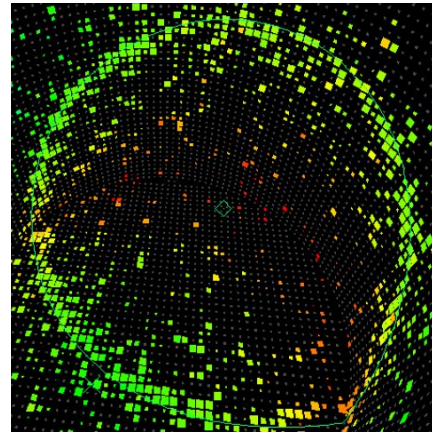


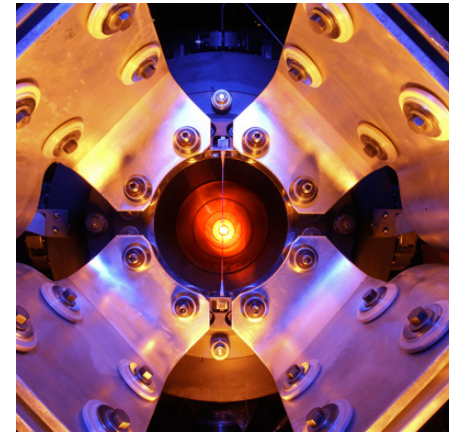


$$\begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{pmatrix}$$



$$\delta_{CP}$$

$$\nu_{\mu} \rightarrow \nu_e$$



Long-Baseline Neutrino Physics: Present and Future

Ruth Toner
Harvard University
FPCP 2014

+ Neutrino Oscillations

➤ Interact weakly via **flavor eigenstates**:

$$\nu_e \quad \nu_\mu \quad \nu_\tau$$

➤ Propagate as **mass eigenstates**:

$$\nu_1 \quad \nu_2 \quad \nu_3$$

Non-zero different masses = neutrino can **slide in and out of phase** as it propagates – “**Oscillation**”

$$P(\nu_\alpha \rightarrow \nu_\beta) = |\langle \nu_\beta | \nu_\alpha(L) \rangle|^2$$

$$= \delta_{\alpha\beta} - 4 \sum_{i>j} \Re(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin^2[1.27 \Delta m_{ij}^2 L/E]$$

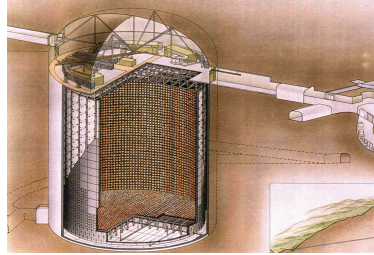
$$+ 2 \sum_{i>j} \Im(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin^2[2.54 \Delta m_{ij}^2 L/E]$$

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

Or, for a two neutrino case:

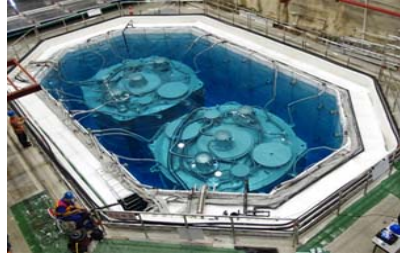
$$P(\nu_\alpha \rightarrow \nu_\beta) = \sin^2 2\theta \sin^2 (1.27 \Delta m^2 L/E)$$

+ Long-Baseline Neutrino Physics



$$U = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix}$$

Atmospheric



$$\begin{bmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{-i\delta} & 0 & c_{13} \end{bmatrix}$$

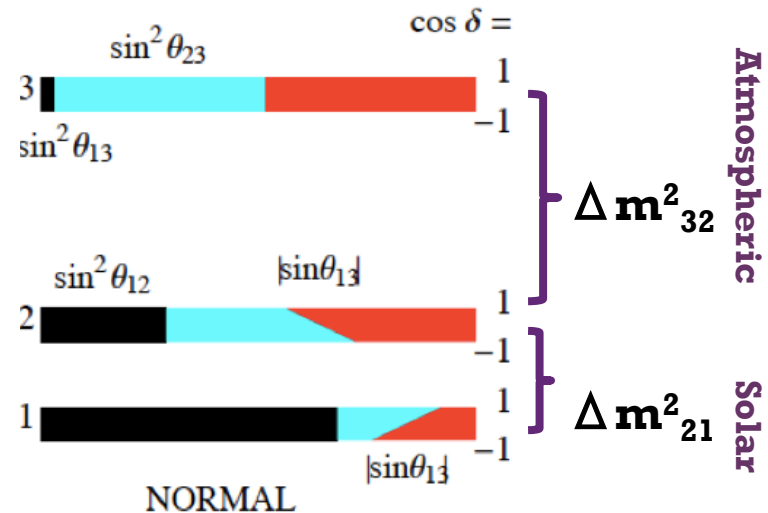
Reactor



$$\begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

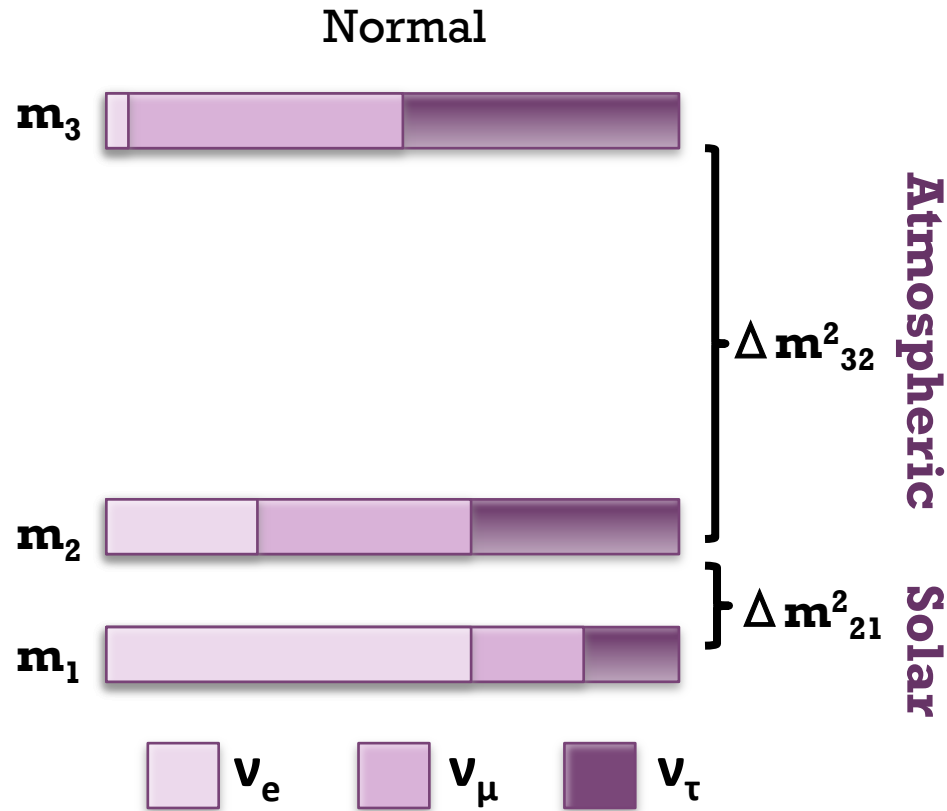
Solar

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$



+ Outstanding Questions

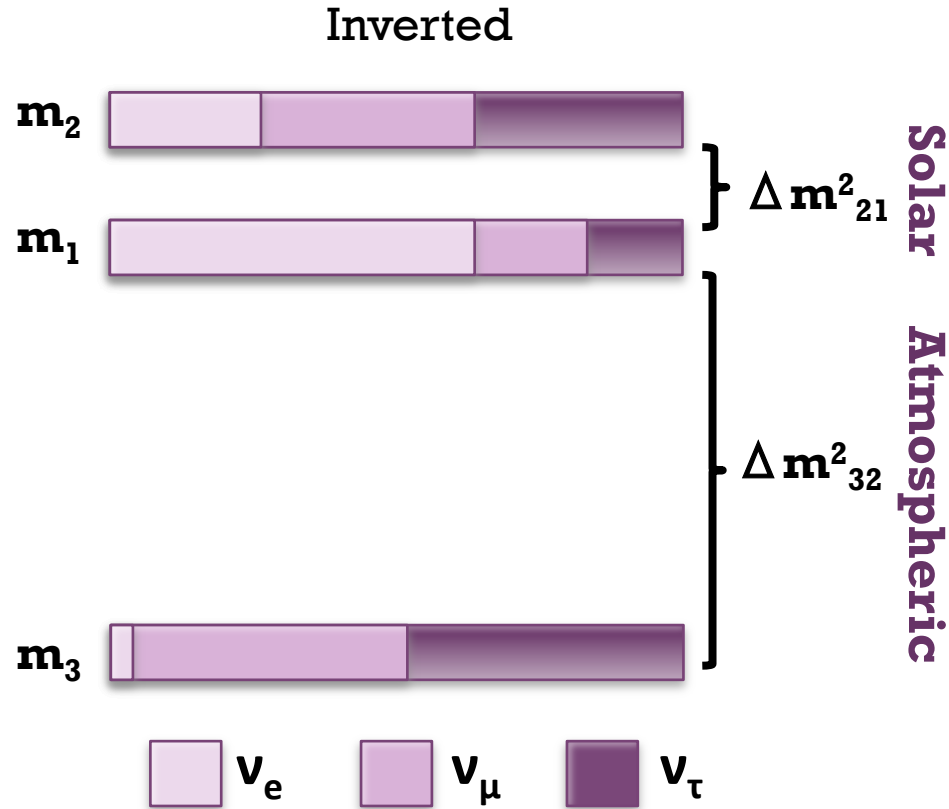
- What is the **value of θ_{13}** ?
 - This is measured with best precision of any mixing angle!
- What is **the sign of Δm^2_{32}** ? Is the **mass hierarchy** “Inverted” or “Normal”?
- Do neutrinos exhibit **CP violation**?
What the size of phase δ_{CP} ?
- Is **θ_{23} exactly 45°** (i.e., what is its “octant”?)
- Do sterile neutrinos exist (mostly short-baseline)?



$$U = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \begin{bmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{-i\delta} & 0 & c_{13} \end{bmatrix} \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

+ Outstanding Questions

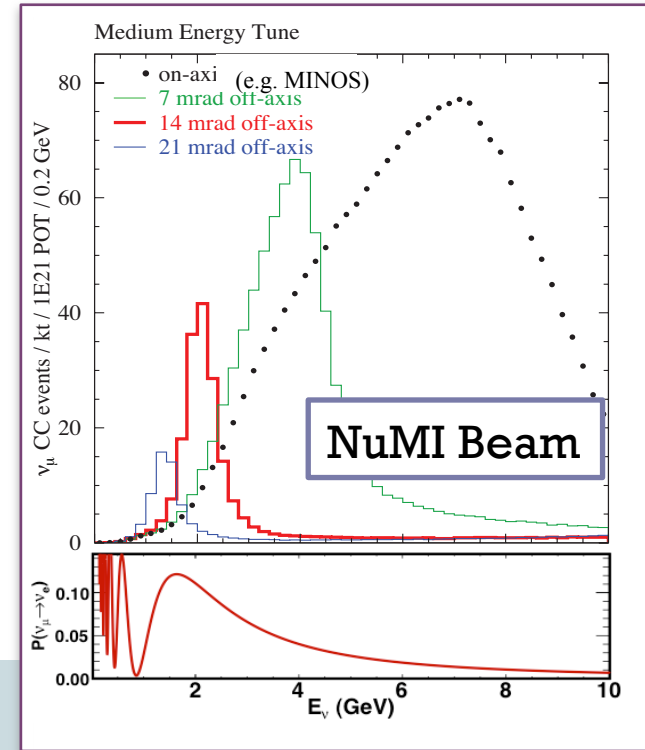
- What is the **value of θ_{13}** ?
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What the size of phase δ_{CP} ?
- Is **θ_{23} exactly 45°** (i.e., what is its “octant”?)
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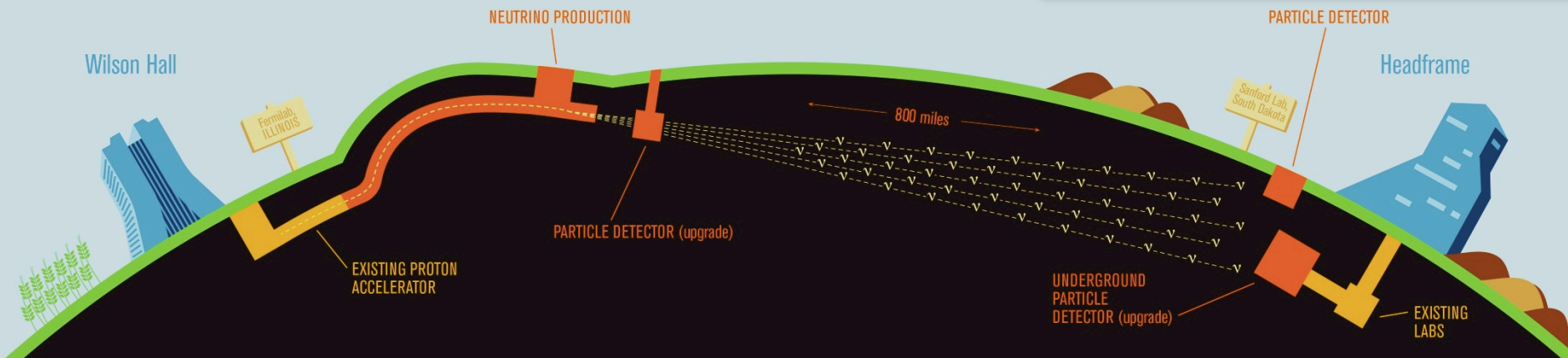
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+ Long-Baseline Neutrino Experiments

- **Several components in common:**
 - **Beam:** Mostly muon neutrinos, produced through decay of particles produced by collision of accelerator protons on stationary target
 - **On-axis beamline:** higher intensity, wide band
 - **Off-axis beamline:** narrow-band beam
 - **Detectors:**
 - Look for products of neutrino interaction
 - Choose a Far Detector location at good L/E for observing oscillations, often underground
 - Often use Near Detector to study pre-oscillation neutrinos, reduce systematic uncertainties



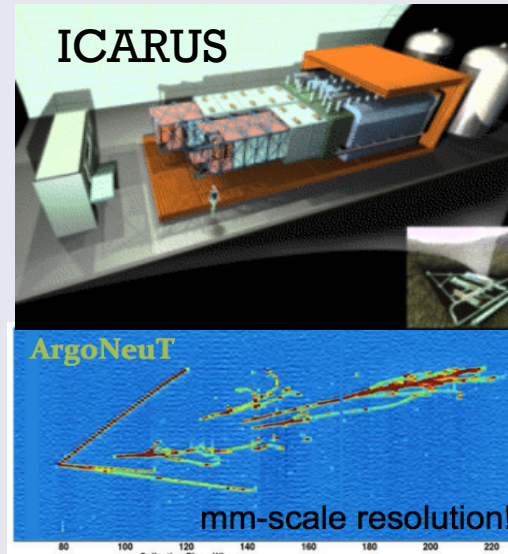
Example: LBNE



+ Modern Detector Technologies

Water Cherenkov:

- Surround large volume of water with PMTs
- Charged particles produce ring-like patterns of light
- Can measure energy, distinguish between different lepton types
- Proven, very scalable

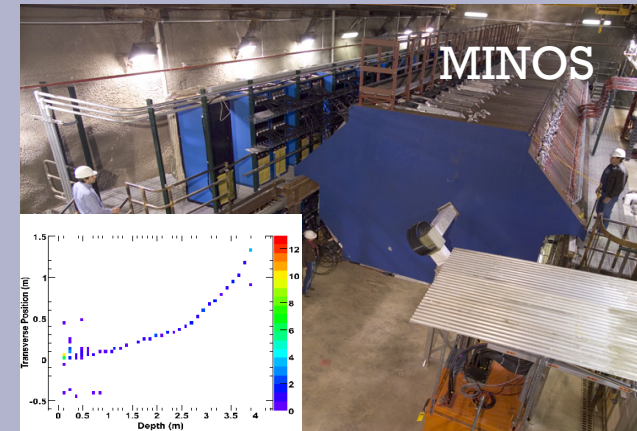


Liquid Argon TPC:

- Charged particle passes through LAr, produces path of ionization e-
- Drift e- with electric field and detect signal on wire frame
- Produces very detailed image of particle interaction with good background rejection

Other tracking technologies:

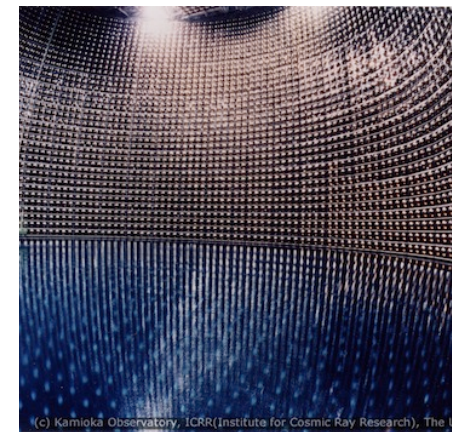
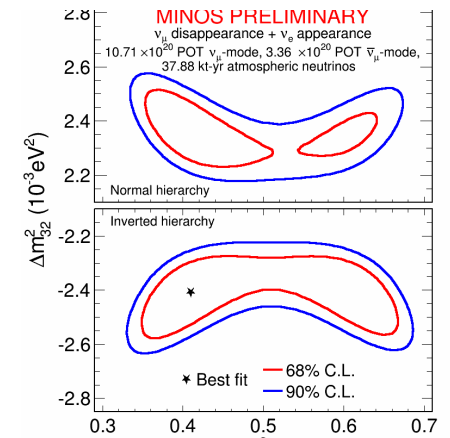
- Various types of tracking calorimeter can be used for higher-energy neutrinos
- Particles pass through strips of solid scintillator, cells of liquid scintillator, emulsion film, etc. and produce signal
- Use photo-detectors to observe and analyze showers and tracks





Current Experiments And Results

T2K, MINOS(+), OPERA, ICARUS, NOvA



+ ν_μ Disappearance: MINOS

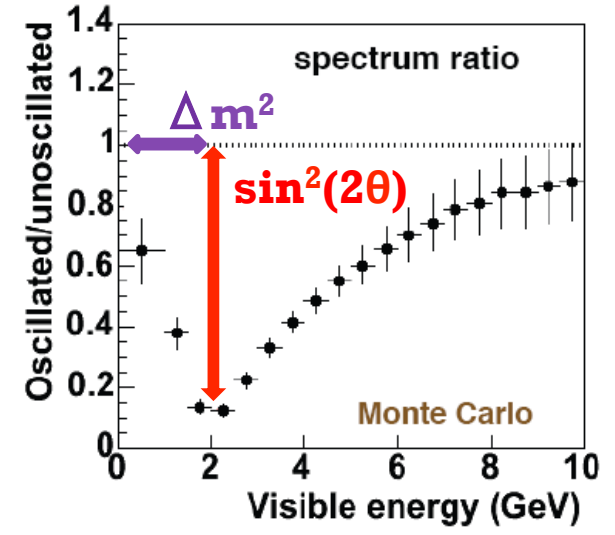
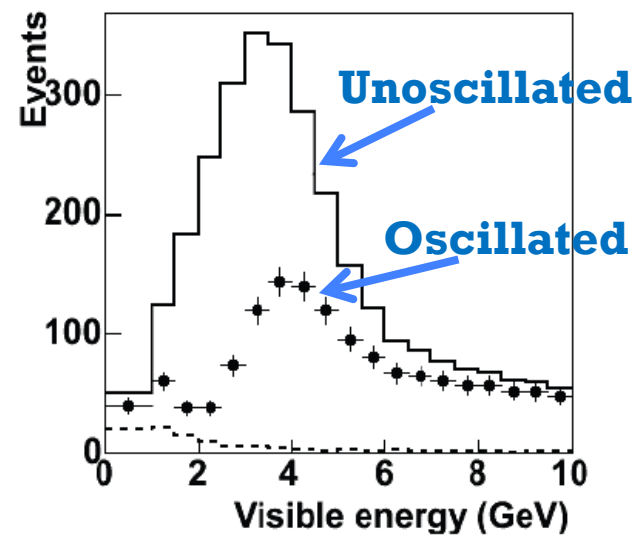
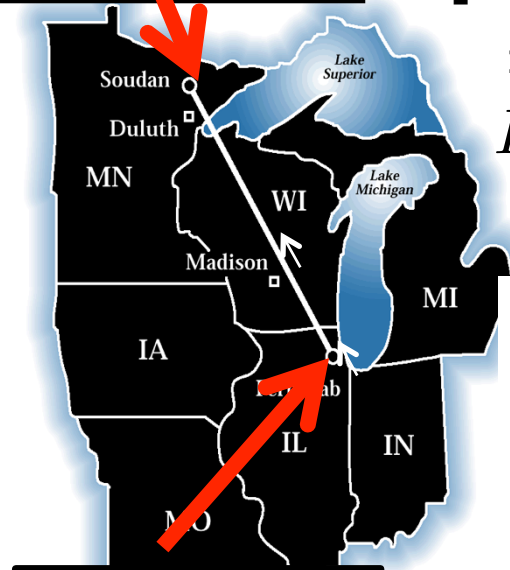


Far Detector

- MINOS consists of two functionally equivalent detectors made of steel and solid scintillator
- Beam:** NuMI on-axis beam (formerly peaked at 3.3 GeV)
- One Near Detector (0.029 kT fiducial), one Far Detector (4.0 kT fiducial at depth of 700 m) at distance of 735 km
- Primary analysis goal: look for disappearance of muon neutrinos, which is approximately:

$$P(\nu_\mu \rightarrow \nu_\mu) = 1 - \sin^2(2\theta_{23}) \sin^2(1.27\Delta m_{32}^2 L/E)$$

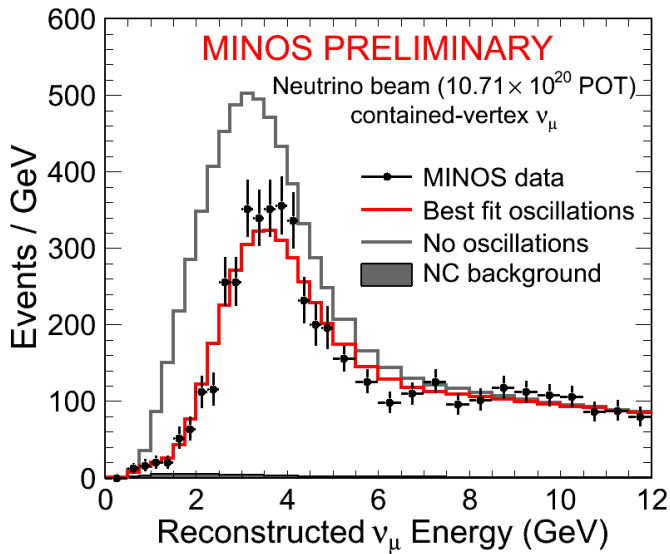
- This allows for the measurement of $\sin^2(2\theta_{23})$ and Δm_{32}^2



Near Detector

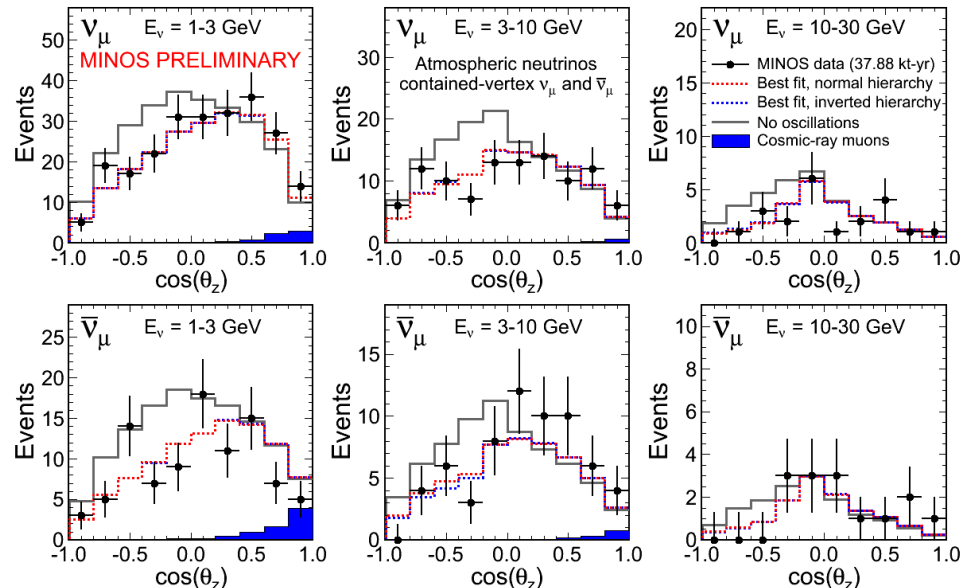
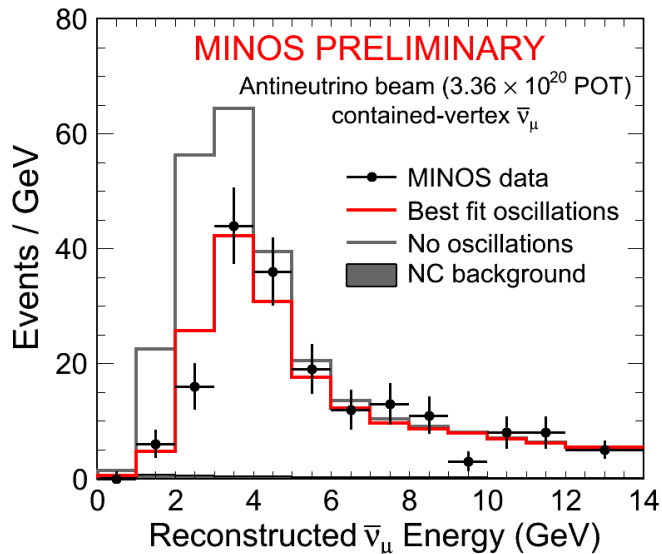
Monte Carlo: (Input parameters: $\sin^2 2\theta = 1.0$, $\Delta m^2 = 3.35 \times 10^{-3} \text{ eV}^2$)

+ ν_μ Disappearance

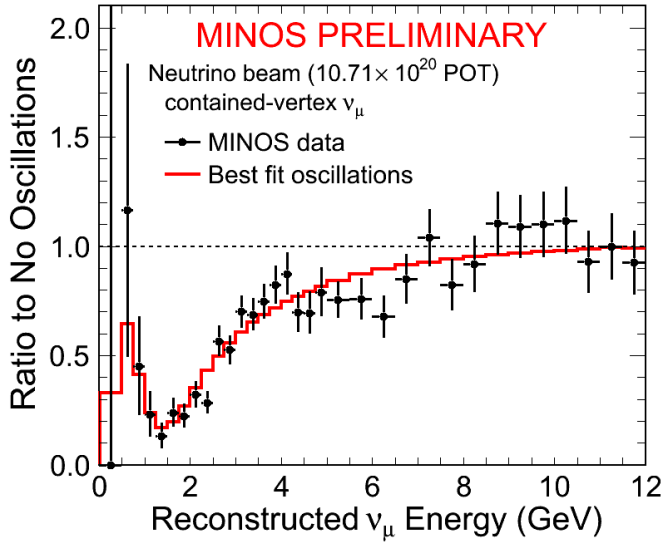


- MINOS previously made measurements using both muon neutrino and anti-neutrino beam
- Recently, have expanded analysis to include information from **atmospheric neutrinos** as well as **electron neutrino appearance** (three-neutrino fit):

	Parameter	Best fit	Confidence limits
Normal hierarchy	$ \Delta m_{32}^2 /10^{-3} \text{eV}^2$	2.37	2.28 – 2.46 (68% C.L.)
	$\sin^2 \theta_{23}$	0.41	0.35 – 0.65 (90% C.L.)
Inverted hierarchy	$ \Delta m_{32}^2 /10^{-3} \text{eV}^2$	2.41	2.32 – 2.53 (68% C.L.)
	$\sin^2 \theta_{23}$	0.41	0.34 – 0.67 (90% C.L.)

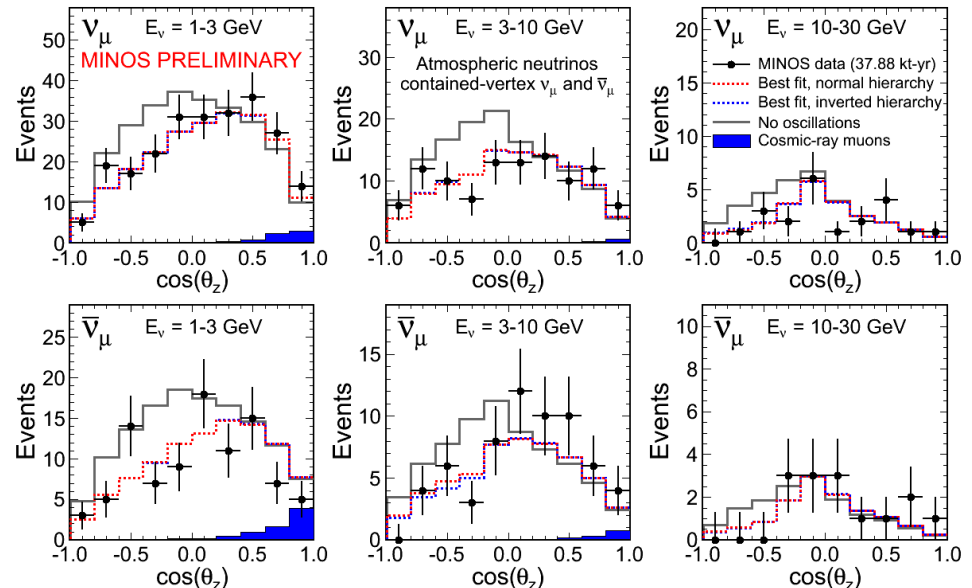
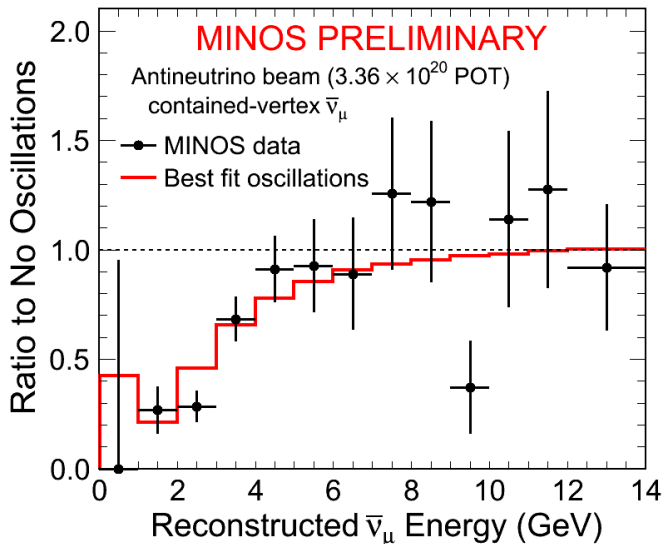


+ ν_μ Disappearance

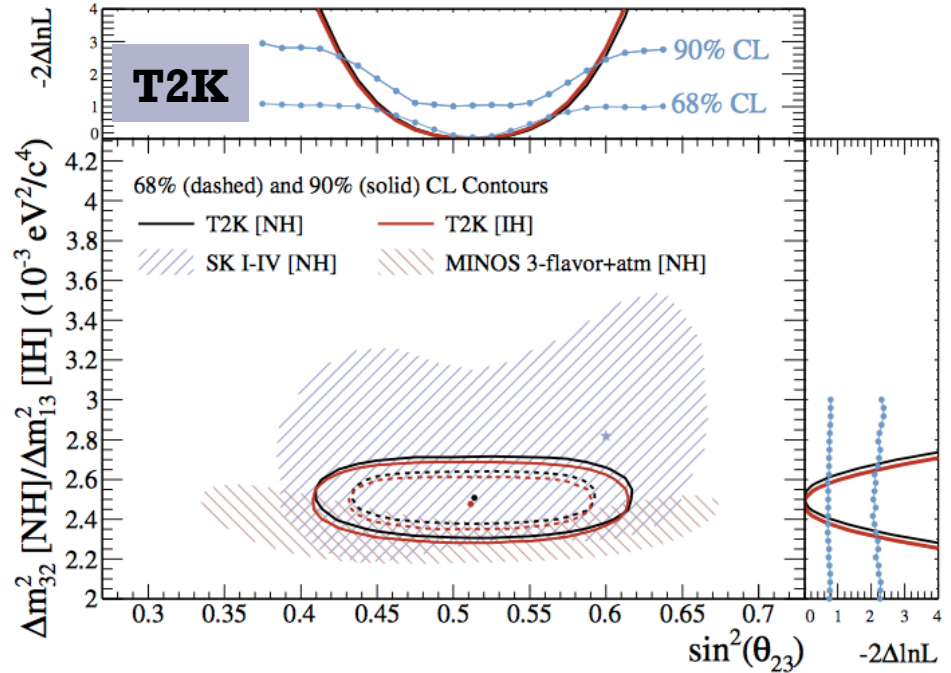
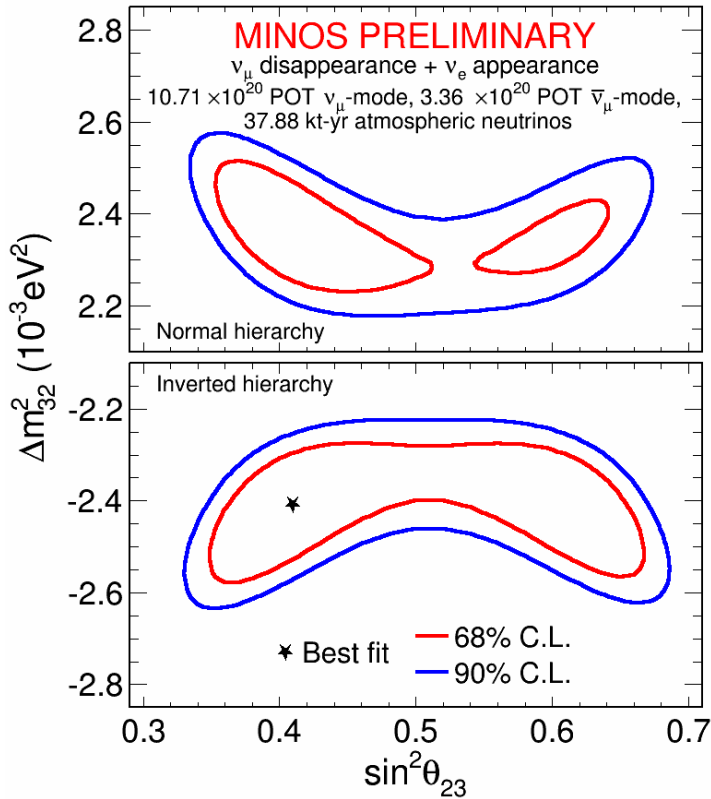


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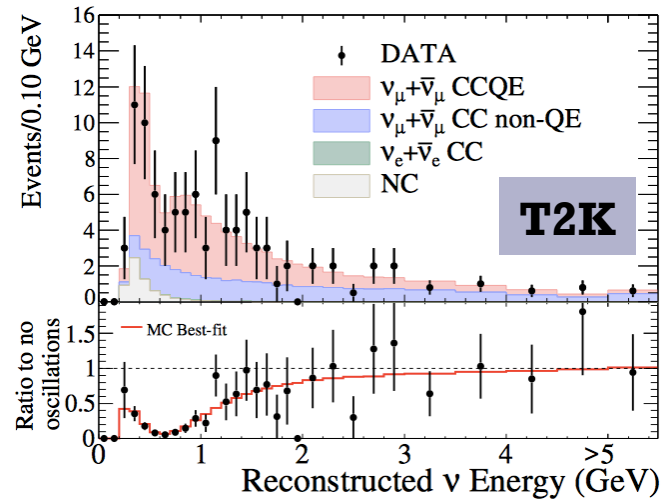
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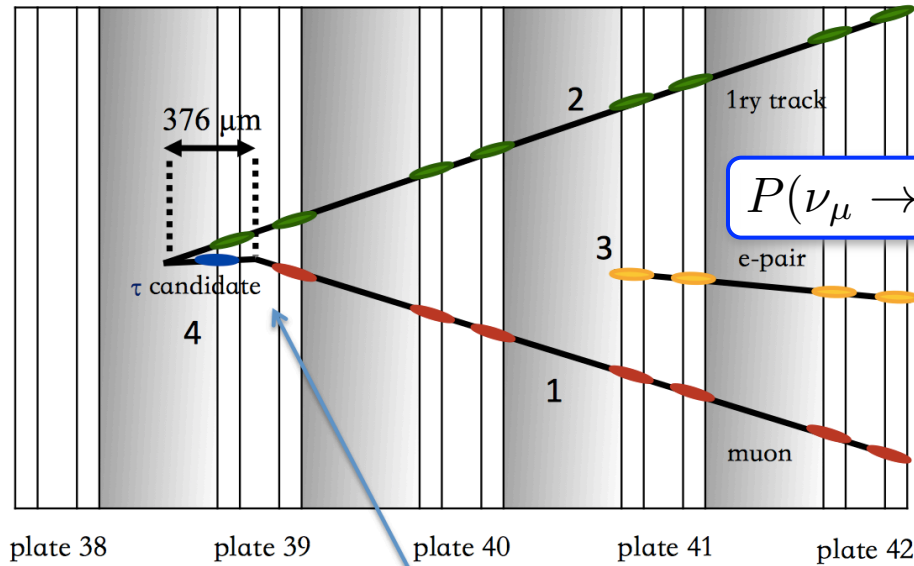
+ θ_{23} Octant?



- MINOS and T2K have made initial attempt to measure the θ_{23} octant
- If θ_{23} is precisely 45° , might indicate some previously unknown symmetry
- Precise knowledge of θ_{23} = less uncertainty in studies of ν_e appearance



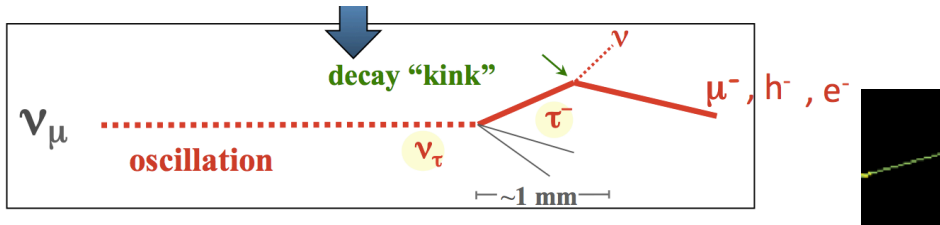
+ OPERA: $\nu_\mu \rightarrow \nu_\tau$ Appearance



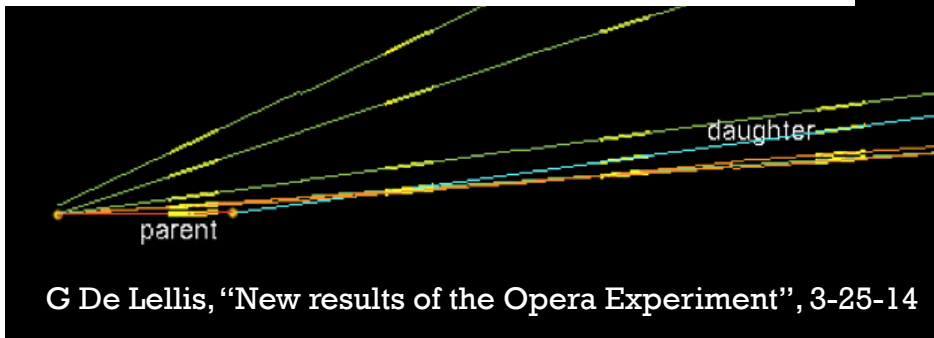
$$P(\nu_\mu \rightarrow \nu_\tau) \sim \sin^2 2\theta_{23} \cos^4 \theta_{13} \sin^2(1.27\Delta m_{32}^2 L/E)$$

- “Disappearing” muon neutrinos in MINOS and T2K should be mostly oscillating to tau neutrinos:

- OPERA experiment designed to observe this oscillation, using 17 GeV muon neutrino CNGS beam
- Detector:** magnetized, constructed from bricks of nuclear emulsion film
 - Located at LNGS (730 km)



- Have now observed **4 tau appearance events**, on top of background expectation of 0.22 evts
 - Probability of being explained by background = 1.1×10^{-5}
 - Corresponds to **4.2 σ significance**



+ $\nu_\mu \rightarrow \nu_e$ Appearance

$$P(\nu_\mu \rightarrow \nu_e) \cong T_1 \sin^2 2\theta_{13} - T_2 \alpha \sin 2\theta_{13} + T_3 \alpha \sin 2\theta_{13} + T_4 \alpha^2$$

$$\alpha = \frac{\Delta m_{21}^2}{\Delta m_{31}^2}$$

atmospheric $T_1 = \sin^2 \theta_{23} \frac{\sin^2 [(1-x)\Delta]}{(1-x)^2}$

interference $T_2 = \sin \delta_{CP} \sin 2\theta_{12} \sin 2\theta_{23} \sin \Delta \frac{\sin(x\Delta)}{x} \frac{\sin[(1-x)\Delta]}{(1-x)}$

$T_3 = \cos \delta_{CP} \sin 2\theta_{12} \sin 2\theta_{23} \cos \Delta \frac{\sin(x\Delta)}{x} \frac{\sin[(1-x)\Delta]}{(1-x)}$

solar $T_4 = \cos^2 \theta_{23} \sin^2 2\theta_{12} \frac{\sin^2(x\Delta)}{x^2}$

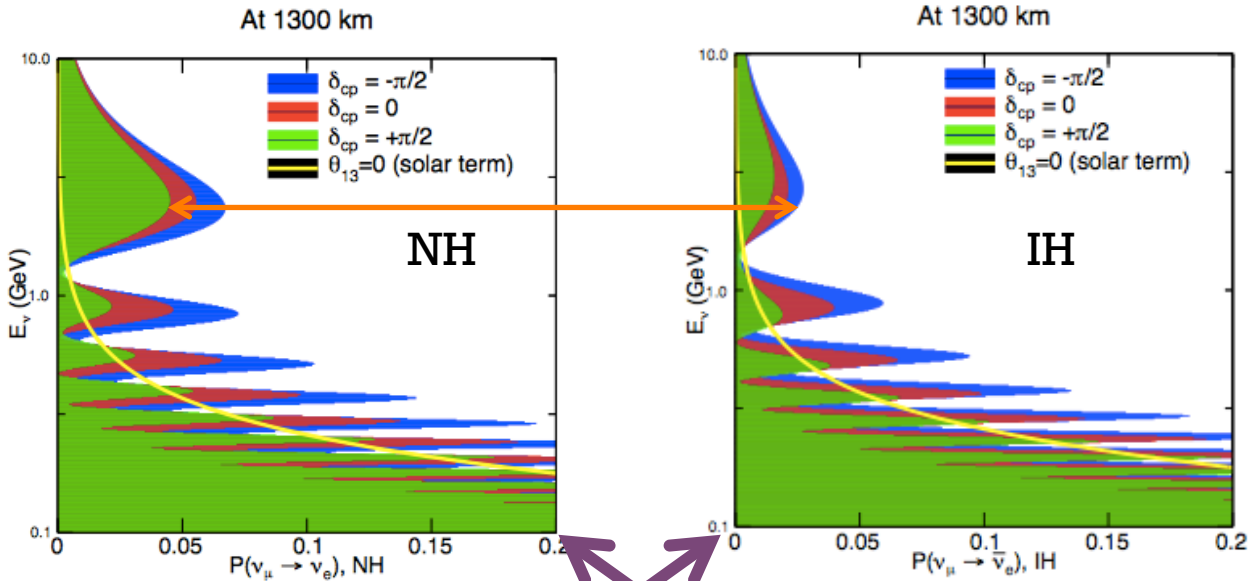
$$\Delta m_{32}^2 \approx \Delta m_{31}^2$$

$$\Delta = \Delta m_{31}^2 L / 4E \quad x = 2\sqrt{2}G_F N_e E / \Delta m_{31}^2 \cong E / 12 \text{ GeV}$$

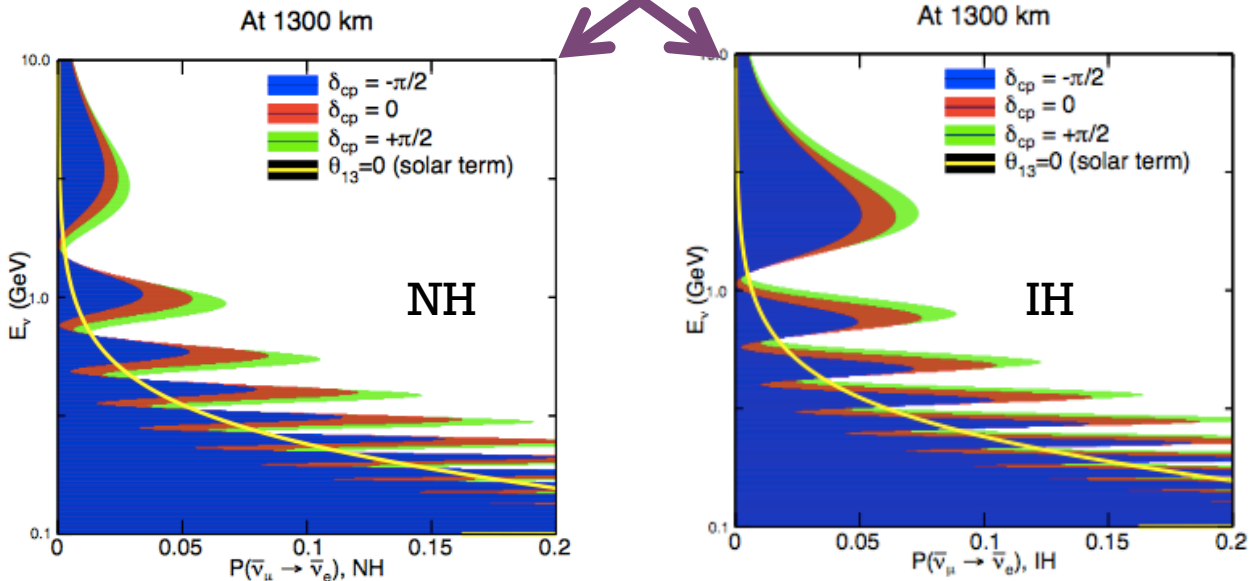
- $\nu_\mu \rightarrow \nu_e$ **appearance** = connected to numerous neutrino mixing parameters:
 - **Value of θ_{13}** : now known to be non-zero, meaning other parameters can be measured
 - **Sign of Δm_{32}^2** : becomes relevant via **matter effects** which occur when beam passes through earth; sign of effect changes for anti-neutrinos
 - **Precise value and octant of θ_{23}**
 - **CP violation phase δ_{CP}** : sign of effect different for neutrinos and antineutrinos

+ Degeneracies...

Neutrino



Antineutrino

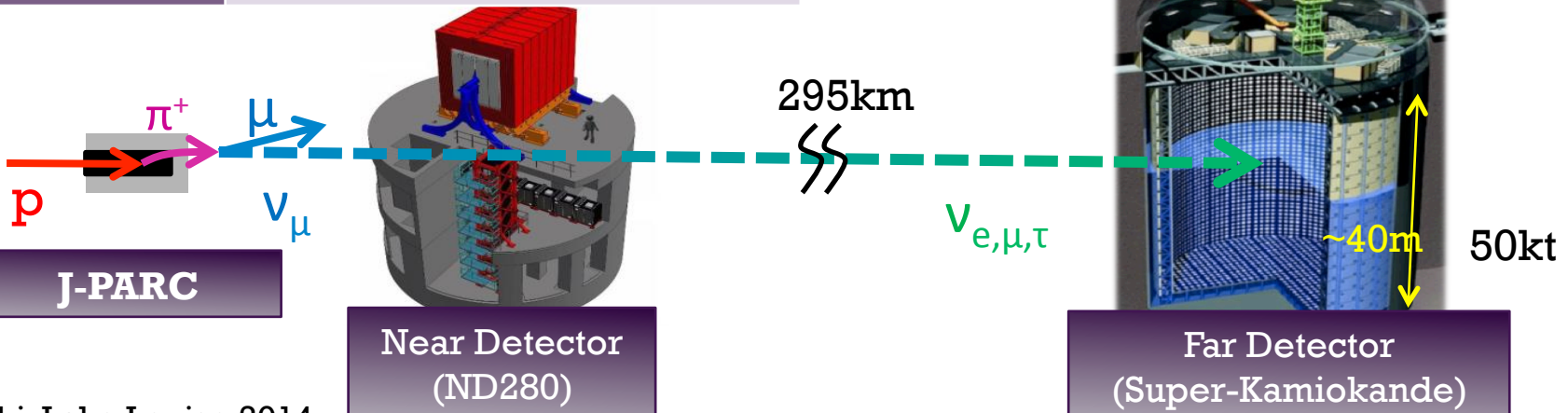
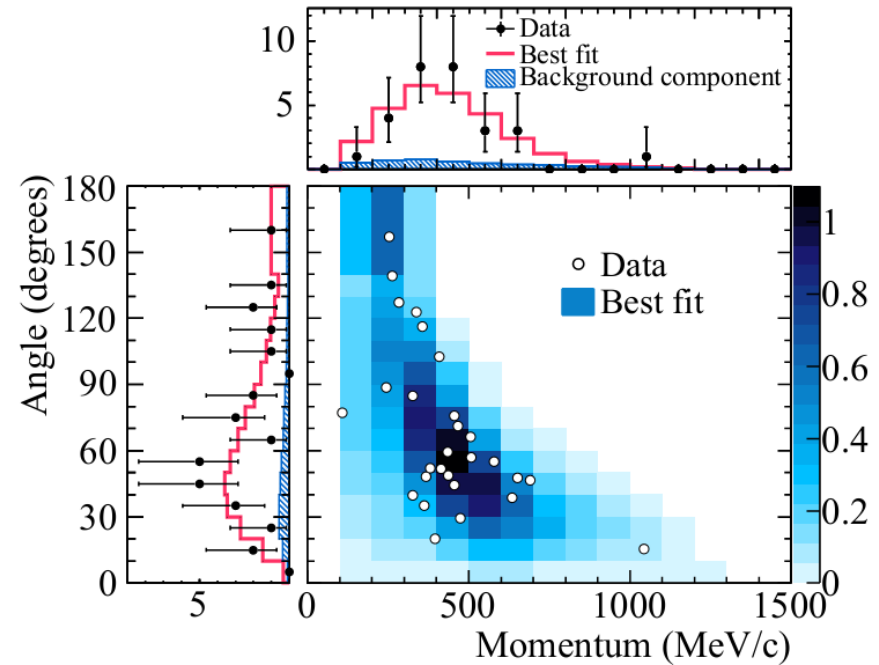


+ ν_e Appearance and θ_{13}

- T2K (Tokai to Kamioka):**
 - Beam = off-axis muon neutrino beam produced at J-PARC, peaked at < 1 GeV, 295 km baseline
 - Near Detector:** ND280
 - Far Detector:** Super-Kamiokande
- 2014 best fits ($\pm 68\%$) for $\sin^2(2\theta_{13})$, rejecting null hypothesis at 7.3σ :

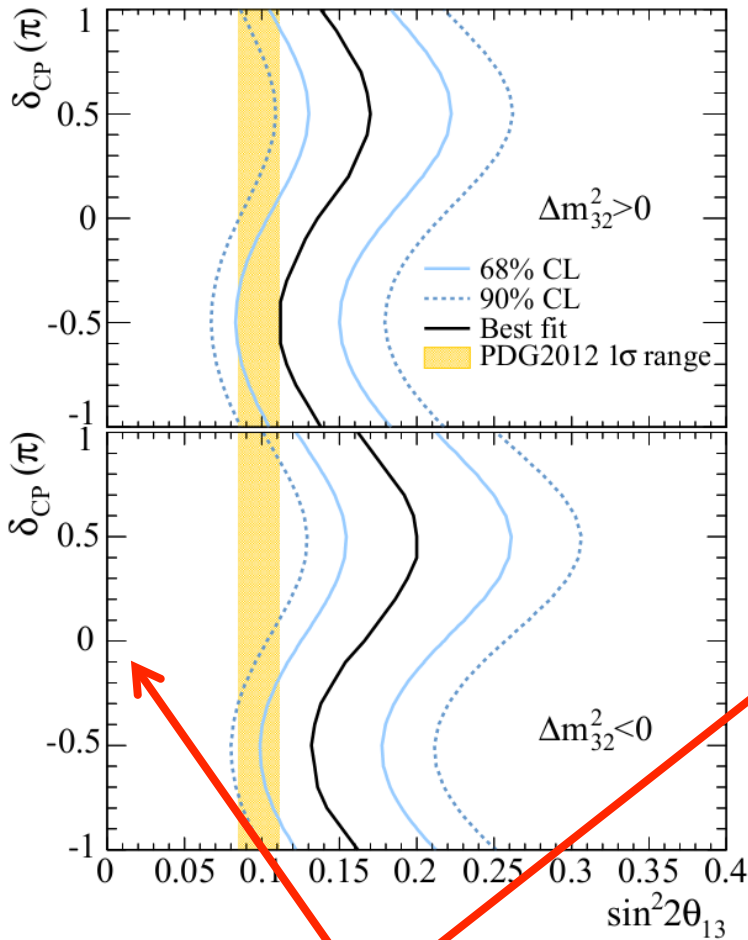
NH 0.140 (+0.036, -0.032)

IH 0.170 (+0.045, - 0.037)

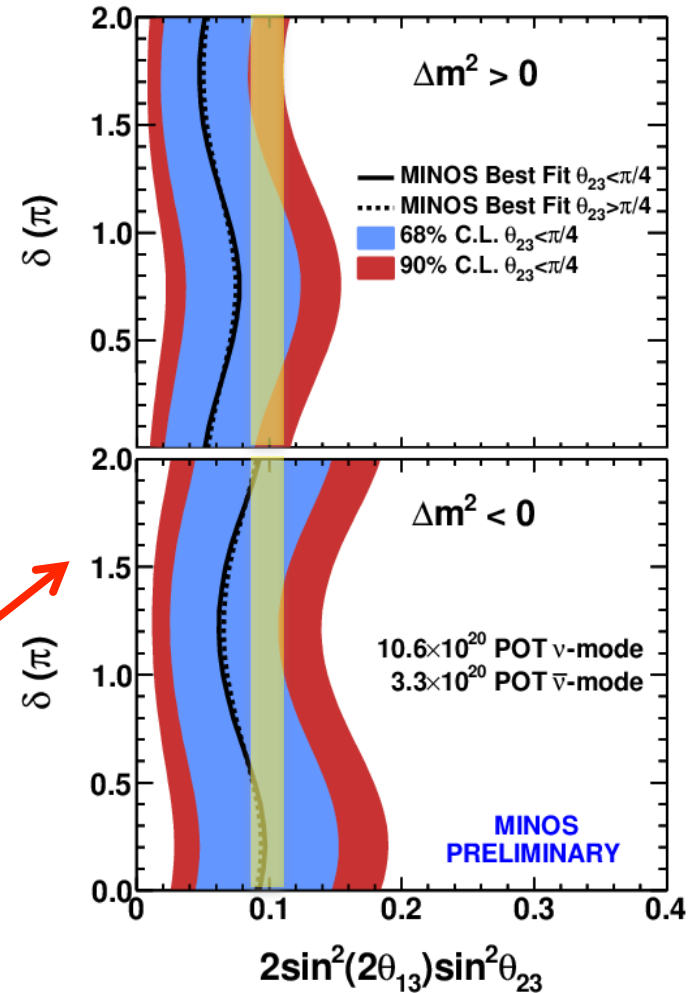


+ ν_e Appearance and θ_{13}

T2K:



MINOS:

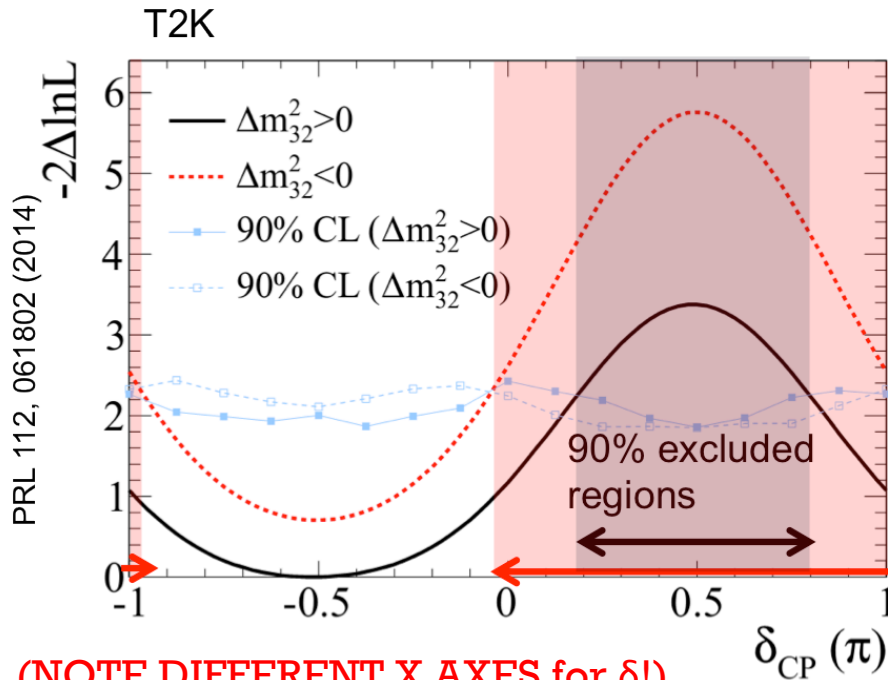


Phys. Rev. Lett. 112, 191801 (2014)

NOTE DIFFERENT Y AXIS for δ !

 = 2013 PDG range for θ_{13}

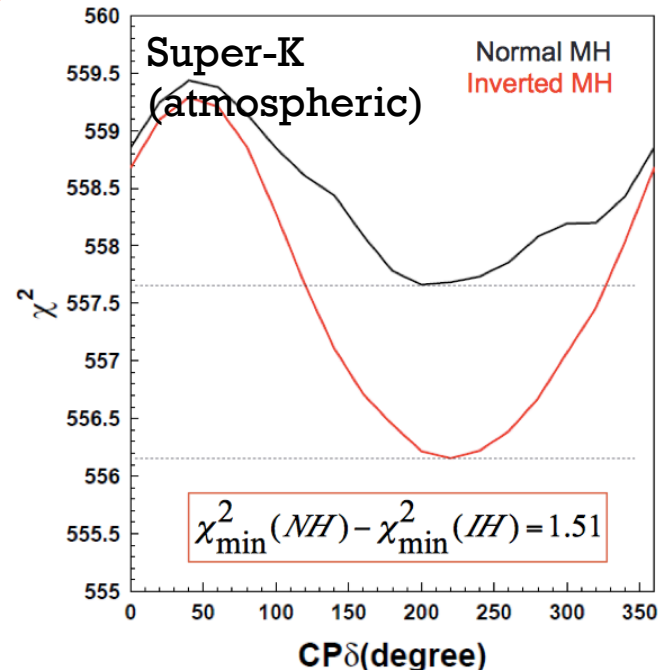
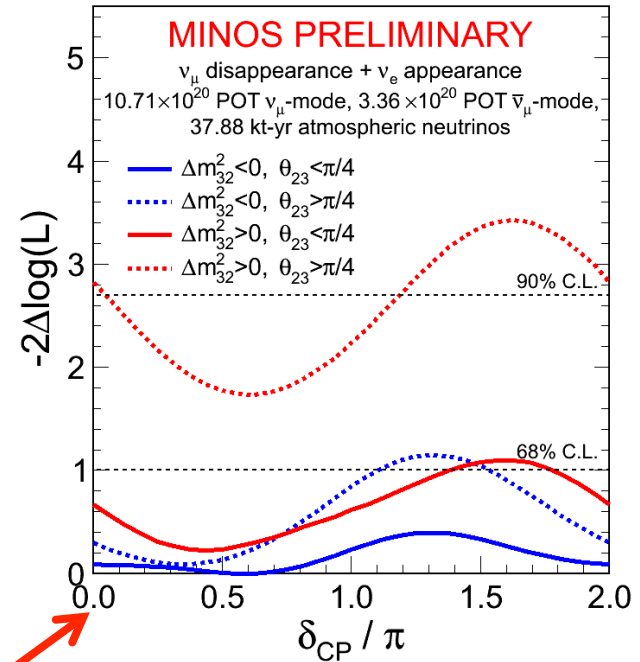
+ CP and Hierarchy?



(NOTE DIFFERENT X AXES for δ !)

- Combining ν_e appearance results with current reactor results can put limits on possible values of δ_{CP}
- MINOS results have larger impact from matter effects (hierarchy and octant)
- Contradictory! But not very strong limits
 - Need more sensitive experiments...

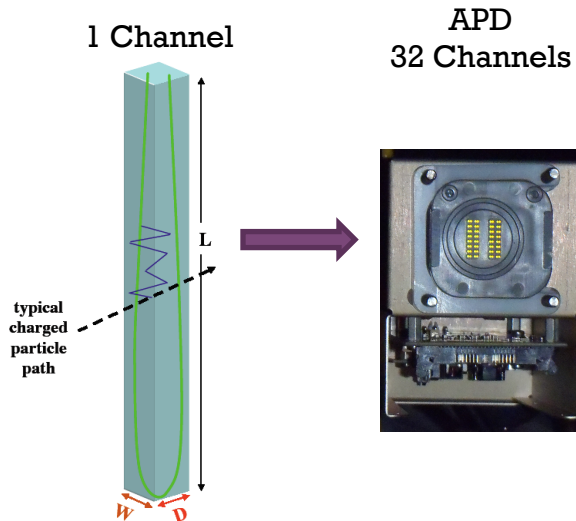
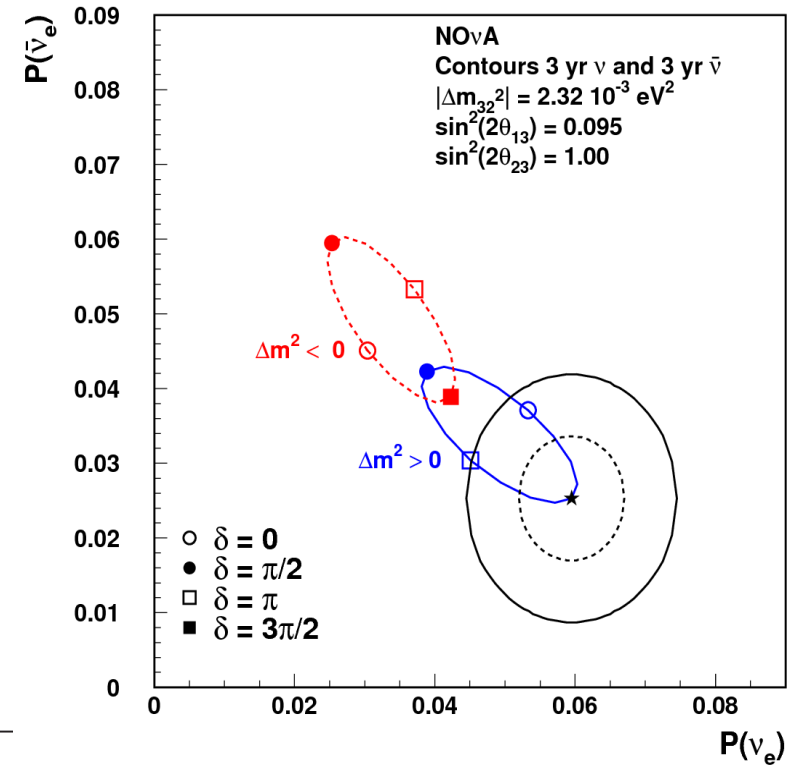
MINOS



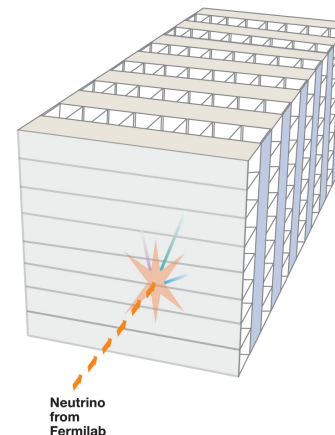
+ NOvA

- Neutrino experiment using the NuMI beam
 - Off-axis, with a 2 GeV beam peak; can be run in both neutrino and anti-neutrino mode
 - Designed to look for ν_e appearance
- Near Detector** (0.3 kT) at FNAL, and **Far Detector** (13 kT) at Ash River (MN), 810 km away
 - For best EM shower resolution, “fully active” detector built from low-Z materials
 - Blocks of extruded PVC cells filled with liquid scintillator
 - Light collected by wavelength shifting fiber and read out by APDs

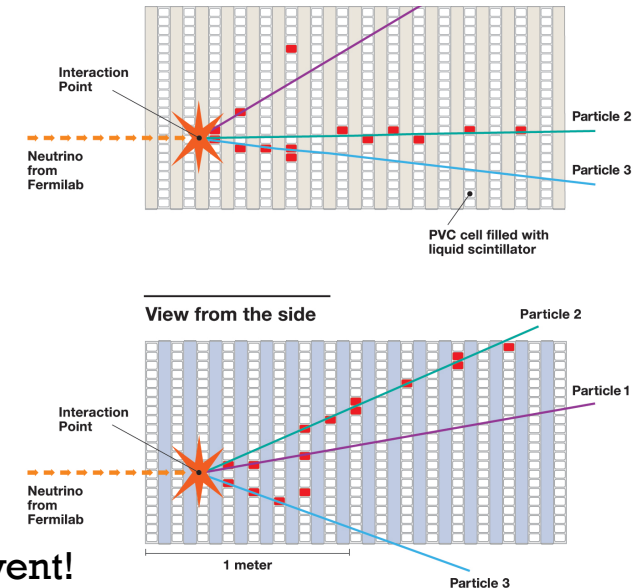
1 and 2 σ Contours for Starred Point



3D schematic of NOvA particle detector

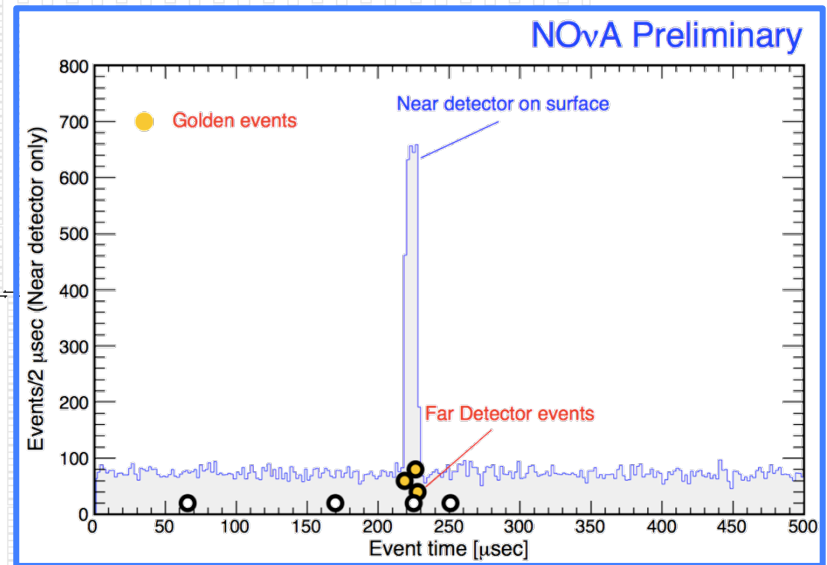
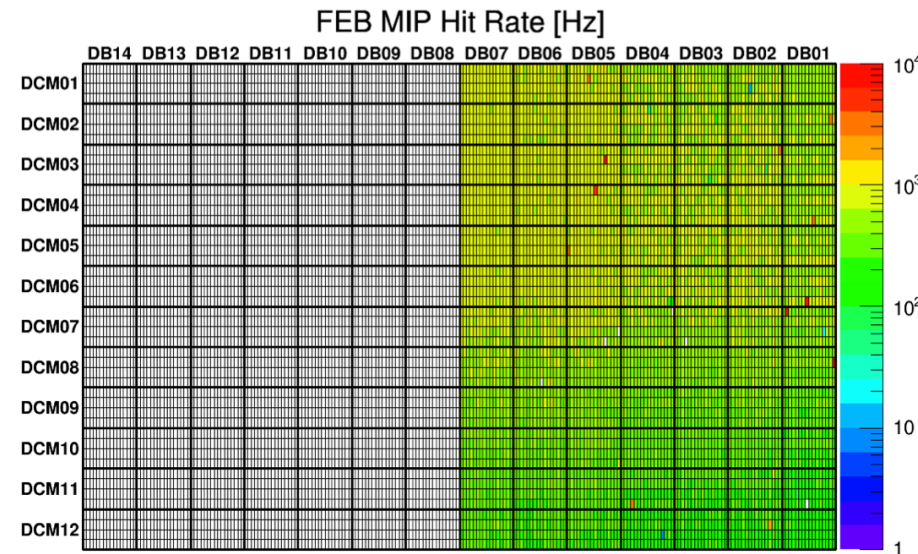
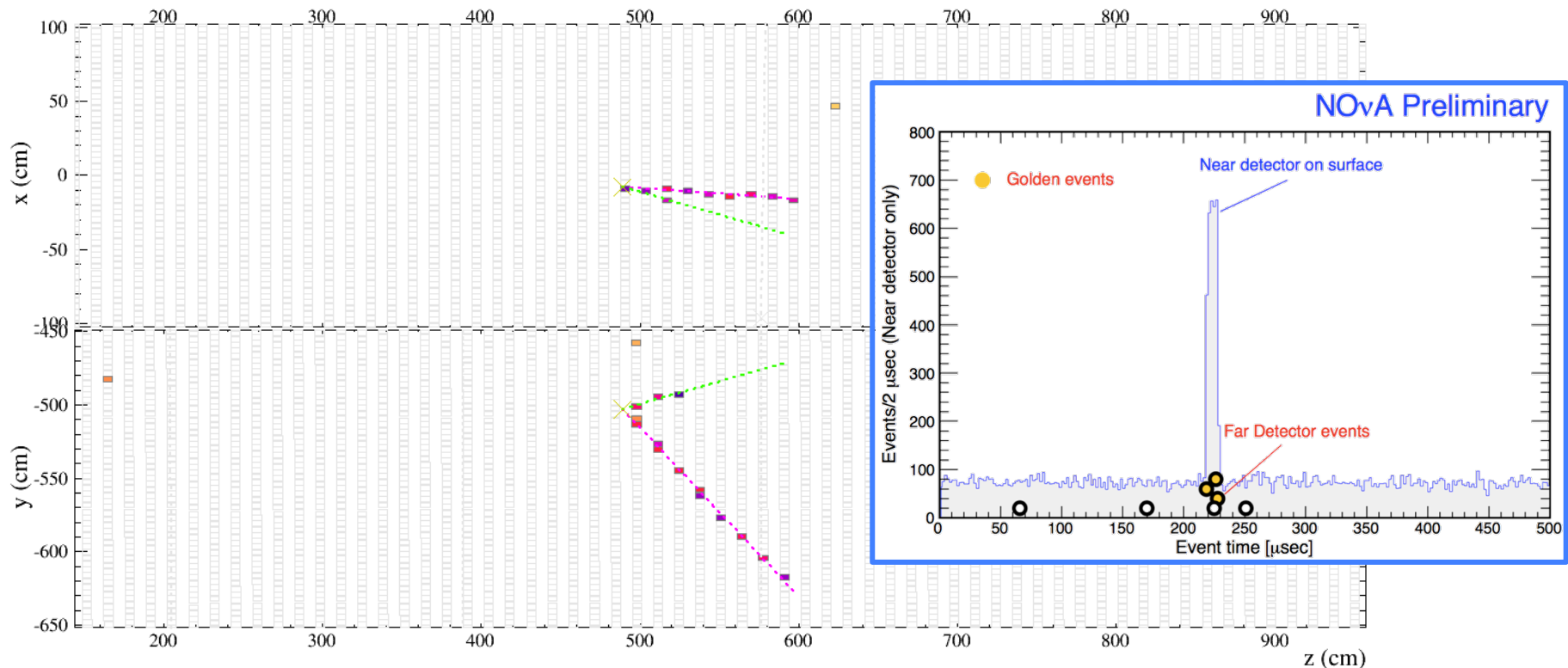


Cartoon of First Event!



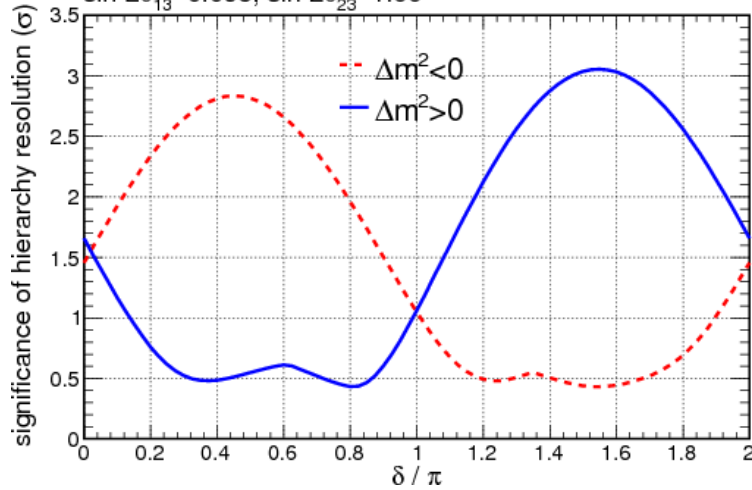
+ NOvA Status

- **Far Detector:** final detector block was placed in February 2014
 - All filled, currently being instrumented (completing this summer)
 - Data is being collected, and have observed beam peak!
- **Near Detector:** all blocks placed and filled, currently being instrumented as well



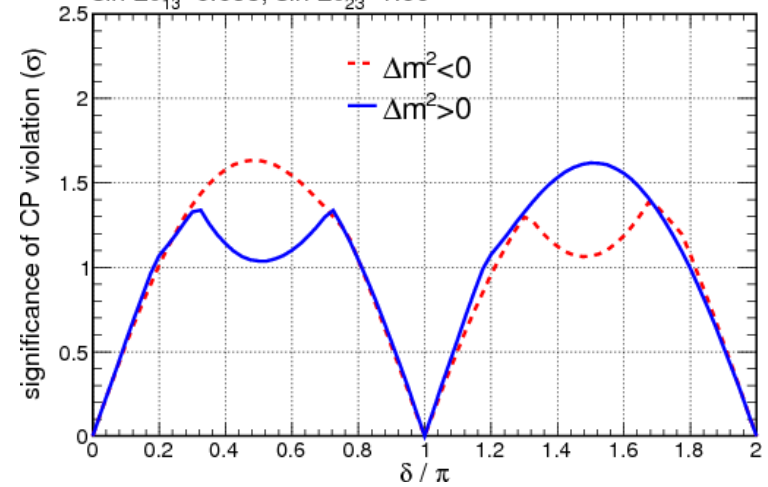
NOvA hierarchy resolution, 3+3 yr

$\sin^2 2\theta_{13}=0.095, \sin^2 2\theta_{23}=1.00$



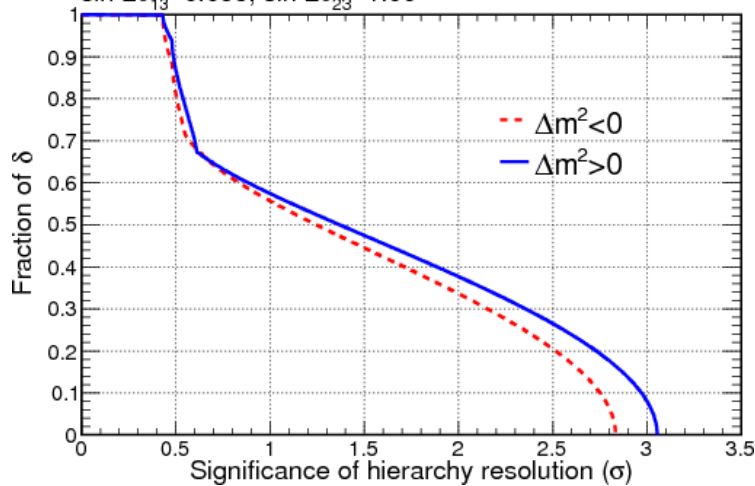
NOvA CPV determination, 3+3 yr

$\sin^2 2\theta_{13}=0.095, \sin^2 2\theta_{23}=1.00$



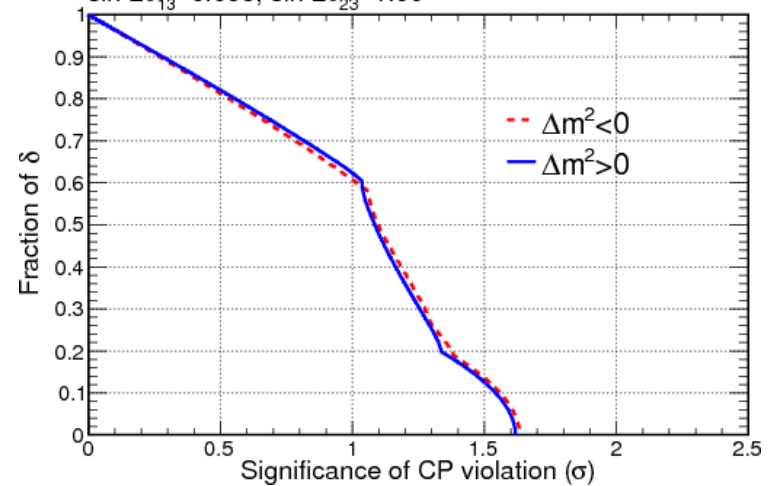
NOvA hierarchy resolution, 3+3 yr

$\sin^2 2\theta_{13}=0.095, \sin^2 2\theta_{23}=1.00$

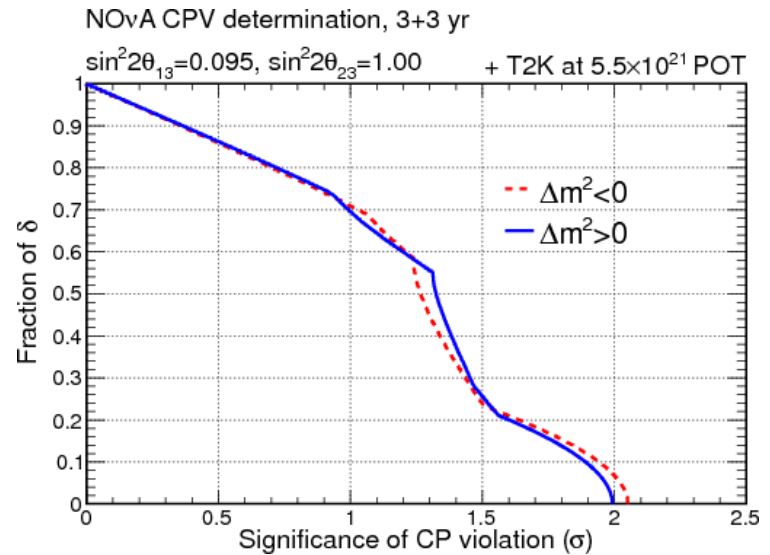
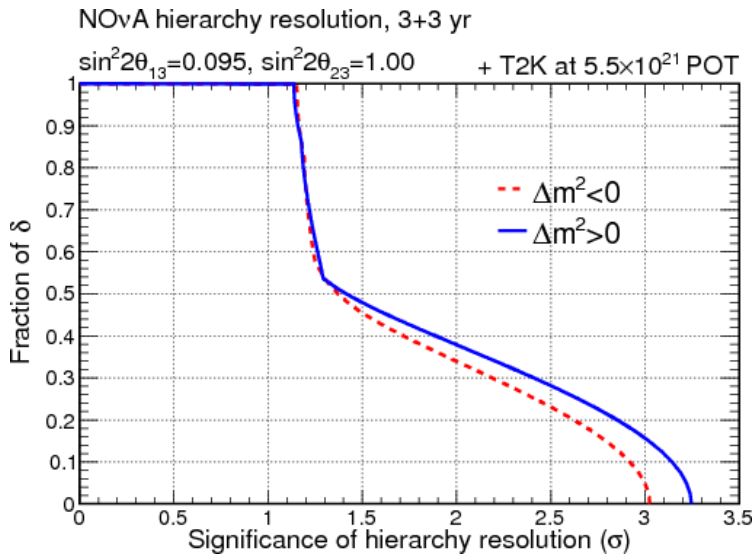
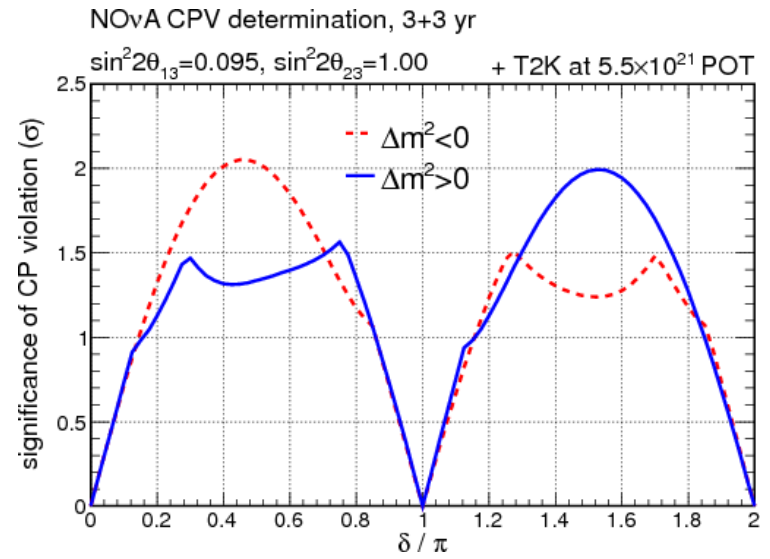
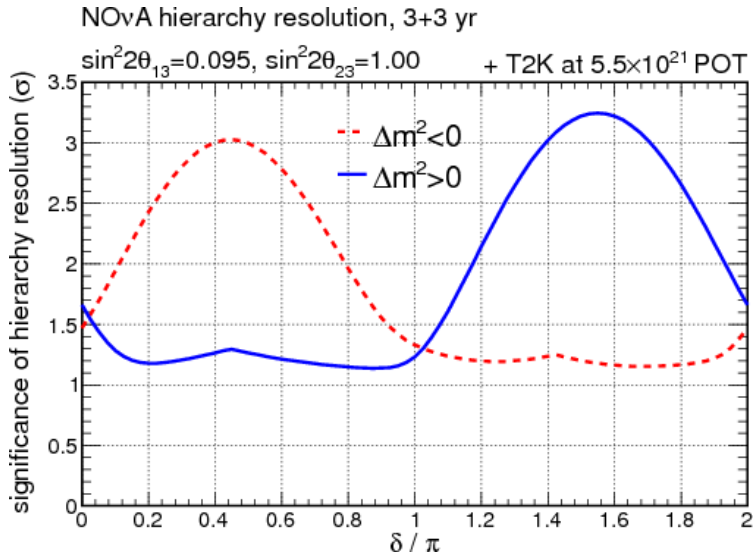


NOvA CPV determination, 3+3 yr

$\sin^2 2\theta_{13}=0.095, \sin^2 2\theta_{23}=1.00$



+ NOvA + T2K

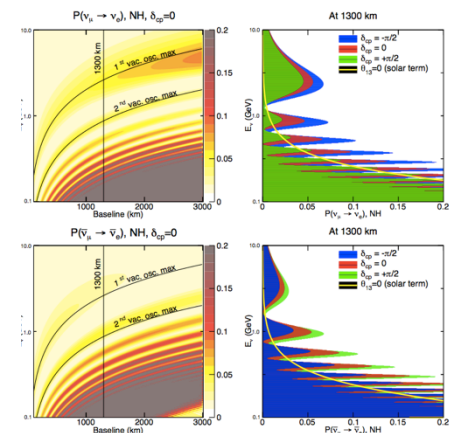
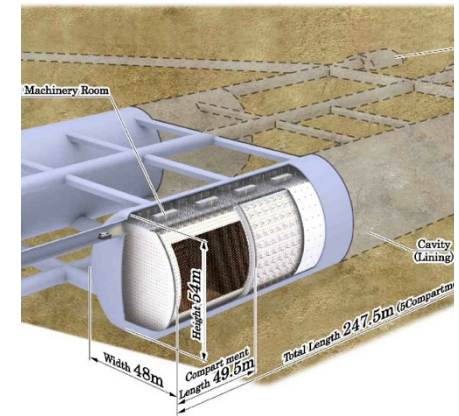




- Need more powerful generation of experiments to resolve degeneracy between mass hierarchy and δ_{CP} ...

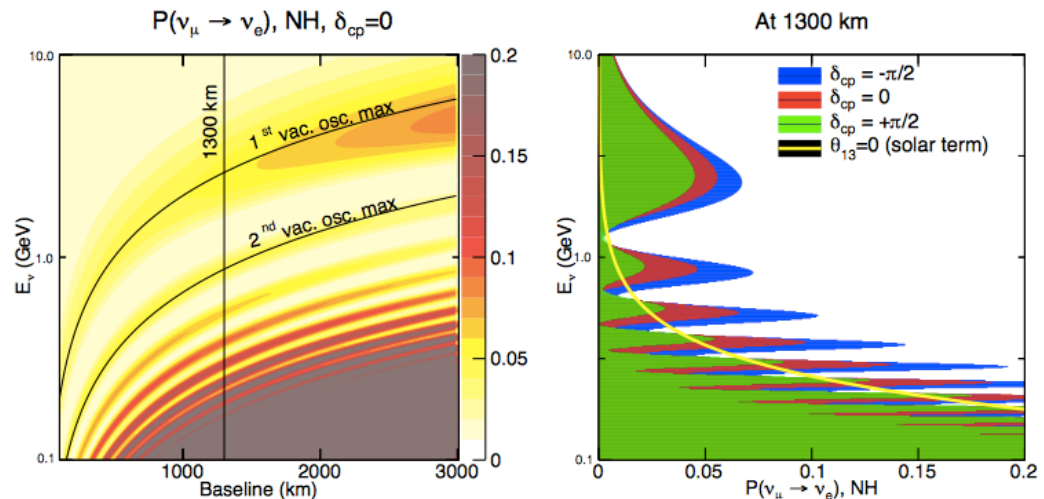
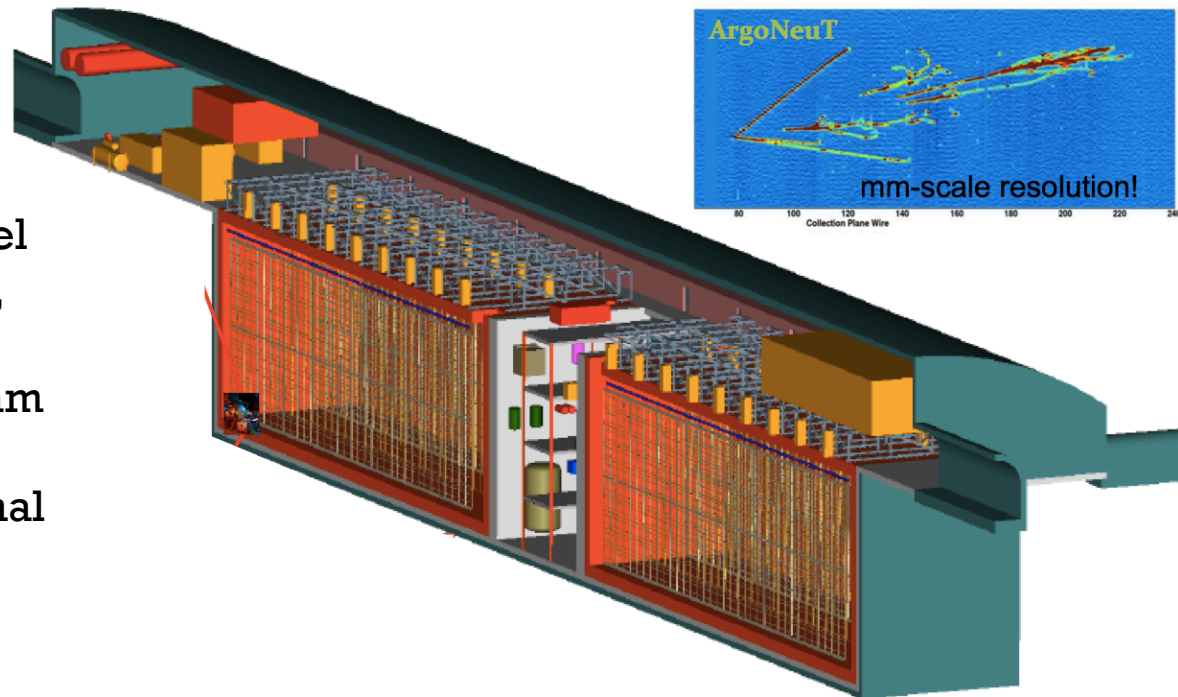
Future Experiments and the Search for CP Violation

LBNE, Hyper-K, LBNO, new neutrino sources



+ LBNE LBNF

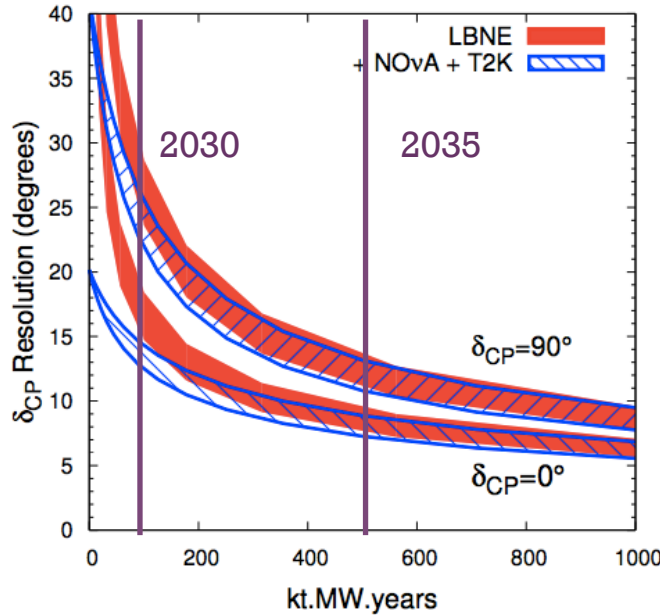
- **Long Baseline Neutrino Experiment Facility**
- **Far Detector:** Liquid Argon TPC, goal is 35 kt fiducial volume, at Sanford 4850 ft level
- **Near Detector:** Fine grained, high-resolution (at FNAL)
- **Beam:** intense wideband beam from FNAL, >1 MW (PIP-II)
 - 1300 km beamline, optimal for oscillation studies
- **Longer baseline** = larger influence from matter effects
 - Larger enhancement/suppression of ν_e appearance due to sign of mass hierarchy
 - At LBNE baseline, this asymmetry exceeds the impact from CP violation and reduces MH/CP ambiguity



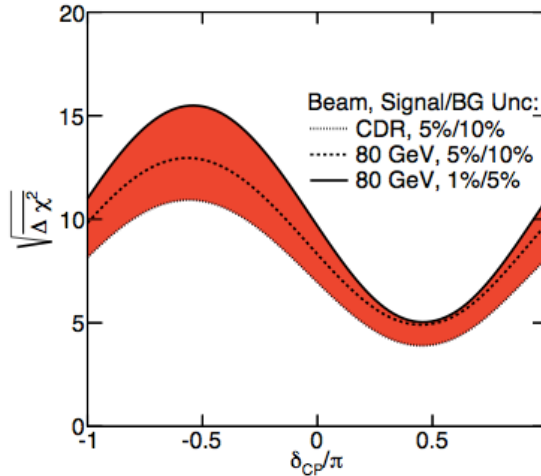
+ LBNE Reach Studies

3yr nu + 3yr anti-nu:

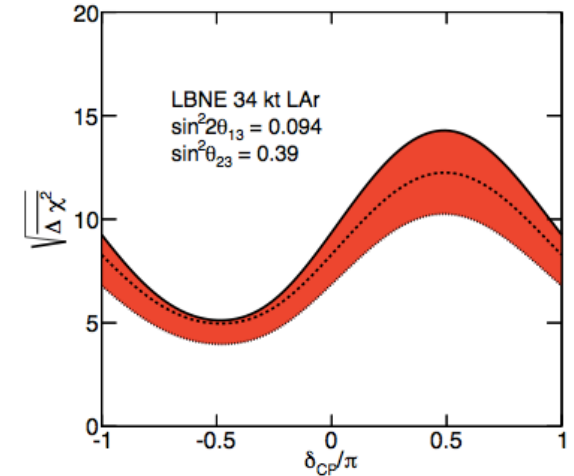
δ_{CP} Resolution



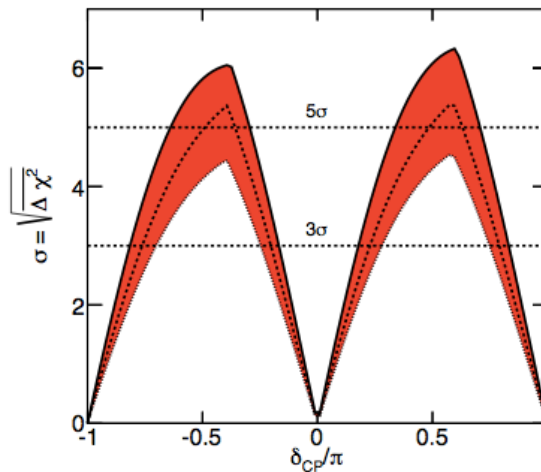
Mass Hierarchy Sensitivity (NH)



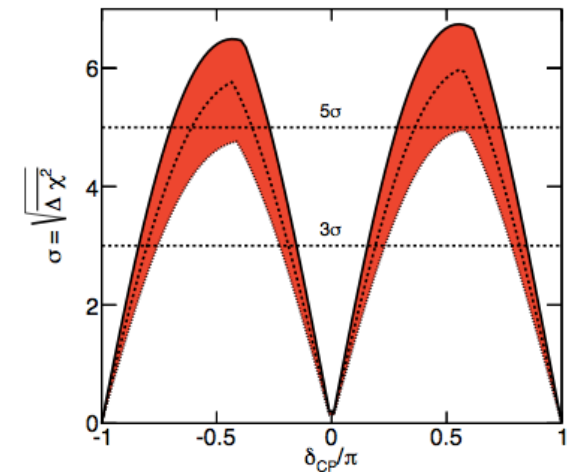
Mass Hierarchy Sensitivity (IH)



CP Violation Sensitivity (NH)



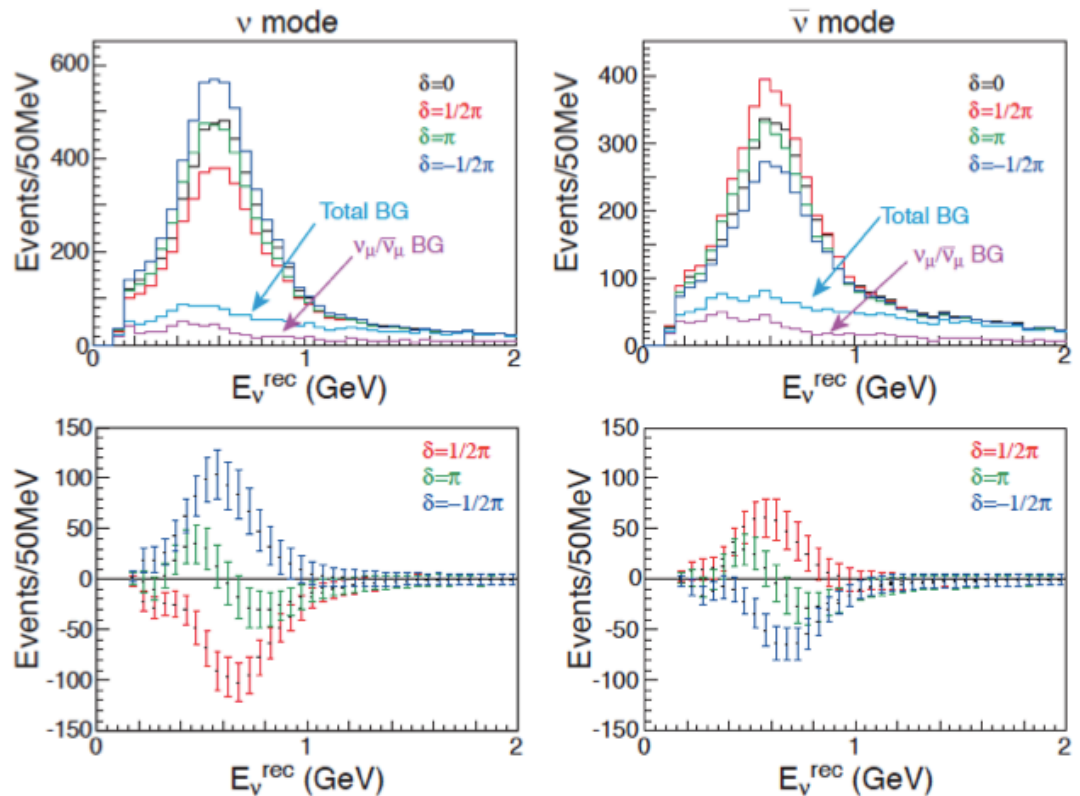
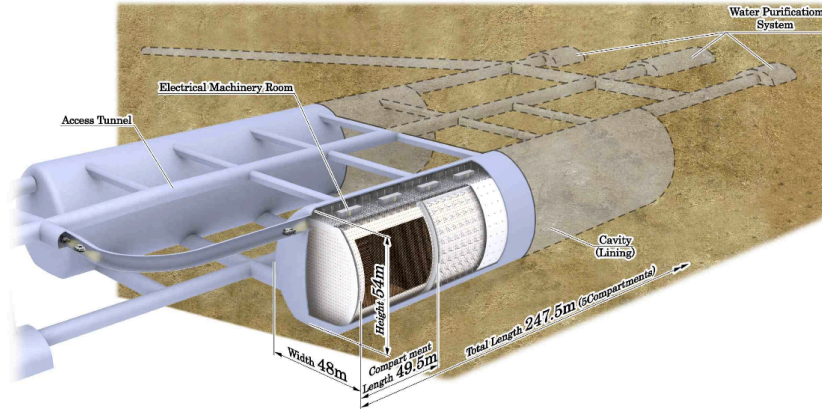
CP Violation Sensitivity (IH)



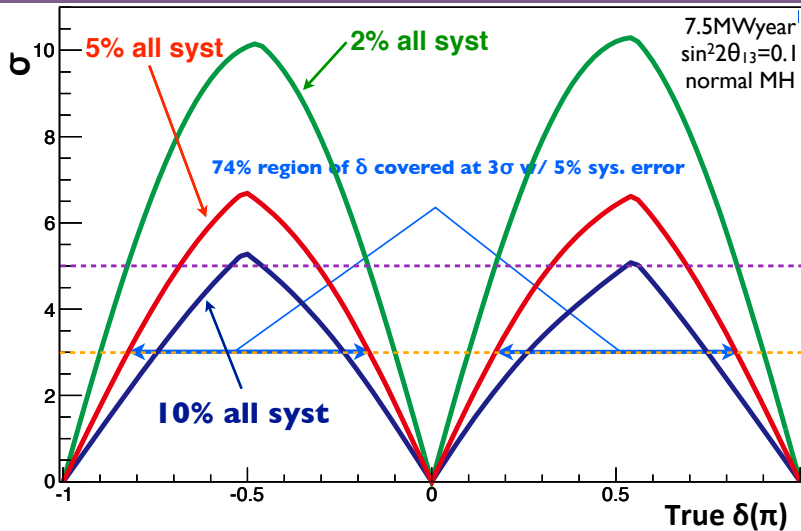
- After several years' running, can accomplish minimum 5σ measurement of mass hierarchy
- $\sigma \approx 5$ for $\sim 50\%$ of δ_{CP}
- **P5 Report, May 2014:** recommends forming new international experiment to accomplish 5σ for 75% of δ_{CP}

+ Hyper-K

- Proposed detector:** 0.99 MT (0.56 MT fiducial) water separated into two tanks
 - 99K 20" PMTs (inner det) + 25K 8" PMTs (outer det)
 - 25x the size of Super-Kamiokande**
- Beam:** Off-axis ~MW beam from J-PARC at baseline of 295km, peaked at ~0.6 GeV
 - Aim for high statistics, excellent signal/bkgd separation at <1 GeV, better than 5% syst error
 - Upgrade ND280 for better flux and cross-section measurements
 - New WC Near Detector at 2-3 km?

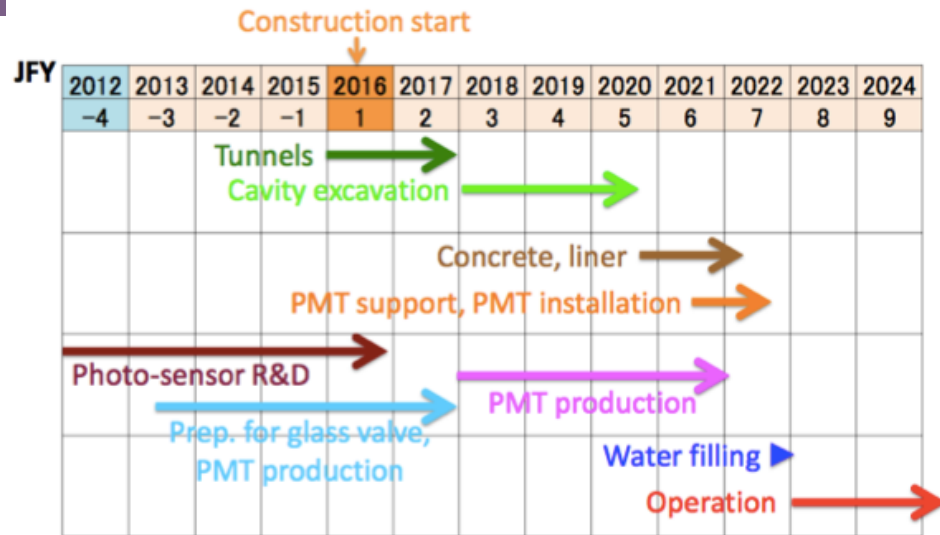
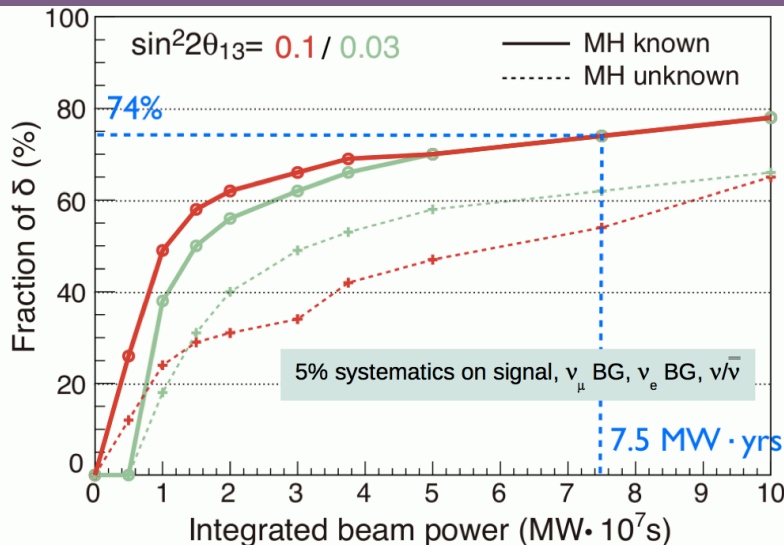


CP Discovery Sensitivity (w/ MH Known)



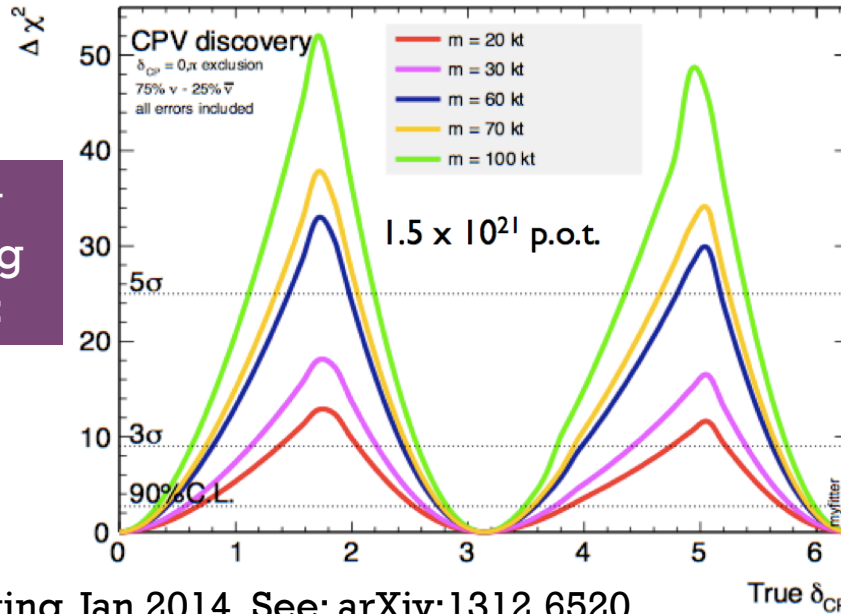
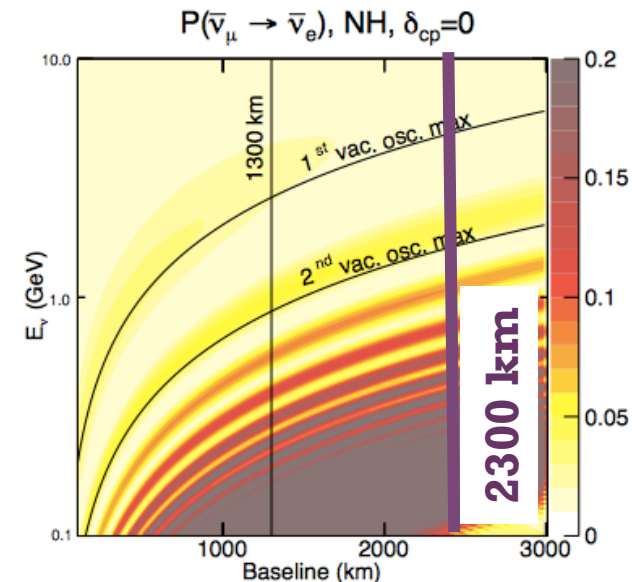
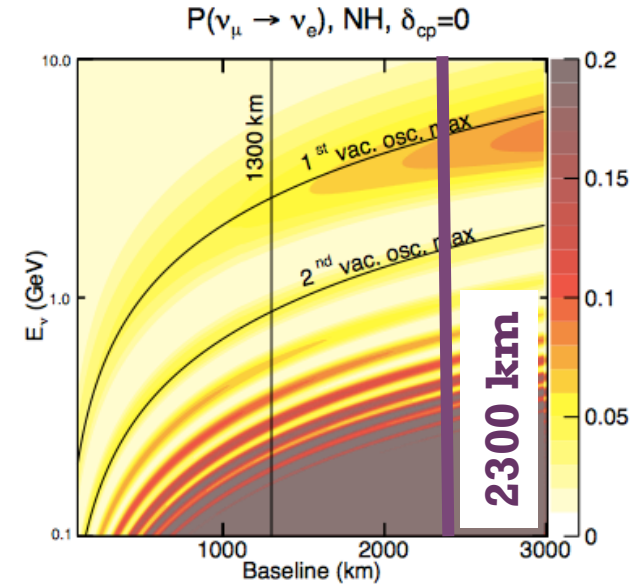
- With 7.5 MW·yr (1.5 MW x 5 yrs), can cover CPV $> 3\sigma$ (5σ) for 74% (55%) of delta range
- 3σ mass hierarchy determination for $\sin^2\theta_{23} > 0.42$ (0.43) for normal (inverted) hierarchy for 10 yrs' data
- Aim to begin construction of 1kt WC prototype in 2016
 - Overall construction = 7 years, assuming funding available 2016

% of δ w/ CPV ($\sin \delta \neq 0$) significance $> 3\sigma$



+ LBNO/LAGUNA

- **LAGUNA/LBNO:**
 - Beam from CERN to far detector at proposed baseline of 2300km
 - Can begin to see 2nd oscillation peak, where there is event greater sensitivity to δ_{CP}
- **Phase I:** 20kt LAr / 750kW conventional beam
 - Guaranteed 5σ sensitivity for MH in 5 years
- **Phase II:** 70kt detector, 2 MW beam
 - Can reach 5σ CPV coverage

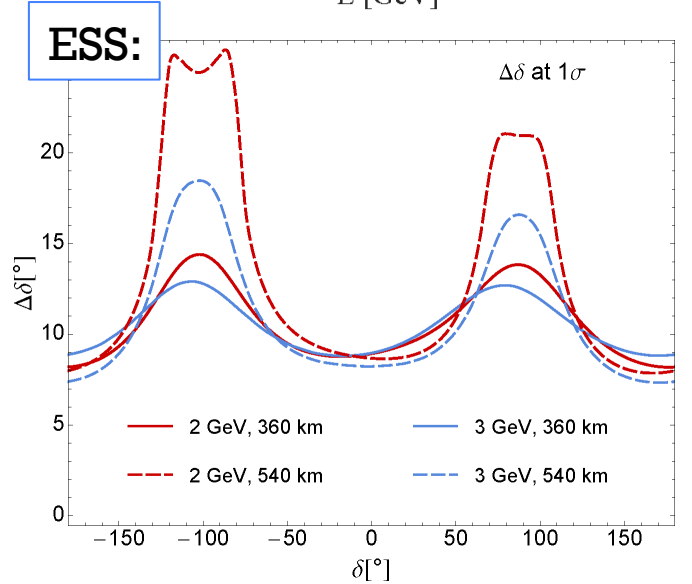
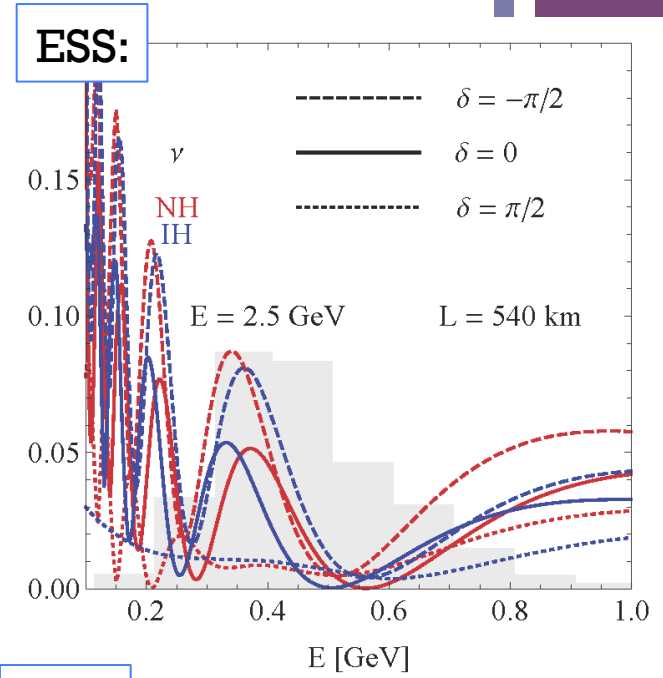
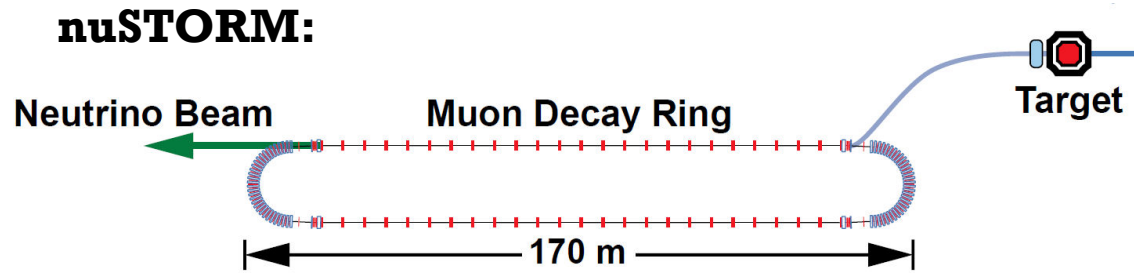


5 years running after determining mass hierarchy:

+ New Neutrino Sources

- **European Spallation Source:** currently being built in Lund, Sweden
 - Will have ~2 GeV 5 MW super-conduction LINAC
 - At least two times higher intensity than any other planned proton driver for a neutrino beam
 - First beam 2019, full power by 2022
 - Very high statistics; lower energy beam (<1 GeV); can put detector at 2nd oscillation max w/ relatively short baseline (~500-1000km)

- **New neutrino sources from stored muons:**
 - nuSTORM (funding?), Neutrino Factory, etc.
 - Reduced systematics from beam, good understanding of flux



+ A (Very Rough) Timeline

Experiment	2014	2016	2018	2020	2022	2024	2026	2028	2030	2032	2034	2036
T2K	[Blue bar from 2014 to 2022]											
NOvA	[Green bar from 2014 to 2016], [Blue bar from 2016 to 2024]											
Hyper-K	[Green bar from 2014 to 2022], [Blue bar from 2022 to 2034]											
LBNF	[Green bar from 2016 to 2024], [Blue bar from 2024 to 2036]											
LBNO	[Green bar from 2016 to 2024], [Blue bar from 2024 to 2036], ??? "MH within 10-15 years" (text above bar from 2022 to 2036)											
ESS	[Green bar from 2014 to 2022] (linac power/beam), [Blue bar from 2022 to 2036] ???											

 = Construction

 = Operation

- Above estimates = based on January ICFA talks, funding reports, etc.
- **This is highly approximate and subject to change**
 - All end dates are extremely rough estimates
 - Heavily dependent on future funding decisions
 - Will probably hear more updates **next week**, at Neutrino 2014 in Boston

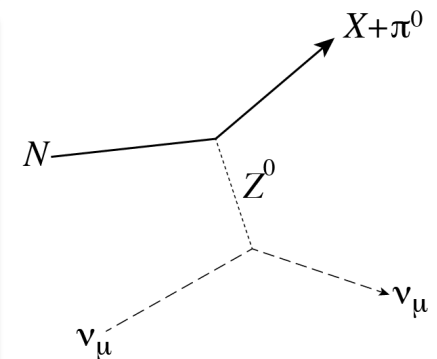
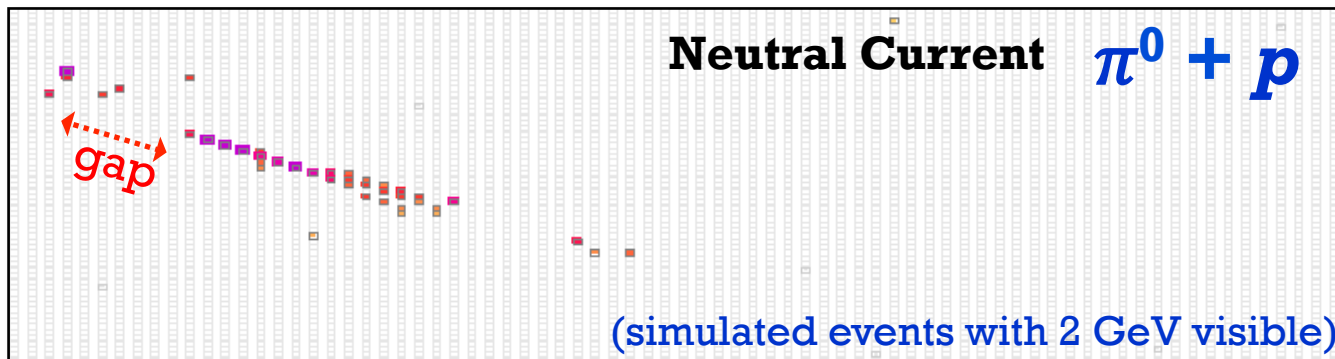
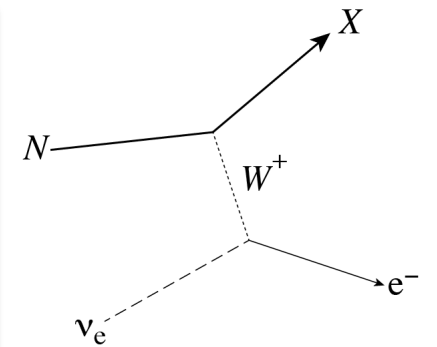
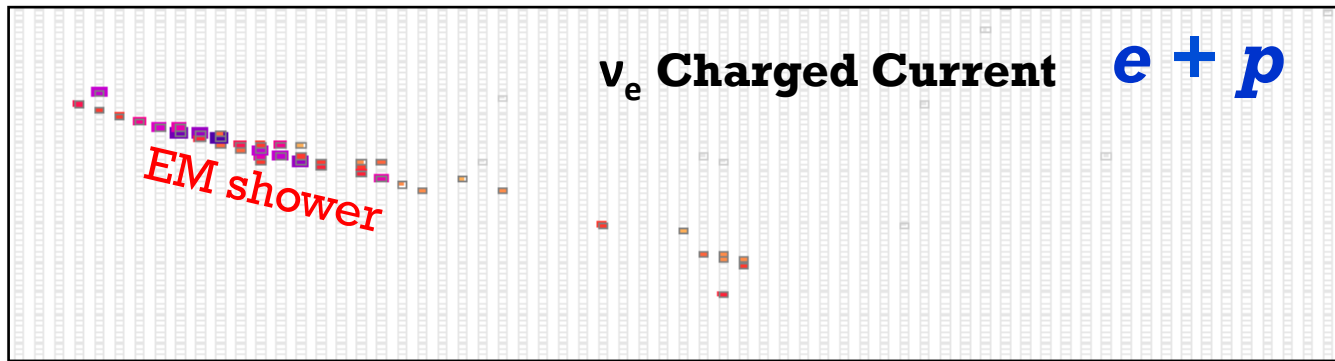
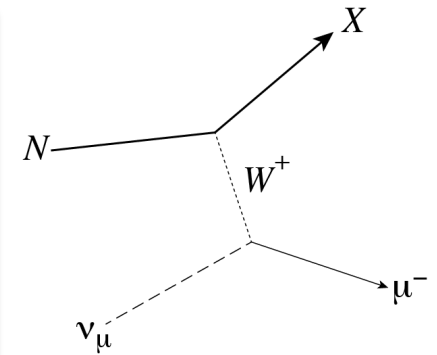
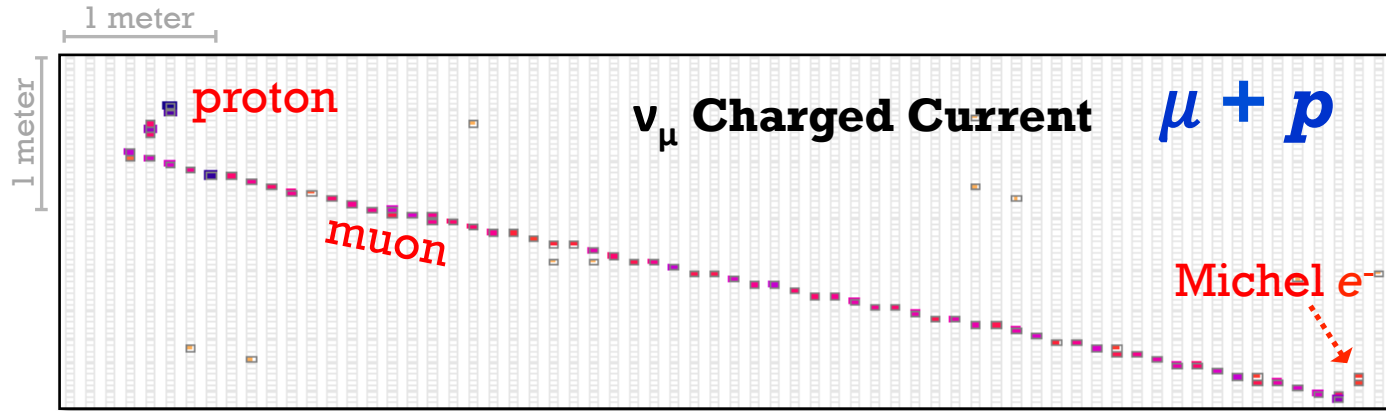
+ Conclusions

- We now have measurements of most of the major parameters involved in neutrino oscillations (mixing angles, mass differences)
 - Long baseline experiments provide key measurements and independent verifications
 - Using current and next-gen experiments, can now begin to answer some very interesting questions
- **Especially: can we see CP Violation in the lepton sector?**



+ Backup Slides

+ Neutrino Events (NOvA Example)

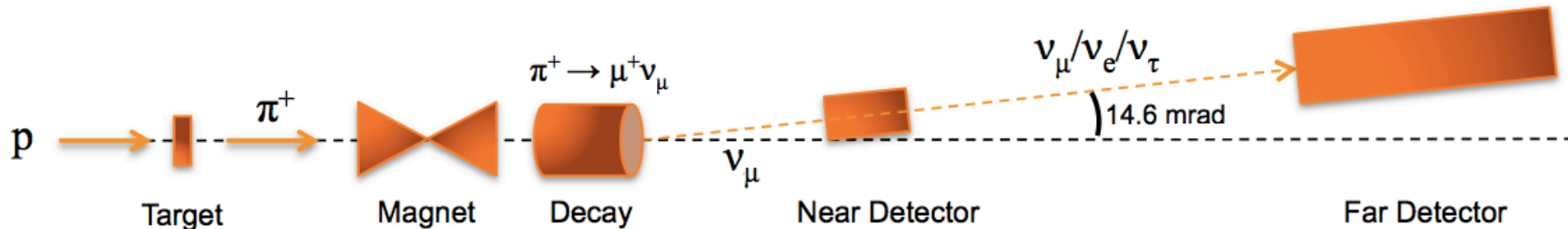
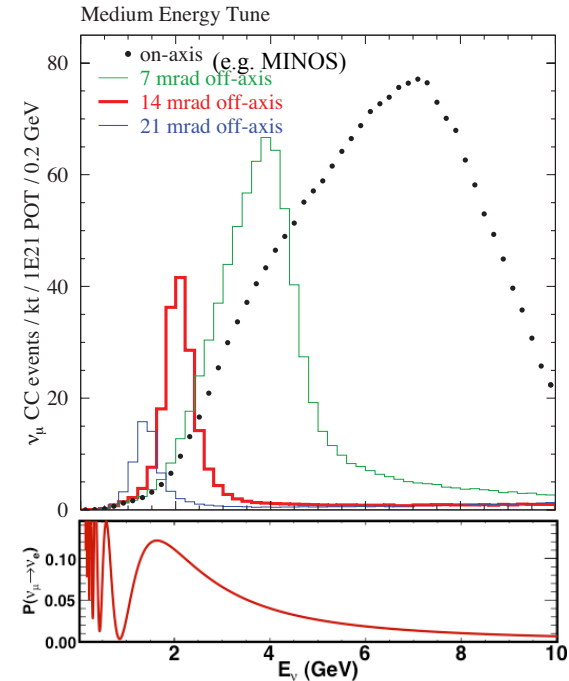


+ Beamline Example: NuMI

- **Production:** 120 GeV p+ from Main Injector collides with graphite target to produce hadrons (mostly pions and kaons)
- **Focusing:** Two magnetic focusing horns focus hadrons
 - Focus pi+/K+ for neutrino beam
 - Focus pi-/K- for antineutrino beam
- **Decay:** Hadrons decay in 675 m long decay pipe
 - End = on-axis wide-band muon neutrino beam
- **Off-axis beam:** take advantage of angular dependence of final neutrino energy from two-body hadron decay:

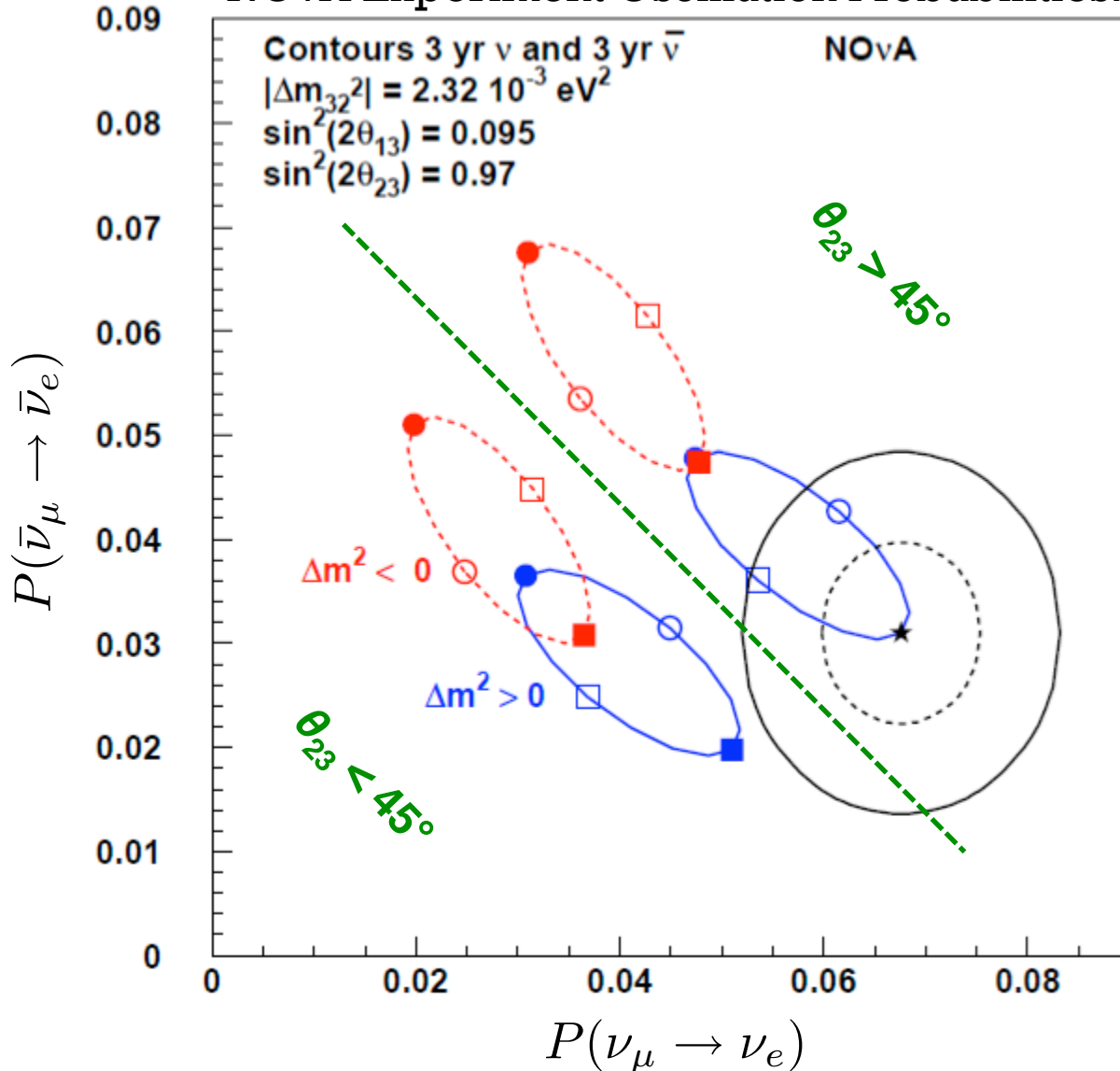
$$E_\nu = \frac{\left(1 - \frac{m_\mu}{M^2}\right) E}{1 + \gamma^2 \tan^2 \theta_\nu}$$

- Lower intensity, but narrower energy profile (can design so this is at L/E oscillation peak!)



+ Effect of Octant on $\nu_\mu \rightarrow \nu_e$

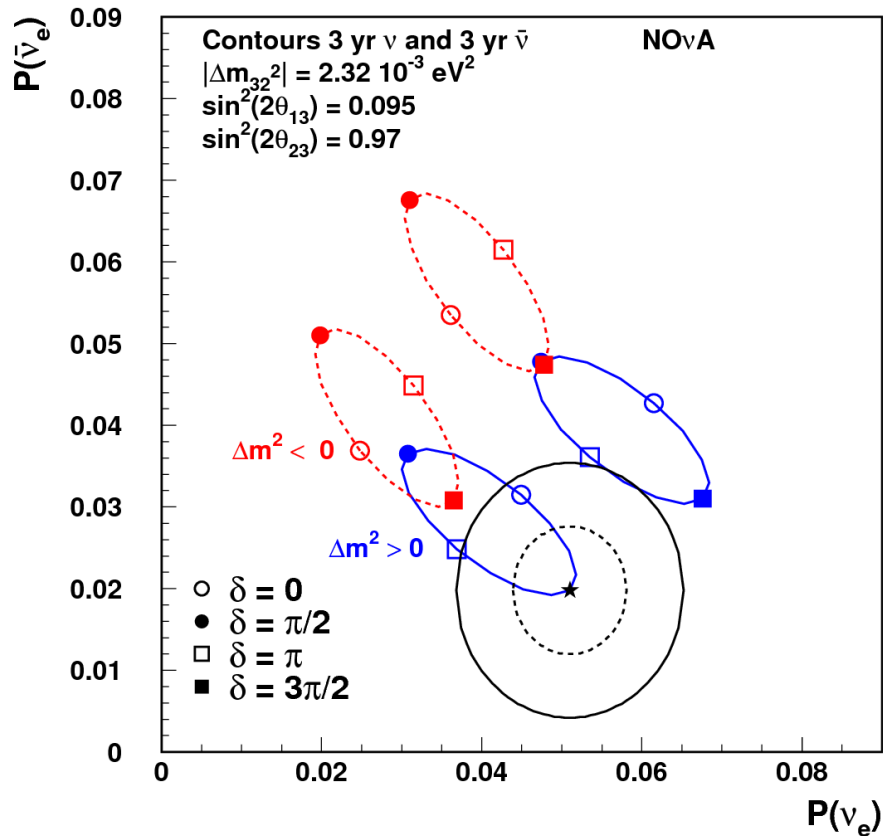
NOvA Experiment Oscillation Probabilities:



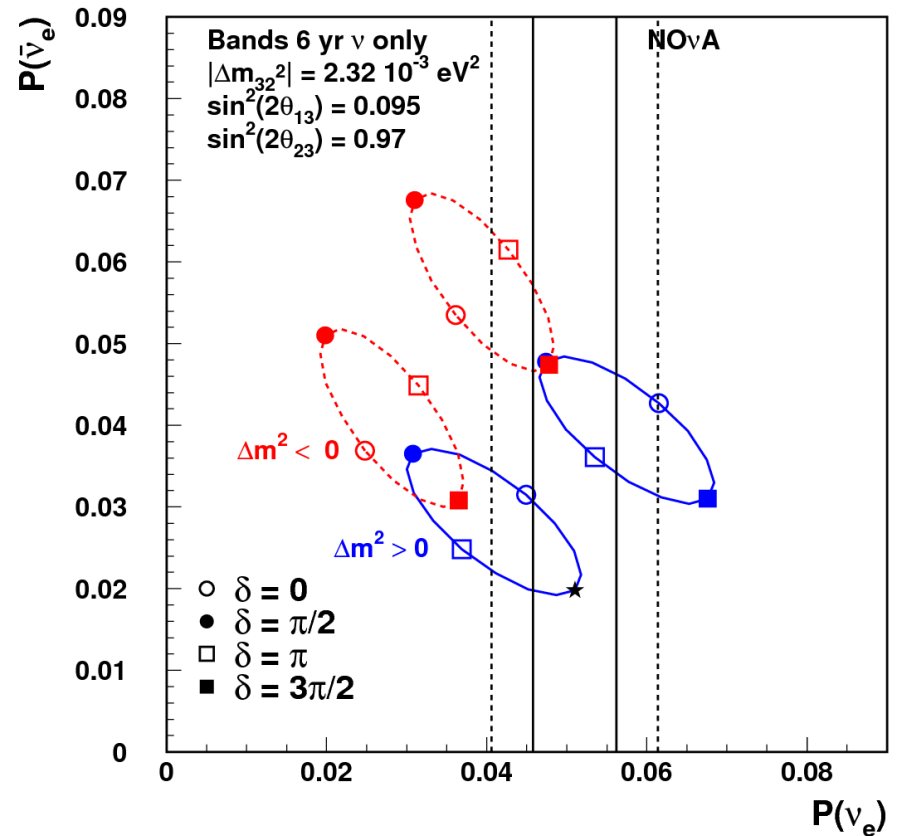
- Measurements of $\sin^2(2\theta_{23})$ show it is close to unity
- Is it in fact unity, or does it fall into one of two “octants”?:
 - $\theta_{23} > 45^\circ$
 - $\theta_{23} < 45^\circ$
- The value of θ_{23} will have an effect on appearance probability for both neutrinos and anti-neutrinos.

+ NOvA Octant Plots

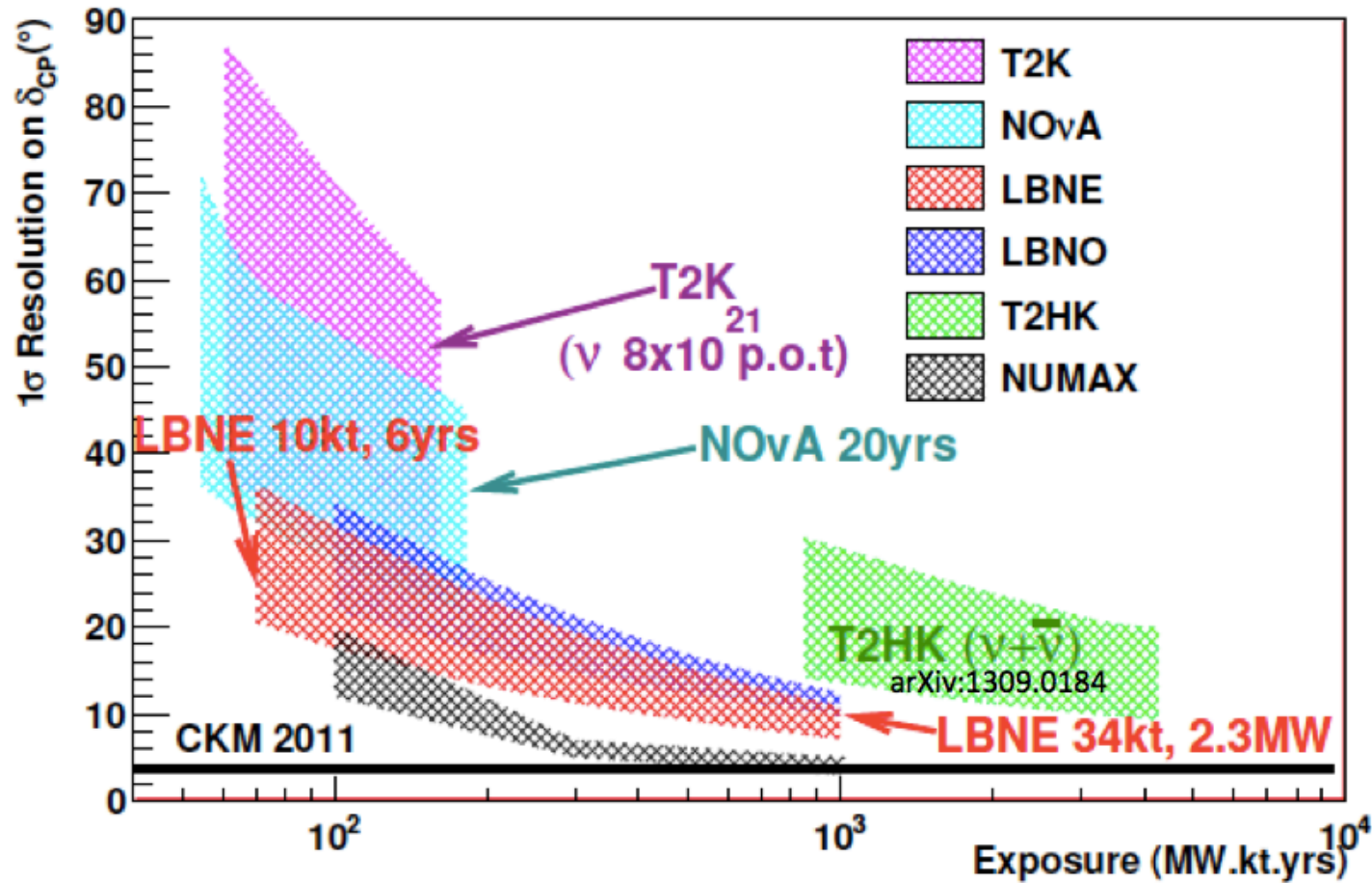
1 and 2 σ Contours for Starred Point



1 and 2 σ Bands for Starred Point

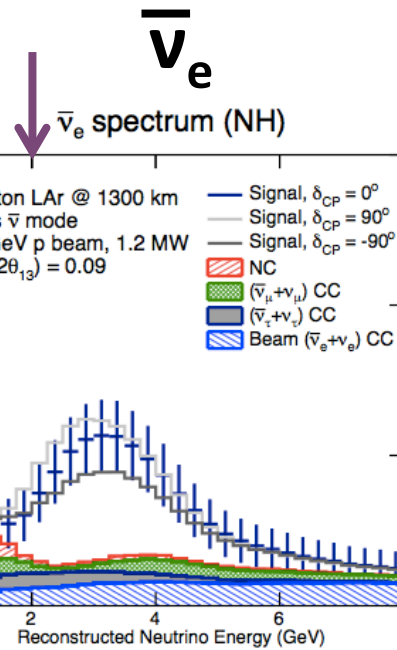
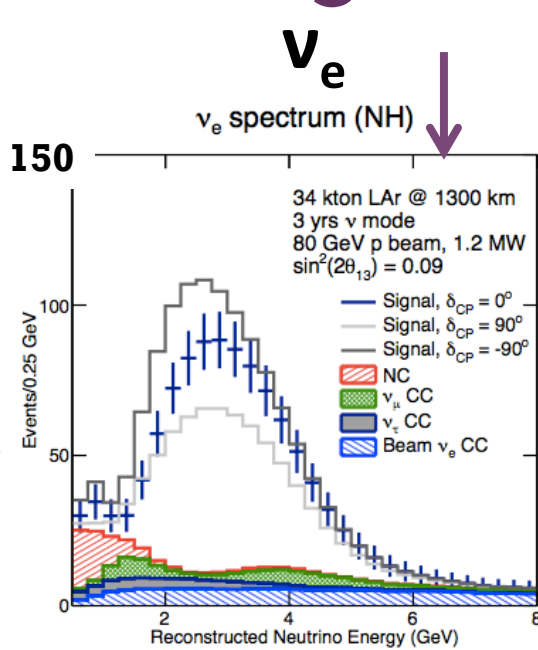


+ Coverage (one version...)

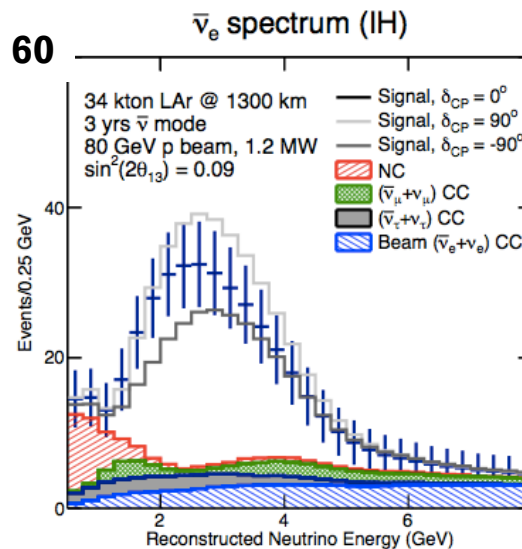
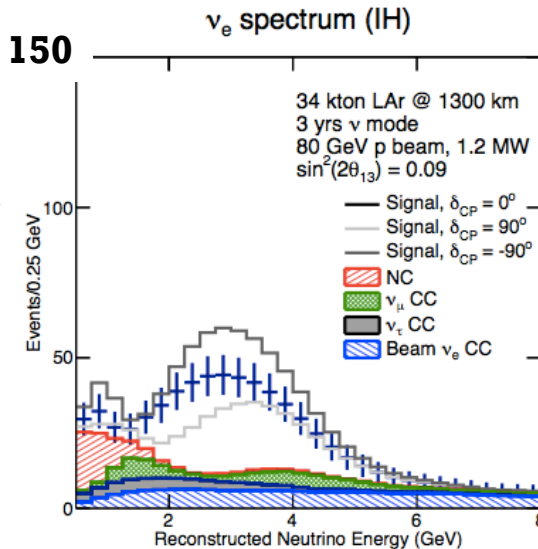


+ Existing LBNE Studies

NH
→



IH
→



- Longer baseline = larger influence from matter effects
- Enhancement/suppression of ν_e appearance is linked to sign of mass hierarchy
- At LBNE baseline, this asymmetry exceeds the impact from CP violation and reduces MH/CP ambiguity

+ Neutrino Mass and Leptogenesis

- Standard **Dirac mass** term allowed: $\mathcal{L}_D = -m_D (\bar{\nu}_L \nu_R + \bar{\nu}_R \nu_L)$
- Can also write additional **Majorana mass** term, if ignore lepton number conservation:

$$\mathcal{L}_M = -\frac{1}{2} m_R (\nu_R^T \nu_R + \bar{\nu}_R \bar{\nu}_R^T)$$

- Neutrinos have no electric charge; also, this means neutrinos = anti-neutrinos
- Rewrite this as a mass matrix:

$$\mathcal{L} = -\frac{1}{2} (\bar{\nu}_L, \nu_R^T) \begin{pmatrix} 0 & m_D \\ m_D & m_R \end{pmatrix} \begin{pmatrix} \bar{\nu}_L^T \\ \nu_R \end{pmatrix} + \text{h.c.}$$

- Diagonalize this to get the following:

$$m_1 \sim \frac{m_D^2}{m_R} \quad m_2 \sim m_R$$

- One choice = m_D near electroweak (~ 100 GeV) scale, m_R near GUT ($\sim 10^{14}$ GeV) scale
- This gives a neutrino mass which resembles reality: $m_1 \sim 0.1$ eV
- Heavy neutrinos (m_2) existed in early universe and they decayed?
- **Leptogenesis:** if $\nu_R \rightarrow l^+ + h^- \neq \nu_R \rightarrow l^- + h^+$, could explain matter/antimatter asymmetry of the early universe
 - Makes lepton-sector CP Violation a very important topic of study

+ PMNS vs CKM

Approximate forms:

$$|U_{\text{PMNS}}| \sim \begin{pmatrix} 0.8 & 0.5 & 0.2 \\ 0.5 & 0.6 & 0.6 \\ 0.2 & 0.6 & 0.8 \end{pmatrix} \quad |V_{\text{CKM}}| \sim \begin{pmatrix} 1 & 0.2 & 0.004 \\ 0.2 & 1 & 0.04 \\ 0.008 & 0.04 & 1 \end{pmatrix}$$

- Precision measurements of neutrino oscillation necessary for understanding why PMNS matrix has the form that it does, and how it relates to quark CP violation (which seems very different)
 - Would like to achieve same degree of precision as CKM
 - E.g., precision can help determine if predictions from Quark-Lepton Universality are true:

$$U^{\text{CKM}} = 1 + \epsilon_{\text{Cabbibo}} \quad \theta_{23} \sim \pi/4 + \Delta\theta \quad \leftarrow \text{Of order } \theta_c$$

$$U^{\text{PMNS}} = T + \epsilon_{\text{Cabbibo}} \quad \theta_{13} \sim \theta_C / \sqrt{2} \quad \theta_C = \theta_{12}^{\text{CKM}}$$

Determined by Majorana Physics

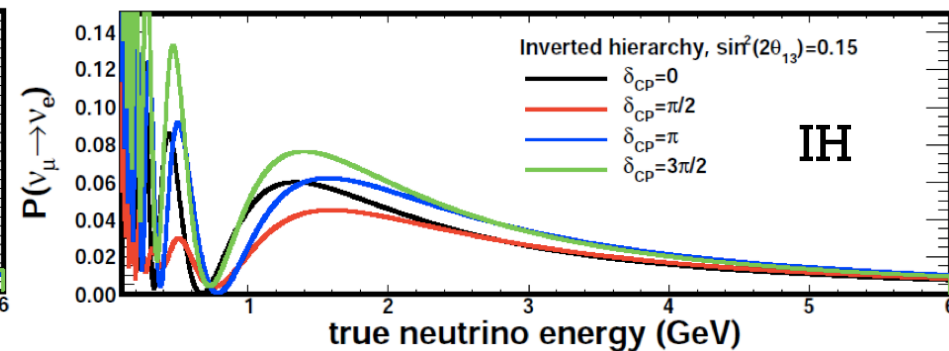
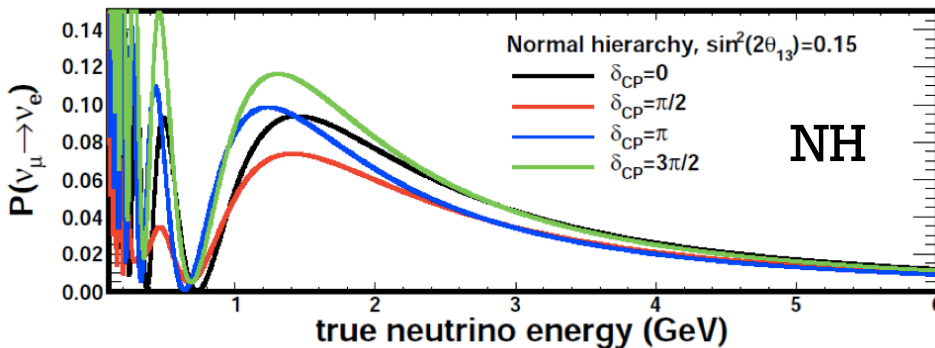
Important to determine octant!

+ $\nu_\mu \rightarrow \nu_e$ Appearance

$$\begin{aligned}
 P(\nu_\mu \rightarrow \nu_e) \approx & \boxed{\sin^2(2\theta_{13})} \boxed{\sin^2(\theta_{23})} \sin^2\left(1.27 \boxed{\Delta m_{31}^2} \frac{L}{E}\right) + \boxed{\Delta m_{32}^2 \approx \Delta m_{31}^2} \\
 & \sin^2(2\theta_{12}) \boxed{\cos^2(\theta_{23})} \sin^2\left(1.27 \Delta m_{21}^2 \frac{L}{E}\right) + \leftarrow \text{Small solar contribution} \\
 & \boxed{\sin(2\theta_{13})} \boxed{\sin(2\theta_{23})} \sin(2\theta_{12}) \sin\left(1.27 \boxed{\Delta m_{31}^2} \frac{L}{E}\right) \sin\left(1.27 \Delta m_{21}^2 \frac{L}{E}\right) \cos\left(1.27 \boxed{\Delta m_{32}^2} \frac{L}{E} \pm \delta_{\text{CP}}\right)
 \end{aligned}$$

CP phase \downarrow

- $\nu_\mu \rightarrow \nu_e$ appearance = connected to numerous neutrino mixing parameters:
 - Value of θ_{13} : now known to be non-zero, meaning other parameters can be measured
 - Sign of Δm_{32}^2 : relevant via **matter effects** when beam passes through earth
 - Precise value and octant of θ_{23}
 - CP violation phase δ_{CP} : sign of effect different for neutrinos and antineutrinos



MINOS Beamline (735 km)