HIGGS COMPOSITENESS: CURRENT STATUS AND FUTURE STRATEGIES

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CERN & EPFL Lausanne

CERN Theory Colloquium - 4 December, 2013

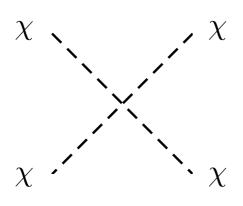
Outline

- Strong vs Weak EWSB
- Current Status of Higgs Compositeness:
 - 1. Higgs mass
 - 2. EW Precision Tests
 - 3. Impact of Searches for top partners
 - 4. Impact of data on Higgs couplings

Future Strategies

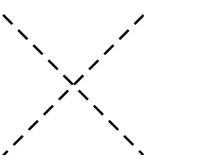
Strong vs Weak EWSB

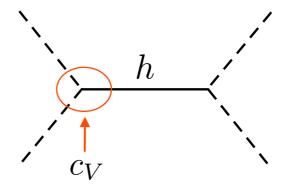
In the
$$\{SM-H\}$$



$$A(W_L W_L \to W_L W_L) = A(\chi \chi \to \chi \chi) \sim \frac{E^2}{v^2} \equiv g^2(E)$$

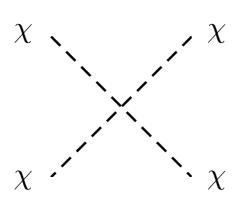
In the $\{SM-H\} + H$





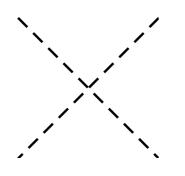
$$A \sim \frac{E^2}{v^2} (1 - c_V^2) - c_V^2 \frac{m_h^2}{v^2} \frac{s}{s - m_h^2}$$

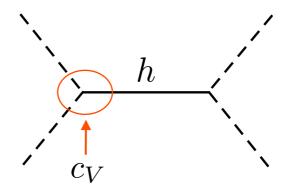
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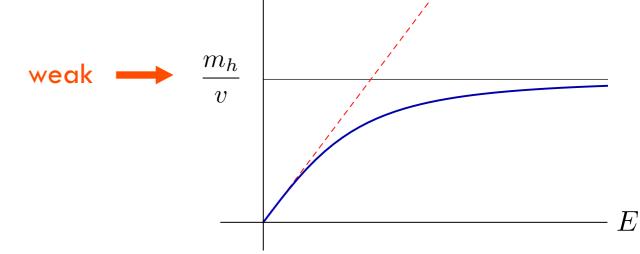




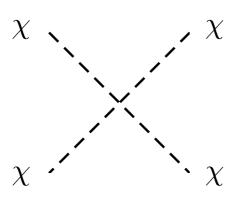
$$A \sim \frac{E^2}{v^2} (1 - c_V^2) - c_V^2 \frac{m_h^2}{v^2} \frac{s}{s - m_h^2}$$

Elementary Higgs:

$$c_V = 1$$

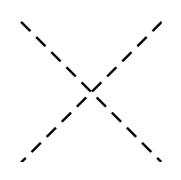


In the $\{SM-H\}$



$$A(W_L W_L \to W_L W_L) = A(\chi \chi \to \chi \chi) \sim \frac{E^2}{v^2} \equiv g^2(E)$$

In the $\{SM-H\} + H_i$



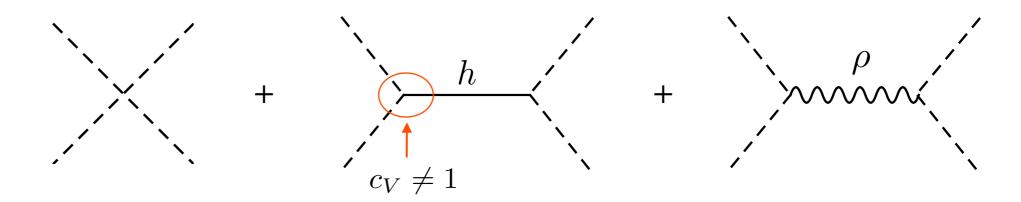
$$h_i$$

$$A \sim \frac{E^2}{v^2} \left(1 - \sum_i c_{Vi}^2 \right) + \dots$$

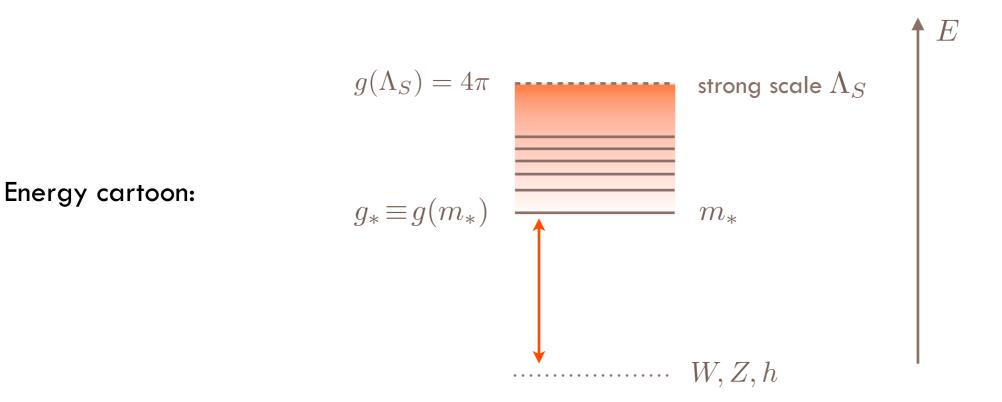
Elementary Higgses: (more than one)

- $\delta c_{Vi} \sim O(1)$ possible
- $\qquad \qquad \text{sum rule:} \qquad \sum_{\cdot} c_{Vi}^2 = 1$





coupling strength grows with energy and saturates at $\,g_* \lesssim 4\pi\,$



$$h \leftrightarrow \sigma$$

Q: why light and narrow?

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Q: why light and narrow?

A: the Higgs is itself a (pseudo) NG boson

Georgi & Kaplan, '80 Kaplan, Georgi, Dimopoulos

ex: $\frac{SO(5)}{SO(4)}$ \rightarrow 4 NGBs transforming as a (2,2) of SO(4)~SU(2)_LxSU(2)_R

Agashe, RC, Pomarol NPB 719 (2005) 165

$$f^{2} \left| \partial_{\mu} e^{i\pi/f} \right|^{2} = (\partial \pi)^{2} + \frac{(\pi \partial \pi)^{2}}{f^{2}} + \frac{\pi^{2} (\pi \partial \pi)^{2}}{f^{4}} + \dots$$

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Giudice et al. JHEP 0706 (2007) 045

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1. $O(v^2/f^2)$ shifts in tree-level Higgs couplings. Ex: $c_V = 1 - c_H \left(\frac{v}{f} \right)^2 + \dots$

Analogy with
$$\pi\pi$$
 scattering in QCD:

$$h \leftrightarrow \sigma$$

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Giudice et al. JHEP 0706 (2007) 045

2. Scatterings involving the Higgs also grow with energy

$$A(WW \to hh) \sim \frac{s}{v^2}(c_V^2 - c_{2V})$$

Linear couplings

D.B. Kaplan NPB 365 (1991) 259

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RS with bulk fermions

Hypothesis: each SM fermion couples to a composite fermionic operator with the same SU(3)_cxSU(2)_LxU(1)_Y quantum numbers

$$\mathcal{L} = \lambda_L \, \bar{q}_L O_R + \lambda_R \, \bar{u}_R O_L + h.c.$$

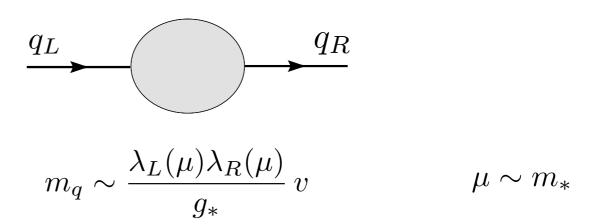
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Quark masses need two such couplings



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Quark masses need two such couplings

$$q_L$$
 q_R

$$m_q \sim \frac{\lambda_L(\mu)\lambda_R(\mu)}{g_*} v$$

$$\mu \sim m_*$$

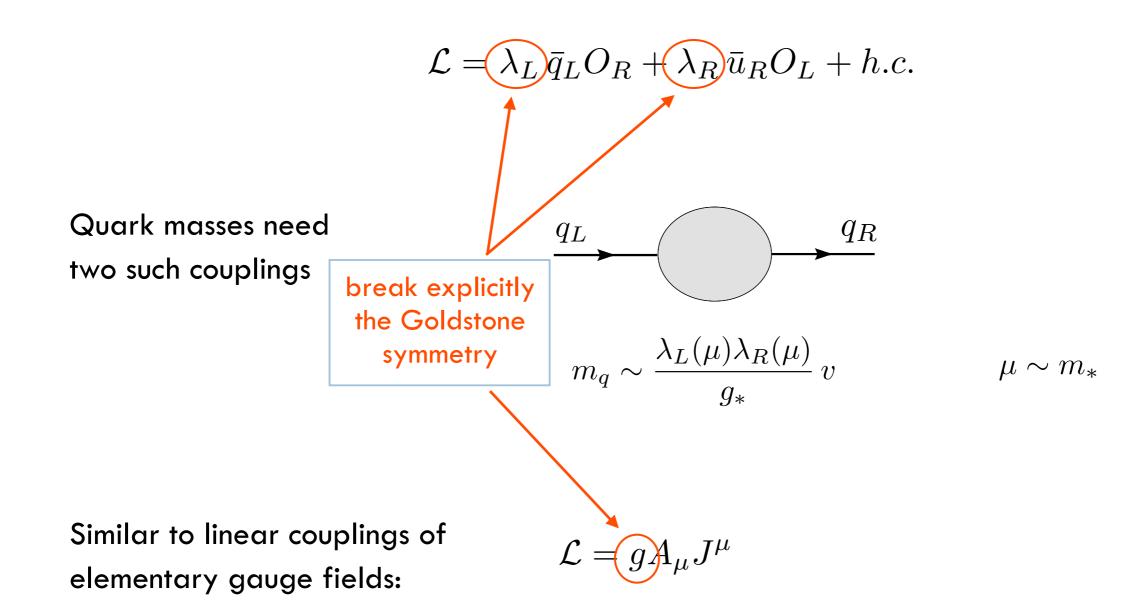
Similar to linear couplings of elementary gauge fields:

$$\mathcal{L} = gA_{\mu}J^{\mu}$$

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Partial compositeness

D.B. Kaplan NPB 365 (1991) 259

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RS with bulk fermions

Fermionic operators can excite composite fermions at low energy:

$$\langle 0|O|\chi\rangle = \lambda f$$

same as for a conserved current:

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Linear couplings imply mass mixings:

$$\mathcal{L} = \bar{\psi} i \partial \!\!/ \psi + \bar{\chi} (i \nabla \!\!\!/ - m_*) \chi + \lambda f \, \bar{\psi} U(\pi) \chi + h.c.$$

rotating to mass eigenbasis:

$$\begin{pmatrix} \psi \\ \chi \end{pmatrix} \to \begin{pmatrix} \cos \varphi & \sin \varphi \\ \sin \varphi & \cos \varphi \end{pmatrix} \begin{pmatrix} \psi \\ \chi \end{pmatrix} \qquad \tan \varphi = \frac{\lambda f}{m_*}$$

 φ parametrizes the degree of compositeness of the SM fermions

$$|SM\rangle = \cos\varphi |\psi\rangle + \sin\varphi |\chi\rangle$$

$$|\text{heavy}\rangle = -\sin\varphi |\psi\rangle + \cos\varphi |\chi\rangle$$

Higgs mass

Can a 125GeV Higgs be composite?

$$V(h) = \frac{m_*^4}{g_*^2} \frac{N_c}{8\pi^2} \left[\lambda^2 \sum_i A_i(h/f) + \lambda^4 \sum_i B_i(h/f) + \dots \right]$$

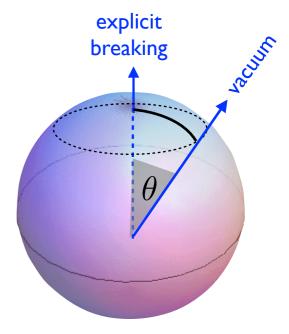
$$h \equiv \sqrt{H^\dagger H}$$

$$A_i(x), B_i(x)$$
 SO(4) structures

ightarrow trigonometric functions: $\sin^2(x)$

 $\sin^4(x)$

:



$$\frac{SO(5)}{SO(4)} = S^4$$
 vacuum manifold is the 4-sphere

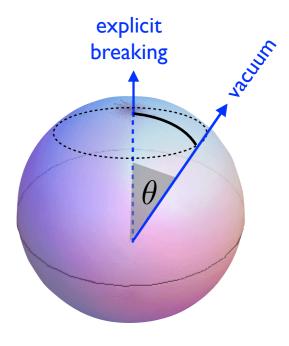
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explicit breaking of Goldstone symmetry (spurion couplings)

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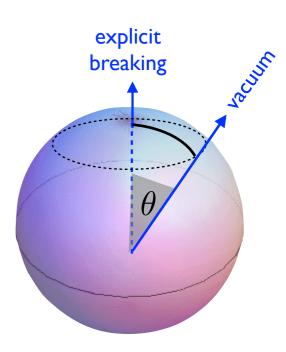
loop integral saturated at

$$V(h) = \frac{m_*^4}{g_*^2} \frac{N_c}{8\pi^2} \left[\lambda^2 \sum_i A_i(h/f) + \lambda^4 \sum_i B_i(h/f) + \dots \right]$$

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 $h \equiv \sqrt{H^{\dagger}H}$

$$rac{SO(5)}{SO(4)} = S^4$$
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loop integral saturated at the compositeness scale

$$V(h) = \frac{m_*^4}{g_*^2} \frac{N_c}{8\pi^2} \left[\lambda^2 \sum_i A_i(h/f) + \lambda^4 \sum_i B_i(h/f) + \dots \right]$$

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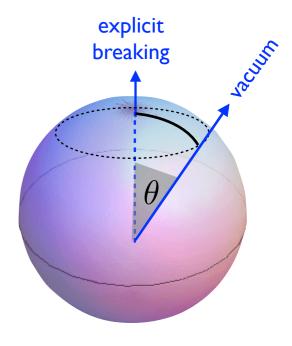
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To get EWSB ($0 < x \ll \pi$) at least <u>two</u> SO(4) structures are needed plus some tuning

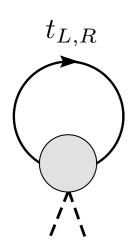
$$FT = O\left(\frac{v^2}{f^2}\right)$$





$$rac{SO(5)}{SO(4)} = S^4$$
 vacuum manifold is the 4-sphere

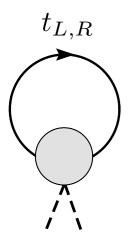
■ If EWSB is triggered at $O(\lambda^2)$



$$V(h) \simeq \frac{m_*^4}{g_*^2} \, \frac{N_c}{8\pi^2} \, \lambda_{L,R}^2 \, A\left(\frac{h}{f}\right)$$

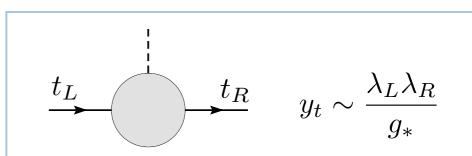
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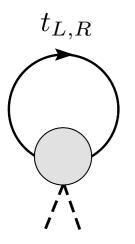




assuming $\lambda_L \simeq \lambda_R$

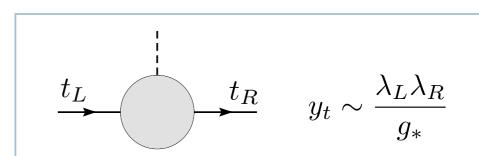
$$m_h^2 \sim \frac{N_c}{4\pi^2} g_*^3 y_t v^2 = \left(330 \,\text{GeV} \times \left(\frac{g_*}{3}\right)^{3/2}\right)^2$$

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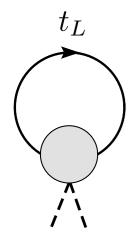


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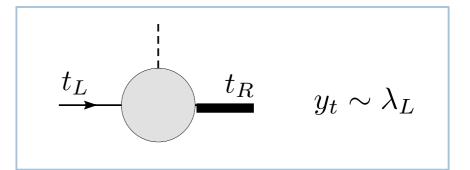
Higgs tends to be too heavy (unless $g_*\!\sim\!1$)

 $\hfill \square$ If EWSB is triggered at $O(\lambda^2)\,$ + t_R fully composite



$$V(h) \simeq \frac{m_*^4}{g_*^2} \, \frac{N_c}{8\pi^2} \, \lambda_L^2 \, A\left(\frac{h}{f}\right)$$

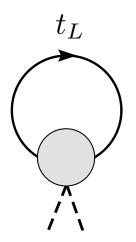
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$$\lambda_L \simeq y_t$$

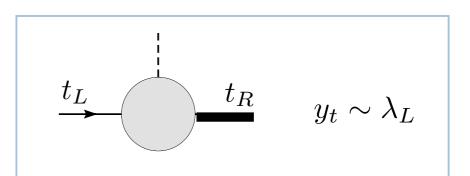
$$m_h^2 \sim \frac{N_c}{4\pi^2} g_*^2 y_t^2 v^2 = \left(175 \,\text{GeV} \times \left(\frac{g_*}{3}\right)\right)^2$$

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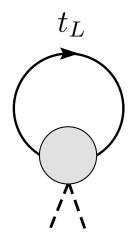
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 $m_H=125GeV$ implies that top partners are naturally

- not too strongly coupled, hence
- not too heavy

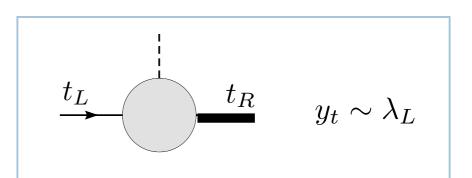
Matsedonskyi, Panico, Wulzer JHEP 1301 (2013) 164
Redi, Tesi JHEP 1210 (2012) 166
Marzocca, Serone, Shu JHEP 1208 (2012) 013
Pomarol, Riva JHEP 1208 (2012) 135
Panico, Redi, Tesi, Wulzer JHEP 1303 (2013) 051
De Simone et al. JHEP 1304 (2013) 004

If EWSB is triggered at $O(\lambda^2)$ + t_R fully composite



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$$m_h^2 \sim \frac{N_c}{4\pi^2} \, \frac{m_*^2}{f^2} \, \lambda_L^2 \, v^2$$





$$\lambda_L \simeq y_t$$

$$m_h^2 \sim \frac{N_c}{4\pi^2} g_*^2 y_t^2 v^2 = \left(175 \,\text{GeV} \times \left(\frac{g_*}{3}\right)\right)^2$$

$$FT \sim \frac{v^2}{f^2} \sim \frac{m_h^2}{m_*^2} \frac{4\pi^2}{N_c y_t^2} = \left(\frac{525 \,\text{GeV}}{m_*}\right)^2$$

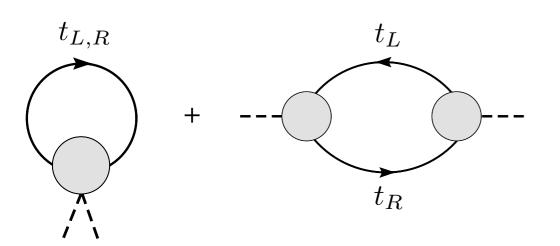
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■ If EWSB is triggered at $O(\lambda^4)$

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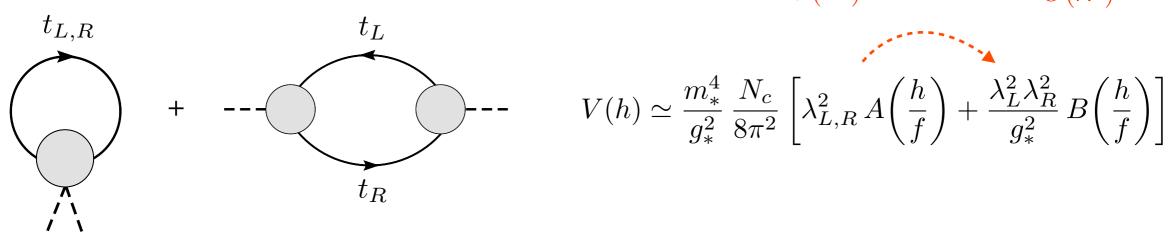


extra tuning required to suppress $O(\lambda^2)$ terms down to $O(\lambda^4)$

$$V(h) \simeq \frac{m_*^4}{g_*^2} \frac{N_c}{8\pi^2} \left[\lambda_{L,R}^2 A\left(\frac{h}{f}\right) + \frac{\lambda_L^2 \lambda_R^2}{g_*^2} B\left(\frac{h}{f}\right) \right]$$

If EWSB is triggered at $O(\lambda^4)$

extra tuning required to suppress $O(\lambda^2)$ terms down to $O(\lambda^4)$



$$m_h^2 \sim \frac{N_c}{4\pi^2} \frac{m_*^2}{f^2} \frac{\lambda_L^2 \lambda_R^2}{g_*^2} v^2 \sim \frac{N_c}{4\pi^2} g_*^2 y_t^2 v^2 = \left(175 \,\text{GeV} \times \left(\frac{g_*}{3}\right)\right)^2$$

If EWSB is triggered at $O(\lambda^4)$

 $O(\lambda^2)$ terms down to $O(\lambda^4)$ $t_{L,R}$ t_L

$$\begin{array}{c} t_{L,R} \\ + \end{array} \begin{array}{c} t_{L} \\ \end{array} \\ + \end{array} \begin{array}{c} V(h) \simeq \frac{m_{*}^{4}}{g_{*}^{2}} \frac{N_{c}}{8\pi^{2}} \left[\lambda_{L,R}^{2} A \left(\frac{h}{f} \right) + \frac{\lambda_{L}^{2} \lambda_{R}^{2}}{g_{*}^{2}} B \left(\frac{h}{f} \right) \right] \end{array}$$

$$m_h^2 \sim \frac{N_c}{4\pi^2} \frac{m_*^2}{f^2} \frac{\lambda_L^2 \lambda_R^2}{g_*^2} v^2 \sim \frac{N_c}{4\pi^2} g_*^2 y_t^2 v^2 = \left(175 \,\text{GeV} \times \left(\frac{g_*}{3}\right)\right)^2$$

$$FT \sim \frac{v^2}{f^2} \times \frac{\lambda^2}{g_*^2} \simeq \left(\frac{525 \,\mathrm{GeV}}{m_*}\right)^2 \times \frac{y_t}{g_*}$$

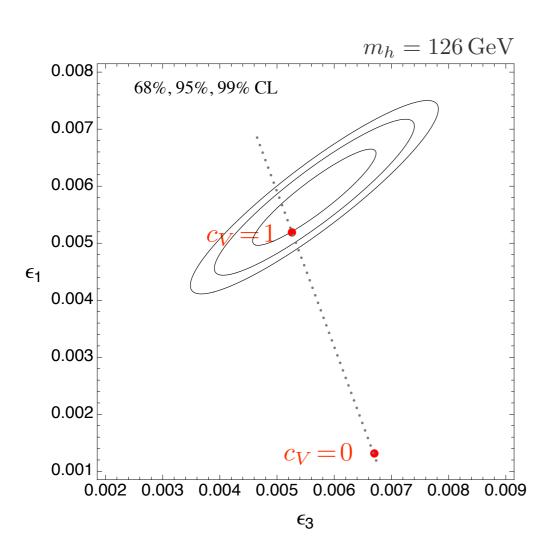
m_H automatically lighter but larger tuning to get EWSB

Panico, Redi, Tesi, Wulzer JHEP 1303 (2013) 051

extra tuning required to suppress

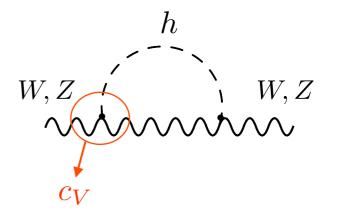
EW Precision Tests

Constraints on c_V from EW Precision Tests

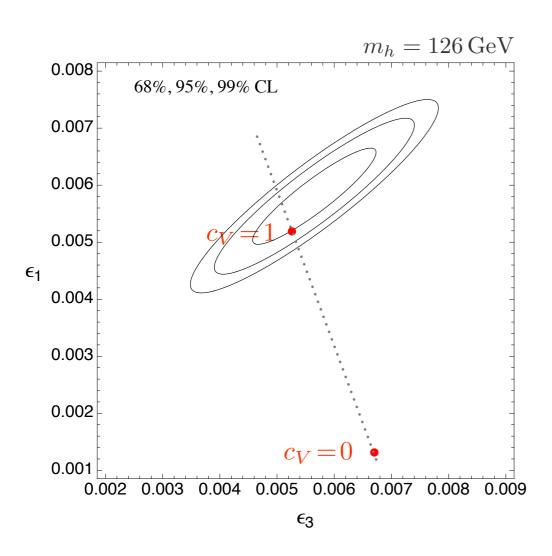


fit from: GFitter coll. Eur. Phys. J. C 72 (2012) 2205

$$\Delta \epsilon_1 = -\frac{3}{16\pi} \frac{\alpha_{em}}{\cos^2 \theta_W} \log \frac{\Lambda^2}{m_Z^2}$$
$$\Delta \epsilon_3 = +\frac{1}{12\pi} \frac{\alpha_{em}}{4 \sin^2 \theta_W} \log \frac{\Lambda^2}{m_Z^2}$$

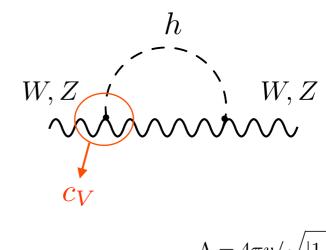


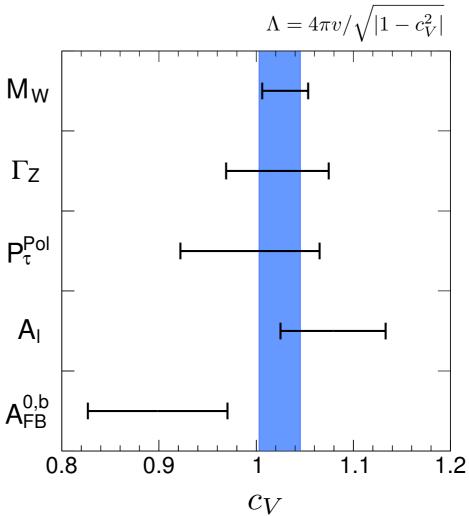
Constraints on c_V from EW Precision Tests



fit from: GFitter coll. Eur. Phys. J. C 72 (2012) 2205

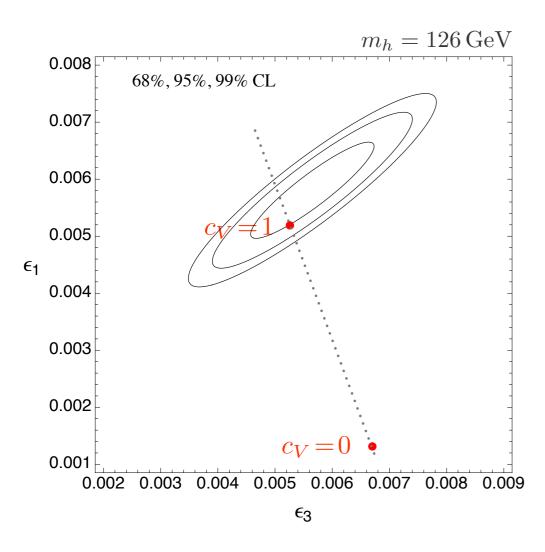
$$\Delta \epsilon_1 = -\frac{3}{16\pi} \frac{\alpha_{em}}{\cos^2 \theta_W} \log \frac{\Lambda^2}{m_Z^2}$$
$$\Delta \epsilon_3 = +\frac{1}{12\pi} \frac{\alpha_{em}}{4 \sin^2 \theta_W} \log \frac{\Lambda^2}{m_Z^2}$$





Ciuchini, Franco, Silvestrini, Mishima, arXiv:1306.4644

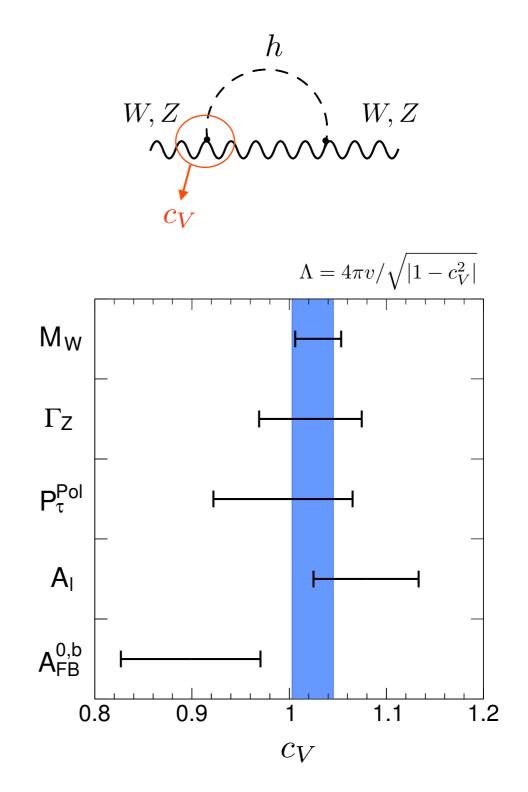
Constraints on c_V from EW Precision Tests



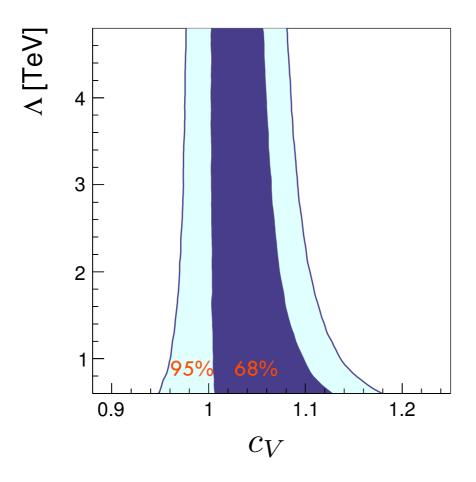
fit from: GFitter coll. Eur. Phys. J. C 72 (2012) 2205

Precision on c_V at the level of $\sim 5\%$!

Contribution from resonances REQUIRED to relax the bound



Ciuchini, Franco, Silvestrini, Mishima, arXiv:1306.4644



M. Ciuchini, E. Franco, L. Silvestrini, S. Mishima, arXiv:1306.4644

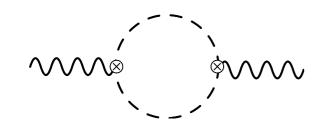
Analyticity and crossing symmetry imply a sum rule on c_V

$$1 - c_V^2 = \frac{v^2}{6\pi} \int_0^\infty \frac{ds}{s} \left(2 \,\sigma_{I=0}^{tot}(s) + 3 \,\sigma_{I=1}^{tot}(s) - 5 \,\sigma_{I=2}^{tot}(s) \right)$$

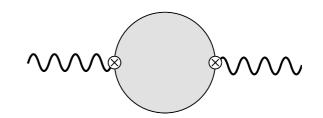
Falkowski, Rychkov, Urbano, JHEP 1204 (2012) 073 Low, Rattazzi, Vichi, JHEP 1004 (2010) 126

 $c_V > 1$ possible only if I=2 ch. dominates $V_L V_L$ scattering (requires: doubly-charged scalar resonance)

S parameter
$$\hat{S} = \hat{S}_{IR} + \hat{S}_{UV}$$

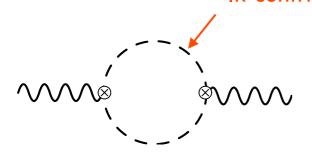


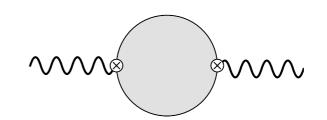
$$\hat{S}_{IR} \sim \frac{v^2}{f^2} \, \frac{g^2}{16\pi^2} \log \left(\frac{\Lambda}{m_Z}\right)$$



$$\hat{S}_{UV} \sim g^2 \frac{v^2}{f^2} \left[\frac{1}{g_*^2} + N_c N_F \frac{1}{16\pi^2} \log \left(\frac{\Lambda}{m_*} \right) + \dots \right]$$

S parameter
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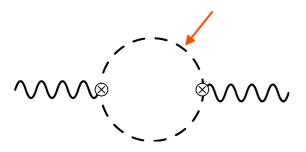




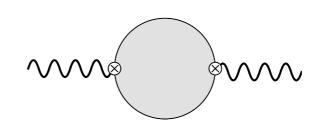
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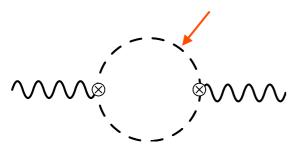


$$\hat{S}_{IR} \sim \frac{v^2}{f^2} \frac{g^2}{16\pi^2} \log\left(\frac{\Lambda}{m_Z}\right)$$

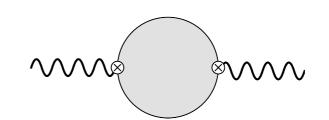


$$\hat{S}_{UV} \sim g^2 rac{v^2}{f^2} \left[rac{1}{g_*^2} + N_c N_F rac{1}{16\pi^2} \log \left(rac{\Lambda}{m_*}
ight) + \ldots
ight]$$
 tree-level (rho)

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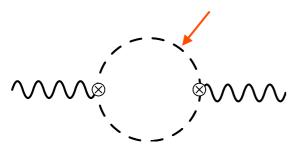


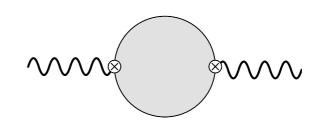
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ight]$$
 tree-level (rho) 1-loop (fermions)

S parameter
$$\hat{S} = \hat{S}_{IR} + \hat{S}_{UV}$$





$$\hat{S}_{IR} \sim \frac{v^2}{f^2} \frac{g^2}{16\pi^2} \log\left(\frac{\Lambda}{m_Z}\right)$$

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 tree-level (rho) 1-loop (fermions)

1-loop contribution from fermions can be large (!)

Golden, Randall, NPB 361 (1991) 3

••••

Barbieri, Isidori, Pappadopulo, JHEP 0902 (2009) 029 Grojean, Matsedonskyi, Panico, JHEP 1310 (2013) 160 Azatov, RC, Di lura, Galloway, PRD 88 (2013) 075019



Best seen using a dispertion relation:

Orgogozo and Rychkov, JHEP 1306 (2013) 014

$$i \int d^4x \, e^{iq \cdot (x-y)} \langle 0| T(J_{\mu}(x)J_{\nu}(y))|0\rangle = (q^2 \eta_{\mu\nu} - q_{\mu}q_{\nu}) \Pi(q^2)$$

$$\Pi(q^2) = \int ds \, \frac{\rho(s)}{q^2 - s + i\epsilon}$$

$$\hat{S}_{UV} = \frac{g^2}{4} \sin^2 \theta \int \frac{ds}{s} \left[\rho_{LL}(s) + \rho_{RR}(s) - 2\rho_{BB}(s) \right]$$



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negative contribution from spectral function of broken SO(5)/SO(4) currents

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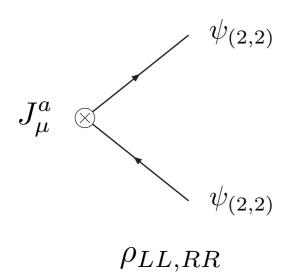
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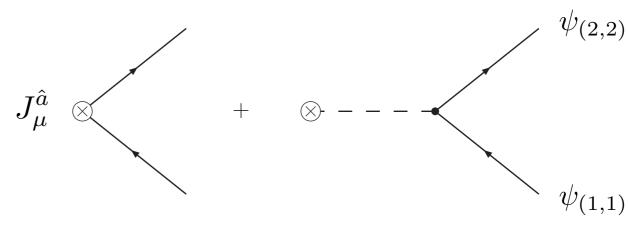
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Example: [Azatov, RC, Di lura, Galloway, PRD 88 (2013) 075019]

$$\psi_5 = (1,1) + (2,2)$$

$$\mathcal{L} = \bar{\psi}_1 (i \not \!\!\!D - m_1) \psi_1 + \bar{\psi}_4 (i \not \!\!\!\nabla - m_4) \psi_4 - \zeta \, \bar{\psi}_4 \gamma^{\mu} d_{\mu} \psi_1 + h.c.$$





 ρ_{BB}

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Orgogozo and Rychkov, JHEP 1306 (2013) 014

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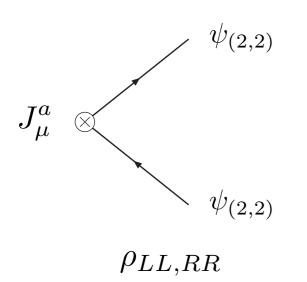
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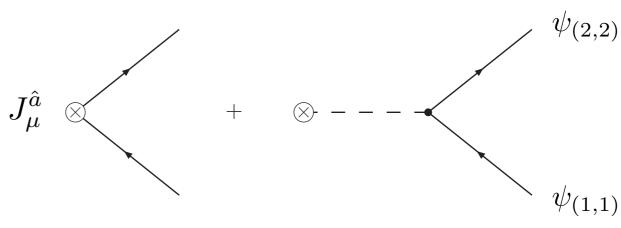
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Example: [Azatov, RC, Di lura, Galloway, PRD 88 (2013) 075019]

$$\psi_5 = (1,1) + (2,2)$$

$$\mathcal{L}=ar{\psi}_1ig(i
ot\!\!\!/-m_1ig)\,\psi_1+ar{\psi}_4ig(i
ot\!\!\!/-m_4ig)\,\psi_4-\zeta\,ar{\psi}_4\gamma^\mu d_\mu\,\psi_1+h.c.$$





 ρ_{BB}

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Orgogozo and Rychkov, JHEP 1306 (2013) 014

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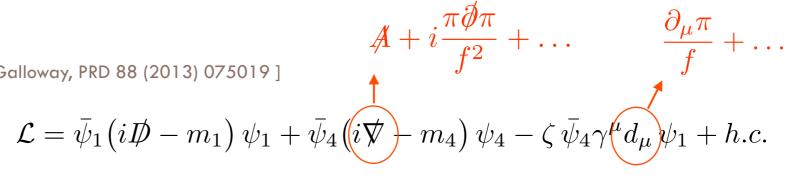
$$\hat{S}_{UV} = \frac{g^2}{4} \sin^2 \theta \int \frac{ds}{s} \left[\rho_{LL}(s) + \rho_{RR}(s) - 2\rho_{BB}(s) \right] - 2\rho_{BB}(s)$$

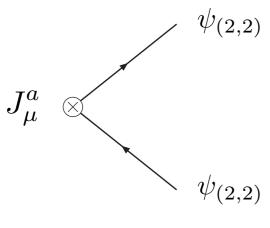
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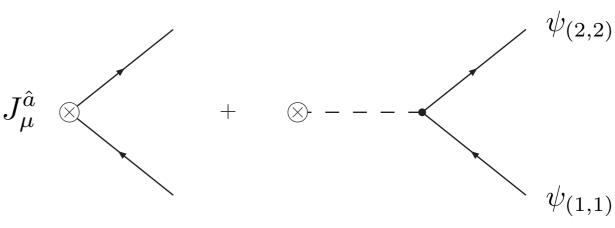
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$$\rho_{LL,RR}$$



Best seen using a dispertion relation:

Orgogozo and Rychkov, JHEP 1306 (2013) 014

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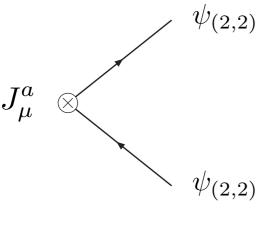
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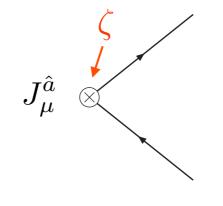
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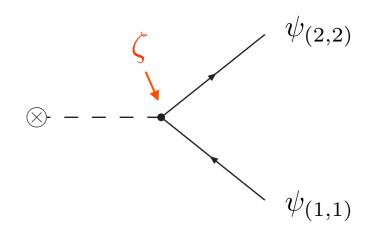
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Example: [Azatov, RC, Di lura, Galloway, PRD 88 (2013) 075019]

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Orgogozo and Rychkov, JHEP 1306 (2013) 014

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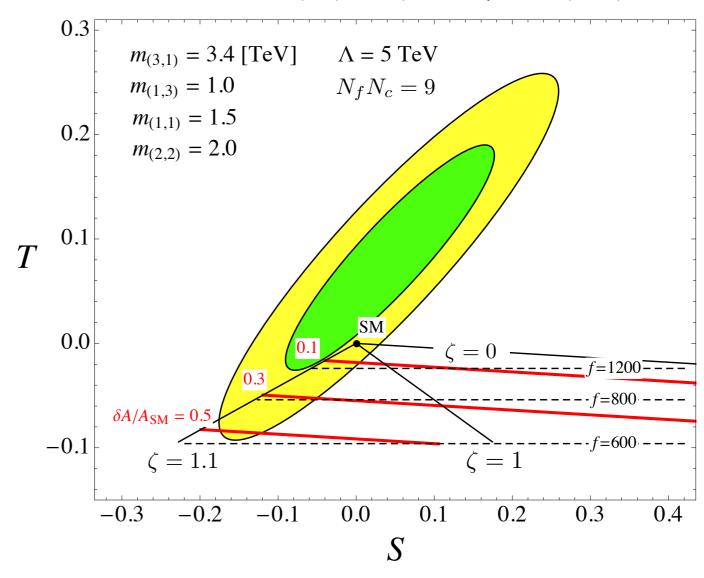
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$$\psi_5 = (1,1) + (2,2) \qquad \qquad \mathcal{L} = \bar{\psi}_1 \big(i \rlap{/}{D} - m_1 \big) \, \psi_1 + \bar{\psi}_4 \big(i \rlap{/}{\nabla} - m_4 \big) \, \psi_4 - \zeta \, \bar{\psi}_4 \gamma^{\mu} d_{\mu} \psi_1 + h.c.$$

$$\hat{S}_{UV} = \frac{8}{3} \frac{m_W^2}{16\pi^2 f^2} N_c N_F \left(1 - |\zeta|^2 \right) \log \left(\frac{\Lambda^2}{m_{(2,2)}^2} \right) + \text{finite terms}$$

SO(5)/SO(4) model:

$$\psi_5 = (1,1)_{2/3} + (2,2)_{2/3}$$

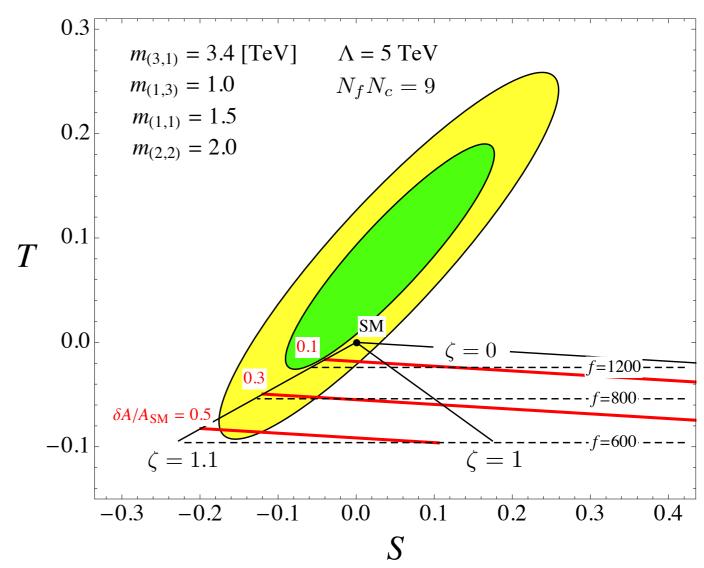
$$\psi_{10} = (2,2)_{-1/3} + (1,3)_{-1/3} + (3,1)_{-1/3}$$



SO(5)/SO(4) model:

$$\psi_5 = (1,1)_{2/3} + (2,2)_{2/3}$$

$$\psi_{10} = (2,2)_{-1/3} + (1,3)_{-1/3} + (3,1)_{-1/3}$$



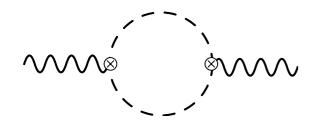
Ex: for $f = 800 \, \mathrm{GeV}$ $g_{\rho} = 3$

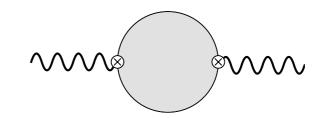
$$\Delta S_{\rho} \simeq 0.13$$
 $\Delta S_{\psi} \simeq 0.8 \times (1 - |\zeta|^2)$

strong sensitivity on ζ

O(10%) tuning required to go back into the experimental ellipse

T parameter
$$\hat{T} = \hat{T}_{IR} + \hat{T}_{UV}$$

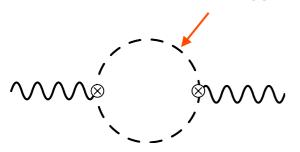


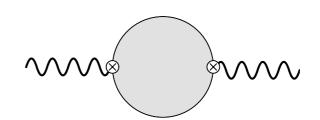


$$\hat{T}_{IR} \sim -\frac{v^2}{f^2} \frac{g'^2}{16\pi^2} \log\left(\frac{\Lambda}{m_Z}\right)$$

$$\hat{T}_{UV} \sim \frac{v^2}{f^2} \left[\frac{g'^2}{16\pi^2} \log\left(\frac{\Lambda}{m_\rho}\right) + N_c \frac{\lambda_L^2}{16\pi^2} \frac{\lambda_L^2}{g_*^2} + \dots \right]$$

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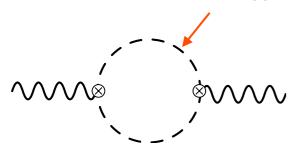


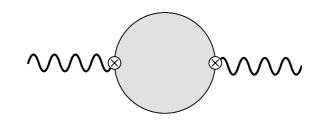


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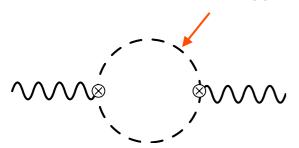




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1-loop (rho)

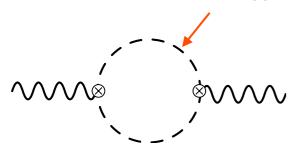
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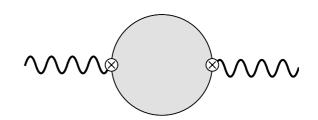


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1-loop (rho)
1-loop (fermions)

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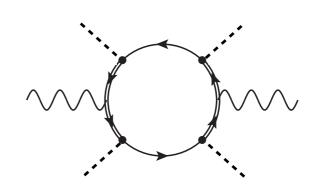




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ight) + N_c rac{\lambda_L^2}{16\pi^2} rac{\lambda_L^2}{g_*^2} + \dots
ight]$$
1-loop (rho)
1-loop (fermions)

- Custodial symmetry implies:
 - 1. No \hat{T} at tree-level
 - 2. fermion correction is finite and starts at $O(\lambda_L^4)$ (only top partners contribute)



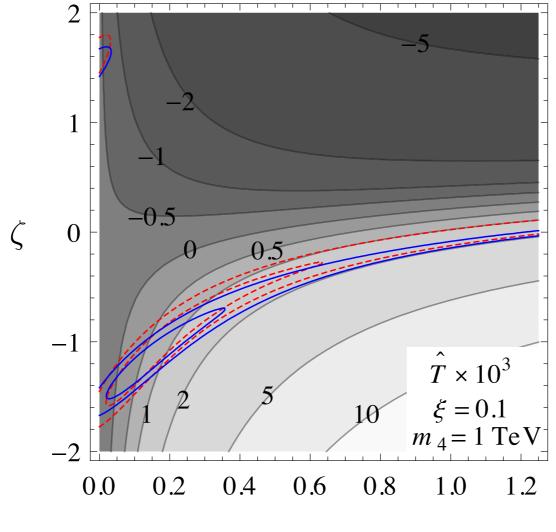
$\Delta \hat{T} > 0$ possible though not fully generic

Example: model with $\psi_4=(2,2)_{2/3}$ + t_R composite

$$\mathcal{L} = \bar{q}_L i \not\!\!D q_L + \bar{t}_R i \not\!\!D t_R + \bar{\psi}_4 (i \not\!\!\nabla - m_4) \psi_4$$
$$+ i \zeta \, \bar{\psi}_4^i \gamma^\mu d^i_\mu t_R + y_{Lt} f \, \bar{q}_L U(\pi) t_R + y_{L4} f \, \bar{q}_L U(\pi) \psi_4 + h.c.$$

Carena, et al. NPB 759 (2006) 202; PRD 76 (2007) 035006
Barbieri et al. PRD 76 (2007) 115008
Lodone JHEP 0812 (2008) 029
Pomarol, Serra, PRD 78 (2008) 074026
Gillioz PRD 80 (2009) 055003

:
Grojean, Matsedonskyi, Panico, JHEP 1310 (2013) 160



Grojean, Matsedonskyi, Panico JHEP 1310 (2013) 160

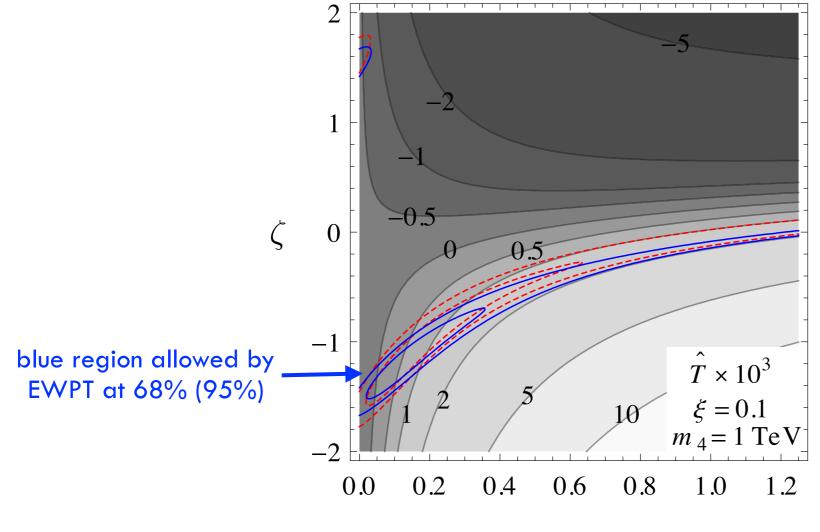
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$$\mathcal{L} = \bar{q}_L i \not\!\!D q_L + \bar{t}_R i \not\!\!D t_R + \bar{\psi}_4 (i \not\!\!\nabla - m_4) \psi_4$$
$$+ i \zeta \, \bar{\psi}_4^i \gamma^\mu d^i_\mu t_R + y_{Lt} f \, \bar{q}_L U(\pi) t_R + y_{L4} f \, \bar{q}_L U(\pi) \psi_4 + h.c.$$

Carena, et al. NPB 759 (2006) 202; PRD 76 (2007) 035006
Barbieri et al. PRD 76 (2007) 115008
Lodone JHEP 0812 (2008) 029
Pomarol, Serra, PRD 78 (2008) 074026
Gillioz PRD 80 (2009) 055003

:
Grojean, Matsedonskyi, Panico, JHEP 1310 (2013) 160

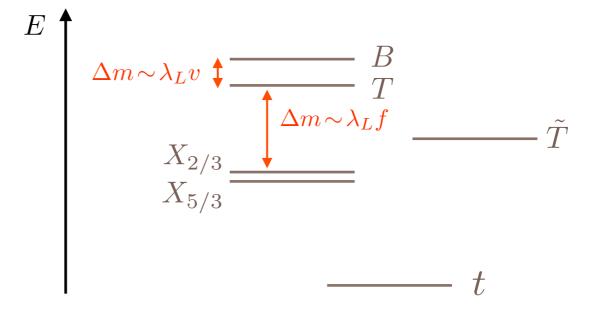


Grojean, Matsedonskyi, Panico JHEP 1310 (2013) 160

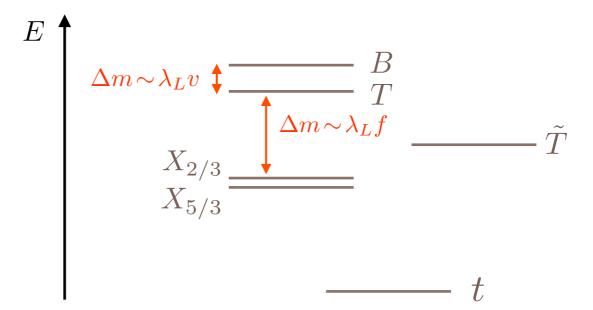
 y_{L4}

Searches of top partners

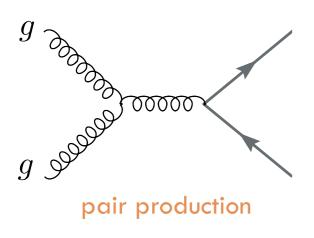
Typical spectrum of top partners

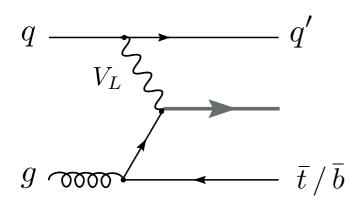


Typical spectrum of top partners



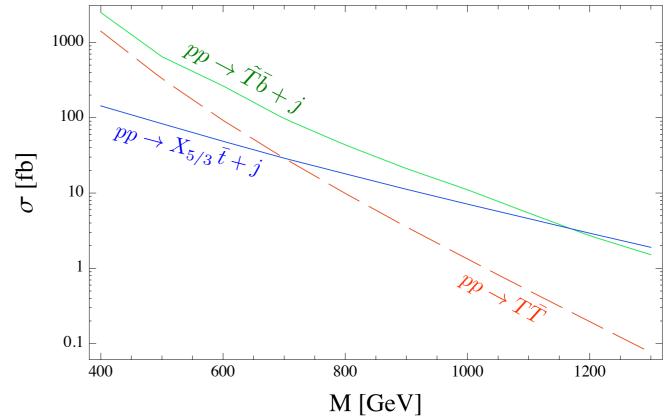
Two main production modes:



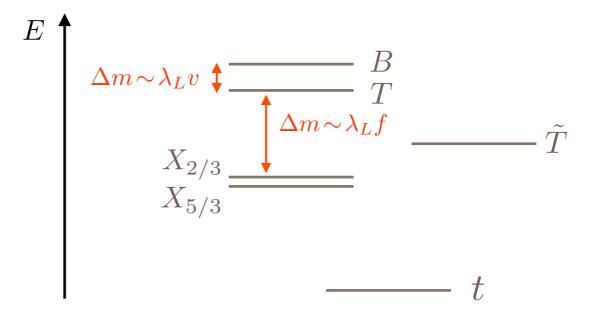


EW single production

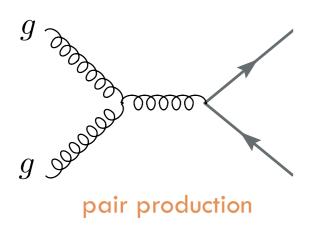
from: De Simone, Matsedonskyi, Rattazzi, Wulzer JHEP 1304 (2013) 004

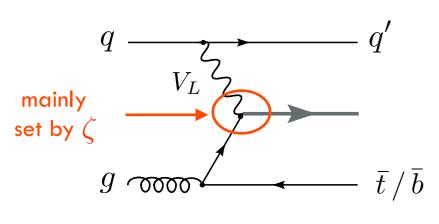


Typical spectrum of top partners

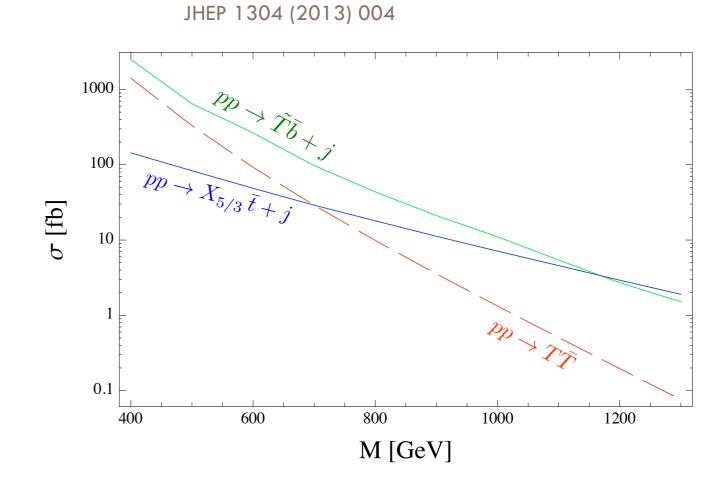


Two main production modes:



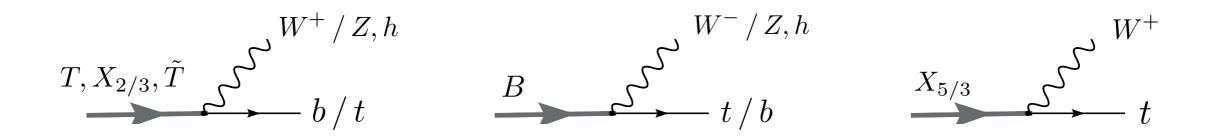


EW single production

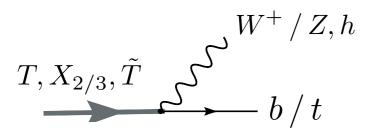


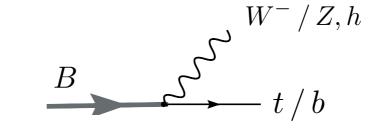
from: De Simone, Matsedonskyi, Rattazzi, Wulzer

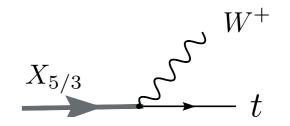
Two-body decay modes:



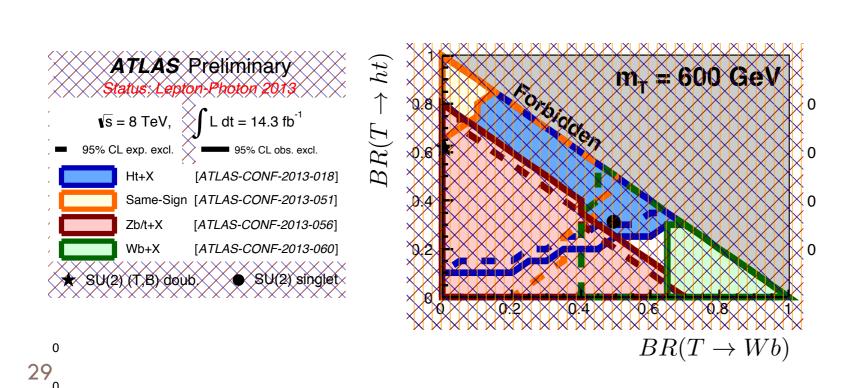
Two-body decay modes:

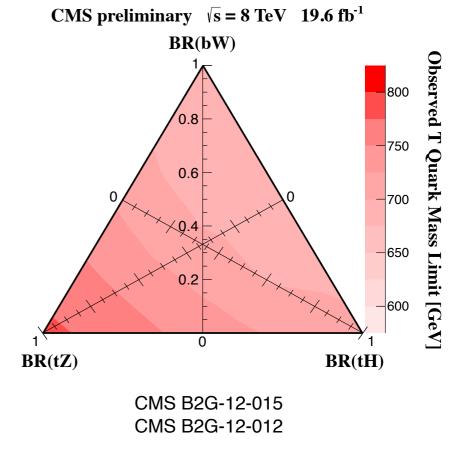




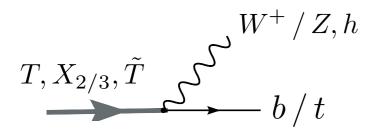


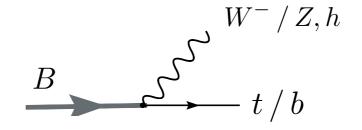
- Current experimental status in a nutshell
 - 1. Almost all decays looked for
 - 2. Analyses optimized on pair production

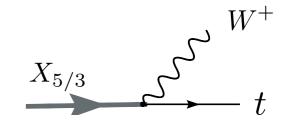




Two-body decay modes:

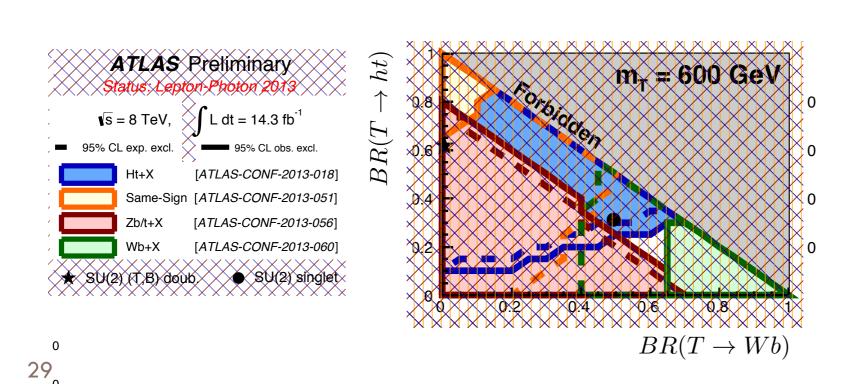


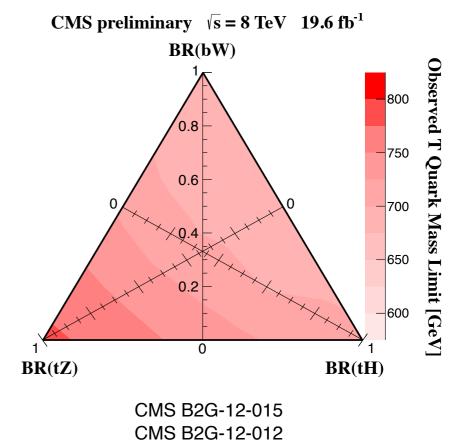


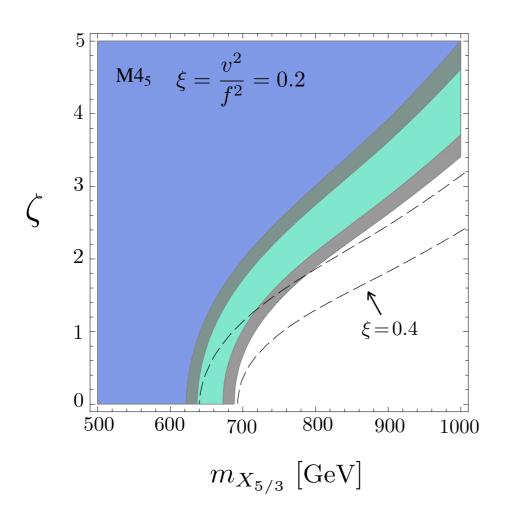


- Current experimental status in a nutshell
 - 1. Almost all decays looked for
 - 2. Analyses optimized on pair production

Limits in the 700-800 GeV range





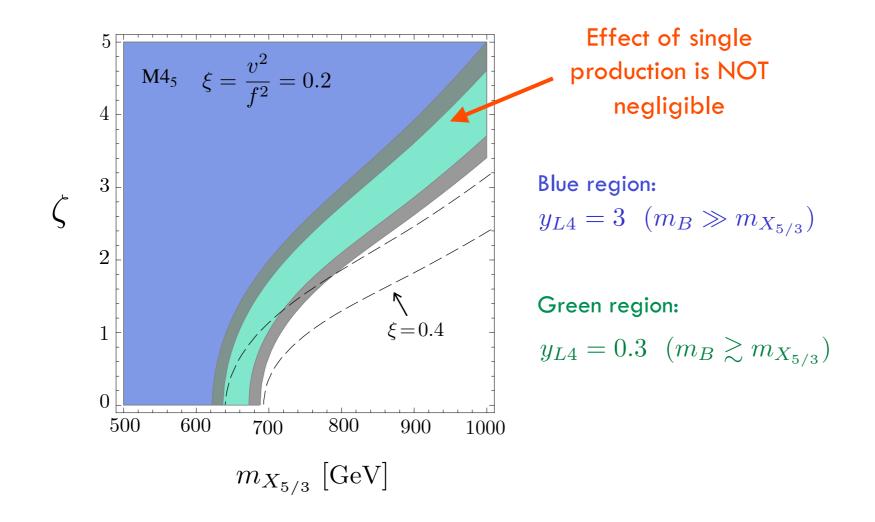


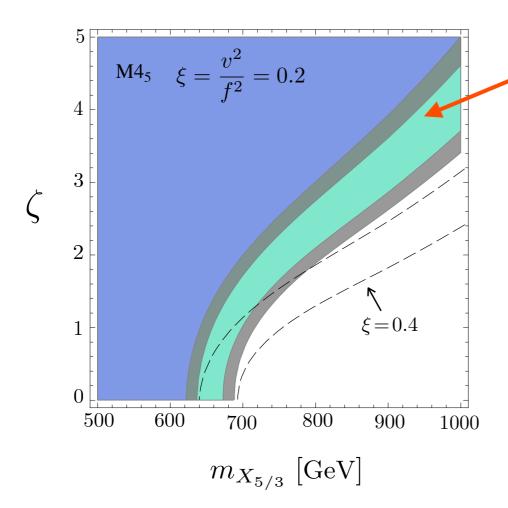
Blue region:

$$y_{L4} = 3 \ (m_B \gg m_{X_{5/3}})$$

Green region:

$$y_{L4} = 0.3 \ (m_B \gtrsim m_{X_{5/3}})$$





Multiplicity of states, connection among masses and inclusion of single production amplify limits on individual particles

Effect of single production is NOT negligible

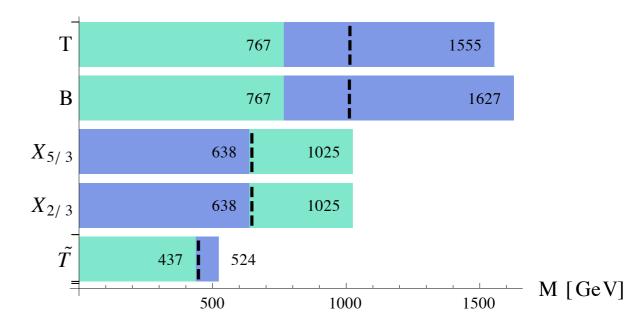
Blue region:

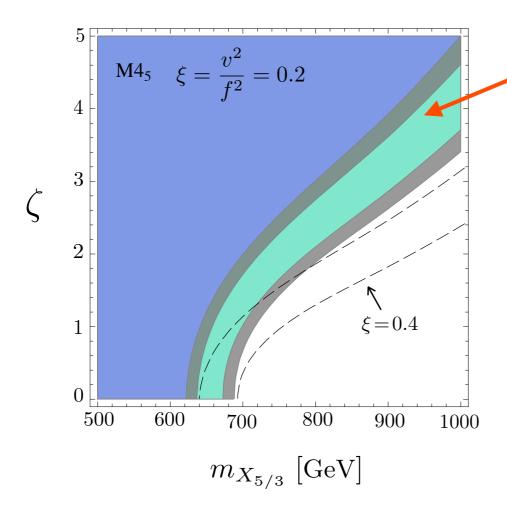
$$y_{L4} = 3 \ (m_B \gg m_{X_{5/3}})$$

Green region:

$$y_{L4} = 0.3 \ (m_B \gtrsim m_{X_{5/3}})$$

---- limits for $\xi=0.1,~\zeta=1,~y_{L4}=1$





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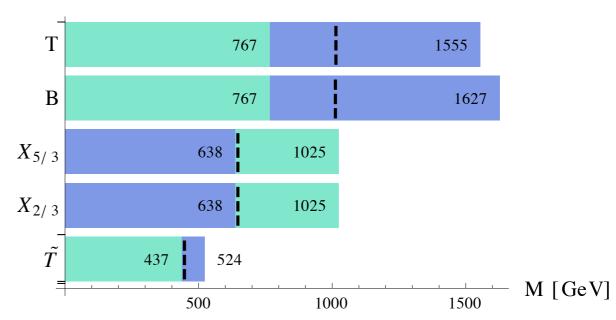
$$y_{L4} = 0.3 \ (m_B \gtrsim m_{X_{5/3}})$$

---- limits for $\xi = 0.1, \; \zeta = 1, \; y_{L4} = 1$

Multiplicity of states, connection among masses and inclusion of single production amplify limits on individual particles

1TeV masses typically excluded

LHC has already eaten up a big part of the natural region

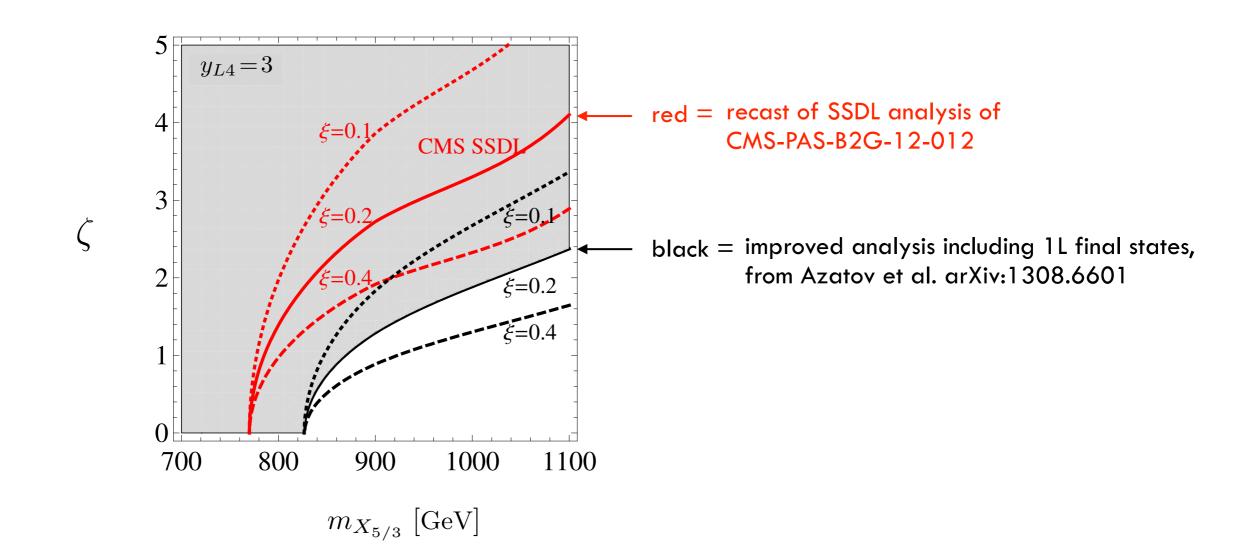


Improving the limits still possible with current data

De Simone et al. JHEP 1304 (2013) 004 Azatov, Salvarezza, Son, Spannowsky arXiv:1308.6601

Ex: - optimize searches to include single production

- include single-lepton final states
- use boosted jet techniques



Higgs couplings

$$c_V = 1 + F\left(\frac{v^2}{f^2}\right) + O\left(\frac{v^2}{f^2} \frac{g_{\mathcal{G}}^2}{g_*^2}\right)$$

$$c_{\psi} = 1 + F_{\psi} \left(\frac{v^2}{f^2}, \frac{m_i}{m_j} \right) + O\left(\frac{v^2}{f^2}, \frac{\lambda^2}{g_*^2} \right)$$

$$O(v^2/f^2)$$
 from Higgs nlom
$$c_V = 1 + F\left(\frac{v^2}{f^2}\right) + O\left(\frac{v^2}{f^2} \, \frac{g_{\mathcal{G}}^2}{g_*^2}\right)$$

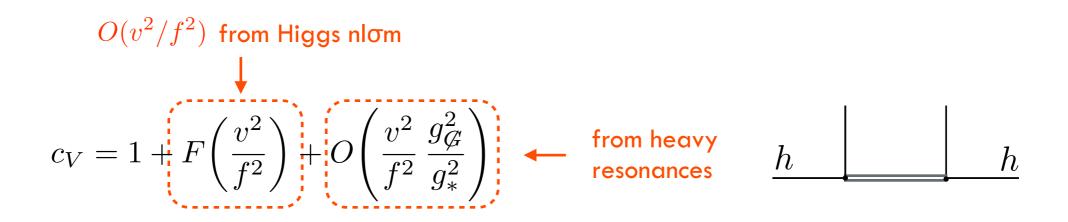
$$c_{\psi} = 1 + F_{\psi} \left(\frac{v^2}{f^2}, \frac{m_i}{m_j} \right) + O\left(\frac{v^2}{f^2}, \frac{\lambda^2}{g_*^2} \right)$$

$$C(v^2/f^2) \text{ from Higgs nlom}$$

$$\downarrow$$

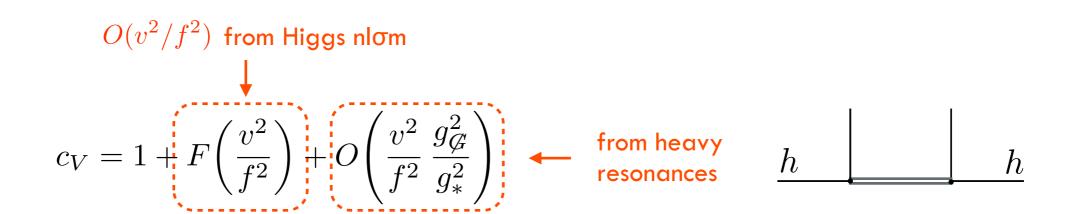
$$c_V = 1 + F\left(\frac{v^2}{f^2}\right) + O\left(\frac{v^2}{f^2} \frac{g_{\mathcal{G}}^2}{g_*^2}\right) \qquad \text{from heavy resonances} \qquad \underline{h} \qquad \underline{h}$$

$$c_{\psi} = 1 + F_{\psi} \left(\frac{v^2}{f^2}, \frac{m_i}{m_j} \right) + O\left(\frac{v^2}{f^2}, \frac{\lambda^2}{g_*^2} \right)$$



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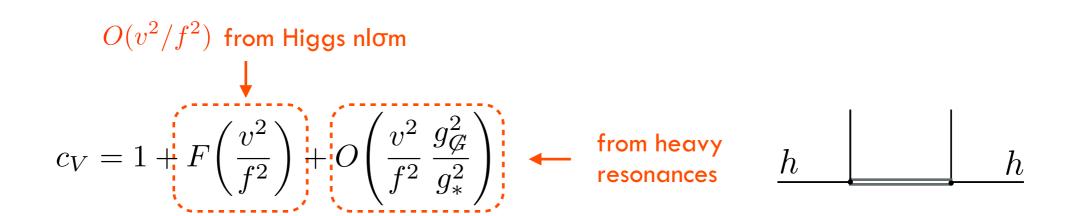
$$\psi_L \qquad \psi_R \qquad \psi_L \qquad \psi_R \qquad + \cdots$$



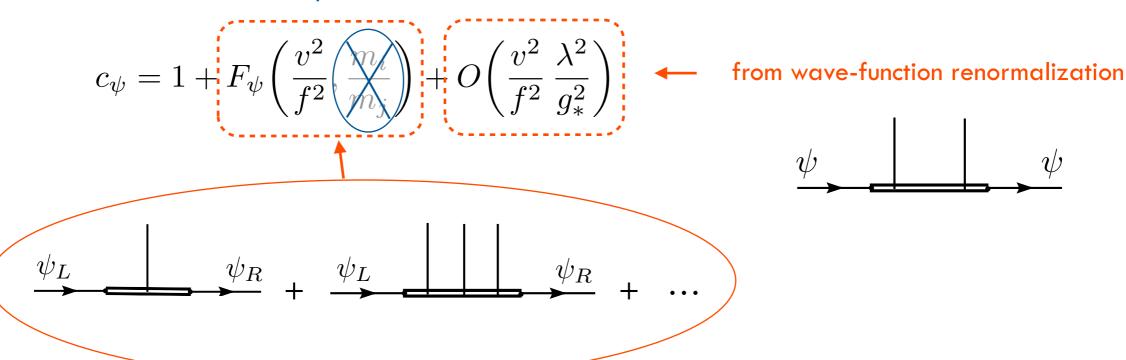
in the simplest models

$$c_{\psi} = 1 + F_{\psi} \left(\frac{v^2}{f^2} \right) + O\left(\frac{v^2}{f^2} \frac{\lambda^2}{g_*^2} \right)$$

$$\psi_L \qquad \psi_R \qquad \psi_L \qquad \psi_R \qquad + \cdots$$



in the simplest models



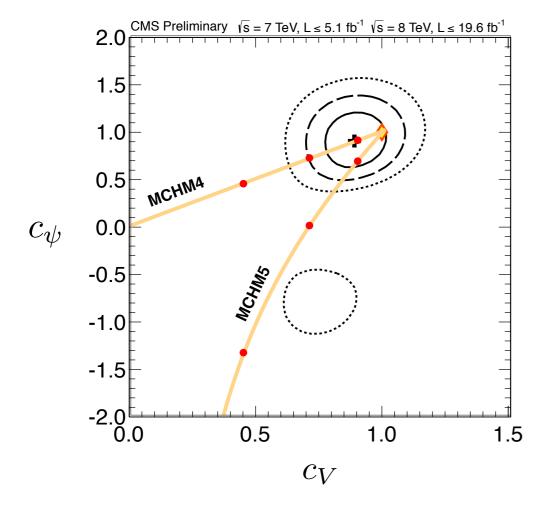
$$\xi \equiv \frac{v^2}{f^2}$$

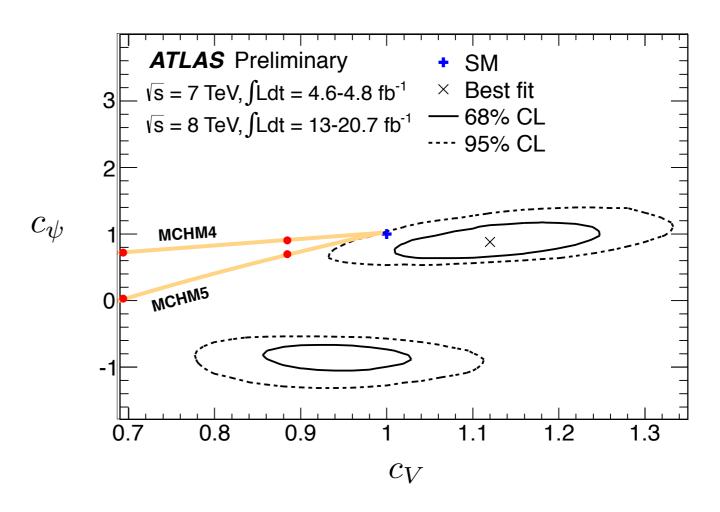
MCHM4:
$$c_V = c_\psi = \sqrt{1-\xi}$$

Agashe, RC, Pomarol, NPB 719 (2005) 165

MCHM5:
$$c_V = \sqrt{1-\xi}$$
 $c_{\psi} = \frac{1-2\xi}{\sqrt{1-\xi}}$

RC, DaRold, Pomarol, PRD 75 (2007) 055014 Carena, Ponton, Santiago, Wagner, PRD 76 (2007) 035006





Red points at $\xi \equiv (v/f)^2 = 0.2, \ 0.5, \ 0.8$

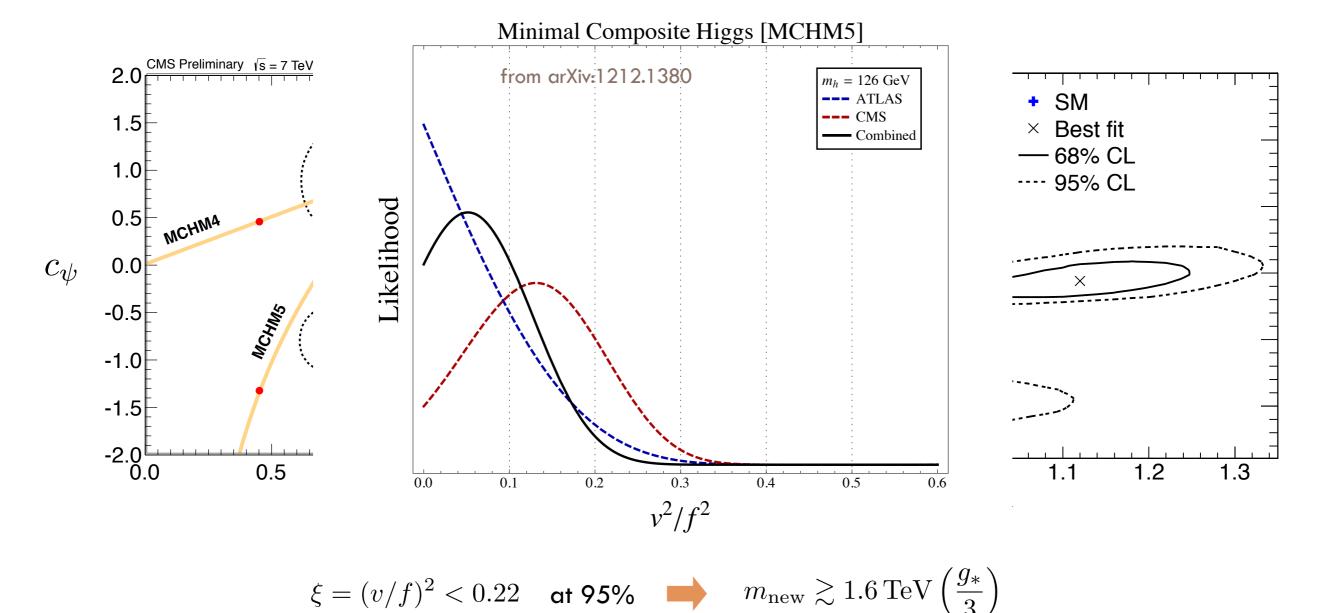
$$\xi \equiv \frac{v^2}{f^2}$$

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Agashe, RC, Pomarol, NPB 719 (2005) 165

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RC, DaRold, Pomarol, PRD 75 (2007) 055014 Carena, Ponton, Santiago, Wagner, PRD 76 (2007) 035006



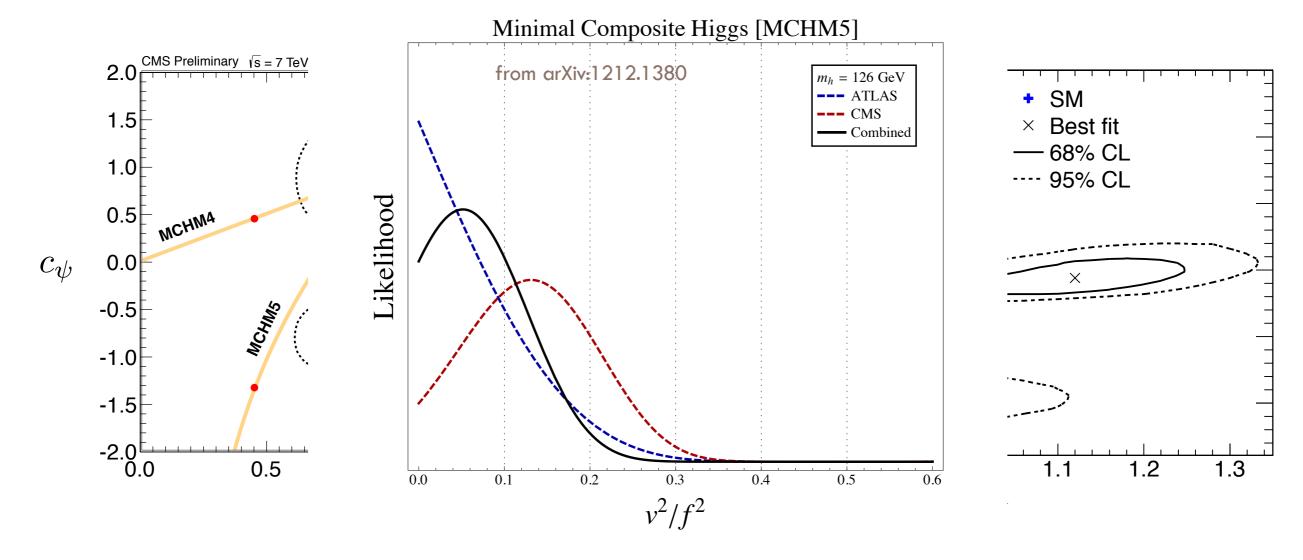
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Agashe, RC, Pomarol, NPB 719 (2005) 165

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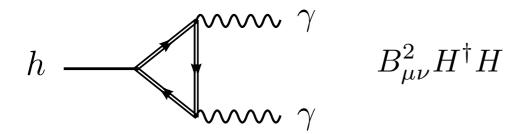


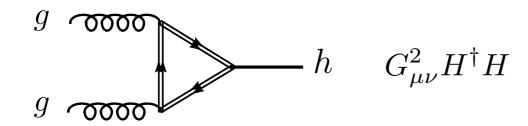
$$\xi = (v/f)^2 < 0.22$$

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 at 95% $m_{\rm new} \gtrsim 1.6 \, {\rm TeV} \left(\frac{g_*}{3} \right)$

Sensitivity comparable to direct searches

• Modifications to loop-level couplings ggh, $\gamma\gamma h$ suppressed due to the Goldstone symmetry

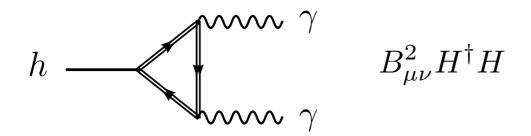


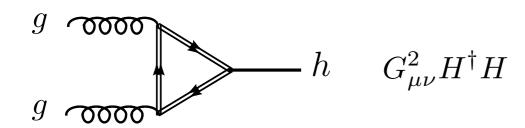


Effective operators violate the Higgs shift symmetry:

$$H^i \to H^i + \zeta^i$$

 Modifications to loop-level couplings ggh, γγh suppressed due to the Goldstone symmetry





Effective operators violate the Higgs shift symmetry:

$$H^i \to H^i + \zeta^i$$

$$\frac{\delta\Gamma}{\Gamma_{SM}} = 1 + O\left(\frac{v^2}{f^2}\right) + O\left(\frac{g_*^2v^2}{m_*^2} \times \frac{\lambda^2}{g_*^2}\right)$$
 'long-distance' SM loops with modified couplings 'short-distance' loops of top partners

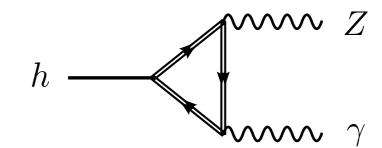
Azatov, RC, Di lura, Galloway, PRD 88 (2013) 075019

$$\frac{\delta\Gamma(Z\gamma)}{\Gamma_{SM}(Z\gamma)} = O\left(\frac{v^2}{f^2}\right) + O\left(\frac{g_*^2v^2}{m_*^2}\right)$$

Relevant operator is $O_{HW} - O_{HB}$

$$O_{HB} = (D^{\mu}H)^{\dagger}(D^{\nu}H)B_{\mu\nu}$$

$$O_{HW} = (D^{\mu}H)^{\dagger} \sigma^i (D^{\nu}H) W^i_{\mu\nu}$$



- 1. Invariant under Higgs shift symmetry
- 2. Odd under LR exchange

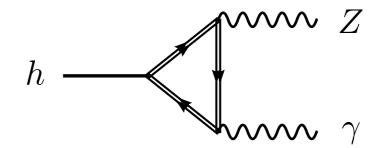
Azatov, RC, Di lura, Galloway, PRD 88 (2013) 075019

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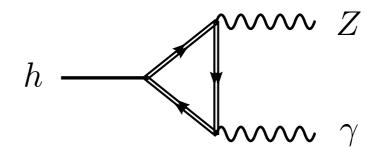
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$$A(h \to Z\gamma) = A_{SM} \times F(\xi) + \delta A$$

$$\frac{\delta A}{A_{SM}} \sim N_c N_F \left(\frac{g_*^2 v^2}{m_*^2}\right) \sim N_c N_F \frac{v^2}{f^2} \frac{\Delta m_*^2}{m_*^2}$$

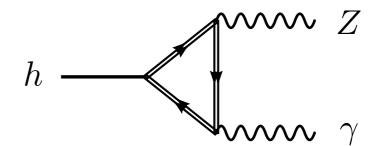
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- 1. Invariant under Higgs shift symmetry
- 2. Odd under LR exchange



$$A(h \to Z\gamma) = A_{SM} \times F(\xi) + \delta A$$
 shift of tree-level

$$1 + O\left(\frac{v^2}{f^2}\right)$$

$$\frac{\delta A}{A_{SM}} \sim N_c N_F \left(\frac{g_*^2 v^2}{m_*^2}\right) \sim N_c N_F \frac{v^2}{f^2} \frac{\Delta m_*^2}{m_*^2}$$

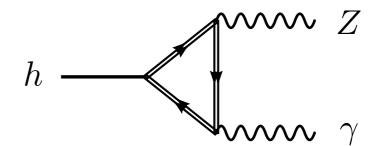
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- 1. Invariant under Higgs shift symmetry
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$$A(h \to Z\gamma) = A_{SM} \times F(\xi) + \delta A$$
 shift of tree-level Higgs couplings
$$1 + O\left(\frac{v^2}{f^2}\right)$$
 from nlom

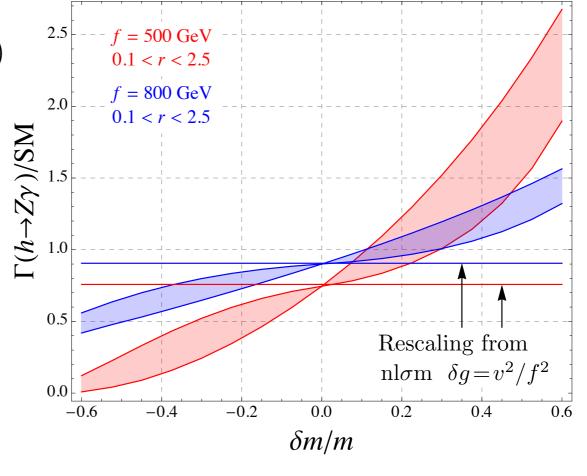
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 multiplicity of composite states

Azatov, RC, Di lura, Galloway, PRD 88 (2013) 075019

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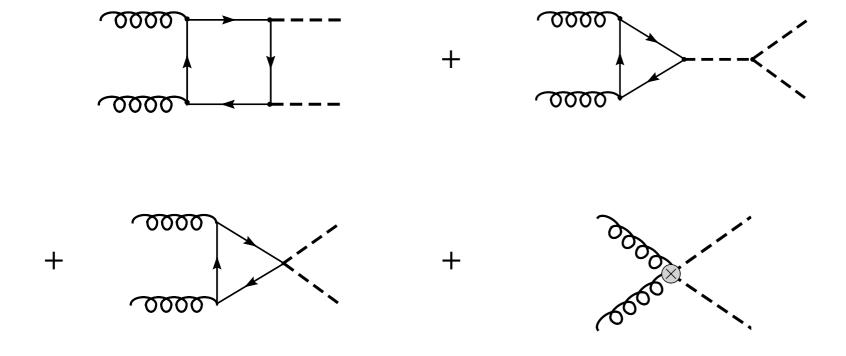
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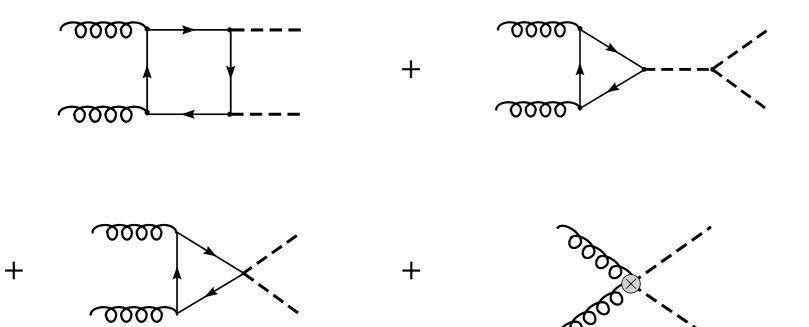
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 multiplicity of composite states

Future strategies

Double-Higgs production



$$\Delta \mathcal{L}^{(6)} = \frac{\bar{c}_H}{2v^2} [\partial_{\mu} (H^{\dagger} H)]^2 + \frac{\bar{c}_u}{v^2} y_u H^{\dagger} H \bar{q}_L H^c u_R - \frac{\bar{c}_6 \lambda}{v^2} (H^{\dagger} H)^3$$



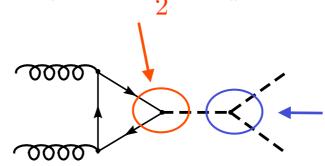
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modified top Yukawa coupl. $c_t \simeq 1 - \frac{\overline{c}_H}{2} - \overline{c}_u$



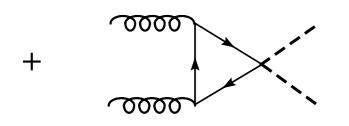
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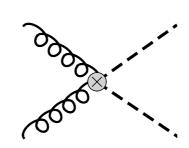
modified Higgs trilinear coupl.

$$c_3 \simeq 1 - \frac{3}{2}\bar{c}_H + \bar{c}_6$$



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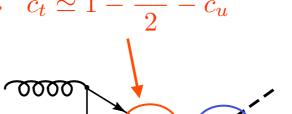
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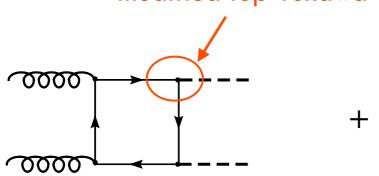
$$\Delta \mathcal{L}^{(6)} = \frac{\bar{c}_H}{2v^2} [\partial_{\mu} (H^{\dagger} H)]^2 + \frac{\bar{c}_u}{v^2} y_u H^{\dagger} H \bar{q}_L H^c u_R - \frac{\bar{c}_6 \lambda}{v^2} (H^{\dagger} H)^3$$

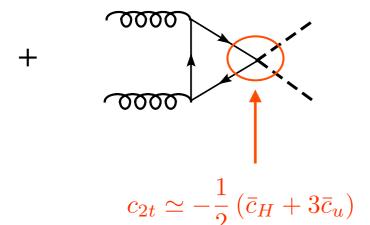
modified top Yukawa coupl. $c_t \simeq 1 - \frac{c_H}{2} - \bar{c}_u$



modified Higgs trilinear coupl.

$$- c_3 \simeq 1 - \frac{3}{2}\bar{c}_H + \bar{c}_6$$



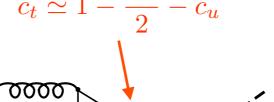


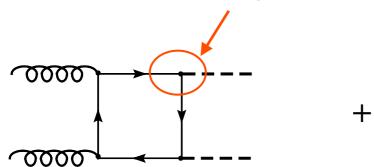
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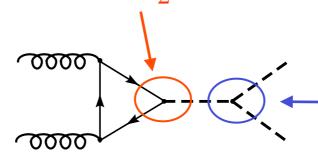
New tthh quartic vertex

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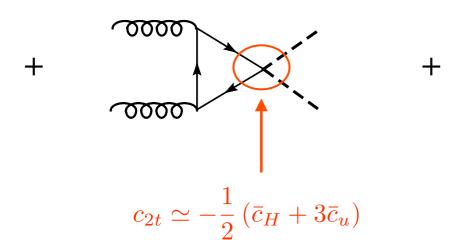




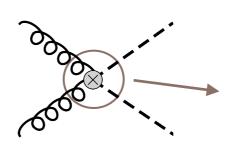


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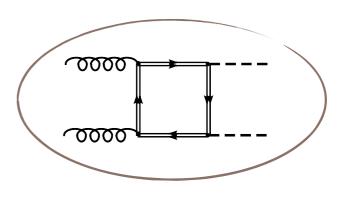


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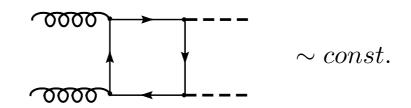


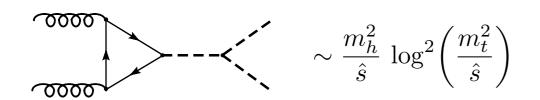
$$G_{\mu\nu}^2 \frac{H^\dagger H}{m_*^2}$$

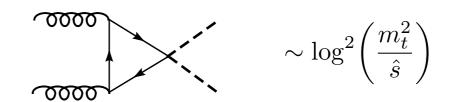
Contact vertex from heavy states

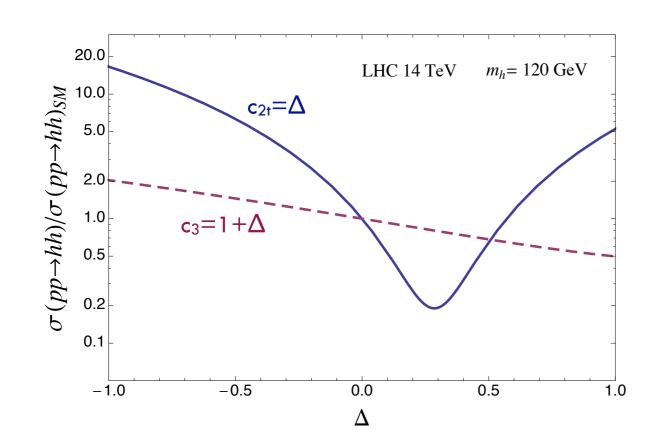


High-energy behavior









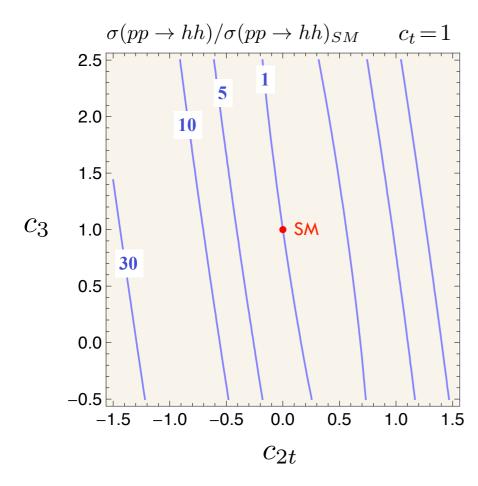
RC, Ghezzi, Moretti, Panico, Piccinini, Wulzer JHEP 1208 (2012) 154

Suppression of SM triangle diagrams at high-energy implies:

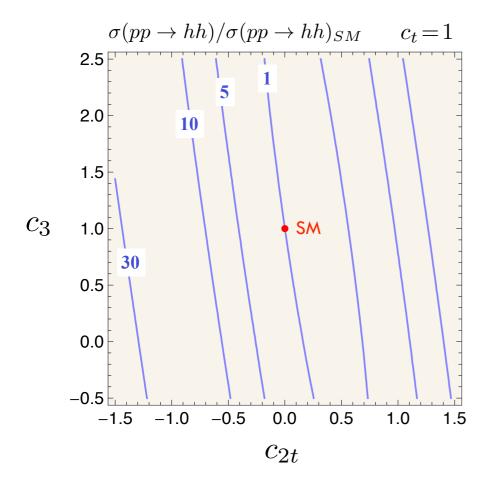
much better sensitivity on c_{2t} than c_3

[First noticed by: Dib, Rosenfeld, Zerwekh, JHEP 0605 (2006) 074 Grober and Muhlleitner, JHEP 1106 (2011) 020]

$$\sigma(pp \to hh + X)_{SM} = 28.7 \,\text{fb}$$



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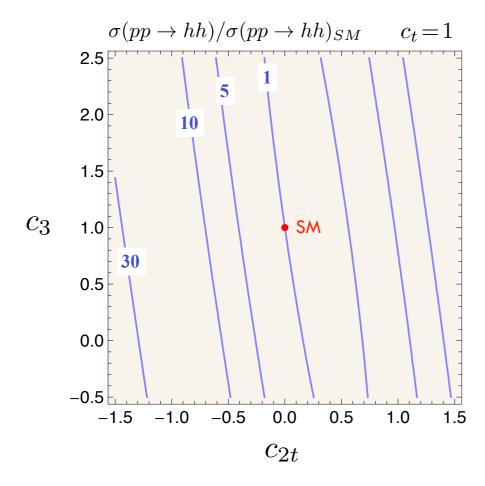
- = $hh o b \overline{b} \gamma \gamma$ seems the best channel Baur, Plehn, Rainwater, PRD 69 (2004) 053004 ATLAS: ATL-PHYS-PUB-2012-004
- $hh o b \overline{b} au au$ promising in the boosted regime

Dolan, Englert, Spannowsky arXiv:1206.5001

- $hh
ightarrow bar{b}WW$ overwhelmed by $tar{t}$ background

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For example: in the MCHM5

$$c_t = c_3 = \frac{1 - 2\xi}{\sqrt{1 - \xi}}$$

$$\xi \equiv \frac{v^2}{f^2}$$

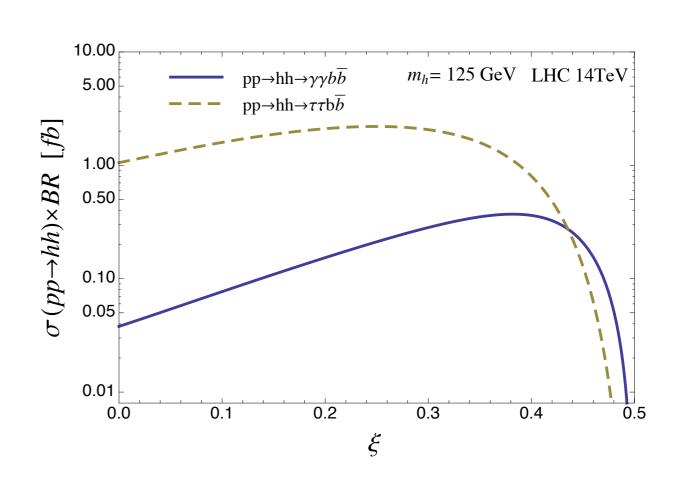
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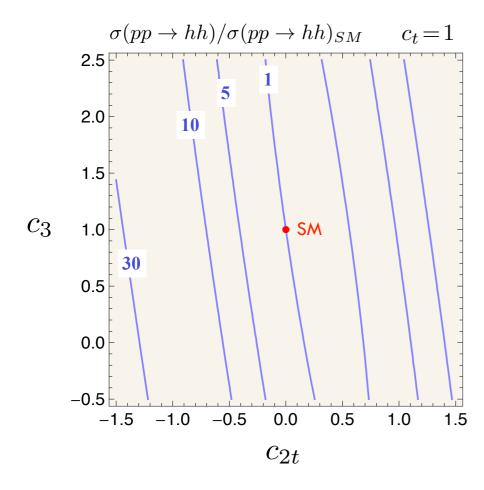
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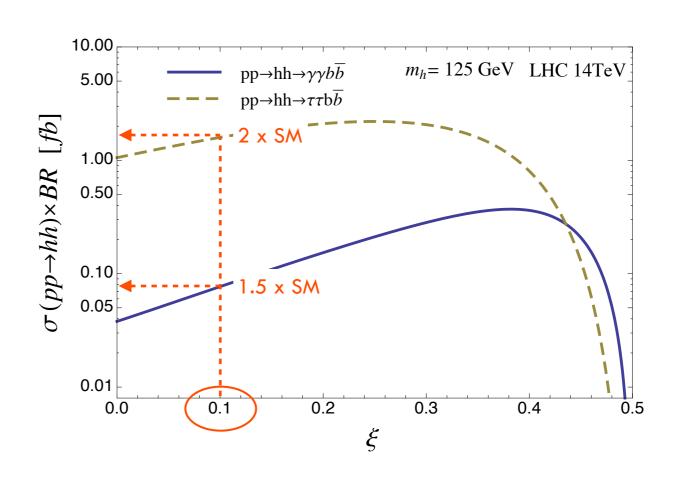
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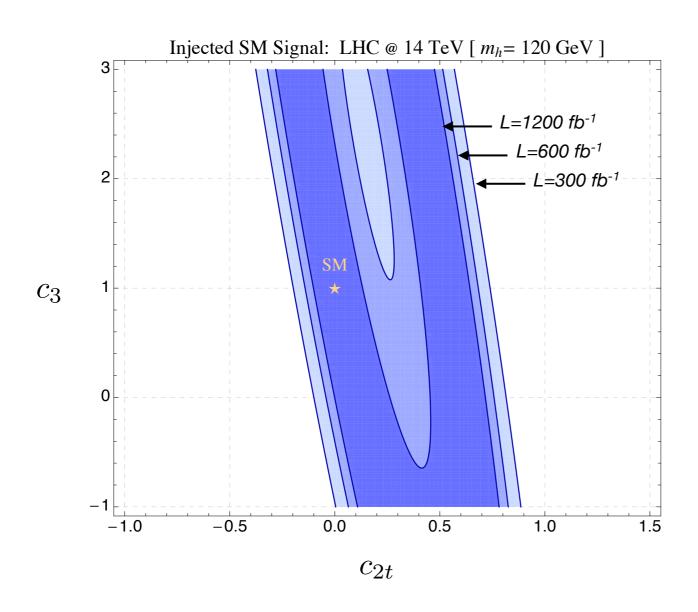
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Dolan, Englert, Spannowsky arXiv:1206.5001



Precision on couplings

Ex: Injected SM $(c_1=c_3=1 c_2=0)$

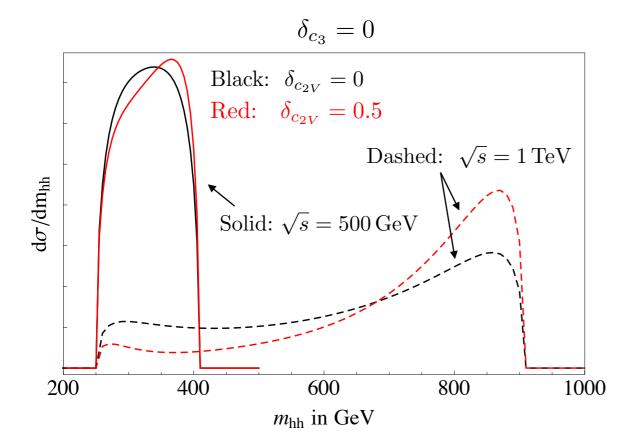


- curves at 68% prob.

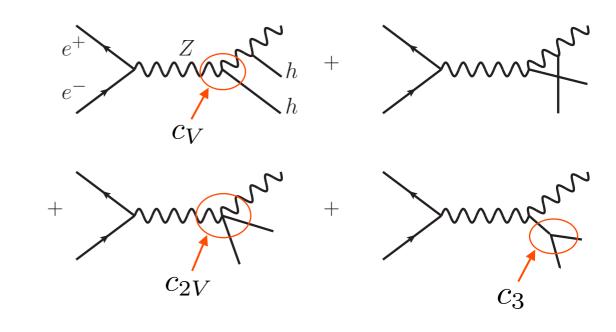
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[RC, Grojean, Pappadopulo, Rattazzi, Thamm arXiv:1309.7038]

\sqrt{s}	$\sigma_{SM}(e^+e^- \to hhZ)$
$500\mathrm{GeV}$	$0.16\mathrm{fb}$
$1\mathrm{TeV}$	$0.12\mathrm{fb}$

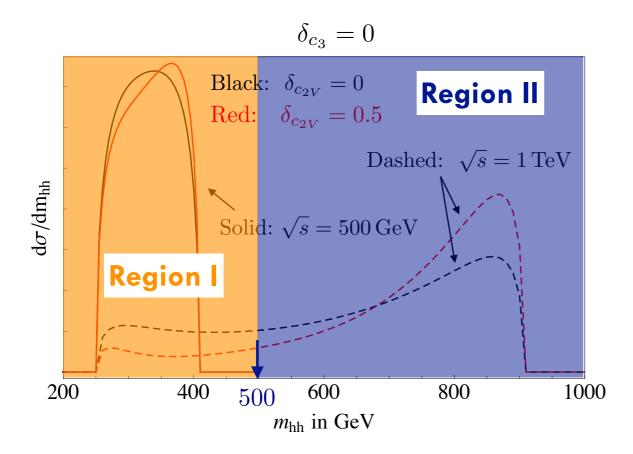


$$\delta_{c_{2V}} \equiv 1 - \frac{c_{2V}}{c_V^2} \qquad \delta_{c_3} \equiv 1 - \frac{c_3}{c_V}$$

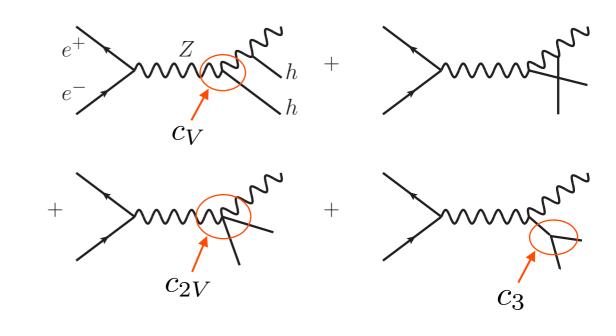


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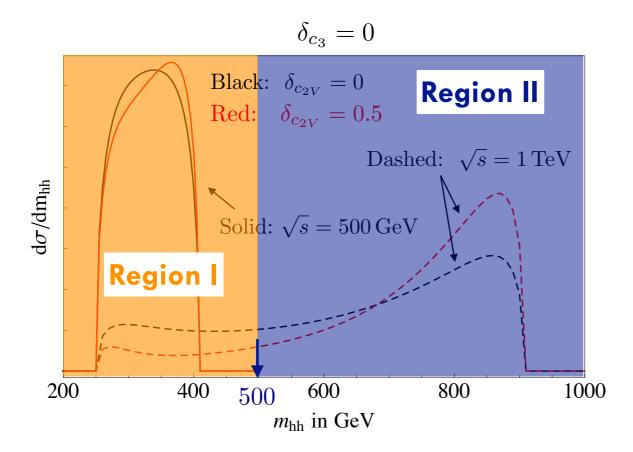


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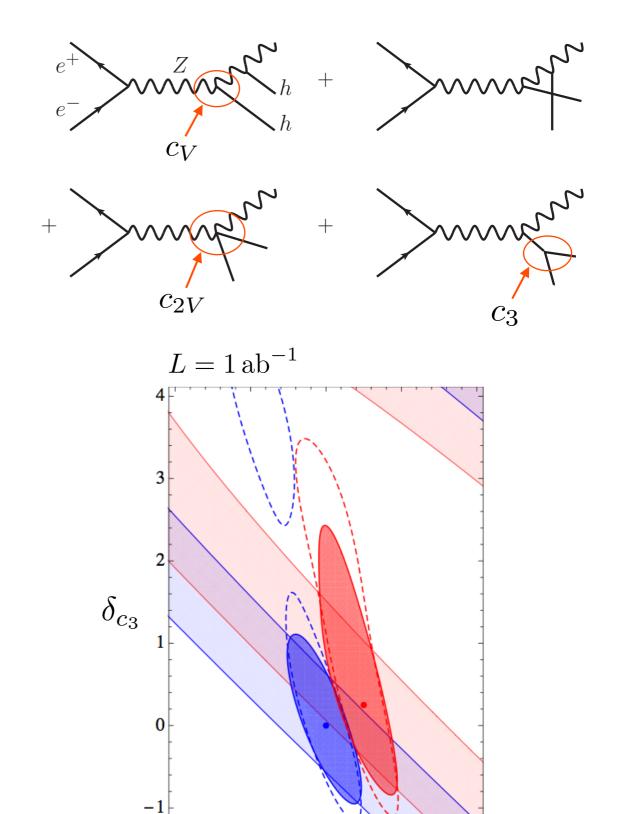


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[Assuming
$$\,c_V^2(BR(b\bar b)/BR(b\bar b)_{SM})=1$$
]

0.5

1.0

0.0

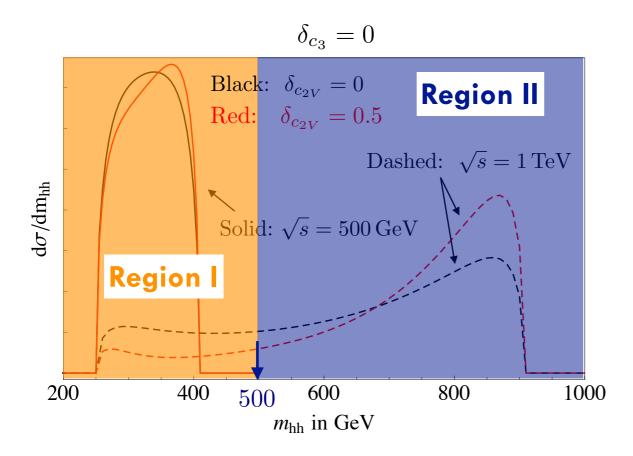
 $\delta_{c_{2V}}$

-0.5

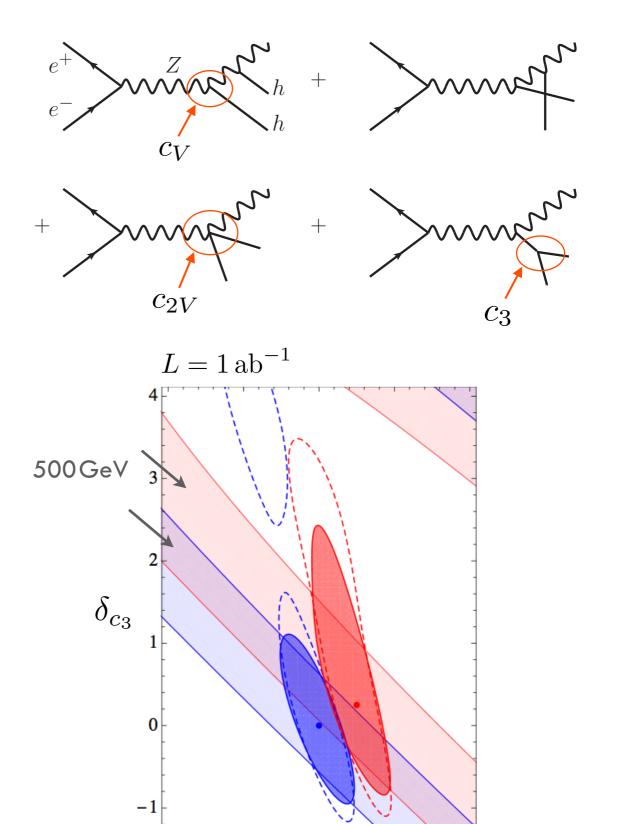
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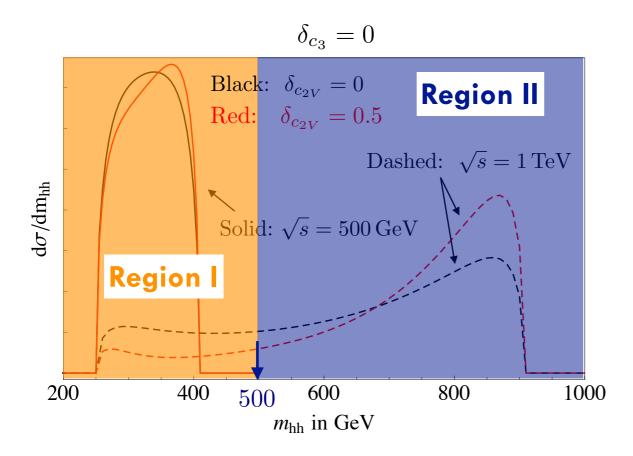
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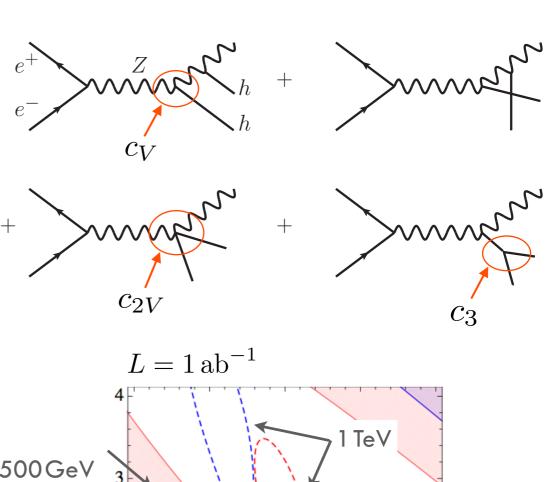
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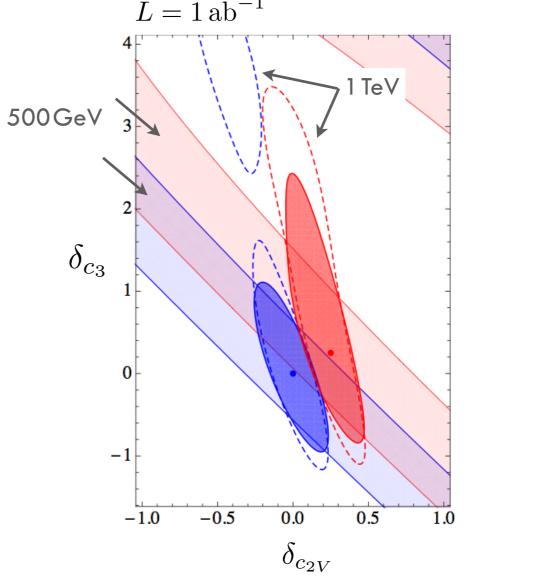
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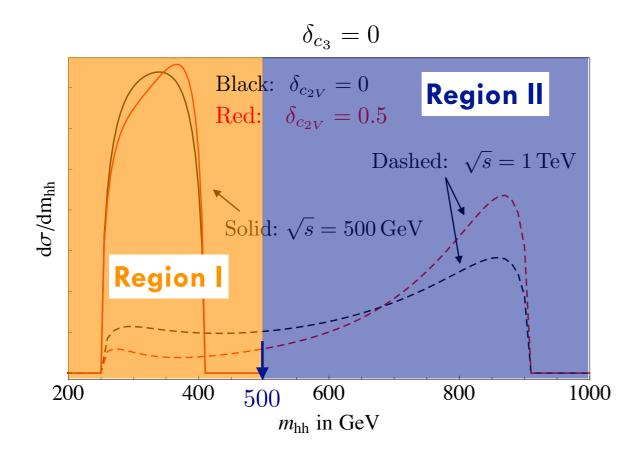




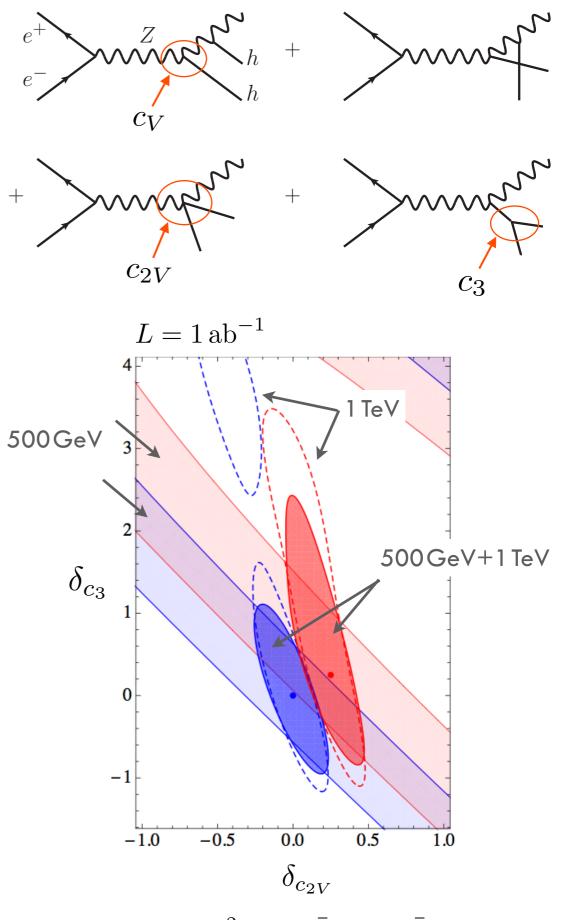
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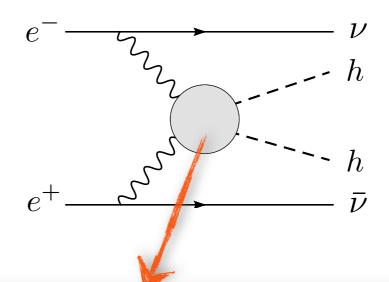
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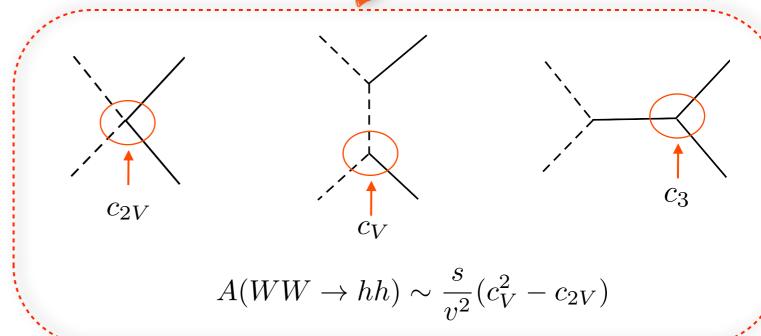
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Double Higgs production via VBF at a 3TeV e⁺e⁻ linear collider (CLIC)

[RC, Grojean, Pappadopulo, Rattazzi, Thamm, arXiv:1309.7038]



$$\sigma_{SM}(e^+e^- \to hh\nu\bar{\nu}) = 0.83 \,\mathrm{fb}$$



dim 6:
$$O_H = \frac{c_H}{2f^2} \partial_\mu |H|^2 \partial^\mu |H|^2$$

dim 8:
$$O_H' = \frac{c_H'}{2f^4} |H|^2 \partial_\mu |H|^2 \partial^\mu |H|^2$$

$$c_V = 1 - \frac{c_H}{2} \frac{v^2}{f^2} + \left(\frac{3c_H^2}{8} - \frac{c_H'}{4}\right) \frac{v^4}{f^4}$$

$$c_{2V} = 1 - 2c_H \frac{v^2}{f^2} + \left(3c_H^2 - \frac{3c_H'}{2}\right) \frac{v^4}{f^4}$$

[Higgs Effective Lagrangian (SILH basis)]

For a PNGB Higgs the whole series in H/f can be re-summed:

$$c_V = \sqrt{1 - \xi}$$

$$c_{2V} = 1 - 2\xi$$

$$\xi = \frac{v^2}{f^2}$$

At dimension-6 level:

$$\Delta c_{2V} = 2\Delta c_V^2 \left(1 + O(\Delta c_V^2) \right)$$

$$\Delta c_{2V} \equiv 1 - c_{2V}$$
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Exp. precision $\sim 1\%$



Test dim-8 operators

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Test dim-8 operators

Expected precision with $L\!=\!1\,\mathrm{ab}^{-1}$: (SM injected)

$$5\%$$
 on c_{2V} 30% on c_3

Much stronger sensitivity on c_{2V} than on c_3

The newly discovered particle at 125GeV looks very much like a Higgs boson, doublet of SU(2)_L

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- Too early to say it is elementary, though (low-energy) compositeness currently not favored by LEP precision tests, searches for top partners and Higgs mass value
- Strength of EWSB dynamics (and its origin) can be inferred from:
 - single-Higgs data (Higgs couplings)
 - key scattering processes

for SUSY: coupling to bottom (c_b); $\gamma\gamma$ and gg rates; production of Heavy Higgses

for Comp. Higgs: tree-level couplings; Zy rate; double Higgs production