



Clues to the identity of dark matter from simulations and observations

Carlos S. Frenk
Institute for Computational Cosmology,
Durham



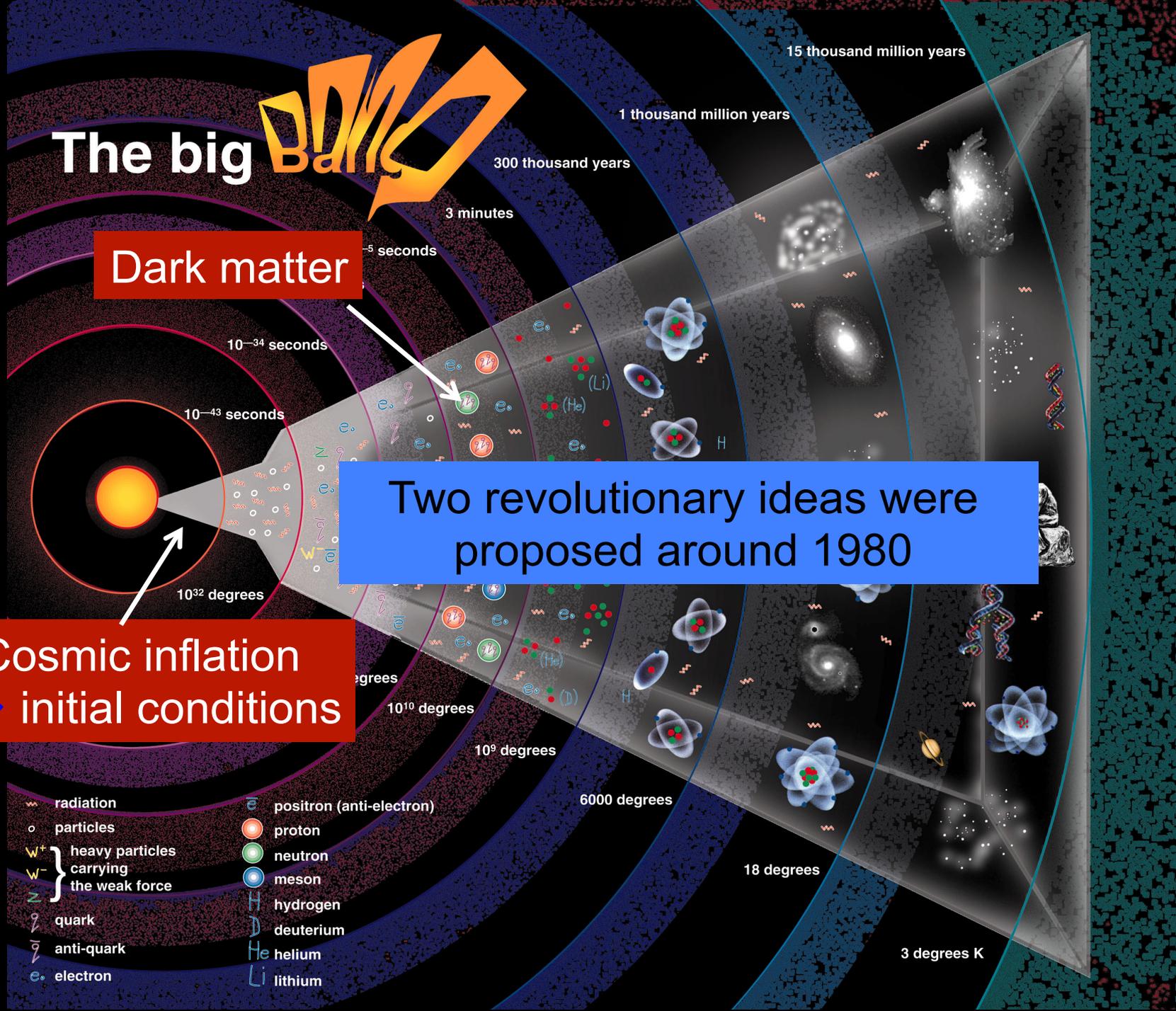
The big Bang

Dark matter

Two revolutionary ideas were proposed around 1980

Cosmic inflation
 → initial conditions

- ⋯ radiation
- particles
- W⁺ heavy particles carrying the weak force
- W⁻ } carrying the weak force
- Z } carrying the weak force
- q quark
- q̄ anti-quark
- e⁻ electron
- e⁺ positron (anti-electron)
- p proton
- n neutron
- M meson
- H hydrogen
- D deuterium
- He helium
- Li lithium



10⁻³⁴ seconds

10⁻⁴³ seconds

10³² degrees

3 minutes

300 thousand years

1 thousand million years

15 thousand million years

degrees

10¹⁰ degrees

10⁹ degrees

6000 degrees

18 degrees

3 degrees K

Non-baryonic dark matter candidates

Type

example

mass

hot	neutrino	a few eV
warm		keV-MeV
cold	axion neutralino	10^{-5} eV - 100 GeV



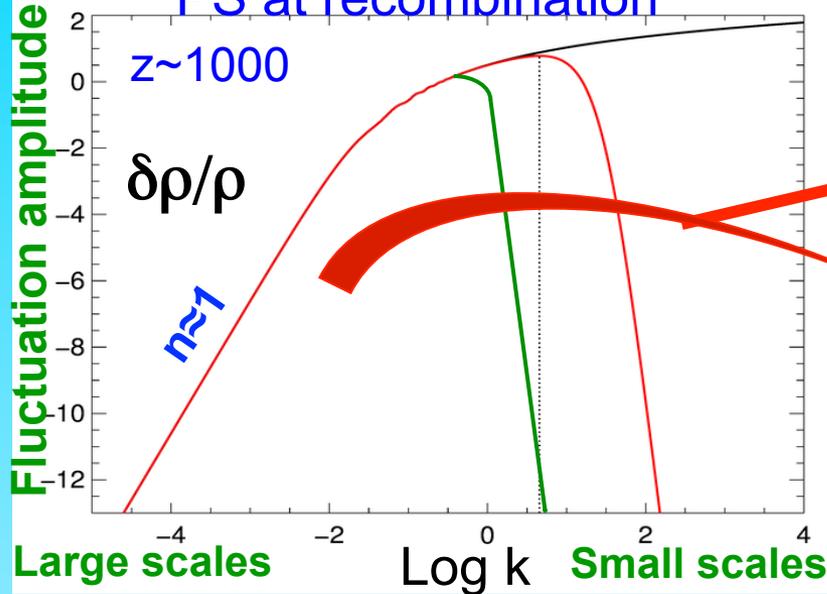
For the first time in Cosmology → a well-defined theory of the initial conditions for the formation of cosmic structure

The formation of cosmic structure

University of Durham

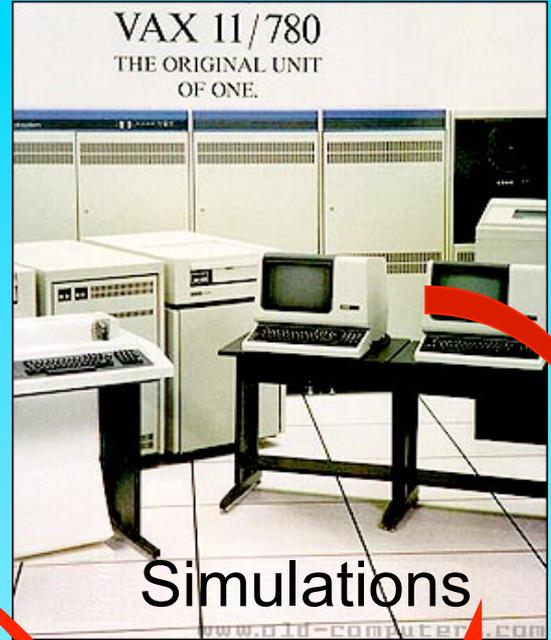
$k^3 P(k)$

PS at recombination



$t = 380,000$ yrs

$\delta\rho/\rho \sim 10^{-5}$



Supercomputer **simulations** are the best technique for calculating how small **primordial perturbations** grow into **galaxies** today

$t = 14.1$ billion yrs

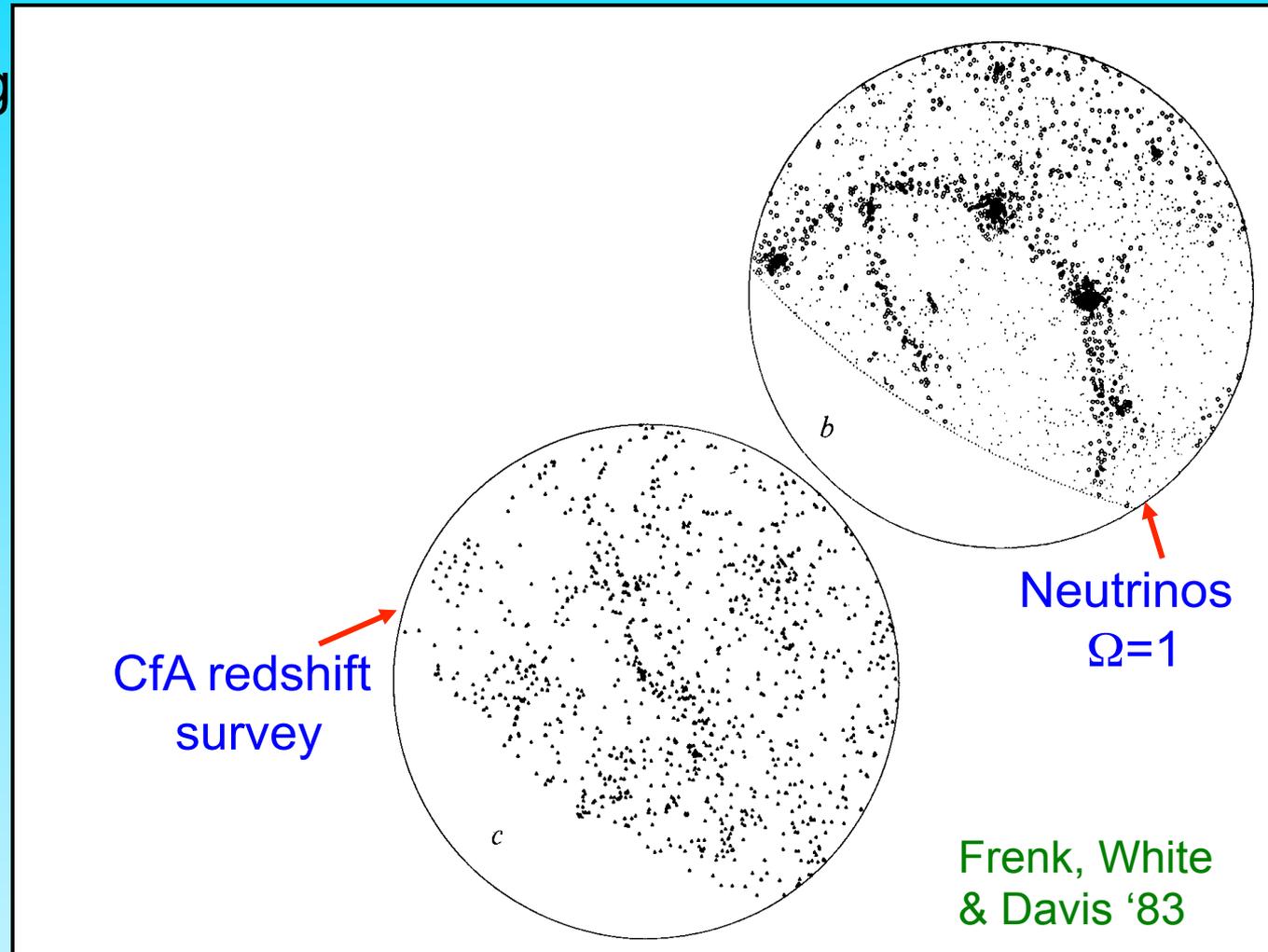
$\delta\rho/\rho \sim 1 - 10^6$



Non-baryonic dark matter cosmologies

Neutrino DM \rightarrow
unrealistic clust'ing

Neutrinos cannot
make appreciable
contribution to Ω
 $\rightarrow m_\nu \ll 10 \text{ eV}$



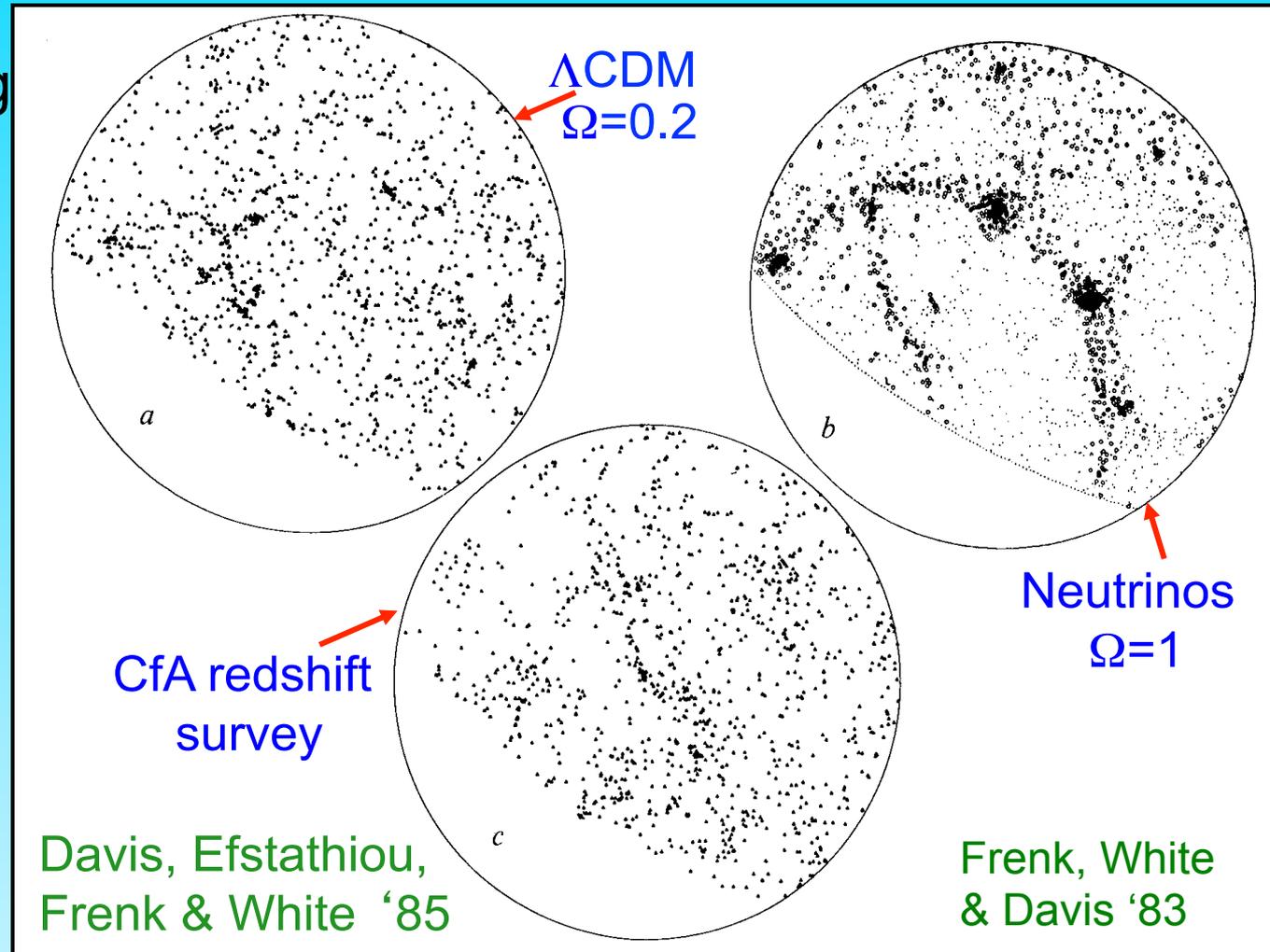
Non-baryonic dark matter cosmologies

Neutrino DM \rightarrow
unrealistic clust'ing

Neutrinos cannot
make appreciable
contribution to Ω
 $\rightarrow m_\nu \ll 10$ eV

Early CDM N-body
simulations gave
promising results

In CDM structure
forms hierarchically



Non-baryonic dark matter candidates

Type example mass

hot	neutrino	a few eV
warm		keV-MeV
→ cold	axion neutralino	10^{-5} eV- >100 GeV

Non-baryonic dark matter candidates

Type example mass

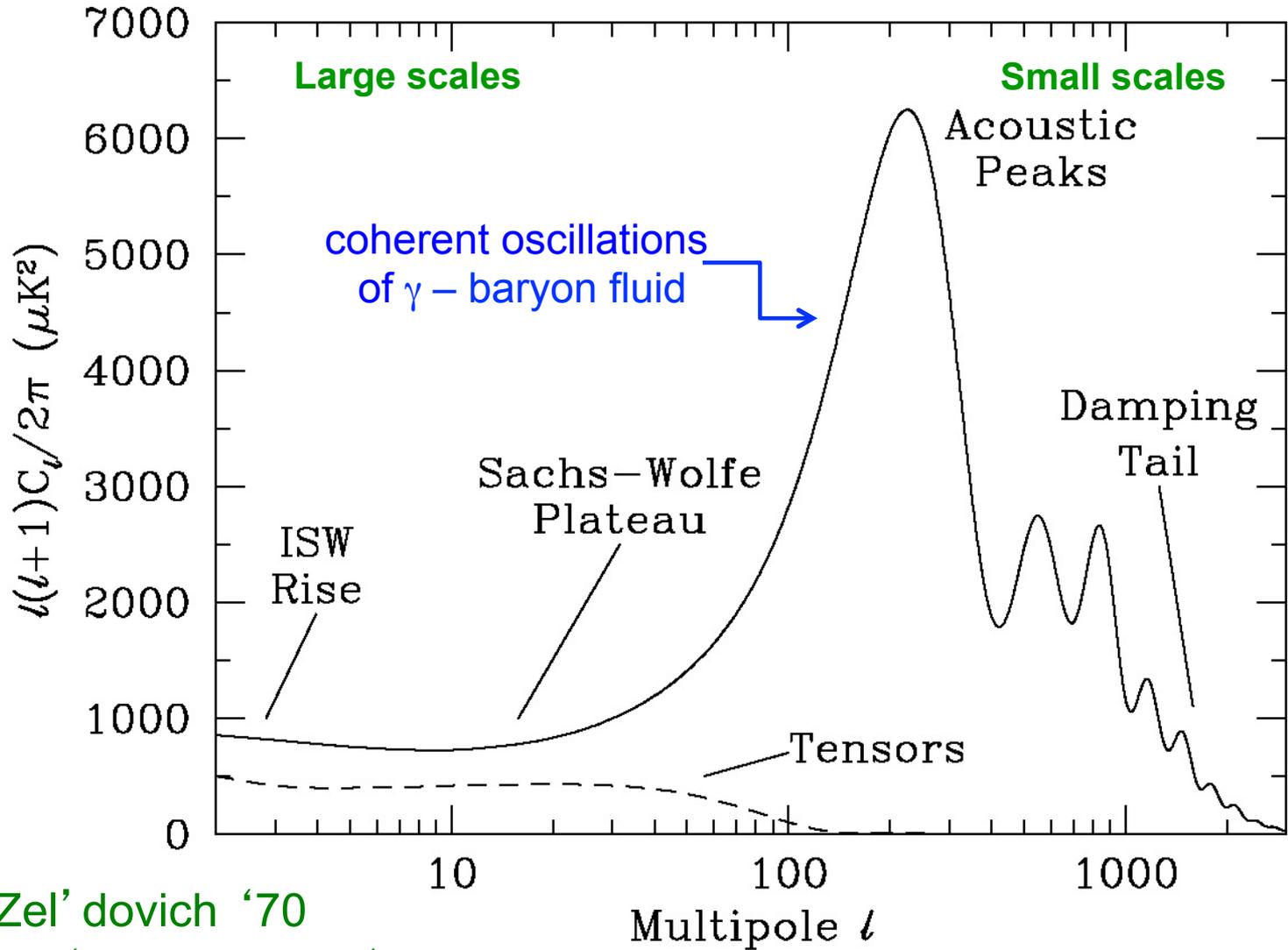
hot	neutrino	a few eV
warm	sterile neutrino majoron; KeVino	keV-MeV
→ cold	axion neutralino	10^{-5}eV - >100 GeV

Main successes of the CDM cosmogony:

1. CMB temp. anisotropies: predicted 1981; discovered 1993
2. Galaxy formation and evolution (modelled early 90s; 1991 -)
3. Galaxy clustering (predicted early 80s; measured 1990-
QDOT, APM, 2dFGRS, SDSS)

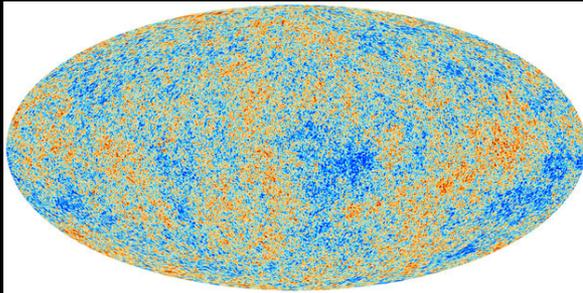
Temperature anisotropies in CMB

2D power spectrum



Sunyaev & Zel'dovich '70

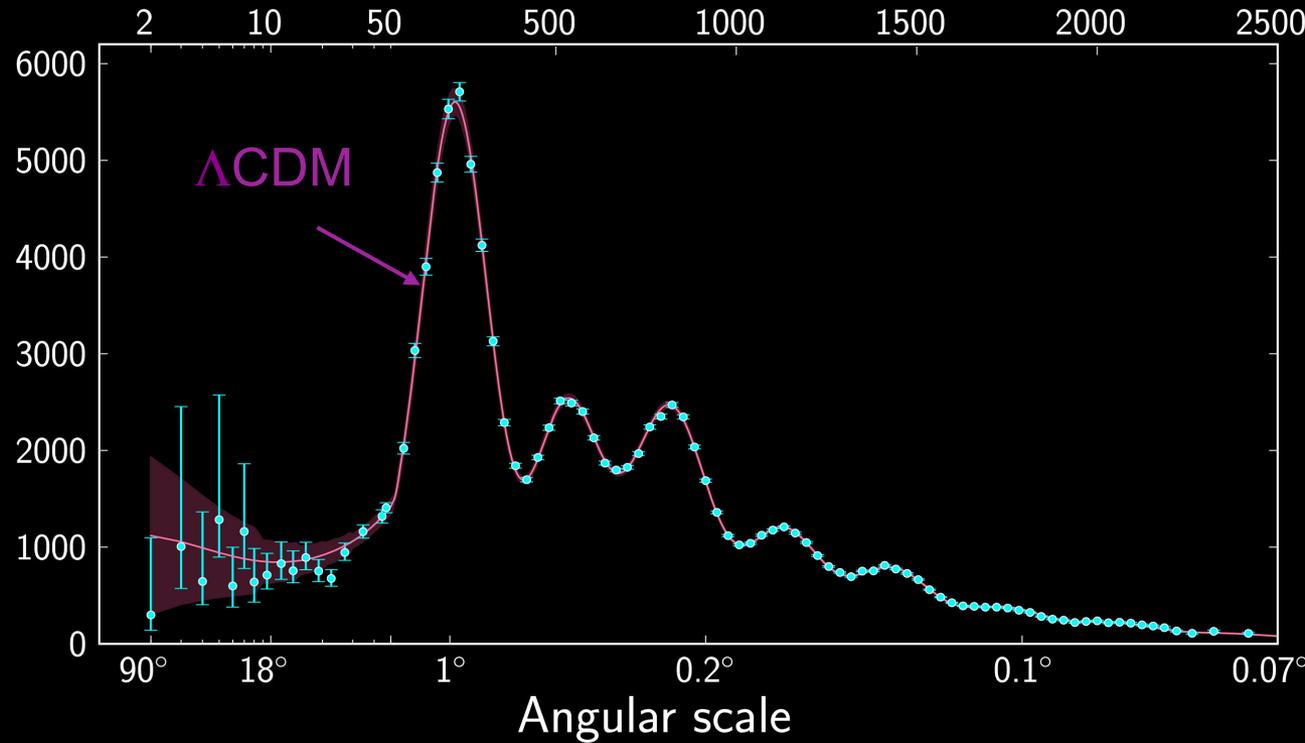
Peebles & Yu '70; Peebles '82



Amplitude of fluctuations at $z \sim 1000$

Multipole moment, ℓ

Temperature fluctuations [μK^2]



The data confirm
the theoretical
predictions
(linear theory)

Peebles '82; Bond &
Efstathiou '80s

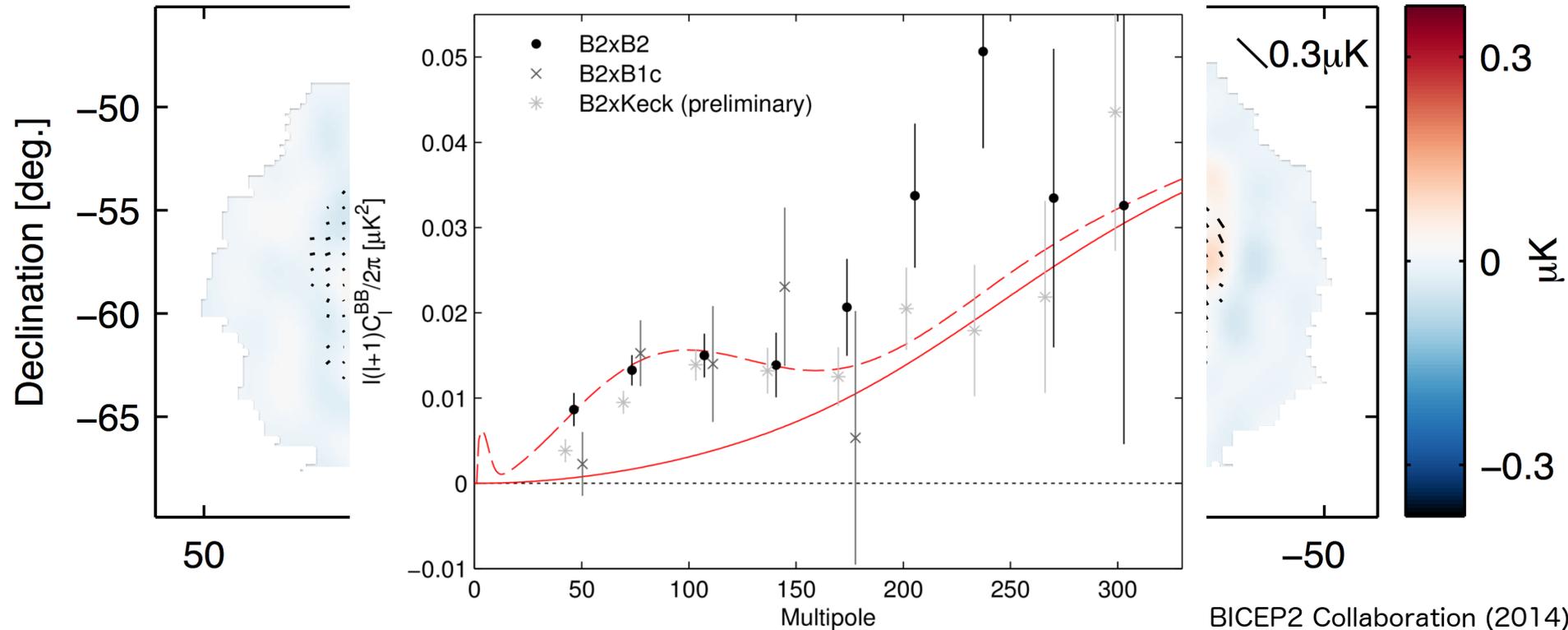
Planck collaboration '13

Detection of B-mode polarization?

Gravitational waves are a fundamental prediction of inflation

They induce B-mode polarization in the CMB at low l

BICEP2: B signal



A NEW TYPE OF ISOTROPIC COSMOLOGICAL MODELS WITHOUT SINGULARITY

A.A. STAROBINSKY

*Department of Applied Mathematics and Theoretical Physics, Cambridge University, Cambridge, England*¹
*and The Landau Institute for Theoretical Physics, The Academy of Sciences, Moscow, 117334, USSR*²

The important property of all nonsingular models with the initial superdense de Sitter state is that, as shown in ref. [8], such a large amount of relic gravitational waves is generated by one-loop processes in these models (in particular, in the range $1-10^{-5}$ Hz) that predictions of the semiclassical theory and the very existence of this state can be experimentally verified in the near future. Adopting such a model, one should also call for some mechanism of baryon-number generation because initial symmetry requires zero initial values of all charges.

Main successes of the CDM cosmogony:

1. CMB temp. anisotropies: predicted 1981; discovered 1993
2. Galaxy formation and evolution (modelled early 90s; 1991 -)
3. Galaxy clustering (predicted early 80s; measured 1990-
QDOT, APM, 2dFGRS, SDSS)

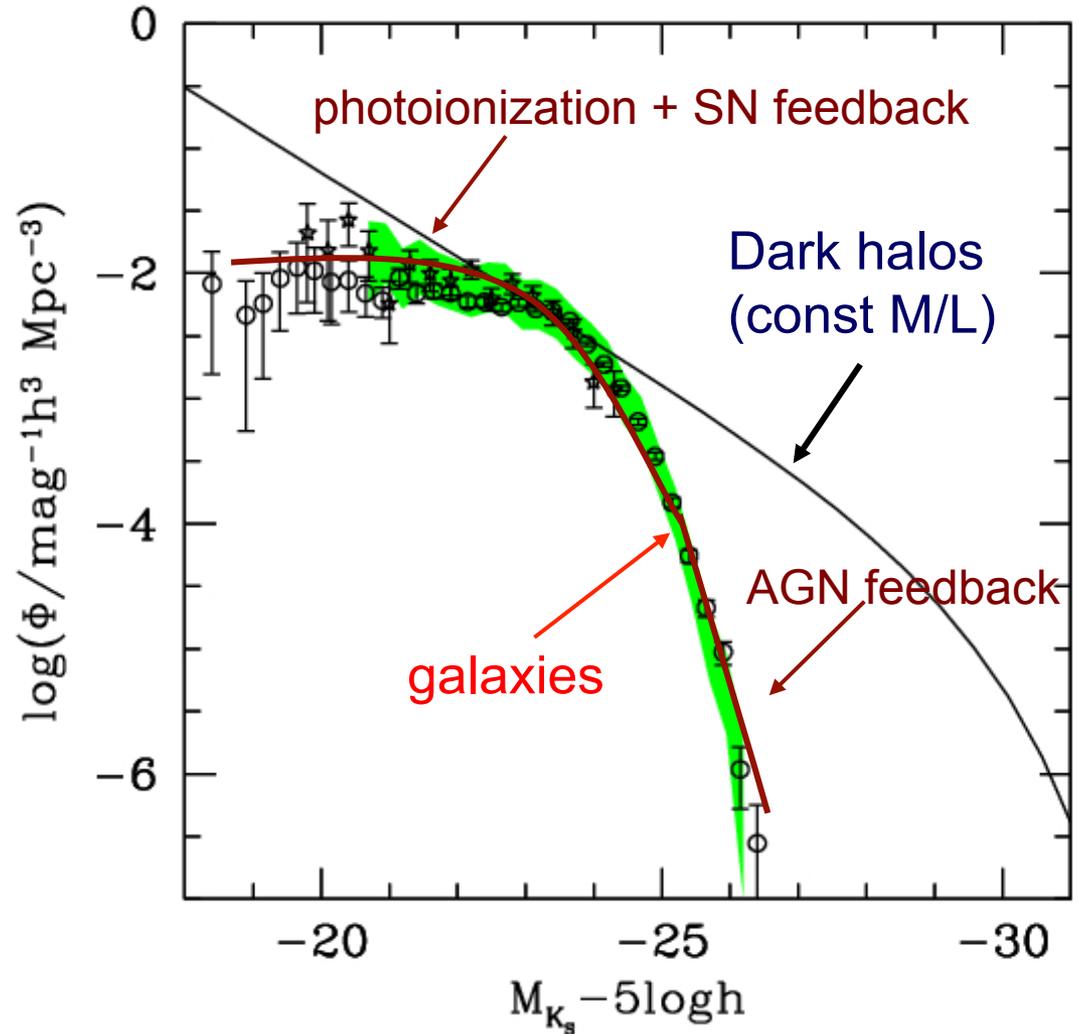
The galaxy luminosity function

The halo mass function and the galaxy luminosity function have different shapes



Galaxy luminosity not just \propto halo mass

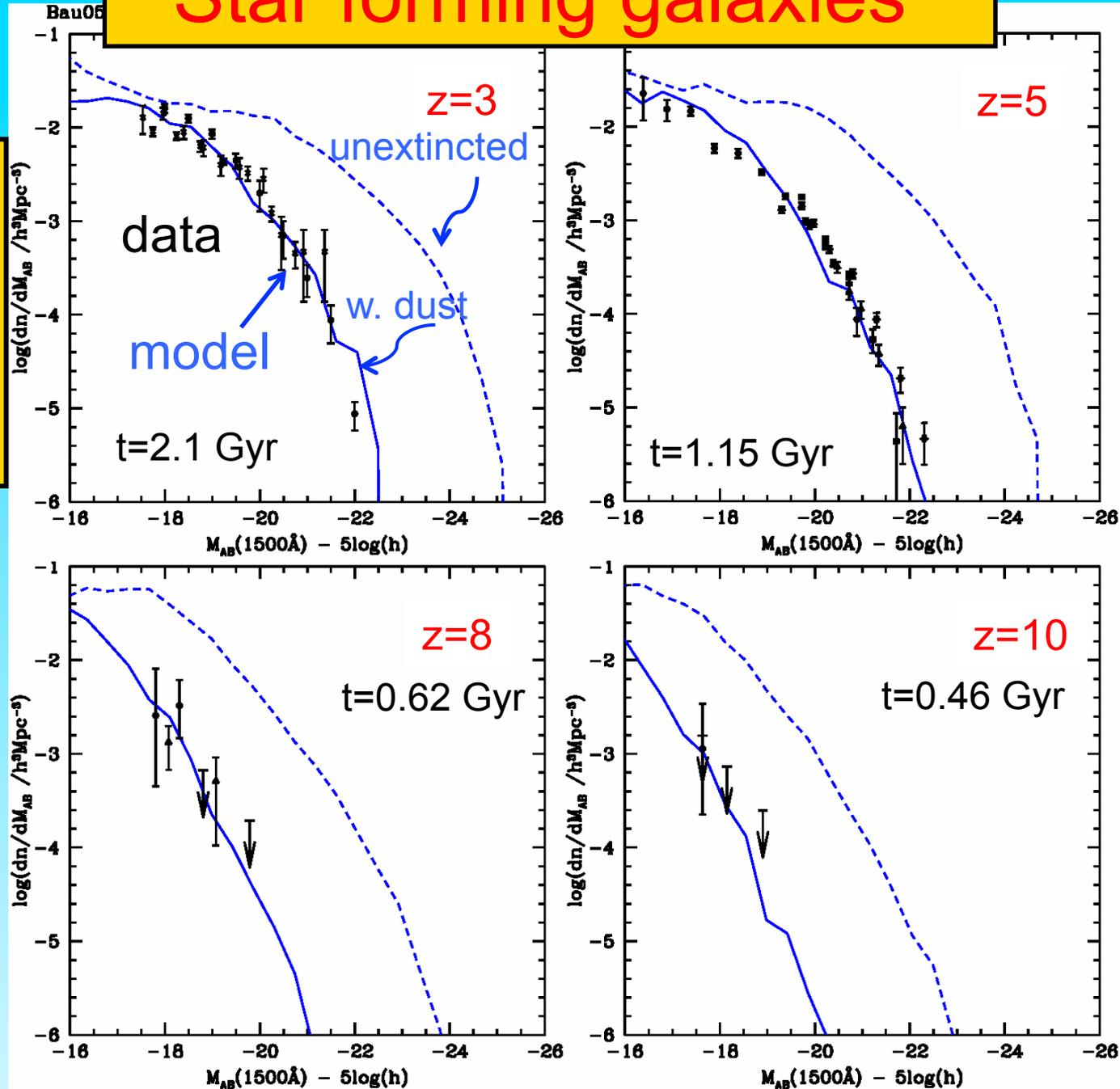
Complicated variation of M/L with halo mass



White & Frenk '91; Kauffmann et al '93; Benson et al '03; Croton et al '05; Bower et al. '06

Star forming galaxies

Evolution of Lyman-break galaxy lum. function

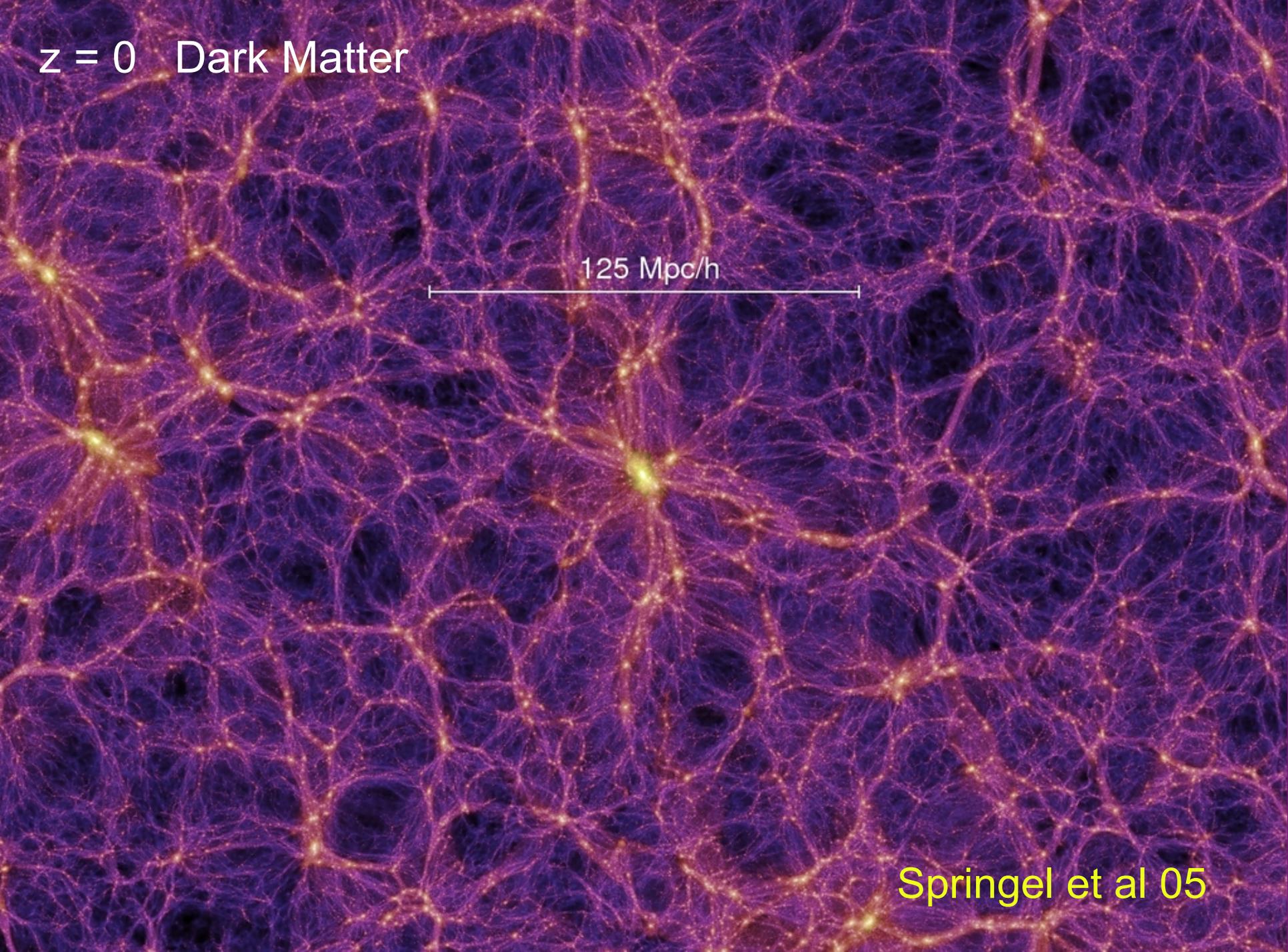


Lacey, Baugh, Frenk, Benson '12

Main successes of the CDM cosmogony:

1. CMB temp. anisotropies: predicted 1981; discovered 1993
2. Galaxy formation and evolution (modelled early 90s; 1991 -)
3. Galaxy clustering (predicted early 80s; measured 1990-
QDOT, APM, 2dFGRS, SDSS)

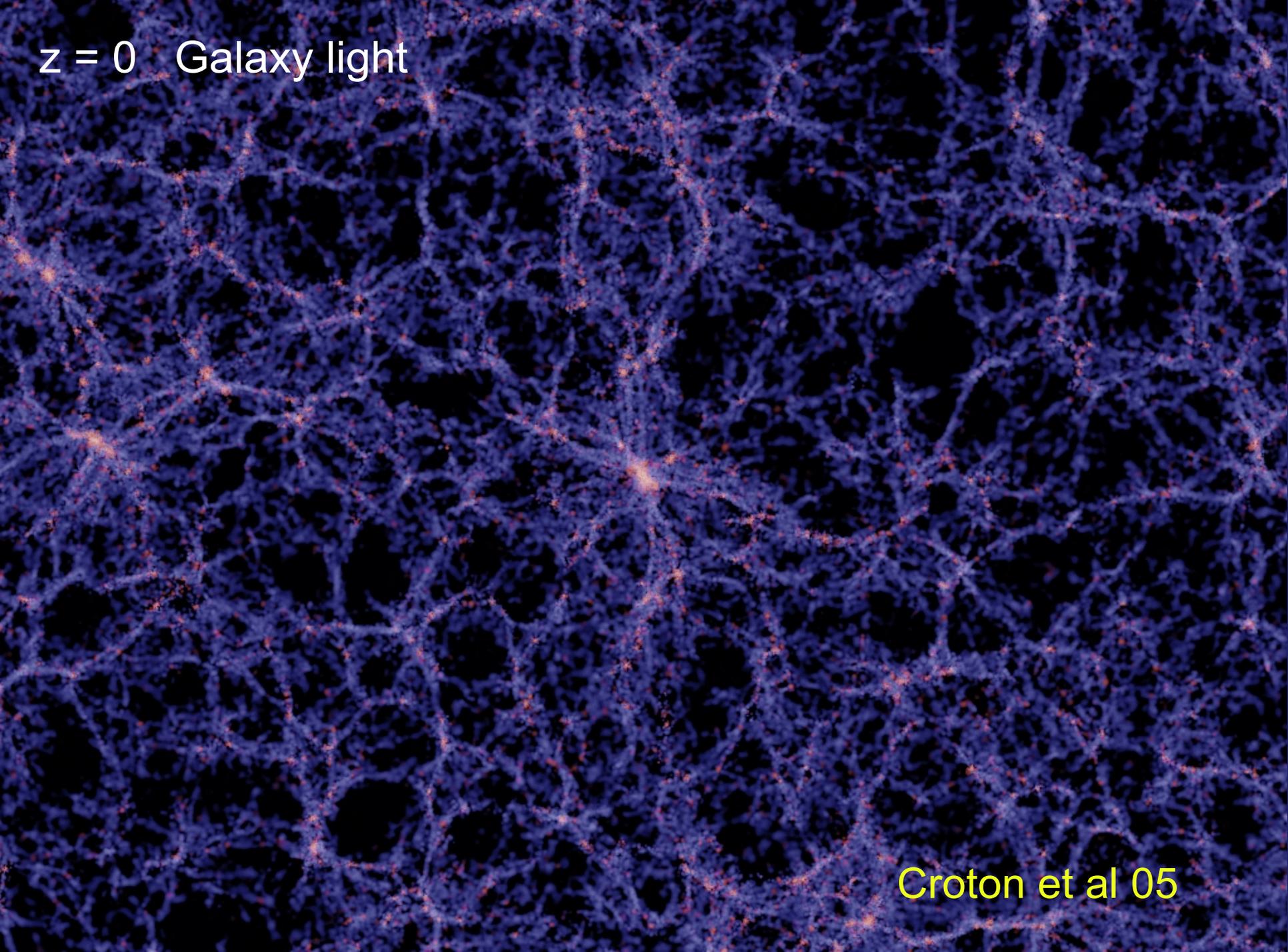
$z = 0$ Dark Matter



125 Mpc/h

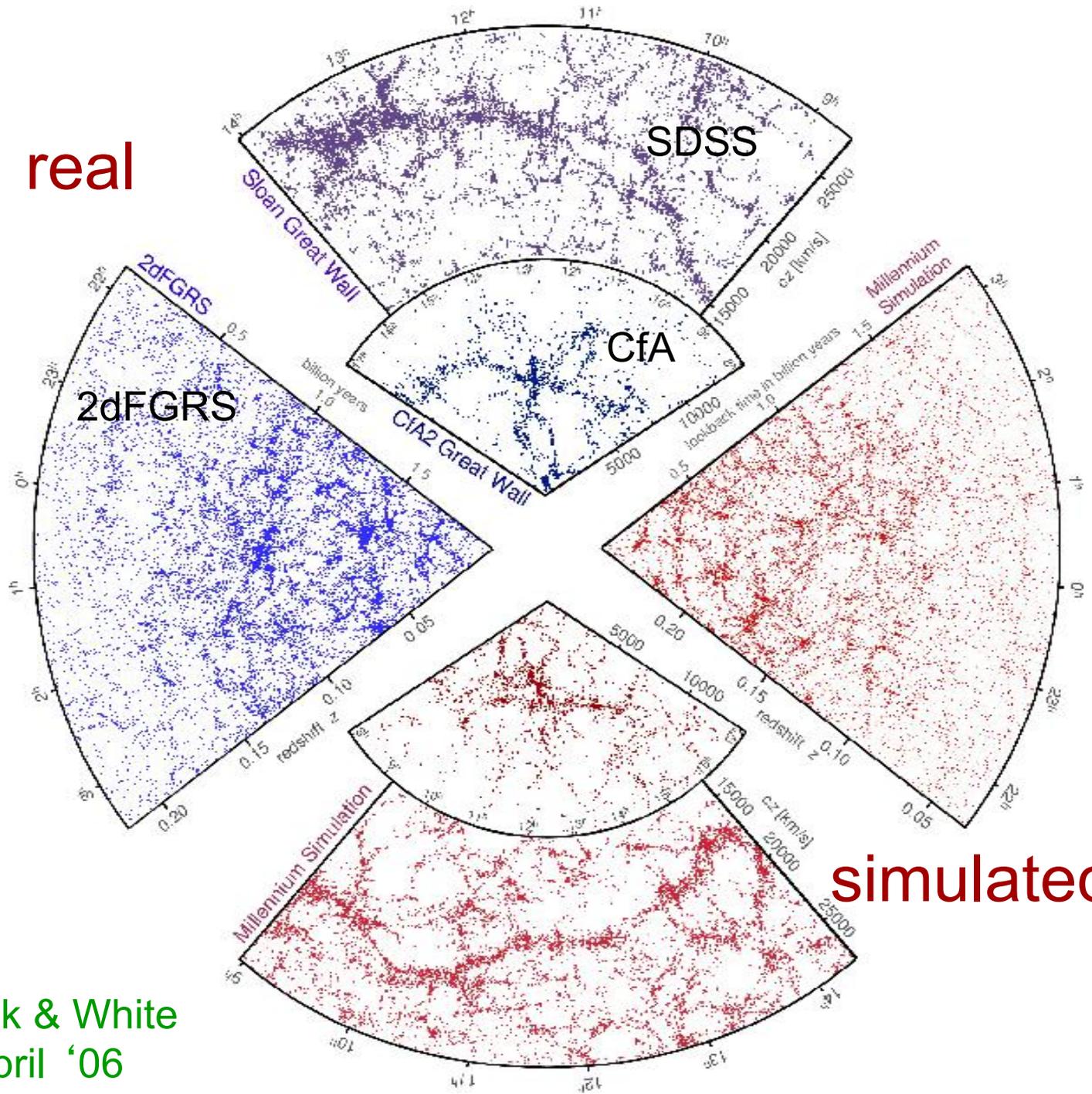
Springel et al 05

$z = 0$ Galaxy light



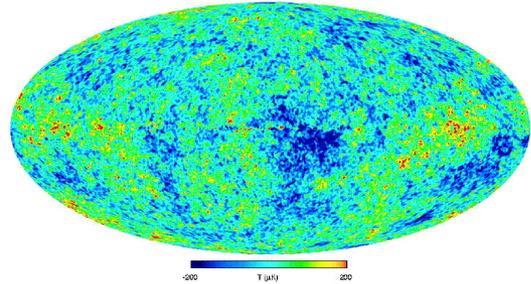
Croton et al 05

real



simulated

The cosmic power spectrum: from the CMB to the 2dFGRS

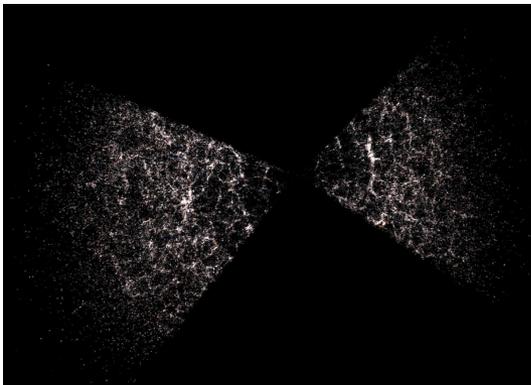


$z \sim 1000$

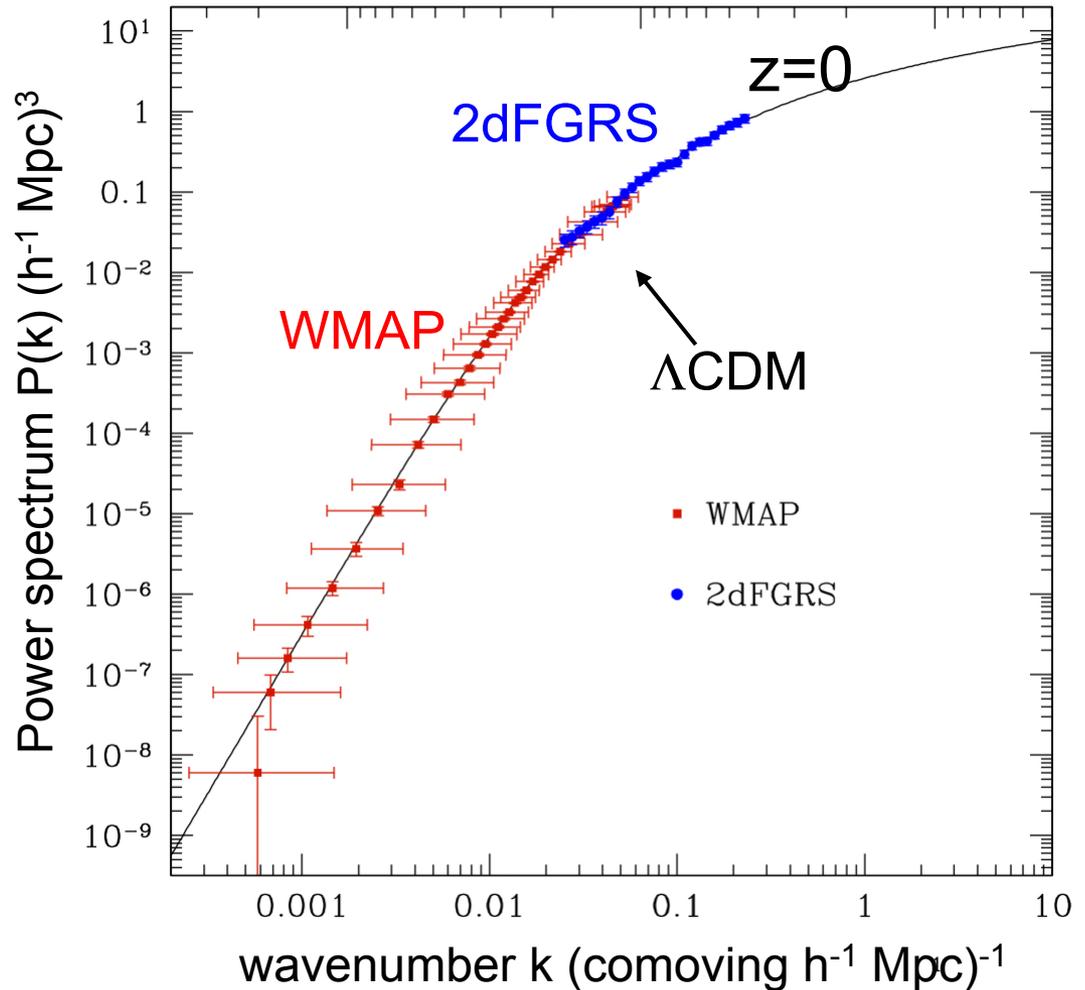
$\text{Log } k^3 P(k)$

wavelength k^{-1} (comoving h^{-1} Mpc)

1 000 100 10



$z \sim 0$



⇒ Λ CDM provides an excellent description of mass power spectrum from 10-1000 Mpc

Sanchez et al 06

The cosmic power spectrum: from the CMB to the 2dFGRS

Free streaming \rightarrow

$$\lambda_{\text{cut}} \propto m_x^{-1}$$

for thermal relic

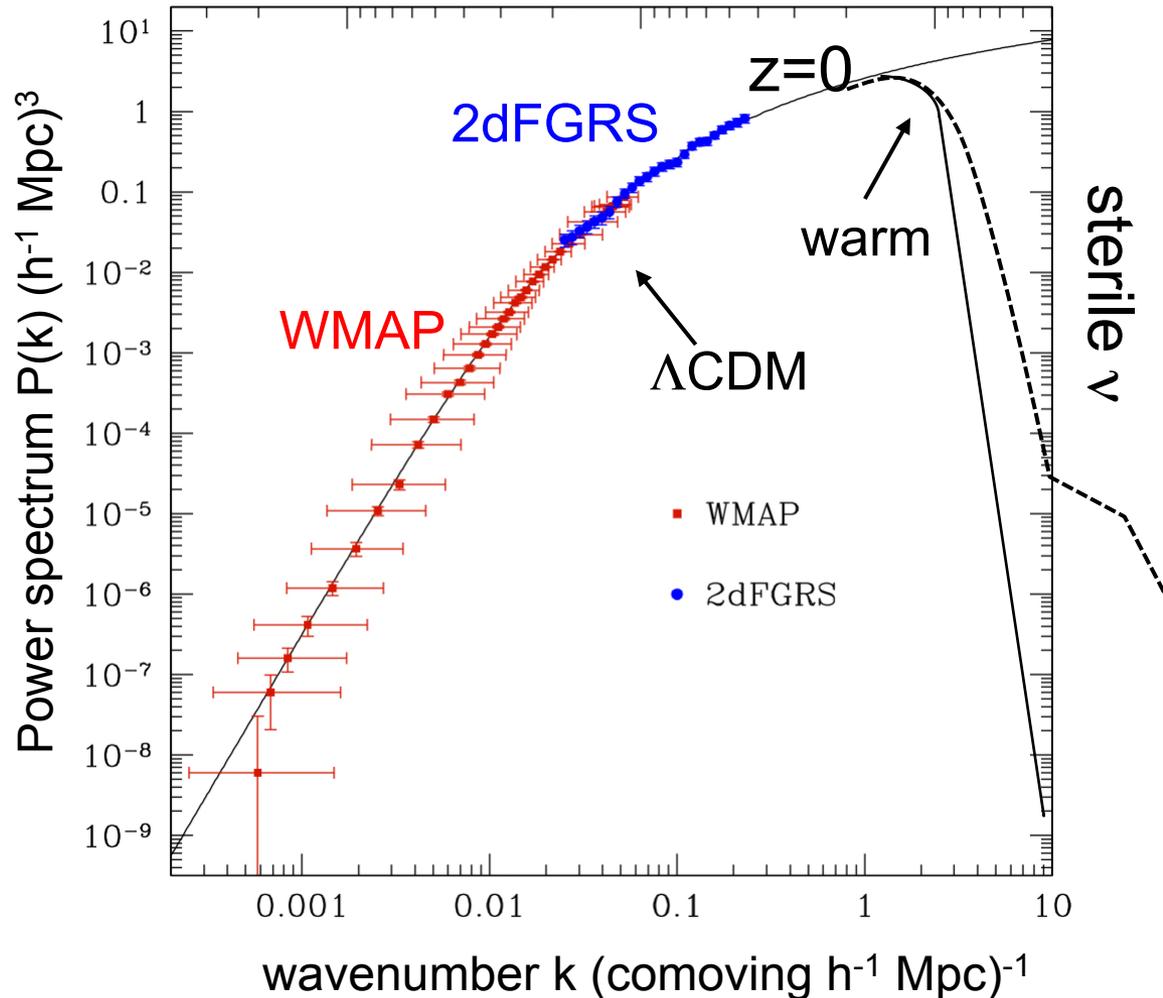
$$m_{\text{CDM}} \sim 100 \text{ GeV}$$

$$\text{susy}; M_{\text{cut}} \sim 10^{-6} M_{\odot}$$

$$m_{\text{WDM}} \sim \text{few keV}$$

$$\text{sterile } \nu; M_{\text{cut}} \sim 10^9 M_{\odot}$$

Log $k^3 P(k)$ wavelength k^{-1} (comoving h^{-1} Mpc)





The ν minimal standard model

- Neutrino Minimal Standard Model (ν MSM) proposed to explain neutrino masses (Asaka & Shaposhnikov '05; Boyarski, Ruchowskyi)
- Adds three **sterile neutrinos** to the SM. The lightest of these would be the **dark matter**

The cosmic power spectrum: from the CMB to the 2dFGRS

Free streaming \rightarrow

$$\lambda_{\text{cut}} \propto m_x^{-1}$$

for thermal relic

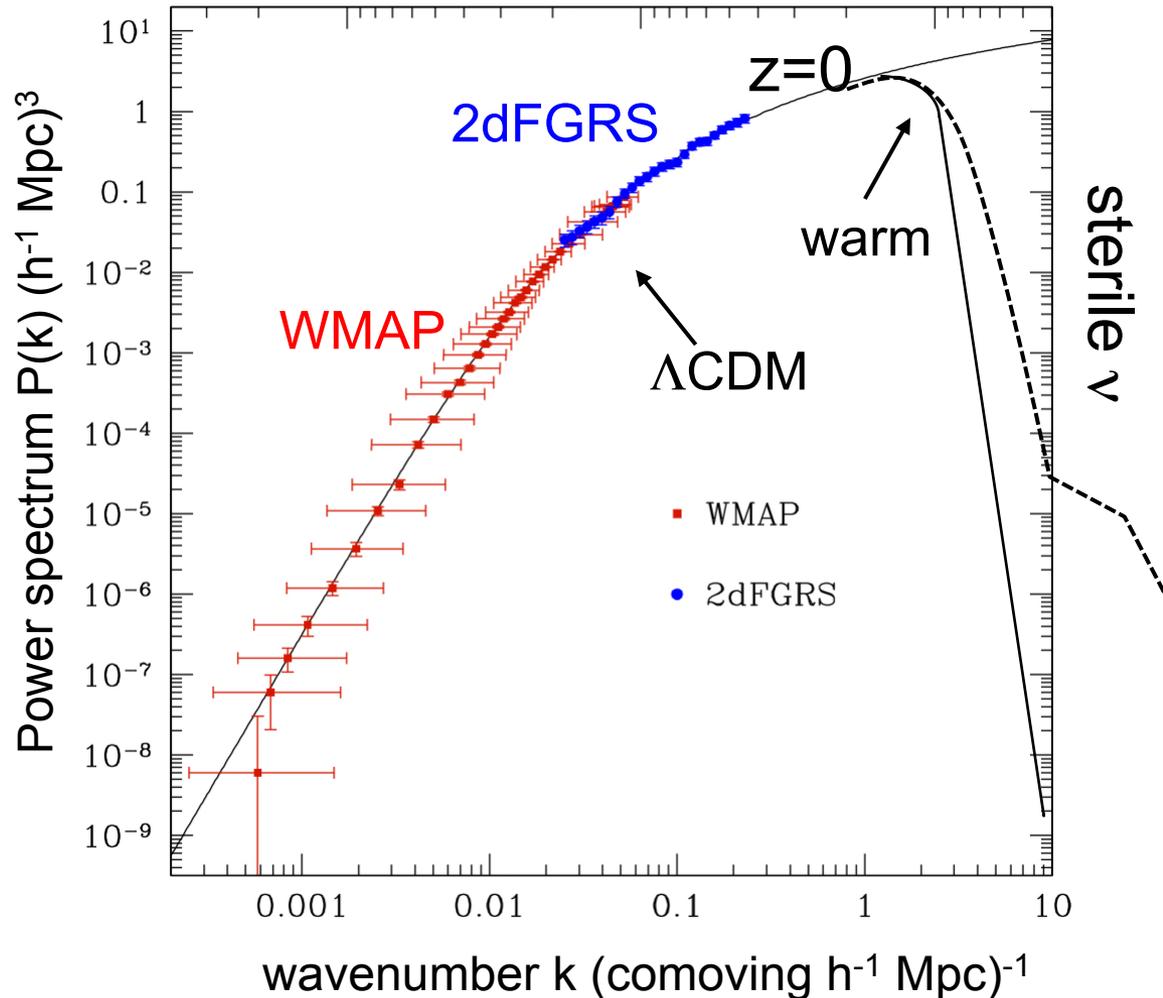
$$m_{\text{CDM}} \sim 100 \text{ GeV}$$

$$\text{susy}; M_{\text{cut}} \sim 10^{-6} M_{\odot}$$

$$m_{\text{WDM}} \sim \text{few keV}$$

$$\text{sterile } \nu; M_{\text{cut}} \sim 10^9 M_{\odot}$$

Log $k^3 P(k)$ wavelength k^{-1} (comoving h^{-1} Mpc)



A. Boyarsky¹, O. Ruchayskiy², D. Iakubovskiy^{3,4} and J. Franse^{1,5}

¹Instituut-Lorentz for Theoretical Physics, Universiteit Leiden, Niels Bohrweg 2, Leiden, The Netherlands

²Ecole Polytechnique Fédérale de Lausanne, FSB/ITP/LPPC, BSP, CH-1015, Lausanne, Switzerland

³Bogolyubov Institute of Theoretical Physics, Metrologichna Str. 14-b, 03680, Kyiv, Ukraine

⁴National University “Kyiv-Mohyla Academy”, Skovorody Str. 2, 04070, Kyiv, Ukraine

⁵Leiden Observatory, Leiden University, Niels Bohrweg 2, Leiden, The Netherlands

SUBMITTED TO APJ, 2014 I
Preprint typeset using L^AT_EX

arXiv:1402.4119v1 [astro-ph.CO] 17 Feb 2014

DETECTION OF AN UNIDENTIFIED

ESRA BULBUL^{1,2}, M

¹ Har

We detect a weak line in the X-ray spectrum of 73 ξ

independently show the presence of the line at consistent energies. When the full sample is divided into three subsamples (Perseus, Centaurus+Ophiuchus+Coma, and all others), the line is seen at $> 3\sigma$ statistical significance in all three independent MOS spectra and the PN “all others” spectrum. The line is also detected at the same energy in the *Chandra* ACIS-S and ACIS-I spectra of the Perseus cluster, with a flux consistent with *XMM-Newton* (however, it is not seen in the ACIS-I spectrum of Virgo). The line is present even if we allow maximum freedom for all the known thermal emission lines. However, it is very weak (with an equivalent width in the full sample of only ~ 1 eV) and located within 50–110 eV of several known faint lines; the detection is at the limit of the current instrument capabilities and subject to significant modeling uncertainties. On the origin of this line, we argue that there should be no atomic transitions in thermal plasma at this energy. An intriguing possibility is the decay of sterile neutrino, a long-sought dark matter particle candidate. Assuming that all dark matter is in sterile neutrinos with $m_s = 2E = 7.1$ keV, our detection in the full sample corresponds to a neutrino decay mixing angle $\sin^2(2\theta) \approx 7 \times 10^{-11}$, below the previous upper limits. However, based



Astrophysical key to identity of dark matter:

→ Subgalactic scales
(strongly non-linear)

$z = 48.4$

$T = 0.05 \text{ Gyr}$

500 kpc



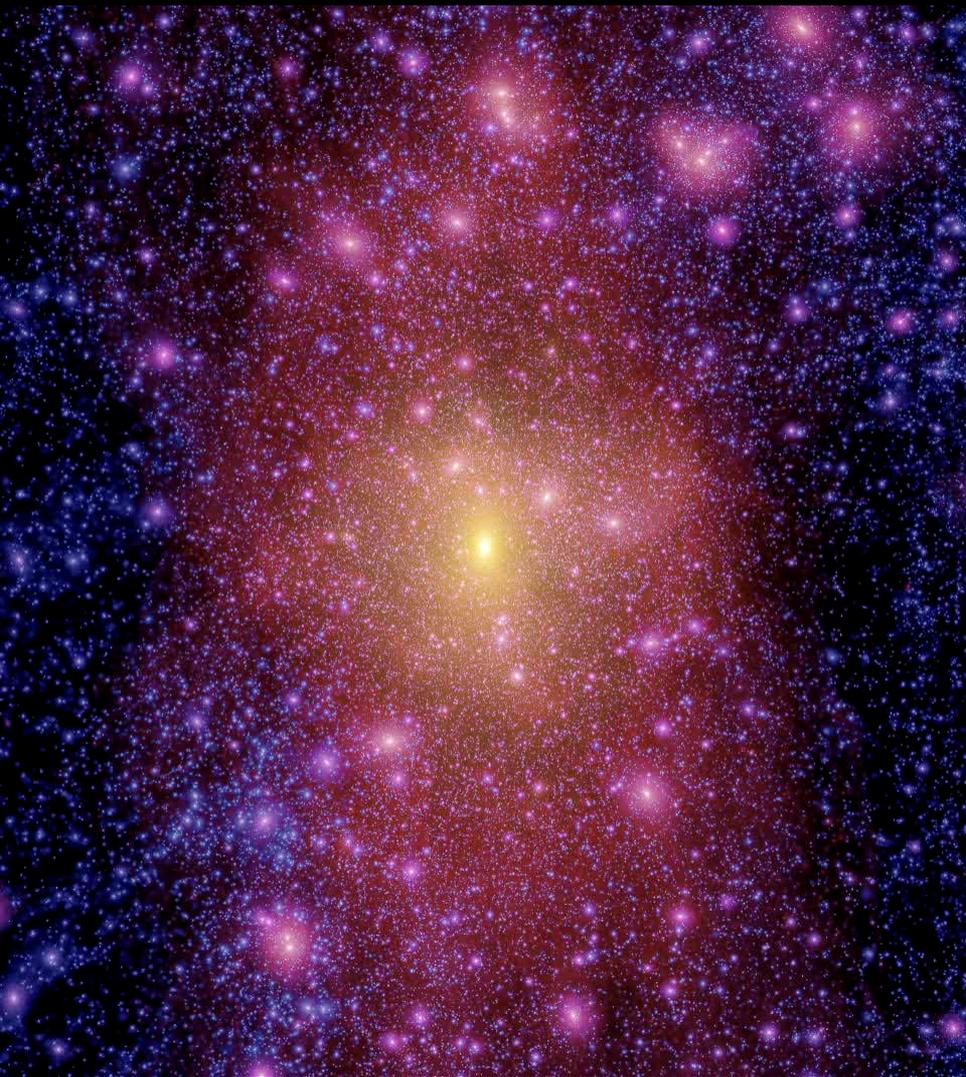


Cold Dark Matter

Warm Dark Matter

13.4 billion years ago

cold dark matter



warm dark matter



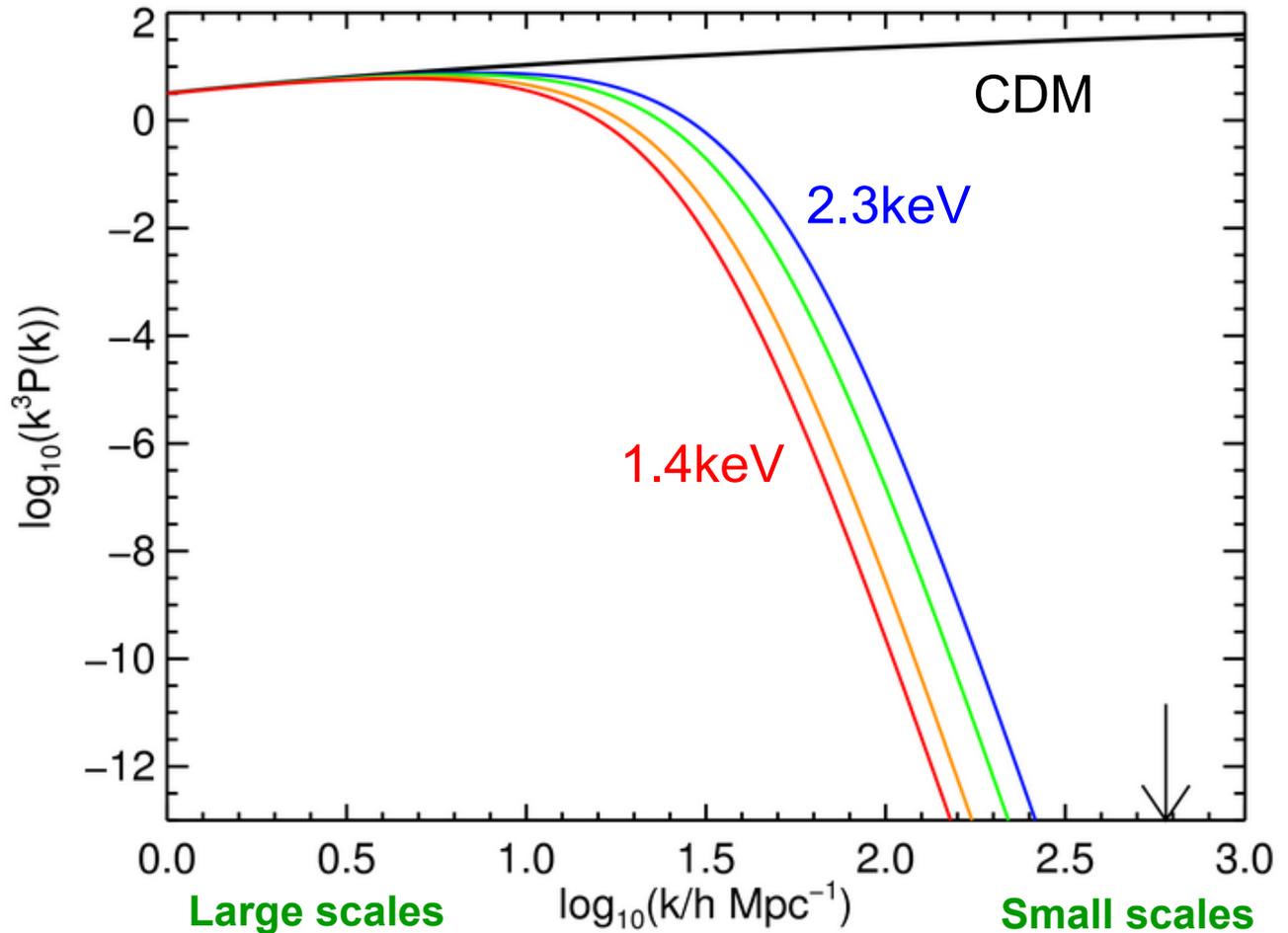
Lovell, Eke, Frenk, Gao, Jenkins, Wang, White, Theuns,
Boyarski & Ruchayskiy '14

Warm DM: different ν mass

$$\lambda_{\text{cut}} \propto m_x^{-1}$$

- WDM
- 2.3 keV
- 2.0 keV
- 1.6 keV
- 1.4 keV

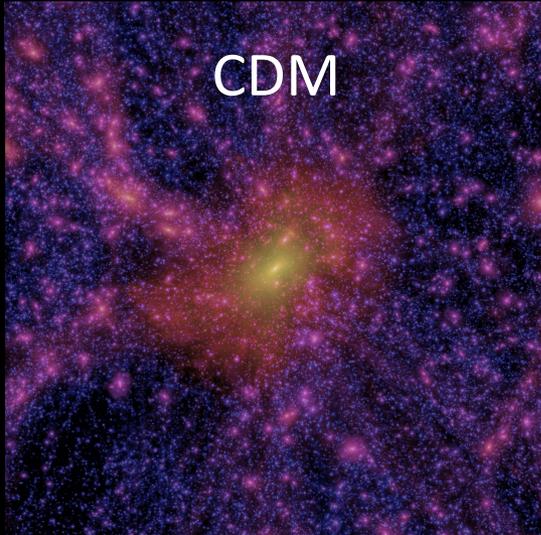
The linear power spectrum (“power per octave”)



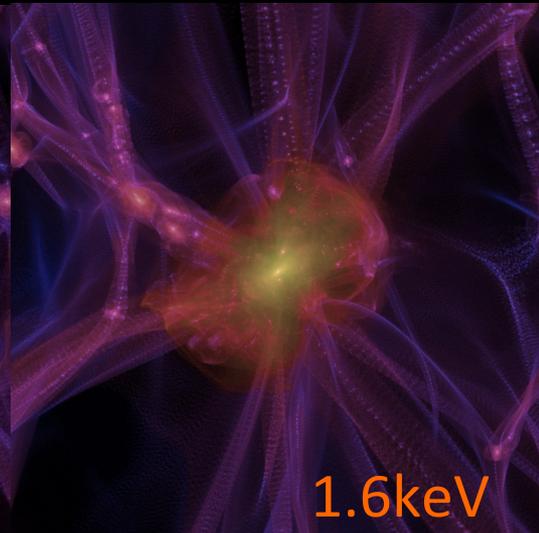
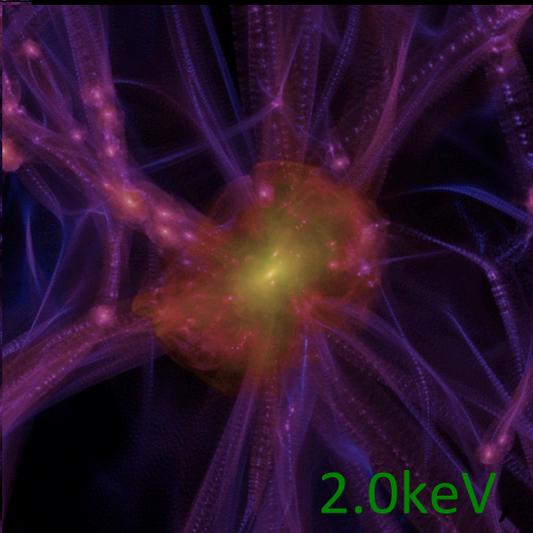
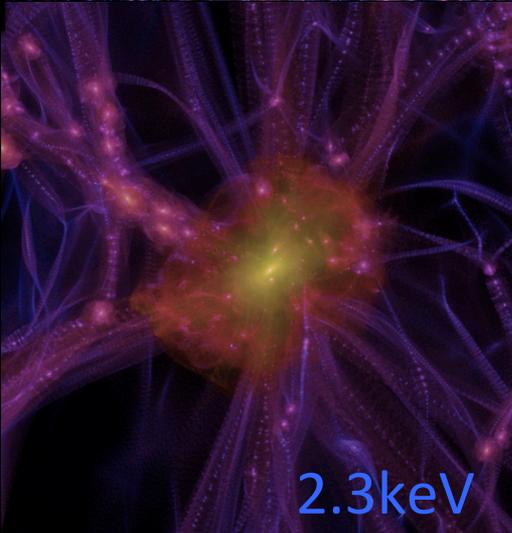
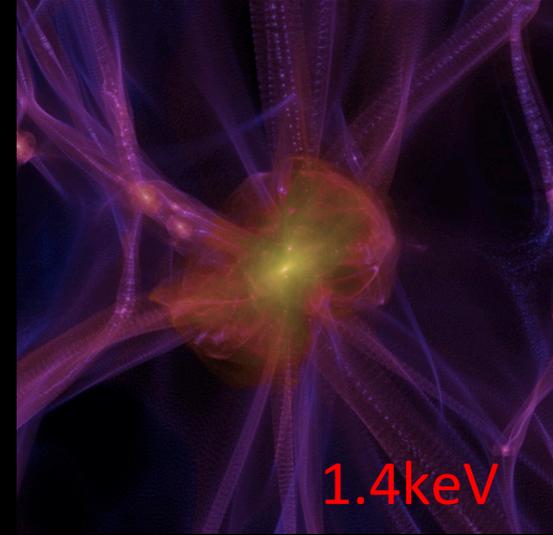
Warm DM: different ν mass

$z=3$

- WDM
- 2.3 keV
- 2.0 keV
- 1.6 keV
- 1.4 keV



WDM



Simulations make 2 important predictions on galactic scales:

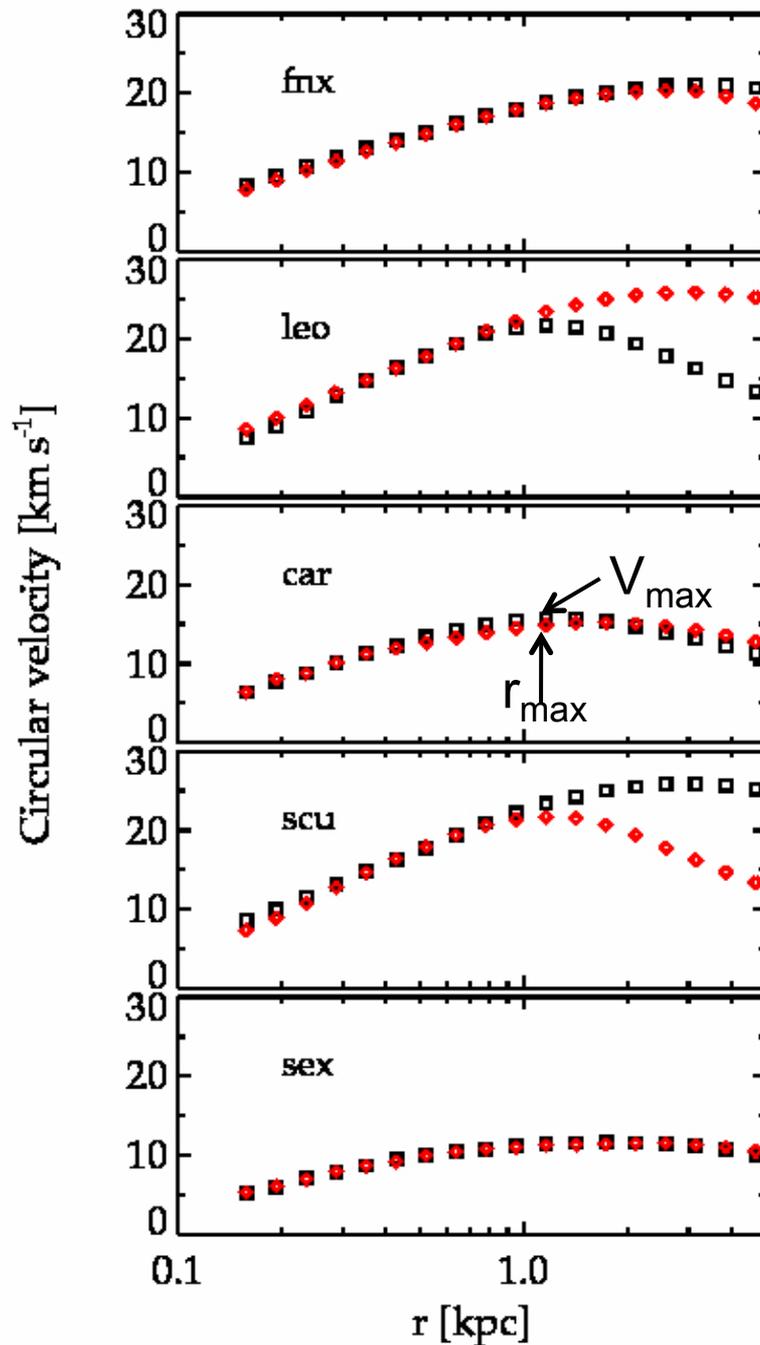
Cold dark matter

- Large number of self-bound substructures (**10% of mass**) survive
- The main halo and its subhalos have “cuspy” density profiles

Warm dark matter

- Far fewer self-bound substructures (**5% of mass**) survive
- Main halo profile identical to CDM; subhalos still “cuspy” but less concentrated than in CDM

The structure of the Milky Way satellites



$$V_c = \sqrt{\frac{GM}{r}}$$

$$V_{\max} = \max V_c$$

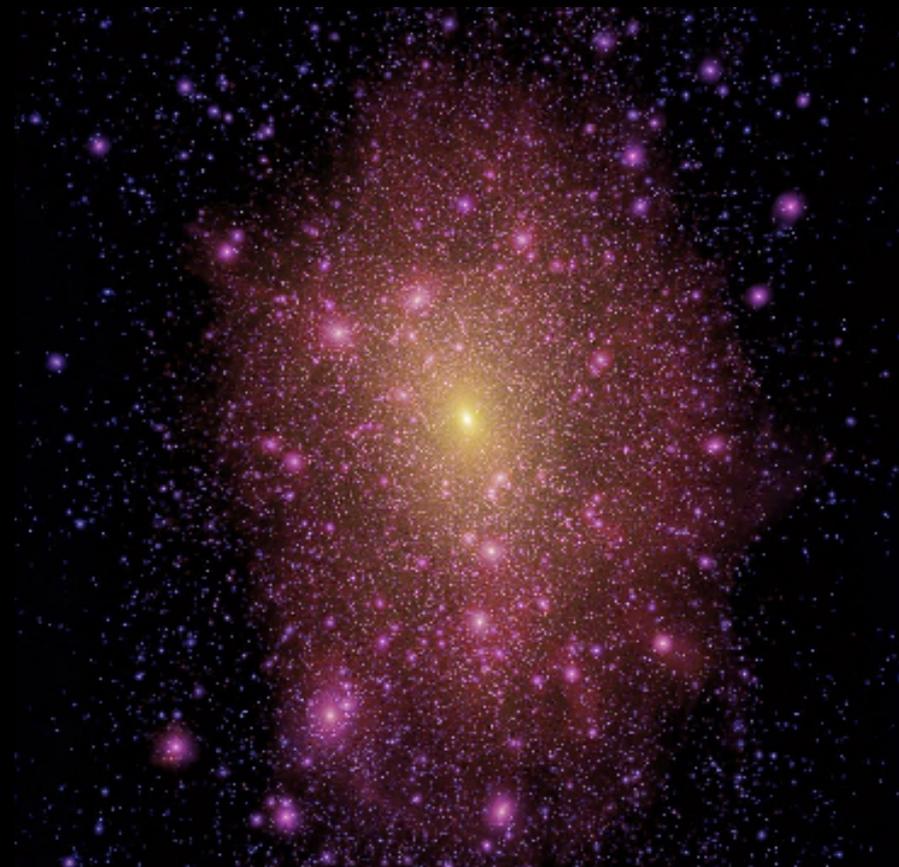
Strigari, Frenk & White 2010



Subhalo abundance

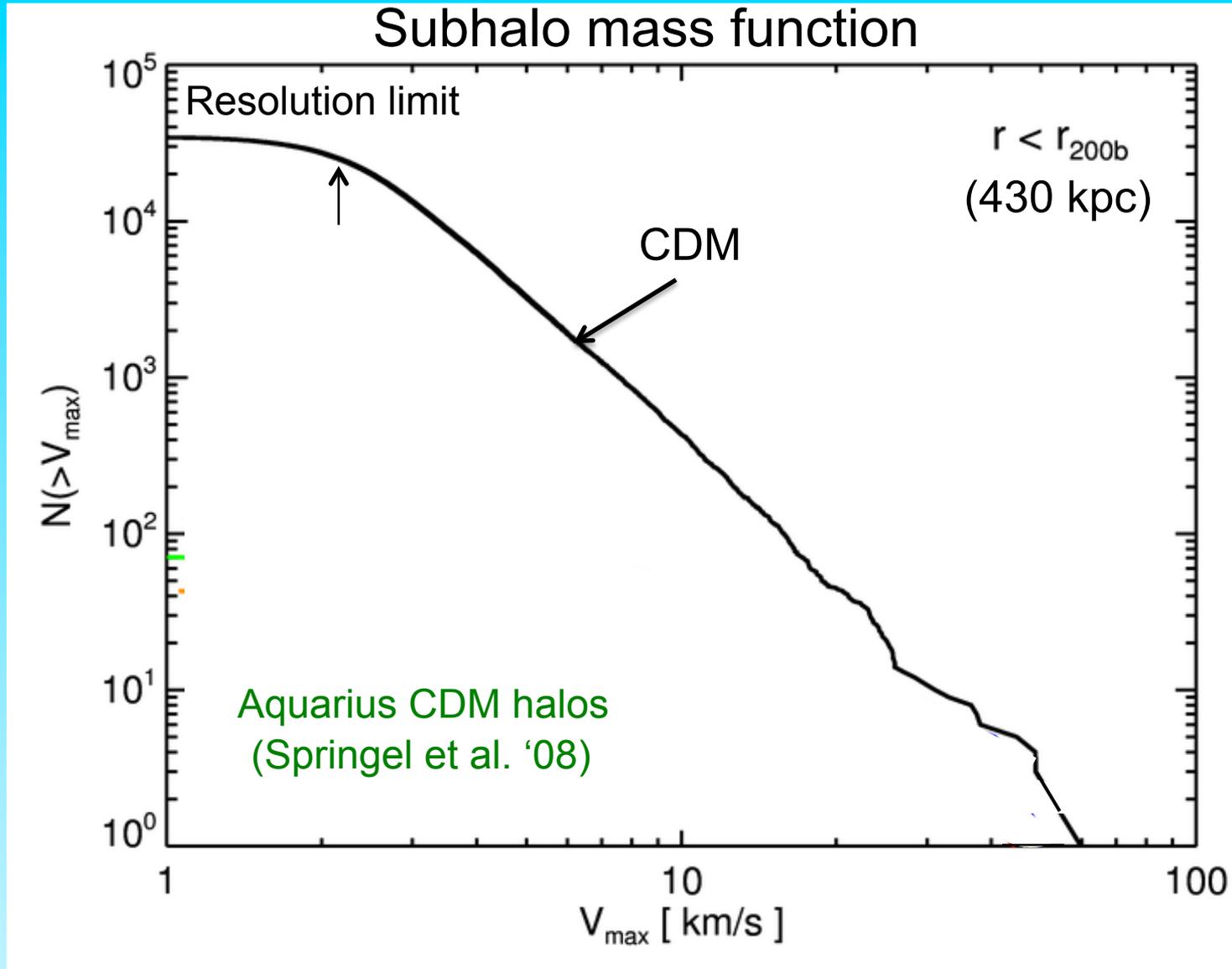
cold dark matter

warm dark matter



Lovell, Eke, Frenk, Gao, Jenkins, Theuns '12

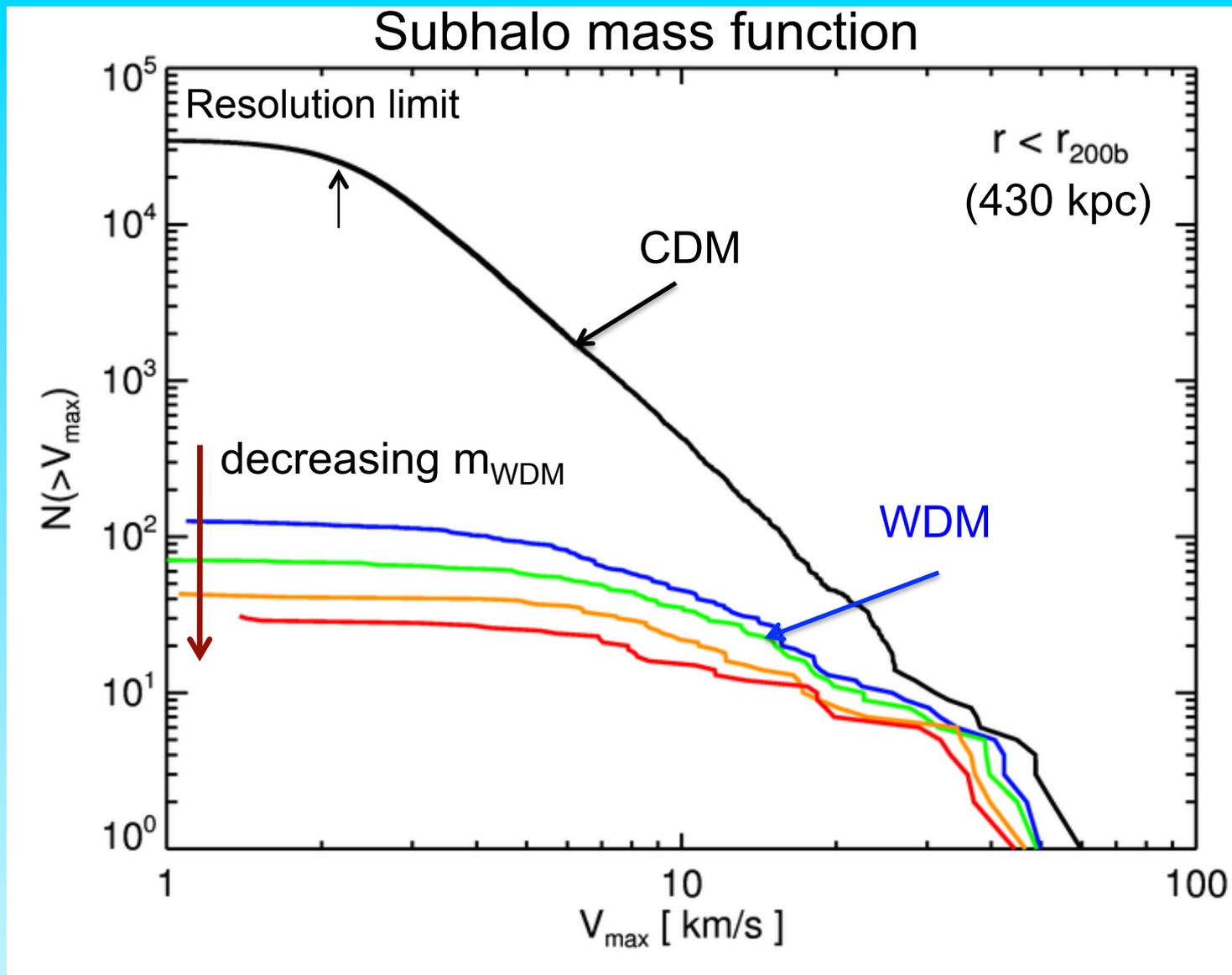
The mass function of substructures



The mass function of substructures

- WDM
- 2.3 keV
- 2.0 keV
- 1.6 keV
- 1.4 keV

No of suhalos
 ↗ with m_{WDM}



Subhalo density profiles

CDM & WDM subhalos have cuspy profiles

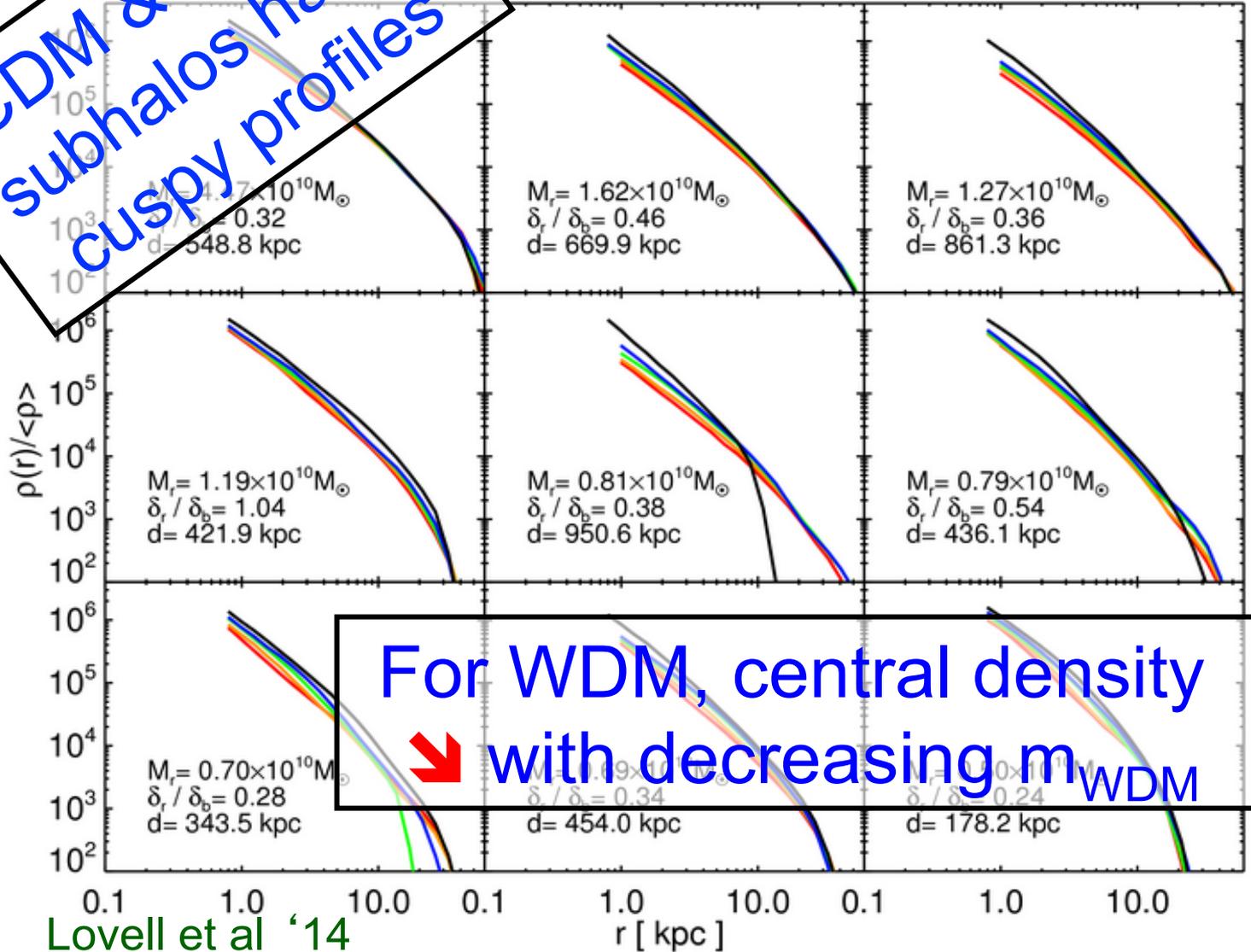
WDM

2.3 keV

2.0 keV

1.6 keV

1.4 keV



For WDM, central density \downarrow with decreasing m_{WDM}



How can we distinguish between CDM & WDM ?



Subhalo abundance

cold dark matter

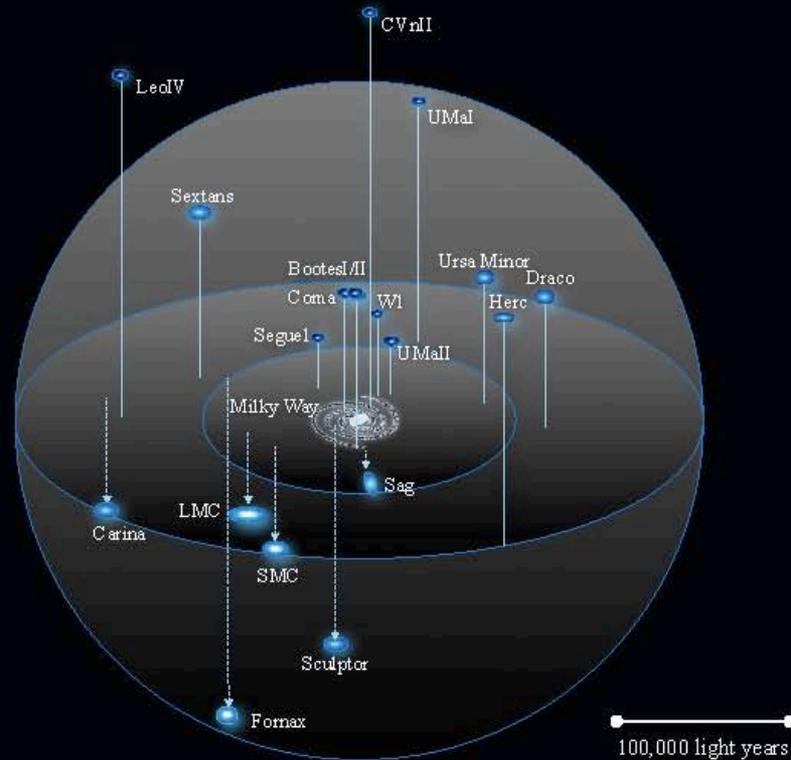
warm dark matter

By looking at number & structure of subhalos

Lovell, Frenk, Eke, Gao, Jenkins, Theuns '12, '13

The satellites of the Milky Way

~25 satellites known
in the MW





Subhalo abundance

cold dark matter

warm dark matter



Lovell, Frenk, Eke, Gao, Jenkins, Theuns '12, '14

CDM simulations produce $>10^5$ subhalos

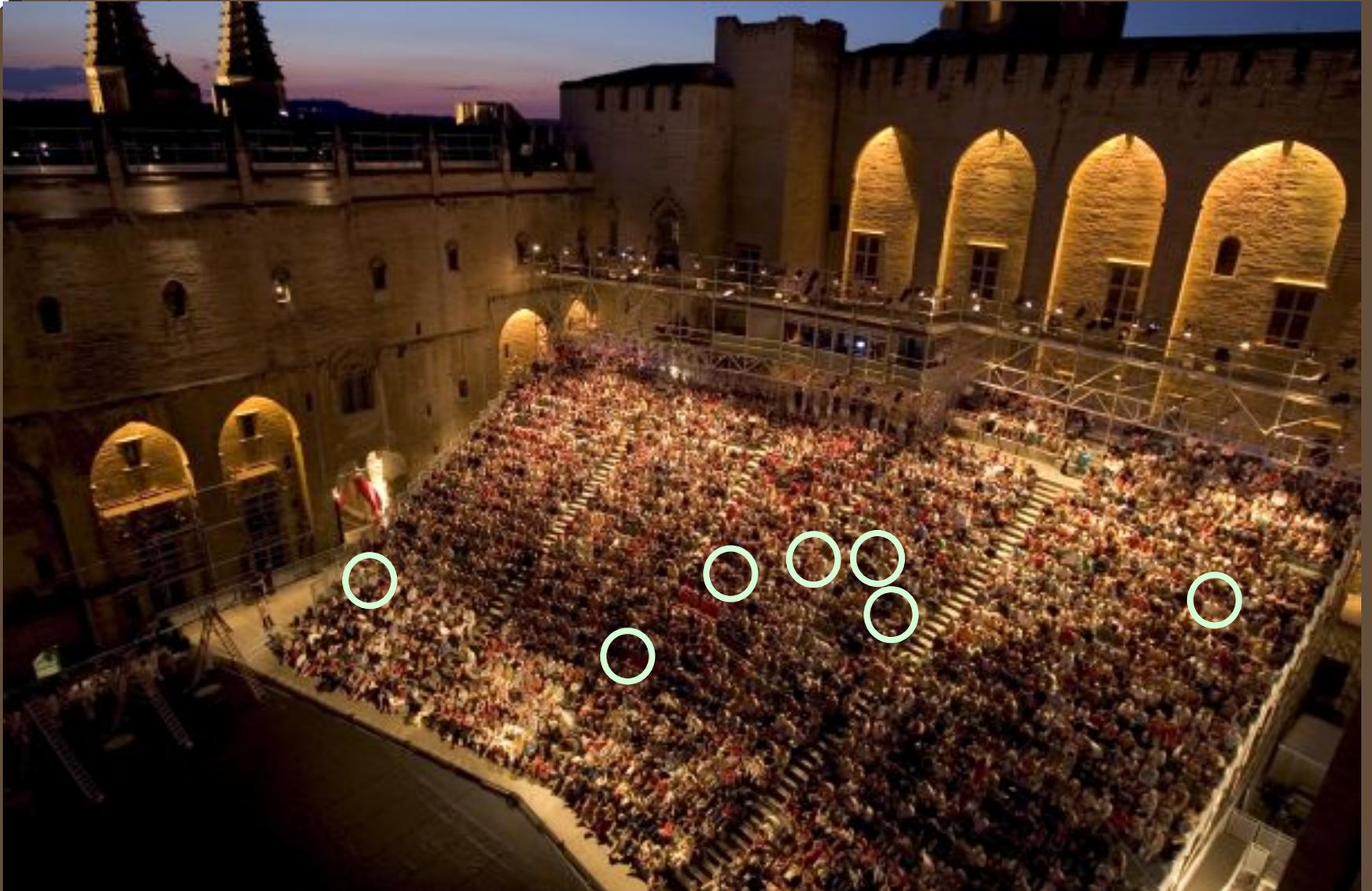
~25 satellites known
in the MW

Making a galaxy in a small halo is hard because:

Reionization heats gas above T_{vir} , preventing it from cooling and forming stars in small halos

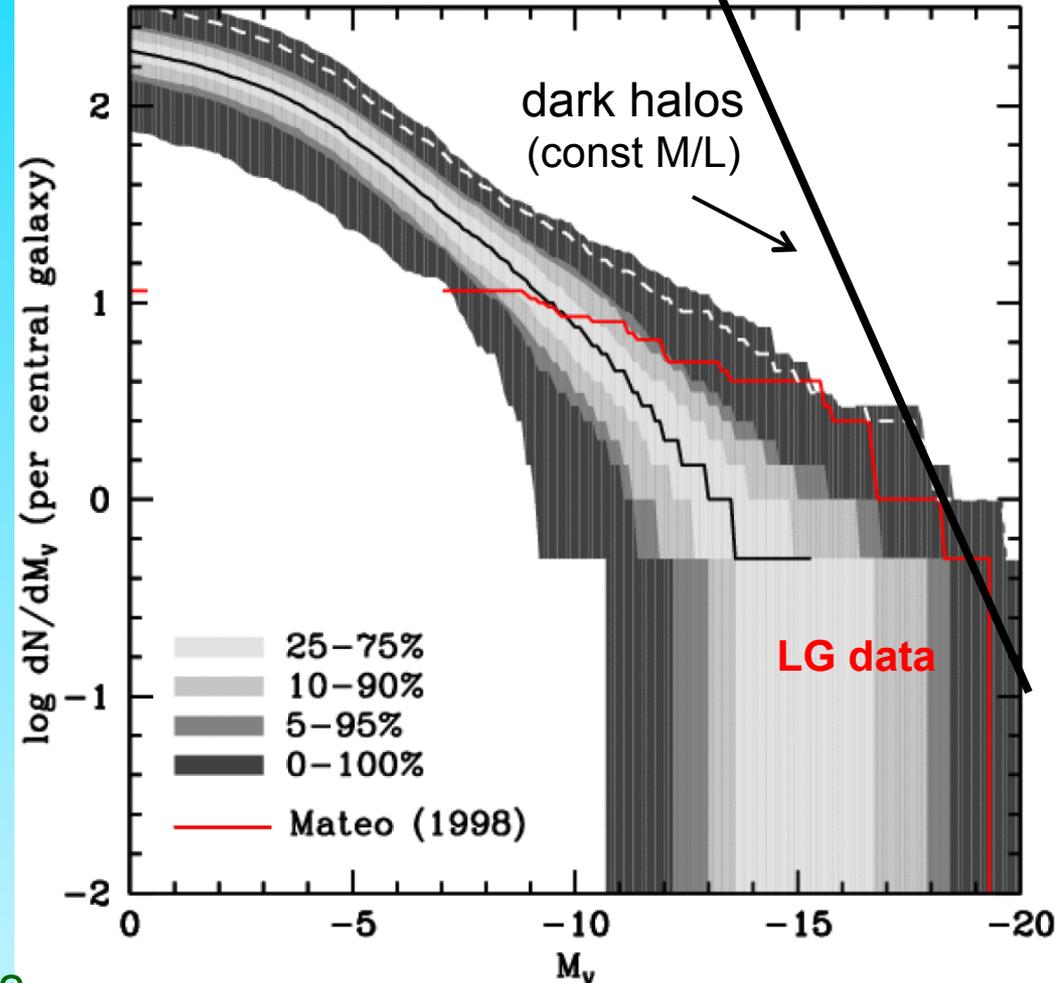
- Supernovae feedback expels gas

Most subhalos never make a galaxy!



Luminosity Function of Local Group Satellites

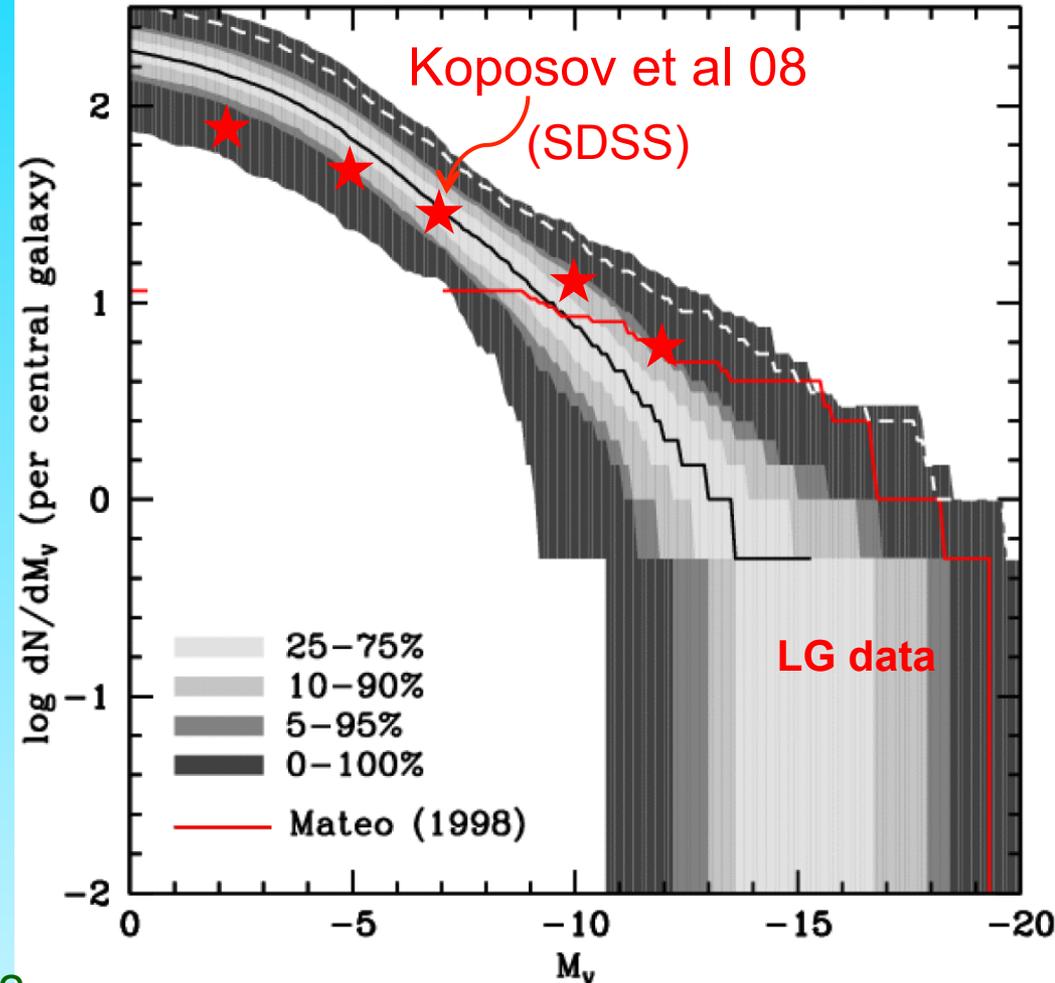
- Median model \rightarrow correct abund. of sats brighter than $M_V = -9$ and $V_{\text{cir}} > 12$ km/s
- Model predicts many, as yet undiscovered, faint satellites
- LMC/SMC should be rare ($\sim 2\%$ of cases)



Benson, Frenk, Lacey, Baugh & Cole '02
 (see also Kauffman et al '93, Bullock et al '01)

Luminosity Function of Local Group Satellites

- Median model → correct abund. of sats brighter than $M_V = -9$ and $V_{\text{cir}} > 12$ km/s
- Model predicts many, as yet undiscovered, faint satellites
- LMC/SMC should be rare (~2% of cases)

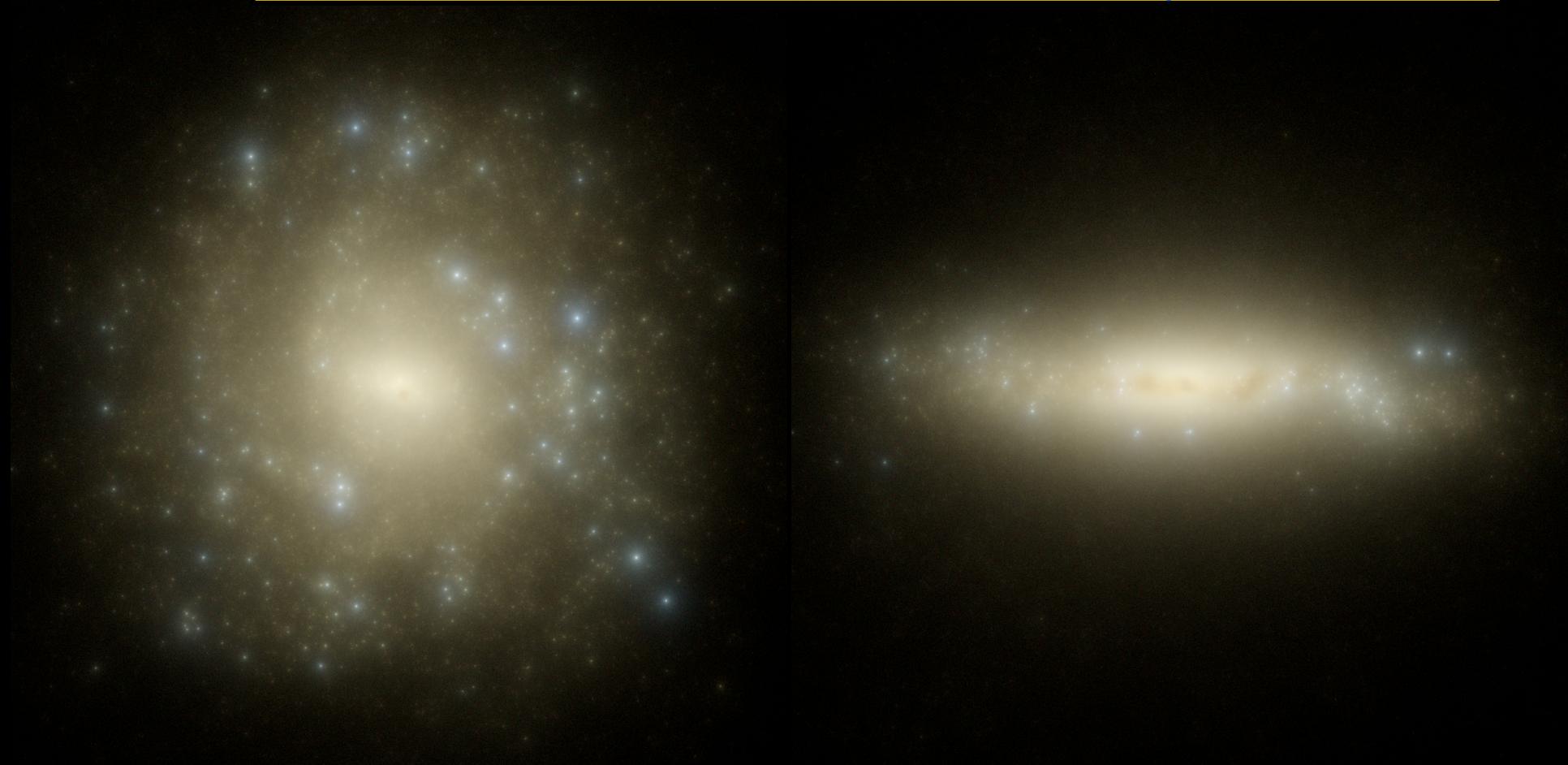


Benson, Frenk, Lacey, Baugh & Cole '02
(see also Kauffman et al '93, Bullock et al '01)



Hydrodynamic simulations

Eagle (Evolution and Assembly of galaxies
and their environment)



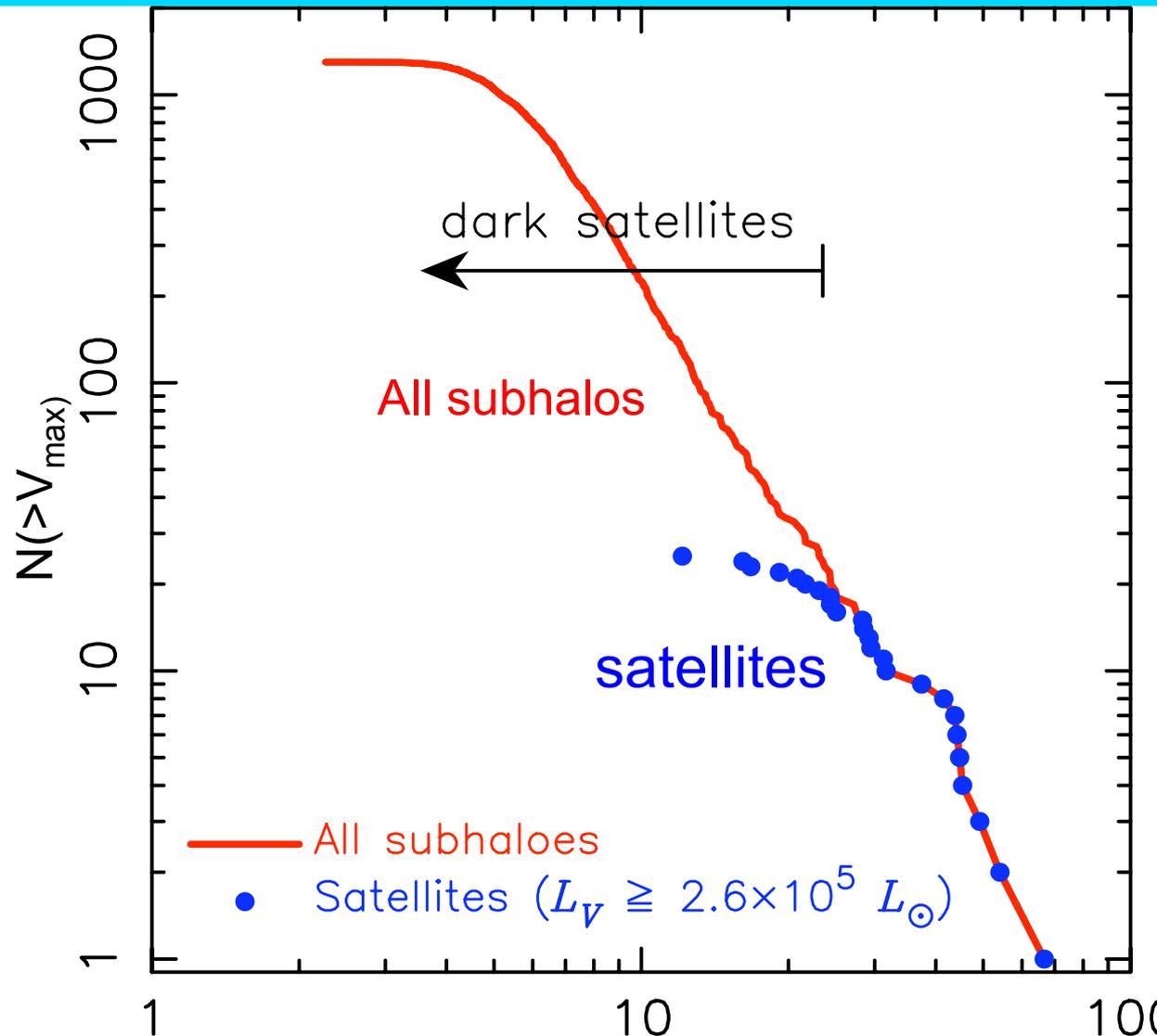
Circular velocity functions

Full hydro simulations

Okamoto & Frenk '10

- All subhalos with $v_c > 20$ km/s make a **satellite** of $L > 2.6 \times 10^5 L_\odot$

- Satellite formation **inhibited** in subhalos of $v_{\max} < 20$ km/s today (12 km/s at $z=9$)



The "satellite problem" in CDM

theguardian | TheObserver

The climate change deniers have won

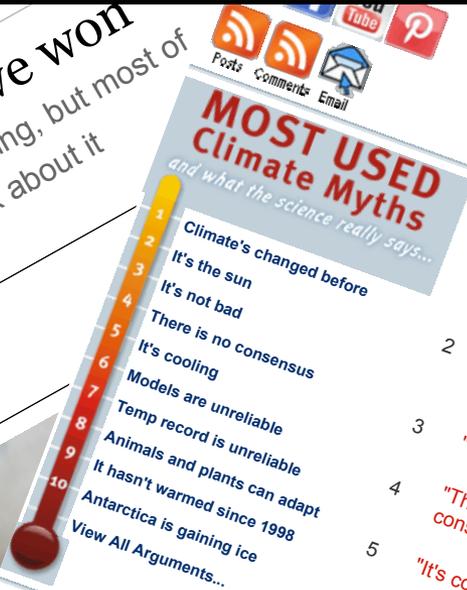
Scientists continue to warn us about global warming, but most of us are interested in not wanting to think about it

Does NOT exist !



Smoke billows as an area of the Amazon rainforest is burnt to clear land.
Doce/Reuters

The American Association for the Advancement of Science C...
respectable institution can to screaming an alarm last week. "A...
role to tell people what they should do," it said as it began one of L...
you know will build to a "but" : "But human-caused climate risks abn...
essentially irreversible changes."



IPCC FACTS Guide to RCPS
the consensus project TREND CALCULATOR

Global Warming & Climate Change Myths

Here is a summary of global warming and climate change myths, sorted by popularity vs what science says. Click the response for a more detailed response, also view them sorted by taxonomy, by popularity, in a print-friendly version, URLs or with fixed numbers you can use for permanent references.

- | Climate Myth | vs | What the Science Says |
|----------------------------------|----|---|
| 1 "Climate's changed before" | | Climate reacts to whatever forces it to change at the time; humans are now the dominant forcing. |
| 2 "It's the sun" | | In the last 35 years of global warming, sun and climate have been going in opposite directions |
| 3 "It's not bad" | | Negative impacts of global warming on agriculture, health & environment far outweigh any positives. |
| 4 "There is no consensus" | | 97% of climate experts agree humans are causing global warming. |
| 5 "It's cooling" | | The last decade 2000-2009 was the hottest on record. |
| 6 "Models are unreliable" | | Models successfully reproduce temperatures since 1900 globally, by land, in the air and the ocean. |
| 7 "Temp record is unreliable" | | The warming trend is the same in rural and urban areas, measured by thermometers and satellites. |
| 8 "Animals and plants can adapt" | | Global warming will cause mass extinctions of species that cannot adapt on short time scales. |
| 9 "It hasn't warmed since 1998" | | For global records, 2010 is the hottest year on record, tied with 2005. |

MW has only 3 very massive satellites: $V_{\max} > 30$ km/s
($\rightarrow M_{\text{sat}} > 0.01 M_{\text{MW}}$) \rightarrow LMC, SMC, Sagittarius

MW has only 3 very massive satellites: $V_{\max} > 30$ km/s
($\rightarrow M_{\text{sat}} > 0.01 M_{\text{MW}}$) \rightarrow LMC, SMC, Sagittarius

This CDM example ($M_{\text{halo}} = 2 \times 10^{12} M_{\odot}$) has
10 massive satellites with $V_{\max} > 30$ km/s

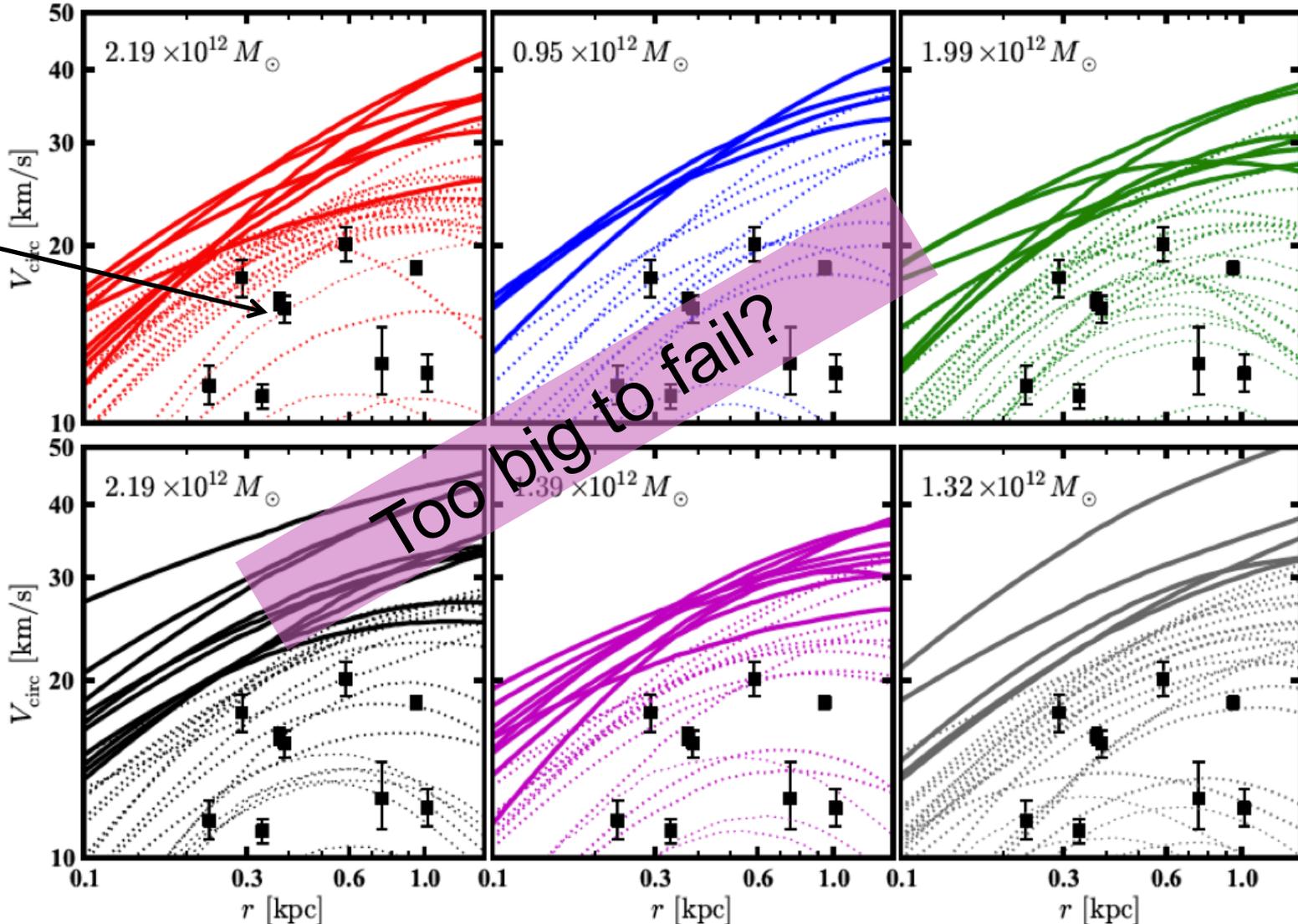
Rotation curves of Aquarius subhalos

Boylan-Kolchin et al. '11

$$V_c = \sqrt{\frac{GM}{r}}$$

9 dwarf satellites of Milky Way: mass within half-light radius

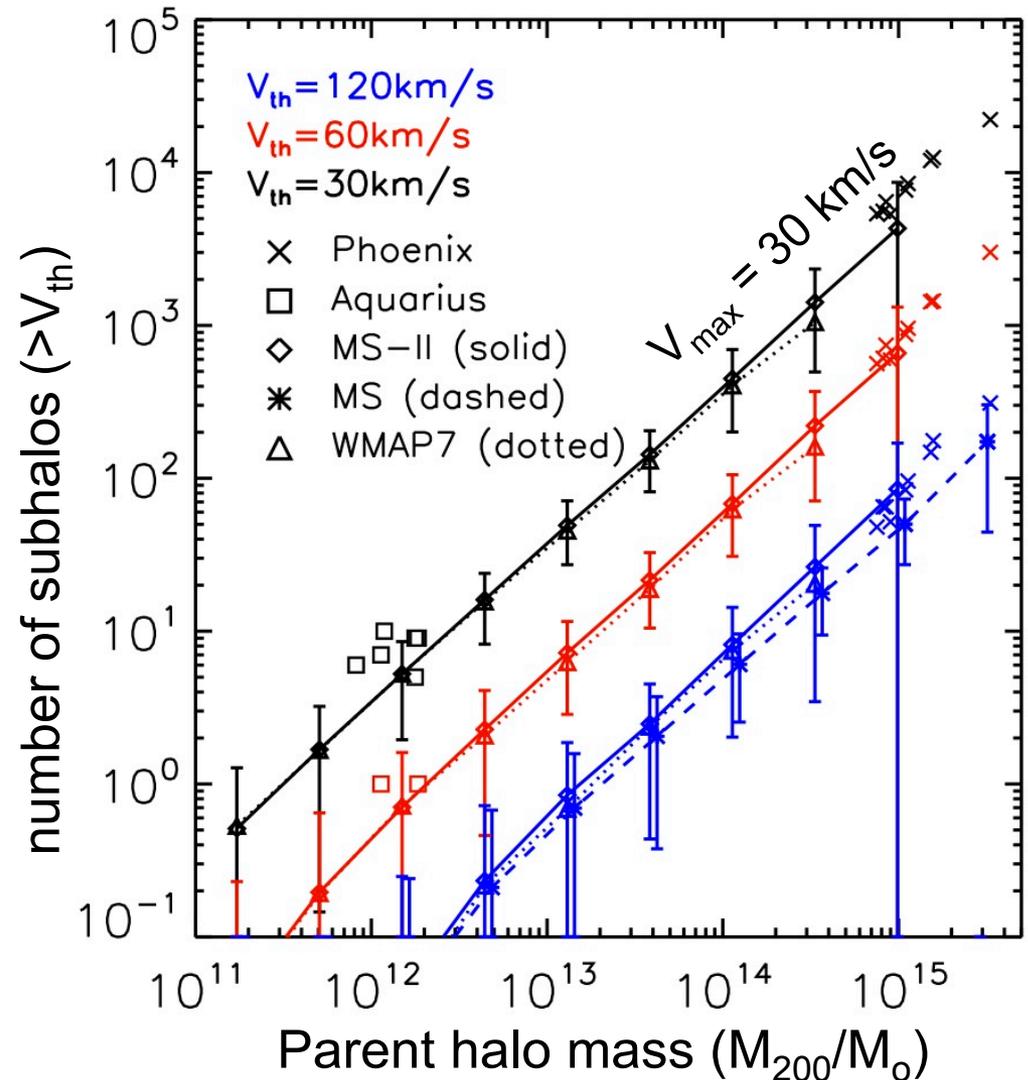
Excludes LMC, SMC, Sagittarius



Number of massive subhalos

Number of massive subhalos increases rapidly with halo mass

→ Milky Way halo mass cannot be too large if CDM is right!



Probability of massive subhalos

Probability of having at least 3 subhalos with $V_{\text{max}} > 30 \text{ km/s}$

1 - prob. that ΛCDM is ruled out

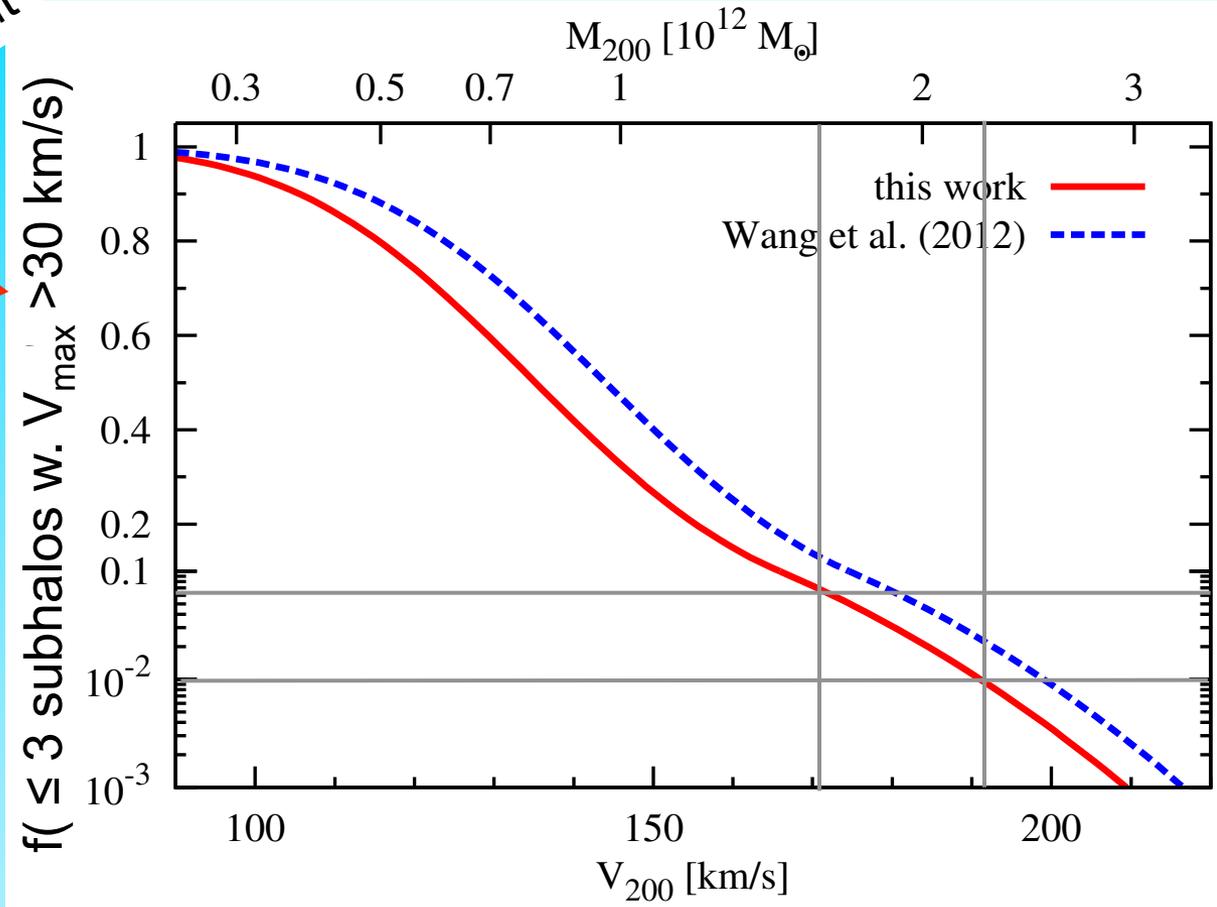
Depends strongly on M_{200} (and V_{cut})

CDM requires

$$M_{\text{halo}} < 1.5 \times 10^{12} M_{\odot}$$

(95% confidence)

If mass of MW halo $> 2.2 \times 10^{12} M_{\odot}$ pure CDM is ruled out (99% conf)



Wang, Frenk, Navarro, Gao '12
 Cautun, Frenk, van den Weygaert, Hellwing '14



University of Durham

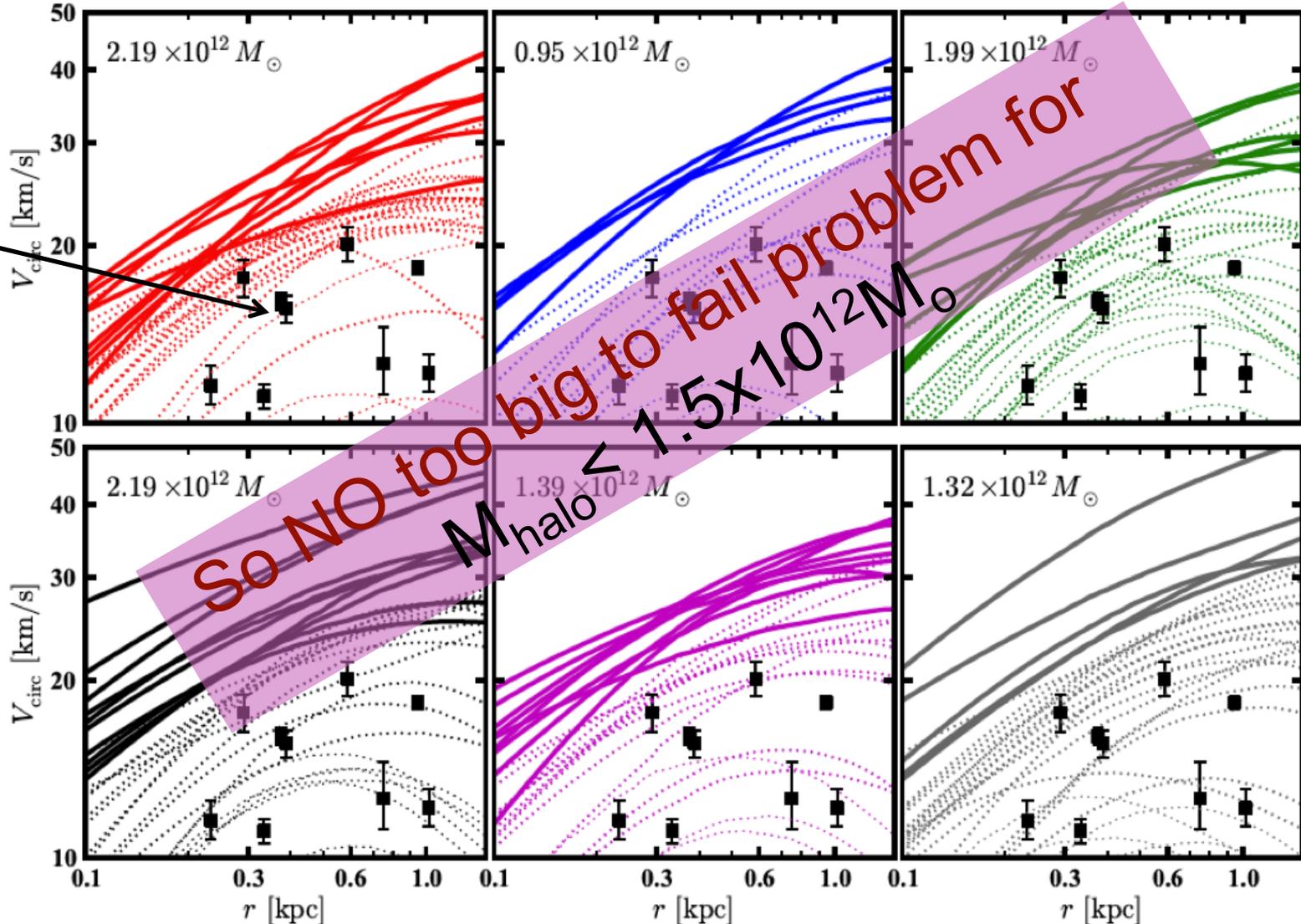
Rotation curves of Aquarius subhalos

Boylan-Kolchin et al. '11

$$V_c = \sqrt{\frac{GM}{r}}$$

9 dwarf satellites of Milky Way: mass within half-light radius

Excludes LMC, SMC, Sagittarius





Cosmology on small scales

- The number of satellites (the “satellite problem”)
- The structure of satellites (the “too-big-to-fail” problem)

How about WDM?



Tests of the nature of the DM

cold dark matter

warm dark matter

WDM does not suffer from the “too-big-to-fail
problem



Lovell, Eke, Frenk, Gao, Jenkins, Wang, White, Theuns,
Boyarski & Ruchayskiy '12

Subhalo density profiles

CDM & WDM subhalos have cuspy profiles

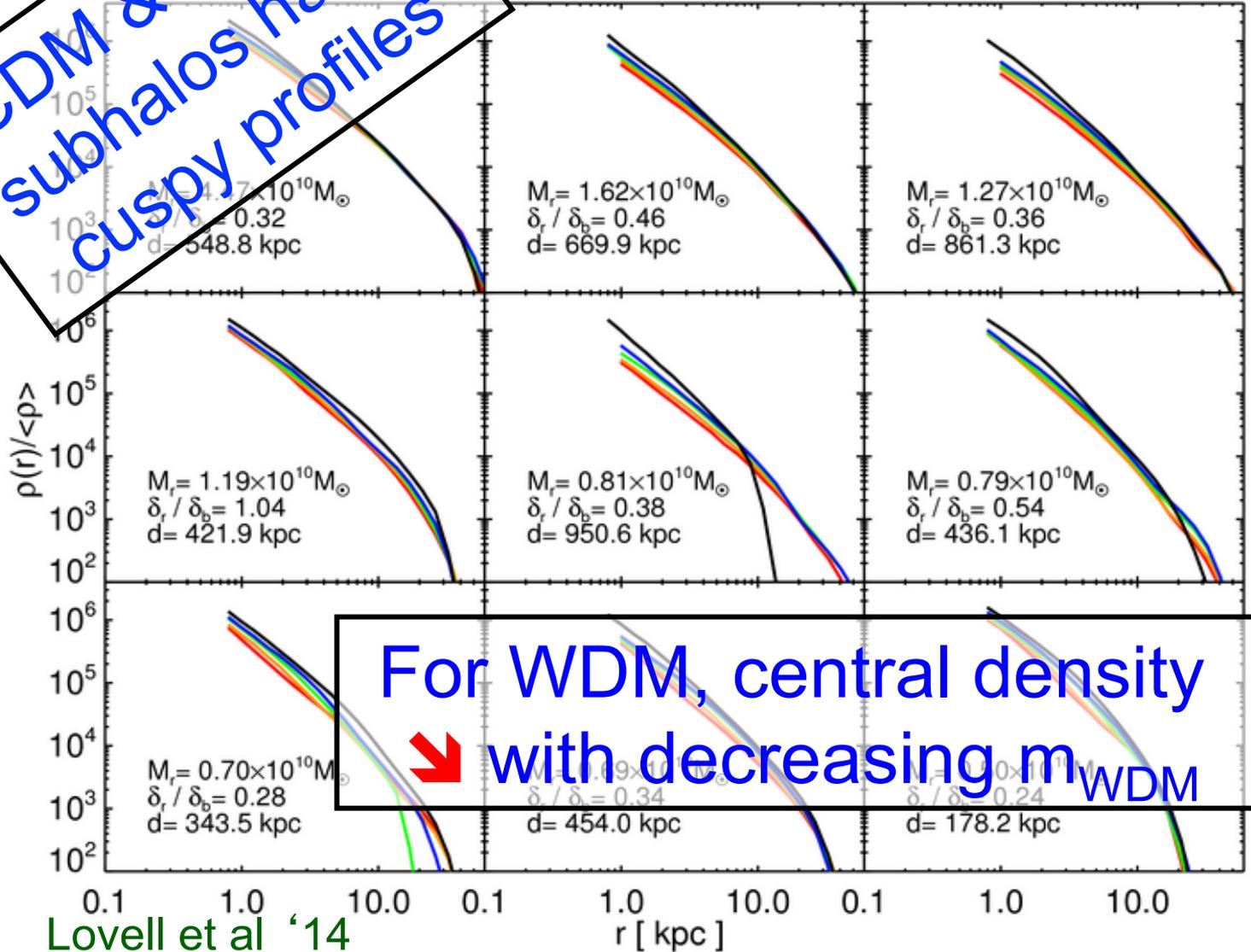
WDM

2.3 keV

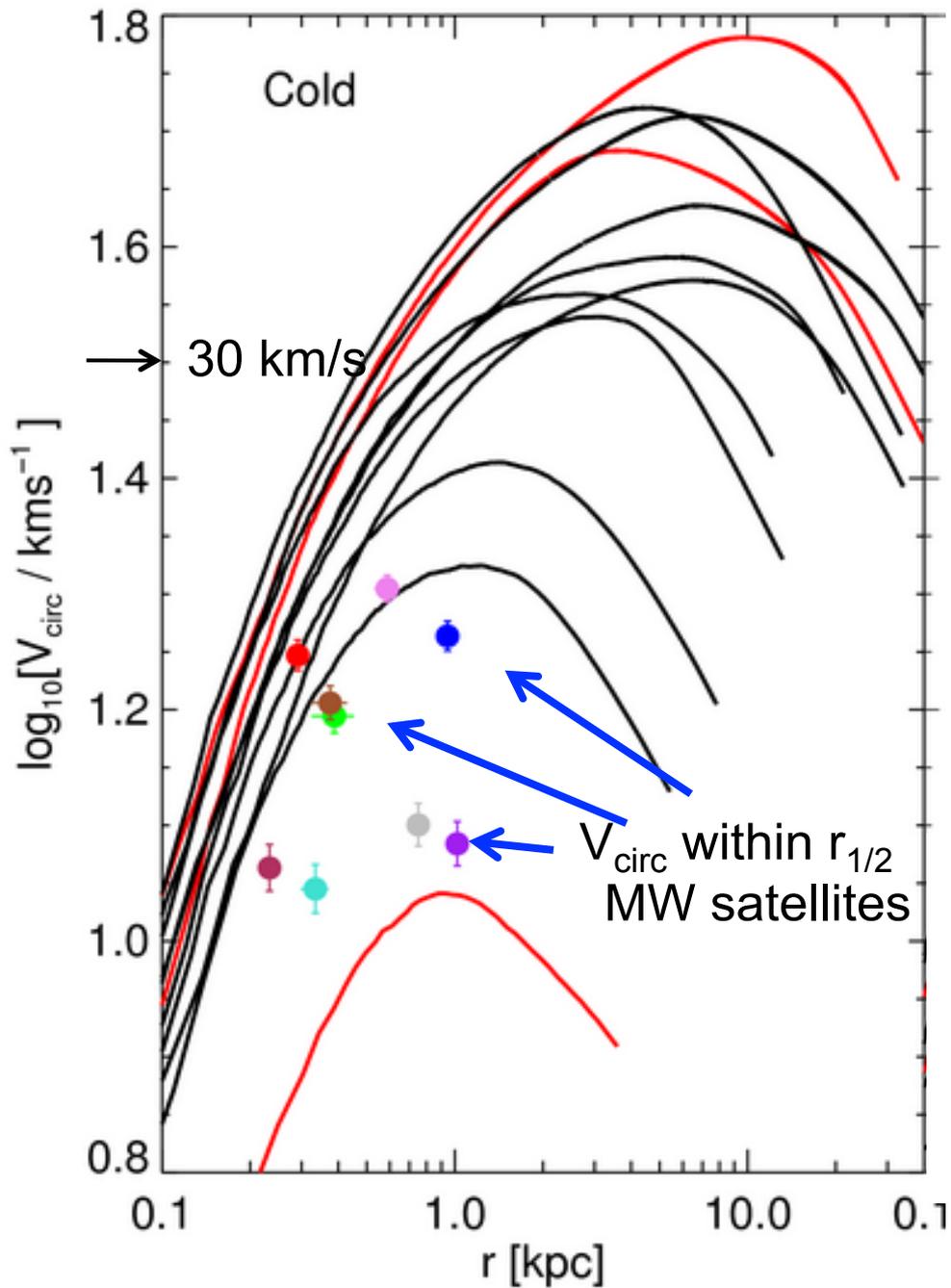
2.0 keV

1.6 keV

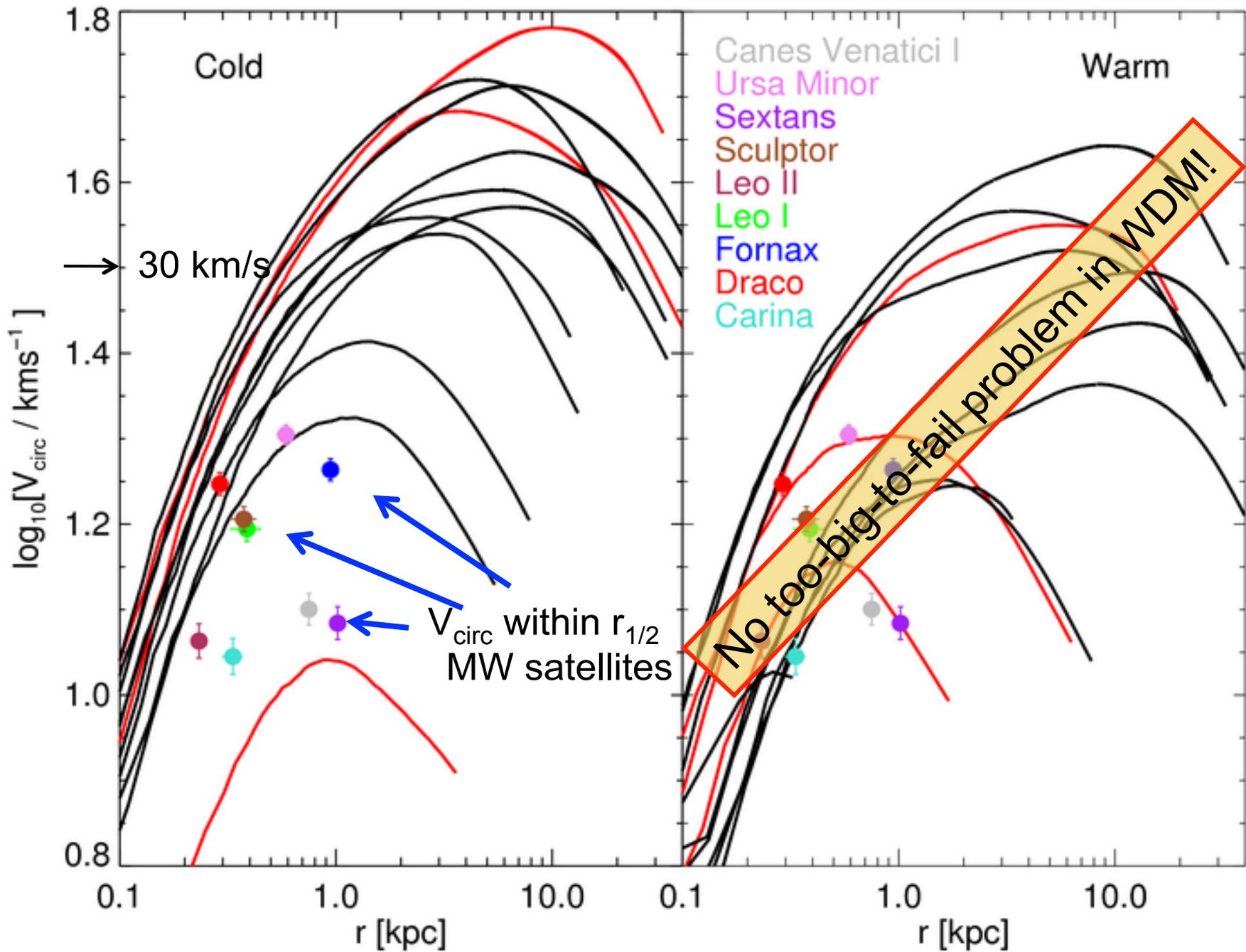
1.4 keV



For WDM, central density \uparrow with decreasing m_{WDM}



Lovell, Eke, Frenk, Gao,
Jenkins, Wang, White, Theuns,
BoyarSKI & Ruchayskiy '11





Cosmology on small scales

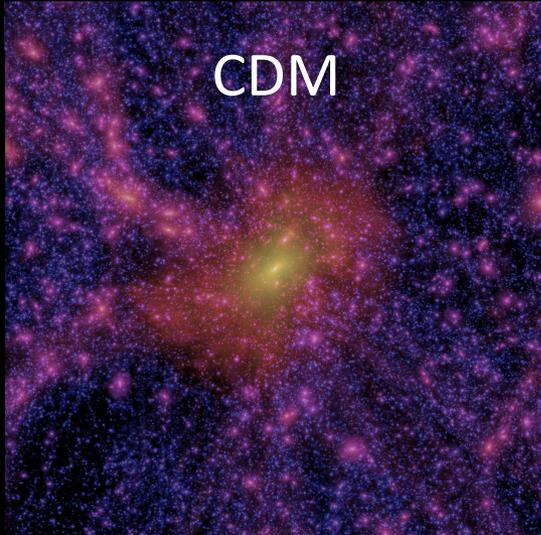
- The number of satellites (the “satellite problem”)
- ✓ • The structure of satellites (the “too-big-to-fail” problem)

How about WDM?

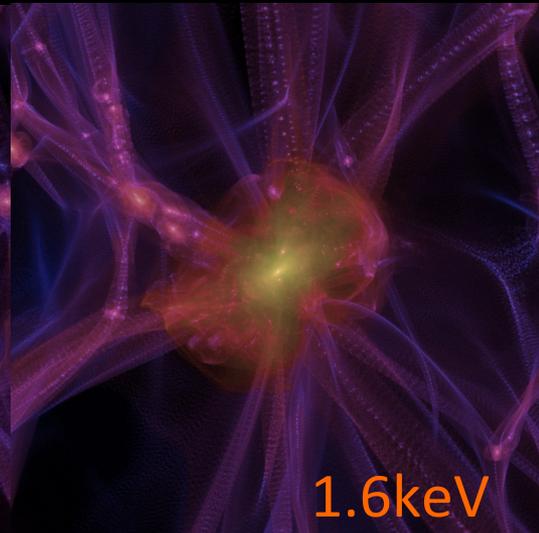
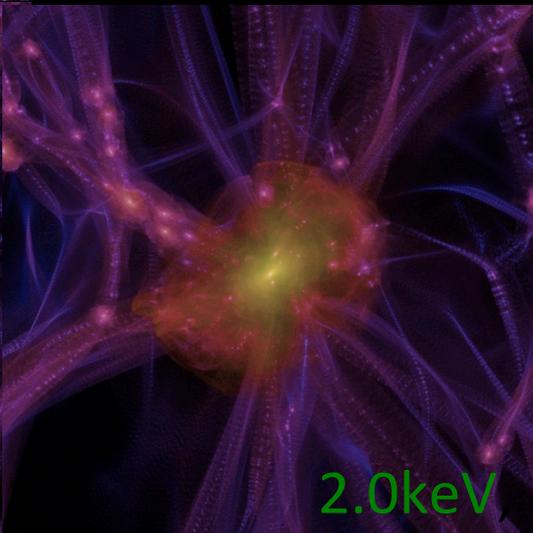
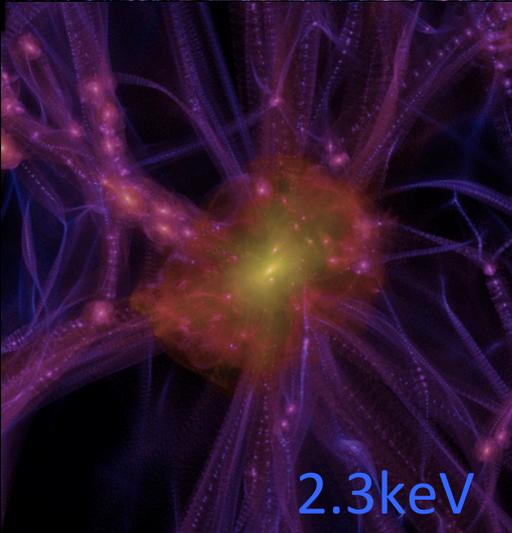
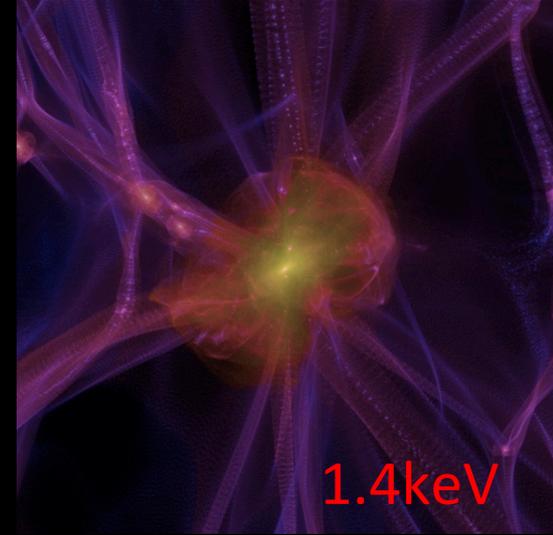
Warm DM: different ν mass

$z=3$

- WDM
- 2.3 keV
- 2.0 keV
- 1.6 keV
- 1.4 keV



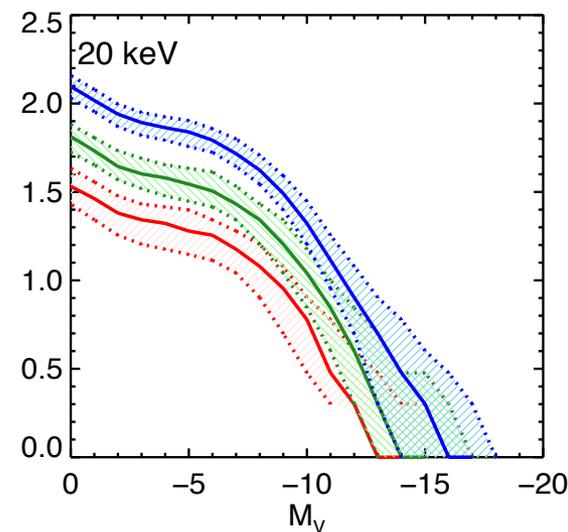
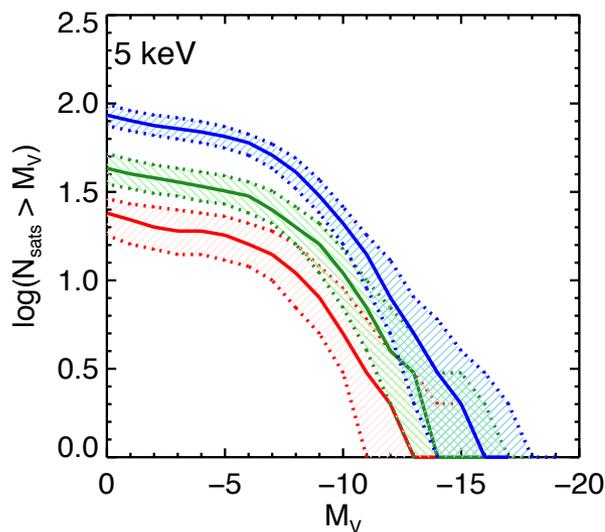
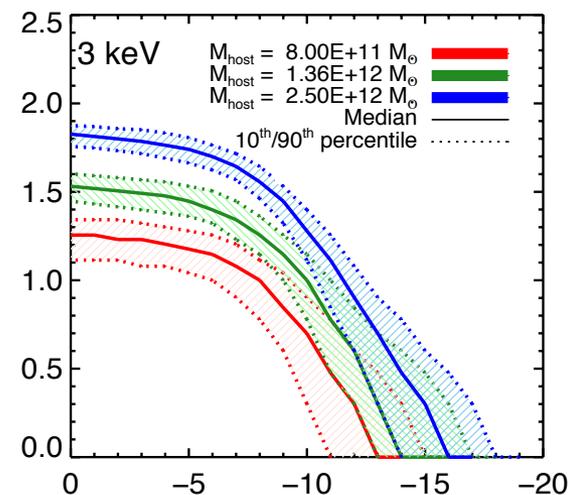
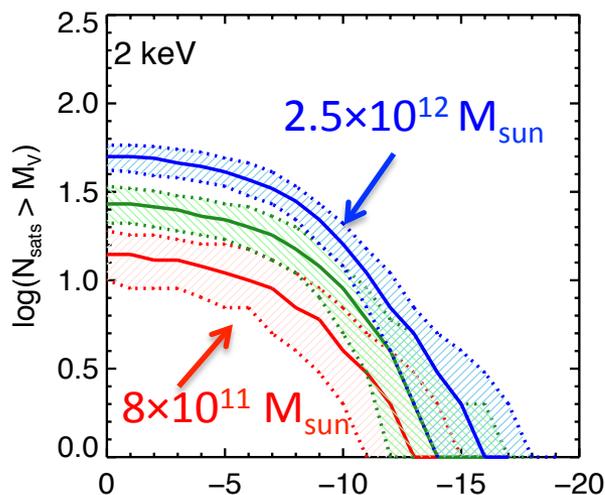
WDM



Luminosity Function of Local Group Satellites in WDM

No of sats \nearrow with:

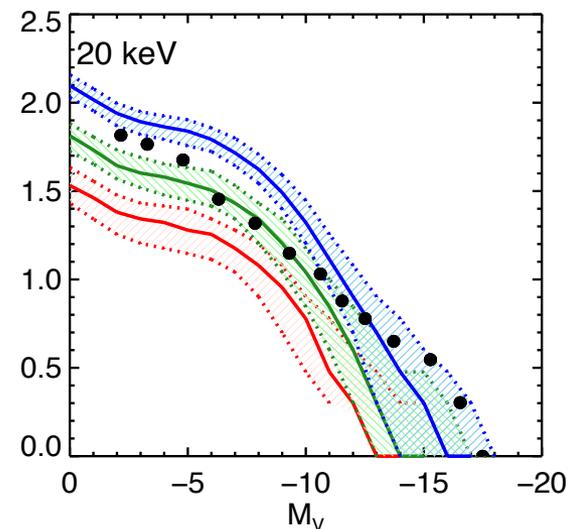
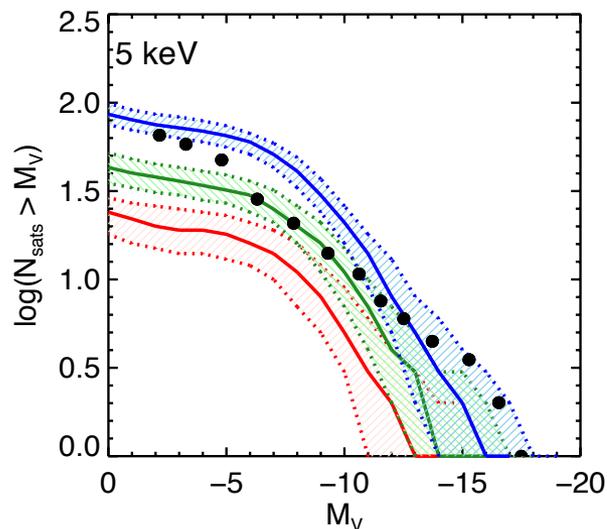
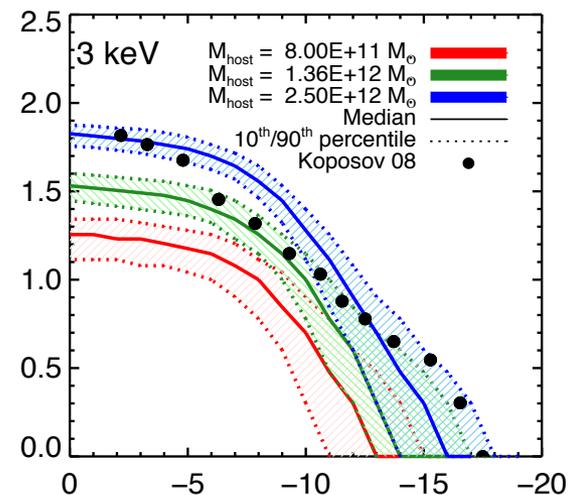
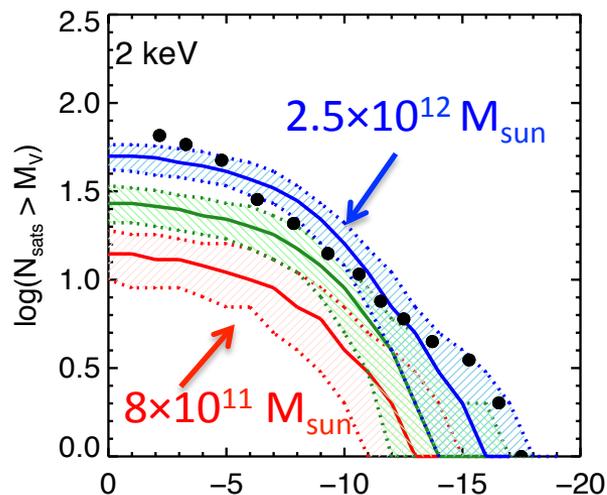
- host halo mass
- WDM particle mass



Luminosity Function of Local Group Satellites in WDM

No of sats \nearrow with:

- host halo mass
- WDM particle mass



If the halo mass is too small and/or the WDM particle mass is too small, there will not be enough subhalos to account for the observed satellites!

→ lower limit on m_{wdm}

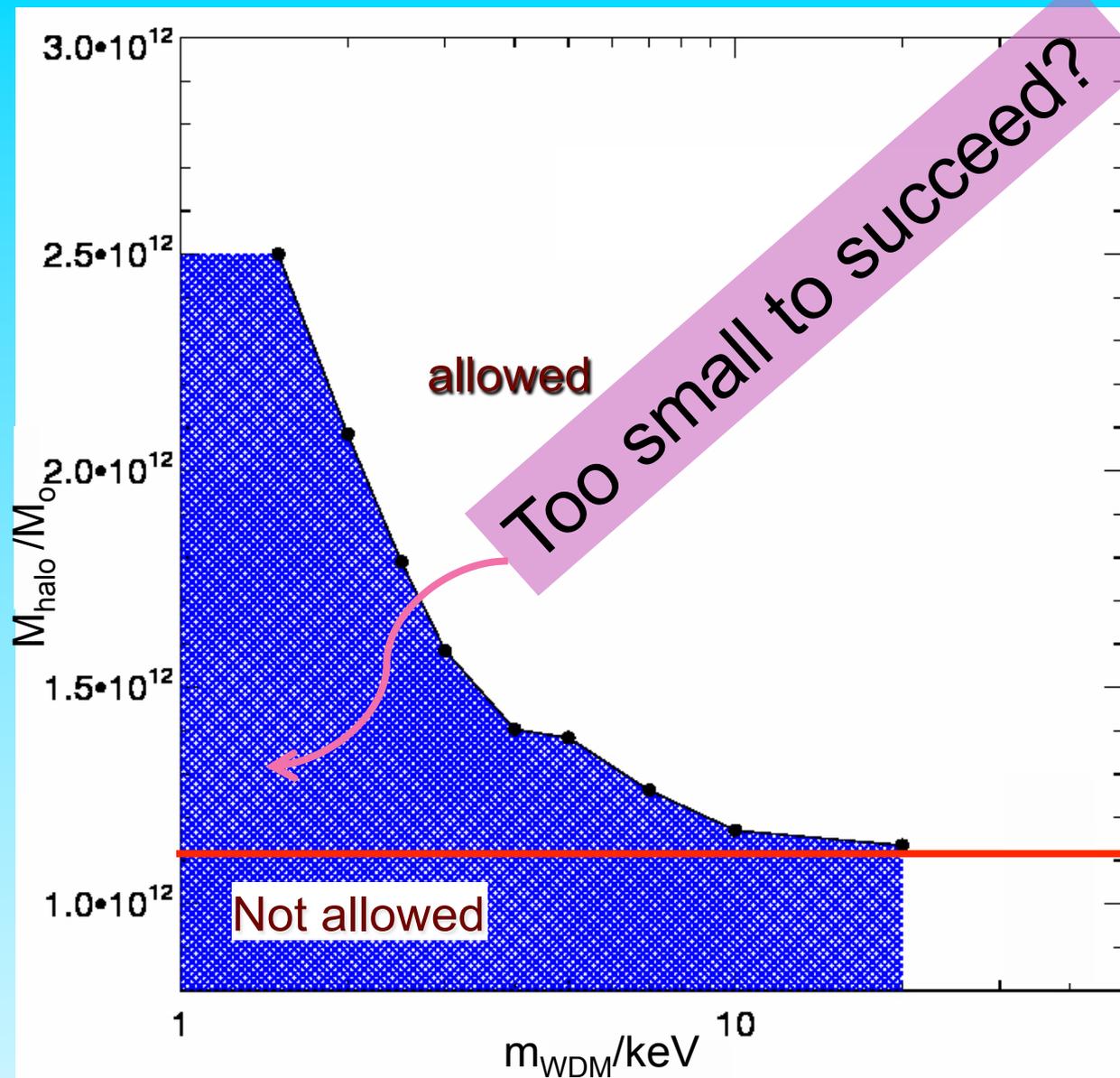


Limits on WDM particle mass

Minimum halo mass consistent (95%) with observed no. of sats for given m_{WDM}

For standard galaxy formation model, WDM ruled out if $M_{\text{halo}} < 1.1 \times 10^{12} M_{\odot}$

Kennedy, Cole & Frenk '14

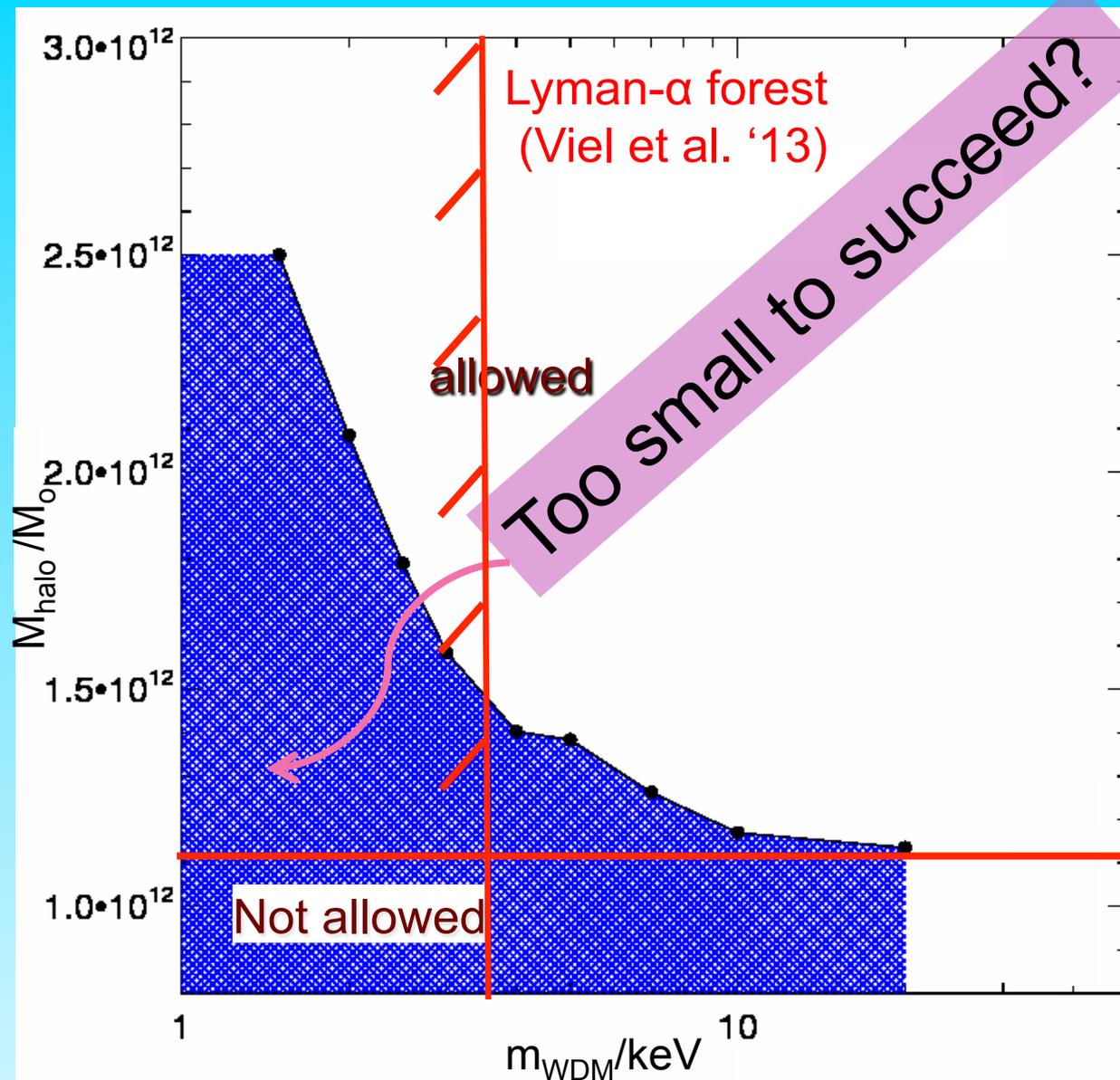


Limits on WDM particle mass

Minimum halo mass consistent (95%) with observed no. of sats for given m_{WDM}

For standard galaxy formation model, WDM ruled out if $M_{\text{halo}} < 1.1 \times 10^{12} M_{\odot}$

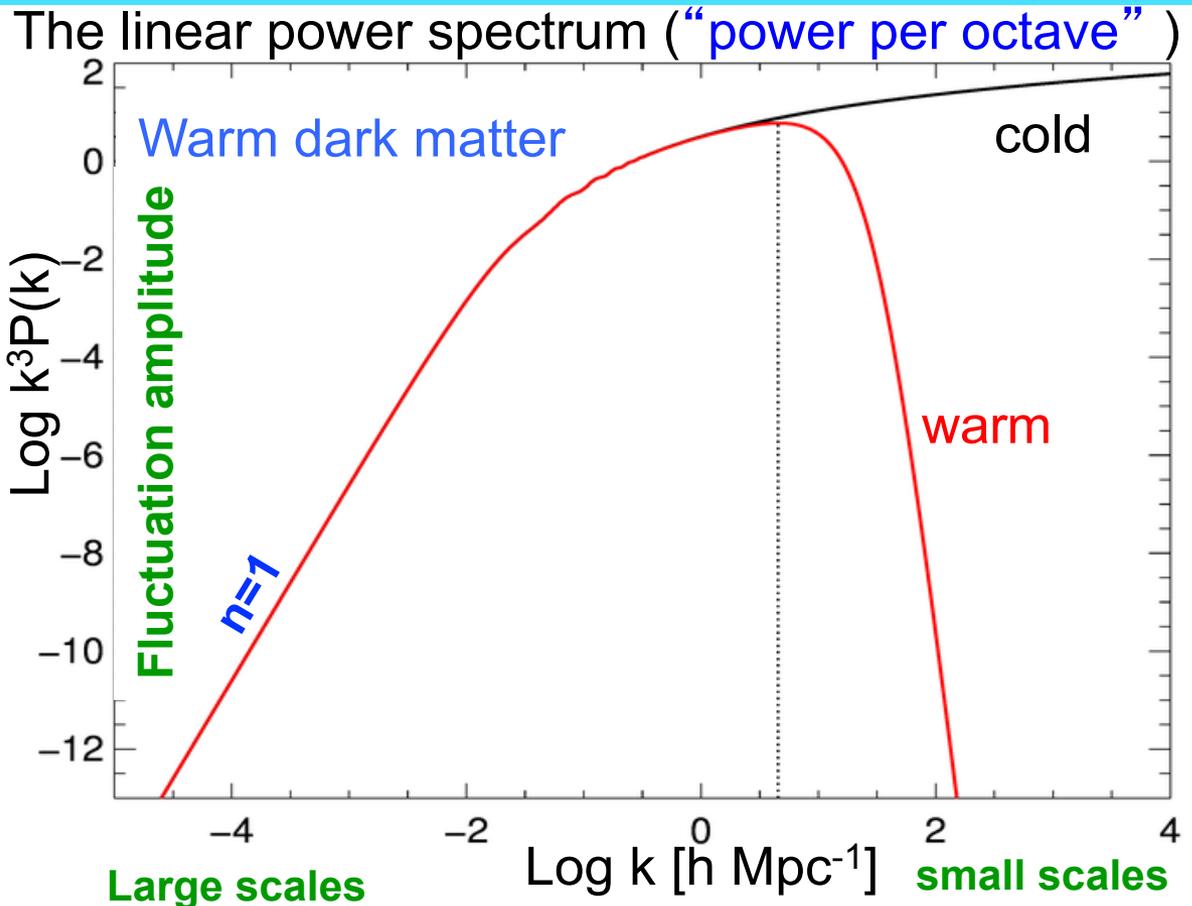
Kennedy, Cole & Frenk '14



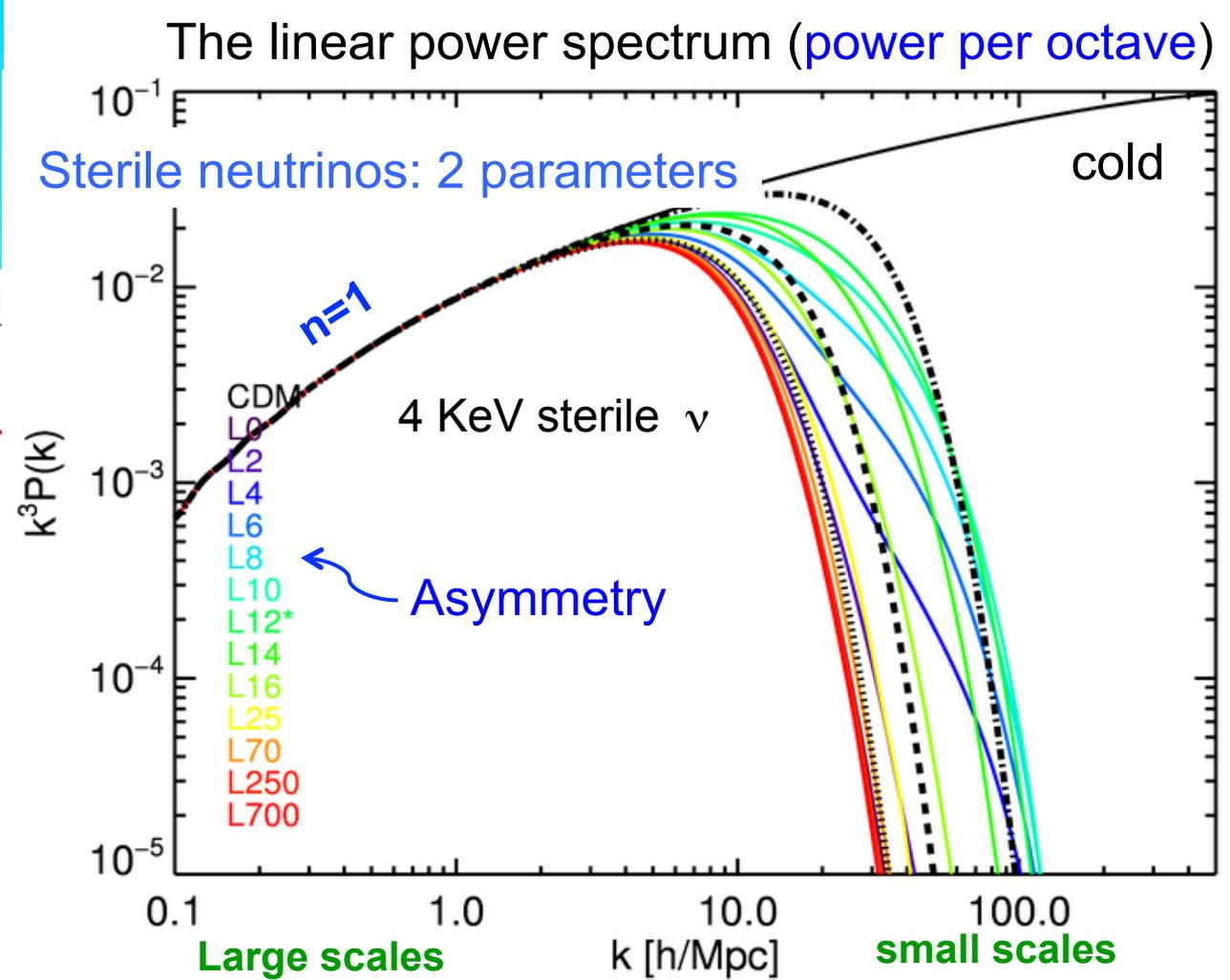
Estimates of the MW halo mass

- Li & White $\rightarrow M_{200} = 2.4 \times 10^{12} M_{\odot}$; $M_{200} > 8 \times 10^{11} M_{\odot}$ at 95% CL
- Guo et al $\rightarrow 8 \times 10^{11} M_{\odot} < M_{200} < 4.7 \times 10^{12} M_{\odot}$
- Deason et al $\rightarrow 5 \times 10^{11} M_{\odot} < M_{150\text{kpc}} < 1 \times 10^{12} M_{\odot}$
- Xue et al $\rightarrow 8 \times 10^{11} M_{\odot} < M_{100} < 1.3 \times 10^{12} M_{\odot}$
- Battaglia et al $\rightarrow 6 \times 10^{11} M_{\odot} < M_{100} < 3 \times 10^{12} M_{\odot}$

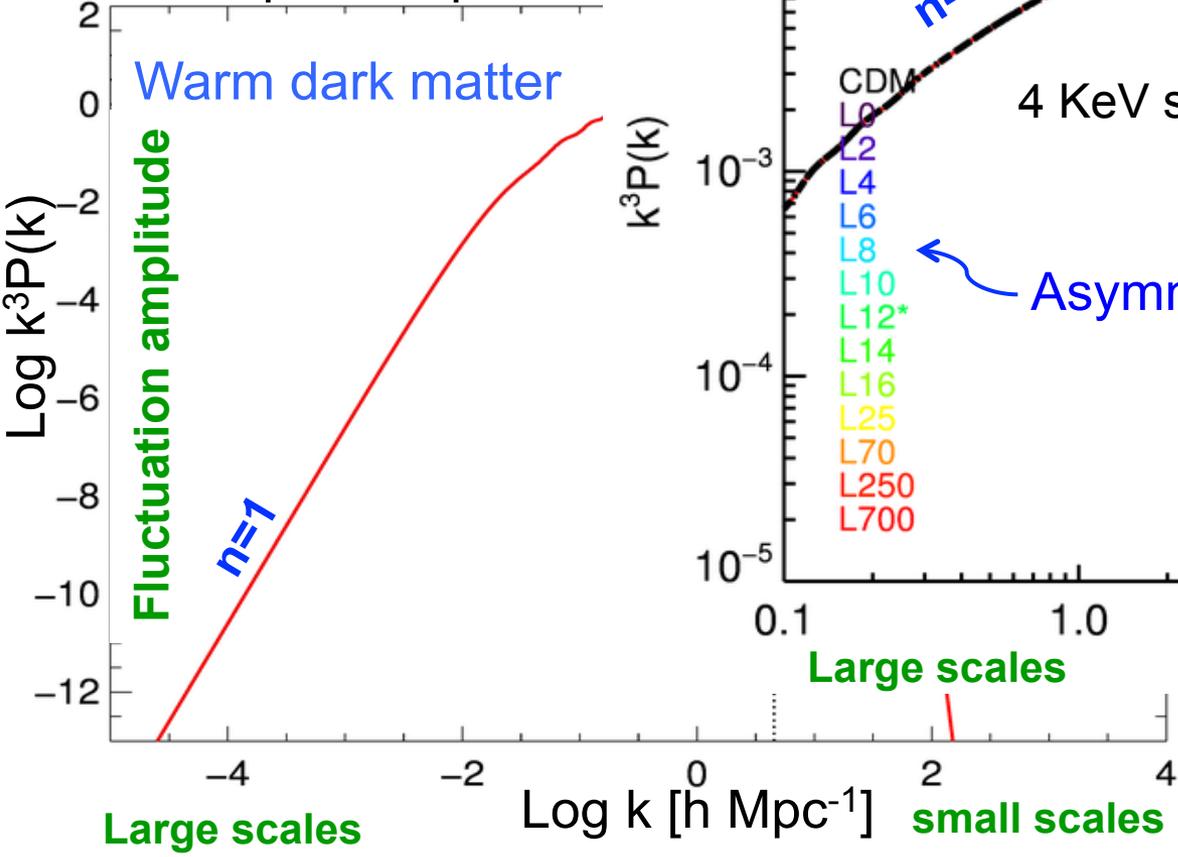
Warm dark matter



Sterile neutrinos



The linear power spectrum

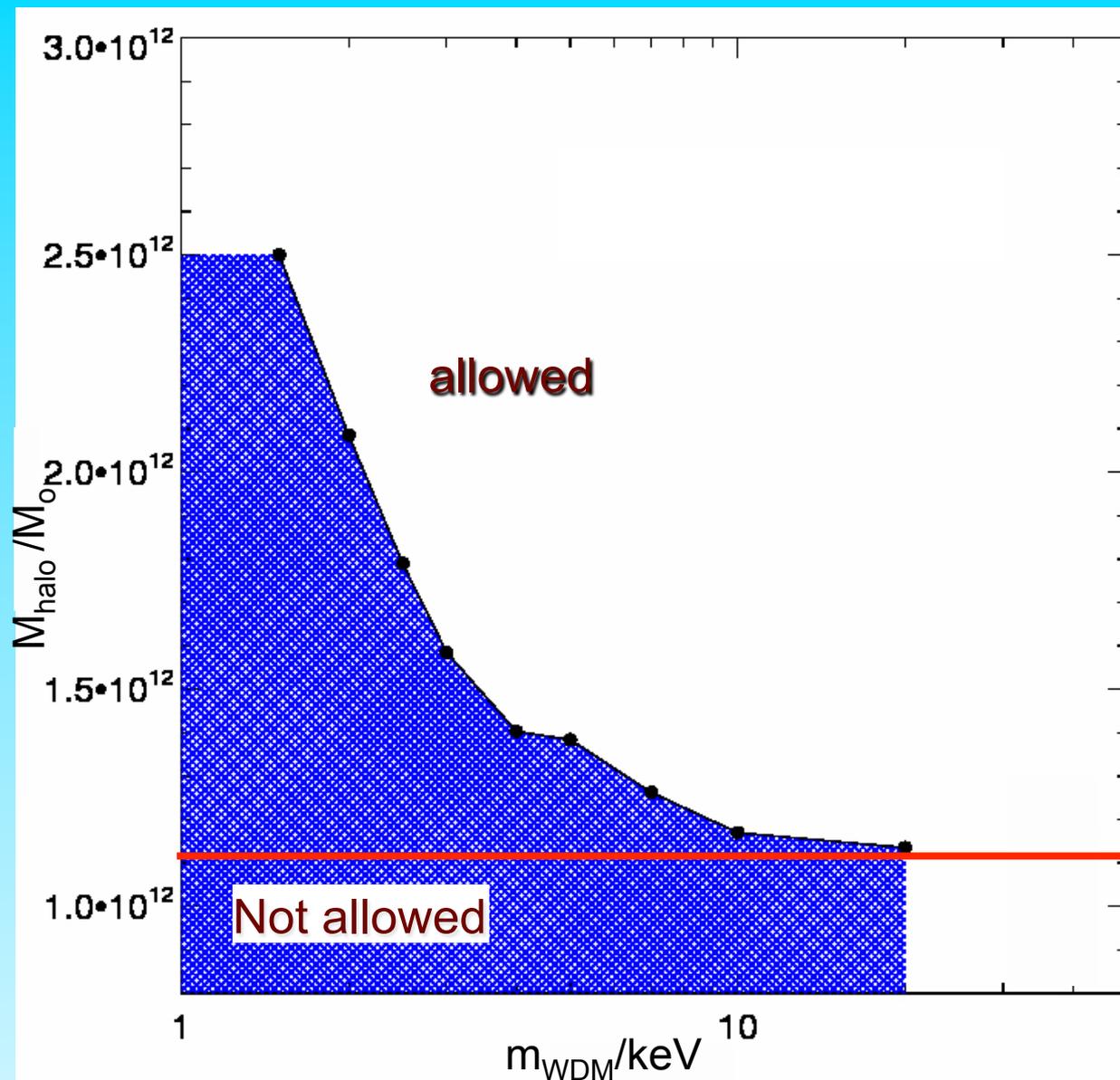


Limits on WDM particle mass

Minimum halo mass consistent (95%) with observed no. of sats for given m_{WDM}

For standard galaxy formation model, WDM ruled out if $M_{\text{halo}} < 1.1 \times 10^{12} M_{\odot}$

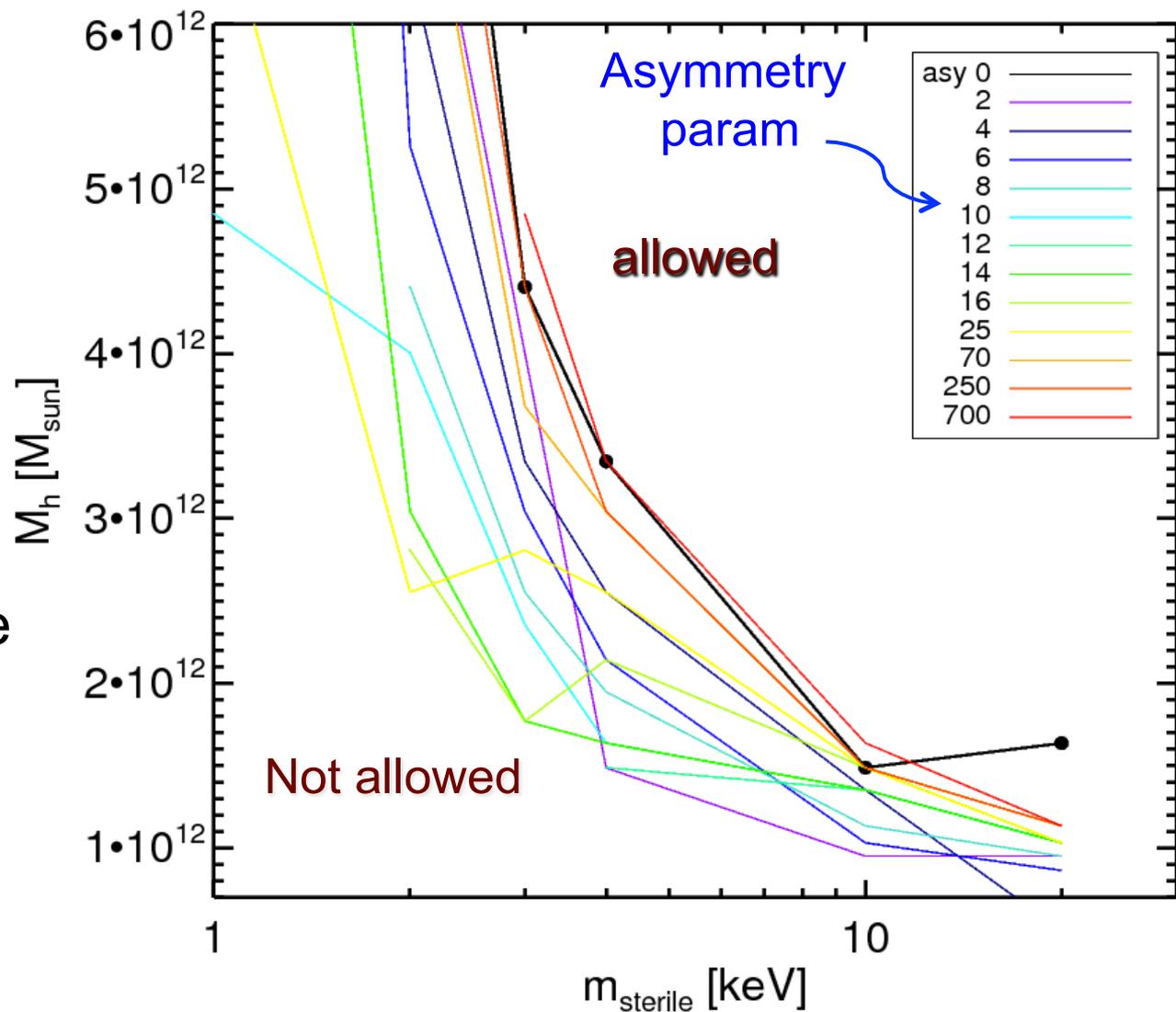
Kennedy, Cole & Frenk '14



Limits on sterile neutrino mass

In ν MSM, the mass power spectrum can be described by 2 params: m_ν and an asymmetry param.

The constraints on the mass generally become weaker



Constraints on CDM & WDM from the Milky Way satellites

With our standard assumptions: at 95% confidence

Cold dark matter :

Ruled out unless $M_{\text{halo}} < 1.5 \times 10^{12} M_{\odot}$

(from abundance of massive satellites)

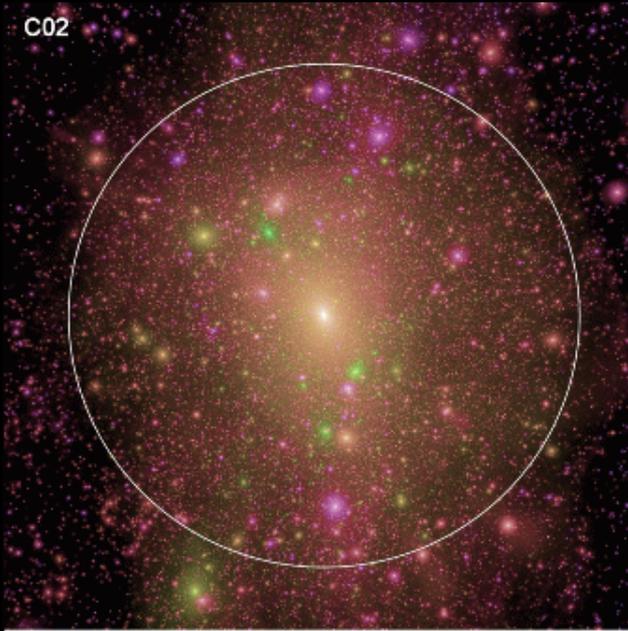
Unless baryon effects are important

Warm dark matter :

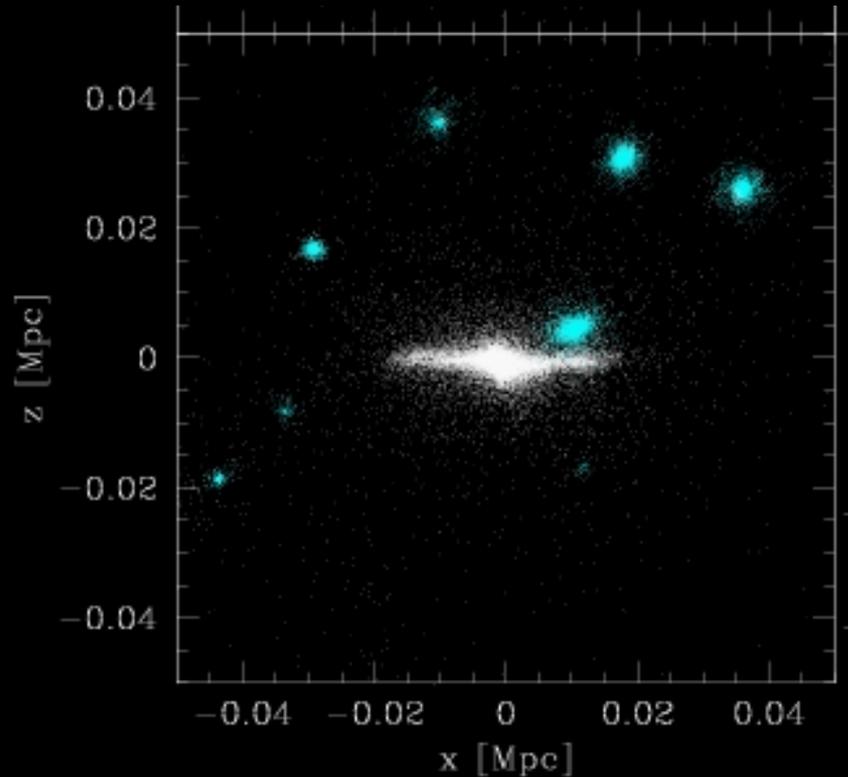
Ruled out unless $M_{\text{halo}} > 1.2 \times 10^{12} M_{\odot}$

(from abundance of satellites)

The satellites of the Milky Way

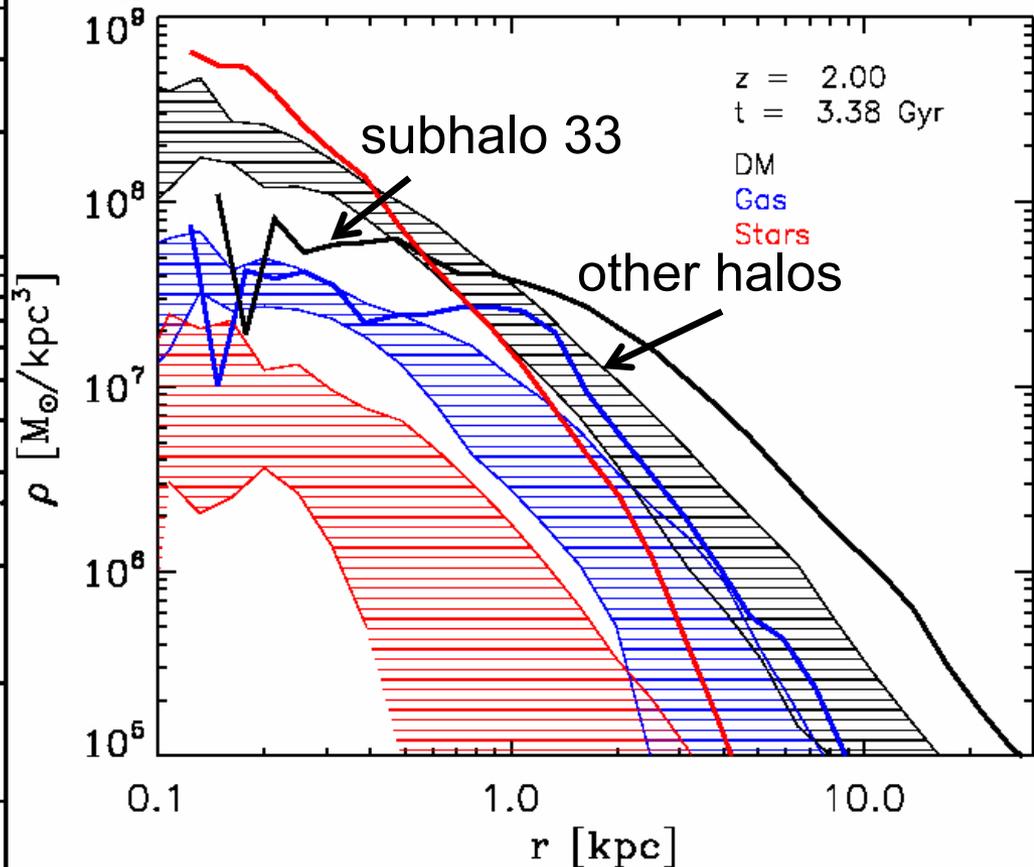
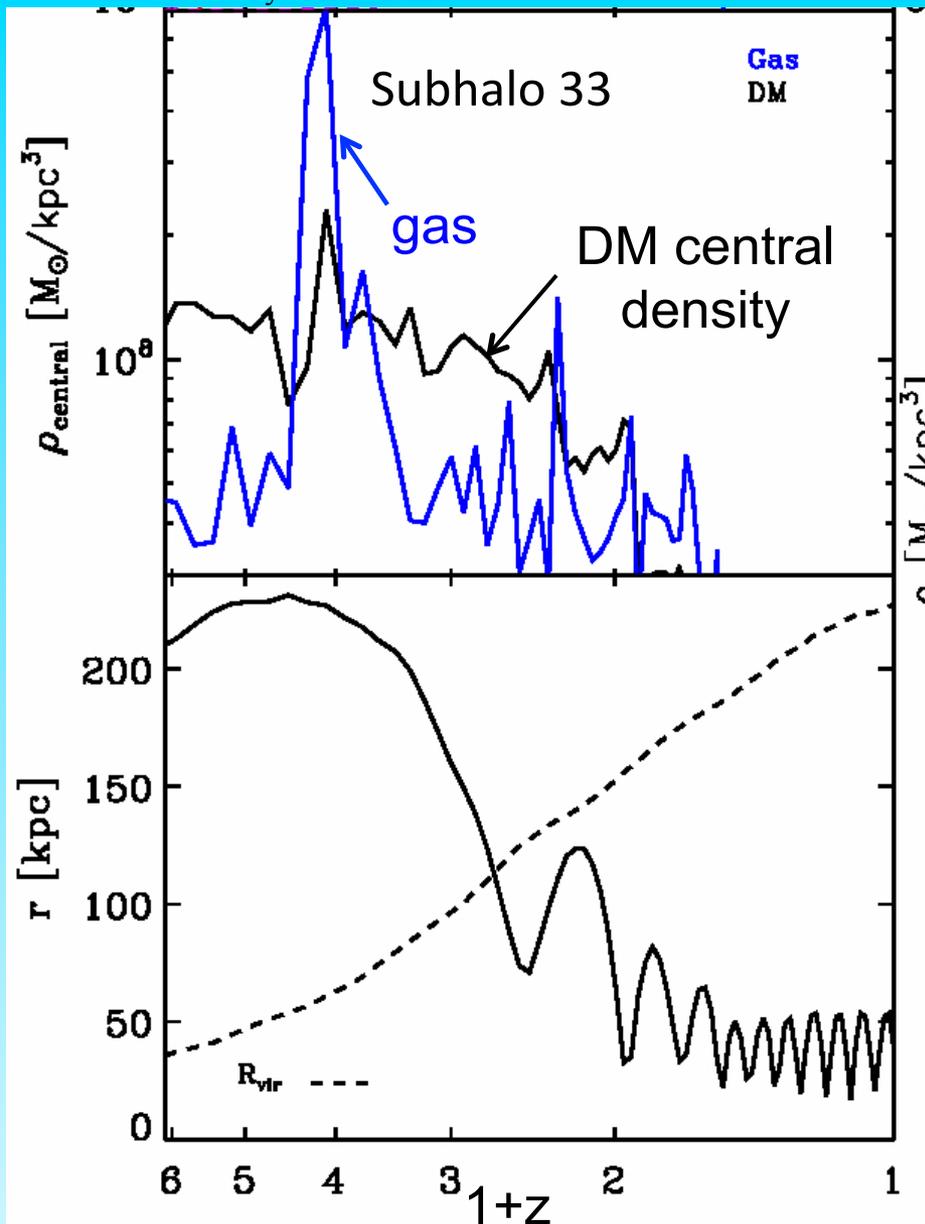


SPH simulations of galaxy formation
in one of the Aquarius halos



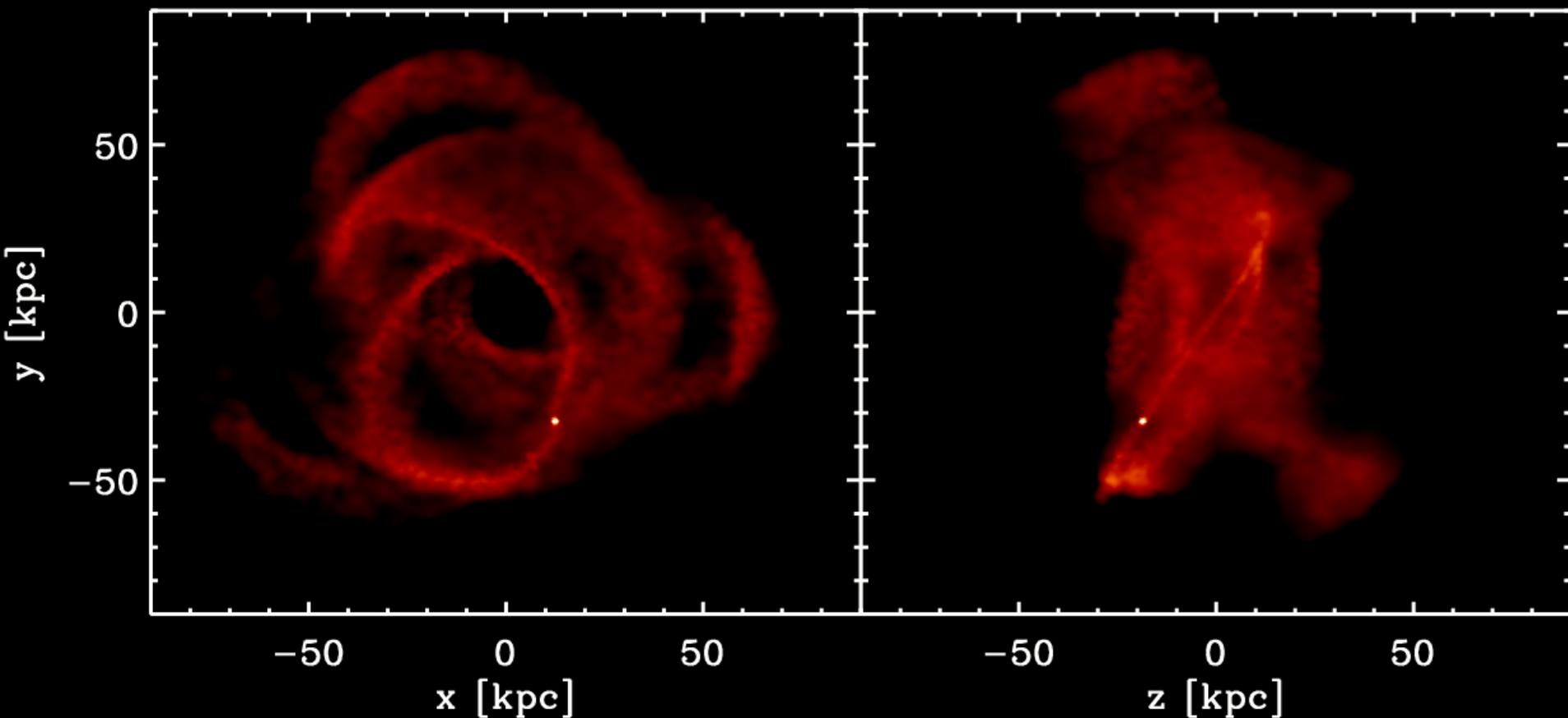
Parry, Eke, Frenk & Okamoto '11

Baryon effects in the MW satellites



Parry, Eke & Frenk '11

Subhalo 33



DM & sats of the MW: conclusions

Abundance and kinematics of MW sats set strong constraints on nature of dark matter

Key properties of sat system: 

- Luminosity function
- Abundance of most massive sats

Model	Sat Lum Fn	Massive sats	Comments
CDM	OK	$M_{\text{halo}} < 1.5 \times 10^{12} M_{\odot}$	Unless baryon effects reduce central density 
WDM	$M_{\text{halo}} > 1.2 \times 10^{12} M_{\odot}$	OK	+ X-ray constraint $M_{\text{halo}} > 1.5 \times 10^{12} M_{\odot}$ $m_x < 5 \text{keV}$