



Tau lepton reconstruction by using SiECAL, ScECAL with SSA, and Hybrid ECAL

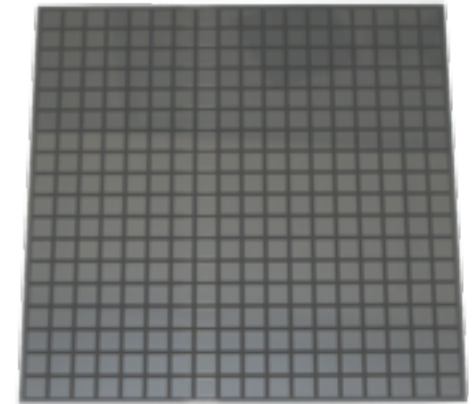
CLIC meeting at CERN
on 2nd October

Katsushige KOTERA
on behalf of Tomohisa OGAWA

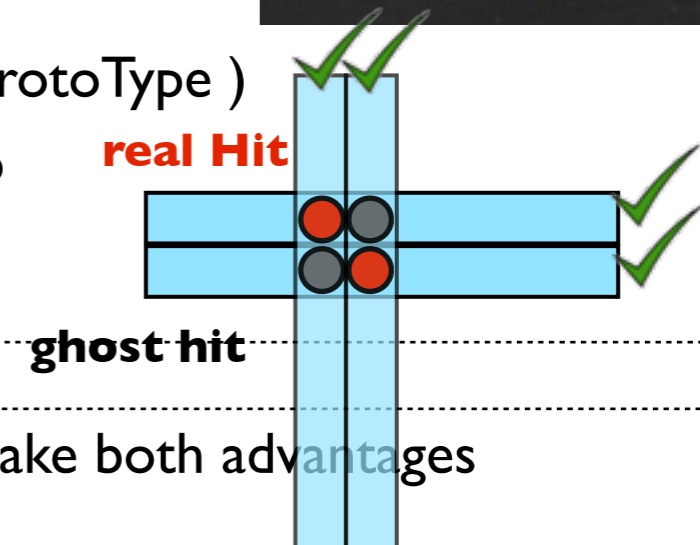
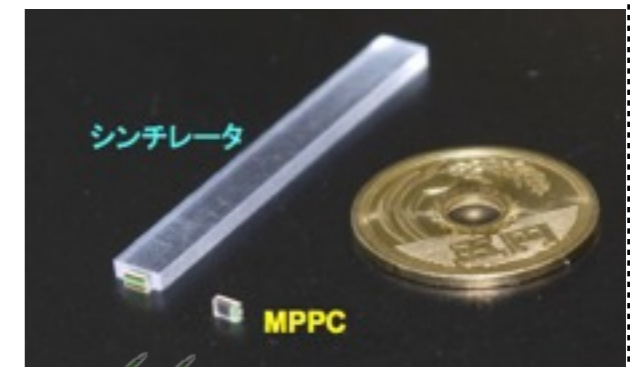
Introduction

ILD ECAL

- Si ECAL : - 5 mm x 5 mm lateral granularity with Si-Pad
 - Easy to make fine granular ECAL
 - Intrinsic energy resolution: $\sim 16\% / \sqrt{E}$ (2006 PhysicsProtoType)
 - Expensive



- Sc ECAL : - 45 mm x 5 mm plastic scintillator strip.
 - layer-layer orthogonal alignment $\rightarrow 5 \times 5 \text{ mm}^2$ granularity.
 - Special algorithm (SSA) is developed as yesterday's my talk .
 - ghosts might appear
 - Intrinsic energy resolution: $\sim 13\% / \sqrt{E}$ (2009 PhysicsProtoType)
 - note 10 x 45 x 3 mm strip
 - less expensive than half as SiECAL.



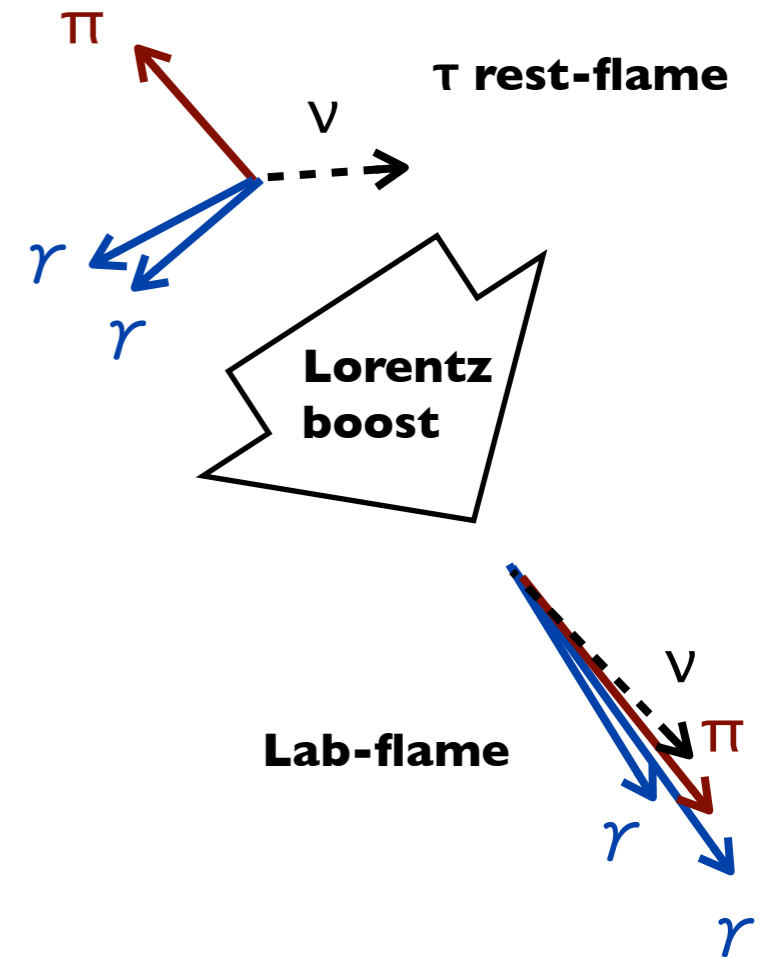
- Hybrid ECAL : - Si layers and Sc layers are piled up alternatively to take both advantages
 - ghosts are almost disappeared.
 - in this talk, not real alternative Hybrid ... study of real alternative one is ongoing

Motivation of this study

- $ee \rightarrow \tau\tau$ is one of the ILD bench mark process to study the ECAL performance

Seeing:

- event selection ability : Efficiency & Purity
 - Physics observables : σ , AFB, tau polarization,
- High Lorentz boost of τ jet ($\sqrt{s} = 500 \text{ GeV}$)
 - Challenge of particle separation by using PFA.
 - Angular distribution provides the polarization of τ
 - requires precise four momentum measurements.
 - including π^0 reconstruction → 2- γ separation ability.



τ decay reconstruction is good examination of performance of ECALs with PFA and Strip Splitting Algorithm for strip ECAL.

Event samples

- Event generation : Whizard.

- Beam condition $\sqrt{s} = 500\text{GeV}$ (ISR-OFF)
- Beam polarization : $e^- e^+ = -80\% +30\%$, $e^- e^+ = +80\% -30\%$,
- Signal : $e^- e^+ \rightarrow \tau \tau$
- BackGround (Temporary) : $e^- e^+ \rightarrow \text{Bhabha}$
 $2-\gamma \rightarrow \tau \tau$
 $e^- e^+ \rightarrow WW$

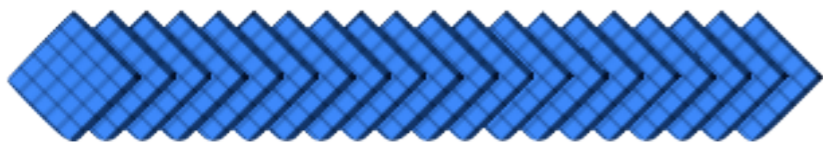
- τ 's branching ratio

$\tau \rightarrow e \nu \nu$	17.8%
$\tau \rightarrow \mu \nu \nu$	17.4%
$\tau \rightarrow \pi \nu$	11.3%
$\tau \rightarrow \rho \nu$	24.9%
$\tau \rightarrow a l \nu$ (1p)	9.0%
$\tau \rightarrow a l \nu$ (3p)	10.0%

- Detector : Mokka (ECAL Configuration)

SiECAL :

0.5 mm of thickness of Si



ScECAL : w/o SSA, w/ SSA

1.5 mm of thickness of Sc



Analysis with more suitable thickness is under going

Hybrid : Alternative Double Layer

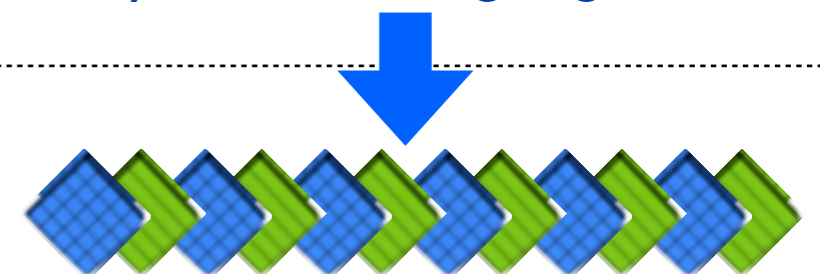
Si+Si+Sc+Sc+Si+Si+.... (w/ SSA)



Analysis with complete alternative Hybrid is under going

- Event reconstruction : Marlin.

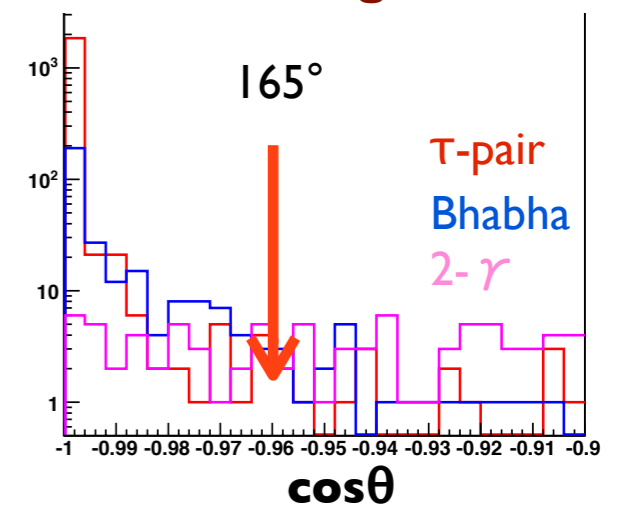
- Reconstruction by using PandoraPFA.
- Mode Selection : cut base.



Reconstruction of τ jet

1. Sort particles in energy order.
2. Select two of the most energetic charged particles (tau candidates) with larger than 165° of their opening angle.

Opening angle between main two charged



→ This set of cuts is called the pre-cuts

BG rejection ratio of the pre-cuts

e-L, e+R	τ -pair	Bhabha	$2-\gamma \rightarrow \tau\tau$	W-pair
Si Ecal	3.5%	67.8%	95.5%	47.3%
Hybrid	3.5%	67.9%	95.3%	48.2%
Sc SSA	3.4%	67.9%	95.4%	49.1%
Sc w/o SSA	9.9%	72.4%	95.4%	49.8%

※ In order to make it simple ISR is off. in this study
2/3 events are rejected with ISR.

3. Merge the four momenta of particles around main candidates

→ particles in 15 deg cone are merged

※ considering Cone of 250 GeV τ , it might be better to set 10 deg cone (we know now).

Background Suppression

- done after pre-cut

1. The number of tracks ≤ 6 .

2. $70 < E_{vis} < 450 \text{ GeV}$. E_{vis} : charged energy

$70 \text{ GeV} >$ to reject $\gamma\gamma \rightarrow \tau\tau$ Cut, $450 \text{ GeV} <$ to reject Bhabha.

3. $172^\circ <$ Opening angle between 2jets.

\rightarrow some BG Cut.

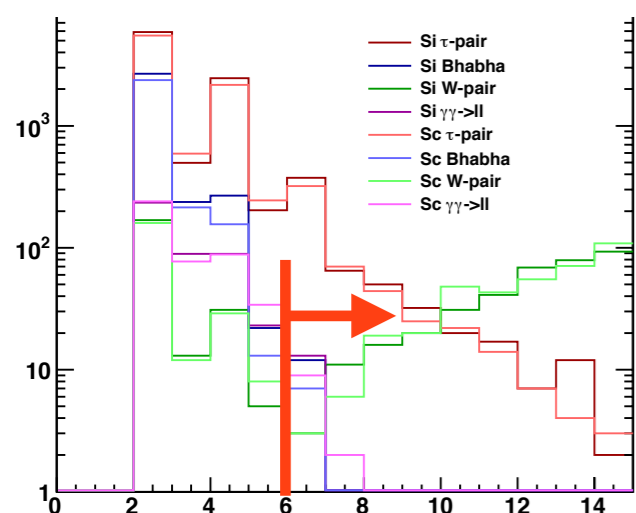
4. $|\cos\theta| < 0.9$ for both jets.

$\rightarrow WW \rightarrow l\bar{l}l\bar{l}$ Cut.

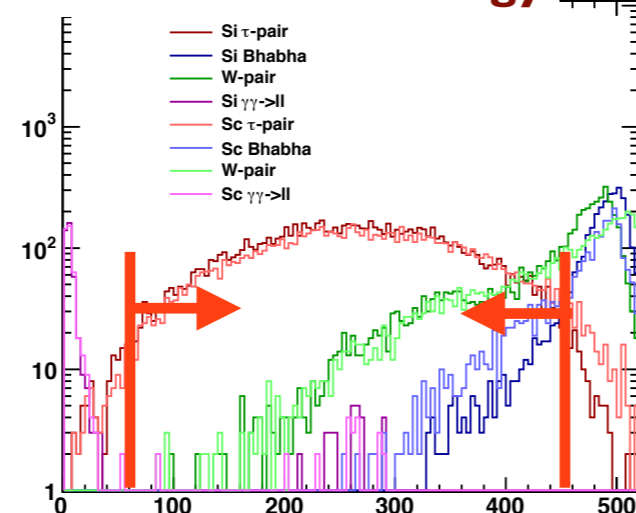
- effect of the background suppression

Cuts	tautau	bhabha	ww	2- γ
No-Cut	100%	100%	100%	100%
Pre-Cut	96.4%	32.2%	50.9%	4.5%
#Tracks	94.1%	32.2%	2.3%	4.5%
Evisible	91.4%	8.3%	2.3%	3.7%
OpenAngle	89.7%	2.1%	0.6%	0.1%
cos(Thrust)	89.7%	2.1%	0.6%	0.1%

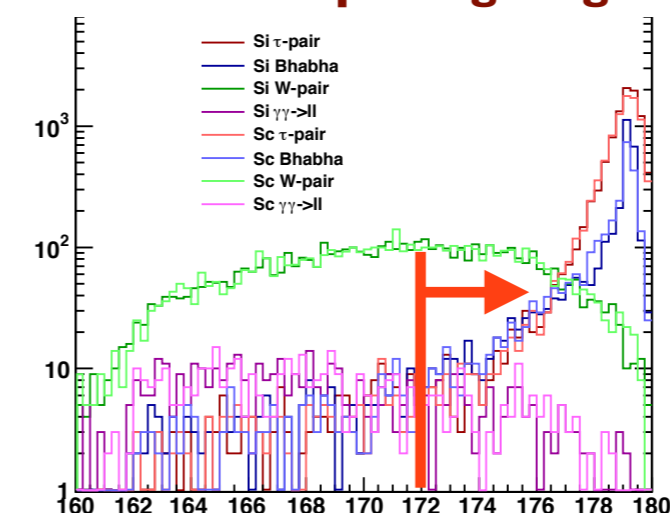
Si/ScECAL N of Tracks



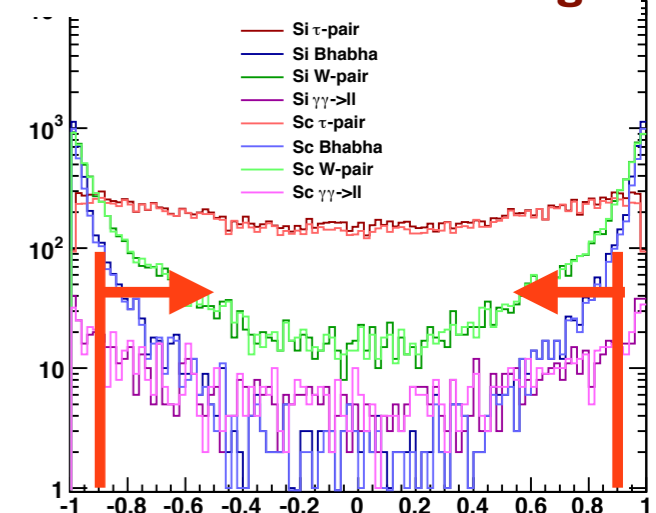
Si/ScECAL Vis Energy



Si/ScECAL Opening Angle



Si/ScECAL Thrust Angle

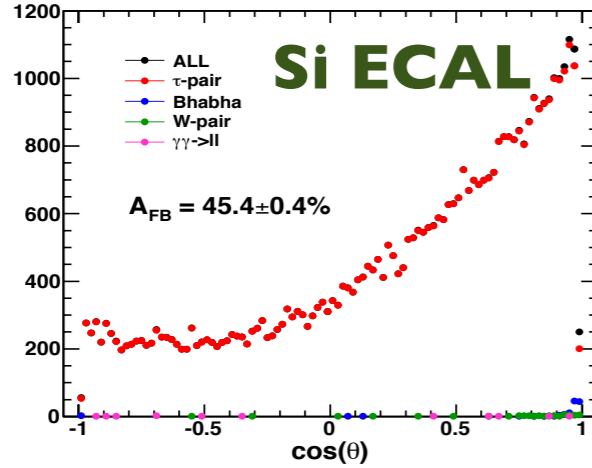


Forward-Backward Asymmetry

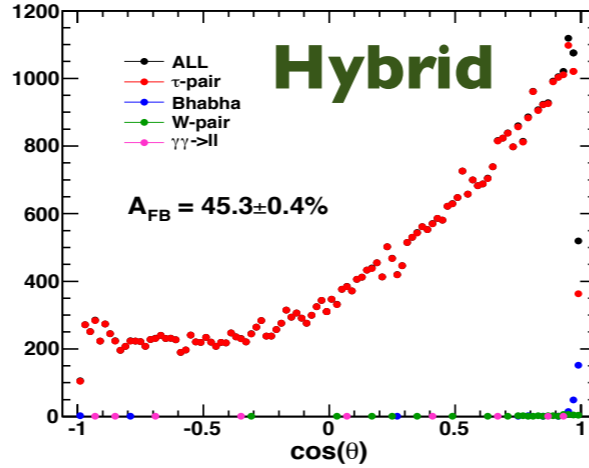
$$\frac{N_F - N_B}{N_F + N_B} \quad N : \# \text{ of } \tau^-$$

e-L e+R

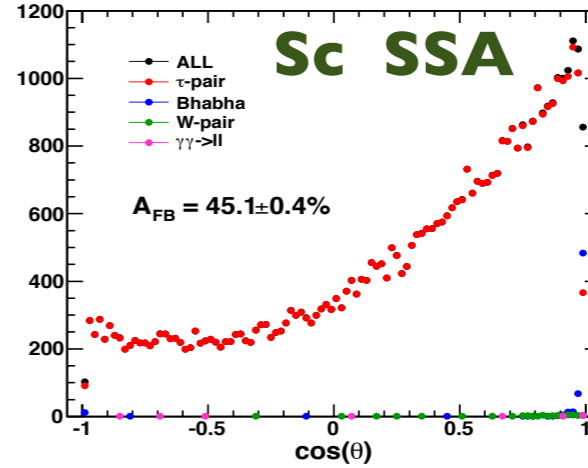
τ^- direction ($e_L^-, e_R^+ = 80\%, 30\%$)



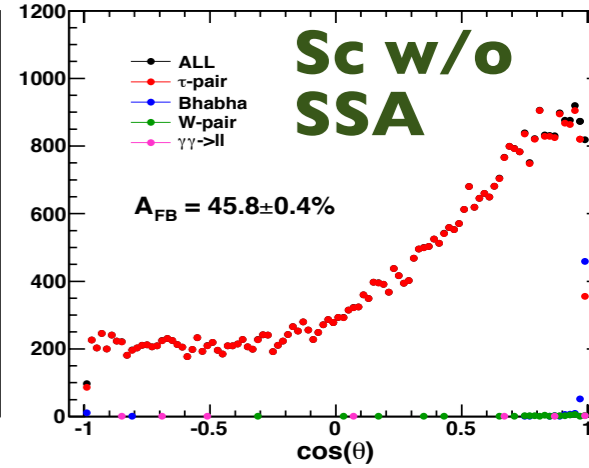
τ^- direction ($e_R^-, e_L^+ = 80\%, 30\%$)



τ^- direction ($e_L^-, e_R^+ = 80\%, 30\%$)

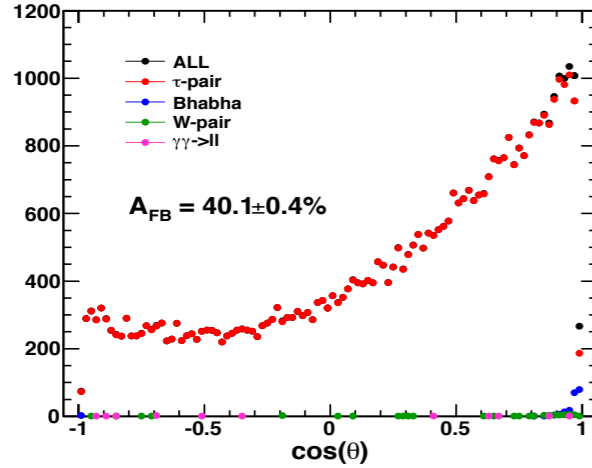


τ^- direction ($e_L^-, e_R^+ = 80\%, 30\%$)

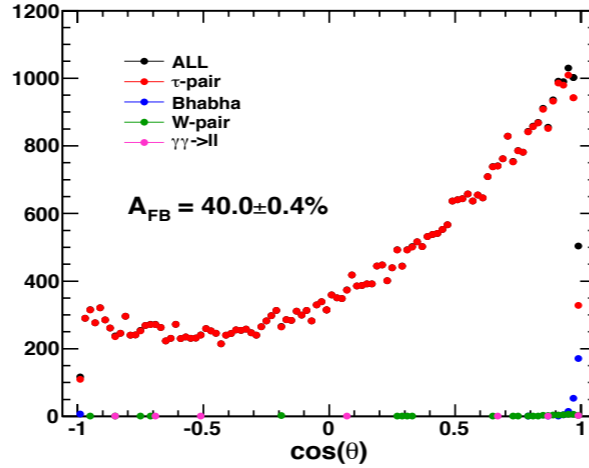


e-R e+L

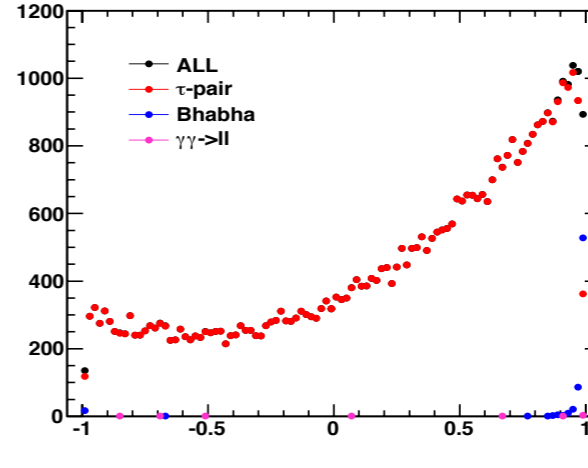
τ^- direction ($e_R^-, e_L^+ = 80\%, 30\%$)



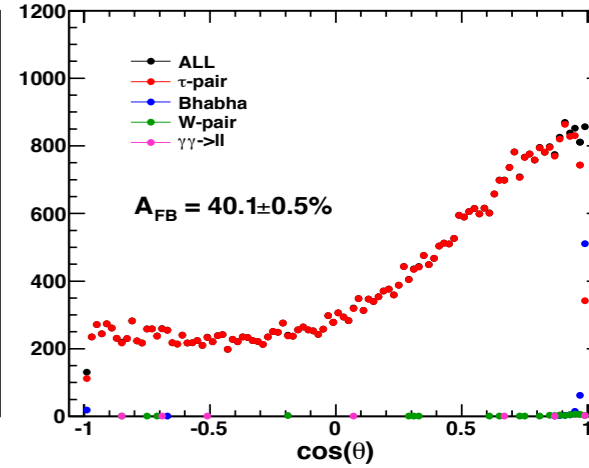
τ^- direction ($e_L^-, e_R^+ = 80\%, 30\%$)



τ^- direction ($e_L^-, e_R^+ = 80\%, 30\%$)



τ^- direction ($e_R^-, e_L^+ = 80\%, 30\%$)



• Forward-Backward Asymmetry

	Si Ecal	Hybrid	Sc SSA	Sc w/o SSA
e-L, e+R	$45.4 \pm 0.4\%$	$45.3 \pm 0.4\%$	$45.1 \pm 0.4\%$	$45.8 \pm 0.4\%$
e-R, e+L	$40.1 \pm 0.4\%$	$40.0 \pm 0.4\%$	$40.2 \pm 0.4\%$	$40.1 \pm 0.5\%$

→ No diff. among ECAL types, ... but Sc w/o SSA fails to reconstruct a part of events at very forward.

Mode selection with a set of trial cuts

- Selection whether leptonic or semi-leptonic and 1 prong or 3 prong

- Lepton ID by PandoraPFA
- The number of charged particle in τ jet \rightarrow 1-prong or 3-prong.

- separation π , ρ , a1 mode in 1 prong event

- Cut by using γ information :

- $E_\gamma > 5.0\text{GeV} \rightarrow \text{Hard} - \gamma$
- $E_\gamma > 0.8\text{GeV} \rightarrow \gamma$

$\rightarrow \pi$ mode : the number of Hard - $\gamma == 0 \ \&\& \ E_\gamma s < 5\text{GeV}$

π Reconstruction \rightarrow charged four momentum with only track information

$\rightarrow \rho$ mode : the number of Hard - $\gamma = 1 \ \&\& \ \gamma \leq 2$ or $\gamma \leq 4 \ \&\& \ \text{Mass } \gamma s (\pi^0) < 0.4\text{GeV}$

ρ reconstruction \rightarrow charged + γs



π^0 Reconstruction

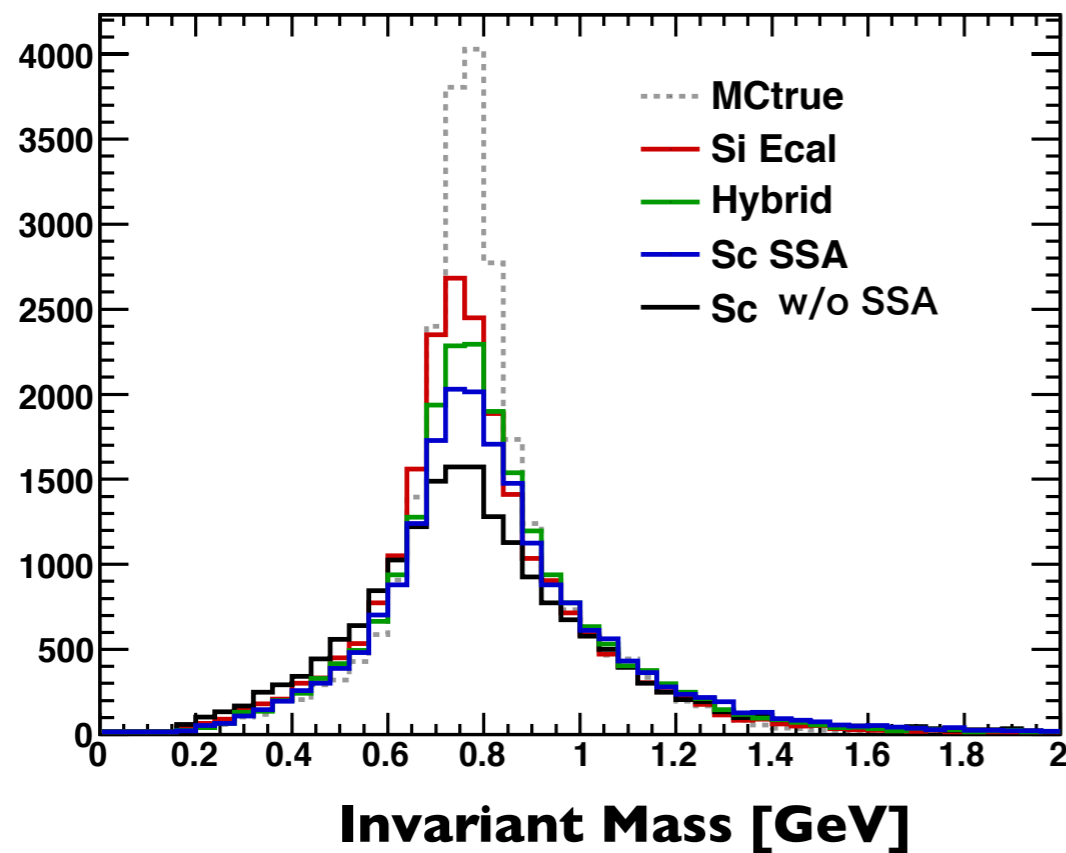
\rightarrow a1 mode : the other events

a1 reconstruction \rightarrow charged + γs

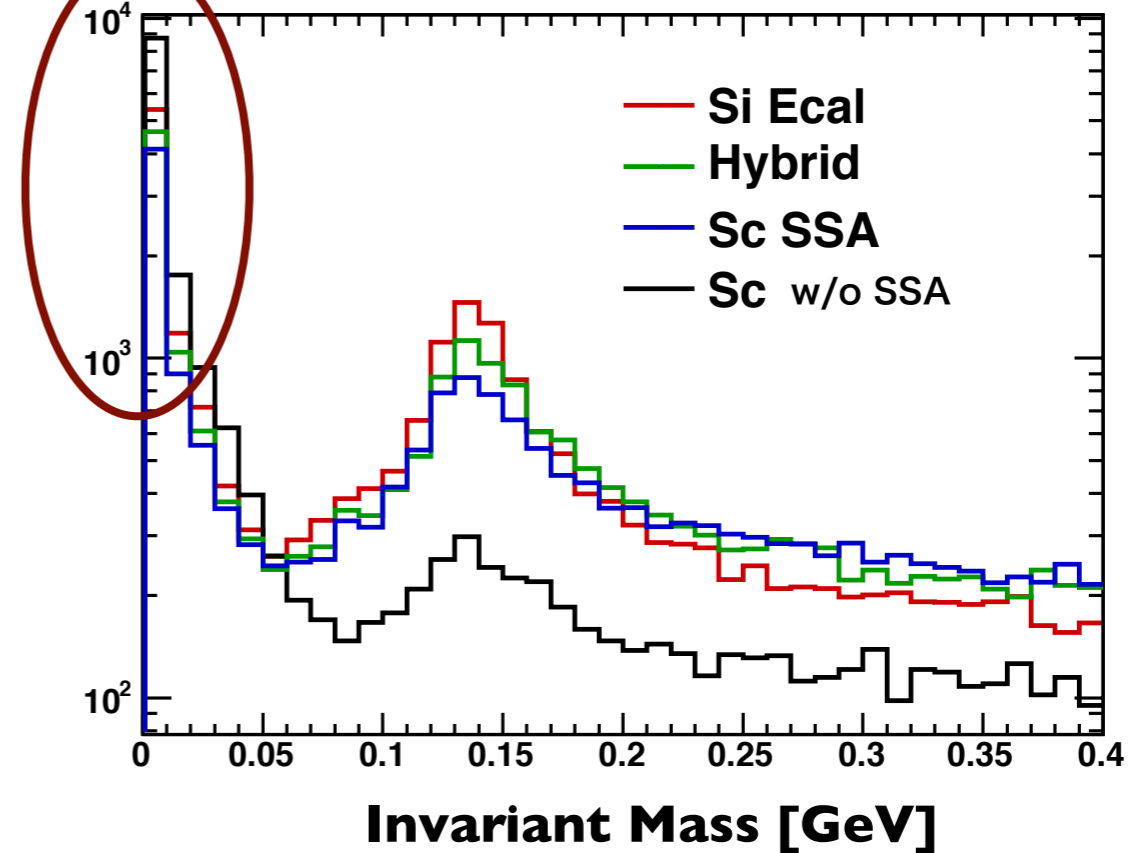
ρ reconstruction including π^0 reconstruction

- Mass of ρ and π^0

4Detectors ρ mass



4Detectors π^0 mass at ρ mode



- ρ reconstruction

performance of reconstruction: Si ECAL > Hybrid Sc w/ SSA > Sc w/o SSA

$$0.89 \pm 0.01, 0.86 \pm 0.01, 0.82 \pm 0.01, 0.77 \pm 0.01$$

note: PandoraPFA is not best tuned for ScECAL (see recent study by John Marshall)

- π^0 reconstruction

SSA drastically improve π^0 reconstruction

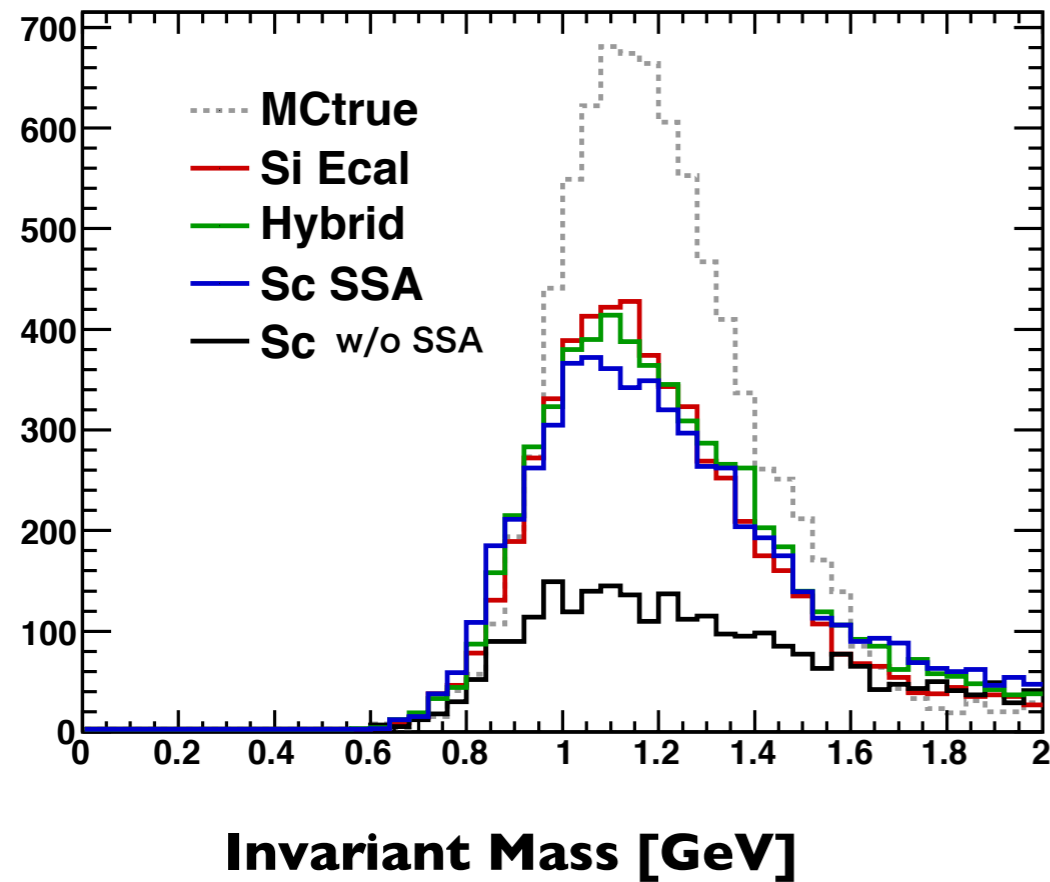
Single photon events are also used in ρ reconstruction



aI reconstruction in 4ECALs

- Mass of aI

4Detectors aI mass



Ecal type	Acceptance
SiECAL	0.796 ± 0.015
Hybrid	0.780 ± 0.012
Sc SSA	0.756 ± 0.012
Sc w/o ssa	0.421 ± 0.008

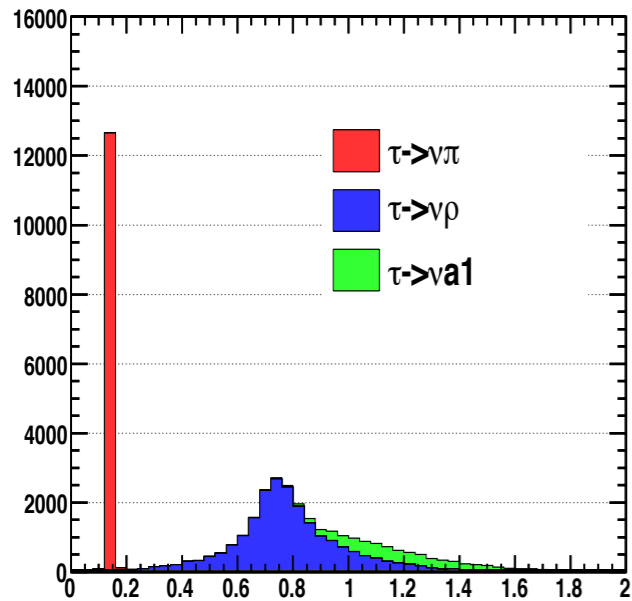
- aI reconstruction

SSA drastically improve aI reconstruction

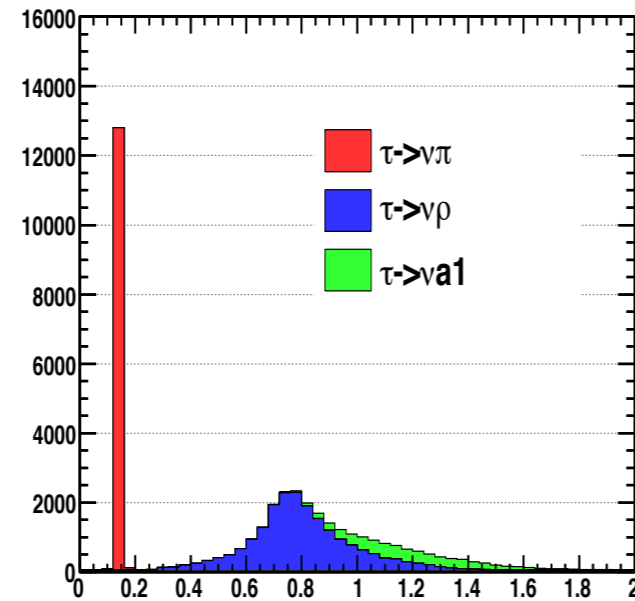
There is no large difference between Ecal types except Sc w/o SSA.

π , ρ , & a_1 mass in 4ECals

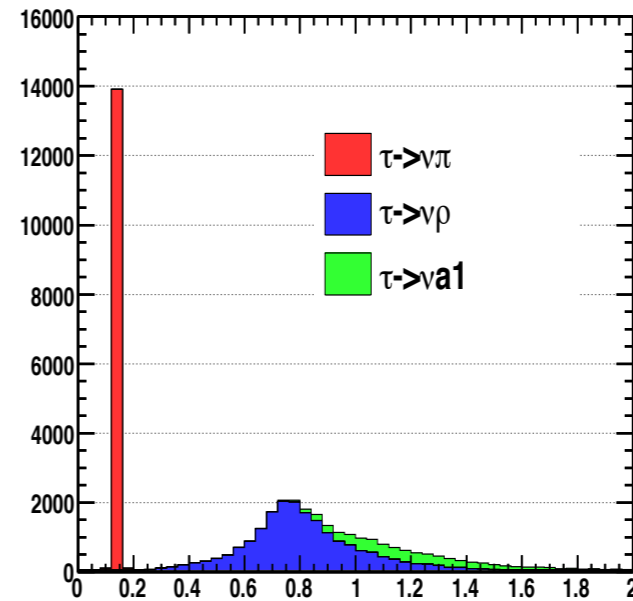
Si ECAL



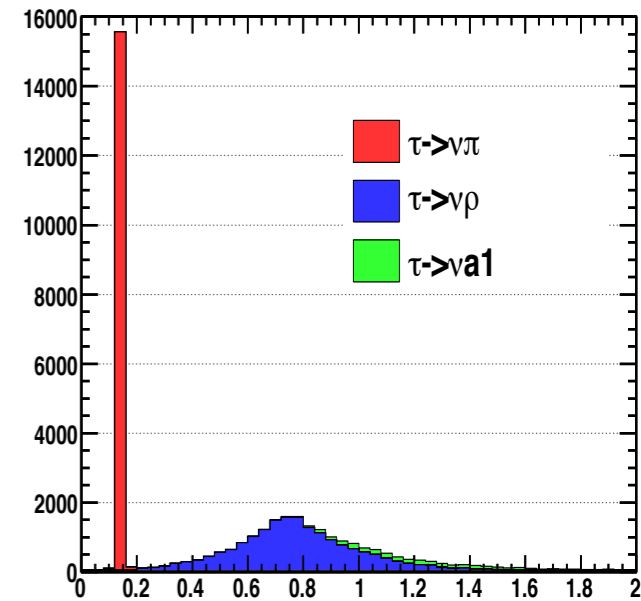
Hybrid_Double



Sc SSA



Sc w/o SSA



Invariant Mass [GeV]

- π^\pm identified events increase with ScECAL
 - ➔ Some ρ^\pm events misidentified as π^\pm with ScECAL ➔ “Hard - γ ” is missed by fragmentation of “Large- γ ” into small γ . ➔ need to try special cone size for ScECAL

Summary

- Performances of four types of ILD-ECAL are compared in τ -pair reconstruction
 - Strip ECAL reconstruction method “SSA” works well to reconstruct ρ and a_1 although some fragmentation of gamma lead to misidentify ρ as π event.
 - Alternative double layer Hybrid improves the situation, not complete.
 - ➔ need study with real alternative Hybrid ECAL

Outlook

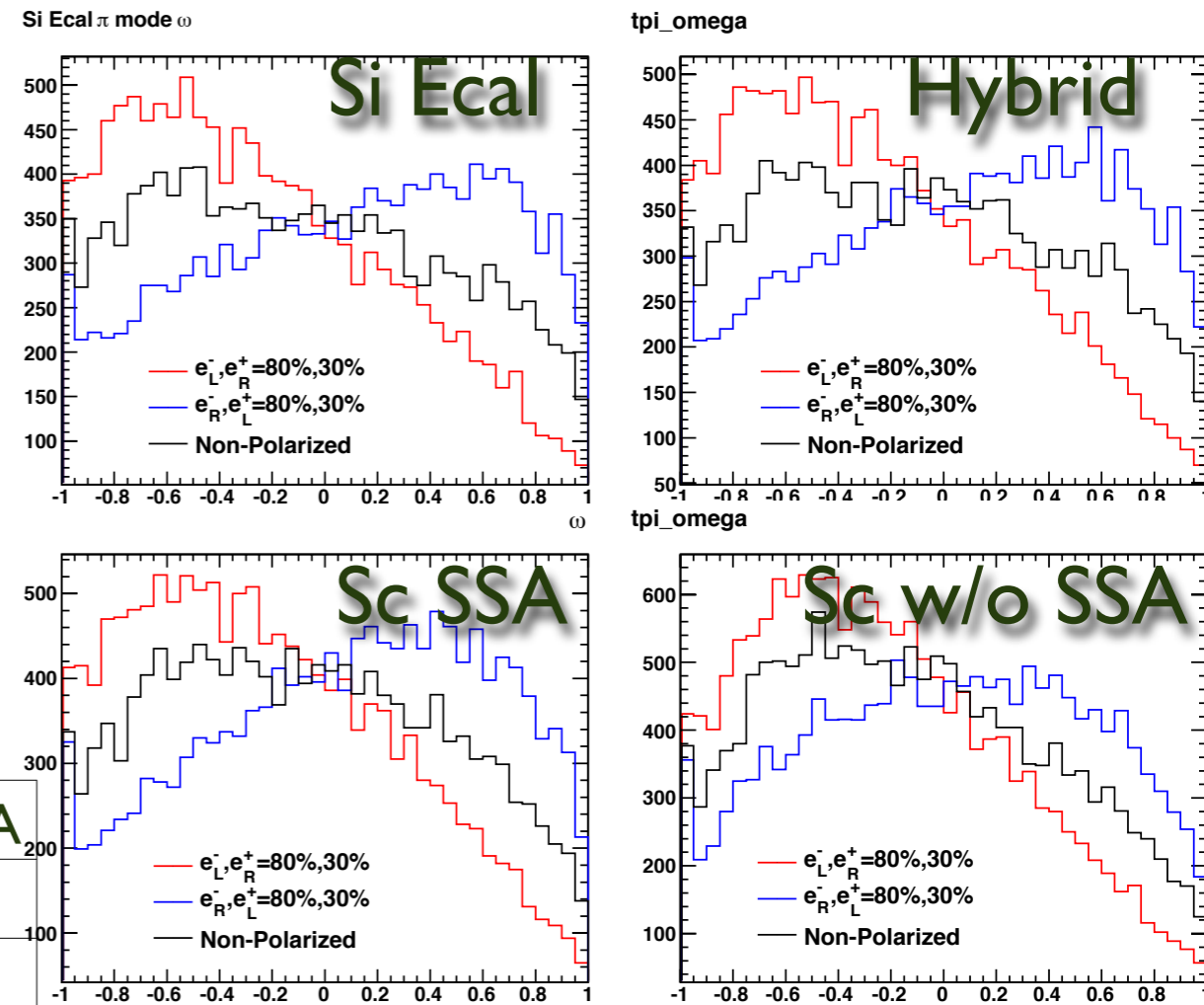
- need study with background events
- need study of real alternative hybrid ECAL
- introduce PandoraPFA tune for ScECAL
- Polarization study.

Angular dist (ω) : π mode

- Since this channel is the simplest, this exhibit the highest sensitivity to polarization.
- Because of no large dependence on γ separation if threshold of counting γ is sufficient, τ 's visible polarity is near about 50% in 4 ECals.
- $P(\tau)$ Result at π

$P(\tau)$	MCtrue	Si Ecal	Hybrid	Sc SSA	Sc w/oSSA
e-L e+R	48%	47%	49%	48%	45%
e-R e+L	57%	51%	50%	52%	46%

• ω distribution

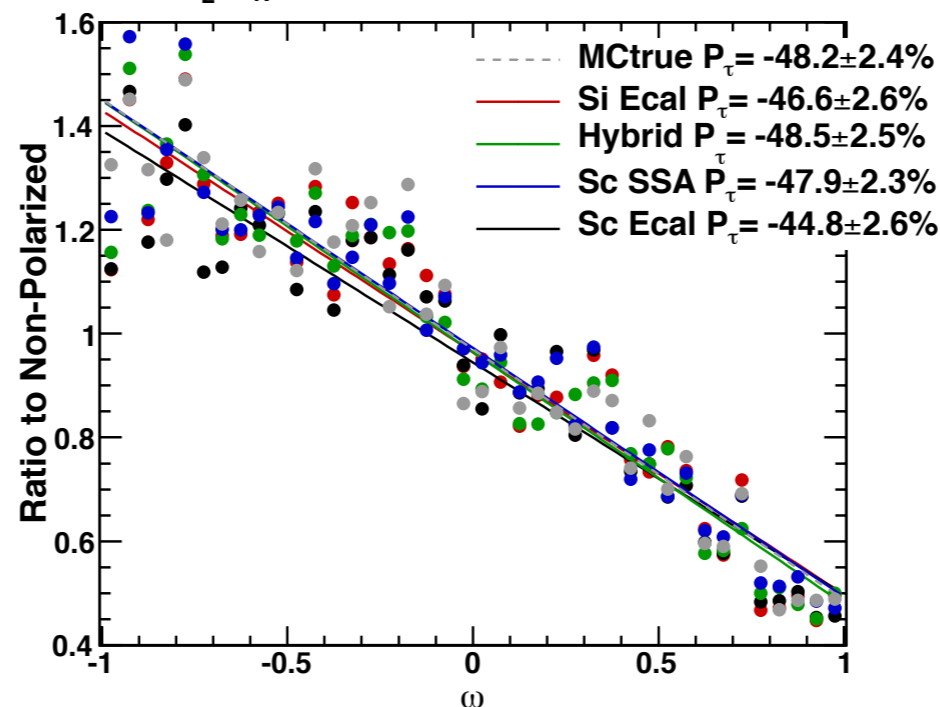


• ω distribution

→ ω distribution divided by non-polarizing sample and Linear fit is applied to obtain $P(\tau)$ value.

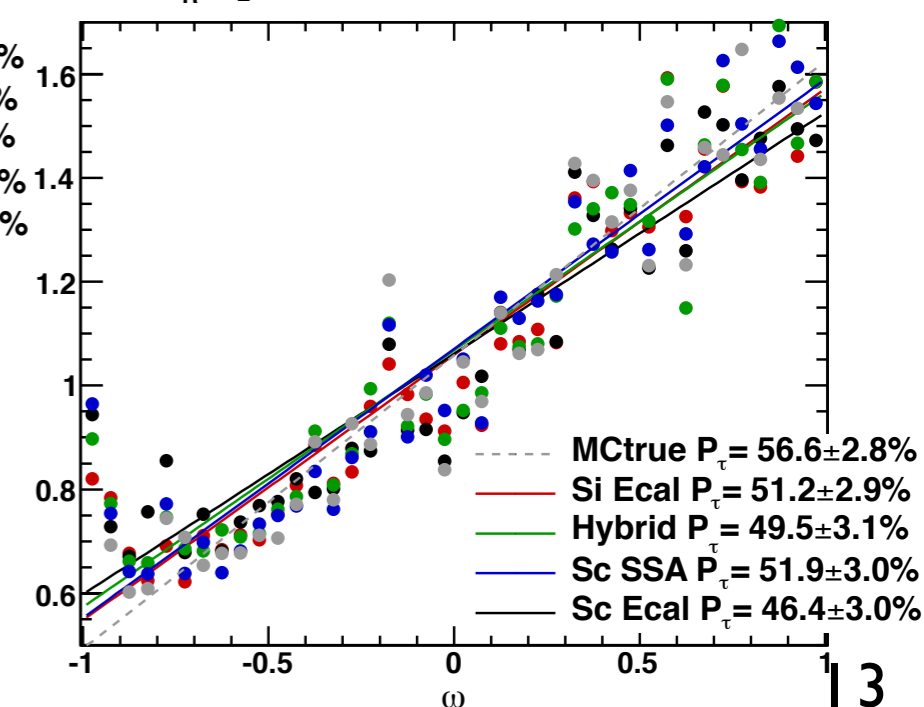
• $P(\tau)$ LR

π mode ($e_L^-, e_R^+ = 80\%, 30\%$)



• $P(\tau)$ RL

π mode ($e_R^-, e_L^+ = 80\%, 30\%$)

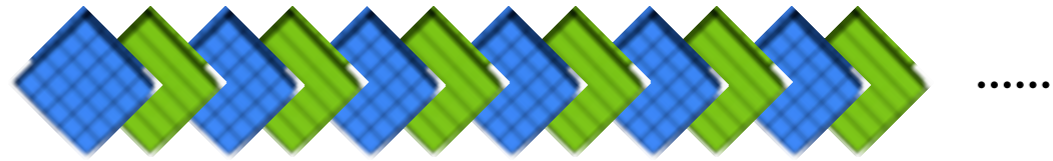


Hybrid Single Alternative

- Hybrid Single Alternative (※ π は γ を含ませてReconstruction)

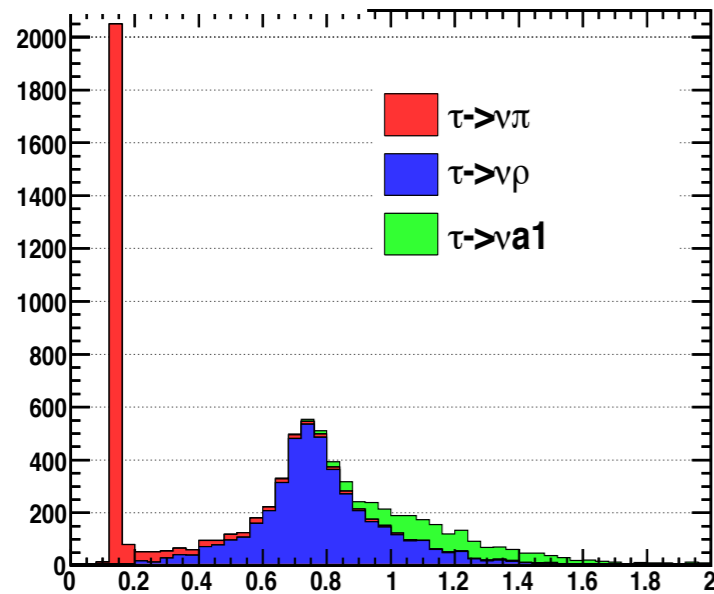
シンチTile 5mmx5mm

シンチStrip 45mmx5mm

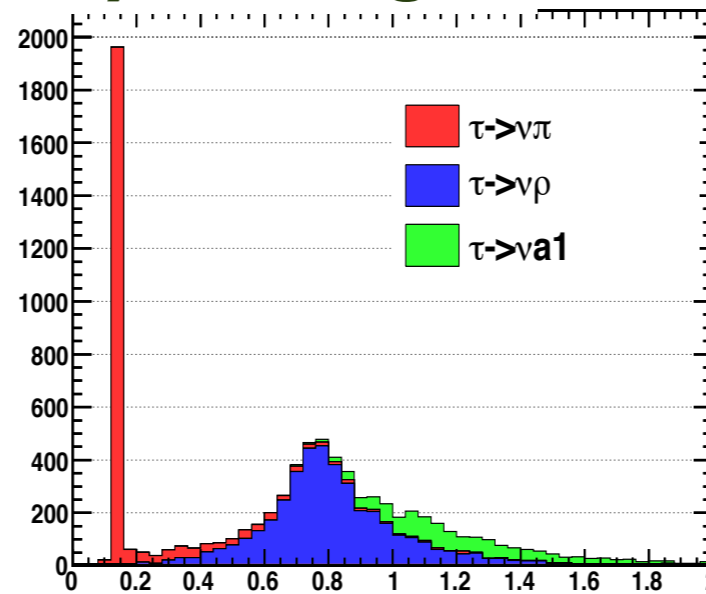


- Alternative Single layer Hybridならゴーストヒットは生じないはずだが、

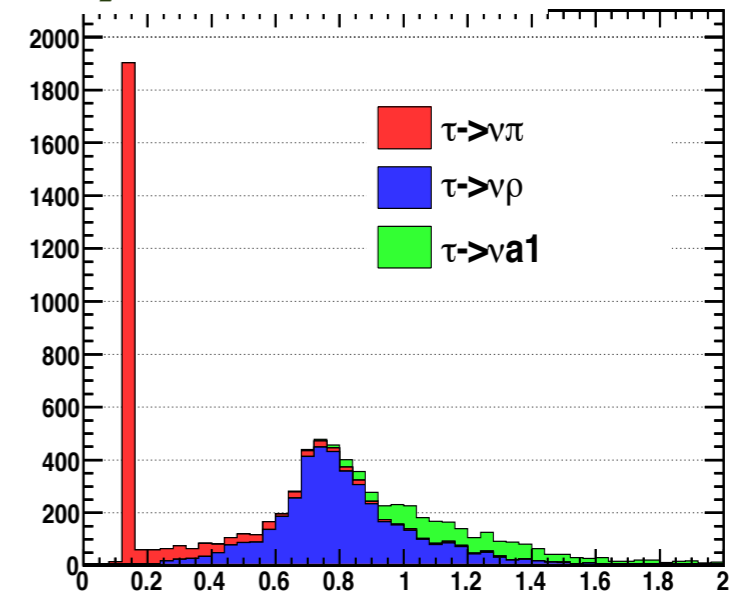
Si ECAL



Hybrid Single

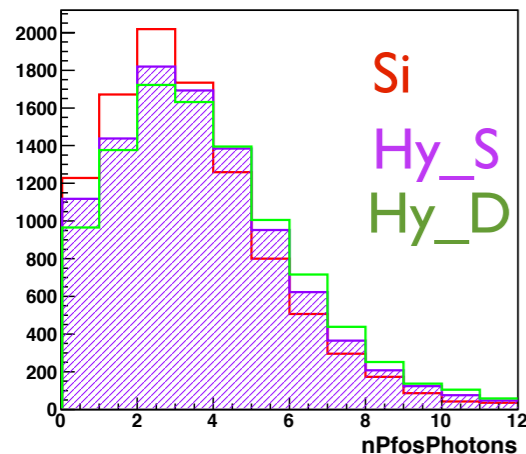


Hybrid Double



Invariant Mass [GeV]

γ s @TT

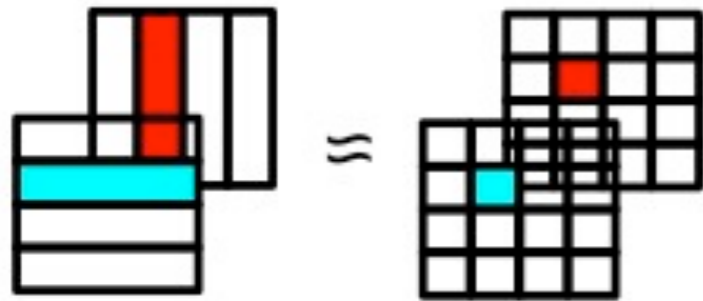


π モードの広がり (余計な γ) 少し抑えられたが、
 まだ、 $\pi\rho$ ともにSi ECALくらいの精度には達していないように思われる。

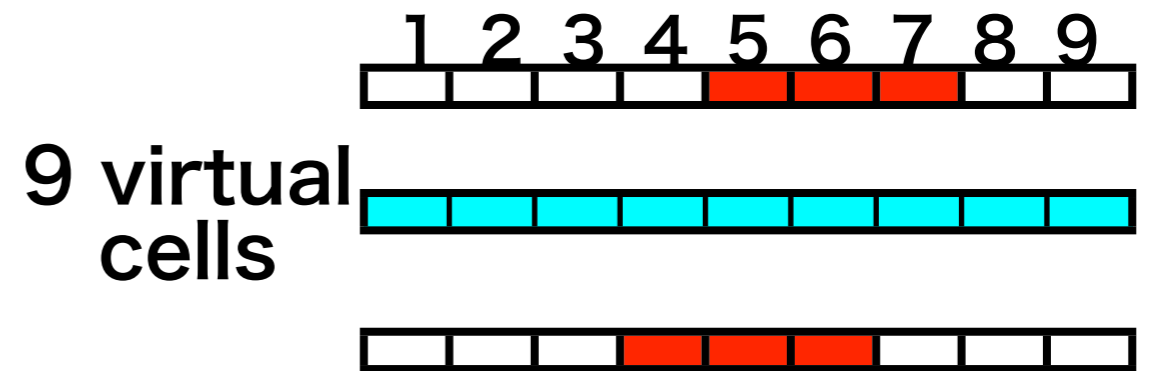
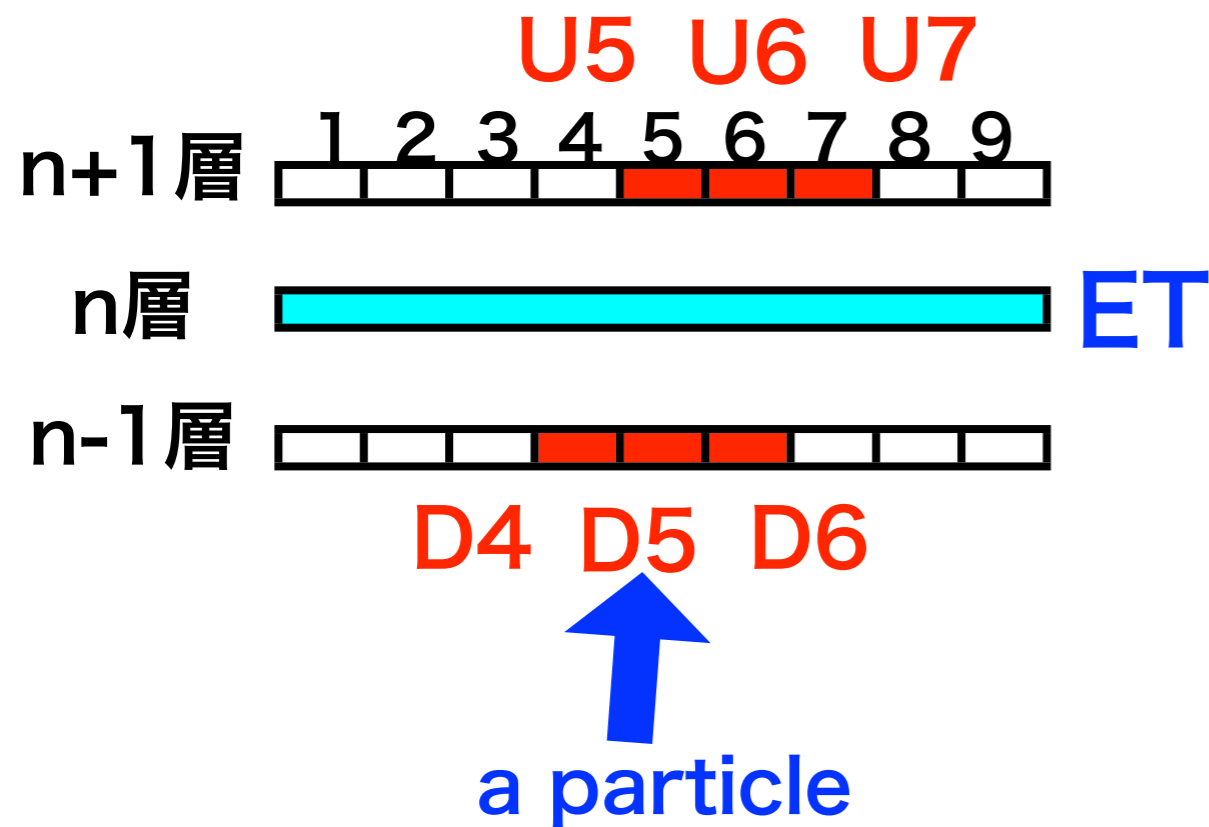
→ SSAが上手く動いていない？

Back Up

Strip Ecal reconstruction with the strip splitting algorithm

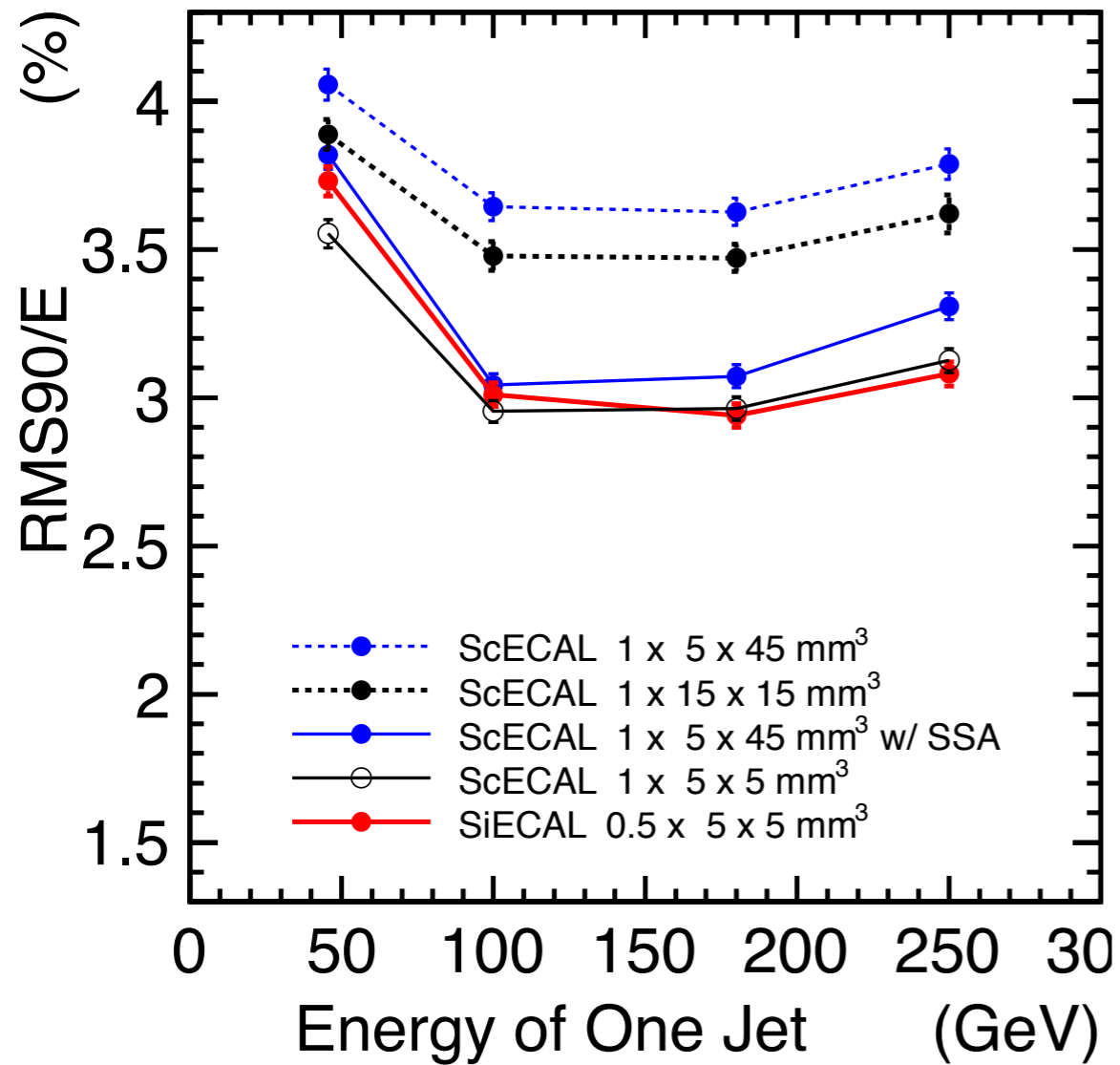


deposited energy on a strip delivered into virtual square cells

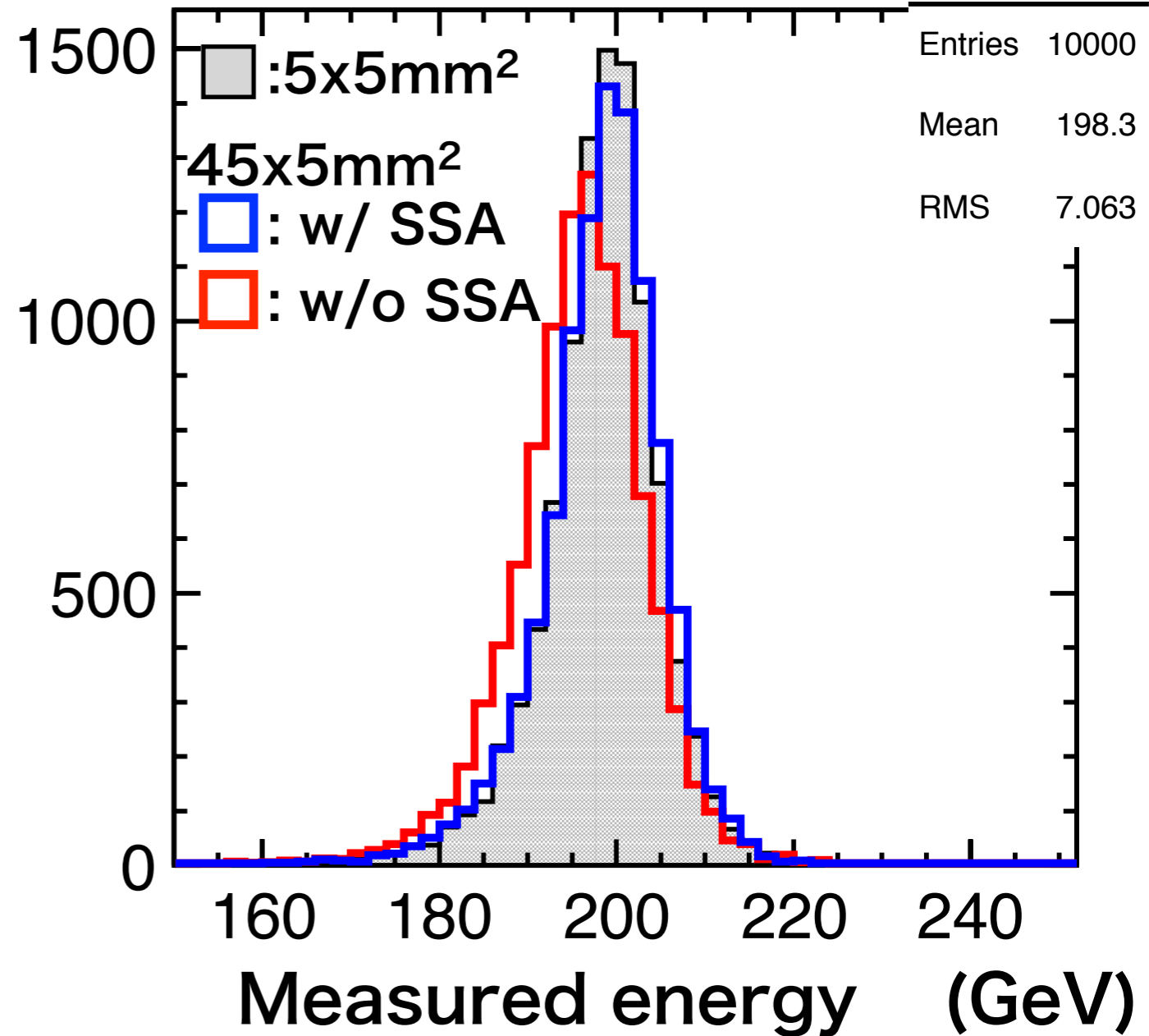


Effect of SSA

$$Z' \rightarrow q\bar{q} \quad q = u, d, s$$



total pfo energy



$\cos(\theta_{\text{Thrust}}) < 0.7$ (Barrel)

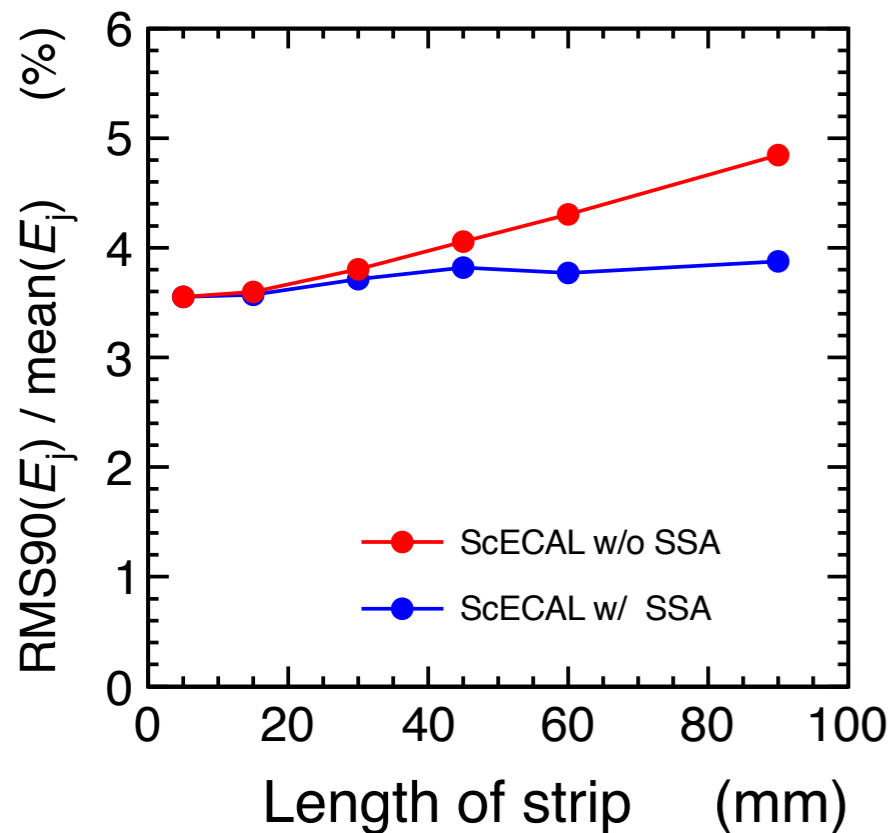
RMS90: RMS of 90% of center events

SSA makes JER of strip ECAL close to 5 x 5 mm² tile ECAL 17

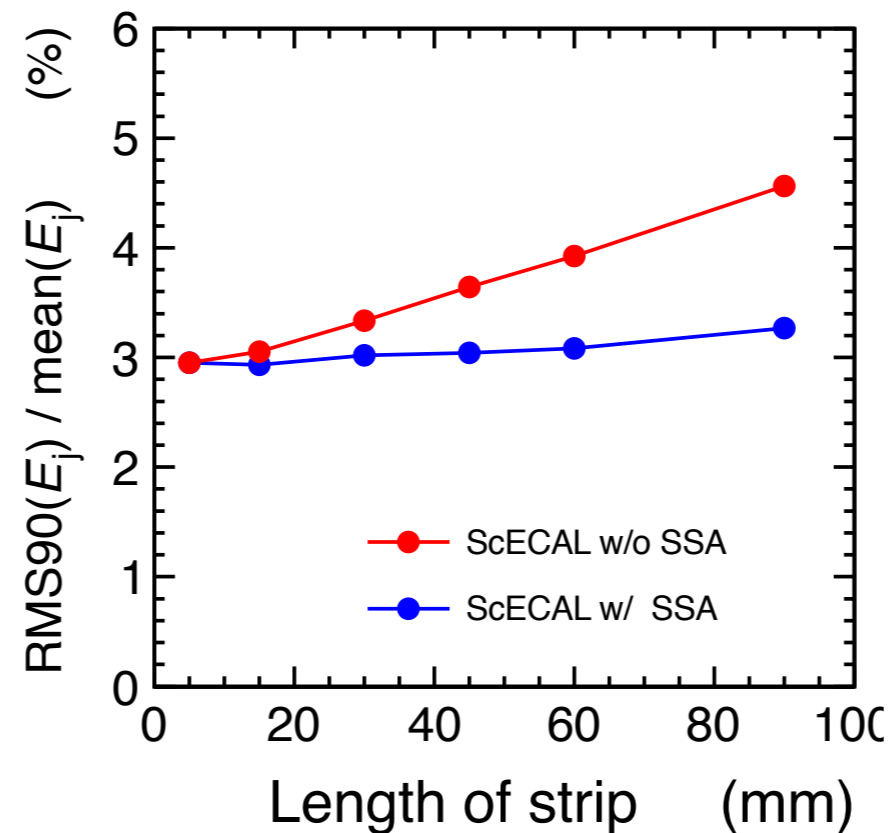
Study two Jet Energy Resolution

depending on the strip length

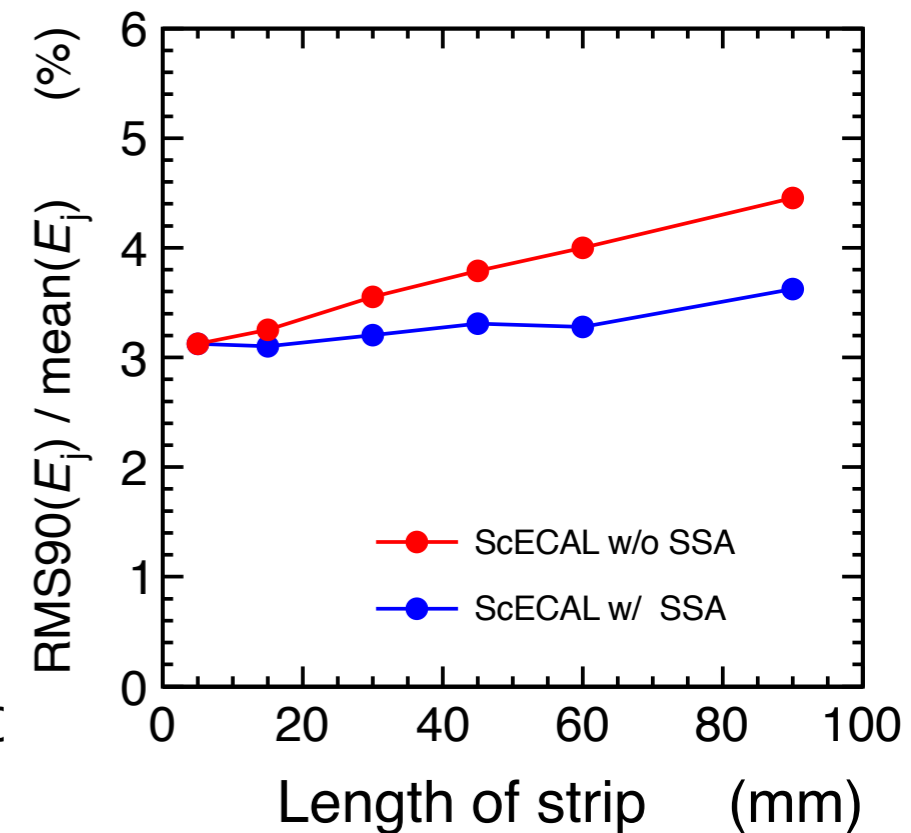
45 GeV



100 GeV

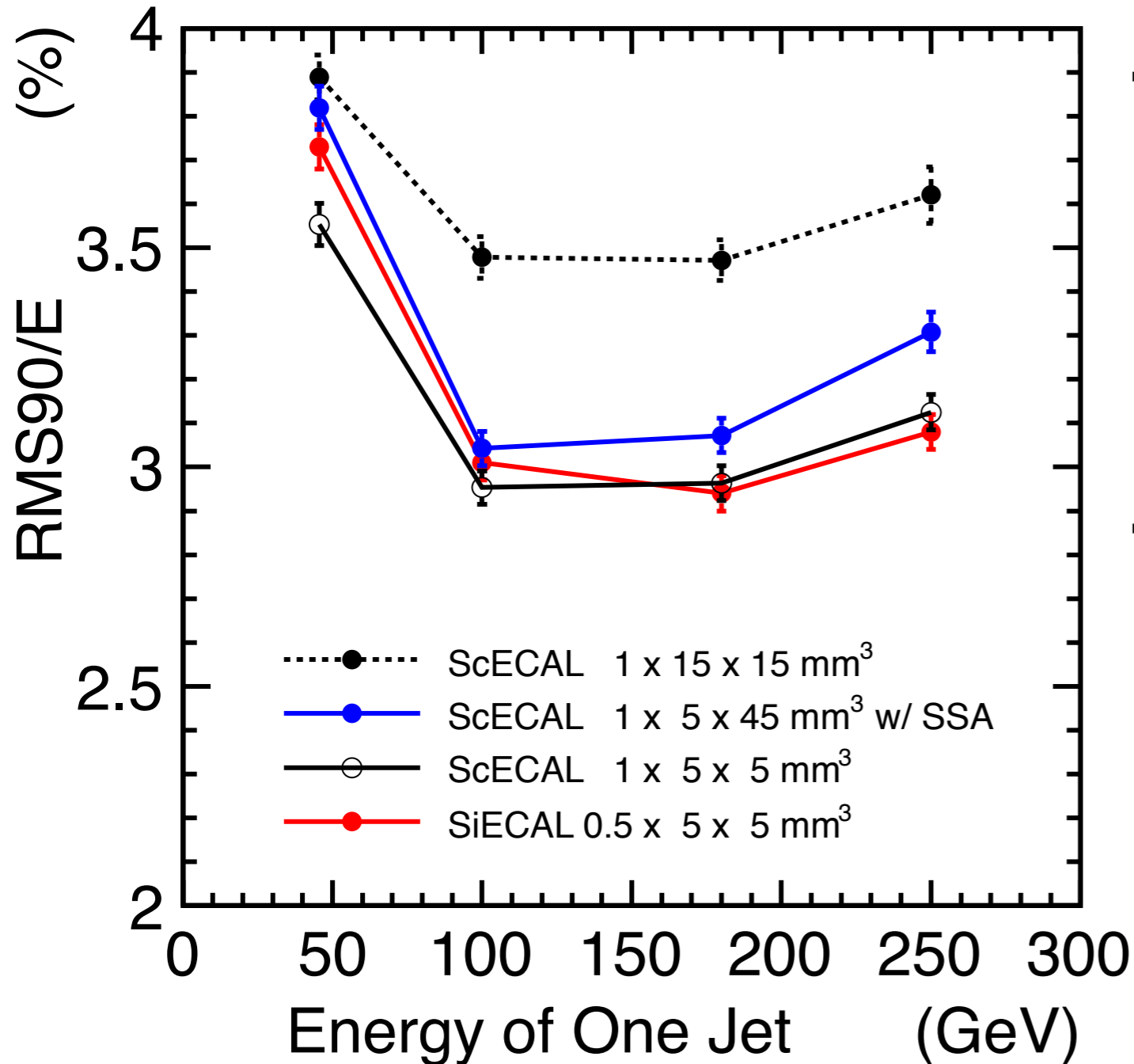


250 GeV



- No large deterioration with increasing the strip length up to 60 mm after applying SSA.

a little more detail

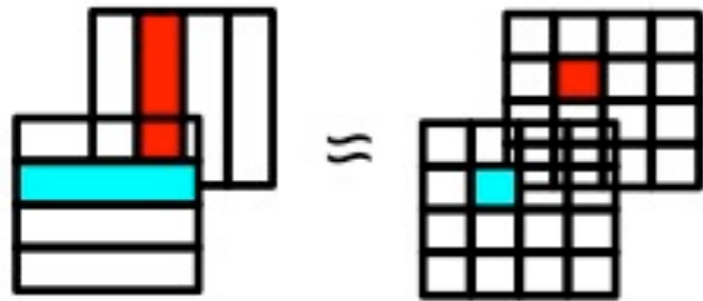


- 5 x 5 mm² tile ScECAL and SiECAL are comparable with each other by John's study. ● ○

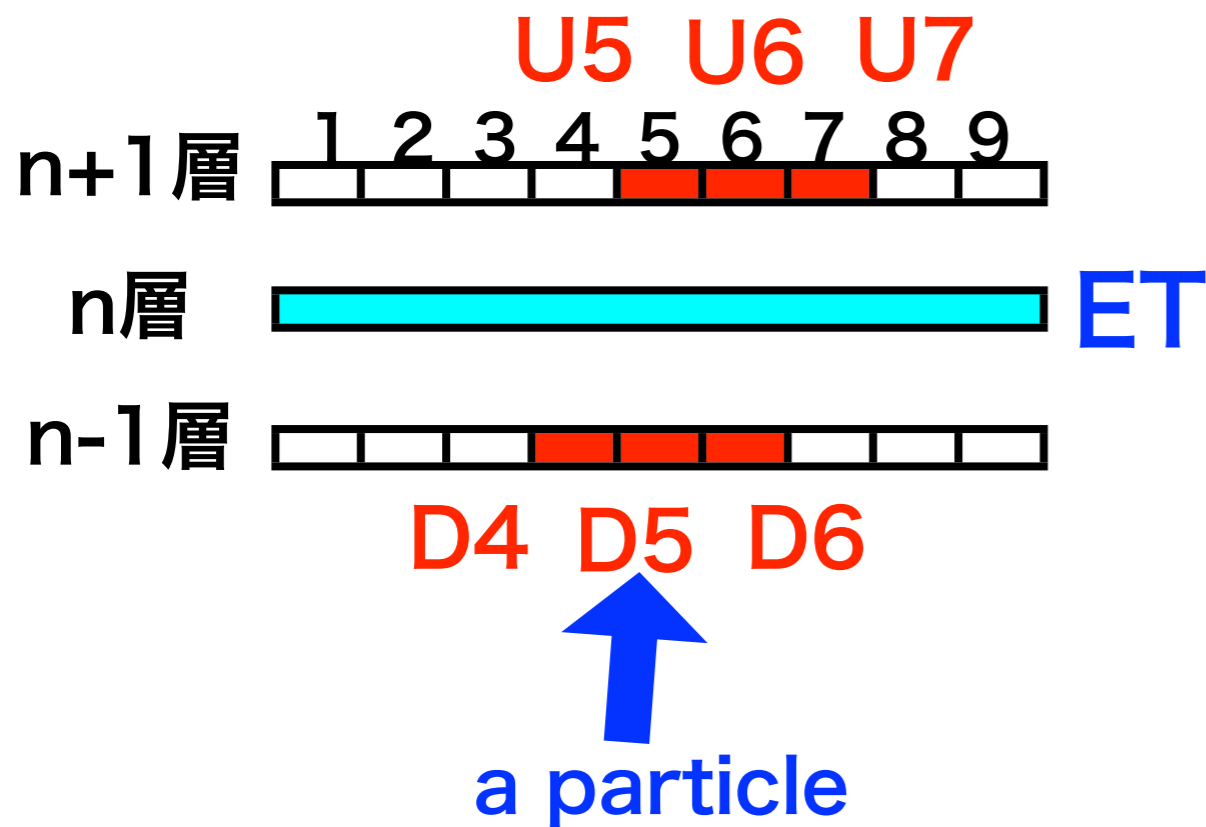
- difference between 5 x 5 mm² ScECAL and 45 x 5 mm² + SSA ScECAL are 0.3% maximum at 45 GeV jet and 0.1-0.2% up to 250 GeV jet. ● ○

What happens at 45 GeV and high energy jets?

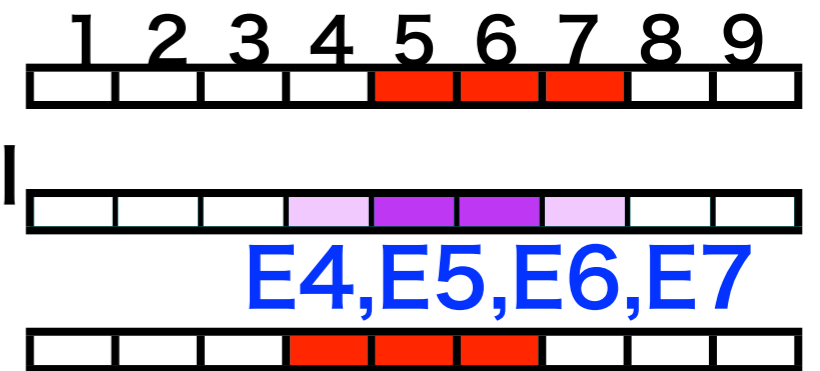
Strip Ecal reconstruction with the strip splitting algorithm



deposited energy on a strip delivered into virtual square cells



9 virtual cells

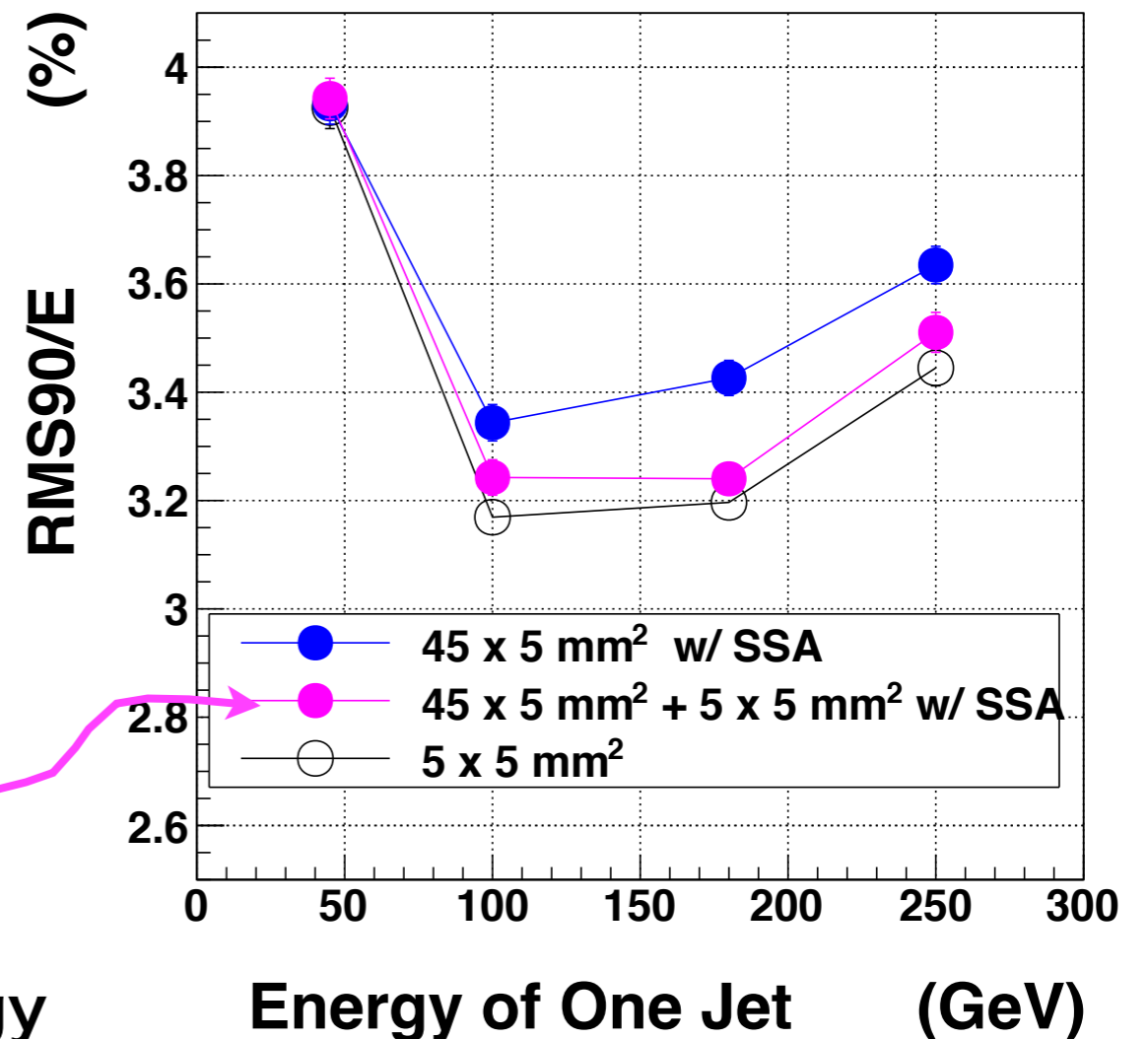
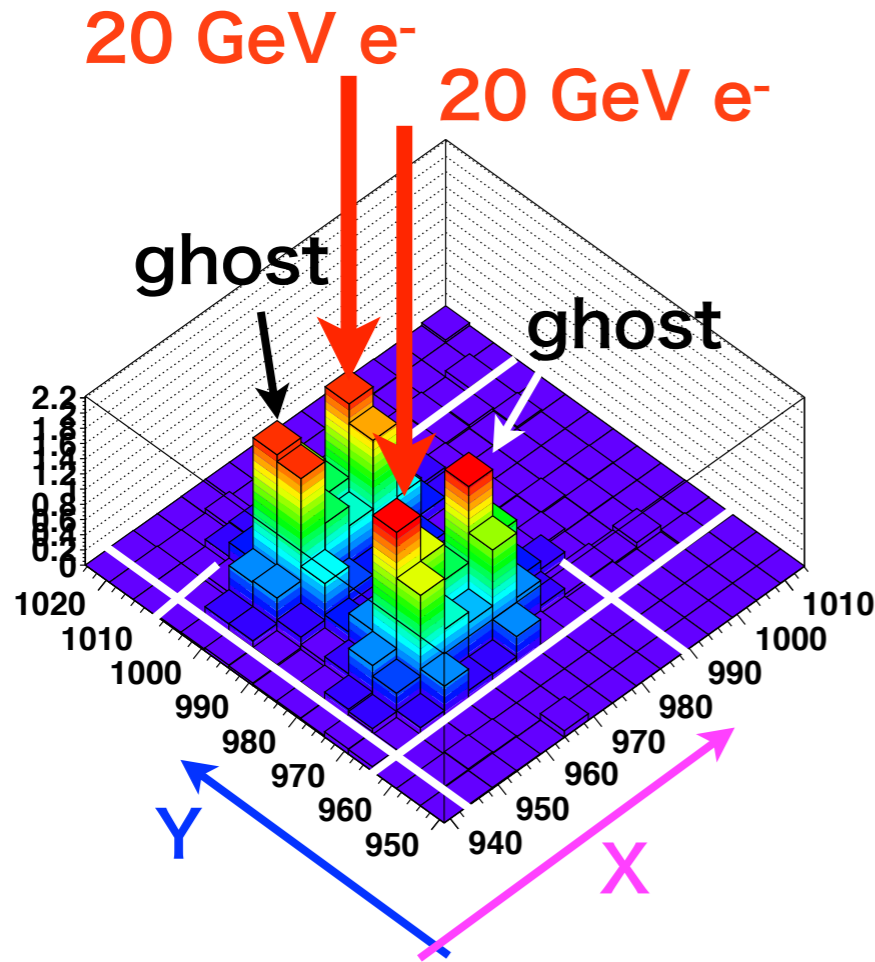


example

$$E5 = ET \times \frac{U5 + D5}{\sum U_j + \sum D_j}$$

positions and energies of all virtual cells are fed into the PandoraPFA program

ghost problem and its solution(1)



Solution

5 x 5 mm² interleaved between strip layers

too small for current technology

Use **Si - layers** for 5 x 5 mm² layers

= Hybrid ECAL

Position

Gravitational center of energy

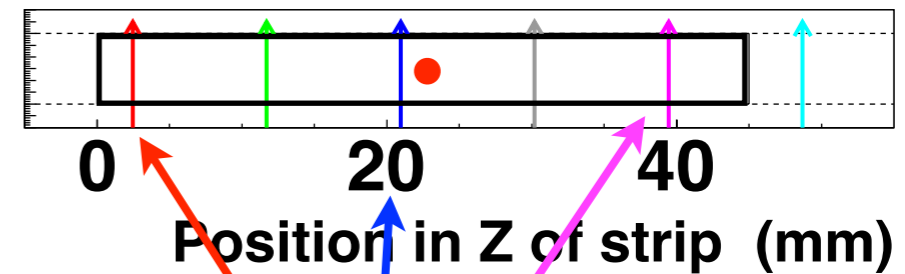
10 GeV photons are injected on the ScECAL of ILD, changing injection position w.r.t. a scintillator of the first layer.

Black hatched:
reconstructed PF object
with SSA, not depend on
injection position.
Position resolution is
~1 mm

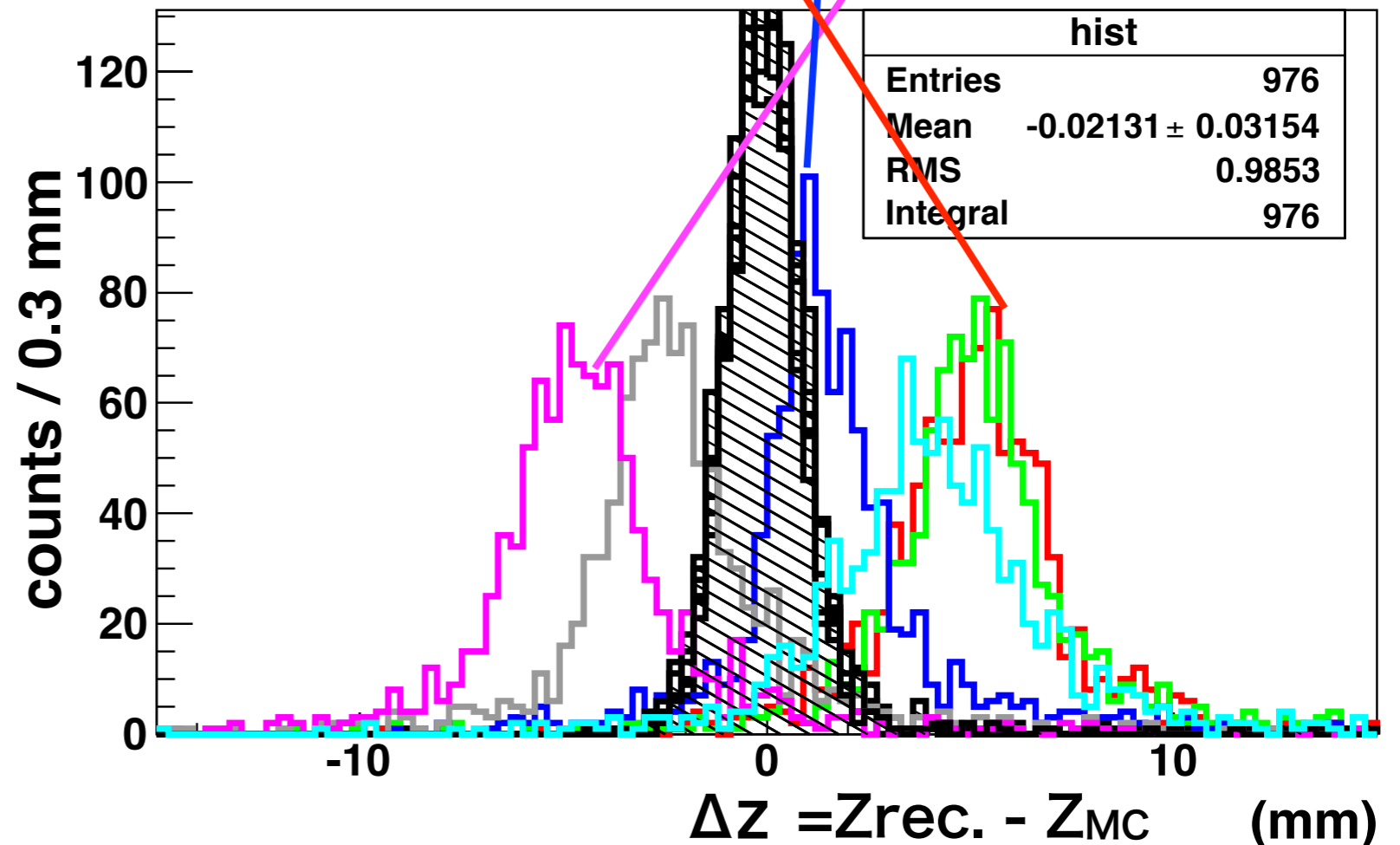
Color lines: without
SSA

Systematic shift is
removed by the SSA

Side view of a scintillator of the first layer and injection point of photons



Distance btw. position of re-constructed PFO and MC true in z.



π , ρ , & a_1 mass in 4ECals with MyCut

- それぞれのECALにおいて、 τ のモードの質量分布。(※ π は γ を含ませてReconstruction)

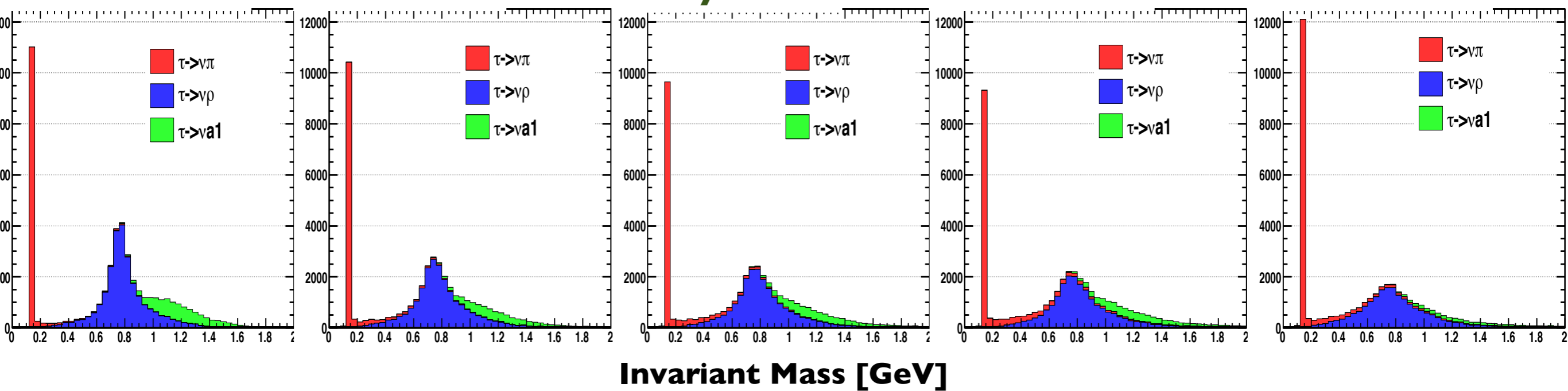
MC Truth

Si ECAL

Hybrid

Sc SSA

Sc ECAL



- SSAにより π のピークが減り、横に広がった。

→ SiECALでは、 π の質量でそんなに広がっていない。

SSAのゴーストヒットによる、 γ フラグメントを含んだと思われる。

- Alternative double layer Hybridでも、まだゴーストヒットによる γ のフラグメントが生成しているように思われる。

→ PFA Cone-Clusteringの拡張により、性能改善の必要。

→ Alternative single layer Hybridを用いればSiECALと同じ分割能力が期待できる。

Mode selection with MyCut

- The efficiency and the purity

- Efficiency with MyCut

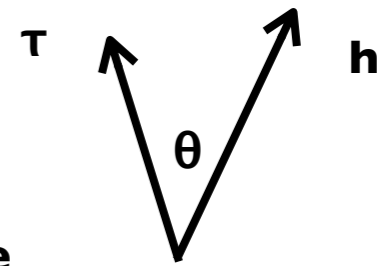
$$\text{efficiency} = \frac{\text{カットベースで選ばれたモード}}{\text{イベント数} \times \tau \times \text{Bratio}}$$

e-L, e+R	MCtrue	Si Ecal	Hybrid	Sc SSA	Sc Ecal
$\tau \rightarrow e\nu\nu$	98%	89%	90%	90%	67%
$\tau \rightarrow \mu\nu\nu$	99%	93%	93%	92%	89%
$\tau \rightarrow \pi\nu$	105%	113%	115%	125%	140%
$\tau \rightarrow \rho\nu$	102%	91%	88%	84%	78%
$\tau \rightarrow a_1\nu(l\rho)$	102%	78%	82%	80%	43%

→ MCtrueでの Efficiencyは100%近い、Cutに大きな問題なし。

- purity with MyCut

Polarization observable I



- The main observable is angle θ in τ rest-frame.

- Since the neutrino is not observed, the angle θ cannot be reconstructed completely.

- In the lab frame the angle θ is related to energy fraction x carried by ...

- Hadronic system : **linear function**

$$\cos\theta^* (= \omega) \approx 2x - 1 \rightarrow \text{this is an optimal observable } \omega$$

$$\pi \text{ mode : } x = E_\pi / E_\tau$$

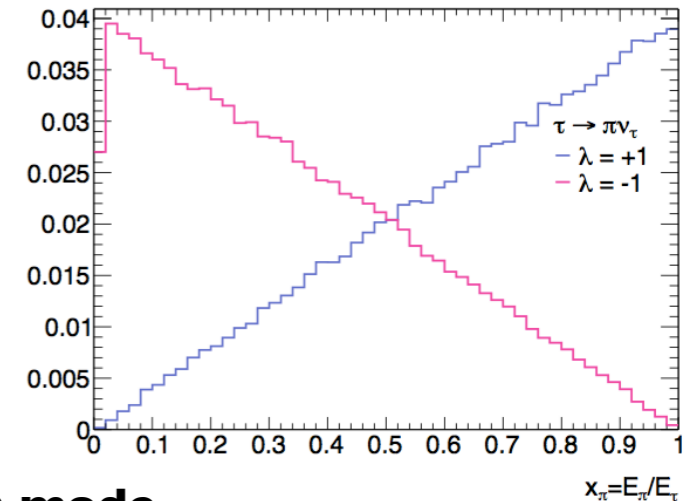
$$\rho \text{ mode : } x = E_\rho / E_\tau$$

- leptonic system :

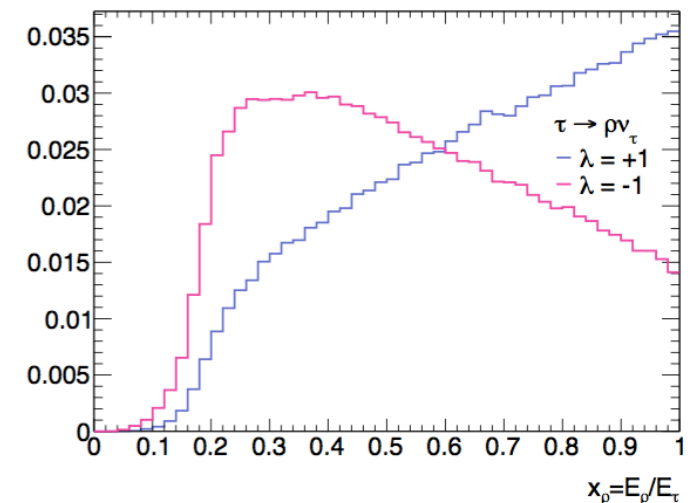
- there are two neutrinos in the final state which makes this decay channel less sensitive to the tau helicity than the hadronic channels.

$$\omega = \frac{1 + x - 8x^2}{5 + 5x - 4x^2}$$

• π mode

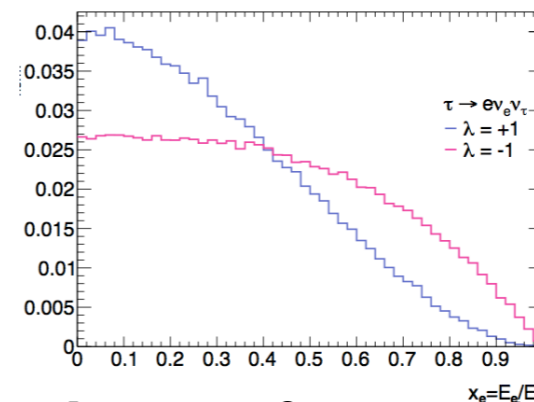


• ρ mode



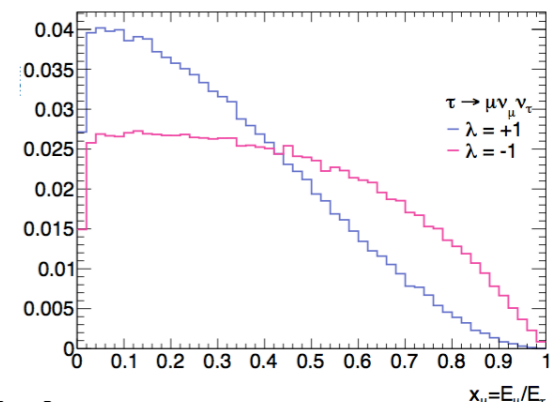
-1 0 1 (ω)

• e mode



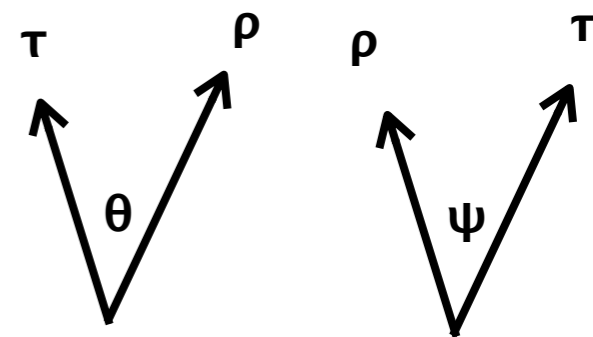
-1 0 1 (ω)

• μ mode



$x_\mu = E_\mu / E_\tau$

Polarization observable 2 (ρ mode)



- Recover optimal observable ω with $\cos\psi^*$ in ρ mode. (BackUp Slides)

- A lot of sensitivity of the polarization is lost compared to the π decay.

→ due to the mixing of longitudinally and transversely polarized vector states.

- Some of the sensitivity can be regained by considering other variables are sensitive to the tau helicity.

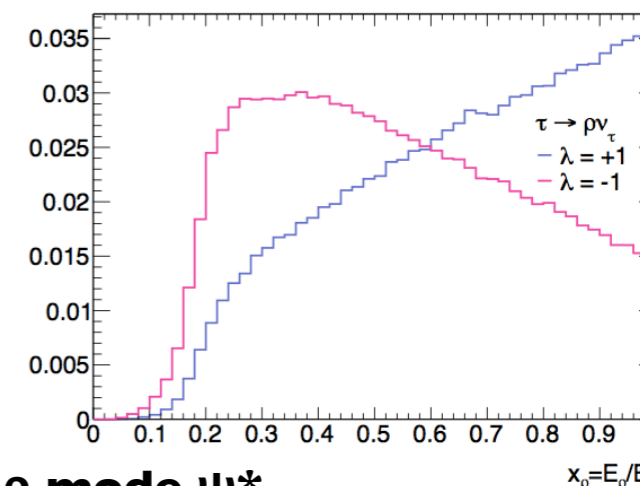
- If one uses information of helicity of intermediate resonance, most of lost sensitivity can be regained.

→ Define ψ as the angle between the charged π and the ρ initial direction

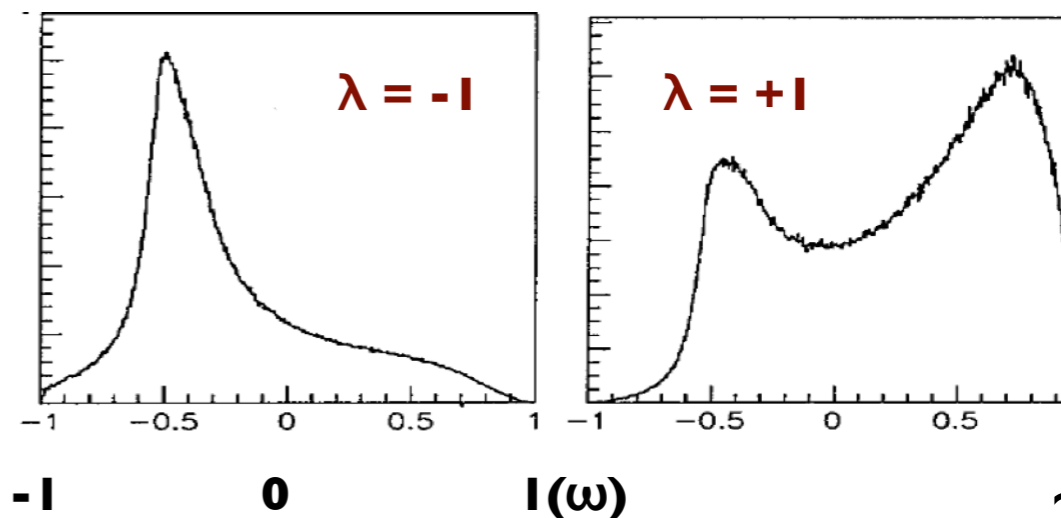
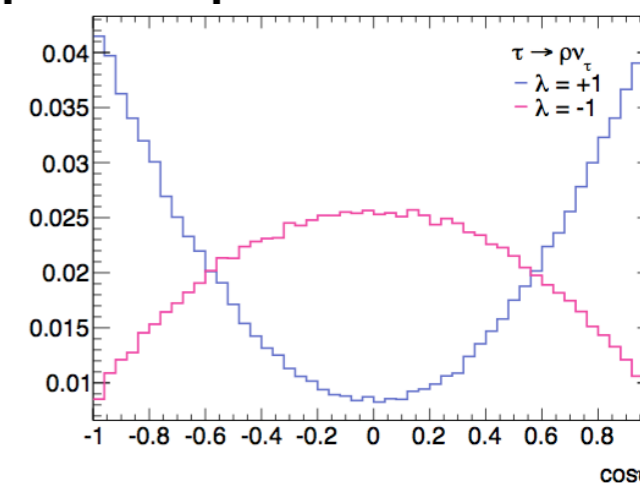
- In terms of the laboratory frame

$$\cos\psi^* = (\mathbf{E}\pi_{\pm} - \mathbf{E}\pi_0) / E\rho$$

- ρ mode θ^*



- ρ mode ψ^*



Angular dist (ω) : ρ mode

- In case of recovering ω with $\cos\psi^*$.

P(τ) Result

P(τ)	MCtrue	Si Ecal	Hybrid	Sc SSA	Sc Ecal
e-L e+R	51%	40%	42%	43%	33%
e-R e+L	52%	52%	47%	47%	38%

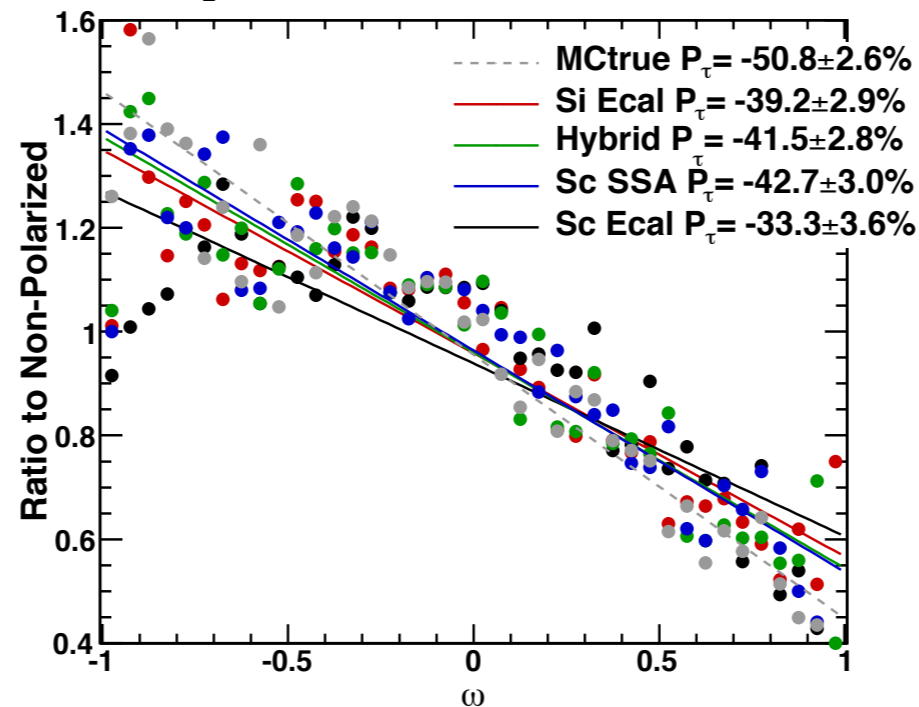
ω distribution

→ ω distribution divided by non-polarizing sample

and Linear fit is applied to obtain P(τ) value.

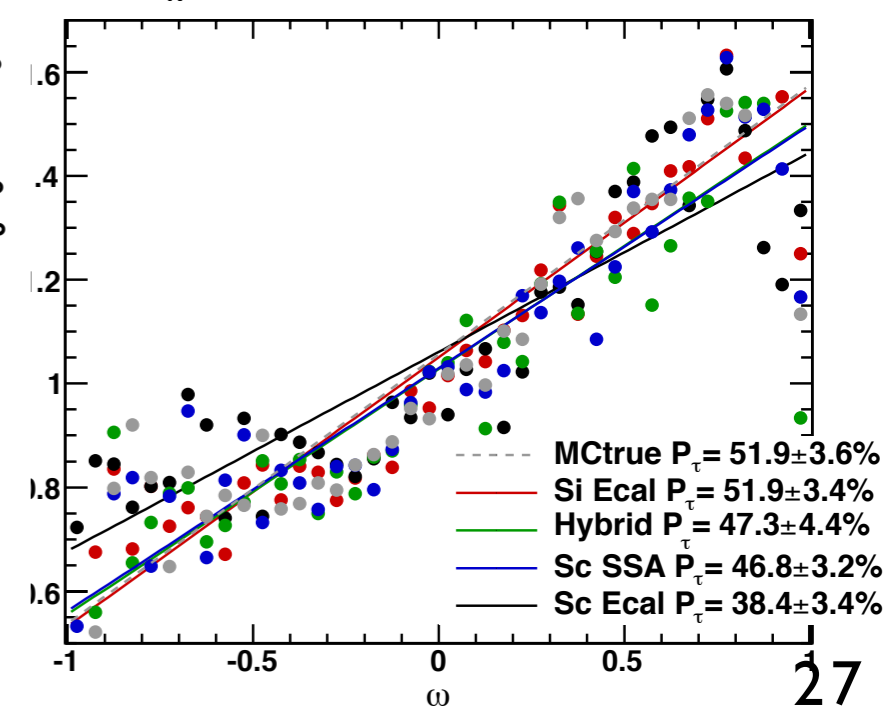
P(τ) LR

ρ mode ($e_L^-, e_R^+ = 80\%, 30\%$)



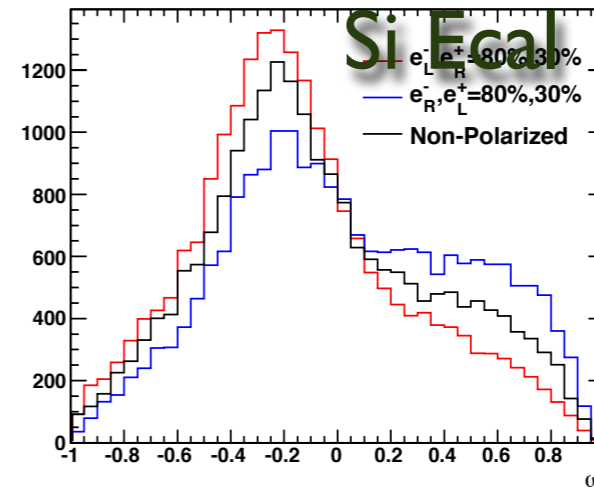
P(τ) RL

mode ($e_R^-, e_L^+ = 80\%, 30\%$)

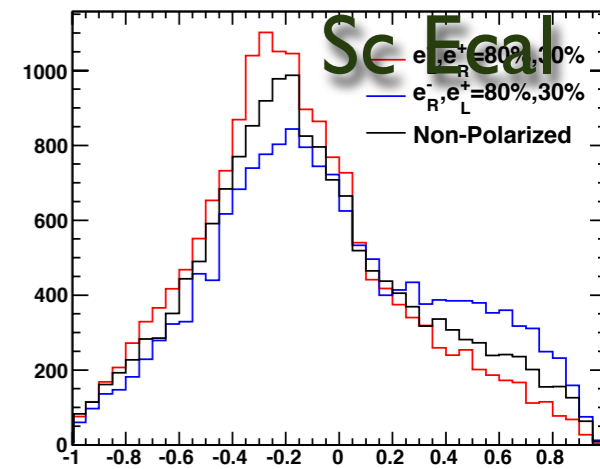
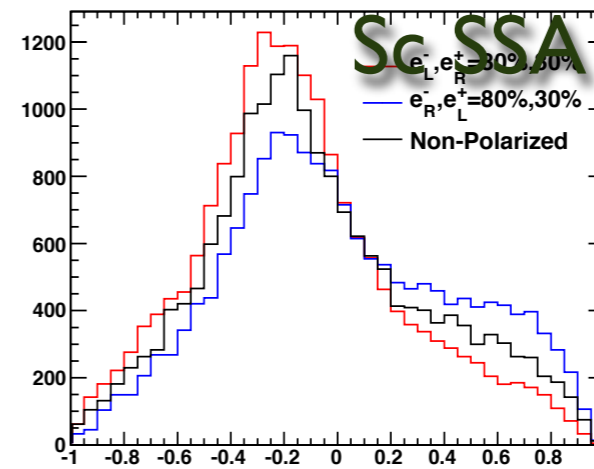
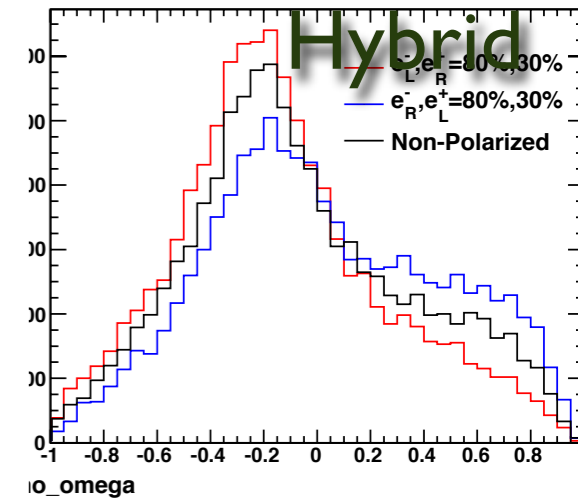


ω distribution

Si Ecal ρ mode ω



io_omega



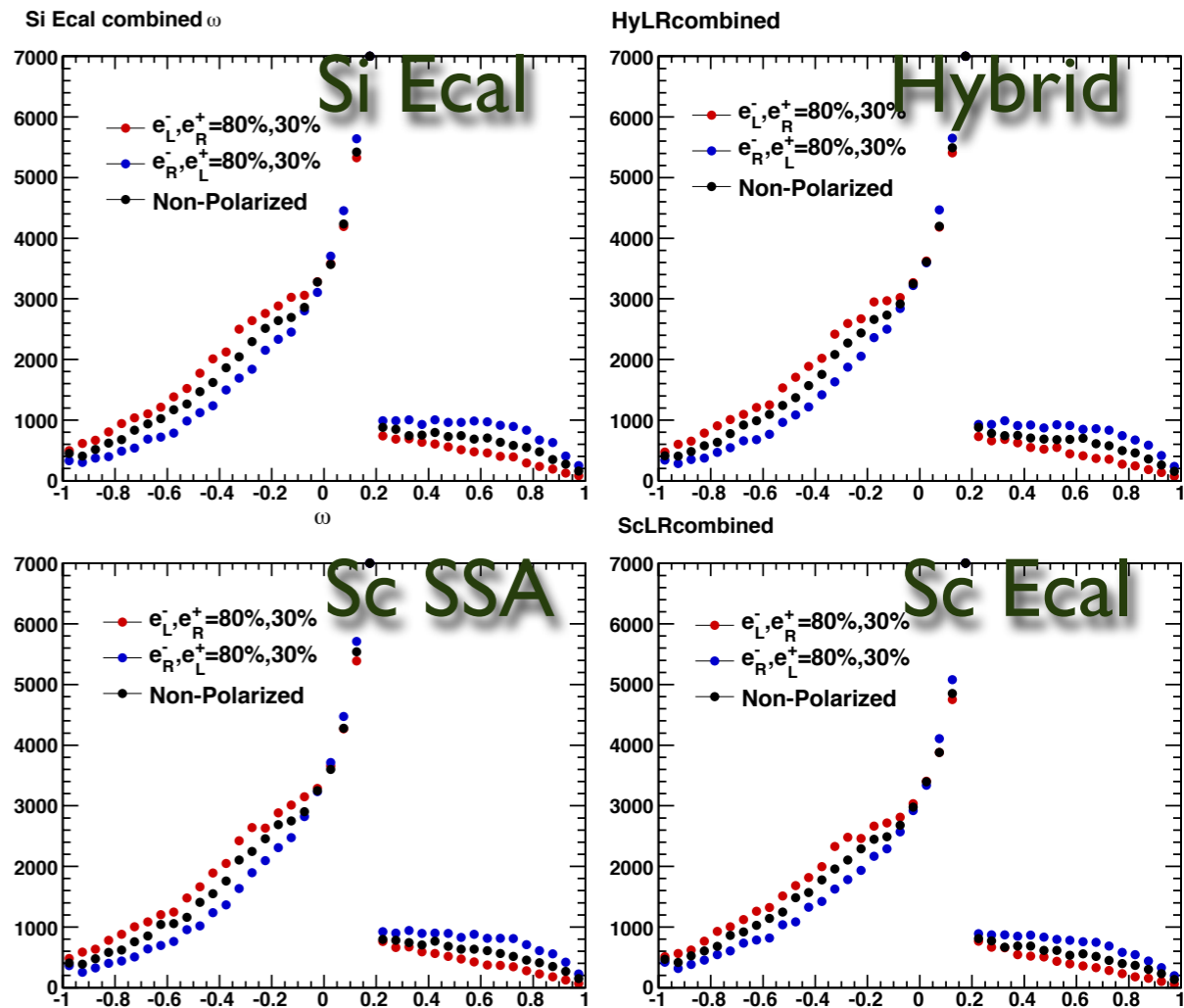
Angular dist (ω) : combined ω

- Distribution of the polarization observable after summing up all decay modes.
- ω distribution divided by non-polarizing sample.

• P(τ) Result

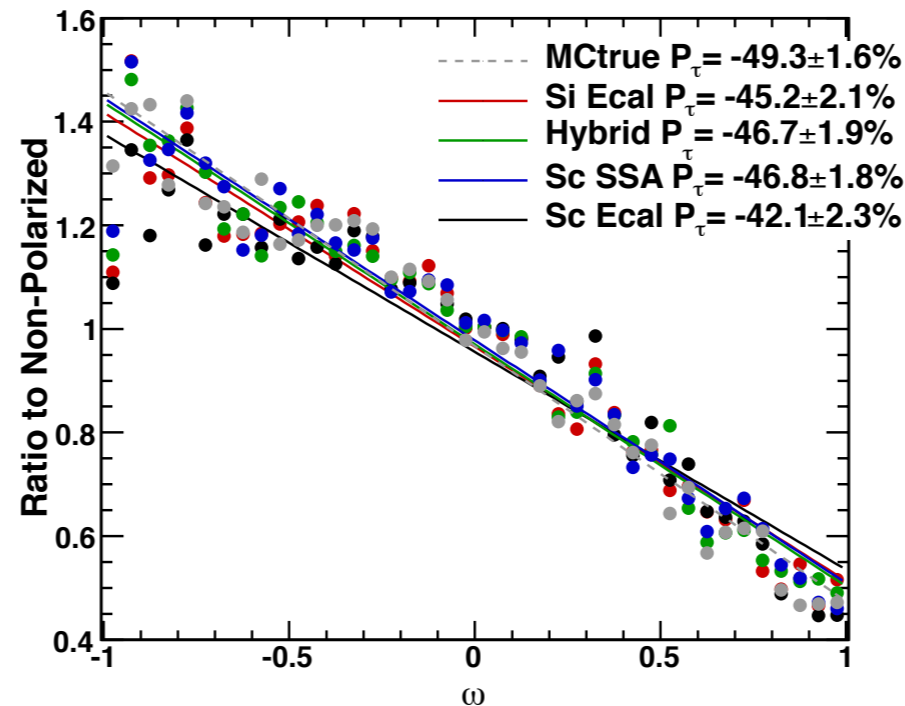
P(τ)	MCtrue	Si Ecal	Hybrid	Sc SSA	Sc Ecal
e-L e+R	49%	45%	47%	47%	42%
e-R e+L	57%	52%	50%	51%	45%

• ω distribution



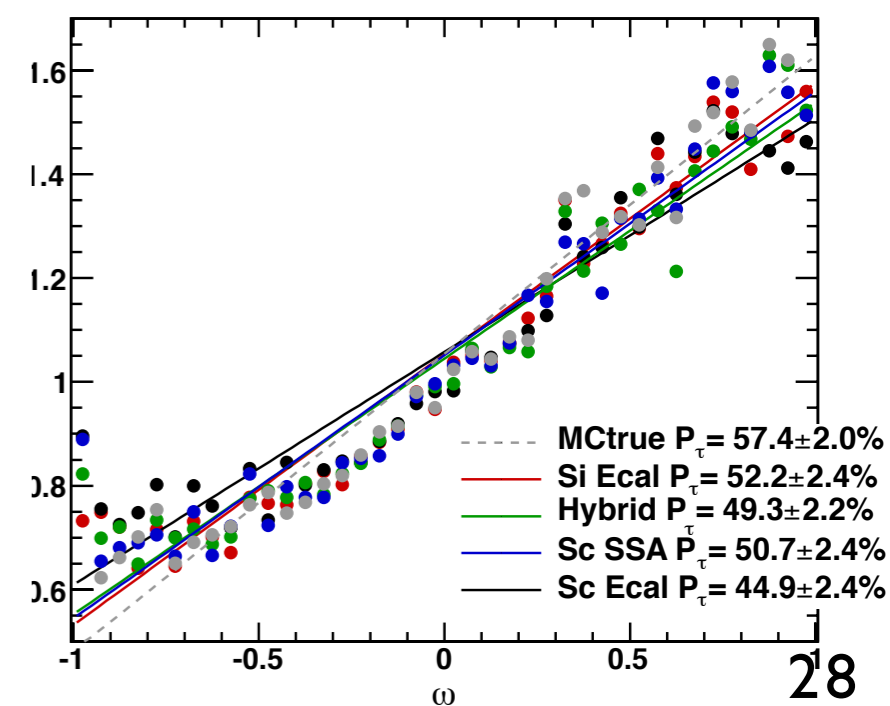
• P(τ) LR

$e^- \mu^- \pi^+ \rho^-$ combined ω ($e_L^-, e_R^+ = 80\%, 30\%$)



• P(τ) RL

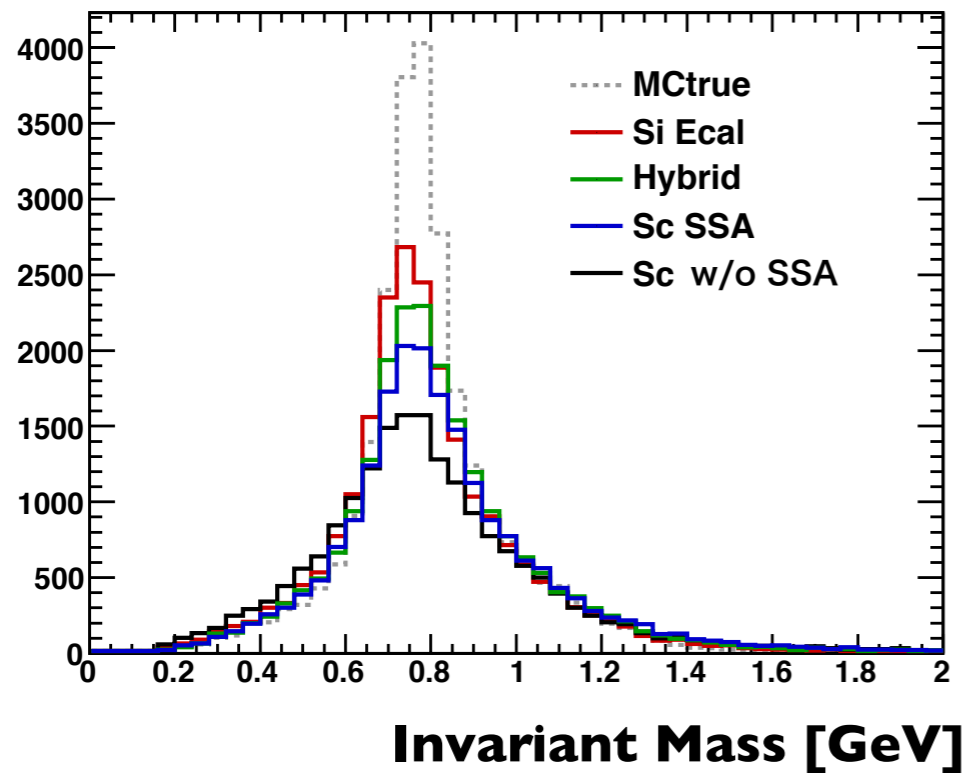
$e^- \mu^+ \pi^- \rho^+$ combined ω ($e_L^-, e_R^+ = 80\%, 30\%$)



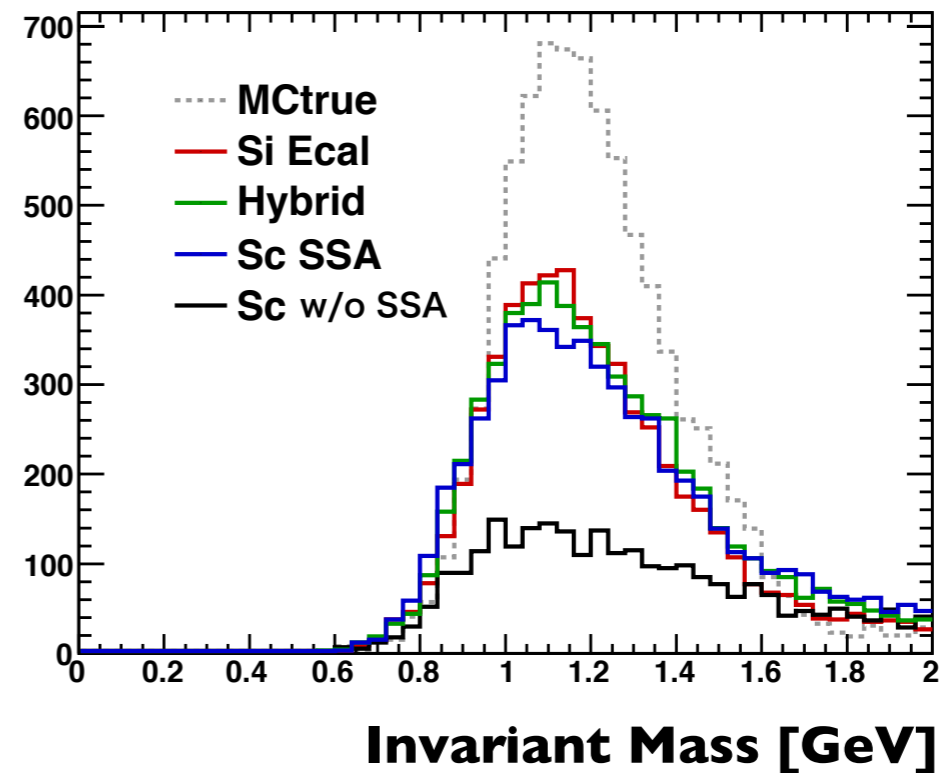
ρ , π^0 & a_1 Mass in 4ECALs with MyCut

- Mass of ρ and a_1

4Detectors ρ mass



4Detectors a_1 mass



- ρ reconstruction

performance of reconstruction: Si ECAL > Hybrid Sc w/ SSA > Sc w/o SSA

- a_1 reconstruction

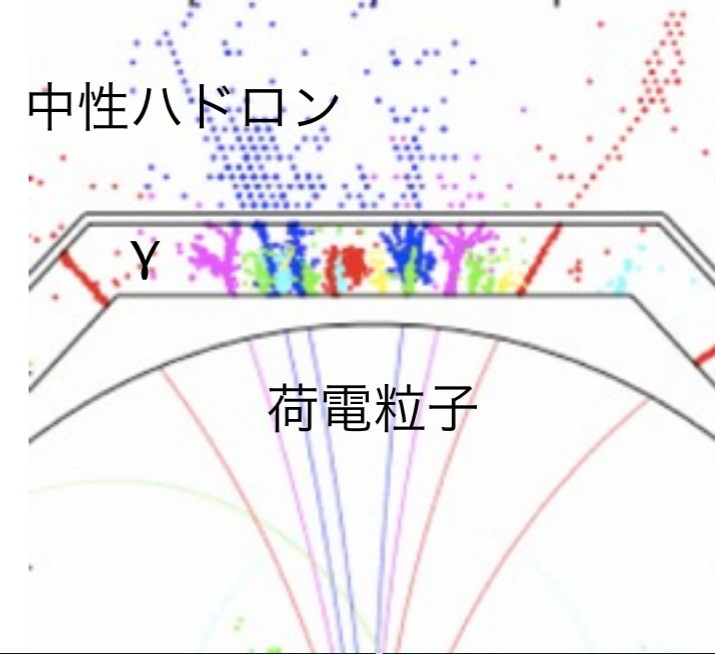
SSA drastically improve a_1 reconstruction

There is no large difference between Ecal types except Sc w/o SSA.

Introduction (ILD ECAL)

- PFAを用いて最高の性能を目指す

Jetを構成する粒子のうち、荷電粒子はtrackerで、 γ はEMCALで、中性ハドロンはHCALで測定する



- Jet Energy Resolution

終状態は、ほぼジェット:

$ee \rightarrow \nu\nu WW / \nu\nu ZZ$ の4jet eventにおいて、質量分解能が、自然幅($\sim 2\text{GeV}$)程度になること

→ $\sigma_{E_{\text{jet}}} / E_{\text{jet}} = 3\sim 4\%$
($30\% / \sqrt{E_{\text{jet}}}$ below 100GeV)

- カロリメータの非常に細かいセグメント化

(- 粒子間隔を広げるための大きな半径と強い磁場 ($d \sim BR^2$))

- ILD ECAL測定器への要求

- 要求されるGranularity:

1cm^2 またはそれ以下のセグメント化 → PFAへの最適化

- 要求されるEnergy Resolution (単粒子に対して): $15\% / \sqrt{E}$

