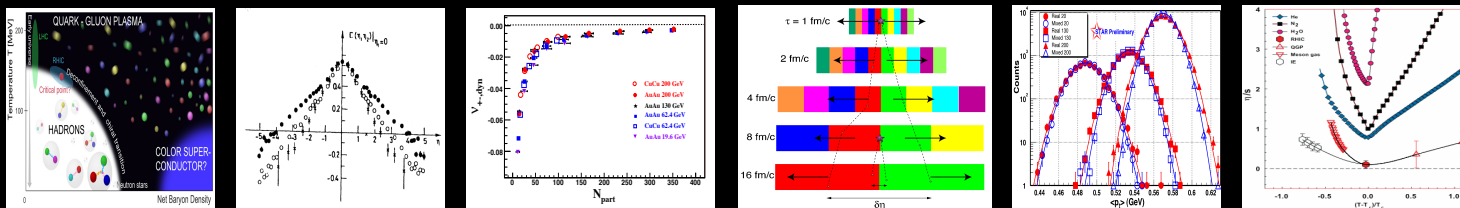




The Multiple Facets of Correlation Functions Kolkata, India, Jan 2014

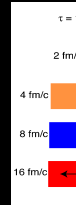
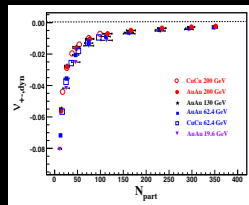
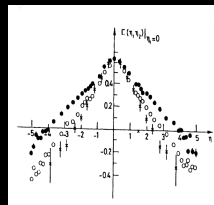
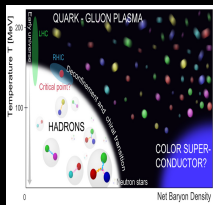


Professor Claude A Pruneau
Physics and Astronomy Department
Wayne State University



The Multiple Facets of Correlation Functions

Kolkata, India, Jan 2014

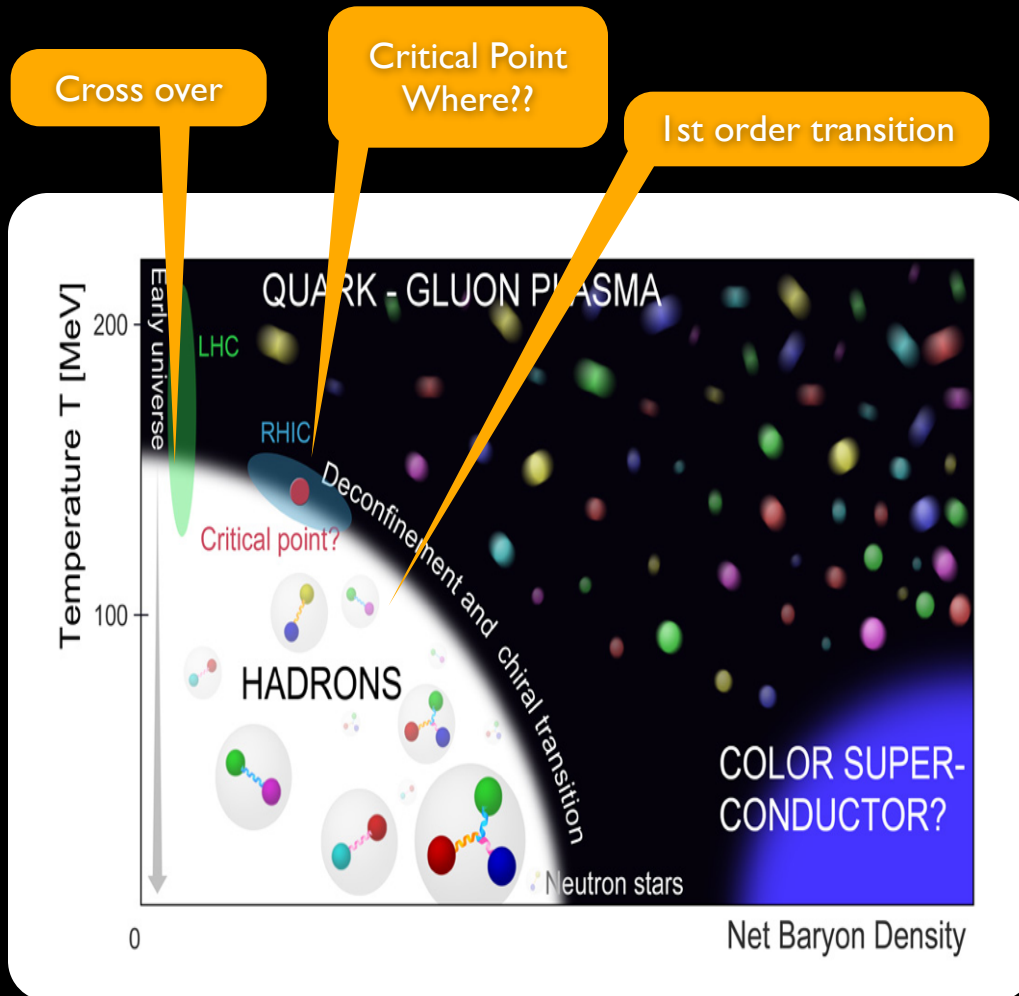


Professor Claude A Pruneau
 Physics and Astronomy Department
 Wayne State University



“Do we have any bedtime stories about charge and transverse momentum fluctuations?”

Motivations



Schematic QCD Phase Diagram

Deconfinement:

- Quark Degrees of Freedom
- Suppression of Net Charge Fluctuations
- Parton Energy Loss (Gluon Radiation)
- J/ψ Suppression (Debye Screening)
- Conical Emission

Critical Point (CP):

- Location unclear!
- Scan phase boundary
- “Divergence” of correlation length ξ near CP
- “Divergence” of pT fluctuations near CP
- Increase Strangeness Production & Fluctuations.

Equation of State (EoS):

- Viscosity
- Heat Capacity
- Flow
- Initial State

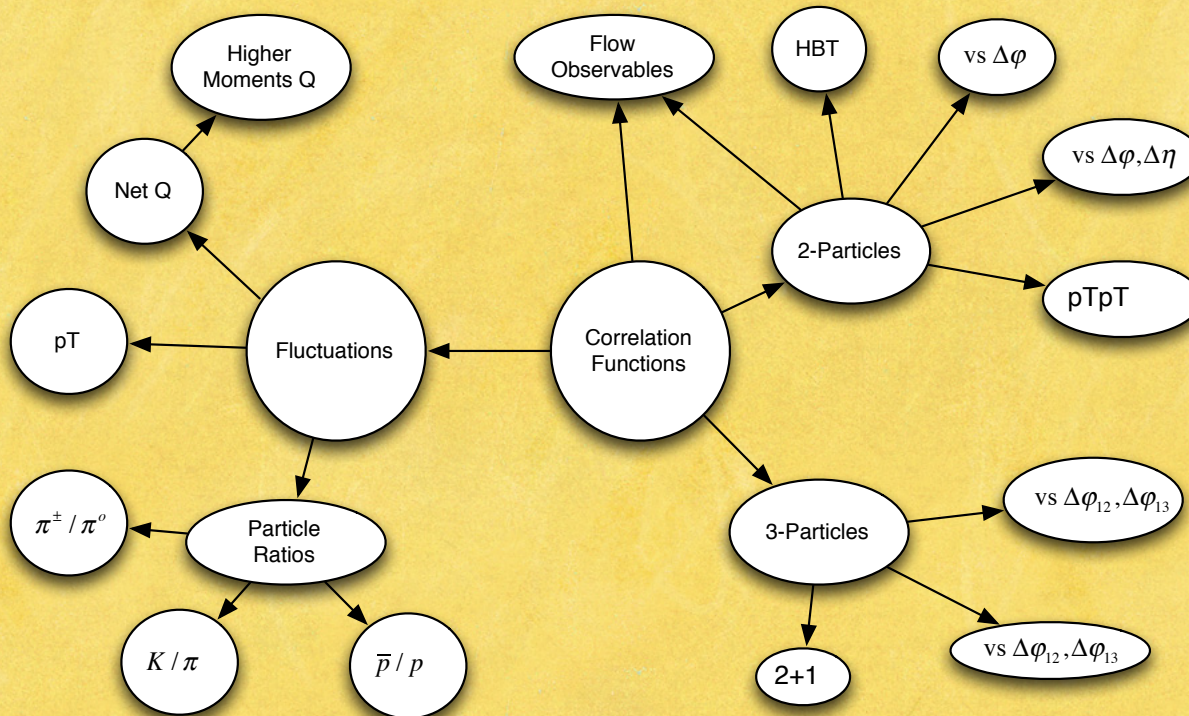
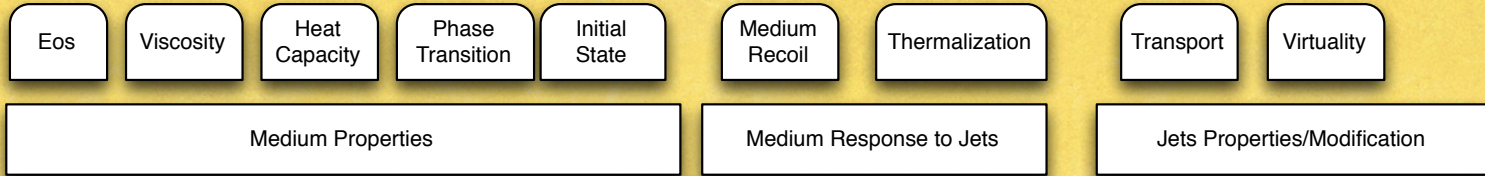
New State of Matter

- DCCs

New Phenomena

- Conical Emission
- Chiral Magnetic Effect

The Multi-facets of Correlations



Deconfinement: Suppression of Net Charge Fluctuations

Koch, Jeon, *et al.*, Asaka *et al.*, Heiselberg *et al.*, and several others:

Expect reduced net charge fluctuation variance in the presence of a QGP.

$$N_{ch} = N_+ + N_-$$

$$Q = N_+ - N_-$$

$$R = \frac{N_+}{N_-}$$

$$\omega_Q = \frac{\langle \delta Q^2 \rangle}{\langle N_{ch} \rangle}$$

$$D \equiv \langle N_{ch} \rangle \langle \delta R^2 \rangle = 4 \frac{\langle \delta Q^2 \rangle}{\langle N_{ch} \rangle} = 4\omega_Q$$

Scenario	ω_Q	D
Free Particles	1	4
Resonance Gas	~0.7	~2.8
QGP	<0.25	<1
QGP+Coalescence		3.3



Dilution of Fluctuations in expanding medium due to diffusion of particles
E.V. Shuryak, M.A. Stephanov, Phys. Rev. C 63, 064903 (2001)

M.A. Aziz, S. Gavin, Phys. Rev. C 70, 034905 (2004).

Collision dynamics

S. Jeon, V. Koch, Phys. Rev. Lett. 85, 2076 (2000).

Radial flow

S. Voloshin, Phys. Lett. B632, 490 (2006).

Resonance decays, final state interactions

J. Zaraneek, Phys. Rev. C66 024905 (2002).

The "Conflict" and The Resolution (QM 2004)

Definitions: $Q = N_+ - N_-$ $N_{CH} = N_+ + N_-$ Variance: $\langle \delta X^2 \rangle = \langle X^2 \rangle - \langle X \rangle^2$

Theoretical Prediction: $R = \frac{\langle N_+ \rangle}{\langle N_- \rangle}$ $D \equiv \langle N_{ch} \rangle \langle \delta R^2 \rangle = 4 \frac{\langle \delta Q^2 \rangle}{\langle N_{CH} \rangle}$



$$\overline{z^2} = 4 \frac{\langle N_+ \rangle \langle N_- \rangle}{\langle N_{CH}^2 \rangle} z = Q - \frac{\langle Q \rangle}{\langle N_{CH} \rangle} N_{CH}$$

$$\Phi_q = \sqrt{\frac{\langle Z^2 \rangle}{\langle N_{CH} \rangle}} - \sqrt{z^2}$$

Weak Evidence for finite dynamic net charge fluctuations



$$v(Q) \equiv \langle \delta Q^2 \rangle / \langle N_{CH} \rangle$$

$$D = 4v(Q)$$

PHENIX (130 GeV): PRL. 89 (2002) 082301.



$$v_{+,dyn} = v_{+-} - v_{+,stat}$$

$$D \approx 4 + \langle N_+ + N_- \rangle v_{+,dyn}$$

Clear Evidence for finite dynamic net charge fluctuations but not for deconfinement

STAR (130 GeV) PRC68, 044905 (2003).

$$v_{+-} = \left\langle \left(\frac{N_+}{\langle N_+ \rangle} - \frac{N_-}{\langle N_- \rangle} \right)^2 \right\rangle$$

Poisson Limit

$$v_{+,stat} = \frac{1}{\langle N_+ \rangle} + \frac{1}{\langle N_- \rangle}$$

Dynamic Fluctuations

$$v_{+,dyn} = v_{+-} - v_{+,stat}$$

Observables Related

$$\Phi_q \approx \frac{\langle N_+ \rangle^{3/2} \langle N_- \rangle^{3/2}}{\langle N_{CH} \rangle^2} v_{+,dyn}$$

Integral Two-Particle Correlation Measure

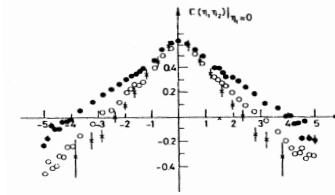
$$v_{+,dyn} = \frac{\langle N_+ (N_+ - 1) \rangle}{\langle N_+ \rangle^2} + \frac{\langle N_- (N_- - 1) \rangle}{\langle N_- \rangle^2} - 2 \frac{\langle N_+ N_- \rangle}{\langle N_+ \rangle \langle N_- \rangle}$$

$$v(Q) \approx 1 + \frac{\langle N_+ + N_- \rangle}{4} v_{+,dyn}$$

$$v_{+,dyn} = R_{++} + R_{--} - 2R_{+-}$$

C.P., S.G., S.V., PRC 66, 44904 (2002)
 S. Mrowczynski, PRC C66, 024904 (2002).
 J. Nystrand, et al., PRC 68, 034902 (2003).

Dynamical Fluctuations and Correlations



FNAL and ISR data.

1-body density $\rho_{1,\alpha}(\eta_\alpha) = \frac{dN}{d\eta_\alpha}$

2-body density $\rho_{2,\alpha\beta}(\eta_\alpha, \eta_\beta) = \frac{d^2N}{d\eta_\alpha d\eta_\beta}$

Differential Correlation

$$C_{\alpha\beta}(\eta_\alpha, \eta_\beta) = \rho_{\alpha\beta}(\eta_\alpha, \eta_\beta) - \rho_\alpha(\eta_\alpha)\rho_\beta(\eta_\beta)$$

$$R_{\alpha\beta}(\eta_\alpha, \eta_\beta) = \frac{\rho_{\alpha\beta}(\eta_\alpha, \eta_\beta)}{\rho_\alpha(\eta_\alpha)\rho_\beta(\eta_\beta)} - 1$$

Robust Observable

Integral Correlation Fluctuations

$$R_{\alpha\beta}(\eta_\alpha, \eta_\beta) = \frac{\int \rho_{\alpha\beta}(\eta_\alpha, \eta_\beta) d\eta_\alpha d\eta_\beta}{\int \rho_\alpha(\eta_\alpha) d\eta_\alpha \otimes \int \rho_\beta(\eta_\beta) d\eta_\beta} - 1$$

Robust Observable

Net Charge Fluctuations

$$v_{+-,dyn} = R_{++} + R_{--} - 2R_{+-}$$

Charge Balance Function

$$B(\Delta\eta) = \frac{N_{+-}}{N_-} + \frac{N_{-+}}{N_+} - \frac{N_{--}}{N_-} - \frac{N_{++}}{N_+}$$

K/Pi Fluctuations (etc)

$$v_{K\pi} = \frac{\langle N_\pi(N_\pi - 1) \rangle}{\langle N_\pi \rangle^2} + \frac{\langle N_K(N_K - 1) \rangle}{\langle N_K \rangle^2} - 2 \frac{\langle N_{K\pi} \rangle}{\langle N_K \rangle \langle N_\pi \rangle}$$

Extensions to pT fluctuations, higher moments, and multi-particle correlation functions.

Dynamical Fluctuations Properties

Independent of volume fluctuations

$$v_{+-,dyn} = R_{++} + R_{--} - 2R_{+-}$$

Independent Particle Production

$$v_{+-,dyn} = 0$$

Superposition of “p-p”

$$\langle N(b) \rangle v_{+-,dyn}(b) = \text{constant}$$

$$\left\langle \frac{dN}{dy} \right\rangle_{AA} v_{AA,dyn} = \left\langle \frac{dN}{dy} \right\rangle_{pp} v_{pp,dyn}$$

Robust Observable
(Independent of efficiency)

$$R_{aa} = \frac{\langle n(n-1) \rangle}{\langle n \rangle^2} = \frac{\varepsilon^2 \langle N^2 \rangle + \varepsilon(1-\varepsilon)\langle N \rangle - \varepsilon \langle N \rangle}{\varepsilon^2 \langle N \rangle^2} = \frac{\langle N(N-1) \rangle}{\langle N \rangle^2}$$

Charge Conservation

$$v_{+-,dyn} = -\frac{2}{\langle N_+ \rangle_{4\pi}} \approx -\frac{4}{\langle N \rangle_{4\pi}}$$

Perfect $N_+ = N_-$ correlation

$$v_{+-,dyn} = -4 / \langle N \rangle_{\eta}$$

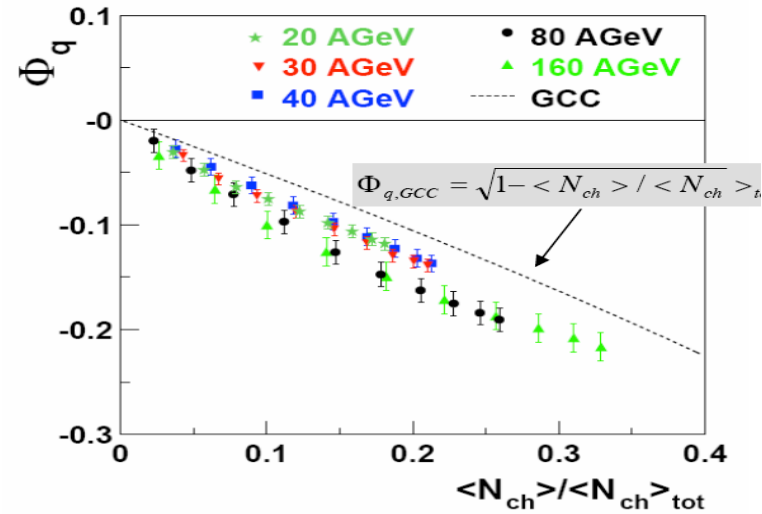
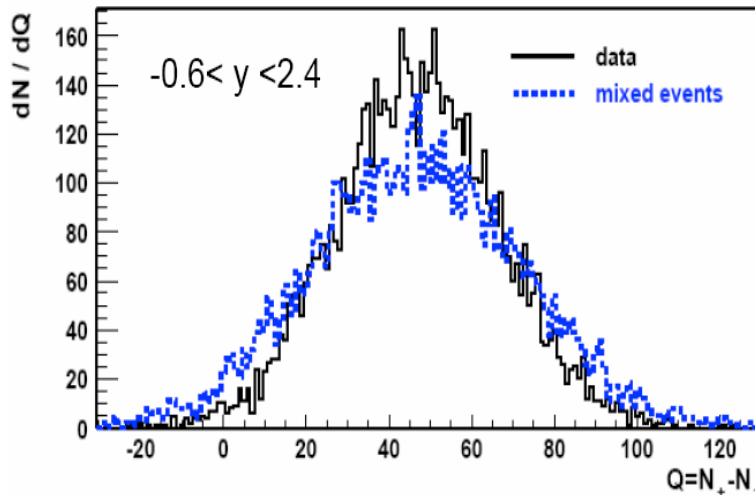
First Measurement



$$\Phi_q = \sqrt{\frac{\langle Z^2 \rangle}{\langle N \rangle}} - \sqrt{Z^2}$$

$$z = q - \bar{q} \quad Z = \sum_{i=1}^N (q_i - \bar{q})$$

Central Pb+Pb collisions 158A GeV



- Weak Evidence for dynamical correlations
- But NO Evidence for QGP Formation

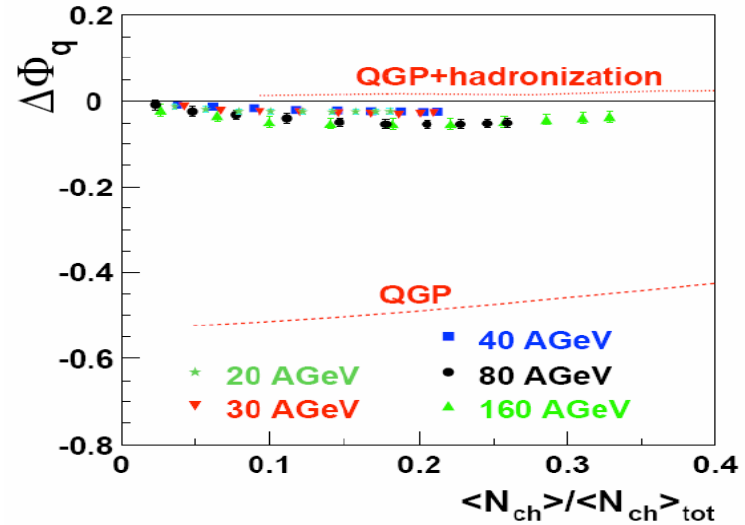
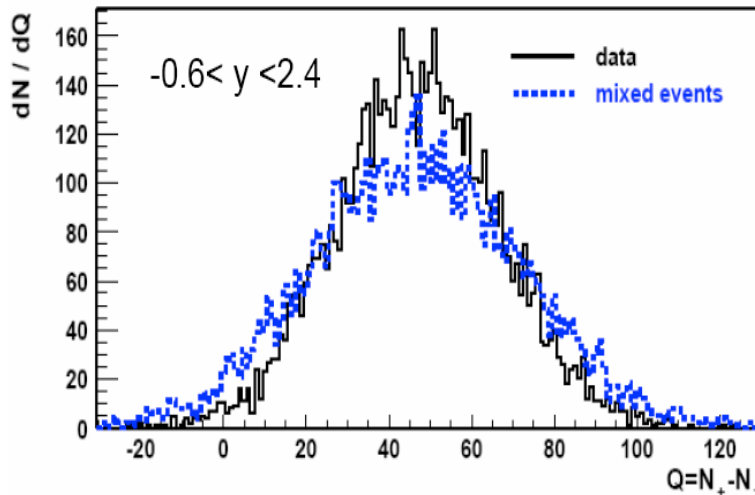
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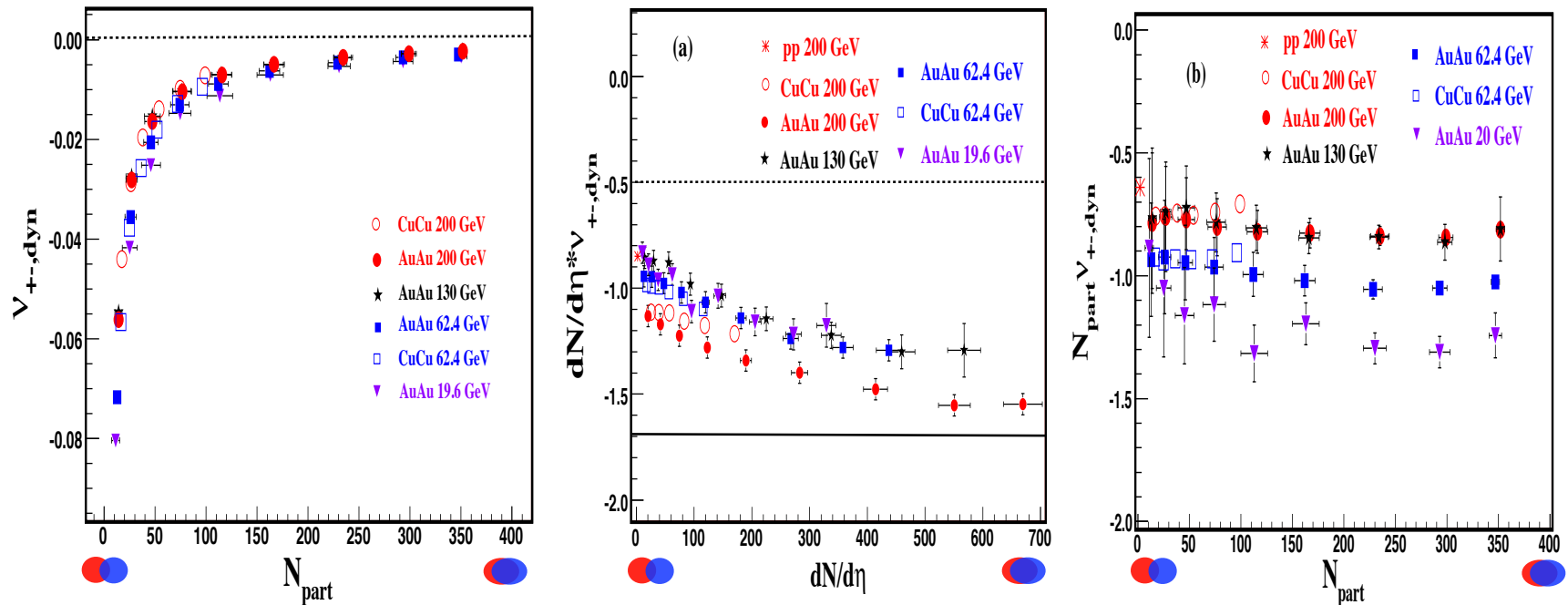


- Weak Evidence for dynamical correlations
- But NO Evidence for QGP Formation

Net Charge Dynamical Fluctuations

Au- Au vs centrality, vs beam energy

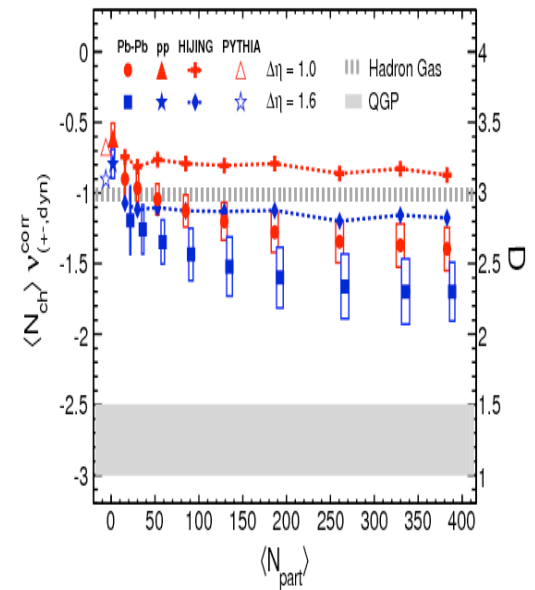
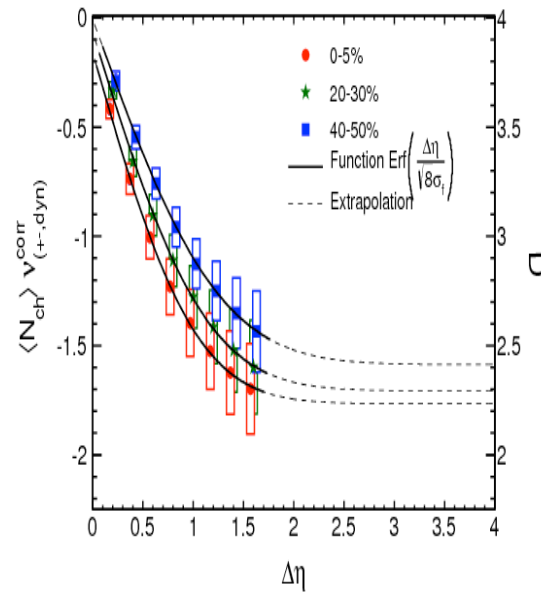
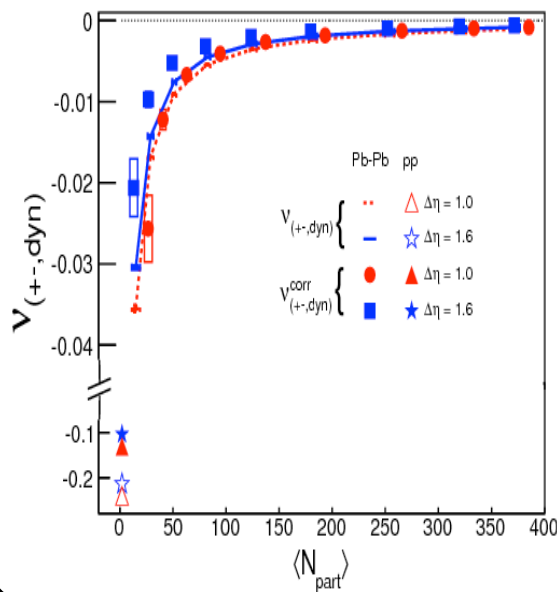
STAR TPC: $|\eta| < 0.5$; $0.2 < p_t < 5.0$ GeV/c



C.P., M. Sharma
STAR, PRC 79 (2009) 024906

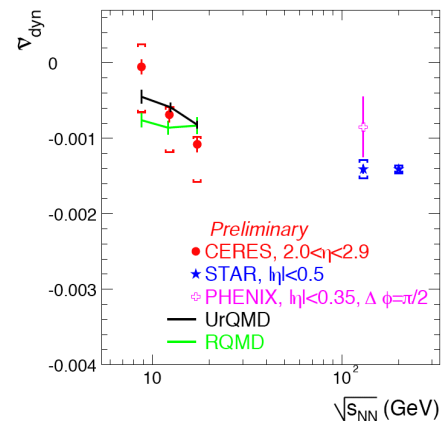
- Evidence for dynamic fluctuations
- Non trivial centrality dependence
- BUT No deconfinement signal

Net Charge Dynamical Fluctuations: ALICE

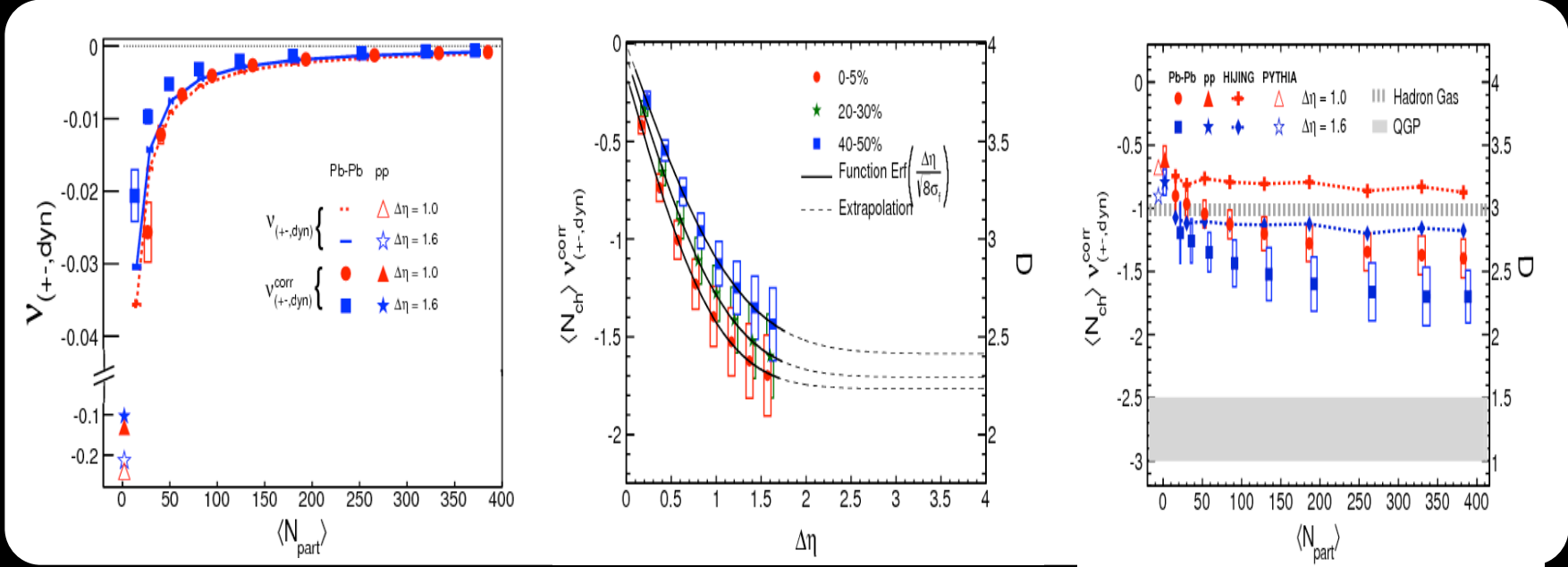


ALICE, Phys.Rev.Lett. 110 (2013) 152301

- Fluctuations suppressed w.r.t. RHIC
- Cannot be explained by radial flow alone
- Clear tendency towards QGP Prediction
- Origin in QGP Phase (?)

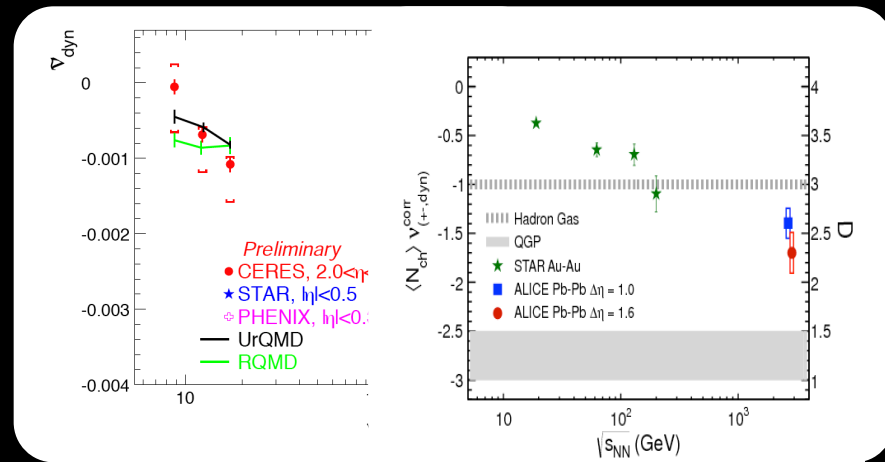


Net Charge Dynamical Fluctuations: ALICE



ALICE, Phys.Rev.Lett. 110 (2013) 152301

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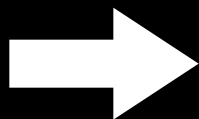


Charge Balance Function

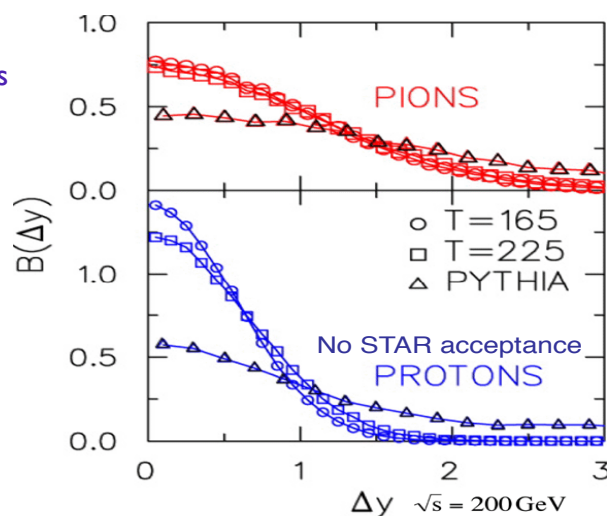
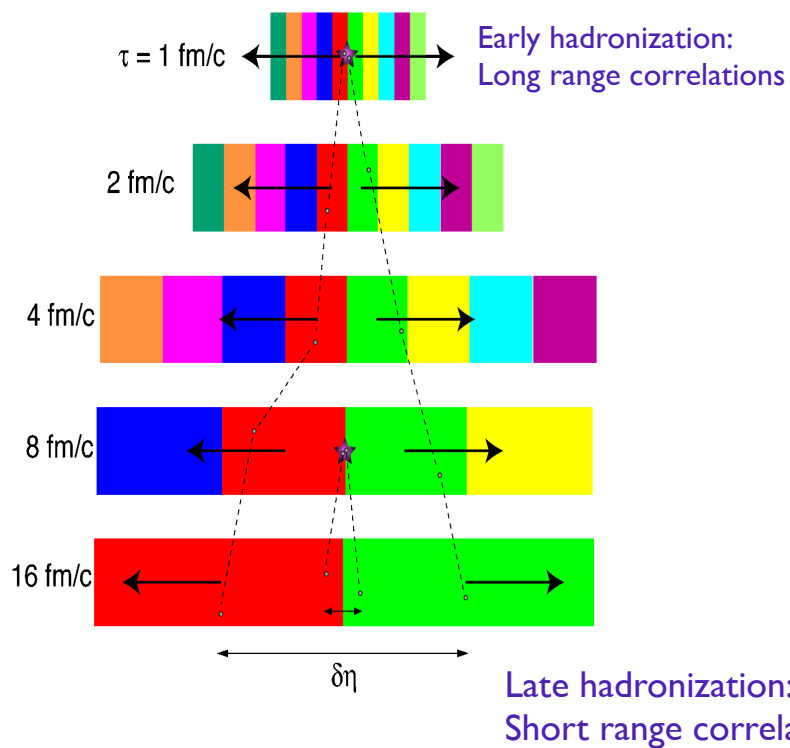
Bass, Danielewicz, and Pratt, PRL 85, 2689 (2000)

Deconfinement:

Delayed Hadronization



Narrowing of Balance Function



$$B(\Delta\eta) = \frac{1}{2} \left\{ \frac{N_{+-}(\Delta\eta)}{N_-} + \frac{N_{-+}(\Delta\eta)}{N_+} - \frac{N_{--}(\Delta\eta)}{N_-} - \frac{N_{++}(\Delta\eta)}{N_+} \right\}$$

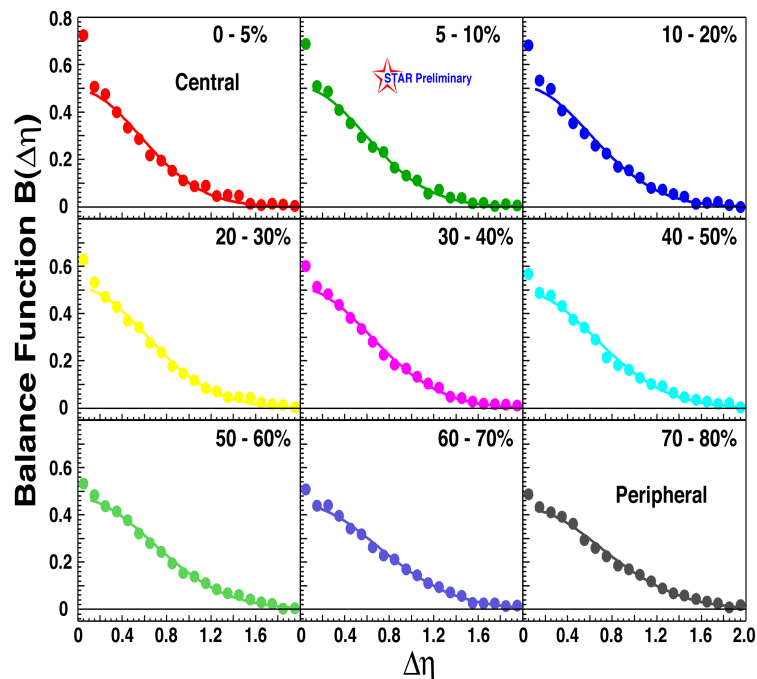
$$\sigma_{\delta y}^2 = \sigma_{\delta\eta}^2 + \sigma_{thermal}^2$$

Charge Balance Function

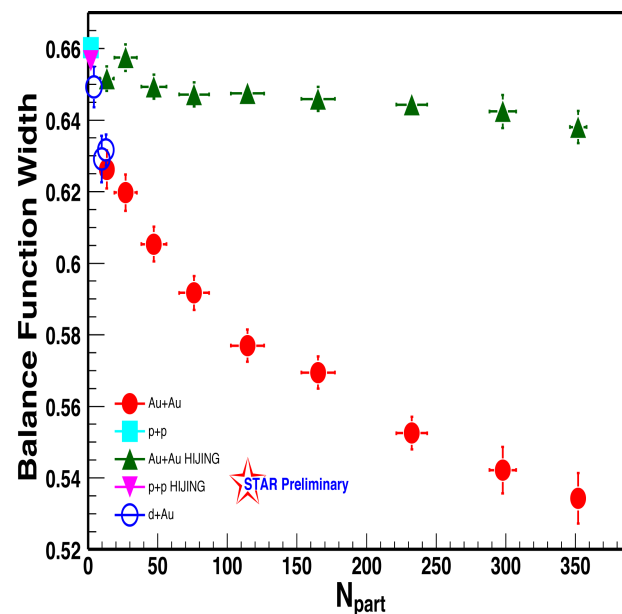


STAR, PRL 90 (2003) 172301

Au + Au $\sqrt{s_{NN}} = 130$ GeV



$$B(\Delta\eta) = \frac{1}{2} \left\{ \frac{N_{+-}(\Delta\eta)}{N_-} + \frac{N_{-+}(\Delta\eta)}{N_+} - \frac{N_{--}(\Delta\eta)}{N_-} - \frac{N_{++}(\Delta\eta)}{N_+} \right\}$$



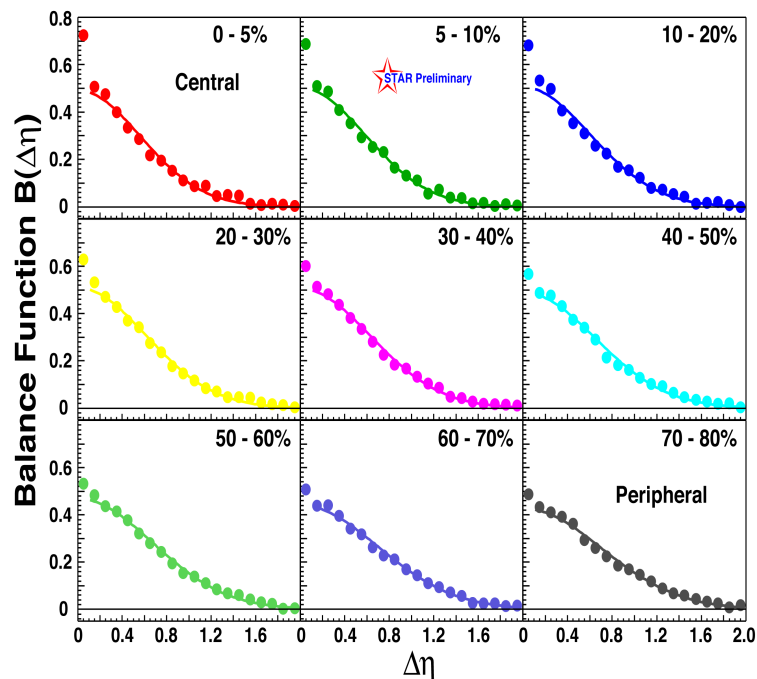
- Narrowing of Balance Function
- Observed for all charges, pions, and kaons
- Also observed at 200 GeV
- Consistent w/ Delayed Hadronization

Charge Balance Function

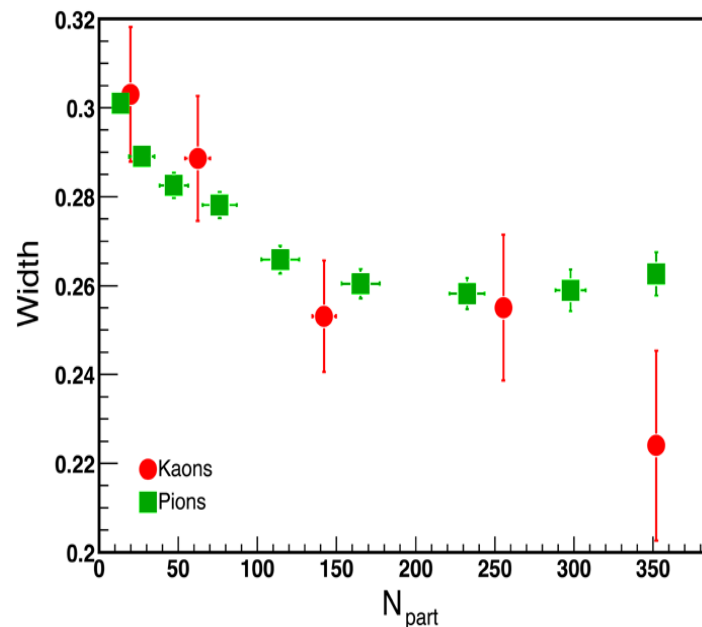


STAR, PRL 90 (2003) 172301

Au + Au $\sqrt{s_{NN}} = 130$ GeV



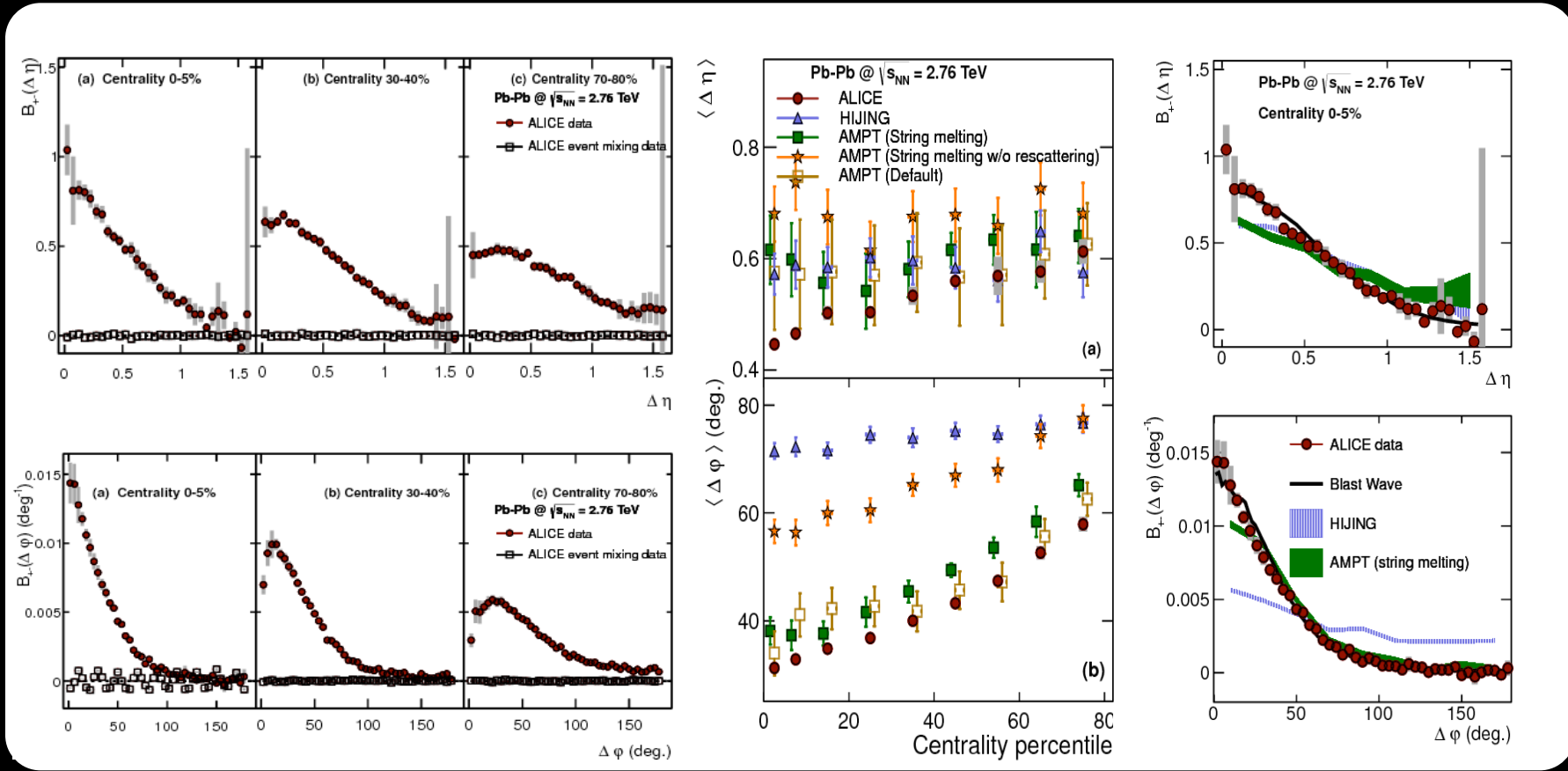
$$B(\Delta\eta) = \frac{1}{2} \left\{ \frac{N_{+-}(\Delta\eta)}{N_-} + \frac{N_{-+}(\Delta\eta)}{N_+} - \frac{N_{--}(\Delta\eta)}{N_-} - \frac{N_{++}(\Delta\eta)}{N_+} \right\}$$



- Narrowing of Balance Function
- Observed for all charges, pions, and kaons
- Also observed at 200 GeV
- Consistent w/ Delayed Hadronization

Charge Balance Function

Pb-Pb @ 2.76 TeV



ALICE, Phys. Lett. B 723 (2013) 267-279

- Narrowing of Balance Function Observed for all charges,
- Consistent w/ Delayed Hadronization, production of a deconfined phase of matter

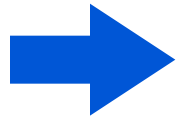
Higher Moments

- Static, infinite medium: **Correlation length** ξ diverges near CP
- Related to moments of net charge, net baryon number, and net strangeness
 - M.A. Stephanov et al., Phys. Rev. D 60, 114028 (1999).
- Finite size and finite lifetime suppress ξ but it might be as large as 2-3 fm in heavy-ion collisions.
 - B. Berdnikov et al., Phys. Rev. D 61, 105017 (2000).
 - M.A. Stephanov, Phys. Rev. Lett. 102, 032301 (2009);
 - K. Rajagopal and M.A. Stephanov, private comm. 2009.
 - M.Asakawa et al., Phys. Rev. Lett. 103, 262301 (2009).

$$\sigma^2 = \langle \Delta N^2 \rangle \propto \xi^2$$

$$\langle \Delta N^3 \rangle \propto \xi^{4.5}$$

$$\langle \Delta N^4 \rangle \propto \xi^7$$



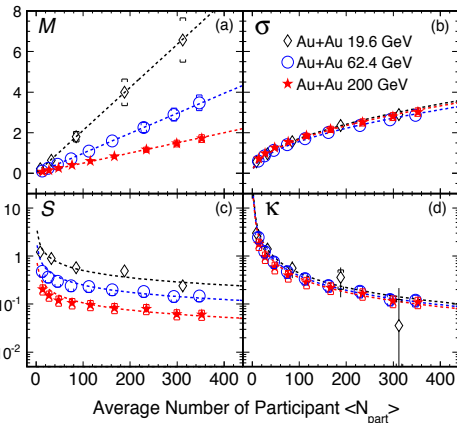
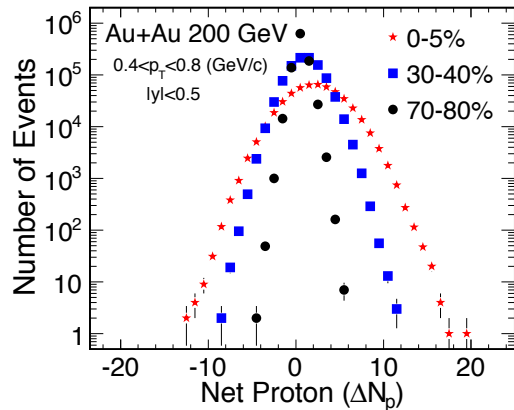
$$S = \gamma_1 = \frac{\langle \Delta N^3 \rangle}{\sigma^3} \propto \frac{\xi^{4.5}}{\xi^3} = \xi^{1.5}$$

$$\kappa = \gamma_2 = \frac{\langle \Delta N^4 \rangle}{\sigma^4} - 3 \propto \frac{\xi^7}{\xi^4} = \xi^3$$

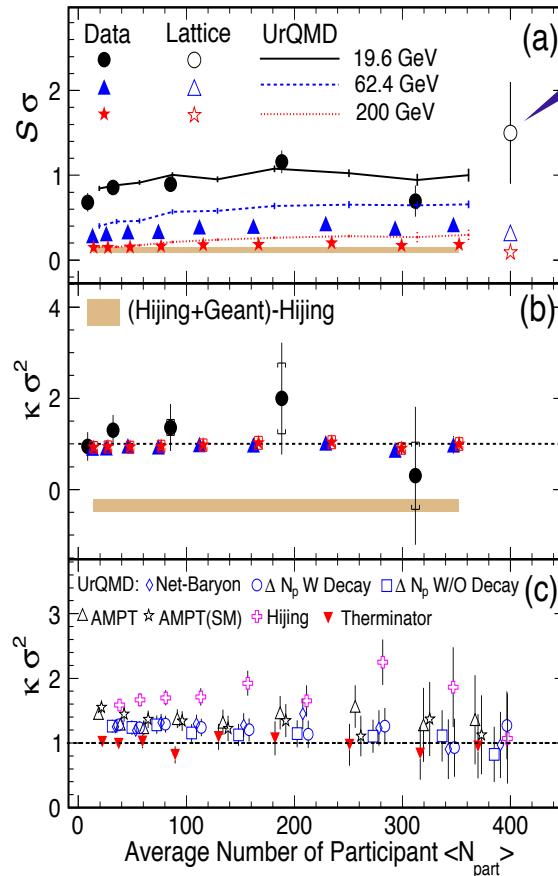
Measurements of
excess skewness and
kurtosis

- Lattice Calculations: Moments of net-baryon related to baryon number susceptibilities $\chi_B = \frac{\langle (\Delta N_B)^2 \rangle}{VT}$
- $\kappa \sigma^2 \sim$ ratio of fourth order, $\chi_B^{(4)}$, to second order $\chi_B^{(2)}$, large deviation from unity near CP.

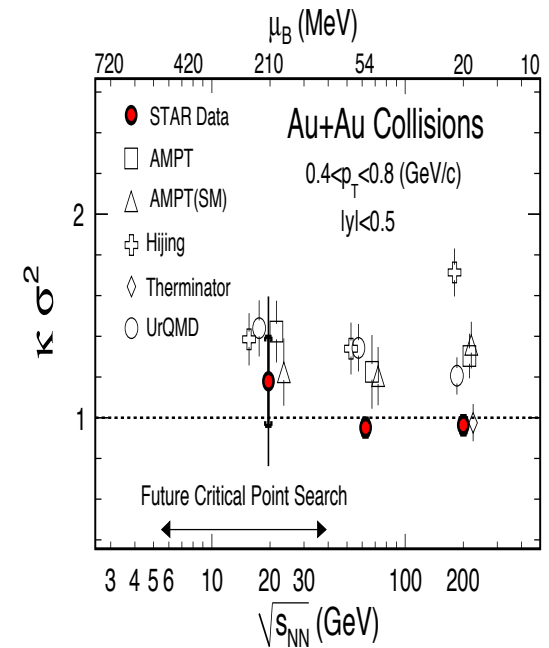
Higher Moments of Net Proton Fluctuations



STAR, Phys. Rev. Lett. **105** (2010) 22302



w/ critical point



S. Ejiri, et al., PRD, 78 (2008) 074507
 M.A. Stephanov, Prog. Th. Phys. Suppl. 153 (2004) 139
 Z. Fodor, S.D. Katz, JHEP 0404 (2004) 50.
 R.V. Gavai, S. Gupta,
 N.R. Sahoo, et al., Phys.Rev. C87 (2013) 044906
 RBC-Bielefeld, Nucl.Phys. A830 (2009) 705C-708C

Interesting Data! But
 Need better precision, extended energy range

Higher Moments: Cautionary Notes

- Efficiency Dependencies
 - and similarly for higher order terms...
- Suggests the use of ratios of factorial moments instead of skewness or kurtosis

$$\frac{\text{Var}[n]}{\langle n \rangle^2} = \frac{\langle n^2 \rangle - \langle n \rangle^2}{\langle n \rangle^2} = \frac{\langle N(N-1) \rangle}{\langle N \rangle^2} - 1 + \frac{1}{\varepsilon \langle N \rangle}$$

- e.g.

$$\frac{\langle N(N-1) \rangle}{\langle N \rangle^2}$$

$$\frac{\langle N(N-1)(N-2) \rangle}{\langle N \rangle^3}$$

$$\frac{\langle N(N-1)(N-2) \rangle}{\langle N(N-1) \rangle^{3/2}}$$

$$\frac{\langle N(N-1)(N-2)(N-3) \rangle}{\langle N(N-1) \rangle^2}$$

- A - A collisions likely to behave as a superposition of sources
- Implies Dilution Effects (**Superposition of m sources**):

$$\rho_1^{(m)} = \langle m \rangle \rho_1^{(1)}$$

$$\rho_2^{(m)} = \langle m \rangle \rho_2^{(1)} + \langle m(m-1) \rangle \rho_1^{(1)} \rho_1^{(1)}$$

$$\rho_3^{(m)} = \langle m \rangle \rho_3^{(1)} + \langle m(m-1) \rangle \rho_2^{(1)} \rho_1^{(1)} + \langle m(m-1)(m-2) \rangle \rho_1^{(1)} \rho_1^{(1)} \rho_1^{(1)}$$

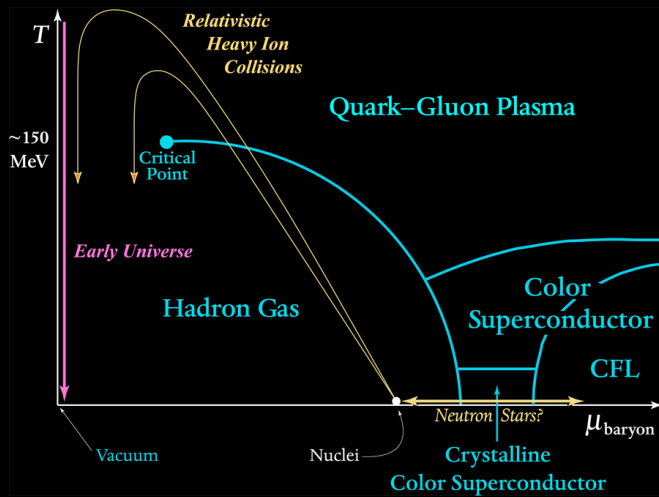
$$\rho_4^{(m)} = \langle m \rangle \rho_4^{(1)} + \langle m(m-1) \rangle \rho_3^{(1)} \rho_1^{(1)} + \langle m(m-1) \rangle \rho_2^{(1)} \rho_2^{(1)} + \langle m(m-1)(m-2) \rangle \rho_2^{(1)} \rho_1^{(1)} \rho_1^{(1)} + \langle m(m-1)(m-2)(m-3) \rangle \rho_1^{(1)} \rho_1^{(1)} \rho_1^{(1)} \rho_1^{(1)}$$

- “Signal” $\frac{\rho_4^{(m)}}{(\rho_1^{(m)})^4} \propto \frac{1}{\langle m \rangle^3} \frac{\rho_4^{(1)}}{(\rho_1^{(1)})^4}$

- Suggests the use of 3rd and 4th order cumulants...

K/ π Fluctuations

Observation of enhanced Kaon to Pion yield at $\sqrt{s} \sim 7$ GeV/u

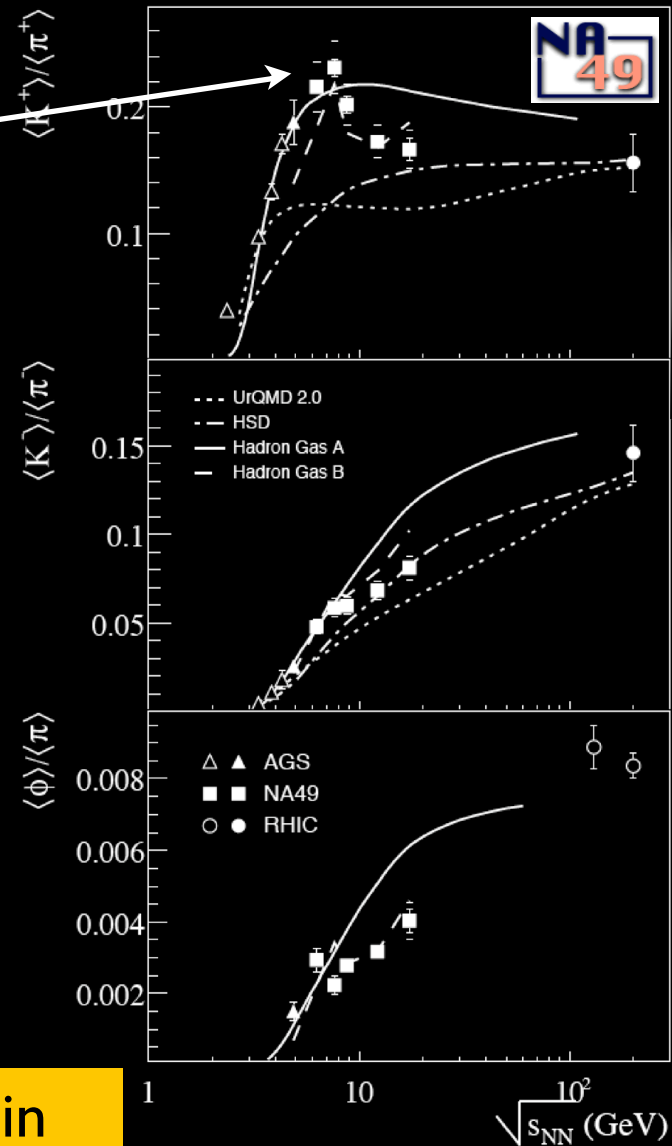


Production of strangeness may be related to the onset of deconfinement

“Event-by-event fluctuations of particle ratios related to the hadrochemical composition of the particle source could provide a direct probe of the existence and nature of the phase transition.”

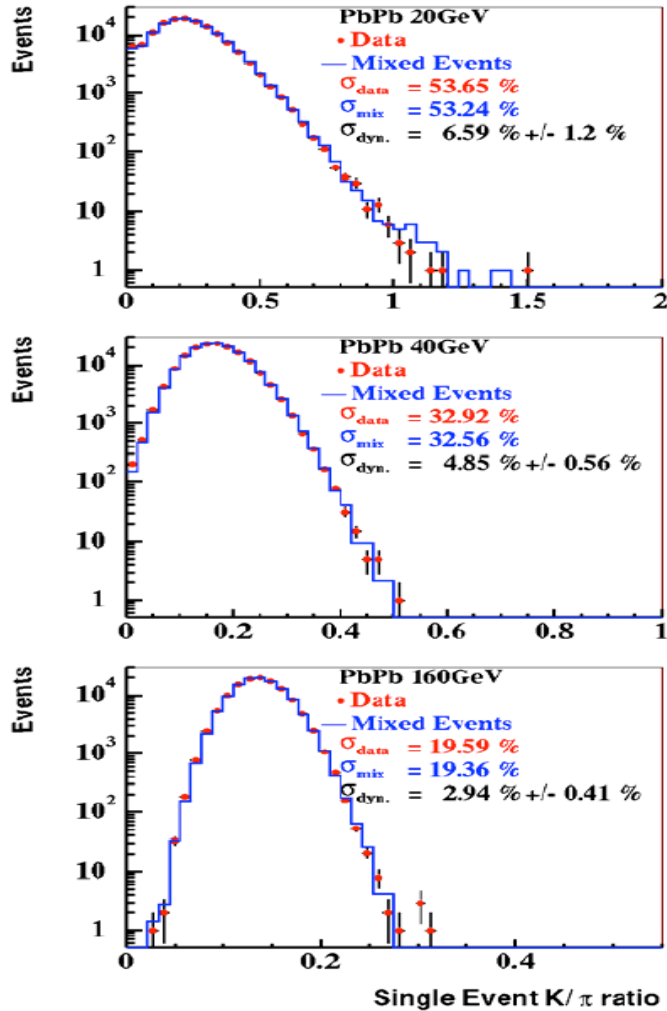
R. Stock, Nature 337 (1989) 319.

Seek evidence for abnormal fluctuations in the relative K to π yields



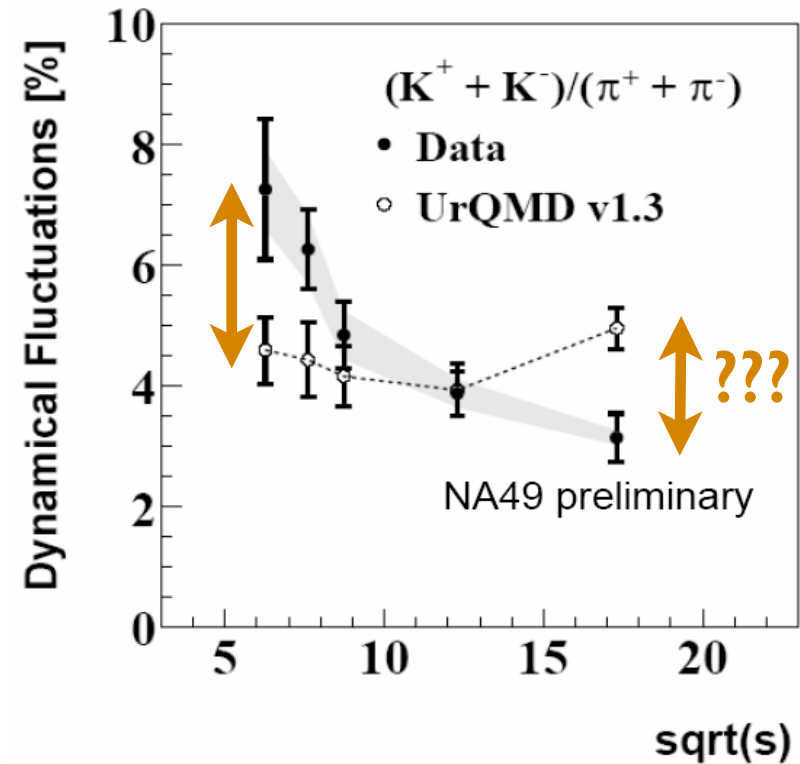
C. Blume (NA49), hep-ph/0505137

K/ π Fluctuations



Pion and kaon yields obtained e-by-e from a maximum Likelihood Fit for each event

$$\sigma_{\text{dyn}}^2 = \sigma_{\text{data}}^2 - \sigma_{\text{mixed}}^2$$



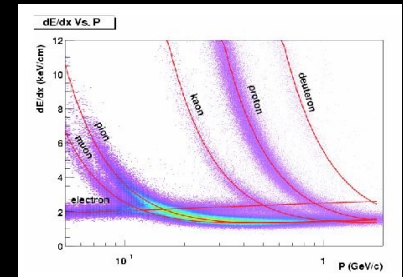
P.Seyboth for NA49 @ Hirscheegg, 16-22/1/05.

K/ π Fluctuations



STAR, Phys. Rev. Lett. 103, 092301 (2009)

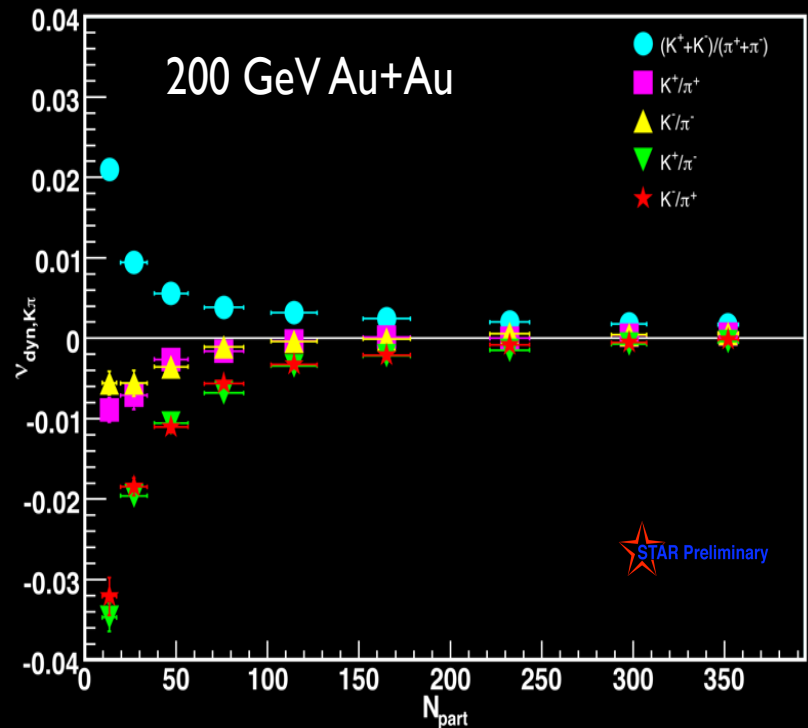
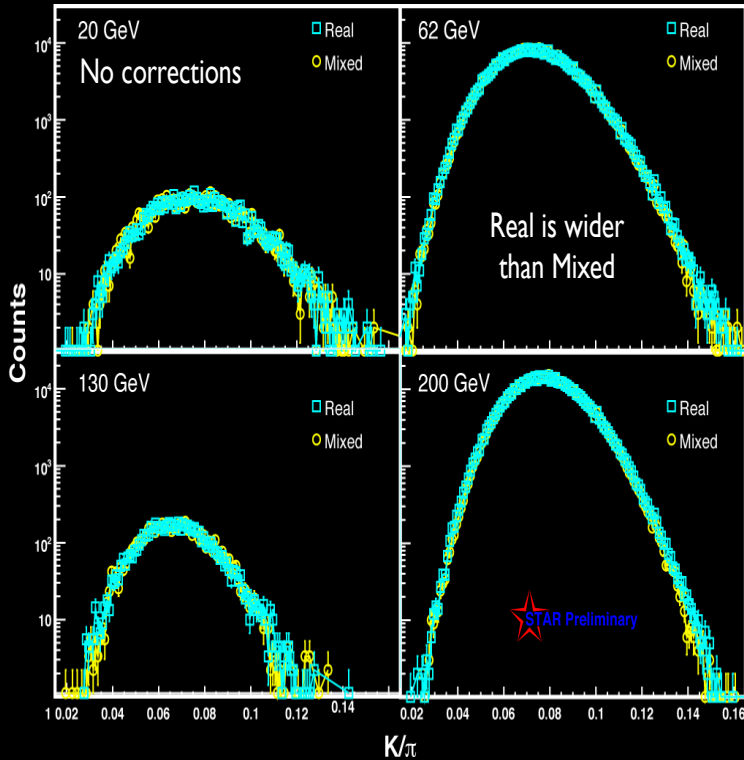
- PID based on TPC dE/dx:
- Measurements:
 - E-by-E Kaon to Pion yields ratio
 - Measure integral correlations



M.Anderson et al. NIMA499 (2003)

$$\sigma_{\text{dyn}}^2 = \sigma_{\text{data}}^2 - \sigma_{\text{mixed}}^2$$

$$v_{K\pi} = \frac{\langle N_\pi(N_\pi - 1) \rangle}{\langle N_\pi \rangle^2} + \frac{\langle N_K(N_K - 1) \rangle}{\langle N_K \rangle^2} - 2 \frac{\langle N_{K\pi} \rangle}{\langle N_K \rangle \langle N_\pi \rangle}$$

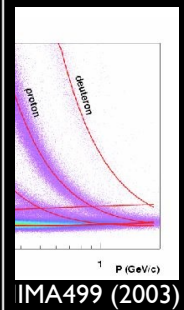
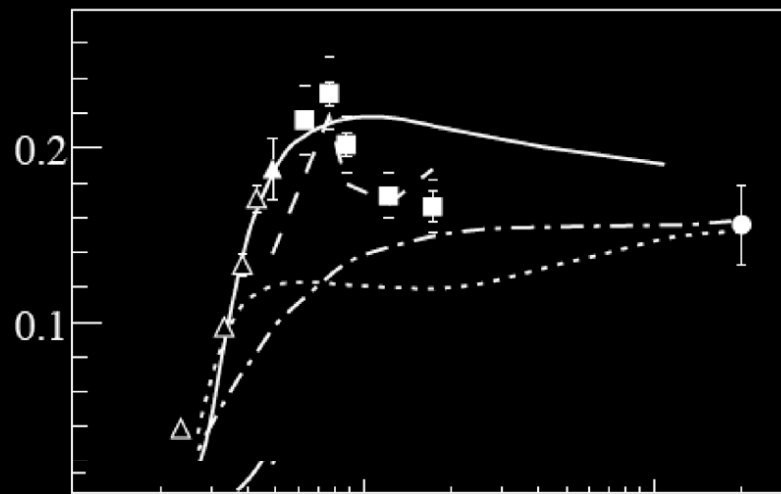


K/ π Fluctuation

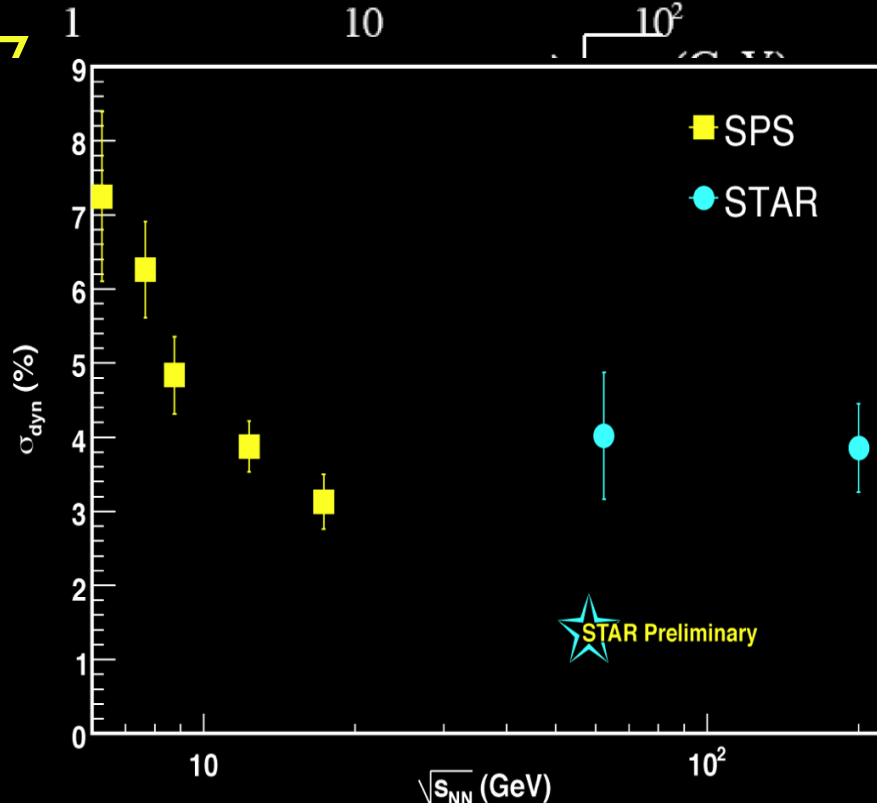
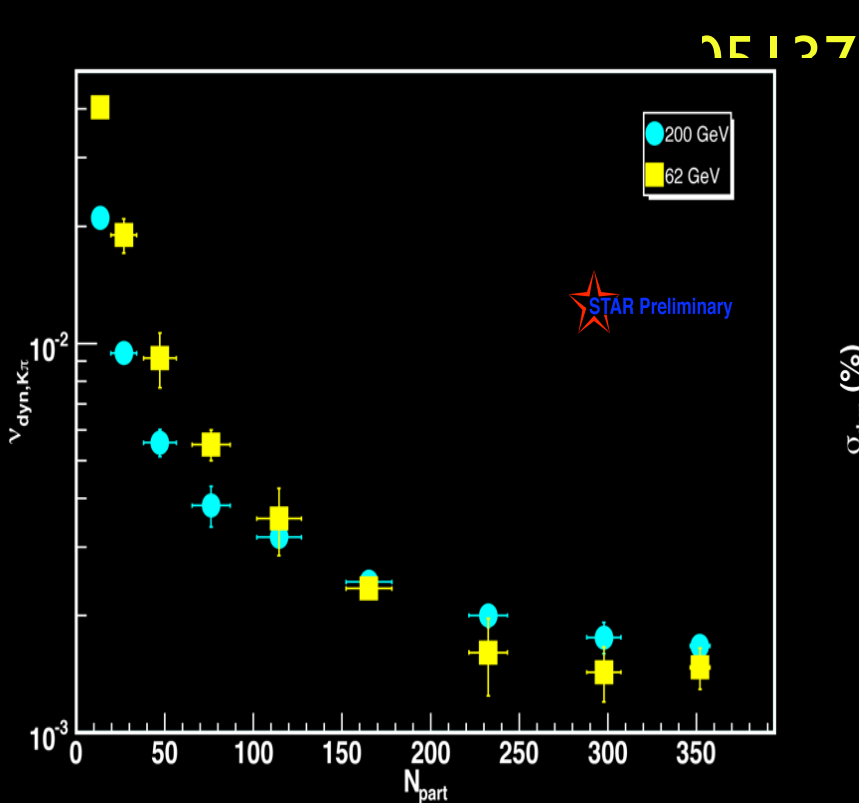
STAR, Phys. Rev. Lett. 103, 092301 (2009)

$$\langle K^+ \rangle / \langle \pi^+ \rangle$$

- PID based on TPC dE/dx:
- Measurements:
 - E-by-E Kaon to Pion yields r_2
 - Measure integral correlations:



IMA499 (2003)

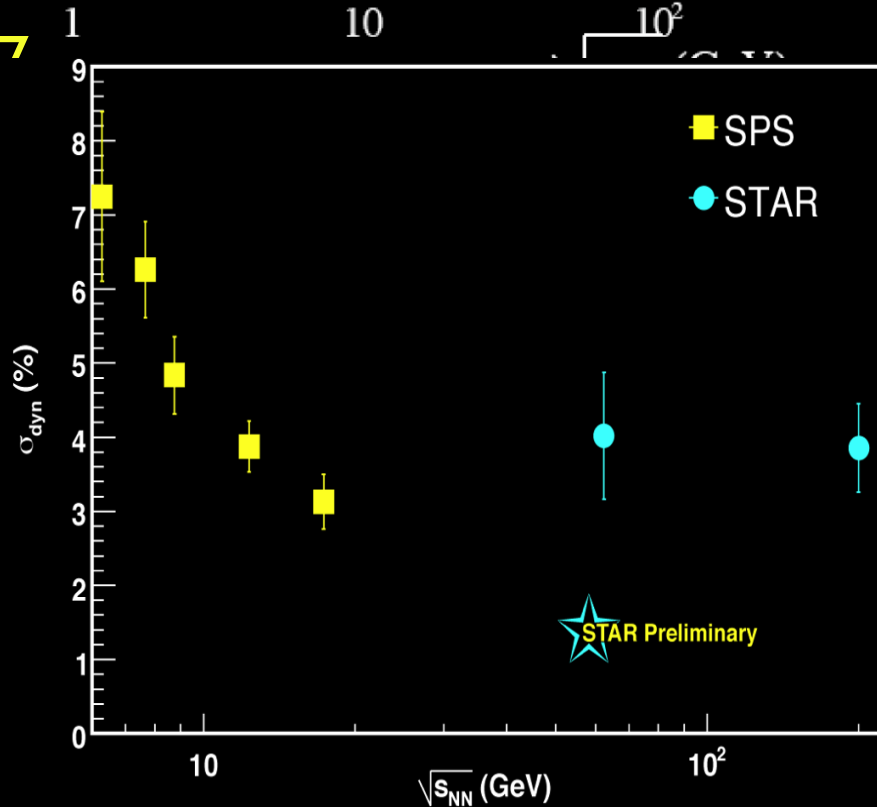
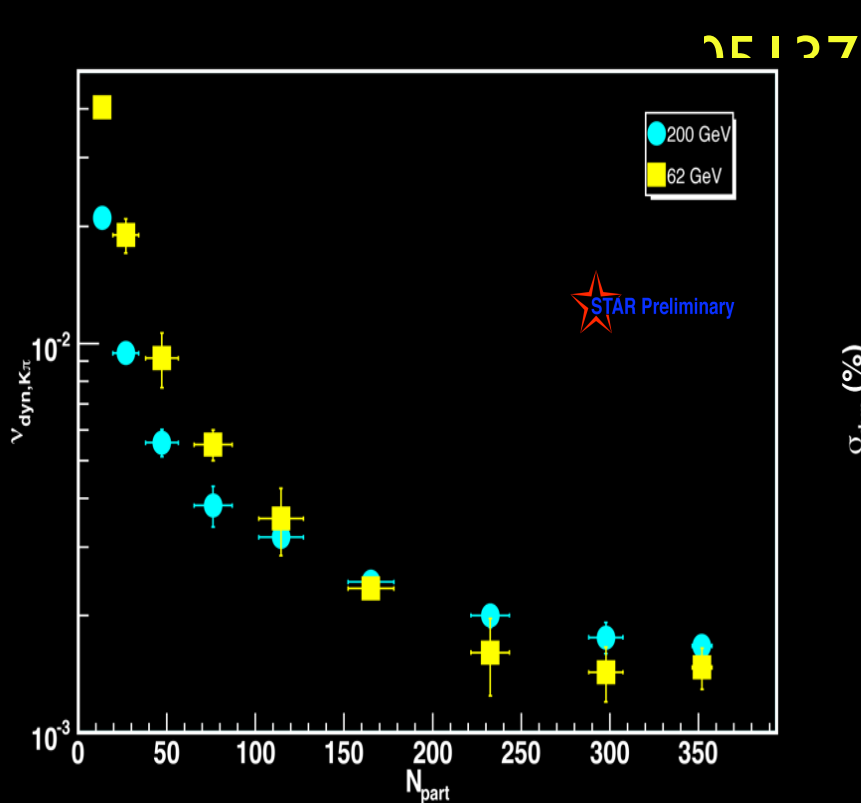
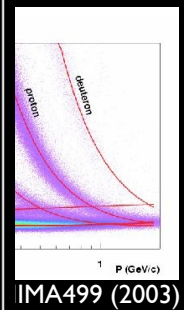
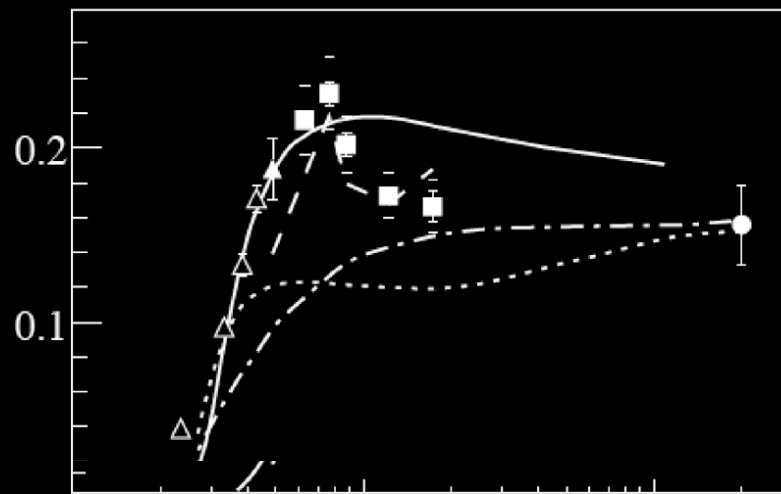


K/ π Fluctuation

STAR, Phys. Rev. Lett. 103, 092301 (2009)

$$\langle K^+ \rangle / \langle \pi^+ \rangle$$

- PID based on TPC dE/dx:
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 - Measure integral correlations:

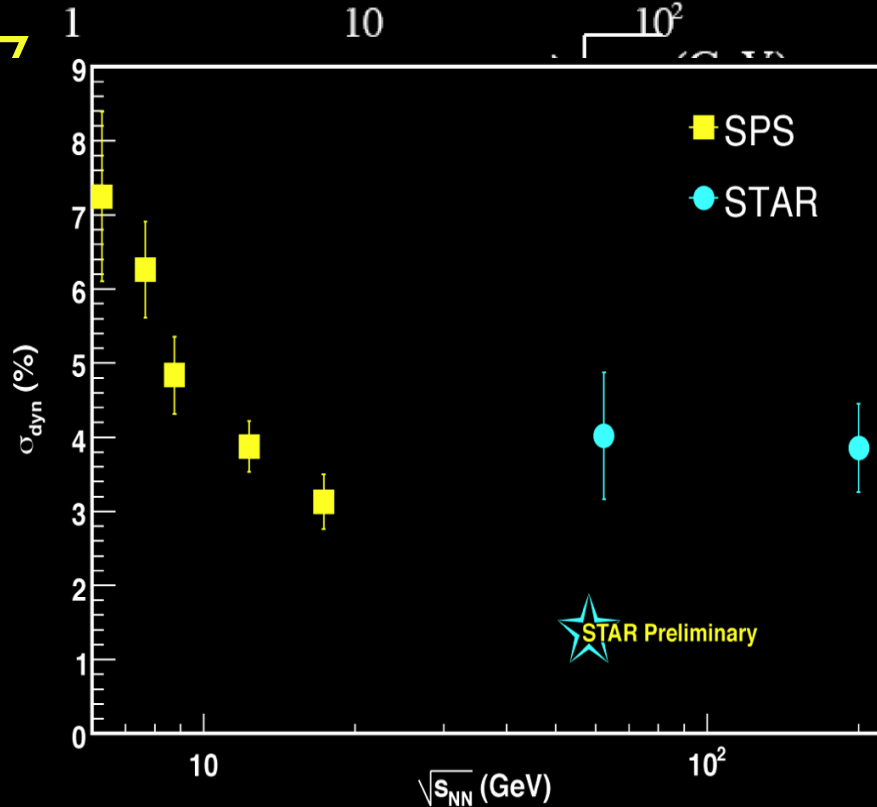
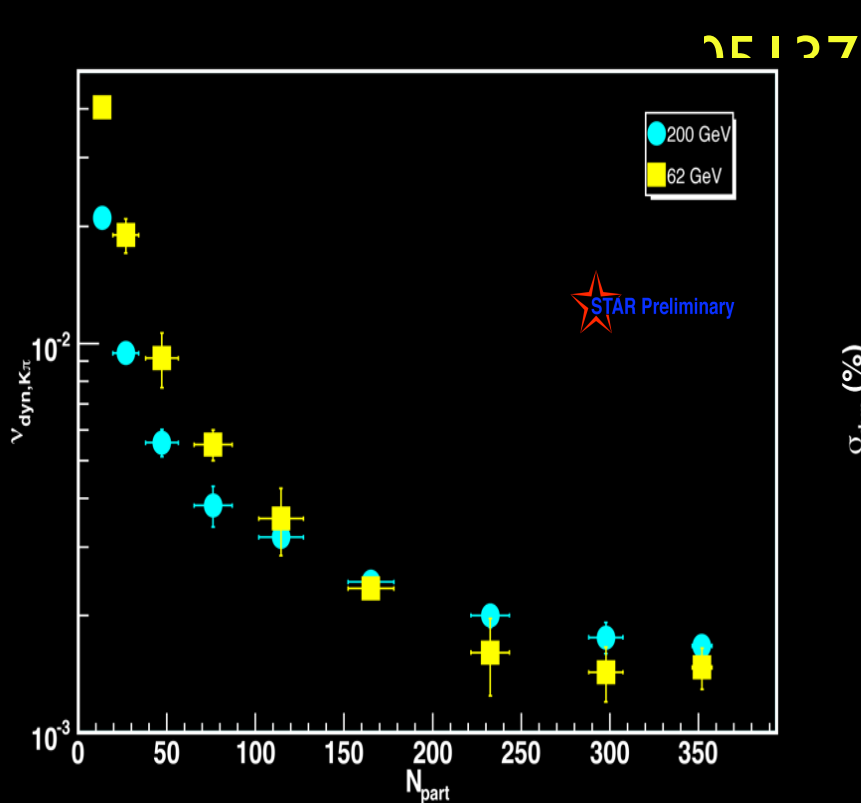
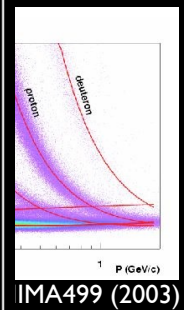
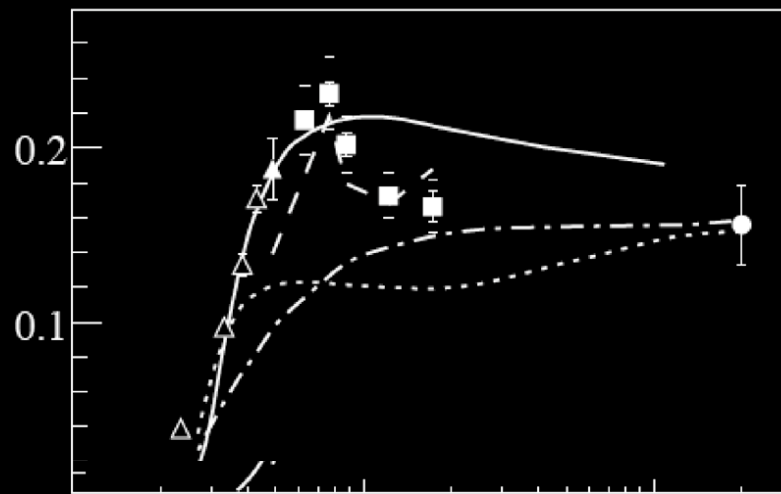


K/ π Fluctuation

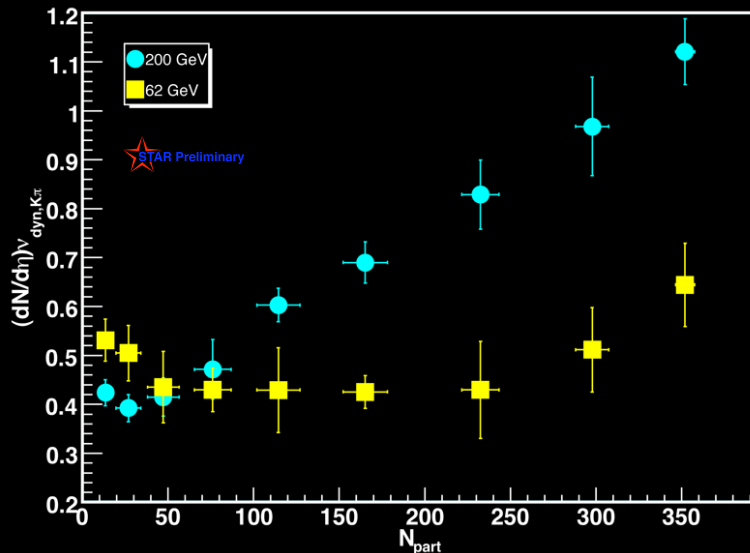
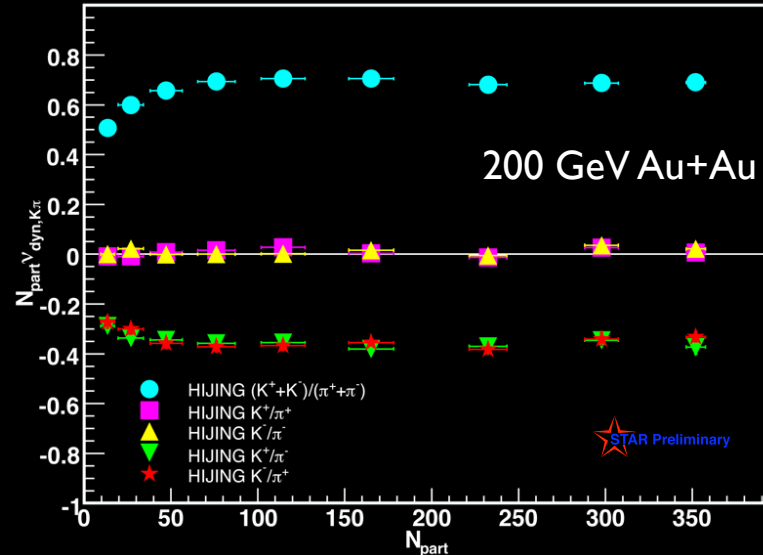
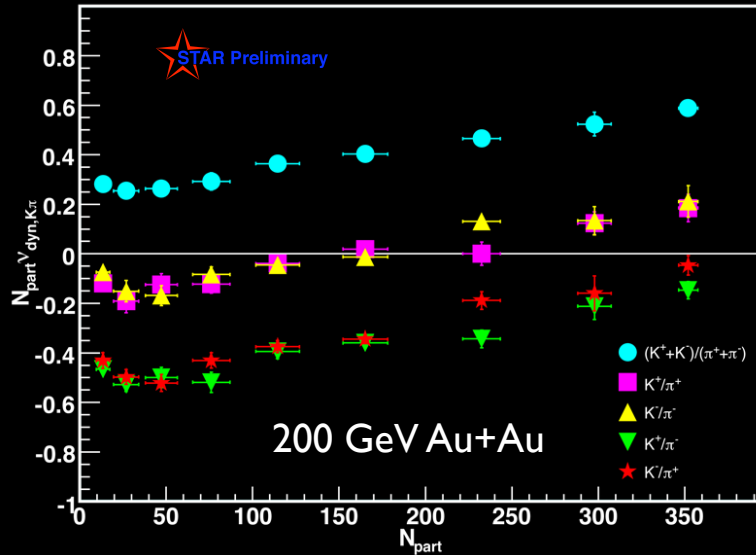
STAR, Phys. Rev. Lett. 103, 092301 (2009)

$$\langle K^+ \rangle / \langle \pi^+ \rangle$$

- PID based on TPC dE/dx:
- Measurements:
 - E-by-E Kaon to Pion yields r_2
 - Measure integral correlations:



K/ π Fluctuations



- Resonance decays (feed down) complicate the interpretation of k/ π fluctuations results.
- Nonetheless, “medium” effects are clearly observed.
- Provide good testing grounds for particle production models.

STAR, Phys. Rev. Lett. 103, 092301 (2009)

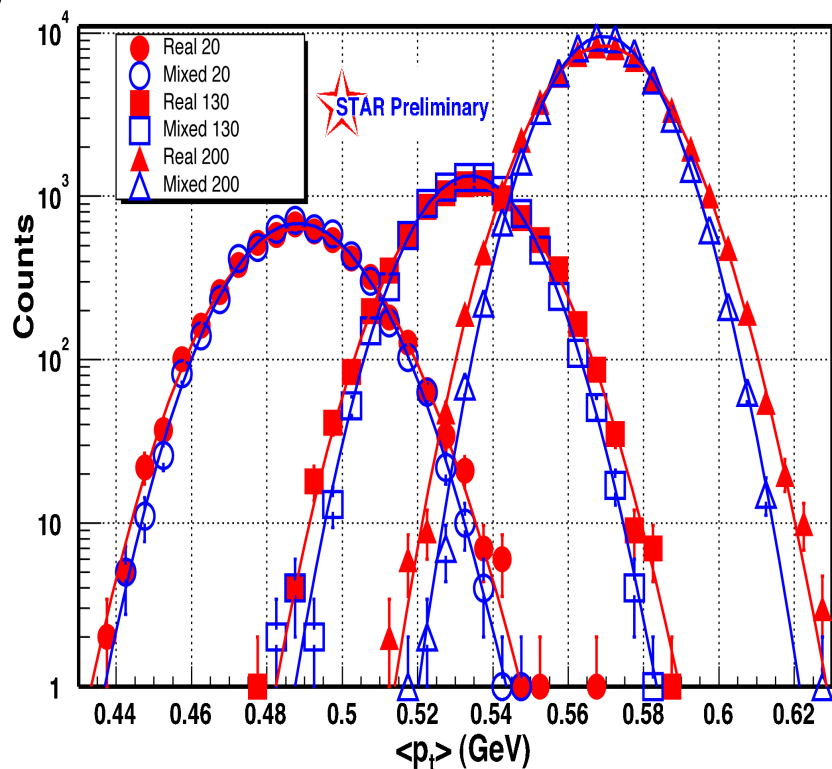
Pt Fluctuations

- Probe of phase instabilities near QCD phase boundary
 - H. Heiselberg, Phys. Rep. 351 (2001) 161
 - M. Stephanov et al. PRL 81 (1998) 4816; PRD 60 (1999) 114028.
- Onset of thermalization
 - S. Gavin, PRL 92 (2004) 162301.
- Main Measurements
 - NA49, Phys. Lett B459 (1999) 679.
 - CERES, Nucl. Phys.A727 (2003) 97.
 - STAR, PRC 71 (2005) 064906.
 - PHENIX, PRL 93 (2004) 092301.
 - ALICE (analysis in progress?)

pT Fluctuations



- Au - Au Collisions



0 - 5 % central ; $|\eta| < 1.0$
 $\langle p_T \rangle$ measured e-by-e
 Real is wider than mixed

$$\langle \langle p_T \rangle \rangle = \sum_{i=1}^{N_{event}} \langle p_T \rangle_i / N_{event}$$

$$\langle \Delta p_{T,i} \Delta p_{T,j} \rangle = \frac{1}{N_{event}} \sum_{i=1}^N \sum_{j=1, i \neq j}^N \frac{(p_{T,i} - \langle \langle p_T \rangle \rangle)(p_{T,j} - \langle \langle p_T \rangle \rangle)}{N(N-1)}$$

N_{event} = number of events

$\langle p_T \rangle_i$ = average p_T for i^{th} event

N = number of tracks for i^{th} event

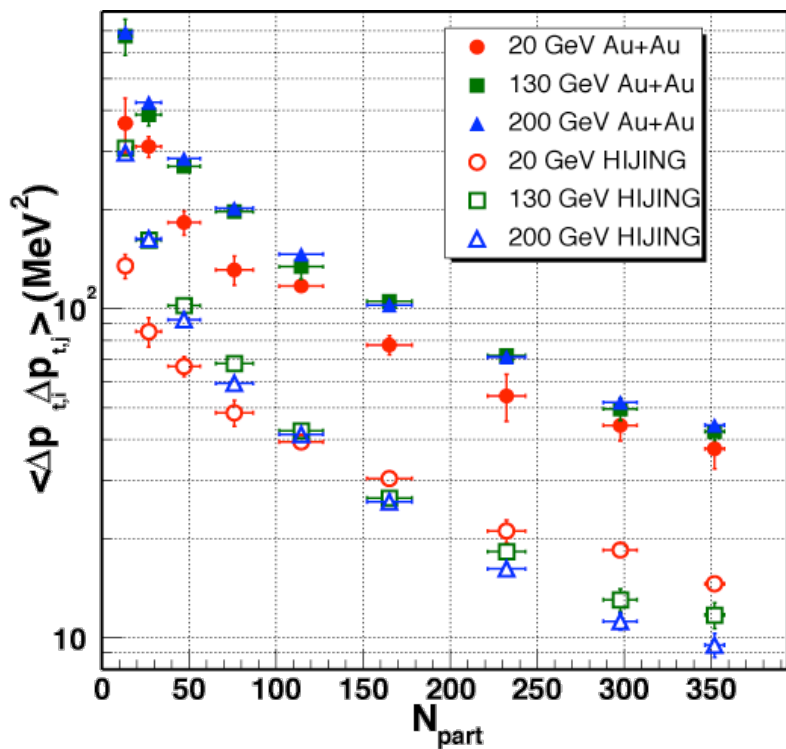
$p_{T,i}$ = p_T for i^{th} track in event

Equivalent to...

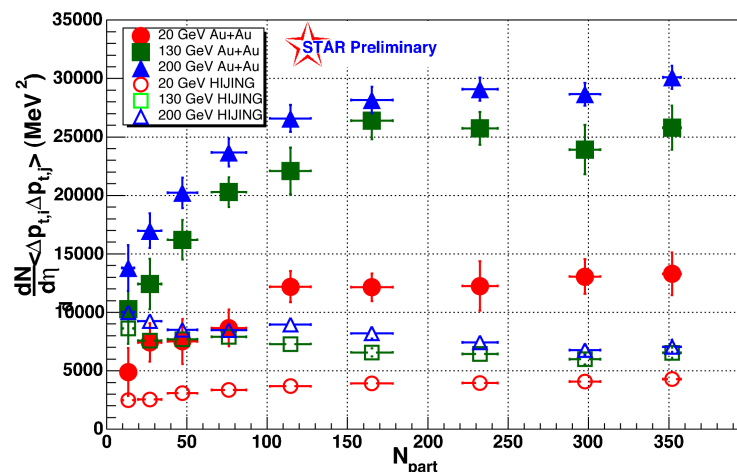
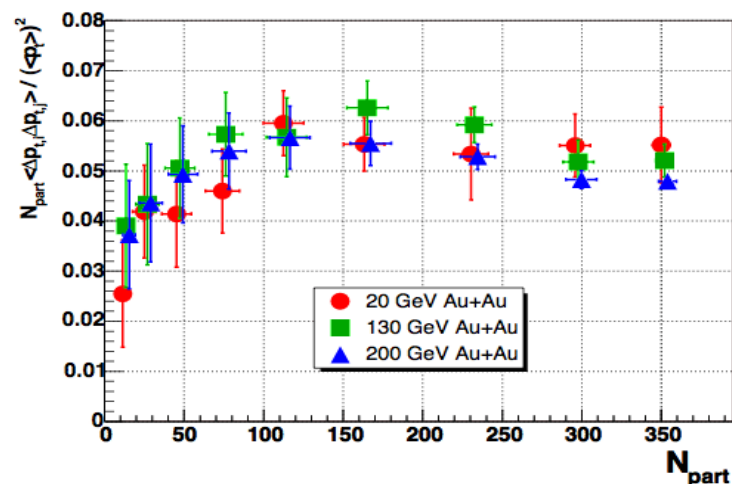
$$\langle \Delta p_T \Delta p_T \rangle = \frac{\int \rho_2 \Delta p_{T,1} \Delta p_{T,2} dp_{T,1} dp_{T,2}}{\int \rho_2 dp_{T,1} dp_{T,2}}$$

pT Fluctuations

Au - Au Collisions



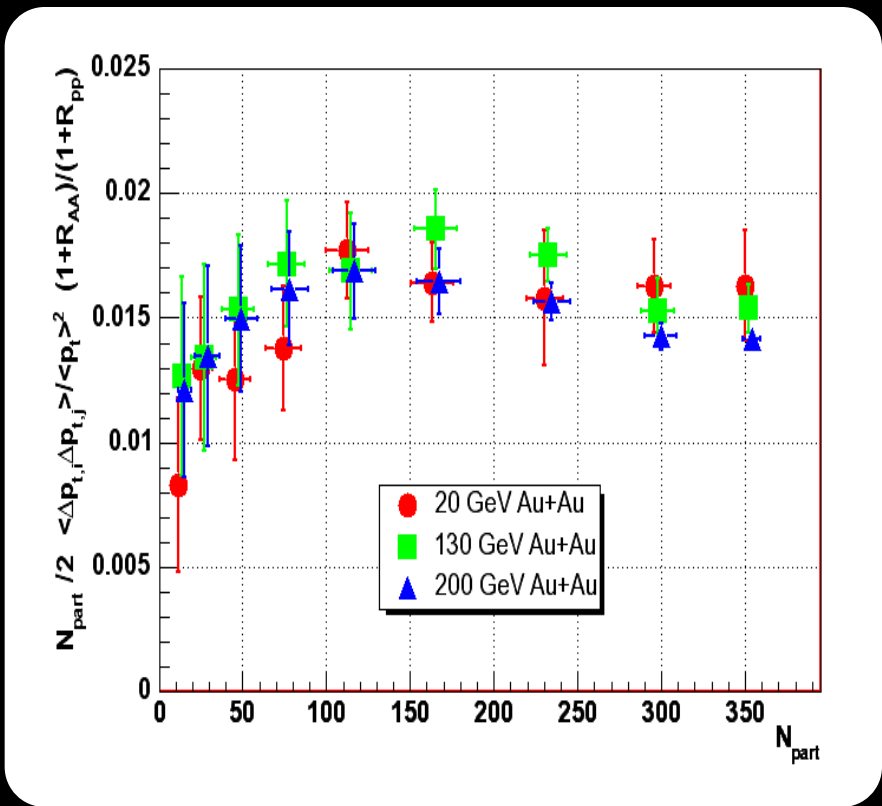
- Dynamic pT Correlations
- Approx $1/N_{\text{part}}$ dependence
- $1/dN/d\eta$ scaling violation
- Modest dependence on beam energy.
- Dramatic Disagreement w/ HIJING



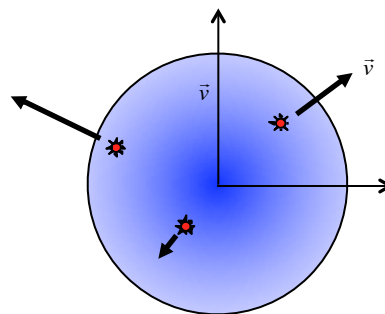
pT Fluctuations

Scaling Behavior

Au - Au Collisions

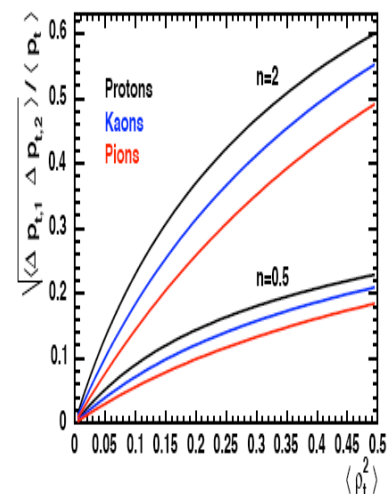
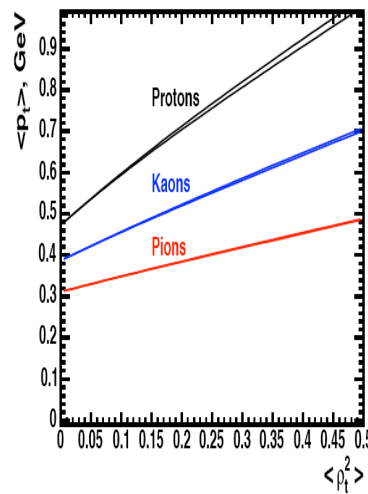


S. Voloshin, nucl-th/0312065



"blast wave" Model

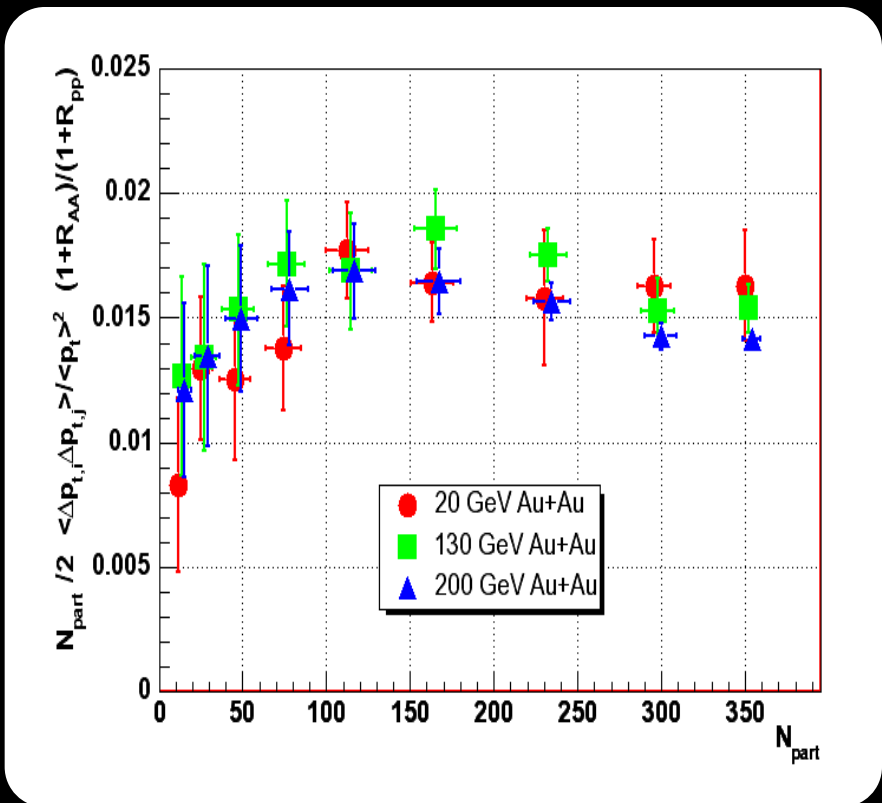
$$v \propto r^n$$



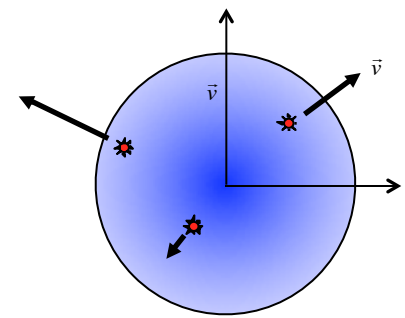
pT Fluctuations

Scaling Behavior

Au - Au Collisions

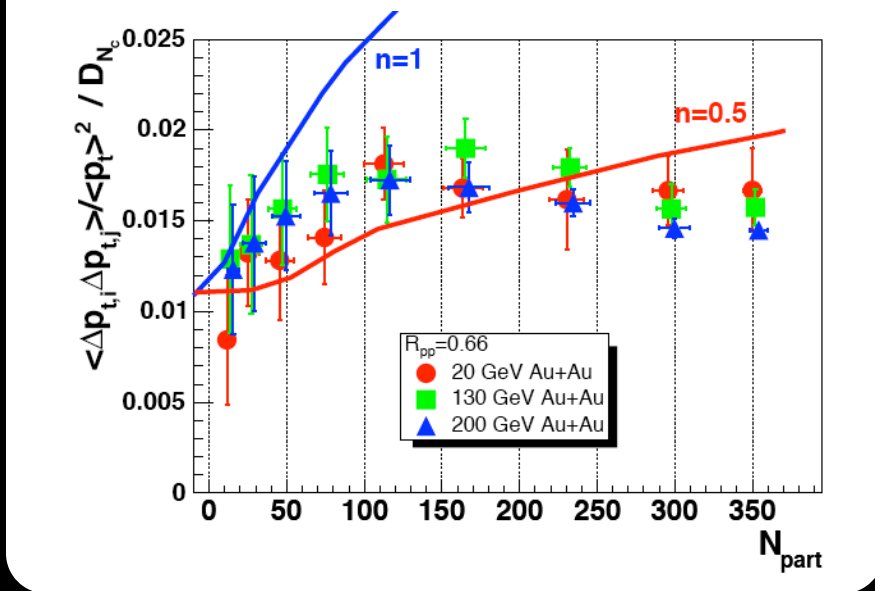


S. Voloshin, nucl-th/0312065

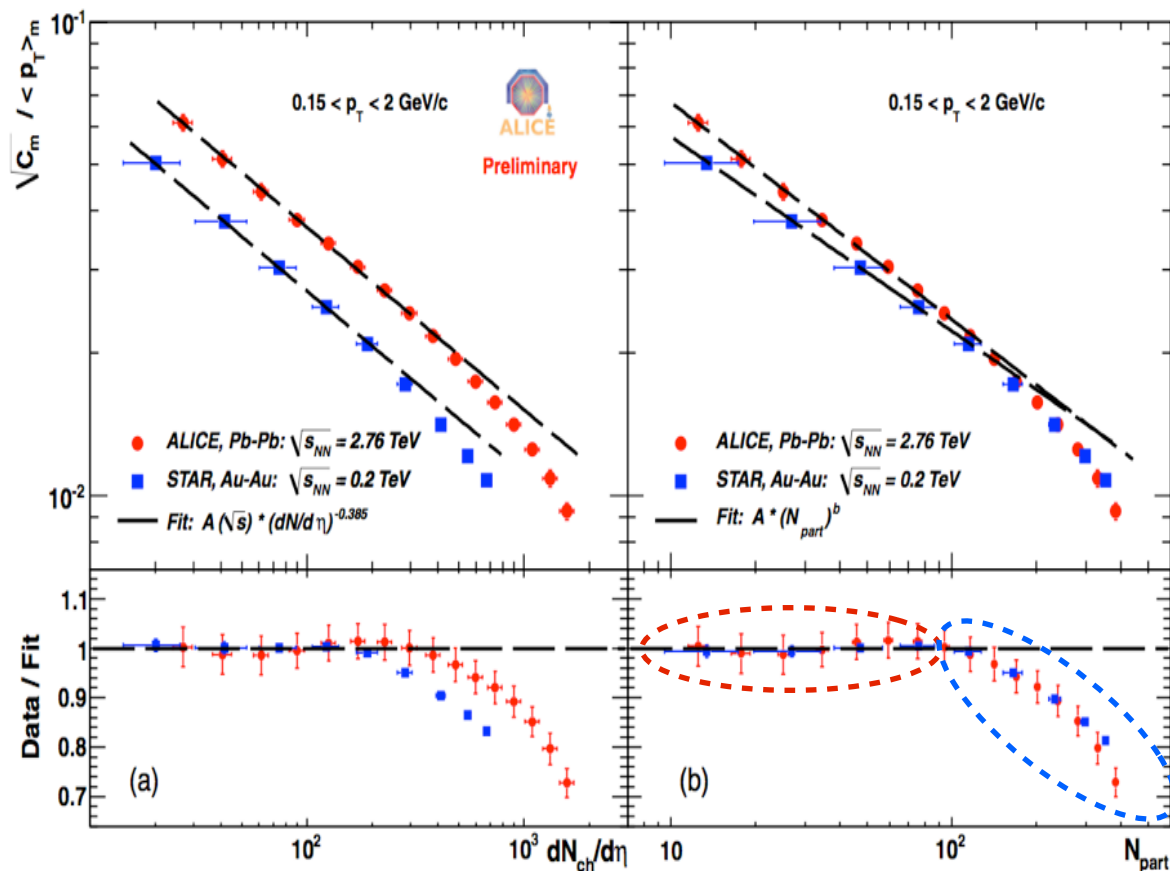
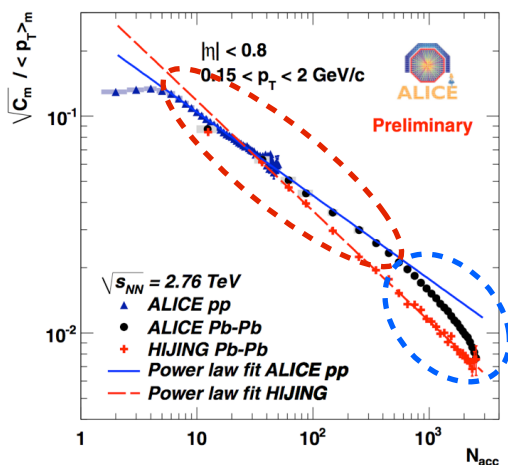
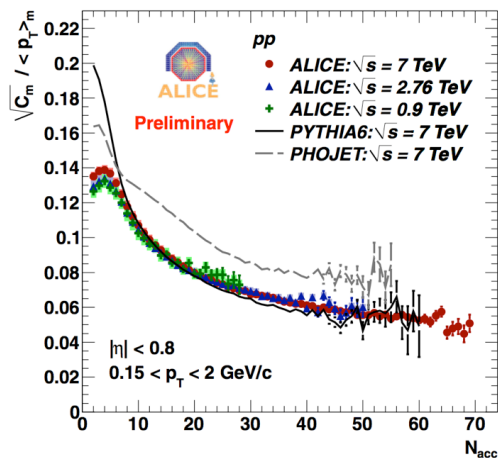


"blast wave" Model

$$v \propto r^n$$



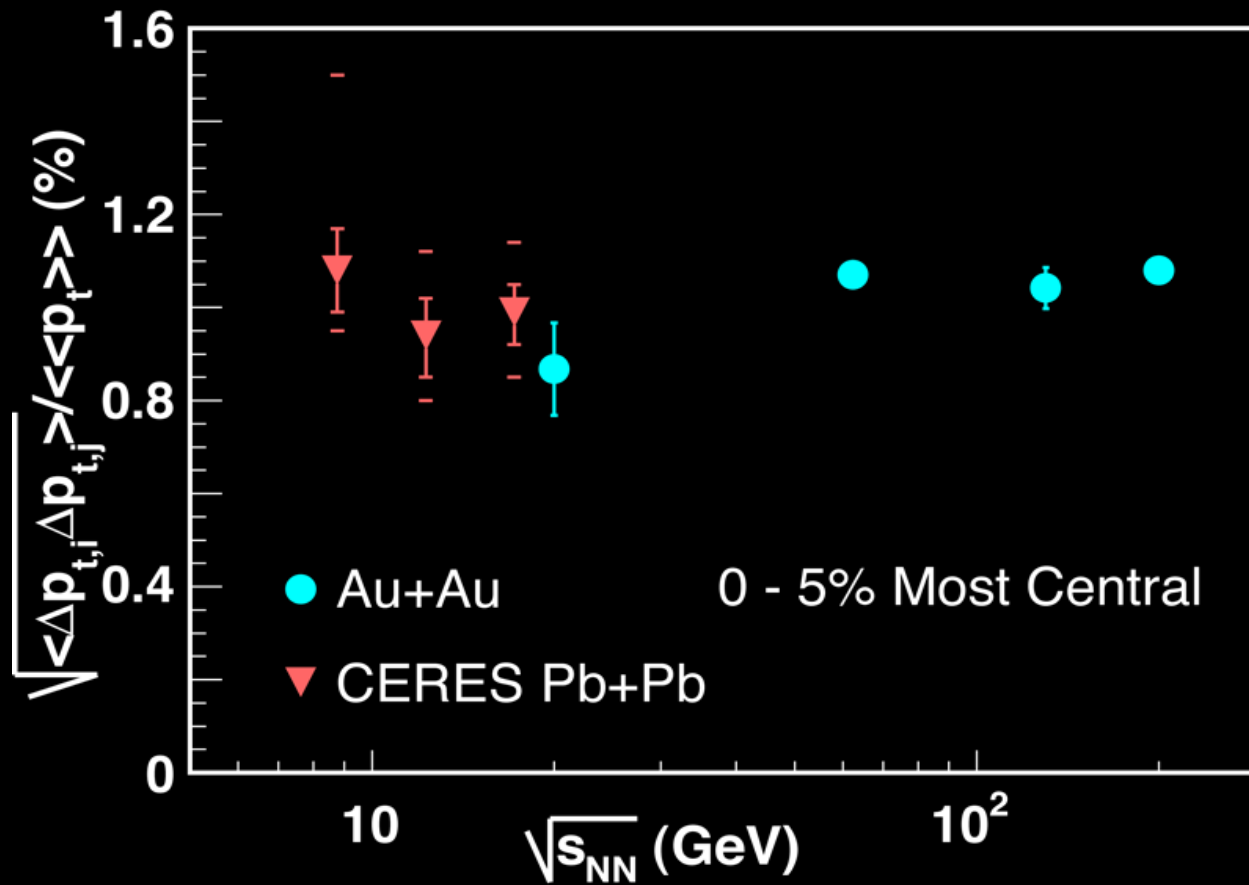
pT Fluctuations (ALICE)



- Dependence on beam energy
- AA scales as pp below $N_{part} \sim 100$
- Substantial “medium” effects for $N_{part} > 100$

J. Phys. G, Nucl. Part Phys. 38 (2011) 124095

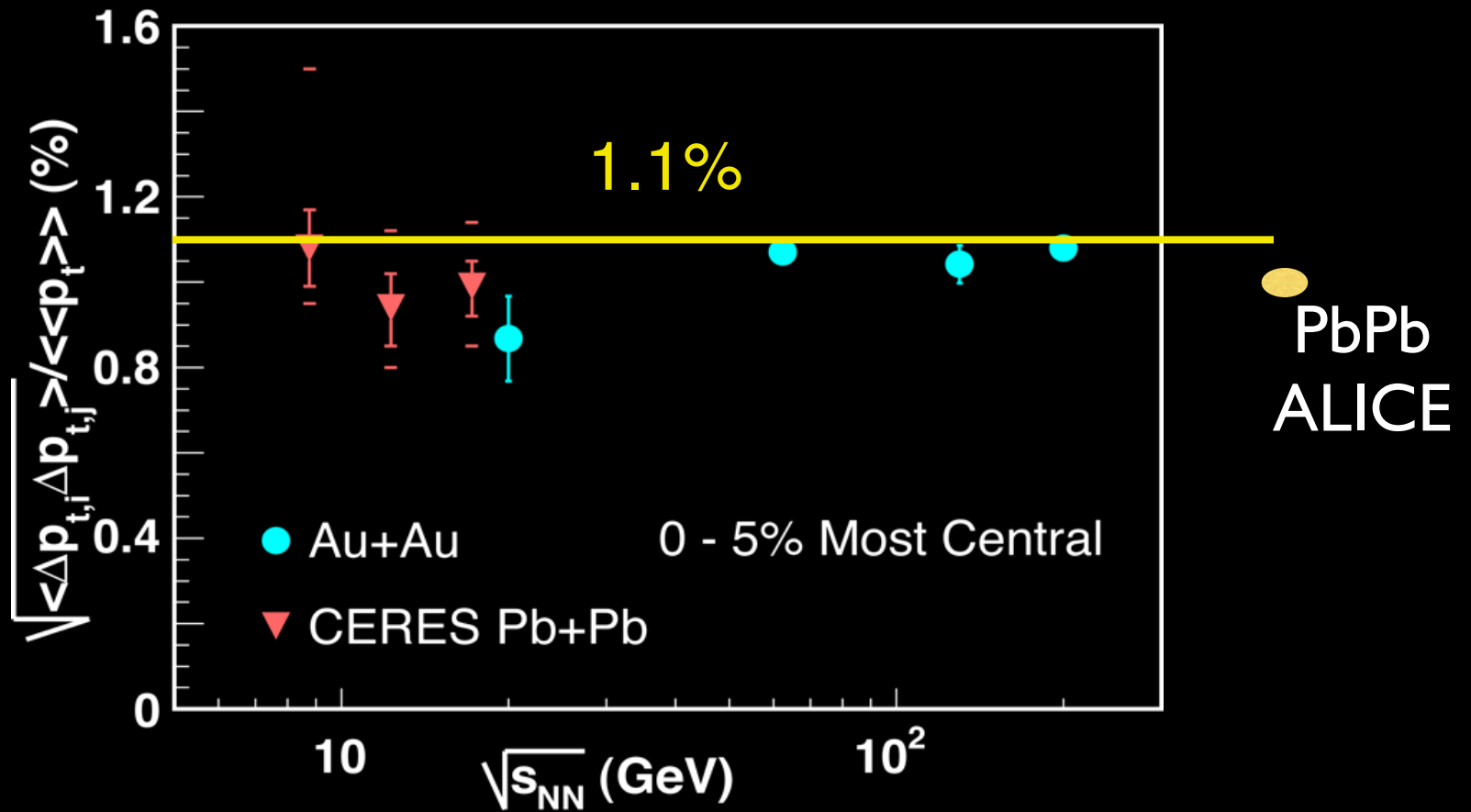
$$(\langle \Delta p_{t,i} \Delta p_{t,j} \rangle)^{1/2} / \langle \langle p_t \rangle \rangle$$



● PbPb
ALICE

No smoking gun!

$$(\langle \Delta p_{t,i} \Delta p_{t,j} \rangle)^{1/2} / \langle \langle p_t \rangle \rangle$$



No smoking gun!

The Mach Cone “Puzzle”

$R_{AA} \sim 0.2$ implies large energy/momentum loss.

Where is the energy/momentum going?

- Mach Cone Emission?
- Medium recoil?

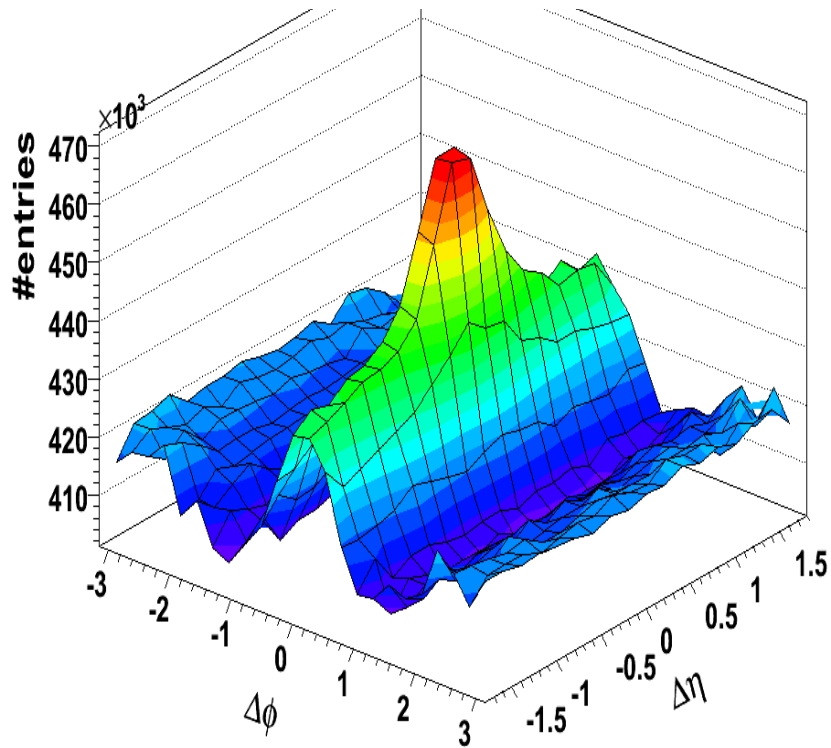
The Ridge and the Dip



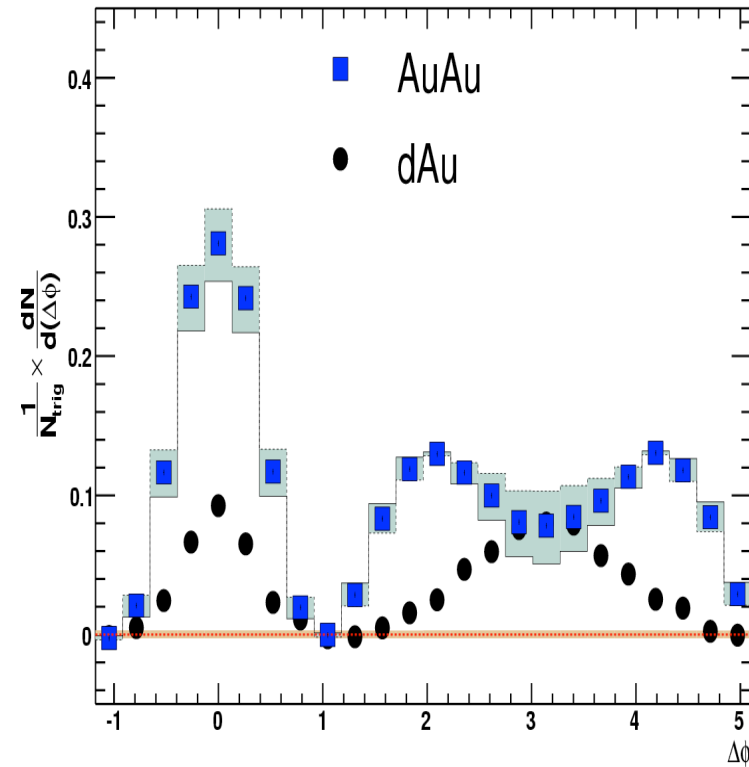
Au+Au 0-10% STAR

$3 < p_{T,trigger} < 4$ GeV; $p_{T,assoc.} > 2$ GeV

$p_{T,trig} = 3.0-4.0$ GeV/c; $p_{T,asso} = 1.0-2.5$ GeV/c



Jörn Putschke, et al., STAR, Quark Matter 2006



Mark Horner, et al., STAR, Quark Matter 2006

Near-Side Ridge

Away-Side Dip

Theoretical Scenarios: Ridge & Dip (2006)

Ridge

Parton radiation (Armesto et al)

- Radiates energy before fragmenting and couples to the longitudinal flow
- Gluon bremsstrahlung of hard-scattered parton
- Parton shifted to lower p_t
- Radiated gluon contributes to broadening
- Near-side jet also loses energy (finite pathlength)!

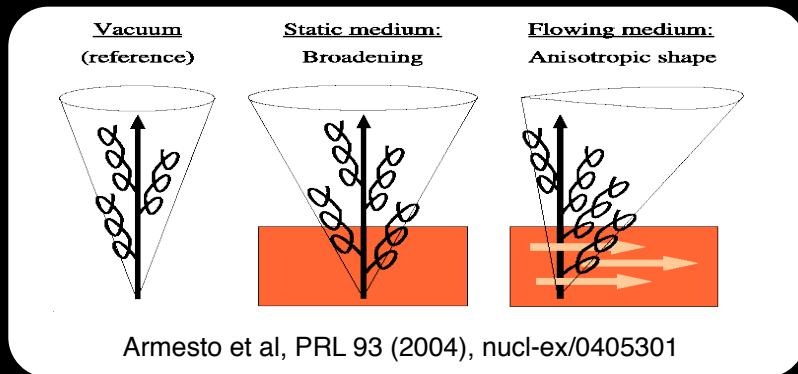
Medium heating + Parton recombination

(Chiu & Hwa Phys. Rev. C72:034903,2005)

- Recombination of thermal partons only indirectly affected by hard scattering \rightarrow not part of the jet

Radial flow + trigger bias

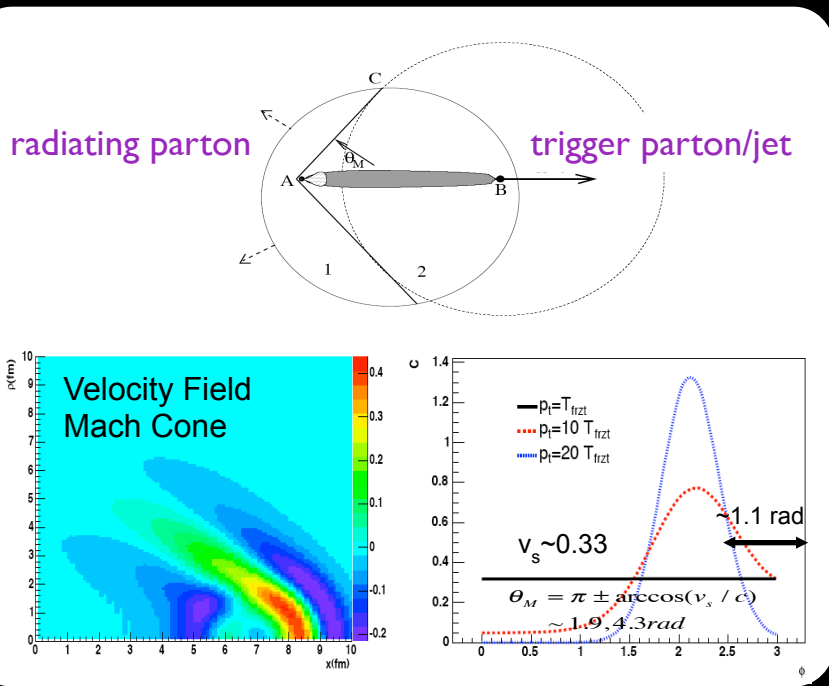
- S.A.Voloshin, Nucl. Phys. A749, 287 (2005)
- C. Pruneau, et al, Nucl.Phys. A802 (2008) 107-121.



Dip

Mach Cone Concept/Calculations

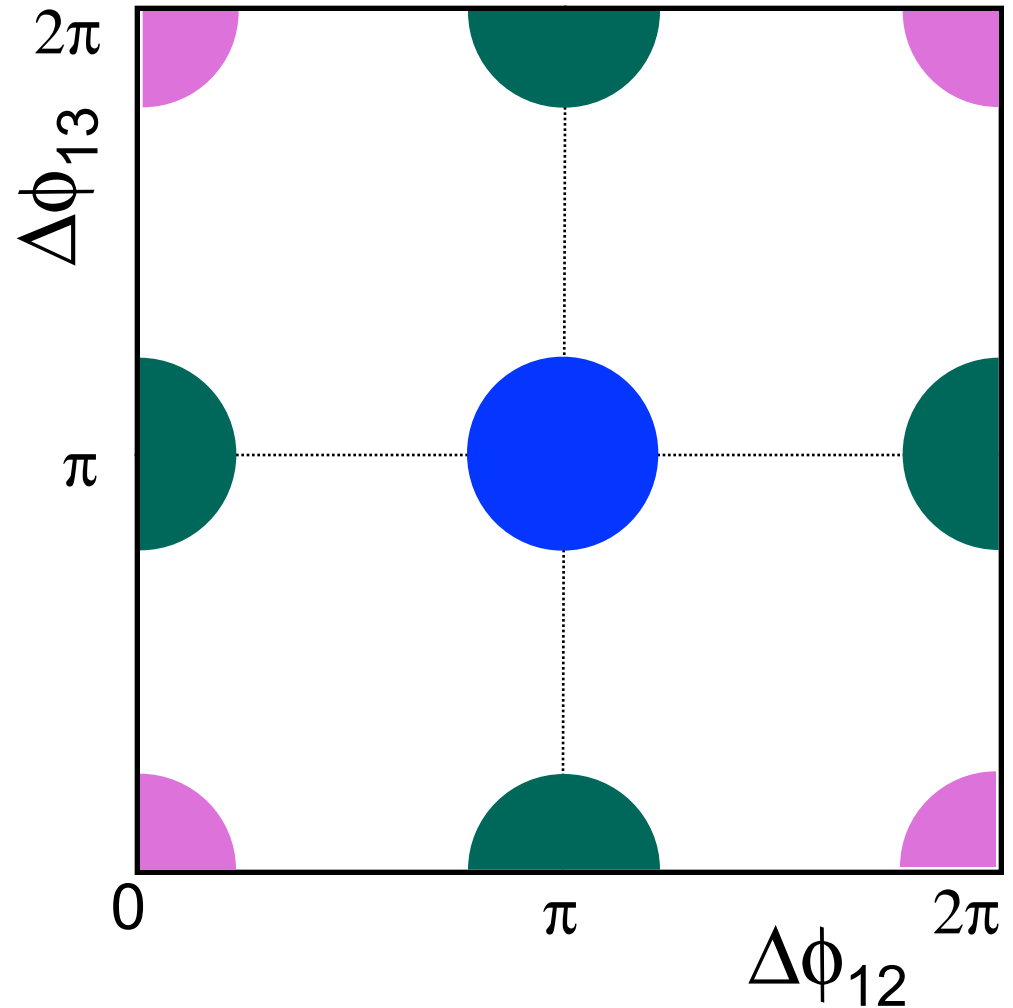
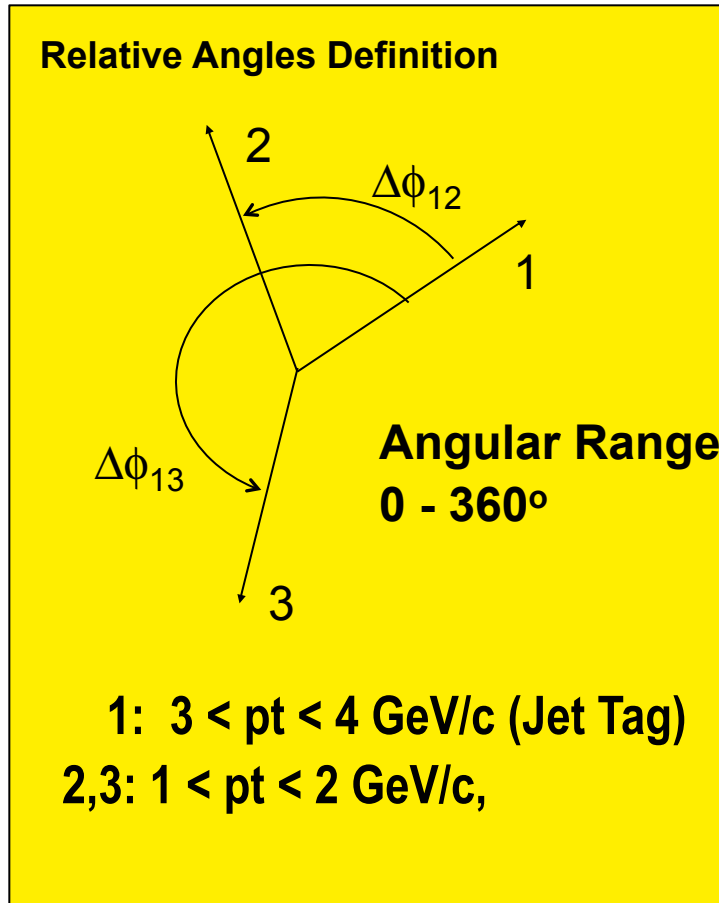
- Stoecker, Casalderry-Solana et al, Muller et al.; Ruppert et al., ...
 - Cherenkov Radiation Majumder, Koch, & Wang; Vitev
- Jet Deflection (Flow)
- Fries; Armesto et al.; Hwa



Mach Cone & Deflection Kinematical Signatures



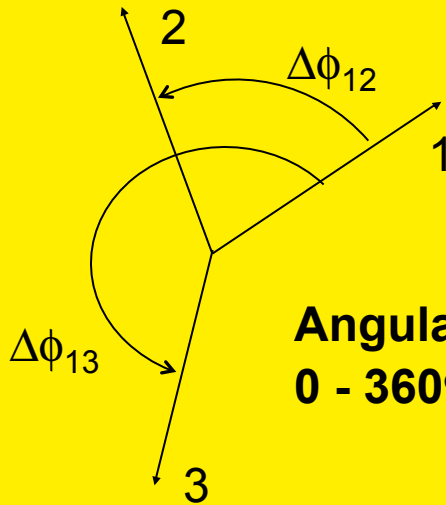
Back-to-back Jets “in vacuum”



Mach Cone & Deflection Kinematical Signatures



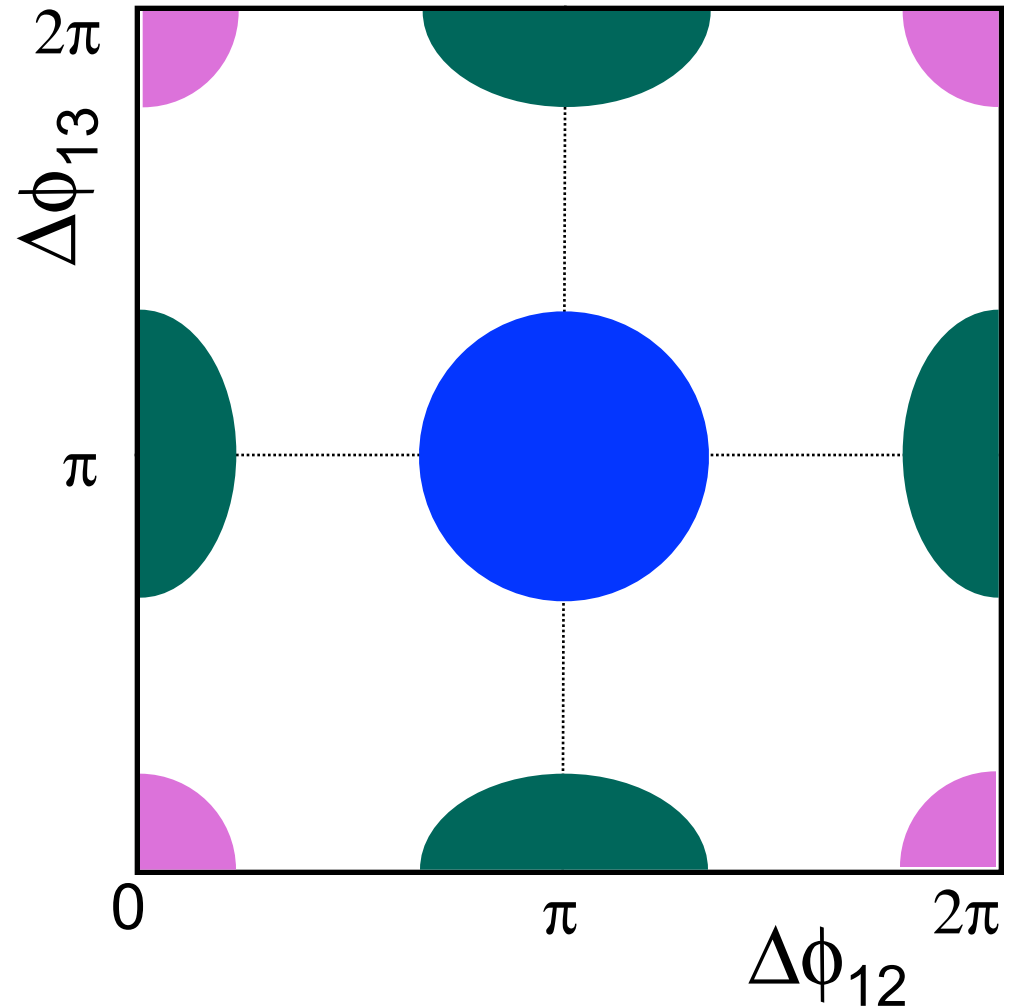
Relative Angles Definition



**Angular Range
0 - 360°**

1: $3 < pt < 4$ GeV/c (Jet Tag)
2,3: $1 < pt < 2$ GeV/c,

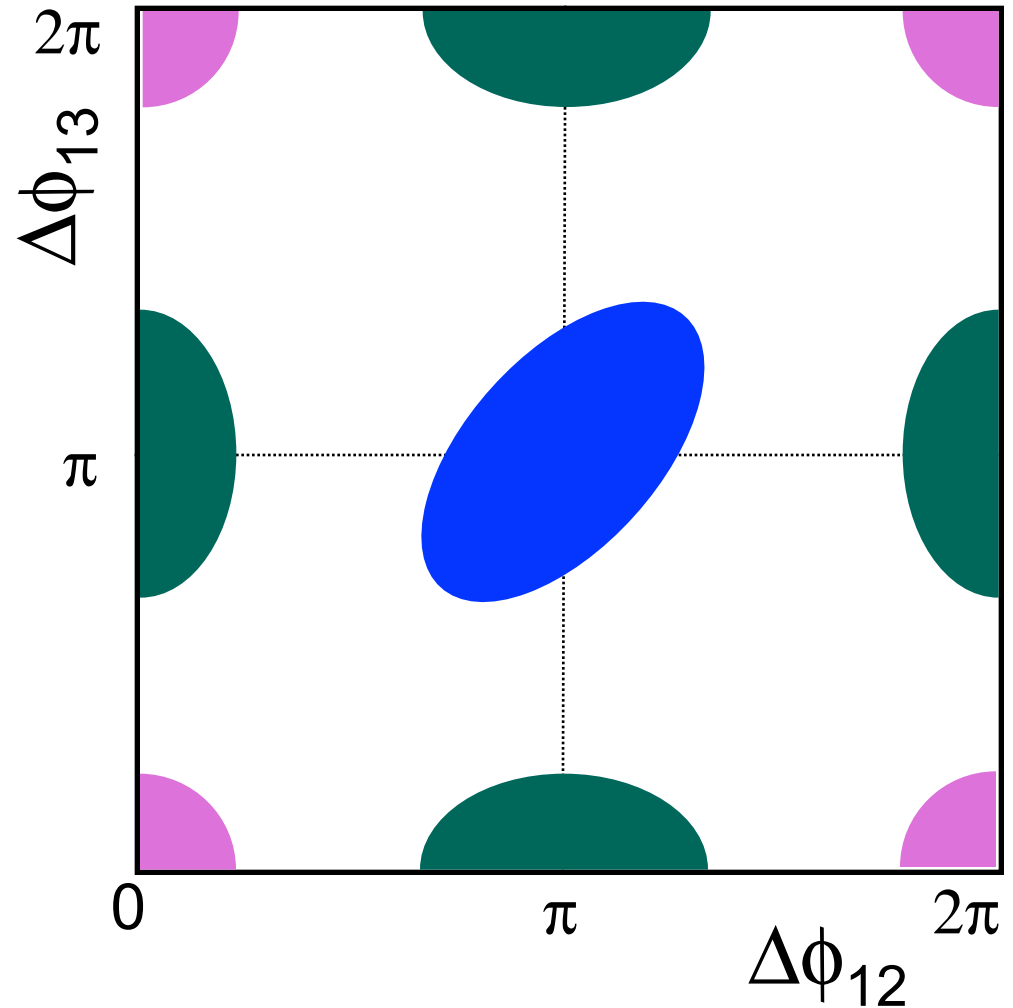
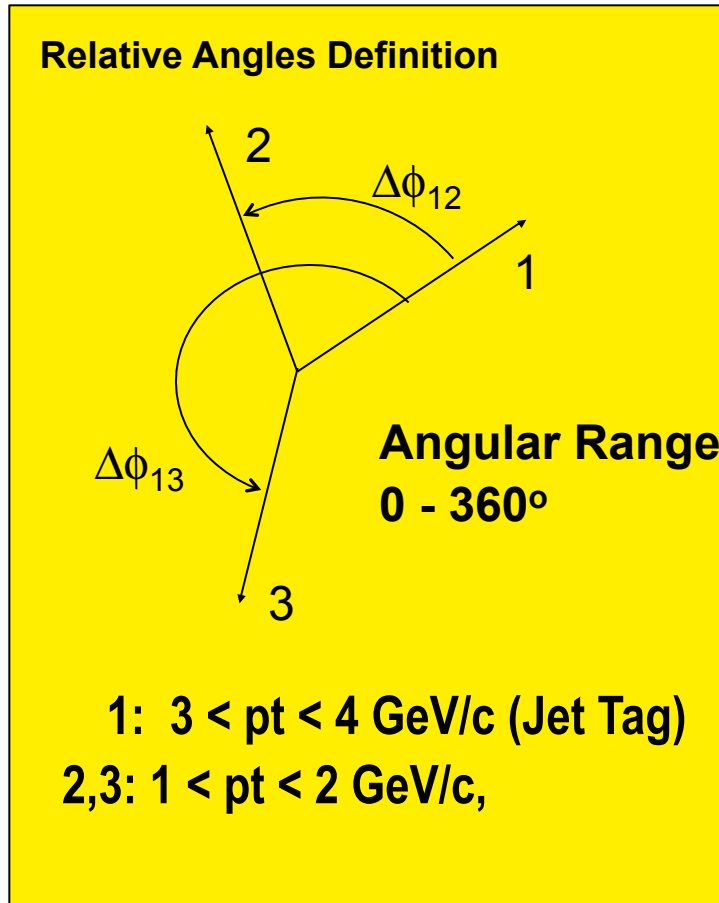
Away-side broadening



Mach Cone & Deflection Kinematical Signatures



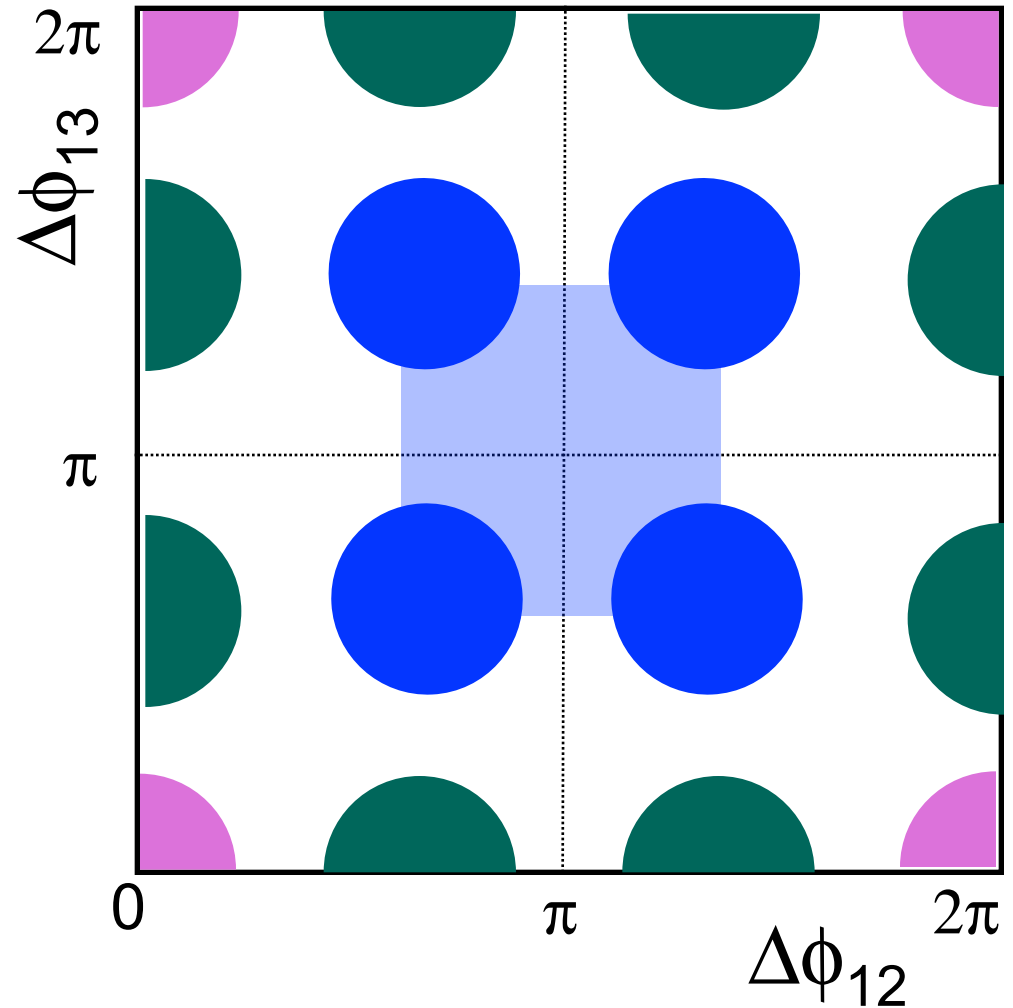
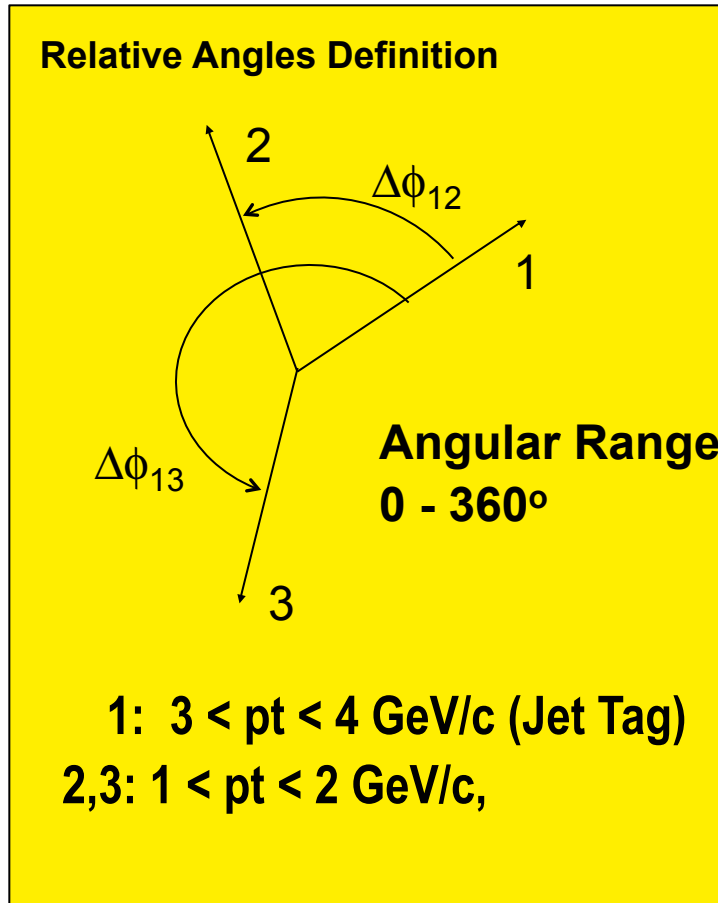
Away-side deflection & flow



Mach Cone & Deflection Kinematical Signatures



Mach Cone



Measurement of 3-Particle Cumulant



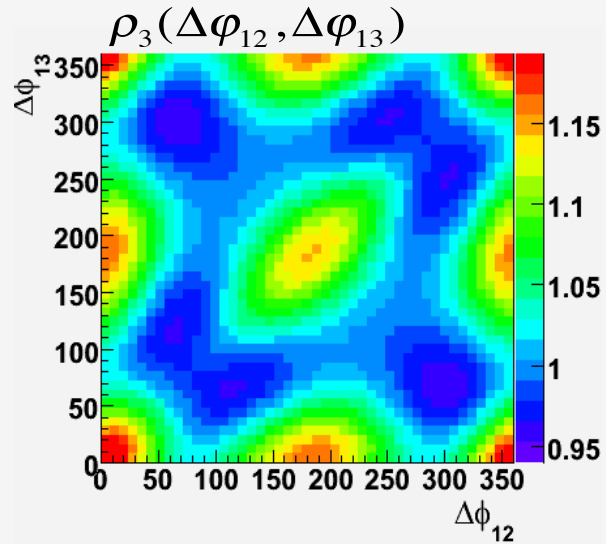
- Jet tag (trigger) : $3 < p_t < 4$, or $20 \text{ GeV}/c$, $|\eta| < 1$
- Associates: $1 < p_t < 2 \text{ GeV}/c$, $|\eta| < 1$

C.P., J.Phys. G34 (2007) S667-S670

Measurement of 3-Particle Cumulant



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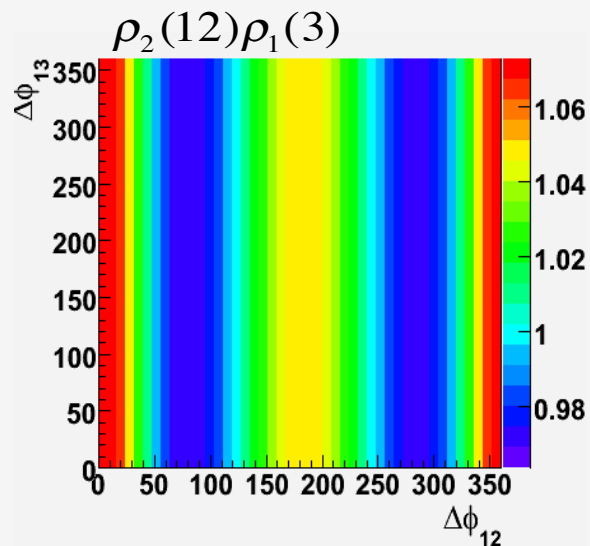
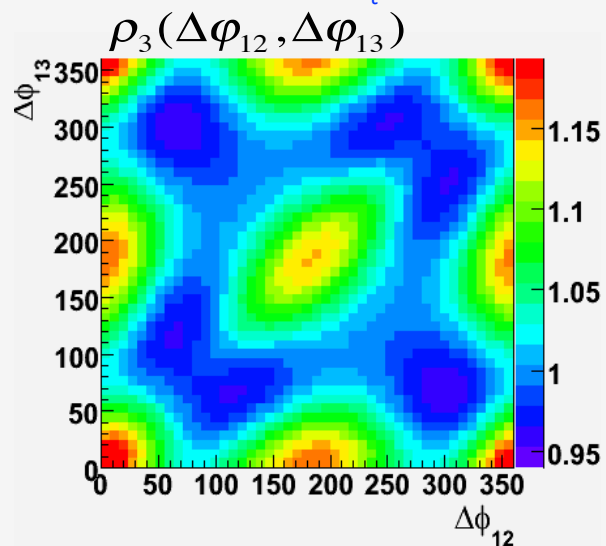


C.P., J.Phys. G34 (2007) S667-S670

Measurement of 3-Particle Cumulant



- Jet tag (trigger) : $3 < p_t < 4$, or 20 GeV/c, $|\eta| < 1$
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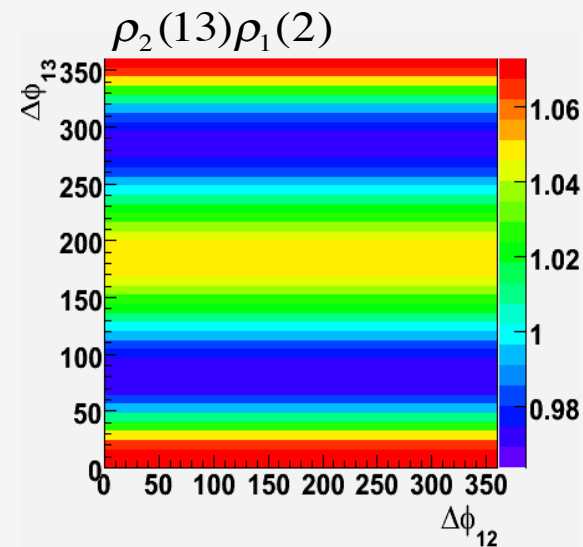
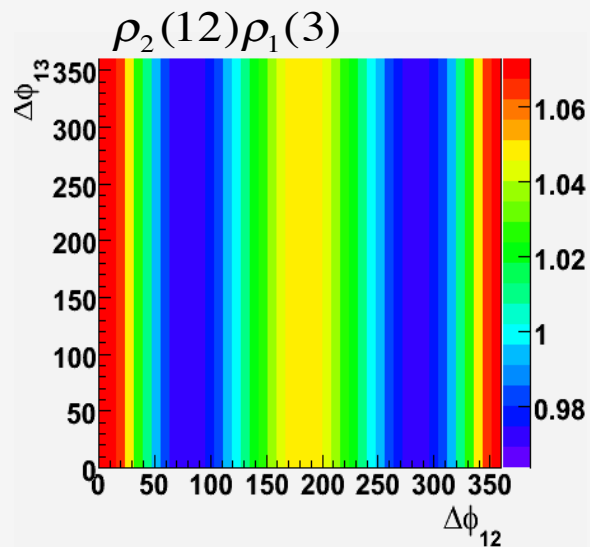
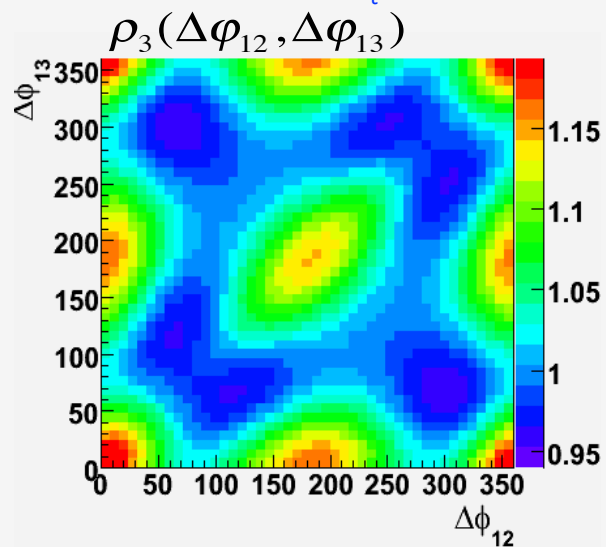


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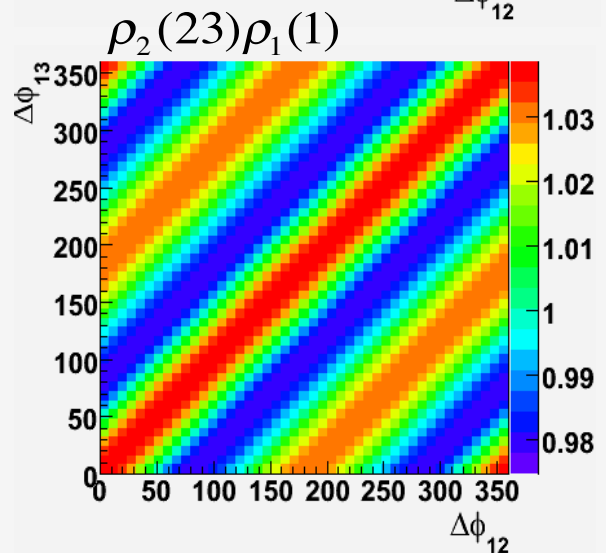
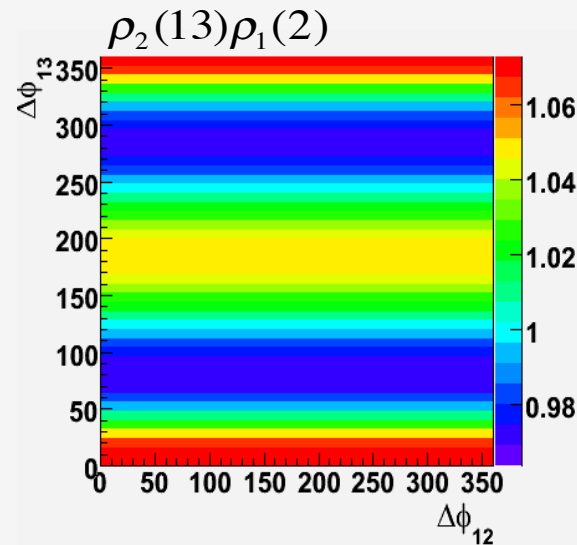
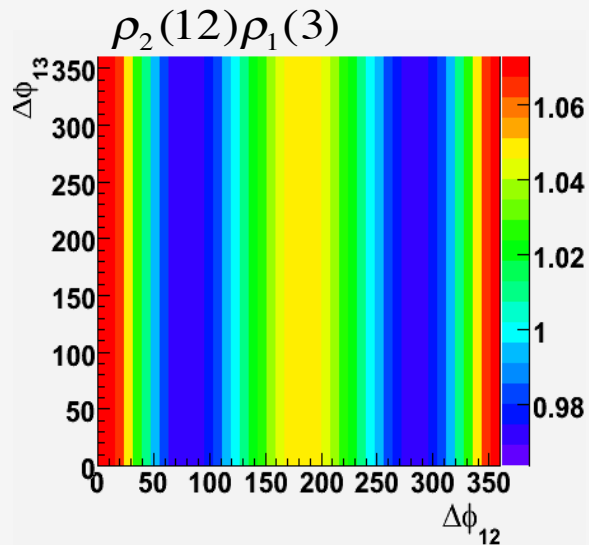
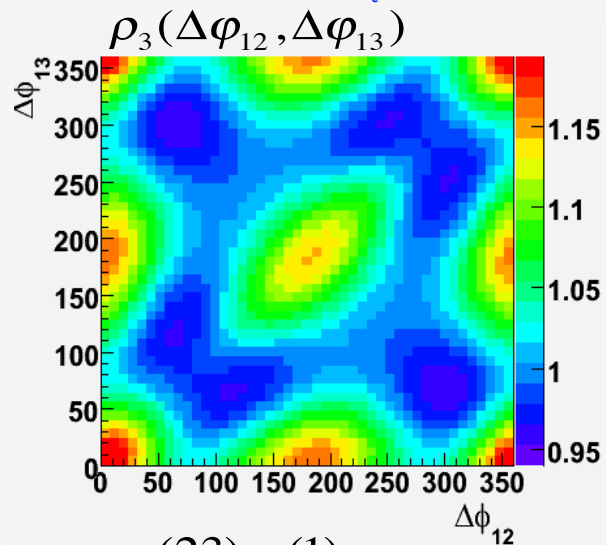


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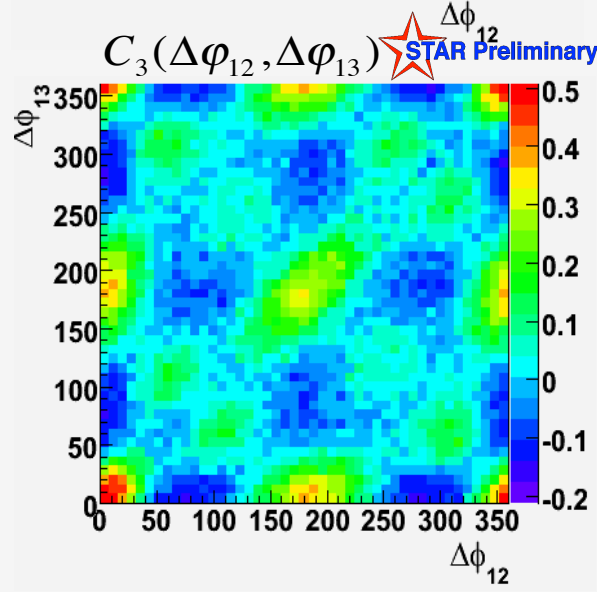
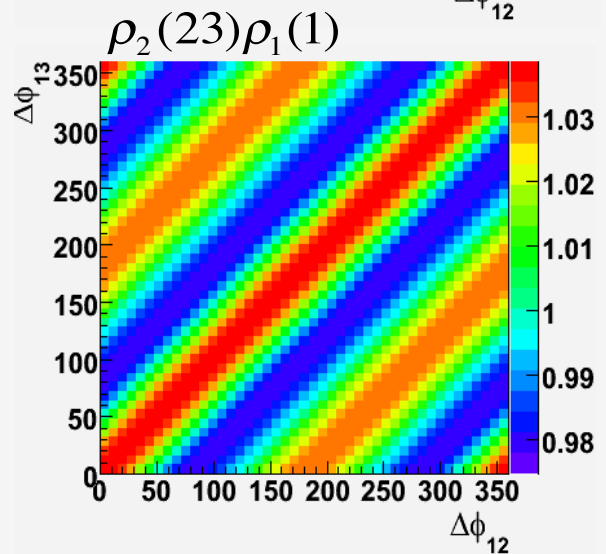
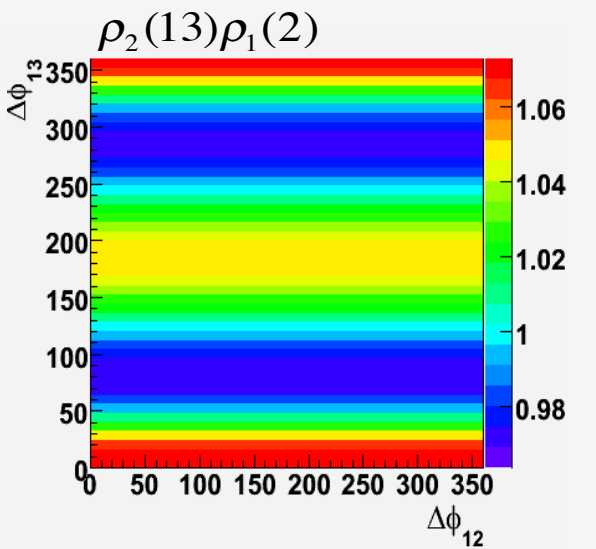
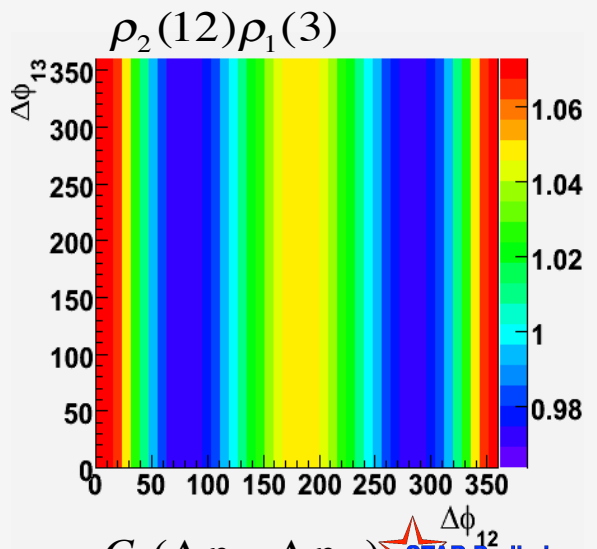
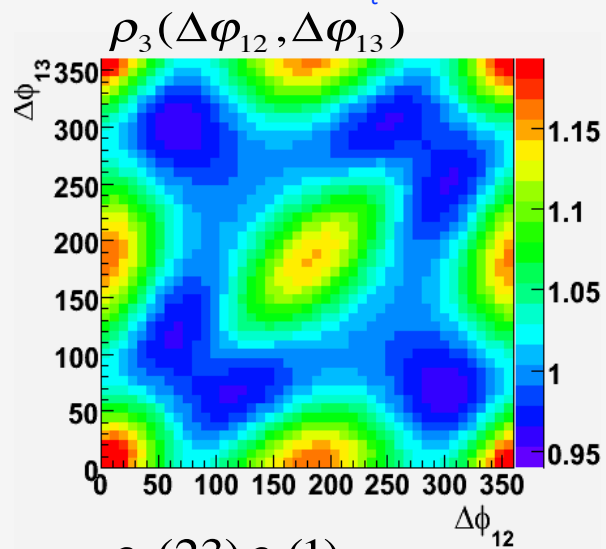


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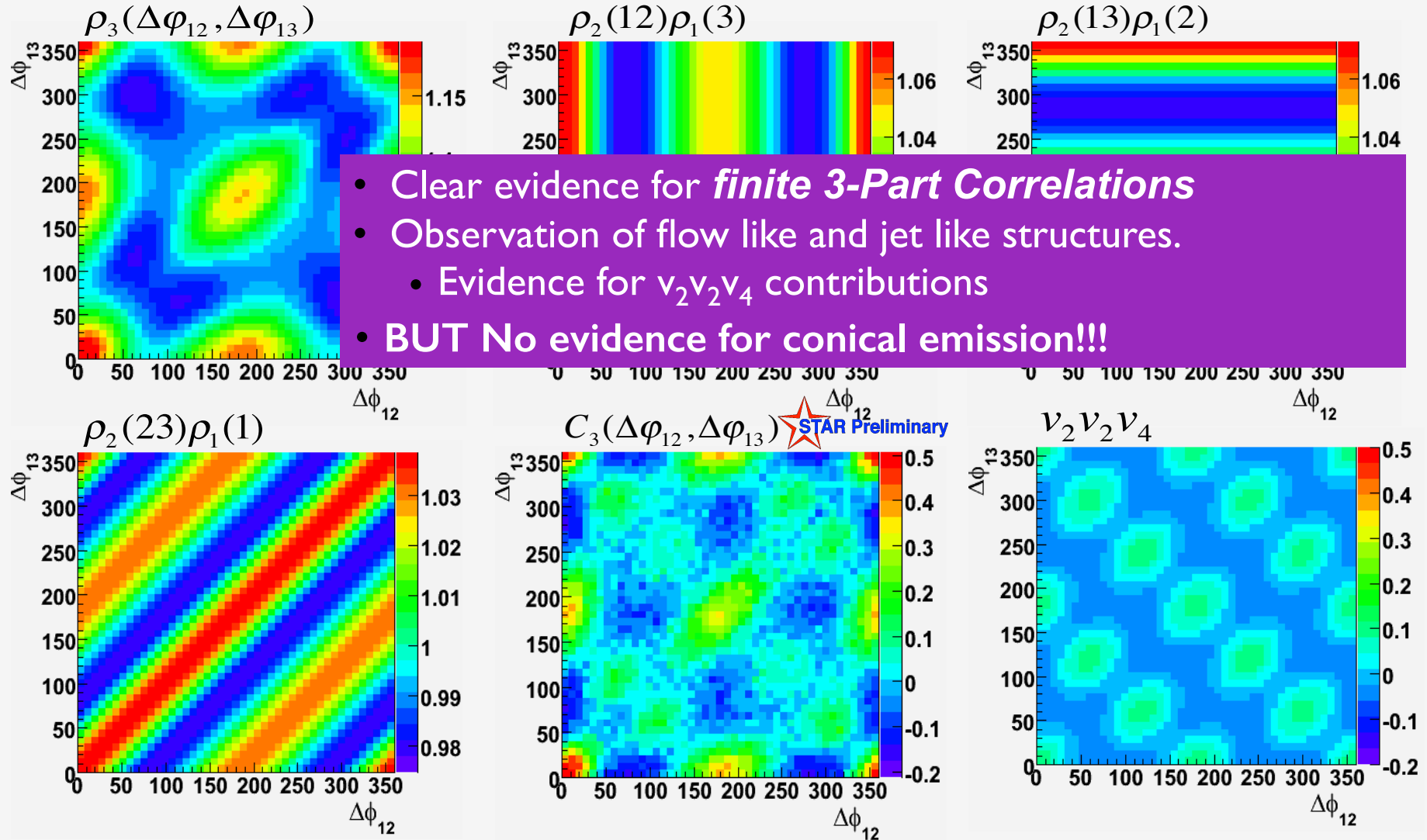


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Measurement of 3-Particle Cumulant



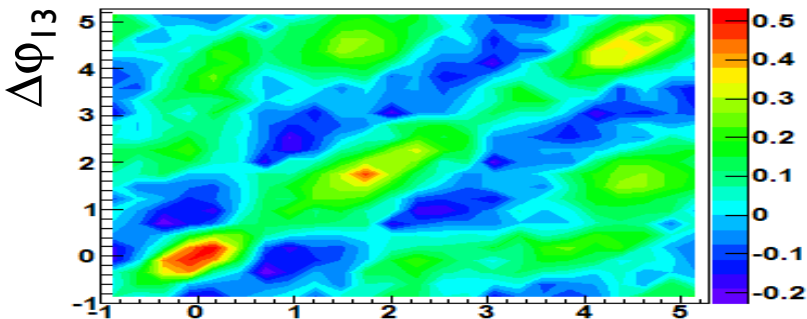
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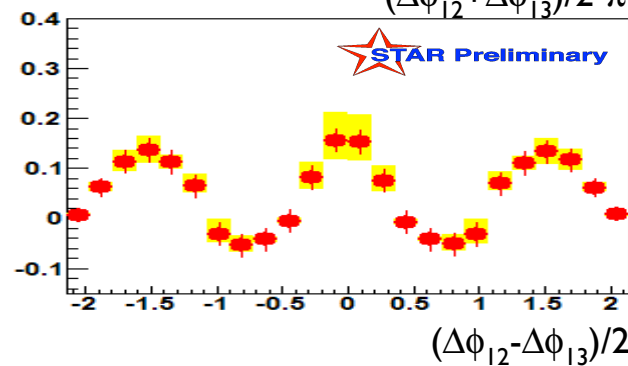
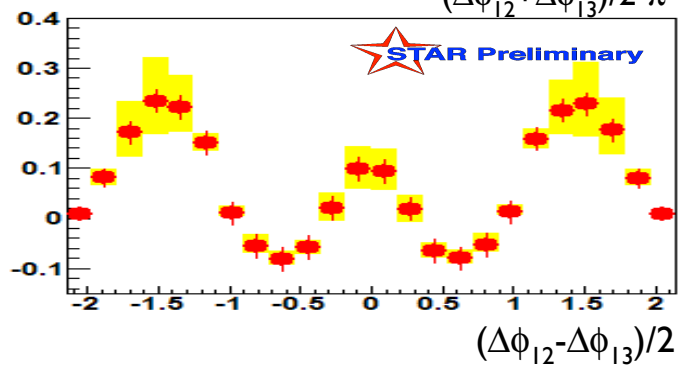
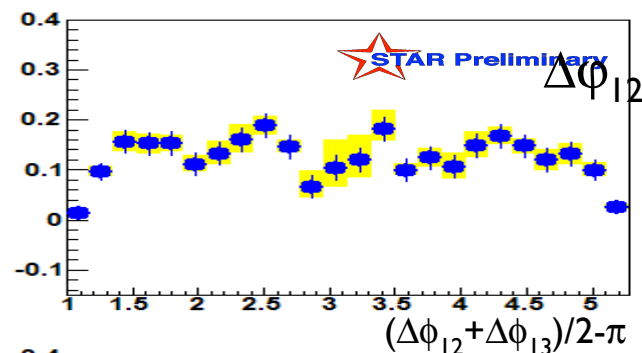
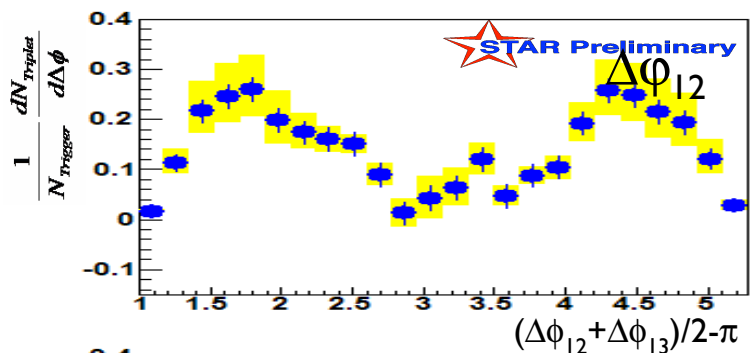
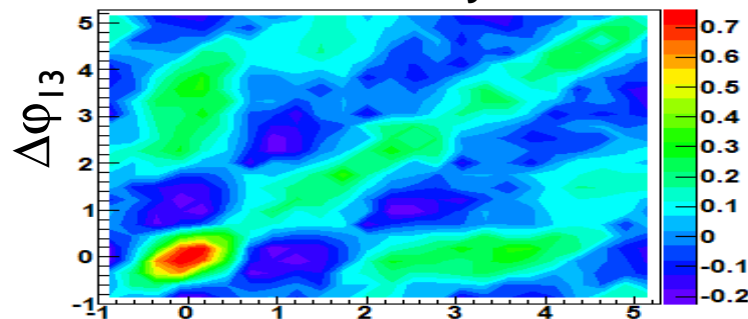
C.P., J.Phys. G34 (2007) S667-S670

Two-Component Model Analysis

Au+Au 0-12%



Au+Au 0-12% No Jet Flow



STAR, Phys.Rev.Lett. 102 (2009) 052302

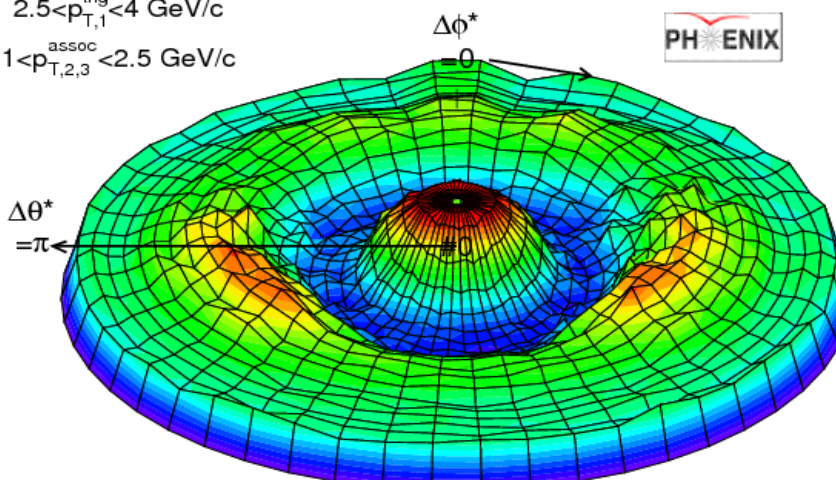
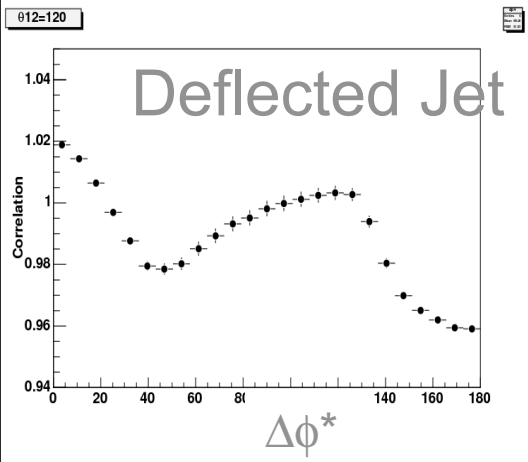
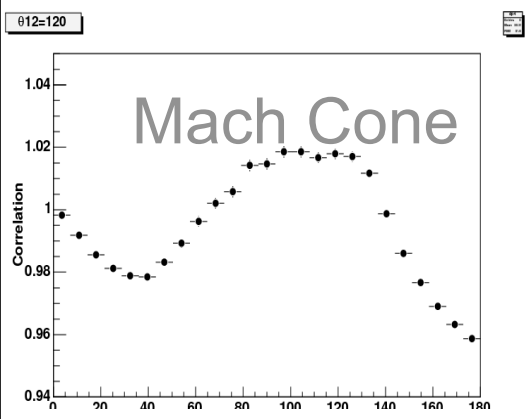
Three particle correlation

Chun Zhang, et al. PHENIX, QM06

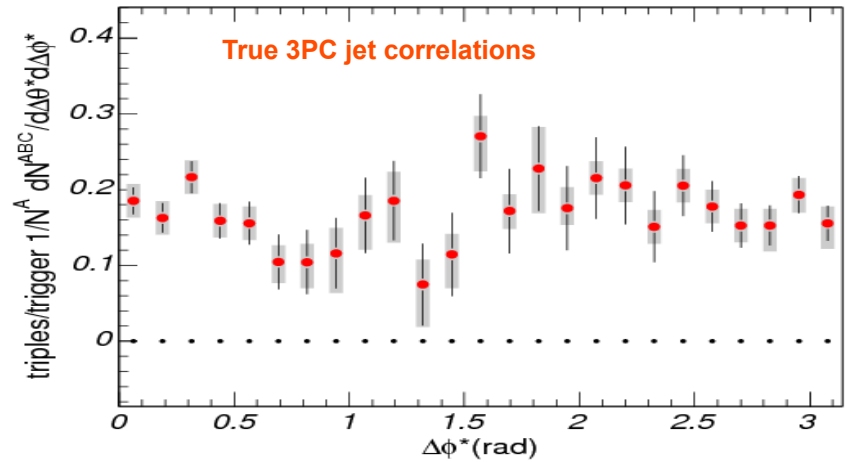
Real data

$\sqrt{s_{NN}}=200\text{GeV}$ PHENIX Total 3-Particle Jet Corrn. Cent = 10-20%
 $2.5 < p_{T,1}^{\text{trig}} < 4 \text{ GeV}/c$
 $1 < p_{T,2,3}^{\text{assoc}} < 2.5 \text{ GeV}/c$

PHENIX simulation



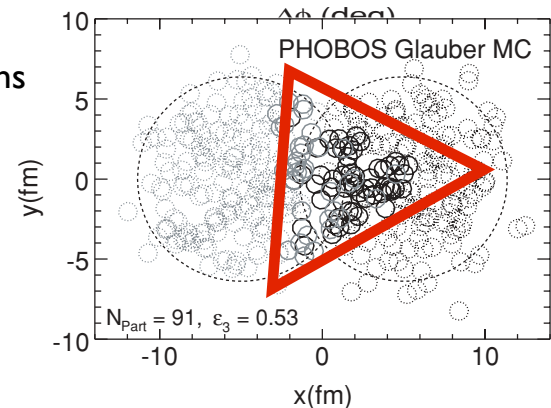
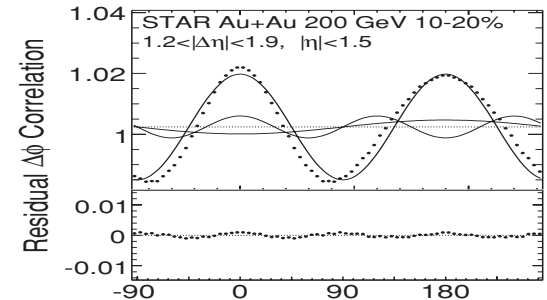
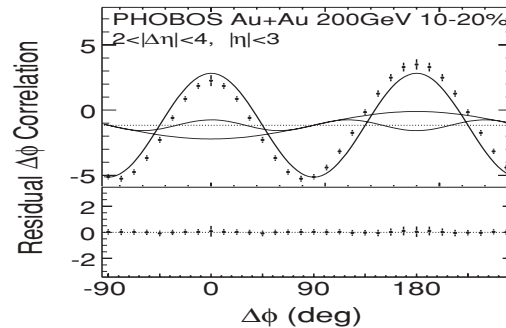
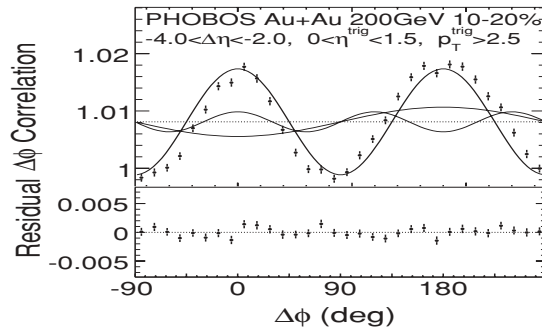
PHENIX Preliminary
 Au+Au $\sqrt{s_{NN}}=200 \text{ GeV}$
 PHENIX η True 3-Particle Jet Correlation along $\Delta\phi^*$
 $2.5 < p_{T,1}^{\text{trig}} < 4 \text{ GeV}/c$ $1 < p_{T,2,3}^{\text{assoc}} < 2.5 \text{ GeV}/c$
 $\Delta\theta^* = \langle 1.65-2.2 \rangle \text{ rad}$ cent 10-20 %



Data is consistent with the presence of a Mach Cone away-side jet but does not rule out small contributions from other topologies.

Paradigm Shift...

B. Alver & G. Roland, PRC 81, 054905 (2010)

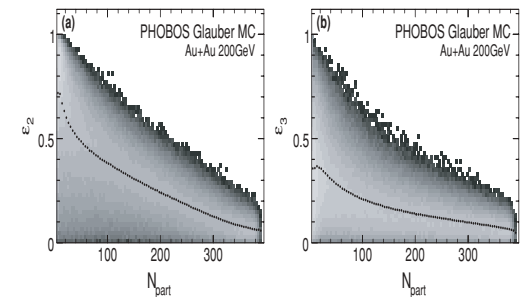


Collision-geometry fluctuations and triangular flow in heavy-ion collisions

- Underlying Assumptions
- Initial Collisions Produce Long Range Correlations
- Fast Thermalization $\gg \gg$ Medium
- Hydrodynamic Evolution
- *Spatial Anisotropy* $\gg \gg$ *Momentum Anisotropy*
- Finite System Has **Non-zero Odd Spatial Eccentricities**

Consequences:

- Initial Geometry Fluctuations Produce Odd Harmonics
- Produces an away-side dip
- **SIMPLE EXPLANATIONS ARE THE BEST!!!!**
- **Most people lost interest in conical emission!**
- **But it might still exist...**
- **There are ways to fish it out if it is there...**

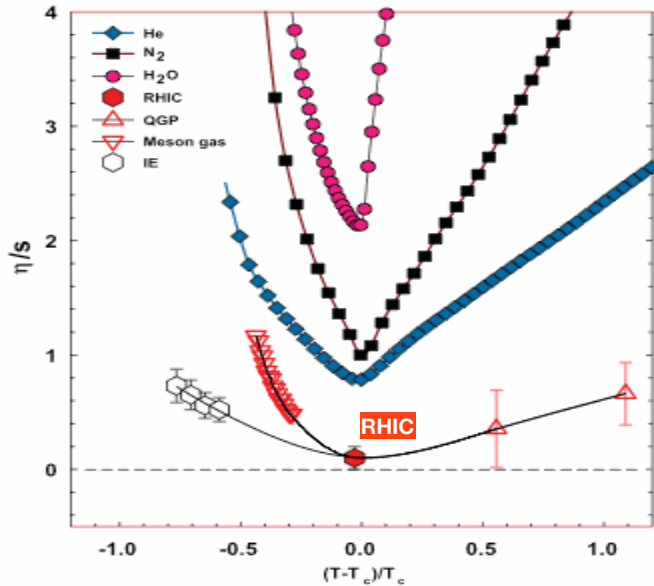




Is the sQGP a Perfect Fluid?

- Superfluid Helium
- Ultra Cold Gasses (few nK)

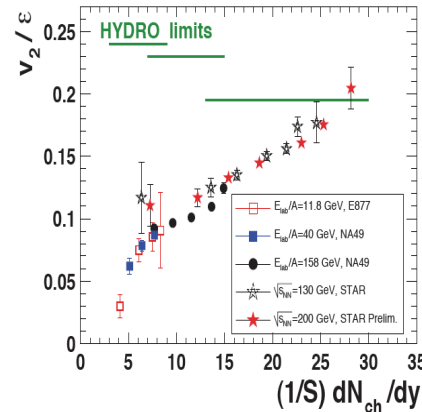
- Quark Gluon Plasma
 $T \sim 200 \text{ MeV} \sim 10^{12} \text{ K}$
 Temperature of early universe at ~ 1 micro-sec



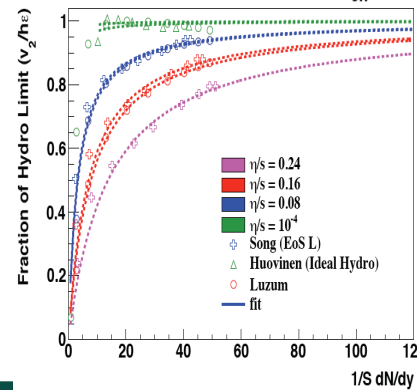
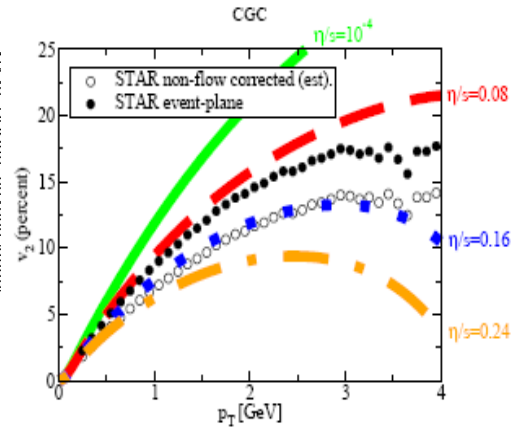
Conjectured low bound of shear viscosity/entropy:

Supersymmetric Yang Mill Theory (Ads/CFT duality
 Kovtun, Son, & Starinets, PRL94(2005))

$$\frac{\eta}{\hbar s} \geq \frac{1}{4\pi}$$



NA49, PHOBOS, U3A903 (2003)
 P.F. Kolb, J. Sollfrank, U.W. Heinz,
 PRC62, 054909(2000)



M. Luzum & P. Romatschke, 0804.4015; 0901.4588

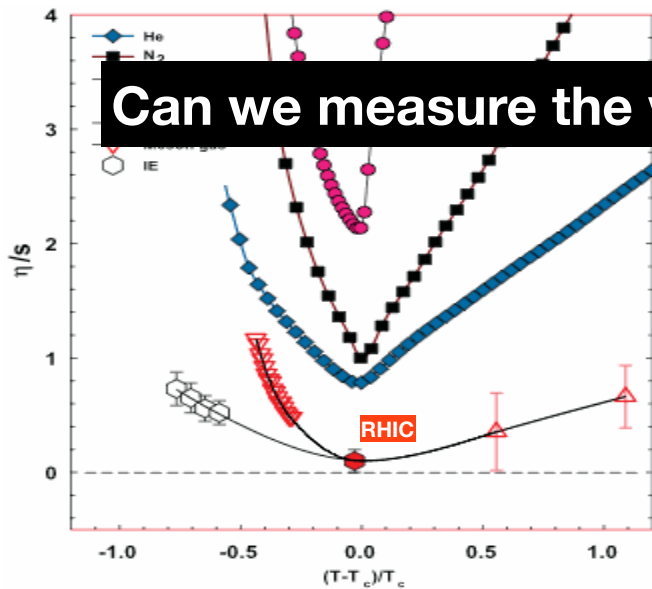
H. Song & U. Heinz 0805.1756v2

P. Huovinen

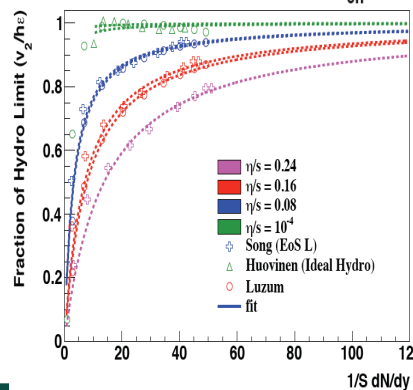
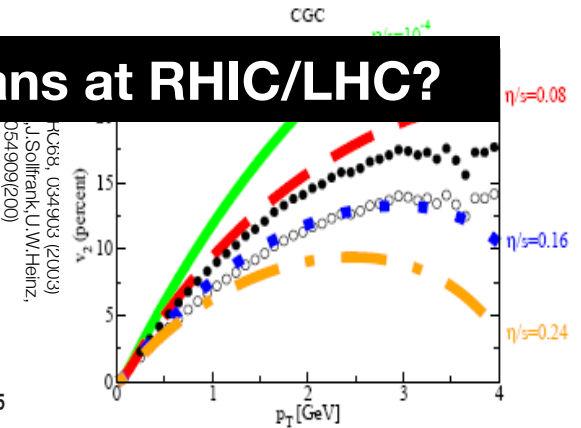
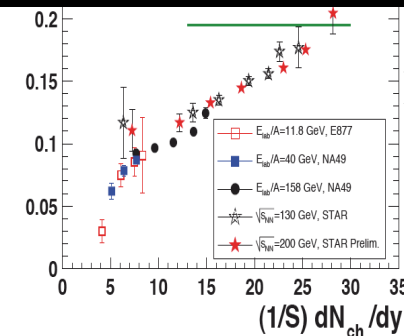


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 Temperature of early universe at ~ 1 micro-sec



Can we measure the viscosity by other means at RHIC/LHC?



Conjectured low bound of shear viscosity/entropy:
 Supersymmetric Yang Mill Theory (Ads/CFT duality
 Kovtun, Son, & Starinets, PRL94(2005)

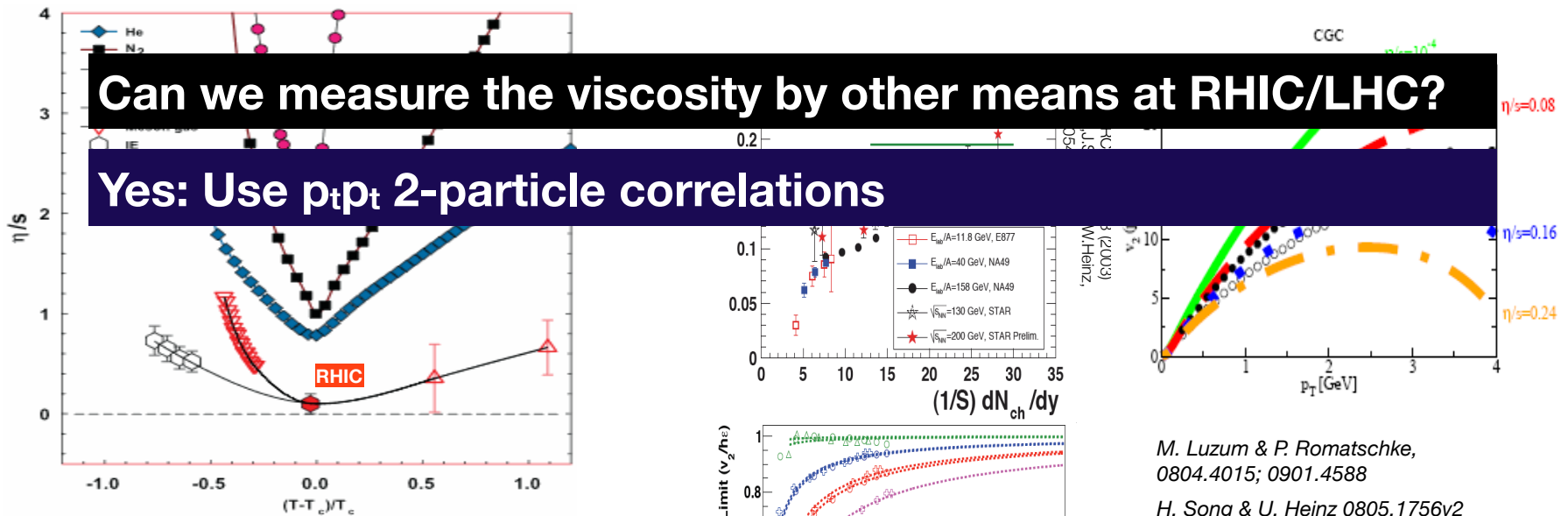
$$\frac{\eta}{\hbar s} \geq \frac{1}{4\pi}$$

M. Luzum & P. Romatschke, 0804.4015; 0901.4588
H. Song & U. Heinz 0805.1756v2
P. Huovinen



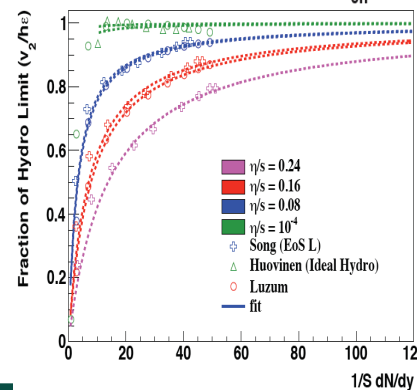
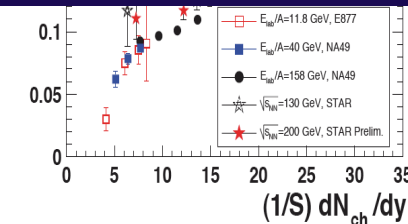
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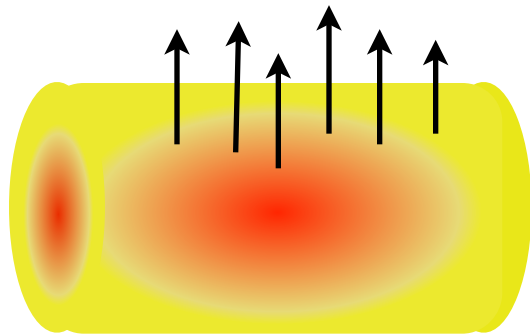
$$\frac{\eta}{\hbar s} \geq \frac{1}{4\pi}$$



M. Luzum & P. Romatschke, 0804.4015; 0901.4588
H. Song & U. Heinz 0805.1756v2
P. Huovinen

Measurement of viscosity based on p_t p_t Correlations

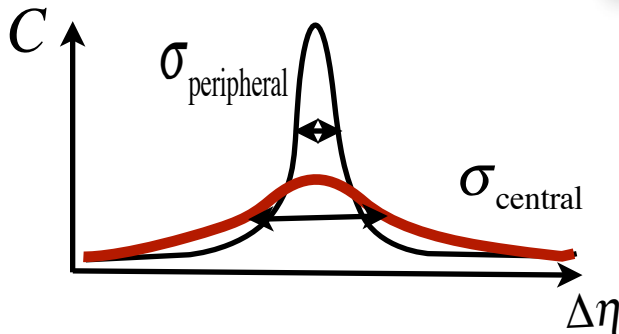
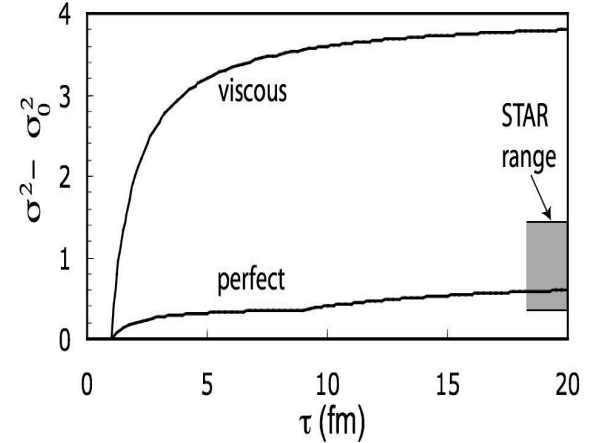
Gavin and Abdel-Aziz, nucl-th/0606061 (2006)



NEAR SIDE: Fluid Cells
Viscous Drag damps their
relative motion and
broadens correlations

$$C(\Delta\eta) = \langle p_{t,1} p_{t,2} \rangle - \langle p_t \rangle^2$$

$$v = \frac{\eta}{T_c s}$$



$$\sigma^2 = \sigma_o^2 + 2\Delta V(\tau_f)$$

$$\Delta V(\tau) \equiv \langle (\eta - \langle \eta \rangle)^2 \rangle = \frac{2v}{\tau_o} \left(1 - \frac{\tau_o}{\tau} \right)$$

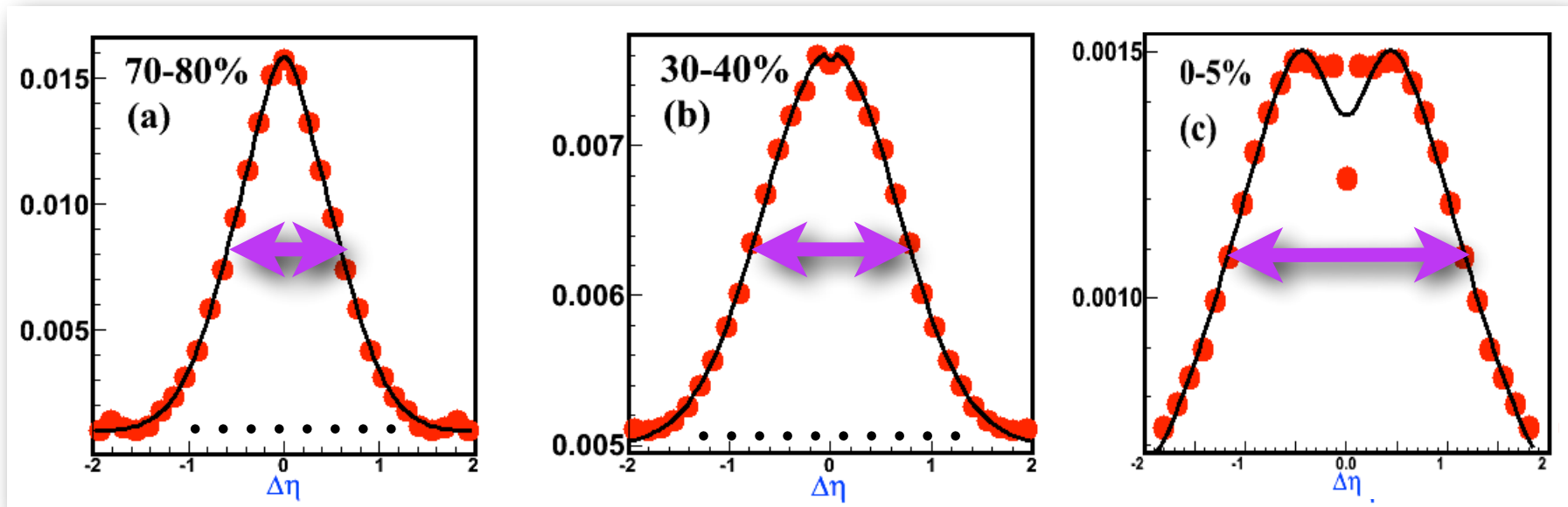
Experimental Observable

$$C(\Delta\eta, \Delta\phi) = \frac{\left\langle \sum_{i=1}^{n_1} \sum_{j \neq i=1}^{n_2} p_{t,i} p_{t,j} \right\rangle}{\langle n_1 \rangle \langle n_2 \rangle} - \langle p_{t,1} \rangle \langle p_{t,2} \rangle$$

NEAR SIDE: Fluid Cells
Viscous Drag damps their
relative motion and
broadens correlations



Results: $C(\Delta\eta, |\Delta\phi| < 1)$



- Correlation Function is not Gaussian
- Characterize width as RMS of the distribution above “pedestal”
- Determine pedestal (offset) based on fit of the line shape

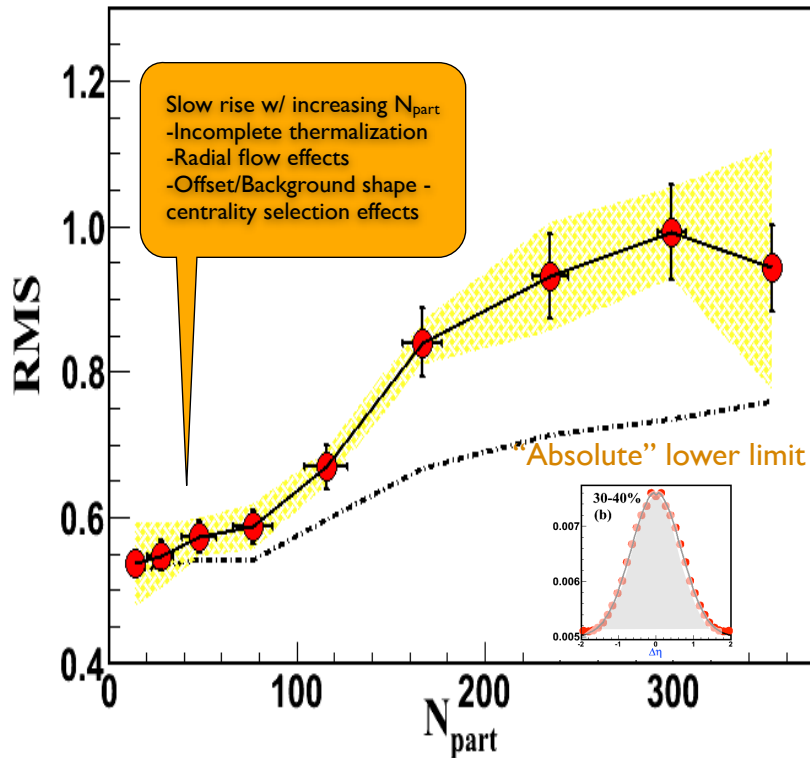
$$b + a_n \exp(-\Delta\eta / 2\sigma_n^2) + a_w \exp(-\Delta\eta / 2\sigma_w^2)$$
- Subtract offset; Set $\Delta\eta = 0$ point equal to neighboring points in 0-5%; Calculate RMS from data, but include $|\Delta\eta| > 2$ extrapolation from fit.

Results: $C(\Delta\eta, |\Delta\phi| < 1)$

Interpretation based on Gavin and Abdel-Aziz,
Phys.Rev.Lett. 97 (2006) 162302; nucl-th/
0606061 (2006)



M. Sharma et al.



Phys.Lett. B704 (2011) 467-473

- Values obtained by this method consistent w/ values obtained by flow measurements
- Similar analysis needed at LHC.

Viscous broadening: $\sigma_{viscous}^2 = \frac{4v}{\tau_o} \left(1 - \frac{\tau_o}{\tau}\right)$

$$v = \frac{\eta}{T_c s}$$

Measured broadening: $\Delta\sigma^2 \approx \sigma_{viscous}^2 = 0.58 \pm 0.28$

Assume Temperature: $T_c = 170 \text{ MeV}$

Formation Time (th. syst.): $\tau_o = 1_{-0.4}^{+0.5}$

Freeze-out Time (central): $\tau = 10 - 20 \text{ fm/c}$

Range defines theory systematic errors

Shear Viscosity/Entropy:

$$\eta/s = 0.14 \pm 0.02(\text{stat}) \pm 0.06(\text{meas syst.})$$

$$\pm 0.14(\text{theory syst.})$$

Shear Viscosity/Entropy - Upper limit:

$$\eta/s^{\text{max}} = 0.2 + 0.14(\text{theory syst.})$$

In agreement w/ estimates from flow measurements

pTpT Correlations

'Number' Correlations

$$R_2(\eta_1, \varphi_1, \eta_2, \varphi_2) = \frac{\rho_2(\eta_1, \varphi_1, \eta_2, \varphi_2)}{\rho_1(\eta_1, \varphi_1)\rho_1(\eta_2, \varphi_2)} - 1$$

pTpT Correlations

$$\langle \Delta p_{t,1} \Delta p_{t,2} \rangle(\eta_1, \varphi_1, \eta_2, \varphi_2) = \frac{\int \rho_2(\eta_1, \varphi_1, p_{t,2}, \eta_2, \varphi_2, p_{t,2}) \Delta p_{t,1} \Delta p_{t,2} dp_{t,1} dp_{t,2}}{\int_{\text{accept}} \rho_2(\eta_1, \varphi_1, p_{t,2}, \eta_2, \varphi_2, p_{t,2}) dp_{t,1} dp_{t,2}}$$

measured as:

$$\langle \Delta p_{t,1} \Delta p_{t,2} \rangle(\eta_1, \varphi_1, \eta_2, \varphi_2) = \frac{\sum_{\text{events}} \sum_{\text{accept}} \Delta p_{t,1} \Delta p_{t,2}}{\sum_{\text{events}} n_2(\eta_1, \varphi_1, \eta_2, \varphi_2)} \quad \Delta p_T = p_T - \langle p_T \rangle$$

Flow Only (corr w.r.t reaction plane):

$$\langle \Delta p_t \Delta p_t \rangle(\eta_1, \eta_2, \Delta\phi) = \frac{2 \sum (v_n^p(\eta_1) - \langle p_t \rangle(\eta_1) v_n(\eta_1)) (v_n^p(\eta_2) - \langle p_t \rangle(\eta_2) v_n(\eta_2)) \cos(n\Delta\phi)}{1 + 2 \sum_n v_n(\eta_1) v_n(\eta_2) \cos(n\Delta\phi)}$$

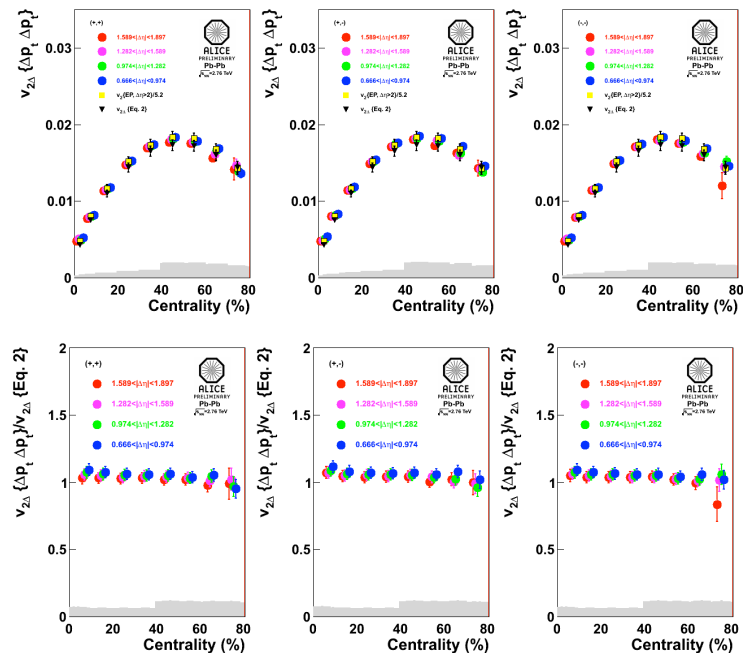
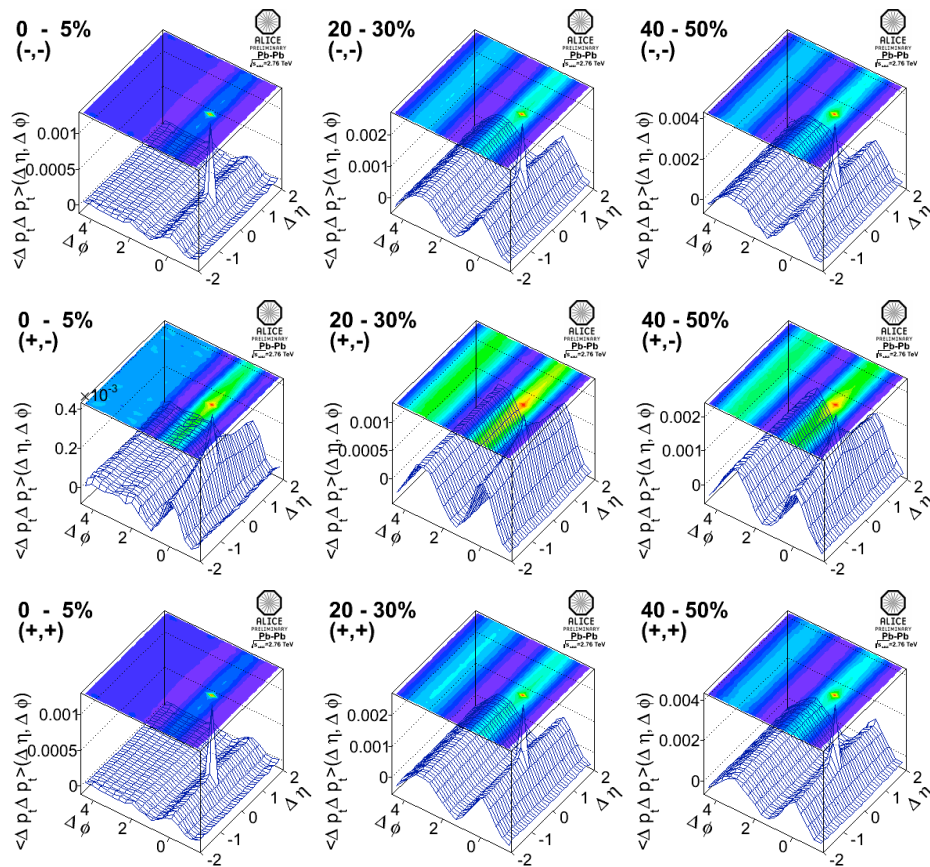
$$v_n(\eta) = \frac{1}{P_n(\eta)} \int P_n(\eta, p) v_n(\eta, p) dp \quad \text{Regular Flow Coefficients}$$

$$v_n^{p_t}(\eta) = \frac{1}{P_n(\eta)} \int P_n(\eta, p) v_n(\eta, p) p dp \quad \text{pT weighted Flow Coefficients}$$

Simple Prediction:

$$v_n^{\Delta p_t \Delta p_t} \simeq v_n^{p_t} - \langle p_t \rangle v_n$$

pTpT Correlations



- Similar results for higher harmonics
- Factorization
- Scaling (Flow Model)

$$v_n^{\Delta p_t \Delta p_t} \simeq v_n^{p_t} - \langle p_t \rangle v_n$$

P. Pujahari + C.P.

Summary (Score Card)

Measurement

Conclusion(s)/Outcome

Net Charge Fluctuations

Tendency towards suppression expected from QGP but suppression not fully realized.



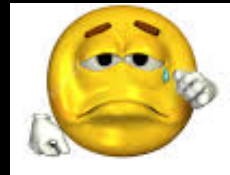
Balance Function

Narrowing observed in central collisions
Consistent with delayed hadronization.



Net Charge Higher Moments

Increased expected not observable
Inconclusive because of background?



Kaon/Pion Fluctuations

Insufficient data at low beam energy



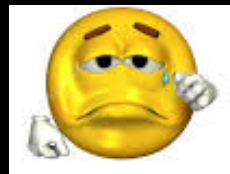
pT Fluctuations

Scaled Correlations suppressed not enhanced.



Ridge/Dip

No Mach Cone: Rise of Triangularity
But where is the medium recoil?



Summary (Score Card cont'd)

Measurement

Conclusion(s)/Outcome

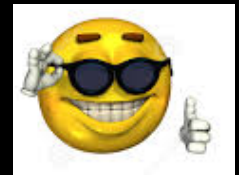
Correlations Longitudinal
Broadening

Estimate of viscosity consistent w/
flow results



DptDpt Correlations

Further evidence for flow &
factorization



Epilog:

- Good (Not excellent) score card!
- A + A collisions are mesoscopic systems: Collision dynamics dominates - must be accounted for before one considers system wide fluctuations.
- Correlation/Fluctuation Observables have nonetheless as a very powerful discovery tool.