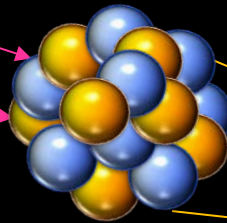


Dense QCD and Compact Stars

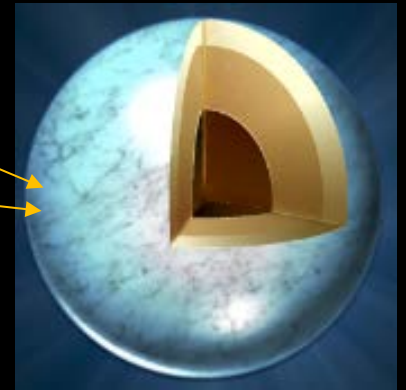
nucleon ~ 1 [fm]



nucleus ~ 10 [fm]



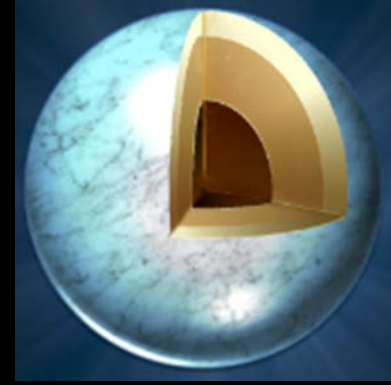
Neutron star ~ 10 [km]



Matter at Extreme Conditions (Jan. 15, 2014)

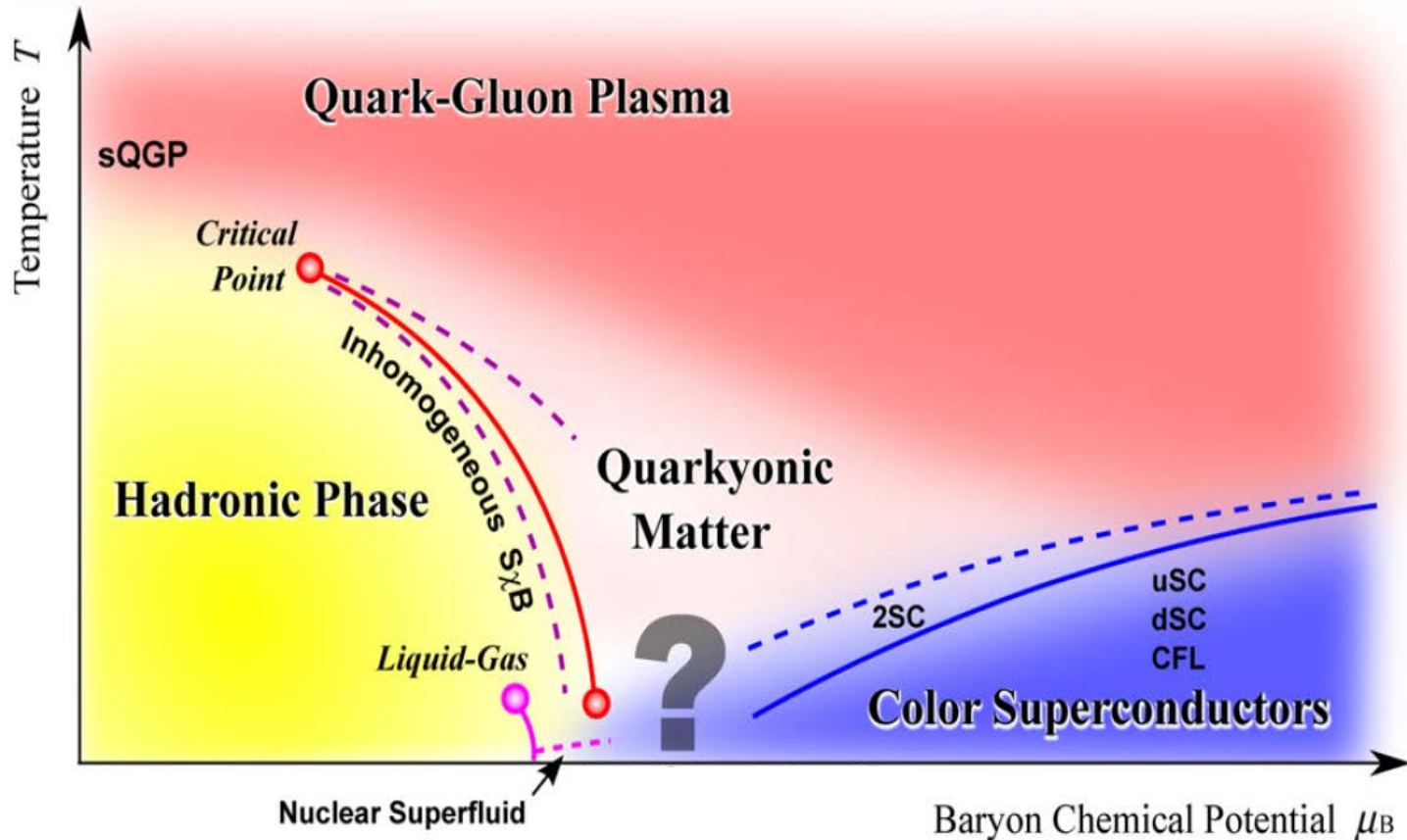
Tetsuo Hatsuda (RIKEN)

Plan of this Talk

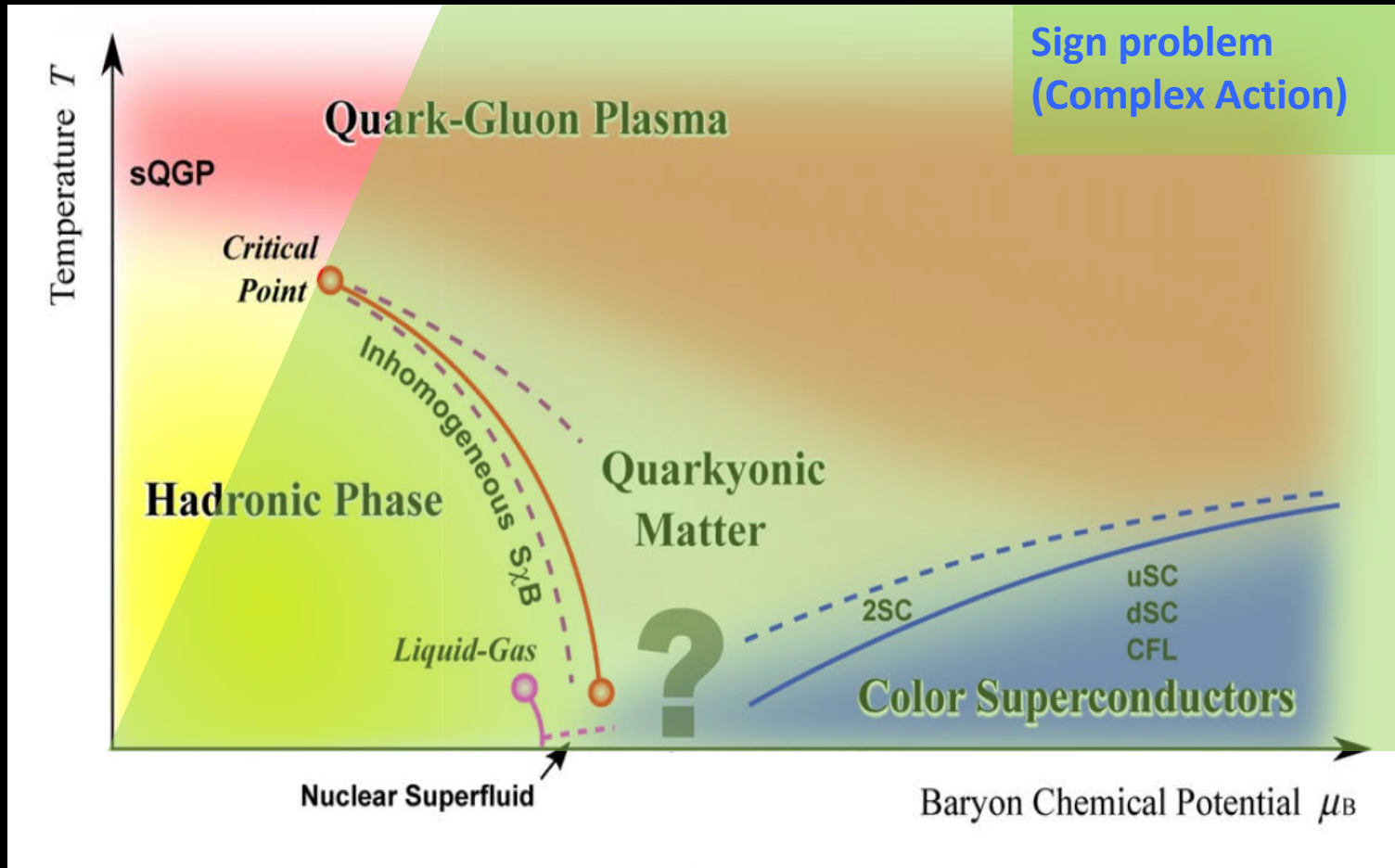


1. QCD Phase Structure
2. **Dense Matter** and Neutron Star
3. **Lattice QCD** and Neutron Star
4. **Hadron-Quark Crossover** and Neutron Star
5. Summary

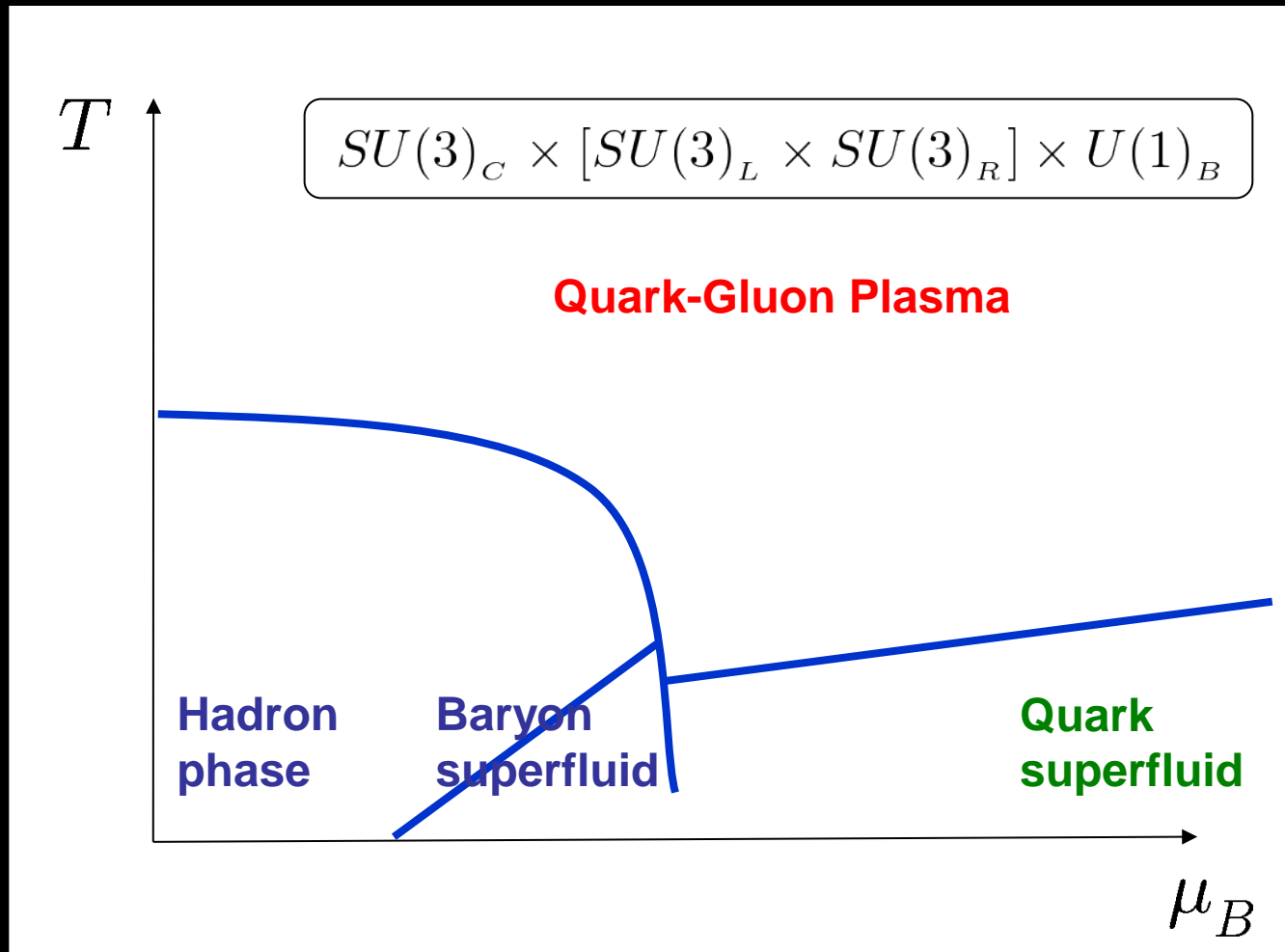
QCD Phase Structure



QCD Phase Structure

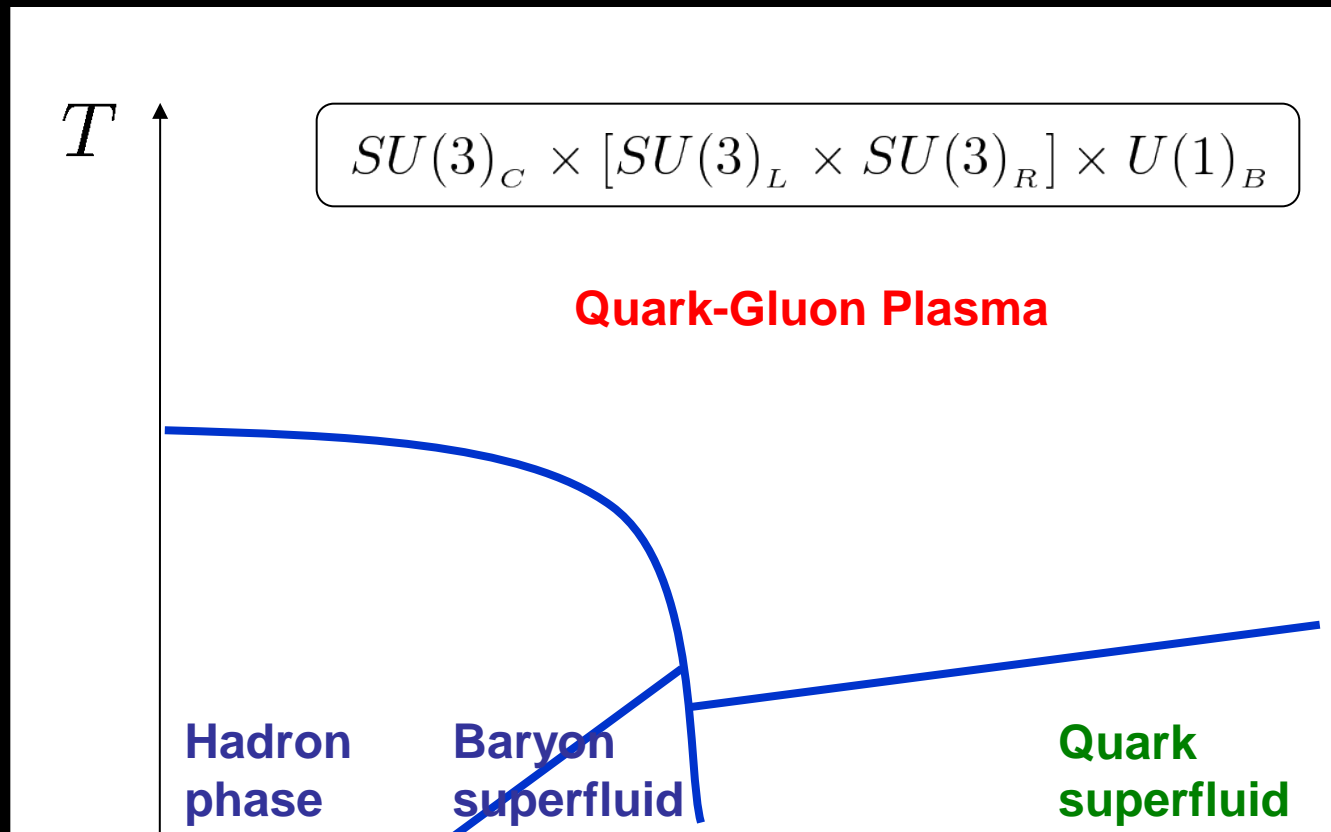


Symmetry Realization in dense QCD ($N_c=3, N_f=3$)



Chiral symmetry is always broken at finite density

Symmetry Realization in dense QCD ($N_c=3, N_f=3$)



$$\langle \bar{q}_L q_R \rangle \neq 0$$

$$SU(3)_C \times SU(3)_{L+R} \times U(1)_B$$

$$\langle BB \rangle \neq 0$$

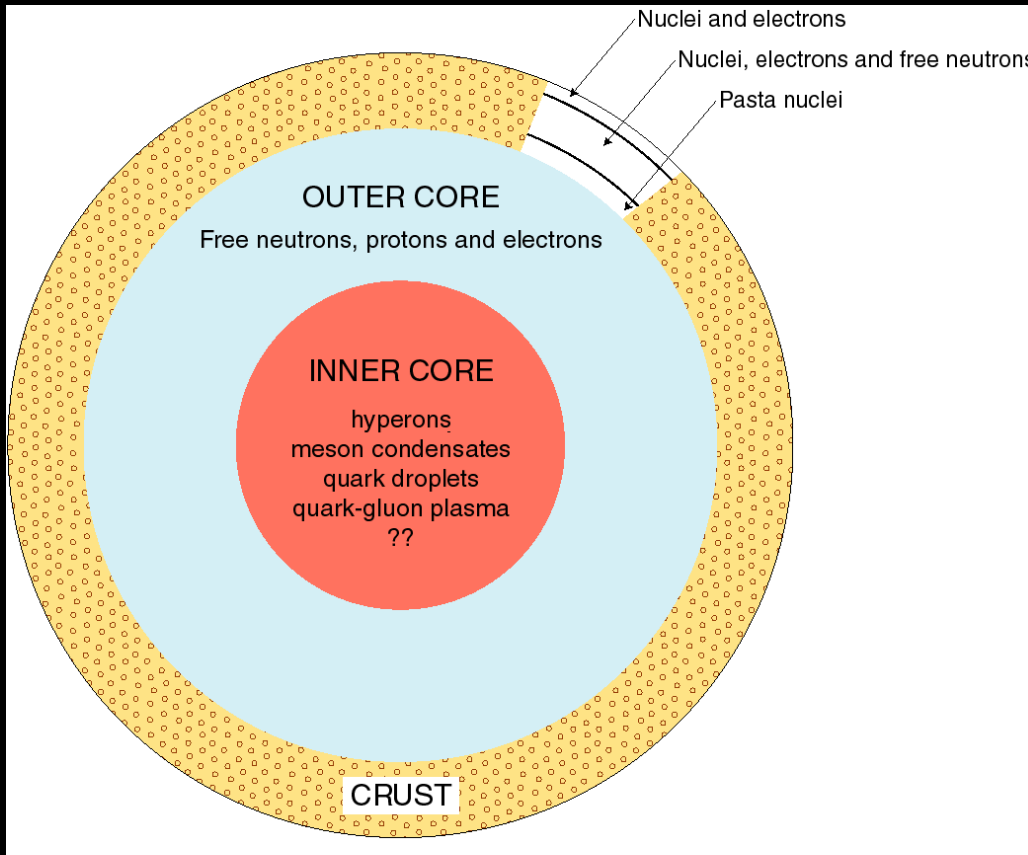
$$SU(3)_C \times SU(3)_{L+R}$$

$$\langle (q_L q_L)(\bar{q}_R \bar{q}_R) \rangle \neq 0$$

$$SU(3)_C \times SU(3)_{L+R}$$

Chiral symmetry is always broken at finite density

Dense matter and Neutron Star



- $M \sim (1-2)M_{\odot}$
- $R \sim 10\text{km}$
- $0 < \rho < 10 \rho_0$

composition

- nuclei
- neutrons & protons
- mesons (π , K)
- hyperons (Λ , Σ^- , Ξ^-)
- quarks (u, d, s)
- + leptons (e, μ)

N_{\star} observations

Current:

$$M = (1.97 \pm 0.04) M_{\odot} \quad (\text{Nature 2010})$$

$$M = (2.01 \pm 0.04) M_{\odot} \quad (\text{Science 2013})$$

\Leftrightarrow cold EOS

X-ray bursts

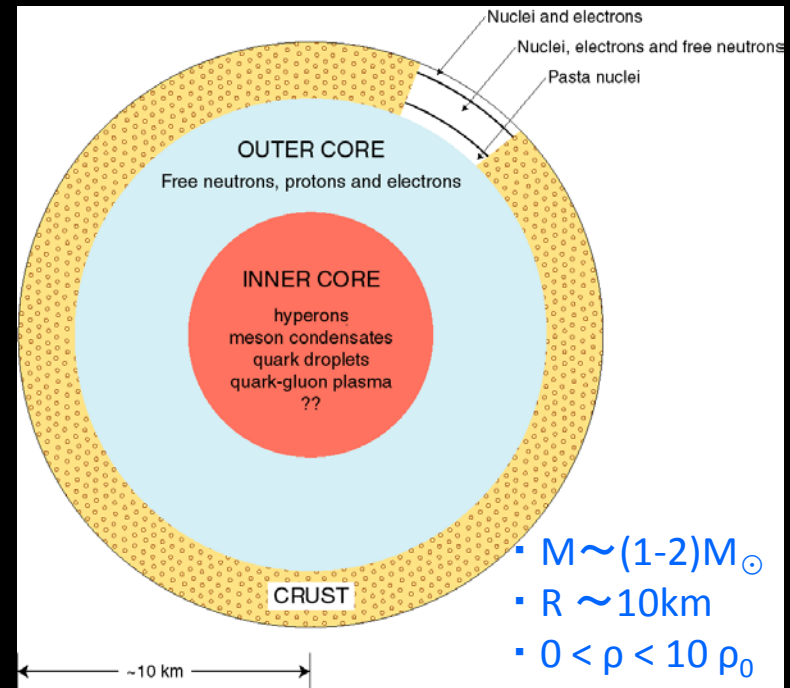
\Leftrightarrow cold EOS

Cooling of CAS-A \Leftrightarrow ${}^3\text{P}_2$ superfluid?

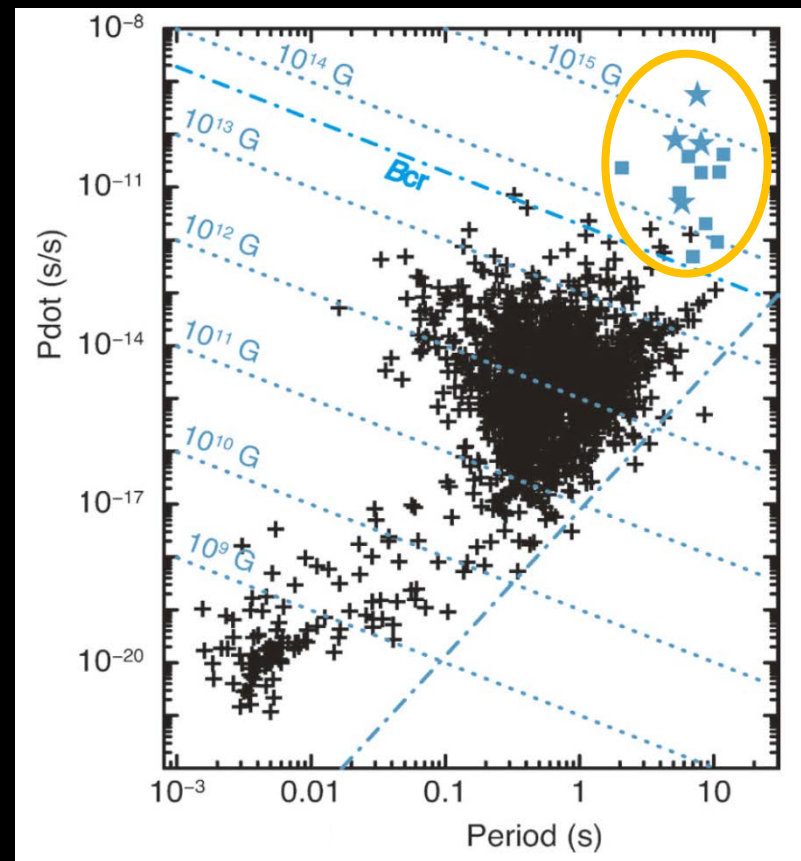
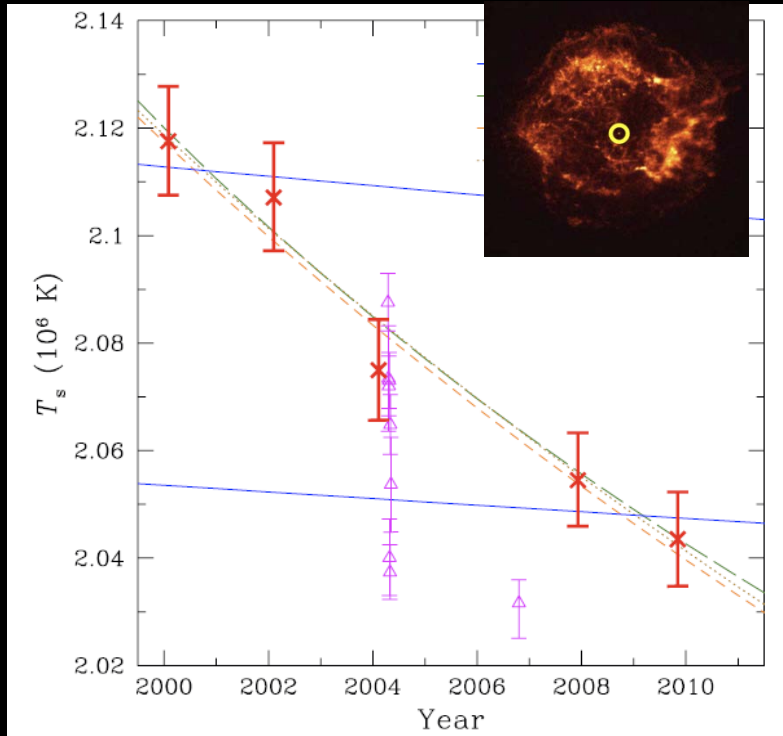
Magnetars \Leftrightarrow ferromagnetic core?

Near Future:

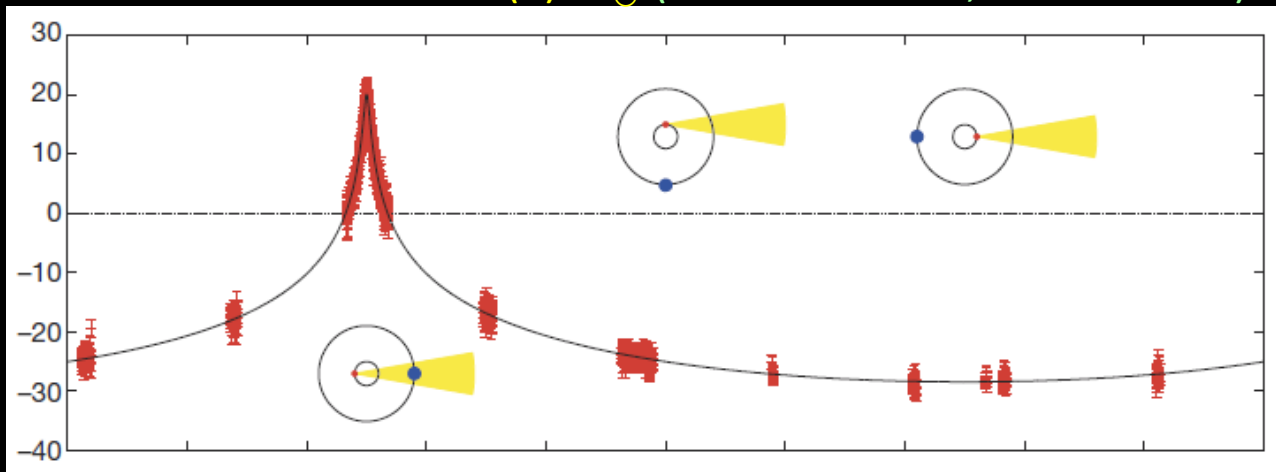
GW from N_{\star} merger \Leftrightarrow hot EOS



Cassiopeia A cooling: T decreases by 4% in 9 years
(Heinke & Ho, ApJ 2010)



PSR J1614-2230 : $M=1.97(4) M_{\odot}$ (Demorest et al., Nature 2010)

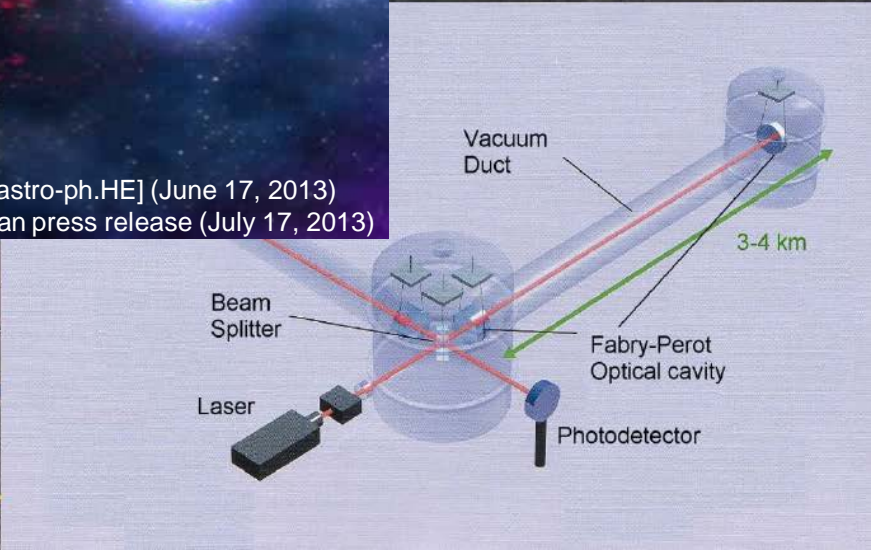
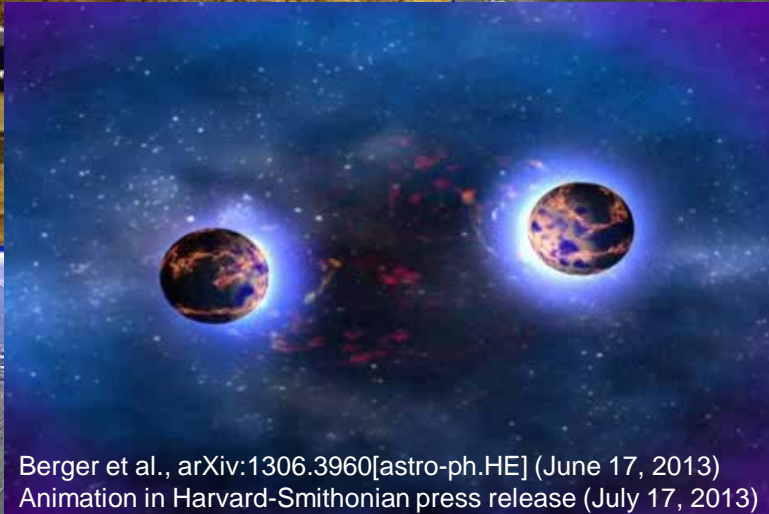


Magnetars: $B \sim 10^{14-15}$ G
(from Enoto, 2012)
 $B_s = 3.2 \times 10^{19} \nu (P \dot{P})$ [G]

T, B, M

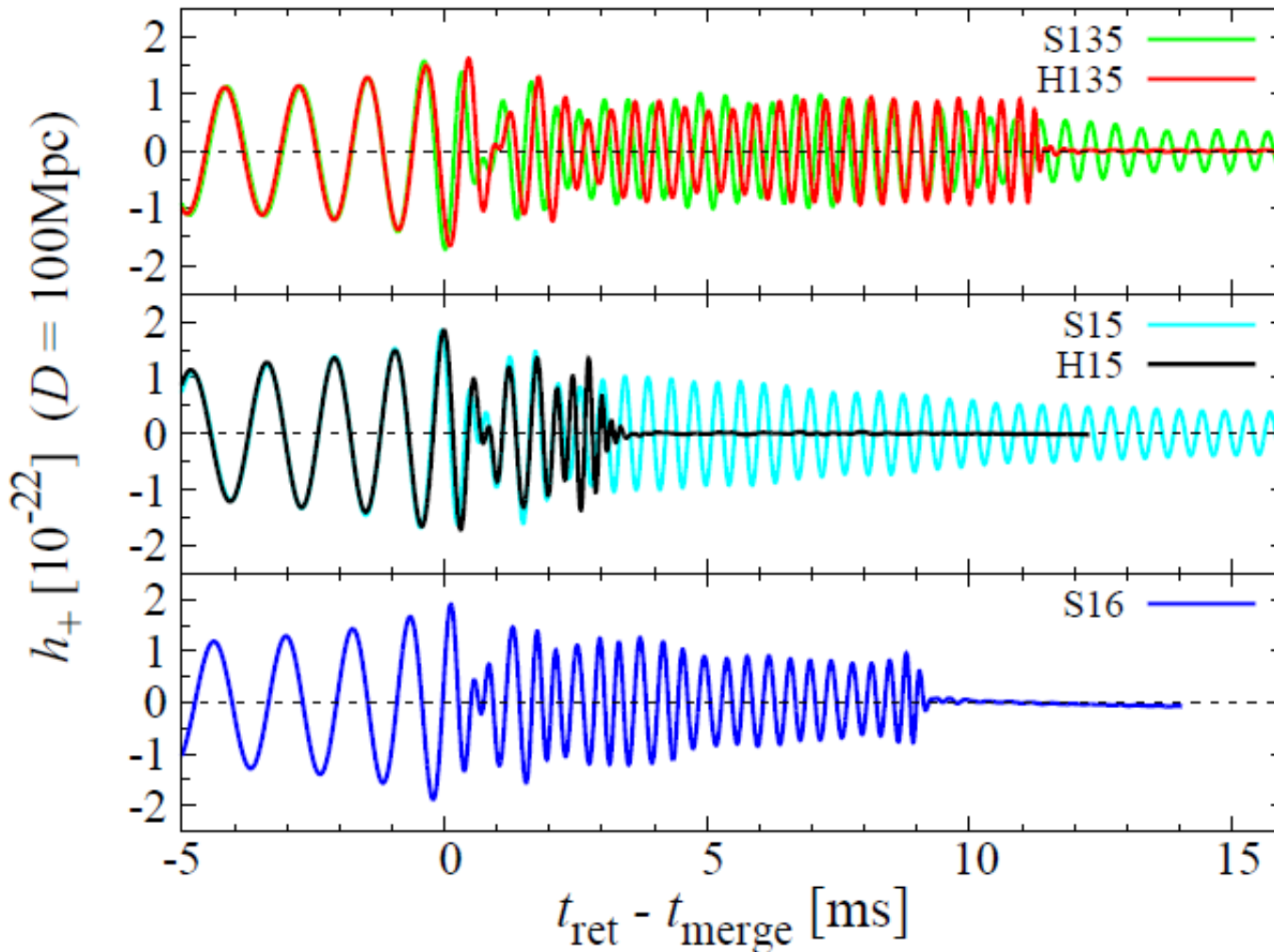
Gravitational wave from N_{\star} merger

-- Detectors --



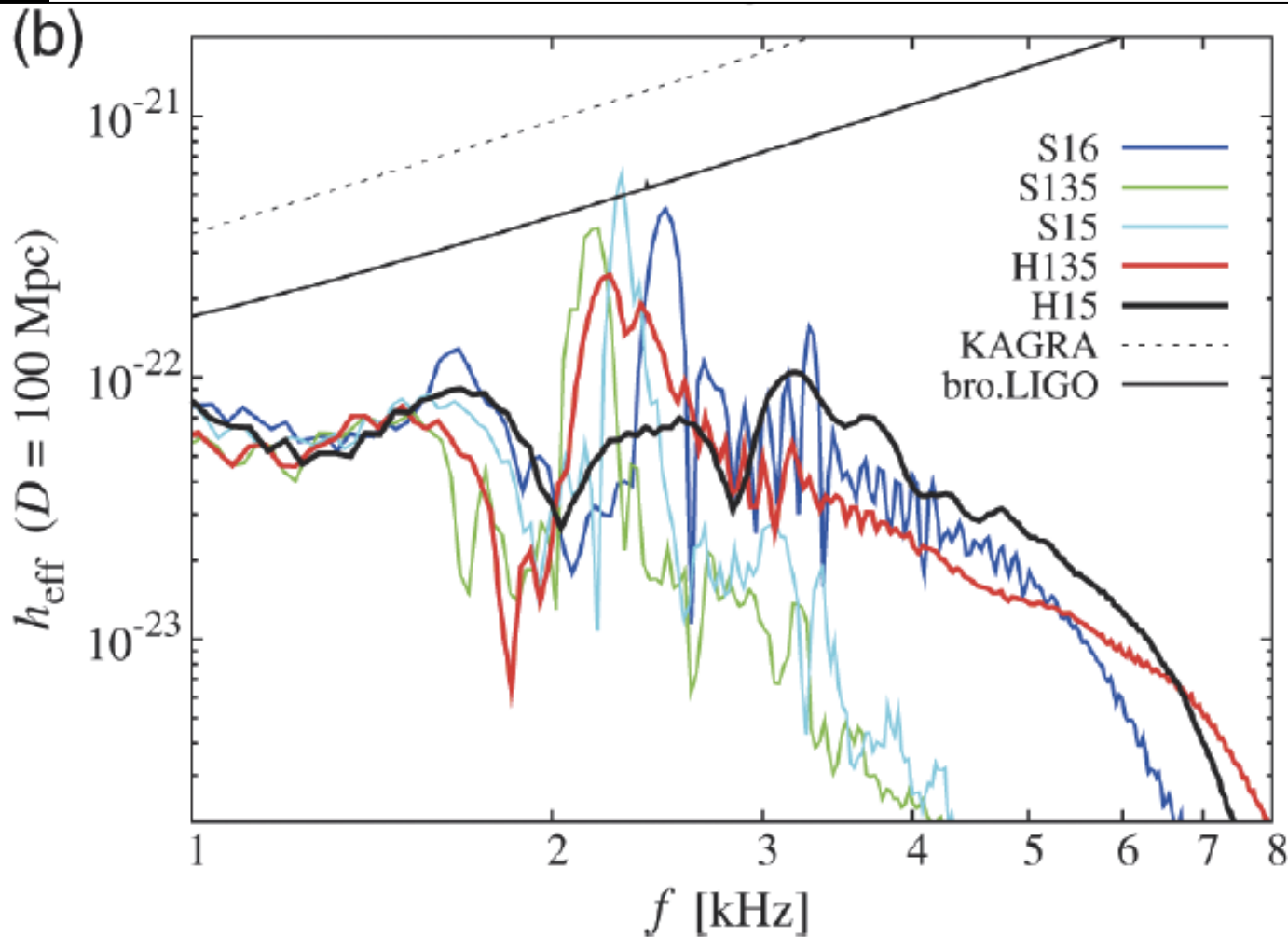
Gravitational wave from N_{\star} merger

-- Expected signal --



Gravitational wave from N_{\star} merger

-- Expected signal --



From QCD to Hot/Dense Matter

Quantum Chromo Dynamics

Relativistic heavy-ion collisions

Neutron stars

From QCD to Hot/Dense Matter

Quantum Chromo Dynamics

Equation of State for Hot Matter

Relativistic
hydrodynamics



Relativistic heavy-ion collisions

Equation of State for Dense Matter

General relativity

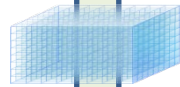


Neutron stars

From QCD to Hot/Dense Matter

Quantum Chromo Dynamics

Lattice
gauge theory



sign
problem



Equation of State for Hot Matter

Relativistic
hydrodynamics

Relativistic heavy-ion collisions

Equation of State for Dense Matter

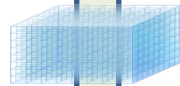
General relativity

Neutron stars

From QCD to Hot/Dense Matter

Quantum Chromo Dynamics

Lattice
gauge theory



sign
problem



Phenomenological
nuclear force

Baryon interactions

Many-body
techniques

Equation of State for Hot Matter

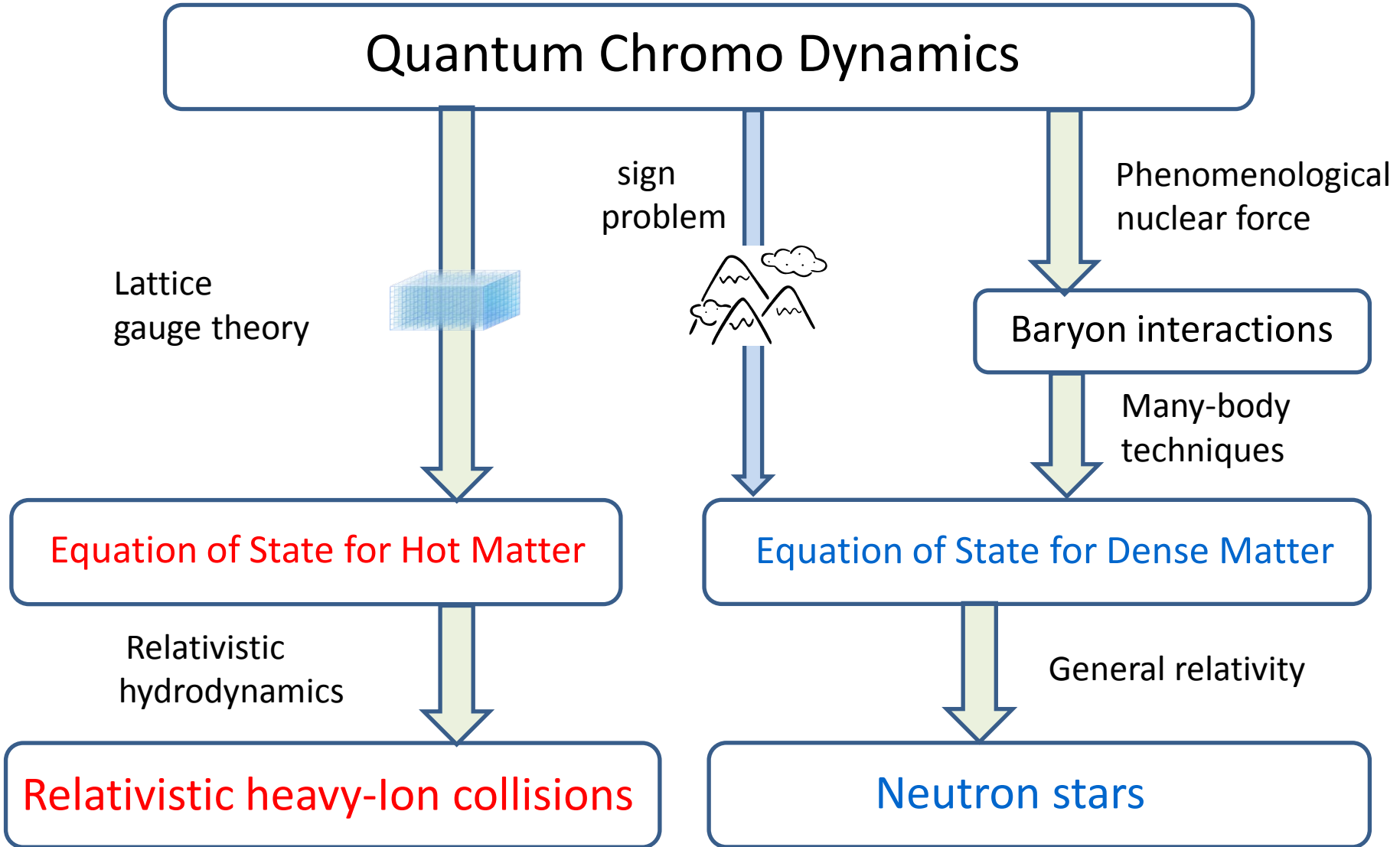
Equation of State for Dense Matter

Relativistic
hydrodynamics

General relativity

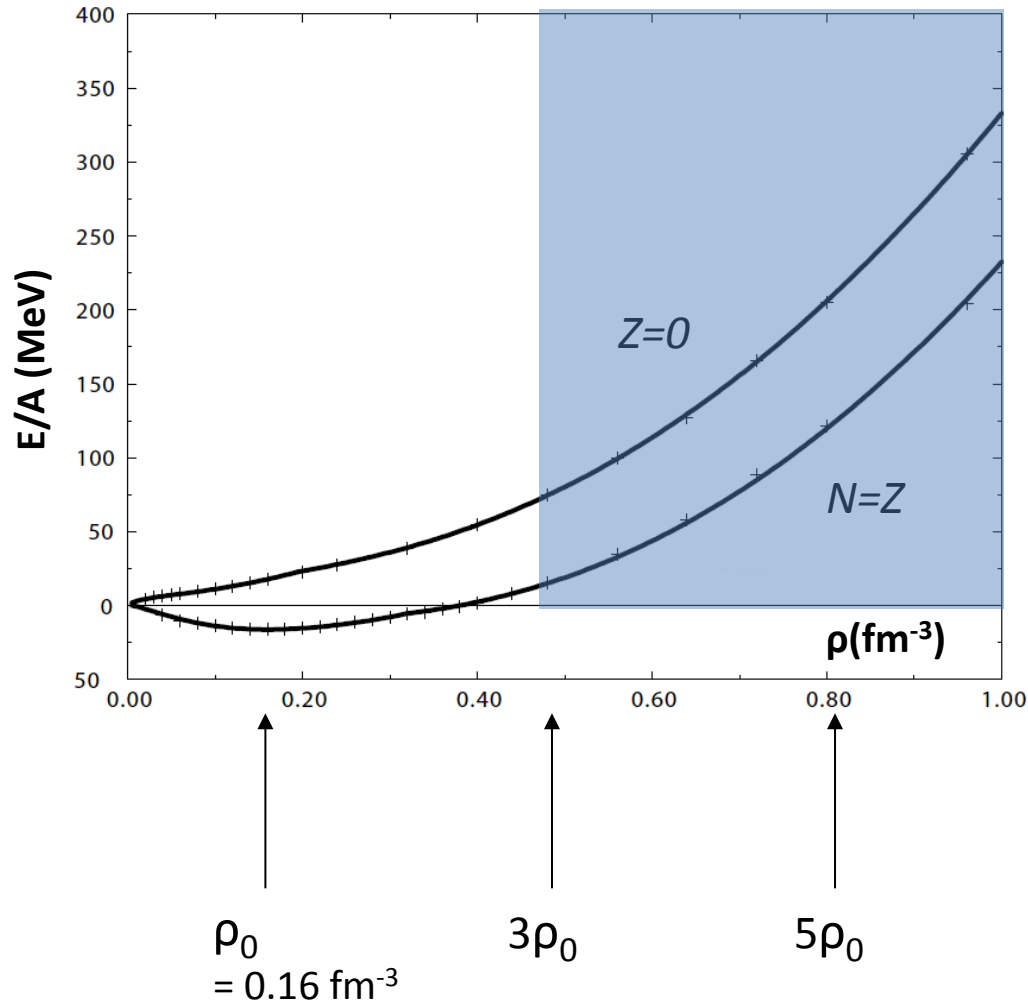
Relativistic heavy-ion collisions

Neutron stars

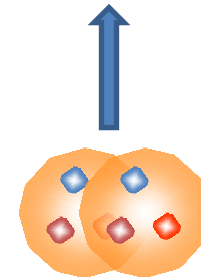
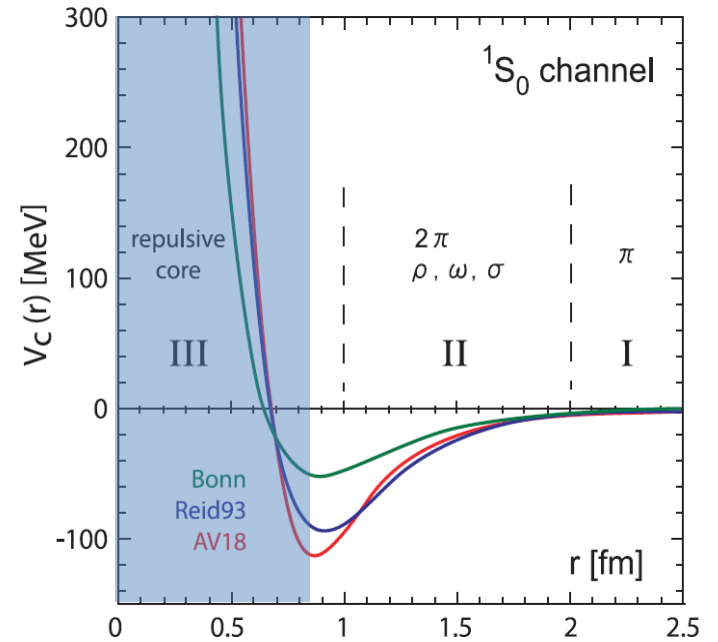


Nuclear Force and dense EOS (nucleons only)

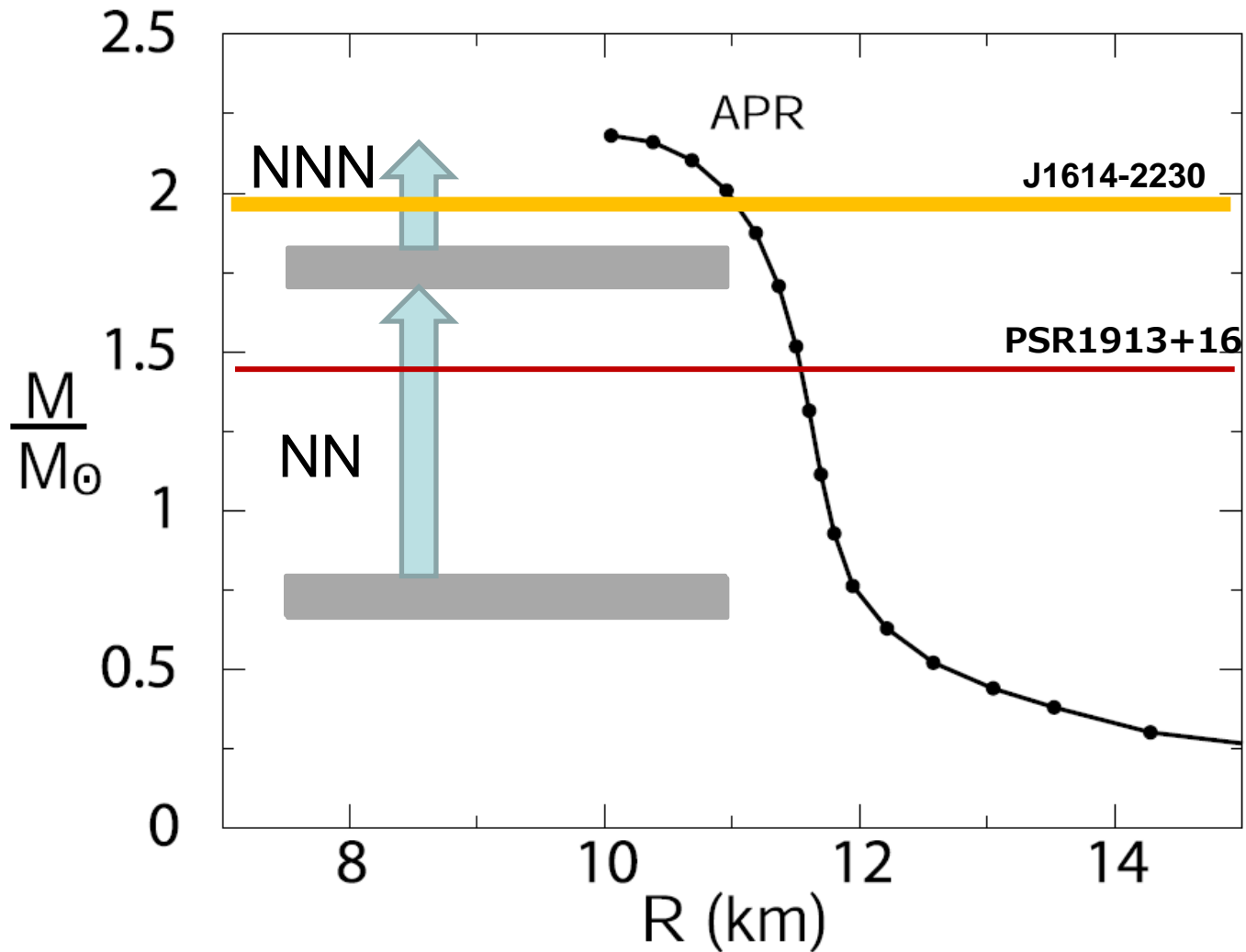
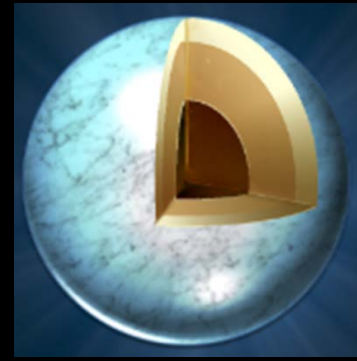
Akmal, Pandharipande & Ravenhall, PRC58 ('98)



Phenomenological nuclear force



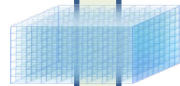
Mass-Radius relation of N_{\star} (nucleons only)



From QCD to Hot/Dense Matter

Quantum Chromo Dynamics

Lattice
gauge theory



sign
problem



Phenomenological
nuclear force

Baryon interactions

Many-body
techniques

Equation of State for Hot Matter

Equation of State for Dense Matter

Relativistic
hydrodynamics

General relativity

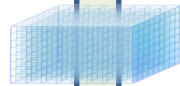
Relativistic heavy-ion collisions

Neutron stars

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sign
problem



Lattice
gauge theory

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techniques

Equation of State for Hot Matter

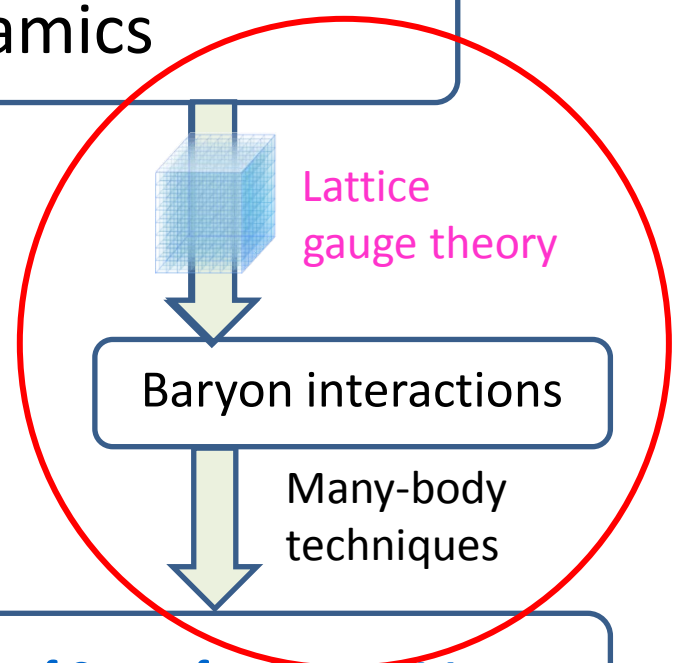
Equation of State for Dense Matter

Relativistic
hydrodynamics

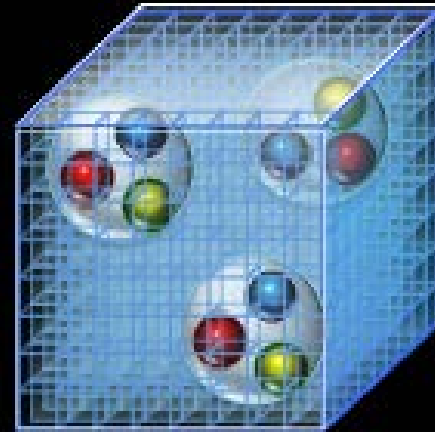
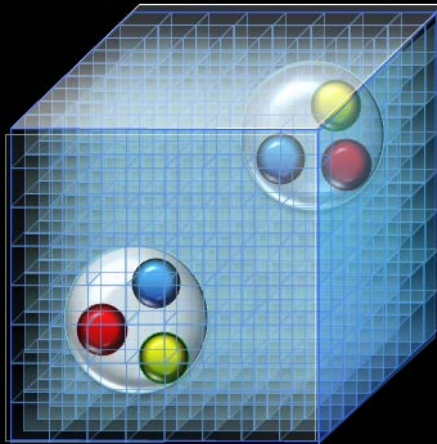
General relativity

Relativistic heavy-ion collisions

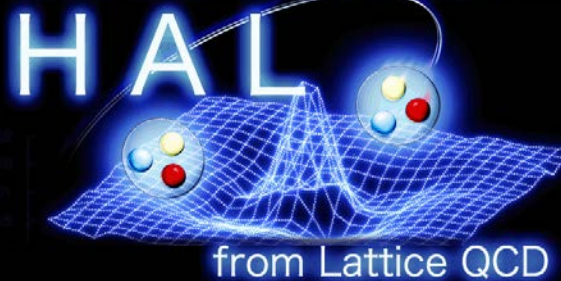
Neutron stars



Multi-baryons on the Lattice



Hadrons to Atomic nuclei



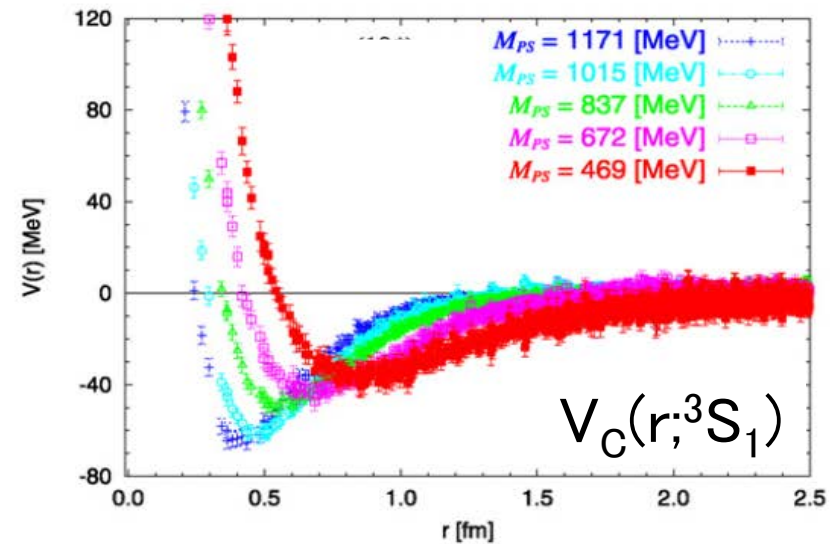
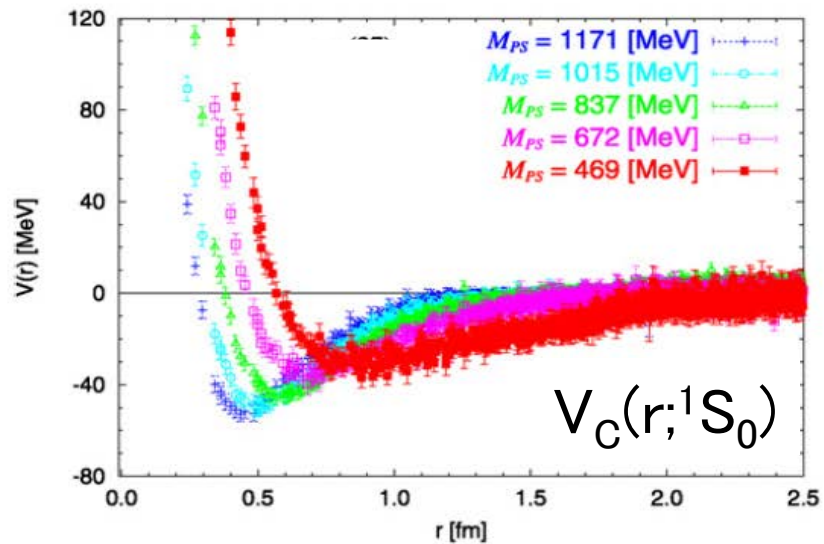
Univ. Tsukuba
RIKEN
Nihon Univ.
Kyoto Univ.
Univ. Tokyo

N. Ishii, H. Nemura, K. Sasaki
T. Doi, T. Hatsuda, Y. Ikeda
T. Inoue
S. Aoki, K. Murano
B. Charron

Review: “Lattice QCD Approach to Nuclear Physics”
HAL QCD Collaboration, Prog. Theor. Exp. Phys. 2012 (2012) 01A105

NN Force in 3-flavor QCD

HAL QCD Coll.
Phys. Rev. Lett. 106 (2011) 162002,
Nucl. Phys. A881 (2012) 28

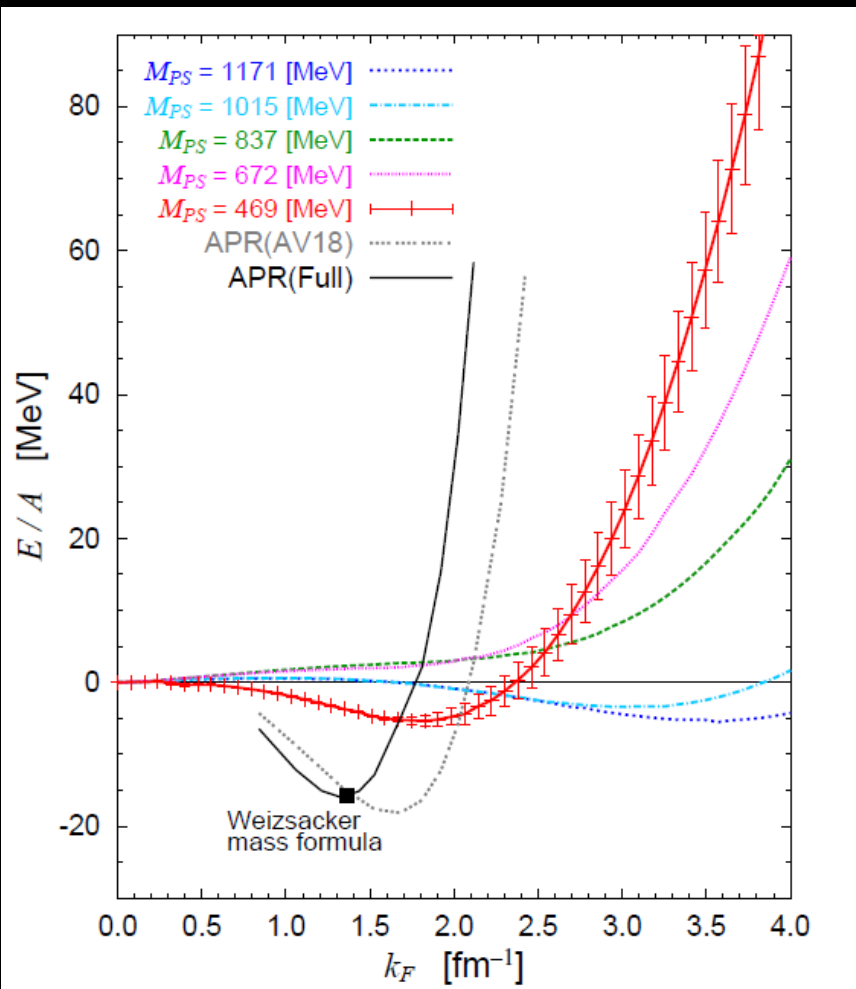


Nuclear EOS from Lattice NN force + BHF calculation

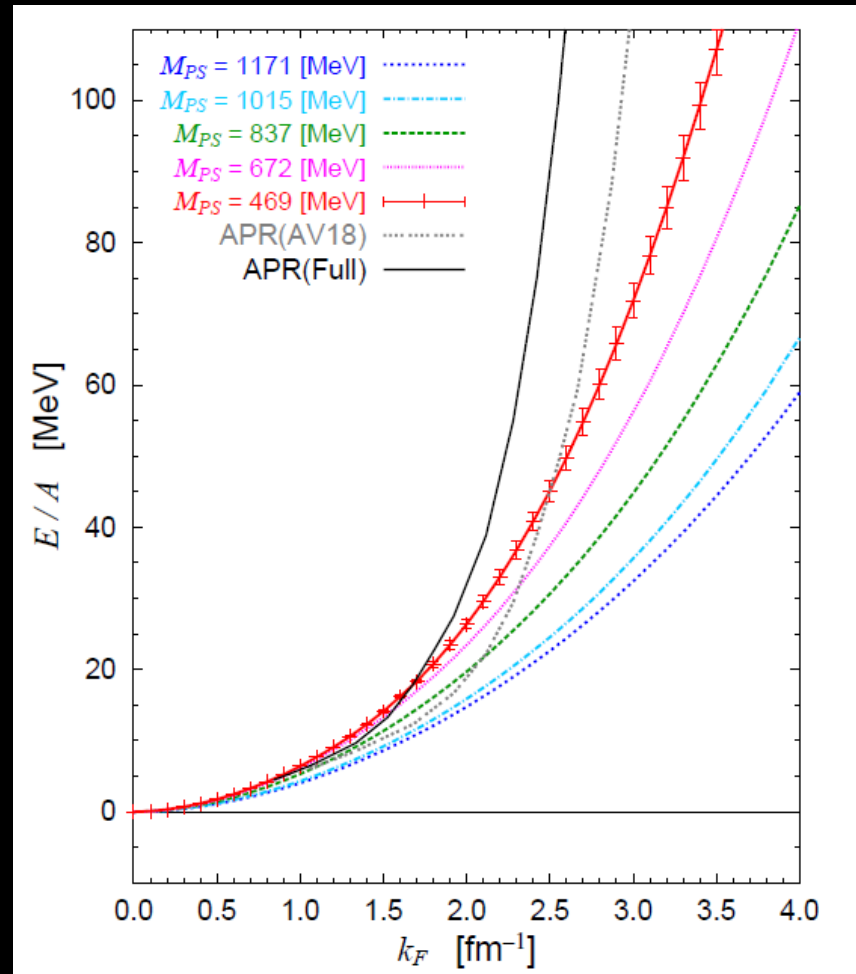
(NN force: 1S_0 , 3S_1 , 3D_1 channels only)

HAL QCD Coll., Phys. Rev. Lett. 111 (2013) 112503

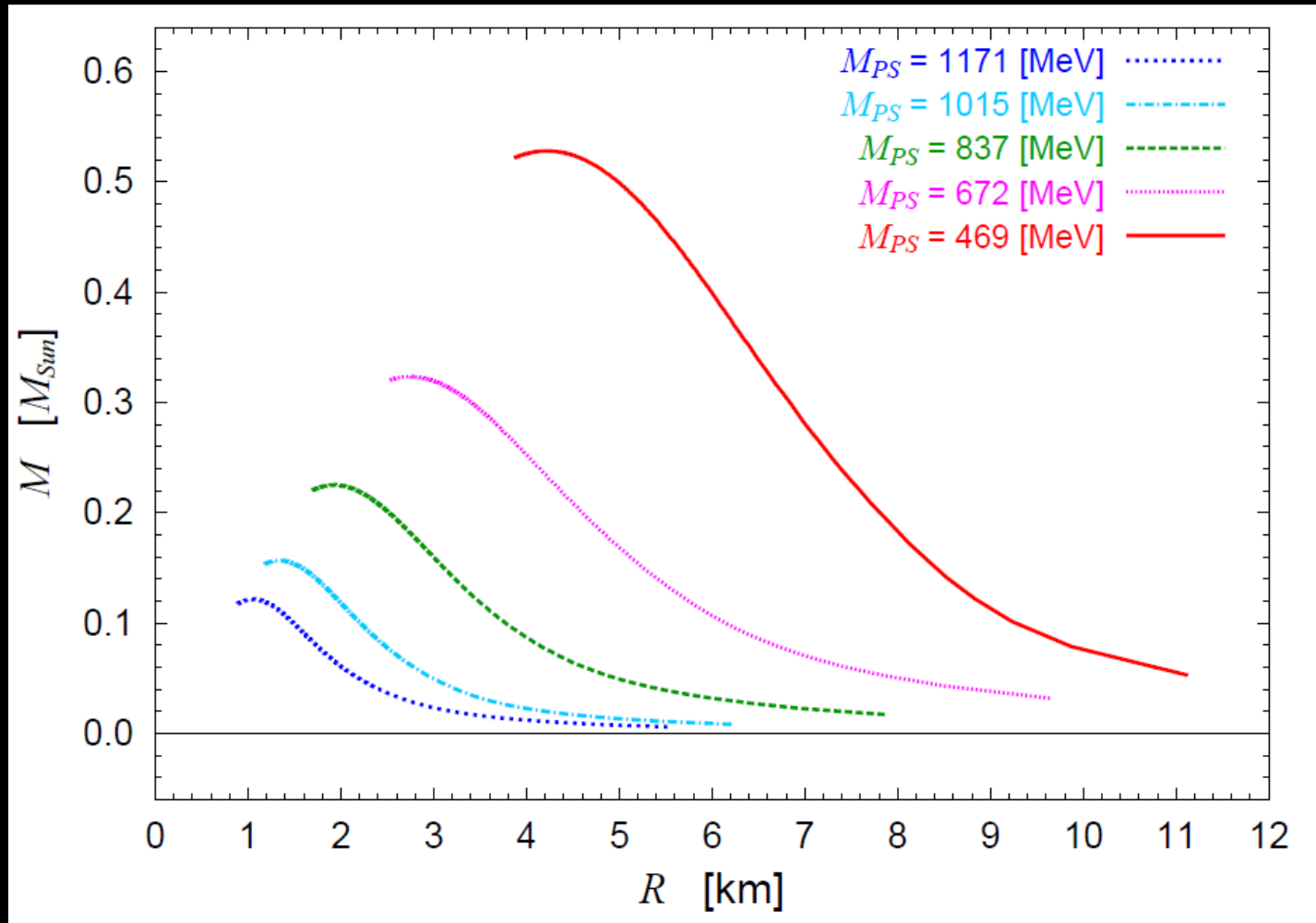
Nuclear Matter



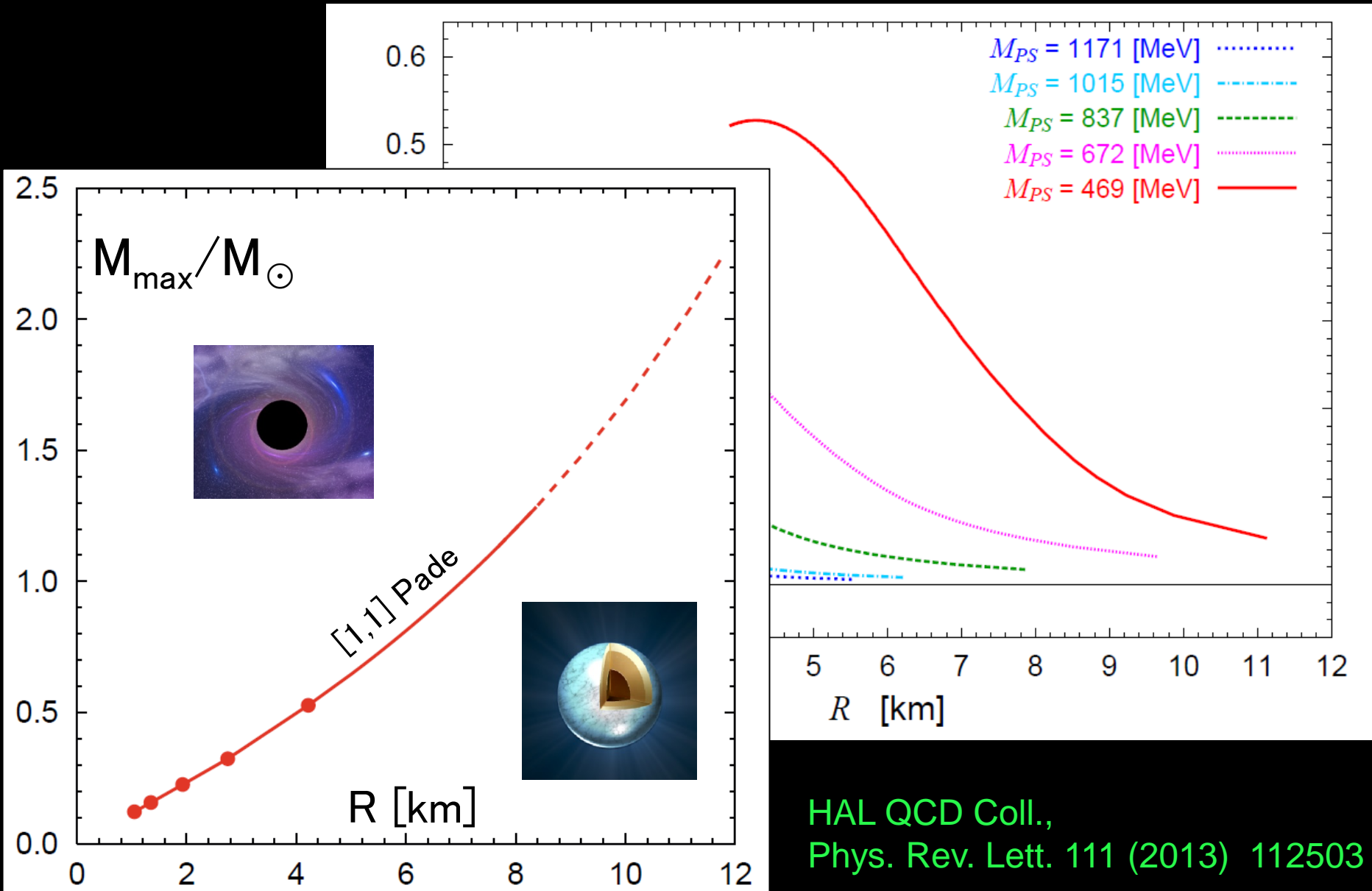
Neutron Matter



Neutron Star from “Lattice EOS”



Neutron Star from "Lattice EOS"

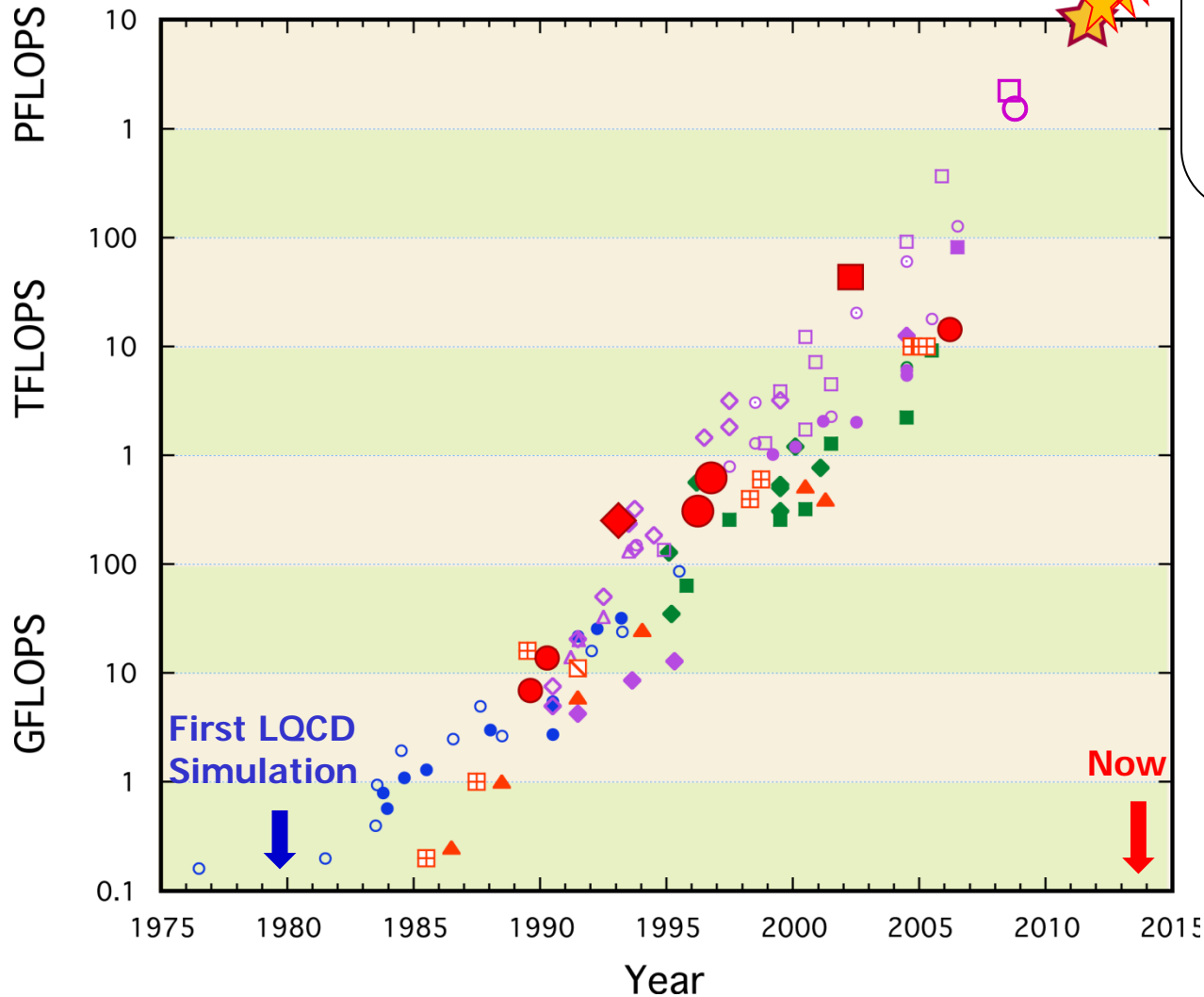


HAL QCD Coll.,
Phys. Rev. Lett. 111 (2013) 112503

High Performance Computers

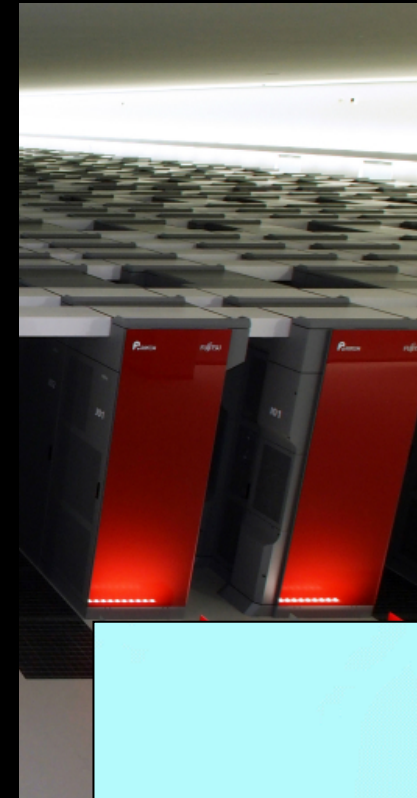
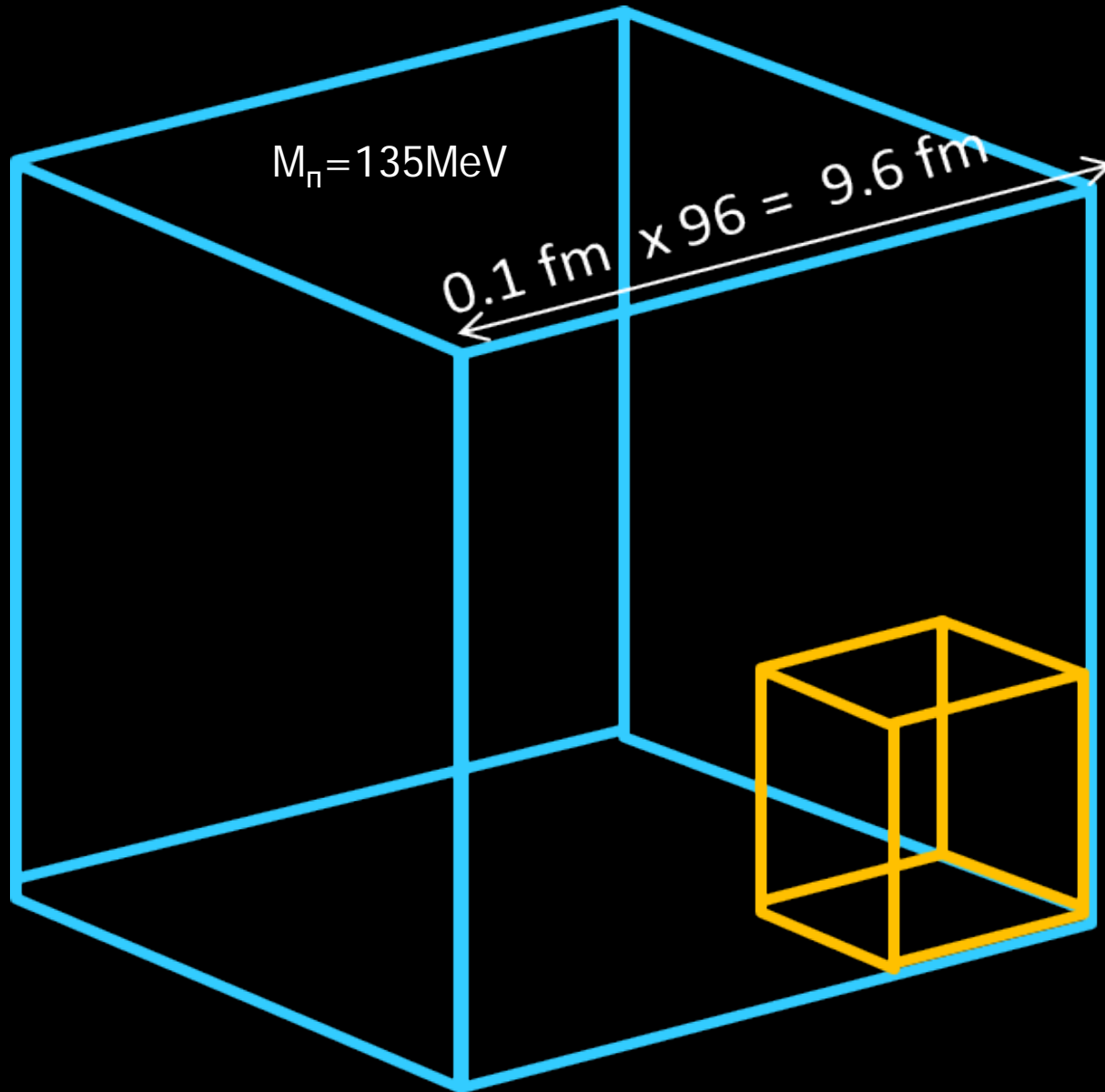
2013 June top5

Tianhe-2 (34 PFlops)
Titan (18 PFlops)
Sequoia (17 PFlops)
K (11 PFlops)
Mira (9 PFlops)

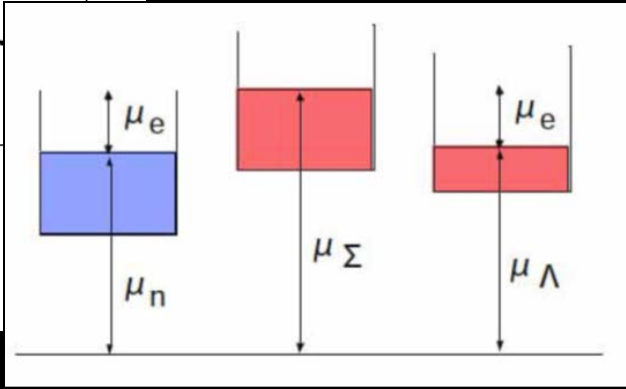
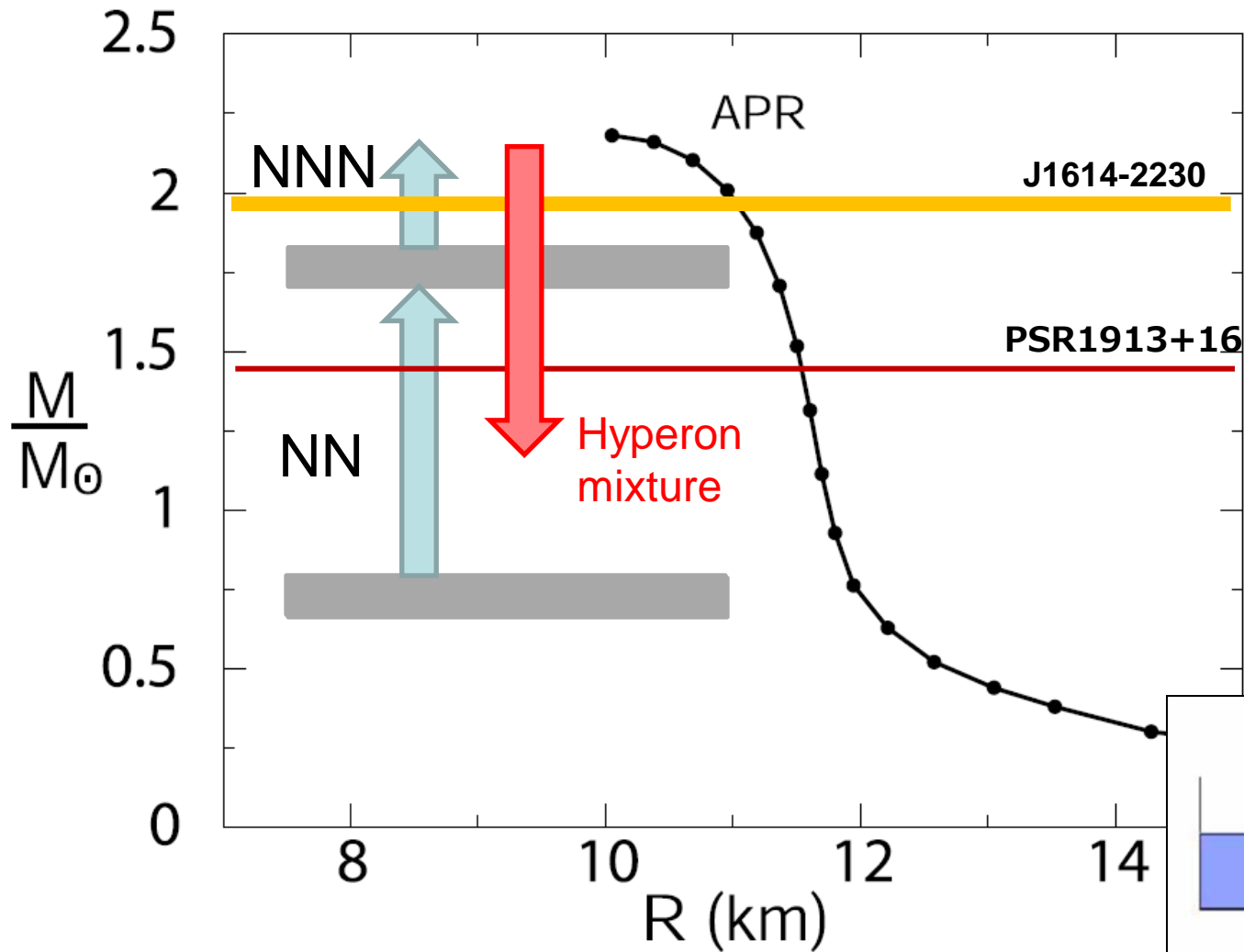
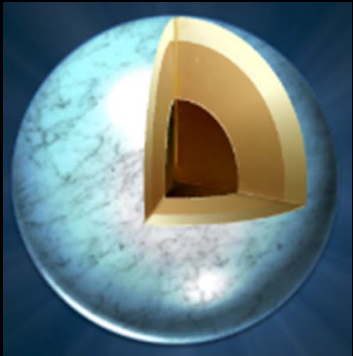


K computer @ RIKEN

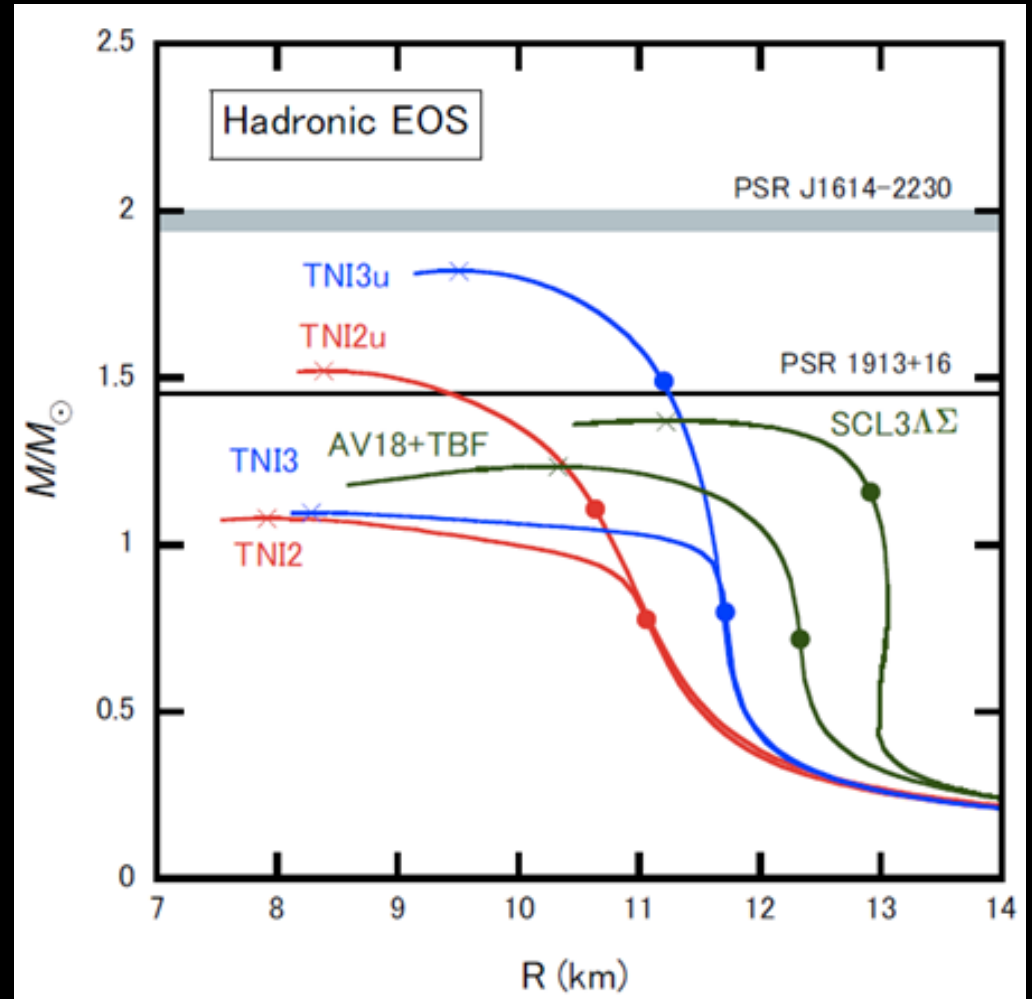
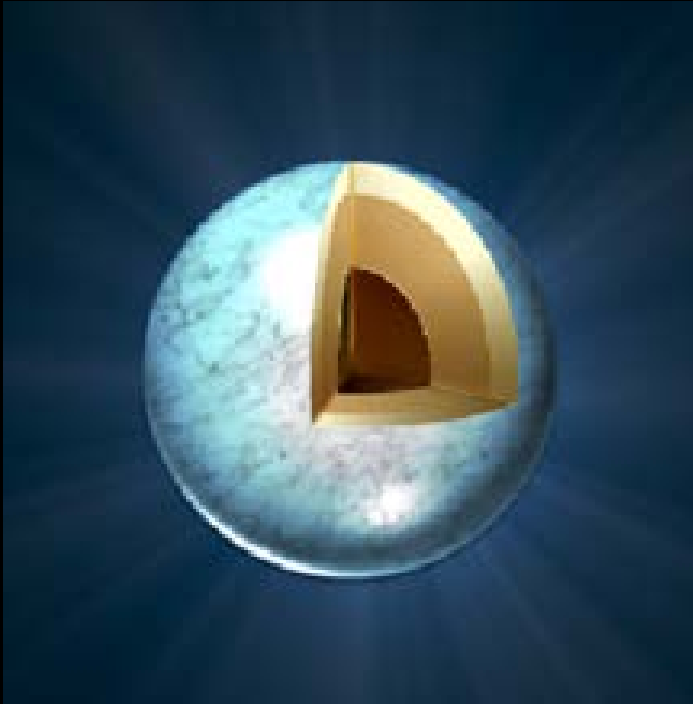
(11.28 PFlops, 80,000 CPUs x 8 = 640,000 cores)



Hyperon Crisis



Hyperon Crisis

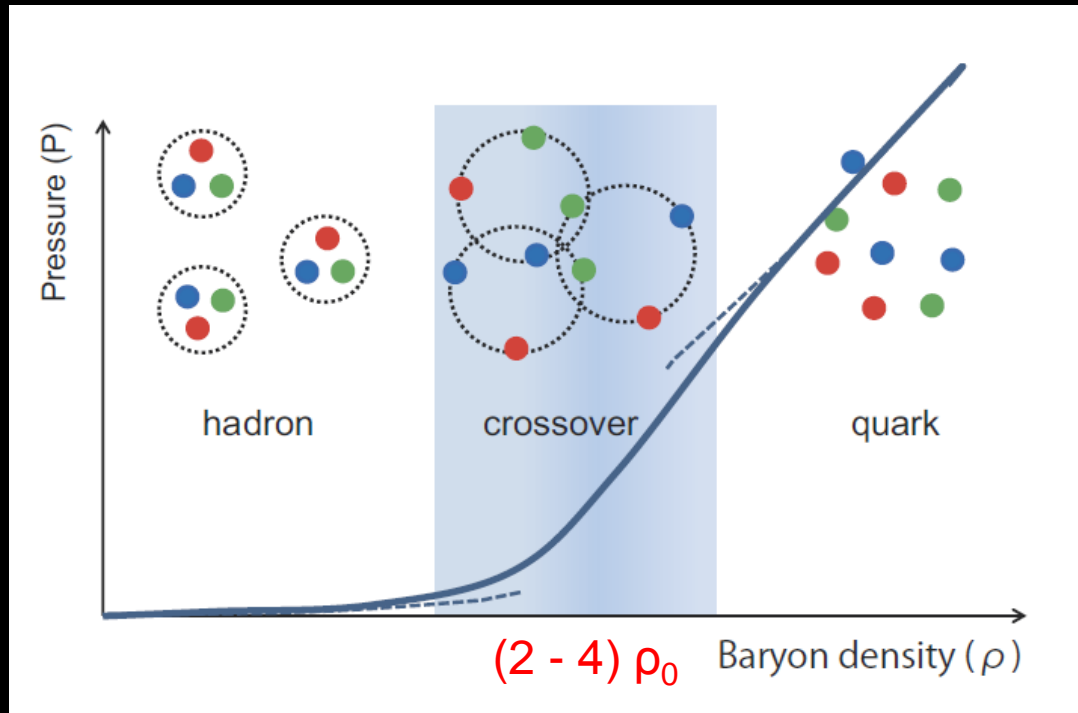


Masuda, Hatsuda & Takatsuka,
Astrophysical Journal Letters 764 (2013) 12

A Possible Resolution of Hyperon Crisis

Crossover to quark matter ?

Hatsuda, Tachibana, Yamamoto & Baym, PRL 97 (2006) 122001
Bratovic, Hatsuda and Weise, Phys.Lett. B719 (2013) 131



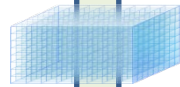
$2M_{\odot}$ neutrons stars require,

- (i) STIFF quark-matter EOS (ii) Crossover at $\rho=(2-4) \rho_0$

From QCD to Hot/Dense Matter

Quantum Chromo Dynamics

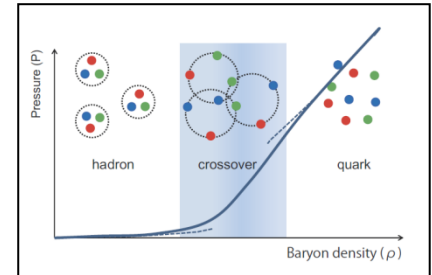
Lattice
gauge theory



sign
problem



Phenome. model



Equation of State for Hot Matter

Relativistic
hydrodynamics

Relativistic heavy-ion collisions

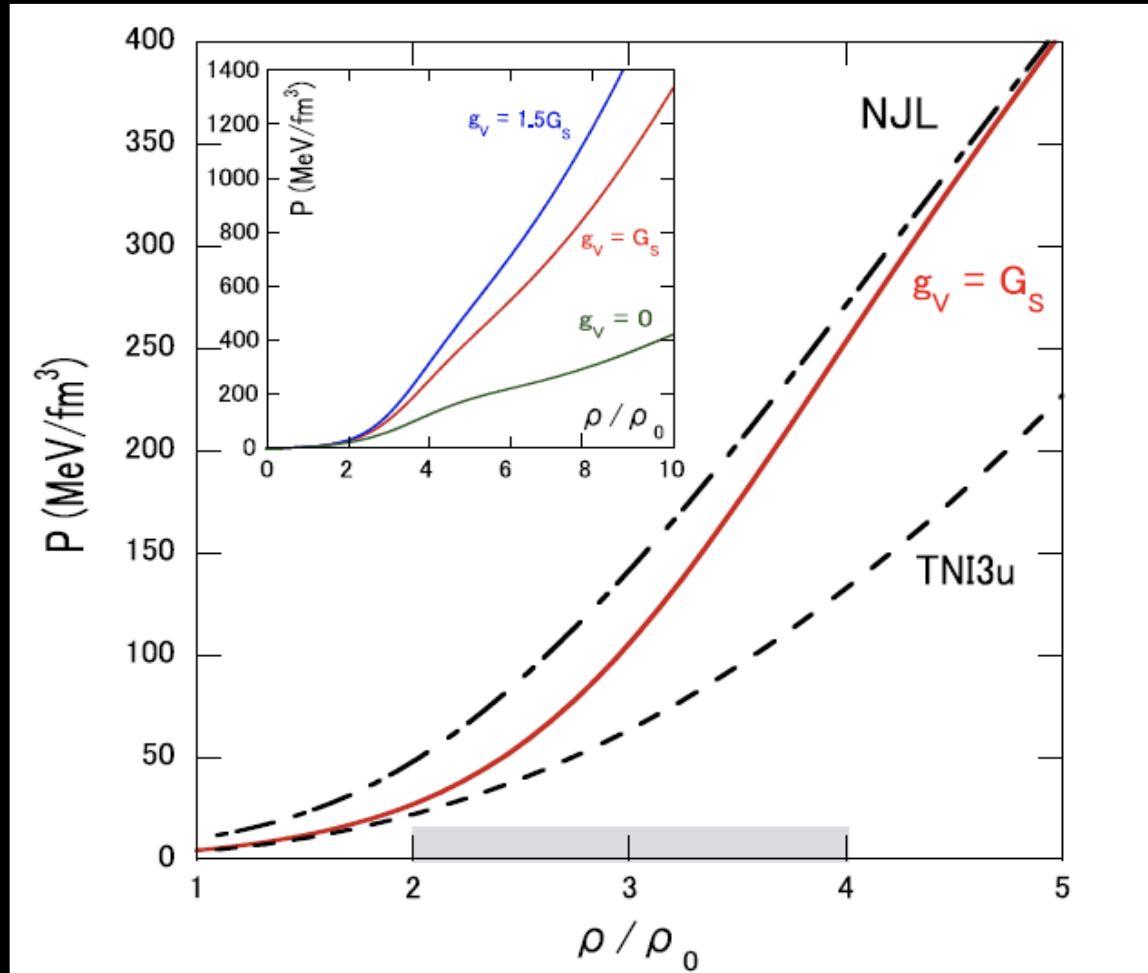
Equation of State for Dense Matter

General relativity

Neutron stars

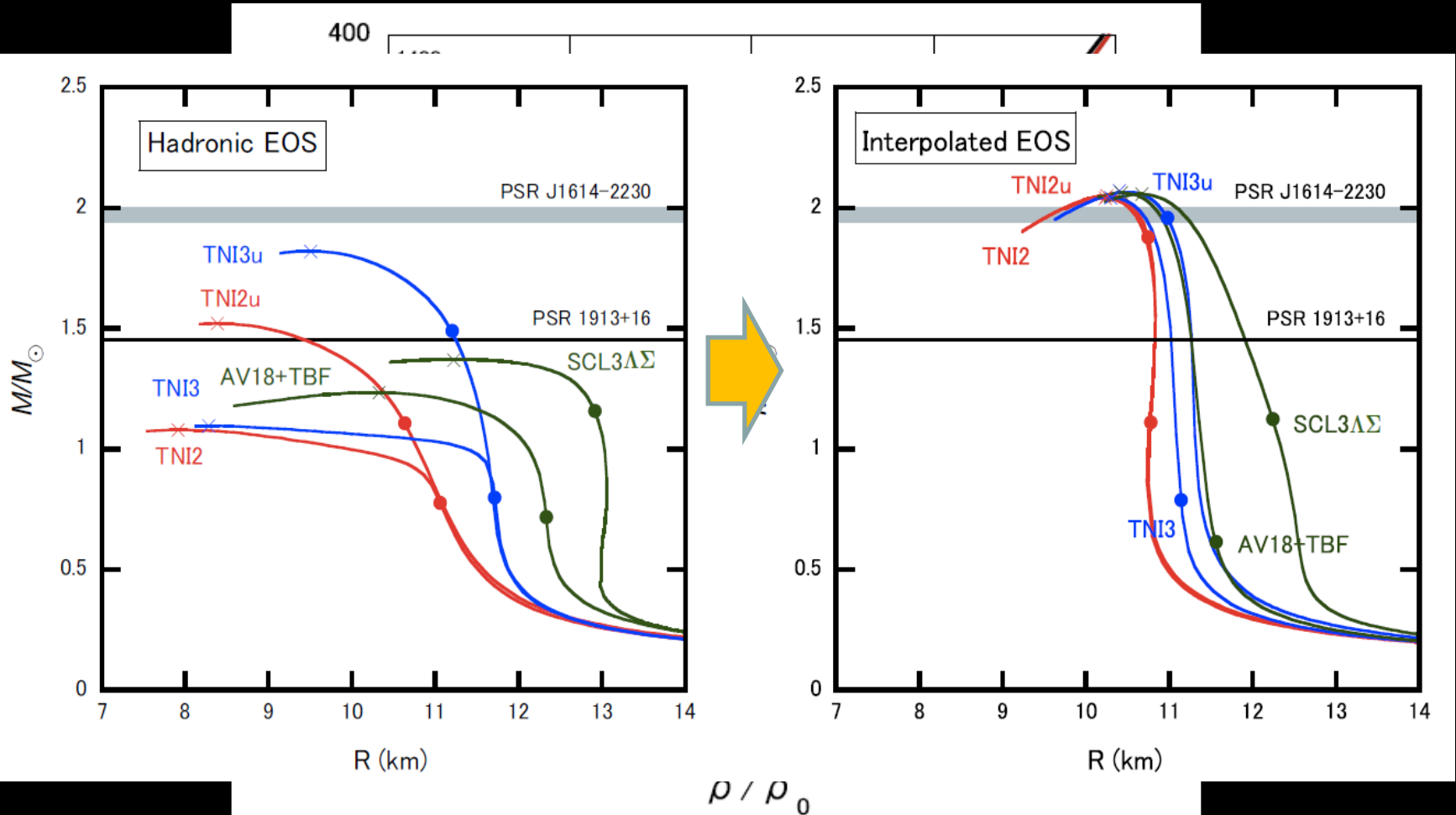
Phenomenological crossover between soft hyperon-matter to stiff quark-matter

(NJL model with vector mean-field)

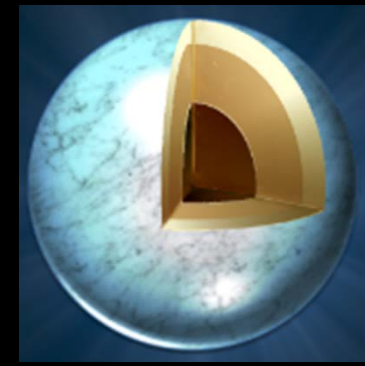


Phenomenological crossover between soft hyperon-matter to stiff quark-matter

(NJL model with vector mean-field)



Summary



1. Dense QCD is a real challenge

theory:

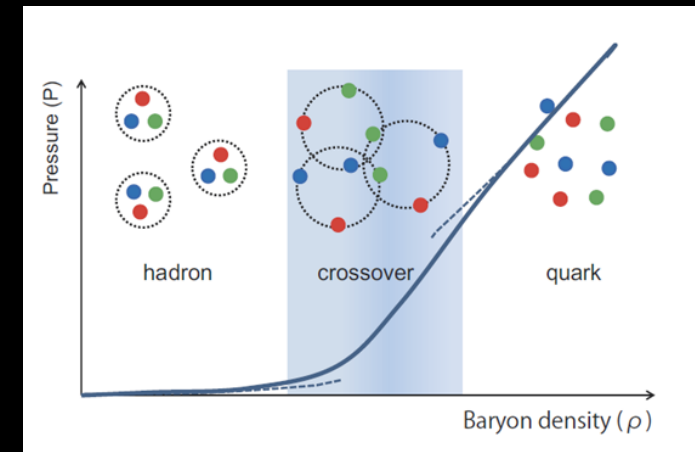
- BB and BBB forces from **lattice QCD** (HAL QCD Coll.)
 - physical point results with $L \sim 10$ fm in a few years
- **sign problem** unsolved

obs.:

- progresses in **M, R, T, B measurements**
 - $2M_{\odot}$ NStars, Magnetars, CAS-A cooling, X-ray bursts
- **Gravitational wave** detections will be ready soon

2. Hyperon Crisis

- no convincing resolution yet
 - n-body hyperon force ?
 - **crossover to stiff quark matter**
 - may be studied by HIC ?
- (Xu, Song, Ko & Li, PRL 2014)



Elliptic flow splitting as a probe of the QCD phase structure at finite baryon chemical potential

Jun Xu,^{1,*} Taesoo Song,² Che Ming Ko,² and Feng Li²

¹Shanghai Institute of Applied Physics, Chinese Academy of Sciences, Shanghai 201800, China

²Cyclotron Institute and Department of Physics and Astronomy,
Texas A&M University, College Station, Texas 77843, USA

(Dated: November 15, 2013)

Using a partonic transport model based on the 3-flavor Nambu-Jona-Lasinio model and a relativistic hadronic transport model to describe, respectively, the evolution of the initial partonic and the final hadronic phase of heavy-ion collisions at energies carried out in the Beam-Energy Scan program of the Relativistic Heavy Ion Collider, we have studied the effects of both the partonic and hadronic mean-field potentials on the elliptic flow of particles relative to that of their antiparticles. We find that to reproduce the measured relative elliptic flow differences between nucleons and antinucleons as well as between kaons and antikaons requires a vector coupling constant as large as 0.5 to 1.1 times the scalar coupling constant in the Nambu-Jona-Lasinio model. Implications of our results in understanding the QCD phase structure at finite baryon chemical potential are discussed.

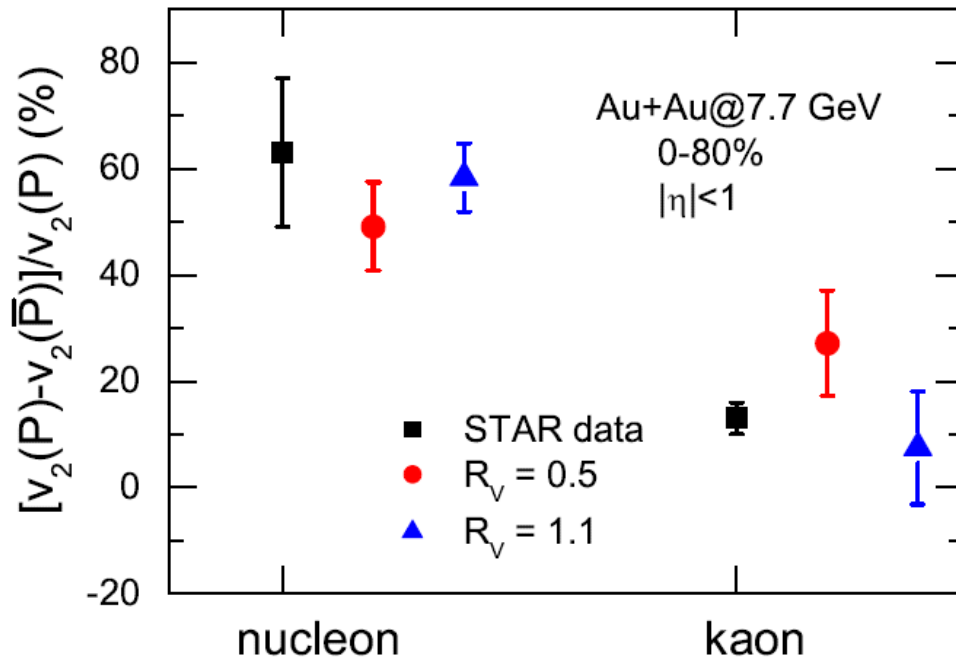


FIG. 4: (Color online) Relative elliptic flow difference between nucleons and antinucleons as well as kaons and antikaons for different values of $R_V = G_V/G$ in the NJL model compared with the STAR data [8].

END

Precision QCD

$$\mathcal{L} = -\frac{1}{4}G_{\mu\nu}^a G_a^{\mu\nu} + \bar{q}\gamma^\mu(i\partial_\mu - gt^a A_\mu^a)q - m\bar{q}q$$

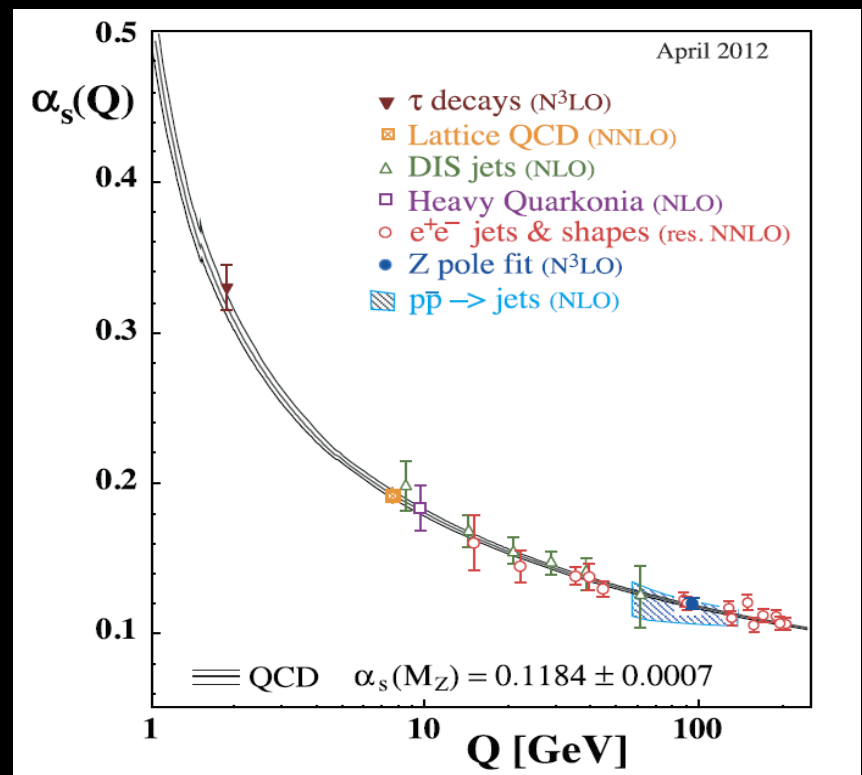
$$G_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + gf_{abc}A_\mu^b A_\nu^c$$

Running masses: $m_q(Q)$

quark masses (from lattice QCD)	[MeV] (MS-bar @ 2GeV)
m_u	2.16 (9)(7)
m_d	4.68 (14)(7)
m_s	93.8 (2.4)

FLAG Collaboration update(July 26, 2013)
<http://itpwiki.unibe.ch/flag/>

Running coupling: $\alpha_s(Q)=g^2/4\pi$



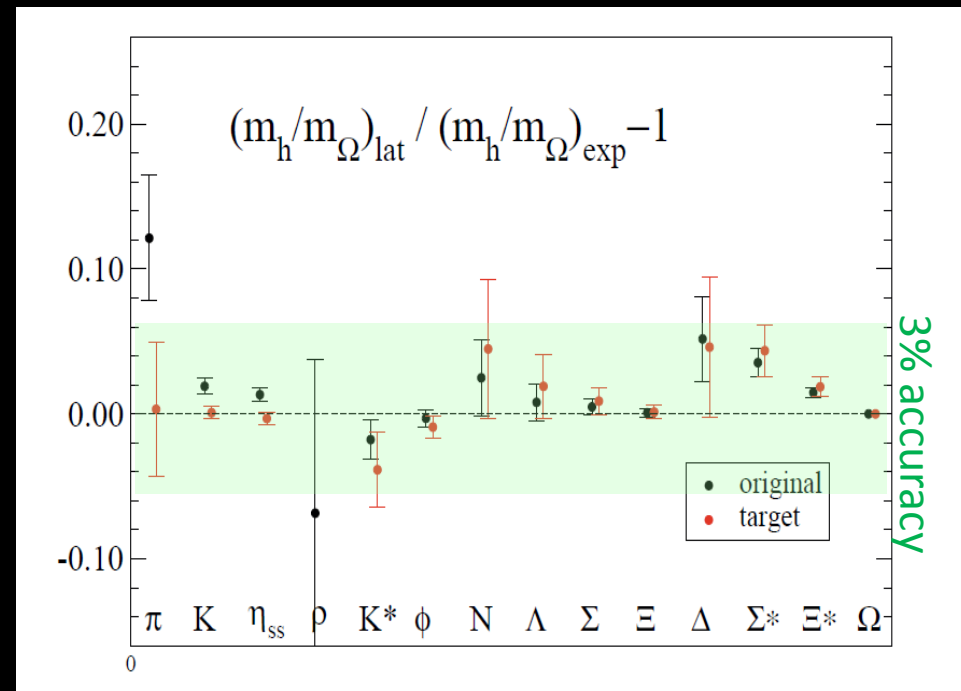
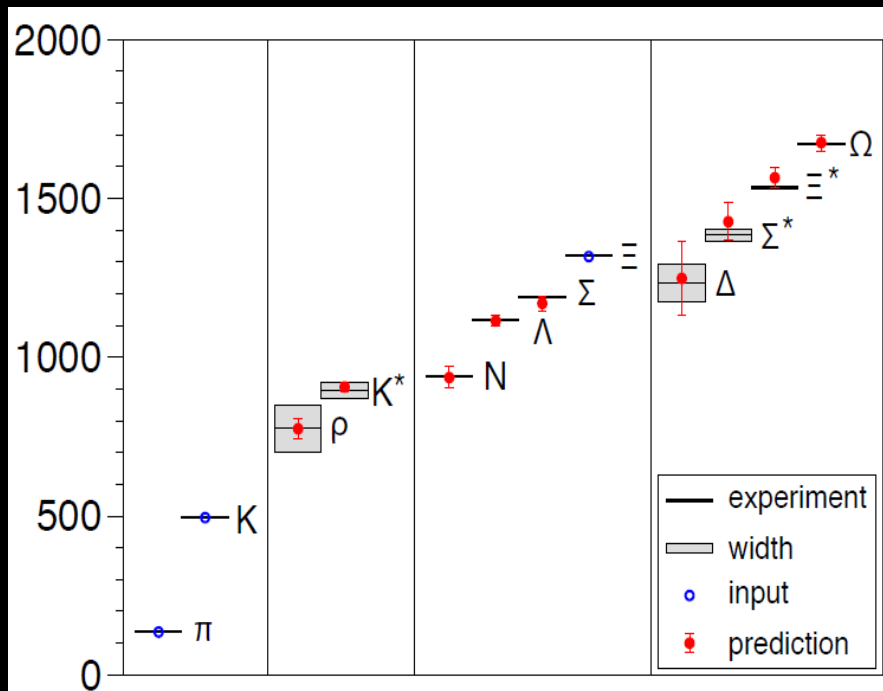
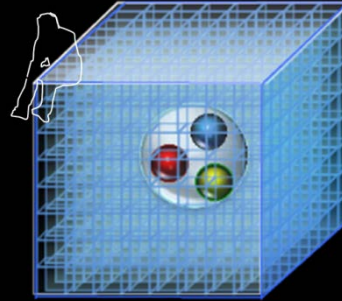
PDG (2012) <http://pdg.lbl.gov/>

Hadron masses (2008)

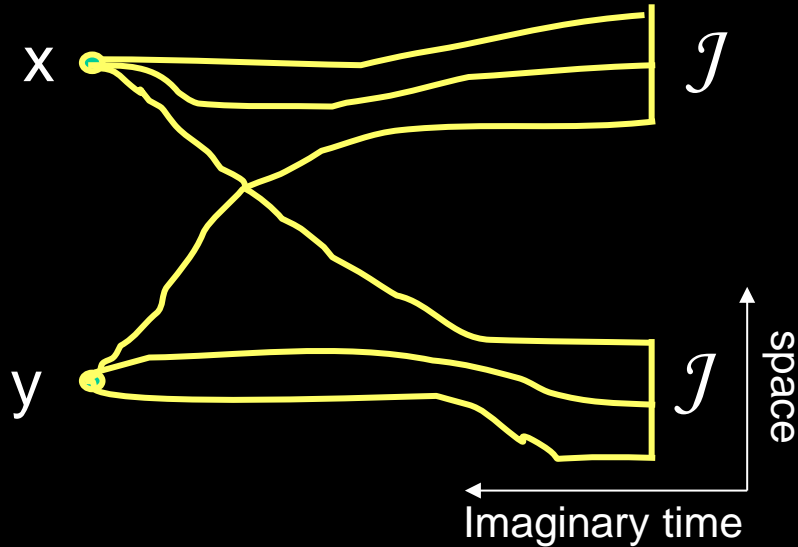
$$m_{\pi} > 190 \text{ MeV}$$

Hadron masses (2010)

$$m_{\pi} = 135 \text{ MeV}$$



Hadronic correlations in LQCD



$$\begin{aligned} & \langle N_1(\mathbf{x}, t) N_2(\mathbf{y}, t) \mathcal{J}_1^\dagger(0) \mathcal{J}_2^\dagger(0) \rangle \\ &= \sum_n \langle 0 | N_1(\mathbf{x}) N_2(\mathbf{y}) | n \rangle a_n e^{-E_n t} \\ & \xrightarrow{t > t^*} \phi(\mathbf{r}, t) = \sum_{n < n^*} b_n \phi_n(\mathbf{r}) e^{-E_n t} \end{aligned}$$

Finite Volume Method

$E_0(L) \rightarrow$ phase shift

Luescher, Nucl. Phys. B354 (1991) 531

HAL QCD Method

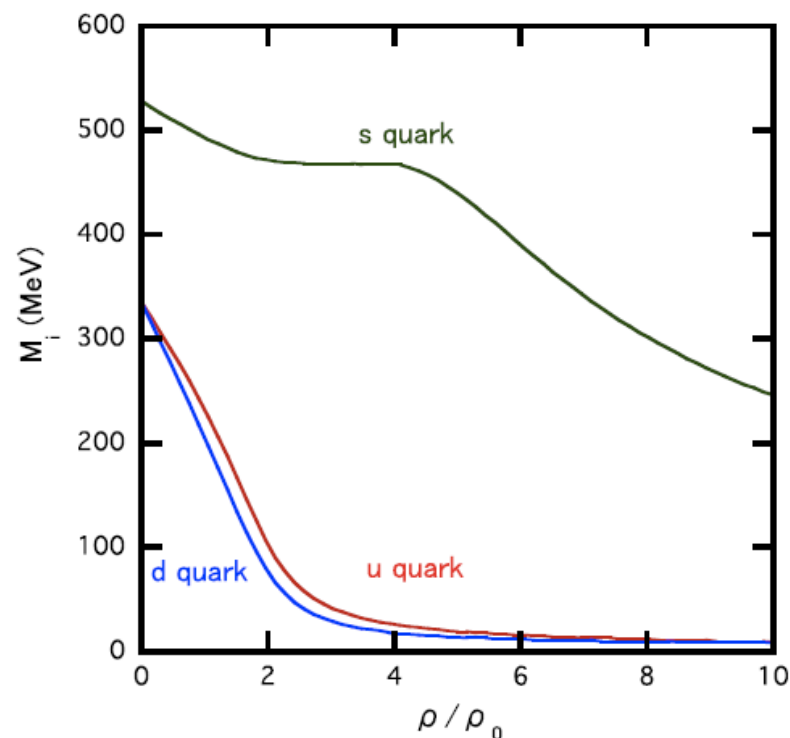
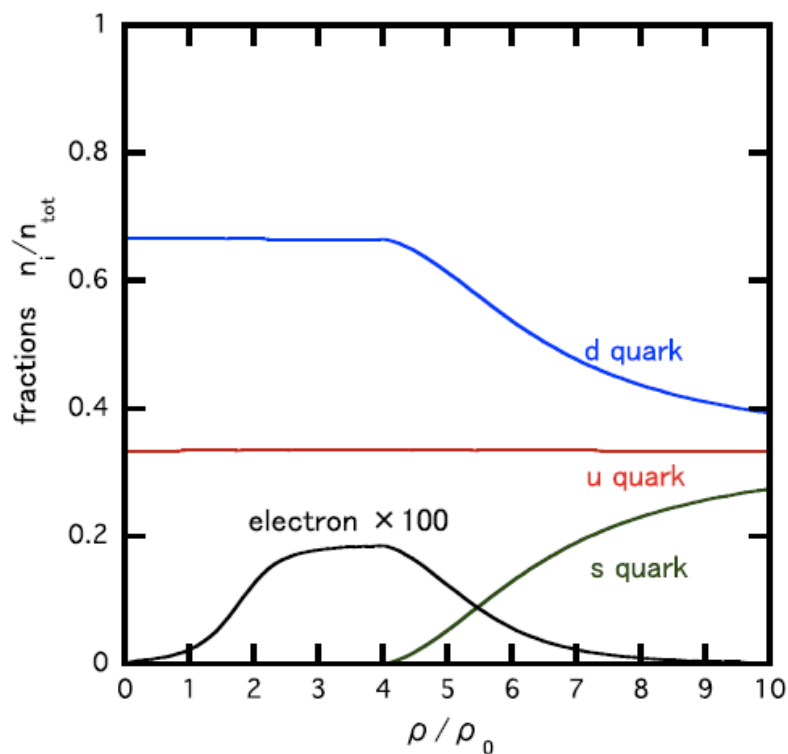
$\phi(\mathbf{r}, t) \rightarrow$ kernel \rightarrow phase shift

Ishii, Aoki & Hatsuda, PRL 99 (2007) 022001
HAL QCD Coll., PLB 712 (2012) 437

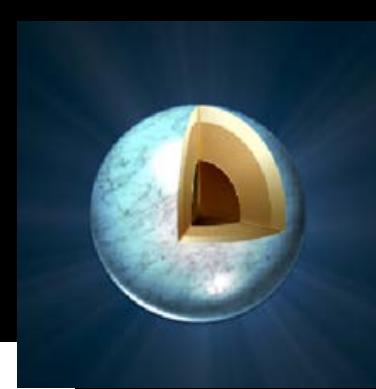
A phenomenological model of strongly interacting Quark Matter

$$\mathcal{L}_{\text{NJL}} = \bar{q}(i\cancel{\partial} - m)q + \frac{1}{2}G_s \sum_{a=0}^8 [(\bar{q}\lambda^a q)^2 + (\bar{q}i\gamma_5\lambda^a q)^2] + G_D [\det\bar{q}(1 + \gamma_5)q + \text{h.c.}]$$

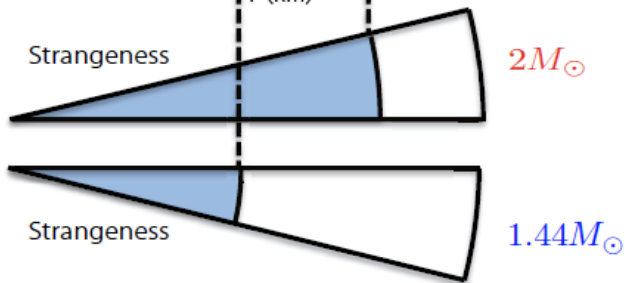
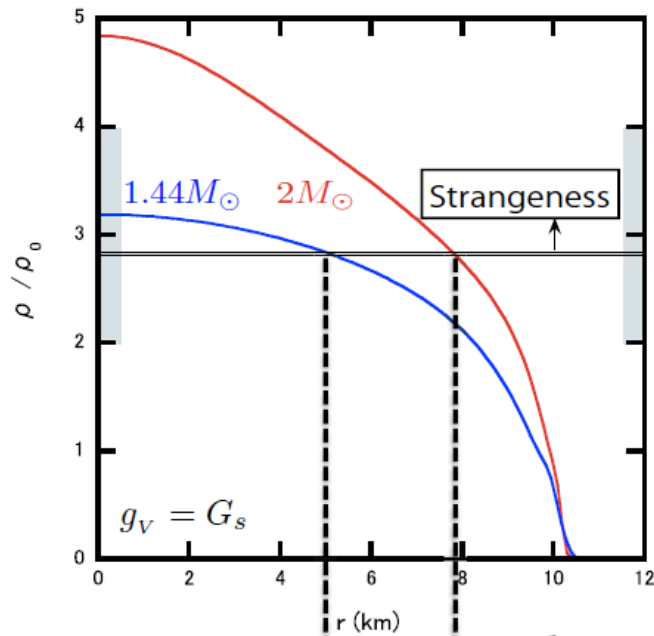
$$- \left\{ \begin{array}{l} \frac{1}{2}g_v (\bar{q}\gamma^\mu q)^2 \\ \frac{1}{2}G_v \sum_{a=0}^8 [(\bar{q}\gamma^\mu\lambda^a q)^2 + (\bar{q}i\gamma^\mu\gamma_5\lambda^a q)^2] \end{array} \right.$$



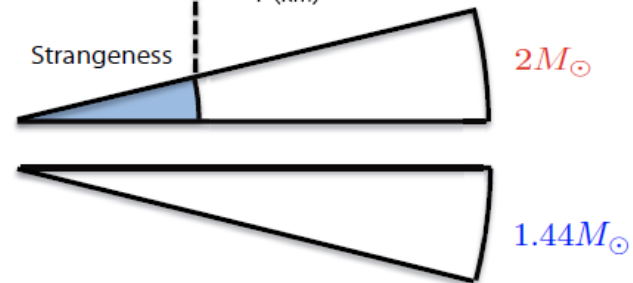
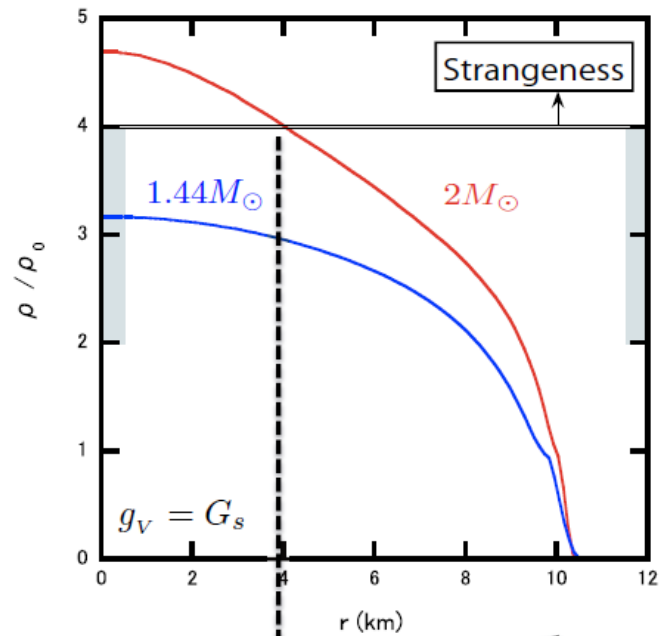
Hyperon 3-body force and onset of strangeness



TNI2



TNI2u



Highly magnetized neutron stars (Magnetars)

Surface $\sim 10^{14-15}$ G
 Interior $\sim 10^{18-19}$ G ?



Physics of strong interaction?

