

The neutron star equation of state

Chiral forces in the Green's functions formalism

Arnau Rios Huguet
STFC Advanced Fellow
Department of Physics
University of Surrey

with A. Carbone & A. Polls

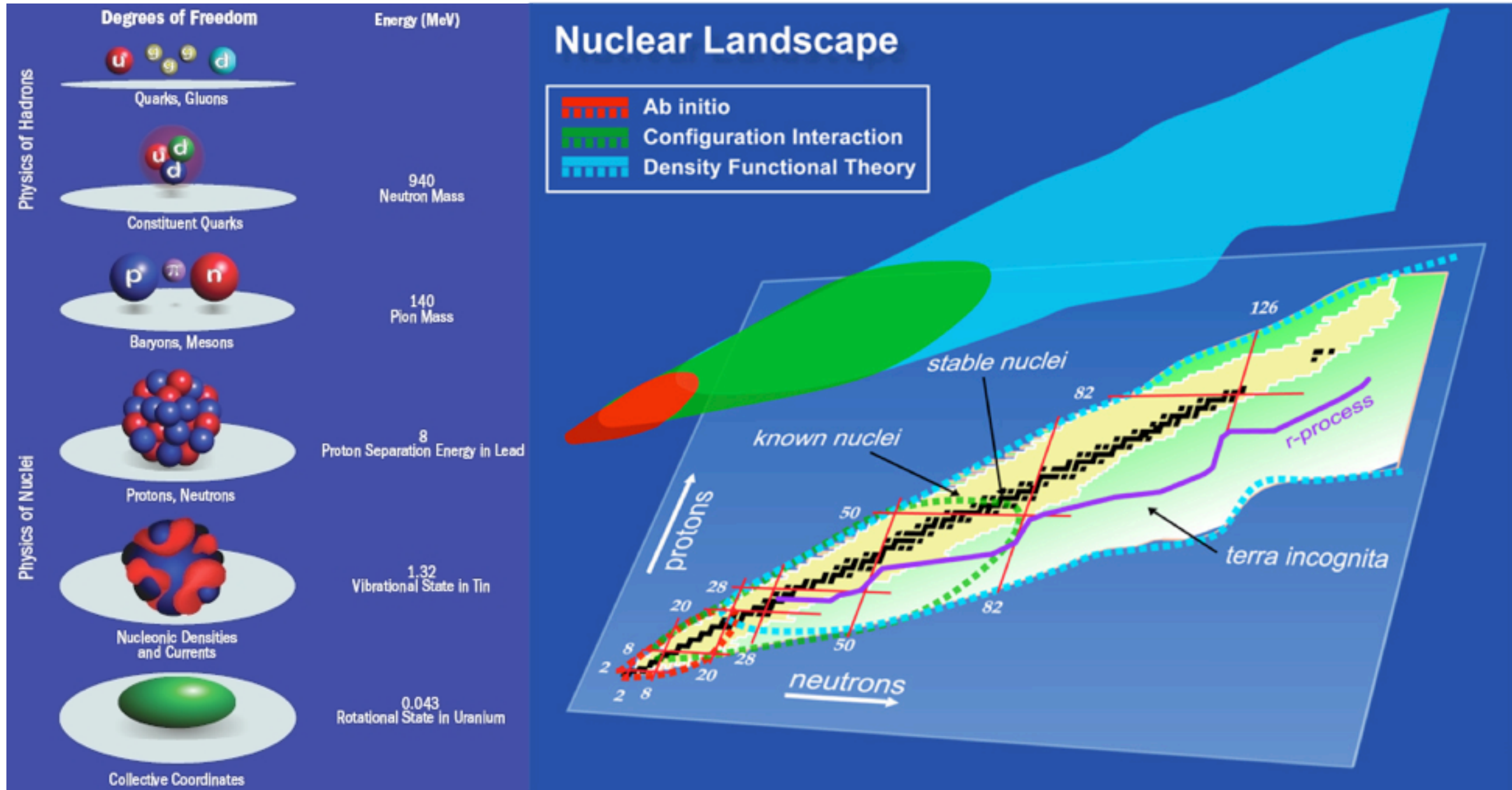


UNIVERSITAT DE BARCELONA



Compstar Conference, Florence, 25 March 2014

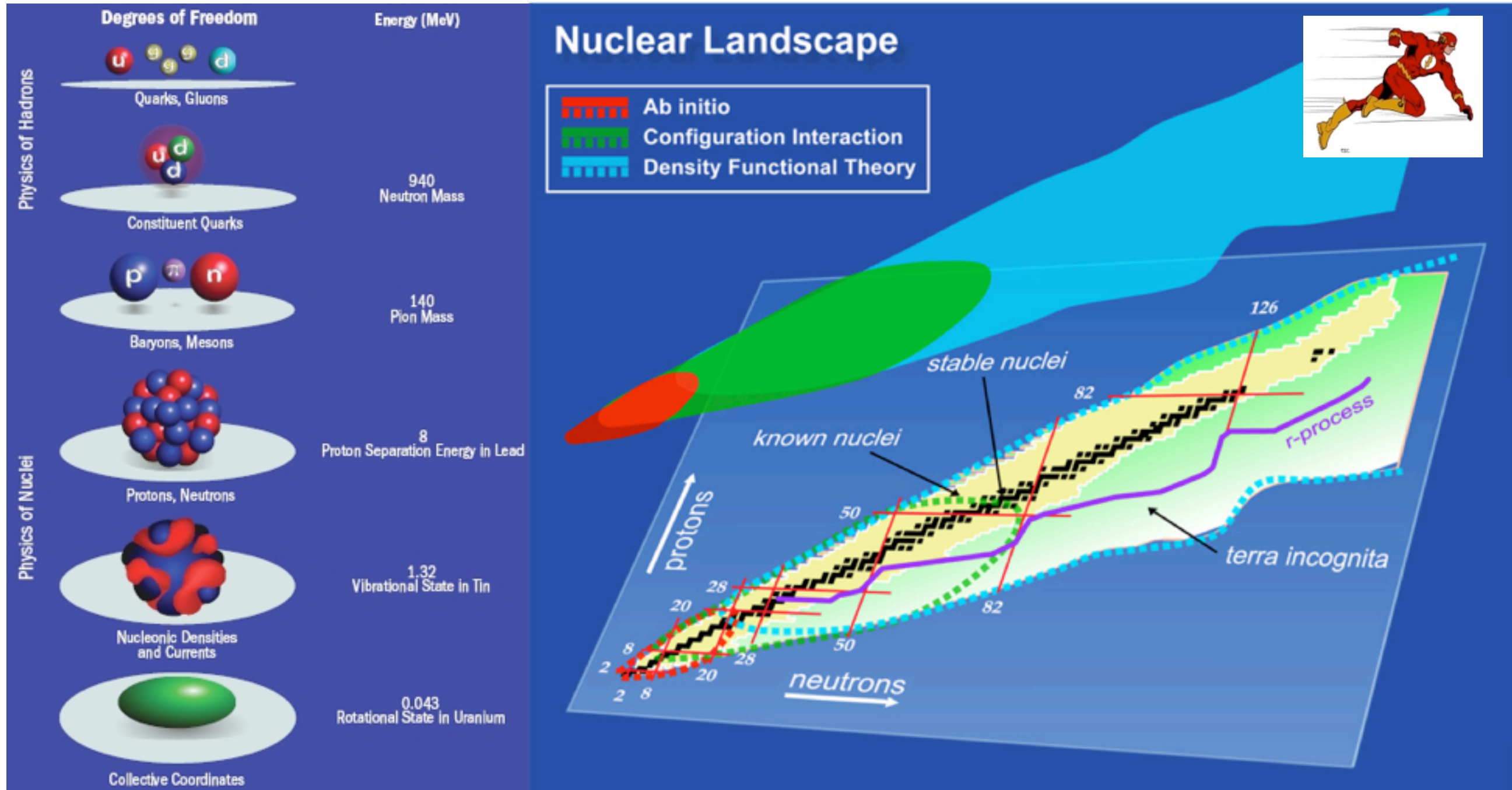
Theoretical nuclear physics



DOE/NSF Nuclear Science Advisory Committee, The Frontiers of Nuclear Science: A Long-Range Plan, 2007.

Two philosophies

Theoretical nuclear physics

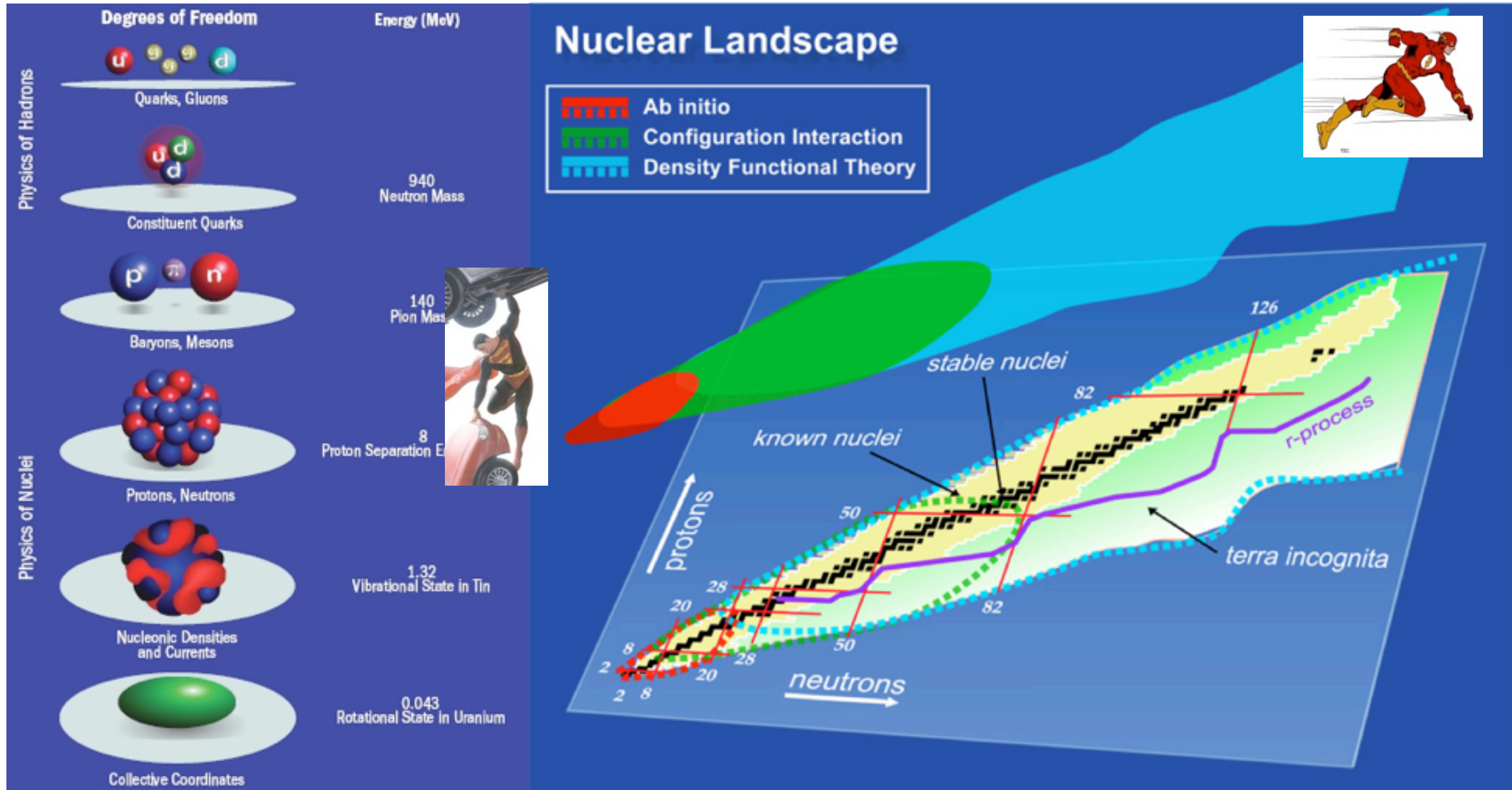


DOE/NSF Nuclear Science Advisory Committee, The Frontiers of Nuclear Science: A Long-Range Plan, 2007.

Two philosophies

- **Phenomenological:** nuclear properties from energy density functional.

Theoretical nuclear physics



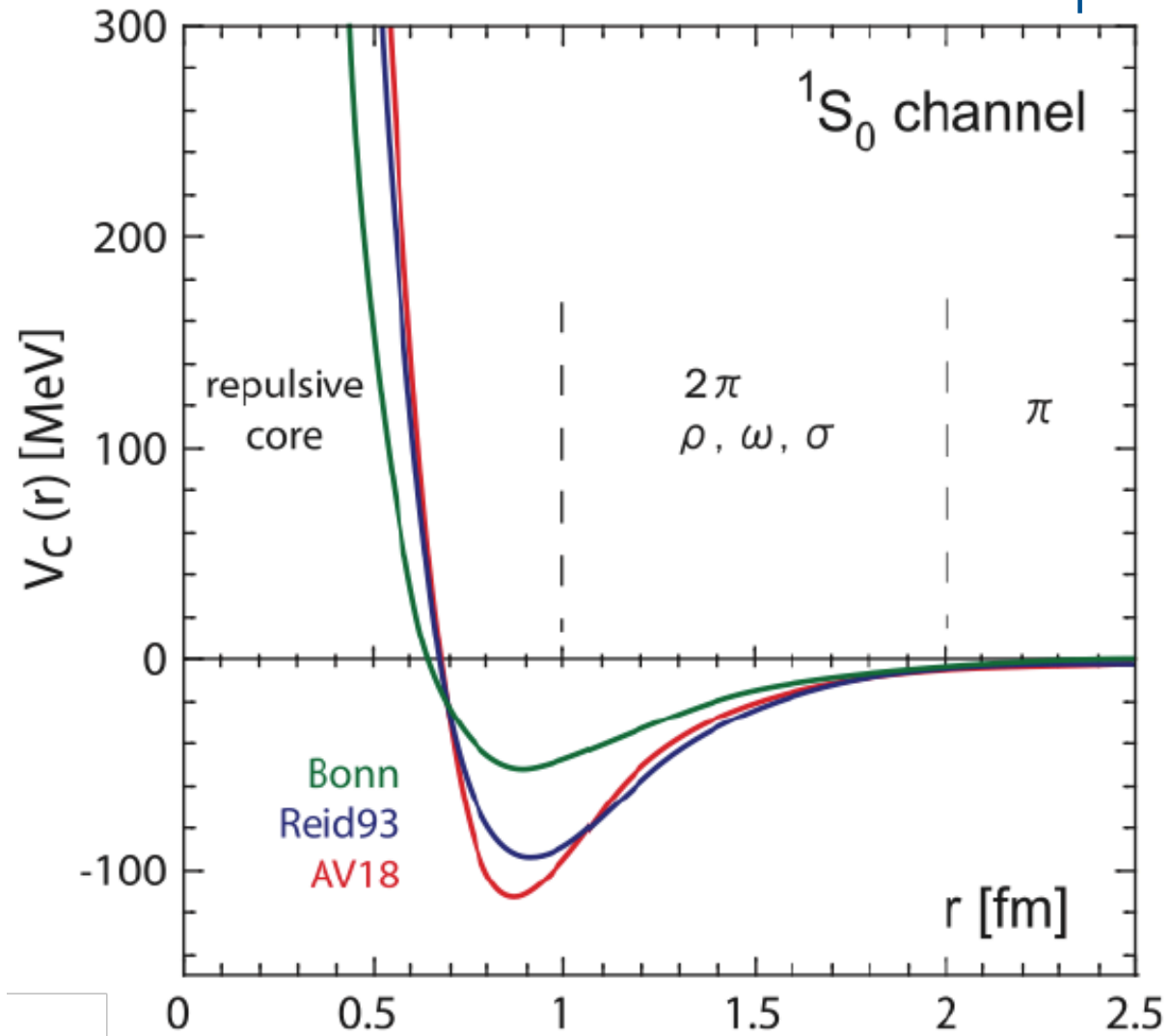
DOE/NSF Nuclear Science Advisory Committee, The Frontiers of Nuclear Science: A Long-Range Plan, 2007.

Two philosophies

- **Phenomenological:** nuclear properties from energy density functional.
- **Ab initio:** from QCD nucleon-nucleon force to nuclei?

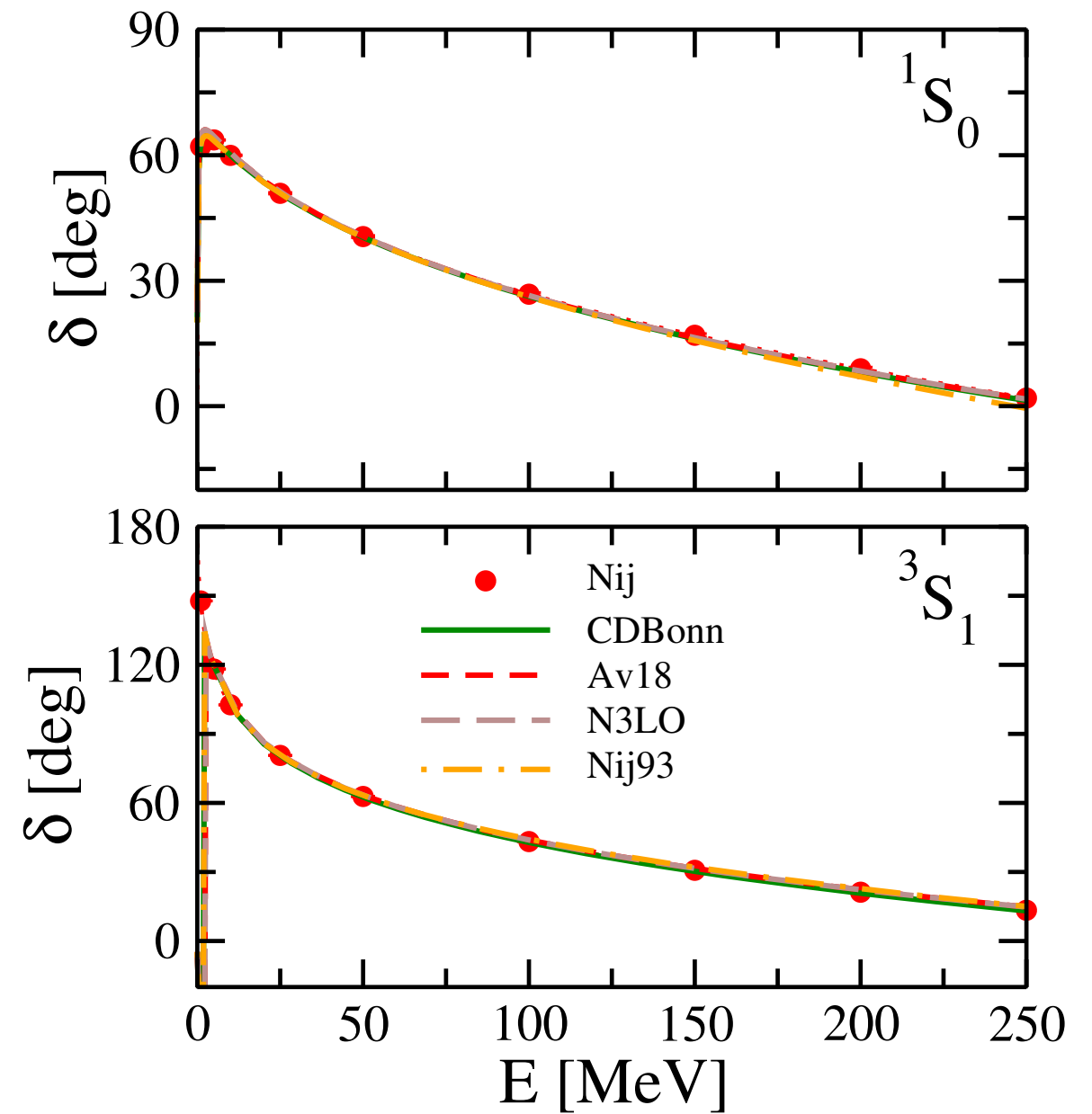
Complications

NN interaction is not unique



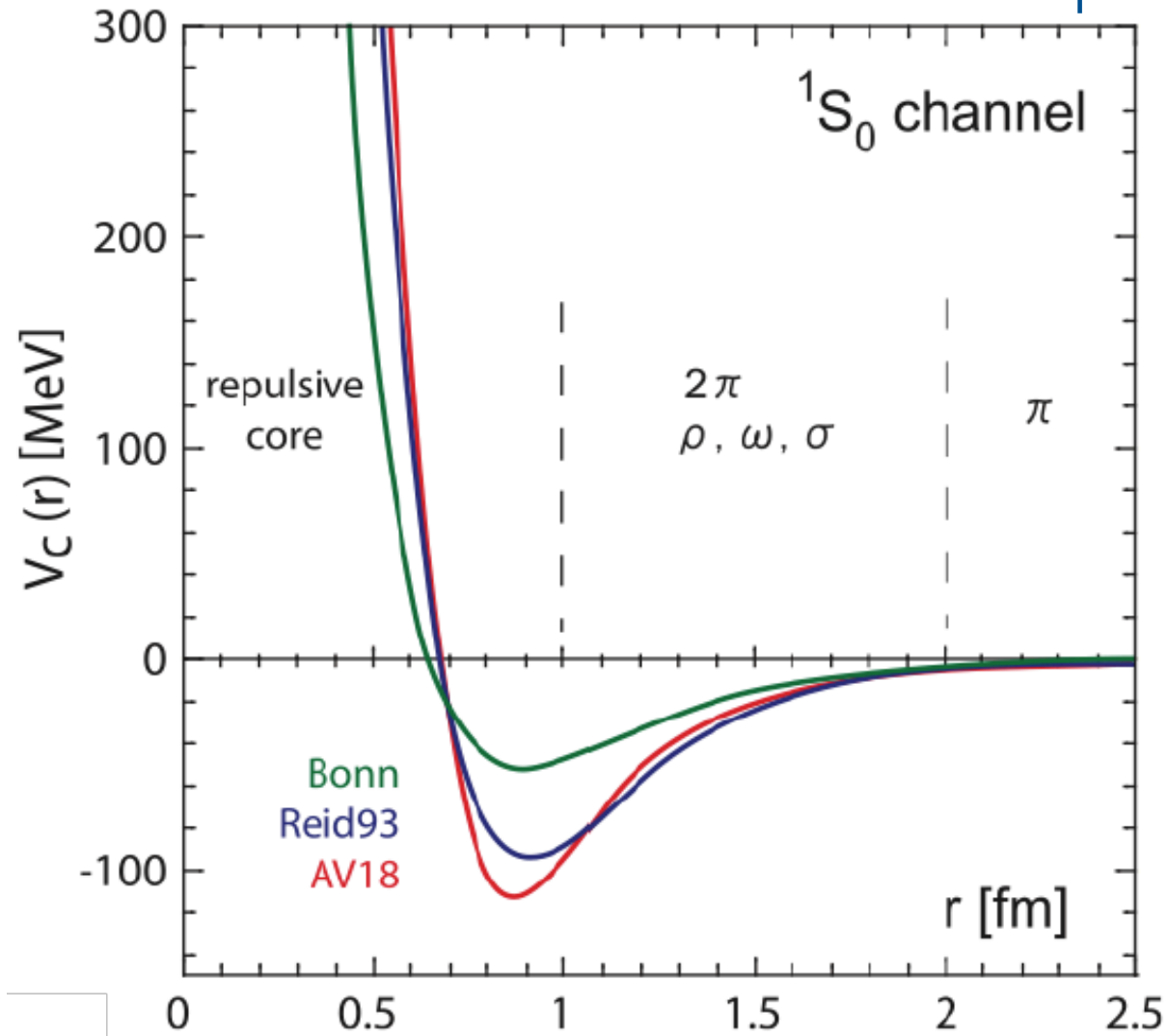
S.Aoki, et al. *Comput. Sci. Dis.* | 015009 (2008)

...but phase-shift equivalent!



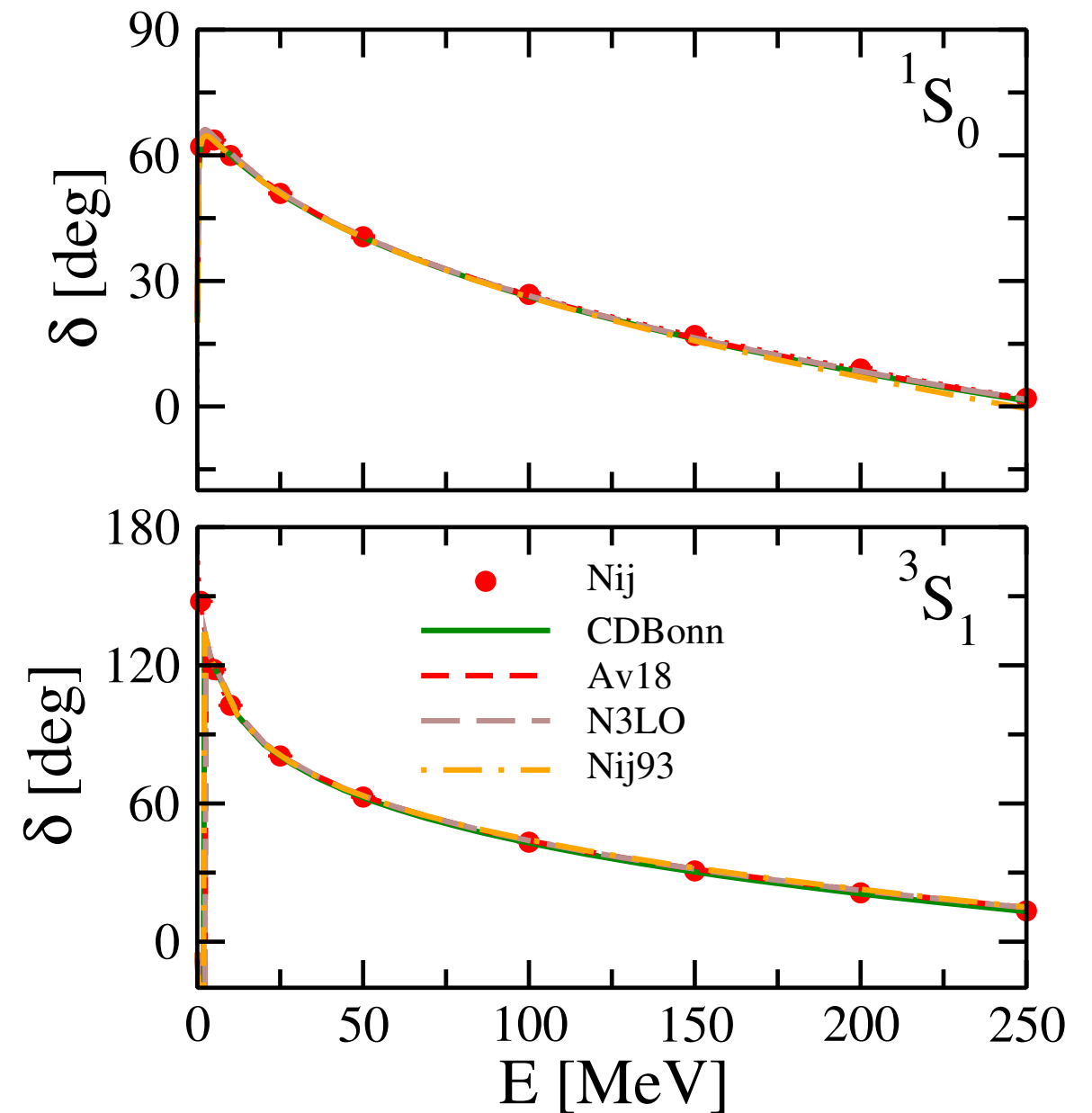
Complications

NN interaction is not unique



S.Aoki, et al. *Comput. Sci. Dis.* | 015009 (2008)

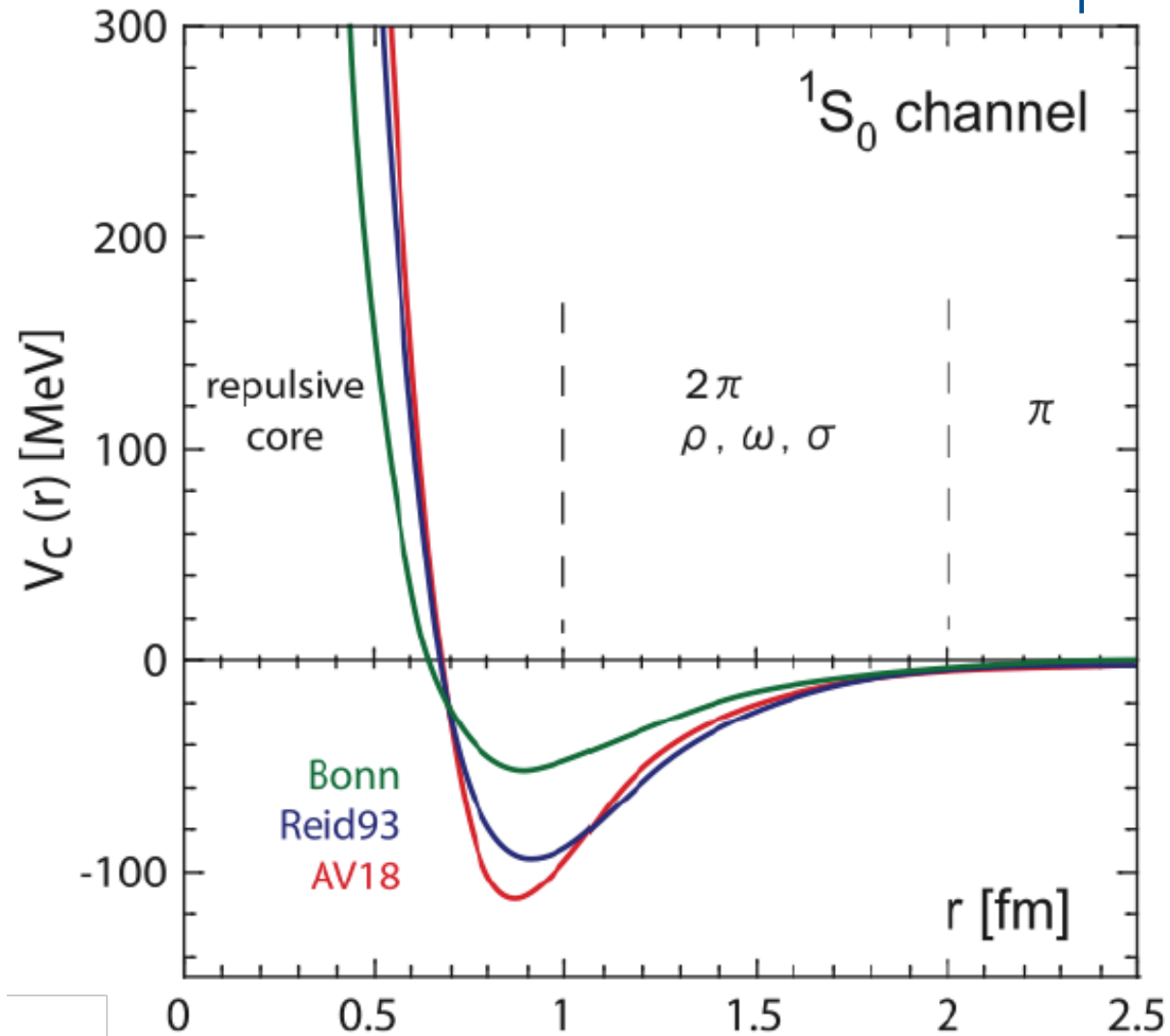
...but phase-shift equivalent!



- Non-uniqueness of nucleon forces ✗

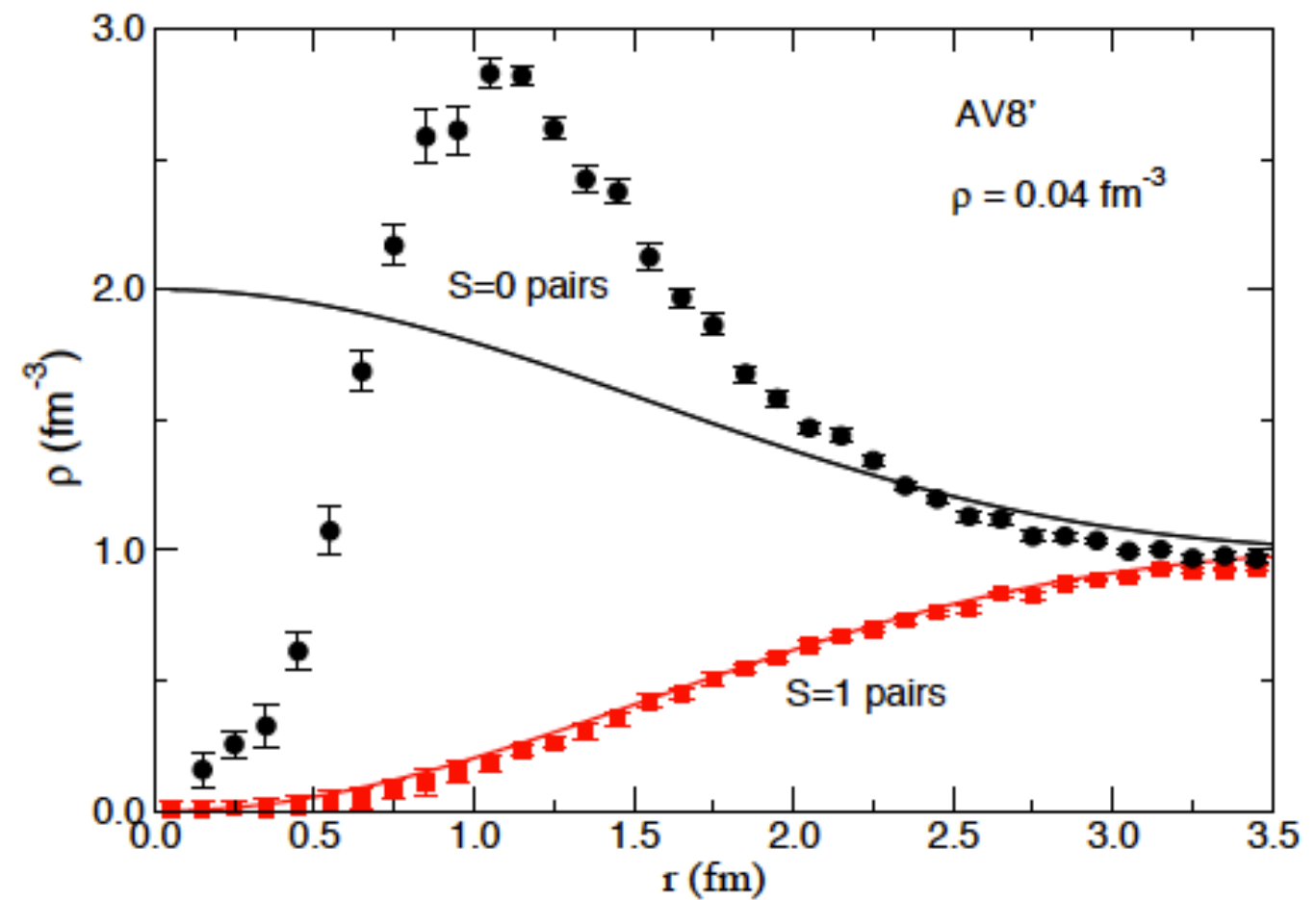
Complications

NN interaction is not unique



S.Aoki, et al. *Comput. Sci. Dis.* **1** 015009 (2008)

Strong short-range correlations

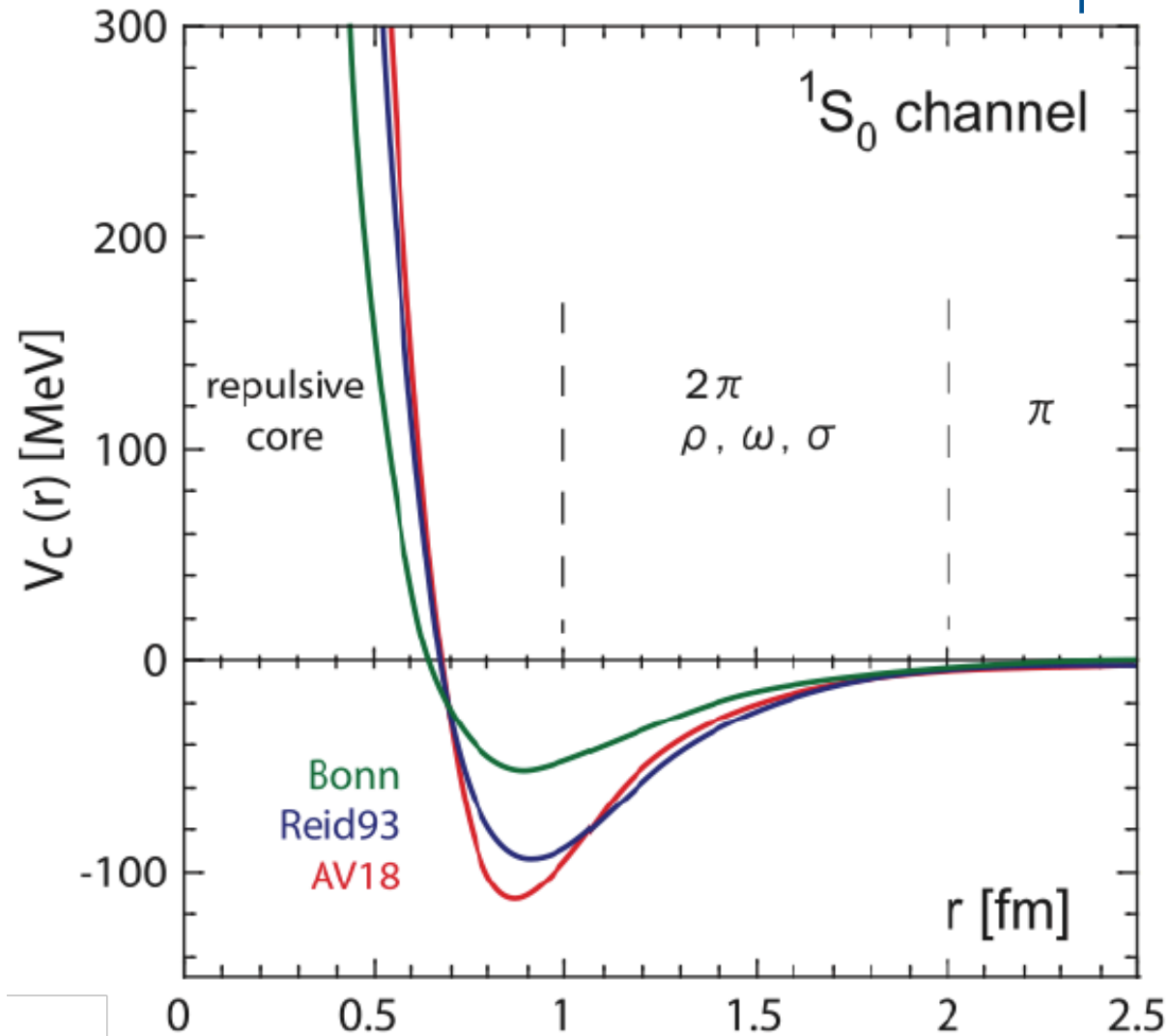


Carlson et al., *Phys. Rev. C* **68** 025802 (2003)

- Non-uniqueness of nucleon forces ✗
- Short-range core needs many-body treatment ✗

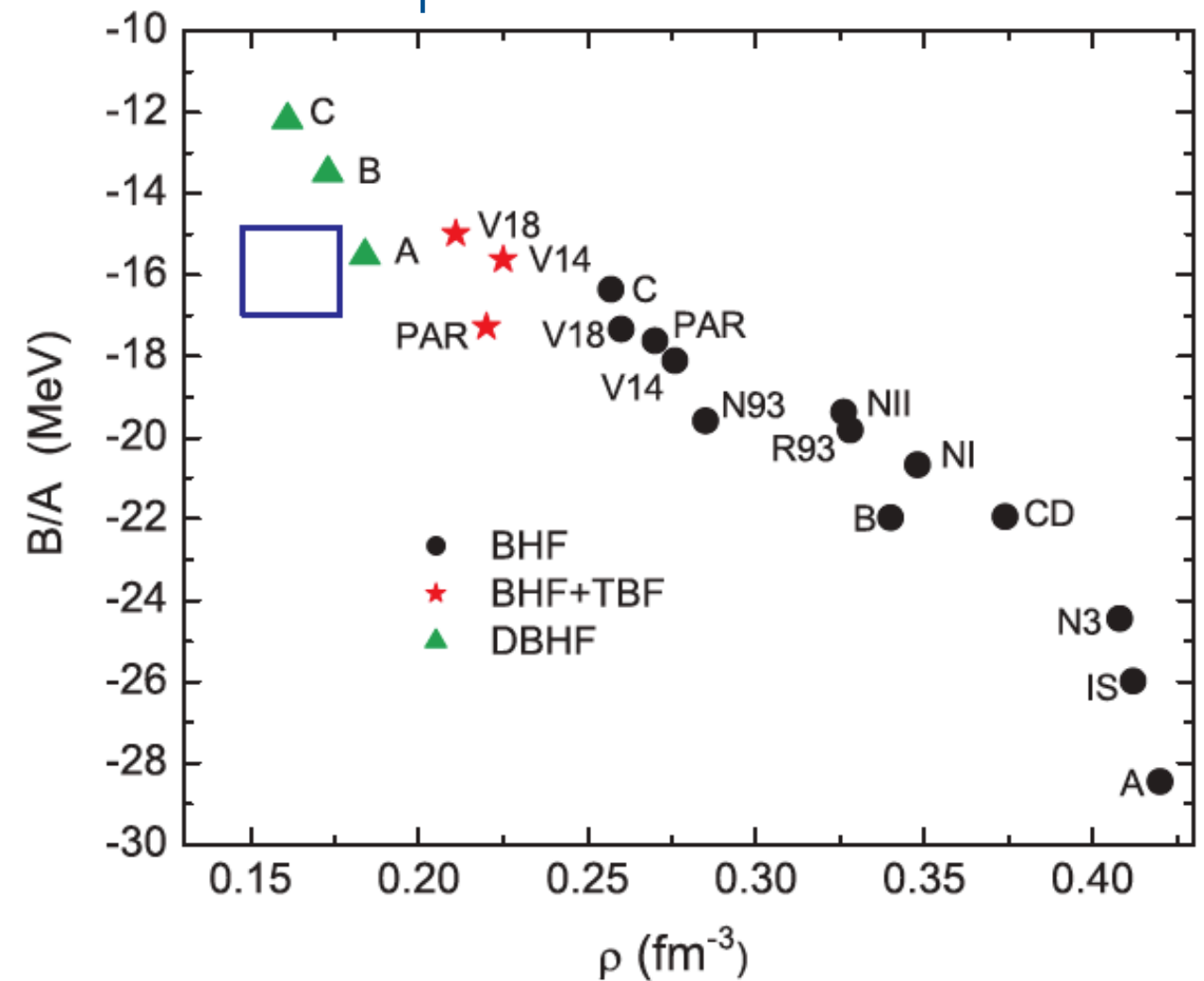
Complications

NN interaction is not unique



S.Aoki, et al. *Comput. Sci. Dis.* | 015009 (2008)

Saturation point of nuclear matter



Li, Lombardo, Schulze et al. *PRC* **74** 047304 (2006)

- Non-uniqueness of nucleon forces ✗
- Short-range core needs many-body treatment ✗
- Three-body forces needed for saturation ✗




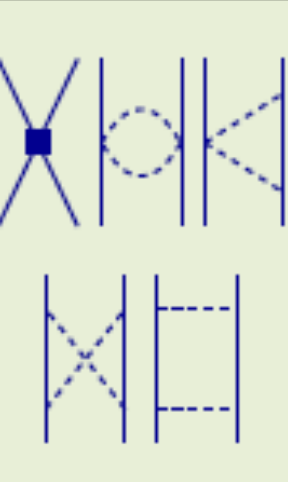


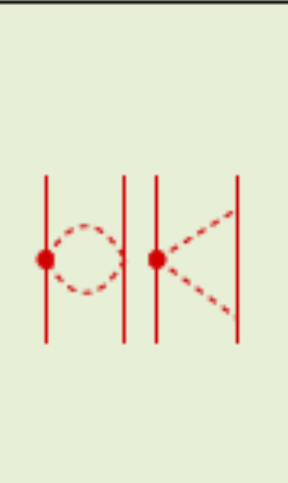
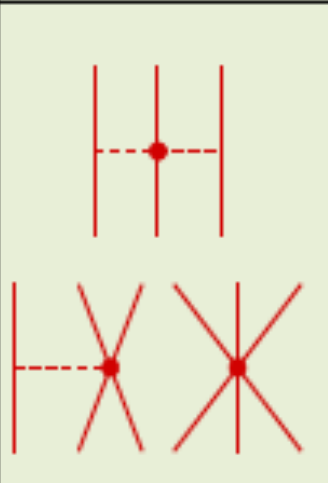




NN forces from EFTs of QCD

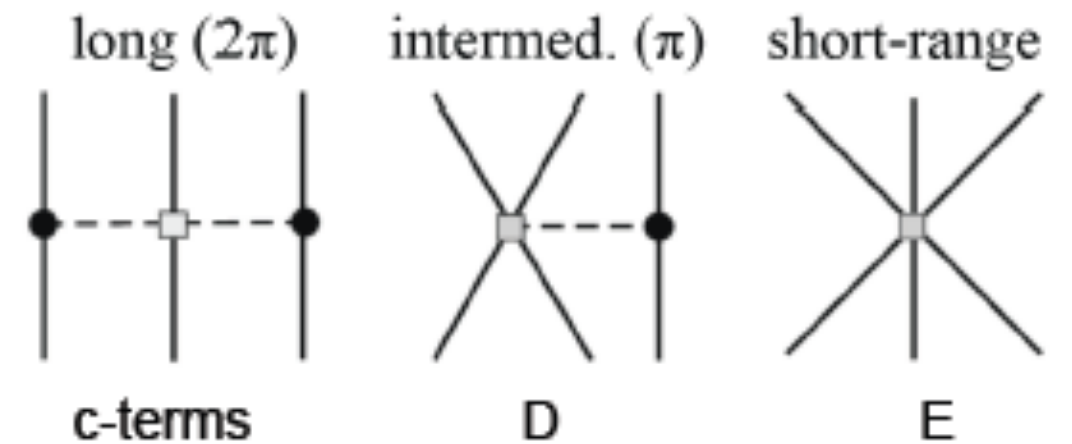
Chiral perturbation theory

- π and N as dof
- **Systematic** expansion
- 2N at N³LO - LECs from π N, NN
- 3N at N²LO - 2 more LECs
- (Often further renormalized)

$$\mathcal{O}\left(\frac{Q}{\Lambda}\right)$$

$\Lambda \sim 1 \text{ GeV}$

	NN	3N	4N
LO			
NLO			
N ² LO			
N ³ LO	 + ...	 + ...	 + ...



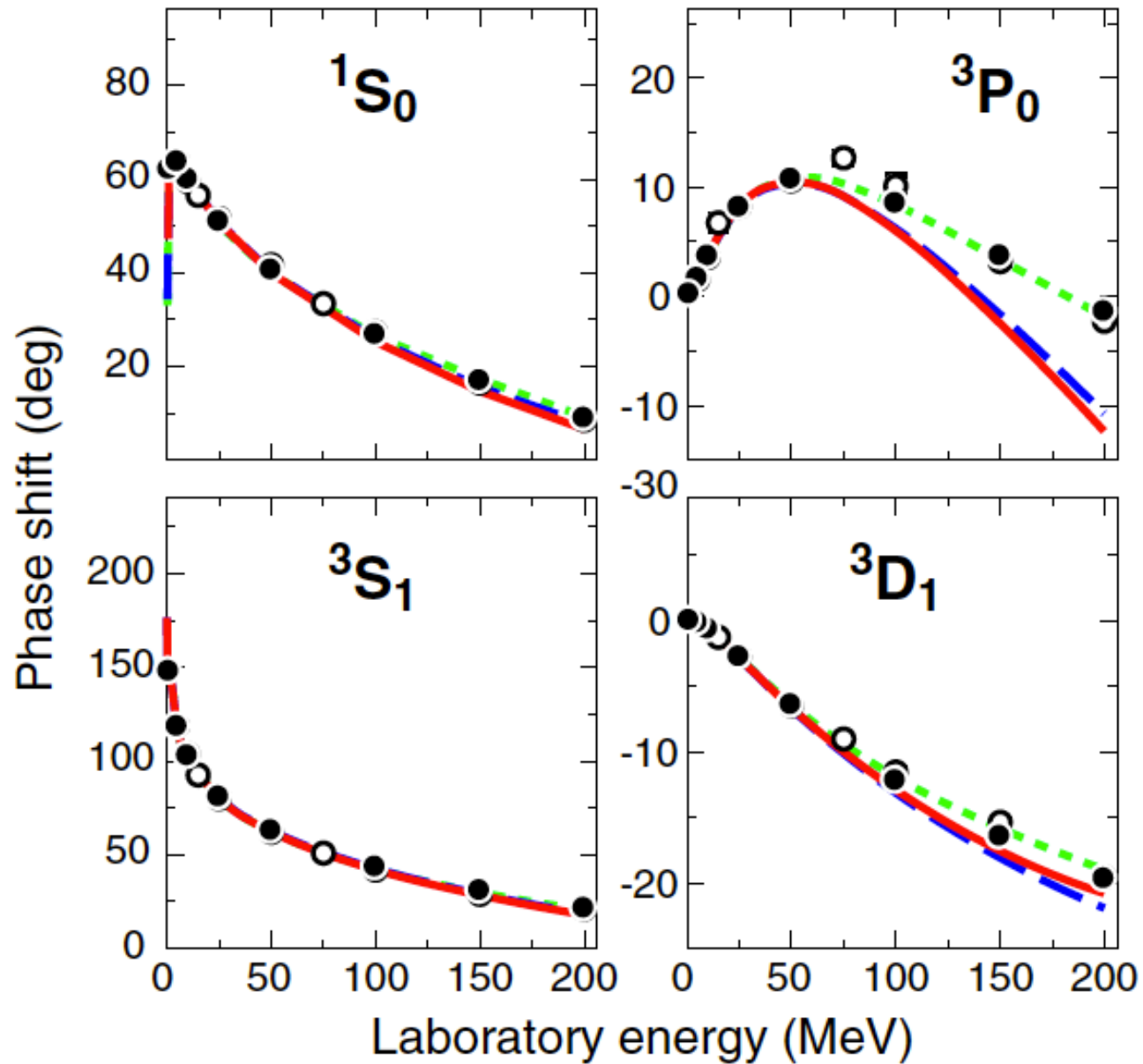
Weinberg, *Phys. Lett. B* **251** 288 (1990), *Nucl. Phys. B* **363** 3 (1991)

Entem & Machleidt, *Phys. Rev. C* **68**, 041001(R) (2003)

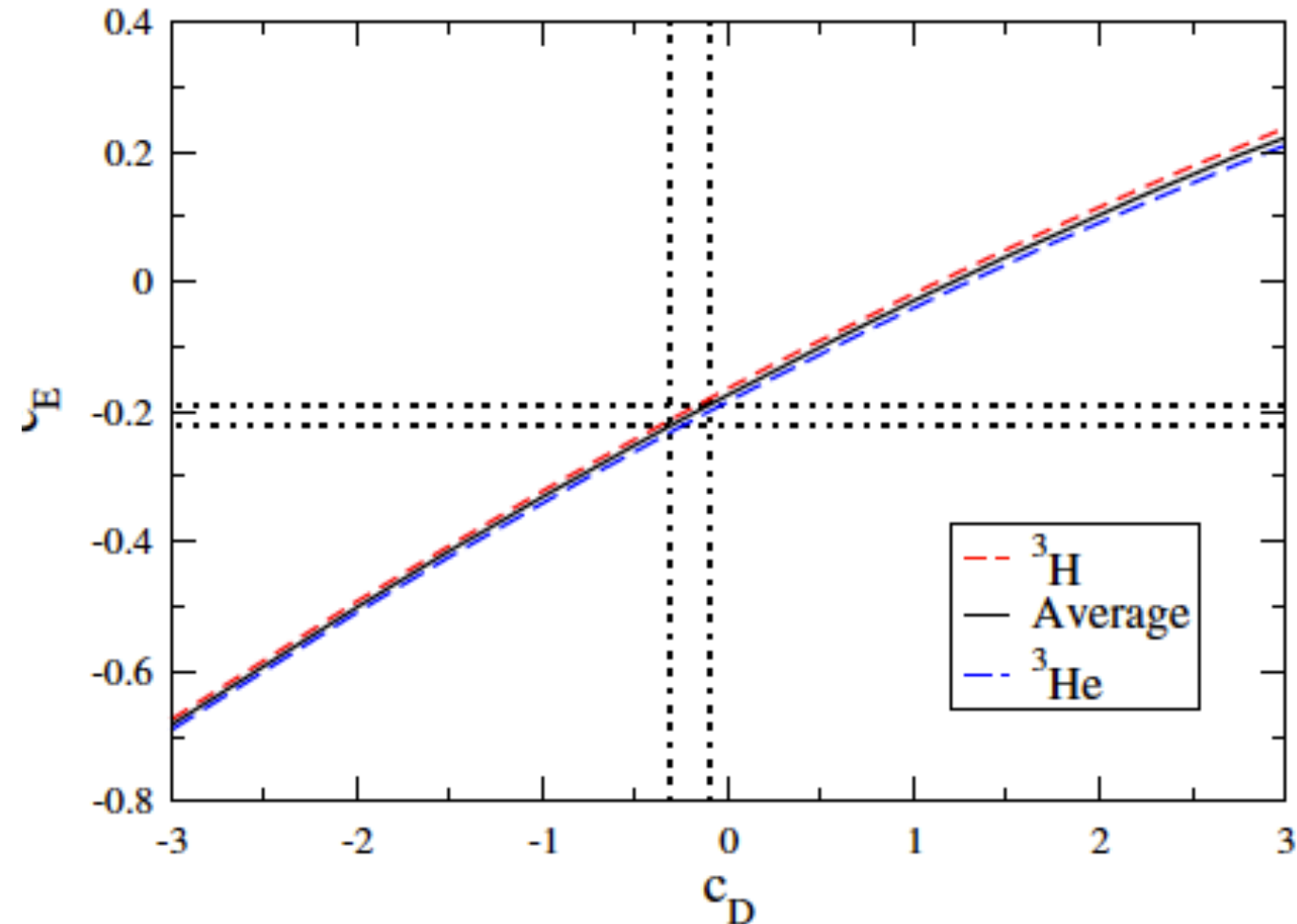
Tews, Schwenk et al., *Phys. Rev. Lett.* **110**, 032504 (2013)

LECs fitting

2NF constants:
deuteron + phase-shifts



3NF constants:
 $A=3 + \beta$ decay



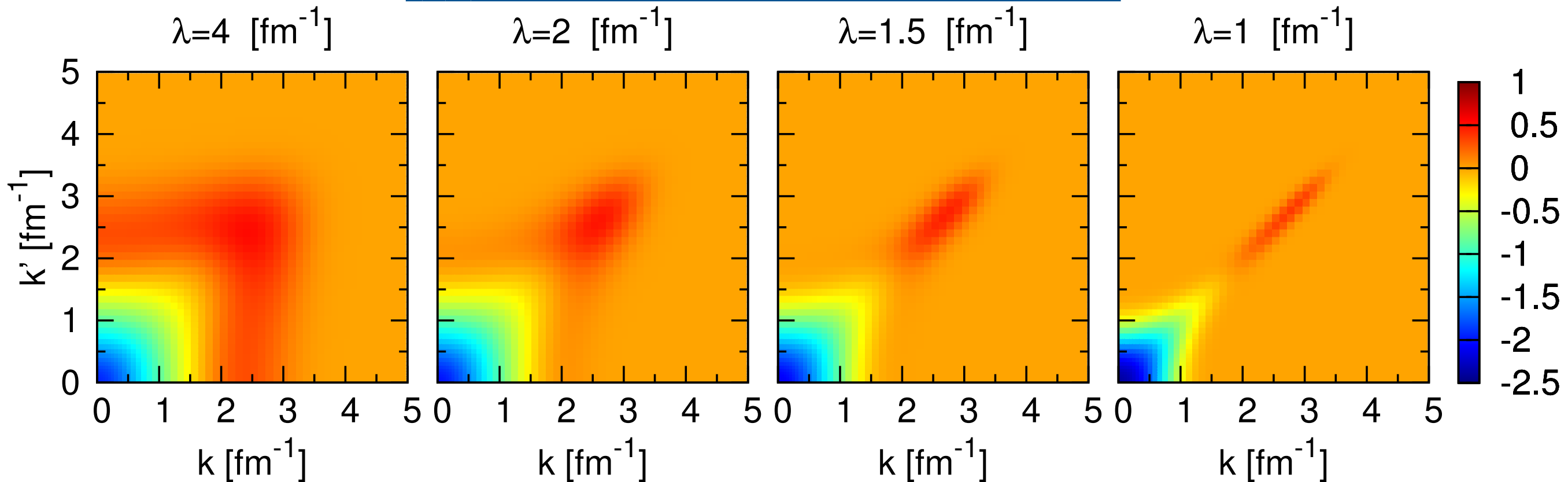
Nogga et al., *Phys. Rev. C* **73** 064002 (2006)
Gazit et al., *PRL* **103** 102502 (2009)

$N^3\text{LO}$: Entem & Machleidt, *Phys. Rev. C* **68** 041001 (2003)
 $N^2\text{LO}$: Ekstrom et al., *PRL* **110** 192502 (2013)

- Non-uniqueness now is **quantifiable!**

Further renormalizations

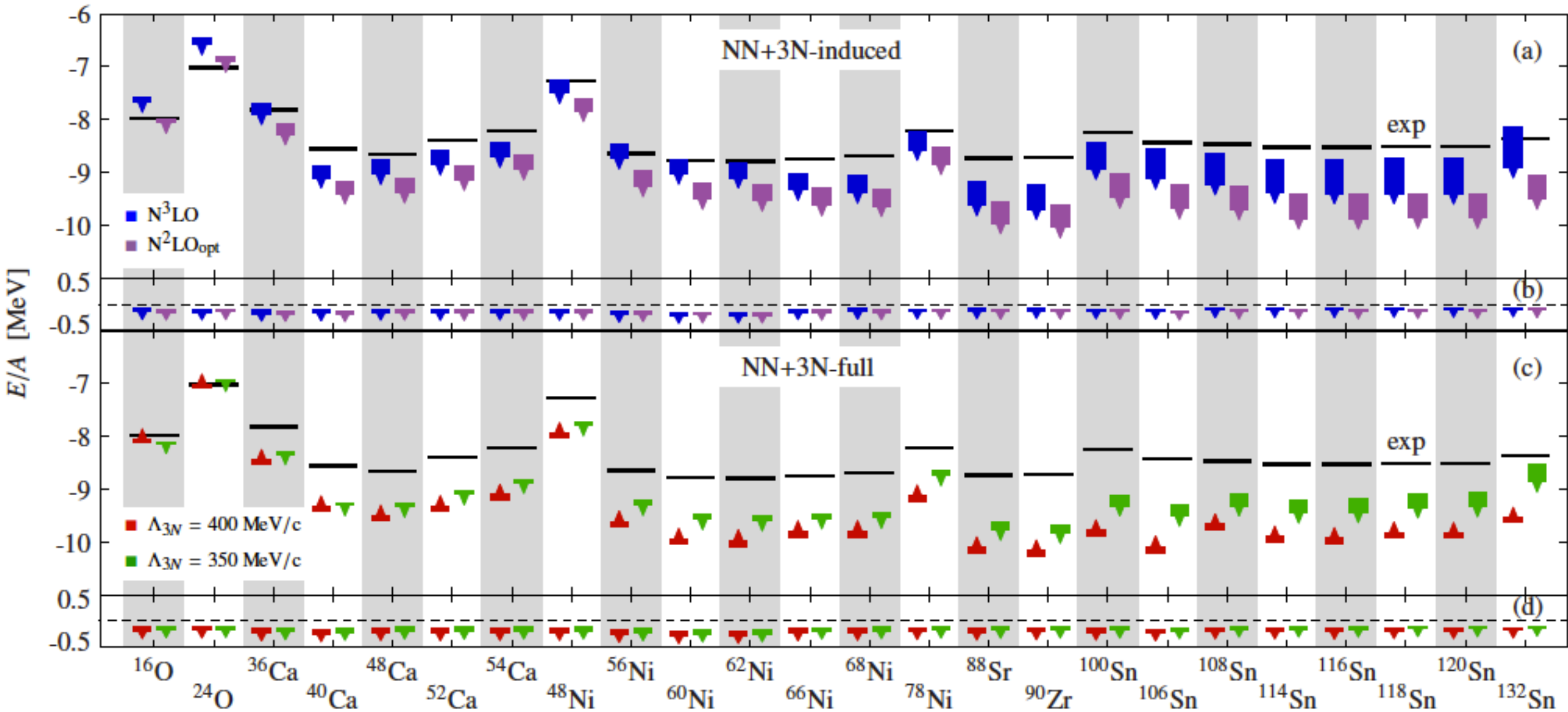
1S_0 NN matrix elements from N3LO



$$\frac{dH_s}{ds} = [[T_{rel}, H_s], H_s] \Leftrightarrow \lambda = s^{-1/4}$$

- Series of **unitary** transformation
- Observables **unaltered**, but force becomes **perturbative**
- **Induces** 3-, 4- and up to A-body forces...
- **If** these can be treated perturbatively, calculation is **easier**

The reach of *ab initio*: 2014

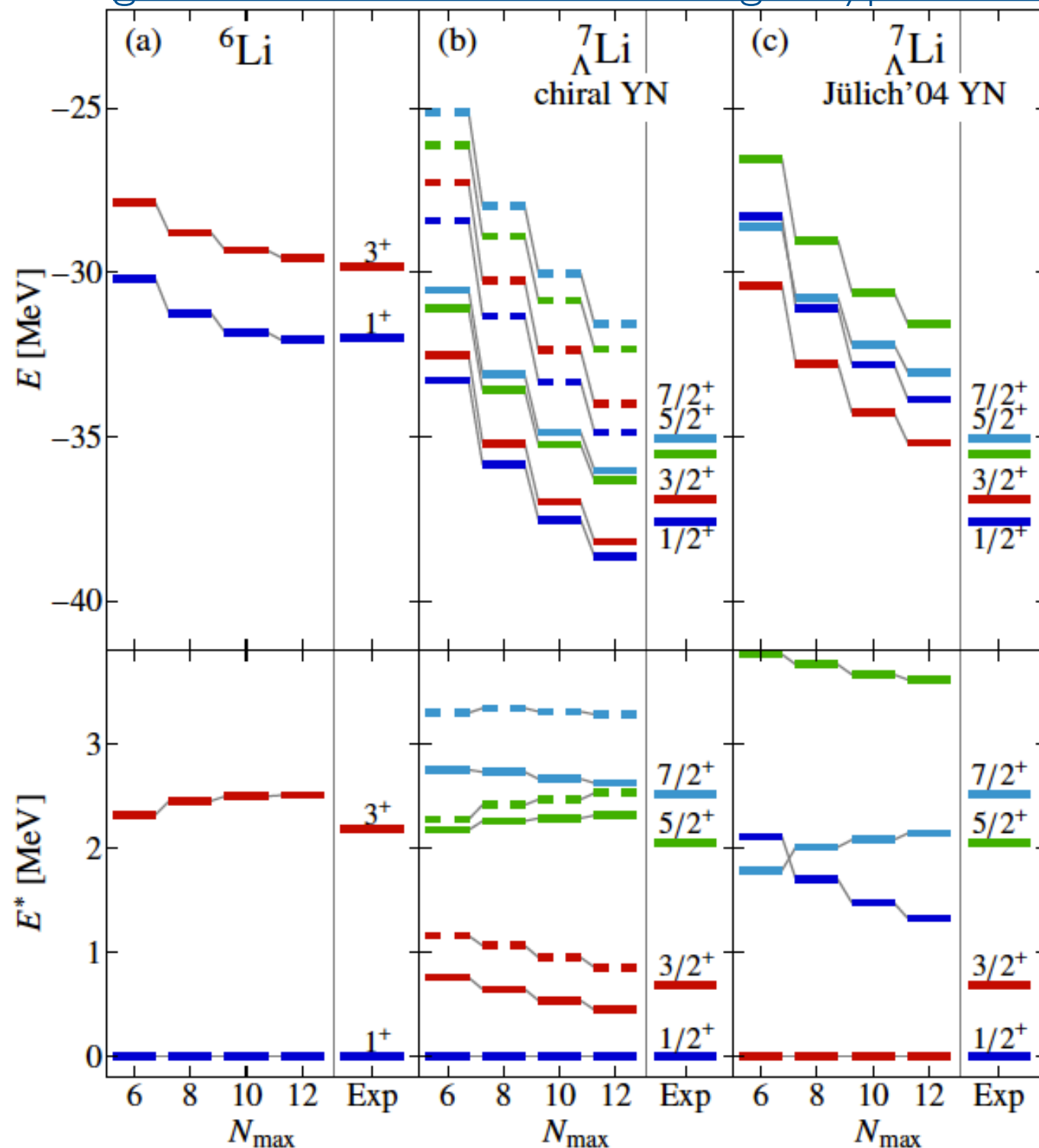


Binder, Langhammer, Calci & Roth, *arxiv:1312.5685*

- Consistent calculations up to $A=132$
- Many-body (CC) errors under control
- Overbinding even when 3NF accounted for
- Radii are too small as well

Hypernuclei!

ground and excited states of light hypernuclei



- IT-NCSM with **chiral** NN & different YN forces
- **Hypernuclear** structure hints at nonperturbative YNN

SCGF: diagrammatic expansion

N-body Green's function

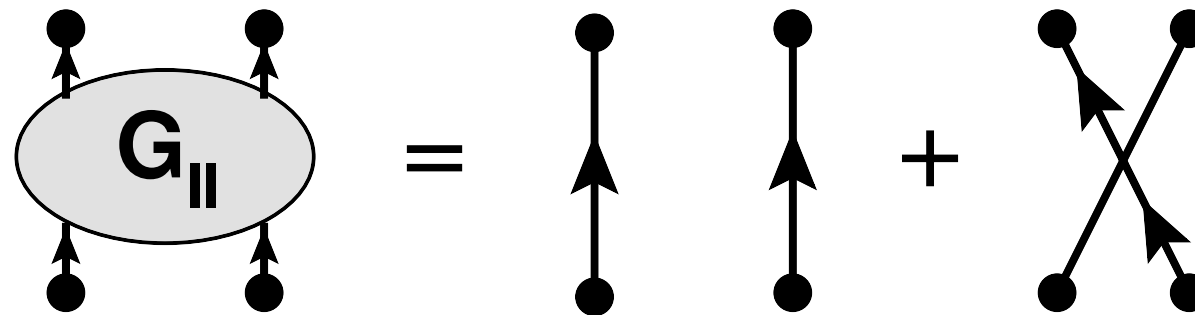
$$i^N G(\mathbf{1}, \dots, \mathbf{N}; \mathbf{1}', \dots, \mathbf{N}') = \left\langle \mathcal{T} \{ a(\mathbf{1}) \cdots a(\mathbf{N}) a^\dagger(\mathbf{N}') \cdots a^\dagger(\mathbf{1}') \} \right\rangle$$

$\langle \cdot \rangle \rightarrow$ average over states

$\mathcal{T} \rightarrow$ some sort of time ordering (real, imaginary, on a contour...)

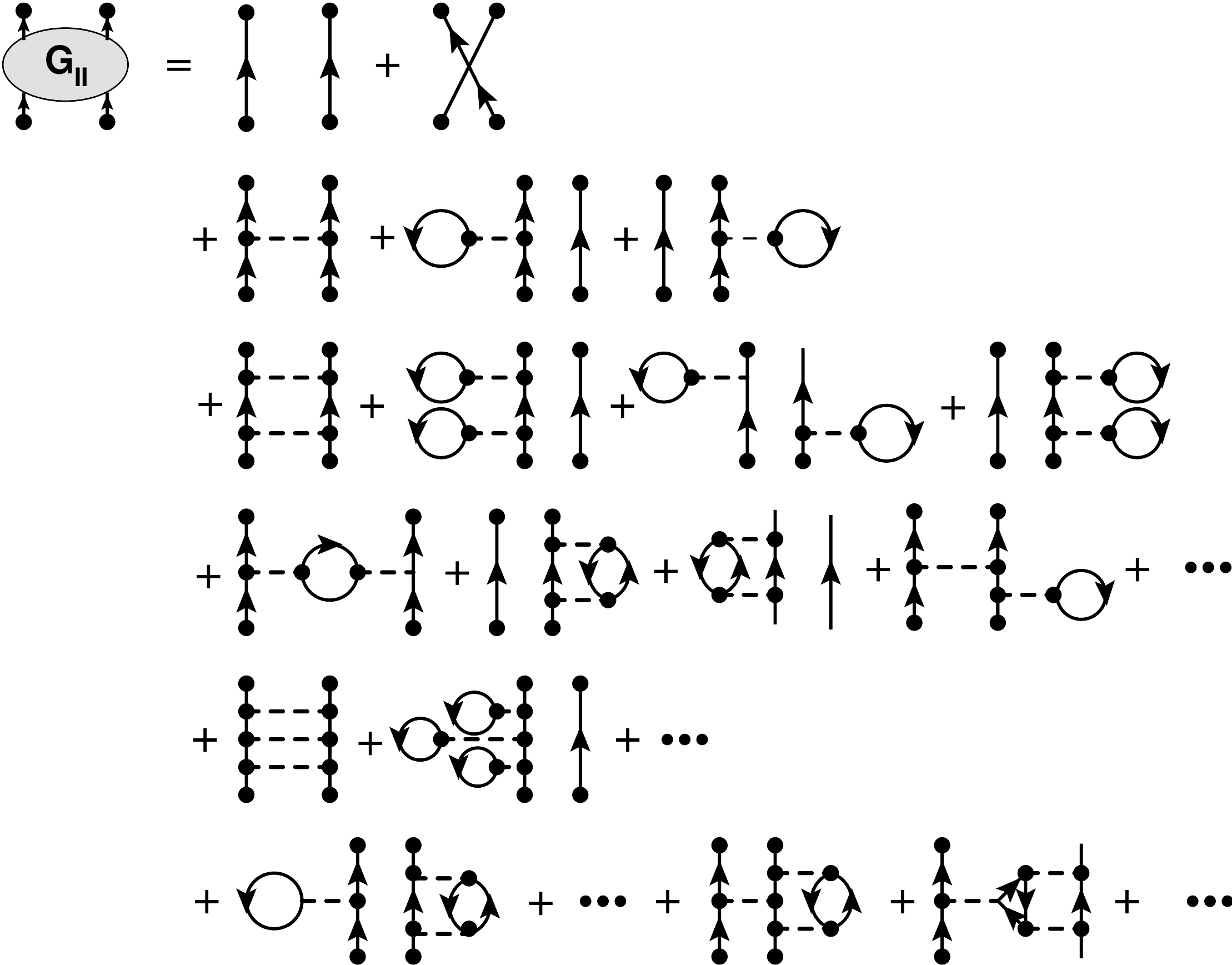
$\mathbf{1} \rightarrow \mathbf{r}_1, t_1, \sigma_1, \tau_1$

Two-body GF, lowest order diagrams

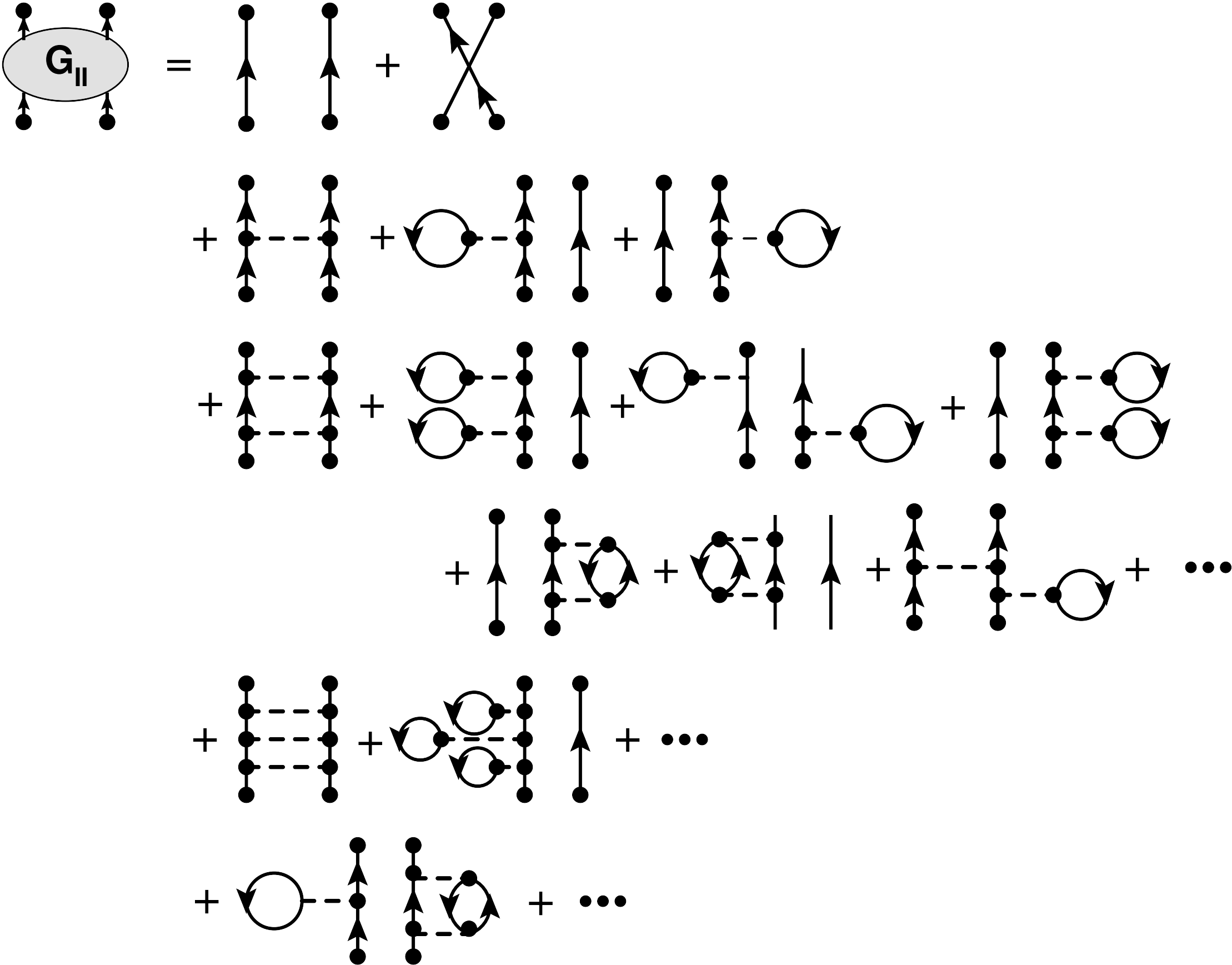


$$G_{II}(1, 2; 1', 2') = G(1, 1')G(2, 2') - G(1, 2')G(1', 2)$$

SCGF: diagrammatic expansion



SCGF: diagrammatic expansion

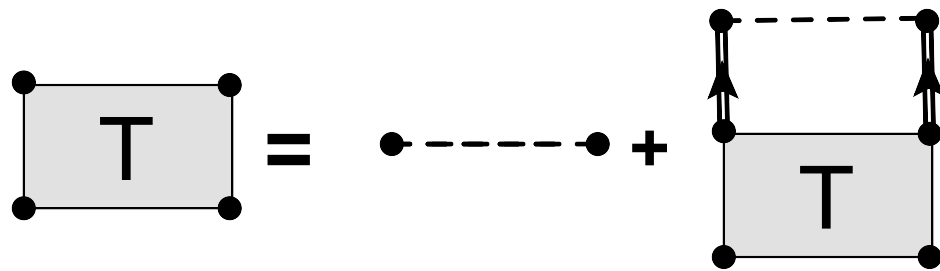


Ladder approximation with 3BF

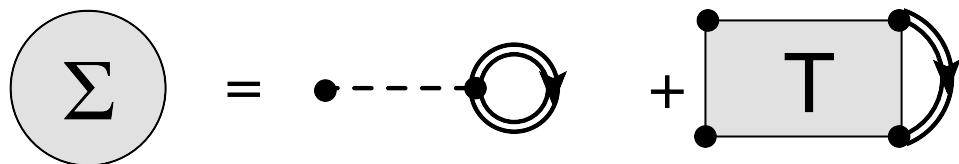
Two-body interaction



In-medium T-matrix

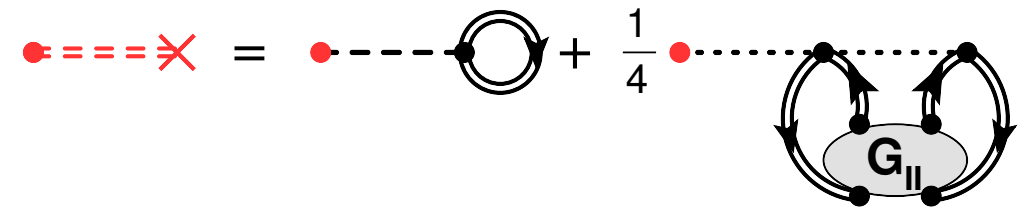


Self-energy



Effective interactions

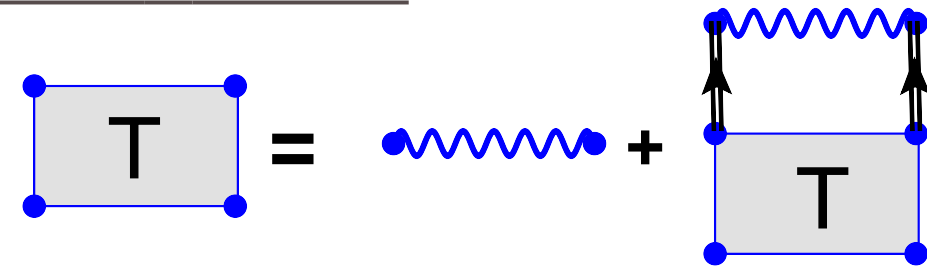
Effective one-body force



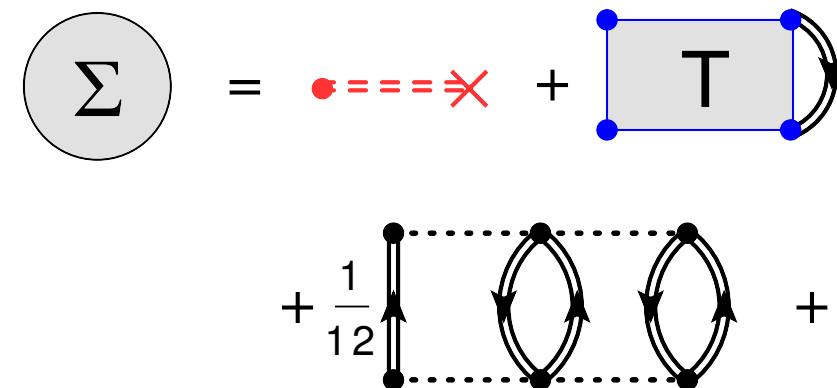
Effective two-body force



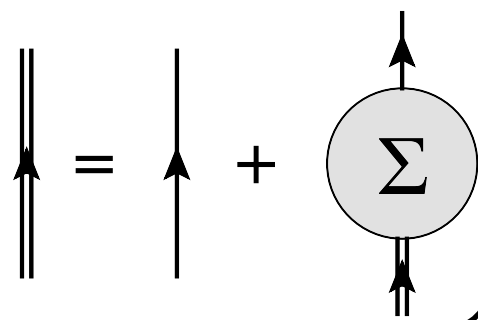
In-medium T-matrix



Self-energy



Dyson equation

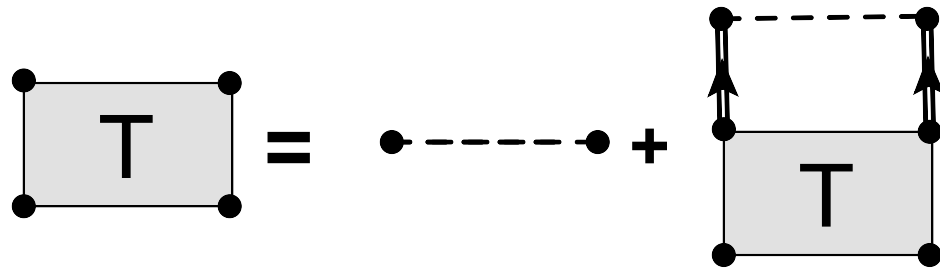


Ladder approximation with 3BF

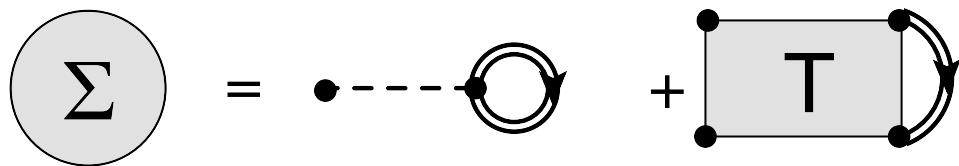
Two-body interaction



In-medium T-matrix

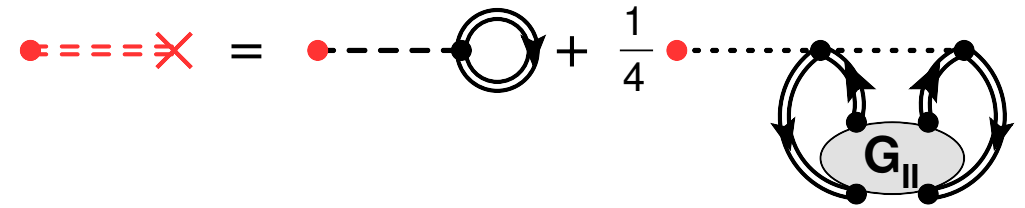


Self-energy

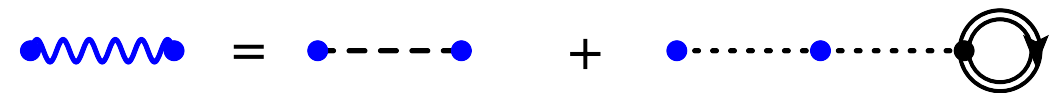


Effective interactions

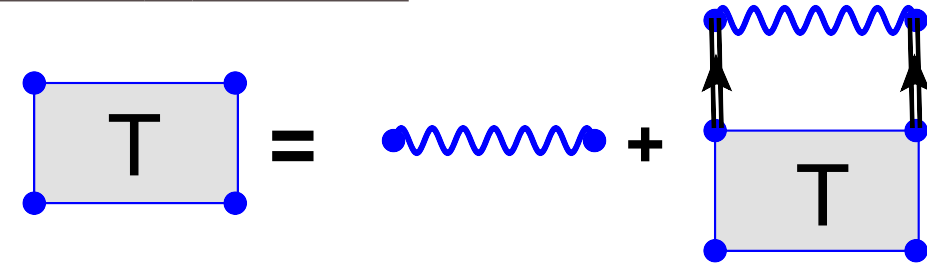
Effective one-body force



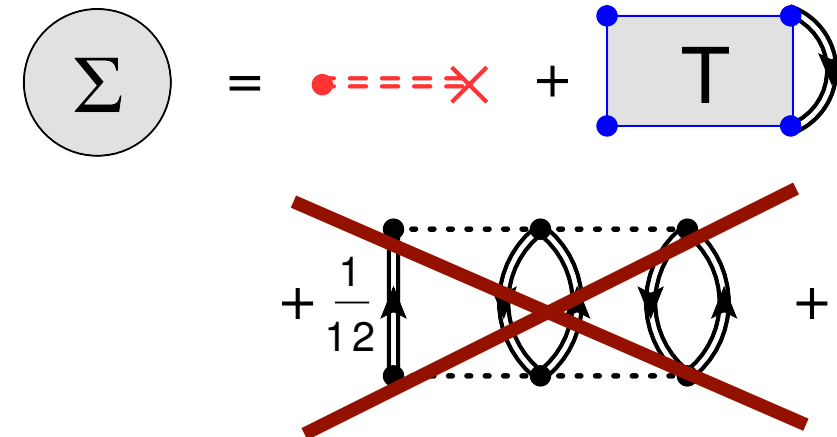
Effective two-body force



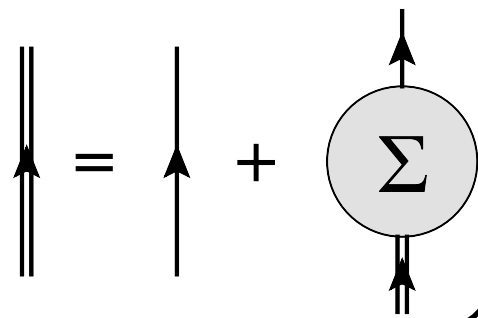
In-medium T-matrix



Self-energy



Dyson equation

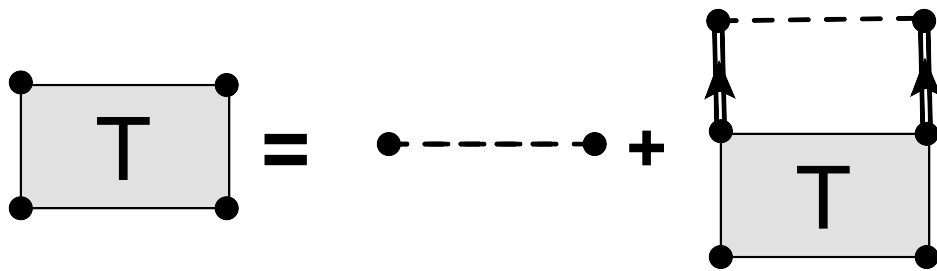


Ladder approximation with 3BF

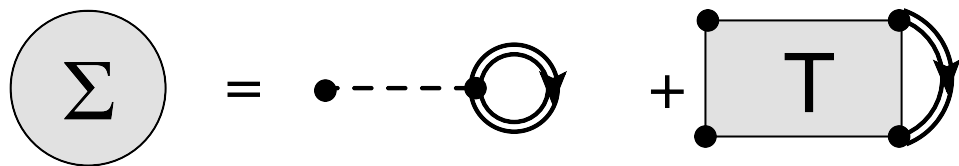
Two-body interaction



In-medium T-matrix

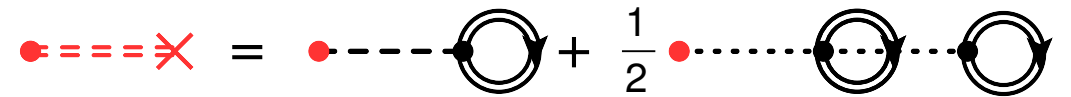


Self-energy

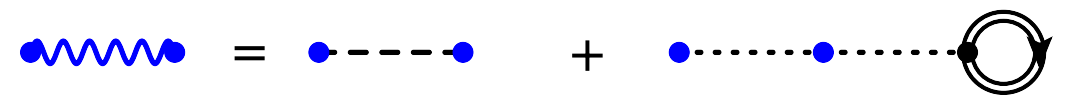


Effective interactions

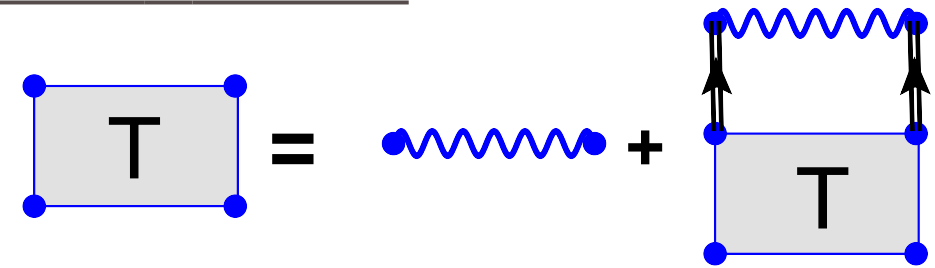
Effective one-body force



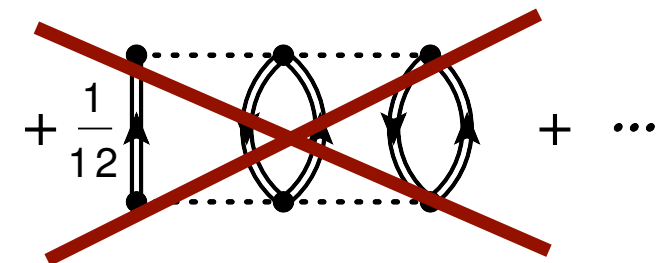
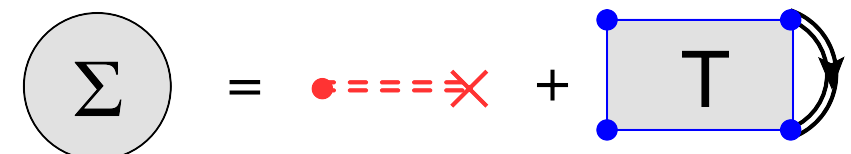
Effective two-body force



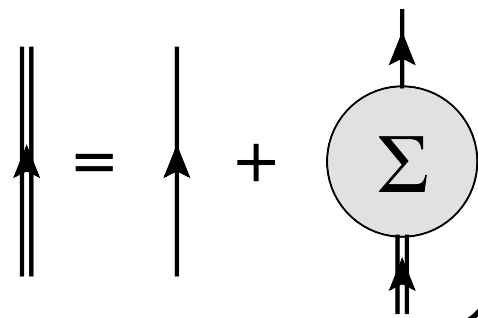
In-medium T-matrix



Self-energy



Dyson equation

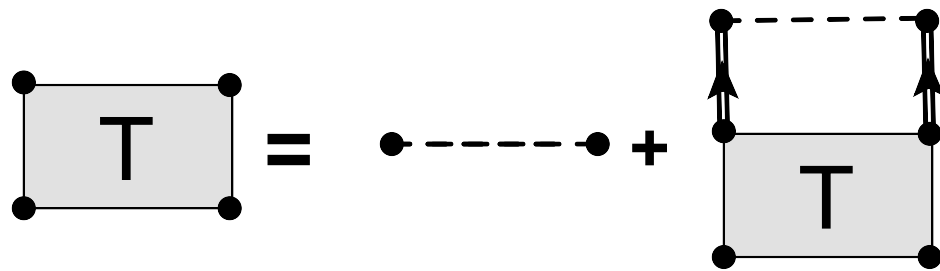


Ladder approximation with 3BF

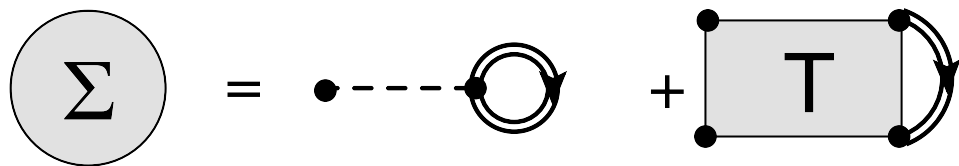
Two-body interaction



In-medium T-matrix

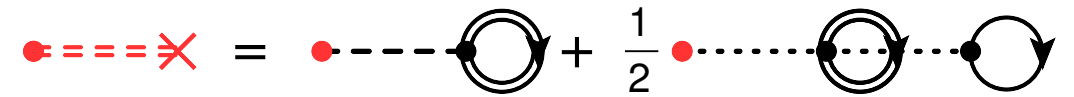


Self-energy

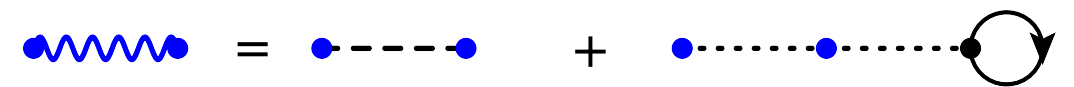


Effective interactions

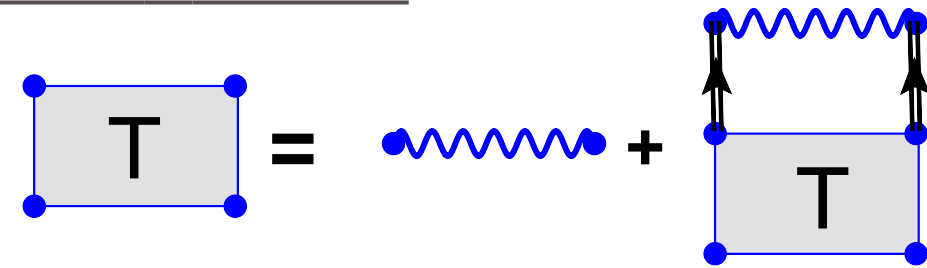
Effective one-body force



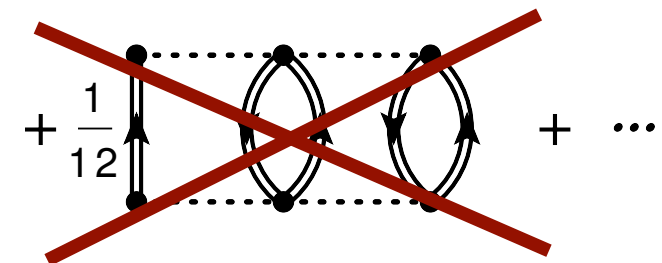
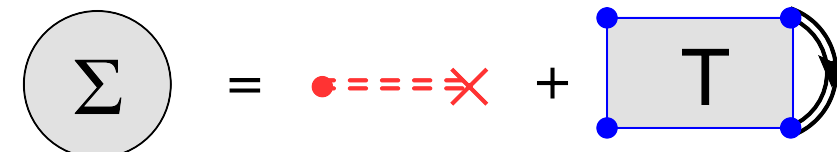
Effective two-body force



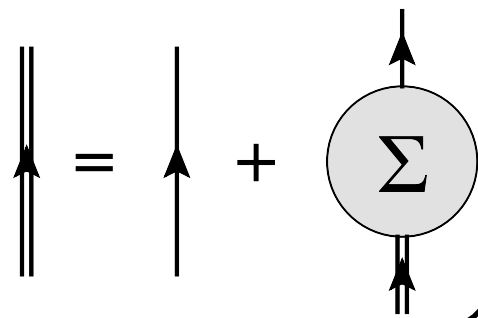
In-medium T-matrix



Self-energy



Dyson equation

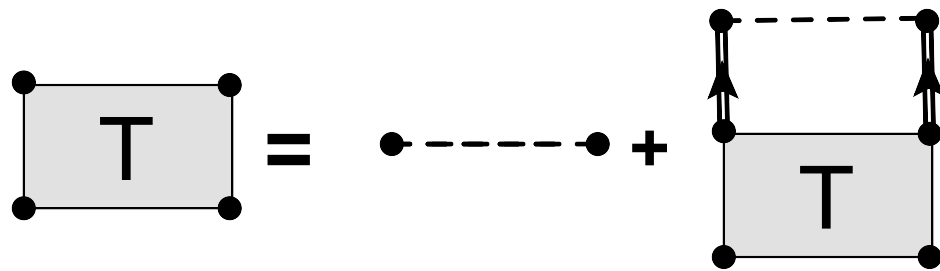


Ladder approximation with 3BF

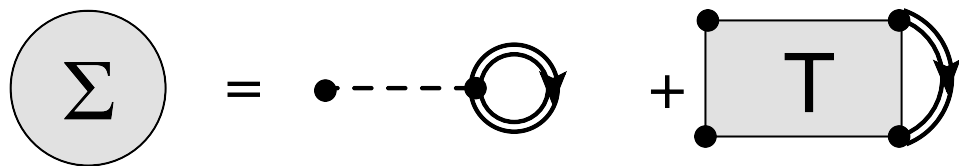
Two-body interaction



In-medium T-matrix

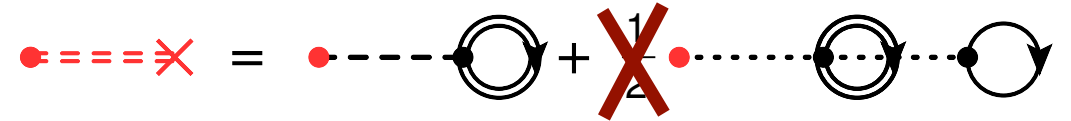


Self-energy

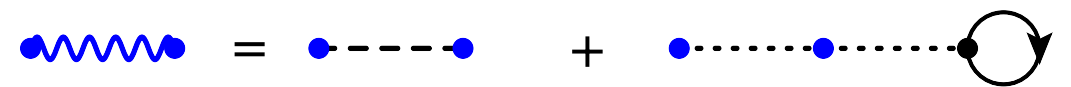


Effective interactions

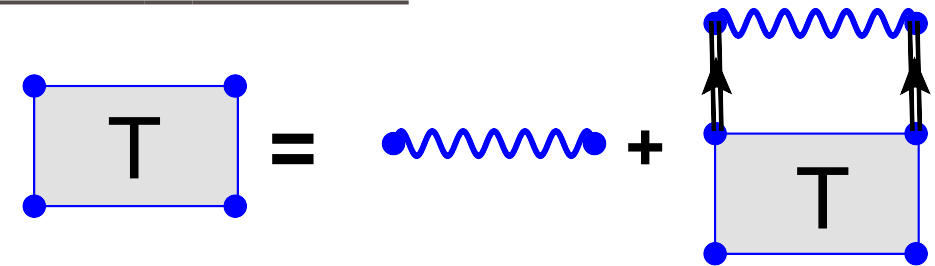
Effective one-body force



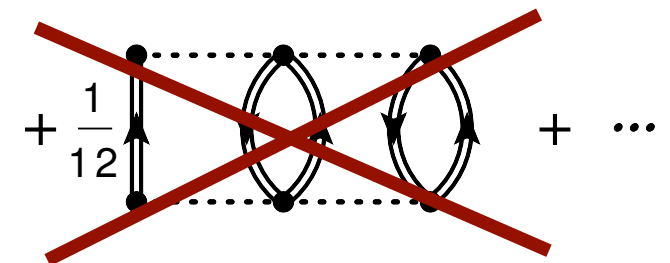
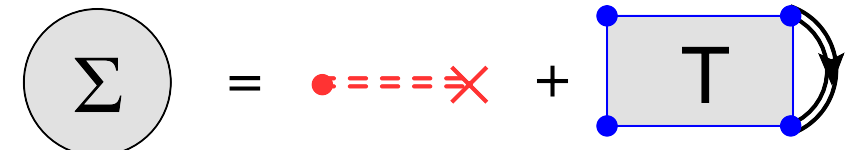
Effective two-body force



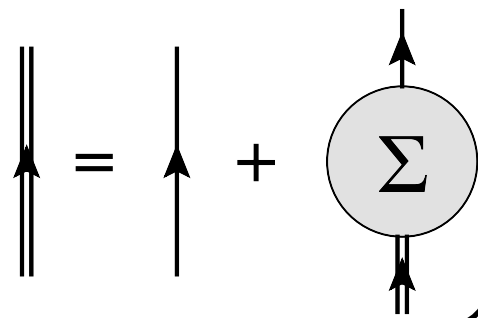
In-medium T-matrix



Self-energy



Dyson equation



Density-dependent interaction

Chiral NN effective 2B forces: symmetric matter

Two-body N3LO



Uncorrelated average¹



Correlated average²

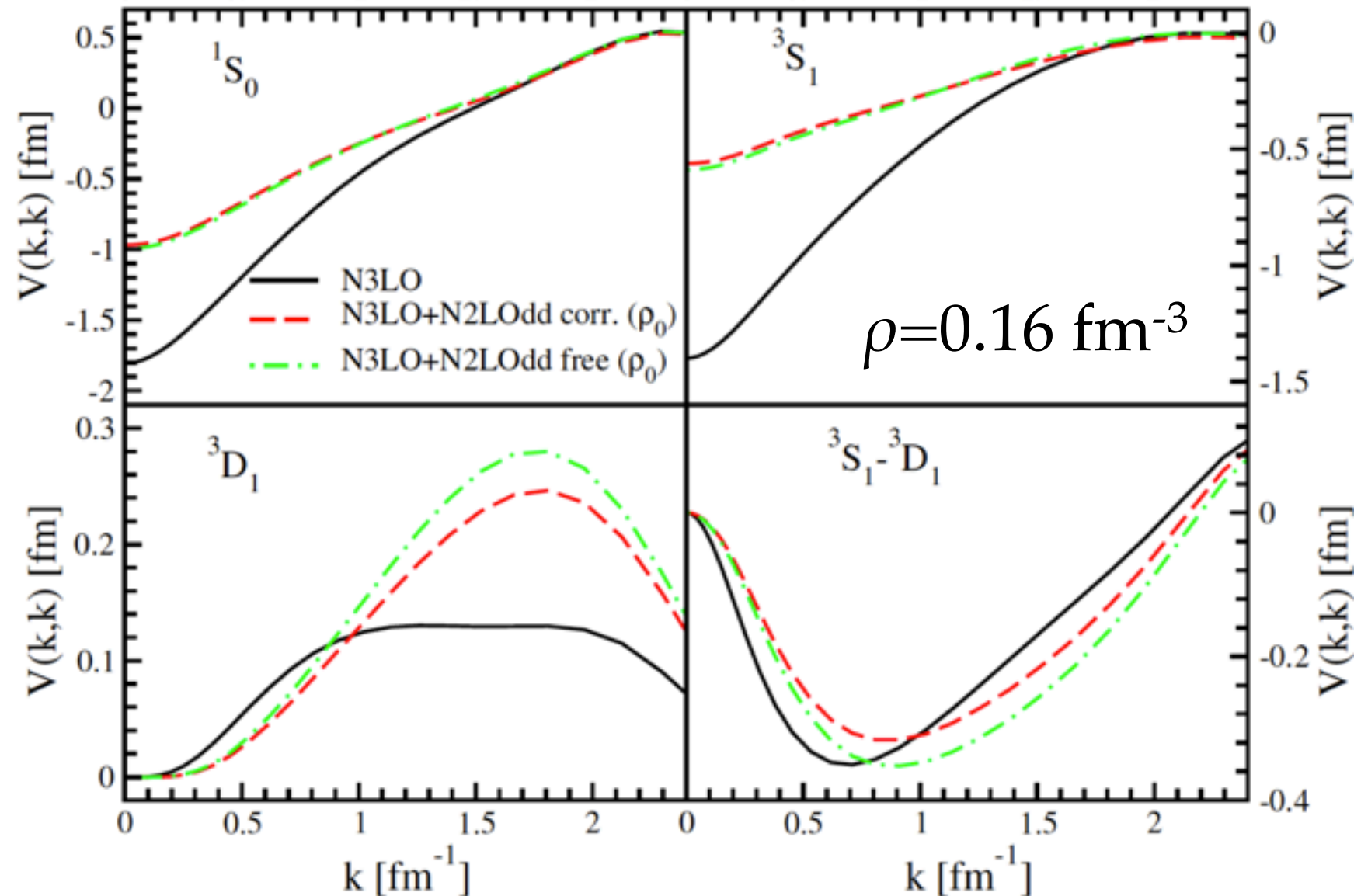


LECs

$$c_D = -1.11$$

$$c_E = -0.66$$

$$k \neq k' \Rightarrow \frac{1}{2}(k + k')$$



- 3NF bring **repulsion**: **correlated** & **uncorrelated** averages are similar
- **Correlated** average brings **small** corrections to 1/2 of terms
- Diagonal $k=k'$ matrix elements computed
- Off-diagonal extrapolated & **regulated**

¹Holt et al. *Phys. Rev. C* **81**024002 (2010)

²Carbone, Polls & Rios, *in preparation*; A. Carbone, PhD thesis ||

Symmetric matter

Theoretical uncertainties: average procedure

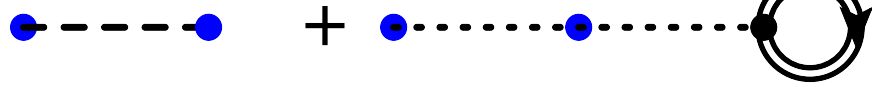
Two-body N³LO



Uncorrelated average



Correlated average



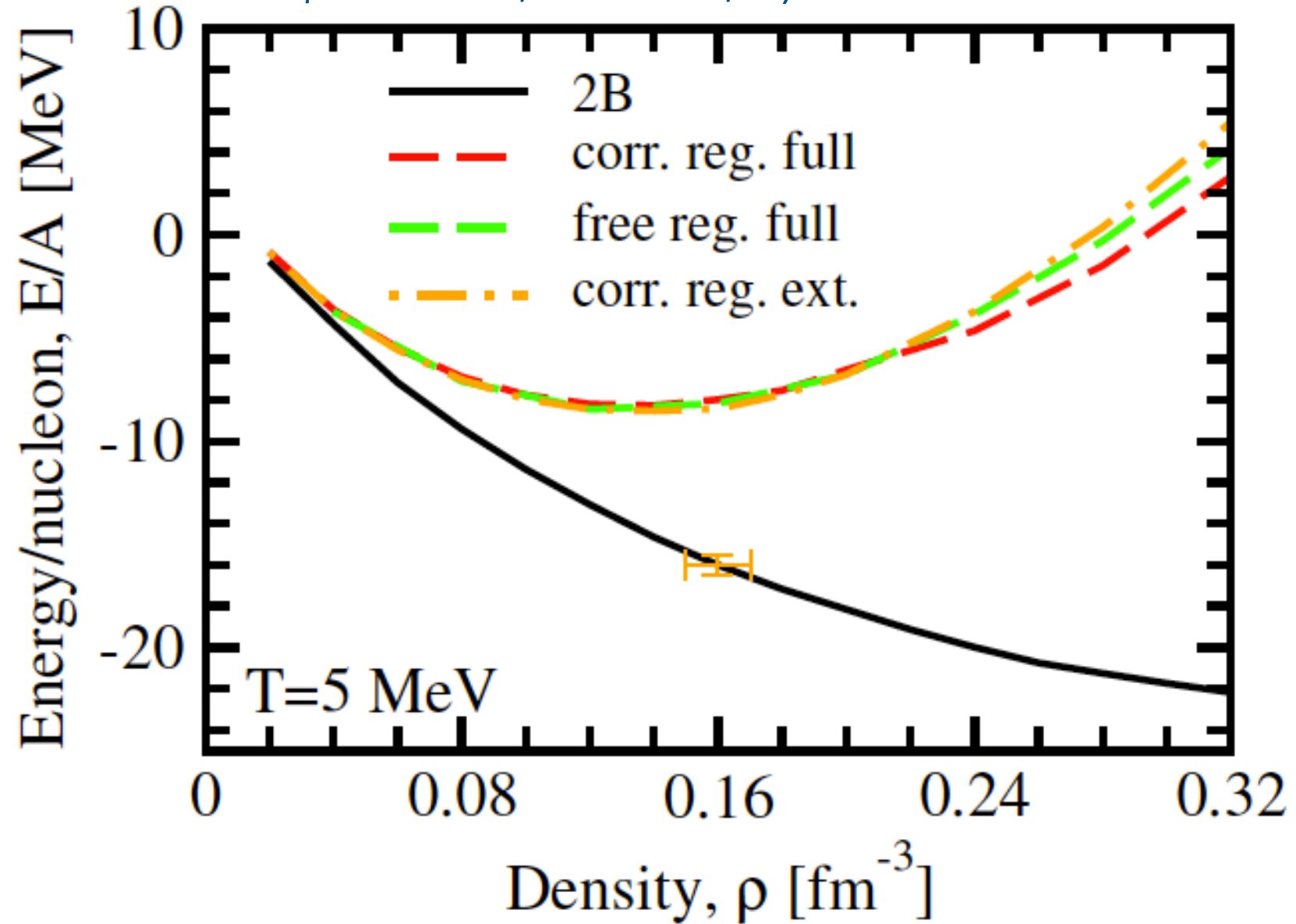
LECs

$$c_D = -1.11$$

$$c_E = -0.66$$

Energy from GMK sum-rule
... with 3N corrections¹ ...

Equation of state of symmetric matter



- **Cor. reg. full** = best we can do now is underbound
- **Previous** work with uncorrelated averages is **validated**
- Regulation at high momentum is **irrelevant**

¹Carbone, Polls & Rios, *Phys. Rev. C* **88** 044302 (2014)
Carbone, Polls & Rios, *in preparation*; A. Carbone, PhD thesis 12

Symmetric matter

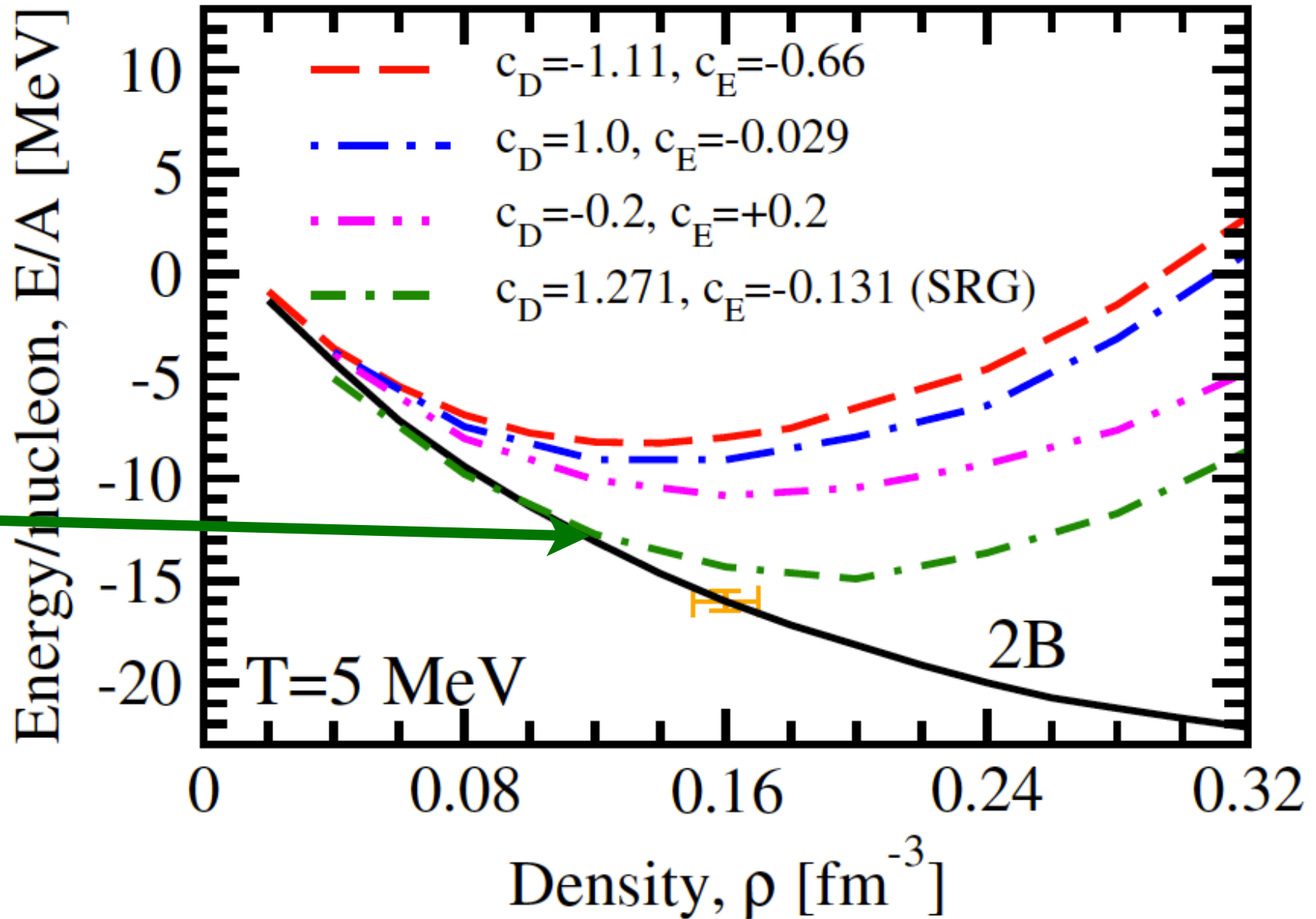
Theoretical uncertainties: NN force

Equation of state: LEC dependence

Uncorrelated average



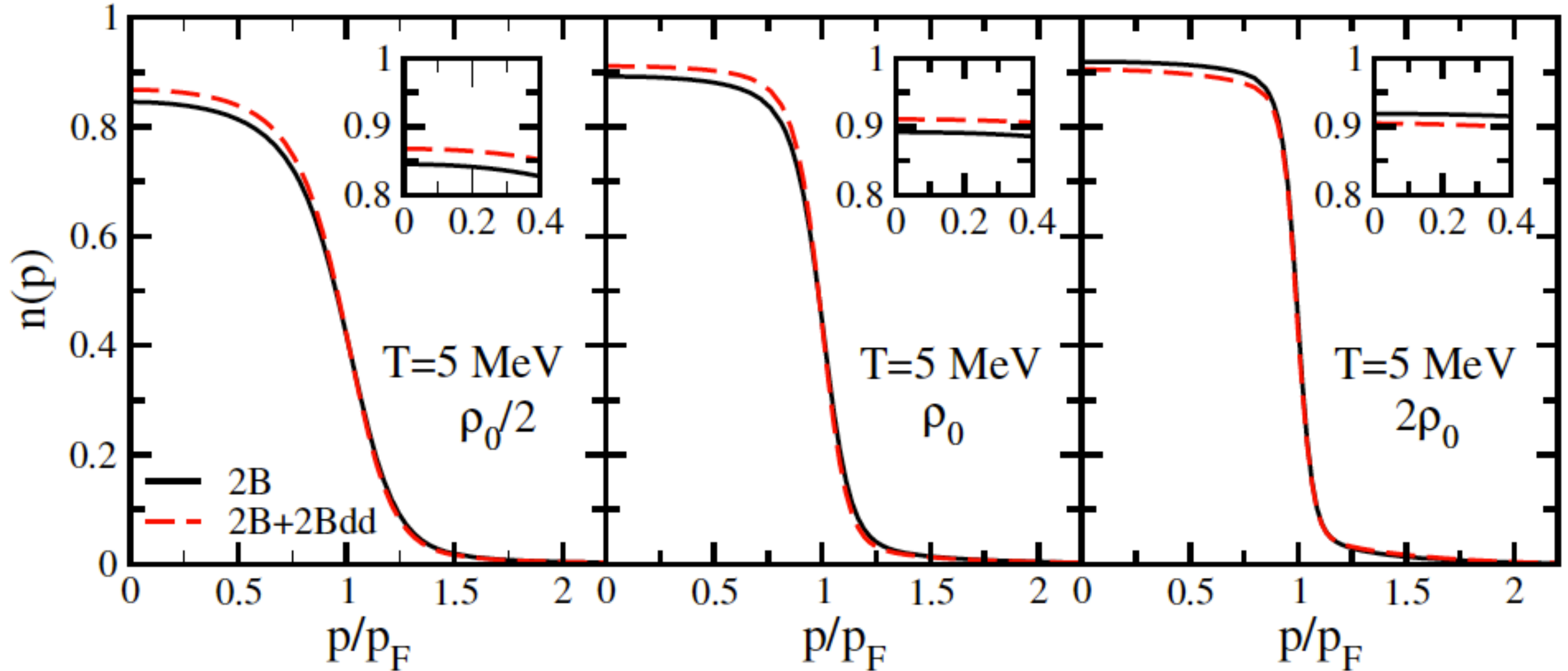
Further renormalized NN force
Nuclear structure calculations



- LECs dependence is strong
- Renormalization via SRG: nuclear structure calculations?
- Small 3NF effects with larger saturation densities \Rightarrow smaller radii

Microscopic properties

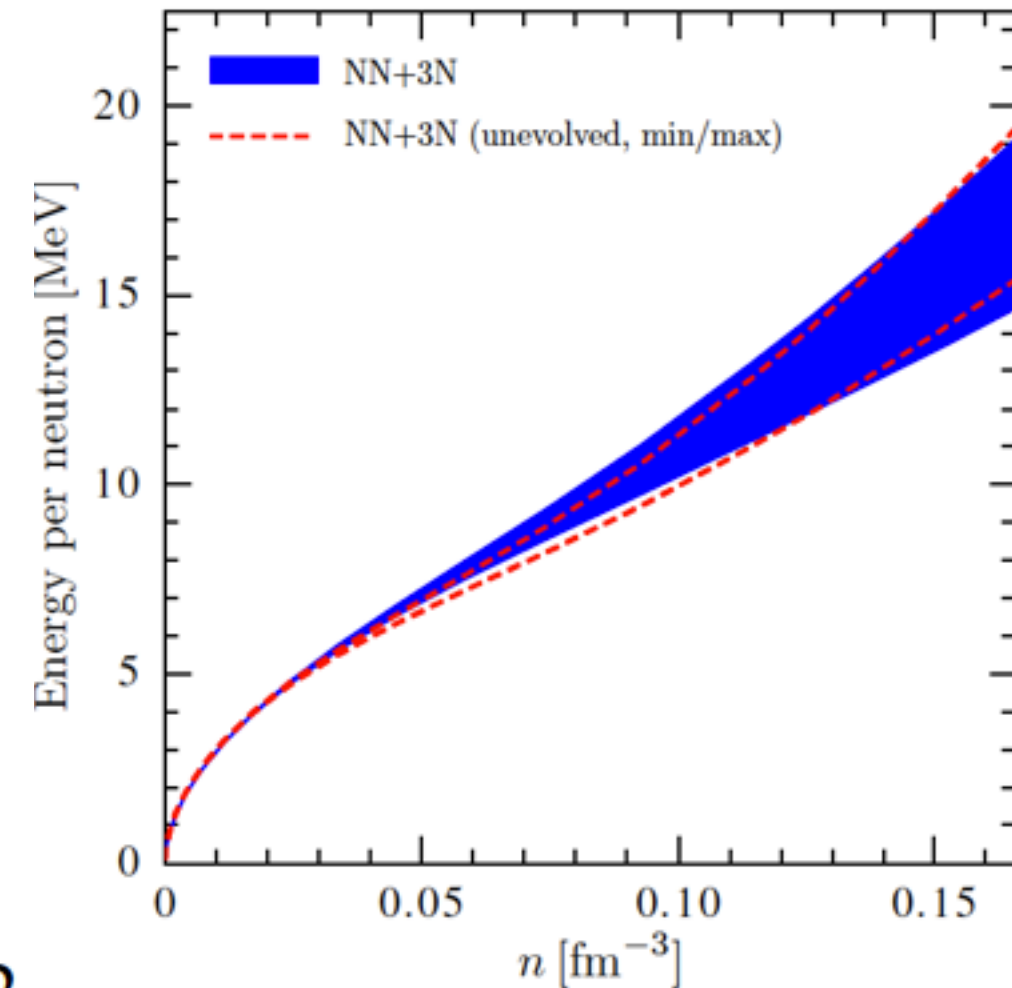
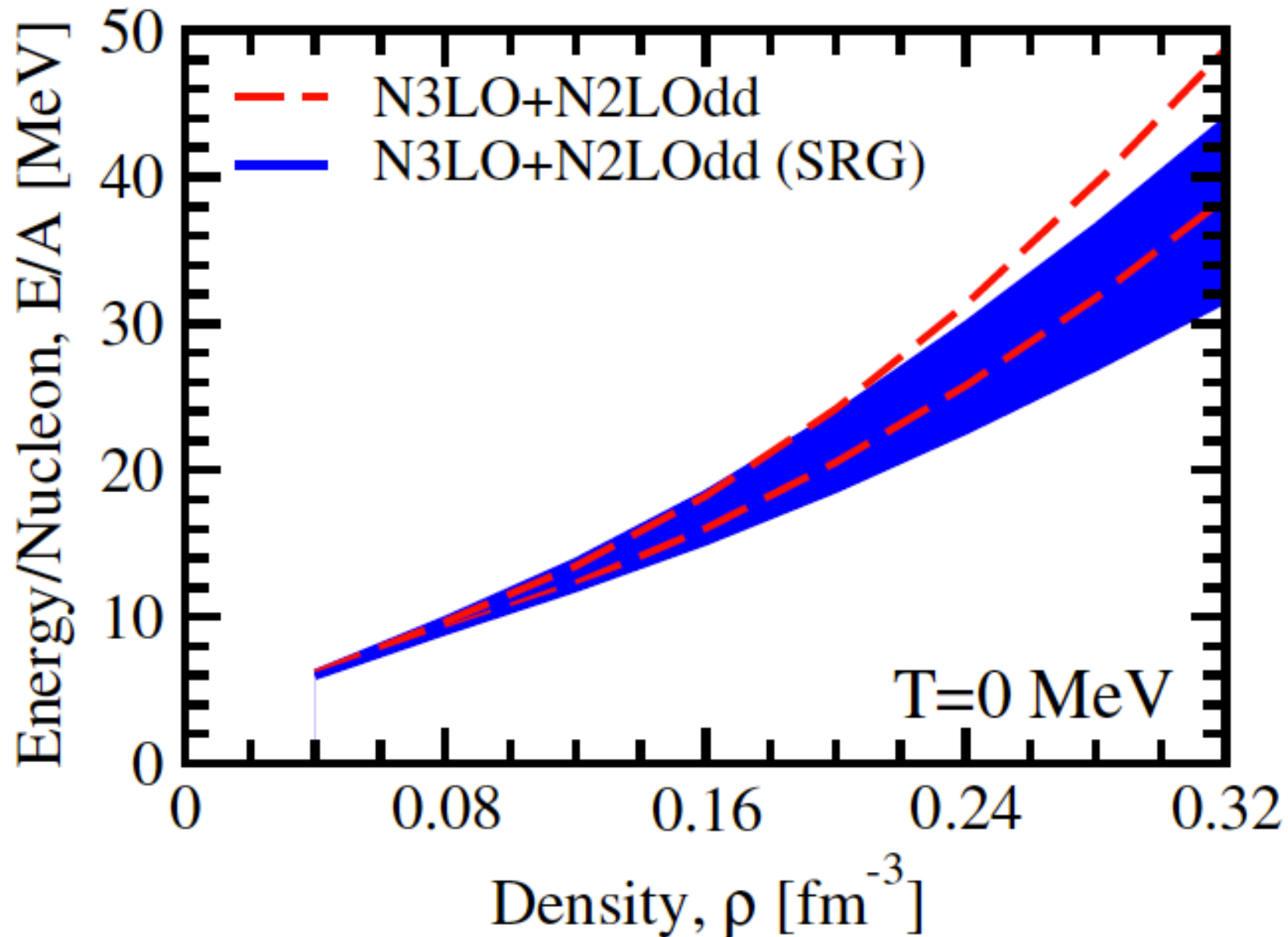
Correlated momentum distribution



- 3NFs induce **different** density dependence
- **Error band** from unknown ChPT parameters
- Finite temperature & **higher densities available**

Neutron matter

EoS for neutron matter: SRG

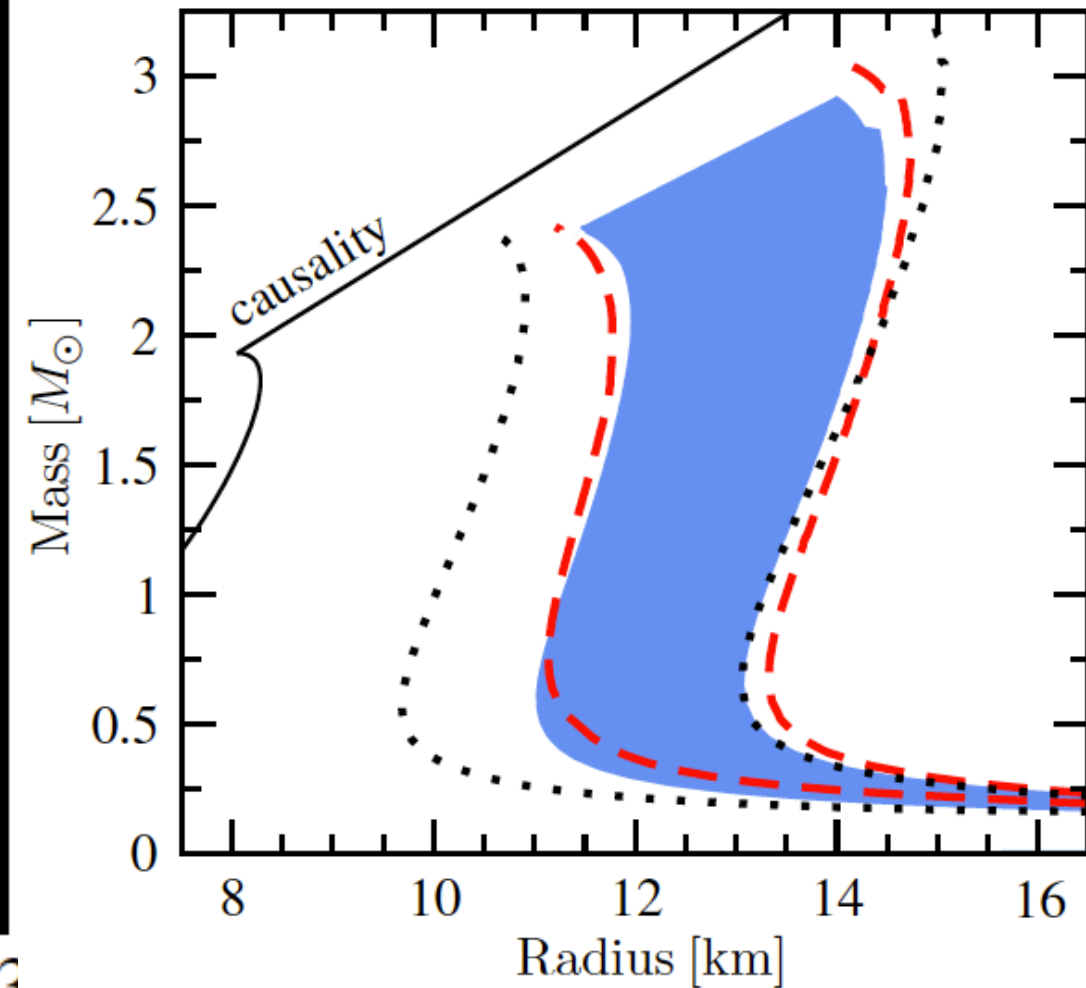
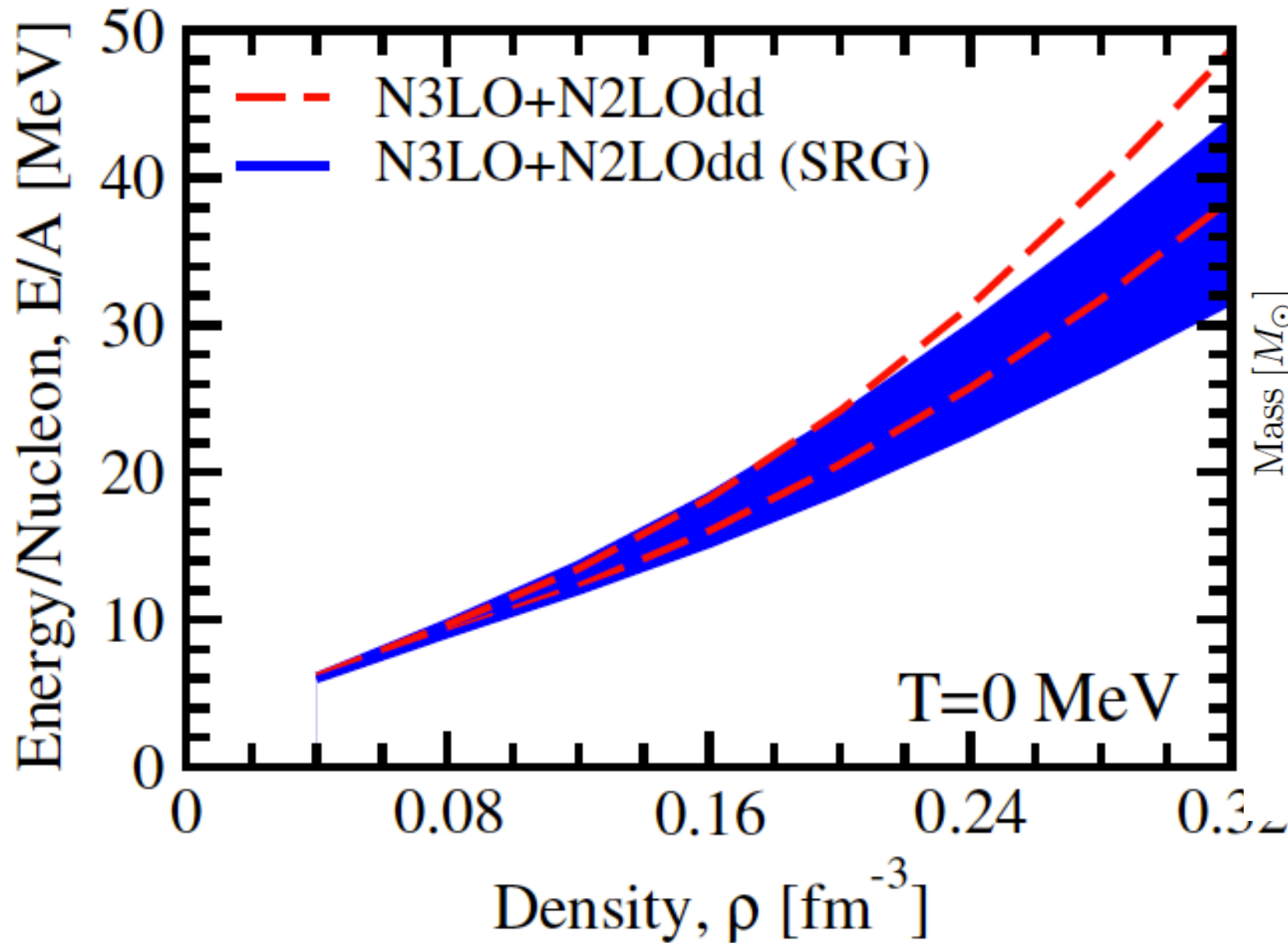


Hebeler, Lattimer, Pethick, Schwenk
ApJ **773** 11 (2013)

- **Error band** from unknown ChPT c_1, c_3 parameters
- Finite temperature & **higher densities available**

Neutron matter

EoS for neutron matter: SRG

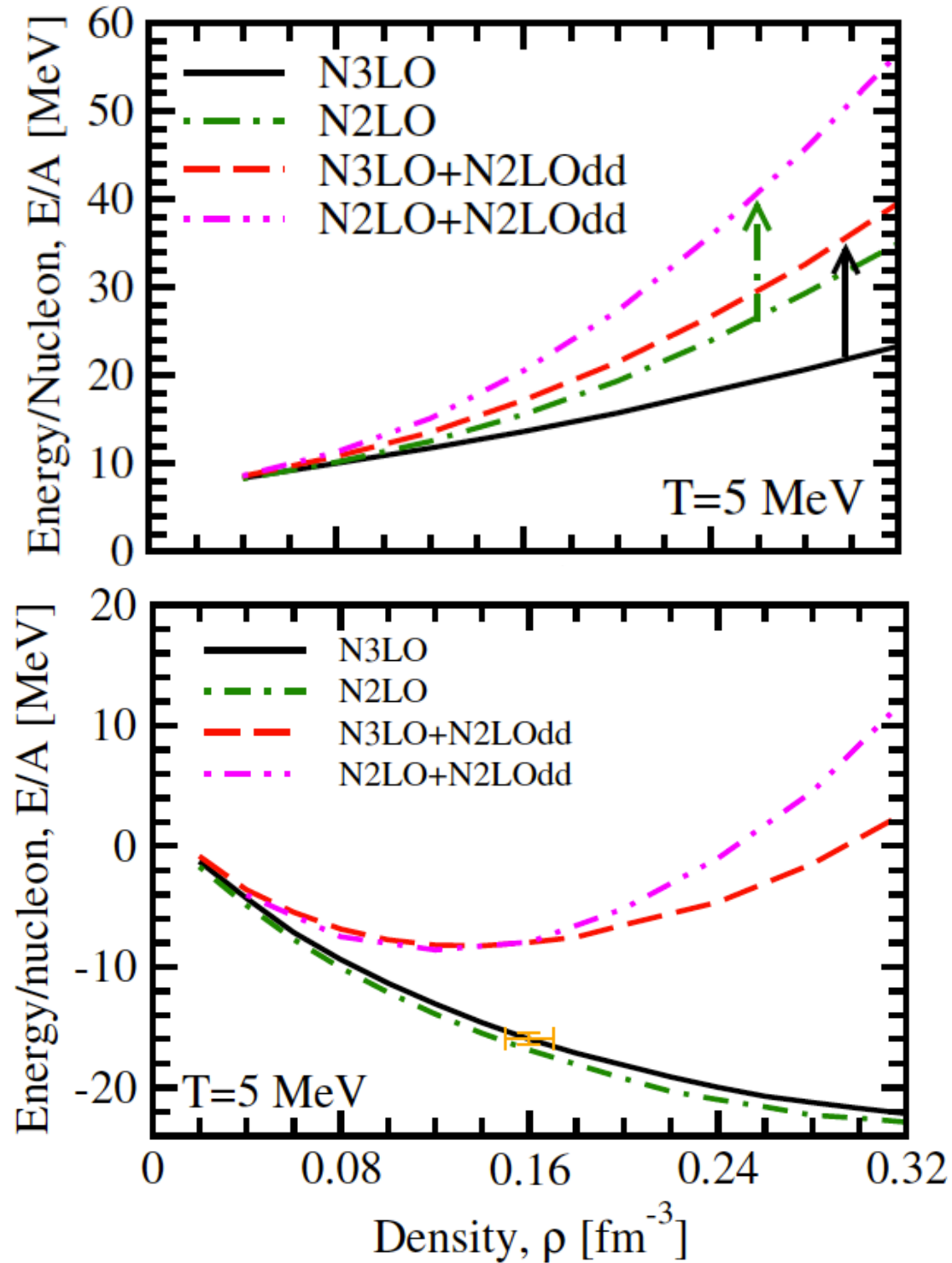


Hebeler, Lattimer, Pethick, Schwenk
ApJ **773** 11 (2013)

- **Error band** from unknown ChPT c_1, c_3 parameters
- Finite temperature & **higher densities available**

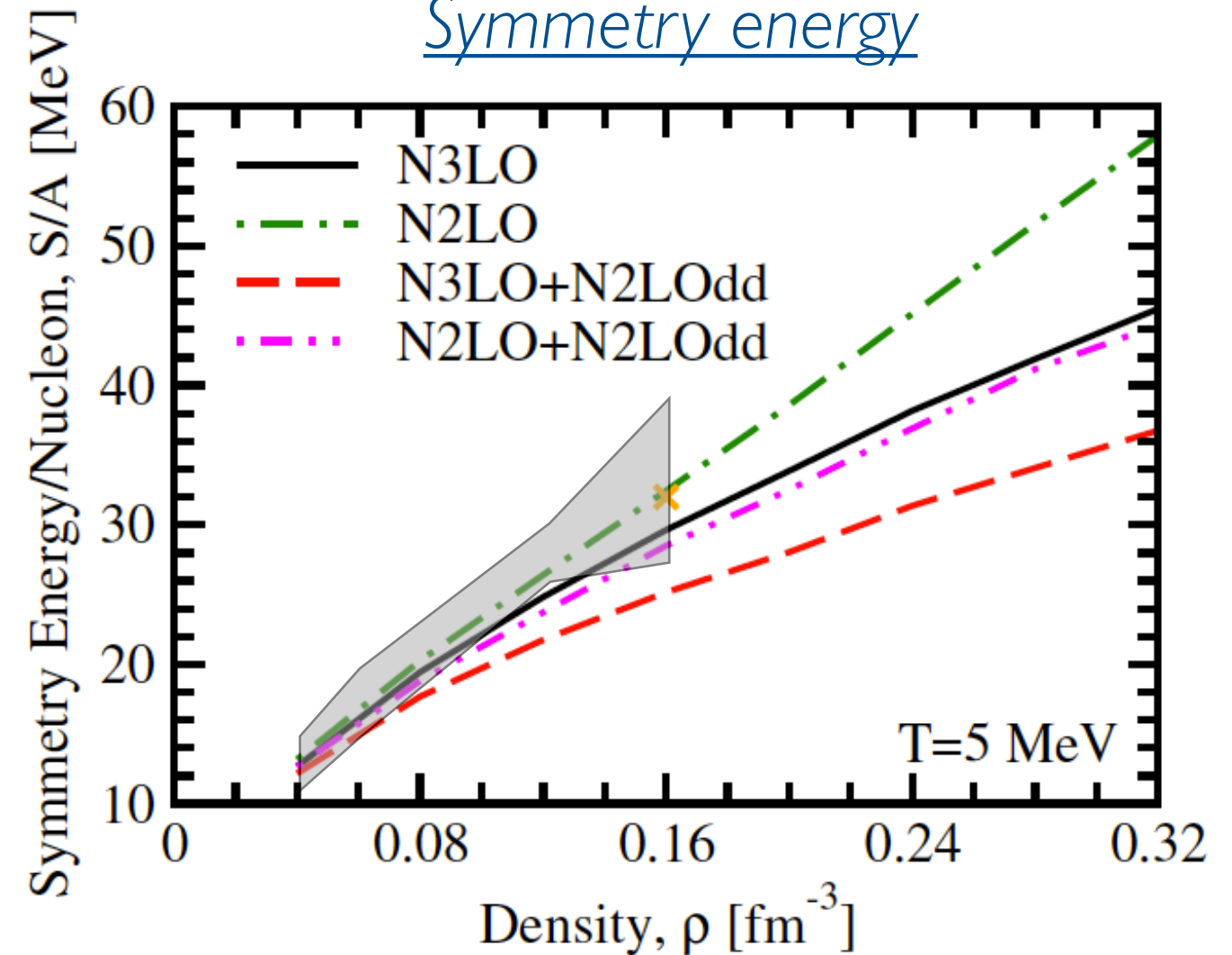
Isovector properties

EoS for SNM & PNM



$$S(\rho) = E_{PNM}(\rho) - E_{SNM}(\rho)$$

Symmetry energy

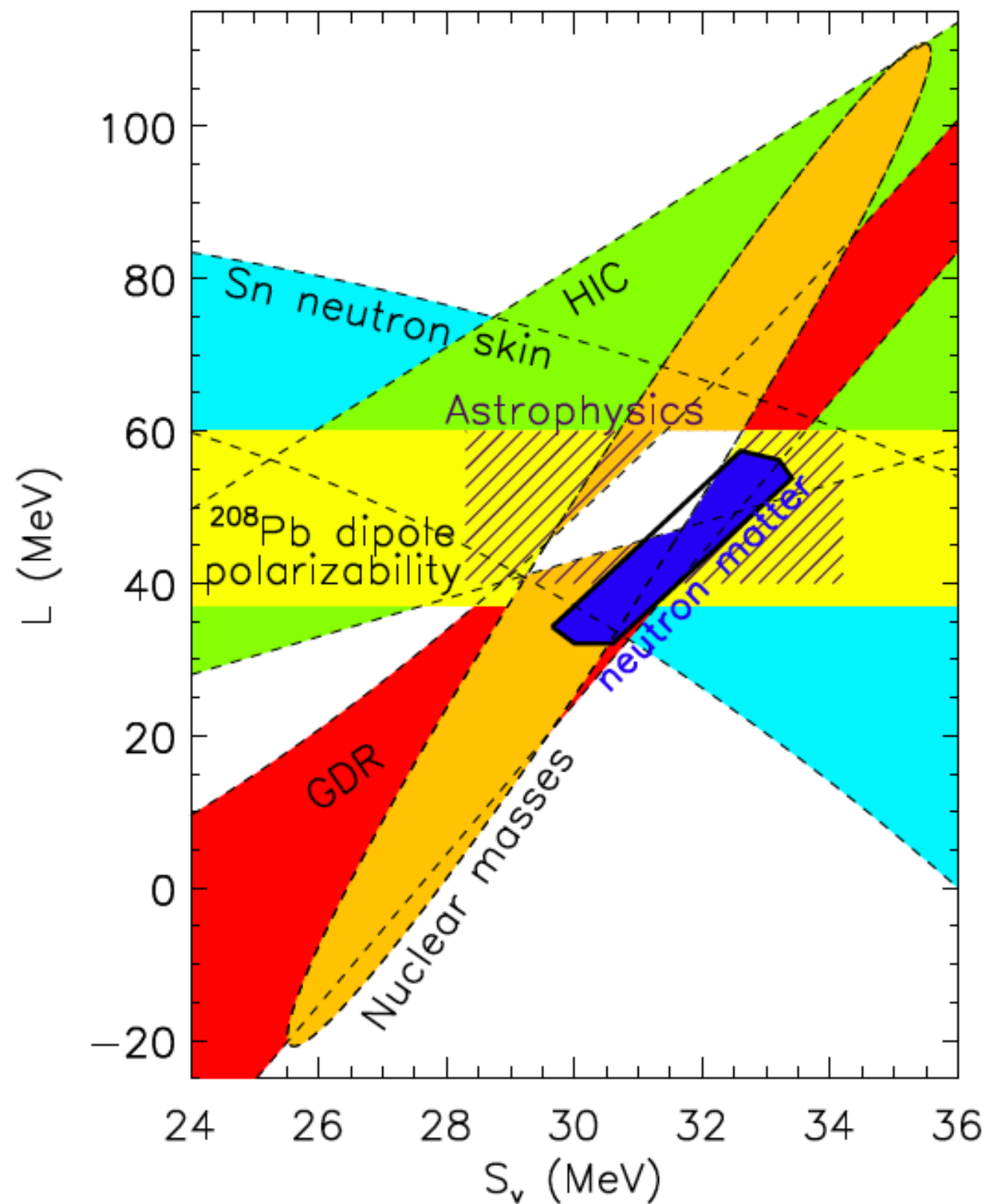
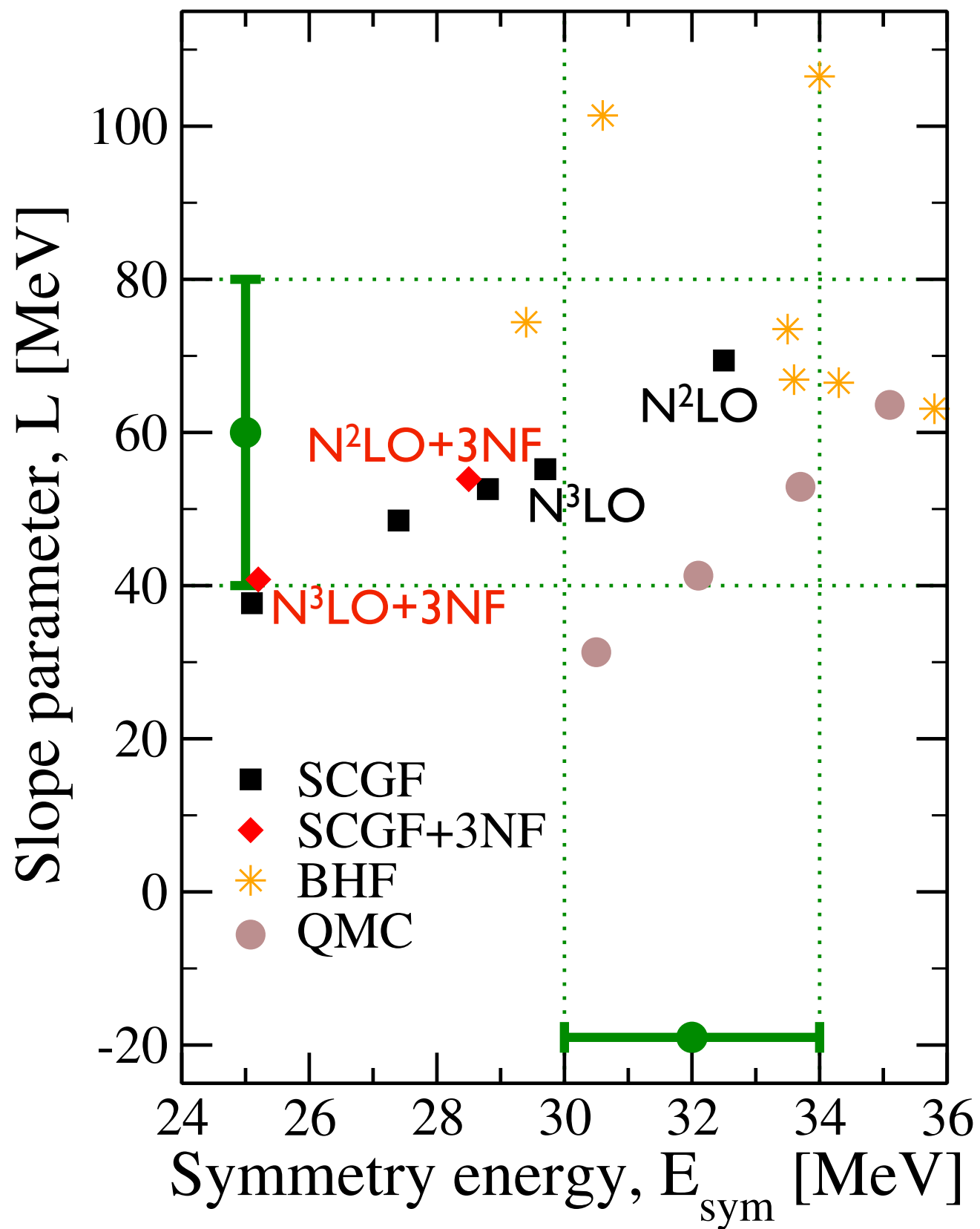


$\rho_0 = 0.16 \text{fm}^{-3}$	E_{PNM}/A	E_{SNM}/A	S/A	L
N3LO	13.6	-16.0	29.6	52.9
N2LOopt	15.6	-16.9	32.5	69.4
N3LO+N2LOdd	17.2	-7.99	25.2	40.8
N2LOopt+N2LOdd	20.5	-7.96	28.5	53.9

Comparison to phenomenology

Correlations from nuclear theory

Experimental constrains

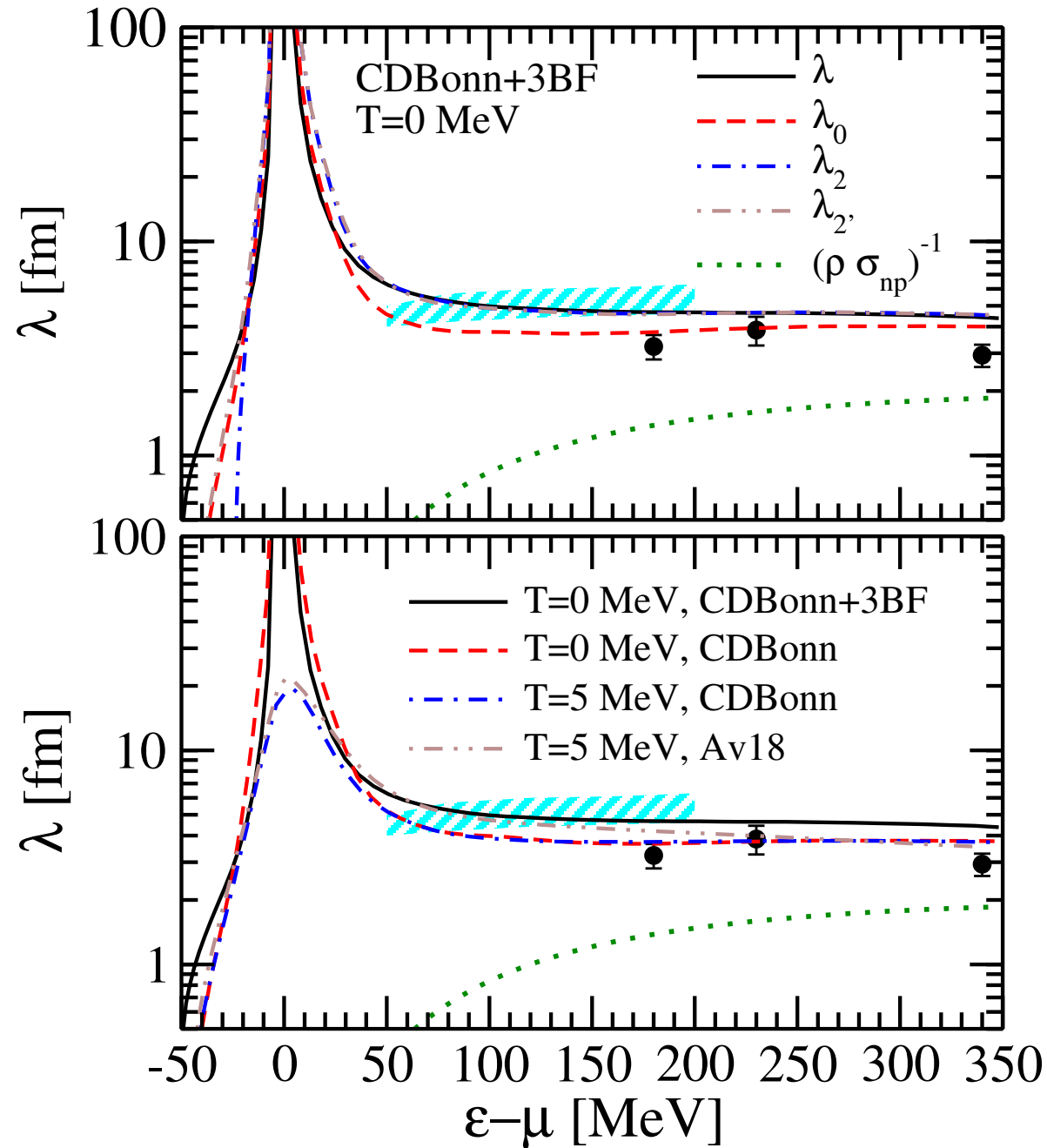


Lattimer & Lim, *Apj* **771** 51 (2013)

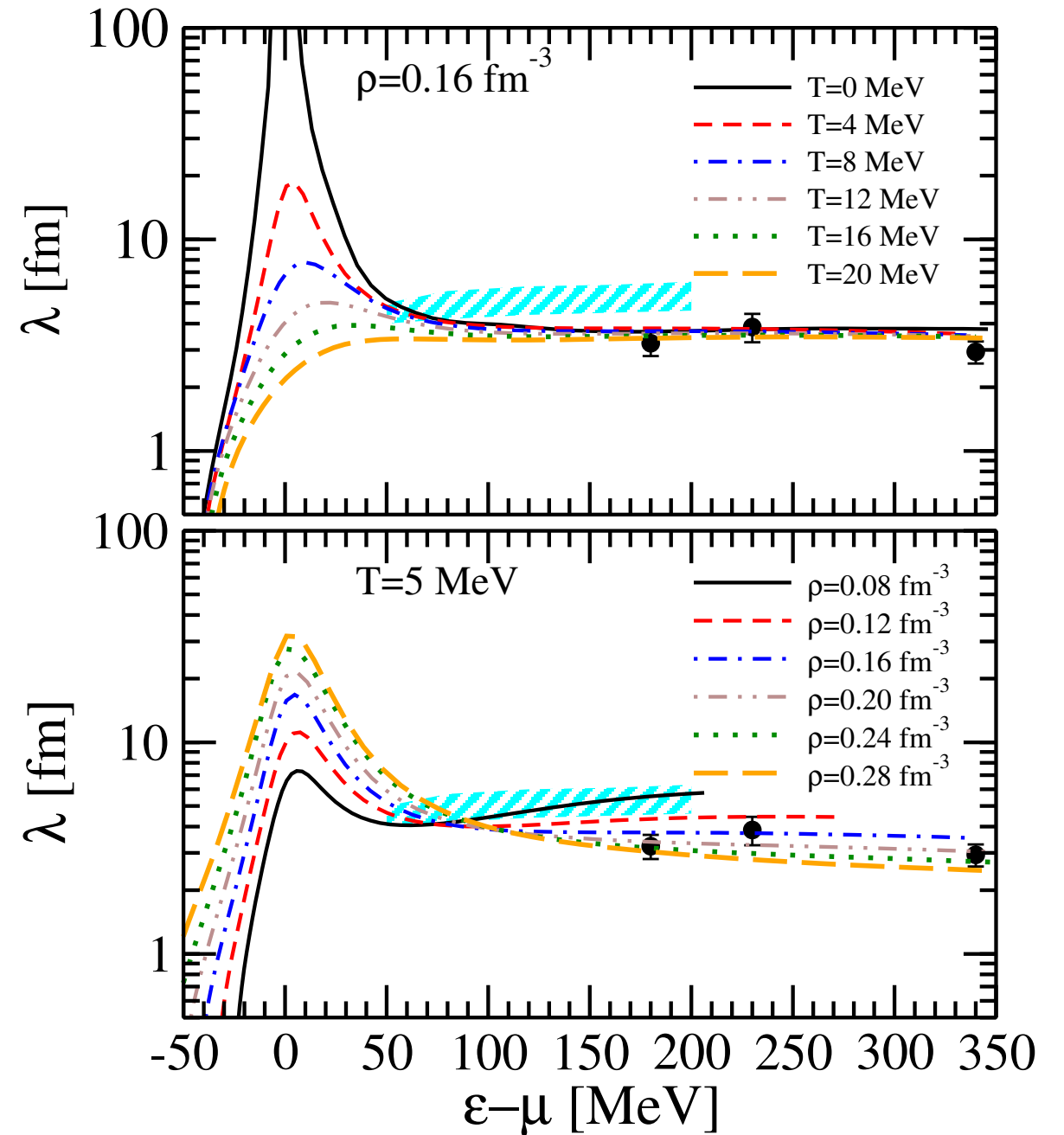
Transport properties

Nucleon mean-free path

Symmetric matter, $\rho=0.16 \text{ fm}^{-3}$



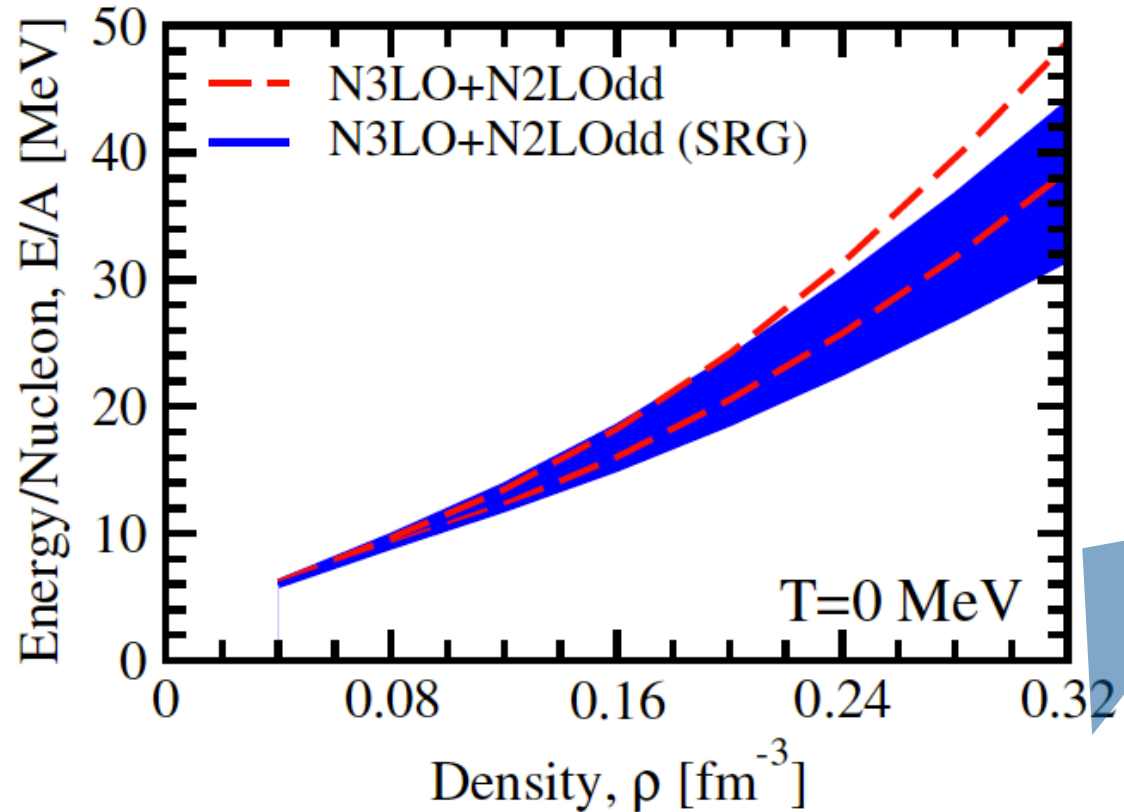
CD-Bonn



- Compatible with pA experiments
- Small model dependence

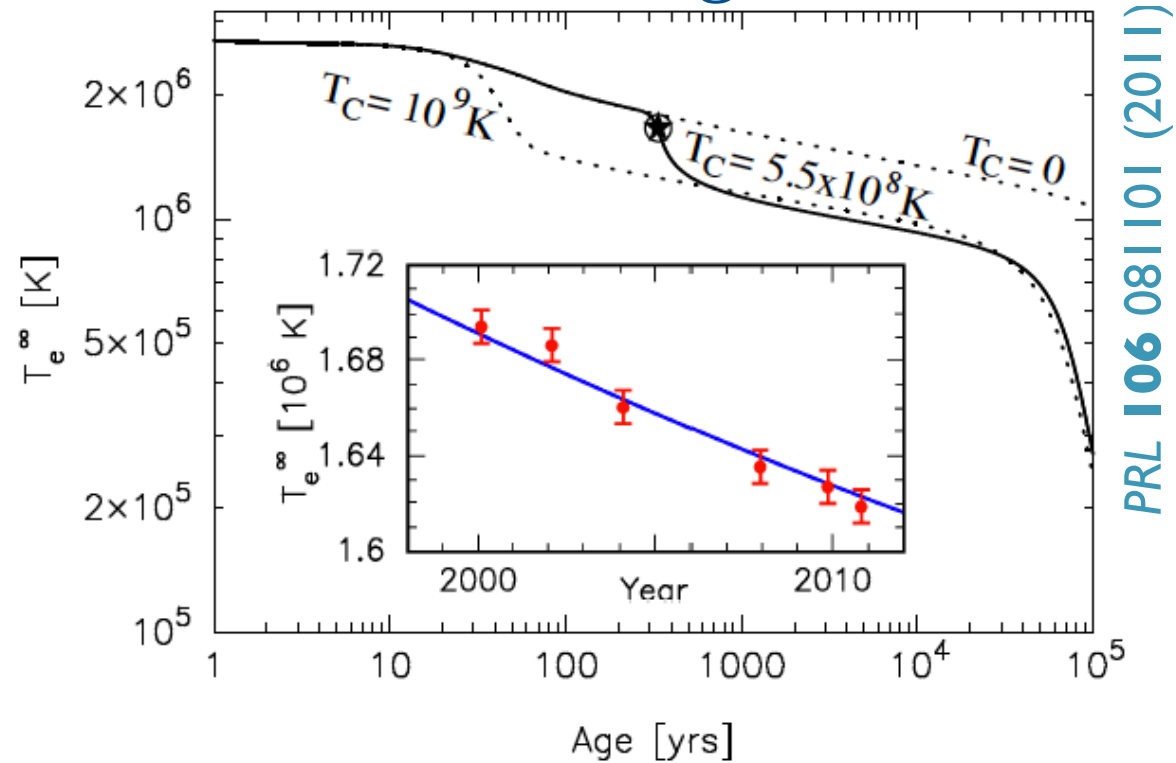
Chiral EoS & pairing gaps

N^3 LO EoS with 3BFs

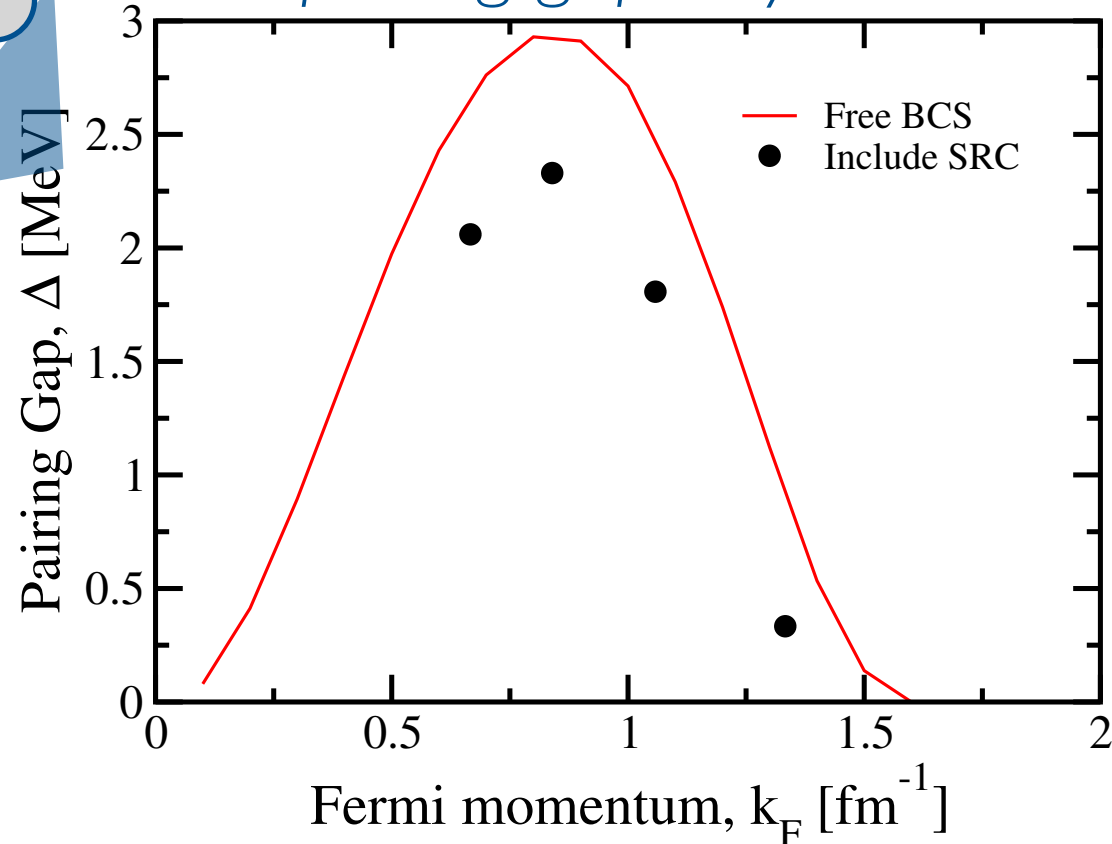


Chiral NN & 3N forces

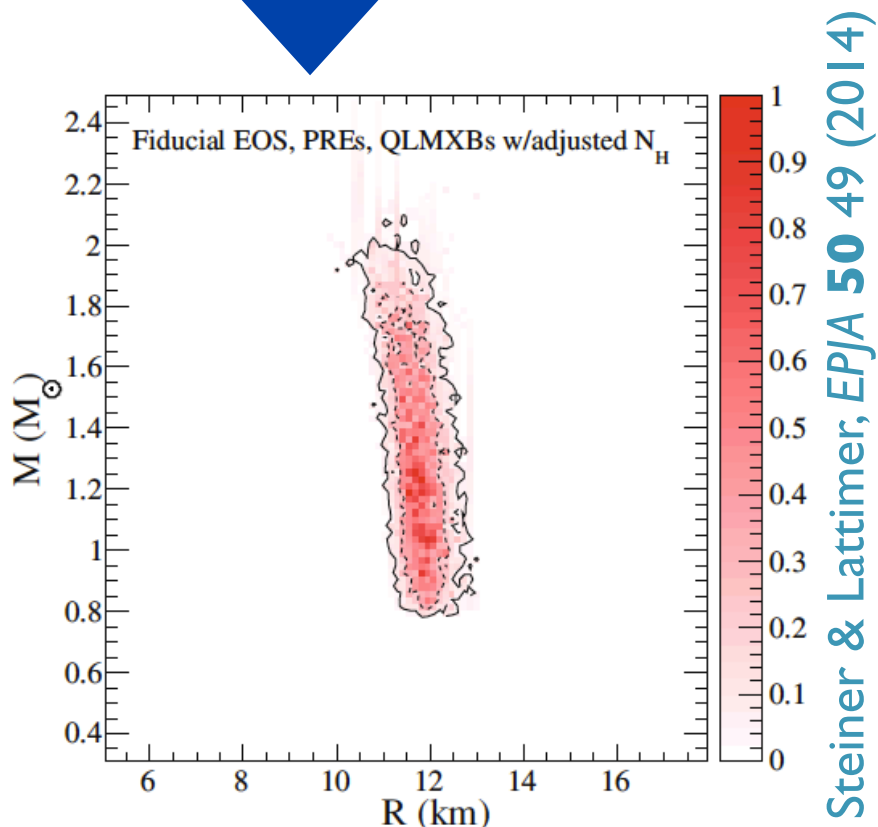
CasA cooling curve



N^3 LO pairing gap: beyond BCS

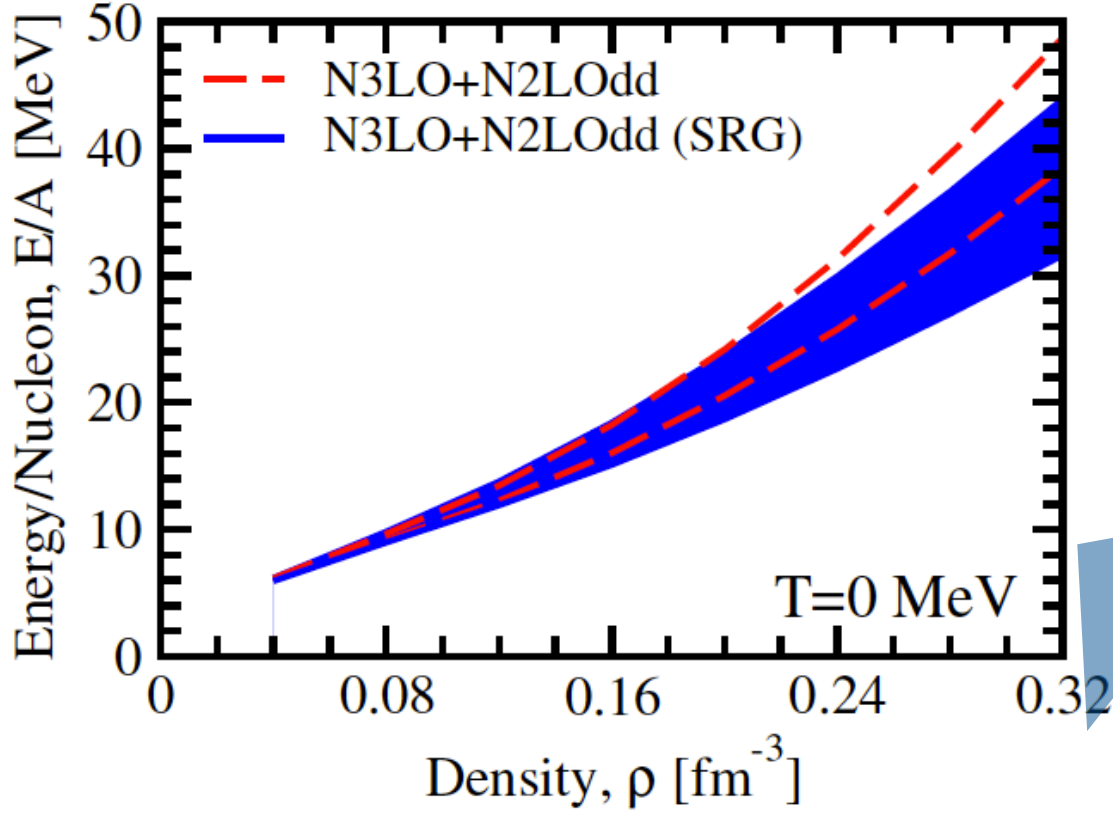


Dickhoff, Rios et al., in preparation 19



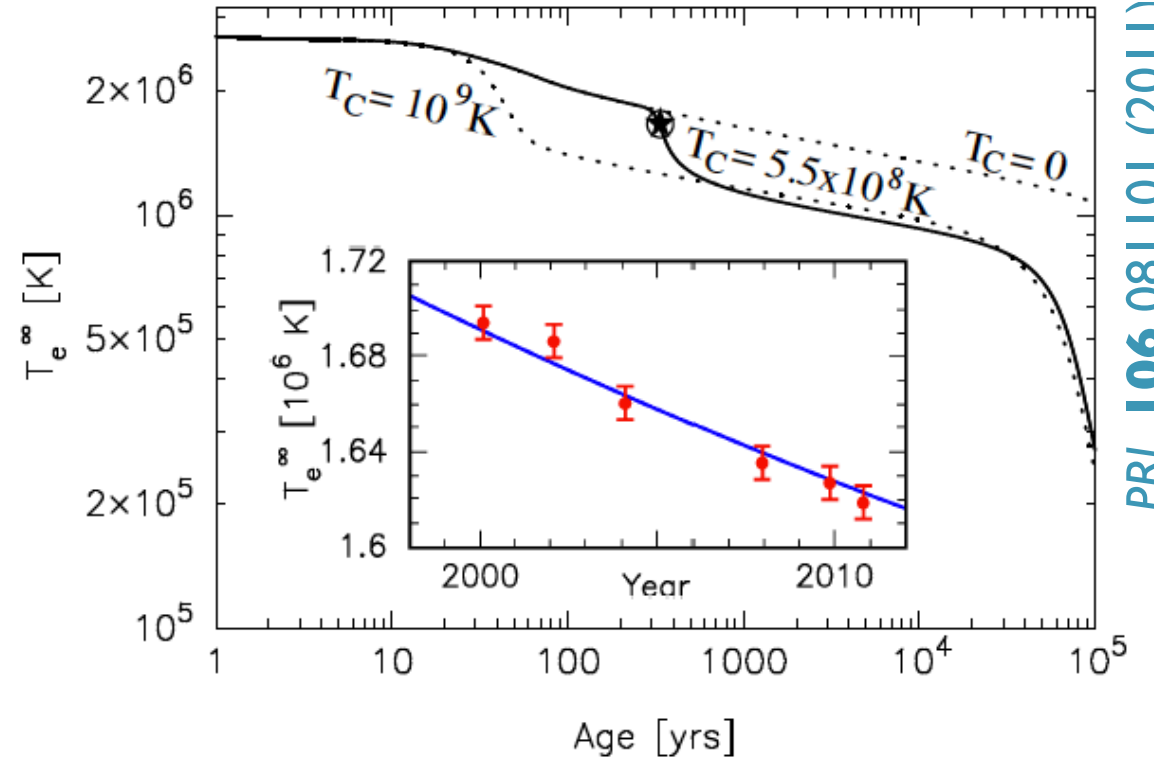
Chiral EoS & pairing gaps

N^3 LO EoS with 3BFs



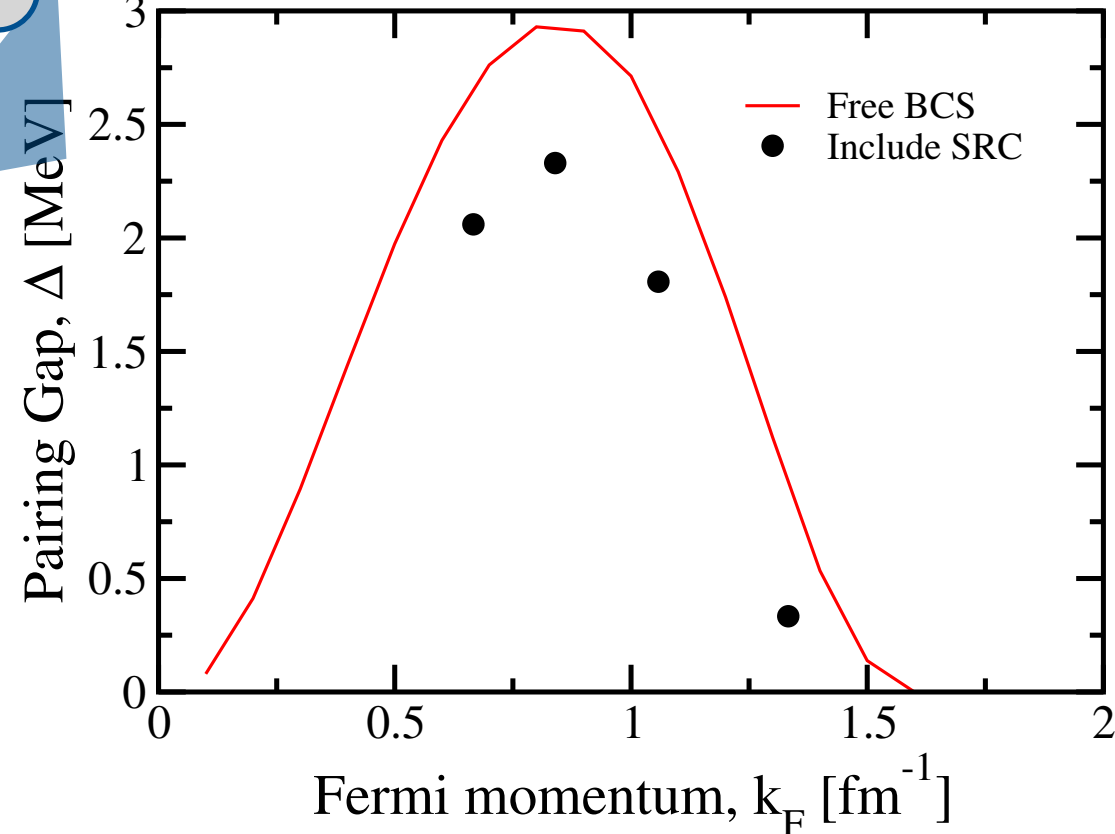
Chiral NN & 3N forces

CasA cooling curve

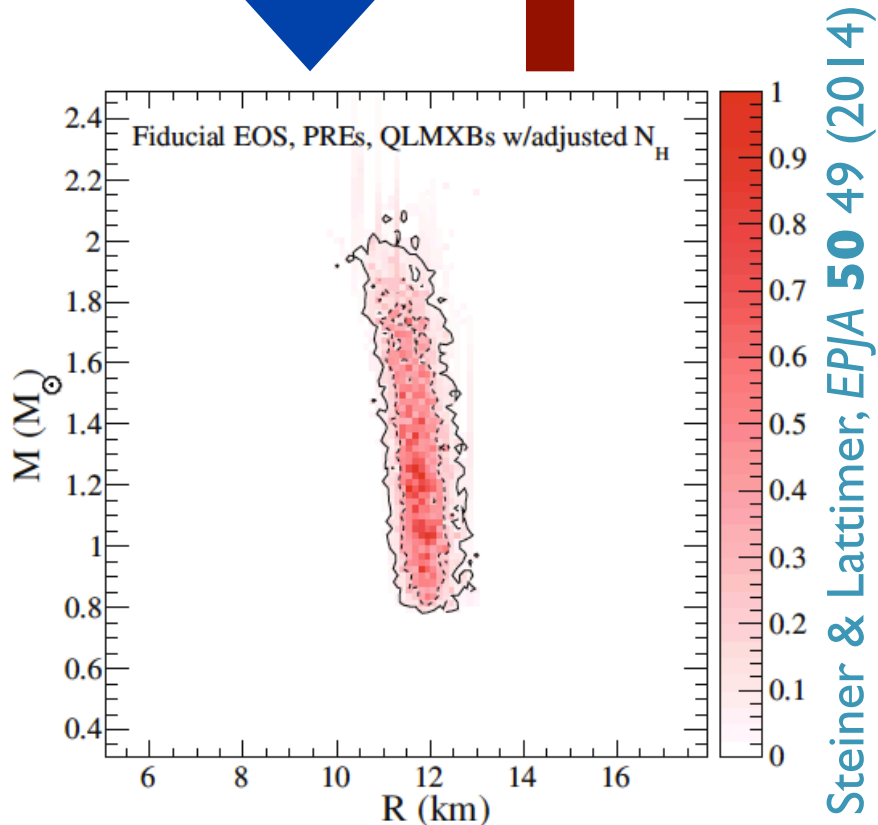


PRL 106 081101 (2011)

N^3 LO pairing gap: beyond BCS



Dickhoff, Rios et al., in preparation 19



- Ab initio nuclear **theory** is expanding
- Neutron star physics is **relevant** for this **endeavor**
- **Many-body** forces can now be **accessed**
- **Micro, macro**, transport, pairing properties on-going
- Hopefully a **coherent** picture will come out!

Thank you!



a.rios@surrey.ac.uk



Science & Technology
Facilities Council