

*Trapping-related negative feedback
as the reason for collected charge restriction
in heavily irradiated Si detectors
operating with avalanche multiplication*

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Outline

- ◆ Motivation
- ◆ PTI model of Q_c enhancement in irradiated Si detectors
- ◆ Restriction on collected charge arisen from negative feedback in irradiated Si detectors: comparison with “Quasi-APD”
- ◆ Stabilization of $E(x)$ in irradiated Si n-on-p strip detectors
- ◆ Gain in Q_c in detectors with various thickness
- ◆ Comparison with experimental data

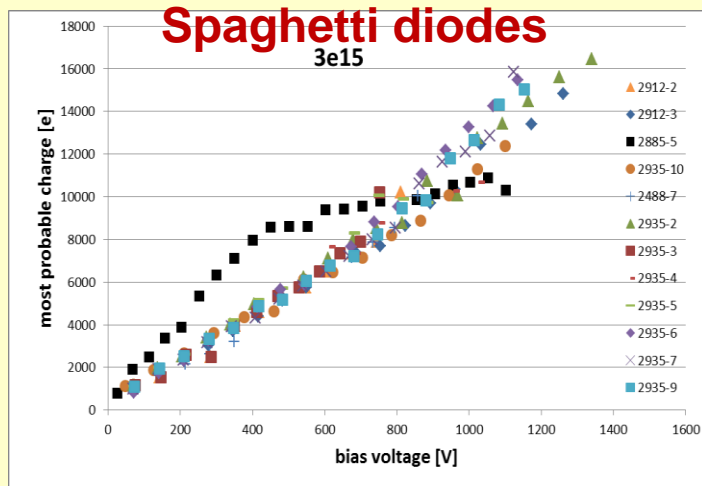
Conclusions

Motivation

Experimental results of RD50

Detector design:

strip n-on-p Q_{cmax}/Q_{mip} 1.5 – 1.8;
pad (Epi p-on-n) 6-9
(e-h near the surface)



Almost no difference in charge collection efficiency for different implants

Extended fluence range

- up to 10^{17} n_{eq}/cm² (2013)
- stable operation

Our calculation

n-on-p, strip
 Q_{cmax}/Q_{mip} 1.5 – 1.9
- as in the experiments

Relatively low!

Avalanche PhotoDiodes (APD)

High electric field + impact ionization -
 E – hundreds kV/cm, internal gain ~200
(Hamamatsu) and even more

What is the origin of restriction on Q_c gain in heavily irradiated Si n-on-p strip detectors?

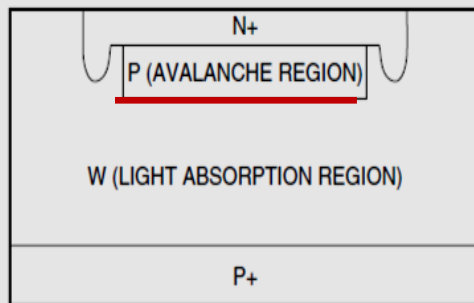
Origin of Q_c restriction: comparison with imaginary "APD"

Hamamatsu APD

Read structures

$I \sim 20 \text{ pA}$ ($\varnothing 1.5 \text{ mm}$)

E – hundreds kV/cm



Irradiated detector is compared with imaginary structure - "Quasi-APD":

- ◆ n-on-p strip diode
- ◆ $E(x)$ as in heavily irradiated detector (high V)
- ◆ carrier avalanche multiplication
- but**
- ◆ no injection and trapping of holes
- ◆ $\tau_{tr} = 1 \text{ ms}$ (no trapping of nonequilibrium carriers)

Q_c enhancement:

$$K_{enh} = Q_{cmax}/Q_{mip}$$

In n-on-p strip detectors

$$K_{enh} = 1.5-1.9 -$$

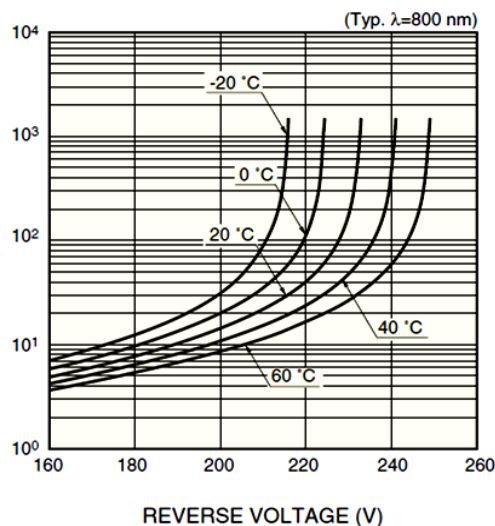
our calculation and experiment

Internal gain

$$G = Q_{am}/Q_o$$

Q_o - signal induced on the strip, calculated without avalanche multiplication

Q_{am} - signal measured or calculated in the same detector with avalanche multiplication



Goal

- ✓ Finding the **origin of restriction** on the collected charge enhancement (gain in collected charge) in heavily irradiated Si n-on-p strip detectors
by simulation $E(x)$ and Q_c and comparison with Quasi-APD
- structure different from classic APD and LGAD

Results are published in:

E. Verbitskaya, et al., NIM A 730 (2013) 66

PTI model of Q_c enhancement due to avalanche multiplication in heavily irradiated n-on-p Si strip detectors

The PTI model considers:

- ✓ formation of Double Peak (DP) electric field profile – DP $E(x)$;
 - ✓ focusing of the electric field and current near the collecting n^+ strips;
 - ✓ avalanche hole generation near the n^+ strips, hole injection into the detector bulk, and hole trapping to radiation-induced deep levels defects
- give rise to the **negative feedback** which stabilizes the avalanche multiplication and total detector performance

V. Eremin, et al., *14 and 15 RD50 workshops, 2009, Freiburg and Geneva*

V. Eremin, E. Verbitskaya, A. Zabrodskii, Z. Li, J. Härkönen, *NIM A 658 (2011) 145*

E. Verbitskaya, V. Eremin, A. Zabrodskii, 2012, *J. Instrum.*, v.7, 2, ArtNo: C02061;
doi: 10.1088/1748-0221/7/02/C02061

E. Verbitskaya, et al., *NIM A 730 (2013) 66*

E. Verbitskaya, et al., 23 RD50 workshop, Nov 13-15, 2013, CERN

PTI model of Q_c enhancement via avalanche multiplication and negative feedback

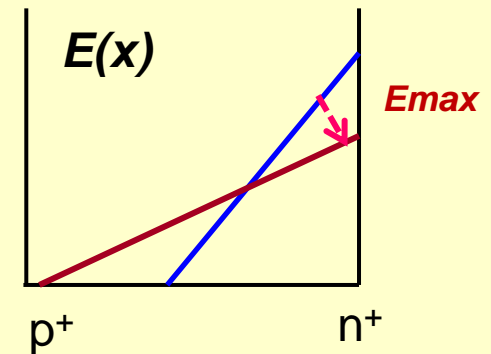
Equilibrium carriers			High bias voltage			Nonequilibrium carriers		
source/ origin	process	characteristic /result		process	characteristic /result	source/ origin	process	characteristic /result
Bulk genera- tion current	Trapping to DLs	I_{bgen} ; steady-state DP $E(x)$	Junction region with high E ; focusing	Impact ioniza- tion, carrier injection into the bulk, trapping to DLs	I_{bgen} increase; Change of steady-state DP $E(x) \rightarrow$ E reduction near the junction	Gene- rated by parti- cles	Trapping to DLs during drift in $E(x)$	$\tau_{tr}(F)$; pulse response, Q_c (CCE)
				Trapping – related negative feedback				

$E(x)$ changes via trapping-related negative feedback

Negative feedback in n-on-p detectors:

- ◆ impact ionization near n^+ (e, h)
- ◆ hole injection
- ◆ hole trapping to DLs

- ◆ reduction of $-N_{eff}$
- ◆ reduction of dE/dx and E_{max} at n^+
- ◆ **reduction of $\alpha_{e,h}$**



Trapping-related negative feedback:

- ◆ stabilizes avalanche multiplication and total detector performance

BUT

- ◆ simultaneously restricts Q_c enhancement

Trapping-related or Space Charge Limited Current negative feedback

Algorithm of $E(x)$ and Q_c simulation

Processes considered:

- ✓ formation of a steady-state $E(x)$ distribution:
equilibrium carriers (bulk generation current) and avalanche generated carriers near n^+ strips, their trapping on radiation-induced DL defects;
- ✓ charge collection in the detector bulk with a calculated $E(x)$ profile;
- ✓ e and h are generated by MIPs

Procedure and main parameters

- ◆ Poisson equation combined with the rate equation
- ◆ one-dimensional approach for detector geometry
- ◆ Effective deep levels: DA $E_c - 0.53$ eV; DD $E_v + 0.48$ eV
- ◆ $1/\tau_{e,h} = \beta_{e,h} F_{eq}$; $\beta_e = 3.2 \times 10^{-16} \text{ cm}^2 \text{ ns}^{-1}$, $\beta_h = 3.5 \times 10^{-16} \text{ cm}^2 \text{ ns}^{-1}$
- ◆ ionization rates $\alpha_{e,h} = A_{e,h} \exp(-B_{e,h}/E)$
(A and B from B. J. Baliga, *Modern Power Devices*, Hoboken, NJ; Wiley, 1987)

◆ numerical calculation

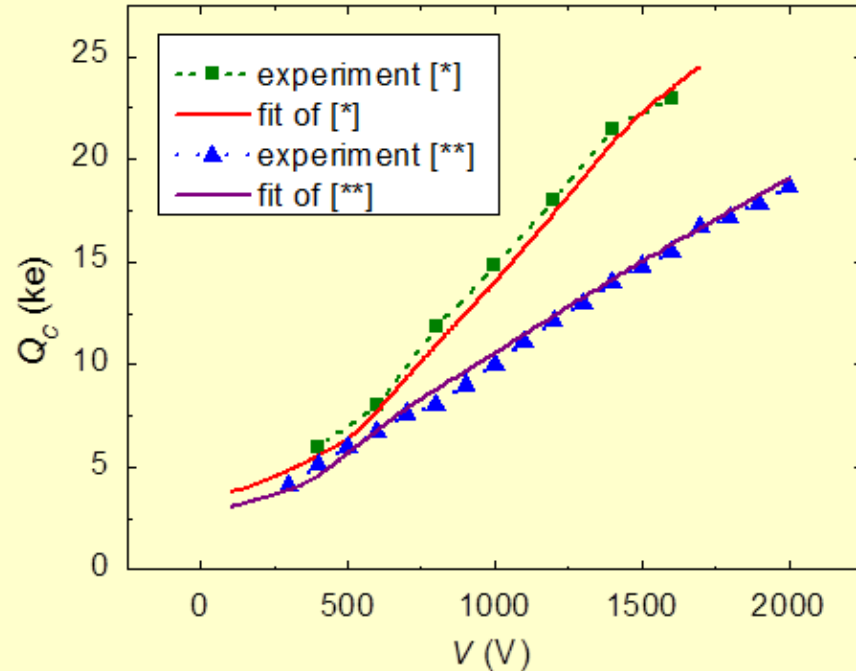
Simulation of Q_c enhancement

Variable parameters

- ◆ detector bias voltage V ,
- ◆ temperature T in the LHC range,
- ◆ irradiation fluence F ,
- ◆ strip detector **geometry** (strip width, detector thickness)

Starting point for simulation –

fit to the curve [*] with maximal Q_c :
 $F = 3 \times 10^{15} \text{ n}_{\text{eq}}/\text{cm}^2$, $T = -20\text{C}$



* I. Mandić, et al., NIM A 612 (2010) 474

** G. Casse, Recent developments in silicon detectors, 13th VCI, Feb 11-15, 2013 Vienna;
<http://vci.hephy.at>

Options for $E(x)$ and Q_c simulations

#	Possible values	K_{aval}	K_{inj}	m_j	τ_{tr}
		1/0	1/0	$1/1 \times 10^{-4}$	$\tau_{tr}(F)/1 \text{ ms}$
1	Detector, no multiplication	0	1/0	1	$\tau_{tr}(F)$
2	Detector, with multiplication	1	1	1	$\tau_{tr}(F)$
3	Detector, with multiplication, NO feedback	1	0	1	$\tau_{tr}(F)$
4	Quasi-APD 1	1	0	1	1 ms
5	Quasi-APD 2	1	0	1×10^{-4}	1 ms

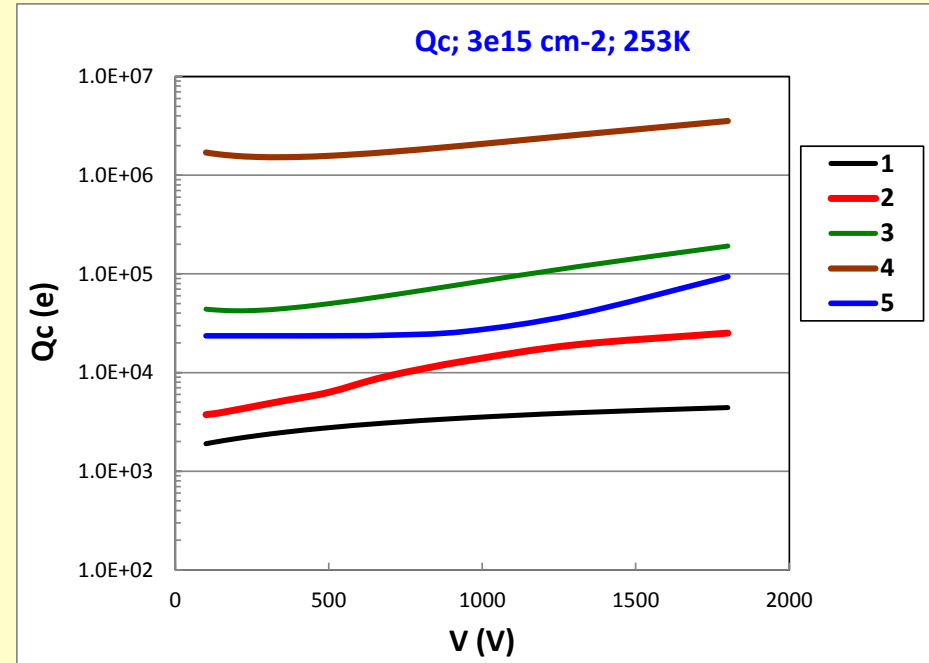
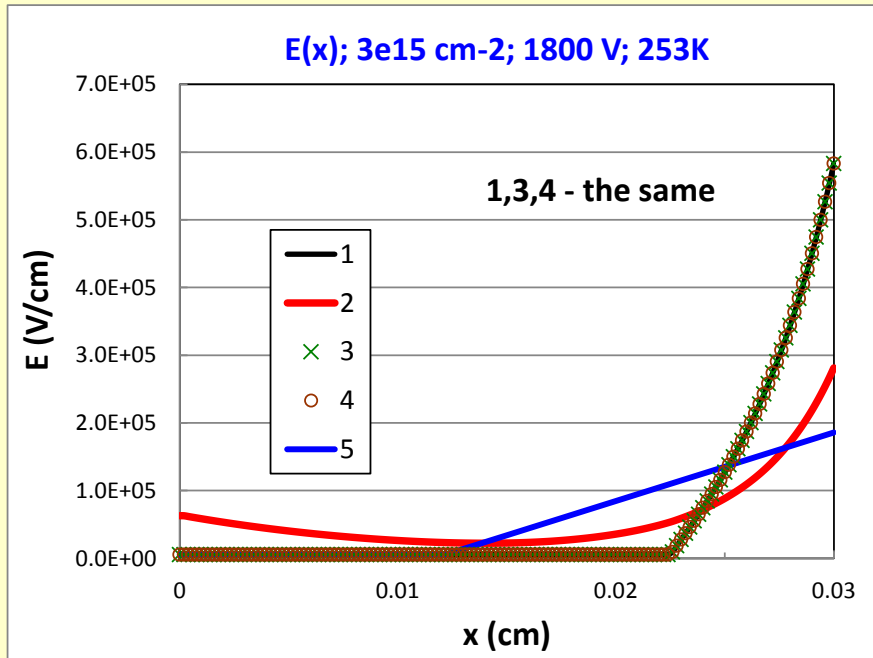
K_{aval} – avalanche multiplication

K_{inj} - injection of avalanche generated holes

m_j - current generation rate

Allows differentiation between impact of different factors - $E(x)$ profile, current generation rate, trapping

Comparative results on $E(x)$, Q_c and G



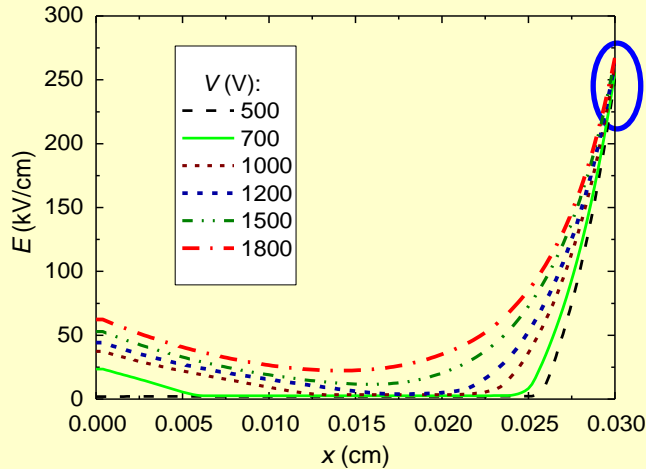
1	Detector, no multiplication	1
2	Detector, with multiplication	5.7
3	Detector, with multiplication, no feedback	43
4	Quasi-APD 1	800
5	Quasi-APD 2	21

Gain at
1800 V

n-on-p strip detector; $d = 300 \mu\text{m}$;
pitch/strip width 80/20 (μm)
 $F = 3 \times 10^{15} \text{ n}_{\text{eq}}/\text{cm}^2$

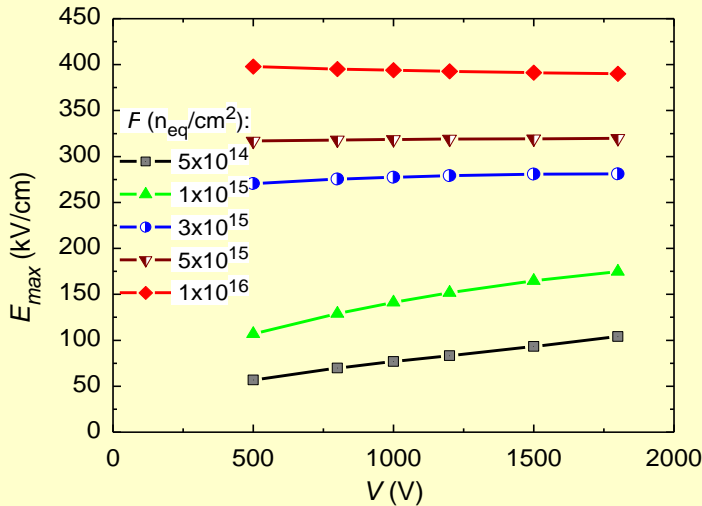
$E(x)$ stabilization at different V and F due to negative feedback

$$F = 3 \times 10^{15} \text{ n}_{\text{eq}}/\text{cm}^2$$

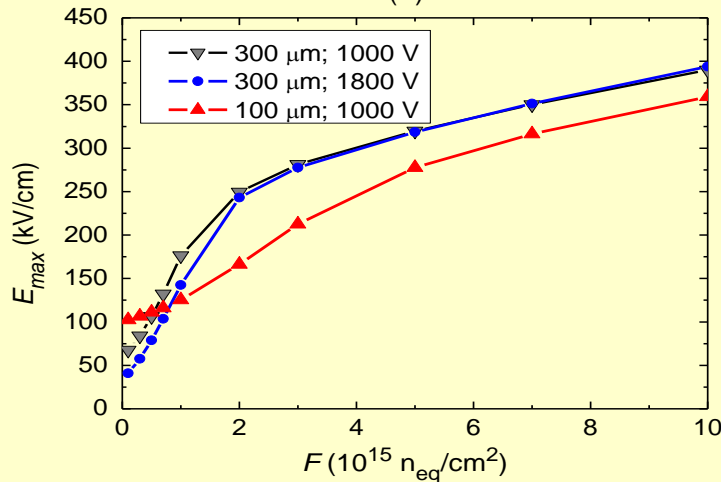


- ✓ DP $E(x)$ in avalanche multiplication mode
- ✓ E_{max} at n^+ strip is stable
- ✓ E_{max} stability reduces sensitivity of Q_c to the design of the region with high E (shown in the experiments e.g. with spaghetti diodes).

Stabilization of E_{max} at n^+ strips

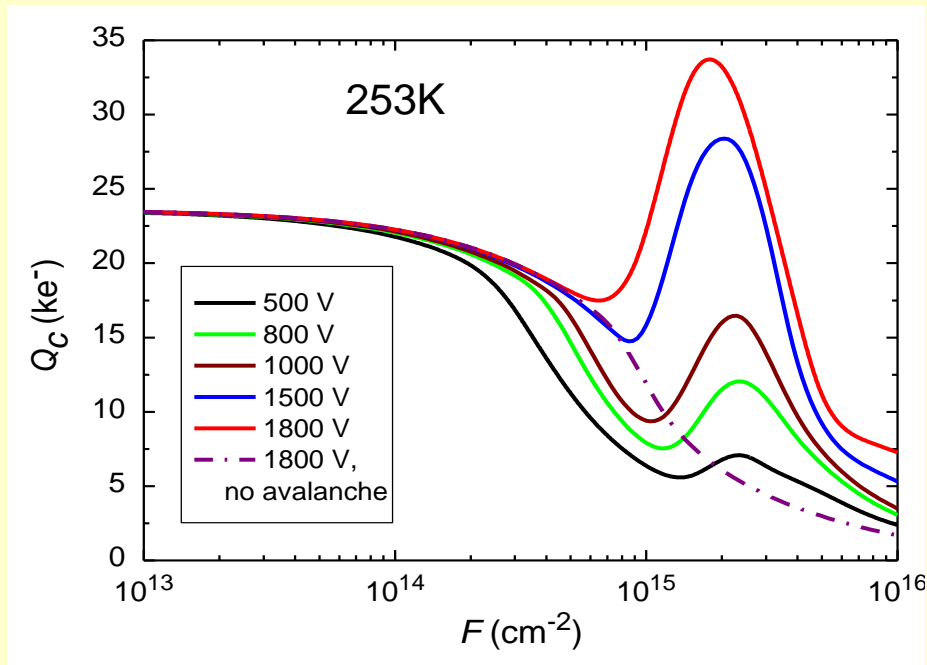


At $F > 1 \times 10^{15} \text{ cm}^{-2}$
 E_{max} is insensitive to V



At $F > 5 \times 10^{15} \text{ cm}^{-2}$
the difference in E_{max} in 300 μm and 100 μm detectors is not essential at fixed V

$Q_c(F)$ dependence in n -on- p strip detectors



- ✔ Q_c enhancement starts at ~ 500 V - DP $E(x)$ ($d = 300$ μm)
- ✔ $Q_c(F)$ is nonmonotonous and shows a **bump**
- ✔ Q_c in bump is larger than Q_{mip}

$$K_{enh} = Q_{cmax}/Q_{mip}$$

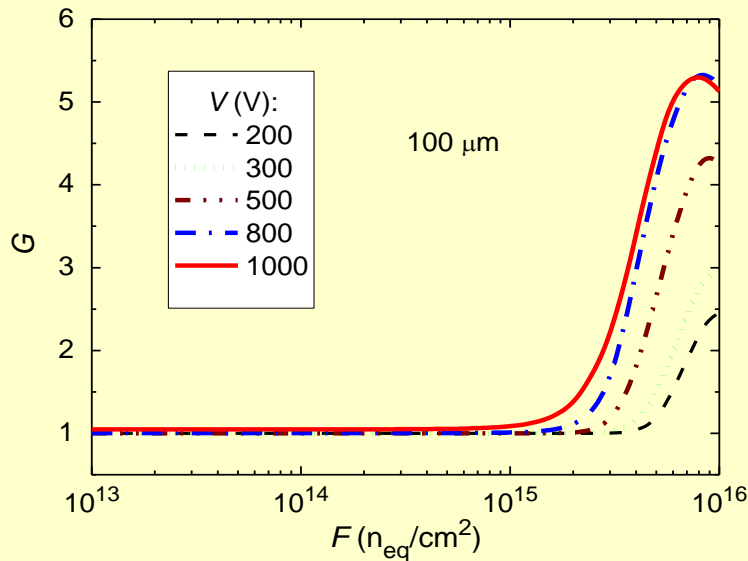
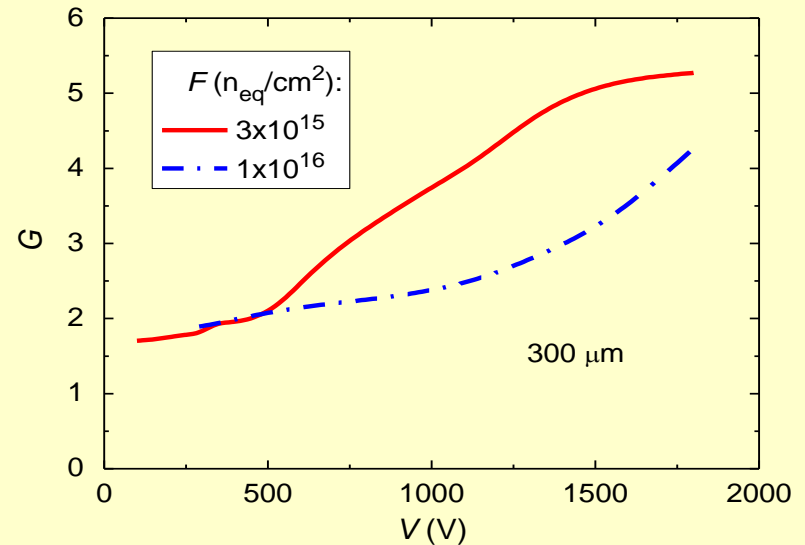
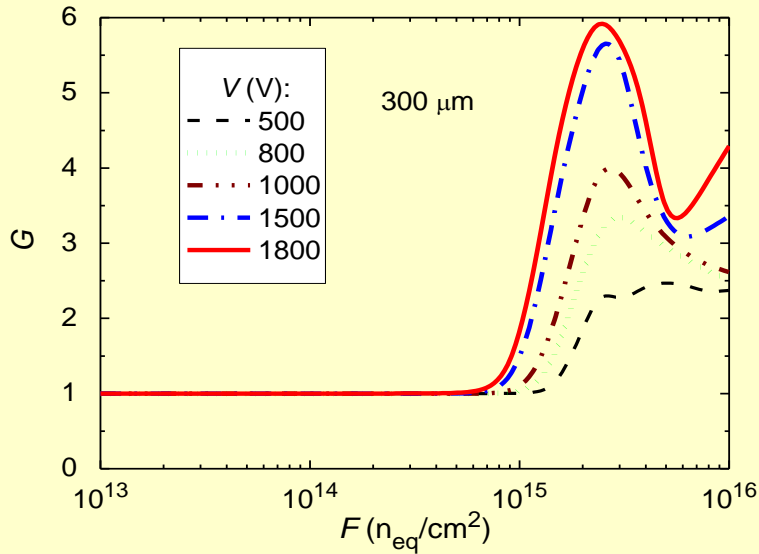
$$= 1.4 - 300 \mu\text{m}$$

$$1.9 - 100 \mu\text{m}$$

- agrees with experiment

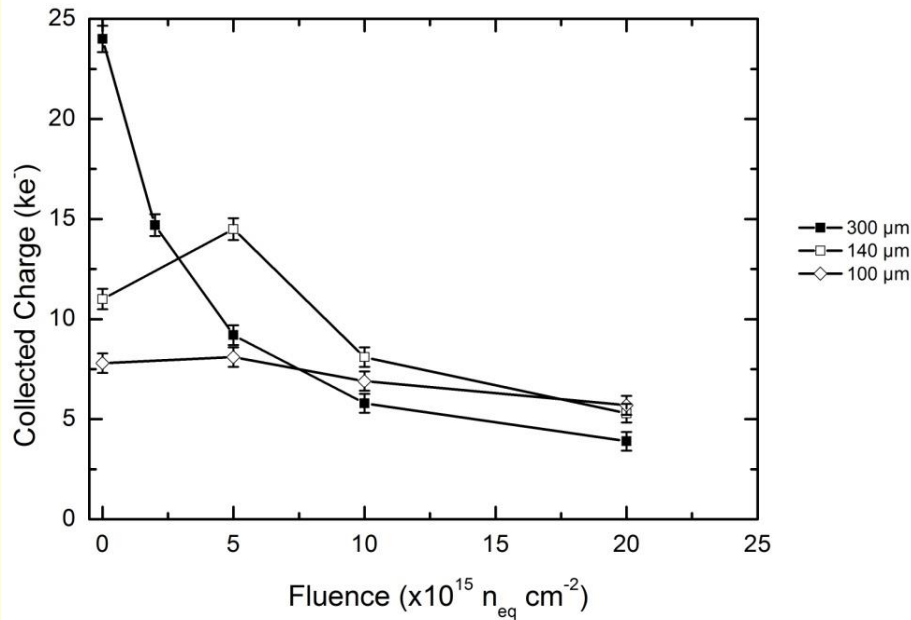
*E. Verbitskaya, et al., 2012, J. Instrum., v.7, 2
C02061*

Gain in strip detectors with various thickness



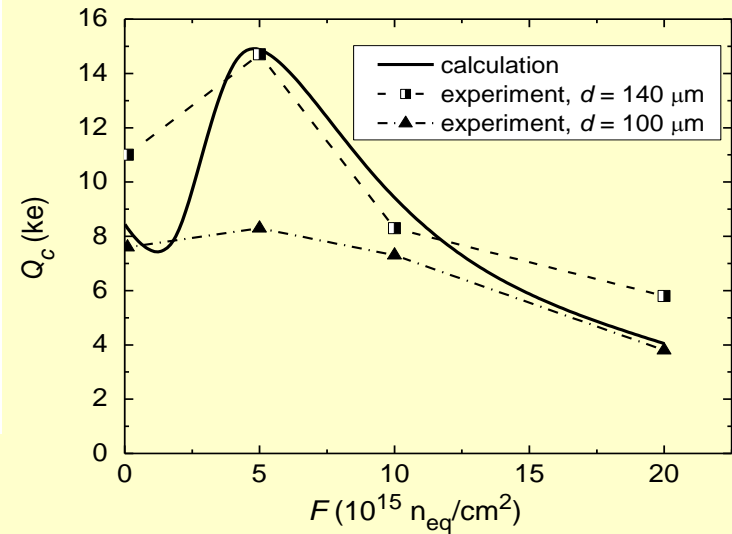
- Similar G in 300 μm and 100 μm detectors at highest V
- Maximum G is shifted to higher F in 100 μm detectors

Comparison with experimental results



G. Casse, 20th RD50 Workshop, Bari,
31/05-02/06 2012

Calculated $Q_c(F)$ with a bump
correlates to the experiment
for thin detectors



Conclusions

- ✔ Internal gain in collected charge due to avalanche multiplication is strongly suppressed and simultaneously stabilized by the trapping-related negative feedback which is a specific of detectors with high concentration of deep levels.
- ✔ The gain is in the range 1-6 for both standard and thin detectors, which defines the limit for the signal enhancement and operational fluence range.
- ✔ Trapping-related negative feedback makes the gain practically insensitive to the design of the detector high field region

Acknowledgments

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Thank you for attention!