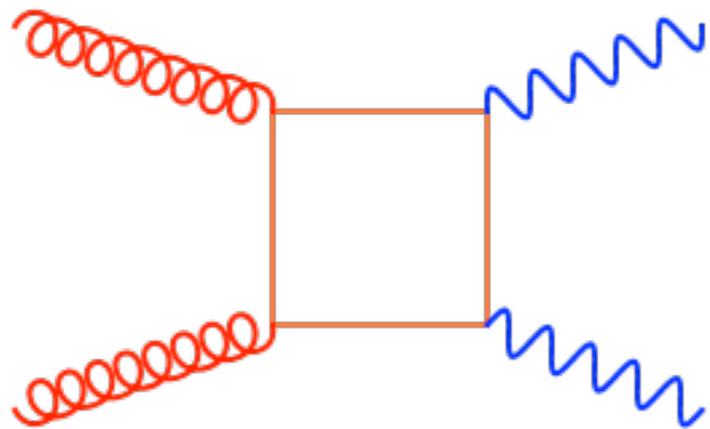
VV^* : [Henn, Smirnov, to appear]



more complicated

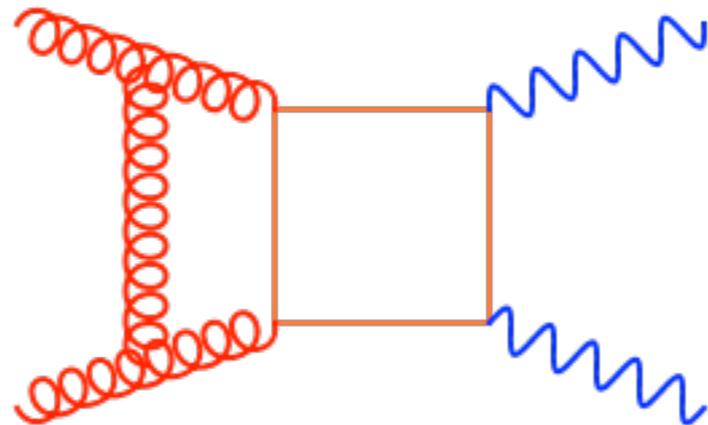
REASONABLE TO EXPECT RESULTS IN THE NOT TOO FAR FUTURE

$gg \rightarrow VV$: worse situation



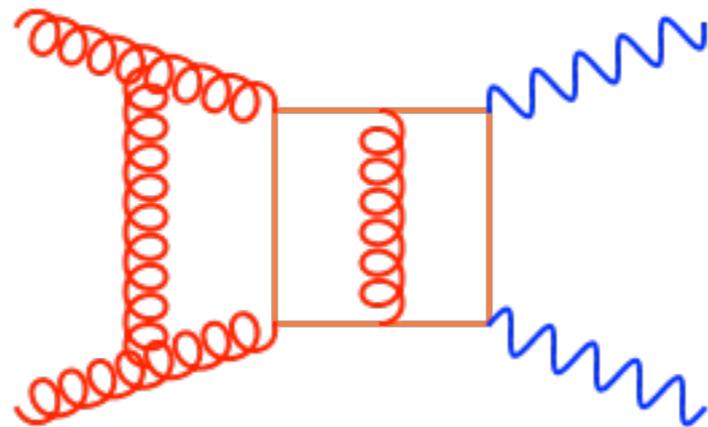
LO: Known

[Glover, van der Bij (1989); Binoth et al (2006,2008); Campbell et al (2011)...]



NLO: Unknown

Apart from $\gamma\gamma$ [Bern et al (2002)]



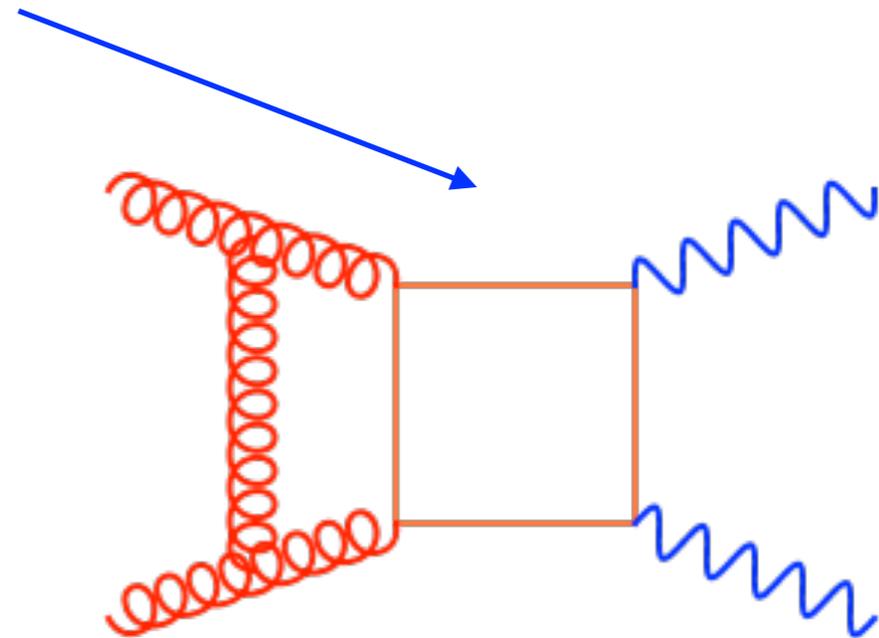
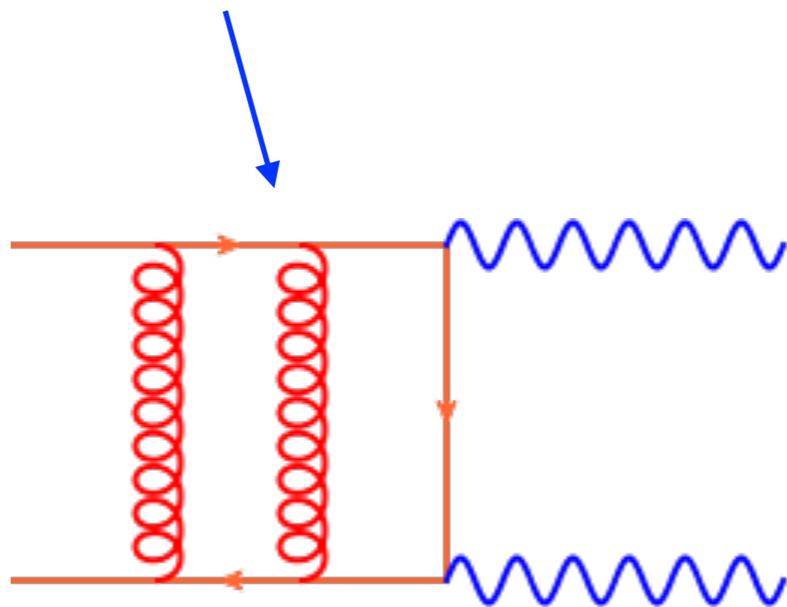
NNLO: Unknown

GLUON-INDUCED PROCESS -> EXPECT LARGE CORRECTIONS

$gg \rightarrow VV$: can we compute at least NLO?

Low invariant mass: neglect the top-loop contribution

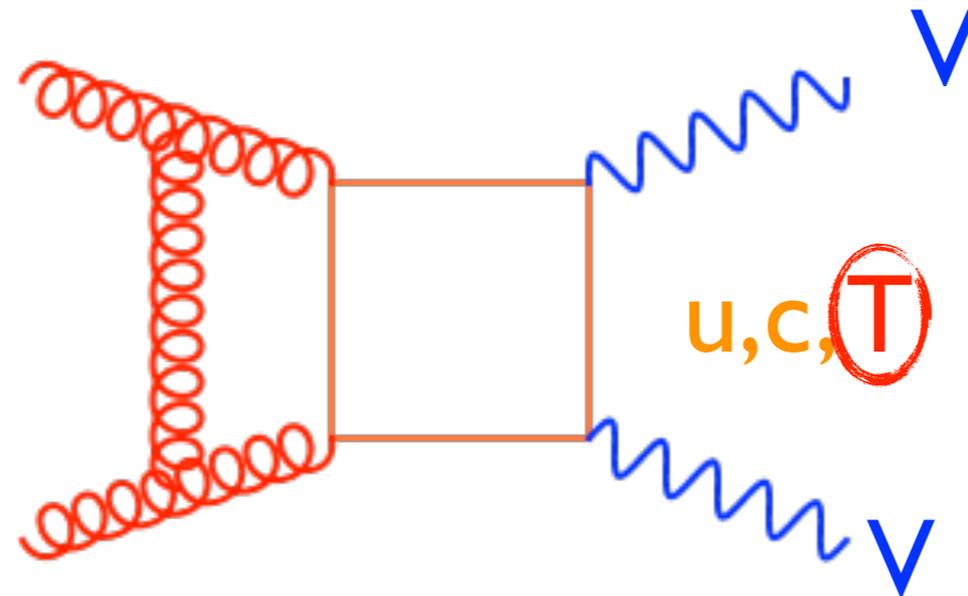
$qq \rightarrow VV$ @ NNLO and $gg \rightarrow VV$ @ NLO same complexity



Profit from acquired knowledge for $qq \rightarrow VV$ @ NNLO

AFTER $QQ \rightarrow VV$ @ NNLO, NEXT NATURAL STEP

At high invariant mass, VV strongly couple to the
THIRD GENERATION



Multi-scale problem
internal masses



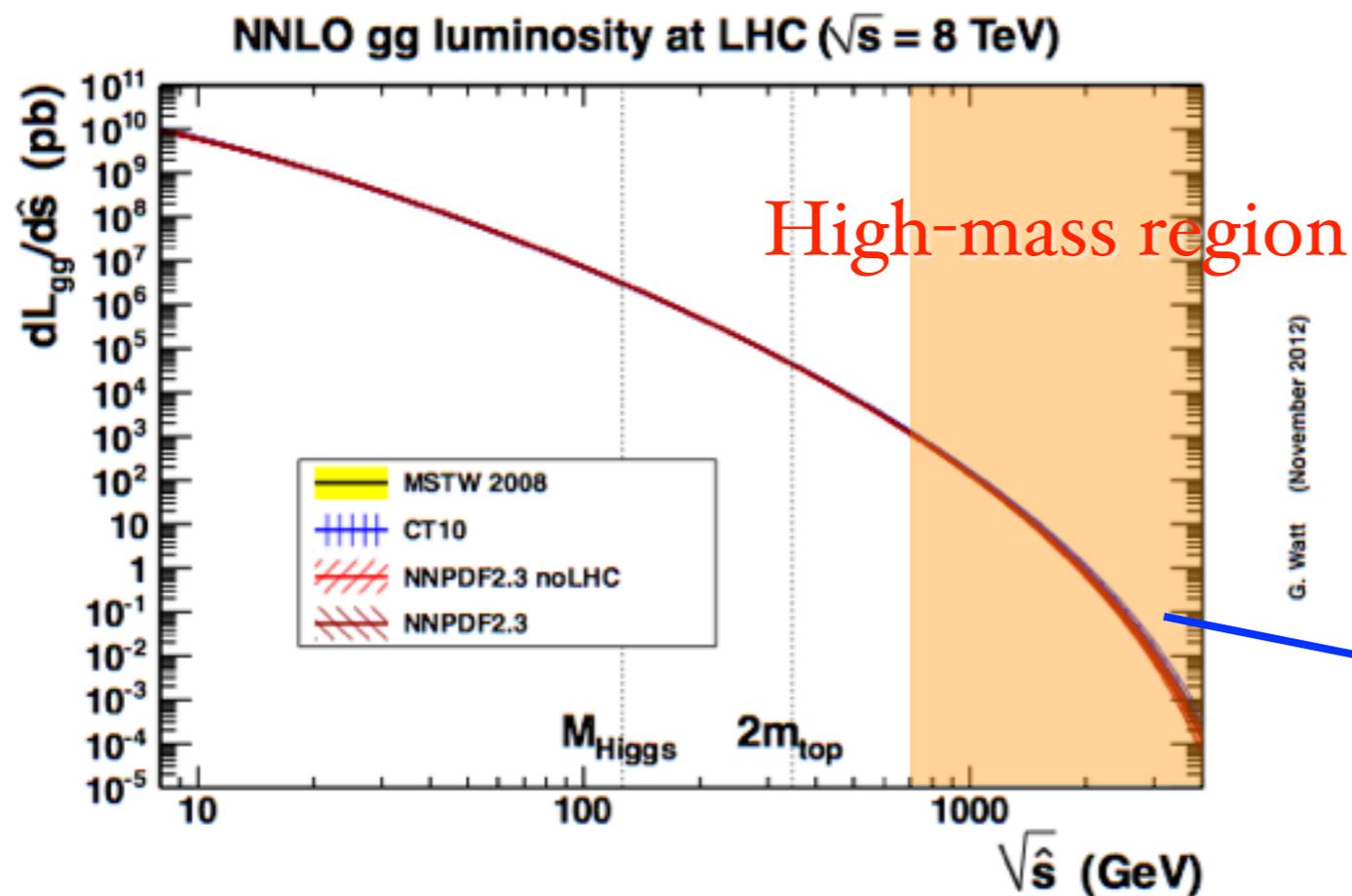
**(WELL) BEYOND OUR CURRENT
COMPUTATIONAL TECHNOLOGY**

Yet **important**:

- off-shell tail -> indirect measurement of the Higgs width
- large p_T tails (coupling extraction, channel separation...)
- irreducible background for SM-like heavy Higgs
- high mass Higgs exclusion limits

(N)NLO in the soft approximation

We are interested in the production of a **high invariant-mass system** in the gluon-gluon channel



$$\sigma = \int_{\tau}^1 \frac{dz}{z} \mathcal{L}\left(\frac{\tau}{z}\right) \hat{\sigma}(z)$$

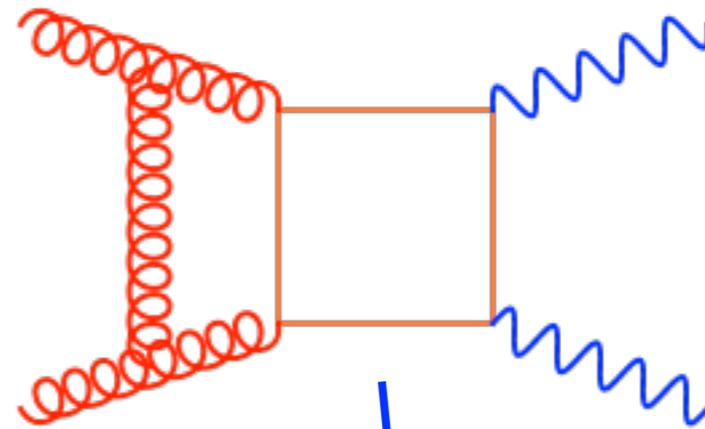
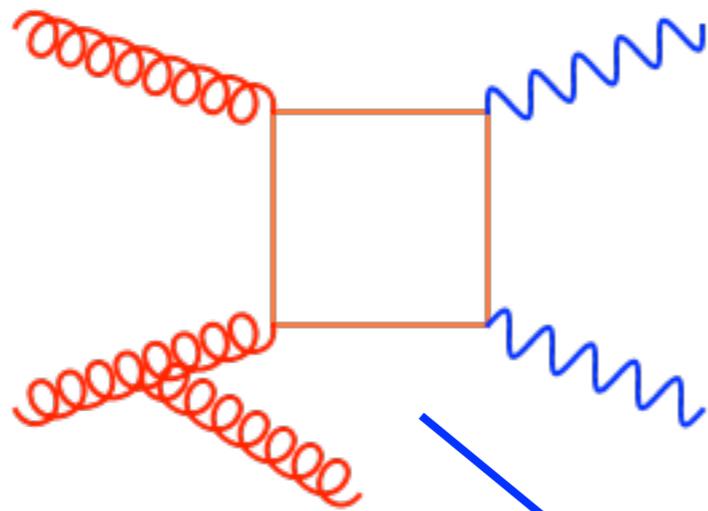
$$\tau = M^2/s$$

Rapidly falling
gluon PDF

The cross section is dominated by the **soft $z \sim 1$ region**

(N)NLO in the soft approximation

Enhanced terms: **emission of soft gluons**



$$\hat{\sigma} = \sigma_0 + \sigma_0 \frac{\alpha_s}{2\pi} \left(8C_A \left[\frac{\ln(1-z)}{1-z} \right]_+ + c_1 \delta(1-z) + \text{reg} \right) + \text{h.o.}$$

Process-dependent

Usually neglected in the soft approximation

Bulk of the result, **universal**

A soft-approximation for $gg \rightarrow VV$ @ (N)NLO

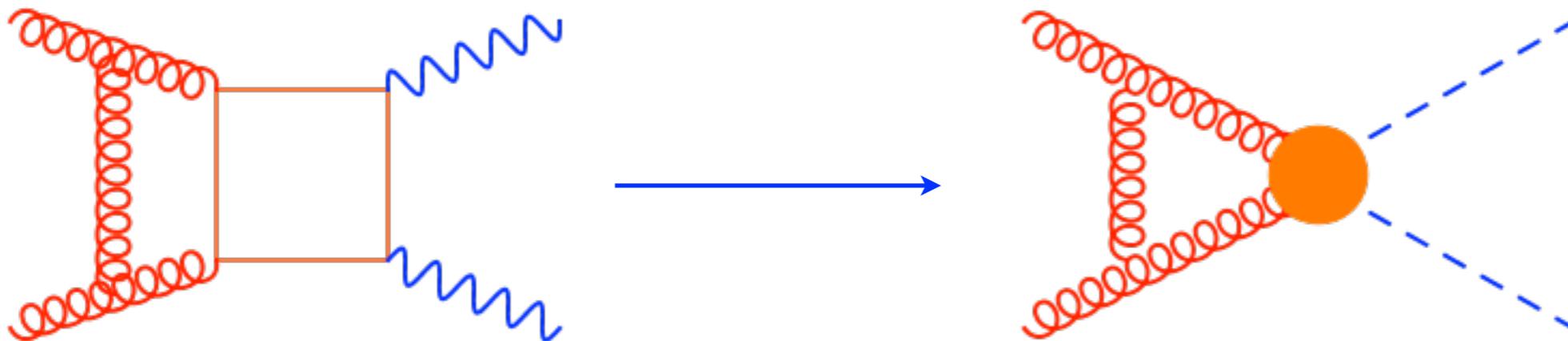
[Bonvini, FC et al (2013)]

Improvements w.r.t traditional soft approximation:

- correct kinematics information [R.D. Ball, Bonvini et al (2013)]
- correct leading collinear behavior [Catani et al (2013)]

$$\left[\frac{\ln^k 1-z}{1-z} \right]_+ \rightarrow A_{gg}(z) \left\{ \left[\frac{\ln^k 1-z}{1-z} \right]_+ + \left(\frac{\ln^k \frac{1-z}{\sqrt{z}}}{1-z} - \frac{\ln^k 1-z}{1-z} \right) \right\}$$

- unknown loop amplitude estimated using EFT

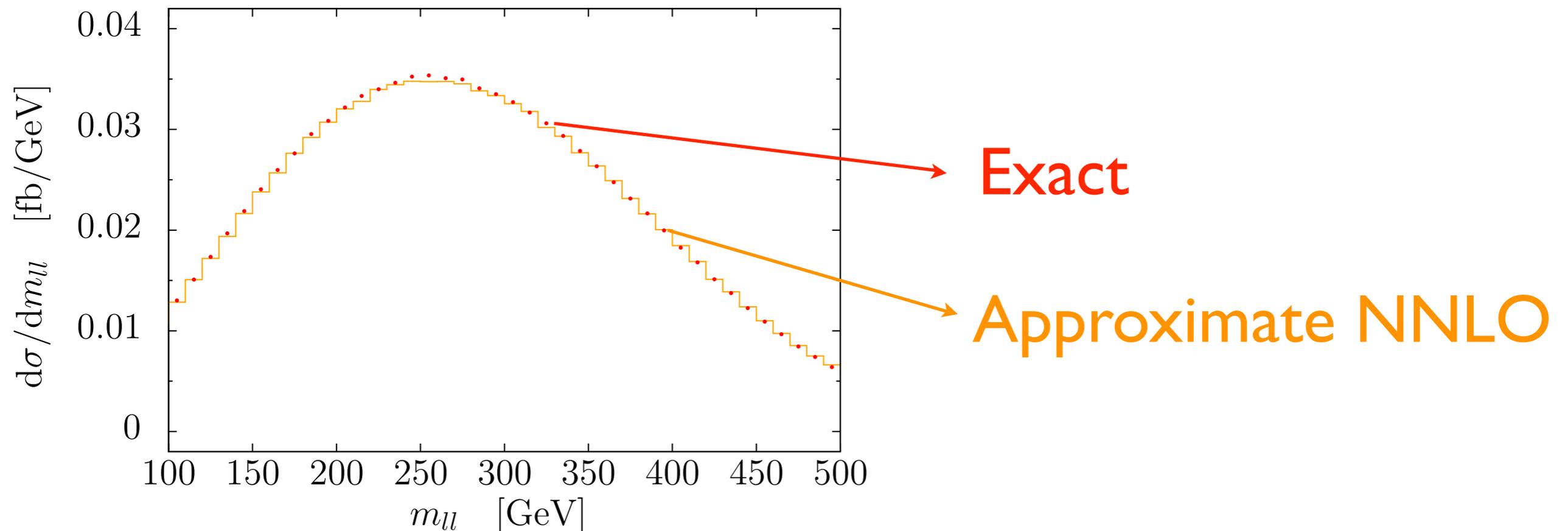


Validating the approximation: $gg \rightarrow H \rightarrow WW$

Inclusive K-factors, high-mass SM-like Higgs

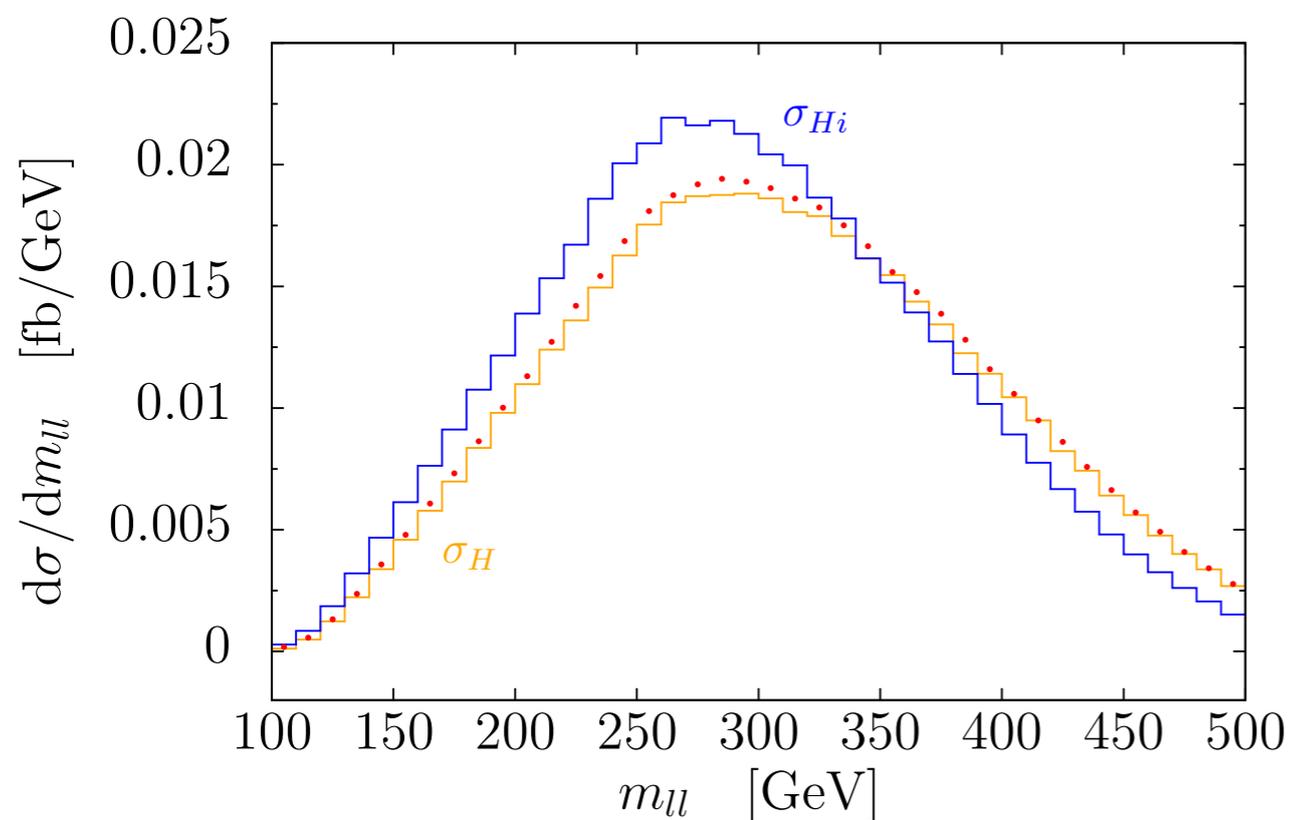
	$\sqrt{s} = 8 \text{ TeV}$		$\sqrt{s} = 13 \text{ TeV}$	
	NLO	NNLO	NLO	NNLO
exact	2.150	2.78	2.074	2.67
soft-collinear	2.19 ± 5	2.82 ± 12	2.13 ± 6	2.73 ± 12

Differential distributions



An application: signal/background interference for heavy Higgs searches

	$\sqrt{s} = 8 \text{ TeV}$			$\sqrt{s} = 13 \text{ TeV}$		
	LO	NLO	NNLO	LO	NLO	NNLO
σ_H	0.379	0.83(2)	1.07(5)	1.55	3.29(8)	4.2(2)
σ_{Hi}	0.427	0.93(3)	1.20(7)	1.66	3.5(1)	4.5(2)
$\sigma_H / \sigma_H^{\text{LO}}$	—	2.19(5)	2.8(1)	—	2.13(5)	2.7(1)
$\sigma_{Hi} / \sigma_{Hi}^{\text{LO}}$	—	2.19(7)	2.8(2)	—	2.12(6)	2.7(1)



We believe that the interference K-factor can be estimated to $\mathcal{O}(10\%)$ accuracy

Conclusions and outlook

- $gg \rightarrow VV$ processes very interesting for Higgs physics
 - as a background
 - as a tool to probe Higgs properties (model independent determination of Higgs width/couplings)
- $gg \rightarrow VV$ currently known **only at LO**
 - but soft approximation is available, reliable in the **high invariant mass region**
 - can be used for instance for high-mass Higgs searches
- **Expect improvements soon**
 - full NNLO for $qq \rightarrow VV$ to be completed soon
 - profit from the acquired knowledge and compute NLO $gg \rightarrow VV$ in the low invariant mass region

Thank you for
your attention!