# HIGGS COMPOSITENESS: CURRENT STATUS AND FUTURE STRATEGIES 

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CERN Theory Colloquium - 4 December, 2013

## Outline

- Strong vs Weak EWSB
- Current Status of Higgs Compositeness:

1. Higgs mass
2. EW Precision Tests
3. Impact of Searches for top partners
4. Impact of data on Higgs couplings

- Future Strategies

Strong vs Weak EWSB

In the $\{\mathrm{SM}-\mathrm{H}\}$


$$
A\left(W_{L} W_{L} \rightarrow W_{L} W_{L}\right)=A(\chi \chi \rightarrow \chi \chi) \sim \frac{E^{2}}{v^{2}} \equiv g^{2}(E)
$$

In the $\{S M-H\}+H$

$$
\begin{aligned}
& \text { ' } \\
& A \sim \frac{E^{2}}{v^{2}}\left(1-c_{V}^{2}\right)-c_{V}^{2} \frac{m_{h}^{2}}{v^{2}} \frac{s}{s-m_{h}^{2}}
\end{aligned}
$$

In the $\{\mathrm{SM}-\mathrm{H}\}$


$$
A\left(W_{L} W_{L} \rightarrow W_{L} W_{L}\right)=A(\chi \chi \rightarrow \chi \chi) \sim \frac{E^{2}}{v^{2}} \equiv g^{2}(E)
$$

In the $\{S M-H\}+H$

Elementary Higgs:

$$
c_{V}=1
$$

$$
\begin{aligned}
& A \sim \frac{E^{2}}{v^{2}}\left(1-c_{V}^{2}\right)-c_{V}^{2} \frac{m_{h}^{2}}{v^{2}} \frac{s}{s-m_{h}^{2}} \\
& \quad=0
\end{aligned}
$$



In the $\{\mathrm{SM}-\mathrm{H}\}$

In the $\{S M-H\}+H_{i}$


$$
\begin{gathered}
A \sim \frac{E^{2}}{v^{2}}\left(1-\sum_{i} c_{V i}^{2}\right)+\ldots \\
=0
\end{gathered}
$$

Elementary Higgses: (more than one)

- $\delta c_{V i} \sim O(1)$ possible
- sum rule:

$$
\sum_{i} c_{V i}^{2}=1
$$

## Composite Higgs:


coupling strength grows with energy and saturates at $g_{*} \lesssim 4 \pi$

Energy cartoon:


Analogy with $\pi \pi$ scattering in QCD: $\quad h \leftrightarrow \sigma$
Q: why light and narrow?

Analogy with $\pi \pi$ scattering in QCD: $\quad h \leftrightarrow \sigma$

Q: why light and narrow?

A: the Higgs is itself a (pseudo) NG boson
Georgi \& Kaplan, '80
Kaplan, Georgi, Dimopoulos
ex: $\quad \frac{S O(5)}{S O(4)} \rightarrow \quad 4 \mathrm{NGBs} \quad$ transforming as a $(2,2)$ of $\mathrm{SO}(4) \sim \operatorname{SU}(2)_{\mathrm{Lx}} \operatorname{SU}(2)_{\mathrm{R}}$
Agashe, RC, Pomarol NPB 719 (2005) 165

$$
f^{2}\left|\partial_{\mu} e^{i \pi / f}\right|^{2}=(\partial \pi)^{2}+\frac{(\pi \partial \pi)^{2}}{f^{2}}+\frac{\pi^{2}(\pi \partial \pi)^{2}}{f^{4}}+\ldots
$$

Analogy with $\pi \pi$ scattering in QCD: $\quad h \leftrightarrow \sigma$
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Agashe, RC, Pomarol NPB 719 (2005) 165

$$
f^{2}\left|\partial_{\mu} e^{i \pi / f}\right|^{2}=\left|D_{\mu} H\right|^{2}+\frac{c_{H}}{2 f^{2}}\left[\partial_{\mu}\left(H^{\dagger} H\right)\right]^{2}+\frac{c_{H}^{\prime}}{2 f^{4}}\left(H^{\dagger} H\right)\left[\partial_{\mu}\left(H^{\dagger} H\right)\right]^{2}+\ldots
$$

Giudice et al. JHEP 0706 (2007) 045

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$$

Giudice et al. JHEP 0706 (2007) 045

1. $O\left(v^{2} / f^{2}\right)$ shifts in tree-level Higgs couplings. $\quad \mathrm{Ex}: \quad c_{V}=1-c_{H}\left(\frac{v}{f}\right)^{2}+\ldots$

Analogy with $\pi \pi$ scattering in QCD: $\quad h \leftrightarrow \sigma$

Q: why light and narrow?

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Georgi \& Kaplan, '80
Kaplan, Georgi, Dimopoulos
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Agashe, RC, Pomarol NPB 719 (2005) 165

$$
f^{2}\left|\partial_{\mu} e^{i \pi / f}\right|^{2}=\left|D_{\mu} H\right|^{2}+\frac{c_{H}}{2 f^{2}}\left[\partial_{\mu}\left(H^{\dagger} H\right)\right]^{2}+\frac{c_{H}^{\prime}}{2 f^{4}}\left(H^{\dagger} H\right)\left[\partial_{\mu}\left(H^{\dagger} H\right)\right]^{2}+\ldots
$$

Giudice et al. JHEP 0706 (2007) 045
2. Scatterings involving the Higgs also grow with energy

$$
A(W W \rightarrow h h) \sim \frac{s}{v^{2}}\left(c_{V}^{2}-c_{2 V}\right)
$$



- Hypothesis:
each SM fermion couples to a composite fermionic operator with the same $S U(3)_{c} x S U(2)_{\llcorner } x U(1)_{y}$ quantum numbers

$$
\mathcal{L}=\lambda_{L} \bar{q}_{L} O_{R}+\lambda_{R} \bar{u}_{R} O_{L}+h . c .
$$

$\square$ Hypothesis: each SM fermion couples to a composite fermionic operator with the same $S U(3)_{c} x S U(2)_{\llcorner x U(1) y ~ q u a n t u m ~ n u m b e r s ~}^{\text {n }}$

$$
\mathcal{L}=\lambda_{L} \bar{q}_{L} O_{R}+\lambda_{R} \bar{u}_{R} O_{L}+\text { h.c. }
$$

Quark masses need two such couplings


$$
m_{q} \sim \frac{\lambda_{L}(\mu) \lambda_{R}(\mu)}{g_{*}} v
$$

$$
\mu \sim m_{*}
$$

$\square$ Hypothesis: each SM fermion couples to a composite fermionic operator with the same $S U(3)_{c} x S U(2){ }_{\llcorner } x U(1)_{y}$ quantum numbers

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$$

Quark masses need two such couplings


$$
m_{q} \sim \frac{\lambda_{L}(\mu) \lambda_{R}(\mu)}{g_{*}} v
$$

$$
\mu \sim m_{*}
$$

Similar to linear couplings of elementary gauge fields:

$$
\mathcal{L}=g A_{\mu} J^{\mu}
$$

$\square$ Hypothesis: each SM fermion couples to a composite fermionic operator with the same $S U(3)_{c} x S U(2)_{\llcorner x U(1) y ~ q u a n t u m ~ n u m b e r s ~}^{\text {n }}$


- Fermionic operators can excite composite fermions at low energy:
same as for a conserved current:

$$
\langle 0| O|\chi\rangle=\lambda f
$$

$$
\langle 0| J_{\mu}|\rho\rangle=\epsilon_{\mu}^{r} f_{\rho} m_{\rho}
$$

- Fermionic operators can excite composite fermions at low energy:
same as for a conserved current:

$$
\begin{aligned}
& \left.\begin{array}{c}
\text { vector-like composite fermion } \\
\downarrow \\
\langle 0| O|\chi\rangle
\end{array}\right)=\lambda f
\end{aligned}
$$

$$
\langle 0| J_{\mu}|\rho\rangle=\epsilon_{\mu}^{r} f_{\rho} m_{\rho}
$$

- Fermionic operators can excite composite fermions at low energy:
same as for a conserved current:

- Linear couplings imply mass mixings:

$$
\mathcal{L}=\bar{\psi} i \not \partial \psi+\bar{\chi}\left(i \not \nabla-m_{*}\right) \chi+\lambda f \bar{\psi} U(\pi) \chi+h . c .
$$

rotating to mass eigenbasis:

$$
\binom{\psi}{\chi} \rightarrow\left(\begin{array}{cc}
\cos \varphi & \sin \varphi \\
\sin \varphi & \cos \varphi
\end{array}\right)\binom{\psi}{\chi} \quad \tan \varphi=\frac{\lambda f}{m_{*}}
$$

$\varphi$ parametrizes the degree of compositeness of the SM fermions

$$
\begin{aligned}
|\mathrm{SM}\rangle & =\cos \varphi|\psi\rangle+\sin \varphi|\chi\rangle \\
|\operatorname{heavy}\rangle & =-\sin \varphi|\psi\rangle+\cos \varphi|\chi\rangle
\end{aligned}
$$

## Higgs mass

Can a 125 GeV Higgs be composite?

## Structure of the Higgs Potential

$$
V(h)=\frac{m_{*}^{4}}{g_{*}^{2}} \frac{N_{c}}{8 \pi^{2}}\left[\lambda^{2} \sum_{i} A_{i}(h / f)+\lambda^{4} \sum_{i} B_{i}(h / f)+\ldots\right]
$$

$A_{i}(x), B_{i}(x) \quad \mathrm{SO}(4)$ structures
$\rightarrow$ trigonometric functions: $\sin ^{2}(x)$
$\sin ^{4}(x)$ !

$$
h \equiv \sqrt{H^{\dagger} H}
$$

explicit


$$
\frac{S O(5)}{S O(4)}=S^{4} \quad \begin{gathered}
\text { vacuum manifold } \\
\text { the } 4 \text {-sphere }
\end{gathered}
$$

## Structure of the Higgs Potential

$$
V(h)=\frac{m_{*}^{4}}{g_{*}^{2}} \frac{N_{c}}{8 \pi^{2}}\left[\lambda^{2} \sum_{i} A_{i}(h / f)+\lambda^{4} \sum_{i} B_{i}(h / f)+\ldots\right]
$$

$$
h \equiv \sqrt{H^{\dagger} H}
$$

explicit breaking of Goldstone
symmetry (spurion couplings)
$A_{i}(x), B_{i}(x) \quad \mathrm{SO}(4)$ structures
$\rightarrow$ trigonometric functions: $\sin ^{2}(x)$
$\sin ^{4}(x)$ :

## Structure of the Higgs Potential

loop integral saturated at the compositeness scale
$V(h)=\frac{m_{*}^{4}}{g_{*}^{2}} \frac{N_{c}}{8 \pi^{2}} \underbrace{\lambda^{2} \sum_{i} A_{i}(h / f)+\lambda_{i}^{4} \sum_{i} B_{i}} \begin{gathered}\text { explicit breaking of Goldstone } \\ \text { symmetry (spurion couplings) }\end{gathered}$
$A_{i}(x), B_{i}(x) \quad \mathrm{SO}(4)$ structures

$$
h \equiv \sqrt{H^{\dagger} H}
$$

explicit breaking

vacuum manifold is the 4 -sphere

## Structure of the Higgs Potential

loop integral saturated at the compositeness scale

$$
V(h)=\frac{m_{*}^{4}}{g_{*}^{2}} \frac{N_{c}}{8 \pi^{2}}\left[\lambda^{2} \sum_{i} A_{i}(h / f)+\lambda^{4} \sum_{i} B_{i}(h / f)+\ldots\right]
$$

explicit breaking of Goldstone
symmetry (spurion couplings)
$A_{i}(x), B_{i}(x) \quad \mathrm{SO}(4)$ structures
$\rightarrow$ trigonometric functions: $\sin ^{2}(x)$

$$
\sin ^{4}(x)
$$

!

- To get EWSB ( $0<x \ll \pi$ ) at least two SO(4) structures are needed plus some tuning

$$
F T=O\left(\frac{v^{2}}{f^{2}}\right)
$$

- If EWSB is triggered at $O\left(\lambda^{2}\right)$


$$
\begin{aligned}
V(h) & \simeq \frac{m_{*}^{4}}{g_{*}^{2}} \frac{N_{c}}{8 \pi^{2}} \lambda_{L, R}^{2} A\left(\frac{h}{f}\right) \\
m_{h}^{2} & \sim \frac{N_{c}}{4 \pi^{2}} \frac{m_{*}^{2}}{f^{2}} \lambda_{L, R}^{2} v^{2}
\end{aligned}
$$

- If EWSB is triggered at $O\left(\lambda^{2}\right)$
$\underbrace{t_{L, R}} \quad V(h) \simeq \frac{m_{*}^{4}}{g_{*}^{2}} \frac{N_{c}}{8 \pi^{2}} \lambda_{L, R}^{2} A\left(\frac{h}{f}\right)$


$$
m_{h}^{2} \sim \frac{N_{c}}{4 \pi^{2}} g_{*}^{3} y_{t} v^{2}=\left(330 \mathrm{GeV} \times\left(\frac{g_{*}}{3}\right)^{3 / 2}\right)^{2}
$$

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$\underbrace{t_{L, R}} \quad V(h) \simeq \frac{m_{*}^{4}}{g_{*}^{2}} \frac{N_{c}}{8 \pi^{2}} \lambda_{L, R}^{2} A\left(\frac{h}{f}\right)$


$$
m_{h}^{2} \sim \frac{N_{c}}{4 \pi^{2}} g_{*}^{3} y_{t} v^{2}=\underbrace{\left.330 \mathrm{GeV} \nsim\left(\frac{g_{*}}{3}\right)^{3 / 2}\right)^{2}}
$$

Higgs tends to be too heavy (unless $g_{*} \sim 1$ )

- If EWSB is triggered at $O\left(\lambda^{2}\right)+t_{\mathrm{R}}$ fully composite
$V(h) \simeq \frac{m_{*}^{4}}{g_{*}^{2}} \frac{N_{c}}{8 \pi^{2}} \lambda_{L}^{2} A\left(\frac{h}{f}\right)$
$m_{h}^{2} \sim \frac{N_{c}}{4 \pi^{2}} \frac{m_{*}^{2}}{f^{2}} \lambda_{L}^{2} v^{2}$


$$
{m_{L}}_{2}^{\sim} \sim \frac{N_{c}}{4 \pi^{2}} g_{*}^{2} y_{t}^{2} v^{2}=\left(175 \mathrm{GeV} \times\left(\frac{g_{*}}{3}\right)\right)^{2}
$$

$\square$ If EWSB is triggered at $O\left(\lambda^{2}\right)+t_{\mathrm{R}}$ fully composite

$$
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& V(h) \simeq \frac{m_{*}^{4}}{g_{*}^{2}} \frac{N_{c}}{8 \pi^{2}} \lambda_{L}^{2} A\left(\frac{h}{f}\right) \\
& m_{h}^{2} \sim \frac{N_{c}}{4 \pi^{2}} \frac{m_{*}^{2}}{f^{2}} \lambda_{L}^{2} v^{2}
\end{aligned}
$$



$$
\begin{aligned}
& \lambda_{L} \simeq y_{t} \\
& m_{h}^{2} \sim \frac{N_{c}}{4 \pi^{2}} g_{*}^{2} y_{t}^{2} v^{2}=\left(175 \mathrm{GeV} \times\left(\frac{g_{*}}{3}\right)\right)^{2}
\end{aligned}
$$

$\mathrm{m}_{\mathrm{H}}=125 \mathrm{GeV}$ implies that top partners are naturally

- not too strongly coupled, hence
- not too heavy

Matsedonskyi, Panico, Wulzer JHEP 1301 (2013) 164
Redi, Tesi JHEP 1210 (2012) 166
Marzocca, Serone, Shu JHEP 1208 (2012) 013
Pomarol, Riva JHEP 1208 (2012) 135
Panico, Redi, Tesi, Wulzer JHEP 1303 (2013) 051
De Simone et al. JHEP 1304 (2013) 004
$\square$ If EWSB is triggered at $O\left(\lambda^{2}\right)+t_{\mathrm{R}}$ fully composite

$$
\begin{aligned}
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\end{aligned}
$$

$$
\lambda_{L} \simeq y_{t}
$$

$$
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$$

$\mathrm{m}_{\mathrm{H}}=125 \mathrm{GeV}$ implies that top partners are naturally

- not too strongly coupled, hence - not too heavy

$$
F T \sim \frac{v^{2}}{f^{2}} \sim \frac{m_{h}^{2}}{m_{*}^{2}} \frac{4 \pi^{2}}{N_{c} y_{t}^{2}}=\left(\frac{525 \mathrm{GeV}}{m_{*}}\right)^{2}
$$

Redi, Tesi JHEP 1210 (2012) 166
Marzocca, Serone, Shu JHEP 1208 (2012) 013
Pomarol, Riva JHEP 1208 (2012) 135
Panico, Redi, Tesi, Wulzer JHEP 1303 (2013) 051
De Simone et al. JHEP 1304 (2013) 004

- If EWSB is triggered at $O\left(\lambda^{4}\right)$


$$
V(h) \simeq \frac{m_{*}^{4}}{g_{*}^{2}} \frac{N_{c}}{8 \pi^{2}}\left[\lambda_{L, R}^{2} A\left(\frac{h}{f}\right)+\frac{\lambda_{L}^{2} \lambda_{R}^{2}}{g_{*}^{2}} B\left(\frac{h}{f}\right)\right]
$$

- If EWSB is triggered at $O\left(\lambda^{4}\right)$
extra tuning required to suppress

$O\left(\lambda^{2}\right)$ terms down to $O\left(\lambda^{4}\right)$

$$
V(h) \simeq \frac{m_{*}^{4}}{g_{*}^{2}} \frac{N_{c}}{8 \pi^{2}}\left[\lambda_{L, R}^{2} A\left(\frac{h}{f}\right)+\frac{\lambda_{L}^{2} \lambda_{R}^{2}}{g_{*}^{2}} B\left(\frac{h}{f}\right)\right]
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$$

$$
m_{h}^{2} \sim \frac{N_{c}}{4 \pi^{2}} \frac{m_{*}^{2}}{f^{2}} \frac{\lambda_{L}^{2} \lambda_{R}^{2}}{g_{*}^{2}} v^{2} \sim \frac{N_{c}}{4 \pi^{2}} g_{*}^{2} y_{t}^{2} v^{2}=\left(175 \mathrm{GeV} \times\left(\frac{g_{*}}{3}\right)\right)^{2}
$$

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extra tuning required to suppress
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$$

$$
F T \sim \frac{v^{2}}{f^{2}} \times \frac{\lambda^{2}}{g_{*}^{2}} \simeq\left(\frac{525 \mathrm{GeV}}{m_{*}}\right)^{2} \times \frac{y_{t}}{g_{*}}
$$

$\mathrm{m}_{\mathrm{H}}$ automatically lighter but larger tuning to get EWSB

Panico, Redi, Tesi, Wulzer JHEP 1303 (2013) 051

## Constraints on $c_{V}$ from EW Precision Tests



fit from: GFitter coll. Eur. Phys. J. C 72 (2012) 2205

$$
\begin{aligned}
\Delta \epsilon_{1} & =-\frac{3}{16 \pi} \frac{\alpha_{e m}}{\cos ^{2} \theta_{W}} \log \frac{\Lambda^{2}}{m_{Z}^{2}} \\
\Delta \epsilon_{3} & =+\frac{1}{12 \pi} \frac{\alpha_{e m}}{4 \sin ^{2} \theta_{W}} \log \frac{\Lambda^{2}}{m_{Z}^{2}}
\end{aligned}
$$

## Constraints on $c_{V}$ from EW Precision Tests


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& \Delta \epsilon_{3}=+\frac{1}{12 \pi} \frac{\alpha_{e m}}{4 \sin ^{2} \theta_{W}} \log \frac{\Lambda^{2}}{m_{Z}^{2}}
\end{aligned}
$$




Ciuchini, Franco, Silvestrini, Mishima, arXiv:1 306.4644

## Constraints on $c_{V}$ from EW Precision Tests


fit from: GFitter coll. Eur. Phys. J. C 72 (2012) 2205

Precision on cv at the level of $\sim 5 \%$ !

Contribution from resonances REQUIRED to relax the bound

Ciuchini, Franco, Silvestrini, Mishima, arXiv:1306.4644


M. Ciuchini, E. Franco, L. Silvestrini,
S. Mishima, arXiv: 1306.4644

- Analyticity and crossing symmetry imply a sum rule on $c_{V}$

$$
1-c_{V}^{2}=\frac{v^{2}}{6 \pi} \int_{0}^{\infty} \frac{d s}{s}\left(2 \sigma_{I=0}^{t o t}(s)+3 \sigma_{I=1}^{t o t}(s)-5 \sigma_{I=2}^{t o t}(s)\right)
$$

Falkowski, Rychkov, Urbano, JHEP 1204 (2012) 073
Low, Rattazzi, Vichi, JHEP 1004 (2010) 126
$c_{V}>1$ possible only if $\mathrm{I}=2$ ch. dominates $\mathrm{V}_{\mathrm{L}} \mathrm{V}_{\mathrm{L}}$ scattering (requires: doubly-charged scalar resonance)

## S parameter $\quad \hat{S}=\hat{S}_{I R}+\hat{S}_{U V}$



$$
\hat{S}_{U V} \sim g^{2} \frac{v^{2}}{f^{2}}\left[\frac{1}{g_{*}^{2}}+N_{c} N_{F} \frac{1}{16 \pi^{2}} \log \left(\frac{\Lambda}{m_{*}}\right)+\ldots\right]
$$

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1-loop contribution from fermions can be large (!)

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Golden, Randall, NPB 361 (1991) 3
Barbieri, Isidori, Pappadopulo, JHEP O902 (2009) }02
Grojean, Matsedonskyi, Panico, JHEP 1310 (2013)160
Azatov, RC, Di lura, Galloway, PRD 88 (2013) 075019
```

$$
i \int d^{4} x e^{i q \cdot(x-y)}\langle 0| T\left(J_{\mu}(x) J_{\nu}(y)\right)|0\rangle=\left(q^{2} \eta_{\mu \nu}-q_{\mu} q_{\nu}\right) \Pi\left(q^{2}\right) \quad \Pi\left(q^{2}\right)=\int d s \frac{\rho(s)}{q^{2}-s+i \epsilon}
$$

$$
\hat{S}_{U V}=\frac{g^{2}}{4} \sin ^{2} \theta \int \frac{d s}{s}\left[\rho_{L L}(s)+\rho_{R R}(s)-2 \rho_{B B}(s)\right]
$$

$$
\begin{array}{ll}
i \int d^{4} x e^{i q \cdot(x-y)}\langle 0| T\left(J_{\mu}(x) J_{\nu}(y)\right)|0\rangle=\left(q^{2} \eta_{\mu \nu}-q_{\mu} q_{\nu}\right) \Pi\left(q^{2}\right) & \Pi\left(q^{2}\right)=\int d s \frac{\rho(s)}{q^{2}-s+i \epsilon} \\
\hat{S}_{U V}=\frac{g^{2}}{4} \sin ^{2} \theta \int \frac{d s}{s}\left[\rho_{L L}(s)+\rho_{R R}(s)-2 \rho_{B B}(s)\right] & \begin{array}{c}
\text { negative contribution from } \\
\text { spectral function of broken } \\
\text { SO(5)/SO(4) currents }
\end{array}
\end{array}
$$

$$
i \int d^{4} x e^{i q \cdot(x-y)}\langle 0| T\left(J_{\mu}(x) J_{\nu}(y)\right)|0\rangle=\left(q^{2} \eta_{\mu \nu}-q_{\mu} q_{\nu}\right) \Pi\left(q^{2}\right) \quad \Pi\left(q^{2}\right)=\int d s \frac{\rho(s)}{q^{2}-s+i \epsilon}
$$

$$
\hat{S}_{U V}=\frac{g^{2}}{4} \sin ^{2} \theta \int \frac{d s}{s}\left[\rho_{L L}(s)+\rho_{R R}(s)-2 \rho_{B B}(s)\right] \quad \begin{aligned}
& \text { negative contribution from } \\
& \text { spectral function of broken } \\
& \mathrm{SO}(5) / \mathrm{SO}(4) \text { currents }
\end{aligned}
$$

Example: [Azatov, RC, Di lura, Galloway, PRD 88 (2013) 075019 ]

$$
\psi_{5}=(1,1)+(2,2) \quad \mathcal{L}=\bar{\psi}_{1}\left(i \not D-m_{1}\right) \psi_{1}+\bar{\psi}_{4}\left(i \not \supset-m_{4}\right) \psi_{4}-\zeta \bar{\psi}_{4} \gamma^{\mu} d_{\mu} \psi_{1}+h . c .
$$


$\rho_{L L, R R}$
$\rho_{B B}$

$$
i \int d^{4} x e^{i q \cdot(x-y)}\langle 0| T\left(J_{\mu}(x) J_{\nu}(y)\right)|0\rangle=\left(q^{2} \eta_{\mu \nu}-q_{\mu} q_{\nu}\right) \Pi\left(q^{2}\right) \quad \Pi\left(q^{2}\right)=\int d s \frac{\rho(s)}{q^{2}-s+i \epsilon}
$$

$$
\hat{S}_{U V}=\frac{g^{2}}{4} \sin ^{2} \theta \int \frac{d s}{s}\left[\rho_{L L}(s)+\rho_{R R}(s)-2 \rho_{B B}(s)\right] \quad \begin{aligned}
& \text { negative contribution from } \\
& \text { spectral function of broken } \\
& \mathrm{SO}(5) / \mathrm{SO}(4) \text { currents }
\end{aligned}
$$

Example: [Azatov, RC, Di lura, Galloway, PRD 88 (2013) 075019]

$$
\not A+i \frac{\pi \not \partial \pi}{f^{2}}+\ldots
$$

$$
\psi_{5}=(1,1)+(2,2)
$$

$$
\left.\mathcal{L}=\bar{\psi}_{1}\left(i \not D-m_{1}\right) \psi_{1}+\bar{\psi}_{4} \xlongequal{\uparrow}-m_{4}\right) \psi_{4}-\zeta \bar{\psi}_{4} \gamma^{\mu} d_{\mu} \psi_{1}+h . c .
$$


$\rho_{L L, R R}$
$\rho_{B B}$

## fermion contribution can be negative

## Best seen using a dispertion relation:

Orgogozo and Rychkov, JHEP 1306 (2013) 014

$$
i \int d^{4} x e^{i q \cdot(x-y)}\langle 0| T\left(J_{\mu}(x) J_{\nu}(y)\right)|0\rangle=\left(q^{2} \eta_{\mu \nu}-q_{\mu} q_{\nu}\right) \Pi\left(q^{2}\right) \quad \Pi\left(q^{2}\right)=\int d s \frac{\rho(s)}{q^{2}-s+i \epsilon}
$$

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$$

$\hat{S}_{U V}=\frac{8}{3} \frac{m_{W}^{2}}{16 \pi^{2} f^{2}} N_{c} N_{F}\left(1-|\zeta|^{2}\right) \log \left(\frac{\Lambda^{2}}{m_{(2,2)}^{2}}\right)+$ finite terms
from: Azatov, RC, Di lura, Galloway PRD 88 (2013) 075019

## $\mathrm{SO}(5) / \mathrm{SO}(4)$ model:

$$
\begin{aligned}
& \psi_{5}=(1,1)_{2 / 3}+(2,2)_{2 / 3} \\
& \psi_{10}=(2,2)_{-1 / 3}+(1,3)_{-1 / 3}+(3,1)_{-1 / 3}
\end{aligned}
$$


$\mathrm{SO}(5) / \mathrm{SO}(4)$ model:
$\psi_{5}=(1,1)_{2 / 3}+(2,2)_{2 / 3}$
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Ex: for $\quad f=800 \mathrm{GeV} \quad g_{\rho}=3$
$\Delta S_{\rho} \simeq 0.13 \quad \Delta S_{\psi} \simeq 0.8 \times\left(1-|\zeta|^{2}\right) \quad \Rightarrow \quad$ strong sensitivity on $\zeta$

O(10\%) tuning required to go back into the experimental ellipse

T parameter $\quad \hat{T}=\hat{T}_{I R}+\hat{T}_{U V}$

$\hat{T}_{U V} \sim \frac{v^{2}}{f^{2}}\left[\frac{g^{\prime 2}}{16 \pi^{2}} \log \left(\frac{\Lambda}{m_{\rho}}\right)+N_{c} \frac{\lambda_{L}^{2}}{16 \pi^{2}} \frac{\lambda_{L}^{2}}{g_{*}^{2}}+\ldots\right]$

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## T parameter $\quad \hat{T}=\hat{T}_{I R}+\hat{T}_{U V}$



- Custodial symmetry implies:

1. No $\hat{T}$ at tree-level
2. fermion correction is finite and starts at $O\left(\lambda_{L}^{4}\right)$ (only top partners contribute)

$\Delta \hat{T}>0$ possible though not fully generic

Example: model with $\psi_{4}=(2,2)_{2 / 3}+t_{R}$ composite

Carena, et al. NPB 759 (2006) 202; PRD 76 (2007) 035006 Barbieri et al. PRD 76 (2007) 115008
Lodone JHEP 0812 (2008) 029
Pomarol, Serra, PRD 78 (2008) 074026
Gillioz PRD 80 (2009) 055003
Grojean, Matsedonskyi, Panico, JHEP 1310 (2013) 160
$\mathcal{L}=\bar{q}_{L} i \not D q_{L}+\bar{t}_{R} i \not D t_{R}+\bar{\psi}_{4}\left(i \not \nabla-m_{4}\right) \psi_{4}$

$$
+i \zeta \bar{\psi}_{4}^{i} \gamma^{\mu} d_{\mu}^{i} t_{R}+y_{L t} f \bar{q}_{L} U(\pi) t_{R}+y_{L 4} f \bar{q}_{L} U(\pi) \psi_{4}+\text { h.c. }
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Grojean, Matsedonskyi, Panico JHEP 1310 (2013) 160

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Searches of top partners

- Typical spectrum of top partners

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- Two main production modes:


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- Two main production modes:


- Two-body decay modes:


- Current experimental status in a nutshell

1. Almost all decays looked for
2. Analyses optimized on pair production

ATLAS Preliminary Status: Lepton-Photon 2013
 $\sqrt{s}=8 \mathrm{TeV}$ $\int L d t=14.3 \mathrm{fb}^{-1}$ $\mathrm{Ht}+\mathrm{X}$ [ATLAS-CONF-2013-018] Same-Sign [ATLAS-CONF-2013-051] Zb/t+X [ATLAS-CONF-2013-056] Wb+X [ATLAS-CONF-2013-060]
$\star \operatorname{SU}(2)(\mathrm{T}, \mathrm{B})$ doub.

- $\operatorname{SU}(2)$ singlet


CMS preliminary $\sqrt{\mathrm{s}}=8 \mathrm{TeV} \quad 19.6 \mathrm{fb}^{-1}$


CMS B2G-12-015 CMS B2G-12-012

- Two-body decay modes:

$\square$ Current experimental status in a nutshell

1. Almost all decays looked for

## Limits in the $700-800 \mathrm{GeV}$ range

2. Analyses optimized on pair production

ATLAS Preliminary Status: Lepton-Photon 2013

|  | $\int L d t=14.3 \mathrm{fb}^{-1}$ |
| :---: | :---: |
| - $95 \%$ CL exp. excl. |  |
| $\mathrm{Ht}+\mathrm{X}$ | [ATLAS-CONF-2013-018] |
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```
M4, \xi=\frac{\mp@subsup{v}{}{2}}{\mp@subsup{f}{}{2}}=0.2
```

Multiplicity of states, connection among masses and inclusion of single production amplify limits on individual particles

$\square$ Once recast on (simplified) theory space exp. bounds already exclude a big portion of the natural region


Multiplicity of states, connection among masses and inclusion of single production amplify limits on individual particles

1 TeV masses typically excluded
LHC has already eaten up a big part of the natural region


- Improving the limits still possible with current data

Ex: - optimize searches to include single production

- include single-lepton final states
- use boosted jet techniques


Higgs couplings

- LHC data currently set limits on modifications of the Higgs couplings at the 20-30\% level

$$
c_{V}=1+F\left(\frac{v^{2}}{f^{2}}\right)+O\left(\frac{v^{2}}{f^{2}} \frac{g_{G t}^{2}}{g_{*}^{2}}\right)
$$

$$
c_{\psi}=1+F_{\psi}\left(\frac{v^{2}}{f^{2}}, \frac{m_{i}}{m_{j}}\right)+O\left(\frac{v^{2}}{f^{2}} \frac{\lambda^{2}}{g_{*}^{2}}\right)
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$$
\begin{gathered}
O\left(v^{2} / f^{2}\right) \text { from Higgs nlom } \\
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| $\xi \equiv \frac{v^{2}}{f^{2}}$ |
| :--- |
| MCHM5: |$c_{V}=\sqrt{1-\xi} \quad c_{V}=c_{\psi}=\sqrt{1-\xi} \quad$| Agashe, RC, Pomarol, |
| :---: |
| NPB 719 (2005) 165 |



Red points at $\xi \equiv(v / f)^{2}=0.2,0.5,0.8$

$\xi \equiv \frac{v^{2}}{f^{2}}$

MCHM4: $\quad c_{V}=c_{\psi}=\sqrt{1-\xi}$

MCHM5: $\quad c_{V}=\sqrt{1-\xi} \quad c_{\psi}=\frac{1-2 \xi}{\sqrt{1-\xi}}$

## RC, DaRold, Pomarol,

## PRD 75 (2007) 055014

Carena, Ponton, Santiago, Wagner, PRD 76 (2007) 035006

Minimal Composite Higgs [MCHM5]



- Modifications to loop-level couplings ggh, $\gamma \gamma h$ suppressed due to the Goldstone symmetry


Effective operators violate the Higgs shift symmetry:

$$
H^{i} \rightarrow H^{i}+\zeta^{i}
$$

- Modifications to loop-level couplings ggh, $\gamma \gamma h$ suppressed due to the Goldstone symmetry


$$
\left.\frac{\delta \Gamma}{\Gamma_{S M}}=1+O\left(\frac{v^{2}}{f^{2}}\right)+O\left(\frac{g_{*}^{2} v^{2}}{m_{*}^{2}} \times \frac{\lambda^{2}}{g_{*}^{2}}\right) \right\rvert\,
$$

Large modifications possible in $\Gamma(h \rightarrow Z \gamma)$
Azatov, RC, Di lura, Galloway, PRD 88 (2013) 075019

Relevant operator is $O_{H W}-O_{H B}$
$O_{H B}=\left(D^{\mu} H\right)^{\dagger}\left(D^{\nu} H\right) B_{\mu \nu}$
$O_{H W}=\left(D^{\mu} H\right)^{\dagger} \sigma^{i}\left(D^{\nu} H\right) W_{\mu \nu}^{i}$


1. Invariant under Higgs shift symmetry
2. Odd under LR exchange

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Large modifications possible in $\Gamma(h \rightarrow Z \gamma)$
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$$
\frac{\delta \Gamma(Z \gamma)}{\Gamma_{S M}(Z \gamma)}=O\left(\frac{v^{2}}{f^{2}}\right)+O\left(\frac{g_{*}^{2} v^{2}}{m_{*}^{2}}\right)
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Strong dynamics MUST break LR
$A(h \rightarrow Z \gamma)=A_{S M} \times F(\xi)+\delta A$

$$
\frac{\delta A}{A_{S M}} \sim N_{c} N_{F}\left(\frac{g_{*}^{2} v^{2}}{m_{*}^{2}}\right) \sim N_{c} N_{F} \frac{v^{2}}{f^{2}} \frac{\Delta m_{*}^{2}}{m_{*}^{2}}
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$$
\left.\begin{array}{l}
\text { shift of tree-level } \\
\begin{array}{l}
\text { Higgs couplings } \\
\text { from nlom }
\end{array} \\
\hline f^{2}
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| shift of tree-level |
| :---: |
| $\begin{array}{c}\text { Higgs couplings } \\ \text { from nlom }\end{array}$ | $1+O\left(\frac{v^{2}}{f^{2}}\right)$

multiplicity of composite states

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multiplicity of composite states

## Future strategies

## Double-Higgs production

## Double Higgs Production via gluon fusion


$+$

$+$


## Double Higgs Production via gluon fusion

$$
\Delta \mathcal{L}^{(6)}=\frac{\bar{c}_{H}}{2 v^{2}}\left[\partial_{\mu}\left(H^{\dagger} H\right)\right]^{2}+\frac{\bar{c}_{u}}{v^{2}} y_{u} H^{\dagger} H \bar{q}_{L} H^{c} u_{R}-\frac{\bar{c}_{6} \lambda}{v^{2}}\left(H^{\dagger} H\right)^{3}
$$


$+$

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## Double Higgs Production via gluon fusion

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$$


modified Higgs trilinear coupl.
$c_{3} \simeq 1-\frac{3}{2} \bar{c}_{H}+\bar{c}_{6}$
$+$

$+$


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New thh quartic vertex

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$c_{3} \simeq 1-\frac{3}{2} \bar{c}_{H}+\bar{c}_{6}$

Contact vertex from heavy states
$+$

$c_{2 t} \simeq-\frac{1}{2}\left(\bar{c}_{H}+3 \bar{c}_{u}\right)$
$+$


New tthh quartic vertex

## High-energy behavior




RC, Ghezzi, Moretti, Panico, Piccinini, Wulzer
JHEP 1208 (2012) 154


$$
\sim \log ^{2}\left(\frac{m_{t}^{2}}{\hat{s}}\right)
$$

## Suppression of SM triangle diagrams at high-energy implies:

much better sensitivity on $c_{2 t}$ than $c_{3}$

[ First noticed by:
Dib, Rosenfeld, Zerwekh, JHEP 0605 (2006) 074
Grober and Muhlleitner, JHEP 1106 (2011) 020 ]

$$
\sigma(p p \rightarrow h h+X)_{S M}=28.7 \mathrm{fb}
$$

$$
\text { (NLO } K=2 \text { incl.) }
$$



$$
\sigma(p p \rightarrow h h+X)_{S M}=28.7 \mathrm{fb}
$$

$$
\text { (NLO } K=2 \text { incl.) }
$$



- $\quad h h \rightarrow b \bar{b} \gamma \gamma$ seems the best channel

Baur, Plehn, Rainwater, PRD 69 (2004) 053004 ATLAS: ATL-PHYS-PUB-2012-004

- $\quad h h \rightarrow b \bar{b} \tau \tau$ promising in the boosted regime

Dolan, Englert, Spannowsky arXiv: 1206.5001

- $\quad h h \rightarrow b \bar{b} W W$ overwhelmed by $t \bar{t}$ background

Dolan, Englert, Spannowsky arXiv: 1206.5001

$$
\sigma(p p \rightarrow h h+X)_{S M}=28.7 \mathrm{fb}
$$

$$
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For example: in the MCHM5
$c_{t}=c_{3}=\frac{1-2 \xi}{\sqrt{1-\xi}}$
$c_{2 t}=-2 \xi$

$$
\xi \equiv \frac{v^{2}}{f^{2}}
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$c_{t}=c_{3}=\frac{1-2 \xi}{\sqrt{1-\xi}}$
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$$
\xi \equiv \frac{v^{2}}{f^{2}}
$$

## Precision on couplings

Ex: Injected SM ( $\left.c_{+}=c_{3}=1 \quad c_{2+}=0\right)$


- curves at 68\% prob.

RC, Ghezzi, Moretti, Panico, Piccinini, Wulzer JHEP 1208 (2012) 154

Double Higgs-strahlung at an $\mathrm{e}^{+} \mathrm{e}^{-}$linear collider with $\sqrt{s}=500 \mathrm{GeV}-1 \mathrm{TeV}$
[ RC, Grojean, Pappadopulo, Rattazzi, Thamm arXiv:1309.7038]

| $\sqrt{s}$ | $\sigma_{S M}\left(e^{+} e^{-} \rightarrow h h Z\right)$ |
| :---: | :---: |
| 500 GeV | 0.16 fb |
| 1 TeV | 0.12 fb |

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\delta_{c_{3}}=0
$$



$+$

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$$
\delta_{c_{2 V}} \equiv 1-\frac{c_{2 V}}{c_{V}^{2}} \quad \delta_{c_{3}} \equiv 1-\frac{c_{3}}{c_{V}}
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Double Higgs production via VBF at a $3 \mathrm{TeV} \mathrm{e}^{+} e^{-}$linear collider (CLIC)
[ RC, Grojean, Pappadopulo, Rattazzi, Thamm, arXiv:1309.7038 ]


$$
\sigma_{S M}\left(e^{+} e^{-} \rightarrow h h \nu \bar{\nu}\right)=0.83 \mathrm{fb}
$$


$\operatorname{dim} 6: \quad O_{H}=\frac{c_{H}}{2 f^{2}} \partial_{\mu}|H|^{2} \partial^{\mu}|H|^{2}$

$$
c_{V}=1-\frac{c_{H}}{2} \frac{v^{2}}{f^{2}}+\left(\frac{3 c_{H}^{2}}{8}-\frac{c_{H}^{\prime}}{4}\right) \frac{v^{4}}{f^{4}}
$$

$\operatorname{dim} 8: \quad O_{H}^{\prime}=\frac{c_{H}^{\prime}}{2 f^{4}}|H|^{2} \partial_{\mu}|H|^{2} \partial^{\mu}|H|^{2}$

$$
c_{2 V}=1-2 c_{H} \frac{v^{2}}{f^{2}}+\left(3 c_{H}^{2}-\frac{3 c_{H}^{\prime}}{2}\right) \frac{v^{4}}{f^{4}}
$$

[ Higgs Effective Lagrangian (SILH basis)]

$$
\text { Ex: } \mathrm{SO}(5) / \mathrm{SO}(4)
$$

For a PNGB Higgs the whole series in $\mathrm{H} / \mathrm{f}$ can be re-summed:

$$
\begin{aligned}
c_{V} & =\sqrt{1-\xi} \\
c_{2 V} & =1-2 \xi
\end{aligned}
$$

$$
\xi=\frac{v^{2}}{f^{2}}
$$

At dimension-6 level:

$$
\Delta c_{2 V}=2 \Delta c_{V}^{2}\left(1+O\left(\Delta c_{V}^{2}\right)\right)
$$

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Suppose:
$\Delta c_{V}^{2} \sim \Delta c_{2 V} \sim 10 \%$
Exp. precision $\sim 1 \%$

Test dim-8
operators

Expected precision with $L=1 \mathrm{ab}^{-1}$ :
(SM injected)
$5 \%$ on $c_{2 V}$
$30 \%$ on $c_{3}$

Much stronger sensitivity on $c_{2 V}$ than on $c_{3}$

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- The newly discovered particle at 125 GeV looks very much like a Higgs boson, doublet of SU(2)
- Too early to say it is elementary, though (low-energy) compositeness currently not favored by LEP precision tests, searches for top partners and Higgs mass value
- Strength of EWSB dynamics (and its origin) can be inferred from:
- single-Higgs data (Higgs couplings)
- key scattering processes
for SUSY: $\quad$ coupling to bottom $\left(c_{b}\right) ; \gamma \gamma$ and $g g$ rates; production of Heavy Higgses
for Comp. Higgs: tree-level couplings; $\mathrm{Z} \gamma$ rate; double Higgs production

